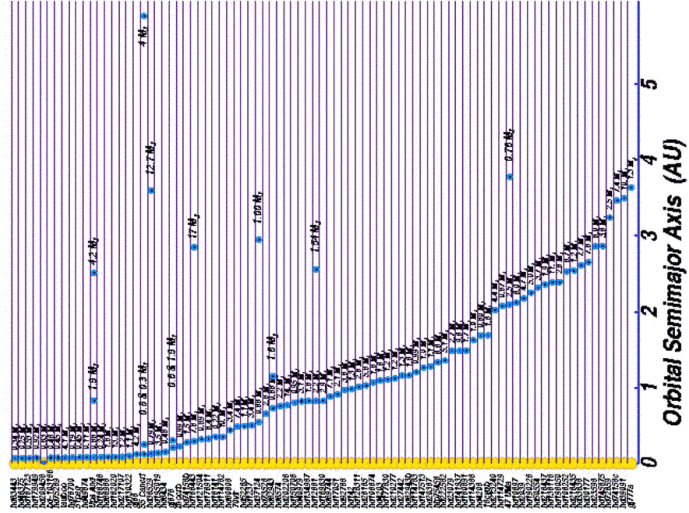


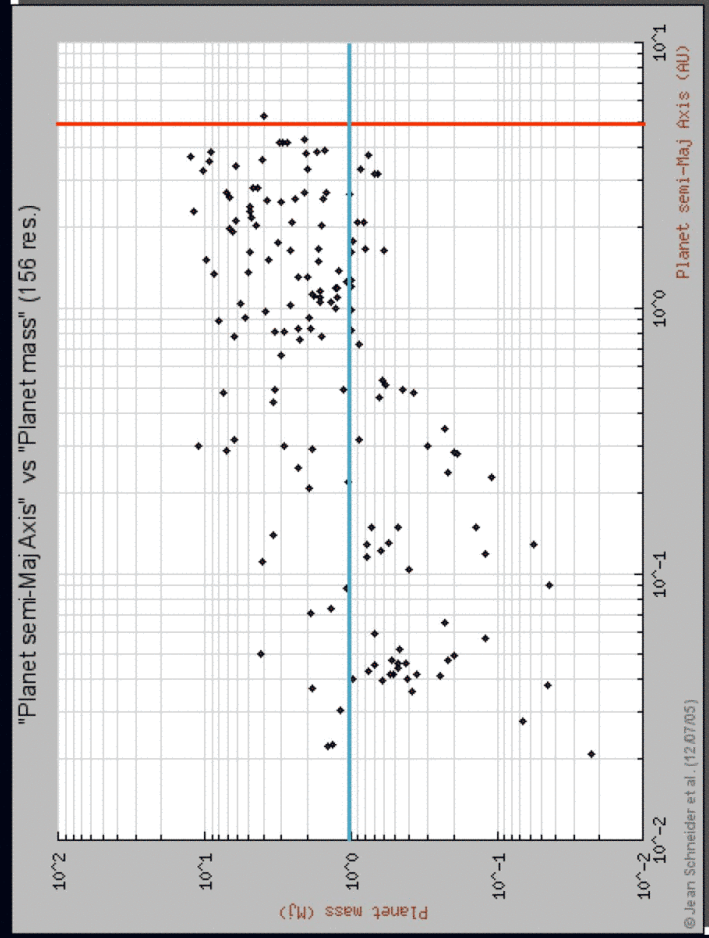


Extrasolar Planets

161 planetary systems
137 planets
18 multiple systems



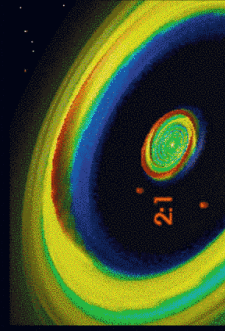
Characteristics of extrasolar planets



What do we need migration for ?



✓ **Hot Jupiters:** forming planets
at small distances:
too hot
not enough material



✓ **Planets in resonances:**
capture

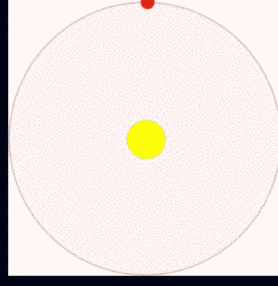
Planet migration

- ✓ Interaction between 2 or more Jupiter-mass planets \rightarrow orbit crossing \rightarrow collision or ejection

(Rasio & Ford '96, Weidenschilling & Marzari '96)

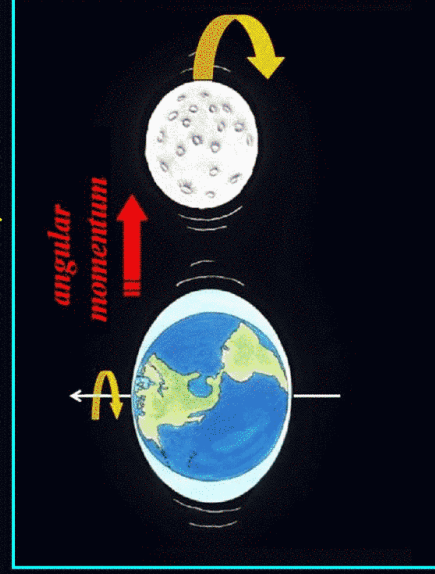
- ✓ “Migration instability”: resonant interaction between planet and planetesimals \rightarrow ejection of planetesimals.
Requires massive disks...

(Murray et al. '98)

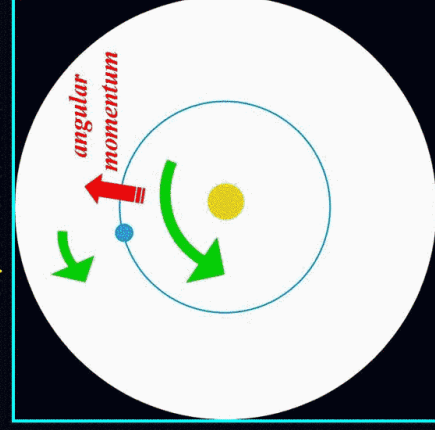


Tidal torques

Earth-Moon system



Keplerian disk



(Goldreich & Tremaine '79)

Type I migration

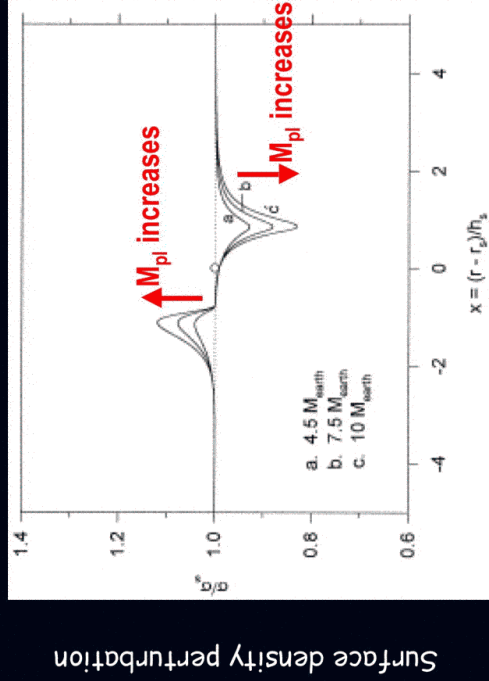
Difference between the torque exerted by the disk interior and the disk exterior
 → the planet migrates **with respect to the disk on a very short timescale ~ 10⁴-10⁵ ans**



$$t(\text{yr}) = 10^8 \left(\frac{M_{\text{pl}}}{M_{\text{earth}}} \frac{\Sigma}{g / \text{cm}^2} \right)^{-1} \left(\frac{r}{\text{au}} \right)^{-1/2} 10^2 \left(\frac{H}{r} \right)^2$$

(Goldreich & Tremaine '79, Ward '97)

Type I migration



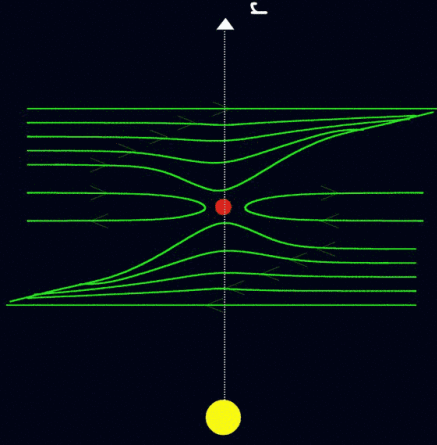
(Ward '97)

Type II migration

The planet opens up a **gap** and is locked into the disk viscous evolution process

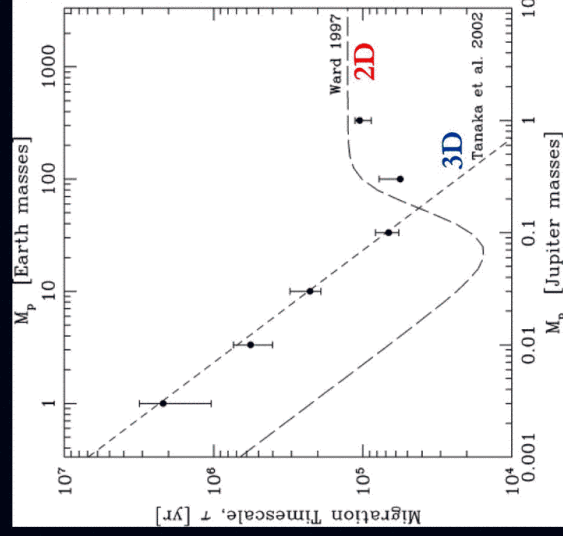
—> migration occurs on **the viscous timescale** $\sim 10^5$ ans

$$t(\text{yr}) = \frac{1}{\alpha} \left(\frac{r}{H} \right)^2 \Omega^{-1} = \frac{0.2}{\alpha} \left(\frac{r}{H} \right)^2 \left(\frac{r}{\text{au}} \right)^{3/2}$$

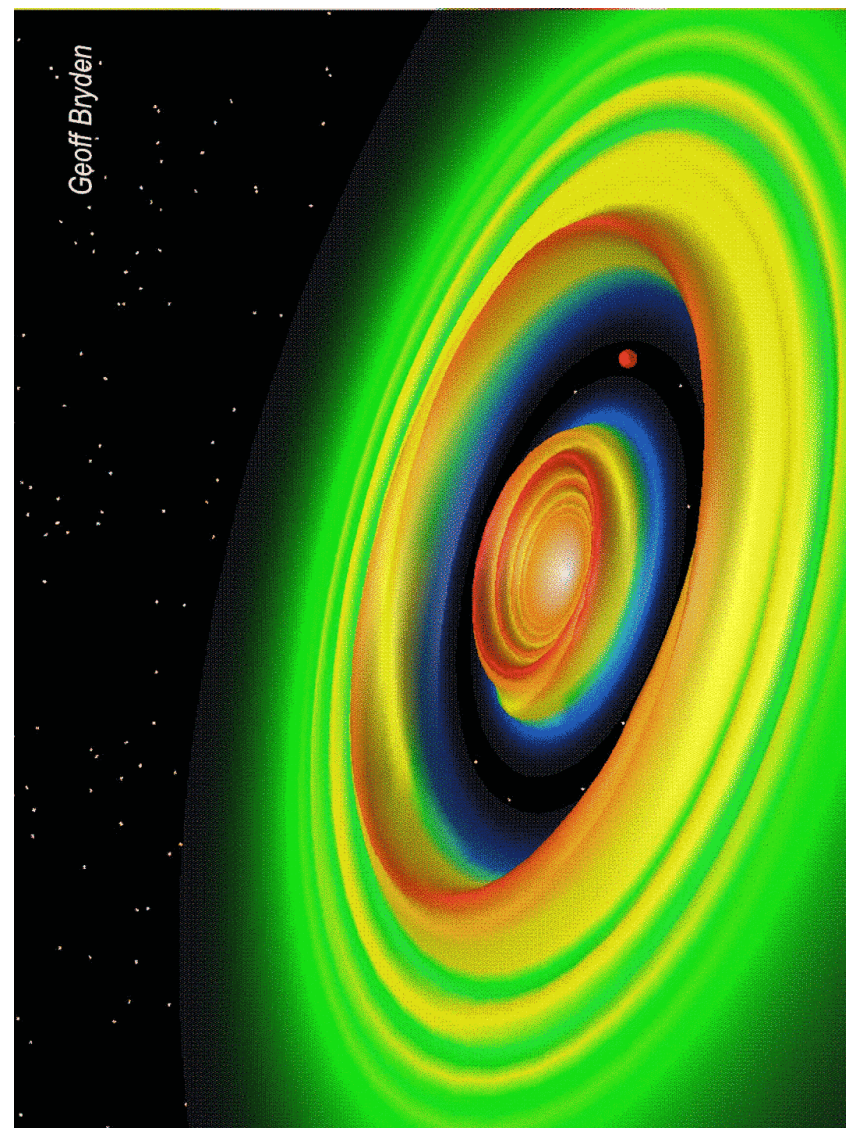
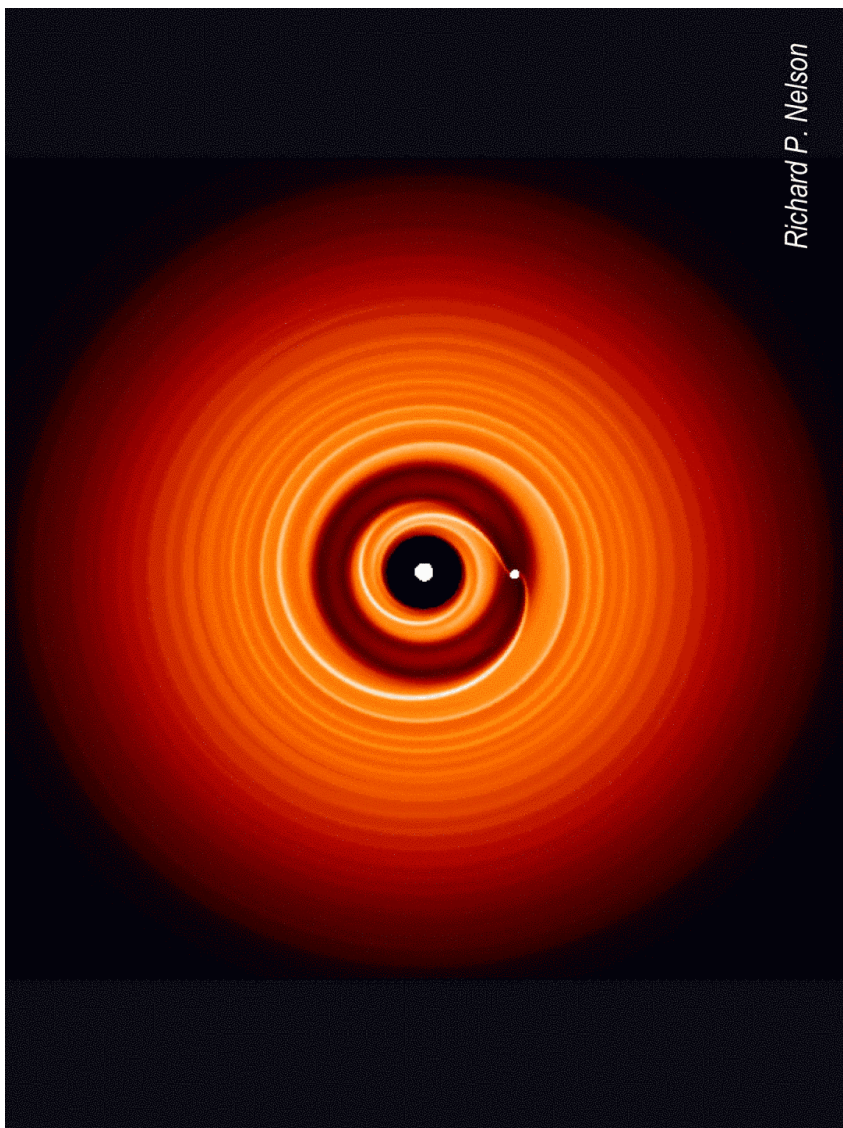


(Goldreich & Tremaine '80, Papaloizou & Lin '84)

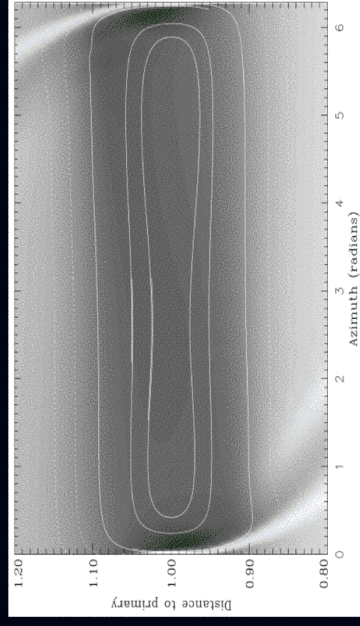
Migration rate



(Bate et al. '03)



Runaway migration

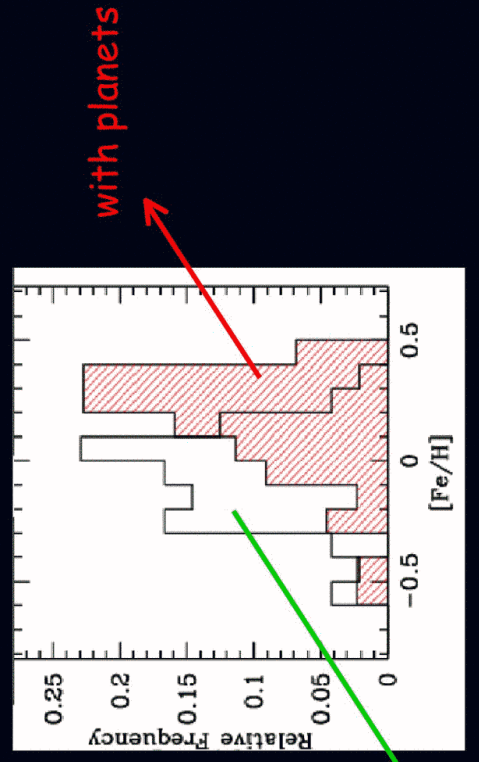


(Masset &
Papaloizou 2003)

- Librating fluid elements: migrate with the planet \rightarrow lose angular momentum \rightarrow positive torque on the planet
- Fluid elements that cross the horseshoe region \rightarrow gain angular momentum \rightarrow negative torque on the planet
- If partial gap \rightarrow net negative torque on the planet which scales with da/dt and the mass deficit

Do planets fall onto their host star?

Metallicity distribution of stars:



without planet

(Santos et al. 2001)

Tidal torque

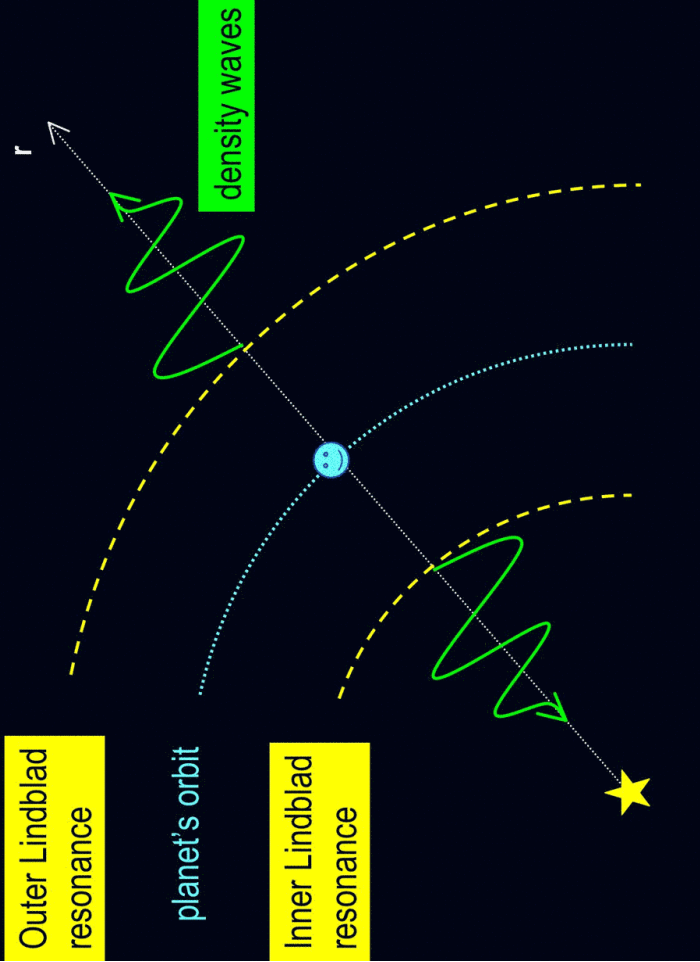
$$T = - \iiint_{disk} \rho' \mathbf{r} \times \nabla \psi'$$

Exerted mainly at **Lindblad** and **corotation** resonances

$T_{Lindblad}$: advected by waves
 —> angular momentum flux

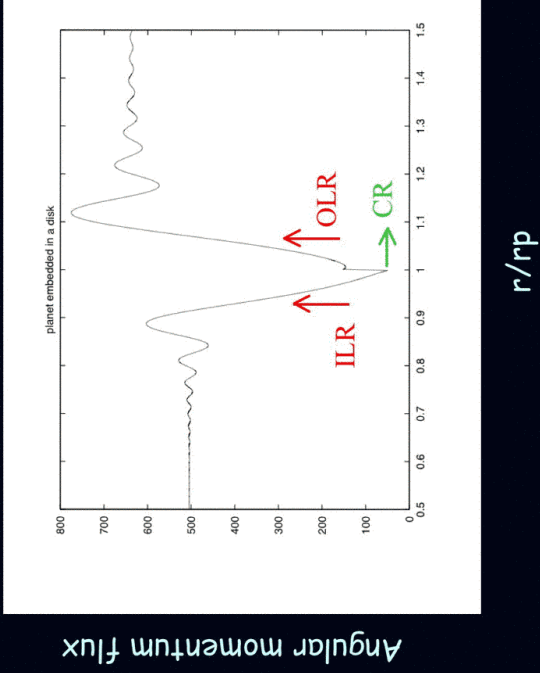
$T_{corotation}$: transferred to the fluid
 (cf. Landau damping)

Disk response

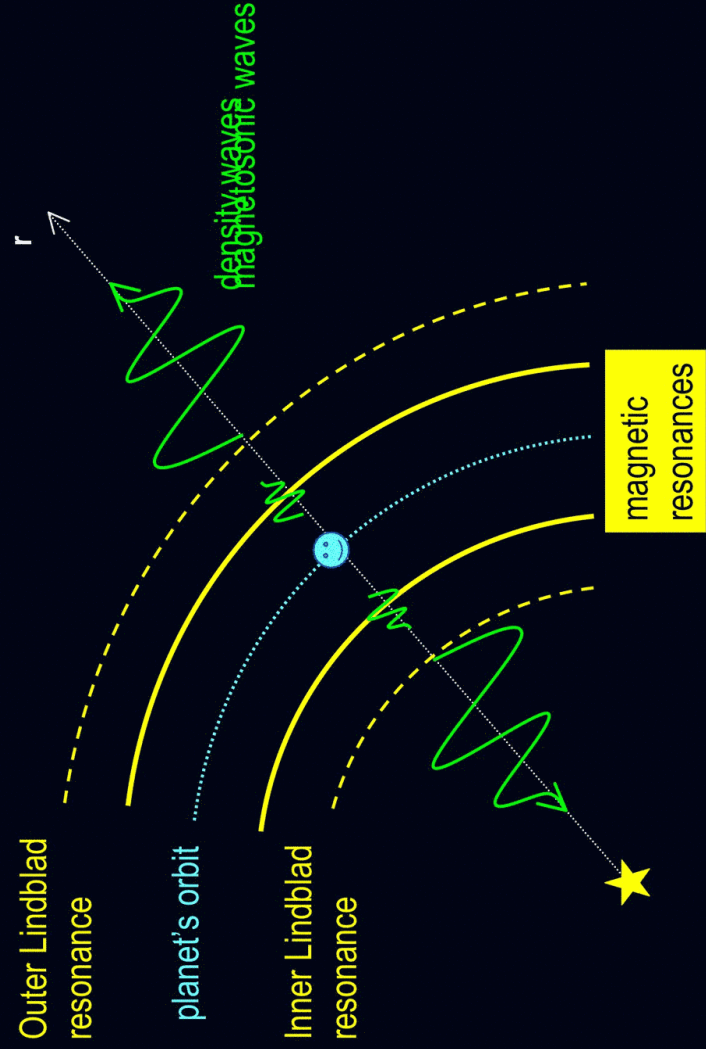


Tidal torque

$$T_d = T_{\text{Lindblad}} + T_{\text{corotation}} = F(r_{\text{out}}) - F(r_{\text{in}}) + \Delta F_{\text{cor}}$$



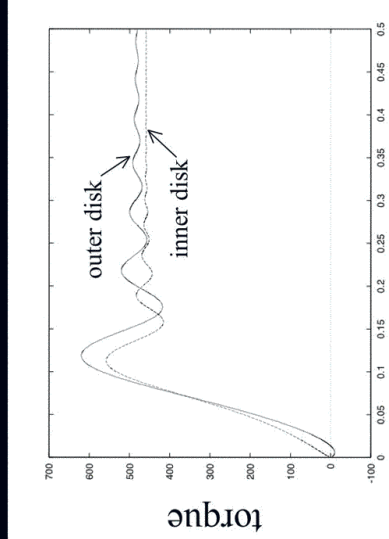
Effect of a magnetic field



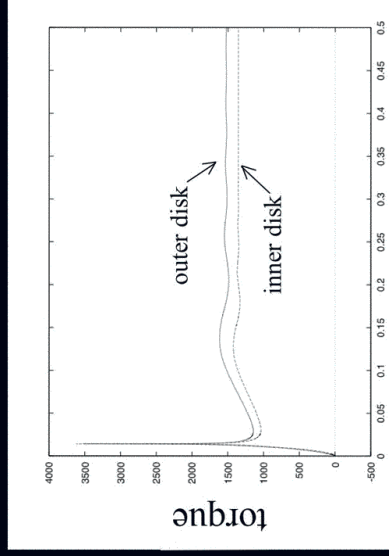
Effect of a magnetic field

Tidal torque:

$$B = 0$$



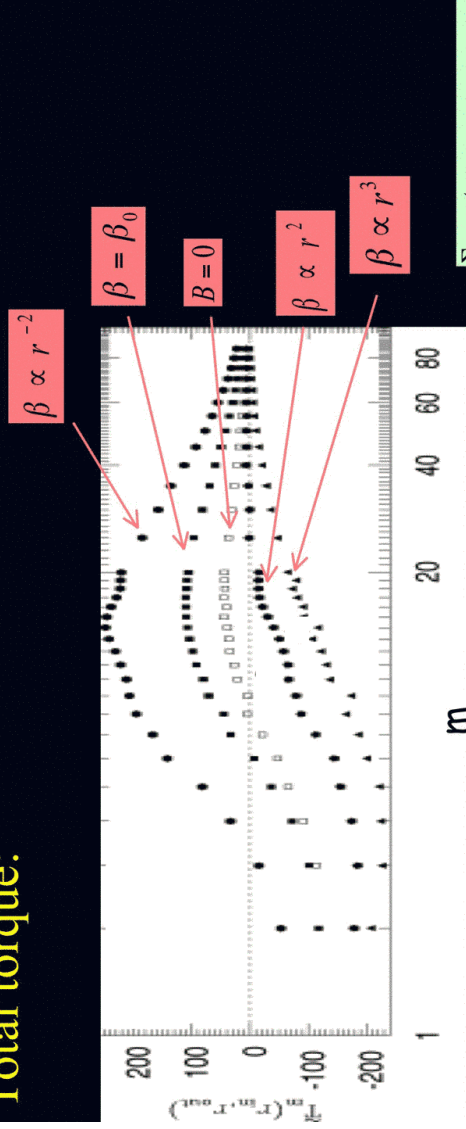
$$B \neq 0$$



$|r-r_p| / r_p$

Effect of a magnetic field

Total torque:



$$\Sigma = c \text{ste}$$

$$c = c \text{ste}$$

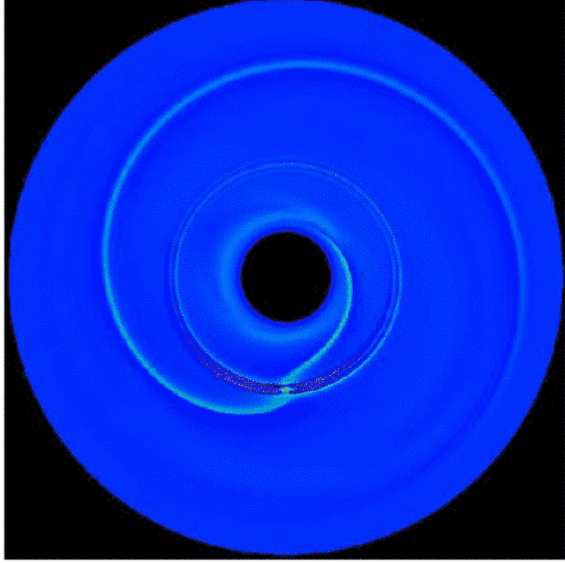
$$H / r = 0.05 \sqrt{r / r_p}$$

$$\beta(r_p) = 1 \text{ with } \beta = c^2 / v^2_A$$

$$M_{\text{planet}} = 5 M_{\text{earth}}$$

$$\beta = c^2 / v_A^2 = 2$$

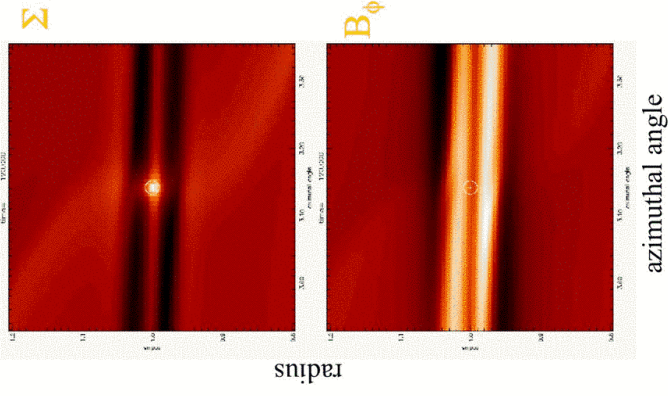
density at $t=10$



(Fromang, Terquem, Nelson 2005)

Numerical Simulations

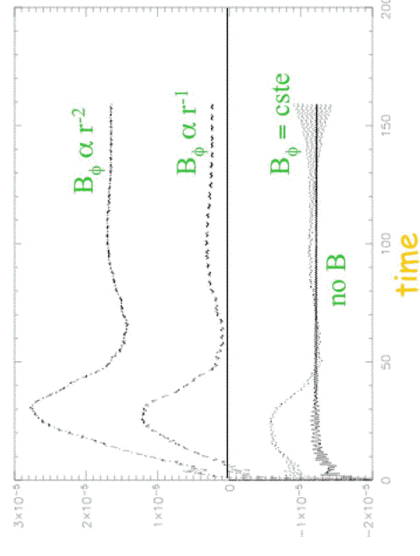
$t=120$



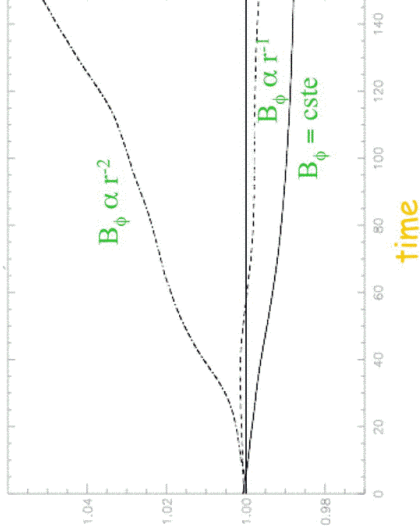
$$M_{\text{planet}} = 5 M_{\text{earth}}$$

$$\beta = c^2 / v_A^2 = 2$$

torque



semi-major axis



Numerical Simulations

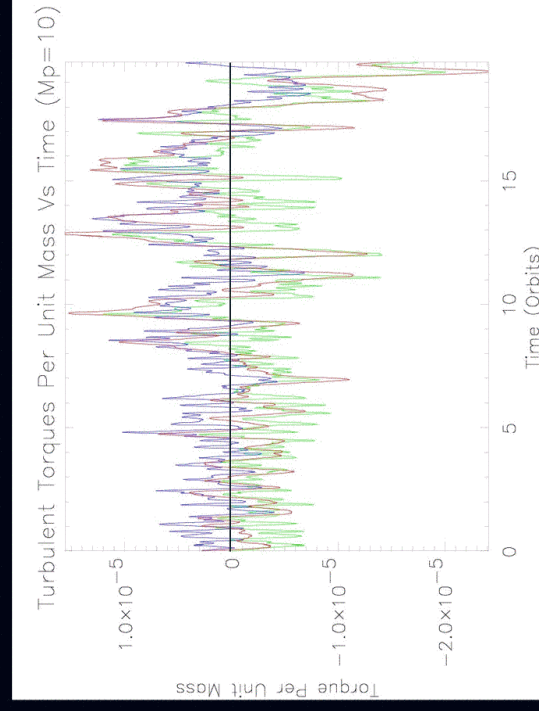
(Fromang, Terquem, Nelson 2005)

Effect of a magnetic field

- Diffusive migration in a turbulent disk if the resonances still exist
- Migration stops at the border between magnetized and non magnetized zones

Planet in a turbulent disk

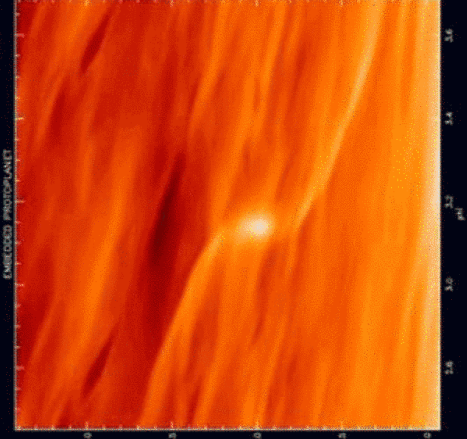
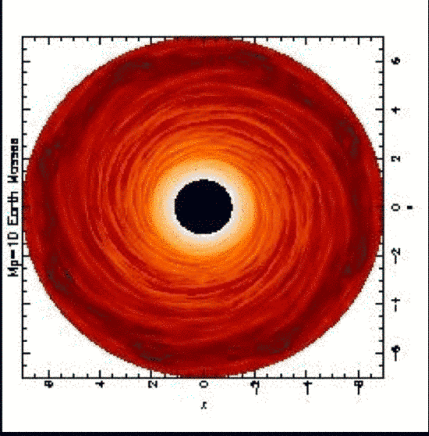
10 Earth masses planet:



(Nelson & Papaloizou 2004)

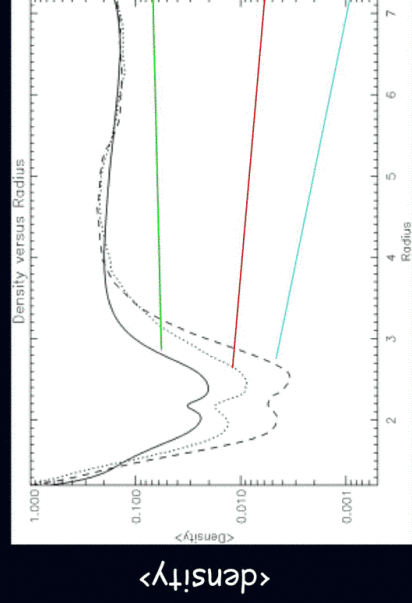
Planet in a turbulent disk

10 Earth masses planet:



(Nelson & Papaloizou 2004)

1 Jupiter mass planet:



radius

(Nelson & Papaloizou 2003;
Winters, Balbus & Hawley 2003)

Planet in a turbulent disk