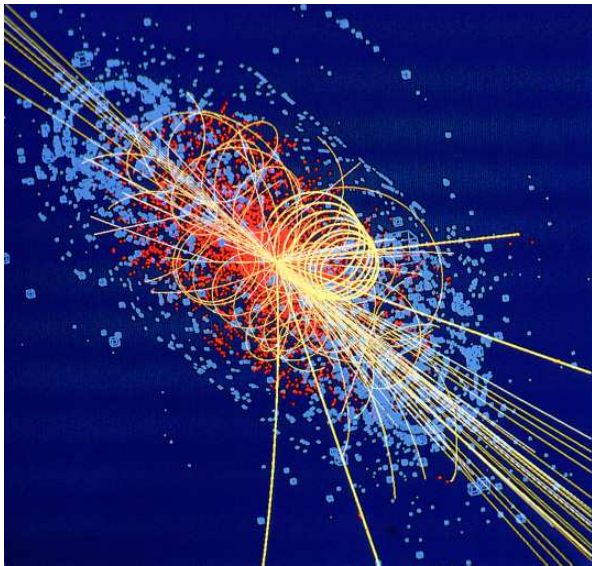


Matching weak boson scattering processes at NLO in QCD with parton shower programs



Barbara Jäger

**Johannes Gutenberg
University Mainz**

**LHC – the first part of the journey
KITP, July 2013**

work done in collaboration with Giulia Zanderighi

[arXiv: 1108.0864, 1301.1695]



- ❖ setting the stage: weak boson scattering
- ❖ developing precision tools:
 - next-to-leading order QCD corrections
 - matching with parton shower
 - phenomenological analyses
- ❖ conclusions & outlook

vector boson fusion (VBF)

Standard Model:

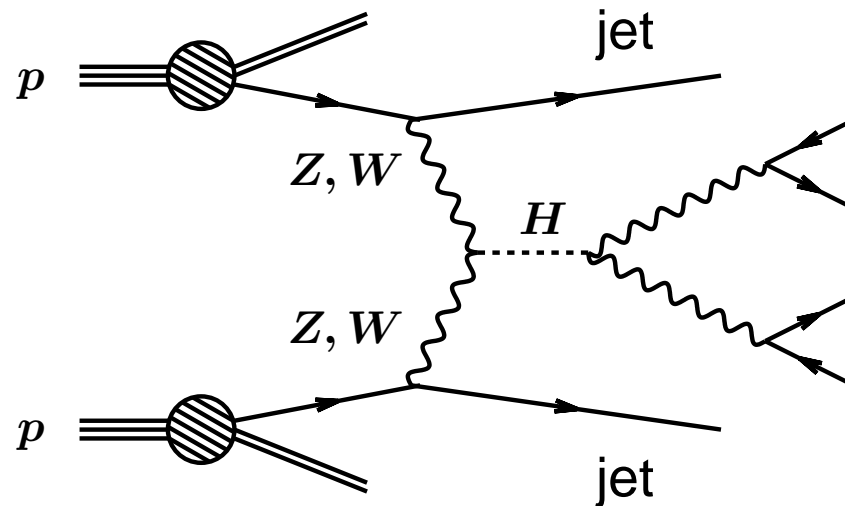
- ❖ $qq \rightarrow qqH$:
prominent production mode
for the Higgs boson
over a wide mass range
- ❖ sensitive to Higgs couplings
and CP properties

✓ the big advantage: backgrounds can be controlled!

beyond the Standard Model:

- $qq \rightarrow qqVV$:
sensitive to the mechanism of
electroweak symmetry breaking
- ↕
- strongly interacting weak sector,
new resonances, ... ?

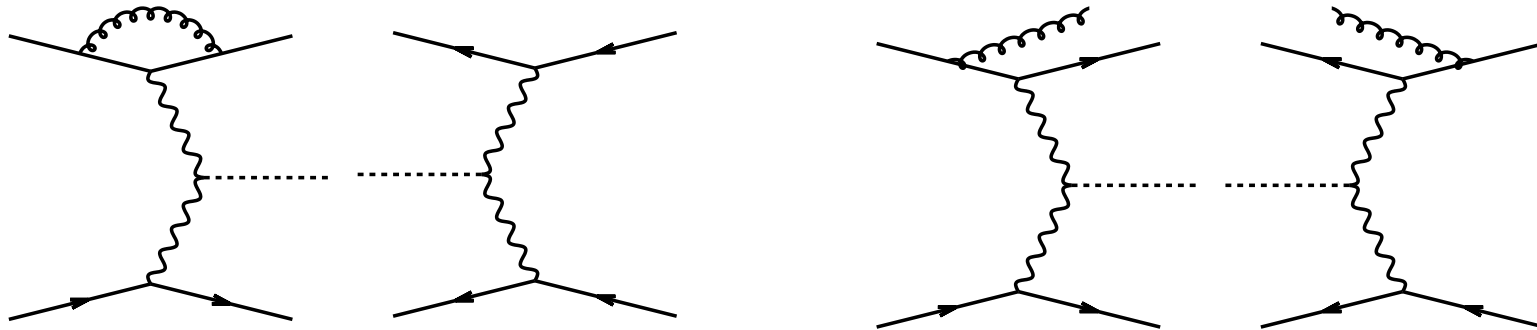
VBF event topology



suppressed color exchange between quark lines gives rise to

- ❖ little jet activity in central rapidity region
- ❖ scattered quarks \rightarrow two forward tagging jets (energetic; large rapidity)
- ❖ Higgs decay products typically between tagging jets

Higgs production in VBF @ NLO QCD



NLO QCD:

inclusive cross section:

Han, Valencia, Willenbrock (1992)

distributions:

Figy, Oleari, Zeppenfeld (2003)

Berger, Campbell (2004)



**NLO QCD corrections
moderate**

and well under control
(order 10% or less)

publicly available
parton-level Monte Carlos:

VBFNLO

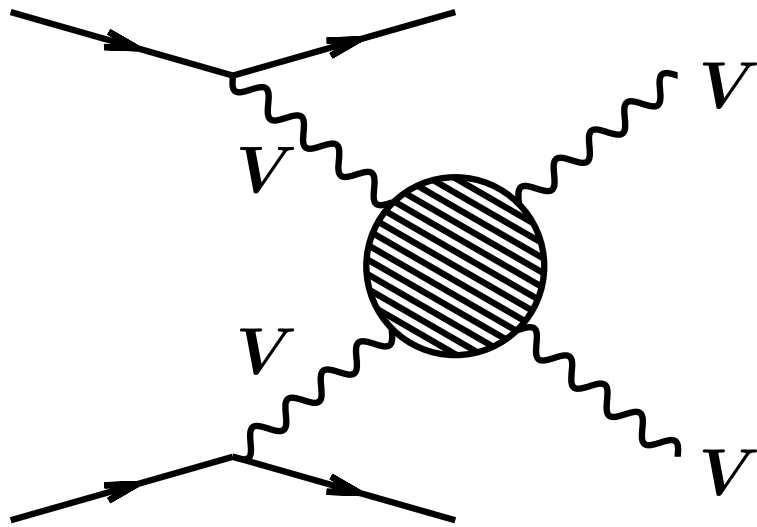
MCFM



Higgs production in VBF: more corrections

- ❖ **NLO EW corrections** to cross sections and distributions: modify K factors and distort distributions by up to 10%
[Ciccolini, Denner, Dittmaier, Mück (2007-10)]
- ❖ **SUSY QCD & EW corrections**: typically $\lesssim 1\%$
[Hollik, Plehn, Rauch, Rzehak (2008) & Figy, Palmer, Weiglein (2010)]
- ❖ sub-set of virtual **NNLO-QCD corrections** (one-loop squared): numerically irrelevant in all considered regions
[Harlander, Vollinga, Weber (2007)]
- ❖ sub-set of **NNLO-QCD corrections** (structure function approach): further reduce scale uncertainties of total cross sections
[Bolzoni, Maltoni, Moch, Zaro (2010-11)]
- ❖ **interference** with Hjj production via gluon fusion: negligible
[Andersen et al.; Bredenstein, Hagiwara, B.J. (2006-08)]

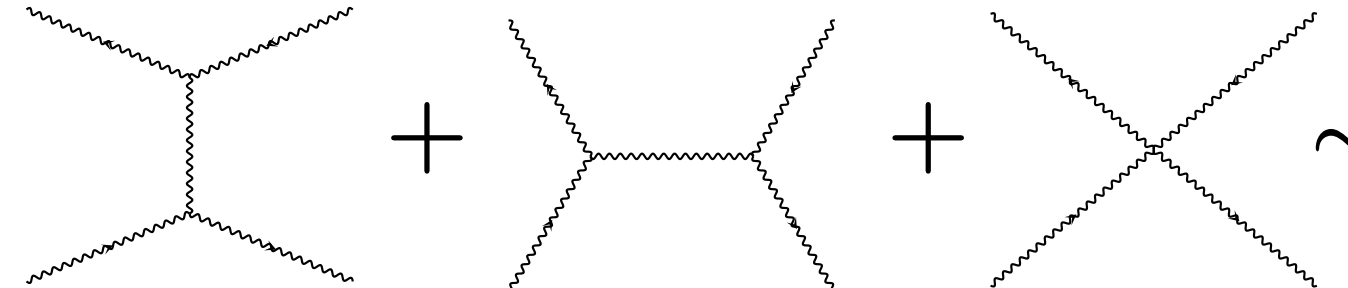
vector boson scattering: $VV \rightarrow VV$



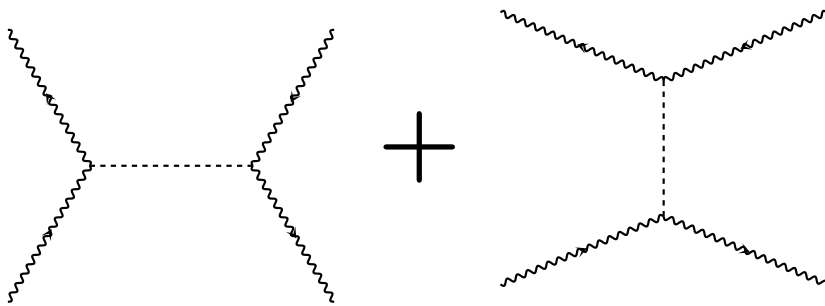
vector-boson scattering processes
are extremely **sensitive to**
new interactions in the
gauge boson sector

vector boson scattering & unitarity

$$W_L^+ W_L^- \rightarrow W_L^+ W_L^- \quad \text{with } \epsilon_L^\mu \sim \frac{\sqrt{s}}{M_W}$$

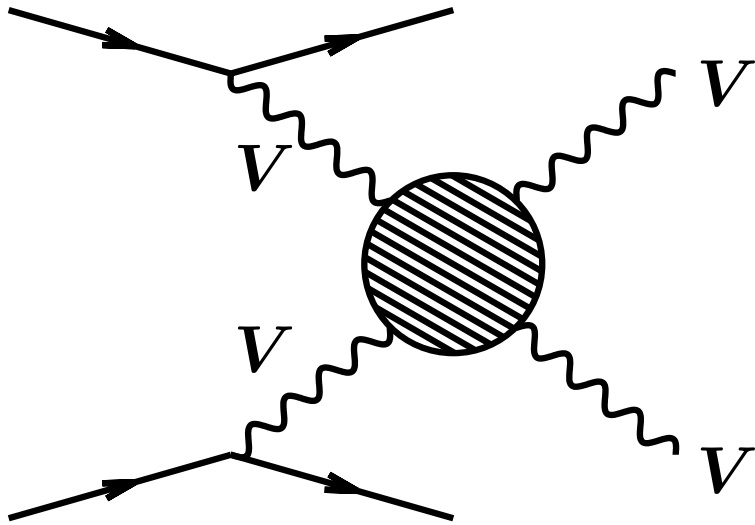
$$\mathcal{M} = \text{[diagram 1]} + \text{[diagram 2]} + \text{[diagram 3]} \sim \frac{s}{M_W^2}$$


growth violates unitarity \rightarrow need:

$$\text{[diagram 4]} + \text{[diagram 5]}$$


Higgs with $M_H \lesssim 1$ TeV
or new physics at TeV scale

vector boson scattering: $VV \rightarrow VV$

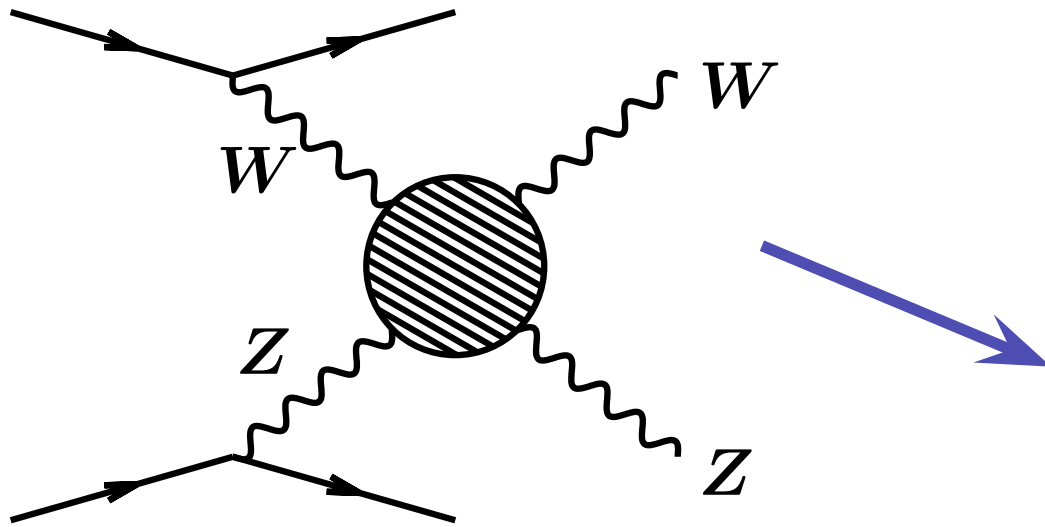


vector-boson scattering processes
are extremely **sensitive to
new interactions in the
gauge boson sector**



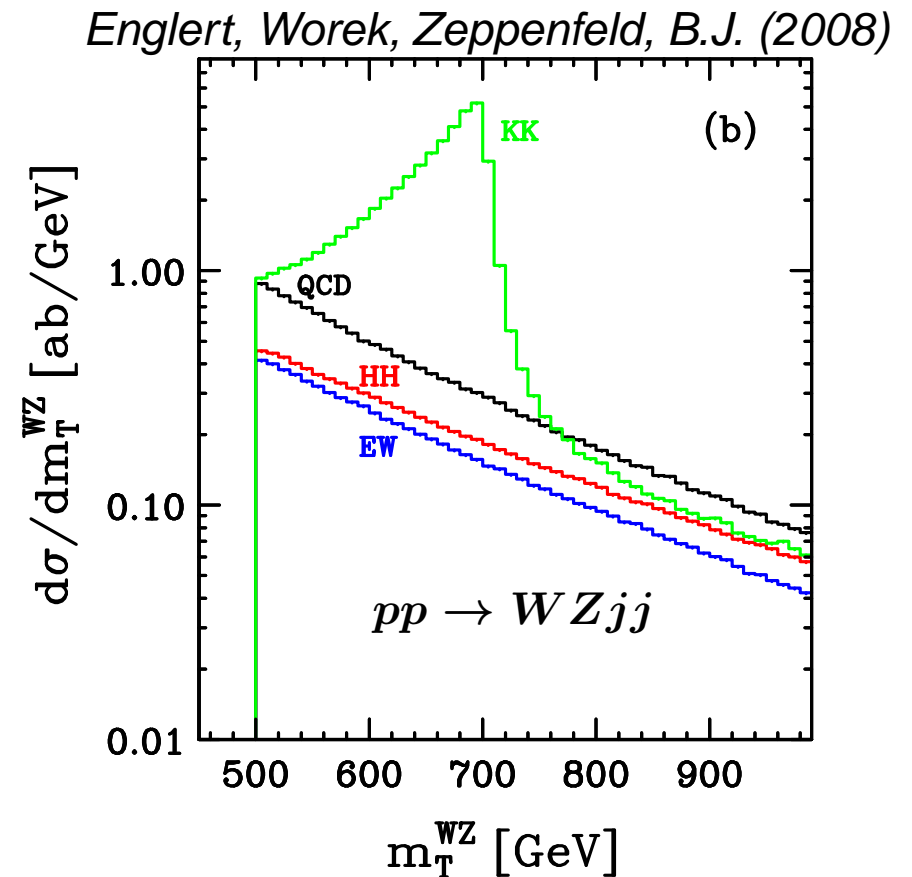
can we spot signatures of
non-standard scenarios for
electroweak symmetry breaking?

vector boson scattering: $VV \rightarrow VV$

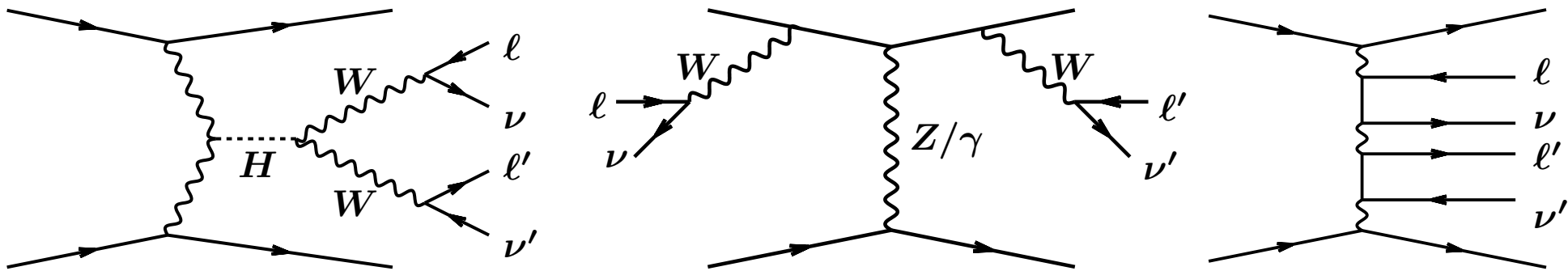


example:

new resonant states are visible as enhancement in characteristic distributions
[here: Kaluza-Klein resonances]



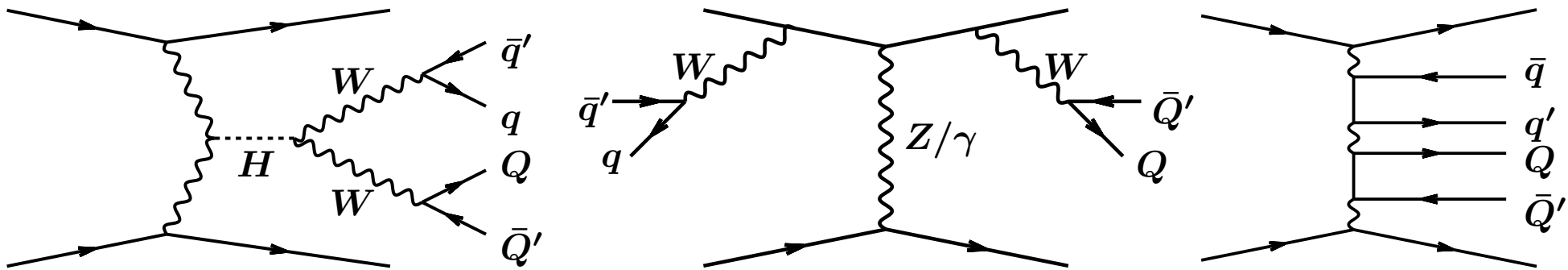
$pp \rightarrow VVjj$: vector boson scattering in the Standard Model



experiment: don't observe $VVjj$ final state, but
hadronic or leptonic decay products

4leptons + jj
low statistics
clean signature

$pp \rightarrow VVjj$: vector boson scattering in the Standard Model



experiment: don't observe $VVjj$ final state, but
hadronic or leptonic decay products

4jets + jj
high statistics
large backgrounds

4leptons + jj
low statistics
clean signature

need **stable, fast & flexible Monte Carlo program** allowing for

- ❖ computation of various jet and lepton observables for

VBF production of

$$W^+W^-jj, ZZjj, W^\pm Zjj, \text{ and } W^\pm W^\pm jj$$

at NLO-QCD accuracy

(leptonic decay correlations fully taken into account)

- ❖ straightforward implementation of experimental selection cuts

C. Oleari, D. Zeppenfeld, B. J. (2006)

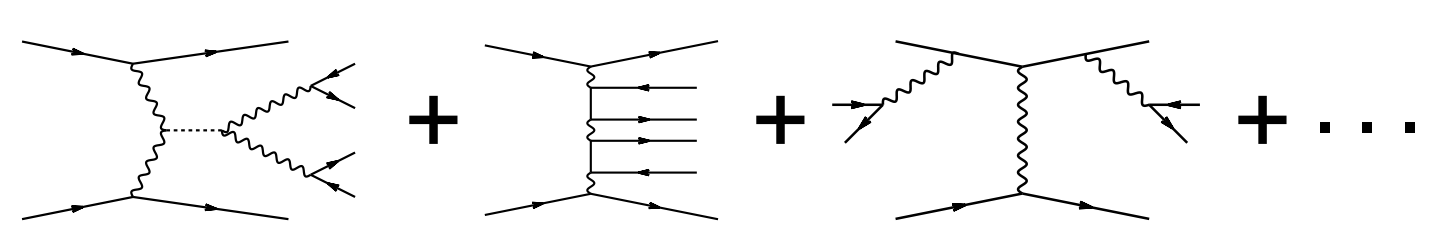
G. Bozzi, C. Oleari, D. Zeppenfeld, B. J. (2007)

C. Oleari, D. Zeppenfeld, B. J. (2009)

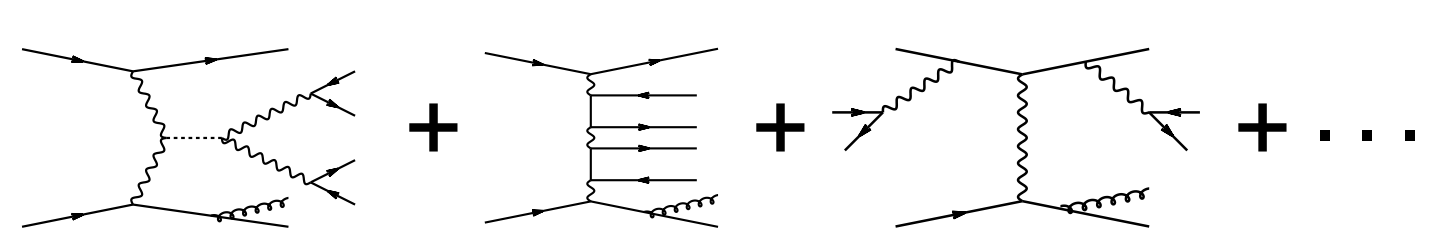
[c. f. also: A. Denner, L. Hosekova, S. Kallweit (2012)]

ingredients of the calculation

need to compute numerical value for ...

$$|\mathcal{M}_B|^2 = \left| \text{diagram 1} + \text{diagram 2} + \text{diagram 3} + \dots \right|^2$$
The equation shows the squared magnitude of the Born amplitude, $|\mathcal{M}_B|^2$. It is represented as the square of a sum of Feynman diagrams. The first diagram is a tree-level process with two incoming fermions and two outgoing fermions, connected by a wavy line. The second diagram is a tree-level process with two incoming fermions and two outgoing fermions, connected by a vertical wavy line. The third diagram is a tree-level process with two incoming fermions and two outgoing fermions, connected by a wavy line. The sum is followed by an ellipsis and a vertical bar with a superscript 2, indicating the square of the sum.

... Born amplitude squared in 4 dim

$$|\mathcal{M}_R|^2 = \left| \text{diagram 1} + \text{diagram 2} + \text{diagram 3} + \dots \right|^2$$
The equation shows the squared magnitude of the real-emission amplitude, $|\mathcal{M}_R|^2$. It is represented as the square of a sum of Feynman diagrams. The first diagram is a tree-level process with two incoming fermions and two outgoing fermions, connected by a wavy line. The second diagram is a tree-level process with two incoming fermions and two outgoing fermions, connected by a vertical wavy line. The third diagram is a tree-level process with two incoming fermions and two outgoing fermions, connected by a wavy line. The sum is followed by an ellipsis and a vertical bar with a superscript 2, indicating the square of the sum.

... real-emission amplitude squared in 4 dim and counter-terms for infrared-divergent configurations

almost 3000 diagrams → essential: organize calculation **economically!**

$$\mathcal{M}_V = \text{[diagram 1]} + \text{[diagram 2]} + \text{[diagram 3]} + \dots$$

$$= \mathcal{M}_B F(Q) \left[-\frac{2}{\epsilon^2} - \frac{3}{\epsilon} \right] + \tilde{\mathcal{M}}_V^{finite}$$

determined numerically

[c. f. Denner, Dittmaier (2002,2005)]

combination of real emission, virtuals,
and subtraction terms:
poles canceled analytically → **finite** results

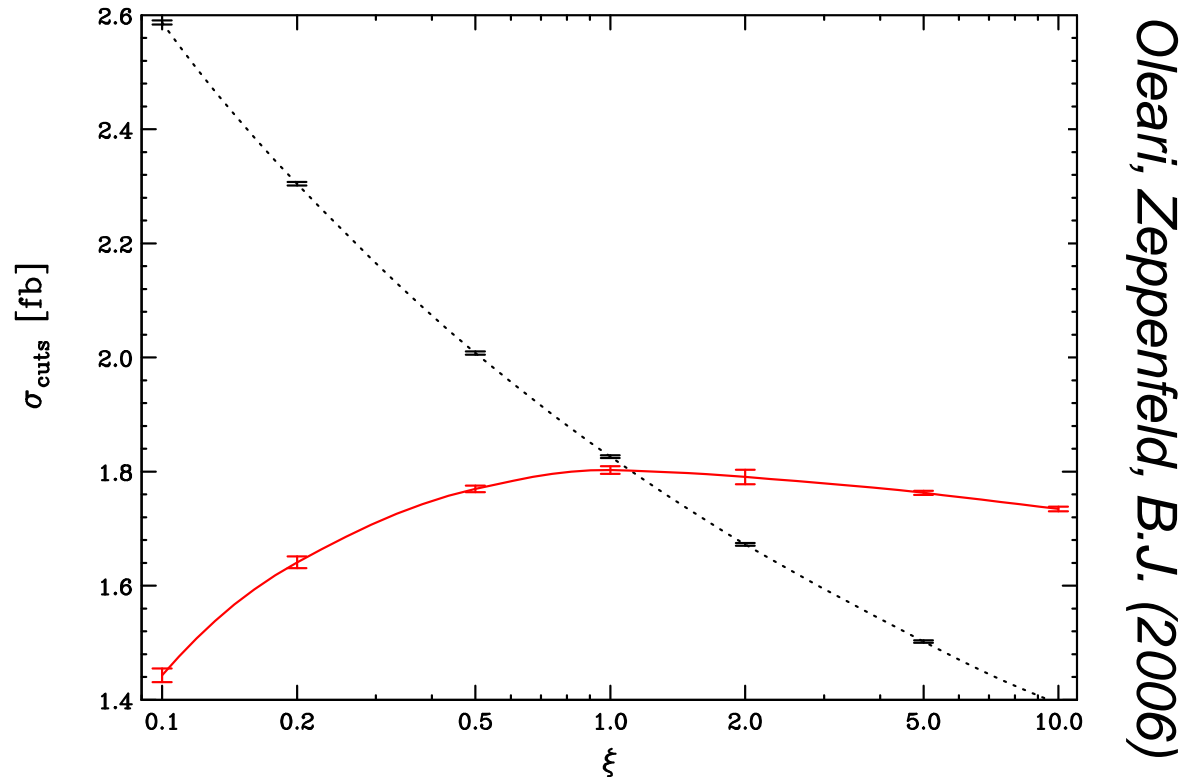
phase-space integration can be performed numerically (Vegas)



... put everything into dedicated
Monte-Carlo program VBFNLO ...

$pp \rightarrow W^+W^-jj$: theoretical uncertainty

estimate theoretical uncertainty by studying dependence of cross section on unphysical scale parameter $\mu = \xi M_W$

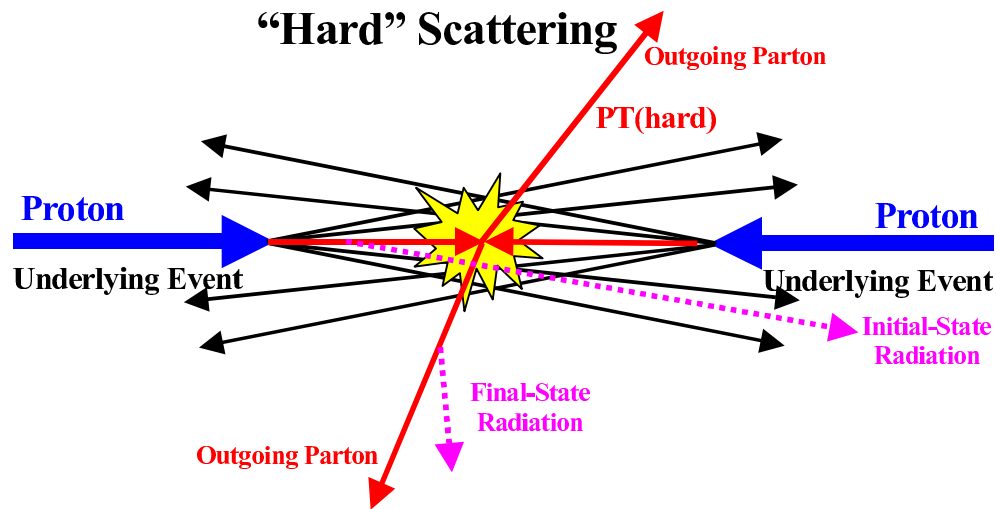


LO: no control on scale

NLO QCD: scale dependence strongly reduced



more realistic simulation



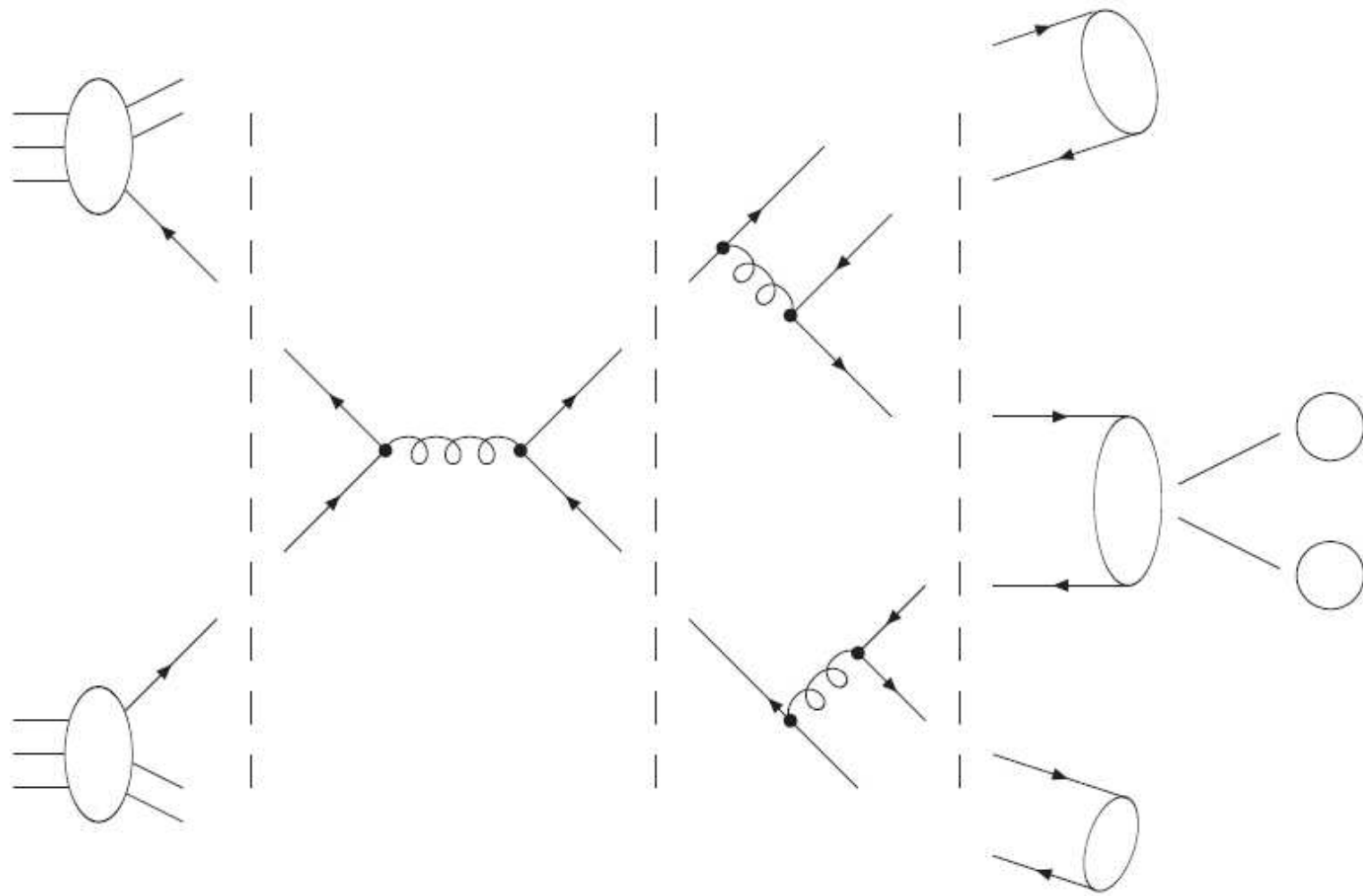
for realistic description of scattering processes at hadron colliders:

- ❖ combine matrix elements for hard scattering with programs for simulation of underlying event, parton shower, and hadronization

(PYTHIA, HERWIG, SHERPA, ...)



stages of a hadronic collision



hard partonic
scattering

$$\mu \sim Q \gg \Lambda_{\text{QCD}}$$

parton
shower

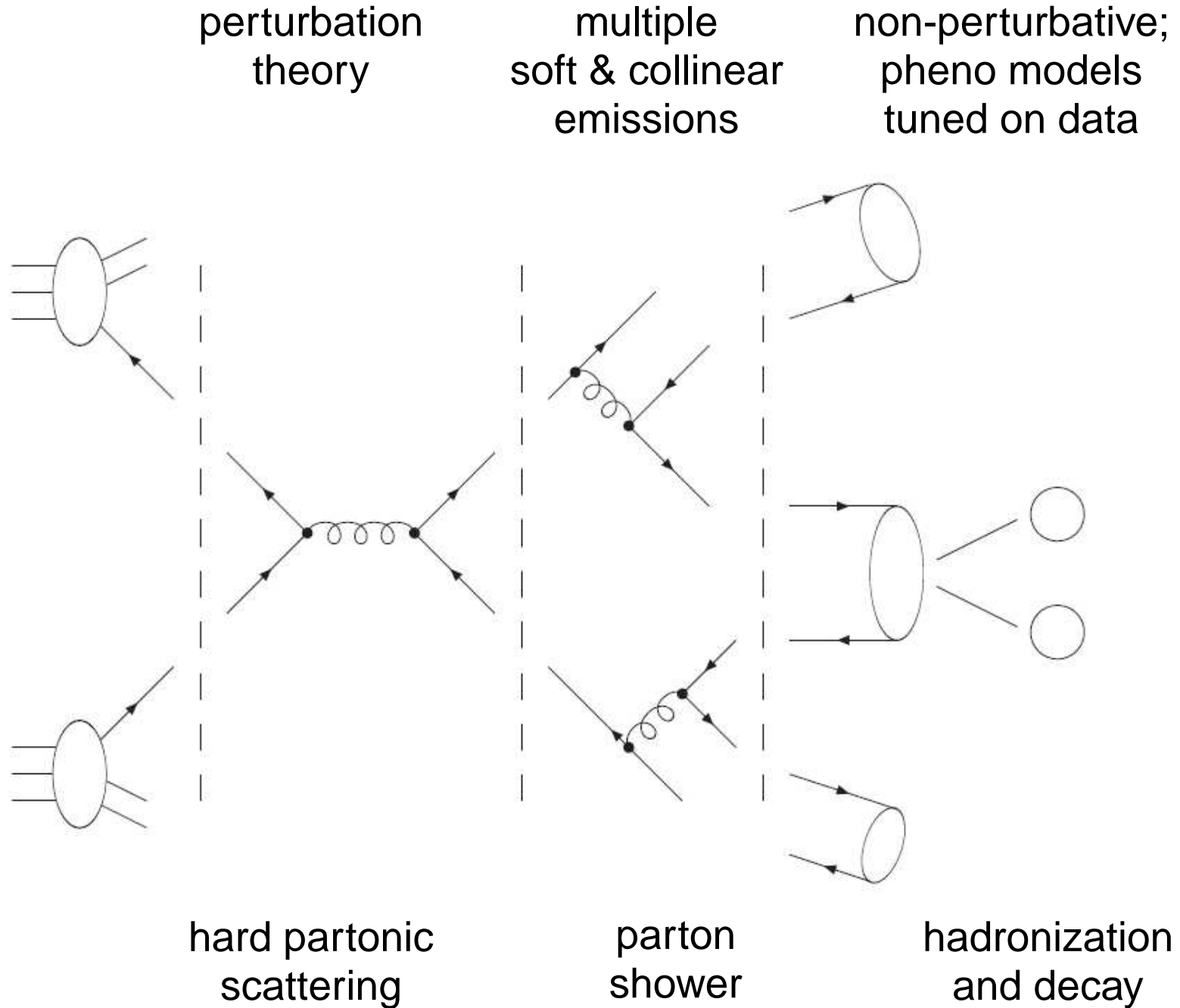
$$Q > \mu > \Lambda_{\text{QCD}}$$

hadronization
and decay

$$\mu \sim \Lambda_{\text{QCD}}$$

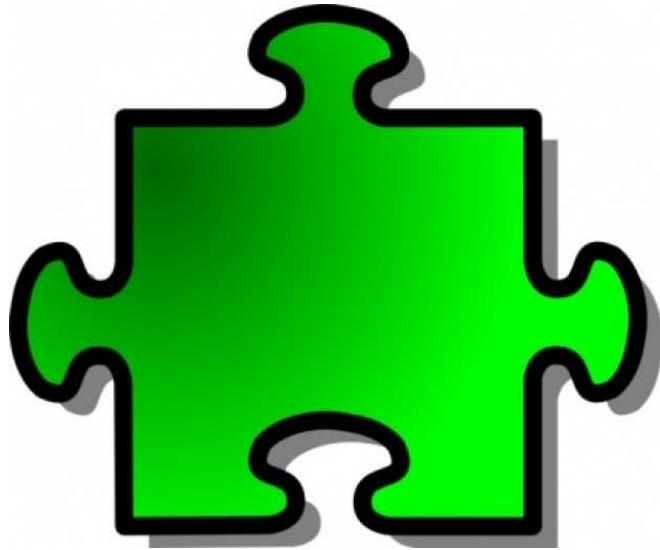


stages of a hadronic collision





realistic & precise predictions



exploit merits of flexible
Monte Carlo tools



retain NLO accuracy
for hard scattering





NLO-QCD vs. Shower Monte Carlo

NLO QCD:

- ✓ accurate shapes at high p_T
- ✓ normalization accurate at NLO
- ✓ reduced scale dependence
- ✗ wrong shapes at low p_T
- ✗ description only at parton level

LO Shower Monte Carlo:

- ✗ bad description at high p_T
- ✗ normalization accurate only at LO
- ✓ Sudakov suppression at low p_T
- ✓ events at hadron level

☞ merge the two approaches, keeping the advantages of both:

- MC@NLO [*Frixione, Webber*]
- POWHEG [*Nason et al.*]

POsitive Weight Hardest Emission Generator

general prescription for **matching** parton-level **NLO-QCD** calculations with **parton shower programs**

[Frixione, Nason, Oleari]

- ❖ generate partonic event with single emission at NLO-QCD
- ❖ all subsequent radiation must be softer than the first one
- ❖ event is written on a file in standard Les Houches format
 - can be processed by default parton shower program (HERWIG, PYTHIA, ...)

POsitive Weight Hardest Emission Generator

general prescription for **matching** parton-level **NLO-QCD** calculations with **parton shower programs**

[Frixione, Nason, Oleari]

- ❖ applicable to any p_T -ordered parton shower program
- ❖ no double counting of real-emission contributions
- ❖ produces events with positive weights
- ❖ tools for “do-it-yourself” implementation
publicly available (the POWHEG-BOX)

[Alioli, Nason, Oleari, Re]

reminder: differential **NLO cross section**

$$d\sigma_{\text{NLO}} = d\Phi_n \left\{ \begin{array}{l} \text{Born} \\ B(\Phi_n) + V(\Phi_n) + \left[R(\Phi_n, \Phi_r) - C(\Phi_n, \Phi_r) \right] d\Phi_r \end{array} \right\}$$

finite virtuals:

$$V_b(\Phi_n) + \int d\phi_r C(\Phi_n, \Phi_r)$$

real emission and counter-terms

radiation phase space:

$$d\Phi_r = dt dz d\phi$$

leading order **shower Monte Carlo** cross section

Born

first emission
(governed by
splitting function P)

$$d\sigma_{\text{LO-SMC}} = d\Phi_n B(\Phi_n) \left\{ \Delta_{t_0} + \Delta_t \frac{\alpha_s}{2\pi} P(z) \frac{1}{t} d\Phi_r \right\}$$

Sudakov factor:

$$\Delta_t = \exp \left[- \int d\Phi'_r \frac{\alpha_s}{2\pi} P(z') \frac{1}{t'} \theta(t' - t) \right]$$

... probability for no emission at scale $t' > t$

$$\bar{B} = \left\{ B(\Phi_n) + V(\Phi_n) + \int d\Phi_r \left[R(\Phi_n, \Phi_r) - C(\Phi_n, \Phi_r) \right] \right\}$$

$$d\sigma_{\text{POWHEG}} = d\Phi_n \bar{B}(\Phi_n) \left\{ \Delta(\Phi_n, p_T^{\min}) + \Delta(\Phi_n, p_T) \frac{R(\Phi_n, \Phi_r)}{B(\Phi_n, \Phi_r)} d\Phi_r \right\}$$

POWHEG “Sudakov” factor:

$$\Delta(\Phi_n, p_T) = \exp \left[- \int d\Phi'_r \frac{R(\Phi_n, \Phi'_r)}{B(\Phi_n)} \theta(k_T(\Phi_n, \Phi'_r) - p_T) \right]$$

$$d\sigma_{\text{NLO}} = d\Phi_n \left\{ B(\Phi_n) + V(\Phi_n) + \left[R(\Phi_n, \Phi_r) - C(\Phi_n, \Phi_r) \right] d\Phi_r \right\}$$

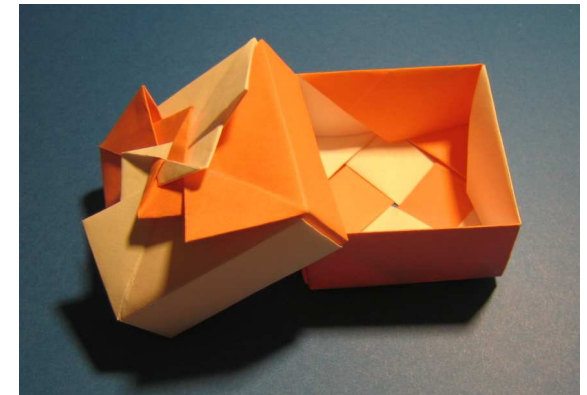
$$d\sigma_{\text{LO-SMC}} = d\Phi_n B(\Phi_n) \left\{ \Delta_{t_0} + \Delta_t \frac{\alpha_s}{2\pi} P(z) \frac{1}{t} d\Phi_r \right\}$$

$$d\sigma_{\text{POWHEG}} = d\Phi_n \bar{B}(\Phi_n) \left\{ \Delta(\Phi_n, p_T^{\min}) \right. \\ \left. + \Delta(\Phi_n, p_T) \frac{R(\Phi_n, \Phi_r)}{B(\Phi_n, \Phi_r)} d\Phi_r \right\}$$

- ✗ **user** has to supply process-specific quantities:
 - ❖ lists of flavor structures for Born and real emission processes
 - ❖ Born phase space
 - ❖ Born amplitudes squared, color-and spin-correlated amplitudes
 - ❖ real-emission amplitudes squared
 - ❖ finite part of the virtual corrections
 - ❖ Born color structure in the limit of a large number of colors
- ✓ all general, process-independent aspects of the matching are **provided by the POWHEG-BOX**

up-to-date info on the POWHEG-BOX
and code download:

<http://powhegbox.mib.infn.it/>



VBF processes in the POWHEG-BOX:

- ❖ Higgs production via VBF [*Oleari, Nason (2009)*]
- ❖ Z -boson production via VBF [*Schneider, Zanderighi, B.J. (2012)*]
- ❖ W^- and Z -boson production via VBF [*Schissler, Zeppenfeld (2013)*]
- ❖ W^+W^+ production via VBF [*Zanderighi, B.J. (2011)*]
- ❖ W^+W^- production via VBF [*Zanderighi, B.J. (2013)*]

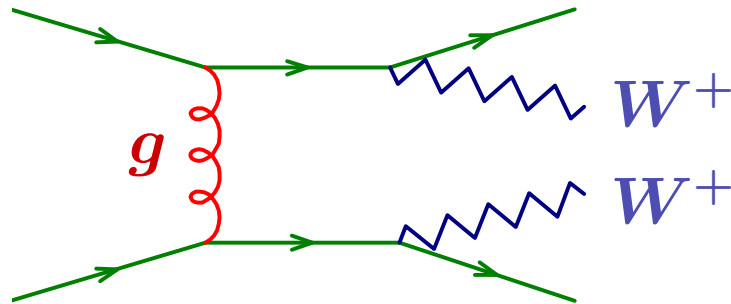
impact of different production modes



QCD-induced production

Melia, Melnikov, Rontsch, Zanderighi (2010);

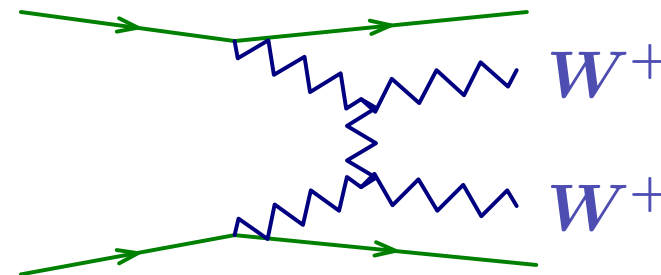
Melia, Nason, Rontsch, Zanderighi (2011)



EW production

Oleari, Zeppenfeld, B.J. (2009);

Zanderighi, B.J. (2011)



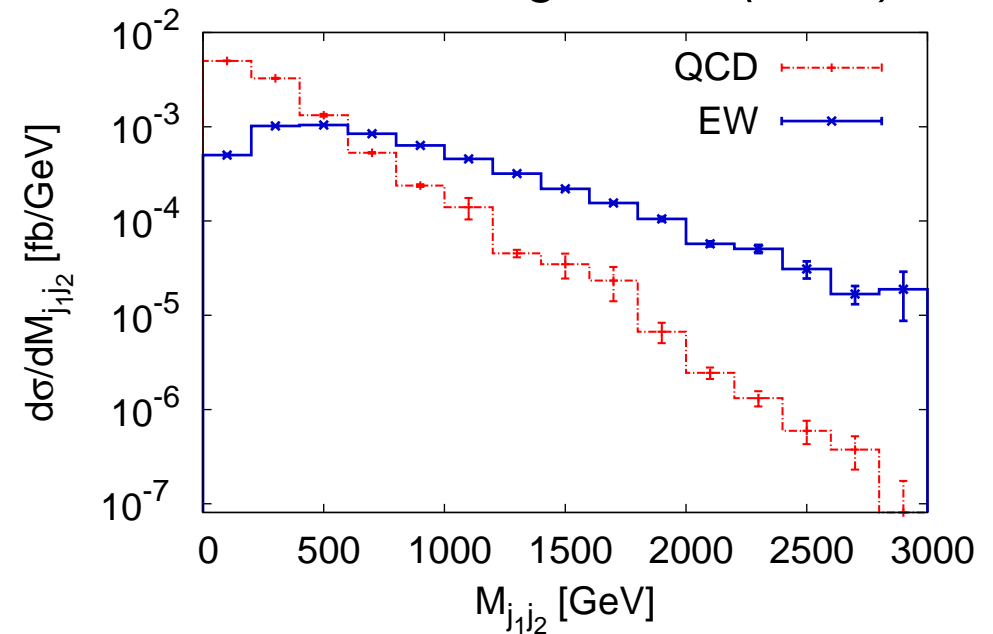
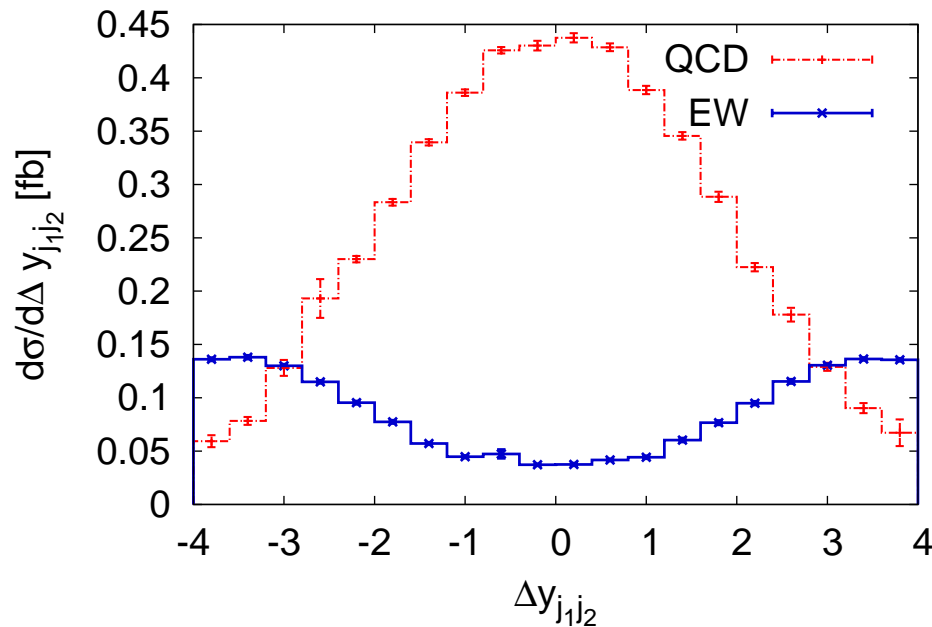
NLO-QCD results for $\sqrt{s} = 7$ TeV with basic jet cuts only ($p_T^{\text{tag}} > 20$ GeV):

$$\sigma_{\text{QCD}}^{\text{inc}} = 2.12 \text{ fb}$$

$$\sigma_{\text{EW}}^{\text{inc}} = 1.097 \text{ fb}$$

$pp \rightarrow W^+W^+jj$: QCD versus EW production

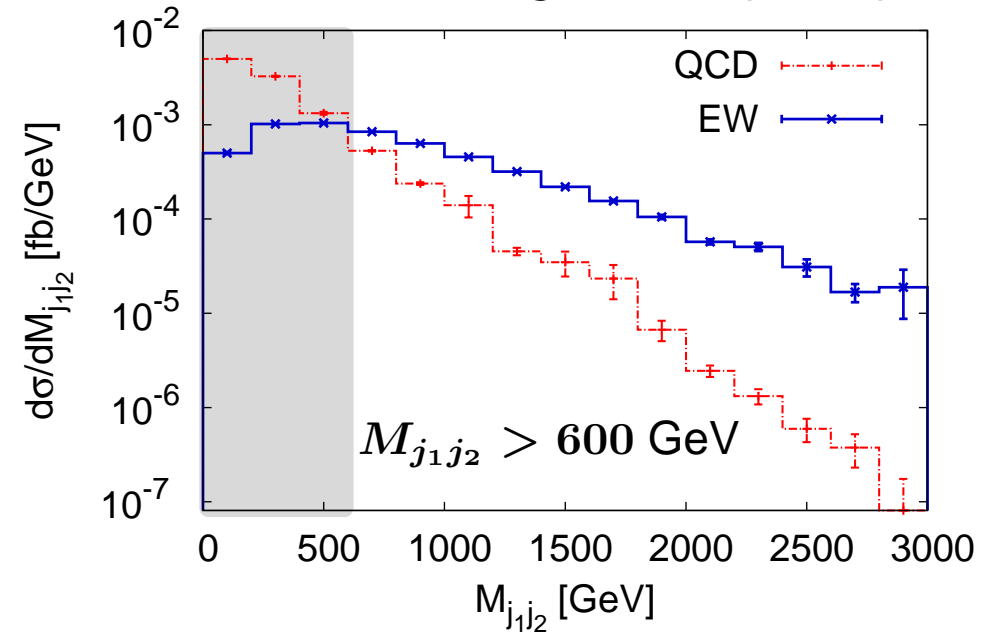
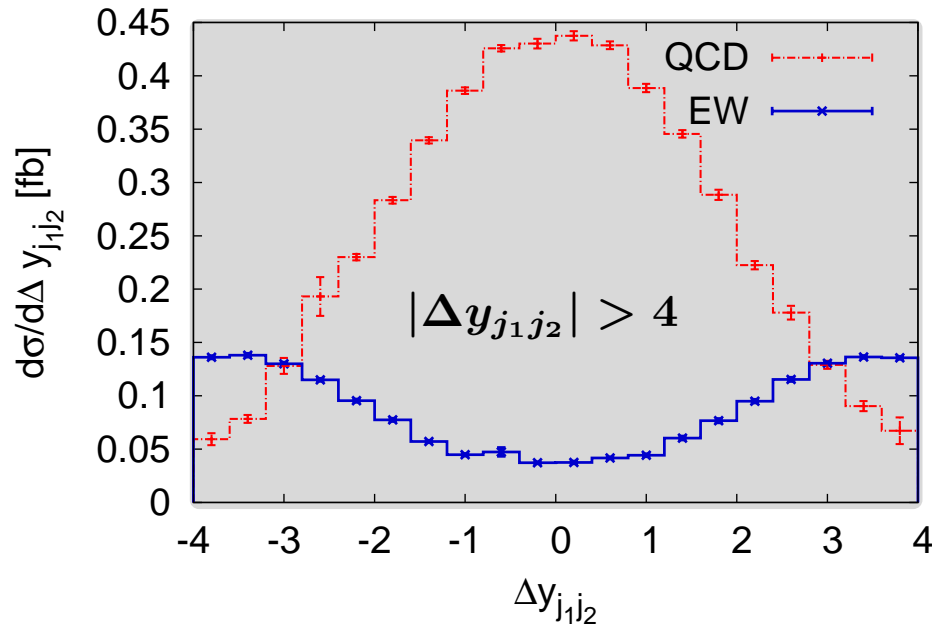
Zanderighi, B.J. (2011)



- $\sqrt{s} = 7$ TeV
- basic jet cuts only
- NLO-QCD accuracy

$pp \rightarrow W^+W^+jj$: QCD versus EW production

Zanderighi, B.J. (2011)

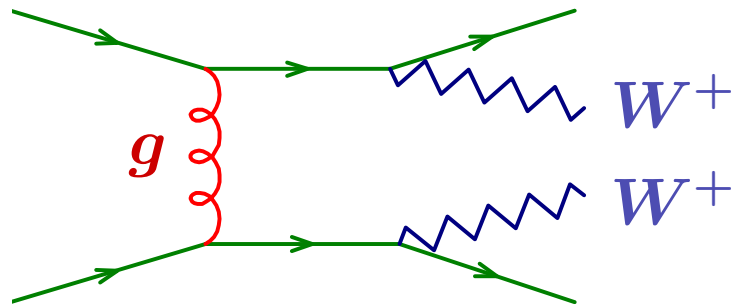


- $\sqrt{s} = 7 \text{ TeV}$
- basic jet cuts only
- NLO-QCD accuracy

$pp \rightarrow W^+W^+jj$ in the POWHEG-BOX

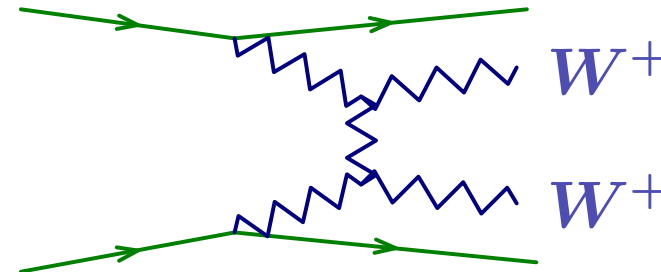
QCD-induced production

Melia, Melnikov, Rontsch, Zanderighi (2010);
Melia, Nason, Rontsch, Zanderighi (2011)



EW production

Oleari, Zeppenfeld, B.J. (2009);
Zanderighi, B.J. (2011)



NLO results for $\sqrt{s} = 7$ TeV with basic jet cuts only ($p_T^{\text{tag}} > 20$ GeV):

$$\sigma_{\text{QCD}}^{\text{inc}} = 2.12 \text{ fb}$$

$$\sigma_{\text{EW}}^{\text{inc}} = 1.097 \text{ fb}$$

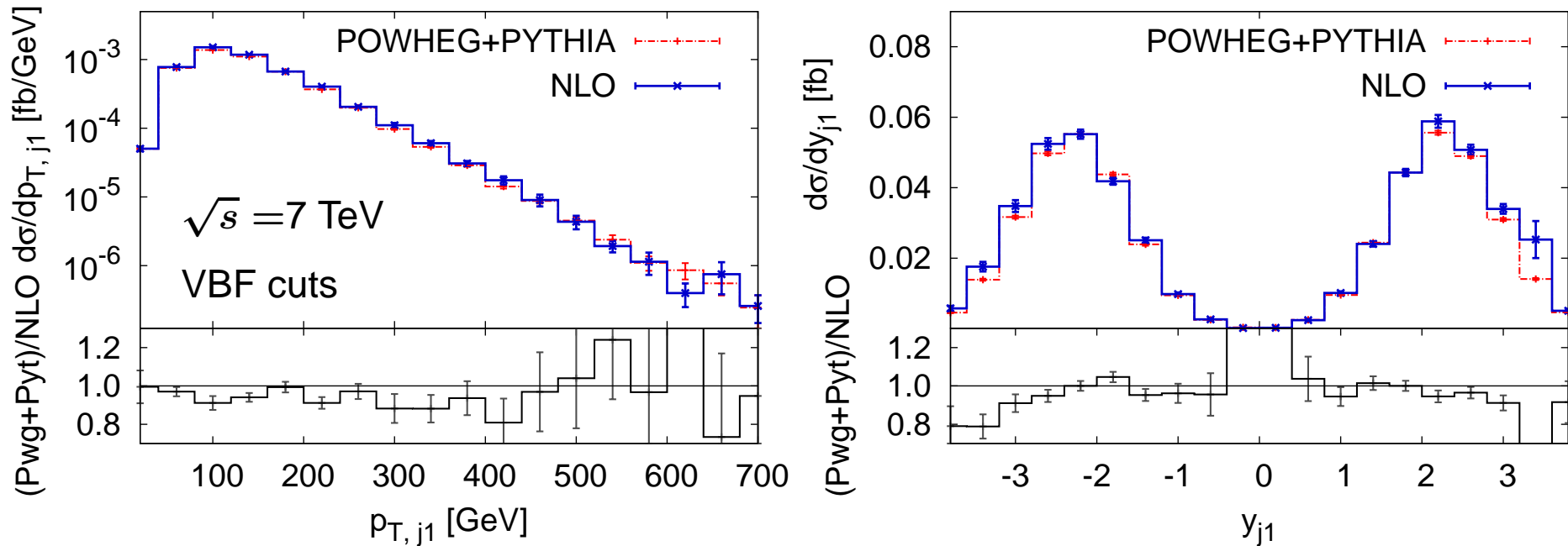
NLO results with VBF cuts:

$$\sigma_{\text{QCD}}^{\text{cuts}} = 0.0074 \text{ fb}$$

$$\sigma_{\text{EW}}^{\text{cuts}} = 0.201 \text{ fb}$$

$pp \rightarrow W^+W^+jj$ in the POWHEG-BOX

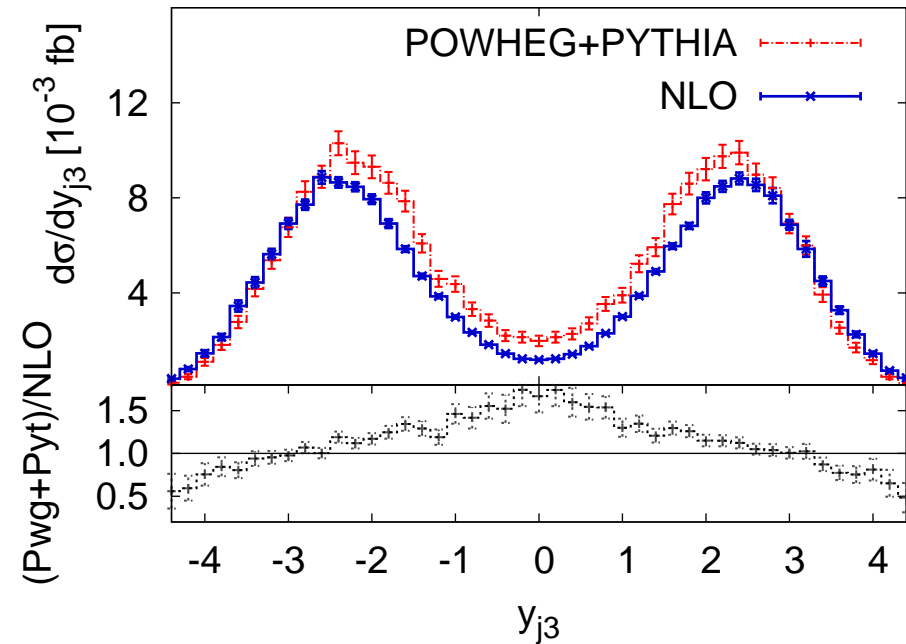
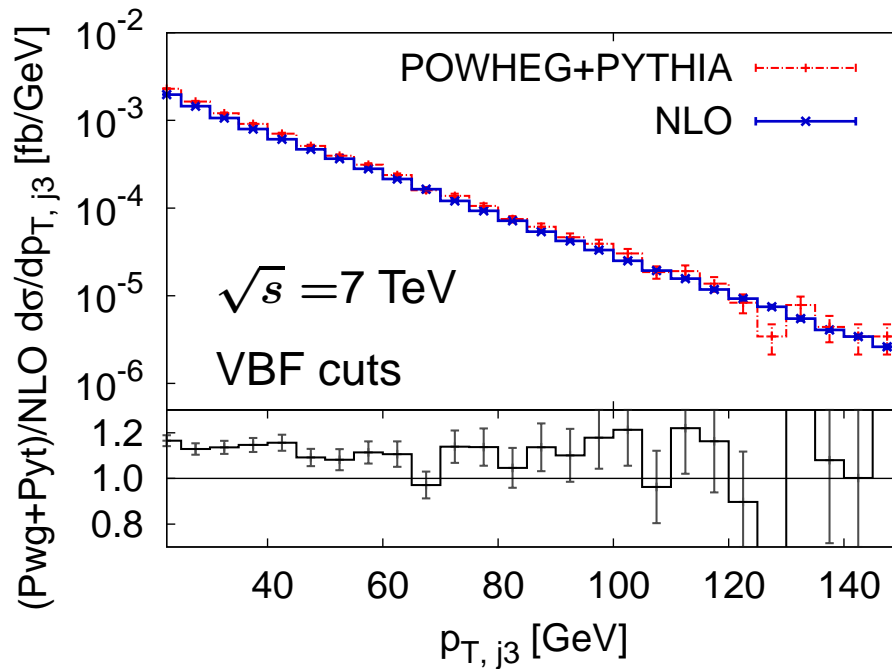
Zanderighi, B.J. (2011)



good agreement between parton-level NLO calculation and POWHEG matched with PYTHIA for many observables

$pp \rightarrow W^+W^+jj$ in the POWHEG-BOX

Zanderighi, B.J. (2011)



typical for VBF processes: little jet activity at central rapidities
→ exploited by central-jet veto techniques

note: parton-shower effects slightly enhance central jet activity

the next step: $pp \rightarrow W^+W^-jj$



full description of EW process $pp \rightarrow W^+W^-jj$,
including fully leptonic and semi-leptonic decays:

matching of hard matrix elements
with parton shower at NLO QCD

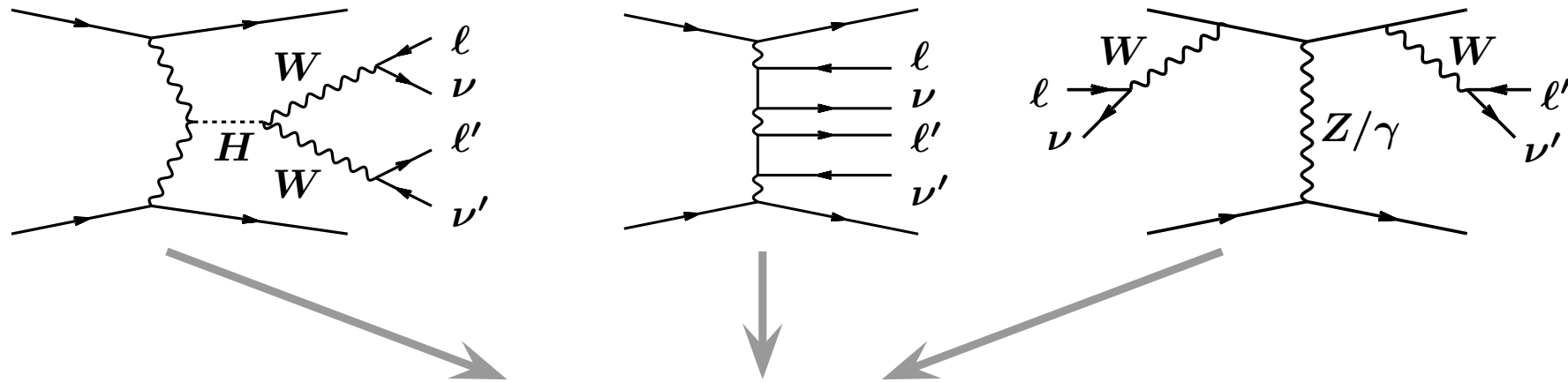
✓ provide implementation in versatile
public program package POWHEG-BOX

✗ challenge: complex multi-leg process with
involved resonance structure

→ conceptually and computationally demanding*

* requires about 12 hours \times 100 nodes on a HPC cluster

$pp \rightarrow W^+W^-jj$: technicalities



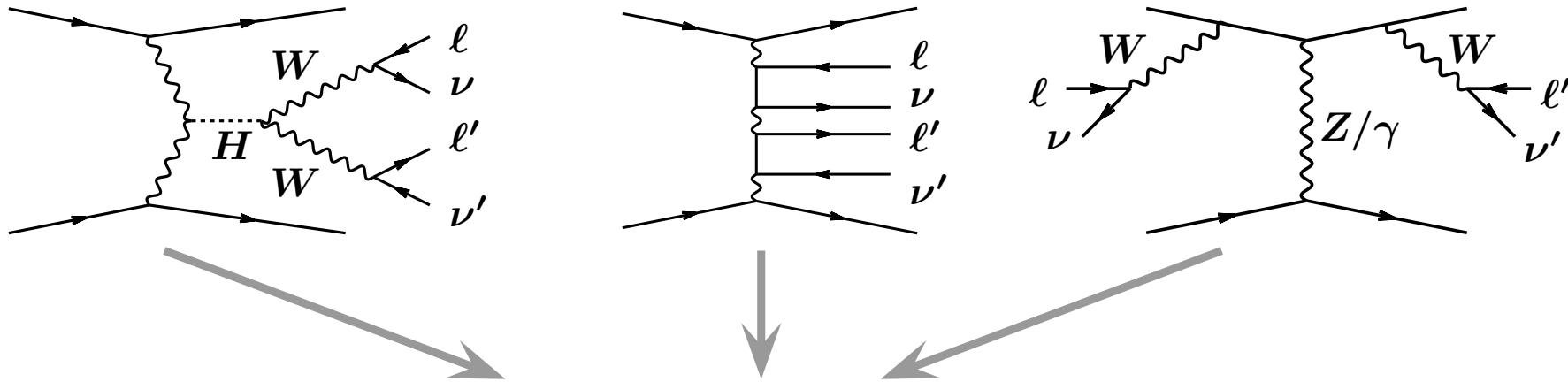
different topologies populate different regions in phase space

☞ split phase space into two regions for :

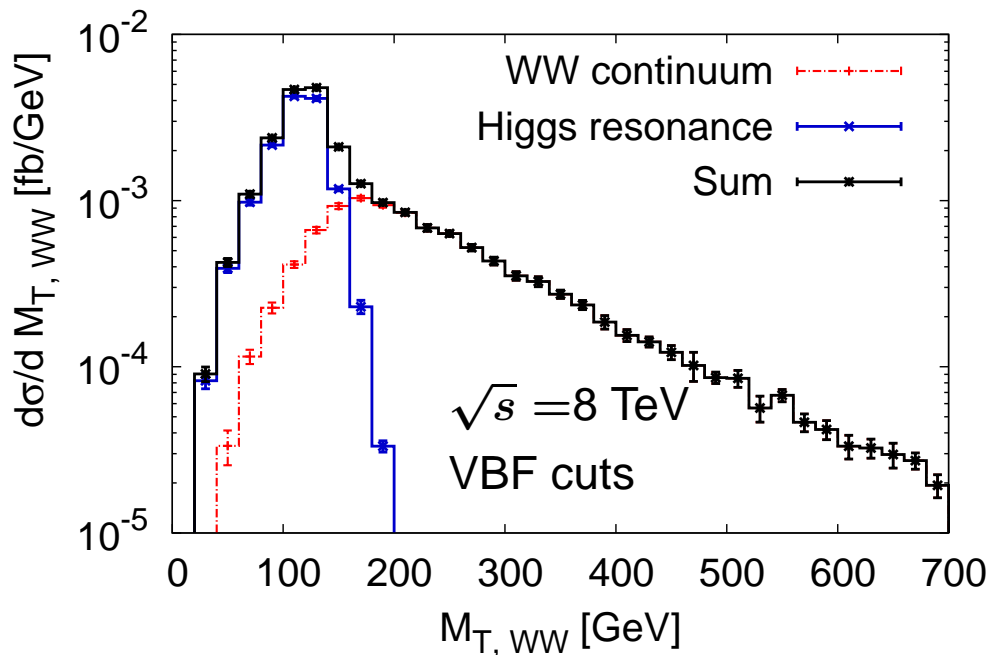
$$\blacklozenge M_H - \Delta M \leq M_{2\ell 2\nu} \leq M_H + \Delta M$$

☞ all other values of $M_{2\ell 2\nu}$

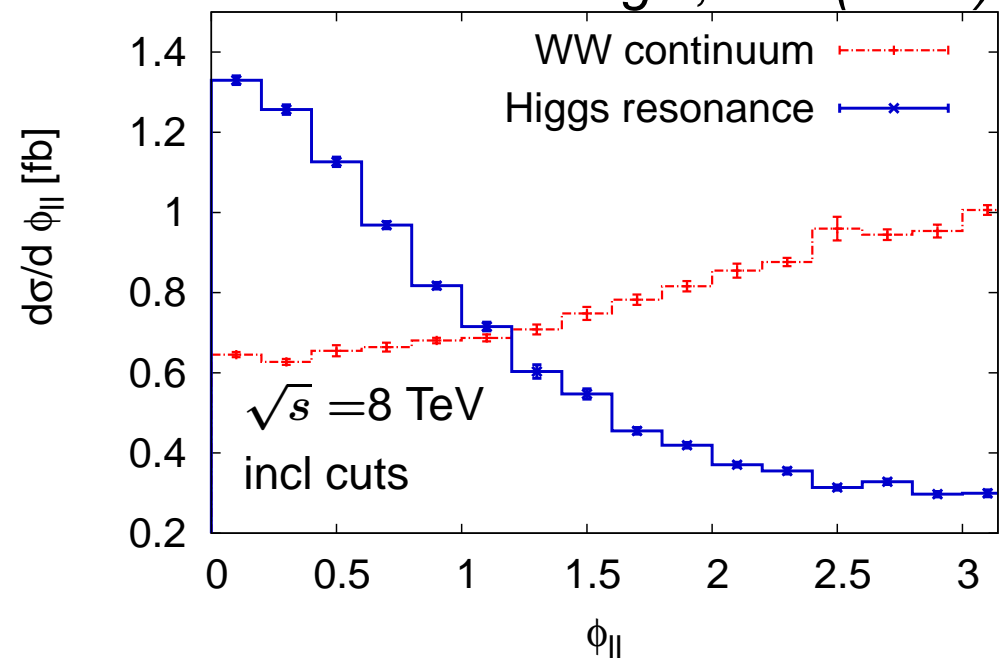
$pp \rightarrow W^+W^-jj$: technicalities



different topologies populate different regions in phase space:

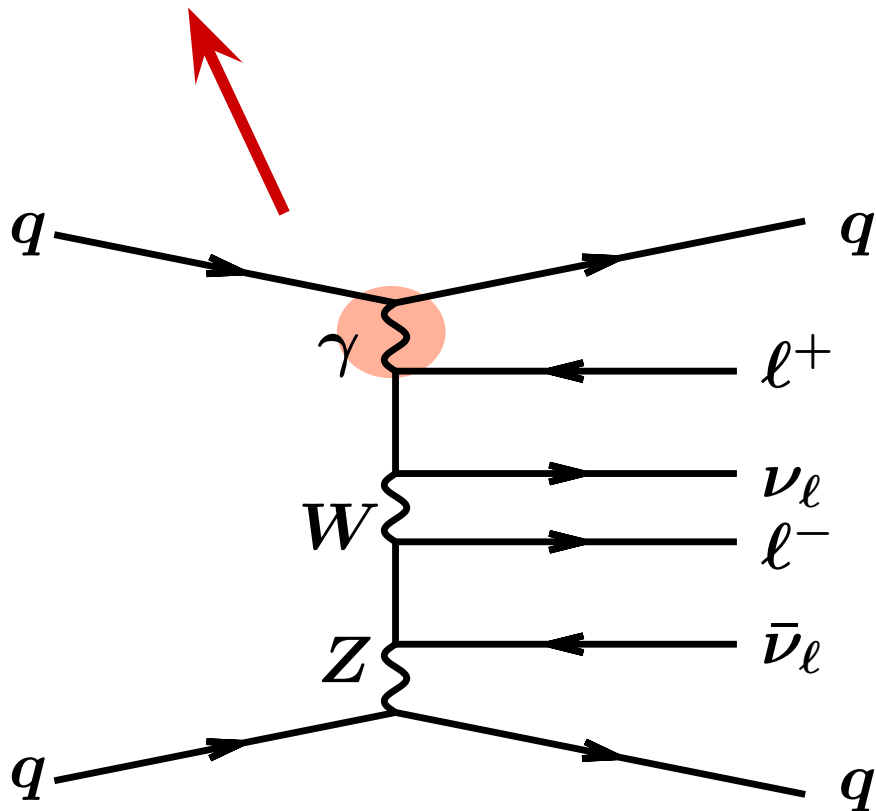


G. Zanderighi, B.J. (2013)



$pp \rightarrow W^+W^-jj$: technicalities

photon propagator $\sim 1/Q_\gamma^2$



need to handle

singularities for photons in t -channel

with $Q_\gamma^2 \rightarrow 0$

(numerically irrelevant for meaningful observables)

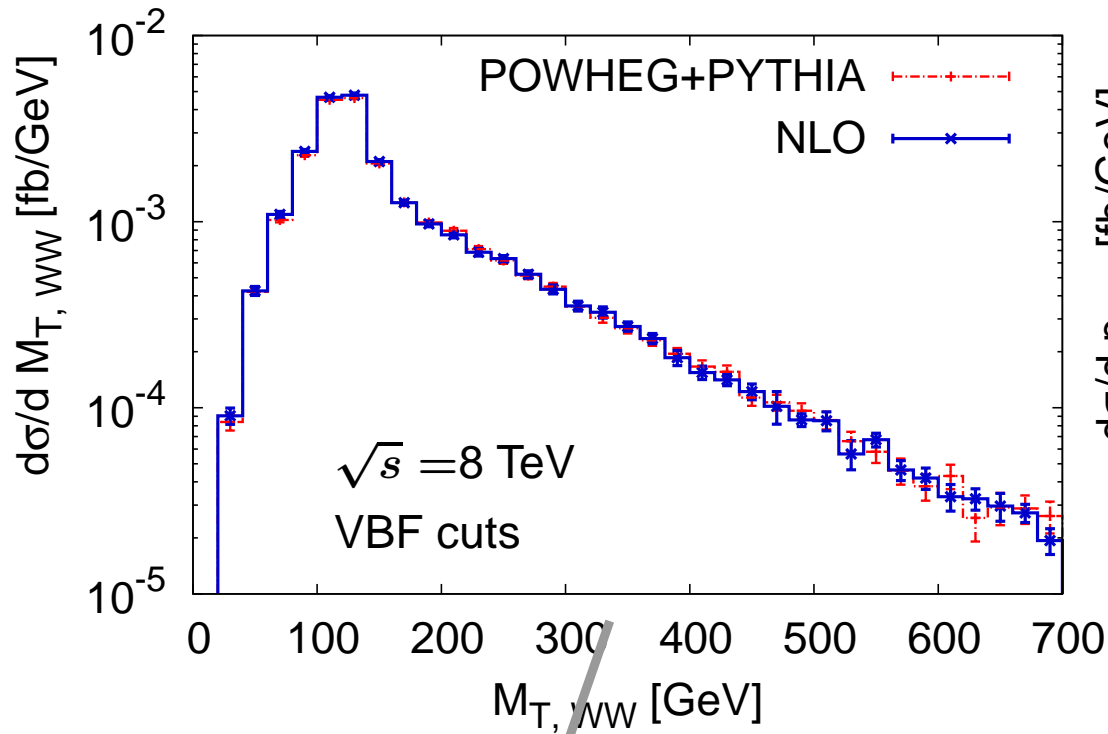
(1) **damping factor** to effectively suppress matrix elements

(2) **Born-suppression factor** to achieve efficient phase space integration

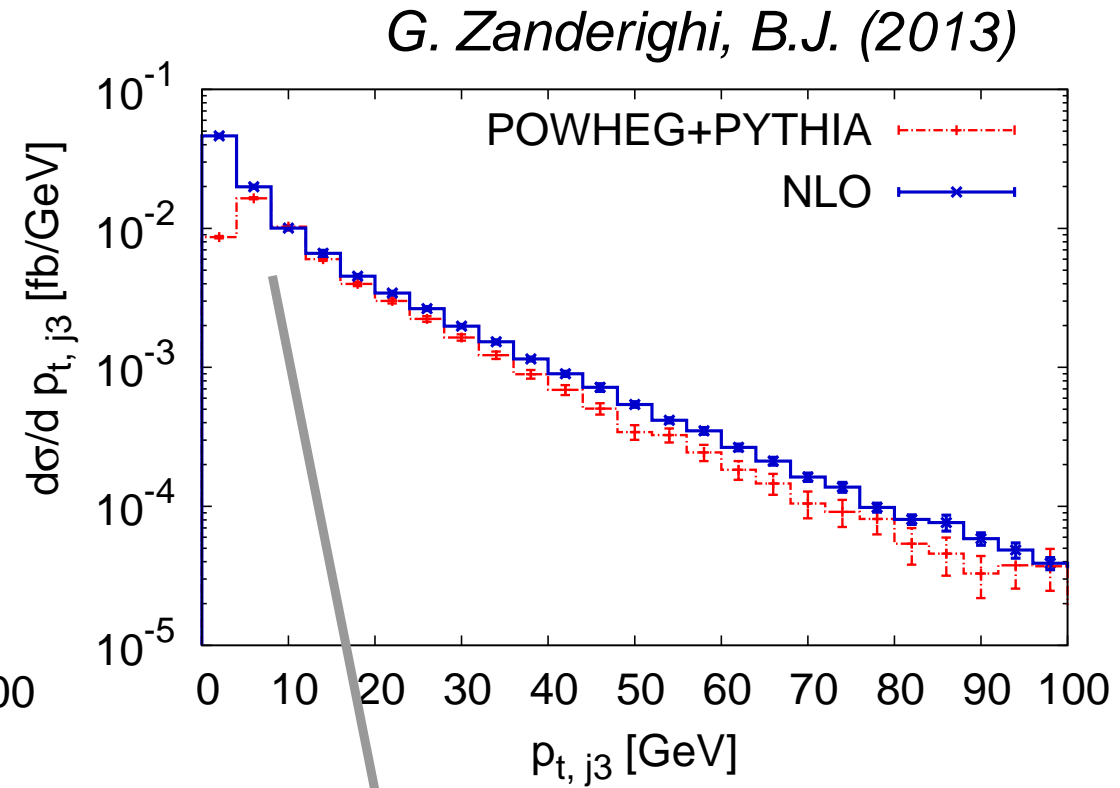
$$F \sim \left(\frac{p_{T,1}^2}{p_{T,1}^2 + \Lambda^2} \right)^2 \left(\frac{p_{T,2}^2}{p_{T,2}^2 + \Lambda^2} \right)^2$$

(alternative: explicit **generation cuts**)

$pp \rightarrow W^+W^-jj$ with leptonic decays: results

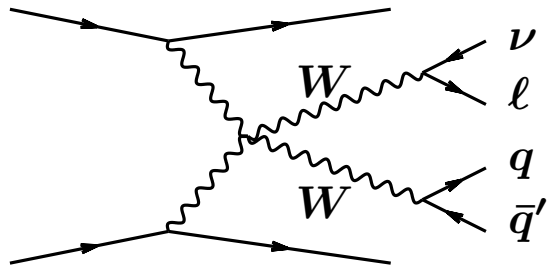


leptonic observables
not very sensitive to
parton shower



growth of jet distribution
tamed by Sudakov factor

$pp \rightarrow W^+W^-jj$ with semi-leptonic decays



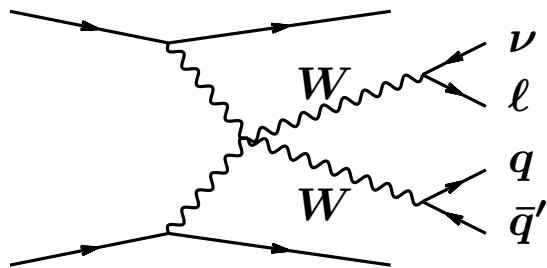
“semi-leptonic” final state:

$$W^+W^- \rightarrow \ell\nu + q\bar{q}'$$

different from fully leptonic modes:

- ✓ branching ratio $\text{BR}_{W \rightarrow q\bar{q}'} \approx 3 \times \text{BR}_{W \rightarrow \ell\nu} \rightarrow$ larger x-sec
- ✓ only one neutrino \rightarrow on-shell: M_{WW} reconstruction possible
- ✗ sophisticated analysis techniques needed to isolate signal

$pp \rightarrow W^+W^-jj$ with semi-leptonic decays



consider fictitious scenario with heavy Higgs

$$m_H = 400 \text{ GeV} > 2M_W$$

→ W bosons are typically on-shell

❖ require VBF topology for **tagging jets**:

$$p_{T,j}^{\text{tag}} > 25 \text{ GeV}, \quad |y_j^{\text{tag}}| < 4.5$$
$$\Delta y_{jj}^{\text{tag}} > 3, \quad m_{jj}^{\text{tag}} > 600 \text{ GeV}$$

❖ two **decay jets** have to be compatible with W decay

$$M_W - 10 \text{ GeV} \leq m_{jj}^{\text{dec}} \leq M_W + 10 \text{ GeV}$$

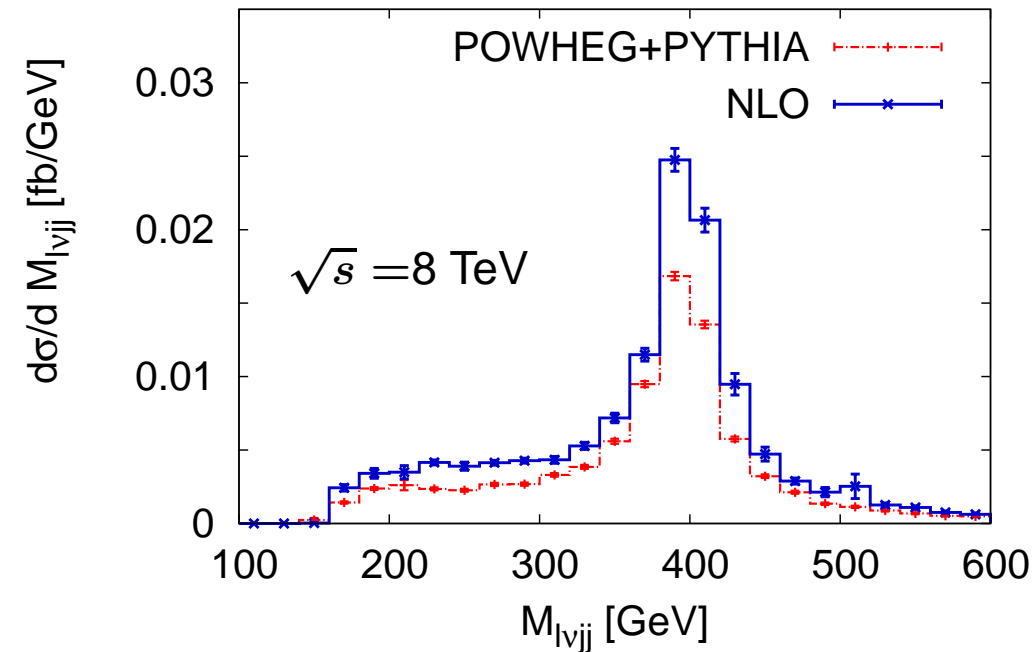
$pp \rightarrow W^+W^-jj$ with semi-leptonic decays

- ◆ reconstruct $M_{\ell\nu jj}$ using the assumption that

$$M_{\ell\nu} = M_W$$

(\rightarrow neutrino momentum)

- ✗ $M_{\ell\nu jj}$ distribution very sensitive to parton-shower effects!

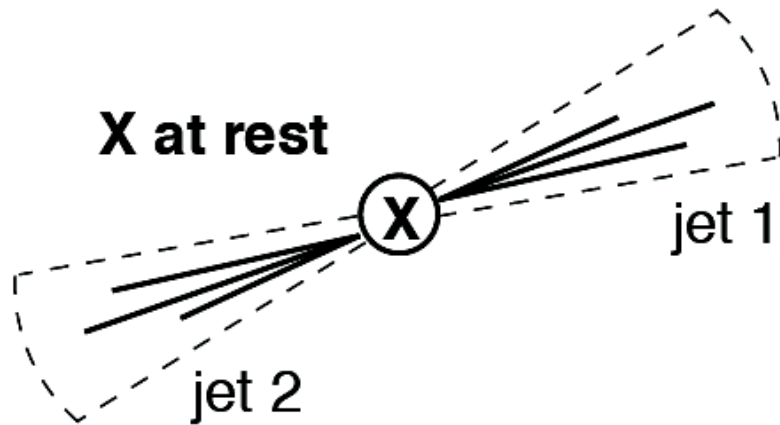


soft radiation smears distribution of W decay jets

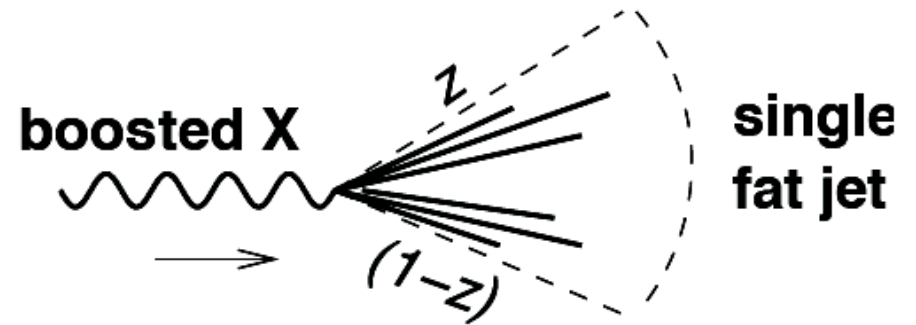
$\rightarrow m_{jj}^{\text{dec}} \sim M_W$ requirement no longer fulfilled

boosted jet techniques

Normal analyses: two quarks from $X \rightarrow q\bar{q}$ reconstructed as two jets



High- p_t regime: EW object X is boosted, decay is collimated, $q\bar{q}$ both in same jet



❖ pioneering work on WW scattering at the LHC

Butterworth, Cox, Forshaw (2002)

❖ break-through in $pp \rightarrow VH$

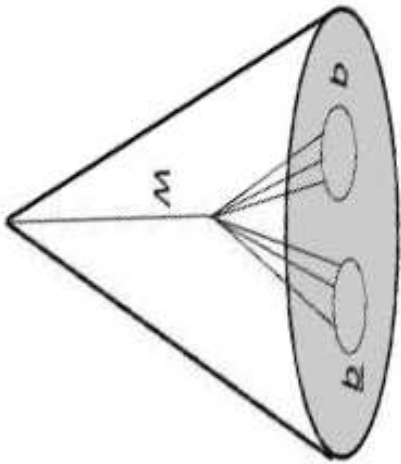
Butterworth, Davison, Rubin, Salam (2008)

❖ today: established field in its own

$pp \rightarrow W^+W^-jj$ with semi-leptonic decays

$$pp \rightarrow W^+(q\bar{q}')W^-(\ell\nu)jj:$$

require a **highly boosted fat jet**
with invariant mass close to M_W



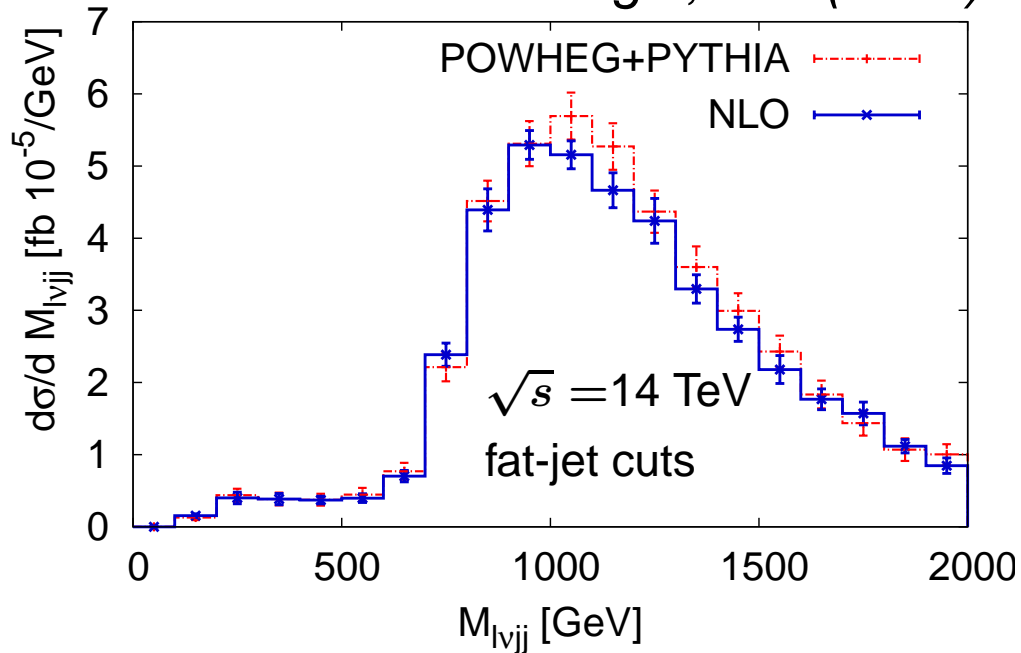
make use of jet properties / composition:

→ distinguish hadronically decaying
heavy bosons
from ordinary QCD jets

(stable against parton-shower effects)

$pp \rightarrow W^+W^-jj$ with semi-leptonic decays

G. Zanderighi, B.J. (2013)



results stable against
parton-shower effects

selection cuts
specific for fat-jet analysis:

$$p_{T,J}^{\text{boosted}} > 300 \text{ GeV},$$
$$M_J \in (M_W \pm 10 \text{ GeV}),$$
$$p_{T,\ell} > 300 \text{ GeV}$$

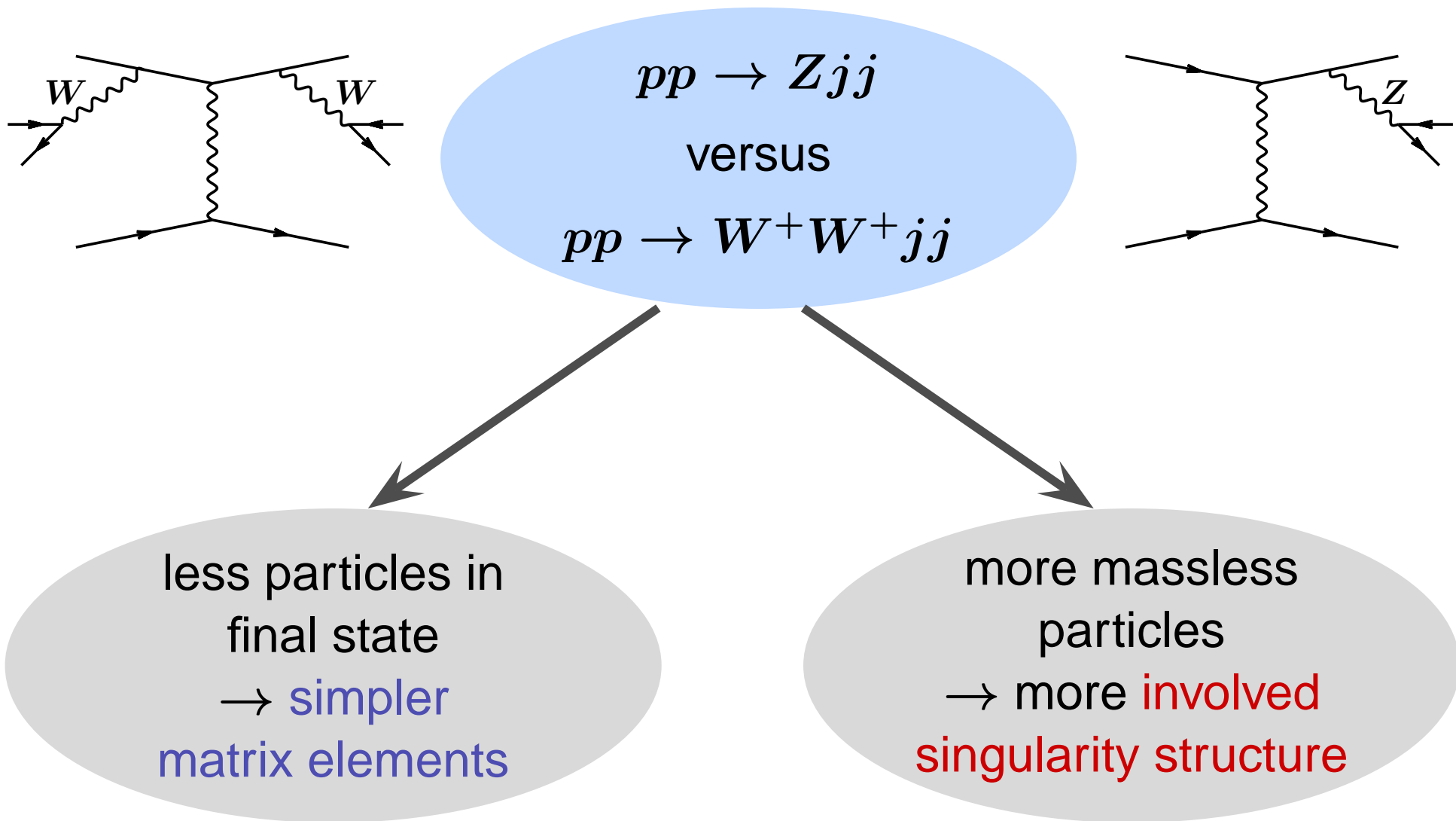
cuts enforce highly energetic
 WW system
(above light Higgs resonance)



less massive final state

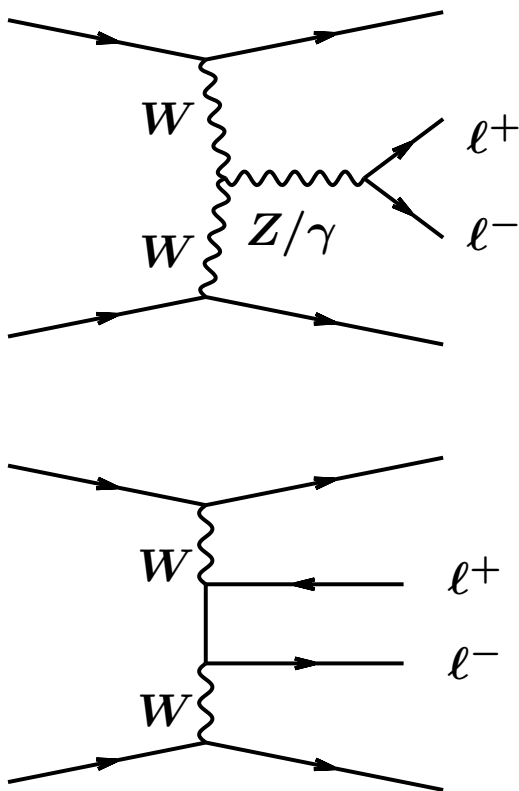


$pp \rightarrow Zjj$ via VBF



$pp \rightarrow Zjj$ via VBF in the POWHEG-BOX

charged current modes:



singularity structure similar to
 $pp \rightarrow W^+W^+jj$ via VBF, but

$\gamma^* \rightarrow l^+l^-$ singular as $Q_{\ell\ell}^2 \rightarrow 0$

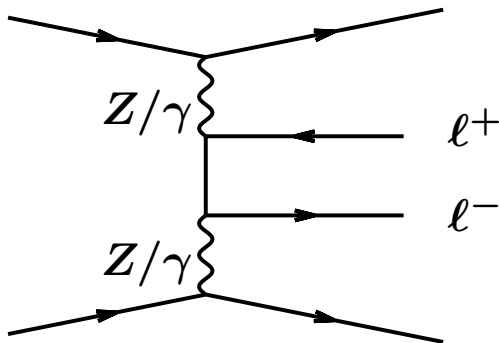
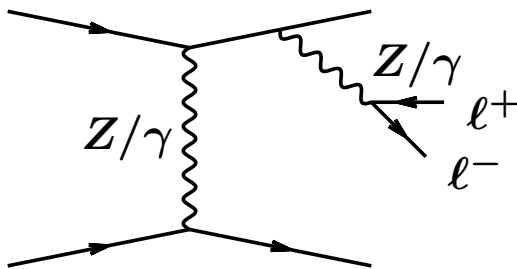
→ introduce generation cut

$$m_{\ell\ell}^{\text{gen}} = 30 \text{ GeV},$$

supplemented by analysis cut

$$m_Z - 10 \text{ GeV} < m_{\ell\ell} < m_Z + 10 \text{ GeV}$$

neutral current modes:



extra singularity for photons in t -channel

with $Q_\gamma^2 \rightarrow 0$

(\leftrightarrow related to low- p_T jets)

➡ damping factor in matrix elements

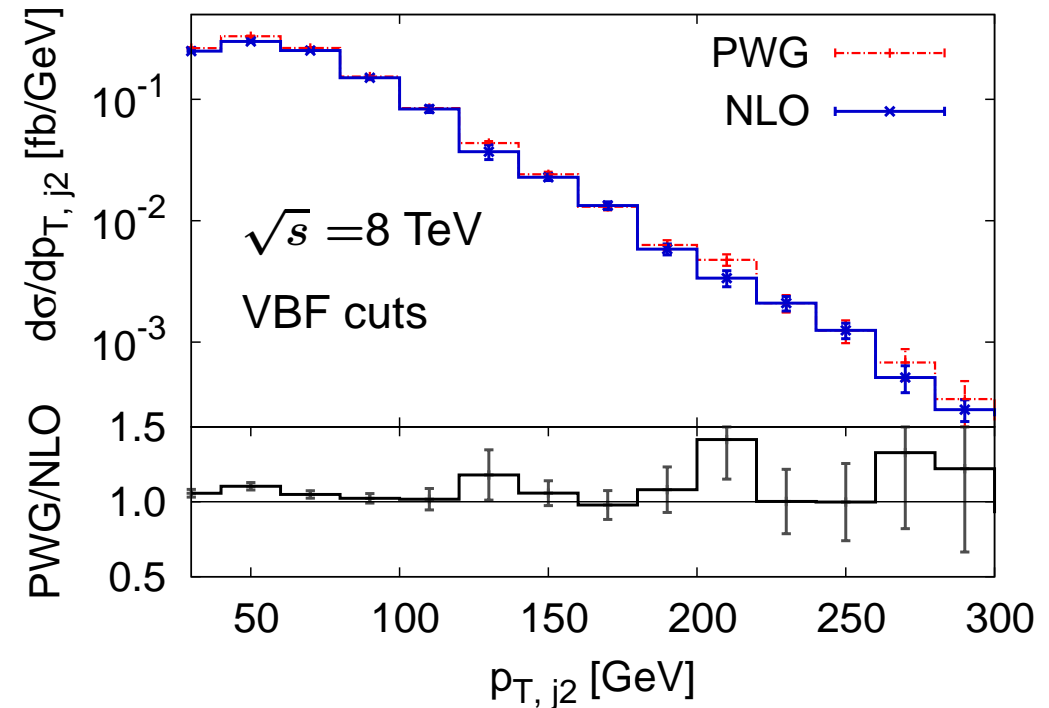
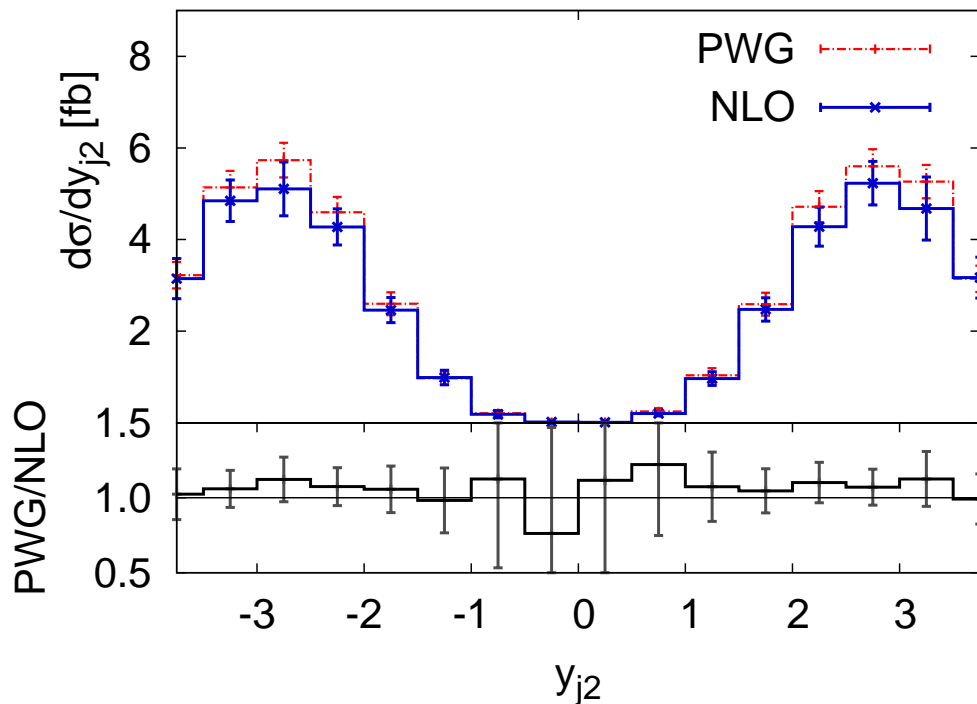
➡ Born-suppression factor

$$F \sim \left(\frac{p_{T,1}^2}{p_{T,1}^2 + \Lambda^2} \right)^2 \left(\frac{p_{T,2}^2}{p_{T,2}^2 + \Lambda^2} \right)^2$$

(alternative: generation cuts)

$pp \rightarrow Zjj$ via VBF in the POWHEG-BOX

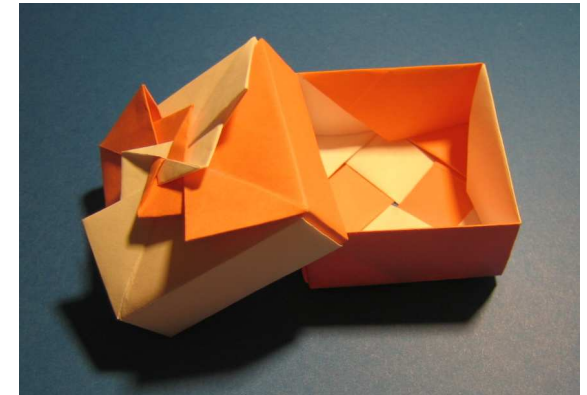
Schneider, Zanderighi, B.J. (2012)



parton shower effects are moderate
for distributions related to hard jets

VBF in the POWHEG-BOX: getting started

- ❖ get access to a computing farm
- ❖ download the POWHEG-BOX from:
`http://powhegbox.mib.infn.it/`
- ❖ go to the directory of the process you are interested in, e.g.,
`$ cd POWHEG-BOX/VBF_Wp_Wm`
- ❖ for instructions on running the code refer to the documentation in `POWHEG-BOX/VBF_Wp_Wm/Docs`
- ❖ use sample files for input and analysis, or replace them with your own files





VBF crucial for understanding mechanism of electroweak symmetry breaking:

- * very clean Higgs production channel
- * sensitive to signatures of new physics in the gauge boson sector

important pre-requisites:

- ✓ explicit calculations revealed that VBF reactions are **perturbatively well-behaved** (NLO-QCD corrections and parton-shower effects moderate)
- ✓ **backgrounds** are well under control



for a quantitative understanding of VBF processes it is vital to provide:

* **precise predictions**, including

- NLO QCD corrections
- NLO EW corrections, interference effects, realistic PDFs, ...

* **realistic predictions**, allowing for

- calculation of distributions within experimental selection cuts
- matching to parton-shower Monte Carlos at NLO-QCD accuracy

* **sophisticated analysis techniques**, requiring cross links
between experimentalists and theorists / phenomenologists



...for your attention