



Technische  
Universität  
Braunschweig

*Kavli Institute for Theoretical Physics*

Magnetism, Bad Metals and Superconductivity:  
Iron Pnictides and Beyond  
September 11, 2014

# Superconductivity in Heavy Fermion Systems: Present Understanding and Recent Surprises

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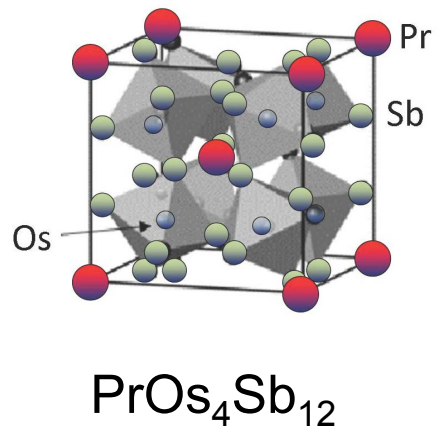
# Outline

1. **Heavy fermion superconductors**
2.  **$\text{Pr}_{1-x}\text{La}_x\text{Os}_4\text{Sb}_{12}$**
3. **Dual character of 5f electrons:  $3=2+1$**
4. **Heavy fermions 4f systems: Kondo scenario**
5. **Renormalized Band method**
6. **Kondo lattices: Instabilities**
7.  **$\text{YbRh}_2\text{Si}_2$**
8. **Summary and outlook**

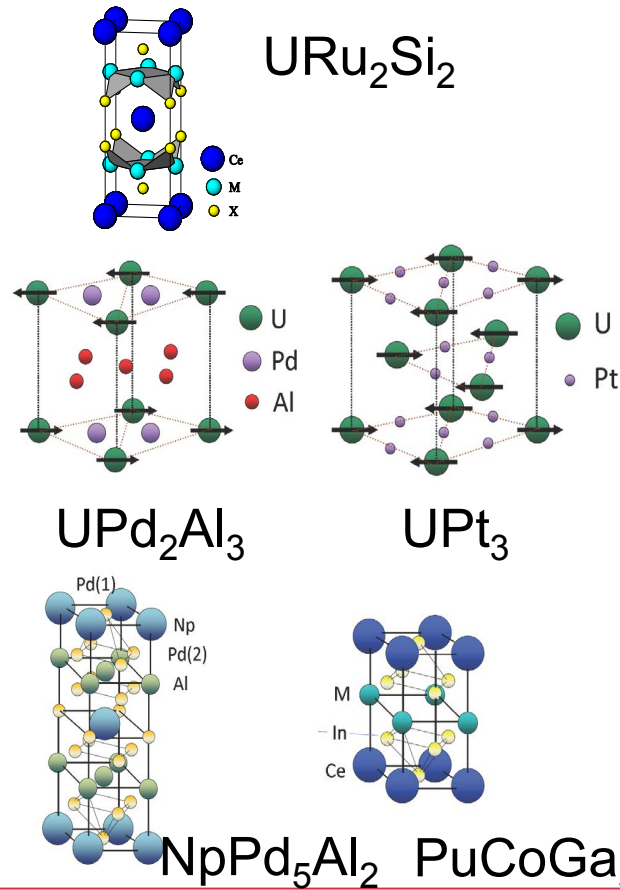


# Heavy Fermion Superconductors: Material classes and typical examples

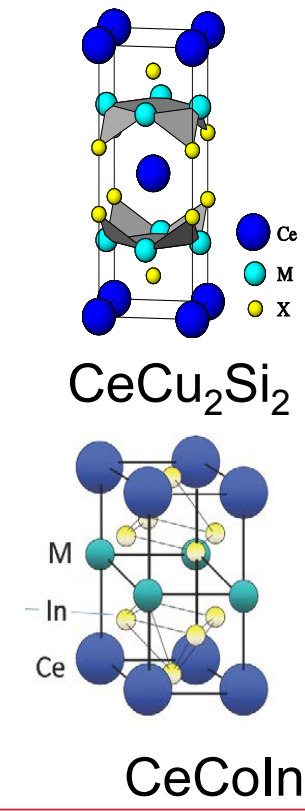
## Pr skutterudites



## Actinide compounds



## Ce compounds



# Heavy fermion superconductors: General properties

- **Normal state**

Usually not so bad metals

Effective Fermi temperature 1-10 meV

However, competing orders => quantum critical points

- **Superconductivity**

Pairing hypothesis works

BCS limit, coherence length  $\xi_0 \gg$  lattice spacing

Pair states unconventional: Symmetry lower than that of lattice

Symmetry classification of pair states accounting for SO interaction

Attractive interaction: Electronic origin



# Heavy fermion superconductors

Formation of the Heavy Fermion state

Partially filled f shells

Strong local correlations => local degeneracies

Characteristic low-energy scale from lifting of local degeneracies

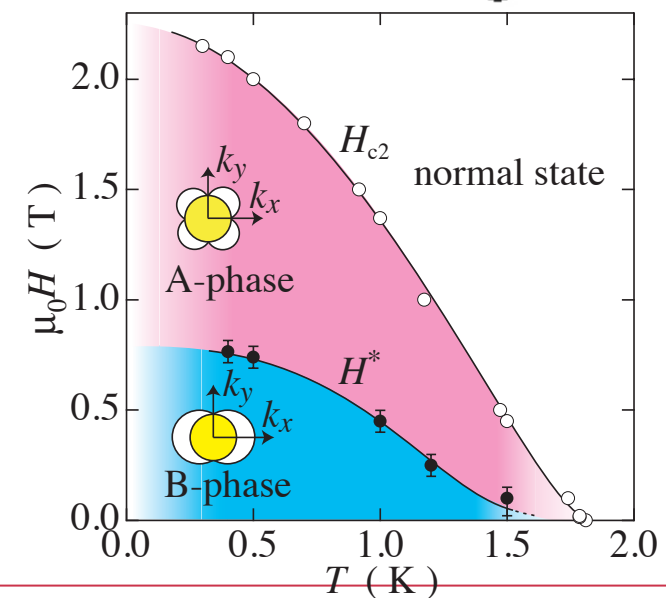
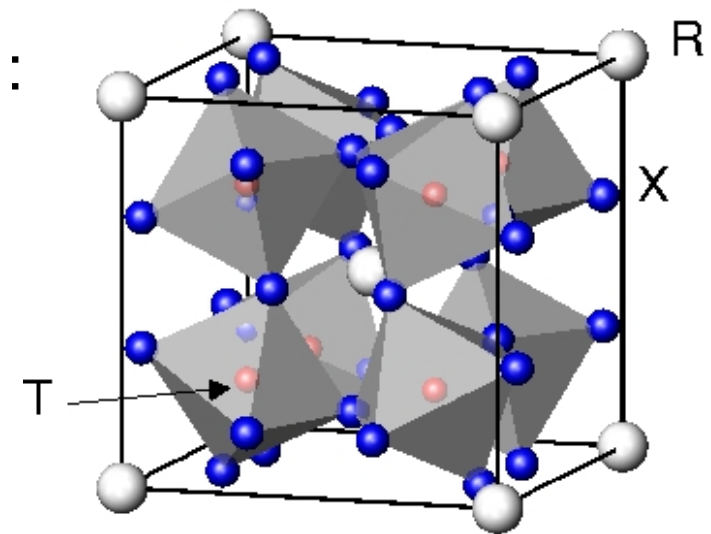
We have to distinguish several cases:

- 4f systems: Stable configurations  $4f^n$   
Non-Kramers vs Kramers ions
- 5f systems: Intermediate-valent systems



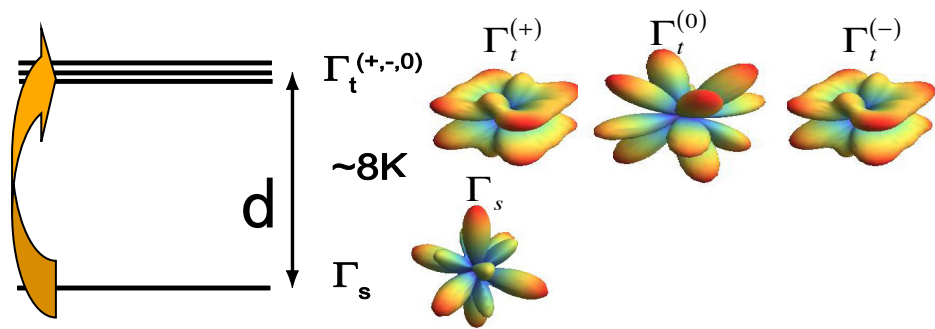
# $\text{Pr}_{1-x}\text{La}_x\text{Os}_4\text{Sb}_{12}$

- Stoichiometric compounds  $x=0$  and  $x=1$ : Fermi liquids
- f-electrons weakly coupled to conduction states
- Mass enhancement due to 4f states  
 $\text{PrOs}_4\text{Sb}_{12}$ :  $\gamma \sim 350\text{-}500 \text{ mJ/mole K}^2$   
 $\text{LaOs}_4\text{Sb}_{12}$ :  $\gamma \sim 36 \text{ mJ/mole K}^2$
- No Kondo effect:  
Pr  $J=4 \Rightarrow$  non-Kramers ion;  
ground state non-degenerate



# Pr<sub>1-x</sub>La<sub>x</sub>Os<sub>4</sub>Sb<sub>12</sub>: Field-dependent mass enhancement

CEF states: T<sub>h</sub> symmetry; Singlet ground state and low-lying triplet; CEF transitions: aspherical Coulomb scattering



## Mass renormalization:

Itinerant conduction electrons  
Scattered off (broadened)  
localized f<sup>2</sup>-excitations



$$\frac{m^*}{m} \sim 1 + \frac{const}{\delta}$$

## Question:

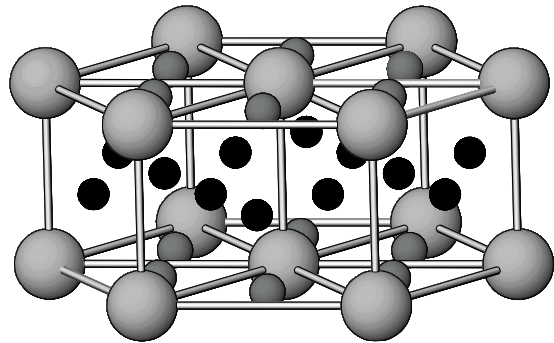
Superconductivity due to “intra-atomic” excitations?

Strong-coupling Eliashberg theory => reasonable Tcs for parameters compatible with mass enhancement

Multi-component order parameter

# Dual character of 5f-electrons: UPd<sub>2</sub>Al<sub>3</sub>

Hexagonal structure **5f moments:**

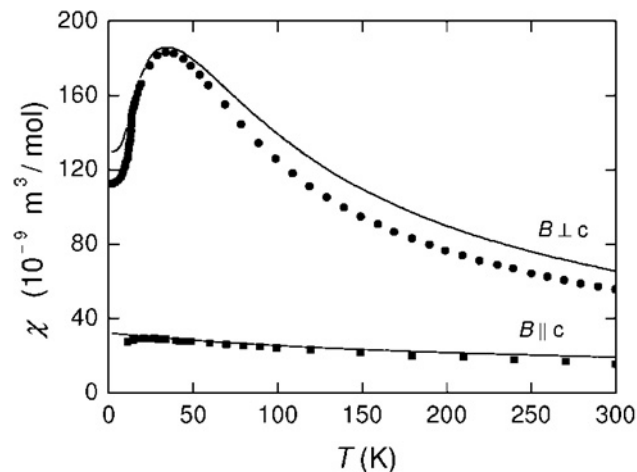


$$T_N = 14.3\text{K}; \quad m = 0.85 m_B$$

**5f bands**

$$\gamma = 140 \text{ mJ/mole K}^2$$

$$T_c = 1.8\text{K}; \quad \Delta C = 1.2\gamma T_c$$



Anisotropic static magnetic susceptibility  
(Grauel et al., 1992)

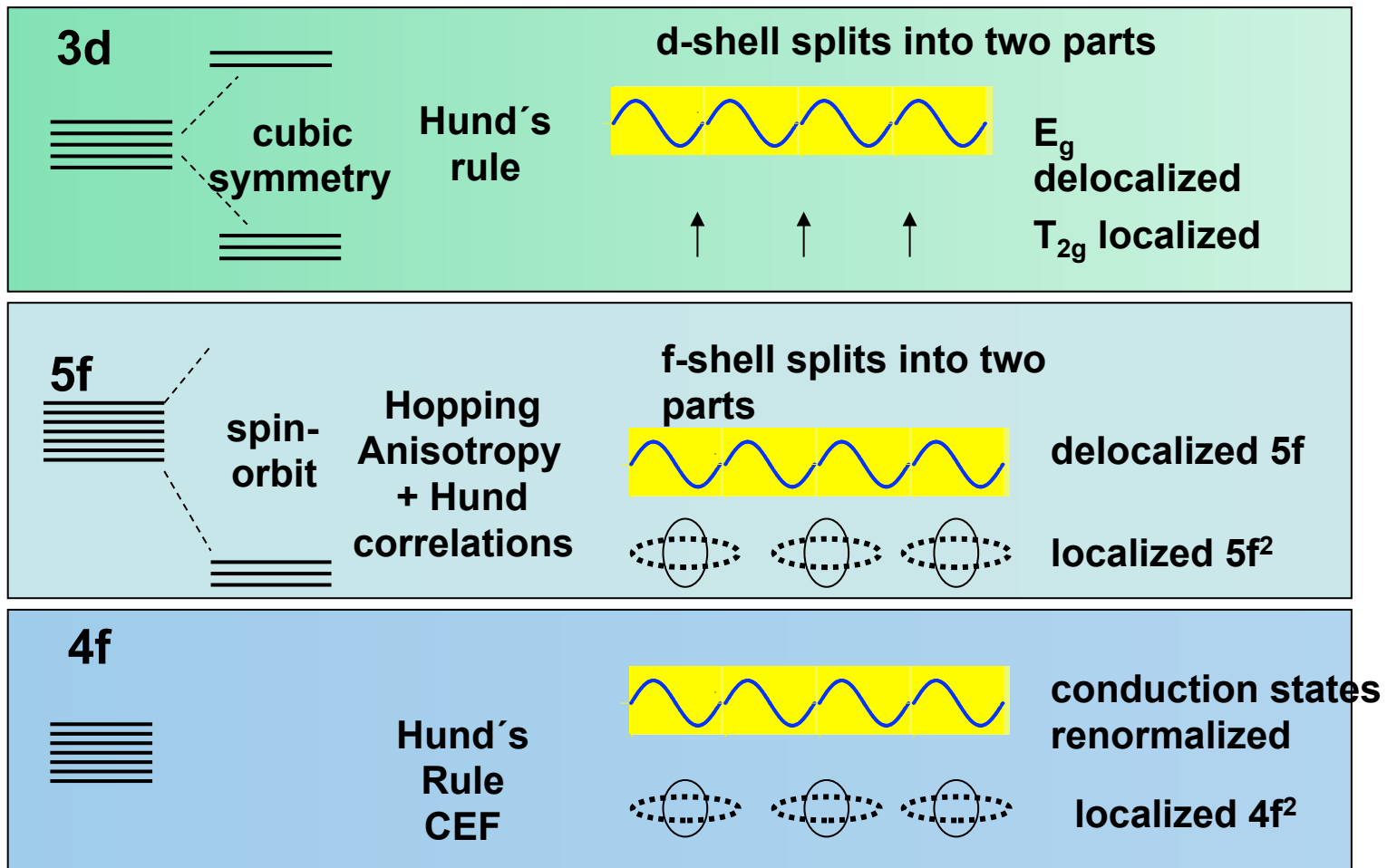
Analysis:

CEF-states of f<sup>2</sup>-configuration  
(Shiina, 2001)





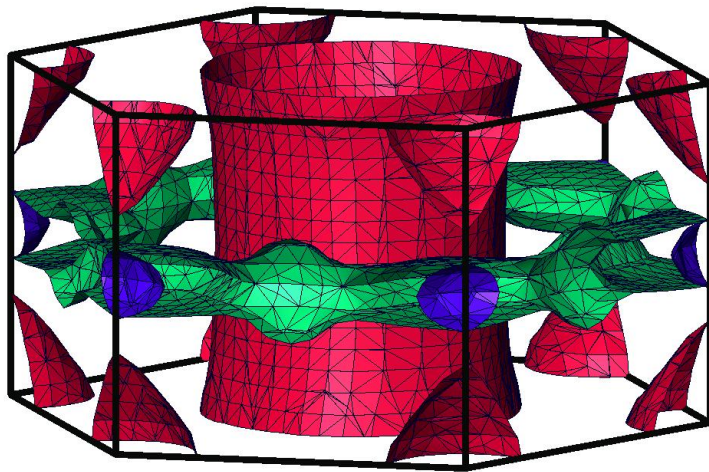
# Dual character of 5f-electrons



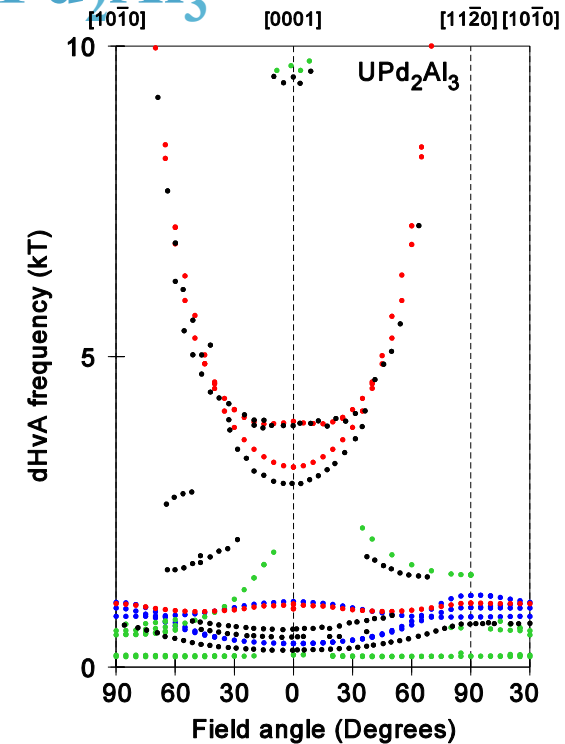
# Dual character of 5f electrons: UPd<sub>2</sub>Al<sub>3</sub>

Co-existence of delocalized and localized 5f electrons

UPd<sub>2</sub>Al<sub>3</sub>: Fermi surface and effective masses reproduced by dual model



Exp: Inada et al (1999)  
Th : GZ et al (2003)

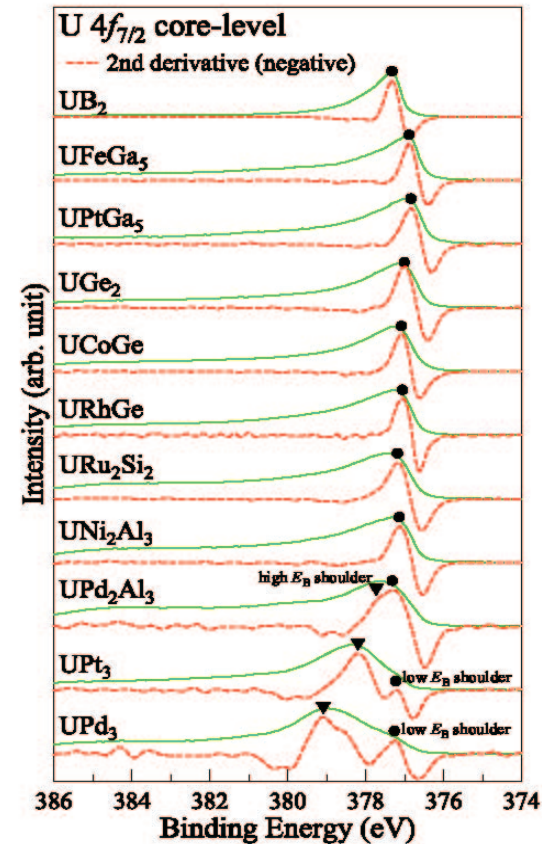
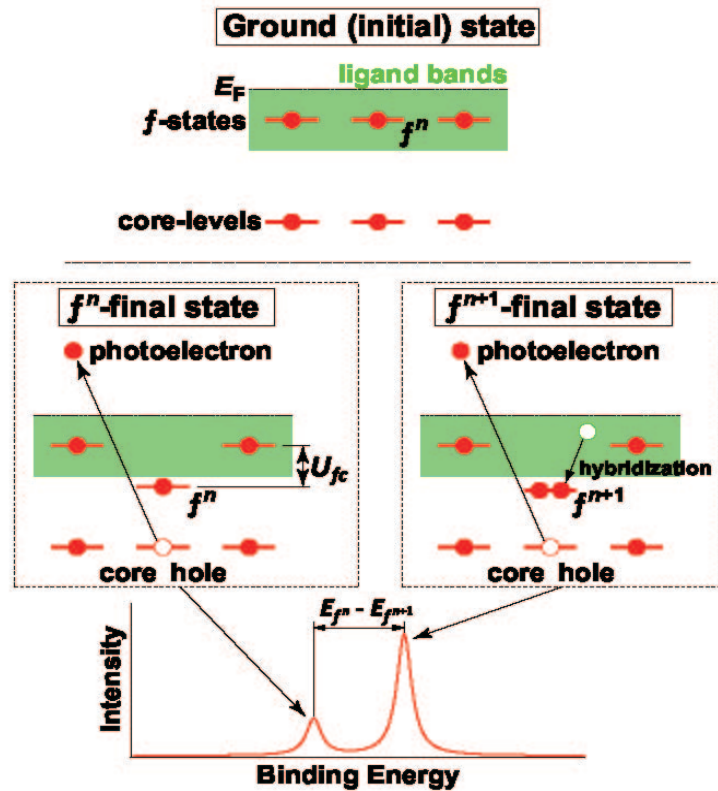


Branch	Exp	Theory
$\gamma$	33	31.9
$\beta$	19	25.1
$\varepsilon_2$	18	17.4
$\varepsilon_3$	12	13.4
$\alpha$	5.7	9.6
$\zeta$	65	59.6



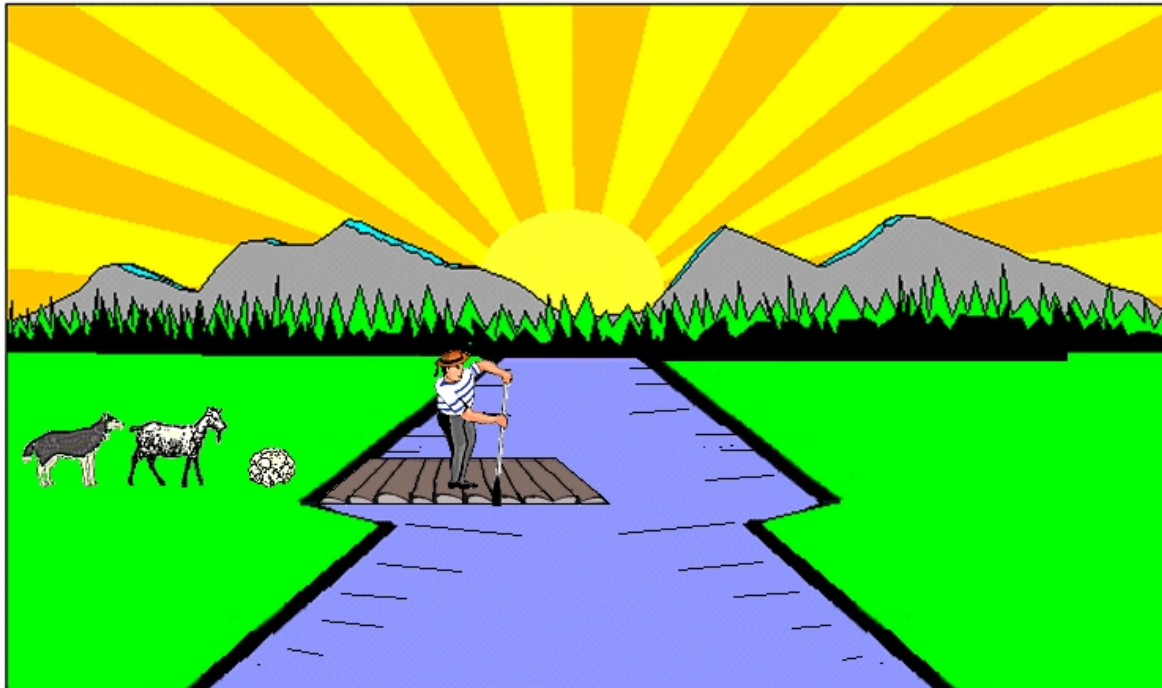
# Dual character of 5f electrons: Core-Level PES Experiment

Localization vs delocalization reflected in screening properties



From S.-i. Fujimori et al, JPSJ (2011)

# Dual character of 5f electrons – a correlation effect



Orbital-selective Mott transition due to competition between anisotropic hybridization and Hund's rule correlations



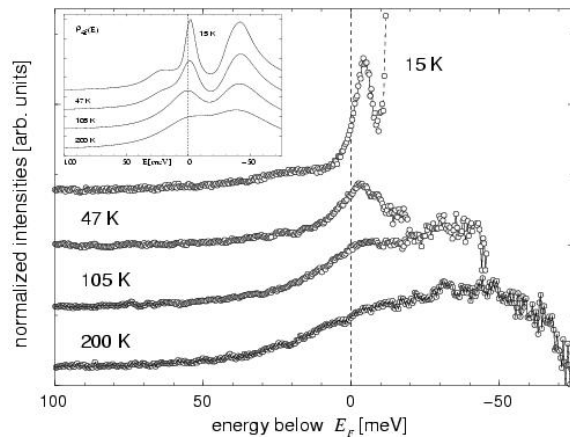
# Dual character of 5f electrons

## Unusual properties of actinide-based SC

- Co-existence of SC and ferromagnetism
- Hidden order in  $\text{URu}_2\text{Si}_2$
- High  $T_c$ s in Pu-compounds
- ...



# Heavy Fermions in 4f-systems: Kondo scenario



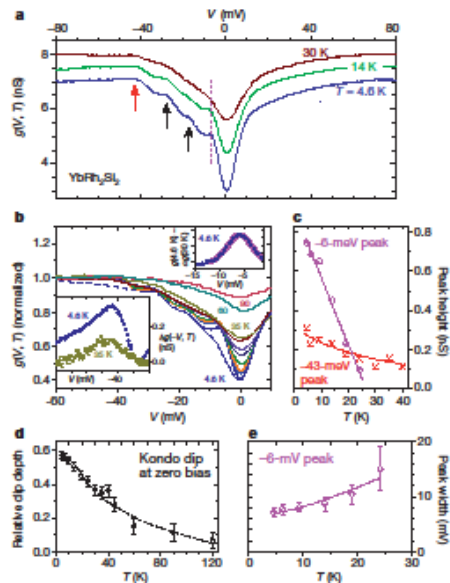
## PES

Kondo resonance in  $\text{CeCu}_2\text{Si}_2$   
(Reinert et al (2001))

Detailed studies in Yb-systems

## STM

Formation of the local Kondo singlet  
Coherence effects from the periodic  
lattice



## LETTER

doi:10.1038/nature

## Emerging local Kondo screening and spatial coherence in the heavy-fermion metal $\text{YbRh}_2\text{Si}_2$

S. Ernst<sup>1</sup>, S. Kirchner<sup>1,2</sup>, C. Krellner<sup>1</sup>, C. Geibel<sup>1</sup>, G. Zwirner<sup>1</sup>, F. Steglich<sup>1</sup> & S. Wirth<sup>1</sup>

# Heavy fermions in 4f-systems

## Construction of realistic models:

Electrons scatter off (effective non-local) potentials at atomic sites

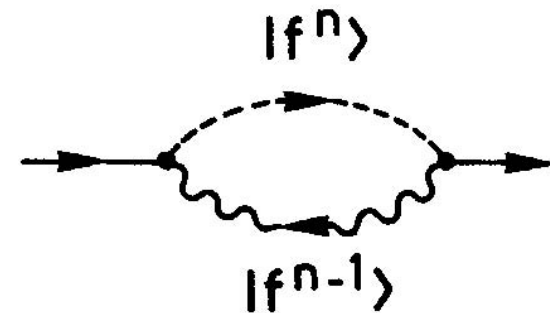
Material-specific information: single-site t-matrix

Kondo lattice:

Use many-body single-site t-matrix for 4f-channels

4f spectral function

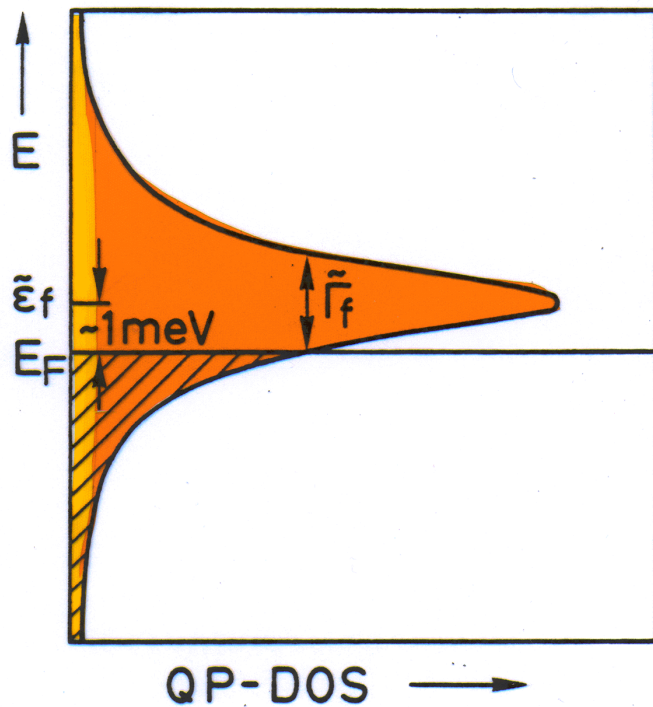
Resonant structure at low temperatures  
parametrization



Non-4f states: t-matrix from standard band structure (DFT)

# Renormalized Band method

Quasiparticle bands



**Phase shift:**  $\tilde{\eta}_f = \arctan \frac{\tilde{\Gamma}_f}{\tilde{\epsilon}_f - E}$

Condition: No re-distribution of charge  $\Rightarrow \tilde{\epsilon}_f$

Single parameter  $\tilde{\Gamma}_f$  adjusted to specific heat

**Magnetic field:** H-dependent parameters

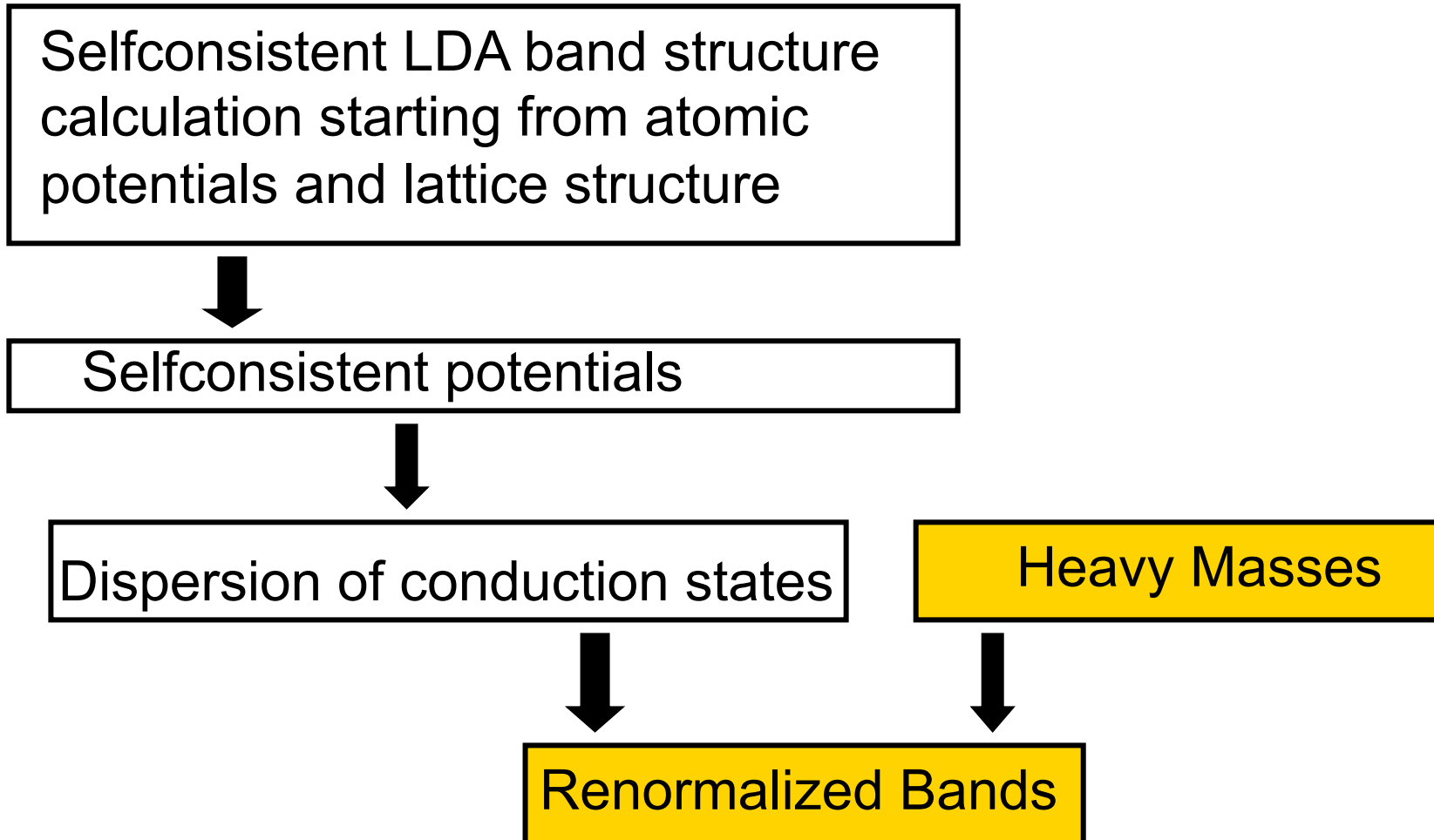
$$\tilde{\epsilon}_f(H) , \tilde{\Gamma}_f(H)$$





# Renormalized Band method

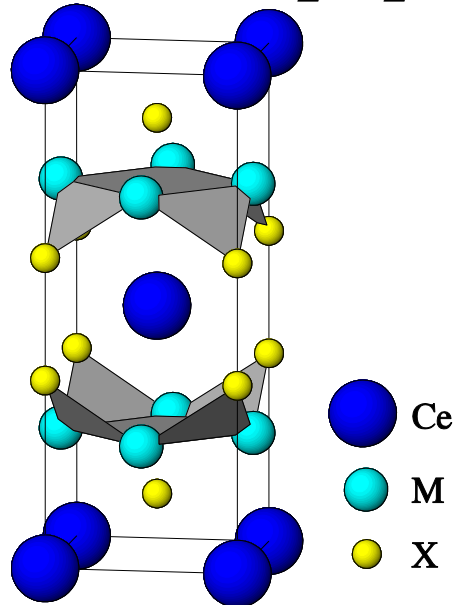
## Calculational scheme:



# Renormalized Band method

## Confirmation of the quasiparticle model

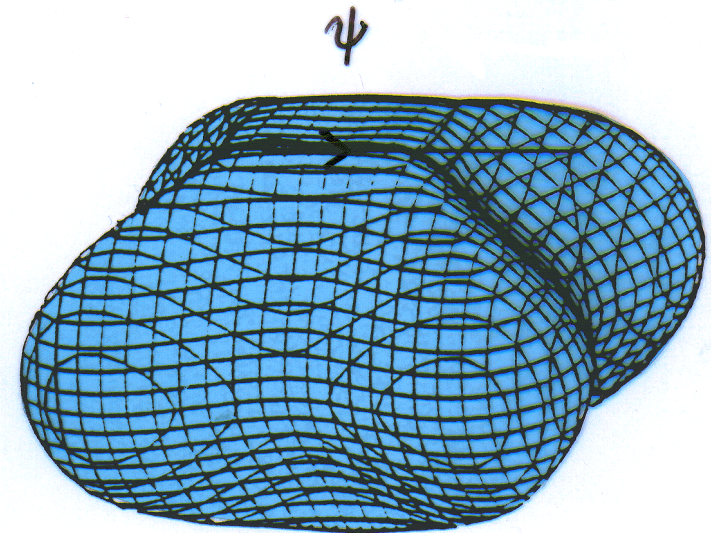
$$\text{CeRu}_2\text{Si}_2 \quad \gamma \sim 350 \text{ mJ} / (\text{mole K}^2)$$



Fermi surface for Heavy Fermions in  
(GZ, E. Runge, N. E. Christensen,  
Physica B 163, 97 (1990))

Experimentally confirmed  
Aoki et al., PRL 72,797 (1992)

Effective mass consistent with  
specific heat

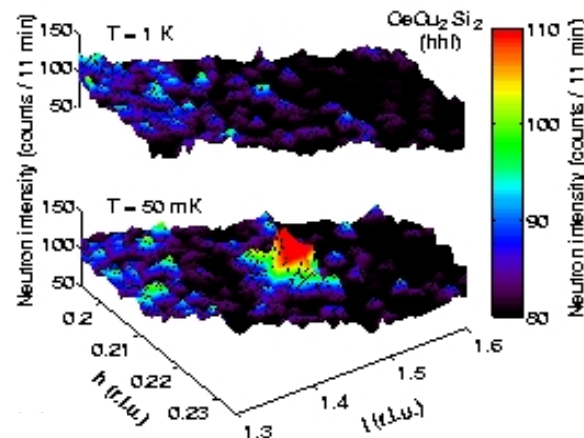


# Kondo lattices: Instabilities of the heavy Fermi liquid

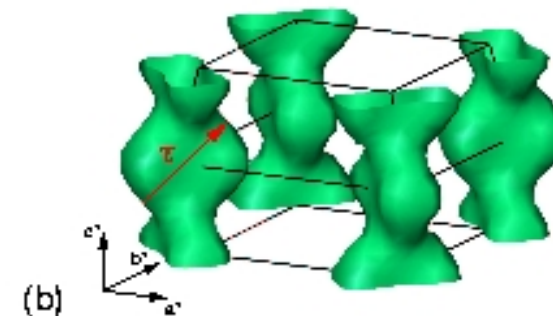
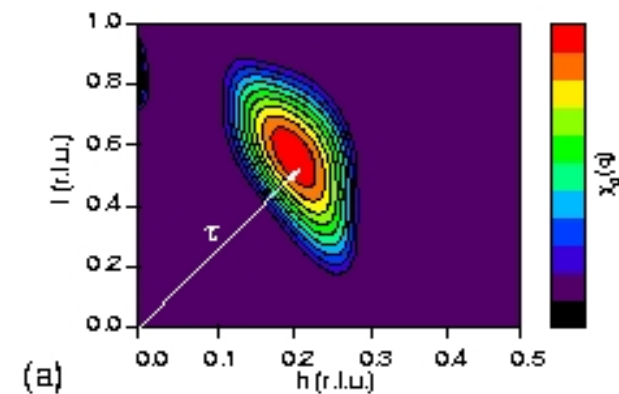
## Spin density wave of heavy fermions in $\text{CeCu}_2\text{Si}_2$

(E. Faulhaber et al PRL **92**, 136401(2004))

Inelastic neutron scattering



Calculated susceptibility of the heavy quasiparticles

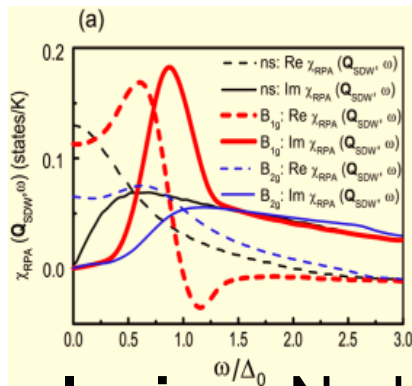
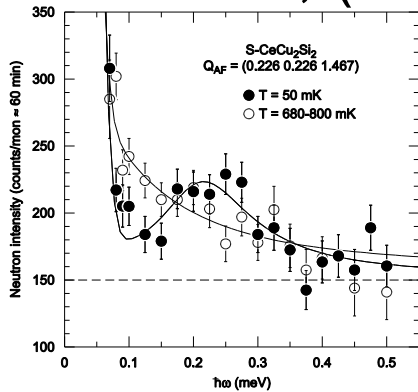


# Kondo lattices: Instabilities of the heavy Fermi liquid

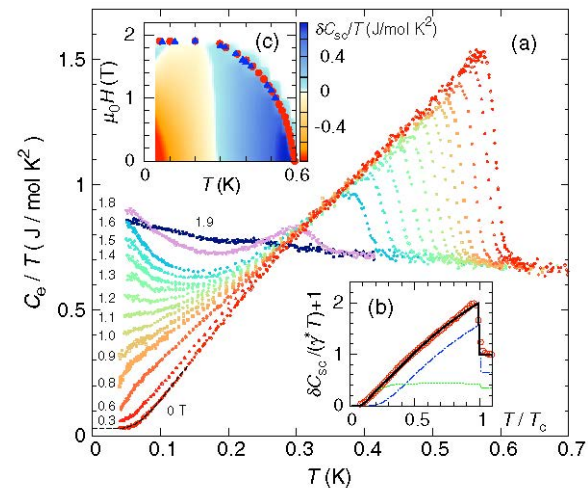
## Resonance peak in superconducting CeCu<sub>2</sub>Si<sub>2</sub>

O. Stockert et al (2008)

I. Eremin et al, (2008)



**Surprise and open question:**  
Exponential specific heat at low T  
Shunichiro Kittaka et al., 2013

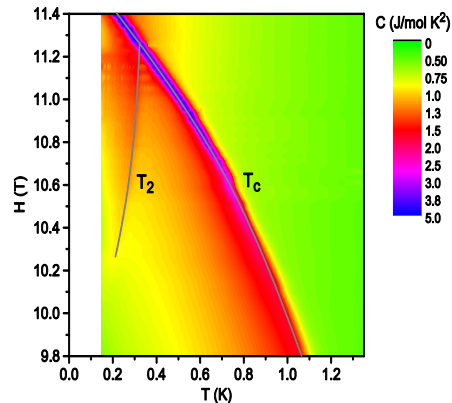


**Conclusion:** Nodal superconducting order parameter  $\Delta(\mathbf{k}) : \cos k_x - \cos k_y$



# Kondo lattices: Instabilities of the heavy Fermi liquid

## Inhomogeneous superconducting state in $\text{CeCoIn}_5$

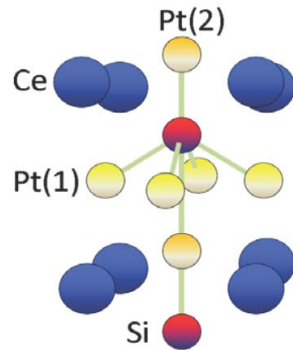


A. Bianchi et al. (2003)

Modulation vector

Complicated interplay with af order  $q \sim a \gg \xi$  weak B dependence => not FFLO

## Unusual properties in non-centrosymmetric SC: $\text{CePt}_3\text{Si}$



Strong SO interaction

Order parameter superposition of singlet and triplet

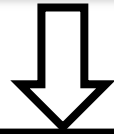


# YbRh<sub>2</sub>Si<sub>2</sub>: Nature of the Quantum Critical Point?

Material-specific treatment of highly correlated metals  
Periodic lattice

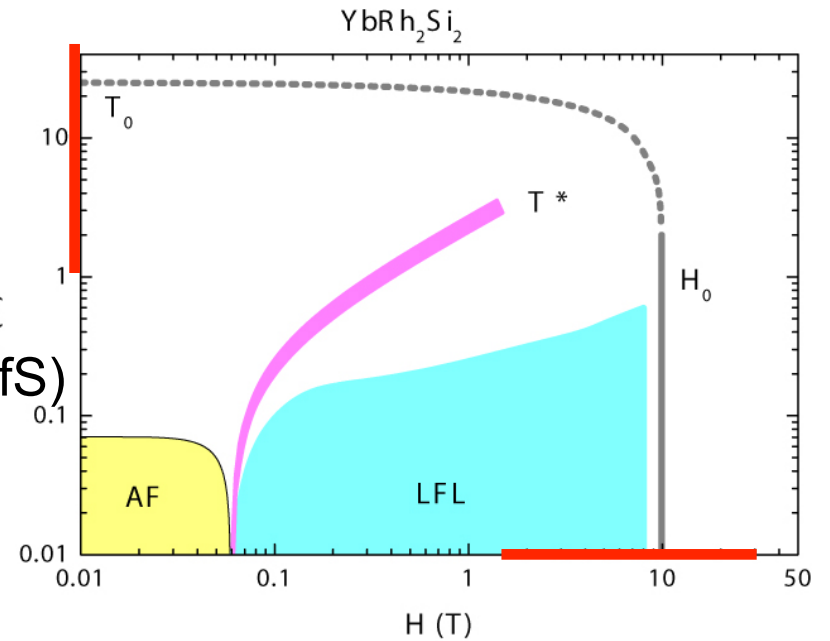


Experimental properties



Identification of unusual phases  
Characterization of reference states  
Nature of quantum phase transitions

ARPES (TUD)  
RXES (ESFR)  
STM (CPfS)  
...



Transport  
CPfS, Grenoble

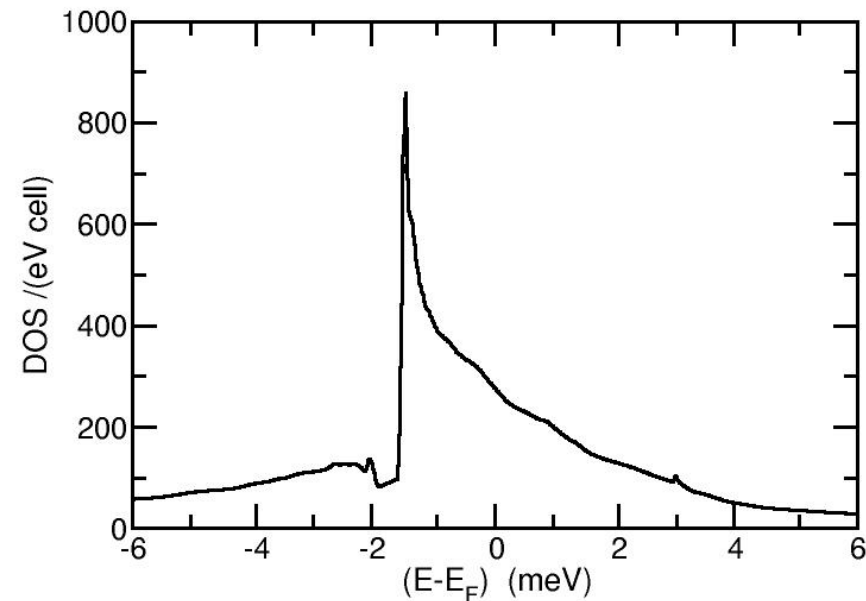
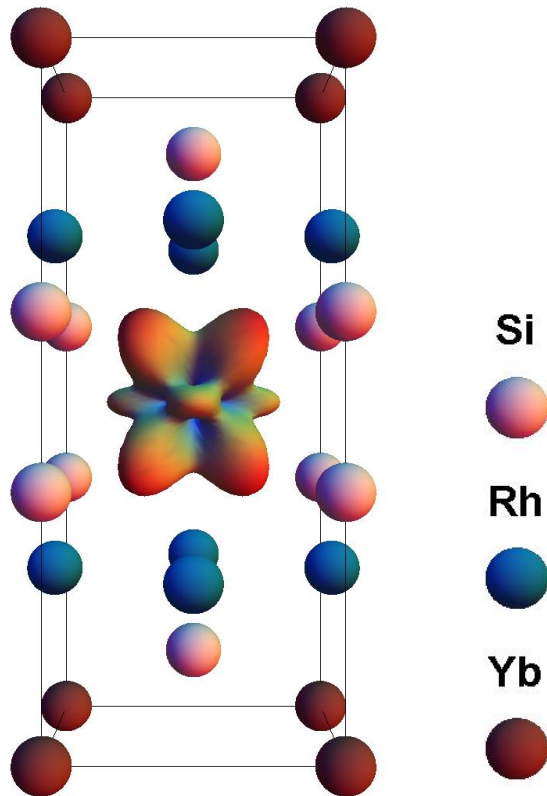


# YbRh<sub>2</sub>Si<sub>2</sub>: Heavy quasiparticles in high magnetic fields

**CEF ground state:** Weak hybridization with conduction states

Anisotropic effective masses, flat dispersion in large parts of BZ

=> van Hove-type singularity in DOS

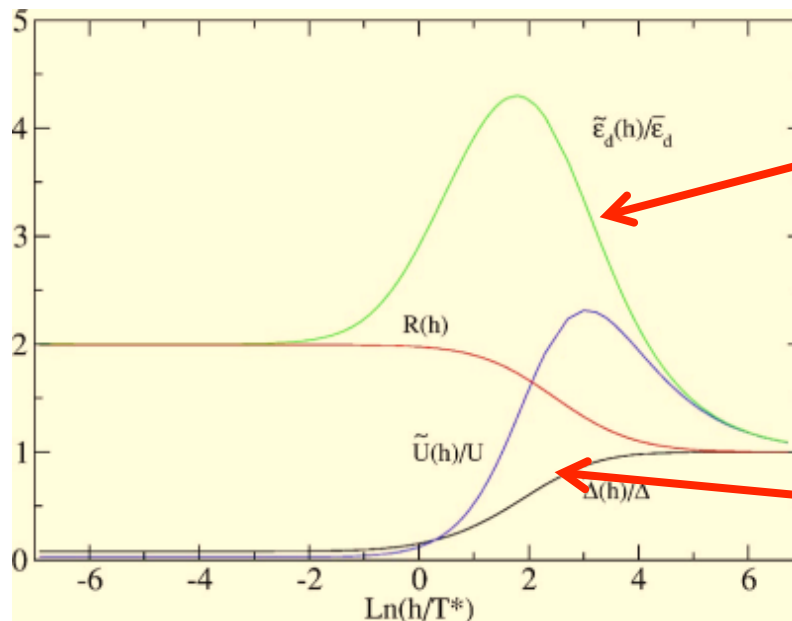


# YbRh<sub>2</sub>Si<sub>2</sub>: Heavy quasiparticles in high magnetic fields

## QP parameters:

Fit to DOS from Numerical Renormalization Group: Highly non-trivial variation with H (Hewson, Bauer (2007), Peters et al (2006)), Anders )

## Example: Particle-hole symmetric case



Zeeman splitting:  
enhanced over free-particle value  
non-monotonic

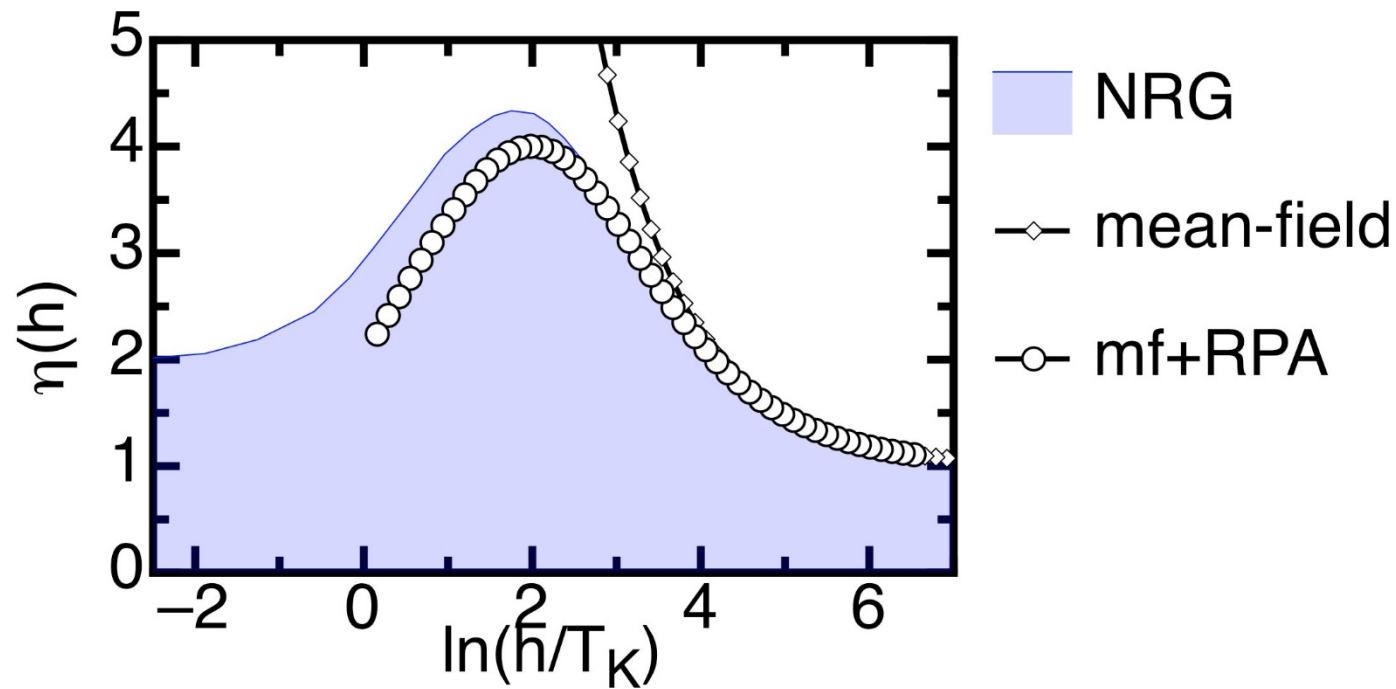
Effective band width





# YbRh<sub>2</sub>Si<sub>2</sub> : Field-dependent qp parameters

Origin of non-monotonic variation with field of enhanced Zeeman splitting



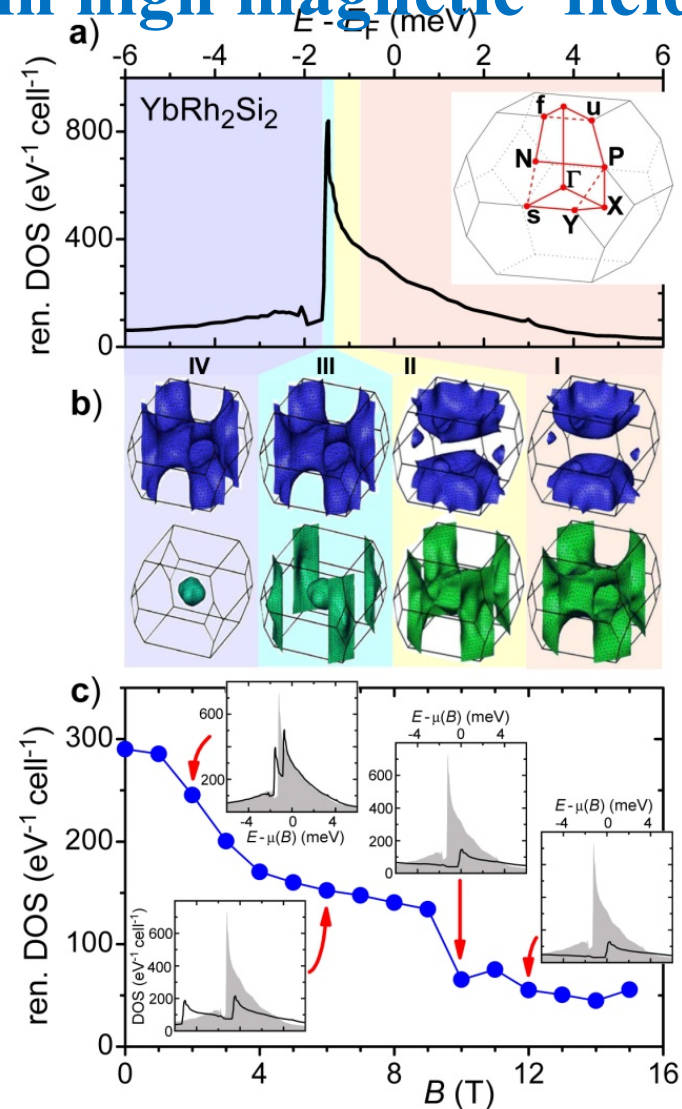
# YbRh<sub>2</sub>Si<sub>2</sub>: Heavy quasiparticles in high magnetic fields

Minority Fermi surface undergoes a series of Lifshitz-transitions

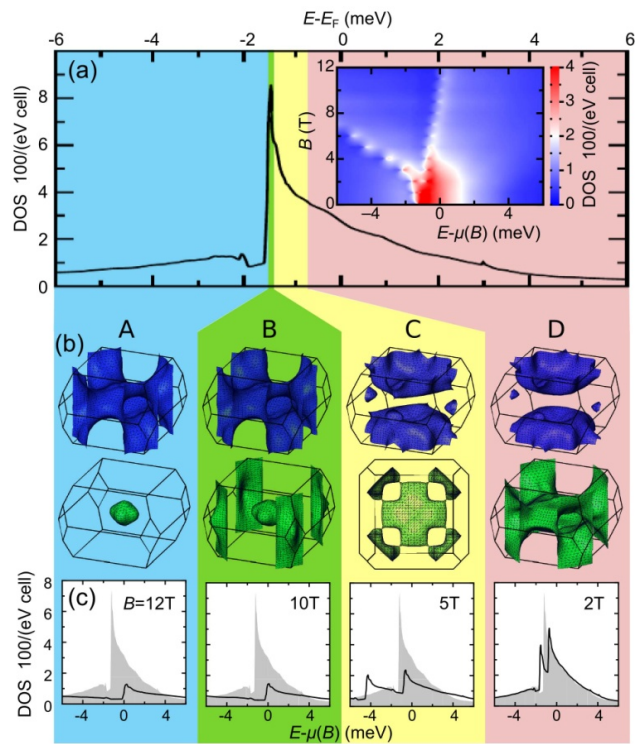
Observed anomalies in thermodynamic and transport properties

Topology of high-field FS differs from H=0 result

GZ, J. Phys.: Condens. Matter (2011)

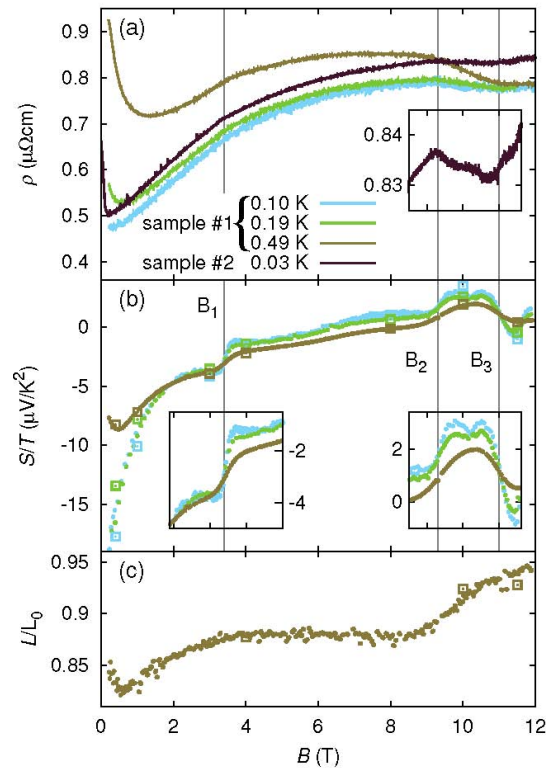


# YbRh<sub>2</sub>Si<sub>2</sub>: Heavy quasiparticles in high magnetic fields



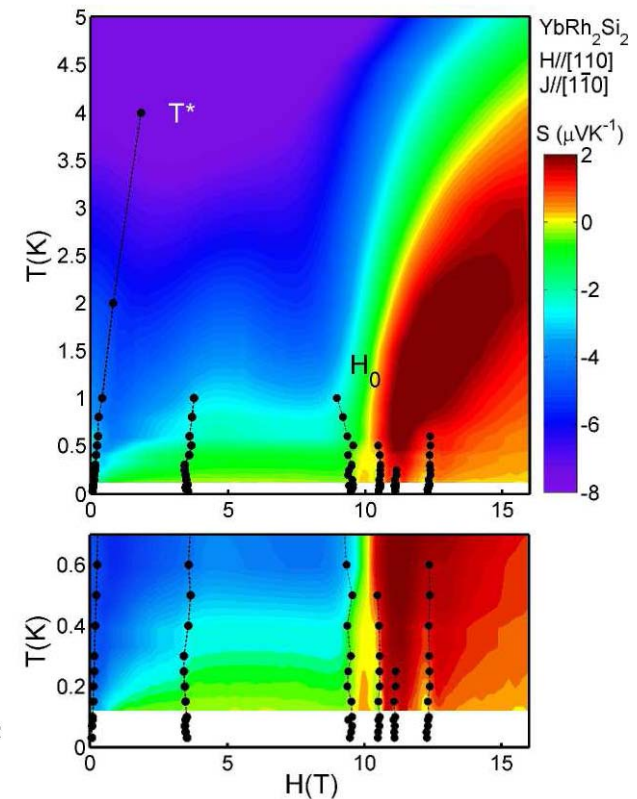
Four major +several small regimes around B=11 T (not displayed here)

Quasiparticle de-renormalization+Sommerfeld-Wilson ratio+ CEF states => Structures at characteristic fields: Lifshitz transitions



H. Pfau et al

PRL **110**, 256403 (2013) **82** (2013) 053704

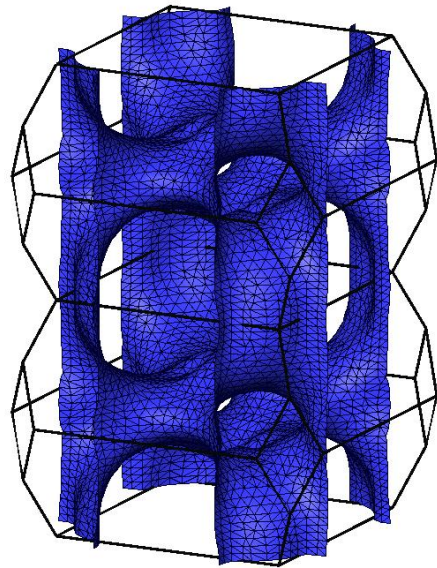


A. Pourret et al., JPSJ

# YbRh<sub>2</sub>Si<sub>2</sub>: Heavy quasiparticles in high magnetic fields

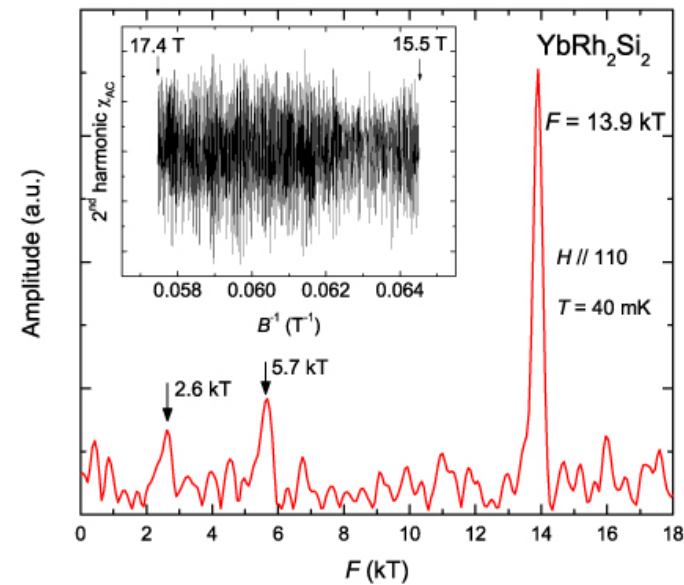
YbRh<sub>2</sub>Si<sub>2</sub>

Quantum oscillations show closed orbit in narrow angle range



$B \parallel 110$

$F \sim 13 \text{ kT}$

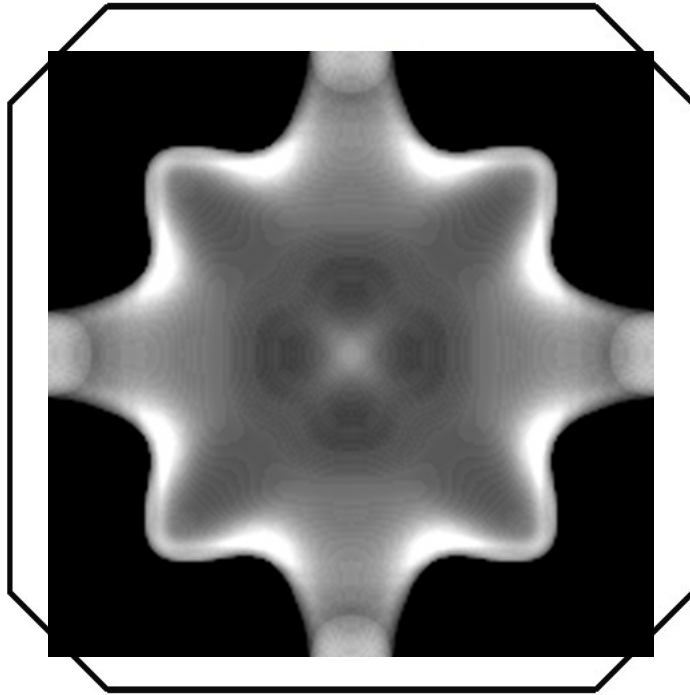


T. Westerkamp (2008)

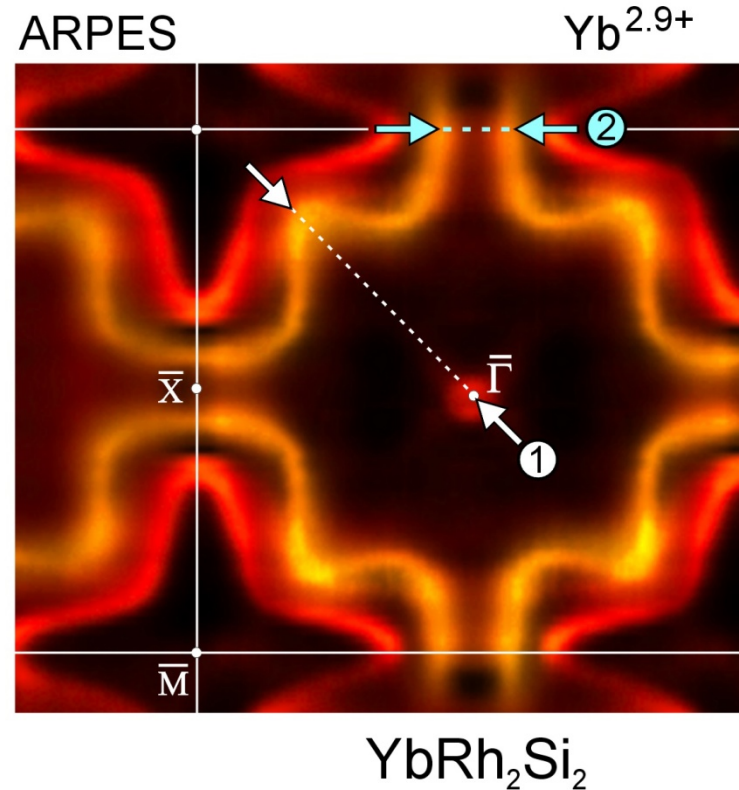


# YbRh<sub>2</sub>Si<sub>2</sub>: Fermi surface

ARPES : B=0, paramagnetic



0 50000 100000  
Fermi velocity in (m/s)

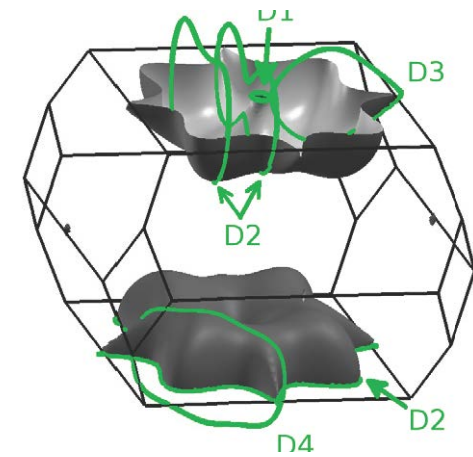
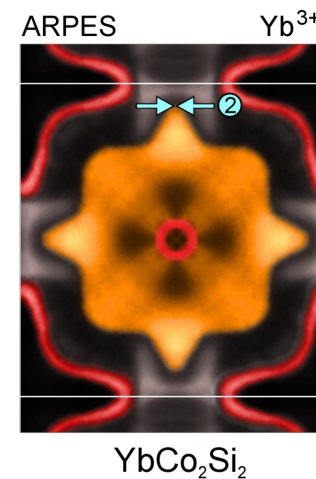
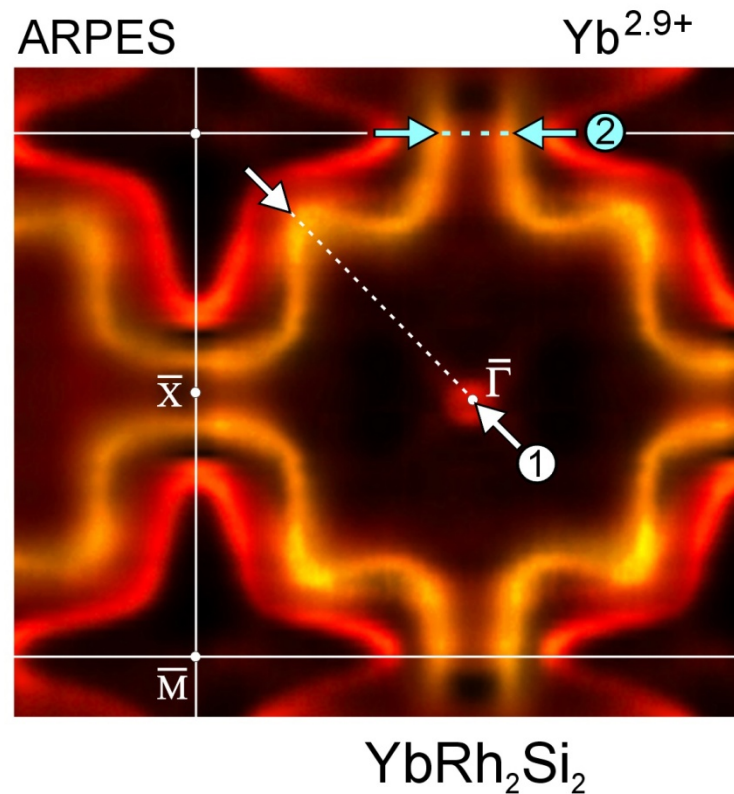


K. Kummer et al (2014)

Low T, low B FS confirmed

# Work in progress: Photoemission from $\text{YbRh}_2\text{Si}_2$ at elevated T

ARPES: f delocalized vs 4f localized



K. Kummer et al (2013)

Relevant temperature scale?

# YbRh<sub>2</sub>Si<sub>2</sub>: 4f spectral function at elevated T

## Theory:

Calculate 4f-spectral function for lattice from 4f propagator

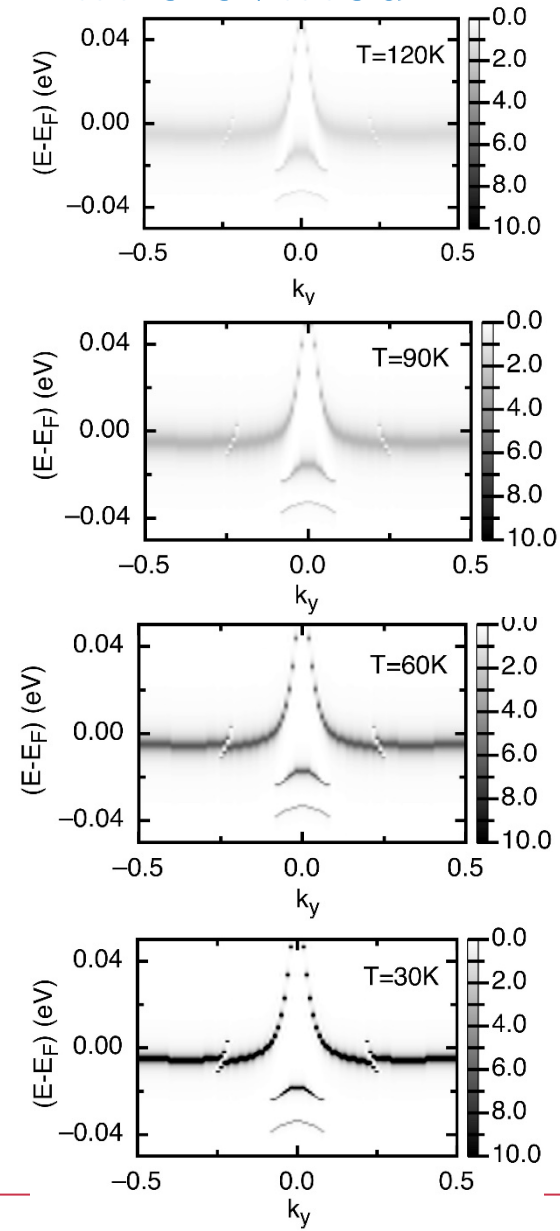
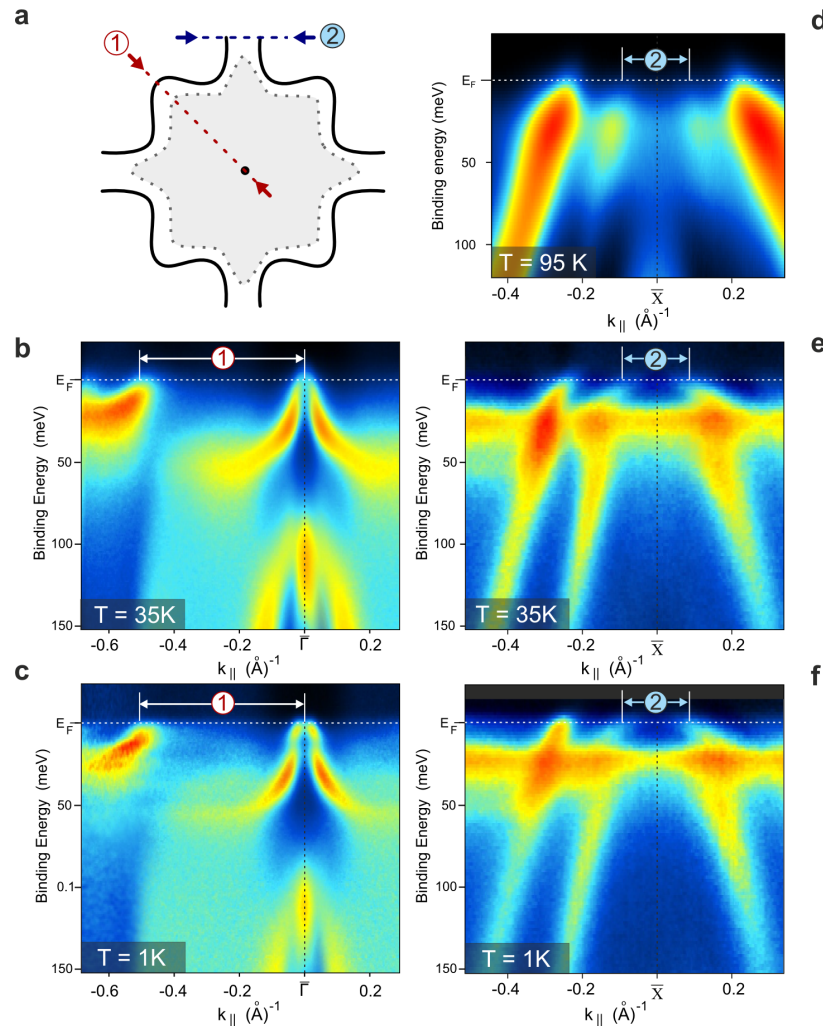
$$\mathbf{G}_{4f}^{-1}(\mathbf{k}\omega; T) = \underbrace{\mathbf{g}_{4f}^{-1}(\omega; T)}_{\substack{\text{local 4f-propagator} \\ \text{T-dependence}}} - \underbrace{\sum_n \left( \mathbf{W}_{n,n}(\mathbf{k}\omega; T) - \sum_{\mathbf{k}} \mathbf{W}_{n,n}(\mathbf{k}\omega; T) \right)}_{\substack{\text{hybridization with conduction states} \\ \text{weak T-, } \omega\text{-dependence}}}$$

Use single-impurity propagator

Close-to-integer limit => small transfer of spectral weight between Kondo resonance and charge fluctuation peak  
=> Keep conduction bands fixed

Rather smooth cross-over expected

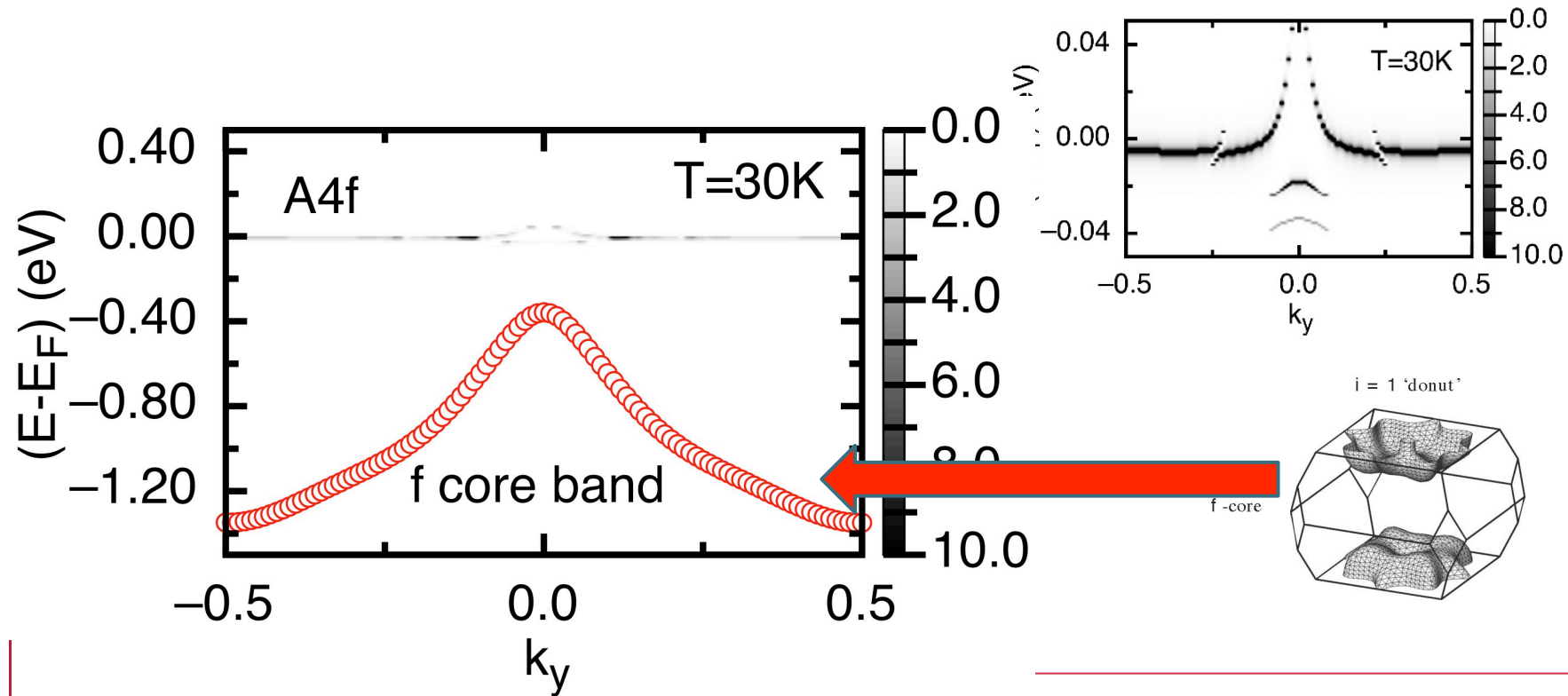
# YbRh<sub>2</sub>Si<sub>2</sub>: 4f spectral function at elevated T





# YbRh<sub>2</sub>Si<sub>2</sub>: 4f spectral function at elevated T

Comparison: 4f spectral function and f core band



# YbRh<sub>2</sub>Si<sub>2</sub>: Critical quasiparticles (?)

PHYSICAL REVIEW B **90**, 045105 (2014)

## Strong-coupling theory of heavy-fermion criticality

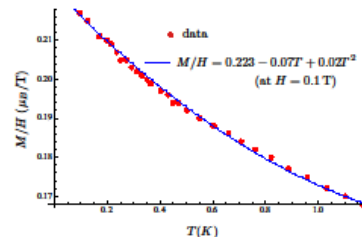
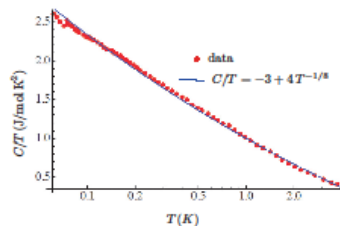
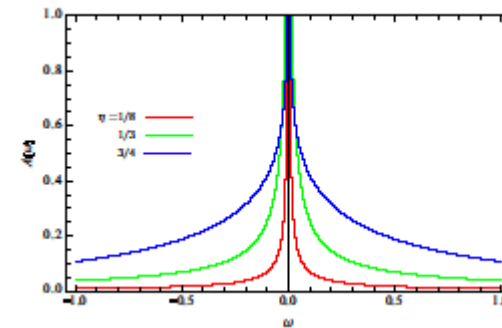
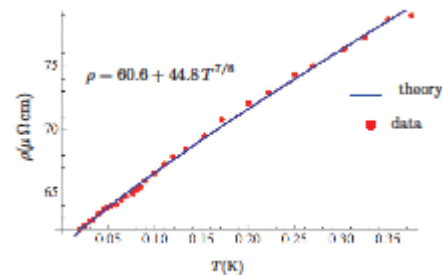
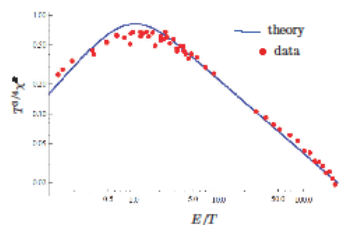
Elihu Abrahams,<sup>1</sup> Jörg Schmalian,<sup>2</sup> and Peter Wölfle<sup>2,3</sup>

<sup>1</sup>Department of Physics and Astronomy, University of California Los Angeles, Los Angeles, California 90095, USA

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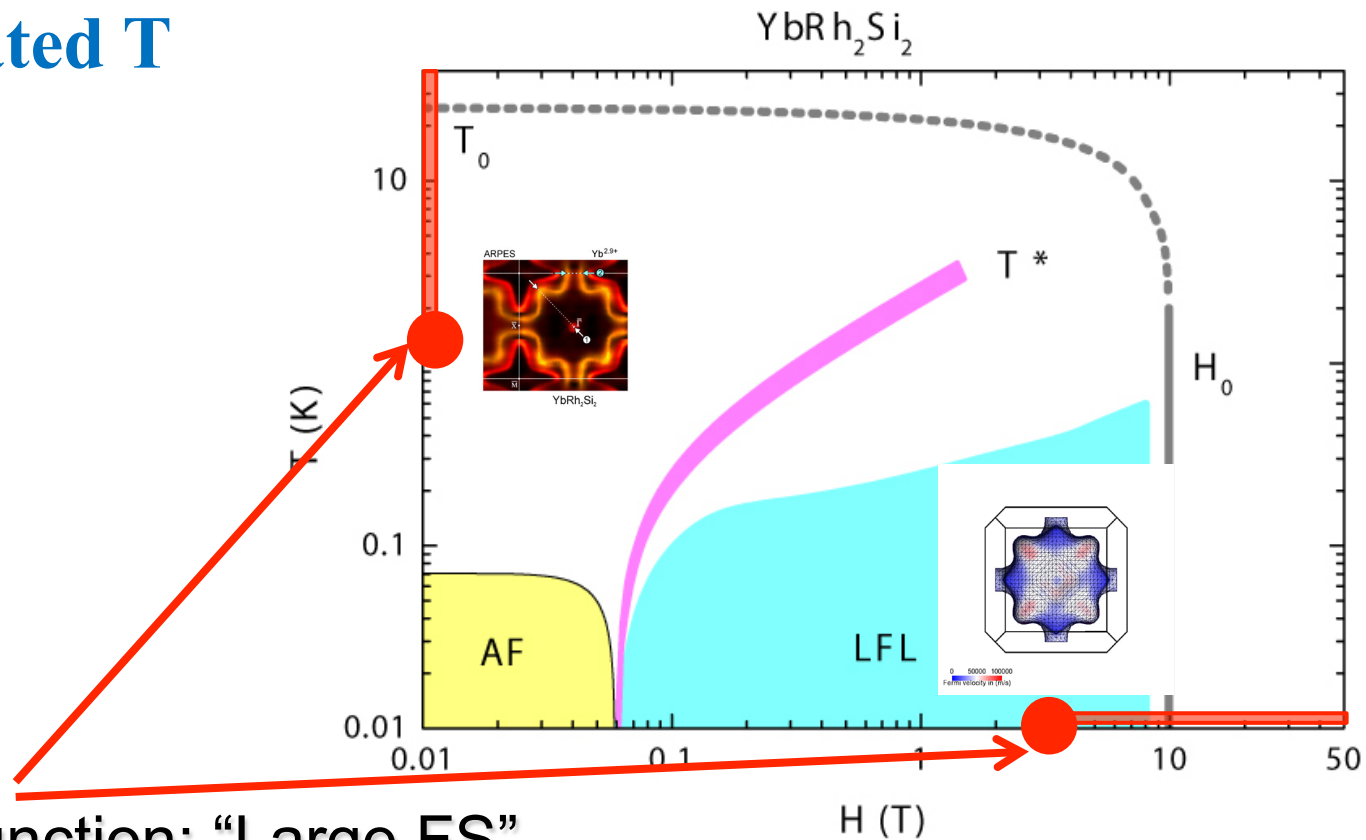
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Finally, we emphasize that we assumed the heavy quasiparticles to be robust, though modified by scattering from critical spin fluctuations. There is no breakdown of the Kondo effect nor an associated collapse of part of the Fermi surface in our scenario. Experimental features, such as the crossover behavior observed in transport properties (and, to a lesser extent, in the thermodynamic quantities) across the “ $T^*$  line” in the  $T$ - $H$  phase diagram of YRS, may be accounted for by a change in quasiparticle scattering strength associated with thermal activation of the (ESR) spin resonance as well as by single-quasiparticle spin-flip scattering [29,30].



# Work in progress: Photoemission from $\text{YbRh}_2\text{Si}_2$ at elevated T



Spectral function: “Large FS”

Variation with B and T from de-renormalization of heavy quasiparticles due to local break-up of Kondo singlets

**“Small” FS related to magnetic order? Meaning of the  $T^*$ -line?**

## Instead of summary and outlook ...

### Questions in HF superconductivity

1. Actinides: 5f valence => Hidden order
2.  $\text{CeCu}_2\text{Si}_2$ : order parameter nodes
3.  $\text{CeCoIn}_5$ : Modulated sc state
4. Ce- Yb asymmetry
5. Nature of QCPs
6. 4f spectral functions at elevated T
7. ....

