

Reshaping of ultrafast light pulses through interaction with atomic structure

Mette Gaarde, Louisiana State University

KITP lecture, September 2014

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Funding

NSF, DOE BES, LONI (computing time)



Outline

Theme: what happens to the XUV light as a result of it's interaction with the atomic system (here: structure)

- Example, HHG: Cooper minimum in argon reshapes asec pulses
 Collaboration Ohio State group
- Example, transient absorption: Macroscopic propagation can also change absorption line shape in presence of IR
 Collaboration Arizona group



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Schrödinger equation, in SAE:

$$i\frac{\partial}{\partial t}\psi(\vec{r},t) = \left[-\frac{1}{2}\nabla^2 + \mathcal{E}(t)z + V(\vec{r})\right]\psi(\vec{r},t)$$

Maxwell wave equation:

$$\nabla_{\perp}^{2} \tilde{\mathcal{E}}(\omega) + \frac{2i\omega}{c} \frac{\partial \tilde{\mathcal{E}}(\omega)}{\partial z} = -\frac{\omega^{2}}{\epsilon_{0} c^{2}} \tilde{P}(\omega)$$



Pseudo potential V(r,l)

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FT of time-dependent dipole



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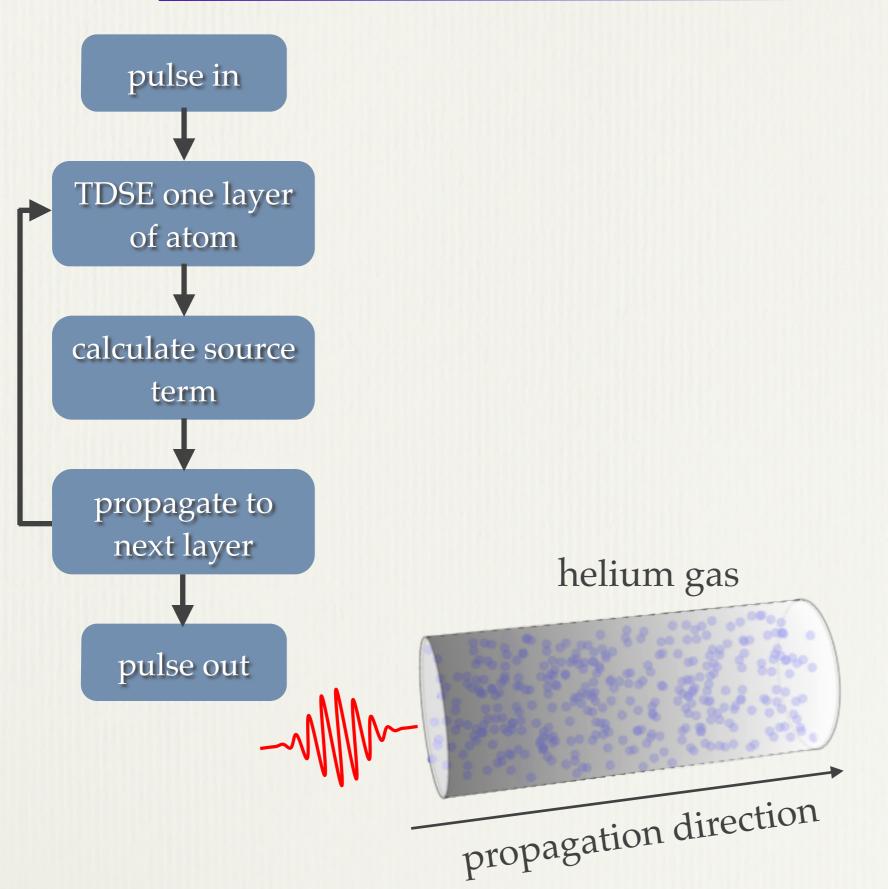
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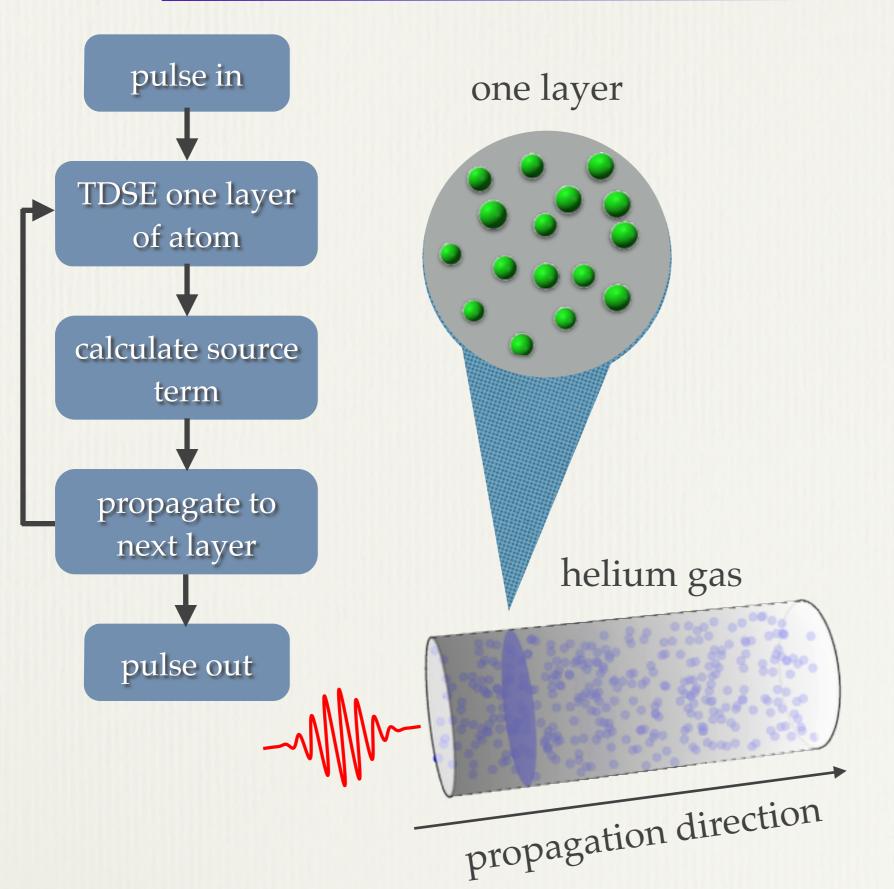
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FT of time-dependent dipole

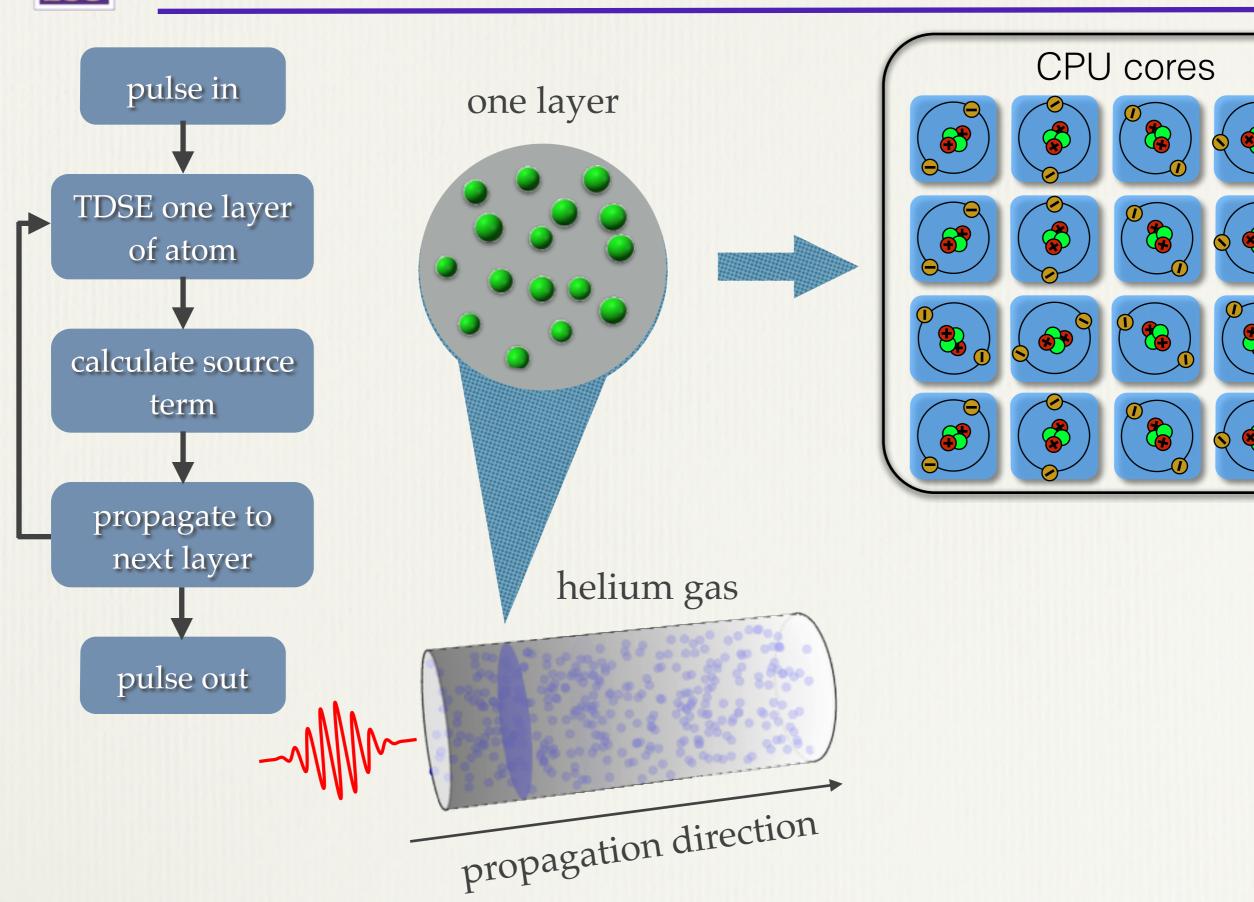




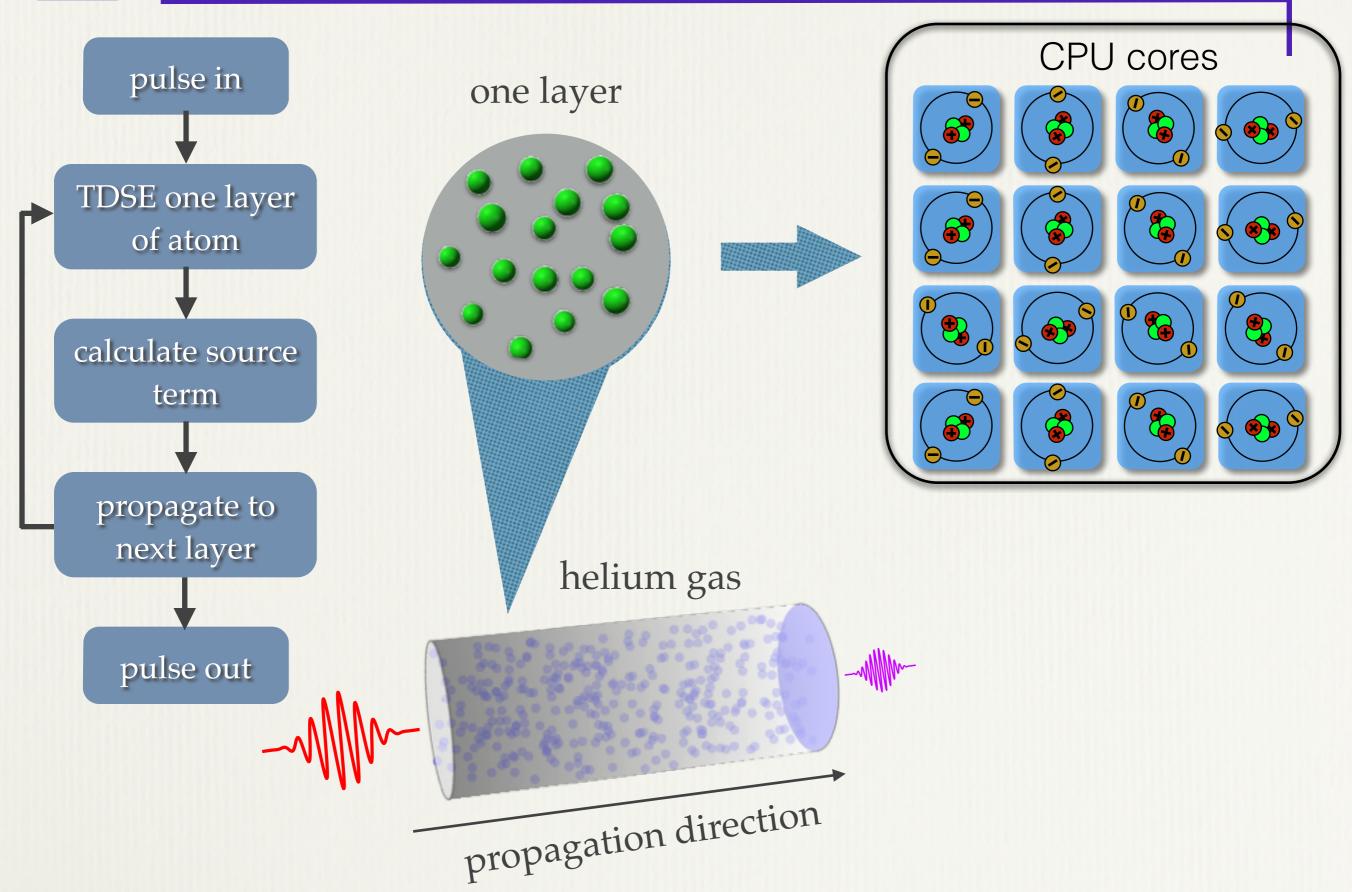




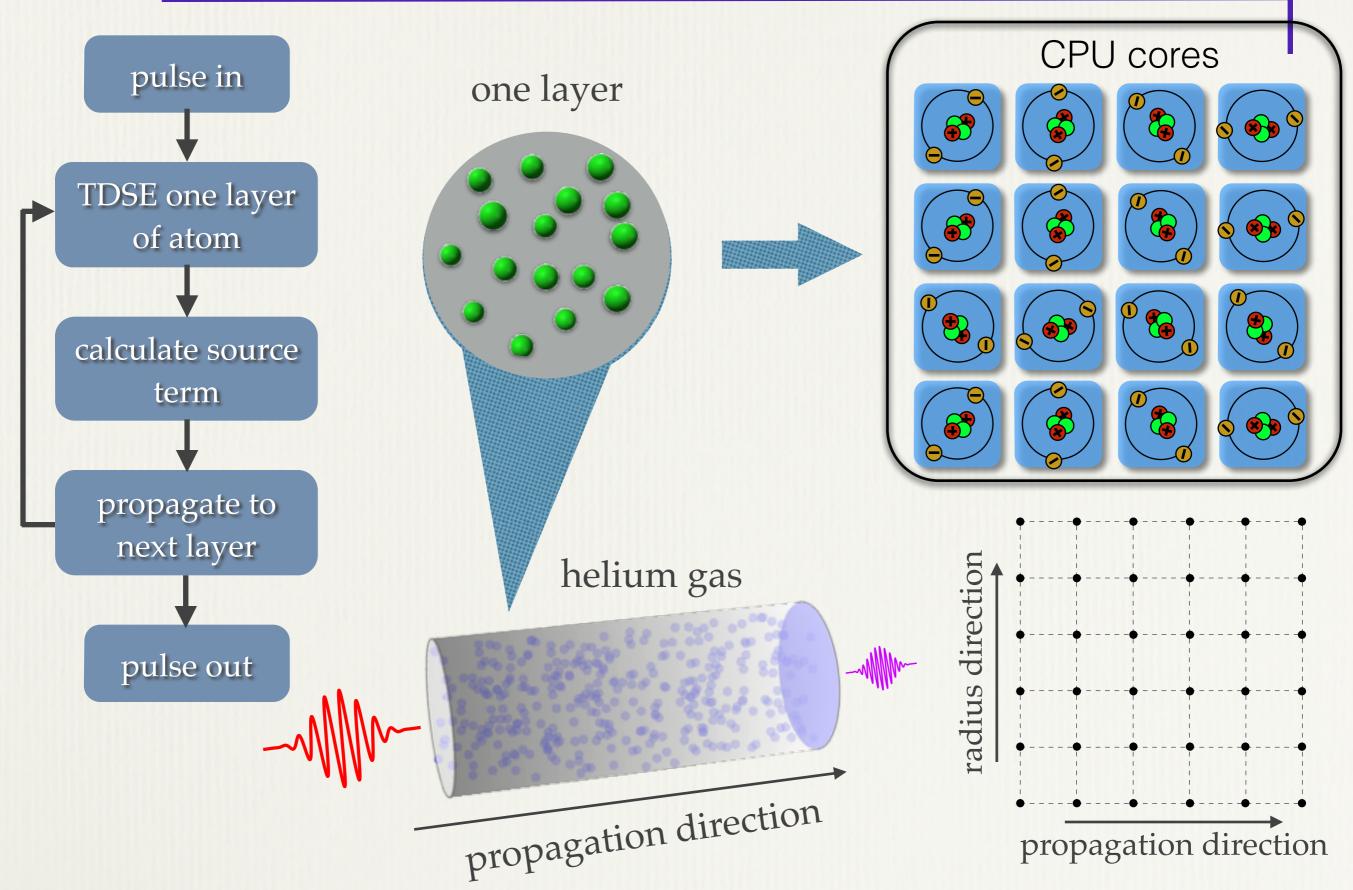












Methods, details

TDSE: Often we care only about transitions/overlap with ground state

$$d(t) = -\langle \psi(\vec{r}, t) | \psi_0 \rangle \langle \psi_0 | z | \psi(\vec{r}, t) \rangle + c.c.$$

Example, Argon has 3p ground state

$$d_s(t) = -e\langle \psi_-(t)|\phi_g\rangle\langle\phi_g|z|\psi_s(t)\rangle + \text{c.c.}$$

$$d_d(t) = -e\langle \psi_-(t)|\phi_g\rangle\langle\phi_g|z|\psi_d(t)\rangle + \text{c.c.}$$

$$\bar{d}_z(t) = d_s(t) + d_d(t)$$

MWE: Sometimes self-consistent solution is not stable/desired

Separate propagation of fundamental and generated fields

$$\nabla_{\perp}^{2} \tilde{\mathcal{E}}_{1} + \frac{2i\omega}{c} \frac{\partial \tilde{\mathcal{E}}_{1}}{\partial z} = \frac{1}{\epsilon_{0}c^{2}} \tilde{FT} \left[\frac{\partial J(t)}{\partial t} \right]$$

$$\nabla_{\perp}^{2} \tilde{\mathcal{E}}_{X} + \frac{2i\omega}{c} \frac{\partial \tilde{\mathcal{E}}_{X}}{\partial z} = \frac{1}{\epsilon_{0}c^{2}} \tilde{FT} \left[\frac{\partial^{2}(P_{L}(t) + P_{NL}(t))}{\partial t^{2}} \right]$$



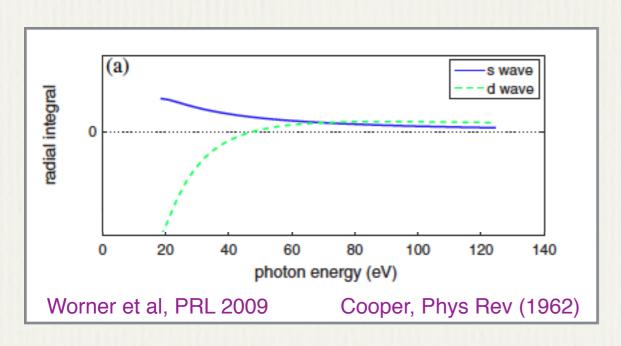
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Example I: Cooper minimum in HHG

Schoun et al, PRL 2014



Min in photoionization cross section due to zero in one angular momentum channel

Argon $\langle \phi_{3p}|z|\phi_{d,E}\rangle = 0$, at $\approx 47 \text{ eV}$

How does this manifest in HHG? Three step model says:

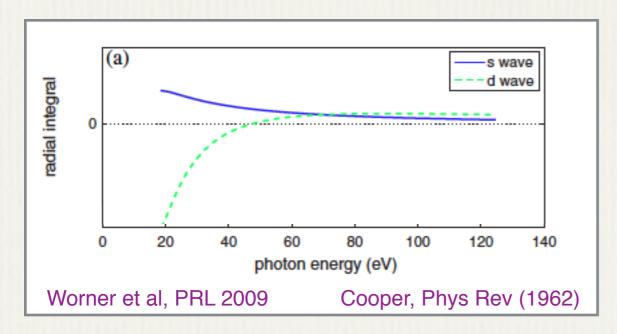
$$D(\omega) = \sqrt{P_{ion}} e^{i\phi_c(\omega)} p_{rdm}(\omega)$$

Recombination dipole moment:

$$p_{rdm}(\omega) = A_s(\omega)e^{i\phi_s(\omega)} + A_d(\omega)e^{i\phi_d(\omega)}$$

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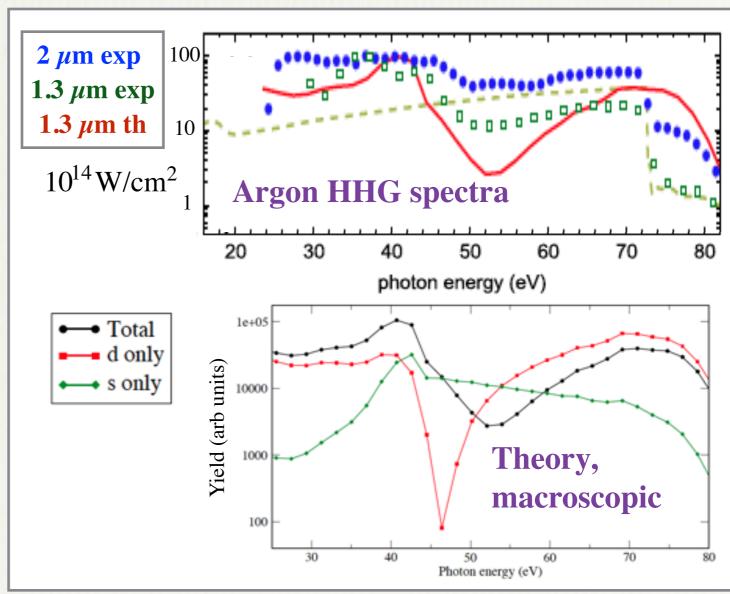
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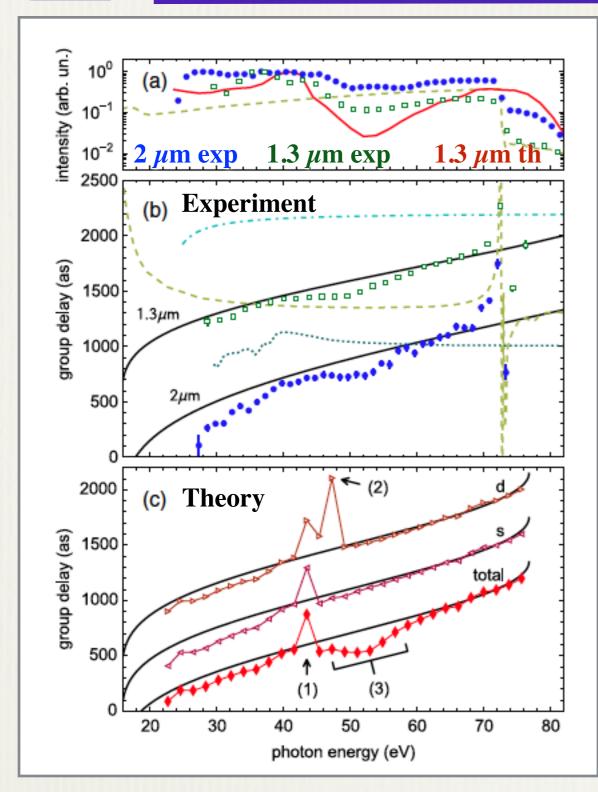
Coherent sum, HHG minimum is at higher energy than Cooper min

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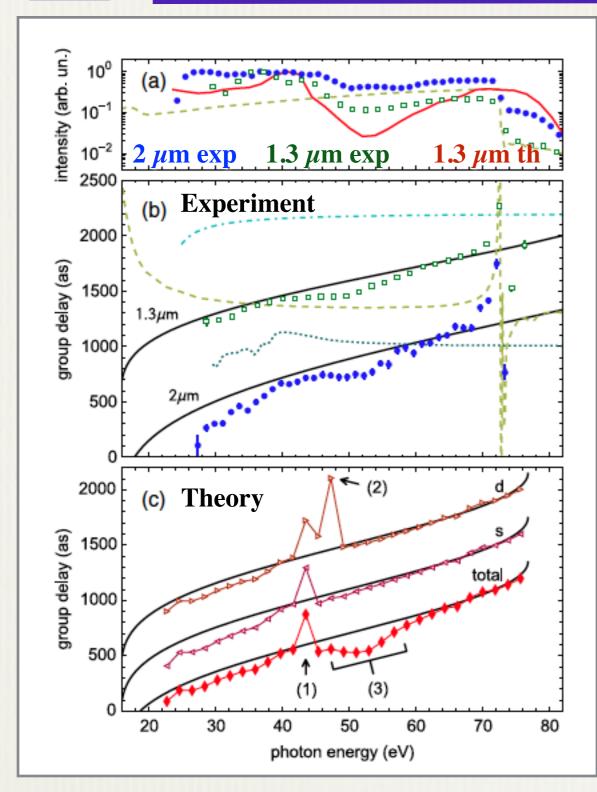
Schoun et al, PRL 2014



Measure group delay $\frac{d\phi(\omega)}{d\omega}$ with RABITT

MIR advantage: higher cutoff and better resolution Two wavelengths (1.3 μ m, 2.0 μ m), approx. 10^{14} W/cm² Optimized for short trajectory, spatially filtered

Schoun et al, PRL 2014

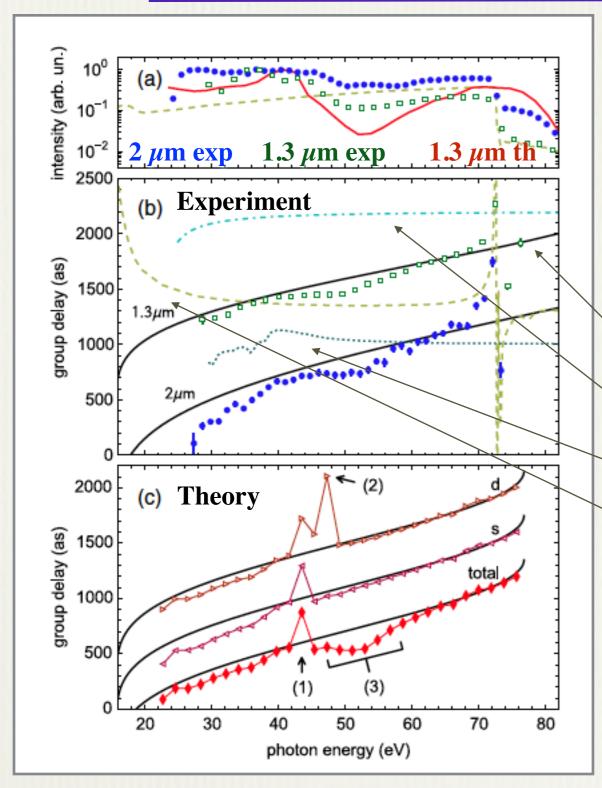


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Extract exp. RDM group delay from total:

Schoun et al, PRL 2014



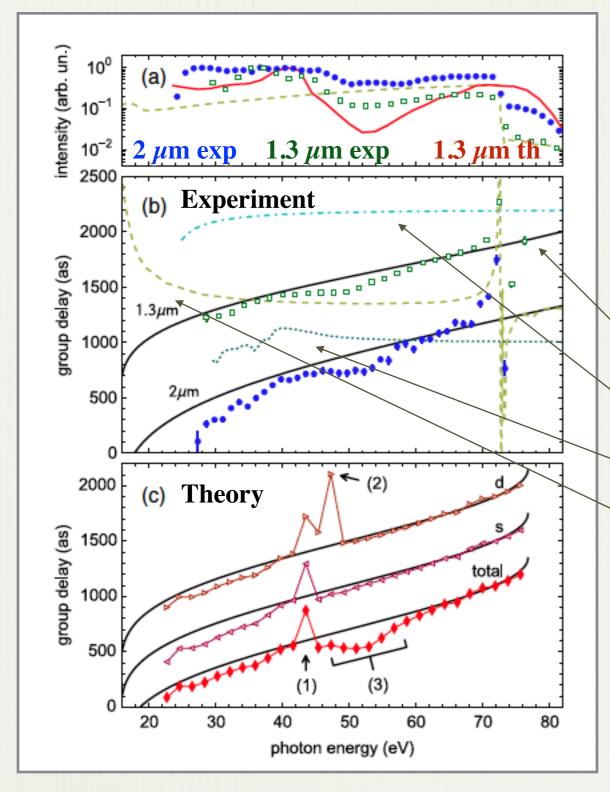
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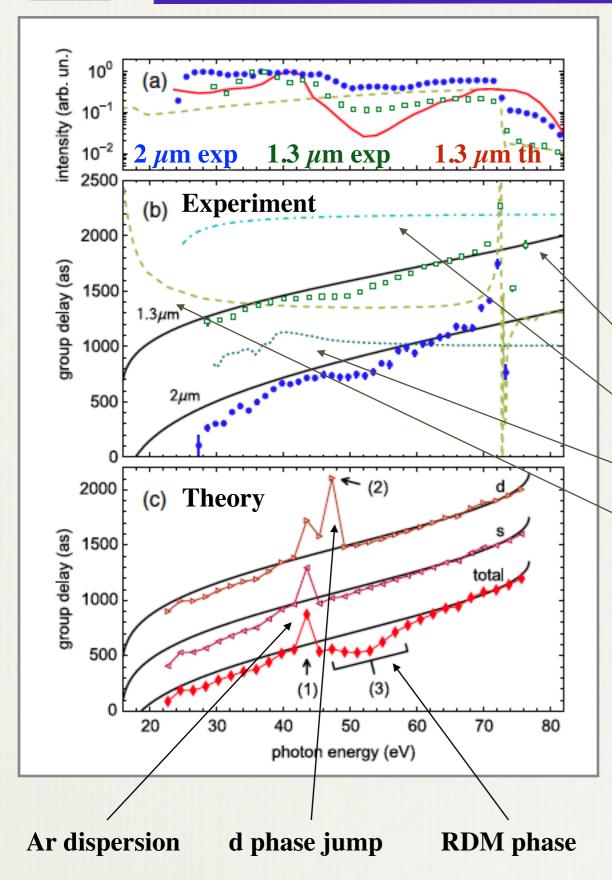
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Theory: coupled TDSE-MWE, 1.3 μ m Optimized for short trajectory, spatially filtered Phase difference averaged over r, harmonic

Extract RDM GD: $GD_{rdm} = GD_{tot} - GD_s$

Schoun et al, PRL 2014



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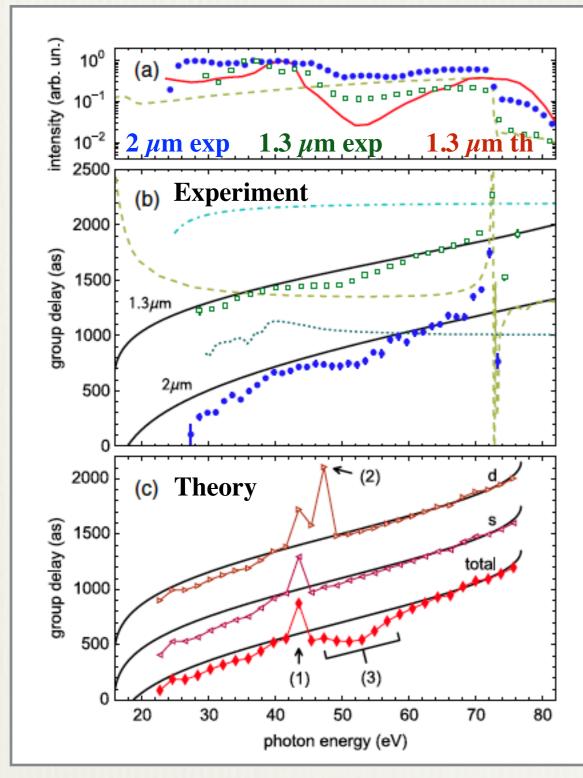
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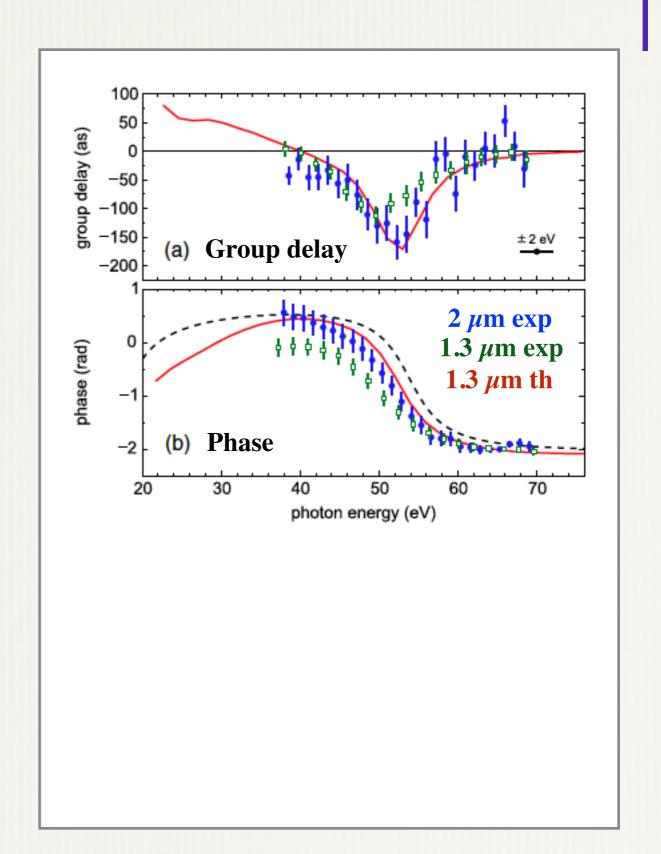
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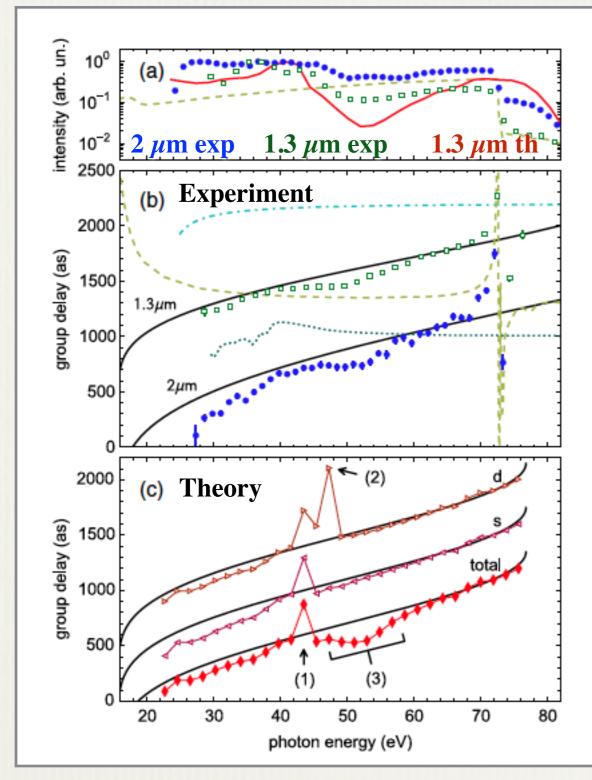
Example I: GD and phase of RDM

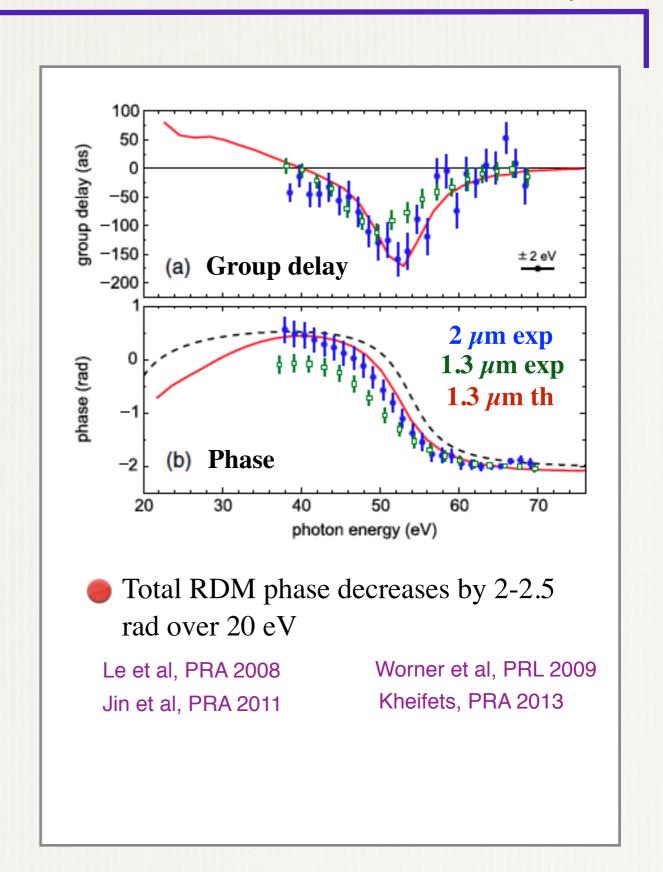






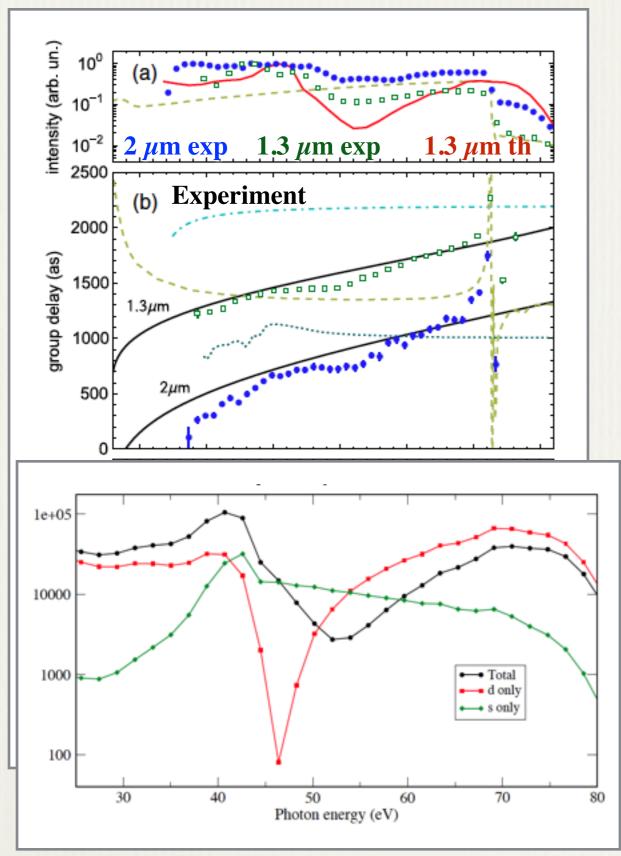
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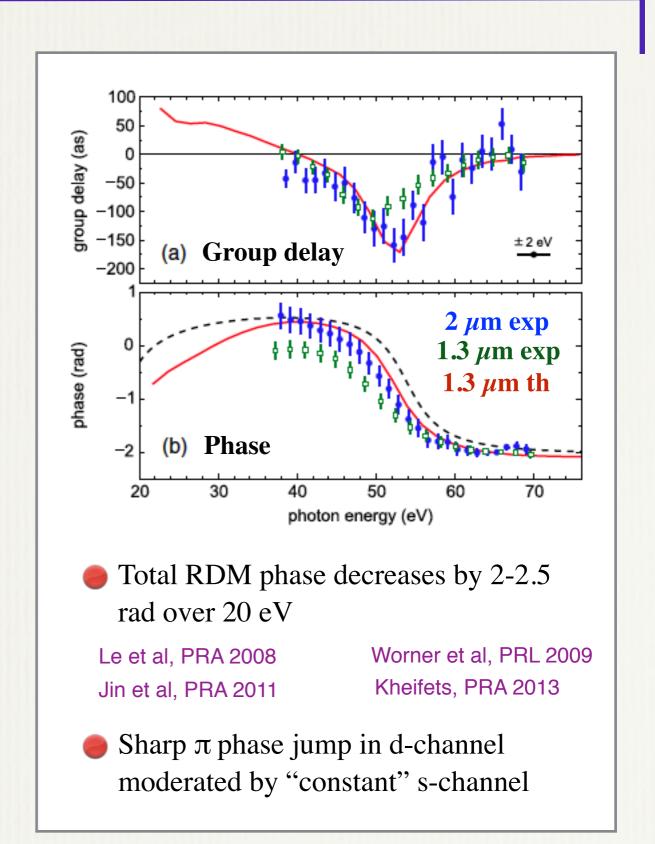






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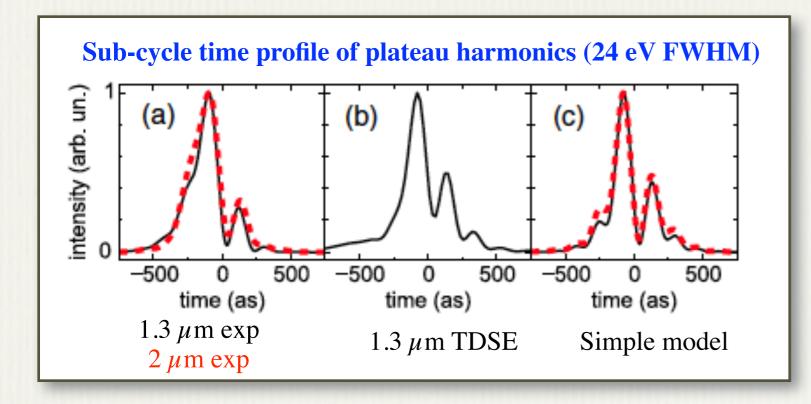






Consequences for XUV attosecond time profile

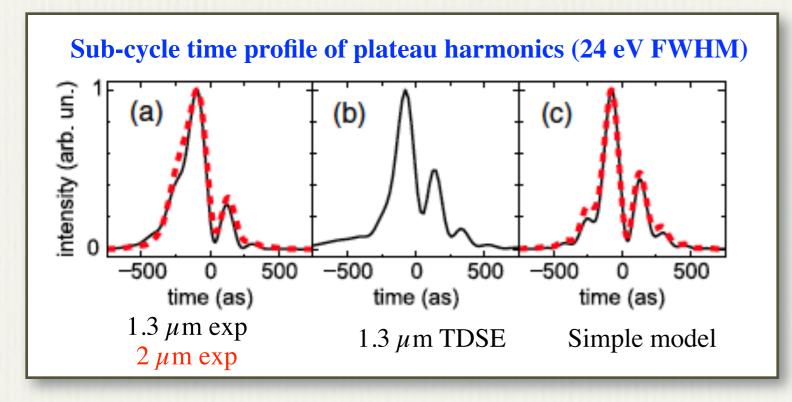
Schoun et al, PRL 2014



- Returning EWP acquires spectral phase over large range
- Leads to reshaping of emitted attosecond pulses - two pulses
- In this case group delay should not be interpreted as time delay

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Simple model for RDM

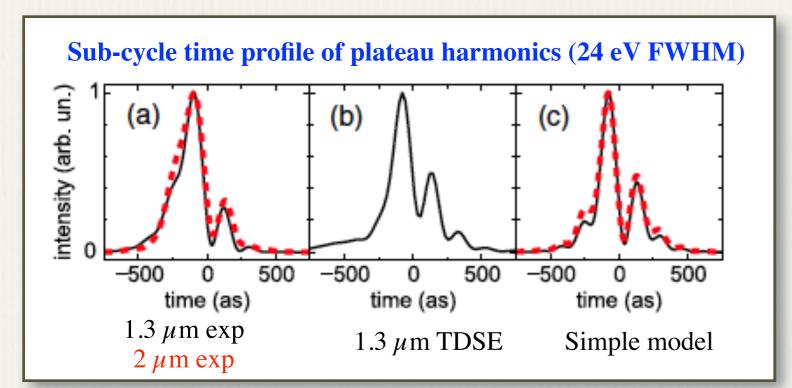
$$p(\omega) = s(\omega)e^{i\eta_0(\omega)}[1 + \chi(\omega)e^{i\xi(\omega)}],$$

$$\chi(\omega) = \frac{d(\omega)}{s(\omega)}, \qquad \xi(\omega) = \eta_2(\omega) - \eta_0(\omega).$$

s(w) constant, d(w) linear:
$$\chi(\omega) = -\frac{\omega - \omega_C}{\Delta \omega}$$

$$\omega_C=48.5~{\rm eV}$$
 $\Delta\omega$ range of d(w) sign change $\xi(\omega)$ scattering phases





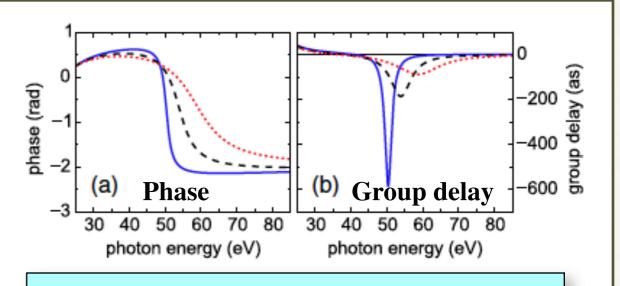
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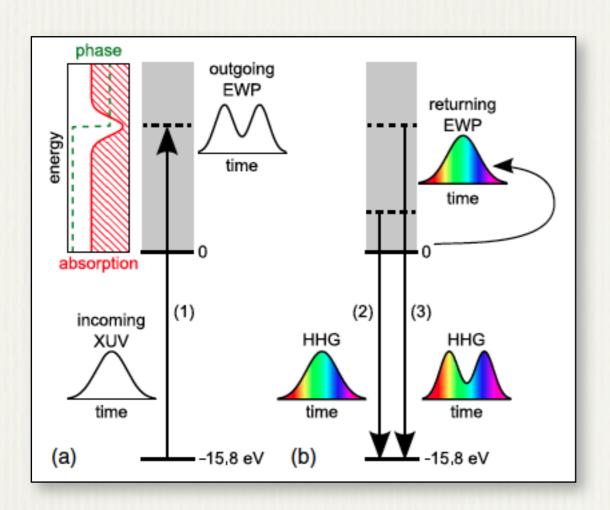
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Rapid variation in d-channel can make group delay arbitrarily large - not meaningful as a time delay



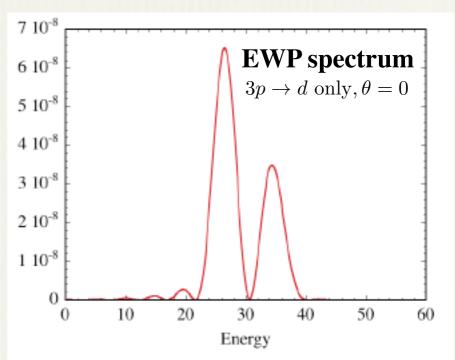
Reciprocal nature of photoionization and recombination



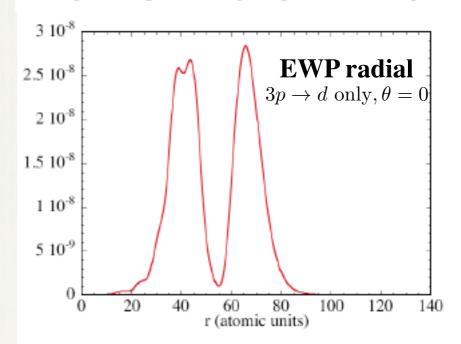
Hole in EWP created by photo ionization first discussed by Noordam et al. Measurement of EWP amplitude and phase challenging though

Hoogenraad et al, PRA 1998

Yakovlev et al, PRL 2010



The spectrum of electrons along theta=0 from a 47 eV pulse on argon where only the 3p -> Ed channel is open.



The electron wave packet along theta=0 about 1 fs after the center of a 300 as FWHM pulse. Only the 3p->Ed channel is open.



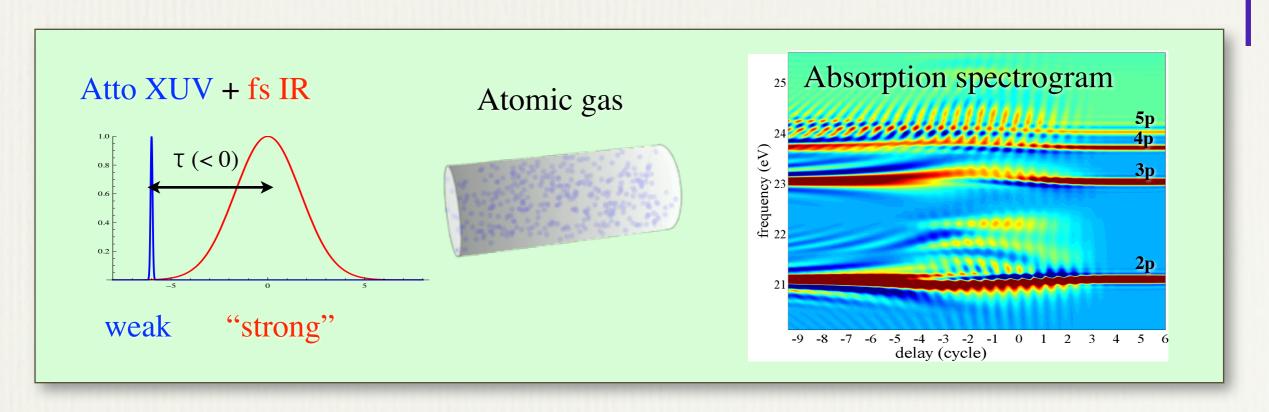
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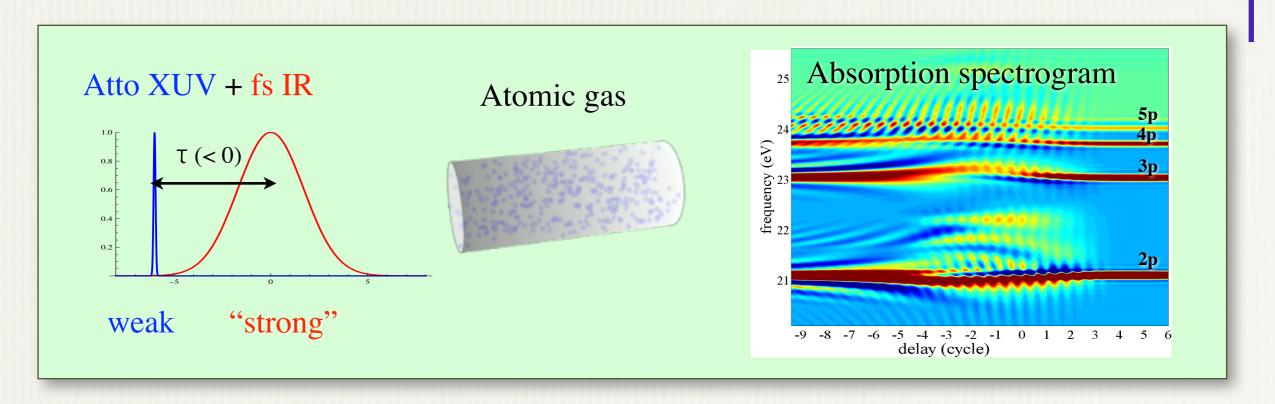
Example II: Introduction to transient absorption



Study electron dynamics from what happens to the XUV light
 From delay-dependence, absorption is time-integrated



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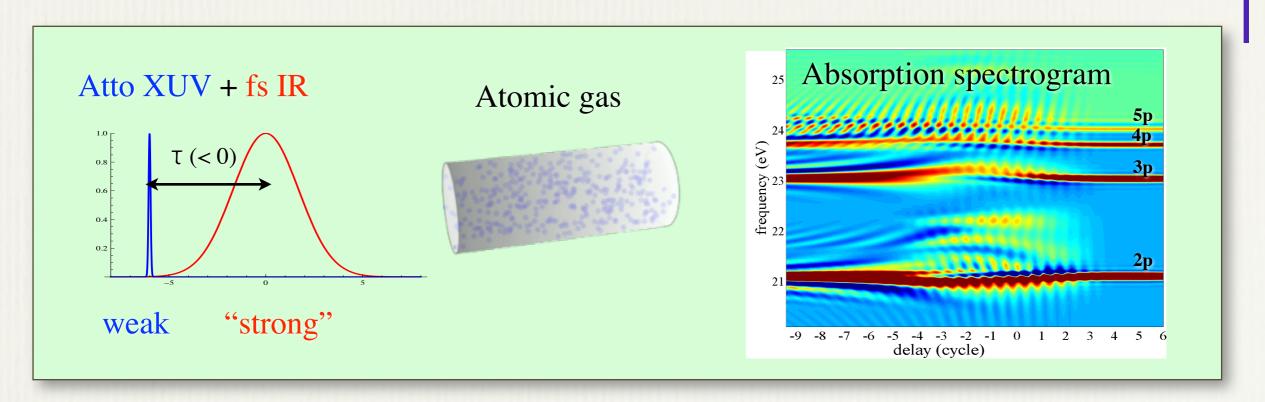


Study electron dynamics from what happens to the XUV light
 From delay-dependence, absorption is time-integrated

Single atom response function $S(\omega) = 2 \text{ Im}[d(\omega)E^*(\omega)]$ find d(t) from TDSE absorption probability per frequency, depends on light field



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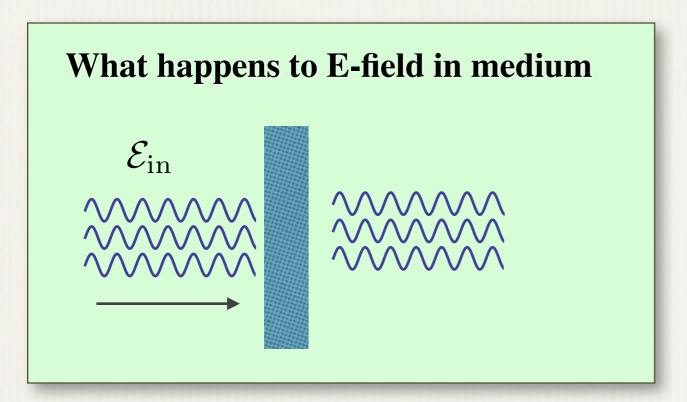
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Macroscopic optical density $OD = -\log[I_{out}/I_{in}]$ find E(t,r,z) by solving coupled, note: if $I(z) = I_0 e^{-\alpha z}$ then OD prop. to cross section

self-consistent TDSE and MWE

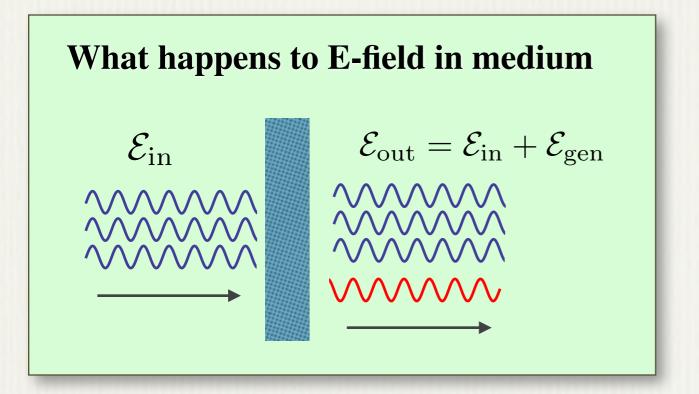


Example II: Absorption in the time domain





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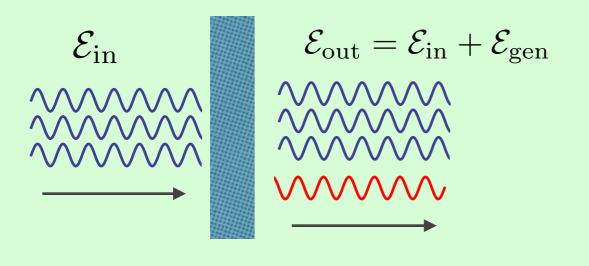


lacktriangle Absorption happens when generated E-field is π out of phase with driving E-field



Example II: Absorption in the time domain

What happens to E-field in medium



- igorealth Absorption happens when generated E-field is π out of phase with driving E-field
- This means that time-dependent dipole moment is $\pi/2$ out of phase with driving field

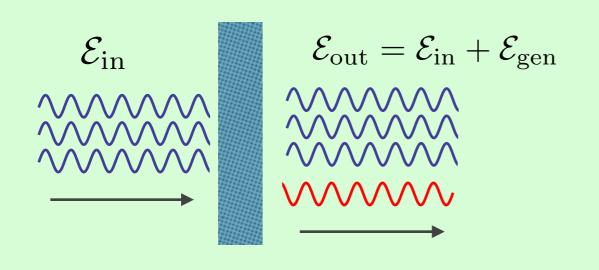
$$\frac{2i\omega}{c}\frac{\partial E}{\partial z} = -\frac{\omega^2}{\epsilon_0 c^2}P \qquad \sigma(\omega) = 2\operatorname{Im}\left[\frac{d(\omega)}{E(\omega)}\right]$$

• Response function $S(\omega) = 2 \operatorname{Im}[d(\omega)E^*(\omega)]$



Example II: Absorption in the time domain

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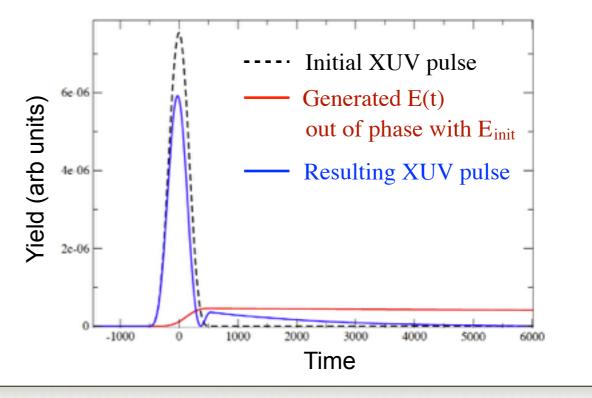


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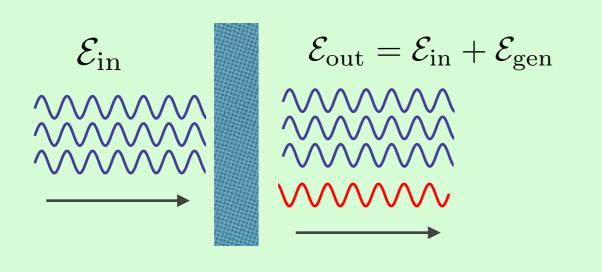
When driving pulse is much shorter than lifetime:





Example II: Absorption in the time domain

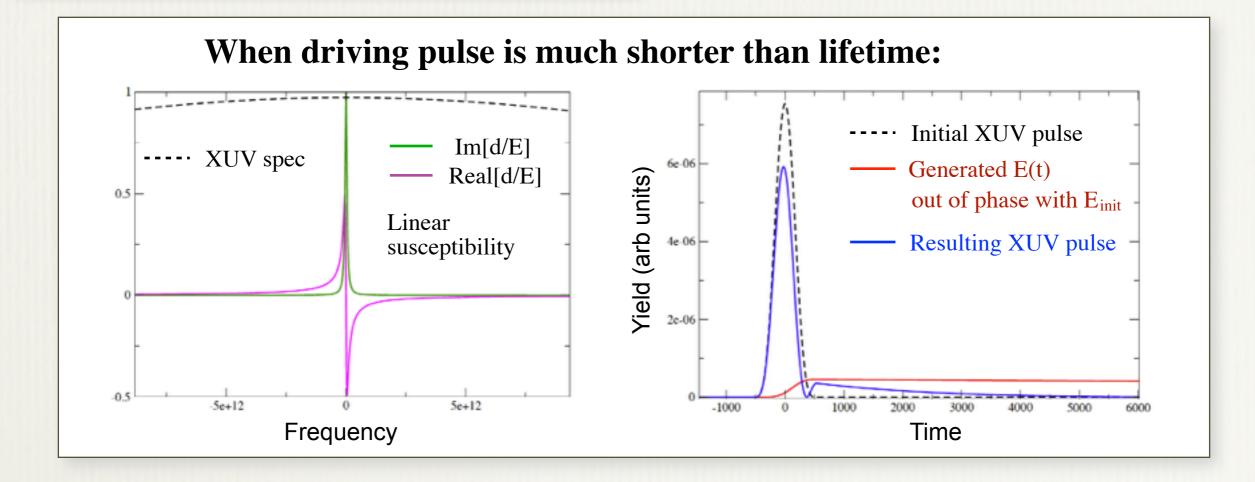
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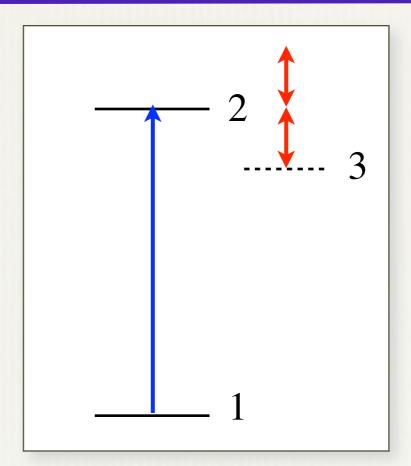




Example II: Line shape changes

Chen et al., PRA 2013

- One photon excitation: absorption
- Access excitation more than once.
 This adds a phase shift to d(t)



Autoionization:

Bound/APT:

Heidelberg (Ott/Pfeifer)

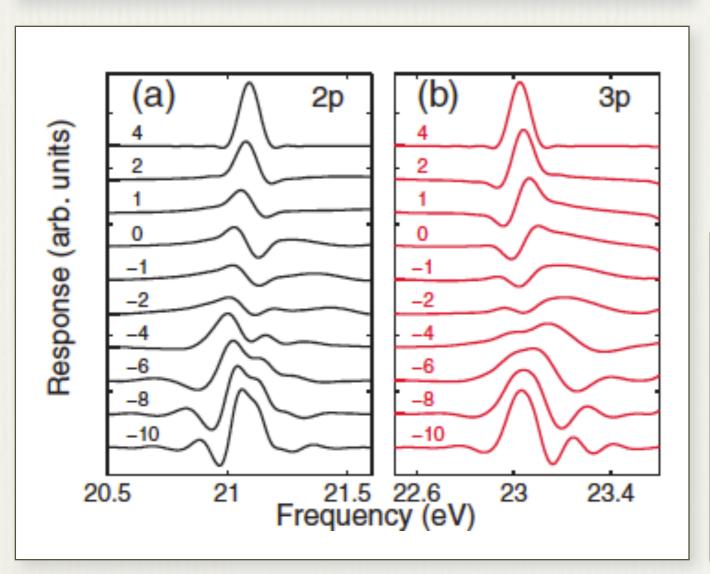
ETH Zurich (Hermann/Keller)

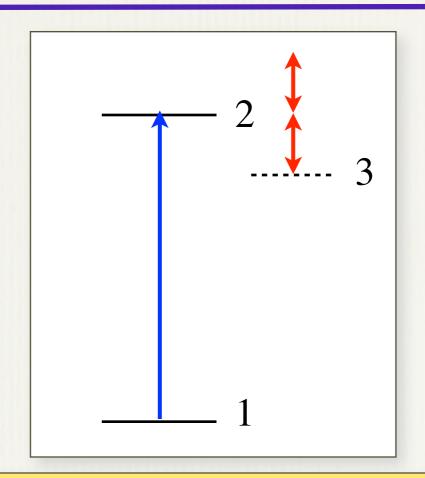
CFEL (Pabst/Santra)

Madrid (Argenti/Martin)

Kansas (Chu/Lin)

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 This adds a phase shift to d(t)





Stark effect

$$\phi(t,\tau) = \int_{\tau}^{t} \left[\delta E_{np}(t') - \delta E_{1s}(t')\right] dt'$$

$$\tilde{S}(\omega,\tau) \approx b \cdot Re \left[e^{i\phi_{0}(\tau)} \int_{\tau}^{\tau+T_{2}} e^{-i(\omega-\omega_{21})t} e^{-t/T_{2}} dt\right]$$

$$\approx \mathcal{L}(\omega) \left[\cos(\phi_{0}) + (\omega - \omega_{21})T_{2}\sin(\phi_{0})\right]$$

Autoionization:

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Madrid (Argenti/Martin)

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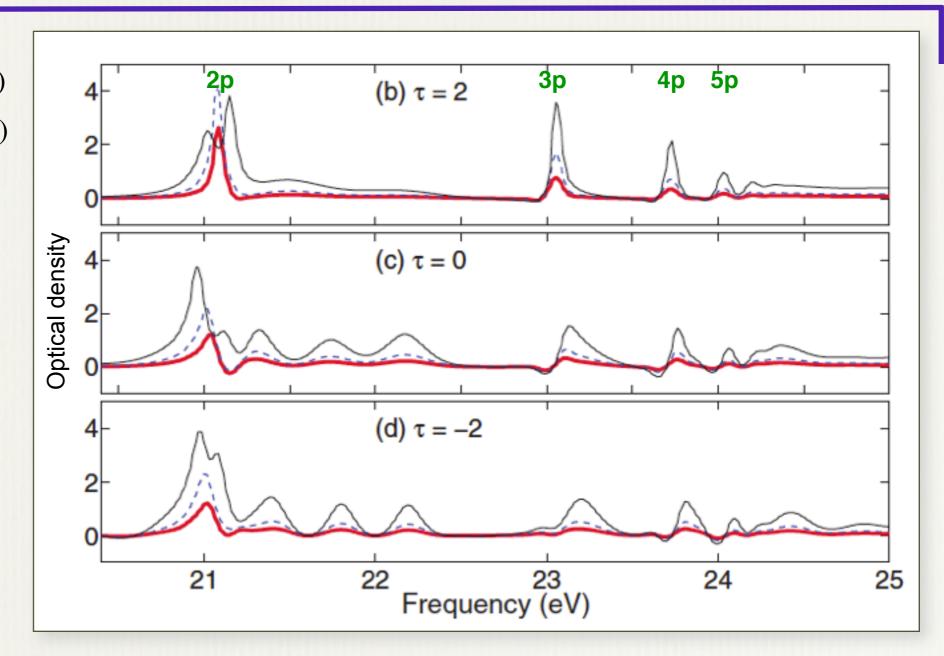


Chen et al., PRA 2013

Low dens (1e17)

High dens (5e17)

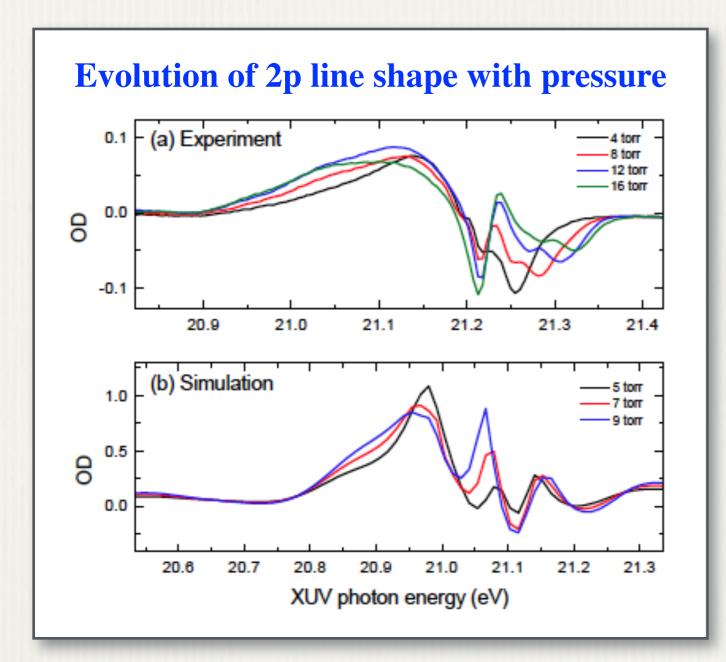
XUV 400 as, 25 eV IR 800 nm, 1e12 W/cm2



Broadening, shifts, new spectral features
 Also observed experimentally (Sandhu & Liao)



Liao et al, in prep.



Experiment and theory

XUV APT, H13 - H17 (440 as pulses)

40 fs IR 800 nm, 3e12 W/cm2

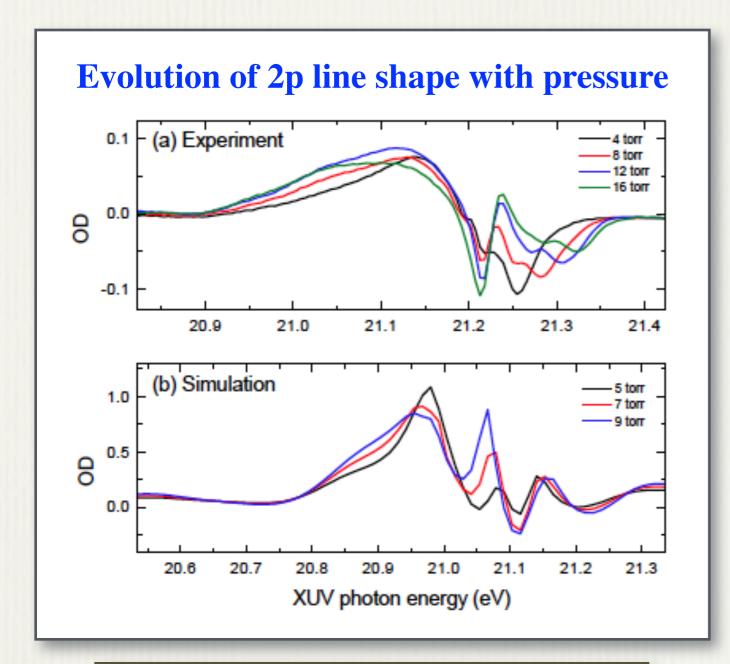
Long medium (1 cm)

Theory: fully coupled, self-

consistent TDSE-MWE



Liao et al, in prep.



Experiment and theory

XUV APT, H13 - H17 (440 as pulses)

40 fs IR 800 nm, 3e12 W/cm2

Long medium (1 cm)

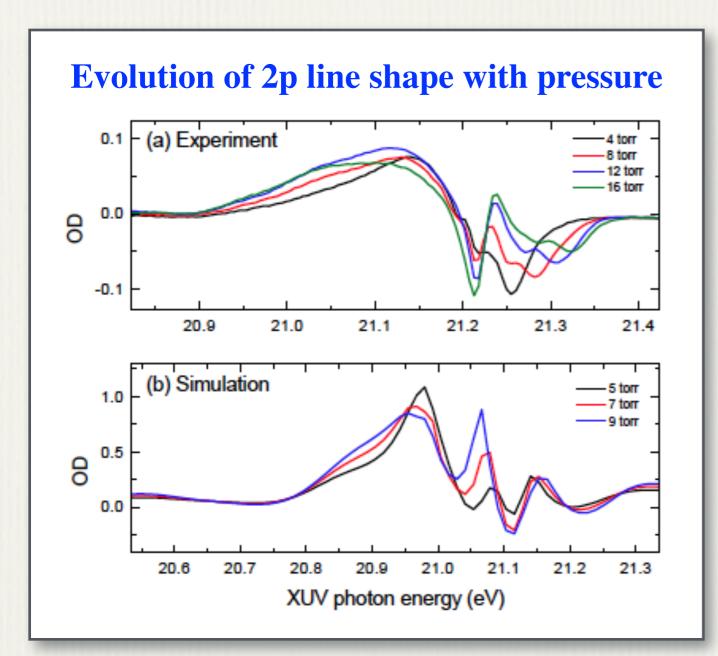
Theory: fully coupled, self-

consistent TDSE-MWE

- Broadening of main feature
- Appearance of new, narrow feature at center of resonance



Liao et al, in prep.



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- Appearance of new, narrow feature at center of resonance

Experiment and theory

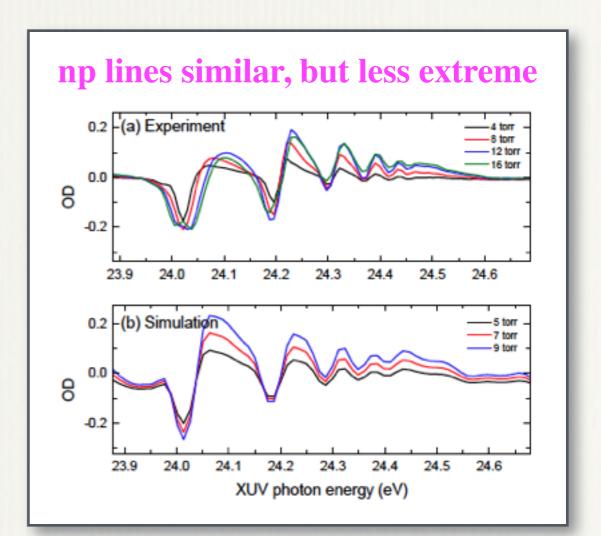
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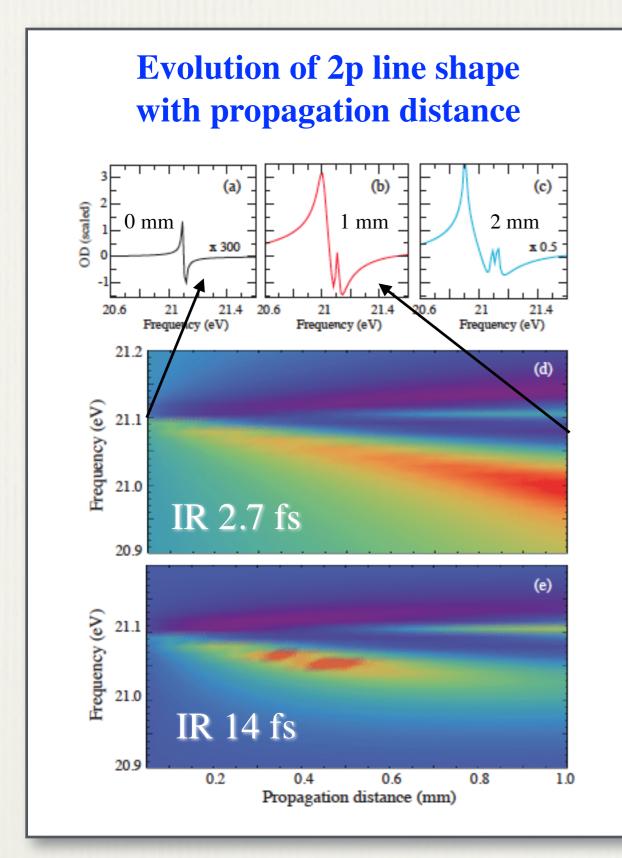
consistent TDSE-MWE





Example II: Simple model for perturbed dipole response

Liao et al, in prep.

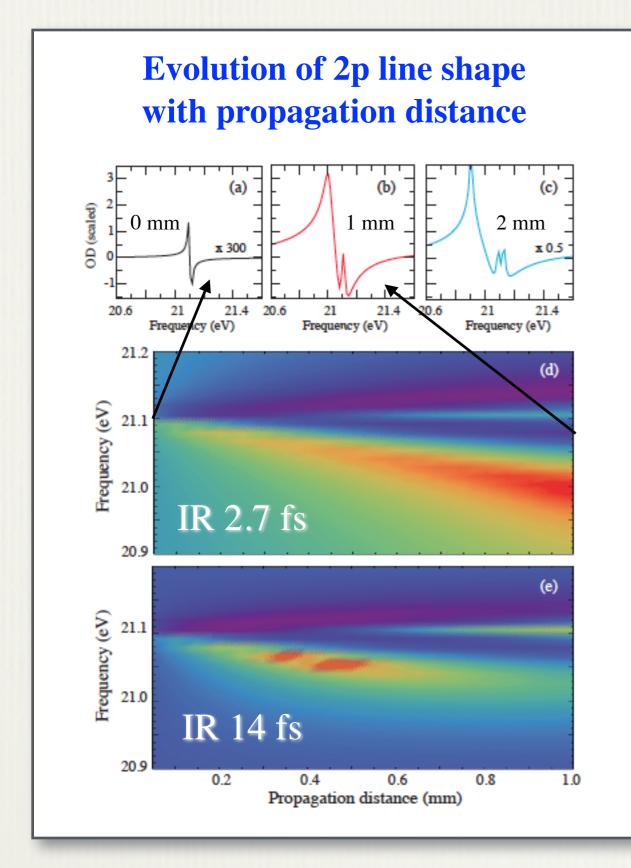


- Time-dependent dipole moment calculated from model atom: two-level system, 1s-2p in He, resonant with XUV SAP
- IR perturbation is time-dependent phase, proportional to IR intensity
- Solve coupled TDSE-MWE with model dipole moment



Example II: Simple model for perturbed dipole response

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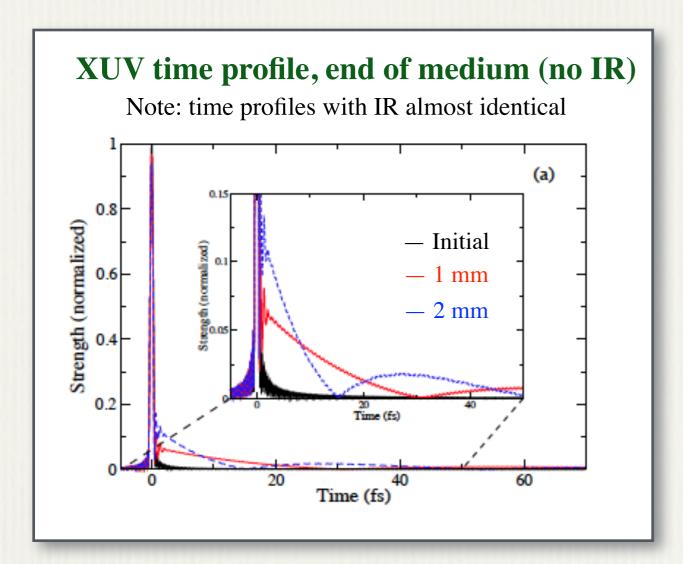


- Time-dependent dipole moment calculated from model atom: two-level system, 1s-2p in He, resonant with XUV SAP
- IR perturbation is time-dependent phase, proportional to IR intensity
- Solve coupled TDSE-MWE with model dipole moment

Observations, short IR case

- Broadening, linear in z
- New features appear, broaden
- Shape of outer feature preserved

Liao et al, in prep.

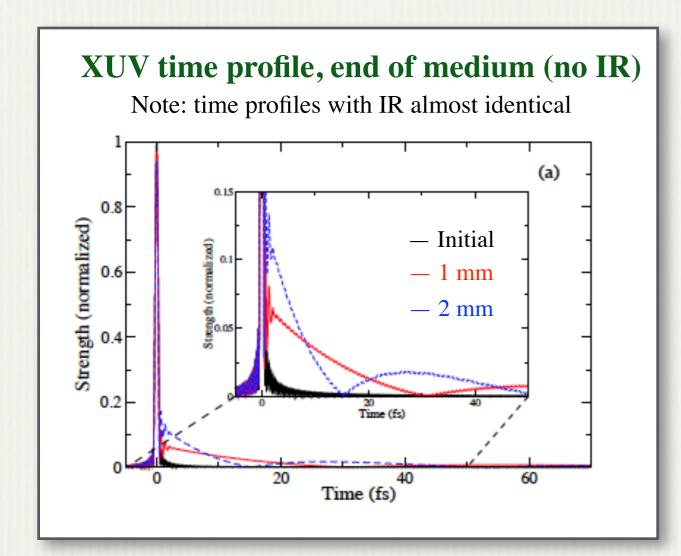


- Extra peaks in time caused by alternating sign of E-field due to absorption (well known) Crisp, PRA 1, 1970
- With longer propagation: move closer to main peak, grow in size and number

IR 2.7 fs

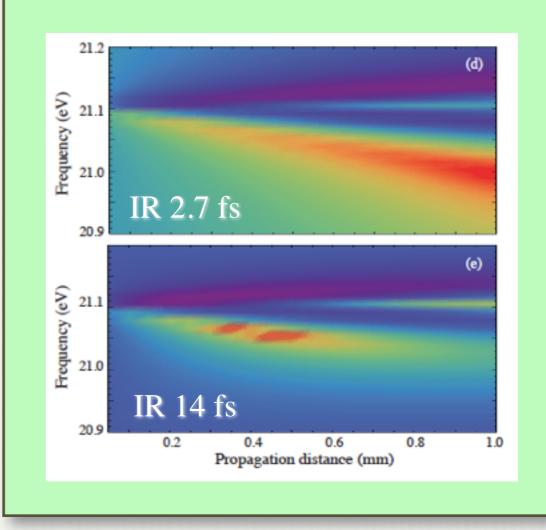
IR 14 fs

Liao et al, in prep.

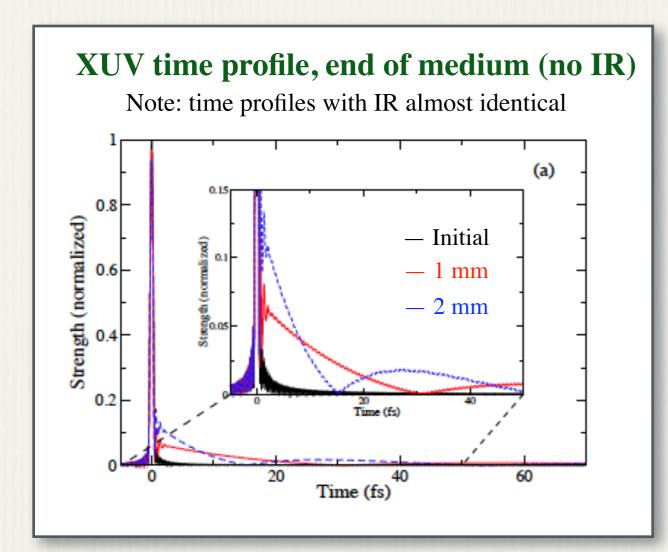


- Extra peaks in time caused by alternating sign of E-field due to absorption (well known) Crisp, PRA 1, 1970
- With longer propagation: move closer to main peak, grow in size and number

 Short IR: first extra burst is new "lifetime" over which perturbed dipole oscillates (bandwidth of outer structure)

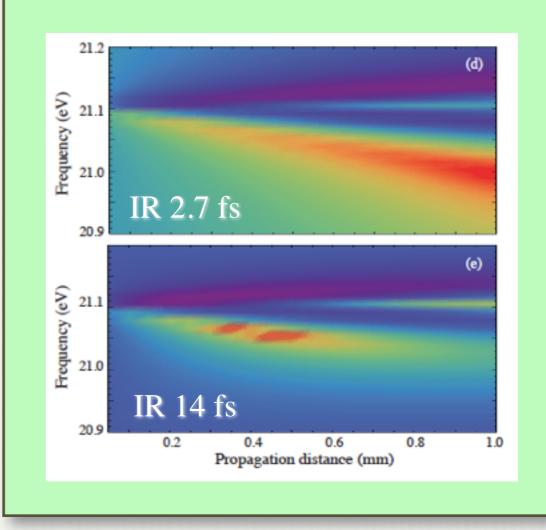




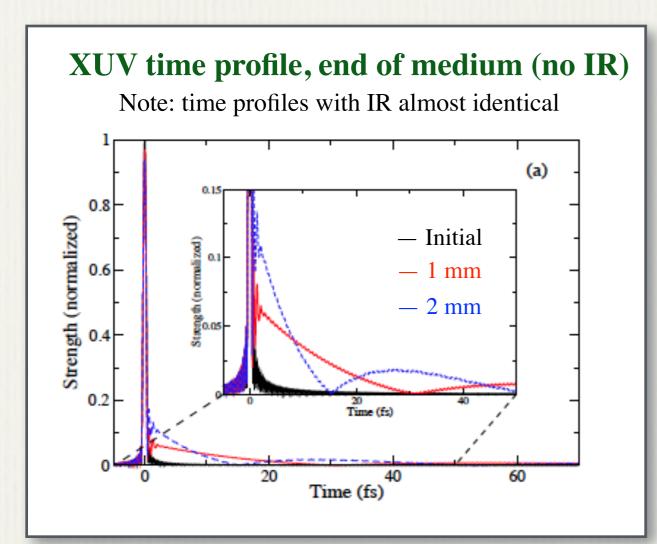


- Extra peaks in time caused by alternating sign of E-field due to absorption (well known) Crisp, PRA 1, 1970
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- Inner structure(s) come from additional bursts in time



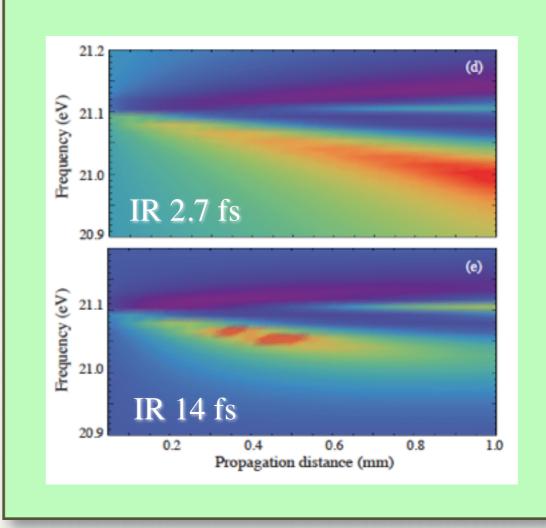




Note: more complicated when first burst becomes comparable to duration of IR perturbation:

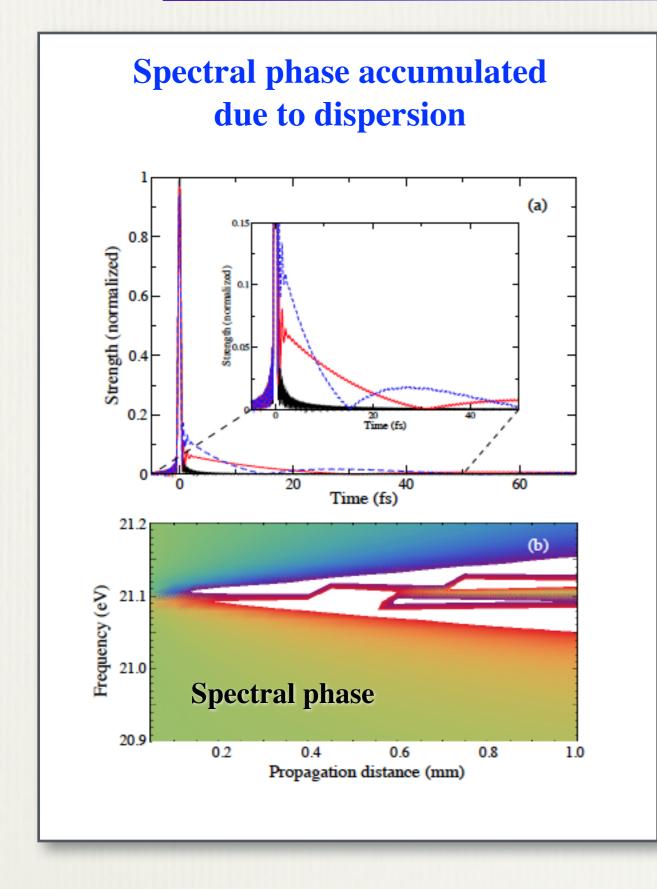
- outer lineshape not preserved
- increase in width not linear in z

- Short IR: first extra burst is new "lifetime" over which perturbed dipole oscillates (bandwidth of outer structure)
- Inner structure(s) come from additional bursts in time

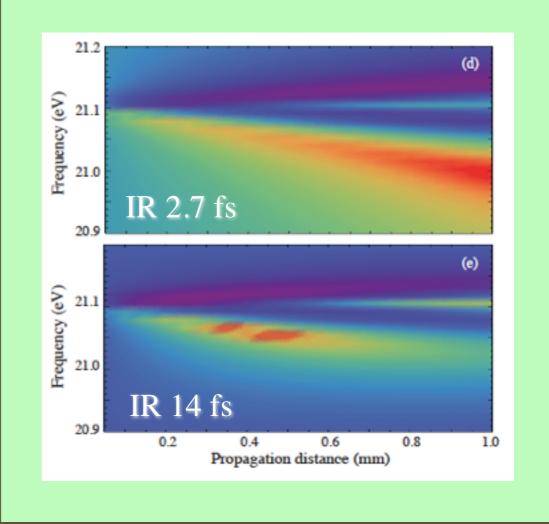




Example II: frequency domain thoughts



- Bandwidth of ±π/2 controls duration of first extra peak causes sign change of E-field
- In absence of IR only broadening through saturation





Summary

- TDSE-MWE, self-consistent solution allows to study reshaping of light by medium
- Argon Cooper min induces reshaping of attosecond pulses even at single atom level
- Reshaping effects of attosecond pulse propagation in dense medium with narrow absorption lines, dressed by IR pulse

LSU Attosecond th. group

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Ken Lopata (Chemistry)

Mengxi Wu

Seth Camp

Paul Abanador

Xiaoxu Guan

Renate Pazourek

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Ohio State exp. group

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Stephen Schoun

Razvan Chirla

Jonathan Wheeler

Christoph Roedig

U Arizona exp. group

Arvinder Sandhu

Chen-Ting Liao

Funding

NSF, DOE BES, LONI (computing time)



Two post doc positions at LSU, starting immediately

- One postdoc in physics (Schafer/Gaarde)
- One postdoc in chemistry (Lopata)

Project: Charge migration using HHS? Collaboration physics/chemistry, exps at OSU/UVA