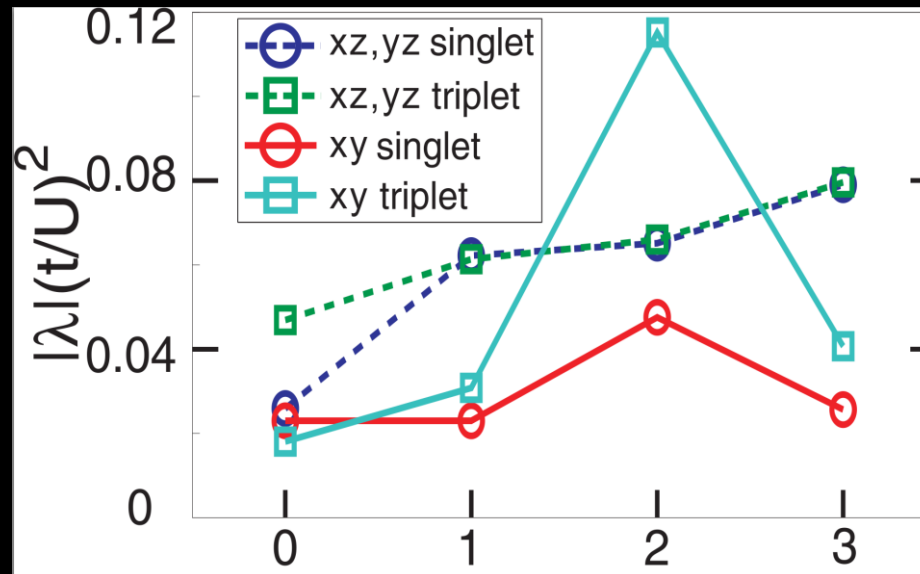
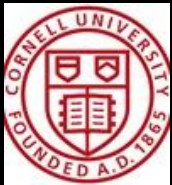


# Towards Higher $T_c$ Topological Superconductors



Eun-Ah Kim  
(Cornell University)





Yi-Ting Hsu



Weejee Cho



Andrew Mulder



Craig Fennie



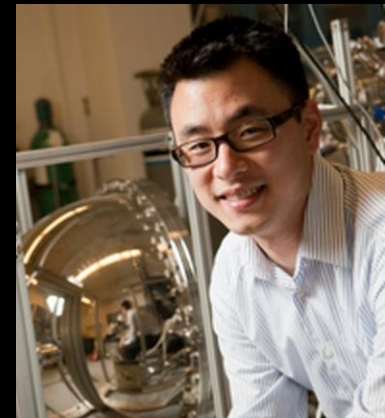
Bulat Burganov



Carolina Adamo



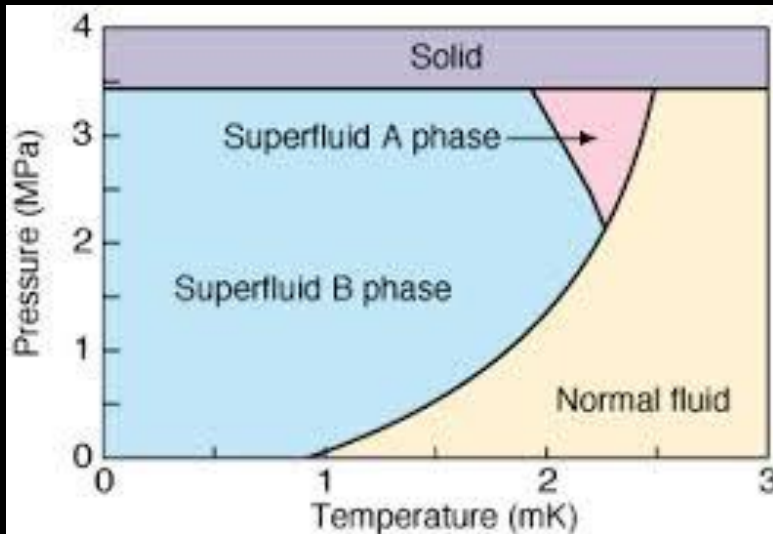
Darrell Schlom



Kyle Shen

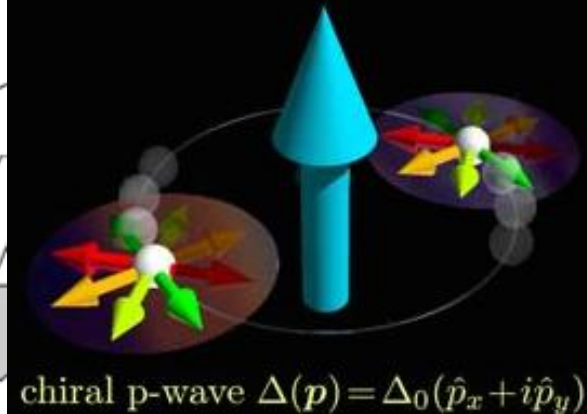
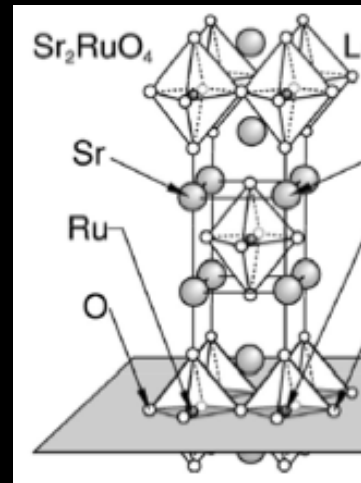
Existing Topo SC

# Superfluid He3



- The original (only) realization of topological superfluid

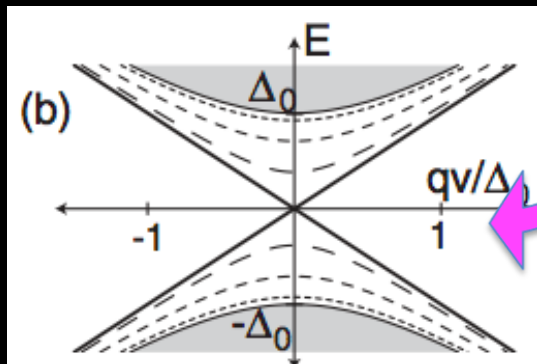
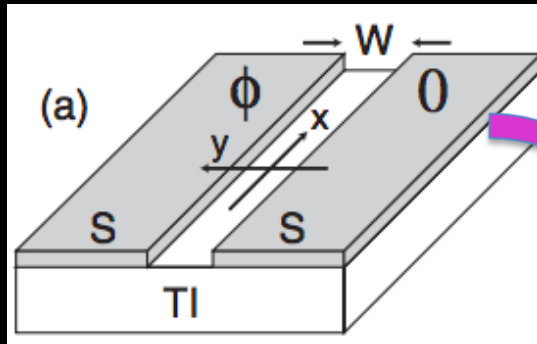
# $\text{Sr}_2\text{RuO}_4$ ?



- Triplet SC with broken TRS
- $T_c=1.5\text{K}$
- Topological?

# Approaches for Engineering New or Improved TopoSC

# Hybrid Films of TI and s-SC

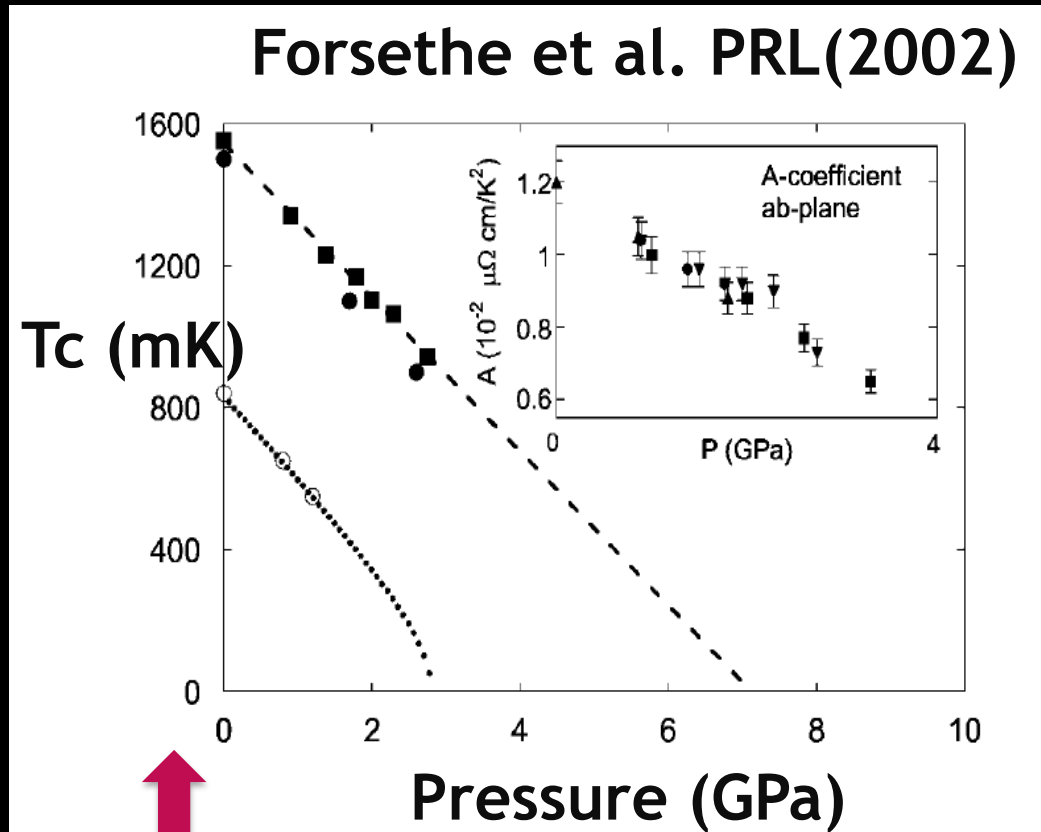


- Experiments observe proximity effect
- Interfacial effect

Fu&Kane PRL (2008)

# Pressurizing Bulk $\text{Sr}_2\text{RuO}_4$ :

## I. Hydrostatic Pressure

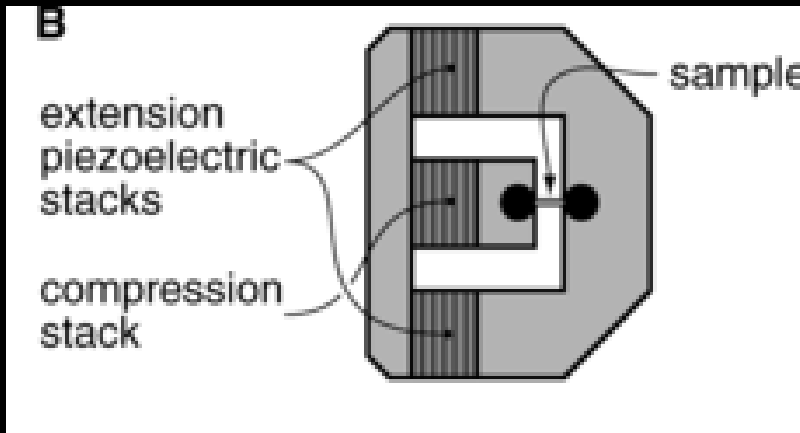


As grown  $\text{Sr}_2\text{RuO}_4$

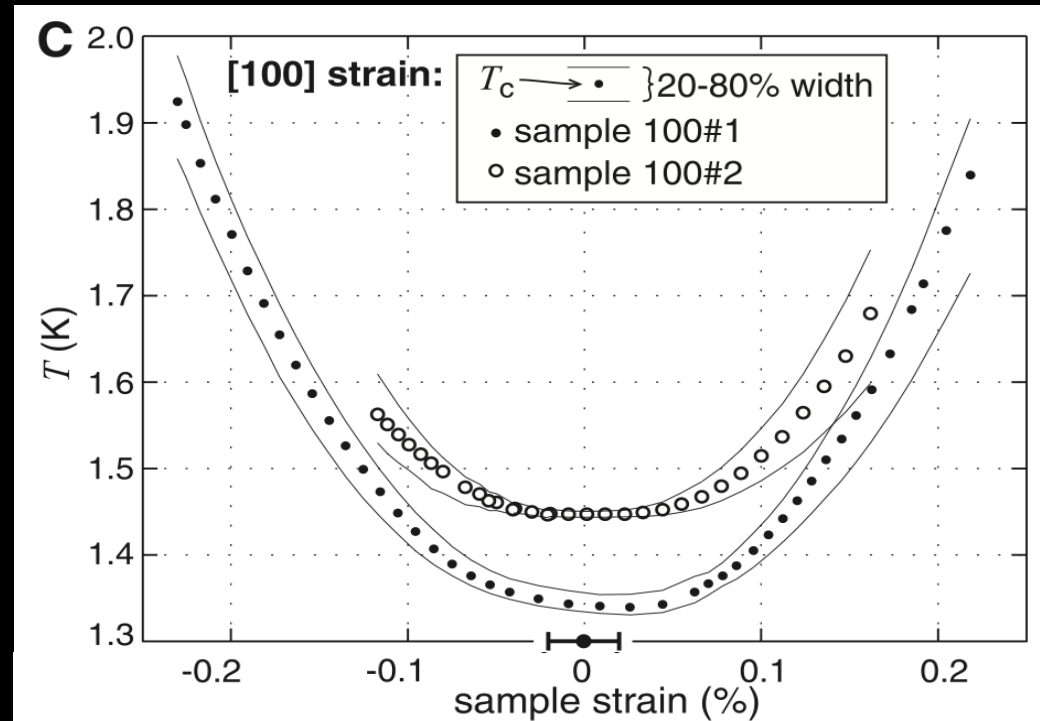
Decrease in  $T_c$



# Pressurizing Bulk $\text{Sr}_2\text{RuO}_4$ : II. Uni-axial Strain



C. Hicks et al,  
Science 2014



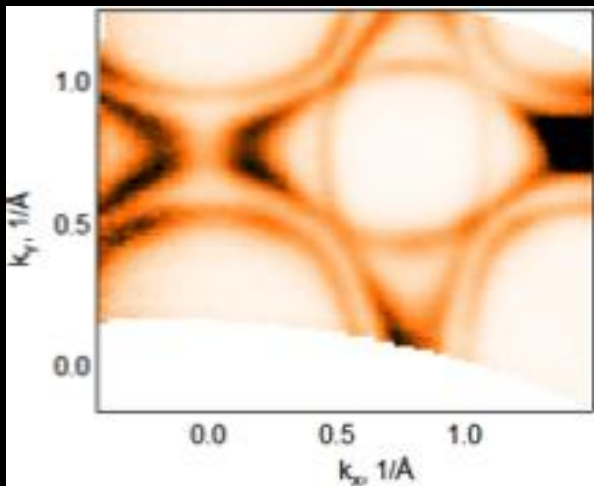
$T_c$  goes up  
Not topological





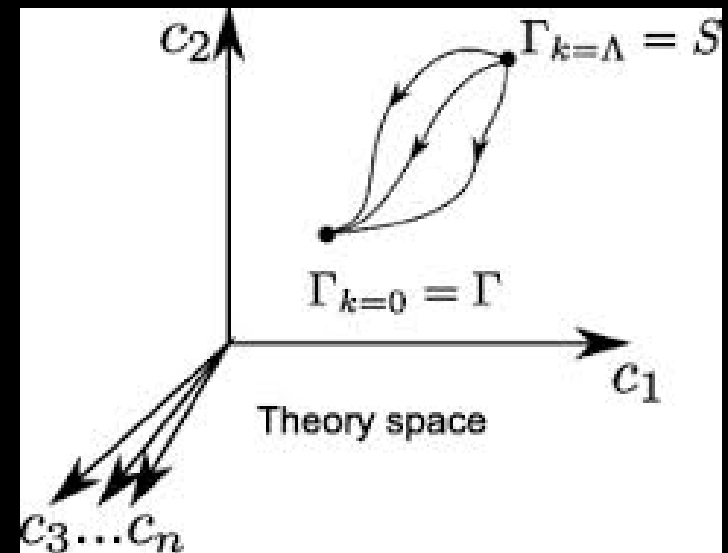
# Our Approach

# Strain Engineering via MBE

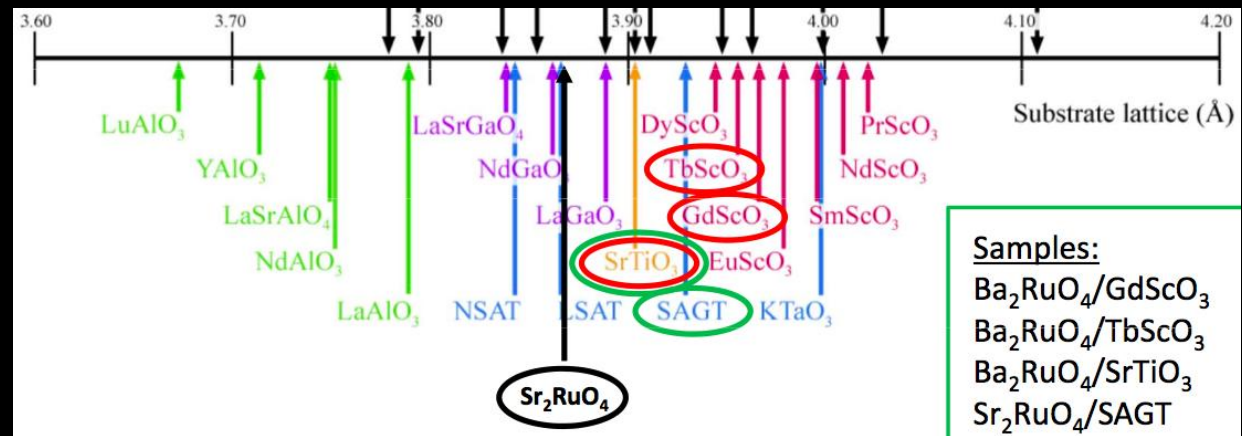
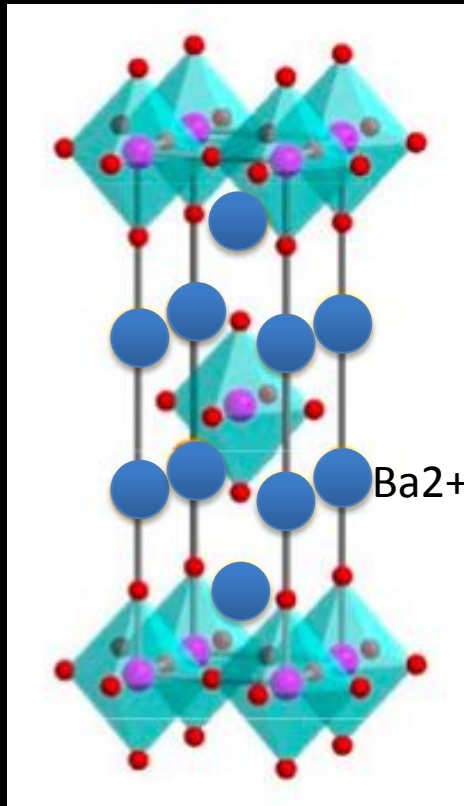


In Situ ARPES

# Predictions based on RG



# Phase Space for Strain Engineering in MBE



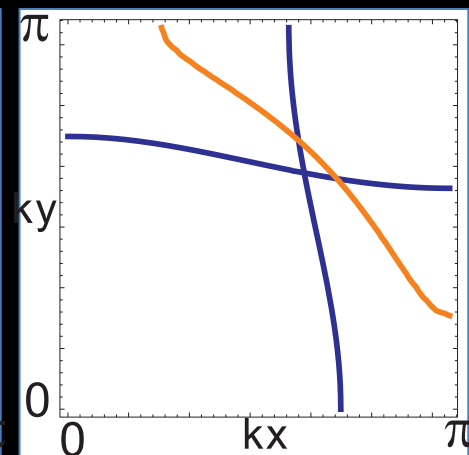
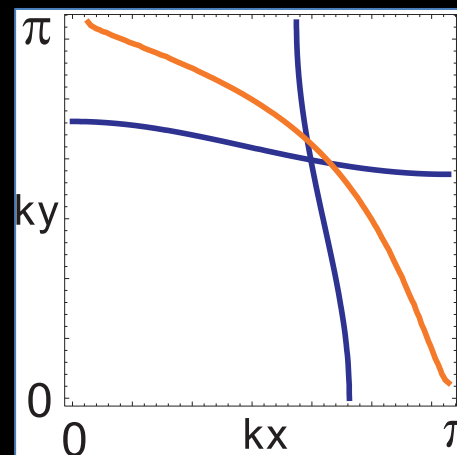
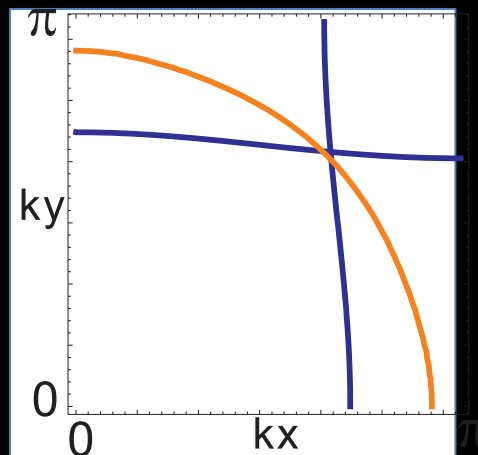
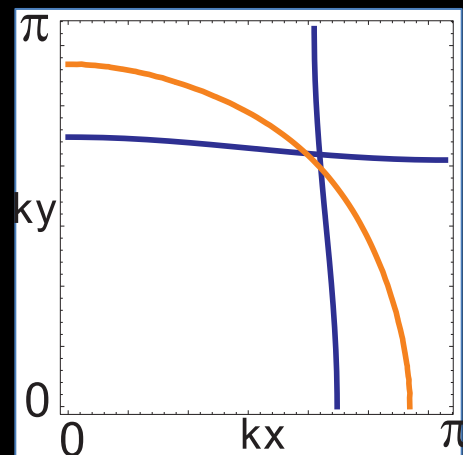
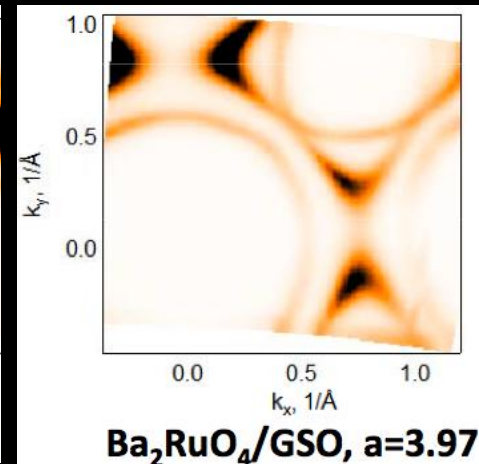
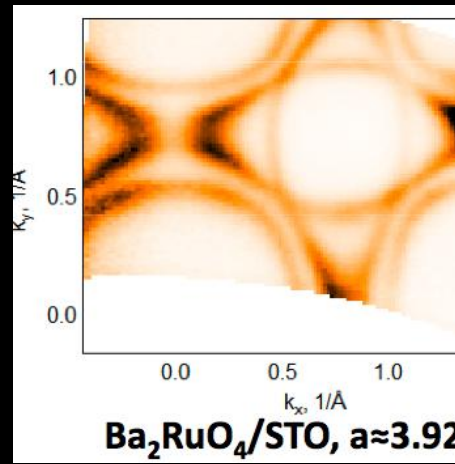
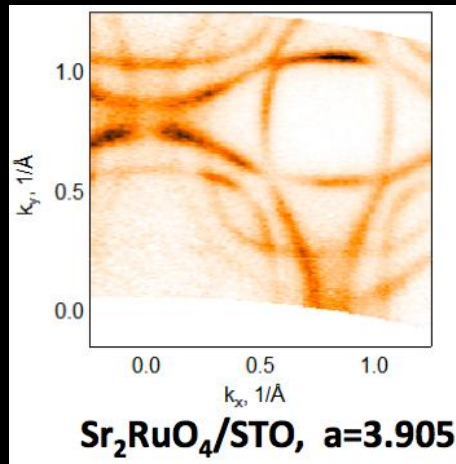
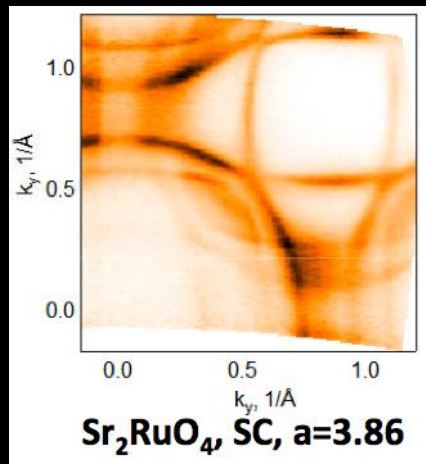
Isovalent Substitution

Film – Substrate Lattice Matching

# Two Step Strategy:

1. Explore the Phase Space for Films
2. Refine a Theoretically Guided Target

# Fermi Surface Data

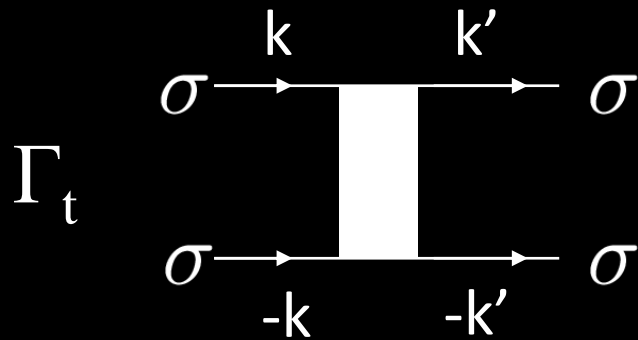
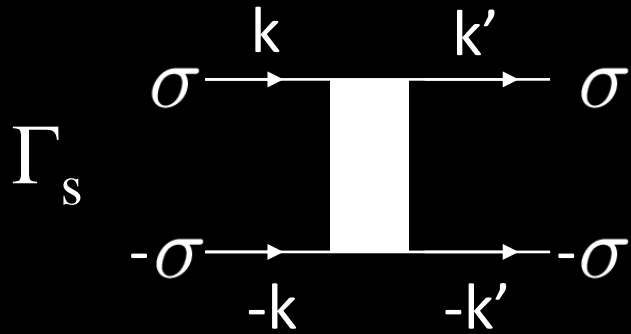


Bulat et al (2014, in preparation)

Lessons from small  $U/t$  limit  
Two stage RG of the  $U>0$   
Hubbard model

Raghu et al. PRB(2010), Raghu et al. PRL(2010)

# 1: Generate an effective interaction Matrix $E=\Lambda_0$



## 2: Eigenvalues each run independently

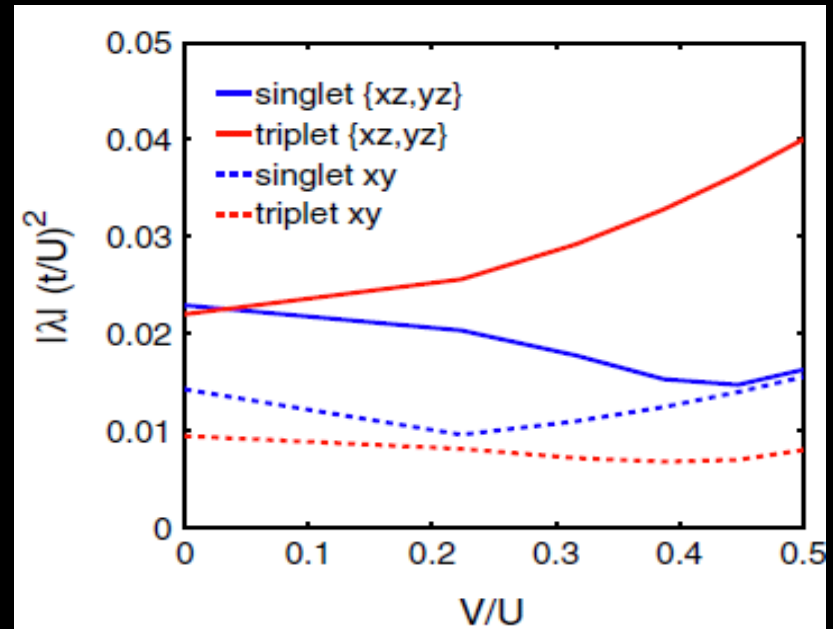
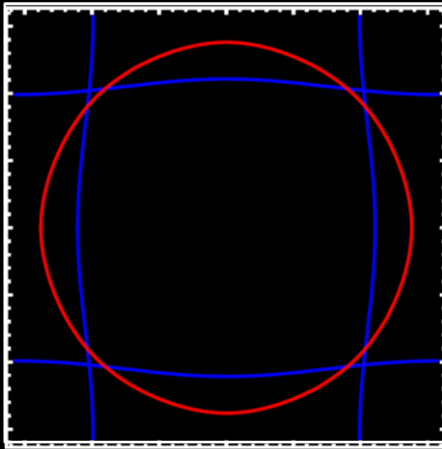
$$\frac{d\lambda_{s/t,n}^{\alpha}}{dy} = -\lambda_{s/t,n}^{\alpha} \quad 2$$

- Most negative eigenvalue at  $\Lambda_0$ ,  $\lambda_{s/t,n}^{\alpha,0}$  determines channel and  $T_c$   $T_c \sim W e^{-1/|\lambda_{s/t,0}^{\alpha,0}|}$ .
- Fermiology controls  $\lambda_{s/t,n}^{\alpha,0}$



# Two-Stage RG applied to bulk $\text{Sr}_2\text{RuO}_4$

Raghu et al. PRL(2010)



- $\Pi_{ph}(\vec{q} = 2k_F)$  rules
- **Triplet SC driven by 1D band at finite  $V$**
- **Can be chiral but not topological**



# Strategy for topological SC:

- Triplet 2D band driven SC with stronger pairing

- Want  $\Pi_{ph}^{xy}(\vec{q} = 0)$  dominating over

$$\Pi_{ph}^{xy}(\vec{q} = \vec{Q}) \quad \text{or} \quad \Pi_{ph}^{x,y}(\vec{q} = 2k_F)$$

Mission: Find Goldilock's Film

# Two stage RG Applied to Film Fermiology

# Model

- Parametrize measured FS and LDA results

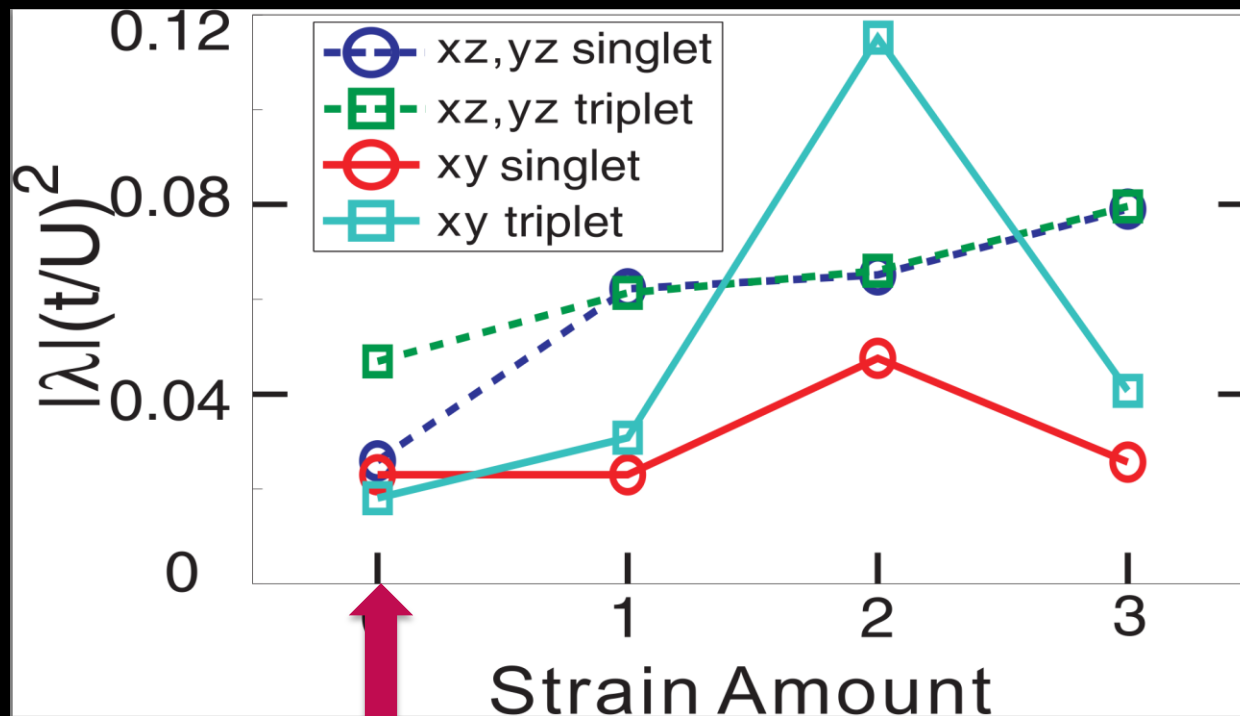
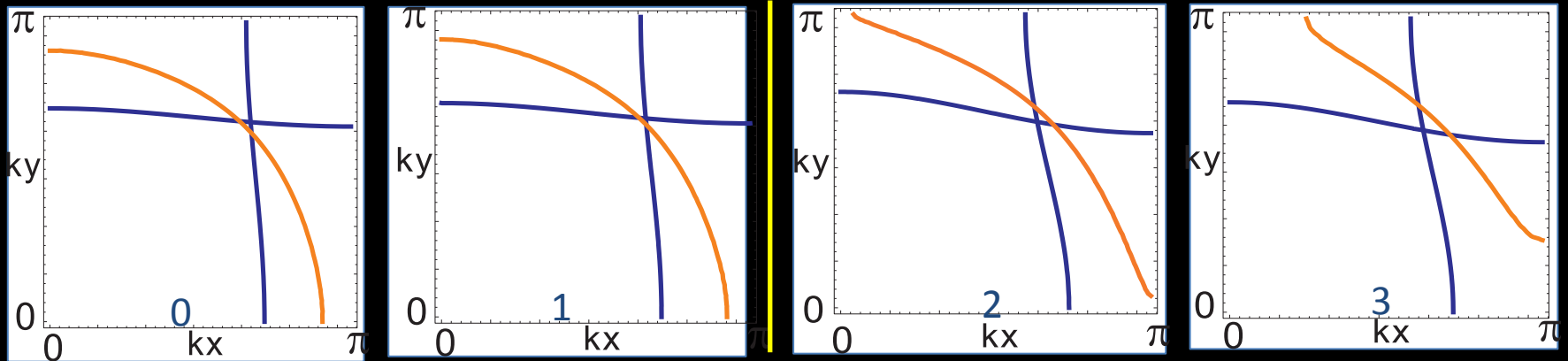
$$\epsilon^{xz(yz)}(\vec{k}) = -2t \cos k_{x(y)} - 2t^\perp \cos k_{y(x)} - \mu_1$$

$$\epsilon^{xy}(\vec{k}) = -2t'(\cos k_x + \cos k_y) - 4t'' \cos k_x \cos k_y - \mu_2,$$

- Start from Hubbard model as the UV limit

$$H = \sum_{\vec{k}\alpha\sigma} \epsilon^\alpha(\vec{k}) c_{\vec{k}\alpha\sigma}^\dagger c_{\vec{k}\alpha\sigma} + U \sum_{i\alpha} n_{i\alpha\uparrow} n_{i\alpha\downarrow}$$

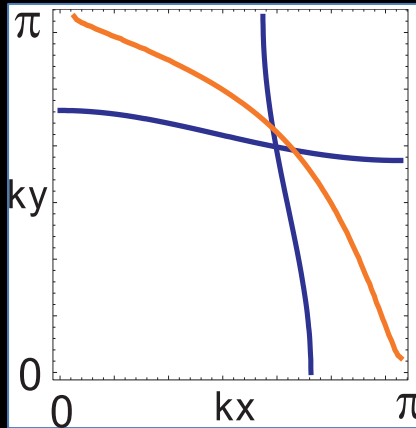
# SC tendencies for Strained Films



As grown  $\text{Sr}_2\text{RuO}_4$

Y. Hsu et al, (2014, in preparation)

# Goldilock's film



- 2D Hole-FS near van-Hove singularity
- Nesting is poor

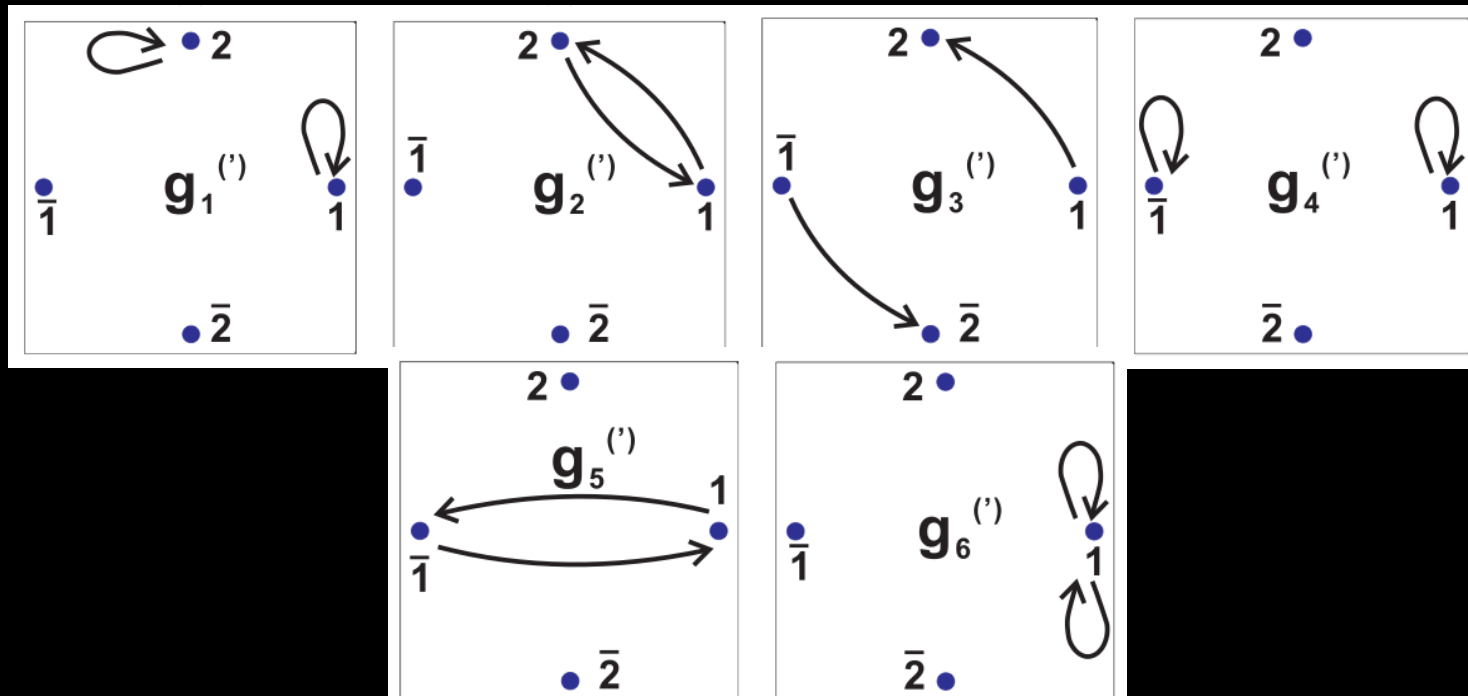
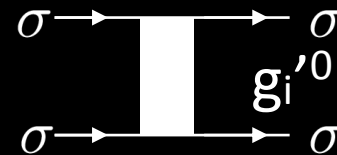
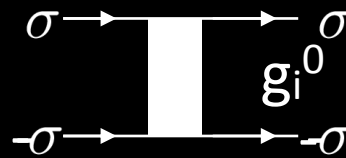
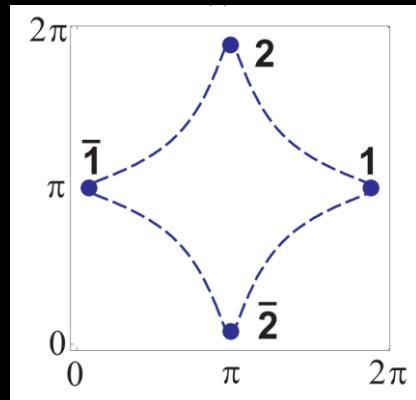
Ba<sub>2</sub>RuO<sub>4</sub>/STO

$$\Pi_{ph}^{xy}(\vec{q} = 0) \gg \Pi_{ph}^{xy}(\vec{q} = \vec{Q}) \text{ or } \Pi_{ph}^{x,y}(\vec{q} = 2k_F)$$

- Escapes symmetry prohibition of triplet pairing for vH point

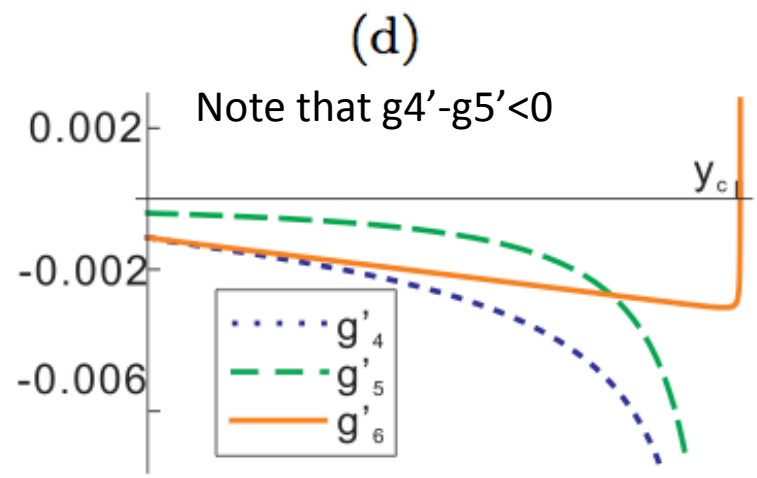
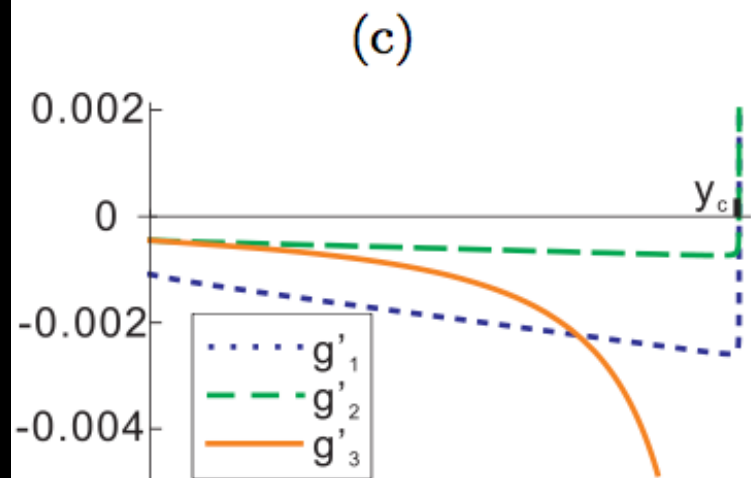
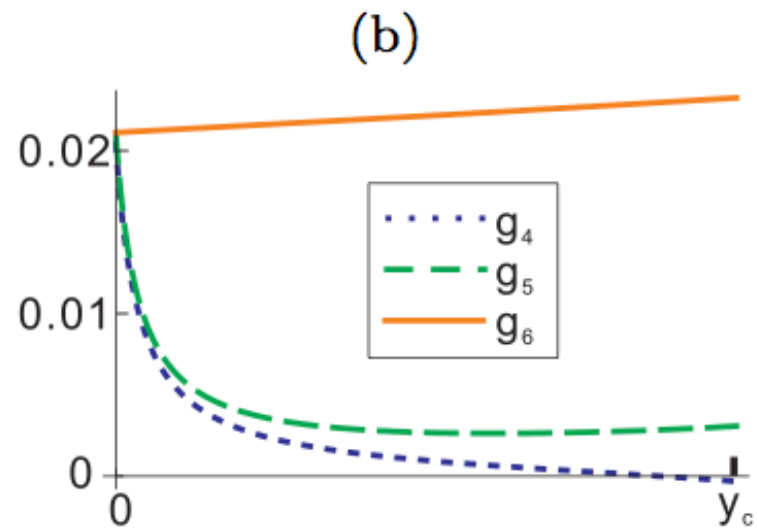
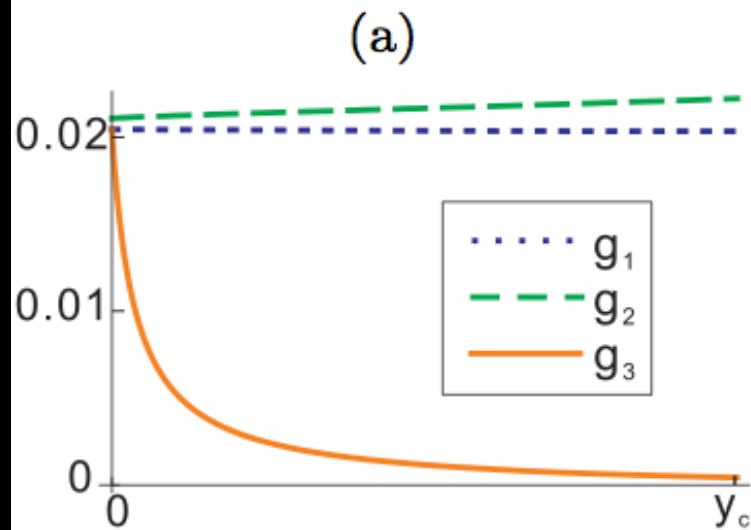
# Patch Parquet RG Starting from the Effective Theory

# 4-Patches and Effective Interactions

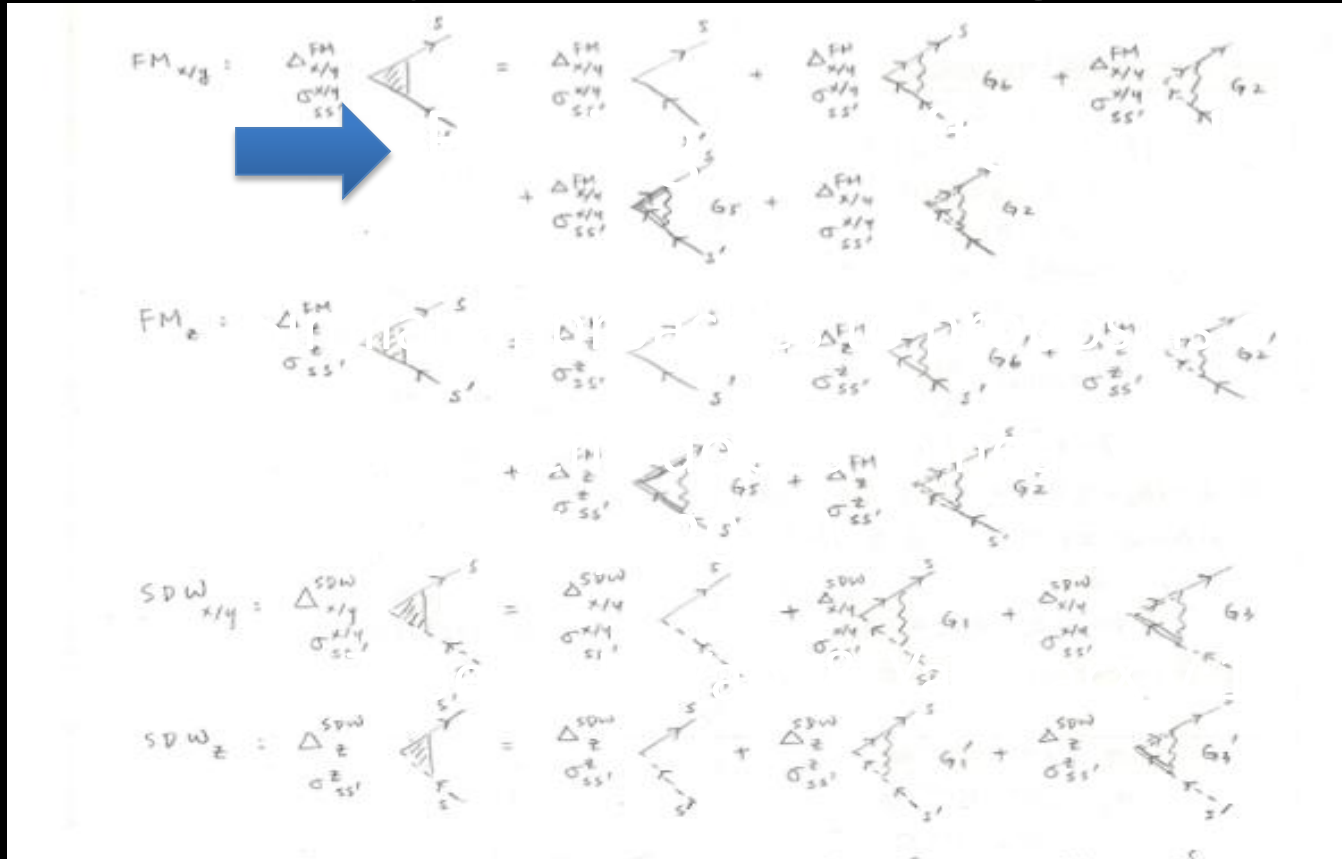




# Parquet RG flow



# Competition among Instabilities



S

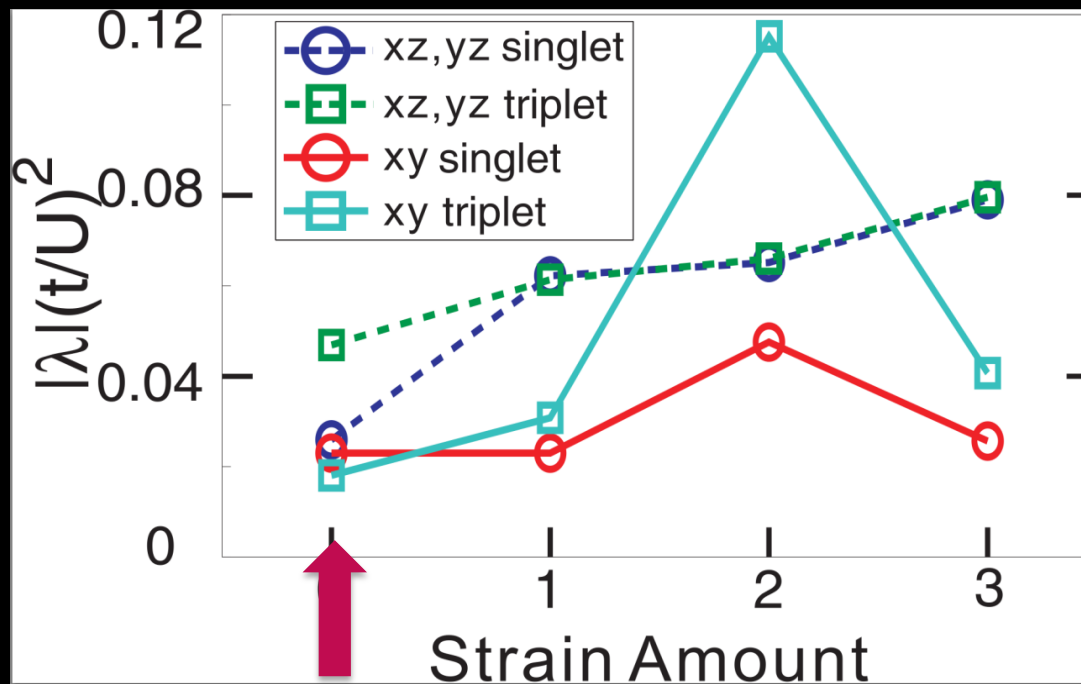
dkishore et al

2.0077

Higher  $T_c$  Topo SC predicted to be dominant in  $Ba_2RuO_4/STO$ , with FM subdominant

# Summary

- Strained Sr/Ba-RuO<sub>4</sub> films: engineer fermiology
- Proximity to vH with poor nesting can lead to higher T<sub>c</sub> topological SC



As grown Sr<sub>2</sub>RuO<sub>4</sub>