



NNLO results for $V+j$ at the LHC using N-jettiness

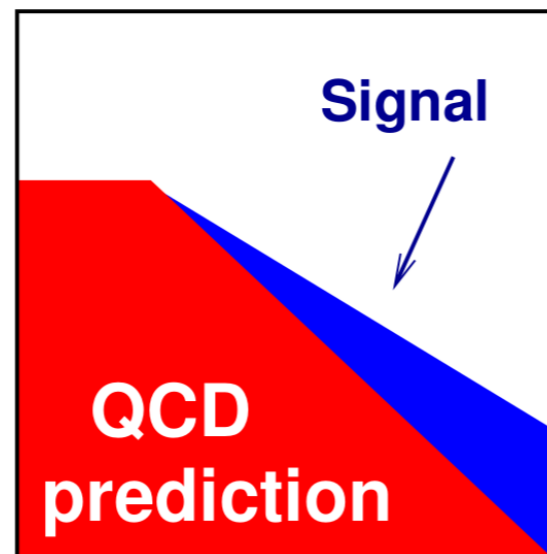
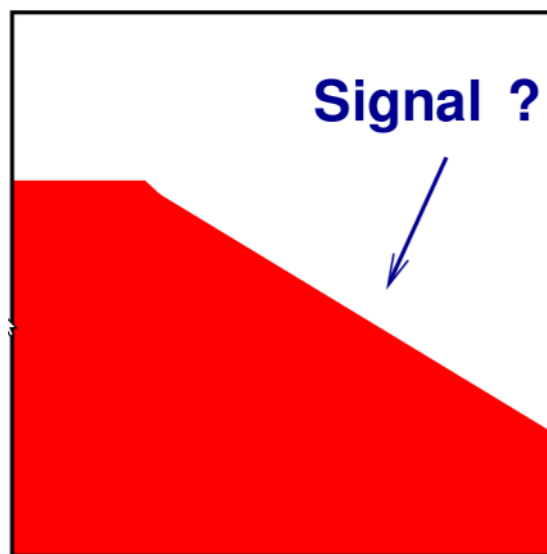
Xiaohui Liu

KITP, 2016

Why V+1j

- SUSY, dark matter mono jet search Background

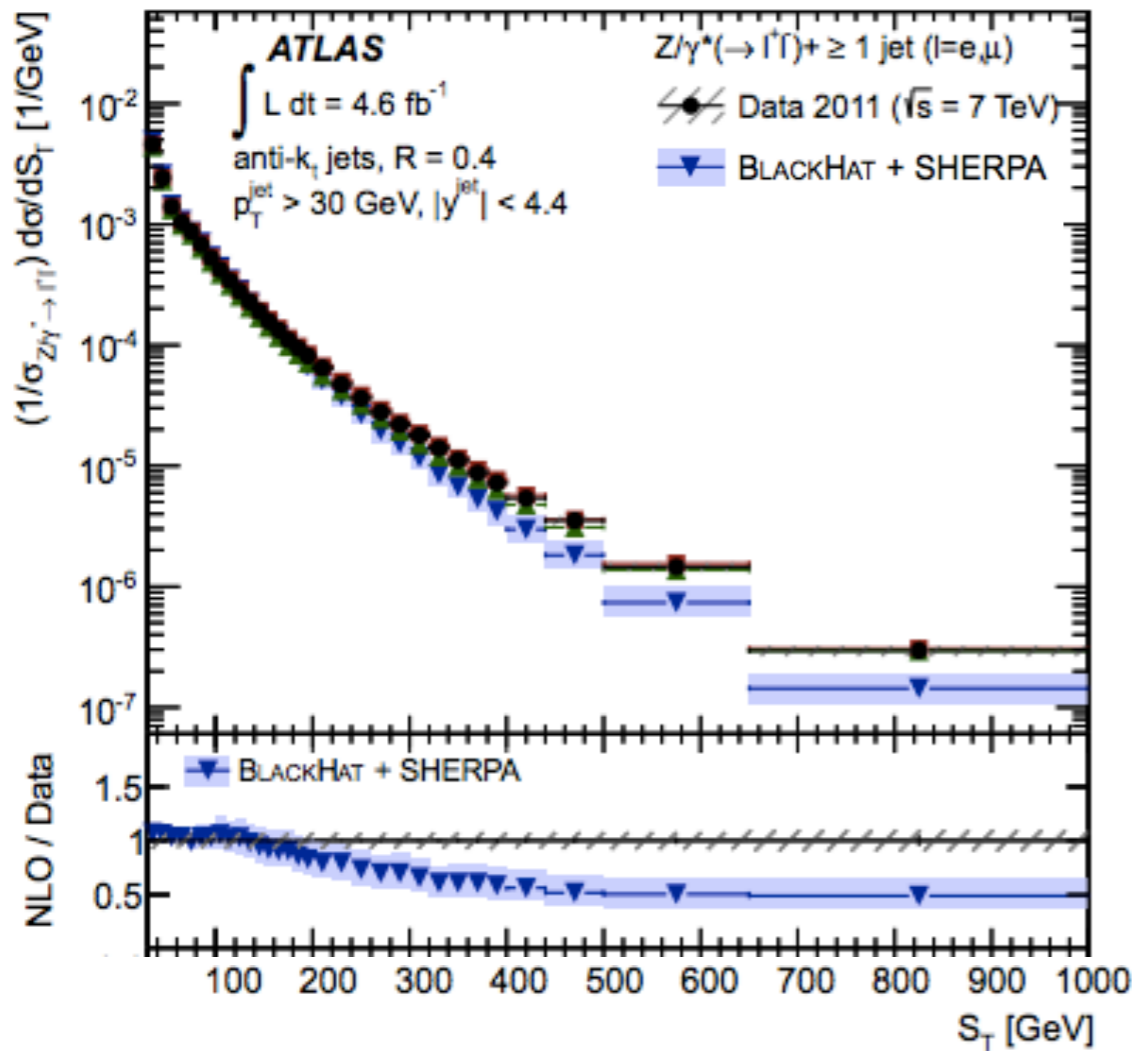
| Background process | Method |
|--|--------------------------------|
| $Z(\rightarrow \nu\bar{\nu})+\text{jets}$ | MC and control samples in data |
| $W(\rightarrow e\nu)+\text{jets}$ | MC and control samples in data |
| $W(\rightarrow \tau\nu)+\text{jets}$ | MC and control samples in data |
| $W(\rightarrow \mu\nu)+\text{jets}$ | MC and control samples in data |
| $Z/\gamma^*(\rightarrow \ell^+\ell^-)+\text{jets}$ ($\ell = e, \mu, \tau$) | MC-only |
| $t\bar{t}$, single top | MC-only |
| Diboson | MC-only |
| Multijets | data-driven |
| Non-collision | data-driven |



- No resonance, only see excess in the data
- Predicting the shape correctly is crucial

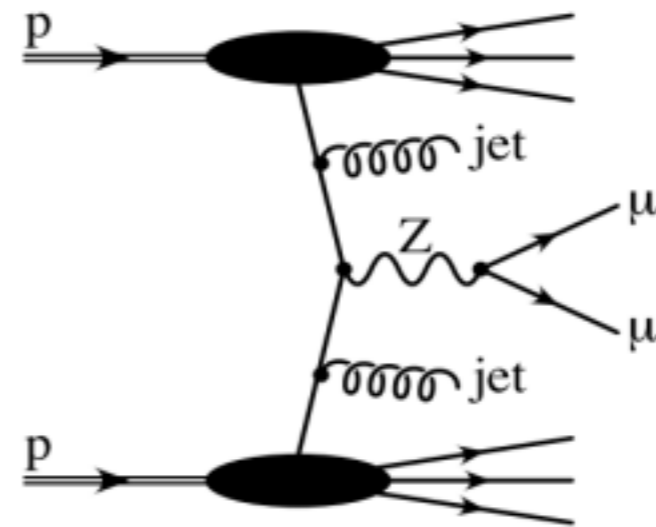
Why V+1j

- Precise experimental measurements



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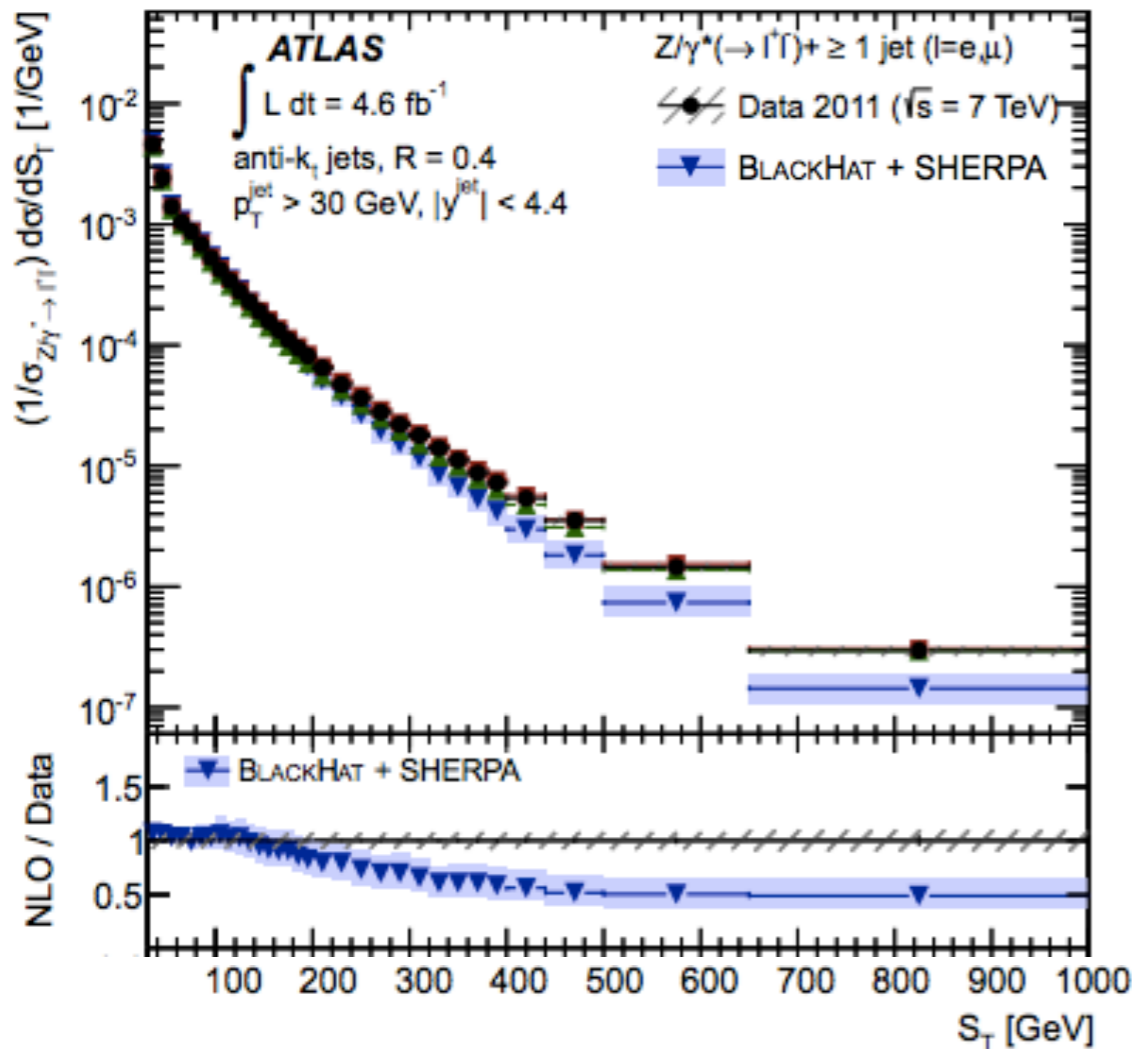
clean signature



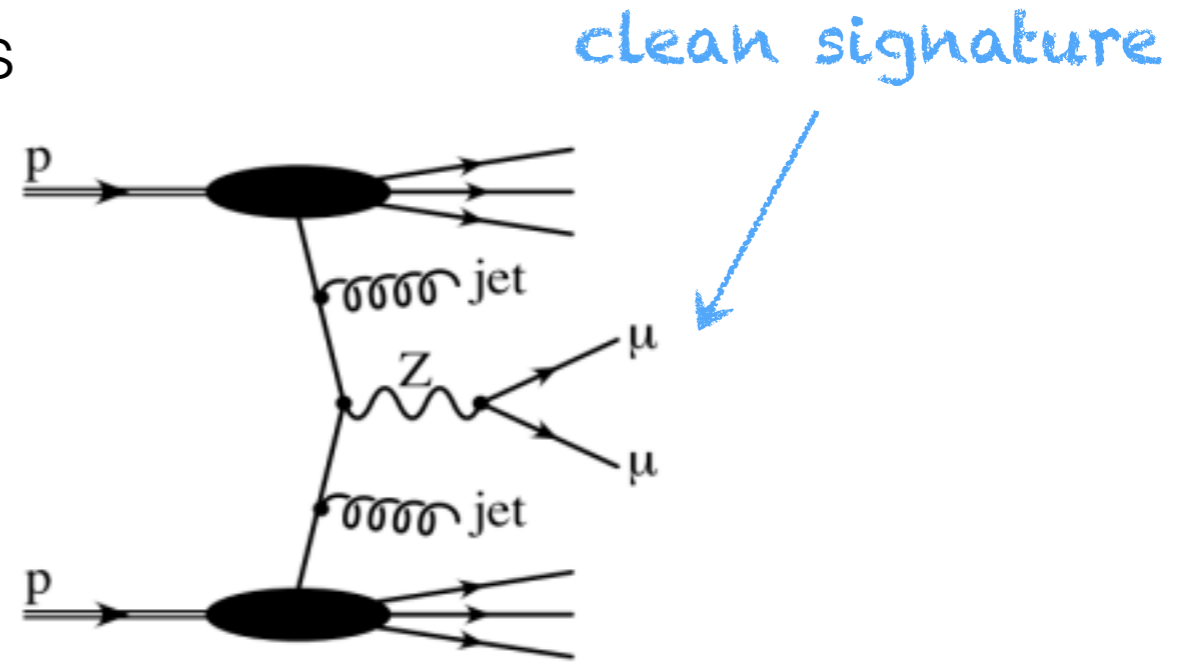
- Uncertainty $\sim \pm 10\%$ up to TeV scale

Why V+1j

- Precise experimental measurements



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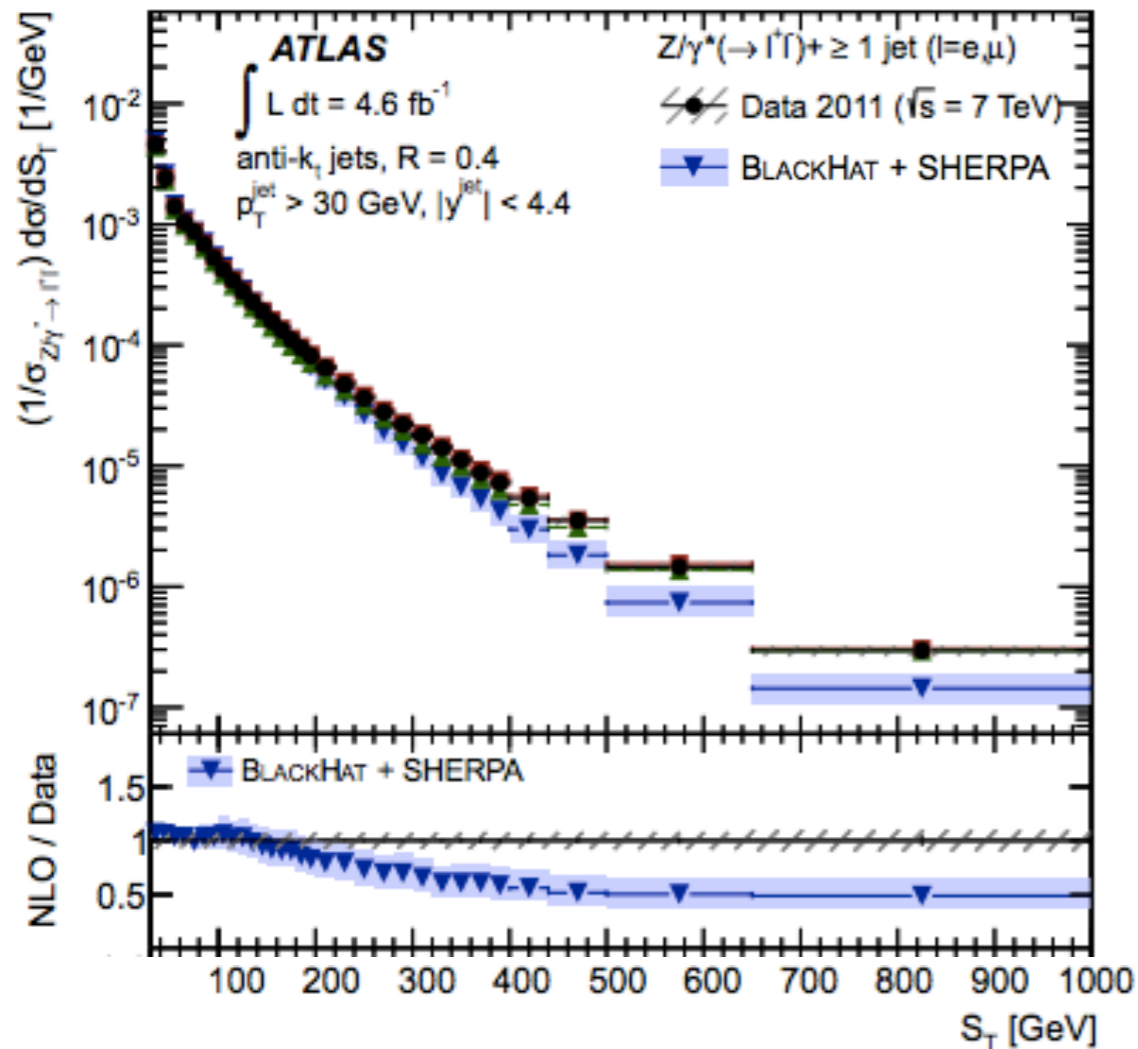


- Uncertainty $\sim \pm 10\%$ up to TeV scale
- Standard candle at the LHC
- Jet energy scale calibration [CERN-PH-EP-2013-222](https://arxiv.org/abs/1307.7132)
- Precision test/measurements of QCD
- constrain PDFs

require high-precision predictions!

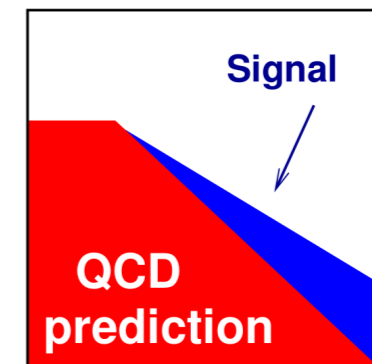
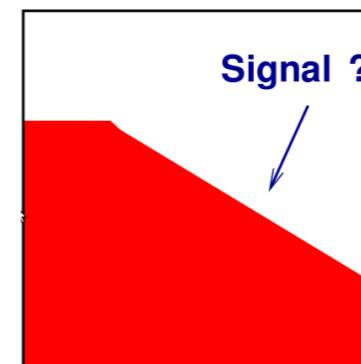
Theory Status

- NLO prediction



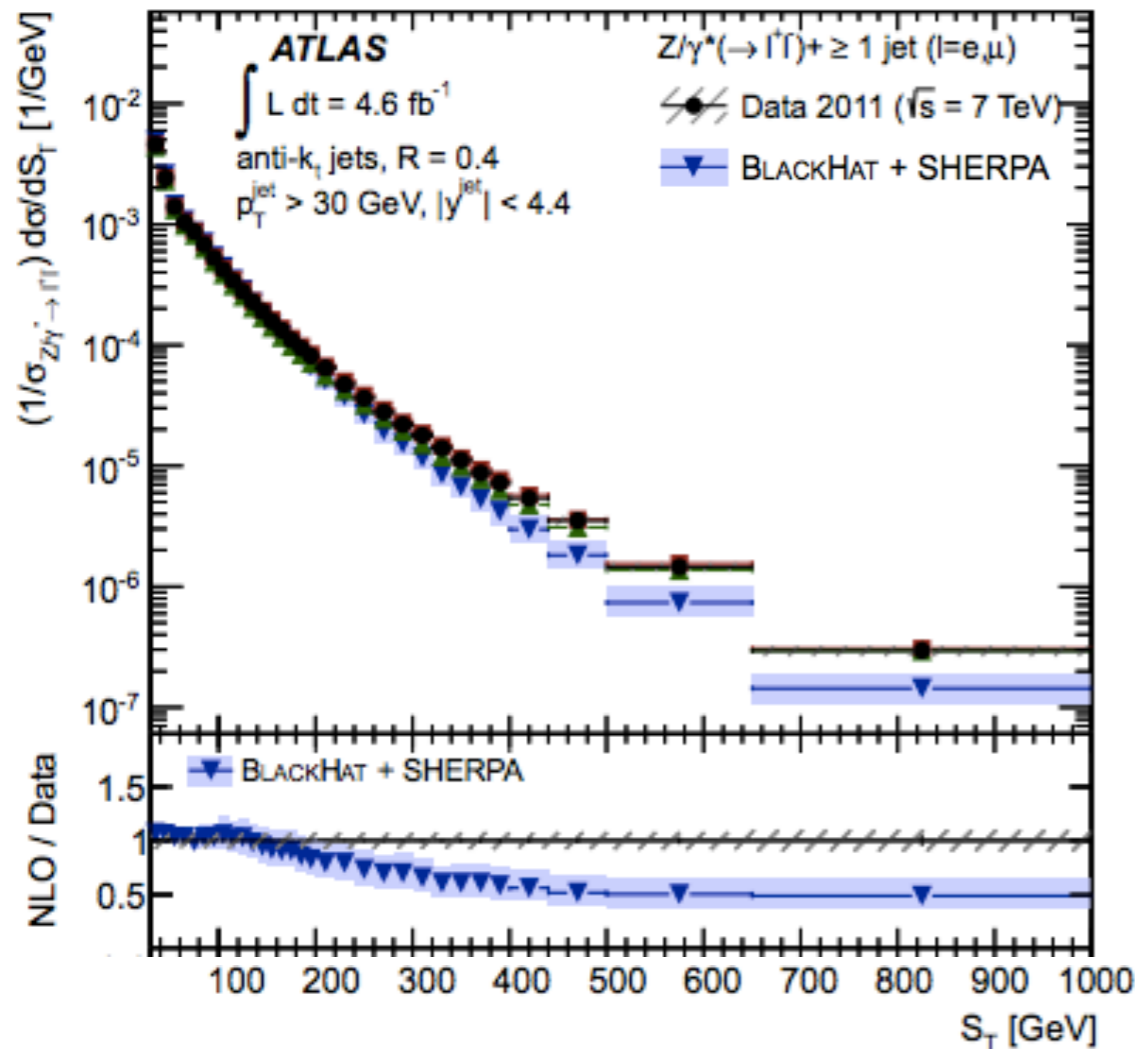
CERN-PH-EP-2013-023

- QCD NLO underestimates the data by 50% at large S_T



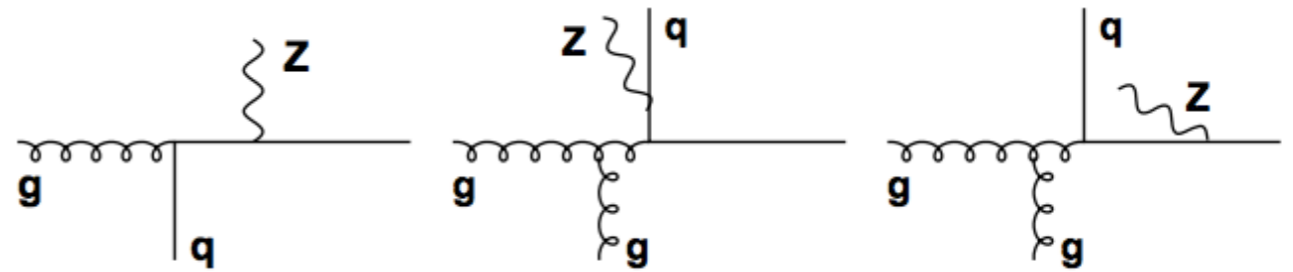
Theory Status

- NLO prediction

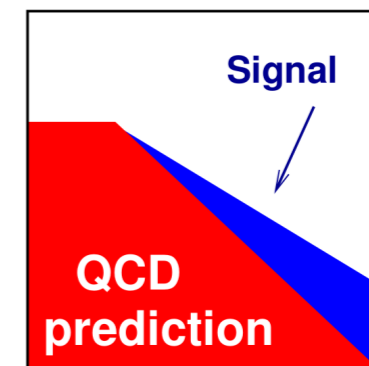
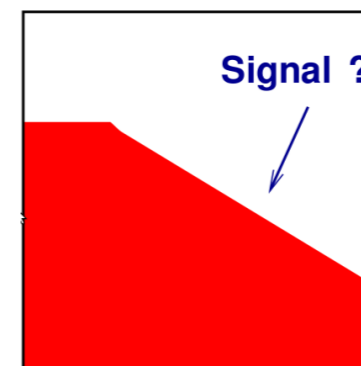


CERN-PH-EP-2013-023

- QCD NLO underestimates the data by 50% at large S_T



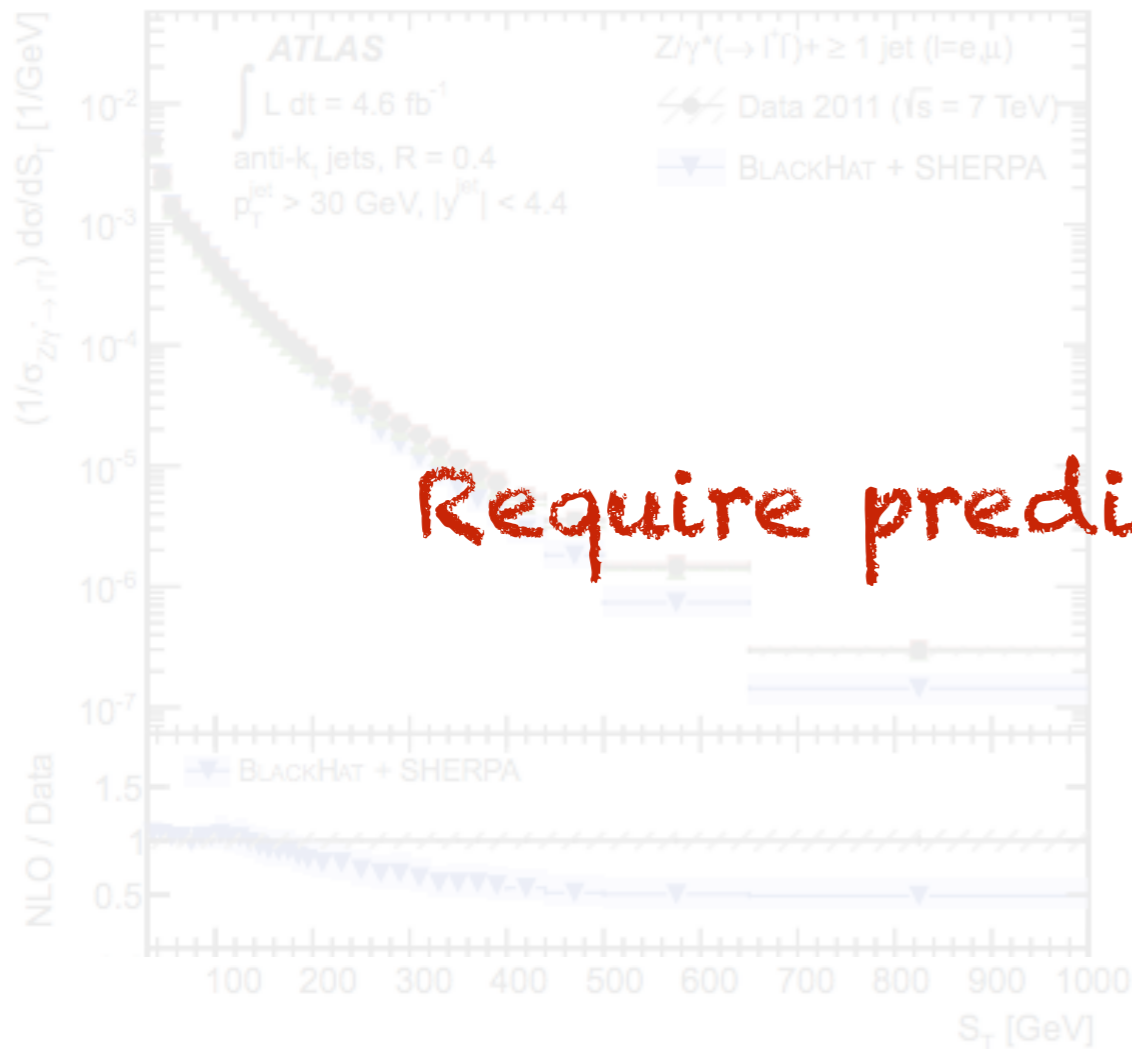
New channels open up at higher orders allow for a soft/collinear Z



Rubin, Salam, Sapeta, '10

Theory Status

- NLO prediction

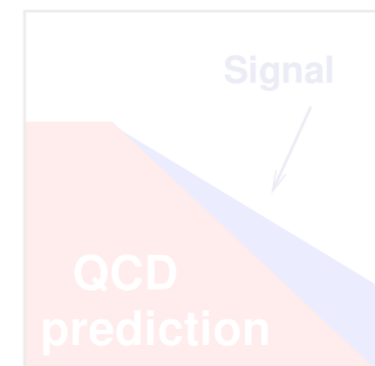
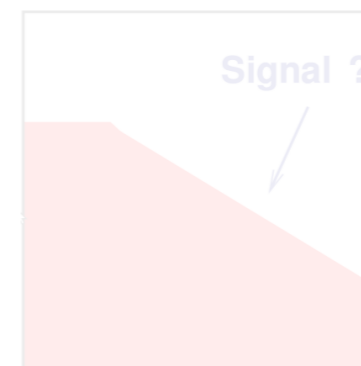


Require predictions from the NNLO

- QCD NLO underestimates the data by 50% at large S_T



New channels open up at higher orders allow for a soft/collinear Z



CERN-PH-EP-2013-023

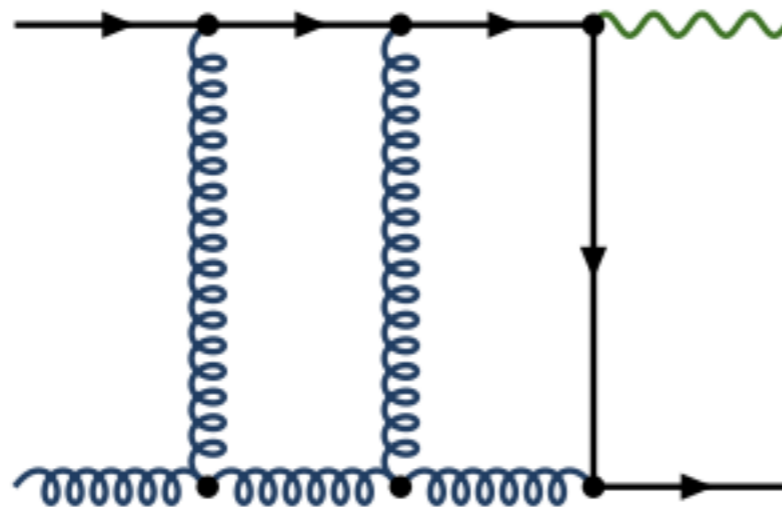
Outline

- Theory Setups
 - N-jettiness subtraction
- NNLO $V + 1\text{jet}$ at the LHC
- Conclusion

Theory Setups

- Virtual corrections
 - Explicit IR poles
 - Known to 2-loop analytically

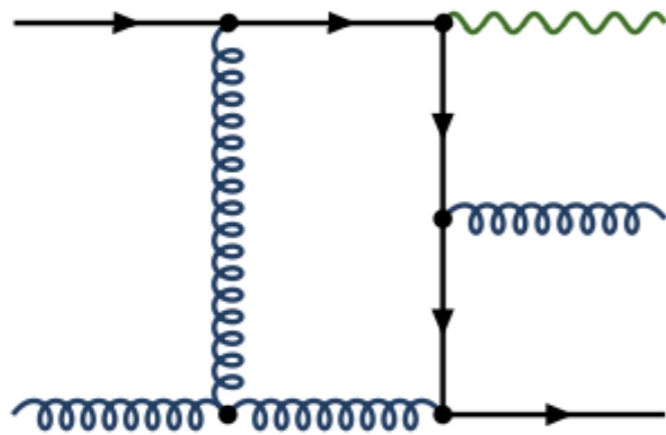
Moch, Uwer, Weinzierl, '02; Garland, Gehrmann, Glover, Koukoutsakis, Remiddi, '02; Gehrmann, Tancredi, '12



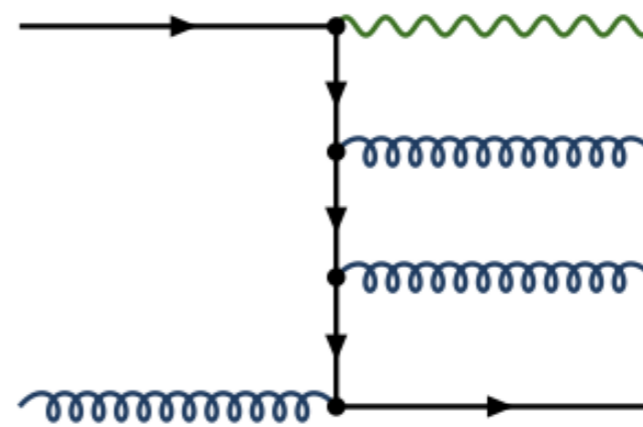
$$\int d\Phi_2 \sum_{i=0}^4 \frac{v v_i}{\epsilon^i}$$

Theory Setups

- Real corrections
- Implicit IR poles



$$\int d\Phi_3 \sum_{i=0}^2 \frac{vr_i}{\epsilon^i}$$



$$\int d\Phi_4 rr$$

IR poles fully show up only after integrating over phase space for degenerate (soft/collinear) states

Theory Setups

- Real corrections
- Various methods proposed to extract implicit IR poles
 - Sector decomposition, Sector-improved residues
Binoth, Heinrich; Anastasiou, Melnikov, Petriello Czakon; Boughezal, Melnikov, Petriello
 - Antenna subtraction Kosower Gehrmann-De Ridder, Gehrmann, Glover
 - q_T subtraction, N-Jettiness subtraction
Catani, Grazzini Boughezal, Focke, XL, Petriello; Gaunt, Stahlhofen, Tackmann, Walsh
 - Projection to Born process Cacciari, Dreyer, Karlberg, Salam, Zanderighi
 - CoLorFul NNLO Del Duca, Somogyi and Trócsányi Del Duca, Duhr, Kardos, Somogyi and Trócsányi

Theory Setups

- N-Jettiness subtraction Boughezal, Focke, XL, Petriello, '15 Gaunt, Stahlhofen, Tackmann, Walsh, '15
- N-jettiness observable Stewart, Tackmann, Waalewijn, '10

$$\mathcal{T}_N = \sum_k \min \{w_a n_a \cdot q_k, w_b n_b \cdot q_k, w_i n_i \cdot q_k, \dots, w_N n_N \cdot q_k\}$$

N the minimum number of jets required

n_i light-like vectors along beam or jet axes

q_k final state partons' 4-momenta

w_k arbitrary positive weight

Theory Setups

- N-Jettiness subtraction

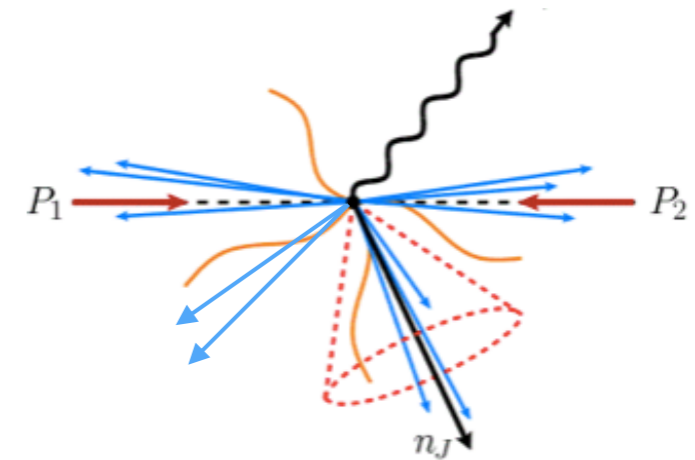
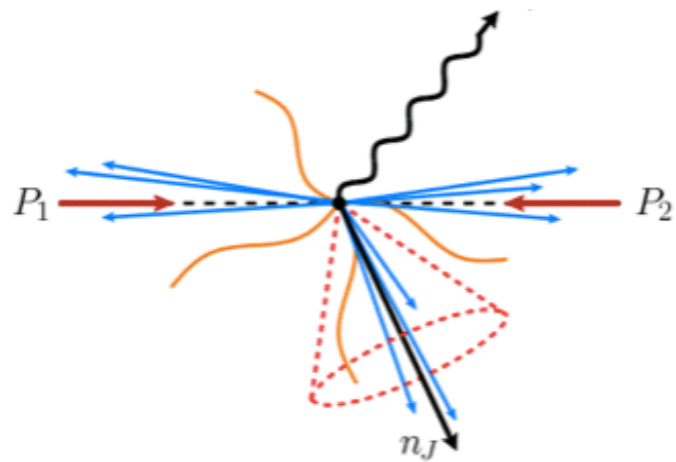
Boughezal, Focke, XL, Petriello, '15 Gaunt, Stahlhofen, Tackmann, Walsh, '15

$$\mathcal{T}_N = \sum_k \min \{ w_a n_a \cdot q_k, w_b n_b \cdot q_k, w_i n_i \cdot q_k, \dots, w_N n_N \cdot q_k \}$$

N jets ← **small** \mathcal{T}_N → **large** **more than N jets**

- Contribution only from 2-loop, soft+collinear radiations

- At least N+1 hard radiations



Theory Setups

- N-Jettiness subtraction

Boughezal, Focke, XL, Petriello, '15 Gaunt, Stahlhofen, Tackmann, Walsh, '15

$$\mathcal{T}_N = \sum_k \min \{ w_a n_a \cdot q_k, w_b n_b \cdot q_k, w_i n_i \cdot q_k, \dots, w_N n_N \cdot q_k \}$$

N jets

← small

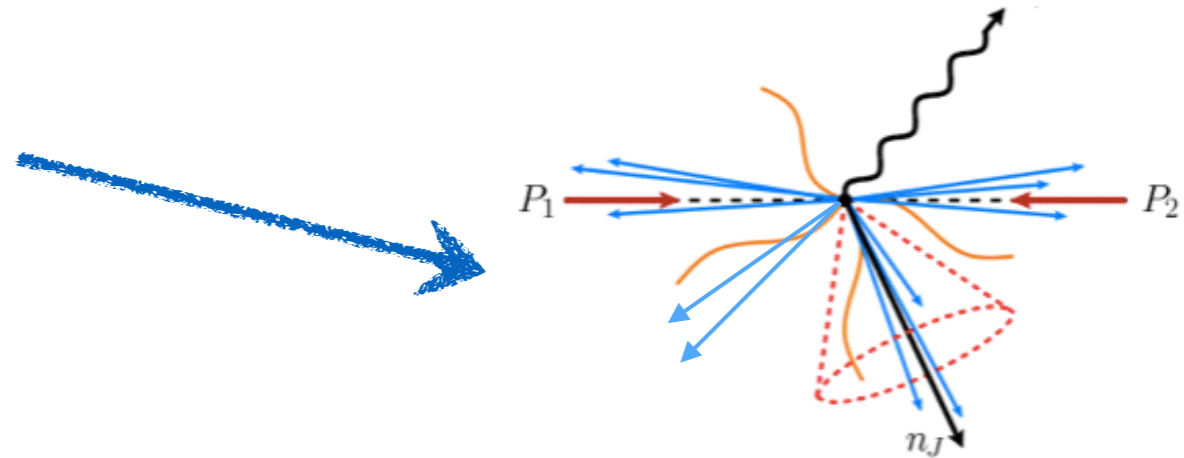
\mathcal{T}_N

→ large

more than N jets

- At least N+1 hard radiations

- NLO N+1 jet calculation
- Simply recycle known NLO results/tools



Theory Setups

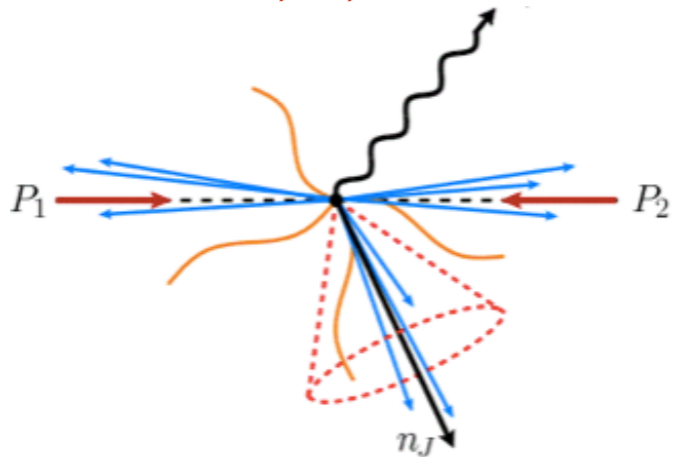
- N-Jettiness subtraction

Boughezal, Focke, XL, Petriello, '15 Gaunt, Stahlhofen, Tackmann, Walsh, '15

$$\mathcal{T}_N = \sum_k \min \{ w_a n_a \cdot q_k, w_b n_b \cdot q_k, w_i n_i \cdot q_k, \dots, w_N n_N \cdot q_k \}$$

N jets ← small \mathcal{T}_N → large **more than N jets**

- Contribution only from 2-loop, soft+collinear radiations



$$\text{Tr}[H \cdot S_N] \otimes B_a \otimes B_b \otimes J_i + \dots$$

Stewart, Tackmann, Waalewijn, '10

- simple calculation based on factorization theorem
- all components known to 2-loop
- most of them are universal, re-usable for other process
- power corrections vanish as $\mathcal{T}_N \rightarrow 0$

jet: Becher and Neubert, '06, Becher and Bell, '10

beam: Gaunt, Stahlhofen, Tackmann, '14

soft: Boughezal, XL and Petriello, '15

Theory Setups

- N-Jettiness subtraction

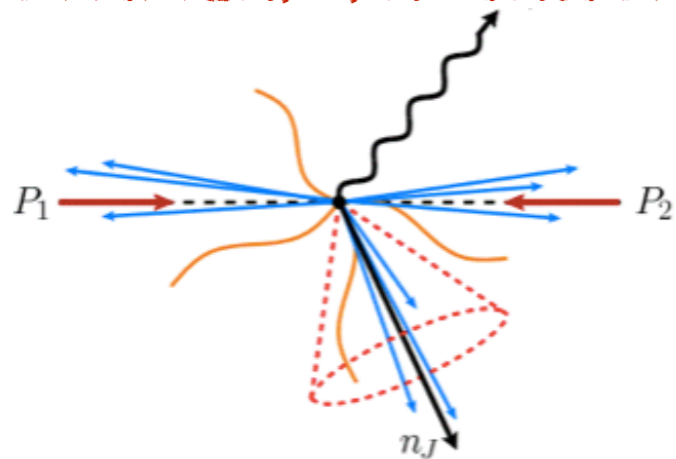
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$$\mathcal{T}_N = \sum_k \min \{ w_a n_a \cdot q_k, w_b n_b \cdot q_k, w_i n_i \cdot q_k, \dots, w_N n_N \cdot q_k \}$$

N jets ← small \mathcal{T}_N large → more than N jets

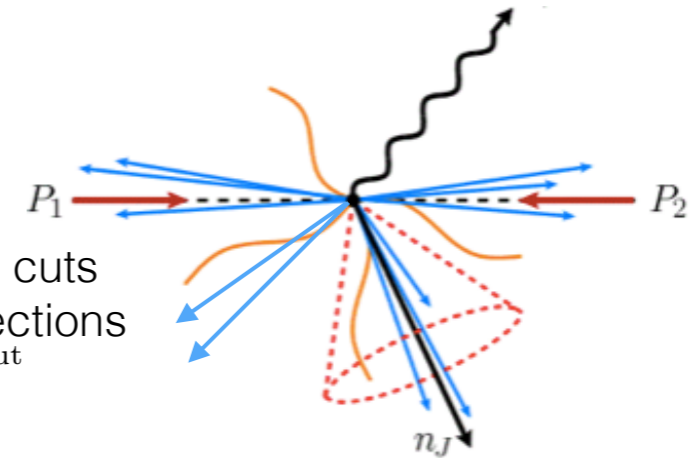
- Contribution only from 2-loop, soft+collinear radiations

- At least N+1 hard radiations



small $\mathcal{T}_N^{\text{cut}}$

smaller than any experimental cuts
small to suppress power corrections
final result independent of $\mathcal{T}_N^{\text{cut}}$



- NLO N+1 jet calculation
- Simply recycle known NLO results/tools

$$\text{Tr}[H \cdot S_N] \otimes B_a \otimes B_b \otimes J_i + \dots$$

Theory Setups

- N-Jettiness subtraction Boughezal, Focke, XL, Petriello, '15 Gaunt, Stahlhofen, Tackmann, Walsh, '15
- Successfully used to provide new results for processes with a jet
 - H/W/Z+1j Boughezal, Focke, XL, Petriello, '15,
Boughezal, Focke, Giele, XL, Petriello, '15
Boughezal, Campbell, Ellis, Focke, Giele, XL, Petriello, '15,
- Successfully used to confirm (and correct) existing results
- H/W/Z production Gaunt, Stahlhofen, Tackmann, Walsh, '15
- VH/Di-photon production Campbell, Ellis, Williams, '16 Campbell, Ellis, Li, Williams, '16

Validation and power correction

- N-Jettiness subtraction Boughezal, Focke, XL, Petriello, '15 Gaunt, Stahlhofen, Tackmann, Walsh, '15
 - Successfully used to provide new results for processes with a jet
 - Successfully used to confirm (and correct) existing results

Validations

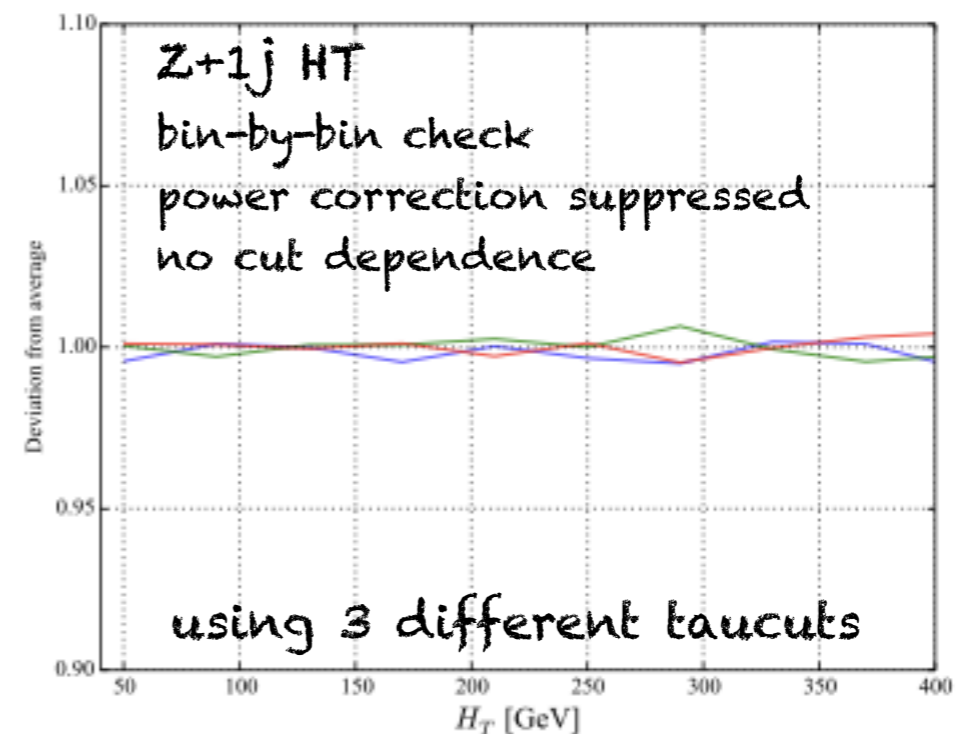
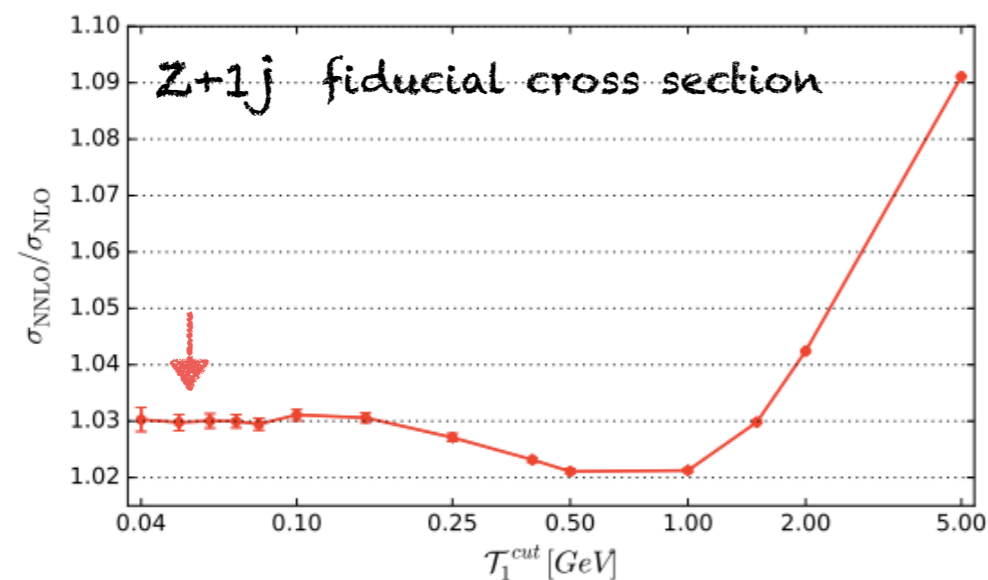
- H+1j agrees with the one using Sector-improved residues method Boughezal, Caola, Melnikov, Petriello, Schulze, '13 '15
- Reproduced existing results (VH by Campbell, et al, '16 inclusive H/W/Z by Gaunt, et al, '15)
- di-photon production using jettiness-subtraction [Campbell, et al, '16] corrected existing results by qT-subtraction for di-photon production [Catani, et al, '11]

Validation and power correction

- N-Jettiness subtraction Boughezal, Focke, XL, Petriello, '15 Gaunt, Stahlhofen, Tackmann, Walsh, '15
 - Successfully used to provide new results for processes with a jet
 - Successfully used to confirm (and correct) existing results

Validations

- τ cut-independence check in all calculations



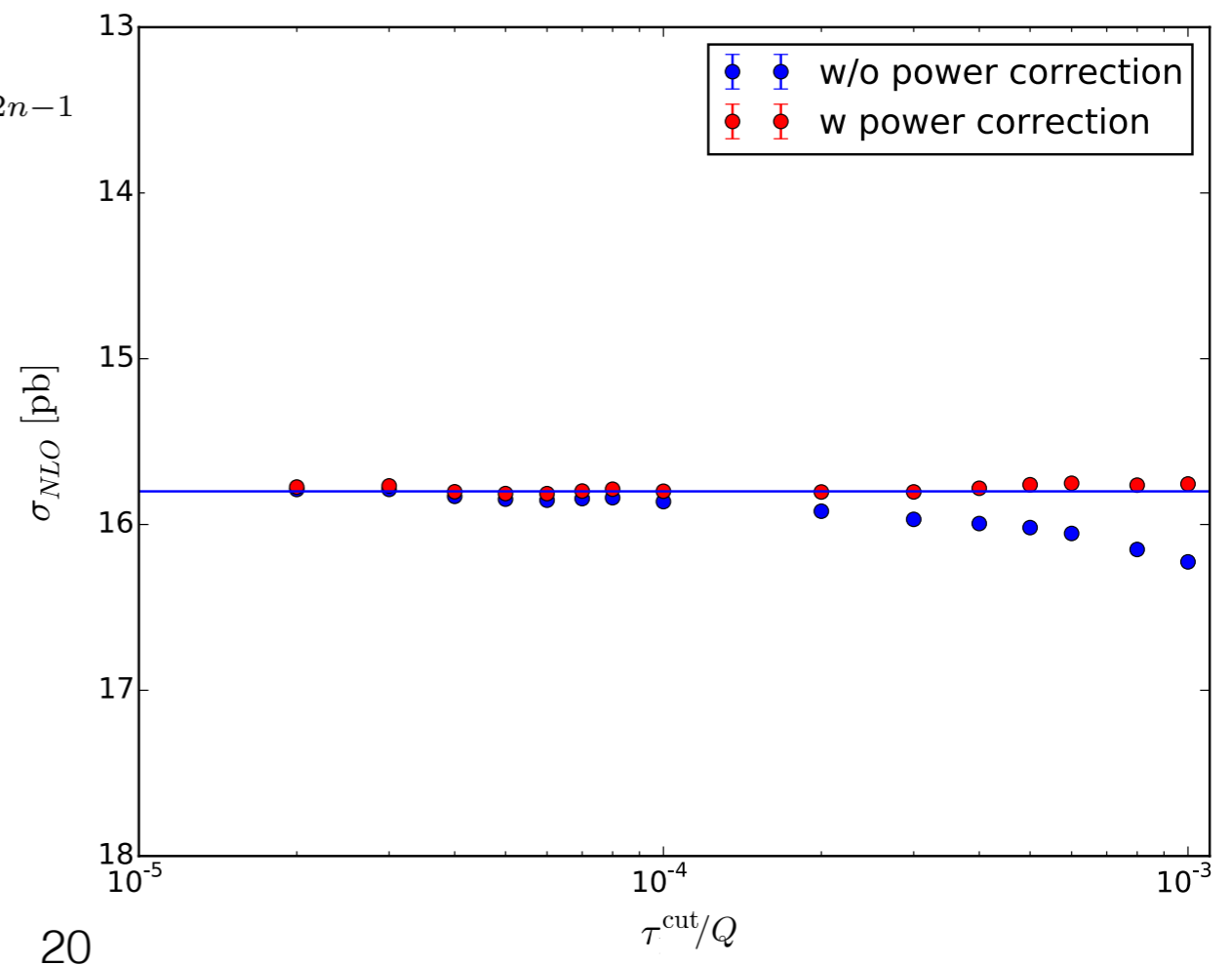
Validation and power correction

- N-Jettiness subtraction Boughezal, Focke, XL, Petriello, '15 Gaunt, Stahlhofen, Tackmann, Walsh, '15
 - Successfully used to provide new results for processes with a jet
 - Successfully used to confirm (and correct) existing results

power corrections

- logarithmic nature of dominant power corrections
- can be calculated in an easy way and higher order power corrections can be predicted from lower order calculations
- including power corrections can improve the convergence

$$\alpha_s^n C_n \mathcal{T}_N^{\text{cut}} L^{2n-1}$$



V+1j at the LHC

- Comparison with 7TeV data
- W+1j

Boughezal, XL, Petriello, '16

| W-boson cuts | ATLAS [10] | CMS [11] |
|--------------------|-----------------------|------------------|
| lepton p_T | $p_T^l > 25$ GeV | $p_T^l > 25$ GeV |
| lepton η | $ \eta^l < 2.5$ | $ \eta^l < 2.1$ |
| missing E_T | $E_T^{miss} > 25$ GeV | – |
| transverse mass | $m_T > 40$ GeV | $m_T > 50$ GeV |
| jet p_T | $p_T^J > 30$ GeV | $p_T^J > 30$ GeV |
| jet η | $ \eta^J < 4.4$ | $ \eta^J < 2.4$ |
| anti- k_T radius | $R = 0.4$ | $R = 0.5$ |

CERN-PH-EP-2014-199

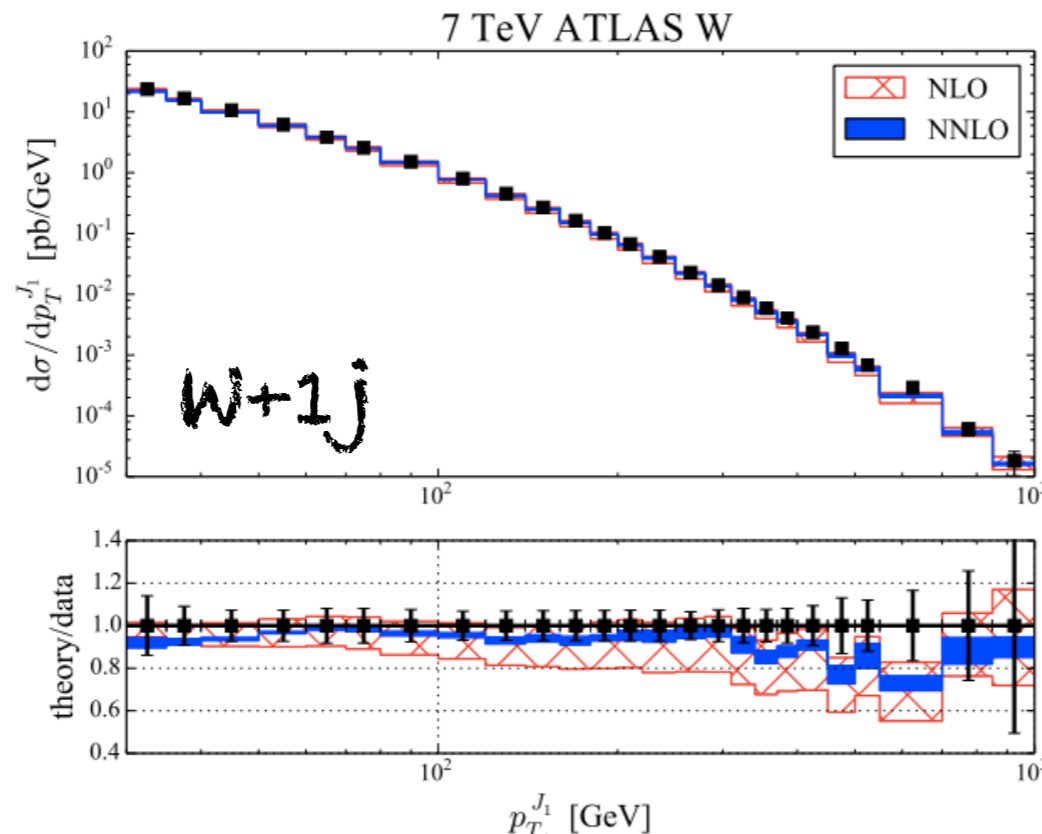
CERN-PH-EP-2014-134

$$\mu_0 = \sqrt{M_V^2 + \sum_i (p_T^{J_i})^2}$$

- CT14NNLO PDFs for NNLO results, CT14NLO for NLO results
- Vary μ_F and μ_R independently
- non-perturbative corrections included for ATLAS p_{TJ} and y_J
- QED FSR factors included for ATLAS p_{TJ} and y_J

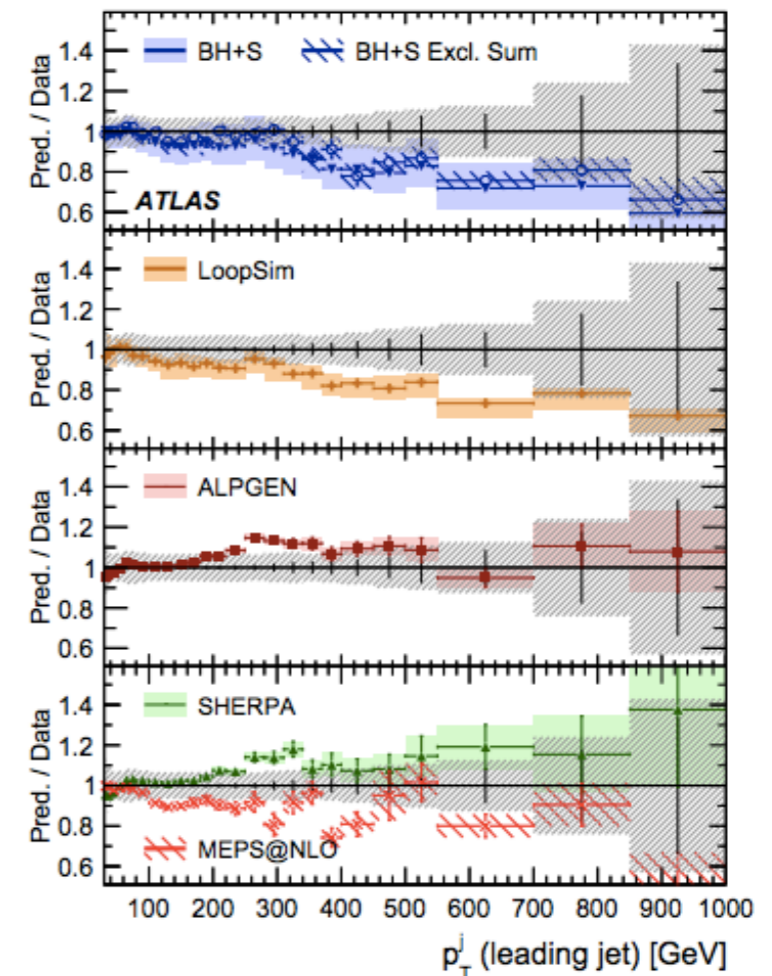
V+1j at the LHC

- Comparison with 7TeV data Boughezal, XL, Petriello, '16



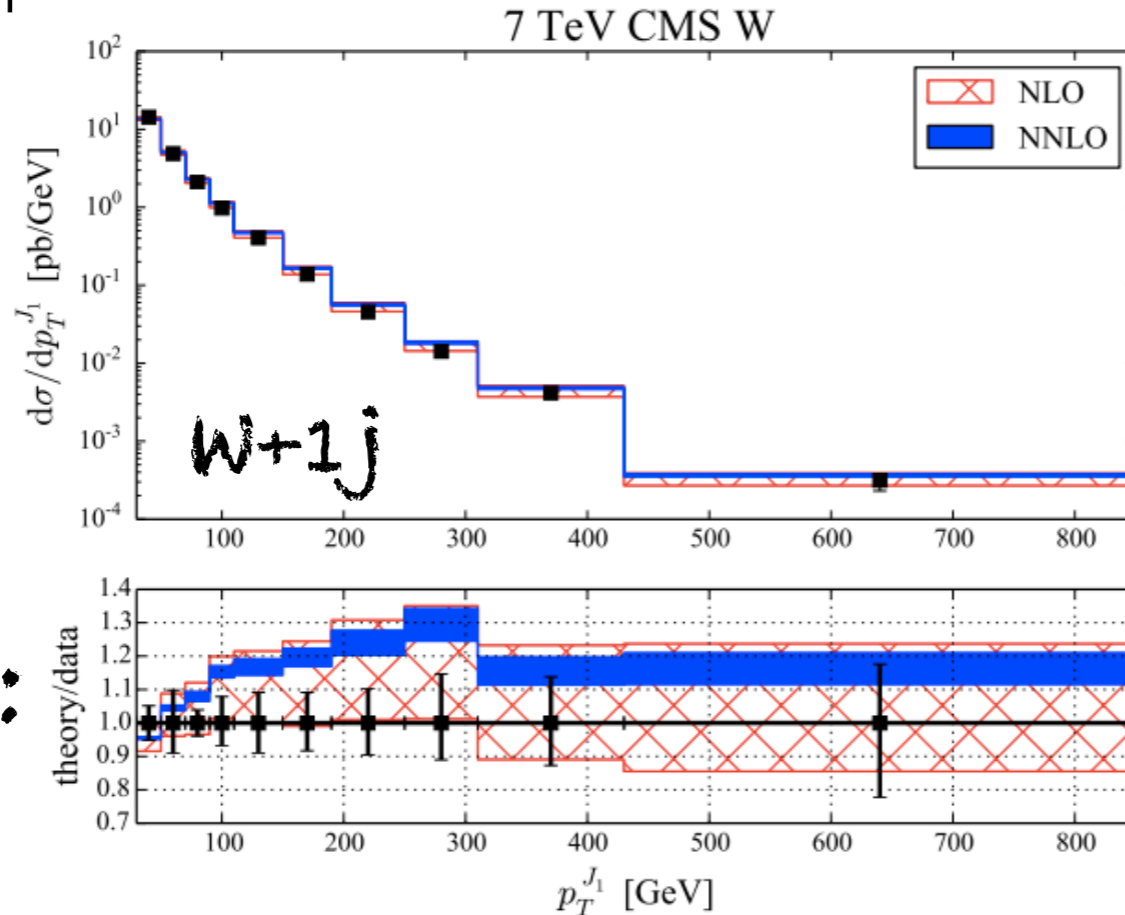
p_{T}^{J1} :

- Merged tree-level amplitudes combined with a parton shower describe the measurements: higher than but within experimental errors
- NLO QCD, LoopSim and MEPS@NLO predictions are all lower than the data.
- NNLO QCD corrections increase the NLO prediction, leading to a better agreement with ATLAS data. Scale uncertainty is reduced

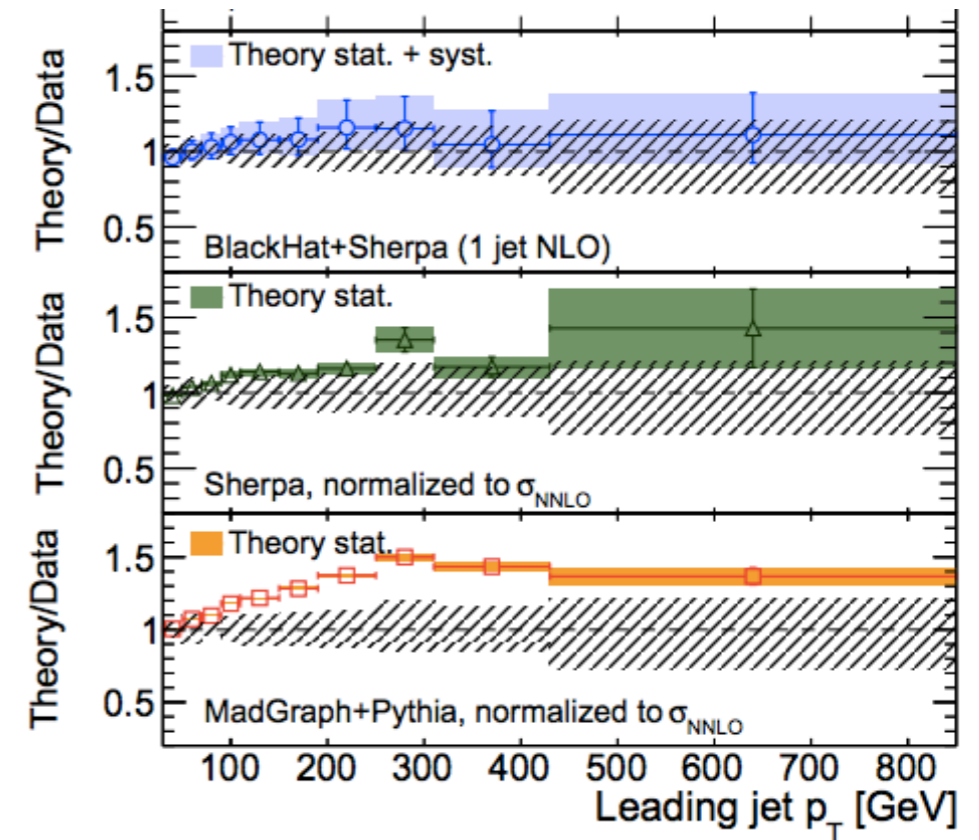


V+1j at the LHC

- Comparison with 7TeV data Boughezal, XL, Petriello, '16

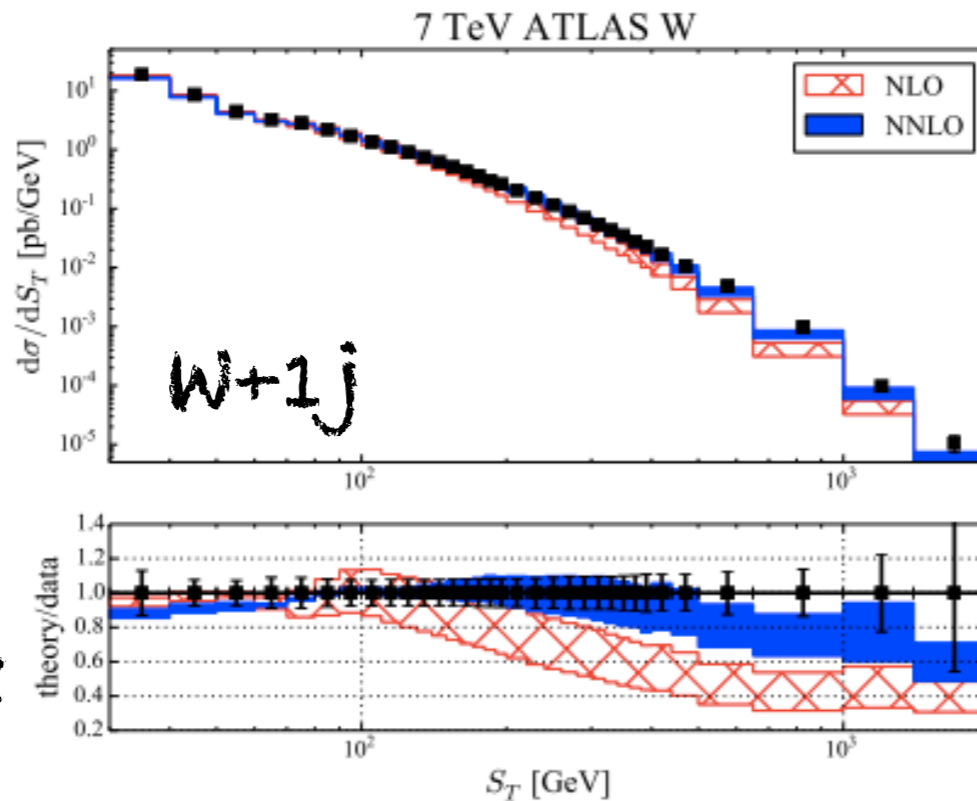


- All predictions compared are systematically higher than the CMS data
- NNLO QCD corrections reduce the NLO scale uncertainty to make it clear



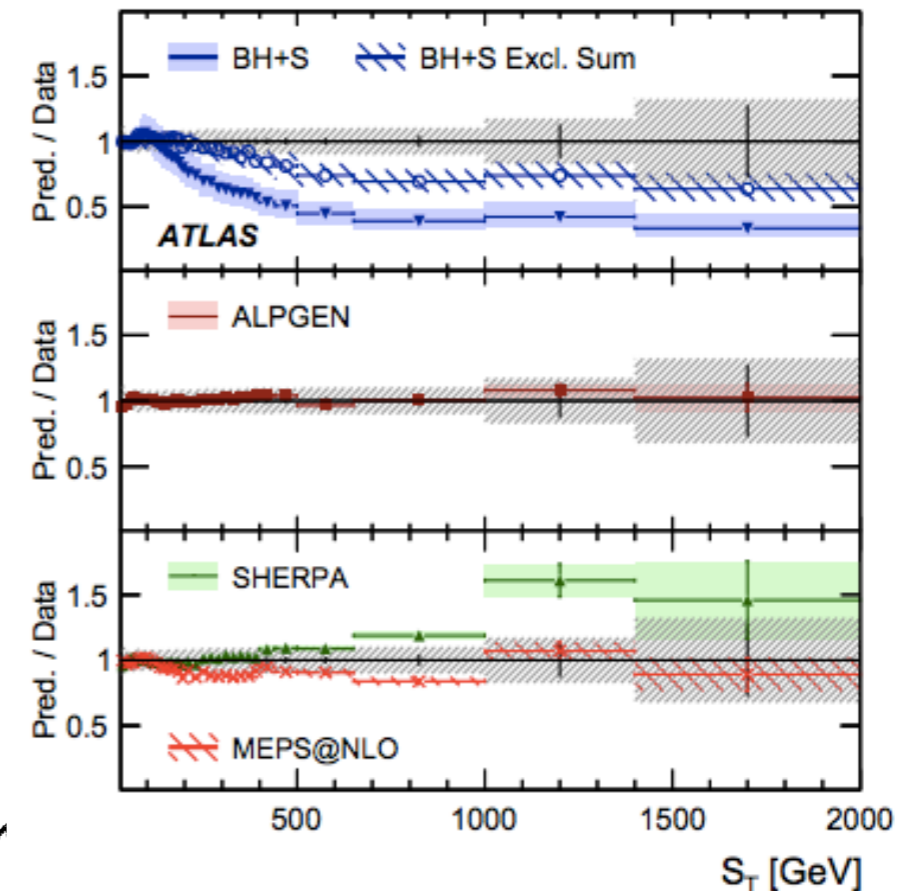
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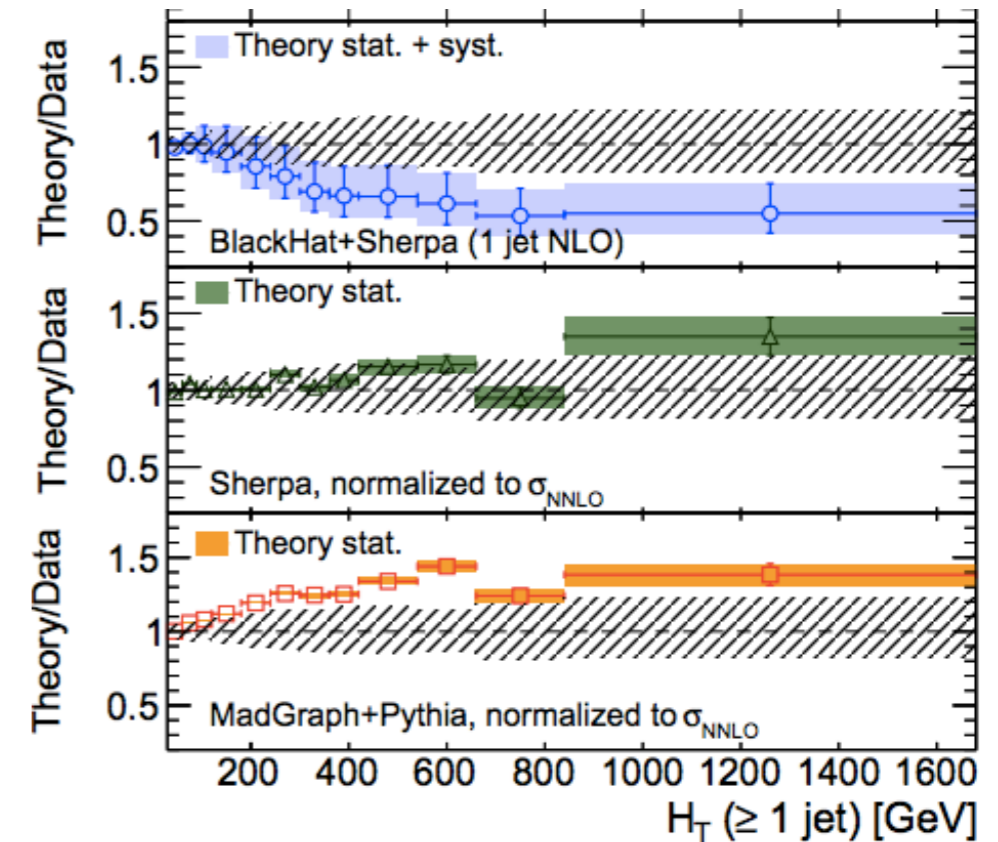
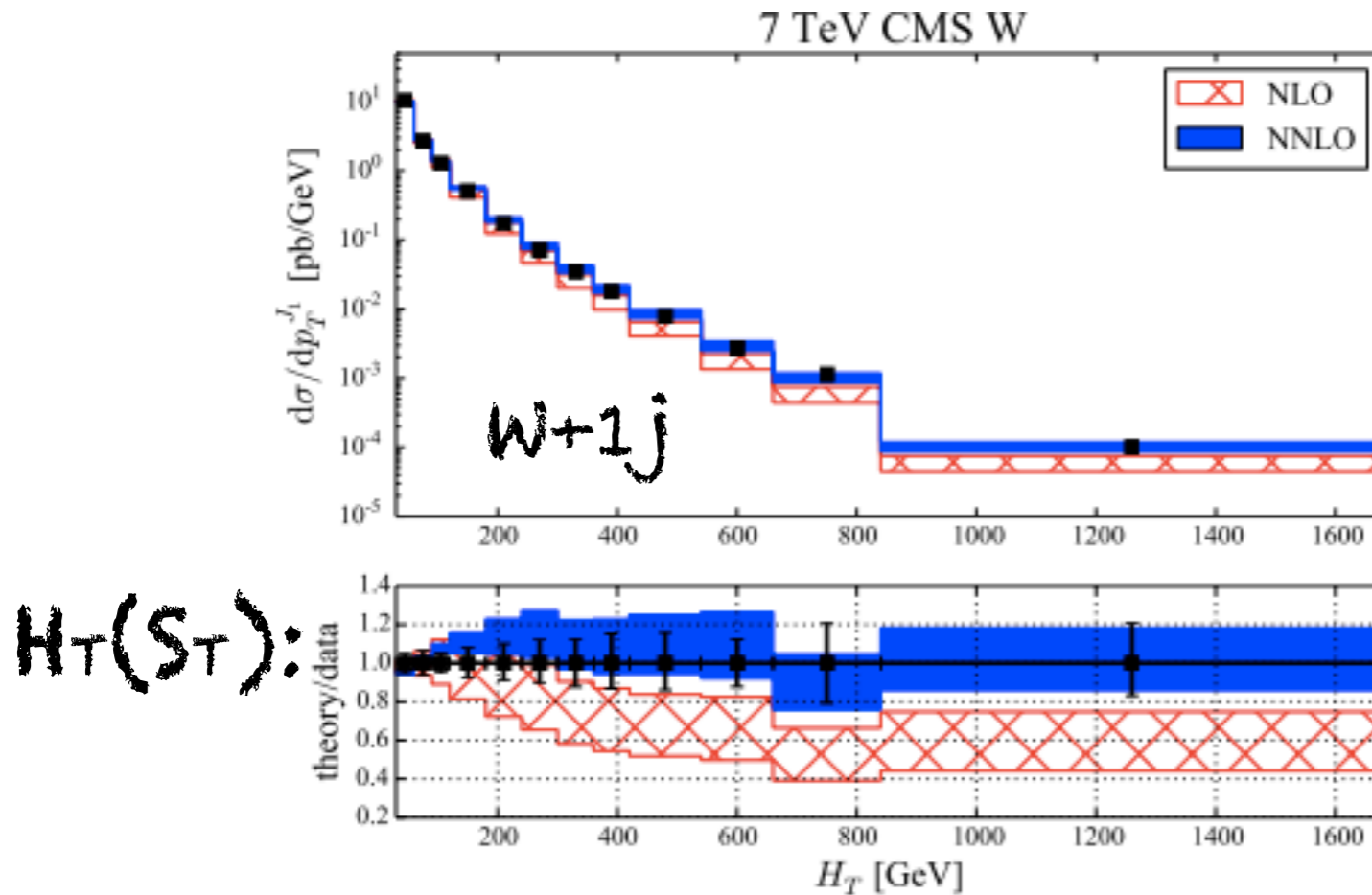
$H_T(S_T)$:

- ALPGEN agrees with data while SHERPA overshoots the measurements
- The NLO predictions far undershoot the data while MEPS@NLO does a good job
- The NNLO corrections bring theory into good agreement with experiment, with a slight undershoot at very high S_T



V+1j at the LHC

- Comparison with 7TeV data Boughezal, XL, Petriello, '16

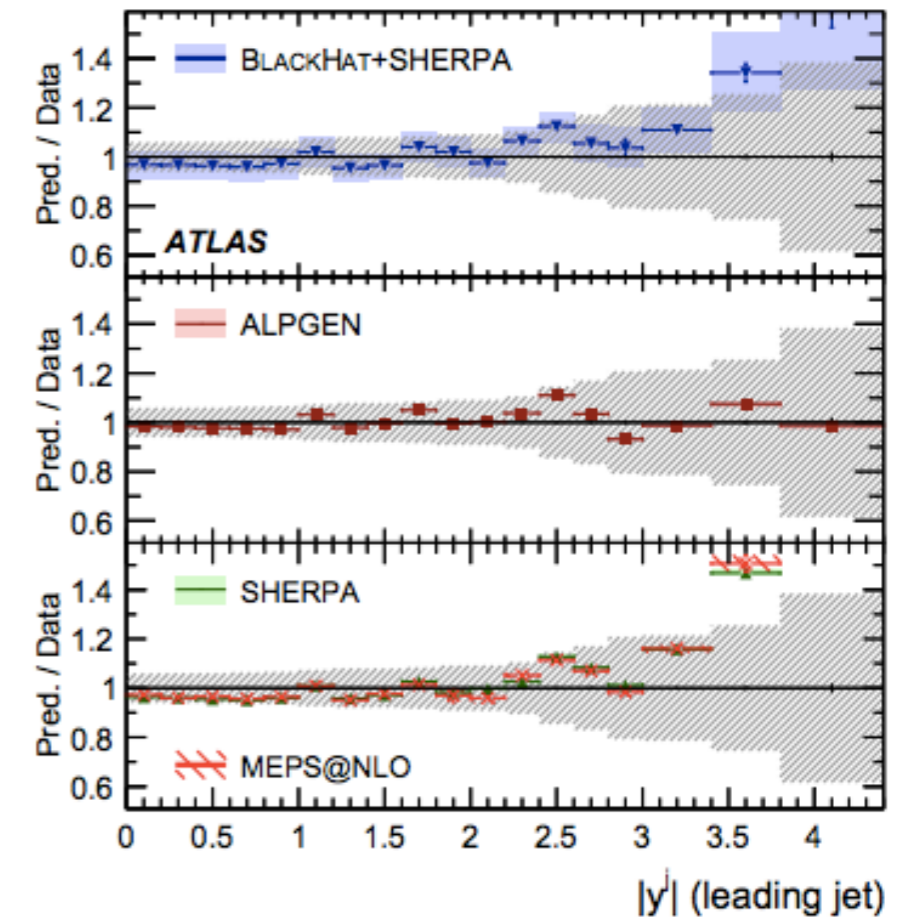
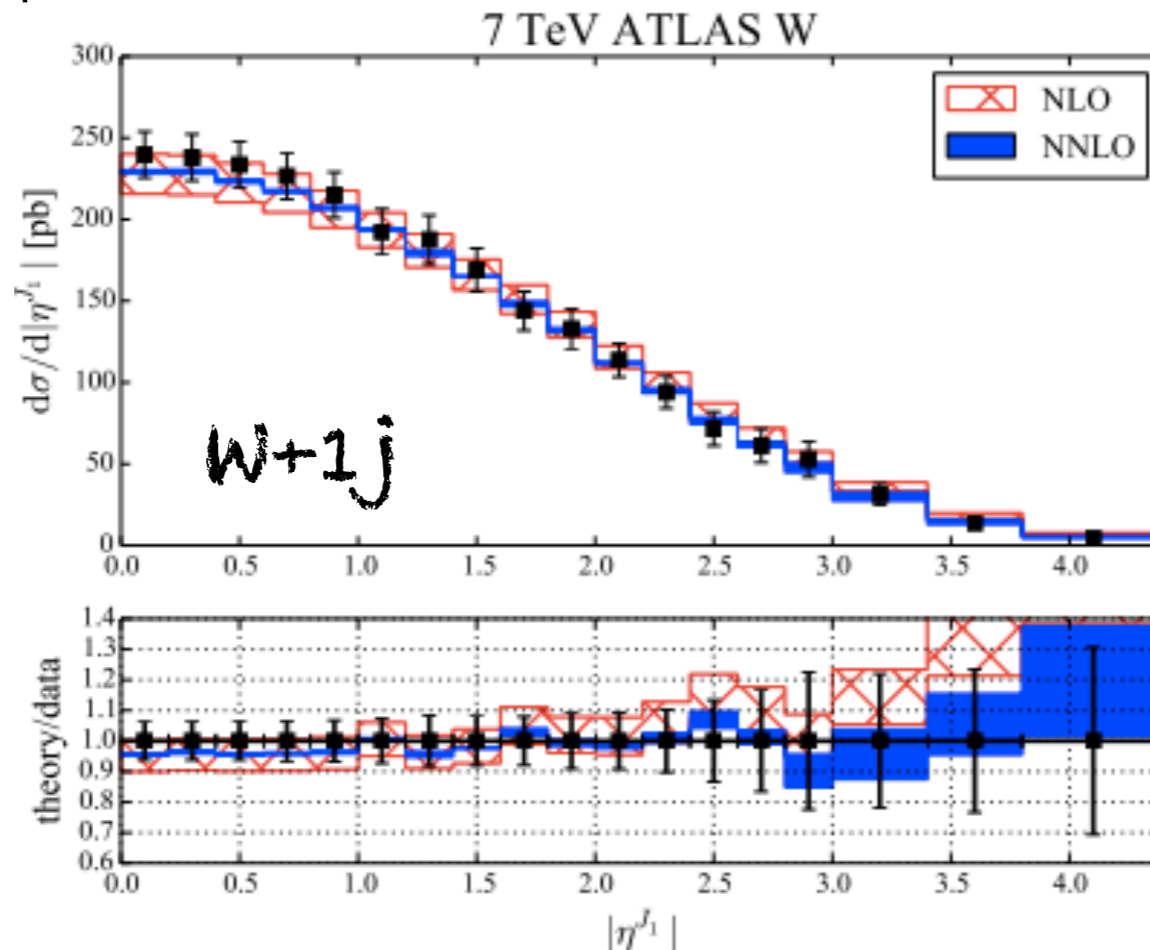


- Merged tree-level amplitudes combined with a parton shower are higher than the measurements.
- NLO QCD corrections lower than the data.
- NNLO can predict this distribution well.

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V+1j at the LHC

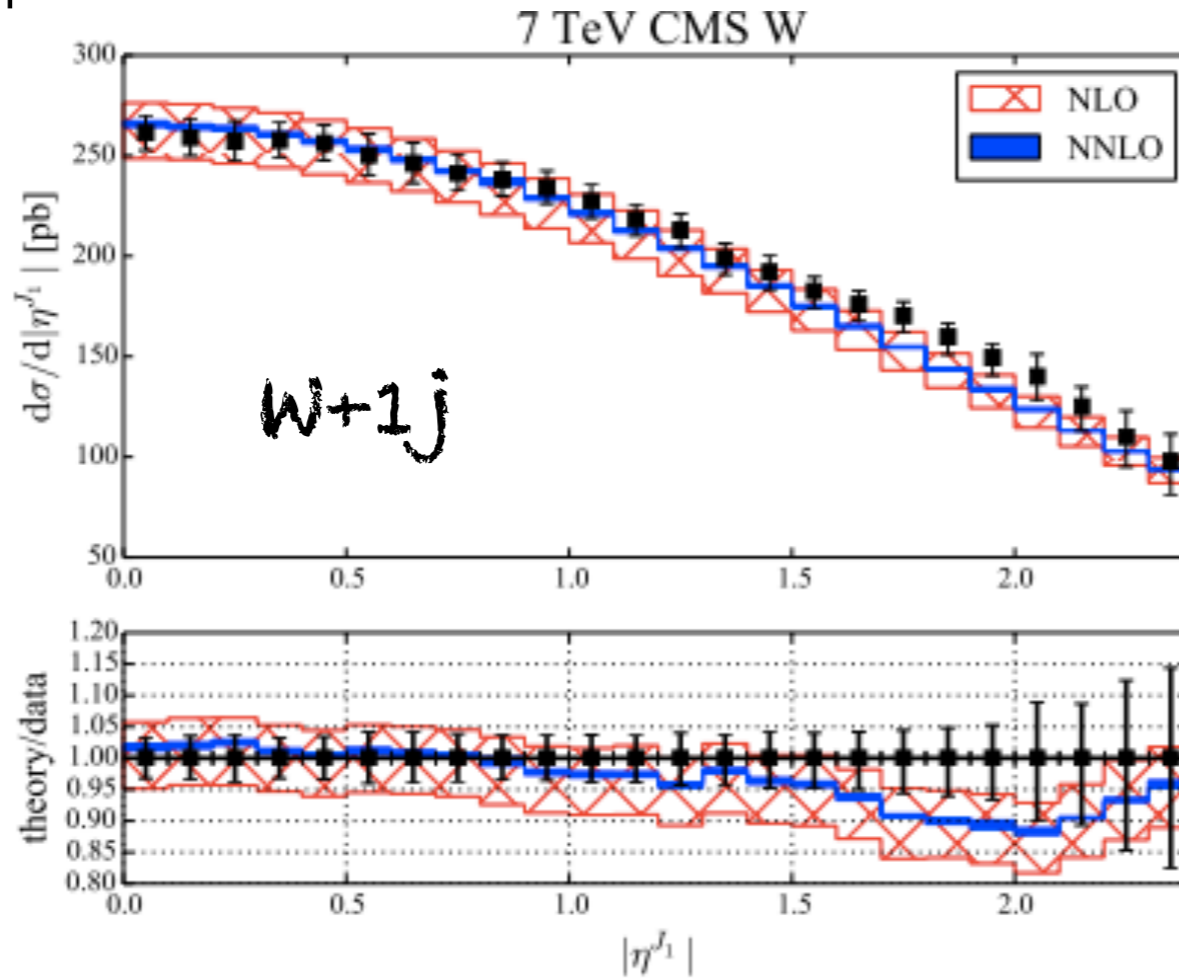
- Comparison with 7TeV data Boughezal, XL, Petriello, '16



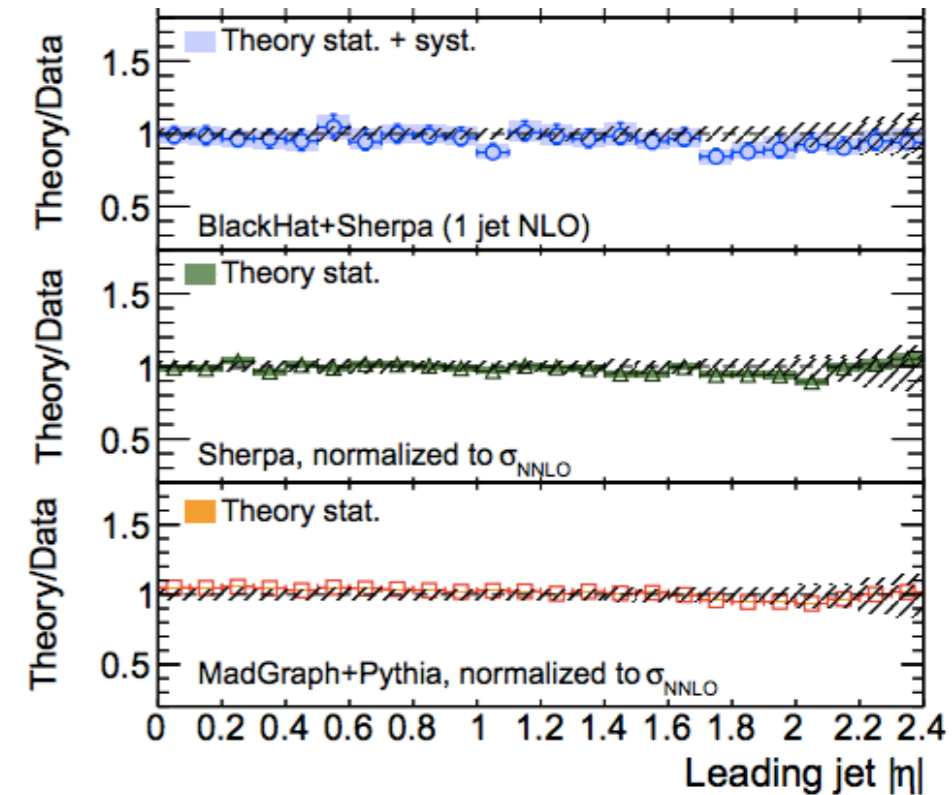
- All predictions are good in the central region
- The NLO predictions far above the data in the forward region
- The NNLO corrections bring theory into good agreement with experiment

V+1j at the LHC

- Comparison with 7TeV data Boughezal, XL, Petriello, '16



- The various tree-level plus parton shower do slightly better in the high rapidity region.
- Slight discrepancy is seen in both NLO and NNLO with data in the high rapidity region.
- NNLO reduces the scale uncertainty dramatically.



CERN-PH-EP-2014-134

V+1j at the LHC

- Comparison with 7TeV data

Boughezal, XL, Petriello, '16

- Z+1j

| Z-boson cuts | ATLAS [12] | CMS [13] |
|-----------------------|---|---|
| lepton p_T | $p_T^l > 20$ GeV | $p_T^l > 20$ GeV |
| lepton η | $ \eta^l < 2.5$ | $ \eta^l < 2.4$ |
| lepton separation | $\Delta R_{ll} > 0.2$ | – |
| lepton invariant mass | $66 \text{ GeV} < m_{ll} < 116 \text{ GeV}$ | $71 \text{ GeV} < m_{ll} < 111 \text{ GeV}$ |
| jet p_T | $p_T^J > 30$ GeV | $p_T^J > 30$ GeV |
| jet η | $ \eta^J < 4.4$ | $ \eta^J < 2.4$ |
| anti- k_T radius | $R = 0.4$ | $R = 0.5$ |

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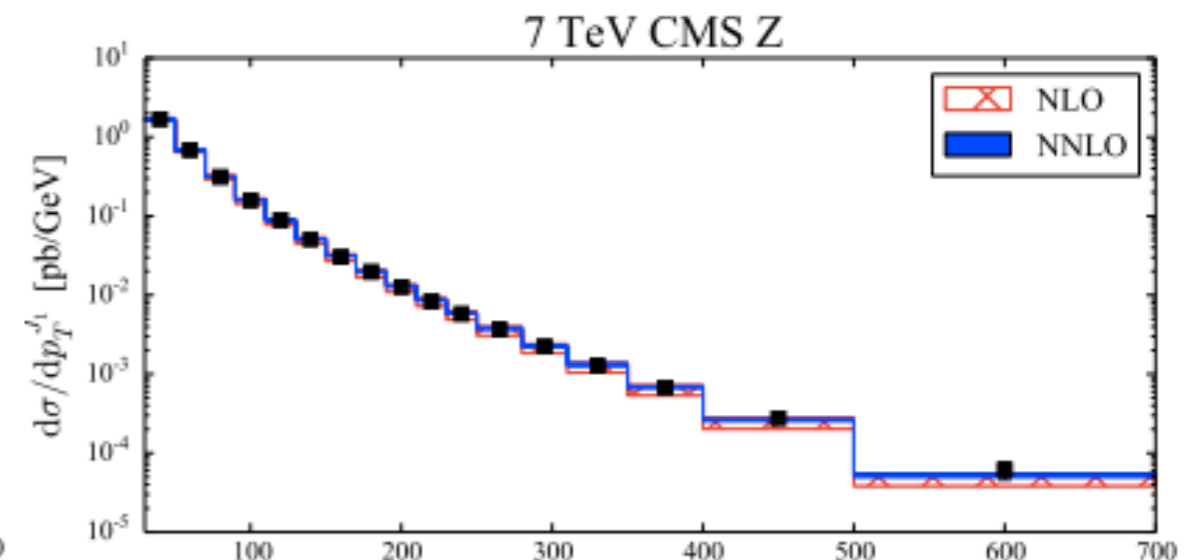
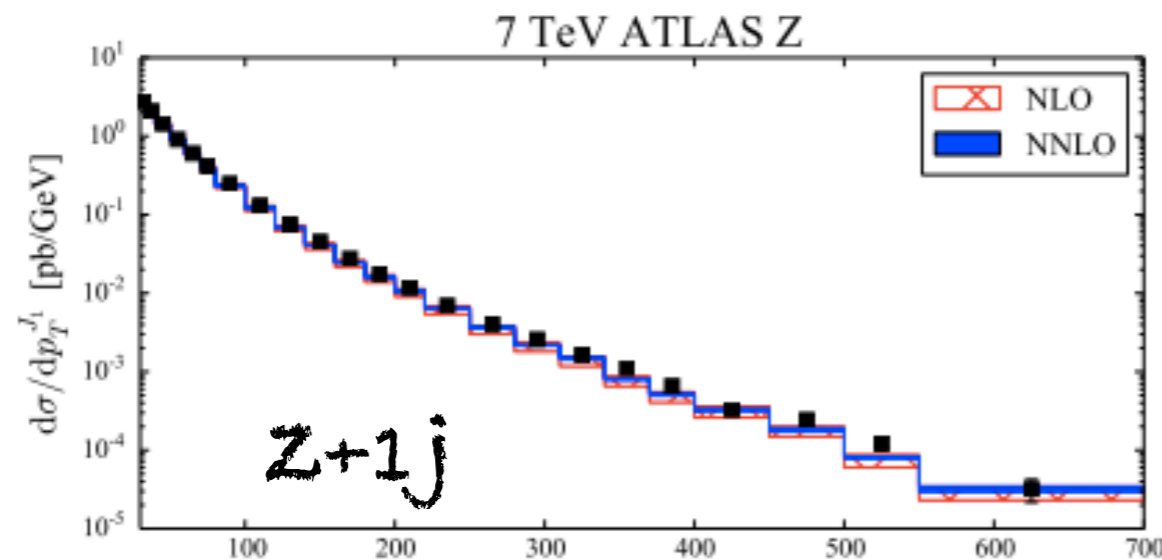
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$$\mu_0 = \sqrt{M_V^2 + \sum_i (p_T^{J_i})^2}$$

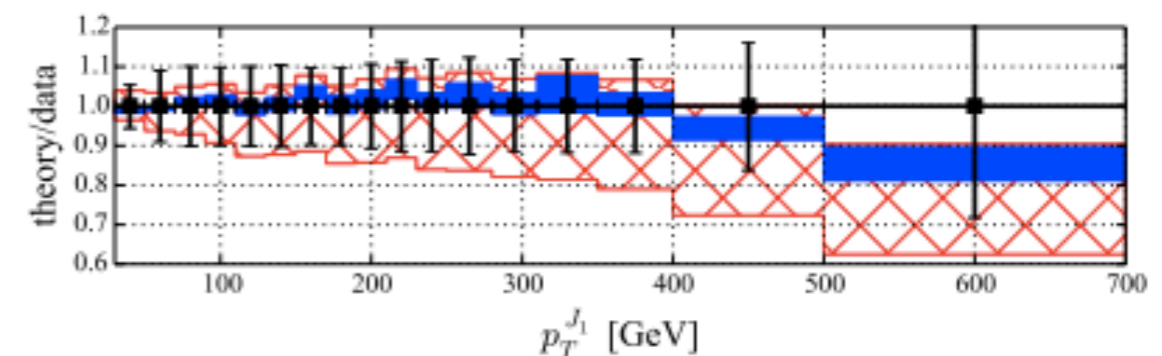
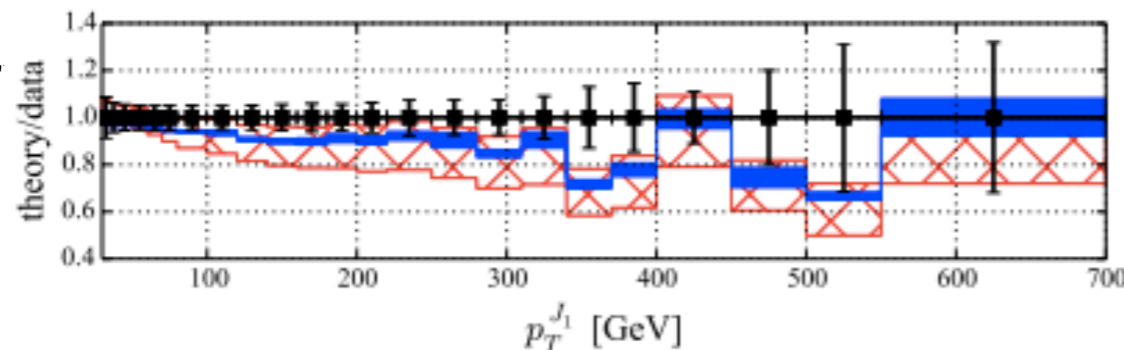
- CT14NNLO PDFs for NNLO results, CT14NLO for NLO results
- Vary μ_F and μ_R independently
- non-perturbative corrections included for ATLAS p_{TJ} and y_J
- QED FSR factors included for ATLAS p_{TJ} and y_J

V+1j at the LHC

- Comparison with 7TeV data Boughezal, XL, Petriello, '16



p_T^{J1} :



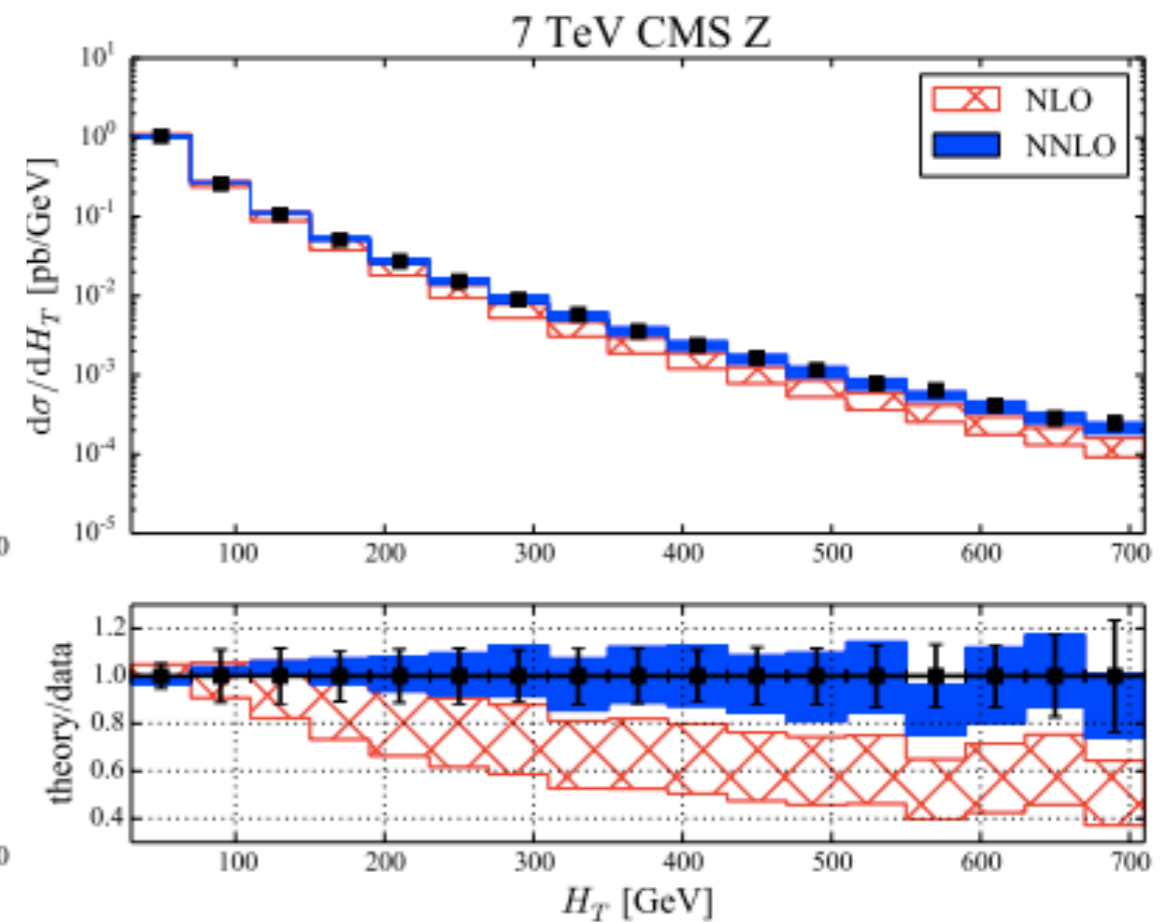
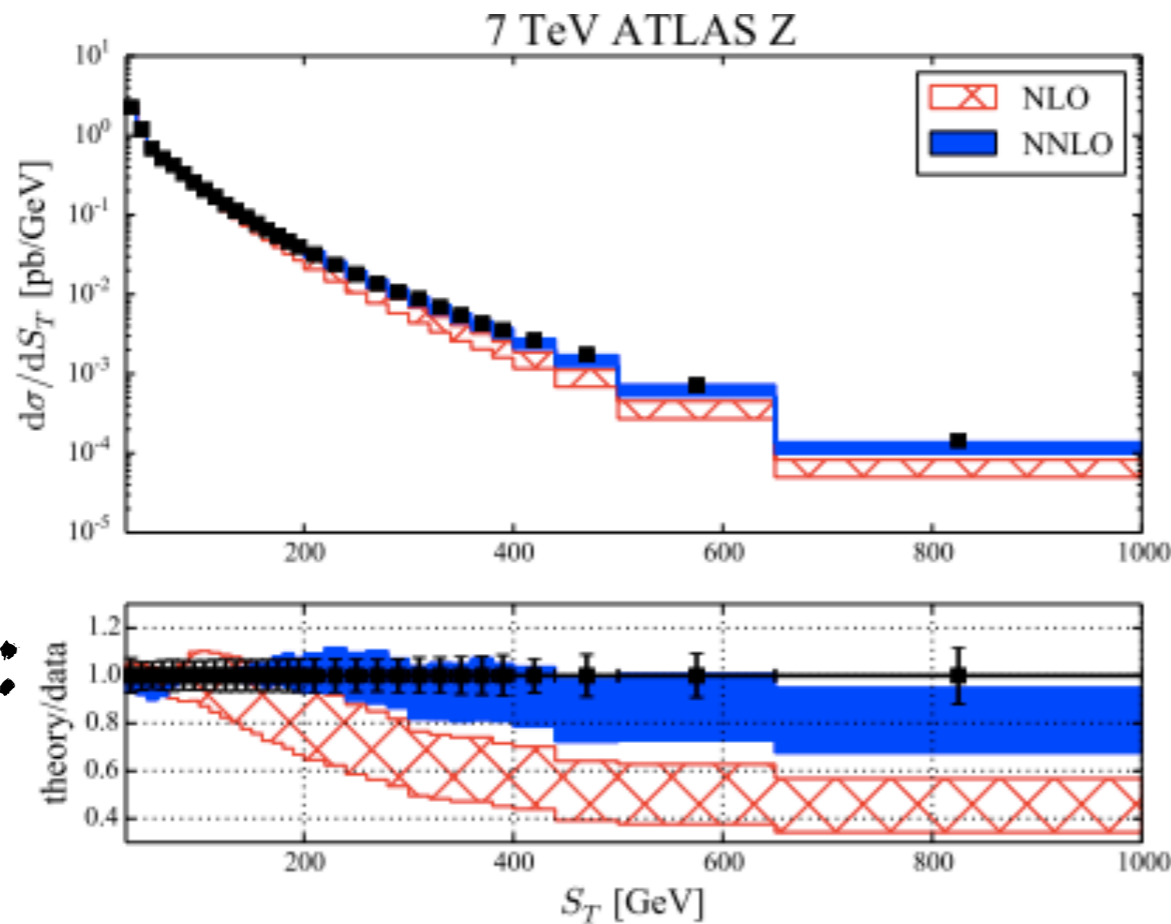
- The NLO prediction agrees with the data within errors.
- The NNLO QCD prediction is in better agreement with the CMS data over the entire p_T^{J1} range.
- The NNLO QCD prediction increases NLO but still undershoots the ATLAS data.

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V+1j at the LHC

- Comparison with 7TeV data Boughezal, XL, Petriello, '16



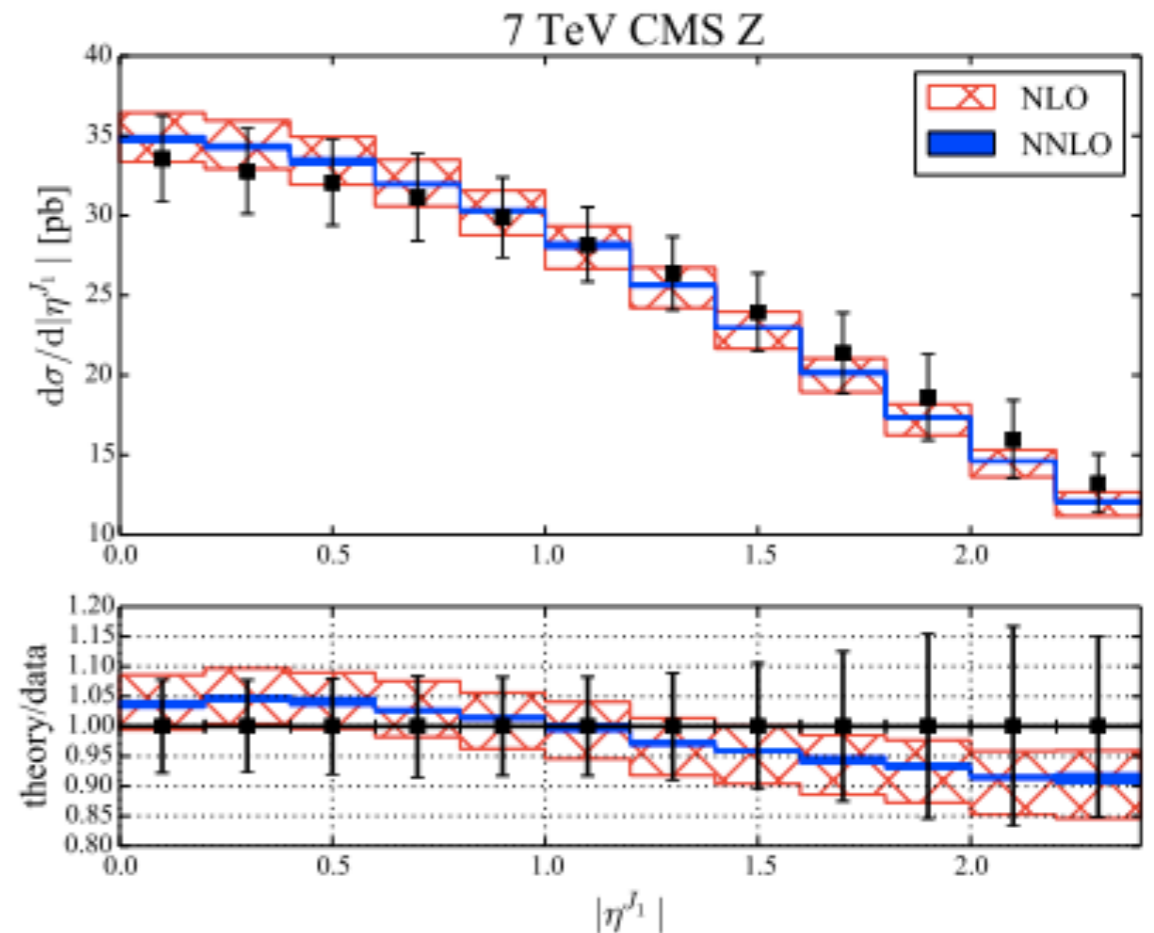
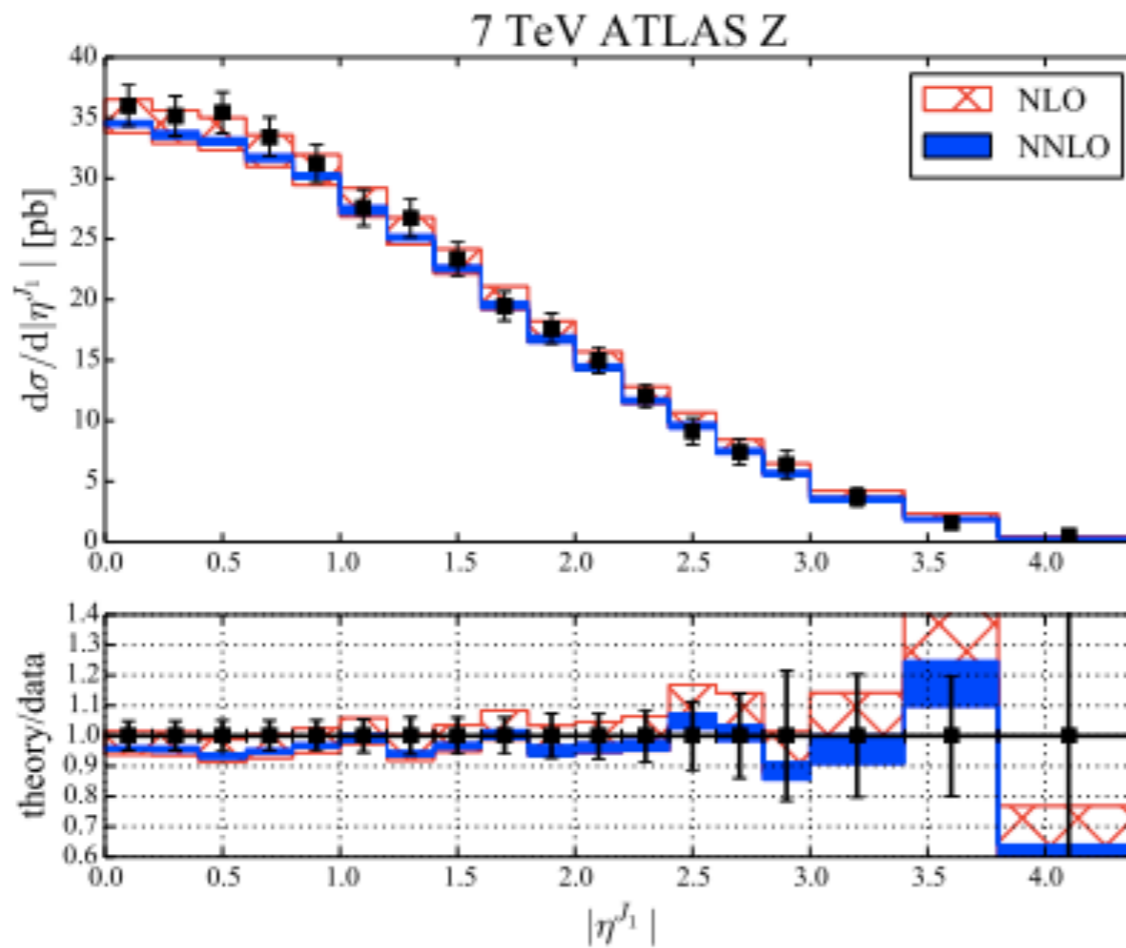
- The NLO prediction below the data.
- The NNLO QCD prediction is in good agreement with both experiments over the entire range.

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V+1j at the LHC

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Yes:

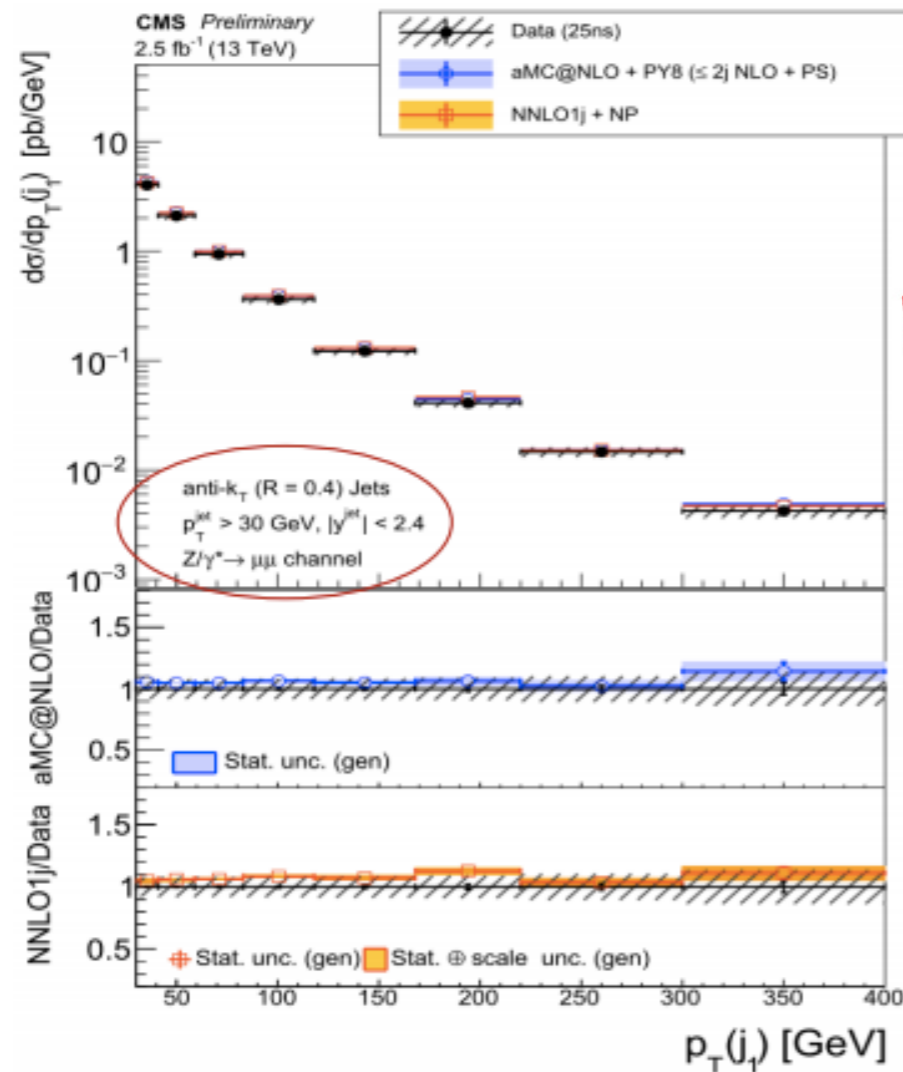
- The NNLO QCD prediction is in good agreement with data.
- Both NLO and NNLO QCD show a slight shape difference with respect to the CMS data. Similar small discrepancies are seen by CMS when they compare to POWHEG and MADGRAPH predictions.

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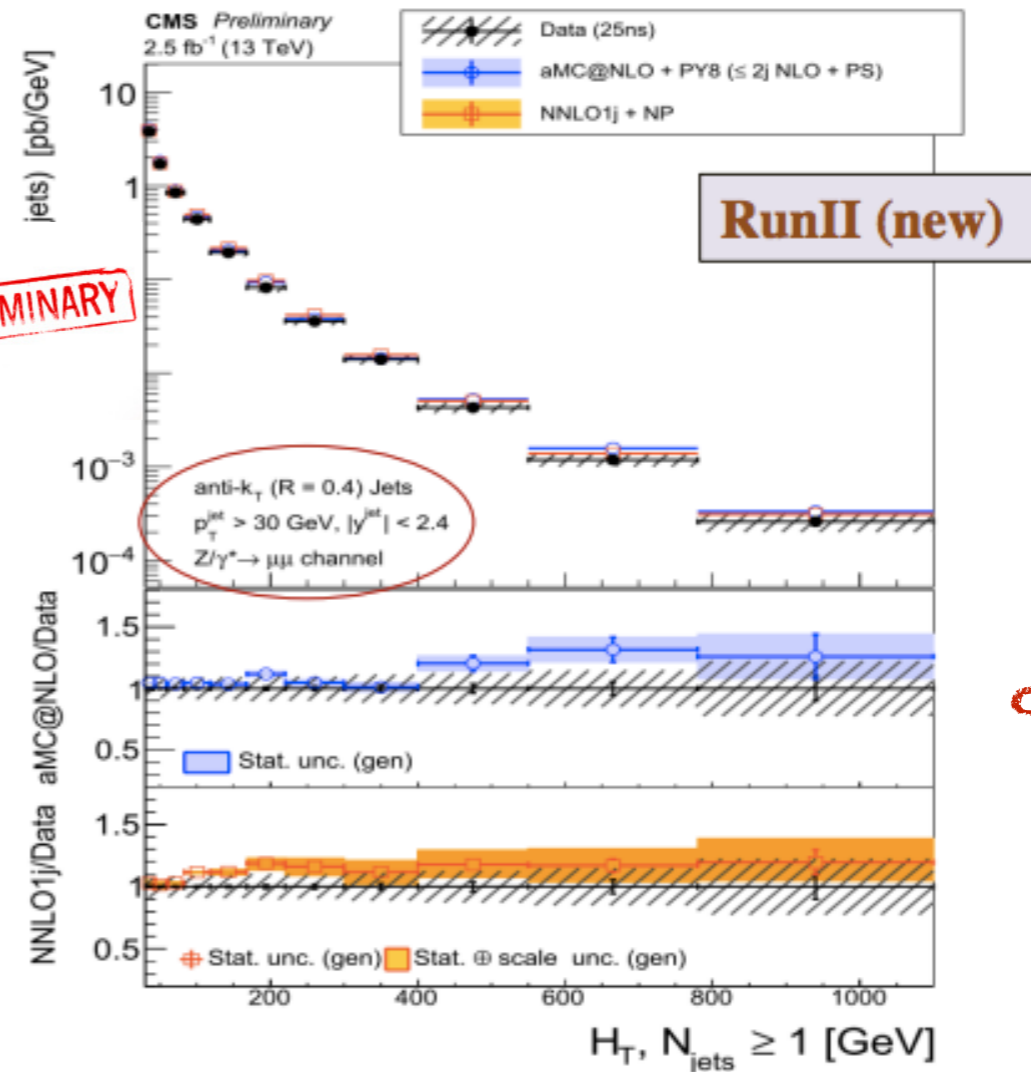
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V+1j at the LHC

- Comparison with 13TeV data Boughezal, XL, Petriello, '16



PRELIMINARY



EW
correction
is not
included

- Good agreement with multileg NLO and NNLO calculations
- The p_T , η , H_T of jet for inclusive jet multiplicities up to 3 jets have also been measured
 - H_T is the scalar sum of the p_T of jets

Conclusions

- N-jettiness subtraction
 - a new subtraction scheme for jet production
 - has been applied to get new results for H/V+1J and confirm the existing V/H inclusive, VH and di-photon productions
- NNLO V + 1jet at the LHC
 - detailed comparisons with data; in better agreement with data
 - reduces scale uncertainty dramatically

Thanks