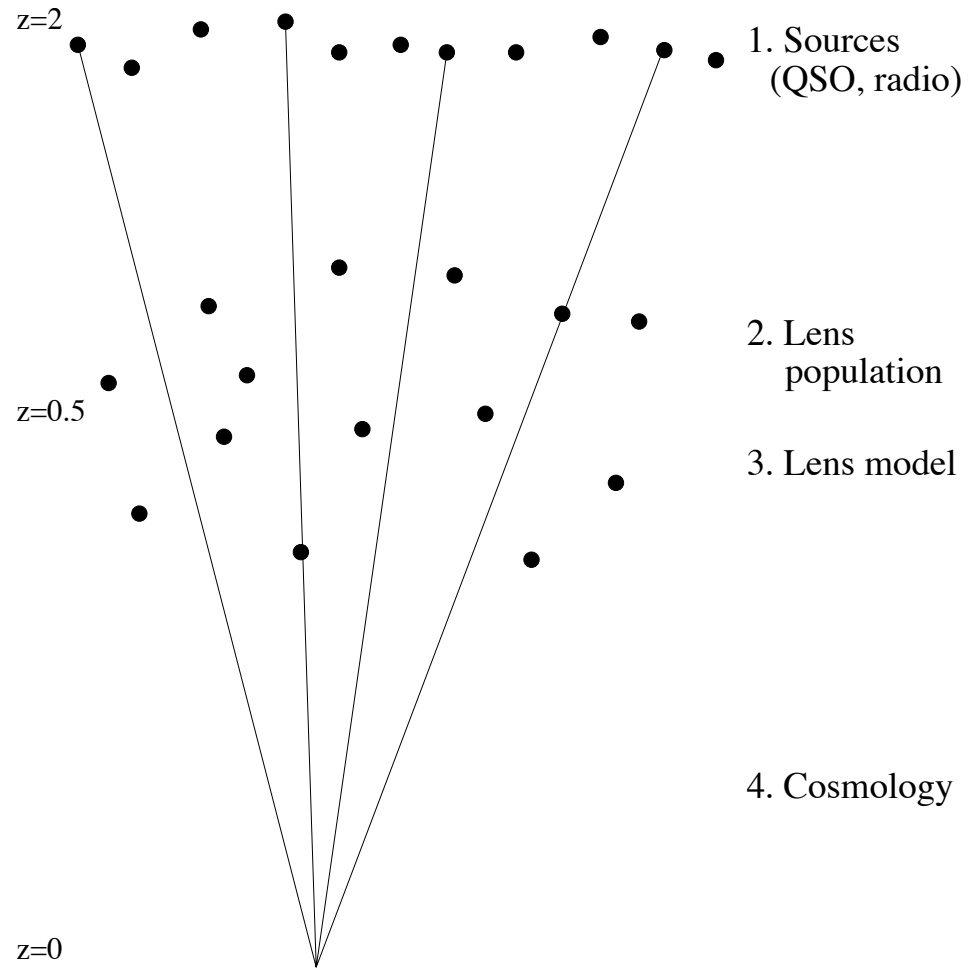


# Cosmology with Strong Lensing

Chuck Keeton (*Rutgers*)



# Flavors

	<i>Direct</i>	<i>Indirect</i>
<i>Then</i>	cosmography	
<i>Now</i>		evolution
<i>When?</i>	lensing Hubble diagram ← alternative cosmologies →	

## Lens Statistics

Non-evolving population of **isothermal spheres**. (e.g., Turner; Kochanek)

Lensing rate

$$\tau(z_s) = \phi_* \sigma_*^4 f(\alpha, \beta) \times \boxed{D(z_s)^3}$$

Volume test!

Depending on what you know, use

$$\frac{\partial \tau}{\partial(\Delta\theta)} \quad \text{or} \quad \frac{\partial^2 \tau}{\partial z_l \partial(\Delta\theta)}$$

Note: redshift distribution

$$p(z_l|z_s) = 30 \frac{D_{ol}^2 D_{ls}^2}{D_{os}^5} \frac{dD_{ol}}{dz_l}$$

# 1. Source Population

## Optical QSOs

- flux and redshift distributions known
- lens selection effects
  - seeing
  - extinction
  - lens galaxy luminosity
- $N = 4$  (pre-SDSS)

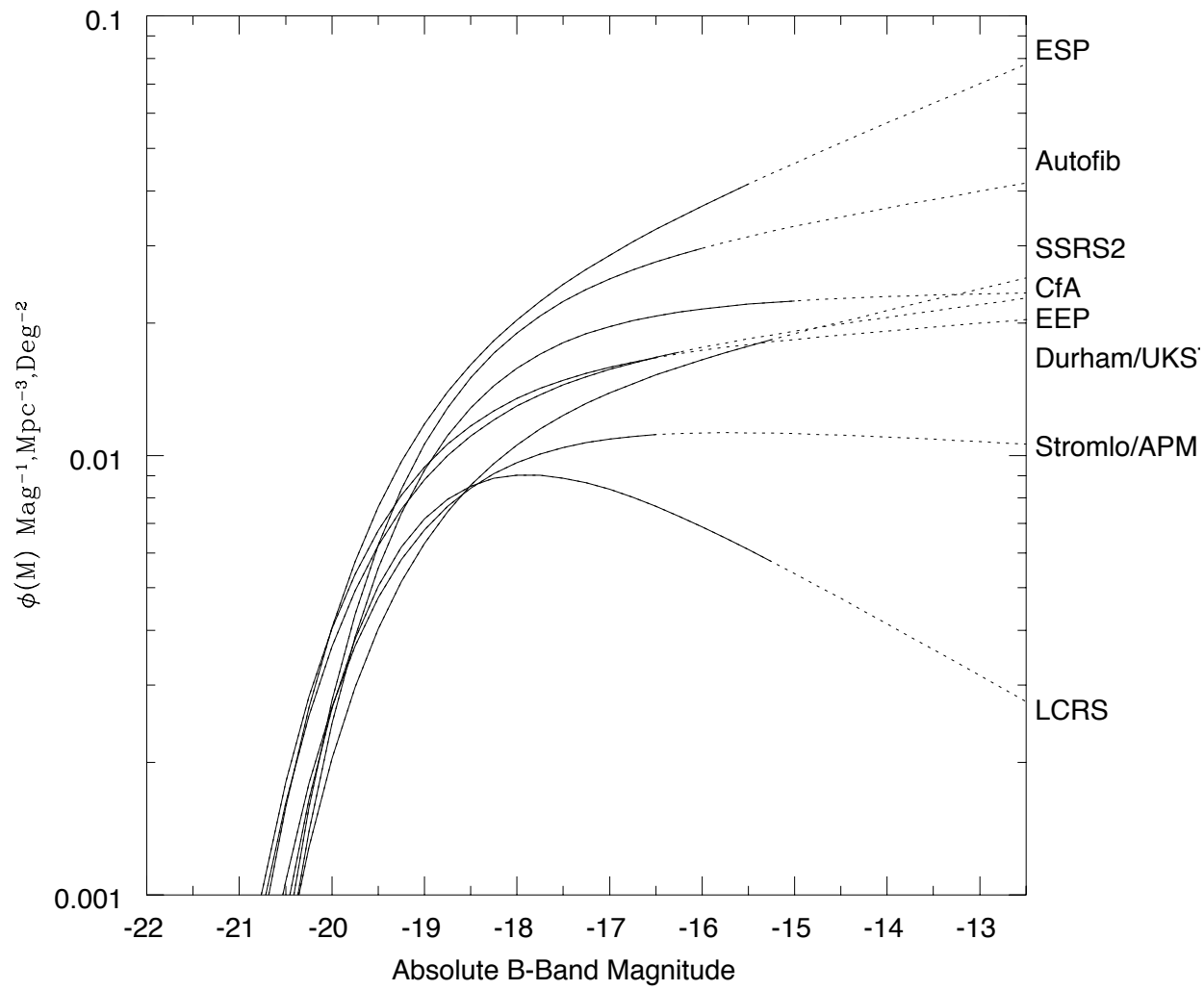
## Radio sources

- flux distribution known
- redshift distribution *not* well known
- selection effects less important
- $N = 13$  from CLASS

## 2. Deflector Population: Velocity Dispersion Function

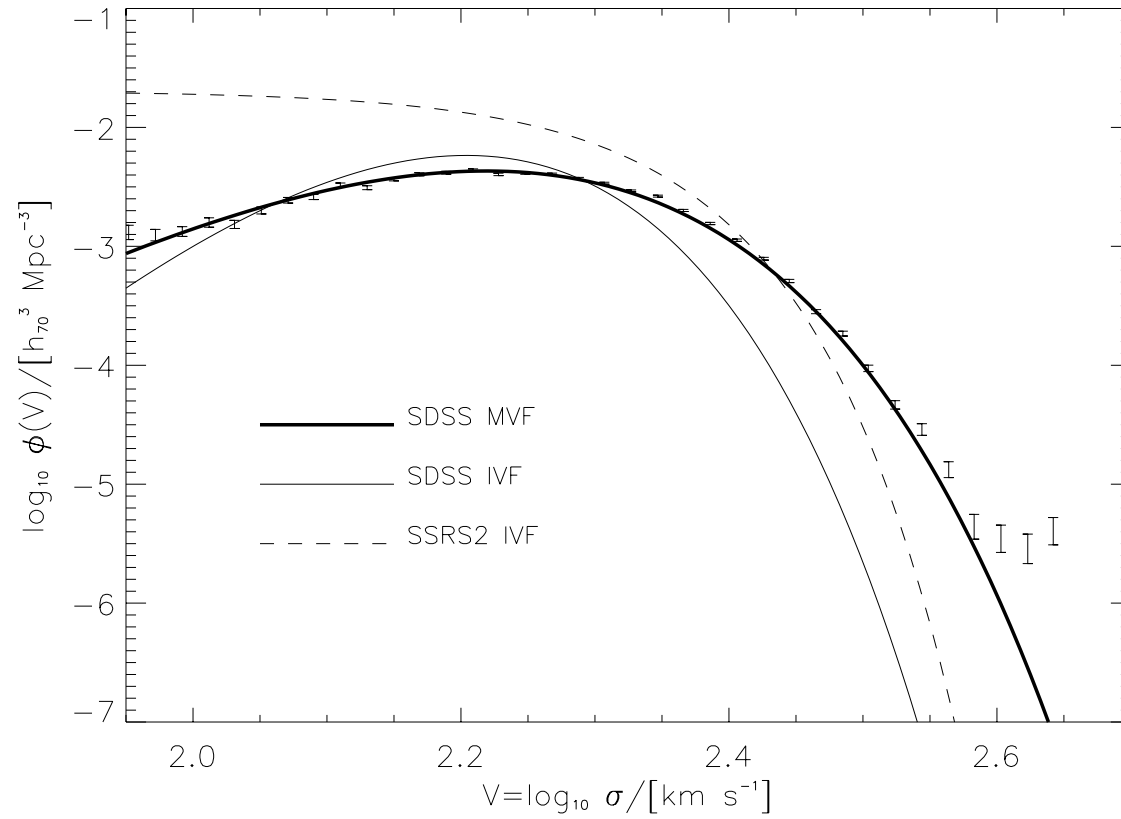
Inferred velocity function (IVF): luminosity function + Faber-Jackson

Study	Lens Sample	LF	$\Omega_\Lambda$ (if flat)
Kochanek (1996)	Opt+Rad	$\equiv$ K96	$< 0.66$
Falco et al. (1998)	Opt/Rad	K96	$< 0.73 / 0.62 / 0.74$
Helbig et al.	Rad	K96	$< 0.65$
Waga & Miceli (1999)	Opt	K96	$< 0.55 / 0.76 / 0.91$
Cooray et al. (1999)	HDF	HDF	$< 0.72\text{---}0.79$
Cooray (1999)	Rad	ESP	$< 0.79$
		EEP	$\simeq 0.5$
Chiba & Yoshii (1999)	Opt+Rad	APM	$\simeq 0.7$
		CfA	$\simeq 0.8$

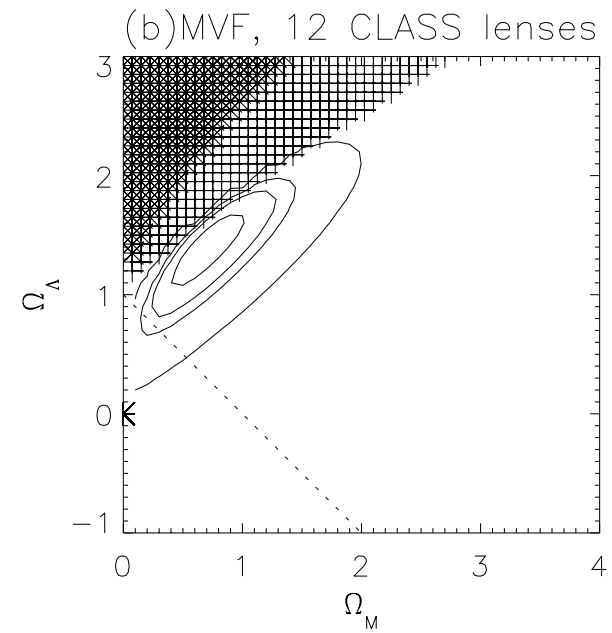
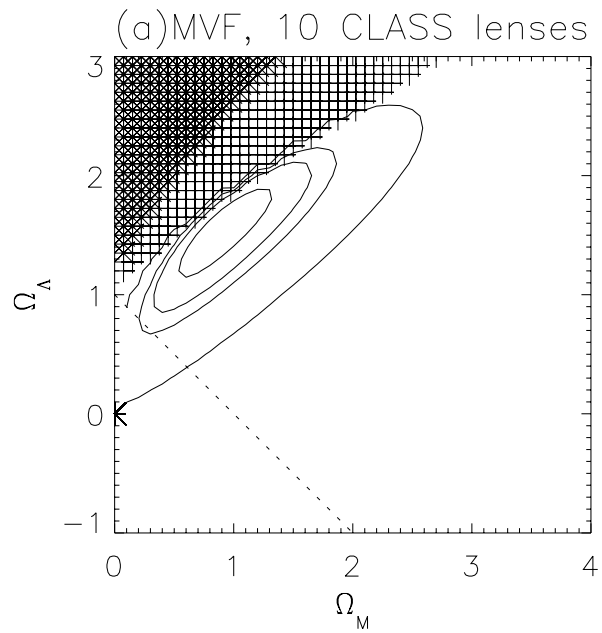


*Cross et al. (2001)*

# Measured velocity function (MVF)



*Sheth et al. (2003); Mitchell et al. (2005)*



Chae (2003) finds similar results.

Agreement with SNe (not forced).

Evolution has little effect (fortuitous).



## “Plus ça change . . .”

Deflector population:

- Chae (2005) suggests the SDSS MVF undercounts early-type galaxies  
⇒ general interest

Source population:

- Radio parent population is poorly characterized (*Maoz 2005*)  
⇒ hard work
- Reconsider optical lens samples (*Maoz; Inada, Oguri, et al.*)  
⇒ selection functions, extinction, . . .

Lens model:

- Ellipticity not so important (*Huterer et al. 2005*)  
⇒ can be incorporated (*e.g., Chae 2003*)
- Environment can boost image separation, magnification (*CRK & Zabludoff 2004*)  
⇒ environments being surveyed (*talks by Zabludoff, Fassnacht*)

## Evolution?

Direct cosmography:  $\phi_*$  and  $\sigma_*$  degenerate with volume

*One man's noise ... is another man's signal.*

Indirect cosmology:

- number, mass evolution — growth of structure
- luminosity evolution — epoch of galaxy formation

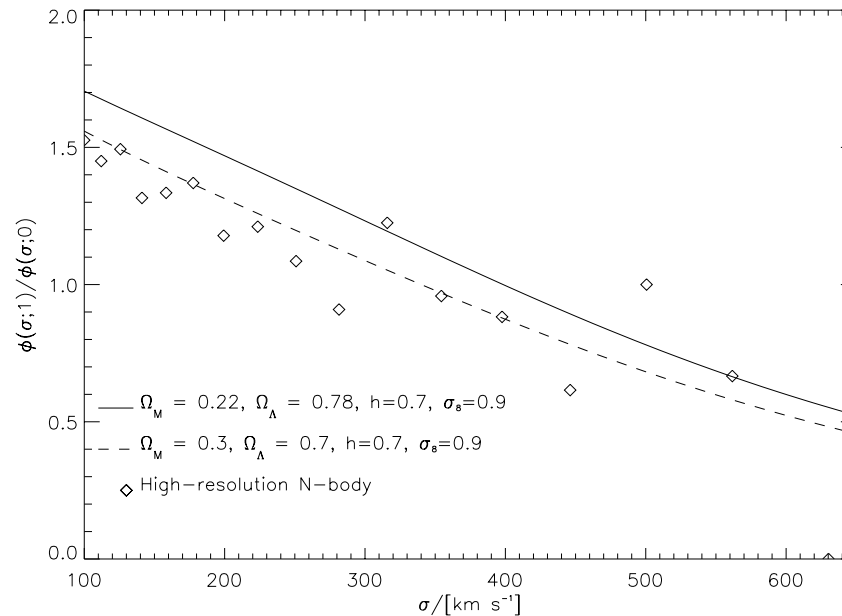
# Mass Evolution I

Build an evolution model into lens statistics ...

If mergers preserve Fundamental Plane  $\Rightarrow$  little effect on  $\tau$ , more on  $p(\Delta\theta)$ .

(Rix et al. 1994; Mao & Kochanek 1994)

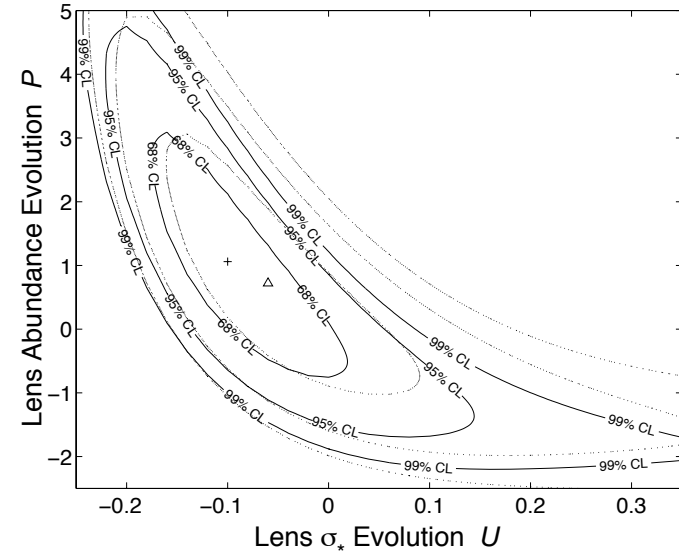
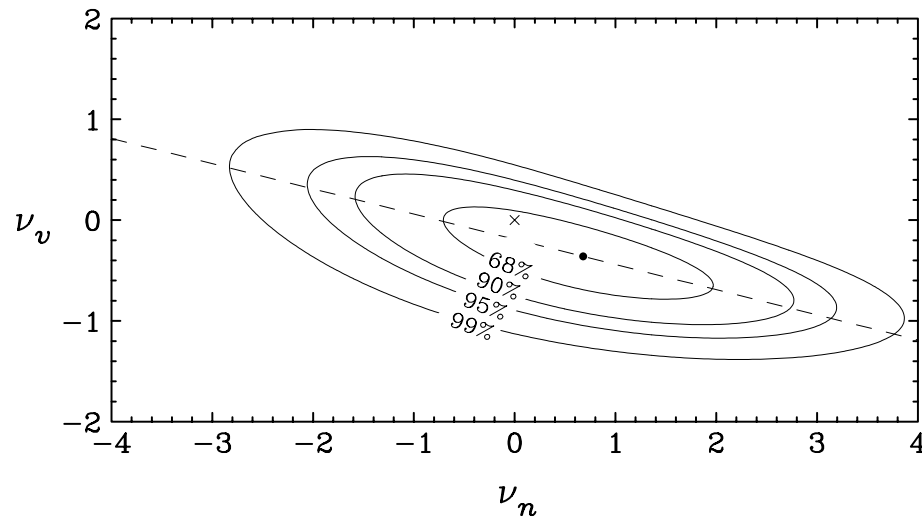
Use extended Press-Schechter theory to predict  $\phi(\sigma, z)/\phi(\sigma, 0)$ .



## Mass Evolution II

Use statistics to constrain a phenomenological evolution model:

- Chae & Mao (2003):  $n_*(z) = n_*(1+z)^{\nu_n}$ ,  $\sigma_*(z) = \sigma_*(1+z)^{\nu_v}$
- Ofek et al. (2003):  $n_*(z) = n_* 10^{Pz}$ ,  $\sigma_*(z) = \sigma_* 10^{Uz}$



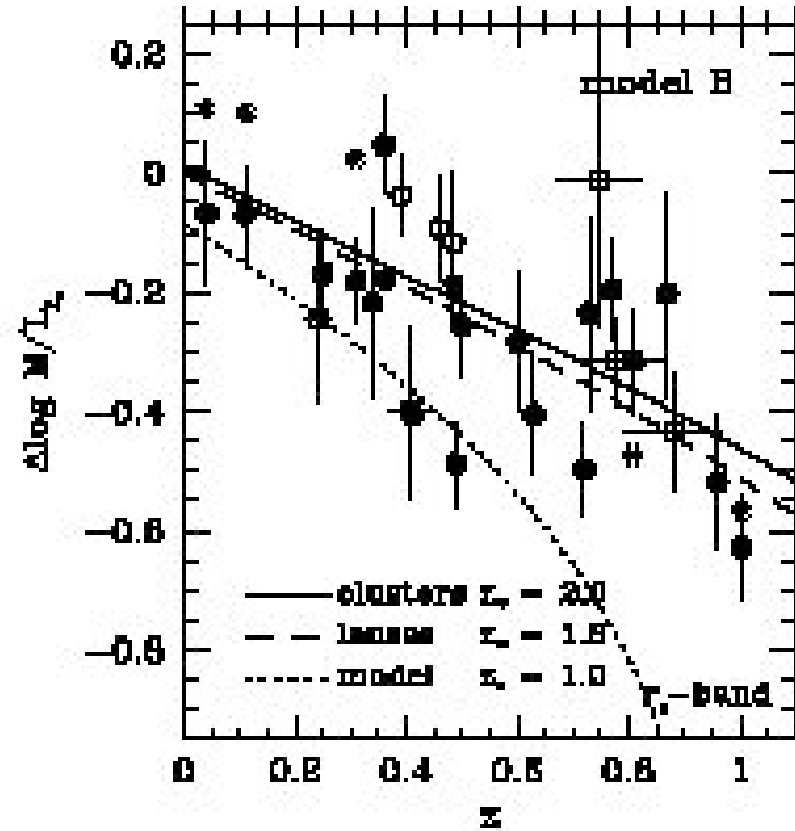
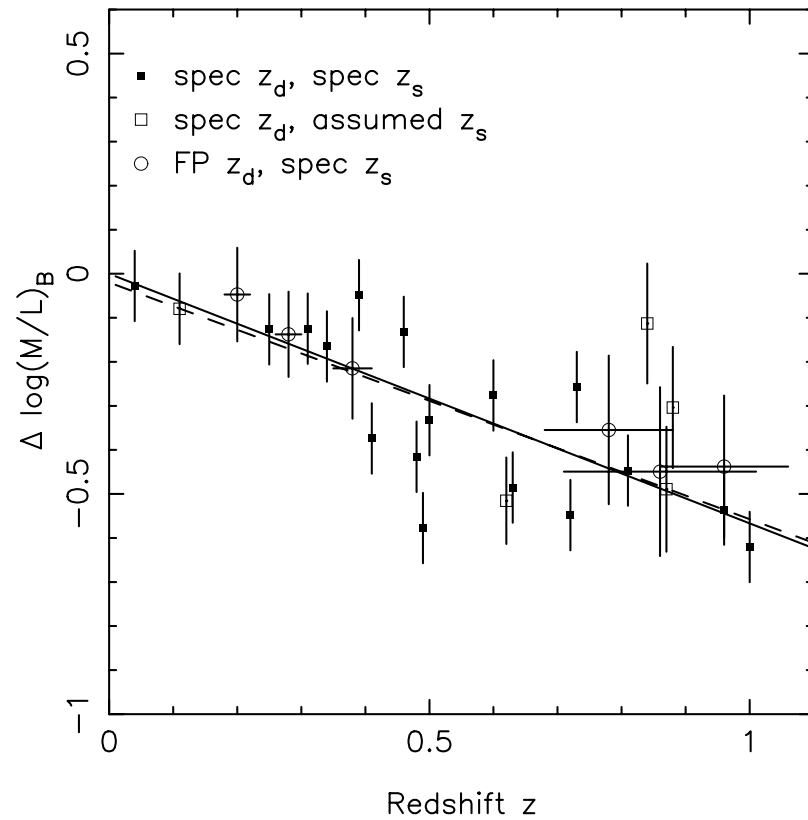
Stronger constraints on mass evolution than number evolution.

Ofek et al.: resurrect redshift test, expand sample.

# Luminosity Evolution

Measure  $M/L$  vs.  $z$ .

(CRK et al. 1998; Treu & Koopmans; Rusin et al.; van de Ven et al.)



# Luminosity Evolution

Can be applied to an [ensemble](#).

Constrains star formation histories of E/S0 lens galaxies.

- stars are old:  $\langle z_f \rangle > 1.5$
- evidence for a range of  $z_f$

(Some debate over the details ...)

E/S0 galaxies in “low-density” environments not much younger than in clusters  
— challenge to CDM galaxy formation models.

# Lensing and Dark Energy

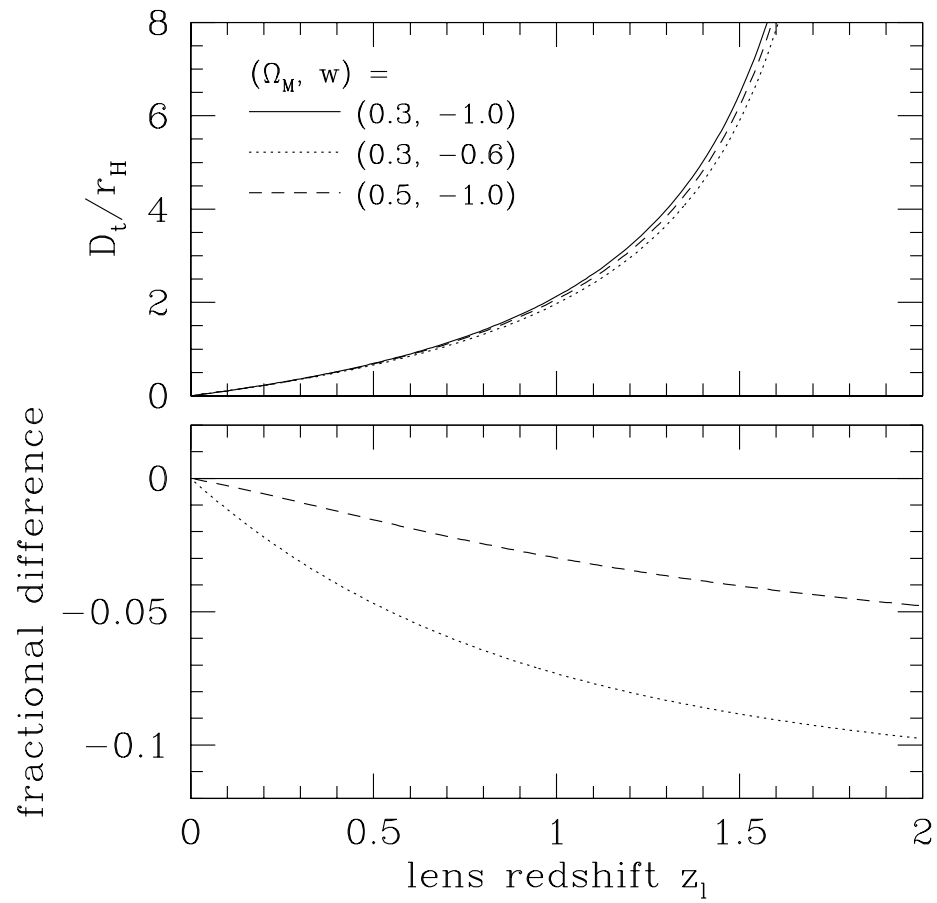
$w$  is all the rage.

Lensing rate: Waga & Miceli (1999), Cooray (1999), Cooray & Huterer (1999)

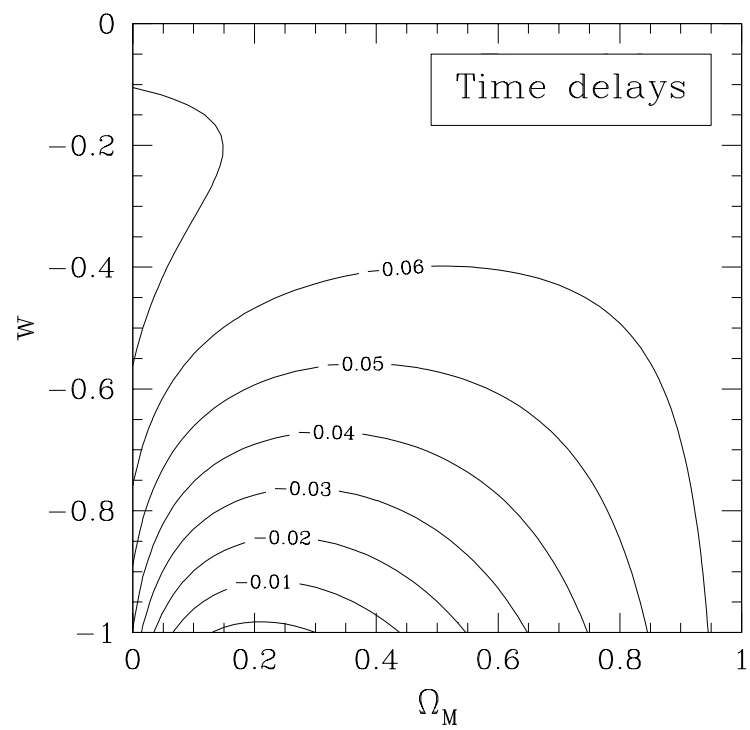
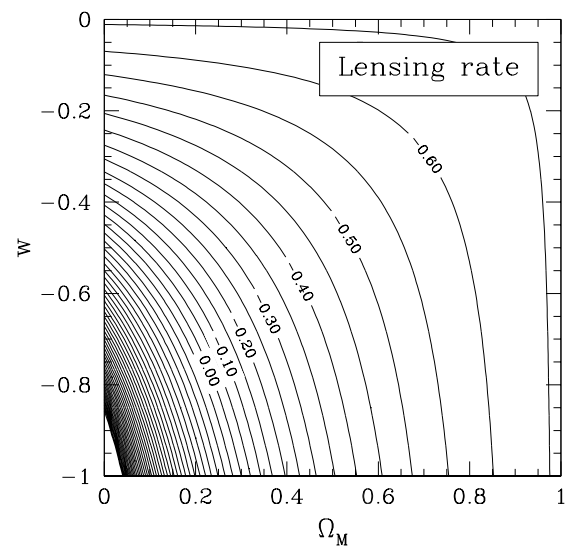
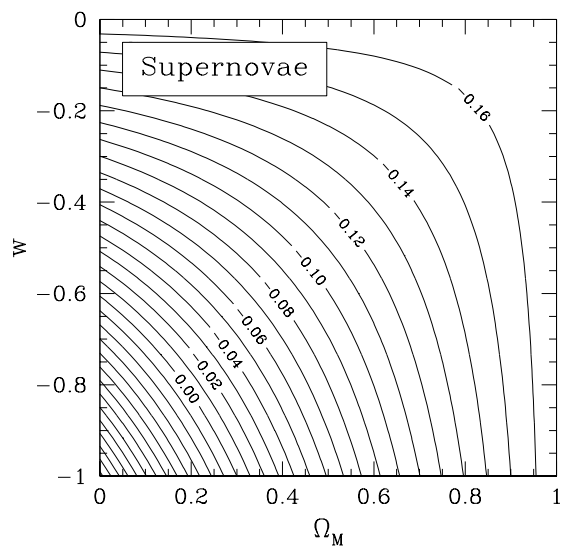
Time delays and image separations: Lewis & Ibata (2002), Linder (2004)

# Lensing Hubble Diagram

“time delay distance”  $D_t = \frac{D_{ol}D_{os}}{D_{ls}}$





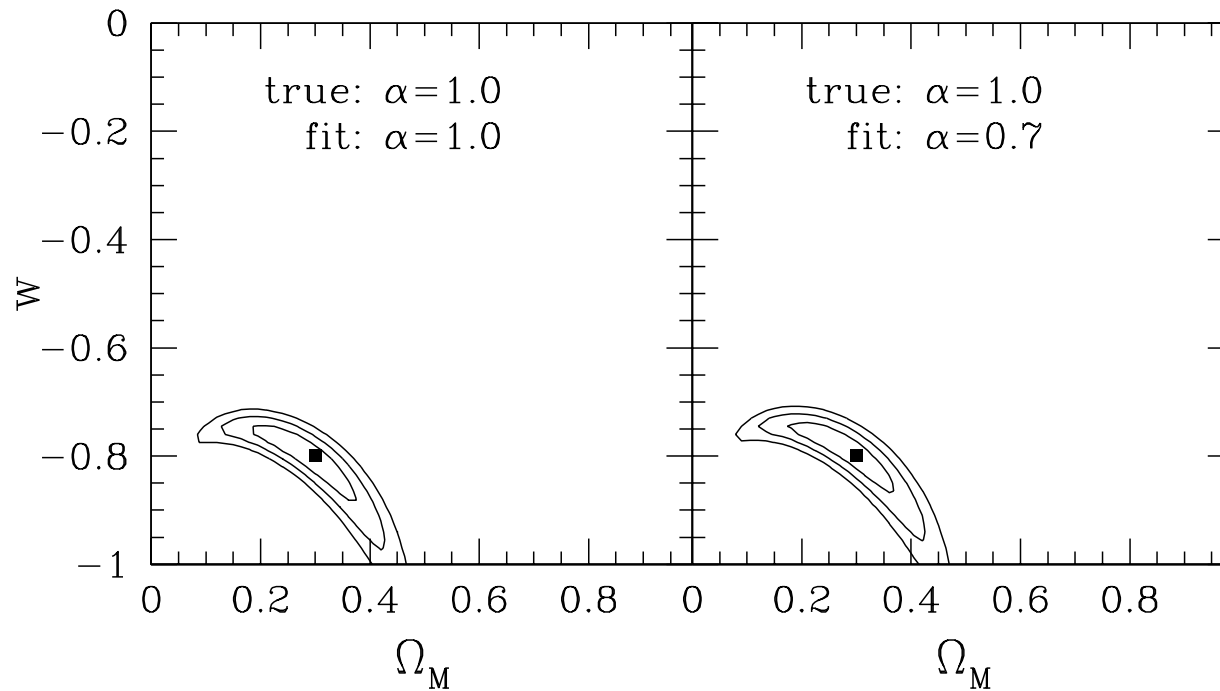


## Practical?

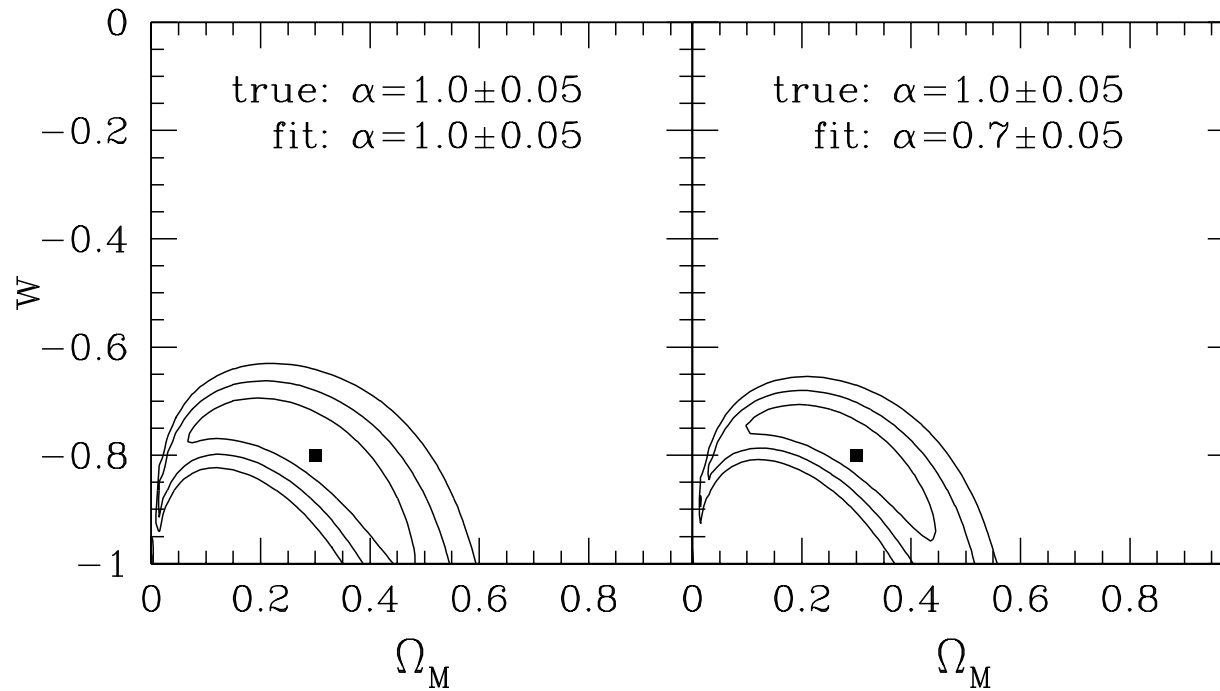
Future: 1000 lenses, to beat down random noise

Use as an [ensemble](#), exactly like SNe.

Finesse radial profile degeneracy:  $\mathcal{H} = H_0 (1 - \langle \kappa \rangle)$  is a nuisance parameter.



## What Matters is Scatter



- profiles
- shapes
- environments

**Lensing cosmology is dead. Long live lensing cosmology!**

Lens statistics ensembles still have something interesting to say.

Now: evolution

Future: lensing Hubble diagram???

*(Ask me about alternative cosmologies ...)*

## Alternative Cosmologies

Change gravity. Some modifications may be amplified near black holes.

CRK & Petters: framework for testing theories of gravity with black hole lensing.

Galactic black hole:

	weak-field	higher-order
image positions	0.01–0.1 arcsec	few microarcsec
time delay	minute	tens of millisecc

A lensed millisecond pulsar?

# Randall-Sundrum Braneworld Gravity

- primordial black holes  $\leftrightarrow$  gamma-ray interference
- “attolensing” of gamma-ray bursts

