

Monopoles and Electroweak Symmetry Breaking

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with Csaba Csaki, Yuri Shirman
[hep-ph/1003.1718](#)

Outline

- * Motivation
- * A Brief History of Monopoles
- * Anomalies
- * Models
- * LHC
- * Conclusions

Hierarchy Problem Now



SUSY

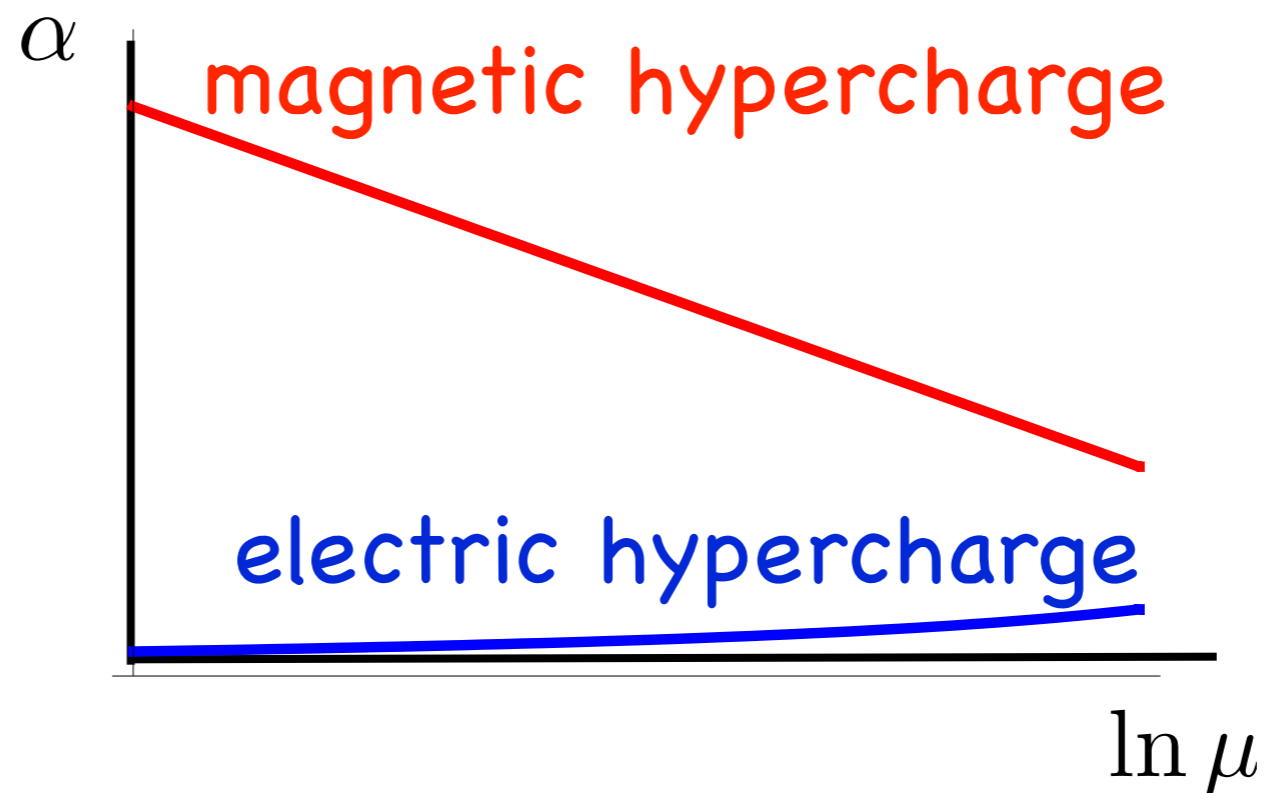
conspicuous in it's
absence so far



Technicolor

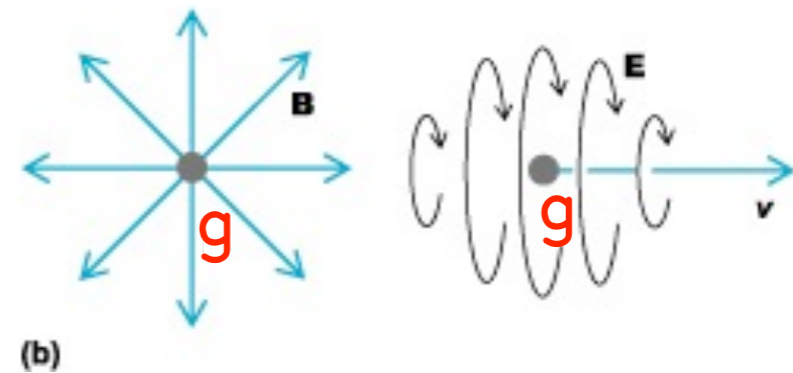
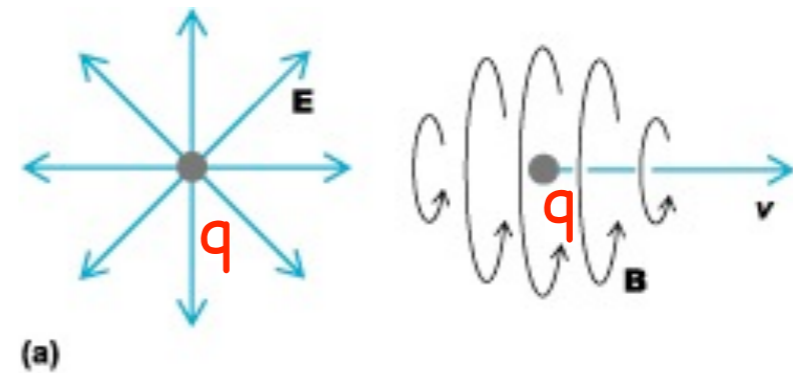
ETC doesn't work

The Vision Thing

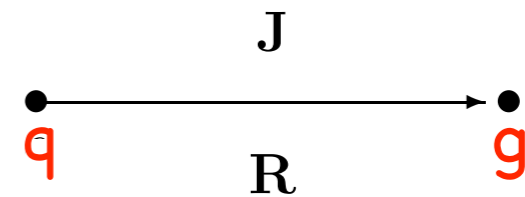


consistent theory of massless dyons?
chiral symmetry breaking \rightarrow EWSB?

J.J. Thomson

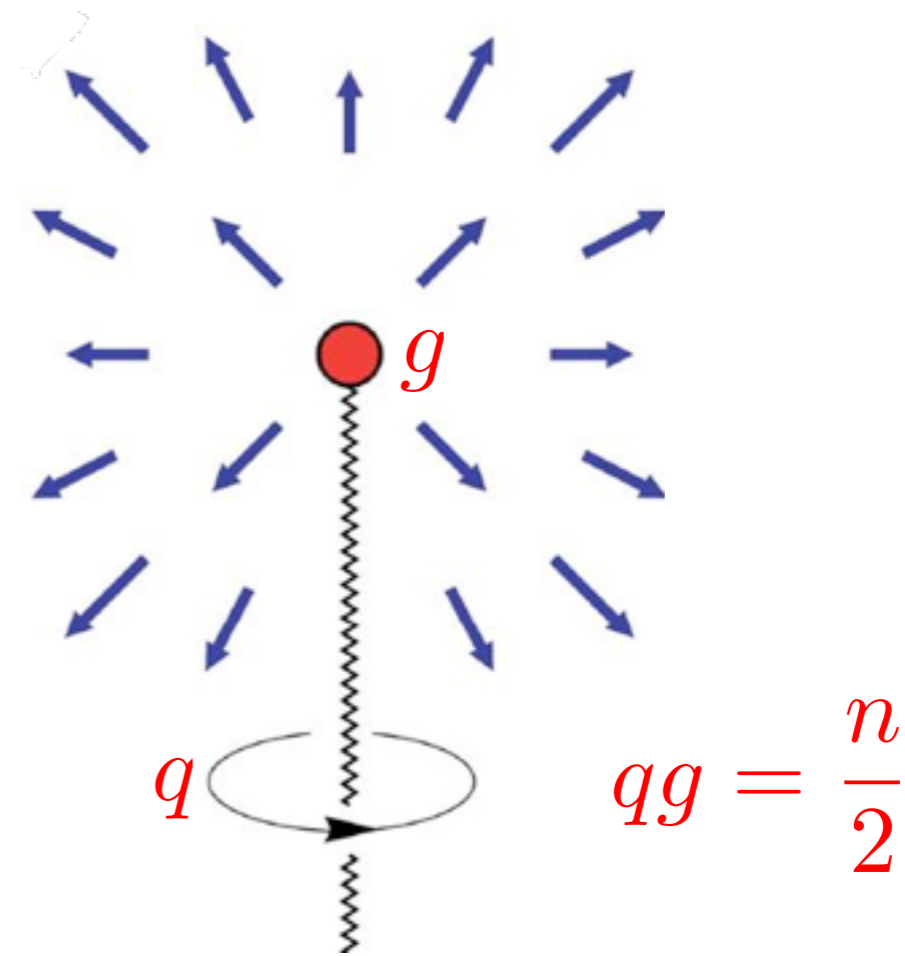


$$J = q g$$



Philos. Mag. 8 (1904) 331

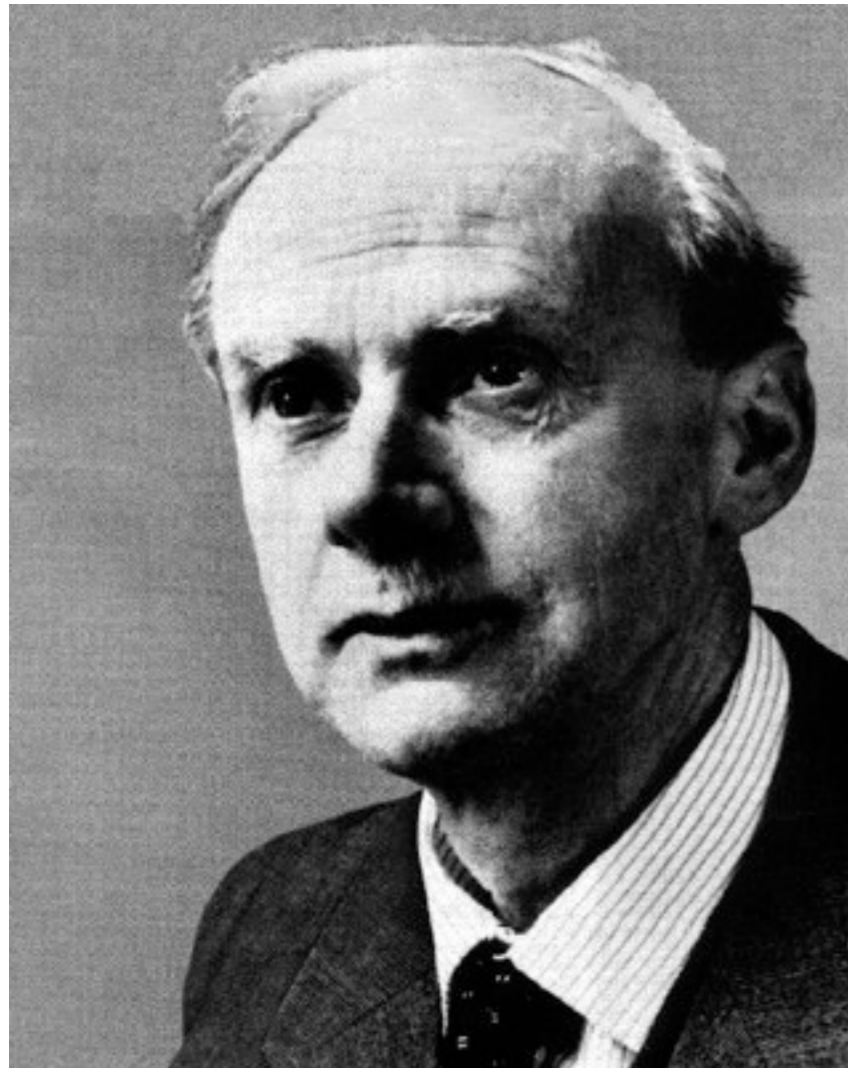
Dirac



charge quantization

Proc. Roy. Soc. Lond. A133 (1931) 60

Dirac



non-local action?

$$F_{\mu\nu} = \partial_\mu A_\nu - \partial_\nu A_\mu + {}^*G_{\mu\nu}$$

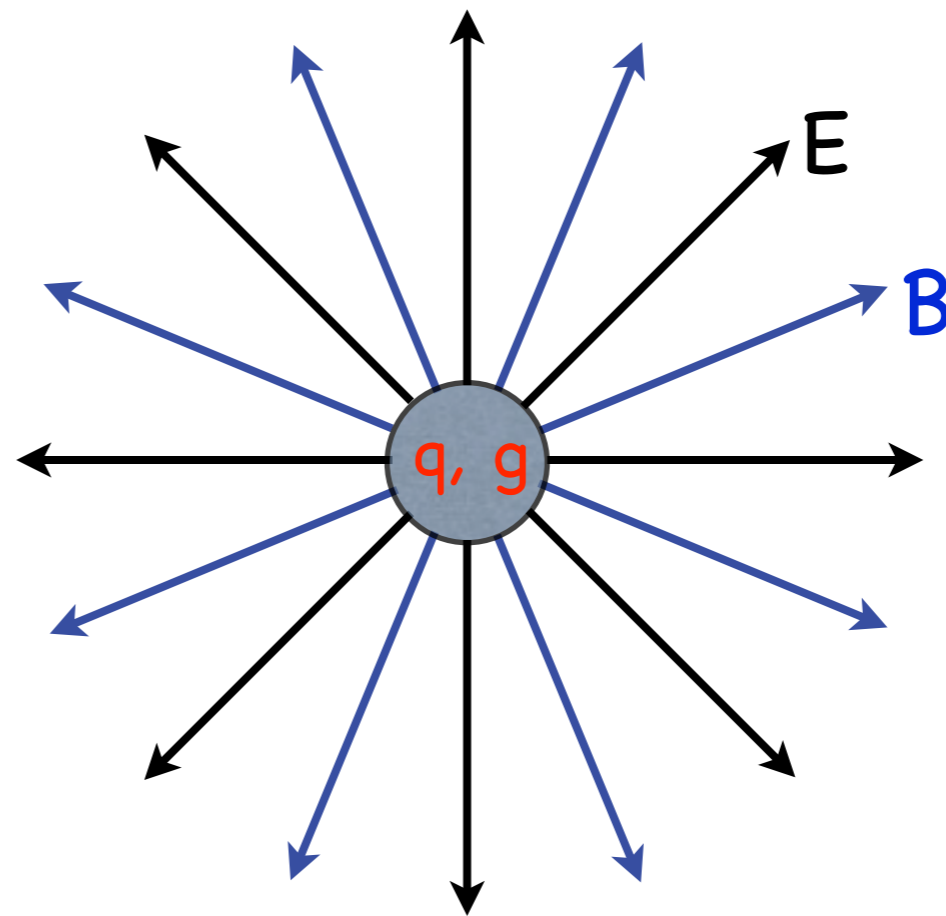
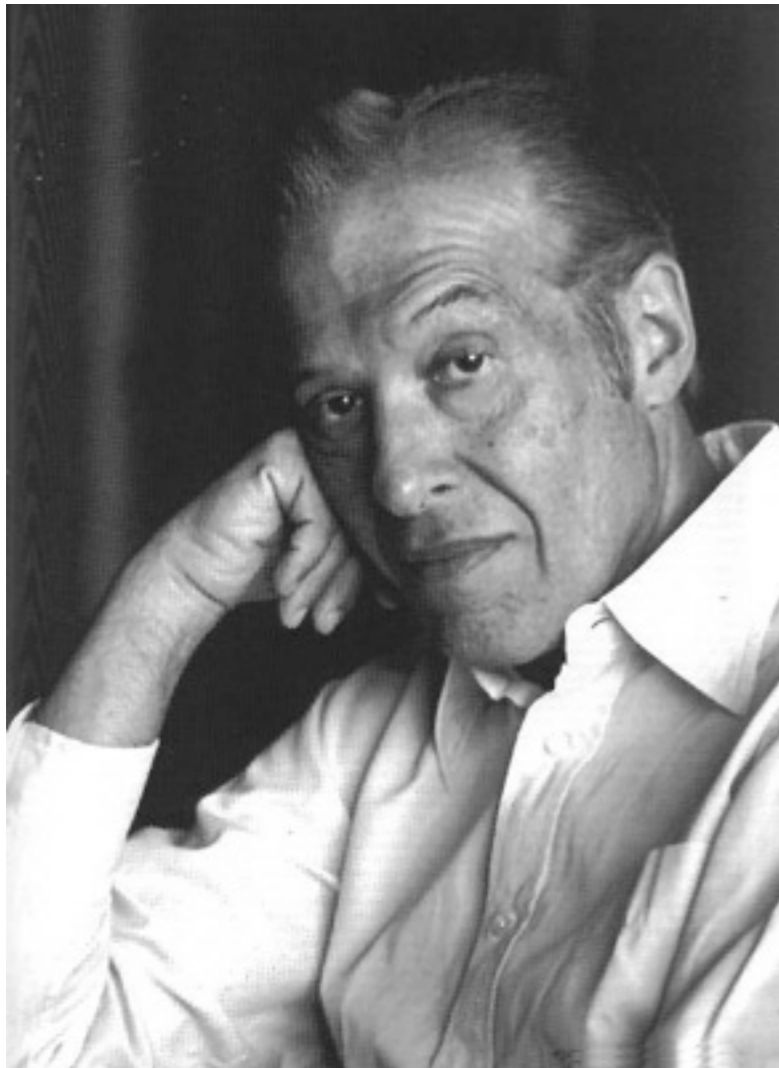
$$\begin{aligned} G_{\mu\nu}(x) &= 4\pi(n \cdot \partial)^{-1} [n_\mu K_\nu(x) - n_\nu K_\mu(x)] \\ &= \int d^4y [f_\mu(x-y)K_\nu(y) - f_\nu(x-y)K_\mu(y)] \end{aligned}$$

$$\partial_\mu f^\mu(x) = 4\pi\delta(x)$$

$$f^\mu(x) = 4\pi n^\mu (n \cdot \partial)^{-1} \delta(x)$$

Phys. Rev. 74 (1948) 817

Schwinger

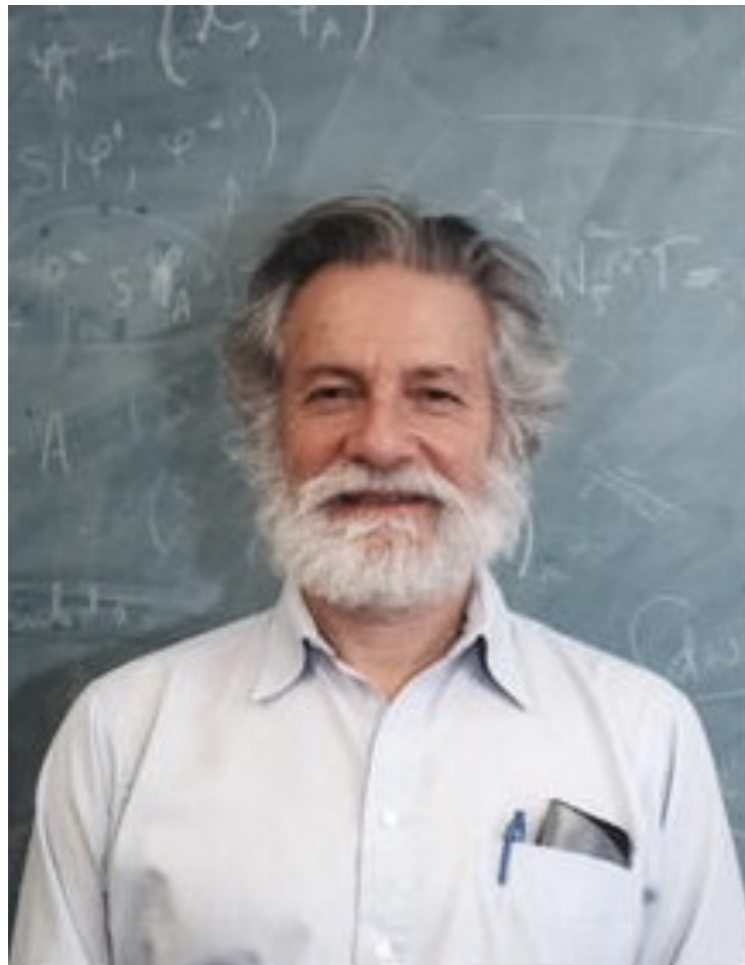


dyons

$$q_1 g_2 - q_2 g_1 = \frac{n}{2}$$

Science 165 (1969) 757

Zwanziger



non-Lorentz invariant, local action?

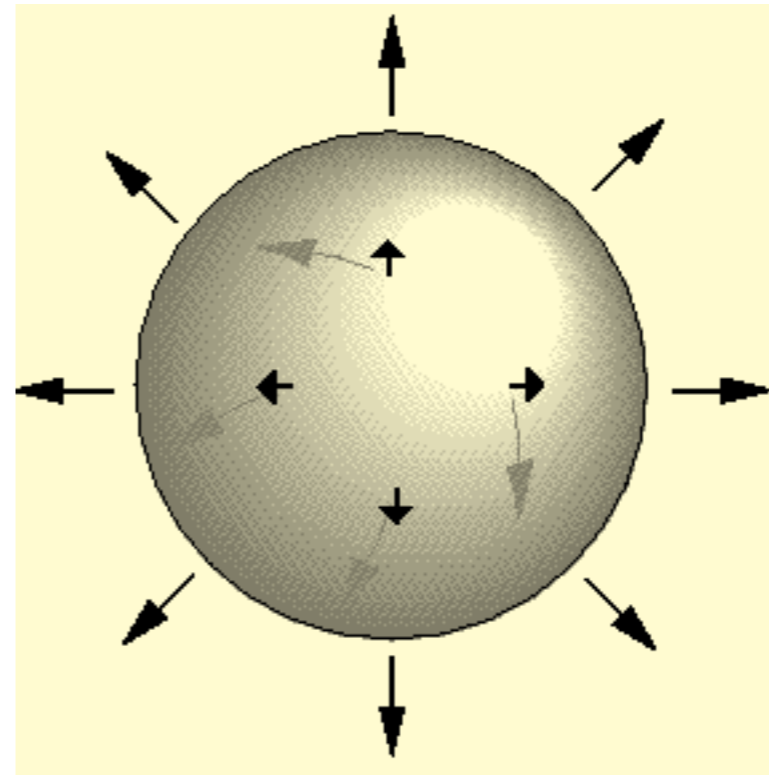
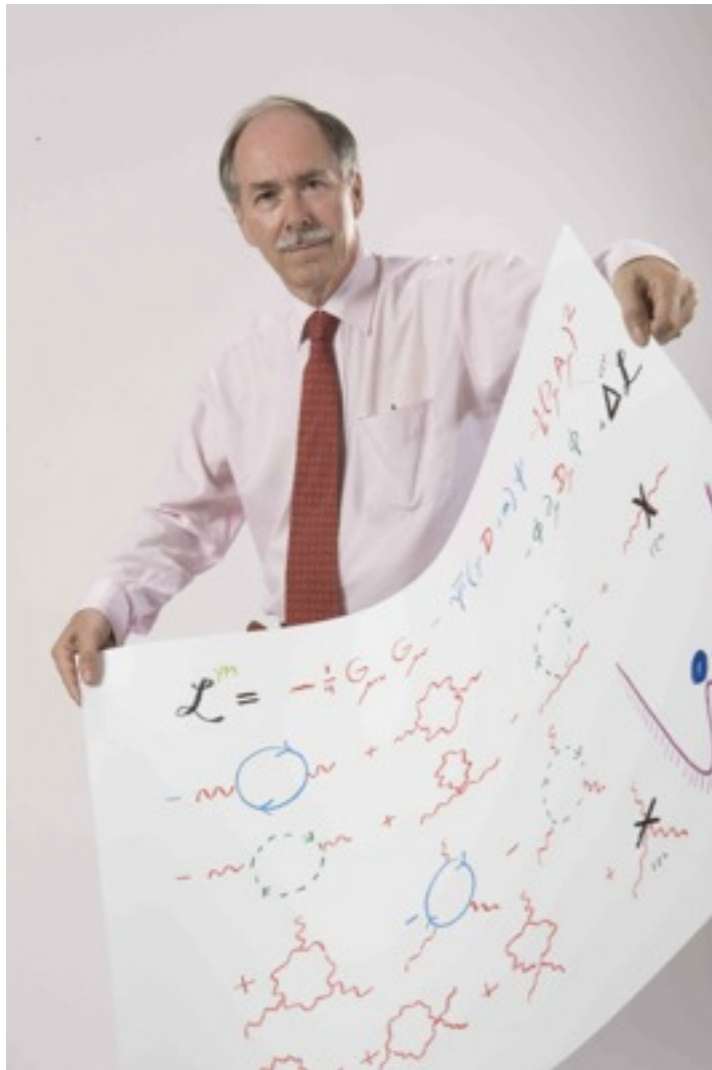
$$\mathcal{L} = -\frac{1}{2n^2 e^2} \{ [n \cdot (\partial \wedge A)] \cdot [n \cdot *(\partial \wedge B)] - [n \cdot (\partial \wedge B)] \cdot [n \cdot *(\partial \wedge A)] \\ + [n \cdot (\partial \wedge A)]^2 + [n \cdot (\partial \wedge B)]^2 \} - J \cdot A - \frac{4\pi}{e^2} K \cdot B.$$

electric magnetic

$$F = \frac{1}{n^2} (\{ n \wedge [n \cdot (\partial \wedge A)] \} - * \{ n \wedge [n \cdot (\partial \wedge B)] \})$$

Phys. Rev. D3 (1971) 880

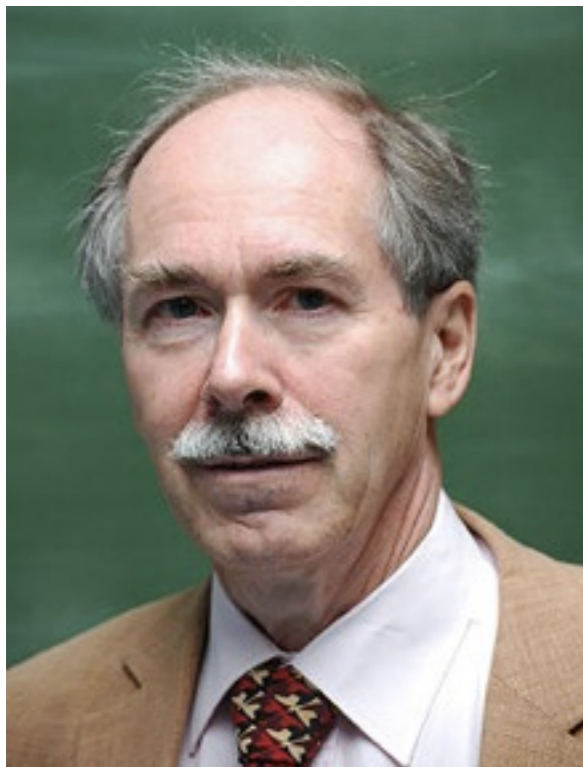
't Hooft-Polyakov



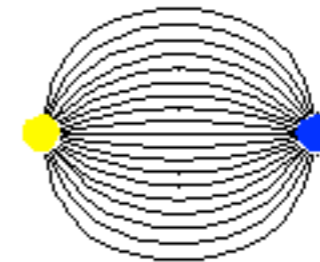
topological monopoles

Nucl. Phys., B79 1974, 276
JETP Lett., 20 1974, 194

't Hooft-Mandelstam

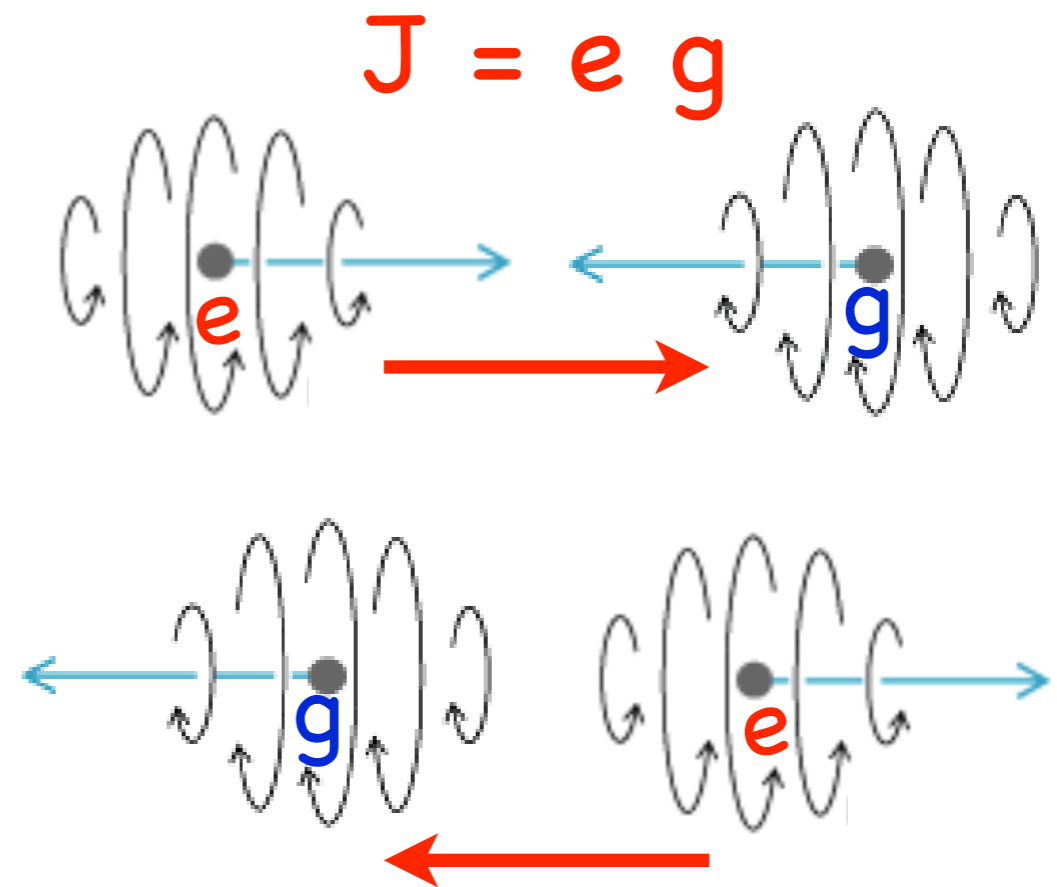


magnetic condensate
confines electric charge



High Energy Physics Ed. Zichichi, (1976) 1225
Phys. Rept. 23 (1976) 245

Rubakov-Callan



new unsuppressed contact interactions!

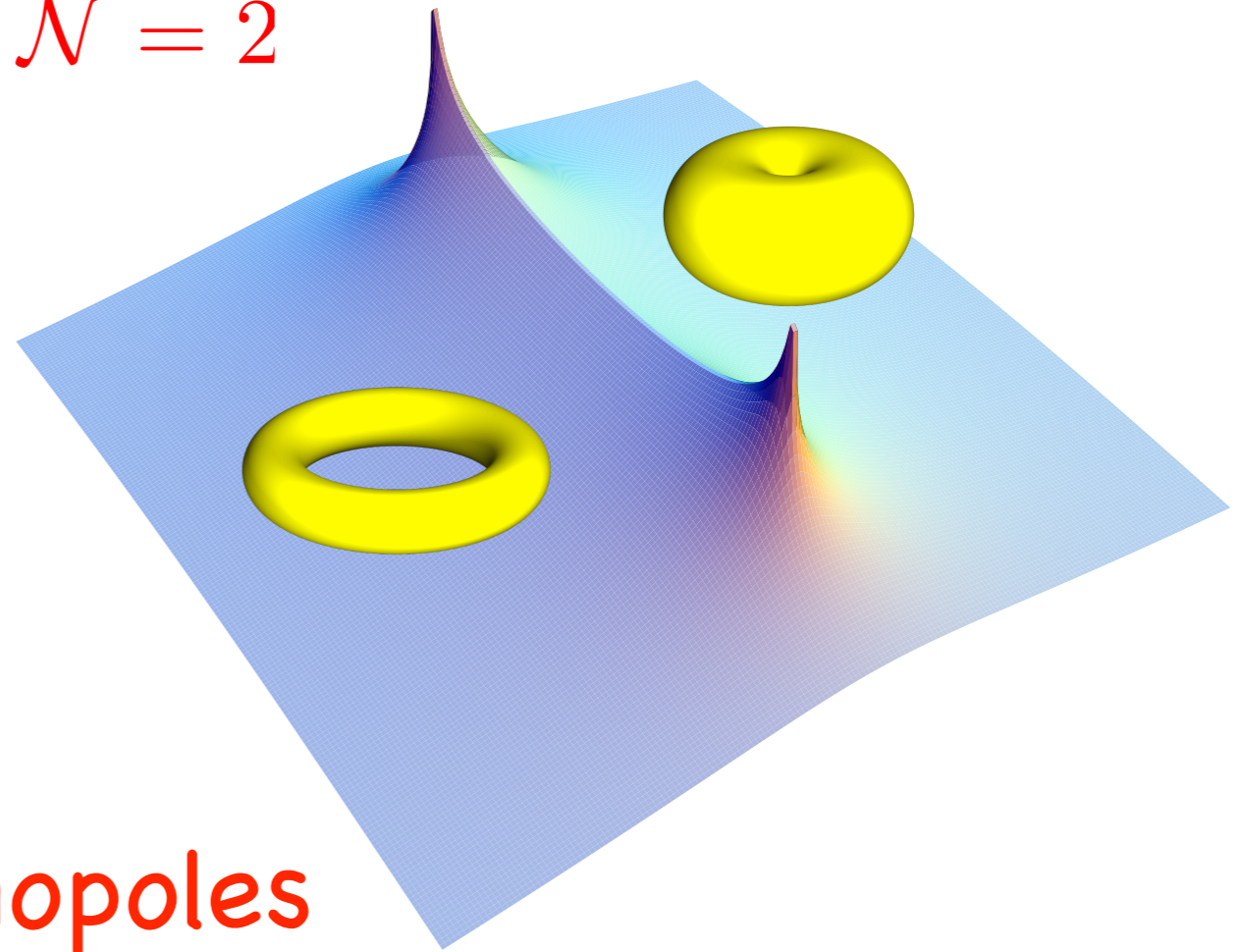
JETP Lett. 33 (1981) 644

Phys. Rev. D25 (1982) 2141

Seiberg-Witten



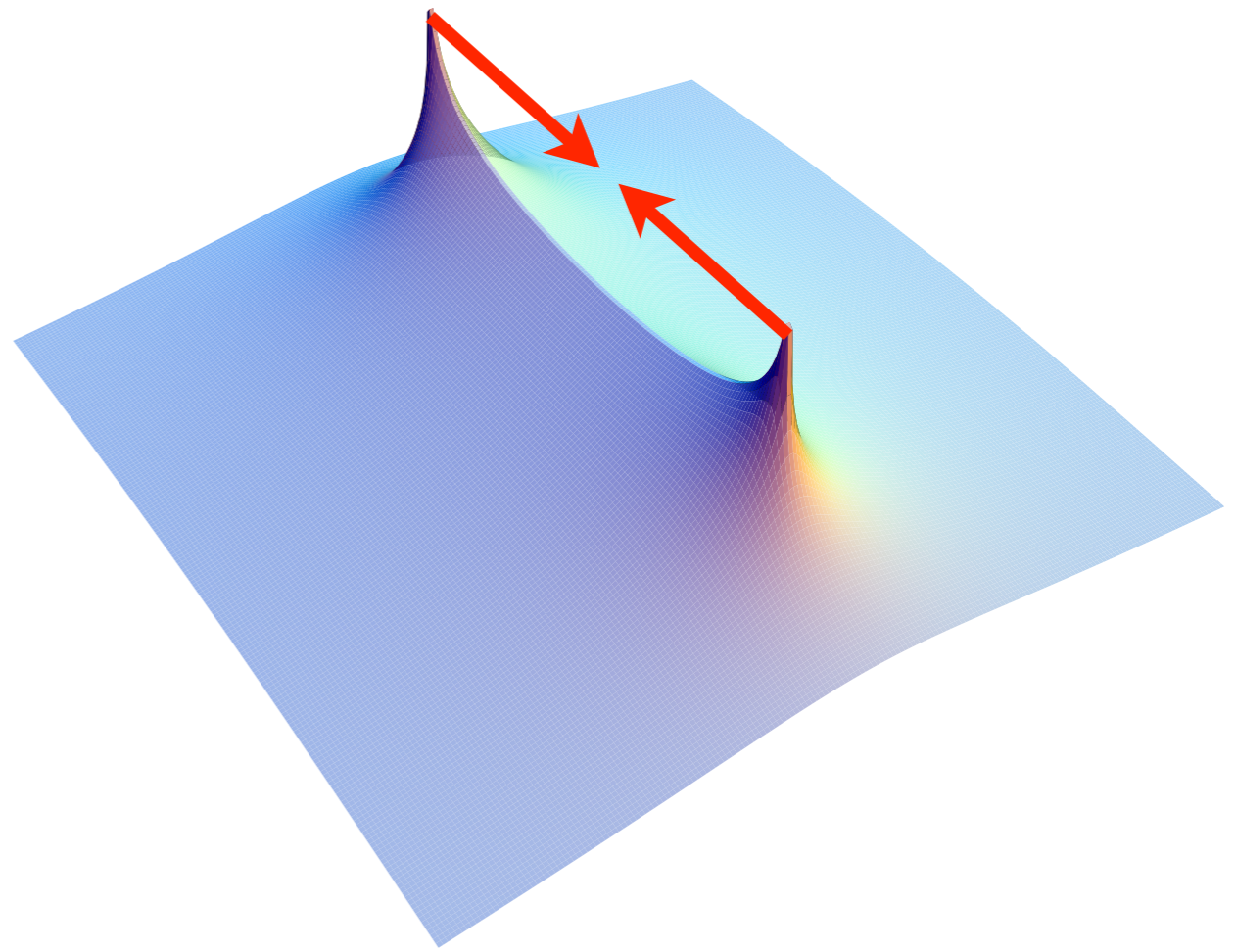
$$\mathcal{N} = 2$$



massless fermionic monopoles

hep-th/9407087

Argyres-Douglas



CFT with massless electric and magnetic charges

[hep-th/9505062](https://arxiv.org/abs/hep-th/9505062)

Toy Model

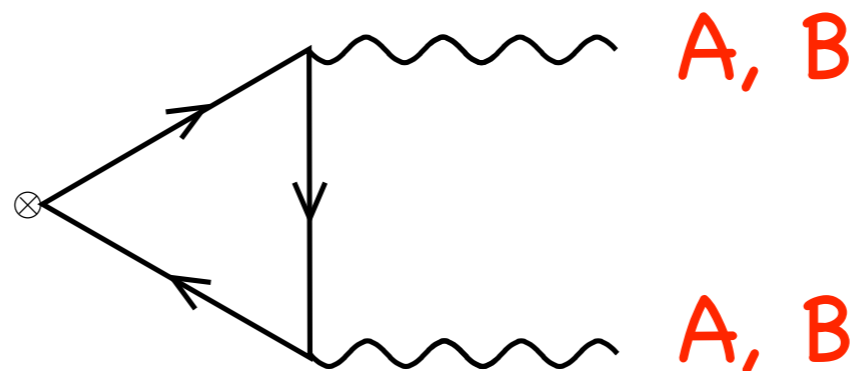
	$SU(3)_c$	$SU(2)_L$	$U(1)_Y : q$	$U(1)_Y : g$
Q	\square	\square	$\frac{1}{6}$	3
L	1	\square	$-\frac{1}{2}$	-9
\bar{U}	$\bar{\square}$	1	$-\frac{2}{3}$	-3
\bar{D}	$\bar{\square}$	1	$\frac{1}{3}$	-3
\bar{N}	1	1	0	9
\bar{E}	1	1	1	9

$$q_i g_j - q_j g_i = \frac{n}{2}$$

is this anomaly free?

Anomalies

$$\mathcal{L} = -\frac{1}{2n^2 e^2} \{ [n \cdot (\partial \wedge A)] \cdot [n \cdot^* (\partial \wedge B)] - [n \cdot (\partial \wedge B)] \cdot [n \cdot^* (\partial \wedge A)] \\ + [n \cdot (\partial \wedge A)]^2 + [n \cdot (\partial \wedge B)]^2 \} - J \cdot A - \frac{4\pi}{e^2} K \cdot B.$$



Csaki, Shirman, JT [hep-th/1003.0448](#)

Toy Model

	$SU(3)_c$	$SU(2)_L$	$U(1)_Y : q$	$U(1)_Y : g$
Q	\square	\square	$\frac{1}{6}$	3
L	1	\square	$-\frac{1}{2}$	-9
\bar{U}	$\bar{\square}$	1	$-\frac{2}{3}$	-3
\bar{D}	$\bar{\square}$	1	$\frac{1}{3}$	-3
\bar{N}	1	1	0	9
\bar{E}	1	1	1	9

$$\sum_j q_j^3 = 0, \quad \sum_j g_j^3 = 0, \quad \sum_j g_j^2 q_j = 0, \quad \sum_j q_j^2 g_j = 0, \quad \sum_j q_j = 0, \quad \sum_j g_j = 0,$$

$$\sum_j \text{Tr } T_{r_j}^a T_{r_j}^b q_j = 0, \quad \sum_j \text{Tr } \tau_{r_j}^a \tau_{r_j}^b q_j = 0, \quad \sum_j \text{Tr } T_{r_j}^a T_{r_j}^b g_j = 0, \quad \sum_j \text{Tr } \tau_{r_j}^a \tau_{r_j}^b g_j = 0$$

Dynamics

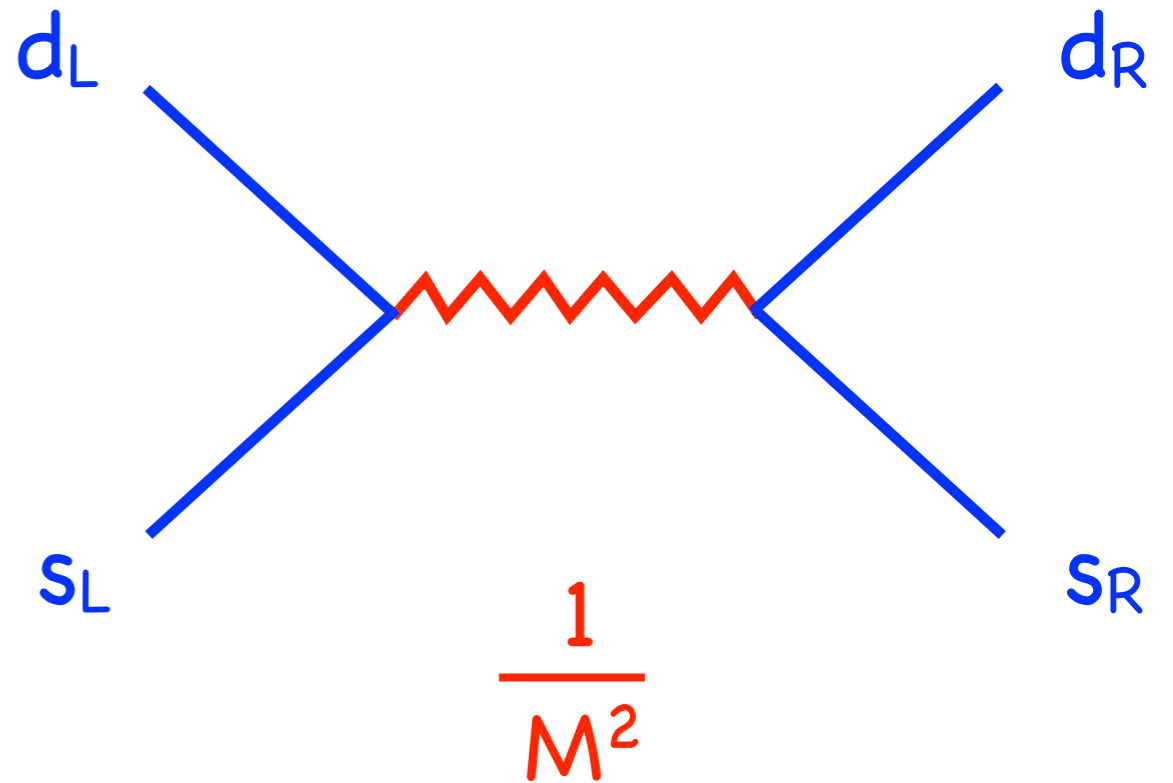
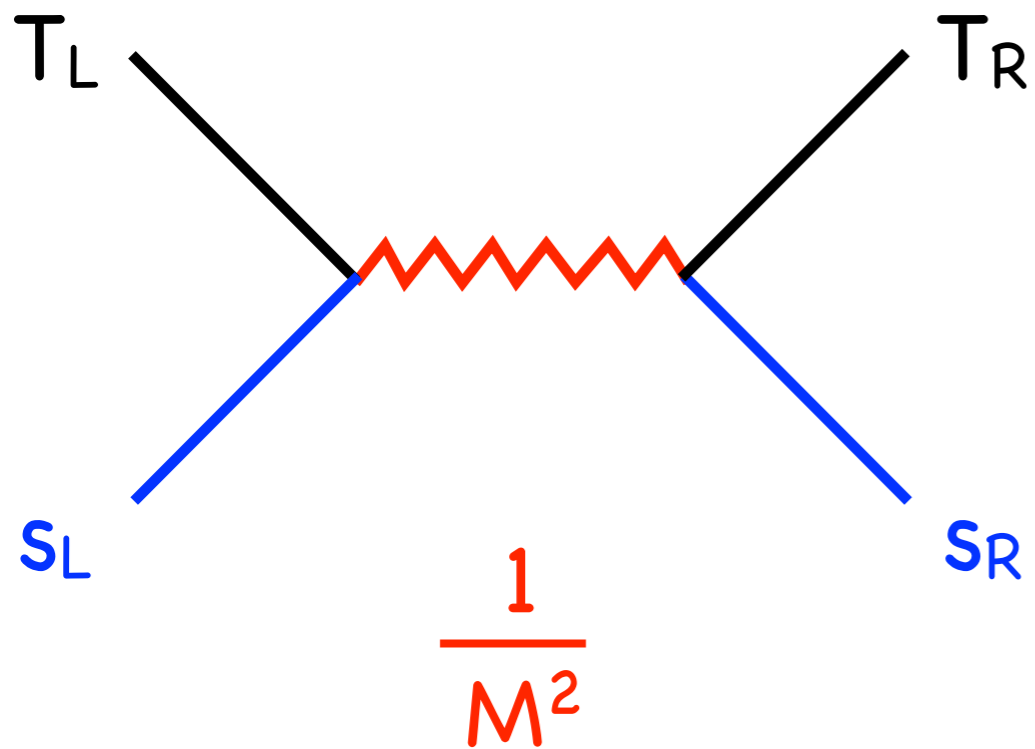
	$SU(3)_c$	$SU(2)_L$	$U(1)_Y : q$	$U(1)_Y : g$
Q	\square	\square	$\frac{1}{6}$	3
L	1	\square	$-\frac{1}{2}$	-9
\bar{U}	$\bar{\square}$	1	$-\frac{2}{3}$	-3
\bar{D}	$\bar{\square}$	1	$\frac{1}{3}$	-3
\bar{N}	1	1	0	9
\bar{E}	1	1	1	9

$$\left(\frac{1}{6}\right)^2 \alpha_Y 3^2 \alpha_m = \frac{1}{4}$$

$$\alpha_m \sim 98$$

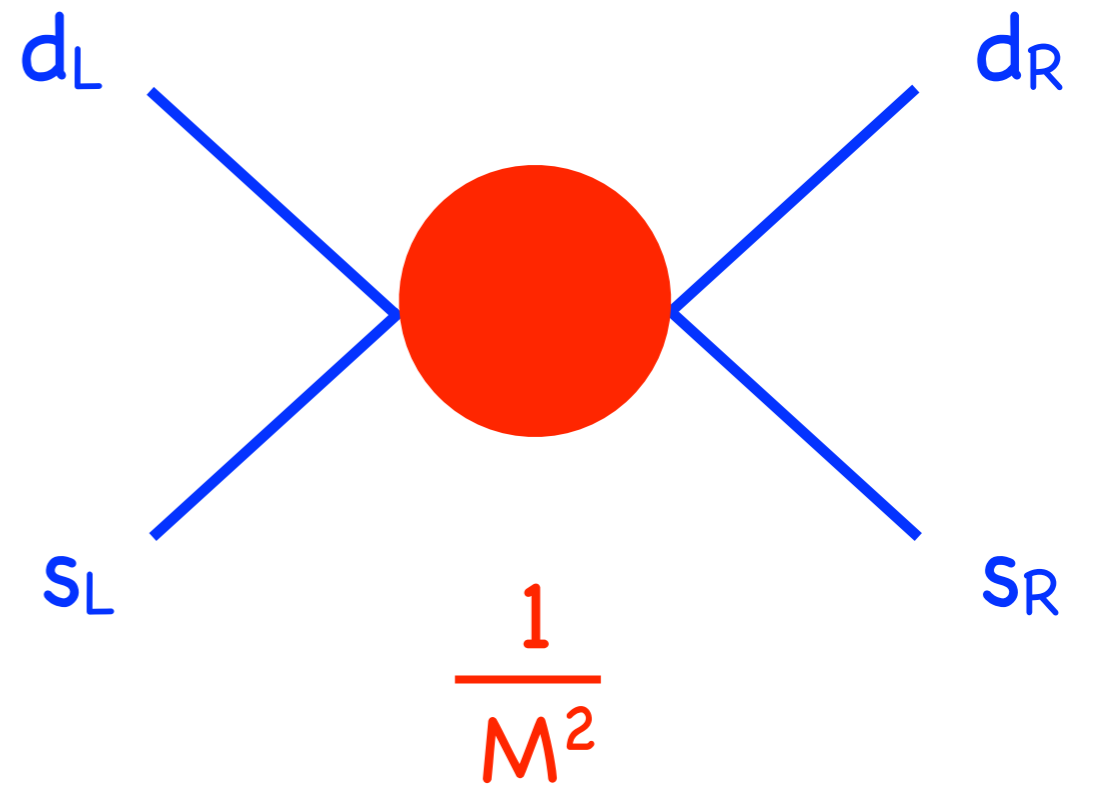
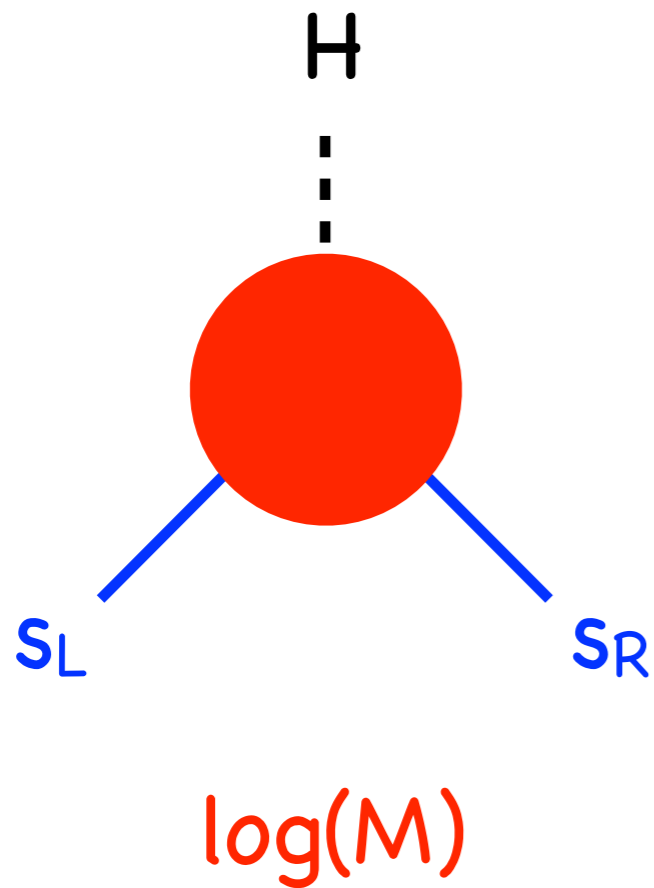
Quark Masses

technicolor: fail

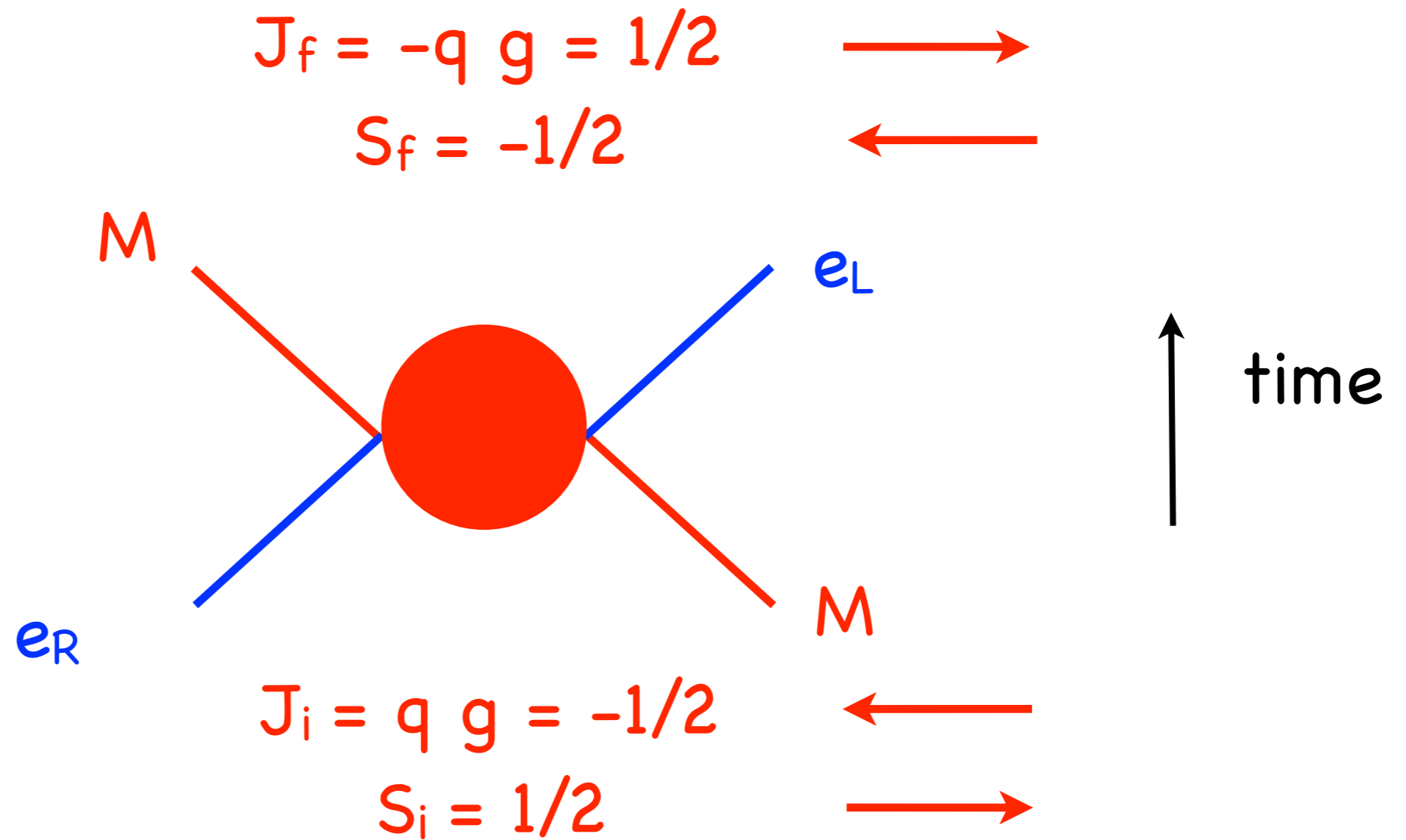


Quark Masses

Standard Model



Rubakov–Callan



New dimension 4, four particle operator

Angular Momentum

Classical:
$$\vec{L} = \vec{r} \times \vec{p} - q g \hat{r}$$

$$L^2 = |\vec{r} \times \vec{p}|^2 + q^2 g^2$$

Quantum:
$$[L_i, L_j] = i \epsilon_{ijk} L_k$$


$$L^2 = \ell(\ell + 1), \quad \ell \geq q g$$

Wu, Yang Nucl. Phys. B107, (1976) 365

Angular Momentum

$$\left[(\partial_\mu - iqA_\mu)^2 - \frac{q}{2} \sigma^{\mu\nu} F_{\mu\nu} - m^2 \right] \Psi = 0$$

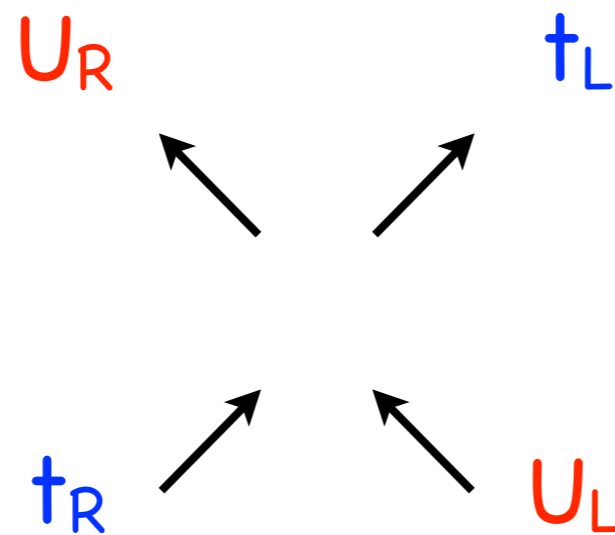
$$\left[-\frac{1}{r^2} \frac{\partial}{\partial r} \left(r^2 \frac{\partial}{\partial r} \right) + \frac{1}{r^2} (\vec{L}^2 - q^2 g^2) - q \vec{\sigma} \cdot \vec{B} - (E^2 - m^2) \right] \Psi = 0$$


$$\frac{1}{r^2} (\ell(\ell + 1) - q^2 g^2) - q g \frac{\vec{\sigma} \cdot \hat{r}}{r^2}$$

for $\ell = qg$ one helicity can reach the origin

Four Fermion Ops

$$J_f = -q \quad g = -1/2 \quad \leftarrow$$
$$S_f = -1 \quad \leftarrow$$

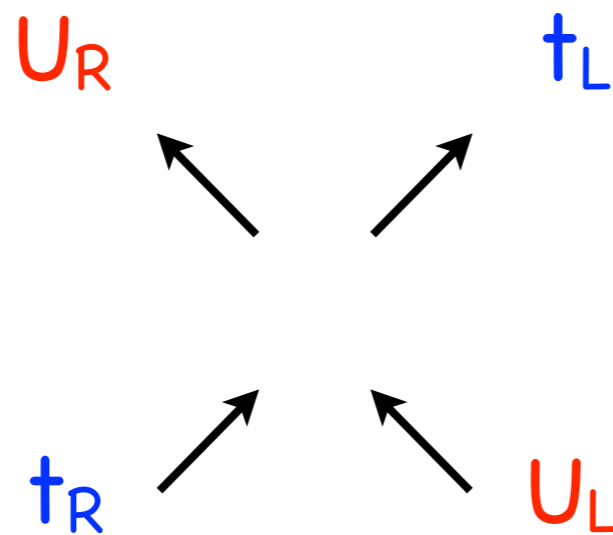


$$J_i = q \quad g = 2 \quad \longrightarrow$$
$$S_i = 1 \quad \longrightarrow$$

time \uparrow

Four Fermion Ops

$$J_f = -q \quad g = -1/2 \quad \leftarrow$$
$$S_f = -1 \quad \leftarrow$$



$$J_i = q \quad g = 2 \quad \longrightarrow$$
$$S_i = 1 \quad \longrightarrow$$

time \uparrow

fail!

Four Fermion Ops

$$J_f = -q \quad g = -2$$

$$S_f = 0$$



U_R

t_R



t_L

U_L



time

$$J_i = q \quad g = 1/2$$

$$S_i = 0$$



Four Fermion Ops

$$J_f = -q \quad g = -2$$

$$S_f = 0$$



U_R

t_R



t_L

U_L



time

$$J_i = q \quad g = 1/2$$

$$S_i = 0$$



fail!

non-Abelian magnetic charge

$$Q = T^3 + Y$$

$$Q_m = T_m^3 + Y_m$$

explicit examples known in GUT models

EWSB is forced to align with the monopole charge

non-Abelian magnetic charge

$$\vec{B}_Y^a = \frac{g}{g_Y} \frac{\hat{r}}{r^2}$$

$$\vec{B}_L^a = \delta_L^{a3} \frac{g \beta_L}{g_L} \frac{\hat{r}}{r^2}$$

$$\vec{B}_c^a = \delta_c^{a8} \frac{g \beta_c}{g_c} \frac{\hat{r}}{r^2}$$

$$4\pi (T_c^8 g \beta_c + T_L^3 g \beta_L + Y g) = 2\pi n$$

non-Abelian magnetic charge

$$4\pi (T_c^8 g \beta_c + T_L^3 g \beta_L + Y g) = 2\pi n$$

$$eA^\mu = g_L A_L^{3\mu} + g_Y A_Y^\mu$$

$$\beta_L = 1$$

$$T_c^8 g \beta_c + q g = \frac{n}{2}$$

The Model

$$(SU(3)_c \times SU(2)_L \times U(1)_Y) / Z_6$$

	$SU(3)_c$	$SU(2)_L$	$U(1)_Y^{el}$	$U(1)_Y^{mag}$
Q_L	\square^m	\square^m	$\frac{1}{6}$	$\frac{1}{2}$
L_L	1	\square^m	$-\frac{1}{2}$	$-\frac{3}{2}$
U_R	\square^m	1^m	$\frac{2}{3}$	$\frac{1}{2}$
D_R	\square^m	1^m	$-\frac{1}{3}$	$\frac{1}{2}$
N_R	1	1^m	0	$-\frac{3}{2}$
E_R	1	1^m	-1	$-\frac{3}{2}$

$$\alpha_m = \frac{1}{4\alpha} \approx 32$$

Four Fermion Ops

$$J_f = -qg = -\frac{2}{3} \begin{pmatrix} 3 \\ -2 \end{pmatrix} \longrightarrow$$

$$S_f = -1 \longleftarrow$$

N_R

t_L



t_R

N_L



$$J_i = qg = \frac{2}{3} \begin{pmatrix} 3 \\ -2 \end{pmatrix} \longleftarrow$$

$$S_i = +1 \longrightarrow$$



time

Four Fermion Ops

$$J_f = -qg = -\frac{2}{3} \begin{pmatrix} 3 \\ -2 \end{pmatrix} \quad \longrightarrow$$

$$S_f = -1 \quad \longleftarrow$$

N_R

t_L



t_R

N_L

$$J_i = qg = \frac{2}{3} \begin{pmatrix} 3 \\ -2 \end{pmatrix} \quad \longleftarrow$$

$$S_i = +1 \quad \longrightarrow$$

hooray!



time

Four Fermion Ops

$$\lambda_{ij}^{(u)} N_R(p_2) \bar{\sigma}^\mu u_L^j(p_1) a_{\mu,-}(p_1, p_2, n) [u_R^i(p_3) \bar{\sigma}^\nu N_L(p_4) a_{\nu,+}(p_4, p_3, n)]^\dagger$$

$$E_R(p_2) \bar{\sigma}^\mu D_L(p_1) a_{\mu,+}(p_1, p_2, n) [D_R(p_3) \bar{\sigma}^\nu E_L(p_4) a_{\nu,-}(p_4, p_3, n)]^\dagger$$

$$N_R(p_2) \bar{\sigma}^\mu U_L(p_1) a_{\mu,-}(p_1, p_2, n) [U_R(p_3) \bar{\sigma}^\nu N_L(p_4) a_{\nu,+}(p_4, p_3, n)]^\dagger$$

$$a_\pm^\mu(p_1, p_2, n) \equiv (\Lambda_{p_1 p_2})^\mu{}_\nu \epsilon_\pm^\nu = \epsilon_2^\mu \pm i \epsilon_1^\mu = -\frac{\epsilon^\mu(p_1, p_2, n)}{|\epsilon^\mu(p_1, p_2, n)|} \pm i \frac{\epsilon^\mu(p_1, p_2, \epsilon(p_1, p_2, n))}{|\epsilon^\mu(p_1, p_2, n)| \sqrt{(p_1 \cdot p_2)^2 - p_1^2 p_2^2}}$$

$$\epsilon^\mu(p_1, p_2, n) = \epsilon^{\mu\nu\alpha\beta} p_{1\nu} p_{2\alpha} n_\beta$$

Effective Theory

$$SU(6)_{qL} \times SU(6)_{qR} \times SU(2)_{\ell L} \times SU(2)_{\ell R} \times U(1)_q \times U(1)_\ell$$



$$SU(6)_q \times SU(2)_\ell \times U(1)_q \times U(1)_\ell$$

3 Nambu-Goldstone Bosons

38 PNGBS

$$(1, 3) + (8, 1) + (8, 3)$$

Effective Theory

$$\Sigma_\ell = e^{2i\pi_\ell^a T^a}, \quad \Sigma_q = e^{2i\pi_q^a T^a}$$

$$\begin{aligned} \mathcal{L} = & \frac{f_{\ell,0}^2}{4} \text{Tr} D^\mu \Sigma_\ell^\dagger D_\mu \Sigma_\ell + \frac{f_{q,0}^2}{4} \text{Tr} D^\mu \Sigma_q^\dagger D_\mu \Sigma_q + (f_{\ell,0} \text{Tr} \Sigma_\ell \lambda^{(u)} q_L u_R + h.c.) \\ & + (a f_{\ell,0}^2 f_{q,0}^2 \text{Tr} (\Sigma_\ell \Sigma_q^\dagger) + h.c.) \end{aligned}$$

$$\Gamma(P^0 \rightarrow \gamma\gamma) \sim \frac{1}{192\pi^3} \frac{m_P^3}{f_P^2}$$

Conclusions

Monopoles are still fascinating
after all these years

monopoles can break EWS and give the
top quark a large mass

monopole phenomenology has open questions