Loopy Ideas About Dark Matter

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based on 1208.4605, 1302.4454 & 13xx.xxxx with Kahlhoefer, Re & Unwin

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Evidence For Dark Matter



Conclusive observational evidence for dark matter (DM) over a wide range of astrophysical scales

Evidence For Dark Matter



[Planck, 1303.5076]

Particle Candidates For DM

Most popular candidate is WIMP, a cold thermal relic with weak-scale mass & interactions (e.g. lightest supersymmetric particle) which can have required relic abundance: the WIMP miracle

But many alternative exists:

Asymmetric DM (same origin as baryon asymmetry)

Warm DM (e.g. sterile keV neutrinos)

Axions

...









DM Direct Detection

- DM particles from galactic halo pass through earth & will occasionally scatter off nuclei
- Resulting recoil energy of nucleus can be measured in dedicated low background detectors



Typical event rates less than 1 event per kg per year. A great experimental challenge

DM Indirect Detection

 Indirect detection experiments search for products of DM annihilation in regions of high DM density (e.g. galactic centre) with satellites, ballons & telescopes



Difficulties arise from astrophysical backgrounds & unknown DM density profile

DM Searches At Colliders



Any DM particle produced directly at collider escapes detector unnoticed. But if DM pair is produced in association with a jet or photon, will observe large amount of missing transverse energy

Synergy & Complementarity



If DM particles give signal in one search, expect to see related processes with distinctive signature in other searches. Conversely, can translate bounds from one kind of search strategy to another

Synergy & Complementarity

typical momentum transfer



While LHC probes TeV scale, DM direct detection tests non-relativistic limit $(v \approx 10^{-3} \cdot c)$

Interactions that look very similar at LHC might look quite different in direct detection

Synergy & Complementarity

Assume that DM particle interacts with quarks via exchange of spin-1 mediator which couples to

 $\bar{\chi}\gamma_{\mu}\chi \qquad \qquad \bar{\chi}\gamma_{\mu}\gamma_{5}\chi$

At LHC: impossible to distinguish between vector & axial couplings since mono-jet cross sections essentially the same

In direct detection:

vector couplings axial couplings mixed couplings



spin independent: $\sigma \propto A^2 = O(10^4)$ spin dependent: $\sigma \propto 1$ momentum suppressed: $\sigma \propto v^2$

Effective Theory Of DM

To compare LHC measurements to direct detection, useful to describe interactions between DM & SM particles in terms of effective operators, which arise from integrating out heavy mediators. E.g.:

$$\mathcal{O}_V = \frac{1}{M_*^2} \left(\bar{\chi} \gamma_\mu \chi \right) \left(\bar{q} \gamma^\mu q \right)$$

vector operator: spin independent

axial operator: spin dependent

$$\mathcal{O}_{AN} = \frac{1}{M_*^2} \left(\bar{\chi} \gamma_\mu \gamma_5 \chi \right) \left(\bar{q} \gamma^\mu q \right)$$

 $\mathcal{O}_{AX} = \frac{1}{M_{\perp}^2} \left(\bar{\chi} \gamma_{\mu} \gamma_5 \chi \right) \left(\bar{q} \gamma^{\mu} \gamma_5 q \right)$

anapole operator: momentum dependent

Direct Detection vs. LHC

Direct detection cross section per nucleon reads



$$m_{\rm red} = \frac{m_{\chi}m_{\chi}}{m_{\chi} + m_{\chi}}$$

Mono-jet cross section given by



Provided effective theory applicable at LHC, can directly relate mono-jet (-photon) searches & direct detection experiments

POWHEG Goes DM



[UH, Kahlhoefer & Re, 13xx.xxx]		
$m_{\chi} \; [{ m GeV}]$	M_* in \mathcal{O}_V [GeV]	
10	786^{+16}_{-22}	
20	785^{+17}_{-21}	
50	784^{+17}_{-22}	
100	782^{+15}_{-21}	
200	765^{+18}_{-20}	
500	623^{+11}_{-16}	
1000	335^{+6}_{-10}	

 $|E_T, p_T^{j_1} > 500 \,\text{GeV}$ $|\eta_{j_1}| < 2 \qquad |\Delta \phi_{\vec{p}_T, \vec{p}_T^{j_2}}| > 0.5$

[see also MCFM implementation by Fox & Williams, 1211.6390]

POWHEG Goes DM



Including NLO corrections reduces scale uncertainties by a factor of 3. Constant K factor of about 1.4 for m_χ < 1 TeV

Operator Mixing

- So far, have ignored an important aspect: to calculate direct detection cross sections, must evolve effective operators from new-physics scale M* down to hadronic scale mN
 - In evolution, new interactions may be induced radiatively, leading to additional operators, which are absent (or small) at M*
 - A full computation should include mixing of all operators & resummation of large logarithms using renormalization group (RG) techniques



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Mixing & Matching

Consider scalar operator

$$\mathcal{O}_S = \frac{m_q}{M_*^3} \left(\bar{\chi} \chi \right) \left(\bar{q} q \right)$$

which may arise from exchange of a spin-0 mediator with couplings proportional to quark mass m_q

At tresholds, heavy quarks can be integrated out leading to a DM-gluon-gluon coupling

$$\mathcal{O}_G = \frac{1}{M_*^3} \mathcal{C}_G \left(\bar{\chi} \chi \right) (G_{\mu\nu})^2$$
$$\mathcal{C}_G(m_t) = -\frac{\alpha_s(m_t)}{12\pi}$$



[Shifman et al., Sov. J. Nucl. Phys. (1979) 30]

Matrix Elements

At low energies need to evaluate hadronic matrix elements of scalar & gluon operator sandwiched between nucleus states:

$$\sum_{q} \langle A | \mathcal{O}_{q} | A \rangle = 2m_{N}A \left(\sum_{q} f_{q}\right) F_{\text{Helm}} \approx 0.14 m_{N}AF_{\text{Helm}}$$

$$\langle A|\mathcal{O}_G|A\rangle = -2\frac{8\pi}{9\alpha_s}m_NAf_GF_{\text{Helm}}\mathcal{C}_G \approx 0.41m_NAF_{\text{Helm}}$$

 $f_u \approx 0.021$ $f_d \approx 0.038$ $f_s \approx 0.013$ $f_G = 1 - \sum_q f_q \approx 0.928$

Loop suppression of DM-gluon-gluon contribution to direct detection overcompensated by large gluon density in nucleons

Scalar Interactions

What is correct way to analyze constraints from LHC monojet searches for scalar operators?

Tree-level cross sections are small because heavy-quark luminosities are tiny & light quarks suffer Yukawa suppression



Scalar Interactions

What is correct way to analyze constraints from LHC monojet searches for scalar operators?

At 1-loop level heavy-quark loops start to contribute to monojet cross section & expected to lift Yukawa suppression



Mono-Jet Analysis

Mono-jet cross sections have been obtained using FeynArts, FormCalc & LoopTools & results were cross-checked with MCFM, modifying pp $\rightarrow h + j \rightarrow \tau^+\tau^- + j$

[Ellis et al., Nucl. Phys. B297 (1988) 221]

Analysis incorporates all cuts imposed in 5 fb⁻¹ CMS search [Chatrchyan et al., 1206.5663]

Shower & hadronization effects are not included, but are expected to be small, because primary jet has very large pT [Bai, Fox & Harnik, 1005.3797]

LHC Bounds: Scalar Case



Inclusion of top-quark loops increases mono-jet cross sections (bound on M_{*}) by a factor of around 500 (3)

Full Calculation Needed?

Tempting to consider $m_t \rightarrow \infty$ limit & use operator

$$\mathcal{O}_{G} = -\frac{\alpha_{s}}{12\pi} \frac{1}{M_{*}^{3}} \, (\bar{\chi}\chi) \, (G_{\mu\nu})^{2}$$

to calculate cross sections

Effective theory calculation overestimates cross sections by at least a factor of 3 & error grows rapidly reaching a factor of 40 for m_χ = 1 TeV

Result unsurprising, as high-pT jet able to resolve structure of top-quark loop. Same happens in h + j production for pT >> mt

[Baur & Glover, Nucl. Phys. B339 (1990) 38]

Accuracy Of Calculation

For pp \rightarrow h + j ratio between NLO & LO is around 1.5, but unclear how this translates into K factor for mono-jet signal, since Higgs result based on m_t $\rightarrow \infty$ limit

Secondary jets allowed in LHC analyses & their impact can be studied by looking at pp → h + 2j. Depending on cuts can lead to enhancements of cross section by a factor of 2

LO results for mono-jet production via (pseudo-)scalar DMtop-quark interactions are therefore not very accurate, but should give conservative lower bounds on new-physics scale

LHC & Direct Detection Bounds



Parameter regions favored by DAMA & CoGeNT clearly excluded by loop-level bound

Pseudoscalar Interactions

For pseudoscalar operator

$$\mathcal{O}_{PS} = \frac{m_q}{M_*^3} \left(\bar{\chi} \gamma_5 \chi \right) \left(\bar{q} \gamma_5 q \right)$$

DM scattering is spin dependent & in addition suppressed by a factor of $q^4/m_N^4 << 1$

As a result, no relevant constraint on M* derives from direct detection experiments (at present & in future)

At LHC scalar & pseudoscalar interactions look very similar, so that one can obtain strong bounds on new-physics scale

LHC Bounds: Pseudoscalar Case



Imposing that DM is not overproduced leads to $m_{\chi} > 44$ GeV (Dirac fermion) & $m_{\chi} > 55$ GeV (Majorana fermion)

Spin-Dependent Interactions

Two operators lead to spin-dependent interactions:

$$\mathcal{O}_{AX} = \frac{1}{M_*^2} \left(\bar{\chi} \gamma_{\mu} \gamma_5 \chi \right) \left(\bar{q} \gamma^{\mu} \gamma_5 q \right) \qquad \text{axial operator}$$
$$\mathcal{O}_T = \frac{1}{M_*^2} \left(\bar{\chi} \sigma_{\mu\nu} \chi \right) \left(\bar{q} \sigma^{\mu\nu} q \right) \qquad \text{tensor operator}$$

For spin-dependent interactions, direct detection bounds are weak due lack of coherent enhancement

Mono-jet searches should thus be superior in constraining spin-dependent cross sections. Naive expectation true?

Let There Be Light!

- However, direct detection bounds boosted if spin-dependent operator induces spin-independent interactions via loops
- Effect most striking in case of tensor operator, since top-quark loops induce a DM magnetic dipole moment:

$$\mathcal{O}_M = \frac{1}{M_*^2} \,\mathcal{C}_M \left(\bar{\chi} \sigma_{\mu\nu} \chi \right) F^{\mu\nu}$$
$$\mathcal{C}_M \simeq \frac{e}{2\pi^2} \,m_t \ln \frac{M_*^2}{m_t^2}$$



[UH & Kahlhoefer, 1302.4454; in context of leptophilic DM see also Kopp et al., 0907.3159]

Induced Dipole Moments

Due to photon pole, DM-nucleon scattering cross sections strongly enhanced for small momentum transfer

DM dipole moments are thus severely constrained by direct detection



Resulting constraints can be translated into bounds on M_{*} & direct detection limits on new-physics scale typically stronger than those from LHC mono-jet searches











Loop- vs. Tree-Level Bounds



Loop- vs. Tree-Level Bounds



Axial Operator

In case of axial operator spinindependent interactions are induced by loop graphs with two operator insertions



A contribution to vector operator is not induced but scalar operator receives logarithmic correction of form:

$$\mathcal{O}_S = \frac{m_q}{M_*^3} \, \mathcal{C}_S \left(\bar{\chi} \chi \right) \left(\bar{q} q \right) \qquad \qquad \mathcal{C}_S \simeq -\frac{1}{2\pi^2} \frac{m_\chi}{M_*} \ln \frac{M_*^2}{m_\chi^2}$$

[UH & Kahlhoefer, 1302.4454; see also Cirelli, Fornengo & Strumia, 0512090; Essig, 0710.1668]

Loop- vs. Tree-Level Bounds



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Loop- vs. Tree-Level Bounds



Conclusions

- Because of large separation of scales, different interactions may be relevant for different kind of DM searches
- For scalar interactions, loops lead to striking enhancement of mono-jet cross section, but need to include full top-quark mass dependence to obtain accurate results

- Certain spin-dependent interactions induce DM dipole moments through heavy-quark loops (& other spin-independent effects), which are strongly constrained by direct detection
- Further studies of loop effects may play an essential part in combining the virtues of different search strategies & may be needed to solve DM problem

LHC Mono-Jet Analyses

POWHEG analysis based on 7 TeV ATLAS search for jets & missing energy (MET) with integrated luminosity of 4.7 fb⁻¹ [ATLAS, 1210.4491]

ATLAS result excludes new contribution to cross section in excess of 6.9 fb at 95% confidence level

Bounds On Pseudotensor Operator



Bounds on New-Physics Scale

		[UH & Kahlhoefer, 1302.4454]
$m_{\chi} \; [\text{GeV}]$	M_* in \mathcal{O}_T [GeV]	M_* in \mathcal{O}_{PT} [TeV]
10	1880^{+360}_{-450}	$65.6^{+5.5}_{-5.6}$
20	3360^{+520}_{-600}	$123.7^{+9.6}_{-9.6}$
50	3740^{+560}_{-640}	$158.2^{+12.0}_{-11.9}$
100	3220^{+500}_{-580}	$144.2^{+11.0}_{-11.0}$
200	2690^{+430}_{-510}	$123.6^{+9.6}_{-9.6}$
500	2070^{+380}_{-470}	$98.3^{+7.9}_{-7.9}$
1000	1680^{+330}_{-440}	$81.6^{+6.7}_{-6.7}$

Bounds On Axial Operator



Top-Flavored MFV DM

Assumption of minimal flavor violating (MFV) automatically leads to stable DM candidate

[Batell, Pradler & Spannowsky, 1105.1781]

Can build simple MFV model where DM carries top flavor:

 $\chi \sim (1,1,0)_{G_{\rm SM}} \otimes (1,3,1)_{G_F} \quad \phi \sim (3,1,2/3)_{G_{\rm SM}} \otimes (1,1,1)_{G_F}$

 $\mathcal{L} \supset -\bar{\chi} \left(m_0 + m_1 Y_u^{\dagger} Y_u + \ldots \right) \chi$ $+ \left[\bar{q}_R \left(g_0 + g_1 Y_u^{\dagger} Y_u + \ldots \right) \chi \phi + \text{h.c.} \right]$

[Kumar & Tulin, 1303.0332]

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Top-flavored MFV DM able to explain large top-asymmetry



[Kumar & Tulin, 1303.0332]

Top-Flavored MFV DM

MFV top-flavored DM model has interesting loop structure



direct detection, relic density & invisible Z width

magnetic dipole moment

mono-jet (?) searches

DM Couplings To Top Quarks

Scalar interactions between top quarks & DM can also be probed in top-pair production plus missing energy (MET)



Naively not as powerful as mono-jets, but shape differences may allow to improve tī + MET search



[Lin, Kolb & Wang, 1303.6638]

What About Indirect Detection?

arXiv:1204.2797v2 [hep-ph] 8 Aug 2012

A Tentative Gamma-Ray Line from Dark Matter Annihilation at the Fermi Large Area Telescope

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Abstract. The observation of a gamma-ray line in the cosmic-ray fluxes would be a smokinggun signature for dark matter annihilation or decay in the Universe. We present an improved search for such signatures in the data of the Fermi Large Area Telescope (LAT), concentrating on energies between 20 and 300 GeV. Besides updating to 43 months of data, we use a new data-driven technique to select optimized target regions depending on the profile of the Galactic dark matter halo. In regions close to the Galactic center, we find a 4.6 σ indication for a gamma-ray line at $E_{\gamma} \approx 130$ GeV. When taking into account the lookelsewhere effect the significance of the observed excess is 3.2σ . If interpreted in terms of dark matter particles annihilating into a photon pair, the observations imply a dark matter mass of $m_{\chi} = 129.8 \pm 2.4_{-13}^{+7}$ GeV and a partial annihilation cross-section of $\langle \sigma v \rangle_{\chi\chi \to \gamma\gamma} =$ $(1.27 \pm 0.32_{-0.28}^{+0.18}) \times 10^{-27}$ cm³ s⁻¹ when using the Einasto dark matter profile. The evidence for the signal is based on about 50 photons; it will take a few years of additional data to clarify its existence.

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Official Fermi-LAT analysis shows less significant effect at around 135 GeV. Unfortunately, there is also line-like feature at same energy in earth limb data (where there should be none)

Cross Section Estimates

Consider effective DM-photon-photon interactions

$$\mathcal{L}_{\text{eff}} = \frac{\alpha}{4\pi} \frac{1}{M_*^{2d_{\chi}}} \left(\bar{\chi}\chi\right) \left(F_{\mu\nu}\right)^2$$

Depending on whether DM particle is a scalar or fermion get different annihilation cross sections into γ -rays:

$$\langle \sigma_{\chi} v \rangle_{\gamma\gamma} \propto \begin{cases} \frac{m_{\chi}^2}{\pi} \left(\frac{\alpha}{4\pi} \frac{1}{M_*^2} \right)^2 \\ \frac{v^2 m_{\chi}^4}{\pi} \left(\frac{\alpha}{4\pi} \frac{1}{M_*^3} \right)^2 \end{cases}$$

s-wave annihilation

p-wave annihilation

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To obtain a γ-ray signal close to 130 GeV with a cross section of 1.3 · 10⁻²⁷ cm³ s⁻¹ requires lowish new-physics scales:

$$\langle \sigma_{\chi} v \rangle_{\gamma\gamma} \propto \begin{cases} \frac{m_{\chi}^2}{\pi} \left(\frac{\alpha}{4\pi} \frac{1}{M_*^2} \right)^2 & \longrightarrow & M_* \approx 100 \,\text{GeV} \\ \frac{v^2 m_{\chi}^4}{\pi} \left(\frac{\alpha}{4\pi} \frac{1}{M_*^3} \right)^2 & \longrightarrow & M_* \approx 10 \,\text{GeV} \end{cases}$$

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Numbers suggest that to get signal in explicit model, need either many states in loop or have resonant s-channel production

Direct Detection From y-Rays?

In view of large γ -ray signal & impressive sensitivity of direct detection experiments, should ask if constraints on DM can arise from latter searches if DM-quark & -gluon interactions loop suppressed

Loop-induced spin-independent direct detection cross sections scale as :

 $\sigma_{N}^{\rm SI} \propto \begin{cases} \frac{m_{\rm red}^{2}}{M_{*}^{4}} & \text{scalar DM} \\ \frac{m_{\rm red}^{2} m_{\chi}^{2}}{M_{*}^{6}} & \text{fermionic DM} \end{cases}$

Formulas imply that only if DM is fermionic (γ-ray signal is v²-suppressed) direct & indirect bounds may be competitive

Rayleigh DM

Interesting operator that gives rise to direct detection signals is hence (M = Majorana fermion)

$$\mathcal{O}_M = \mathcal{C}_M \left(\bar{M} M \right) \left(F_{\mu\nu} \right)^2$$



Photons interact coherently with entire nucleus (similar to Rayleigh scattering)

Amplitude thus proportional to Z^2 & cross section proportional to Z^4

RG Evolution

But if DM-photon-photon interaction induced at M*, QED radiation will lead to DM-quark coupling:

$$\mathcal{O}_q = \mathcal{C}_q m_q \left(\bar{M} M \right) \left(\bar{q} q \right) \quad \mathcal{C}_q(m_N) \simeq -\frac{3e_q^2 \alpha}{\pi} \ln \left(\frac{M_*^2}{m_N^2} \right) \mathcal{C}_M(M_*)$$



At scale m_N this leads to standard spin-independent interactions

Amplitude proportional to target nucleus mass, resulting in cross section proportional to A^2

[Frandsen et al., 1207.3971]



 $\mathcal{C}_q(m_N) \simeq -\frac{3e_q^2 \alpha}{\pi} \ln\left(\frac{M_*^2}{m_N^2}\right) \mathcal{C}_M(M_*)$





 $\mathcal{C}_q(m_N) \simeq -\frac{3e_q^2 \alpha}{\pi} \ln\left(\frac{M_*^2}{m_N^2}\right) \mathcal{C}_M(M_*)$ Two effects interfere destructively





 $\mathcal{C}_q(m_N) \simeq -\frac{3e_q^2 \alpha}{\pi} \ln\left(\frac{M_*^2}{m_N^2}\right) \mathcal{C}_M(M_*)$









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Sensitivity Of XENON



If Majorana DM operator is responsible for γ-ray excess, claim can be tested in future with XENON1T