Higgs Boson Self-Coupling Measurements Using Ratios of Cross Sections

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FG, Papaefstathiou, Yang, Zurita, 1301.3492, accepted for publication in JHEP

Outline

- Motivation
- Higgs-Pair Production Analysis
 - → Different decay channels
 - → Dissection of the cross section
 - Theoretical Errors Ratio of cross sections
 - Yariation with self coupling and top yukawa
- •Expected Constraints on Trilinear Self Coupling
- Outlook and Conclusions

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Is it the SM-Higgs Boson?

Measure further properties like its decay rates







Measuring λ using Ratios of Cross Sections

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Is it the SM-Higgs Boson?

Measure further properties like its decay rates to other SM fields

Couplings to gauge bosons and fermions

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Is it the SM-Higgs Boson?

Measure self couplings!

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Is it the SM-Higgs Boson?

Measure self couplings! test Higgs potential

$V(H) = \frac{1}{2}M_{H}^{2}H^{2} + \lambda_{HHH}vH^{3} + \frac{1}{4}\lambda_{HHHH}H^{4}$

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Measure self couplings! test Higgs potential $V(H) = \frac{1}{2}M_{H}^{2}H^{2} + \lambda_{HHH}vH^{3} + \frac{1}{4}\lambda_{HHHH}H^{4}$

Only remaining free SM parameter $M_H \simeq 125 \, \mathrm{GeV}$ measured @LHC

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$V(H) = \frac{1}{2}M_{H}^{2}H^{2} + \lambda_{HHH}vH^{3} + \frac{1}{4}\lambda_{HHHH}H^{4}$ $\lambda_{HHH}^{SM} = \lambda_{HHH}^{SM} = \lambda_{HHHH}^{SM} = \frac{M_{H}^{2}}{2v^{2}} \approx 0.13$

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 $V(H) = \frac{1}{2}M_H^2 H^2 + \lambda_{HHH}vH^3 + \frac{1}{4}\lambda_{HHHH}H^4$

 λ_{HHH} can be measured in Higgs-pair production

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Triple Higgs production -Extremeley challenging @(V)LHC-0.06 fb @ LHC14 9.45 fb @ VLHC (200 TeV) Plehn, Rauch, hep-ph/0507321

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Higgs-Pair Production Analysis

Higgs-Pair Production

• Most important production mechanism: $\mathrm{gg} \to HH$



Eboli, Marques, Novaes, Natale, PLB 197(1987)269; Glover, van der Bij, NPB 309(1988)282 Dawson, Dittmaier and M. Spira, PRD 58(1998)115012

$$\sigma(gg
ightarrow HH)_{
m LO} \sim 17\,{
m fb}$$
 14TeV LHC $_{
m M_{_H}\sim125\,GeV}$ $\sigma(gg
ightarrow HH)_{
m NLO} \sim 33\,{
m fb}$

Theoretical error (mostly scale variation): ~ 20% @NLO, large m,

recent Grigo,Hoff,Melnikov, Steinhauser,1305.7340 [1/mtⁿ corrections]

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Higgs-Pair Production

- Other production channels $qq' \rightarrow HHqq', VHH, t\bar{t}HH$
 - ~10-30 times smaller (neglect in following)



See [e.g.] Baglio, Djouadi, Grober, Muhlleitner, Quevillon, Spira, 1212.5581, and refs. therein

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Discovery potential for LHC studied in different channels



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Discovery potential for LHC studied in different channels

• Before 2008:

@600fb-1

Only $HH \rightarrow b\bar{b}\gamma\gamma$ promising (for M_H~120 GeV): S/B=6/12.5 \Rightarrow 1.5 σ Baur, Plehn, Rainwater, hep-ph/0310056

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 After 2008: Boosted jet+substructure techniques Butterworth, Davison, Rubin, Salam, 0802.2470



 $S/B=12/8 \implies 3.3 \sigma$

 $HH \rightarrow b\bar{b}W^+W^-$

Papaefstathiou, Yang, Zurita, 1209.1489

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- In $b\bar{b}\gamma\gamma$ analysis, expected LHC constraints on λ have been derived, using fits to the visible mass distribution



Optimistic assumptions for background subtraction
Need good knowledge of shapes, low number of events...

define $\lambda \equiv \lambda_{HHH} / \lambda_{HHH}^{SM}$

 $\lambda \in (0.26, 1.94) @ 600 \, \text{fb}^{-1}, \quad \lambda \in (0.54, 1.52) @ 6000 \, \text{fb}^{-1}(\text{SLHC})$

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- In promising $b\bar{b}\tau^+\tau^-$, $b\bar{b}W^+W^-$ only established these channels for discovering HH production, no limits on λ

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Higgs-Pair Production

- In the following derive expected constraints on λ for $M_{\rm H}$ ~125 GeV, using the most promising channels at the 14TeV LHC @600fb⁻¹, 3000fb⁻¹
- Relatively low number of signal events (or difficult final states), control shapes of backgrounds/signal?
 Use *total* cross section, try to reduce theoretical error
- Study dependence on y_t

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In the DM. $\alpha_q = \lambda g_q$, $\beta_q = \gamma_q =$

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In the SM: $\alpha_q = \lambda y_q$, $\beta_q = \gamma_q = y_q^2$

 $\sigma_{HH}^{\rm LO}[{\rm fb}] = 5.22\lambda^2 y_t^2 - 25.1\lambda y_t^3 + 37.3y_t^4 + \mathcal{O}(y_b y_t^2 \lambda_{HHH})$ $\sigma_{HH}^{\rm NLO}[{\rm fb}] = 9.66\lambda^2 y_t^2 - 46.9\lambda y_t^3 + 70.1y_t^4 + \mathcal{O}(y_b y_t^2 \lambda_{HHH})$

Fits obtained from hpair, http://people.web.psi.ch/spira/hpair/, $y_t \equiv y_t/y_t^{SM}$ using MSTW2008lo68cl and MSTW2008nlo68cl pdfs

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- Model dependence of analysis? Beyond consistency check of SM?
- Assume $\mathcal{L} = \mathcal{L}_{\text{SM}}$ everywhere to leading approximation besides potentially in the $(D \leq 4)$ Higgs potential and the (SM-like) Yukawa couplings, where allow for $\lambda \neq 1, y_t \neq 1$
- Realized e.g. in 2HDM, Higgs-Portal models in certain parts of parameter-space

Theoretical Errors and Ratios

- Ratio of cross sections $C_{HH} = \frac{\sigma(gg \rightarrow HH)}{\sigma(gg \rightarrow H)} \equiv \frac{\sigma_{HH}}{\sigma_{H}}$ expected to be more accurately determined theoretically than double-Higgs cross section itself A. Djouadi, 1208.3436
- Both gluon-gluon initiated and expected to feature similar higher order QCD corrections (initial state gluon radiation)
 → QCD uncertainties drop out to some extent
- Check in following

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 $\begin{array}{l} \text{used: M. Spira, hpair,} \\ \text{HIGLU, hep-ph/9510347} \\ \mu \in [0.5\mu_0, 2\mu_0] \\ \mu_0 = M_H(M_{HH}) \end{array} \text{ error due to scale variation significantly reduced in ratio} \\ \end{array}$

(similar results if $M_{HH} \rightarrow M_H$)



 $\begin{array}{l} \text{used: M. Spira, hpair,} \\ \mu_{IGLU, \text{hep-ph/9510347}} \\ \mu \in [0.5\mu_0, 2\mu_0] \\ \mu_0 = M_H(M_{HH}) \end{array} \bullet \text{Error due to scale variation significantly reduced in ratio} \\ \begin{array}{l} \Delta_{\sigma^{\text{NLO}}}^{\text{scale}} \simeq \pm 17\% \rightarrow \Delta_{C_{HH}}^{\text{scale}} \simeq \pm 1.5\% \end{array}$

(similar results if $M_{HH} \to M_H$)



 Verification that uncertainty due to the QCD corrections (partially) cancels: K-factors in the individual cross sections are large, but also very similar ~2

Central value of the ratio only decreases by small amount from LO (~1.25) to NLO (~1.0)

- Indication that higher order corrections (NNLO) are likely to change ratio by an even smaller fraction, whereas single Higgs production cross section has K-factor of ~1.5 when compared to NLO LHC Higgs Cross Section Working Group, 1101.0593
- Supports reduced size of theoretcial error found in scale variation



Combining scale variation and pdf errors in quadrature

$$\Rightarrow \Delta_{C_{HH}^{\text{NLO}}} \sim \mathcal{O}(\pm 3\%)$$

See also recent Shao, Li, Li, Wang, 1301.1245 : [threshold resummation in SCET] Grigo, Hoff, Melnikov, Steinhauser, 1305.7340 [1/mtⁿ corrections]

- To be compared with $\Delta_{\sigma_{HH}^{
 m NLO}}\simeq\pm17\%$
- Conservative assumption for the following:

$$\Delta_{C_{HH}^{\text{NLO}}} = \pm 5\%, \ \Delta_{\sigma_{HH}^{\text{NLO}}} = \pm 20\%$$

Variation with Self-Coupling and Top-Quark Yukawa



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Variation with Self-Coupling and Top-Quark Yukawa



Expected Constraints on Trilinear Self Coupling

Constraining the Self-Coupling

- Use theoretically more stable ratio of cross sections C_{\rm HH} to derive expected constraints on λ
- Furter benefit when using C_{HH}: Experimental uncertainties can also be reduced, e.g. some systematic uncertainties are expected to cancel (Luminosit uncertainty)

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Assumptions for Experimental Uncertainties

 $\sigma_{HH}^{bbxx} \equiv 2 \sigma_{HH} \times BR(b\bar{b}) \times BR(xx)$ $\sigma_{H}^{b\bar{b}} \equiv \sigma_{H} \times \mathrm{BR}(b\bar{b})$ $C_{HH}^{\text{exp.}} = \left. \frac{\sigma_{HH}^{b\bar{b}xx}}{2\,\sigma_{H}^{b\bar{b}} \times BR(xx)} \right|_{\text{exp.}}$ $\left(\frac{\Delta C_{HH}}{C_{HH}}\right)^2 = \left(\frac{\Delta \sigma_{HH}^{b\bar{b}xx}}{\sigma_{HH}^{b\bar{b}xx}}\right)^2 + \left(\frac{\Delta BR(xx)}{BR(xx)}\right)^2 + \left(\frac{\Delta \sigma_{H}^{b\bar{b}}}{\sigma_{HH}^{b\bar{b}}}\right)^2$

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Assumptions for Experimental Uncertainties



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Assumptions for Experimental Uncertainties

$$\left(\frac{\Delta C_{HH}}{C_{HH}}\right)^2 = \left(\frac{\Delta \sigma_{HH}^{b\bar{b}xx}}{\sigma_{HH}^{b\bar{b}xx}}\right)^2 + \left(\frac{\Delta BR(xx)}{BR(xx)}\right)^2 + \left(\frac{\Delta \sigma_{H}^{b\bar{b}}}{\sigma_{H}^{b\bar{b}}}\right)^2$$

 $\begin{array}{l} \Delta\sigma_{HH}^{b\bar{b}xx}/\sigma_{HH}^{b\bar{b}xx} \text{ obtained from} \\ \overline{bb\tau^+\tau^-} \ \overline{bbW^+W^-} \ \overline{bb}\gamma\gamma \\ \text{analyses via } \Delta S = \sqrt{N+B} \\ \text{after bringing channels to} \\ \text{equal footing} \end{array}$

$$\begin{split} &\Delta \sigma_H^{b\bar{b}} \sim \pm 20\% \\ &\Delta \mathrm{BR}(\tau^+\tau^-) \sim \pm 12\% \\ &\Delta \mathrm{BR}(W^+W^-) \sim \pm 12\% \\ &\Delta \mathrm{BR}(\gamma\gamma) \sim \pm 16\% \end{split}$$

"European Strategy for Particle Physics" https://indico.cern.ch/contributionDisplay.py? contribId=144&confId=175067, 2012

Assume no improvement beyond 300 fb⁻¹

Process	$S/B(600 \text{ fb}^{-1})$	$\Delta C_{HH} / C_{HH} \ (600 \ {\rm fb}^{-1})$	$\Delta C_{HH}/C_{HH} \ (3000 \ {\rm fb}^{-1})$
$b\bar{b}\tau^+\tau^-$	50/104	0.400	0.279
$b\bar{b}W^+W^-$	11.2/7.4	0.513	0.314
$b\overline{b}\gamma\gamma$	6/12.5	0.964	0.490

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SM.

- We now want to use C_{HH} to constrain the parameters {p_i} of a model
- Expected exclusion in parameter-space depends on true parameters of the model

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Deriving Constraints – General Strategy

- Calculate C_{HH} as a function of the set of parameters {p_i}
 (e.g. new couplings/Wilson coefficients, masses) as well as theoretical error
- Estimate expected experimental errors arising from measurements of components that comprise $C_{HH}^{\rm exp.}$

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Deriving Constraints – General Strategy

- Calculate C_{HH} as a function of the set of parameters {p_i}
 (e.g. new couplings/Wilson coefficients, masses) as well as theoretical error
- Estimate expected experimental errors arising from measurements of components that comprise $C_{HH}^{\rm exp.}$
- Question to address: Given an assumption for the 'true' values of the model parameters, what is the constraint we *expect* to impose on the parameters through Higgs-pair production?

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- In the following: simplified framework $\{p_i\} = \{\lambda, y_t\}$
- Start with assuming $y_t = y_{t,true} = 1$
- Draw curves of λ that lead to a theoretically predicted cross section of one or two standard deviations away from the true cross section, derived with the underlying true λ_{true}
- In the following focus on $\lambda \in (-1.0, \lambda_{min} \sim 2.5)$

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Expect to exclude values outside regions at 1 σ (2 σ)

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Process	$600 \text{ fb}^{-1} (2\sigma)$	$600 \text{ fb}^{-1} (1\sigma)$	$3000 {\rm ~fb^{-1}} {\rm ~} 2\sigma$	$3000 {\rm ~fb^{-1}} {\rm ~1}\sigma$
$b\bar{b}\tau^+\tau^-$	(0.22, 4.70)	(0.57,1.64)	(0.42,2.13)	(0.69, 1.40)
$b\overline{b}W^+W^-$	(0.04, 4.88)	(0.46,1.95)	(0.36, 4.56)	(0.65, 1.46)
$b\overline{b}\gamma\gamma$	(-0.56, 5.48)	(0.09, 4.83)	(0.08, 4.84)	(0.48, 1.87)
assume λ_{i}	$-\eta = -1$ for d	isconnected regio	ns only show be	$\alpha_{\rm W} \lambda \cdot \sim 2.43$

- Possible to constrain trilinear self coupling to be positive at 95% CL with 600fb⁻¹ using C_{нн}
- Comparable for $b\bar{b}\gamma\gamma$ to shape analysis $\lambda \in (0.26, 1.94) @ 600 \, {\rm fb}^{-1}$ Baur, Plehn, Rainwater, hep-ph/0310056

actually also $\lambda \in (2.98, 4.66),$ optimistic asmpt

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- Comparable for $b\bar{b}\gamma\gamma$ to shape analysis $\lambda \in (0.26, 1.94) @ 600 \, {\rm fb}^{-1}$ Baur, Plehn, Rainwater, hep-ph/0310056
- Improve predictions due to new channels
- Combination of channels yields ~ +30% and ~ -20% accuracy with 3000fb⁻¹

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Measuring λ using Ratios of Cross Sections

actually also

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assume $\lambda_{true} = u_{t,true} = 1$, for disconnected regions only show below $\lambda_{min} \simeq 2.43$.				

- Combination of channels yields ~ +30% and ~ -20% accuracy with 3000fb⁻¹
- Compare to ILC ILC-TDR (2012, to be published) $\sqrt{s} = 500 \text{ GeV}, \quad \mathcal{L} = 2000 \text{ fb}^{-1} \text{ ~40\%}$ $\sqrt{s} = 1000 \text{ GeV}, \quad \mathcal{L} = 1000 \text{ fb}^{-1} \text{ ~25\%}$

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Outlook and Conclusions

Outlook

- Do full "model independent" survey of double Higgs production, supplementing the SM Lagrangian with dimension 6 operators
- Use equations of motion to arrive at most appropriate basis for the analysis

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Outlook

- Employ precision constraints to further reduce the operator basis
- Use information from single Higgs production to constrain operators and derive expectations for double-Higgs production
- Study different scenarios

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Conclusions

- Examined theoretical error on ratio of dobule-tosingle Higgs production cross section C_{HH}
- Using this ratio, derived expected exclusions on the trilinear H coupling in the $b\bar{b}\gamma\gamma$, $b\bar{b}W^+W^-$, $b\bar{b}\tau^+\tau^-$ channels
- Obtained the most precise expected determination of the Higgs trilinear self-coupling at the 14TeV LHC: -20/+30% achievable (in the SM)
- Good knowledge of top-quark yukawa important
- Outlook: Full operator analysis of HH production

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Thank you for the attention!