

Magnetism and doping effects in spin-orbit coupled Mott insulators

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1. *Introduction*: spin-orbit coupled magnets
2. *d⁵ ions*: perovskite & honeycomb iridates
3. *d⁴ ions*: excitonic magnetism (ruthenates)

d-electron in TM compounds



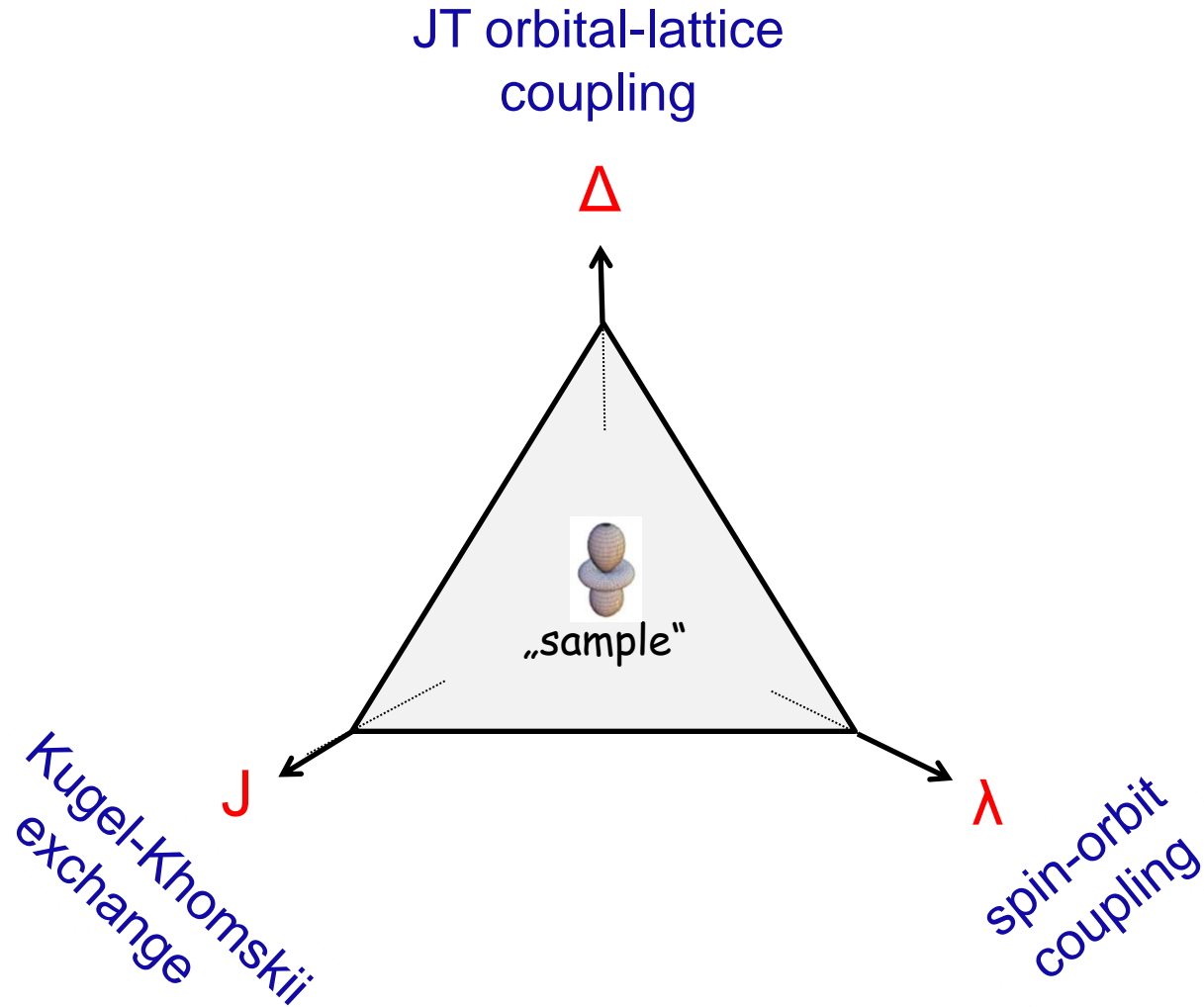
Magnetism and the Chemical Bond

BY JOHN B. GOODENOUGH

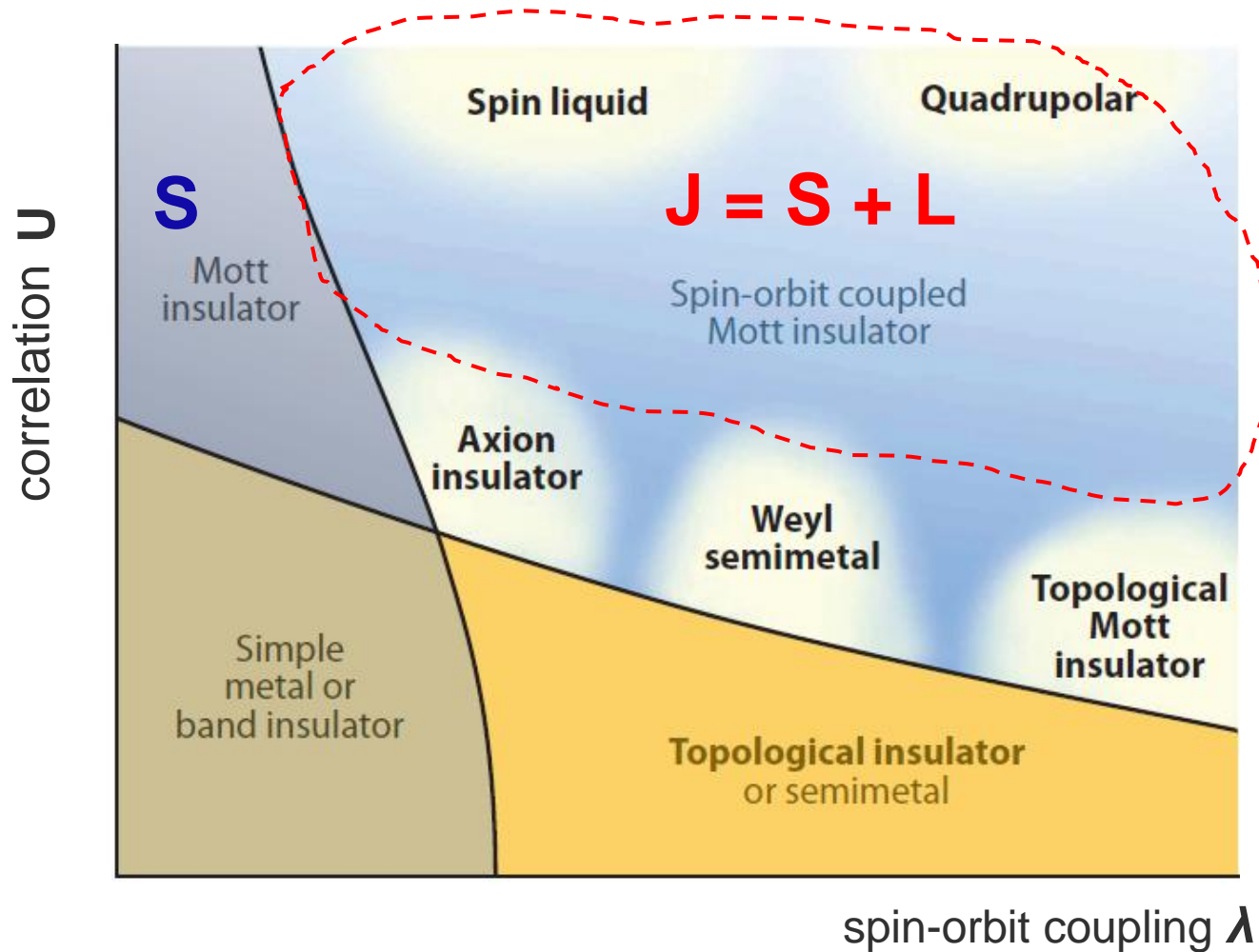
Interscience Publ. 1963

Goodenough-Kanamori
rules

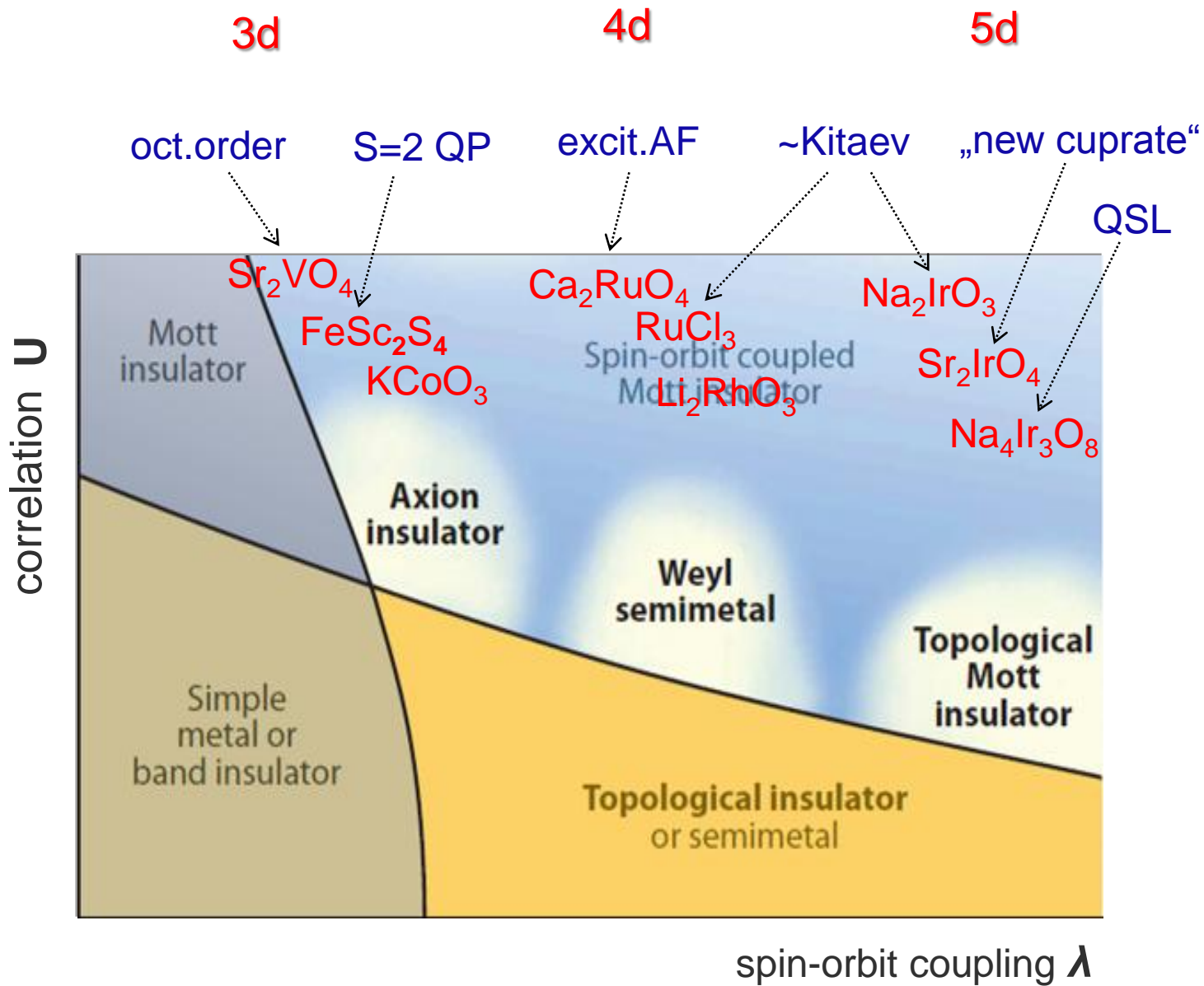
Three competing interactions: Δ , J , λ ($\ll W \sim U$)



Hubbard model with spin-orbit coupling

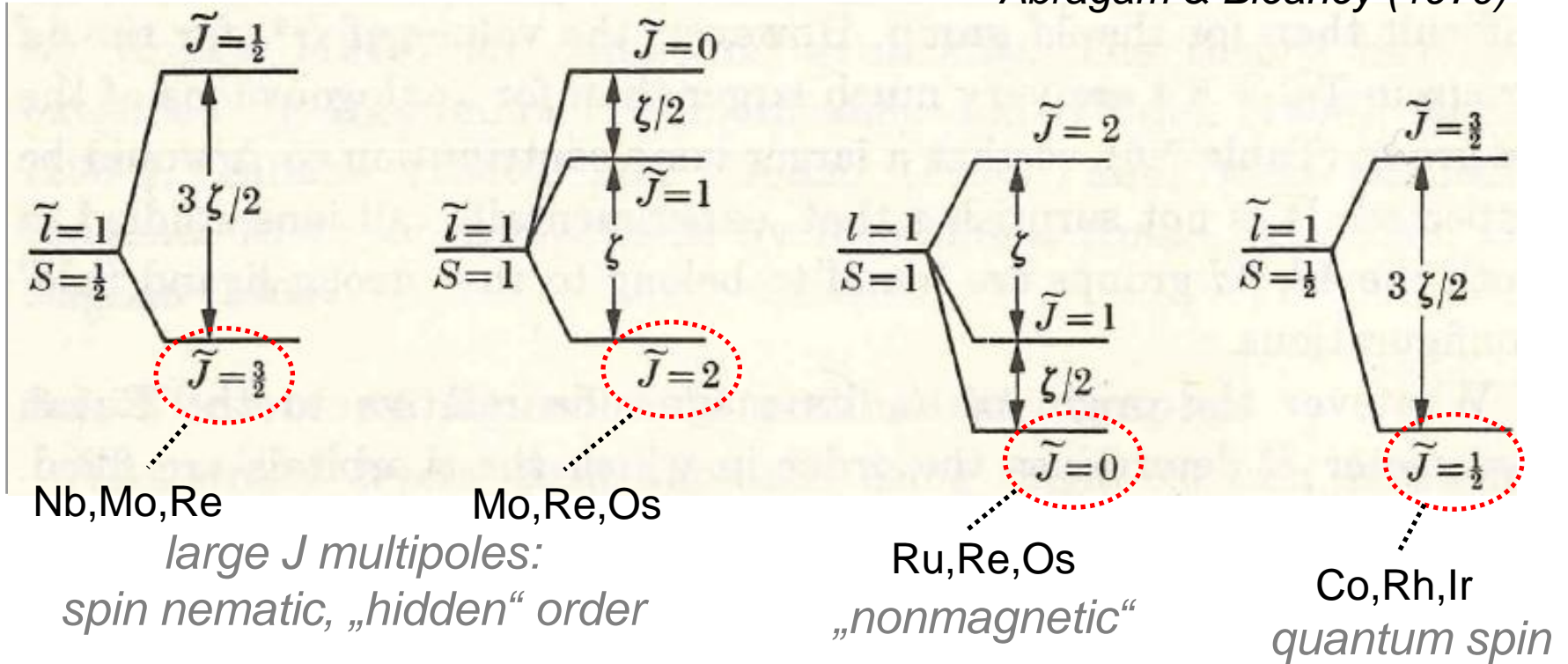


Spin-orbit magnets: some examples



Spin-orbit multiples of TM ions

Abragam & Bleaney (1970)

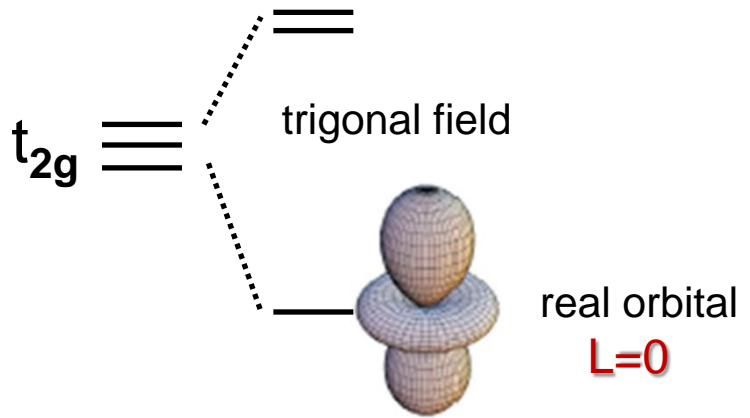


GS-degeneracy: pseudospin \tilde{J}

Kramers: dipole, octupole, ...
non-Kramers: quadrupole, ...

Lifting the orbital degeneracy

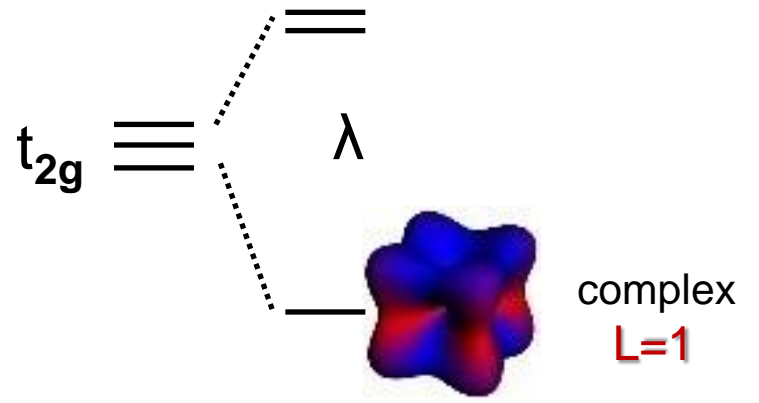
Jahn-Teller



$$|xy + yz + zx\rangle \times |\uparrow\uparrow\rangle$$

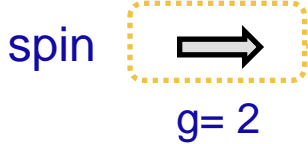
quadrupole spin

Spin-orbit



$$|xy \uparrow\rangle + |yz \downarrow\rangle + i|zx \downarrow\rangle$$

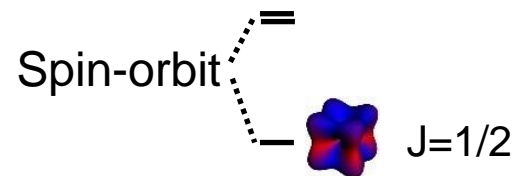
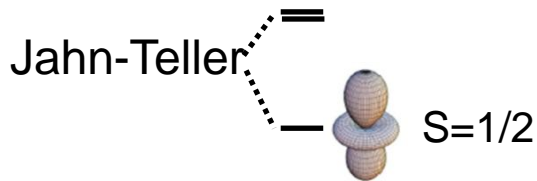
pseudospin $J=S+L$



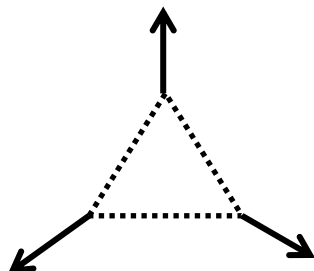
Spin $\frac{1}{2}$ algebra



Magnetism

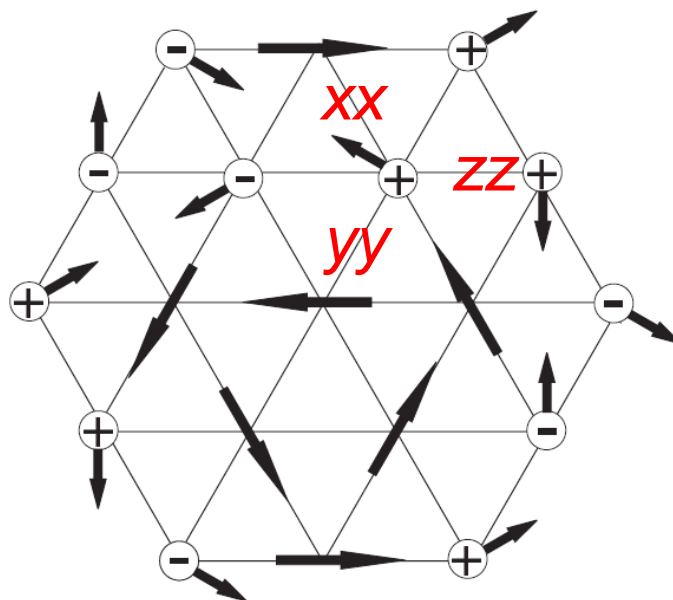


$$H = (SS)$$



*coplanar,
single-Q*

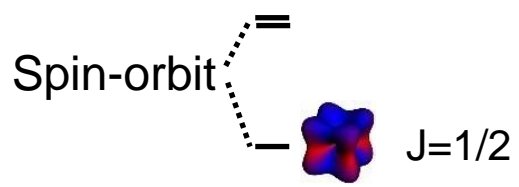
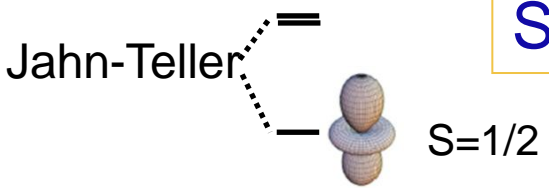
$$H = - (SS) + I \text{sing}(\alpha)$$



*large magnetic unit cell
non-coplanar, multi-Q
hosts spin vortex*

GKh (PTPS, 2005)

SC pairing



**Spin-singlet
d-wave**

$|\uparrow\downarrow - \downarrow\uparrow\rangle$

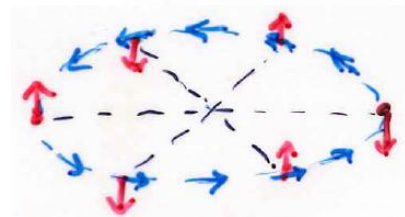
Baskaran (2003)
Kumar, Shastry (2003)
Ogata (2003)
P. Lee et al. (2004)

**Pseudospin-triplet
p+f wave**

$$\Delta_{tr} = \alpha_0 |\tilde{\uparrow}\tilde{\downarrow} + \tilde{\downarrow}\tilde{\uparrow}\rangle_j + \alpha_1 e^{i\varphi_{ij}} |\tilde{\uparrow}\tilde{\uparrow}\rangle_j + \alpha_1 e^{-i\varphi_{ij}} |\tilde{\downarrow}\tilde{\downarrow}\rangle_j$$

nondegenerate

\vec{d} -vector pattern on FS :



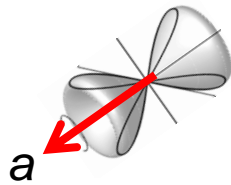
$d_x, d_y, d_z \neq 0$

„p + f“ Knight-shift finite in all directions

GKh, Koshibae, Maekawa (PRL 2004)
GKh (PTPS, 2005)

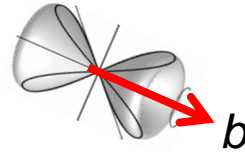
The origin of „unconventionality“: ORBITAL magnetism

Orbital moment **L** has a „shape“:



$$L_x=1$$

$$x(y+iz)$$



$$L_y=1$$

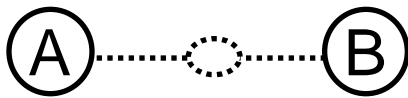
$$y(z+ix)$$



$$L_z=1$$

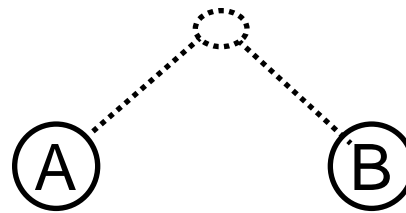
$$z(x+iy)$$

Hopping amplitude:



real

(inversion)



complex

(no inversion)



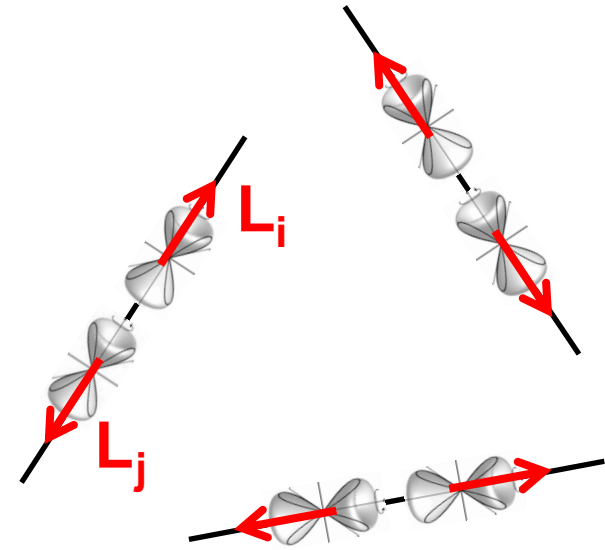
nontrivial band topology
Shitade *et al.* (2009)

ORBITAL MAGNETISM

Orbital moment **L** interactions:

non-Heisenberg

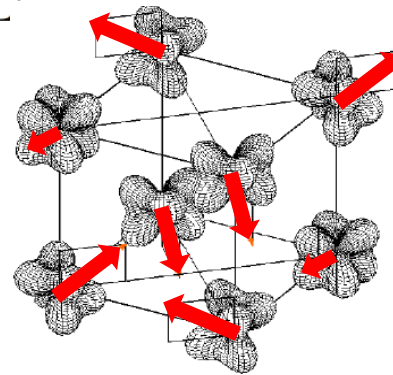
bond-dependent



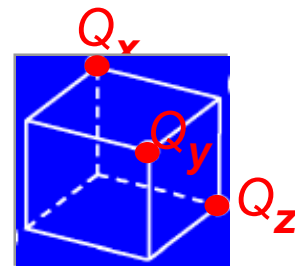
$$\mathcal{H}_{ij}^{(c)} = (L_i^x L_j^x)^2 + (L_i^y L_j^y)^2 + L_i^x L_i^y L_j^y L_j^x + L_i^y L_i^x L_j^x L_j^y$$

cubic lattice:

GKh & Okamoto (2002)

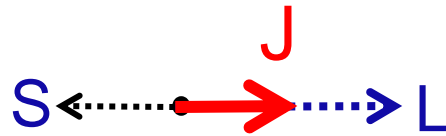


non-coplanar



multi-Q

no LRO at finite T



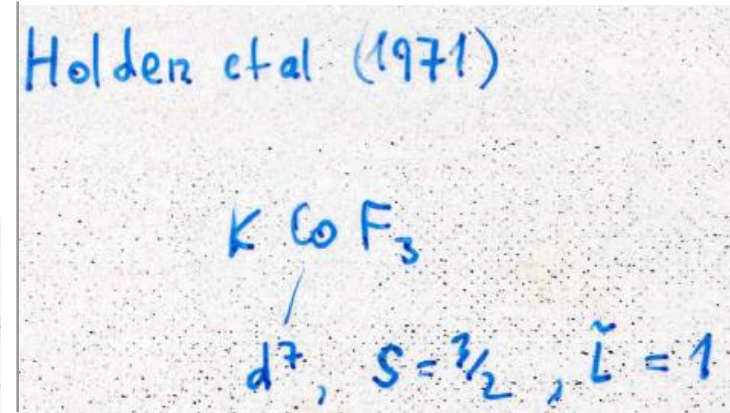
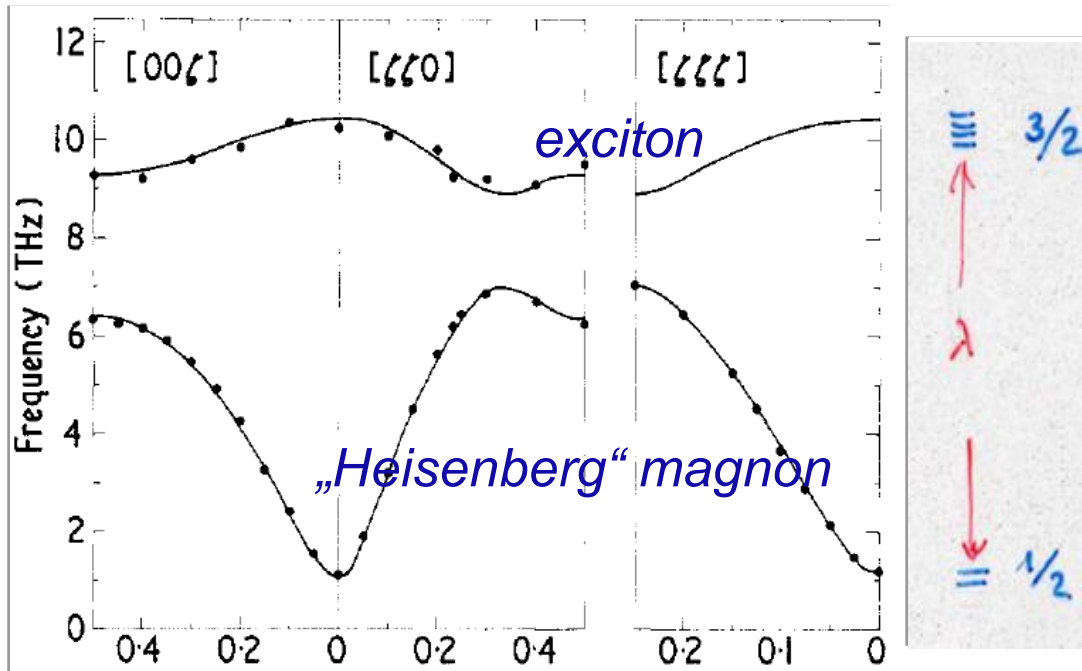
*Pseudospin $J=S+L$ inherits
bond-dependent and frustrated
nature of orbitals*



„unconventional“ magnetism

The „old“ pseudospin $J=1/2$

3d Co-fluoride, neutron scattering

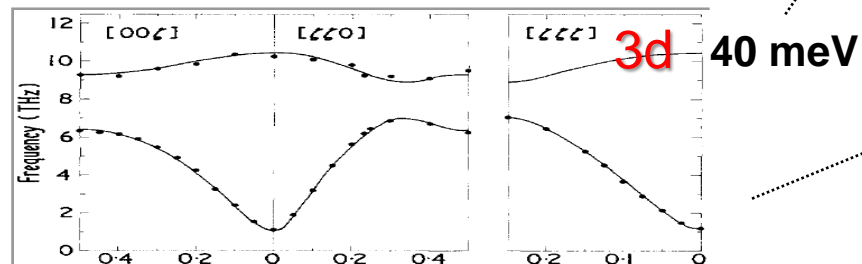


Two branches split by spin-orbit:
magnon & exciton

from **3d** Co to **5d** Ir

B.J.Kim, Takagi, ...

	3d	4d	5d
	Co ⁴⁺	Rh ⁴⁺	Ir ⁴⁺
λ :	80 meV	190 meV	380 meV

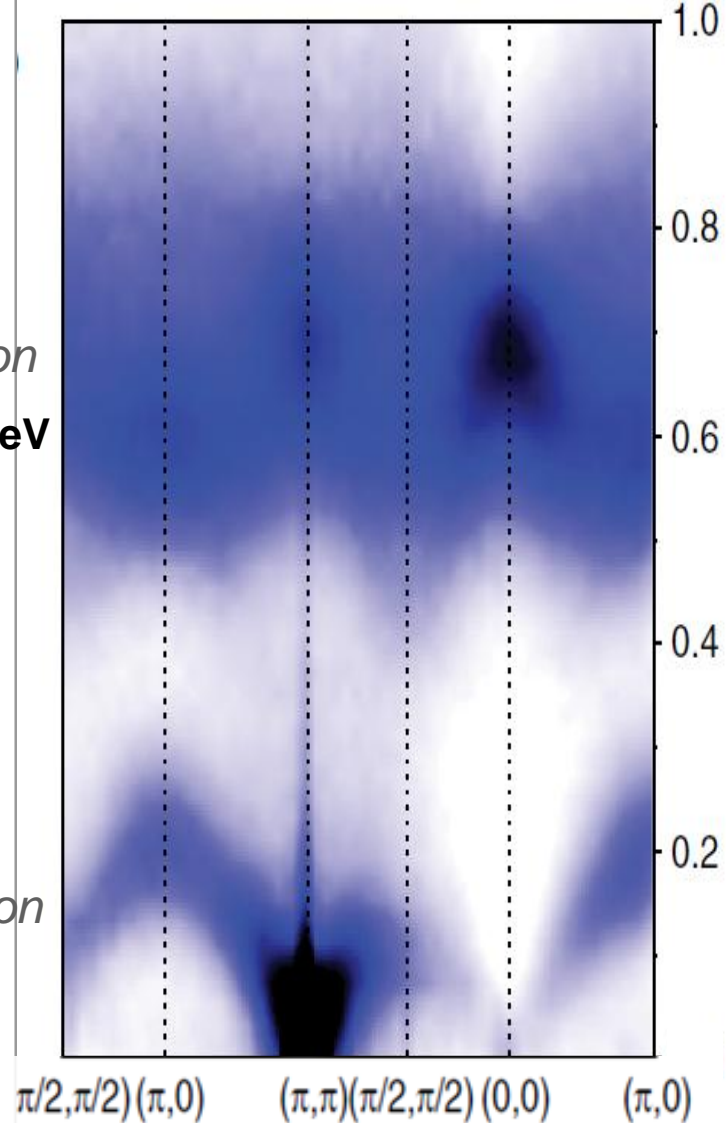


KCoF₃

Holden *et al.* (1971)
neutron scattering

Exciton
5d 600 meV

Magnon



Sr₂IrO₄

Kim *et al.* (2012)
RIXS data

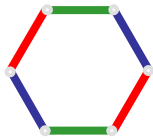
J=1/2 magnetism in iridates: *basic theory*

Jackeli & GKh (2009)

Two-parameter Hamiltonian = Kitaev + Heisenberg:

$$\mathcal{H}_{ij}^{(\gamma)} = 2K S_i^\gamma S_j^\gamma + J \mathbf{S}_i \cdot \mathbf{S}_j$$

dominant in 90-bonding
(honeycomb Na_2IrO_3)



= *Kitaev model (2006)*



„Majorana world“ ?

dominant in 180-bonding
(Sr_2IrO_4 perovskite)



= „cuprate“ model



high- T_c SC ?

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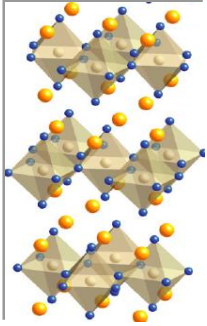
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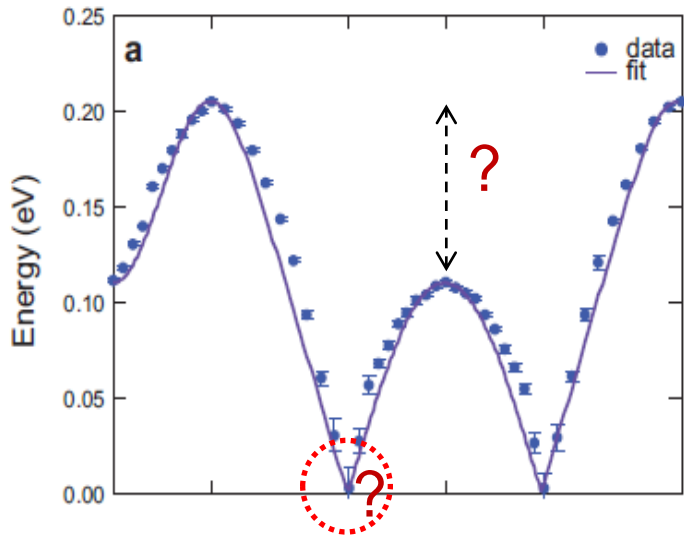
high- T_c SC ?



Sr₂IrO₄

Pseudospin 1/2 in perovskites:

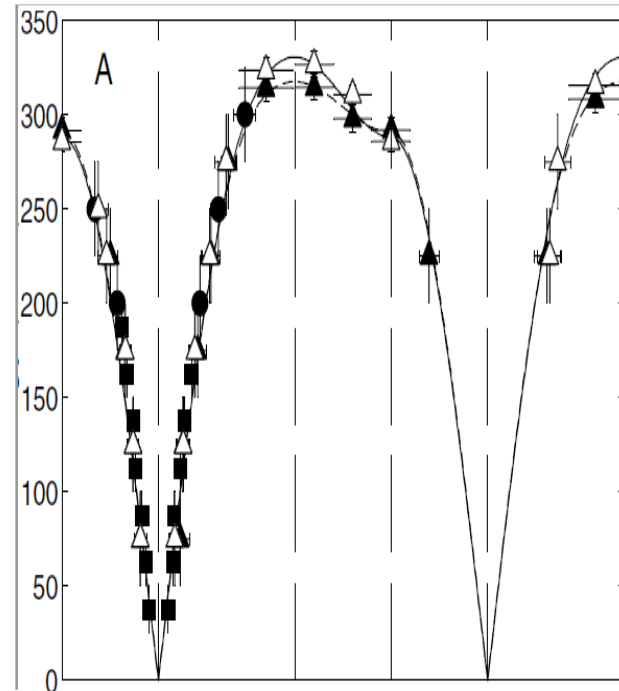
-theory predicts
„nearly“ Heisenberg AF



Sr₂IrO₄

T_N~240 K

Kim et al.(2012)



La₂CuO₄

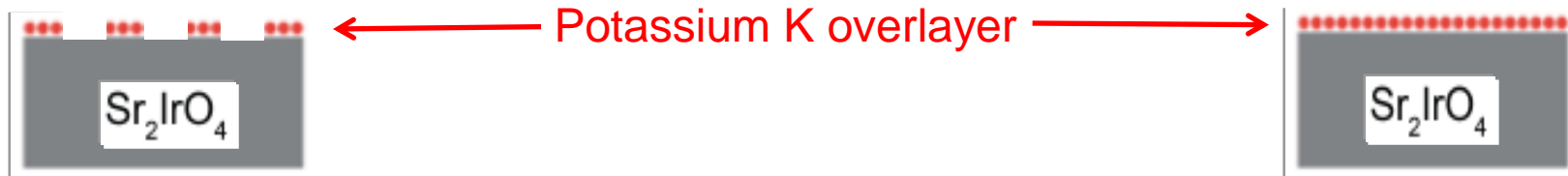
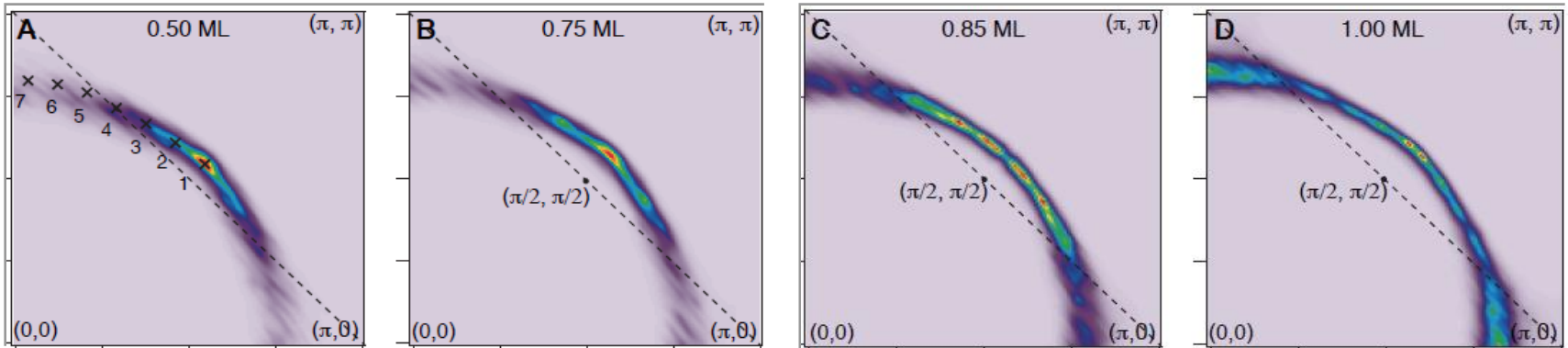
T_N~320 K

Coldea et al.(2001)

Fermiology of electron doped Sr_2IrO_4

„Fermi-arcs“ at low doping

„normal“ FS

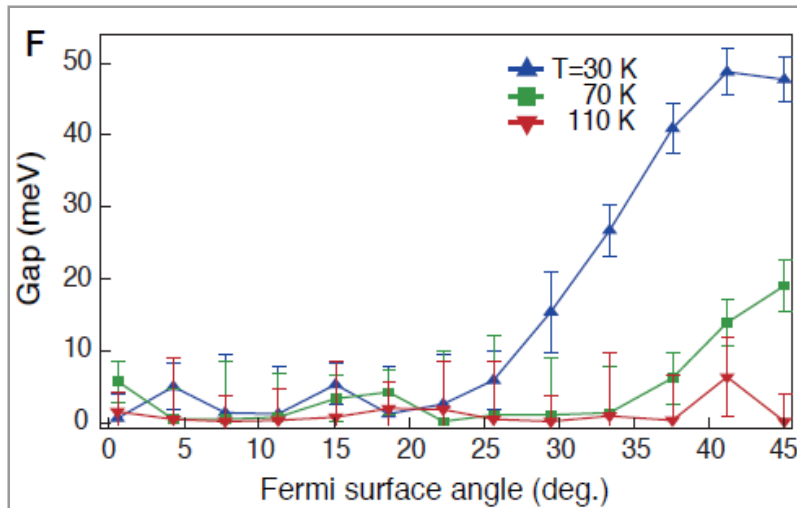
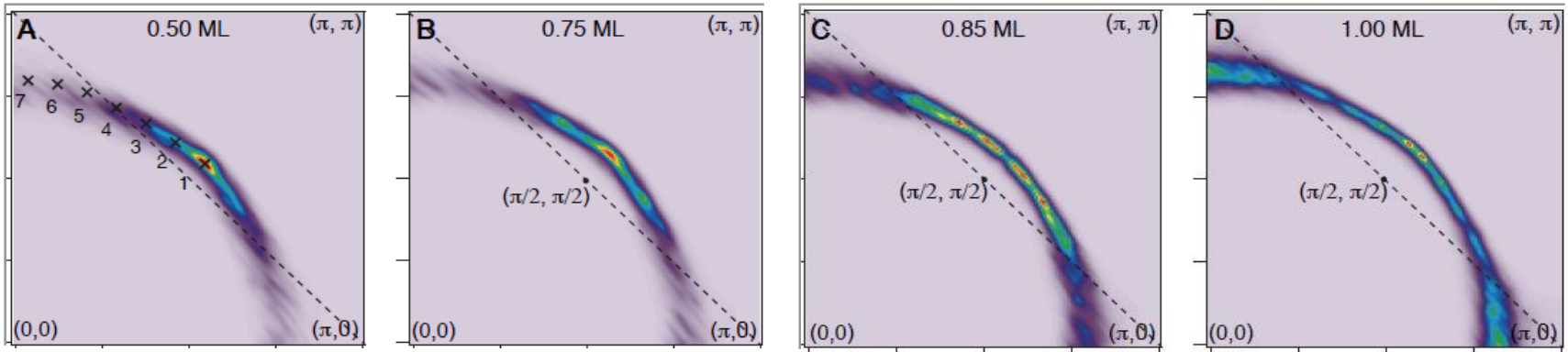


B.J. Kim *et al.* (Science 2014)

T-dependent „pseudogap“ in Sr_2IrO_4

„Fermi-arcs“ at low doping

„normal“ FS



Pseudogap opens at low T

many-body effect !

...and closes at 110 K

Sr_2IrO_4 magnetism, fermiology & lattice: *same as in* La_2CuO_4



superconductivity?

YES

SUPER!
GREAT!

NO

.....find 10 differences..."

Sr_2IrO_4



La_2CuO_4



YES or NO? -- no definite answer yet...

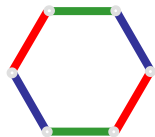
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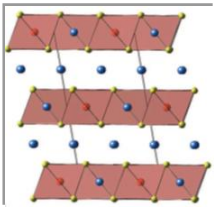
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(Sr_2IrO_4 perovskite)



= „cuprate“ model



high- T_c SC ?

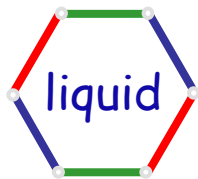


honeycomb lattice

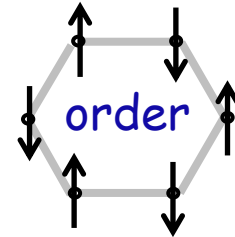
KH model

$$\mathcal{H}_{ij}^{(\gamma)} = 2K S_i^\gamma S_j^\gamma + J \mathbf{S}_i \cdot \mathbf{S}_j$$

Kitaev model

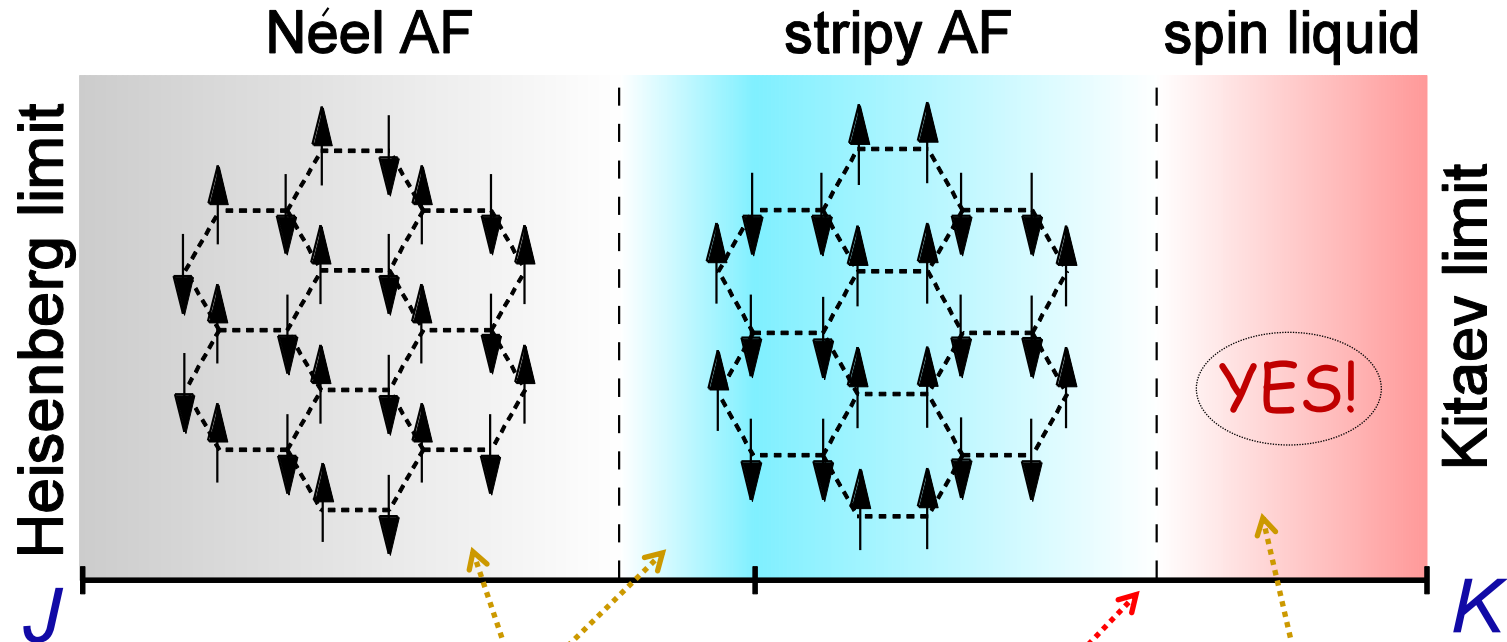
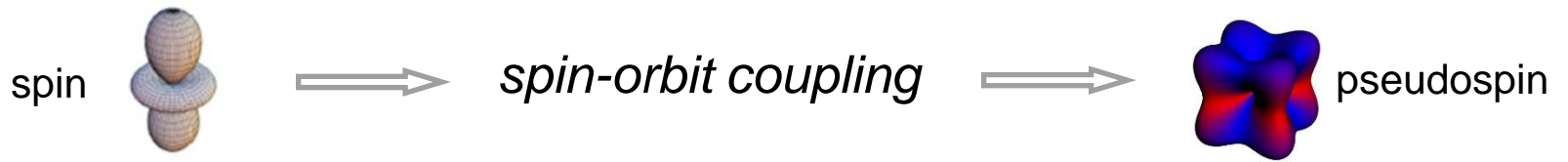


Heisenberg model



What is in between?

- if „some liquid“ left?



Spins, magnons

Majorana land

*Quantum phase transition:
spin fractionalization*

Chaloupka, Jackeli, GKh (2010)

real world: Na_2IrO_3



Exp. data

AM order $T_N \sim 15\text{K}$

(1) Mag. bandwidth: $40 \text{ meV} \sim 30 T_N$
(*Gretarrson et al.*)

(2) Intense $q=0$ scattering
(*Gretarrson et al.; B.J. Kim et al.*)

(3) SW gap is small $< 2 \text{ meV}$
(*Coldea et al.; B.J. Kim et al.*)

Interactions:

strongly frustrated

non-Heisenberg

C3 symmetric

Kitaev-Heisenberg model **with large $K > J$**

makes all these „for free“ but...

real world: Na_2IrO_3



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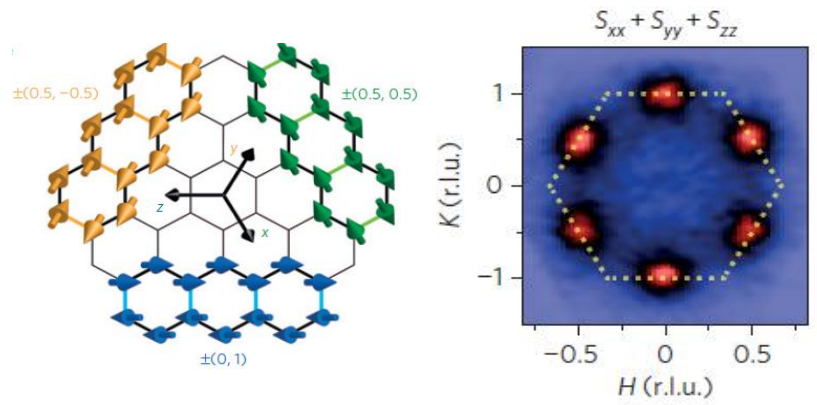
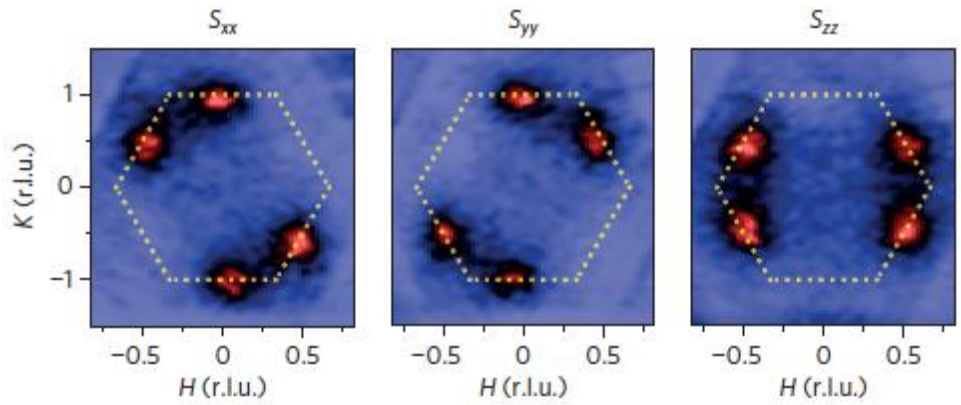
Kitaev-Heisenberg model **with large $K > J$**

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B.J. Kim et al. (2015): **moment direction unexpected for KH model**

Diffuse magnetic X-ray scattering intensities above T_N

B.J. Kim et al. (2015)

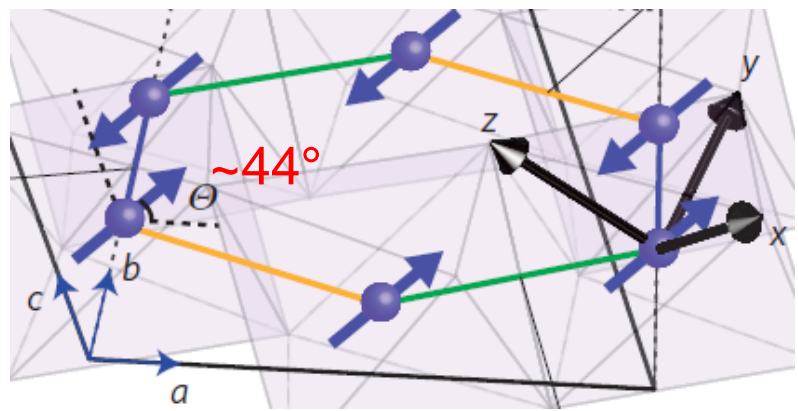


Each spin-component has its own Bragg-spot : **non-Heisenberg**

three equivalent zigzags

average

C3-symmetry involving both spin and lattice: **natural for KH-model**



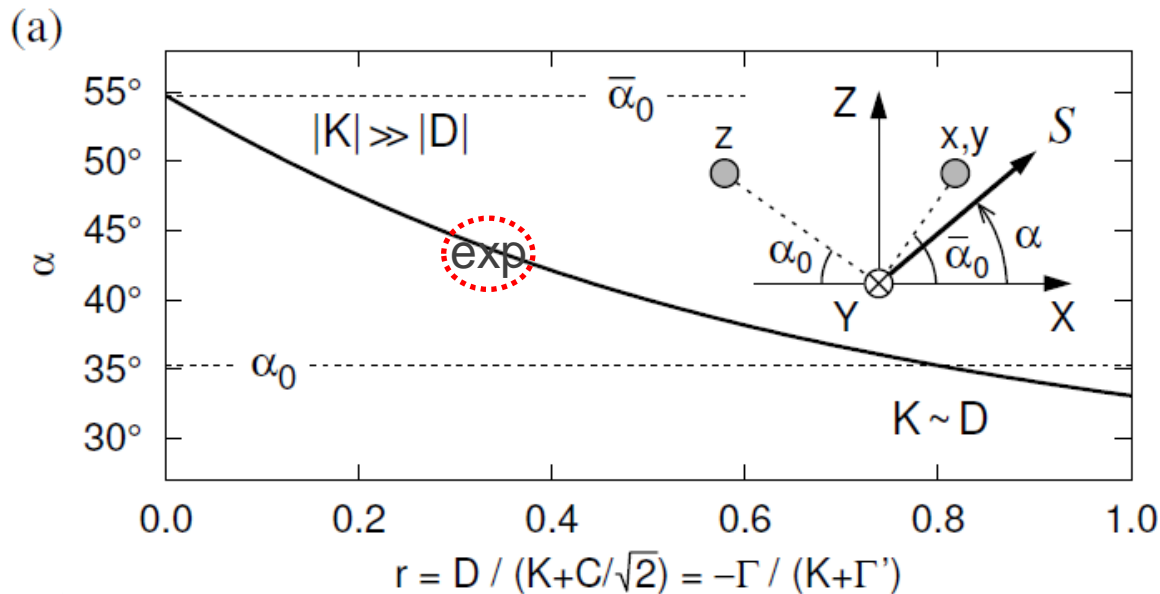
„Wrong“ easy axis:
spins look „nowhere“ away from the symmetry axes

NB: Kitaev term wants spin parallel to Ir-O bond

„Extended“ KH-model: (H.-Y. Kee ...; van den Brink ...; Imada ...)

$$\mathcal{H}_{\langle ij \rangle \| c} = J \mathbf{S}_i \cdot \mathbf{S}_j + K S_i^z S_j^z + D (S_i^x S_j^x - S_i^y S_j^y) + C (S_i^y S_j^z + S_i^z S_j^y)$$

Two new terms: D and C

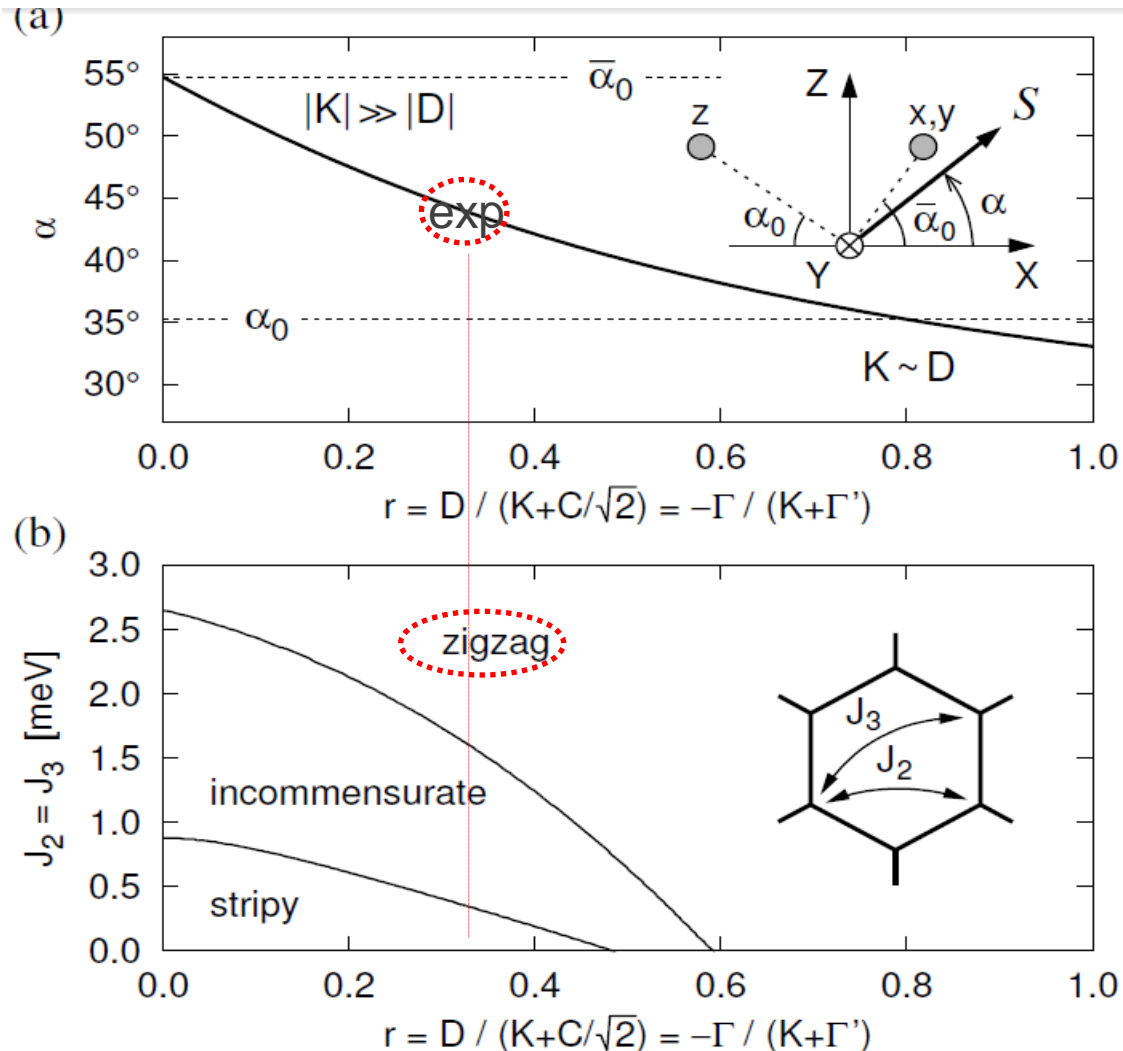


Chaloupka & GKh (2015)

Spin direction as a function of the departure from KH model

D and C make the right angle.
 However, zigzag gets unstable. *We need longer range interactions.*

$$\mathcal{H}_{\langle ij \rangle \parallel c} = J \mathbf{S}_i \cdot \mathbf{S}_j + K S_i^z S_j^z + D (S_i^x S_j^x - S_i^y S_j^y) + C (S_i^y S_j^z + S_i^z S_j^y) + J_{2,3}(\text{SS})$$



anisotropy D
&
long-range $J_{2,3}$



Right moment
direction
&
zigzag order

PHYSICAL REVIEW B 88, 035107 (2013)

***Ab initio* analysis of the tight-binding parameters and magnetic interactions in Na_2IrO_3**

Kateryna Foyevtsova,¹ Harald O. Jeschke,¹ I. I. Mazin,² D. I. Khomskii,³ and Roser Valentí¹



... the nnKH model, is, apparently, inadequate.

Spatially extended, „quasimolecular“ orbitals:
longer-range couplings $J_{2,3}$

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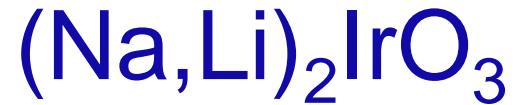
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... the nnKH model, is, apparently, ~~inadequate.~~ *insufficient*

Spatially extended, „quasimolecular“ orbitals:
longer-range couplings $J_{2,3}$

yes, indeed



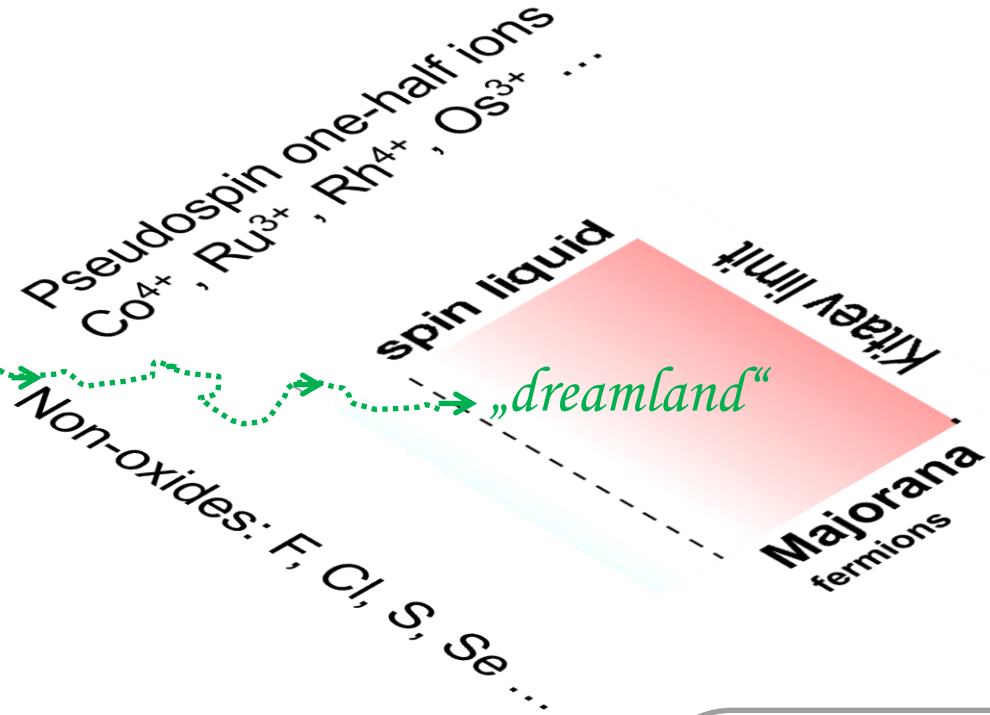
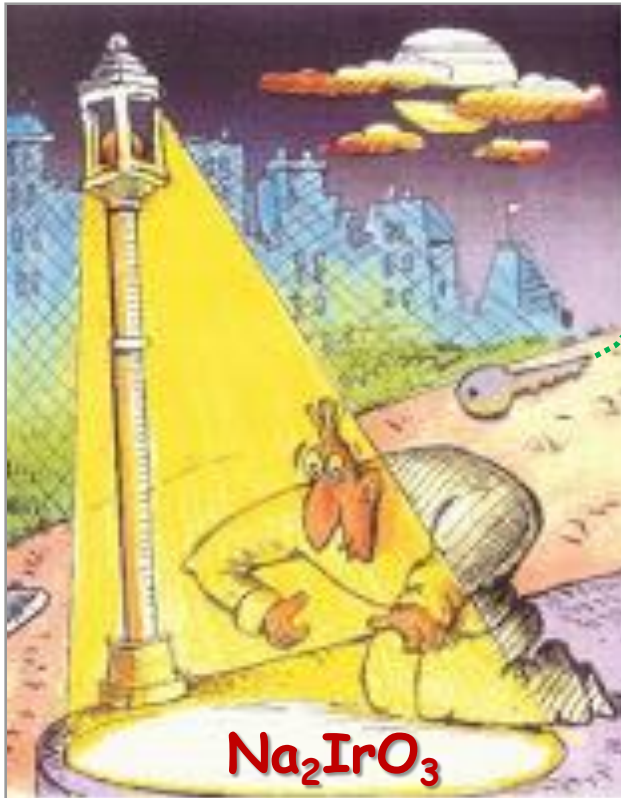
Data collected so far suggests that

- Kitaev term seems to be dominant
- Other terms are substantial, yet to be sorted out

*measure and fit,
measure and fit...*

*most wanted:
single-crystal
 $S(q,w)$*

The streetlight effect



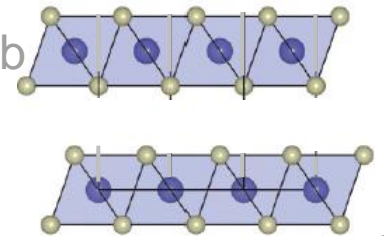
- Did you lose your Majoranas here?
- No, but the light is much better over here!

New candidate:



Plumb et al, 2014

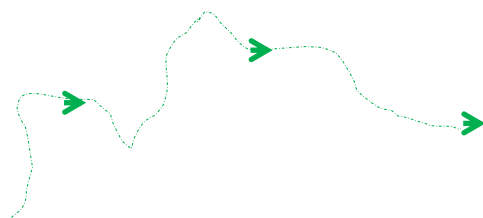
honeycomb



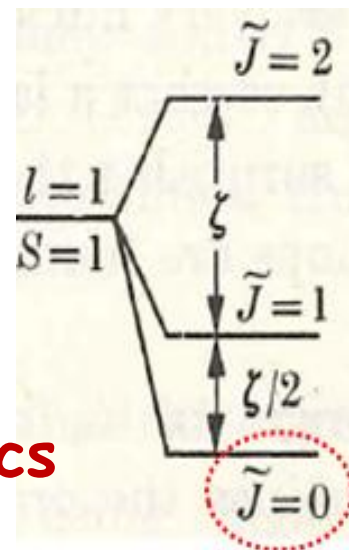
...farther away from the streetlight



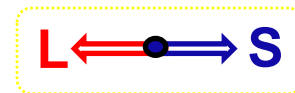
d^5 Co, Rh, Ir



J=0 physics



d^4 Ru, Os, ...



„nonmagnetic“ Mott insulators

GKh (2013)

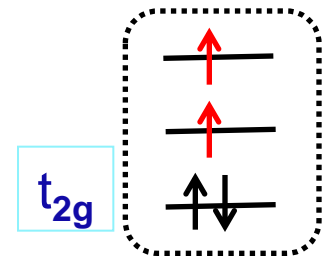
Meetei, Cole, Randeria, Trivedi (2015)

d^4 Mott insulators



4d, 5d electrons

1. Low-spin $S=1$
2. Unquenched $L=1$



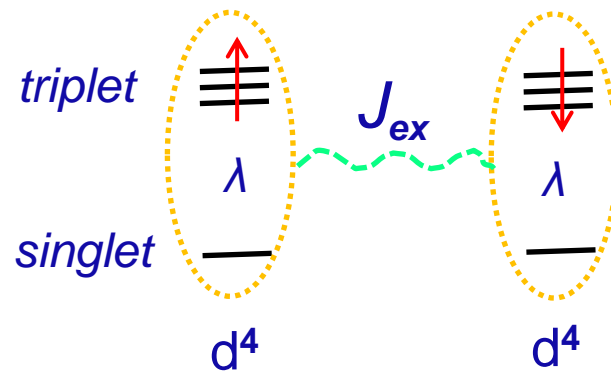
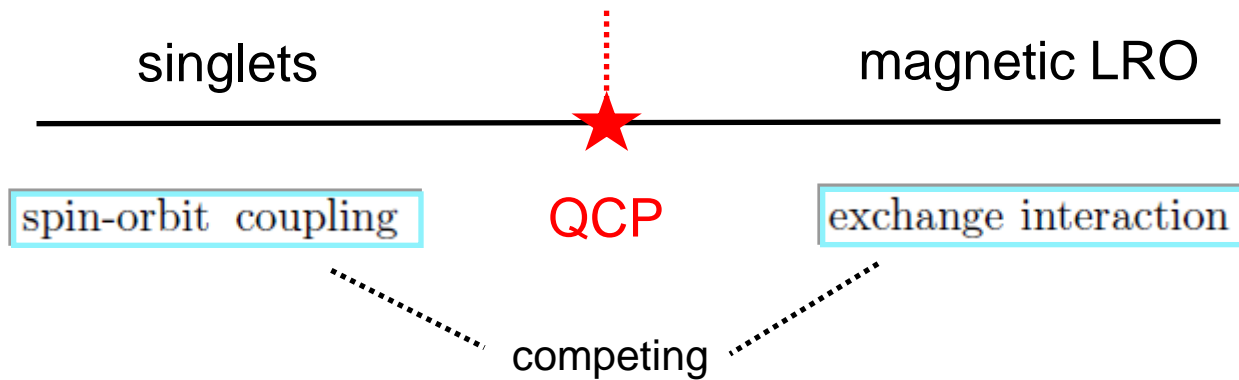
$\lambda(\text{LS})$



$$J=S+L=0$$

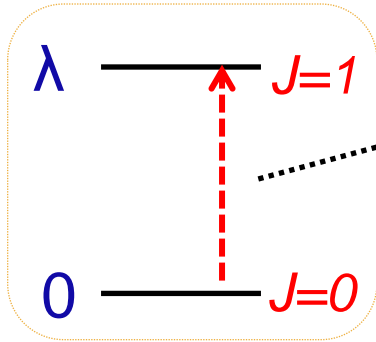
...no spin left to play with ...

$J=0$ physics: *spin-orbit driven magnetic QCP*



d^4 ion: Van-Vleck magnetism

(i) *There are no „pre-existing“ moments*

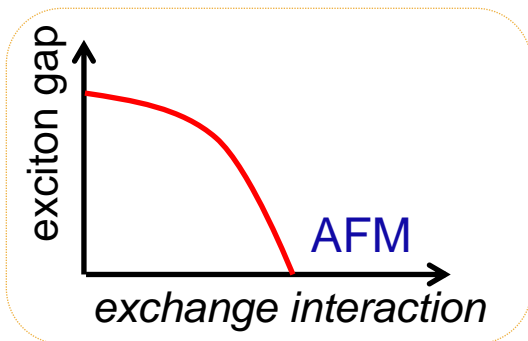


(ii) $J=0$ to $J=1$ transition: off-diagonal magnetic moment $M=2S-L$
(„spin-orbit exciton“)

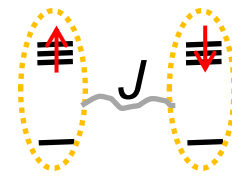
(iii) *Condensation of spin-orbit exciton*



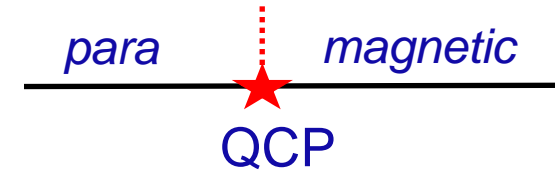
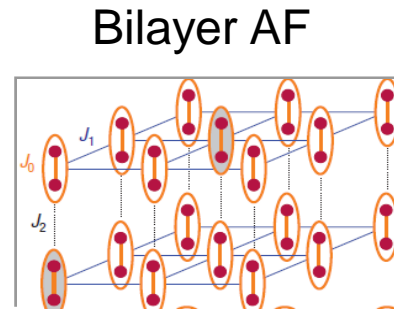
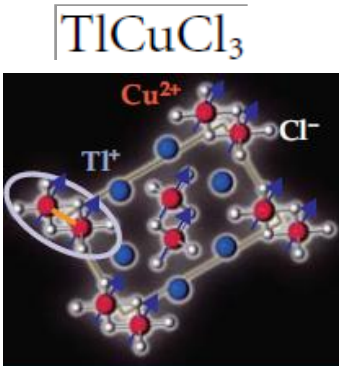
„excitonic“ magnetism



Singlet-triplet examples



(A) Weakly coupled dimers



THIERRY GIAMARCHI^{1*}, CHRISTIAN RÜEGG^{2*}
AND OLEG TCHERNYSHYOV^{3*} (*Nat.Phys.* 2009)

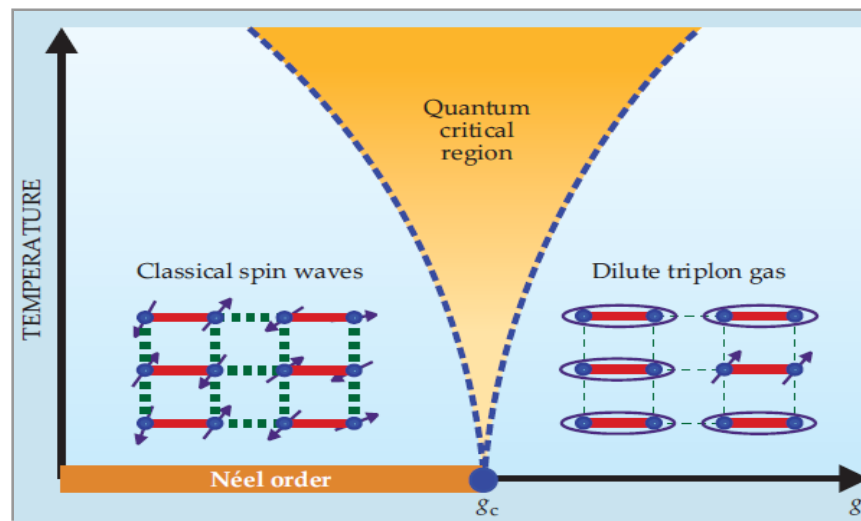
(B) *4f Pr compounds* (broad literature since 1970's)

(C) *e_g orbital FeSc₂S₄* (Chen, Balents, Schnyder, 2009)

(D) *Spin-state-crossover in Fe-based SC* (Chaloupka & GKh, 2013)

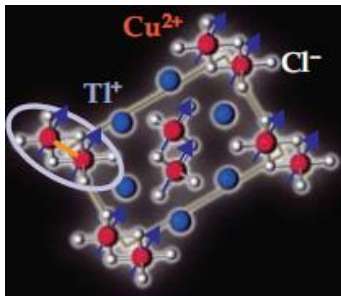
QUANTUM CRITICALITY

Sachdev, Keimer,
Phys.Today, 2011



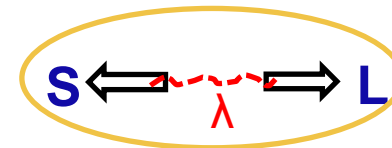
*birthplace for
„unconventional“ physics*

Inter-ionic dimers



-small energies
-special geometry

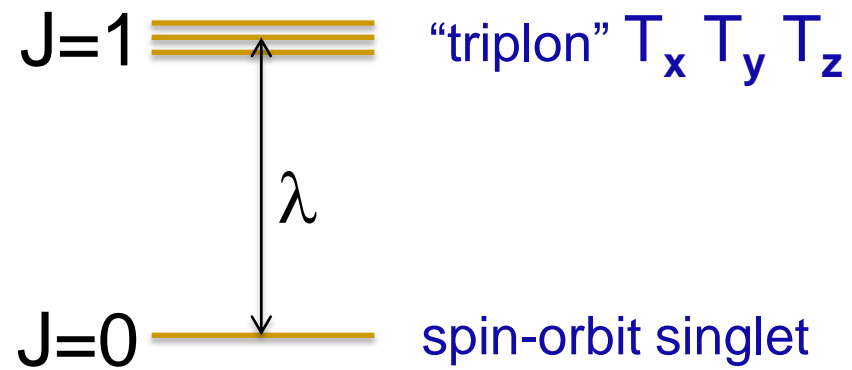
d^4 : Intra-ionic „dimer“
made of S and L



- 1) energetic (~ 100 meV)
- 2) generic (any lattice)

GKh (2013)

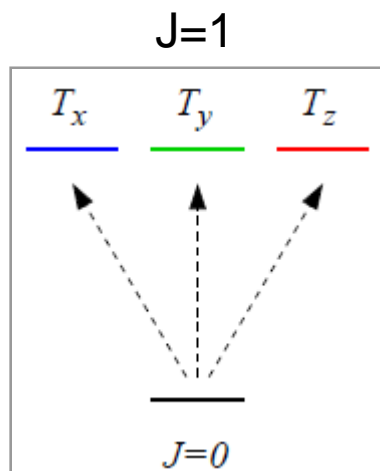
d^4 Mott insulator: single-ion states



express S and L via spin-one T-bosons

$$S = -i\sqrt{\frac{2}{3}}(T - T^\dagger) + \frac{1}{2}J$$

$$L = i\sqrt{\frac{2}{3}}(T - T^\dagger) + \frac{1}{2}J$$



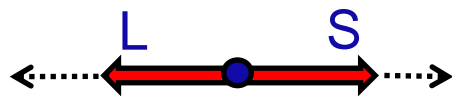
magnetic moment $M=2S-L$:

$$M = -i\sqrt{6} (T - T^\dagger) + g_J J$$

condensed

uncondensed

Bose condensation of T bosons:
finite L and S, finite M



However, $J=S+L=0$!

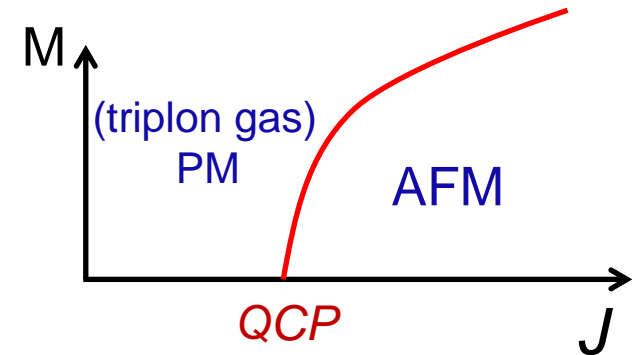
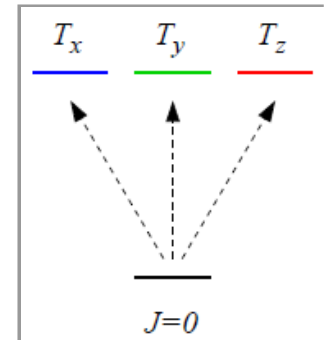
d⁴ Mott insulator: singlet-triplet model (180°)

GKh (2013)

(e.g. 214-perovskite)

$$H = \lambda \sum_i n_i + J \frac{2}{9} \sum_{ij} [T_i^\dagger \cdot T_j - \frac{7}{16} (T_i \cdot T_j + H.c.)]$$

spin-orbit
 exchange
 S=1 boson



LRO moment:

$$M_z = 2\sqrt{6\rho(1-\rho)}$$

$$\rho = \frac{1}{2}(1 - \tau^{-1})$$

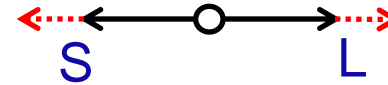
cond. density

$$\tau = \kappa/\kappa_c > 1$$

distance from QCP

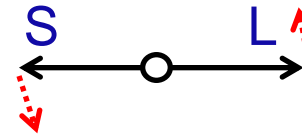
Excitations:

1. The amplitude mode
changing the lengths of S & L



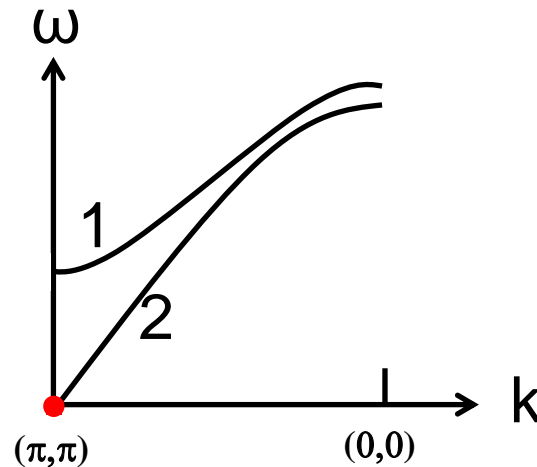
„Higgs“

2. The phase modes
in-phase rotation of S & L



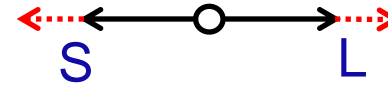
Goldstone

*magnons in
excitonic AF*



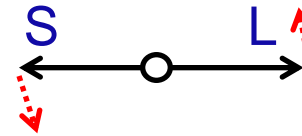
Excitations:

1. The amplitude mode
changing the lengths of S & L

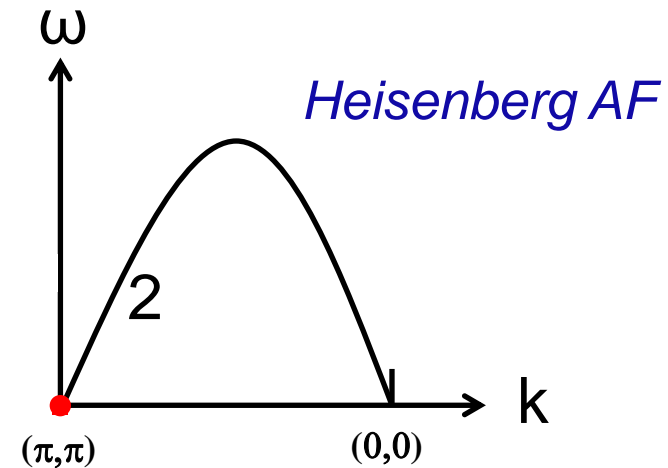
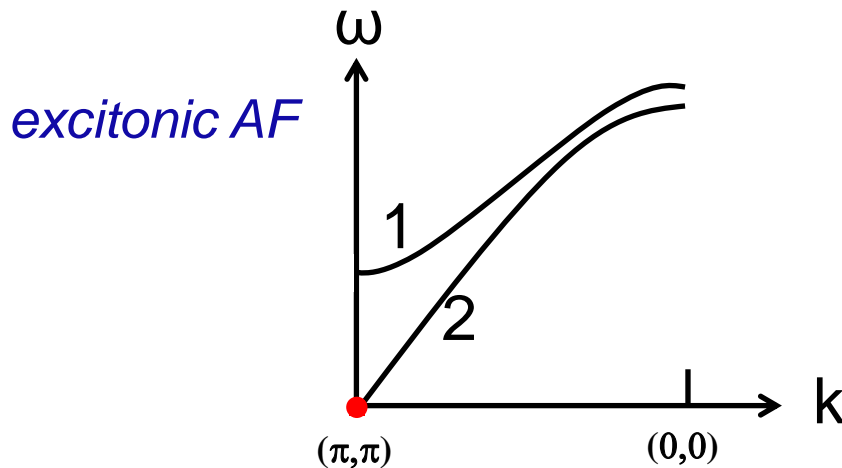


„Higgs“

2. The phase modes
in-phase rotation of S & L

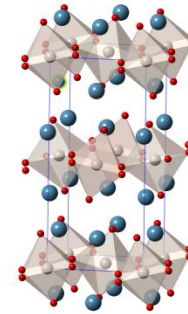


Goldstone



Van Vleck-type d^4 Mott insulators:
EXCITONIC magnetism

Candidate material:



- Metal-to-insulator transition at 360 K
- Phase transition of unknown origin at 260 K (*Keimer et al. 2005*)
- Canted AF below $T_N=110$ K

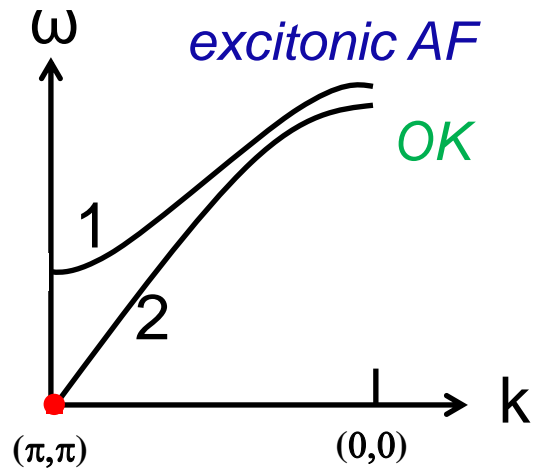
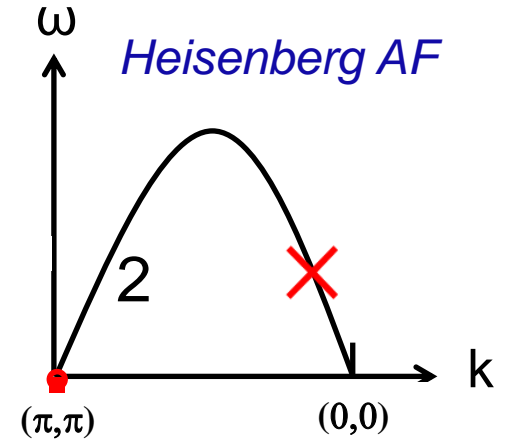
Ca_2RuO_4 single crystal, INS (B.J. Kim et al, 2015)

data

✓ far from Heisenberg

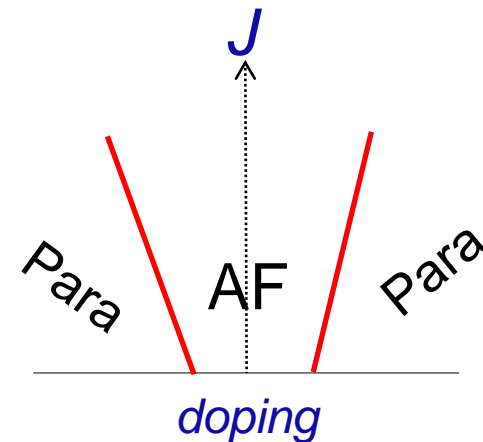
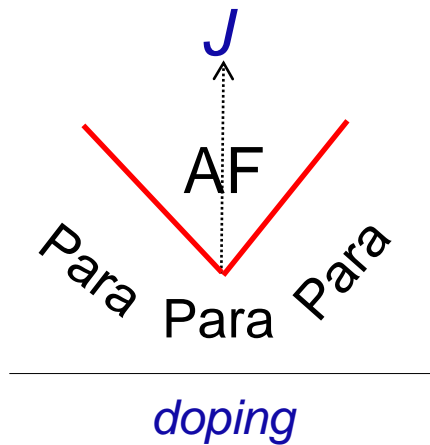
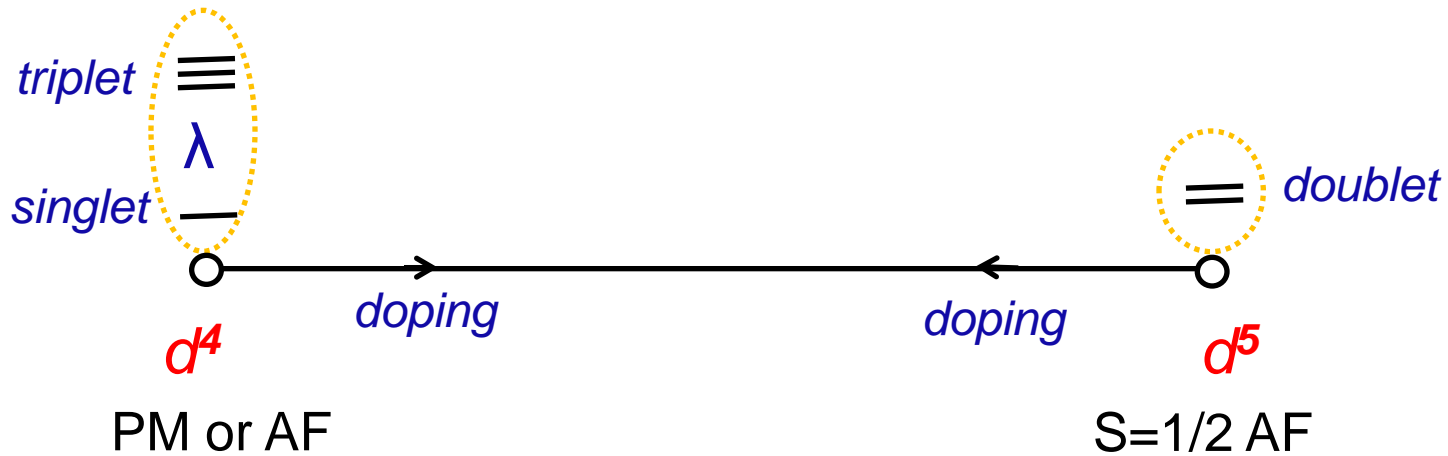
✓ strong SOC

(to be published)

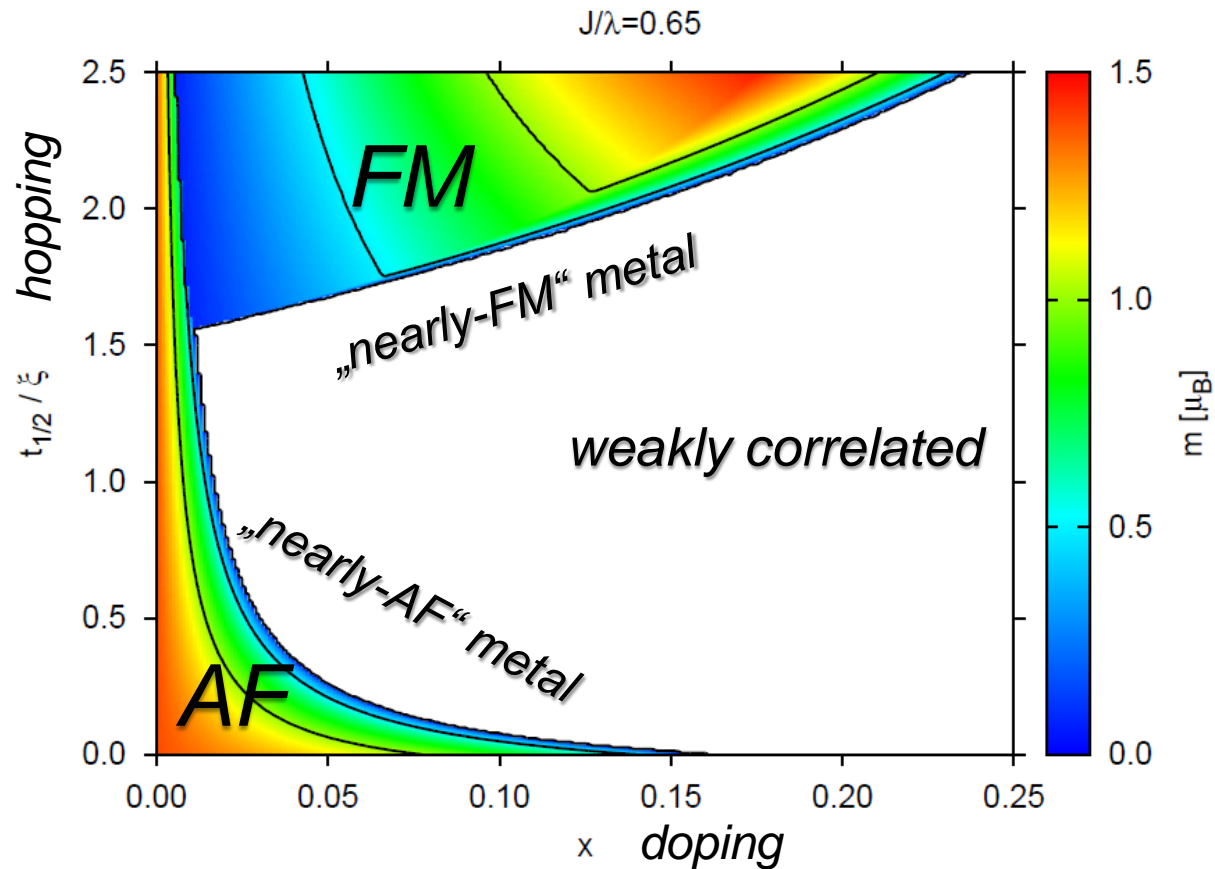


Doping of „nonmagnetic“ d^4 Mott insulators

Chaloupka & GKh (unpublished)



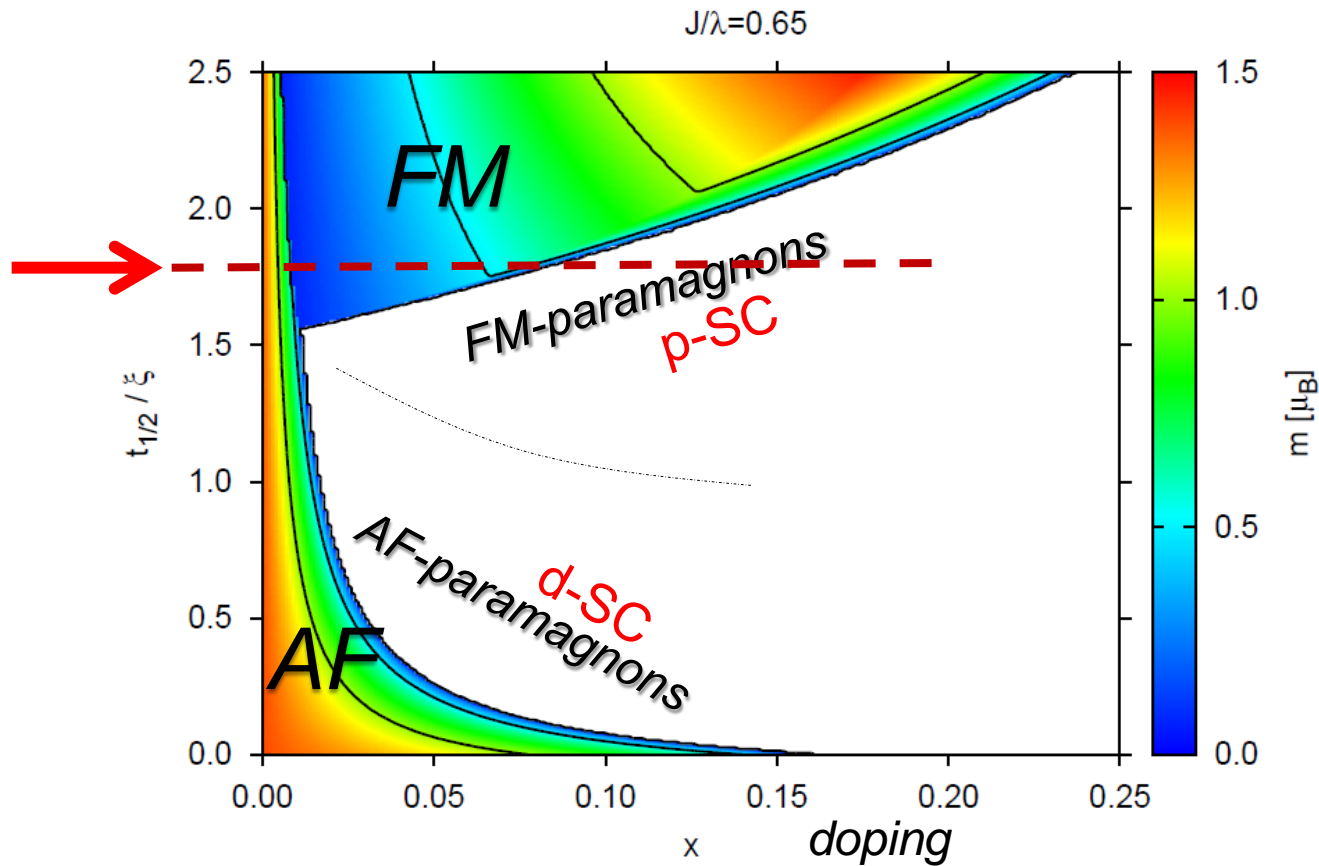
Phase diagram: doping x vs hopping t



AF --- nearly AF metal --- nearly FM metal --- FM

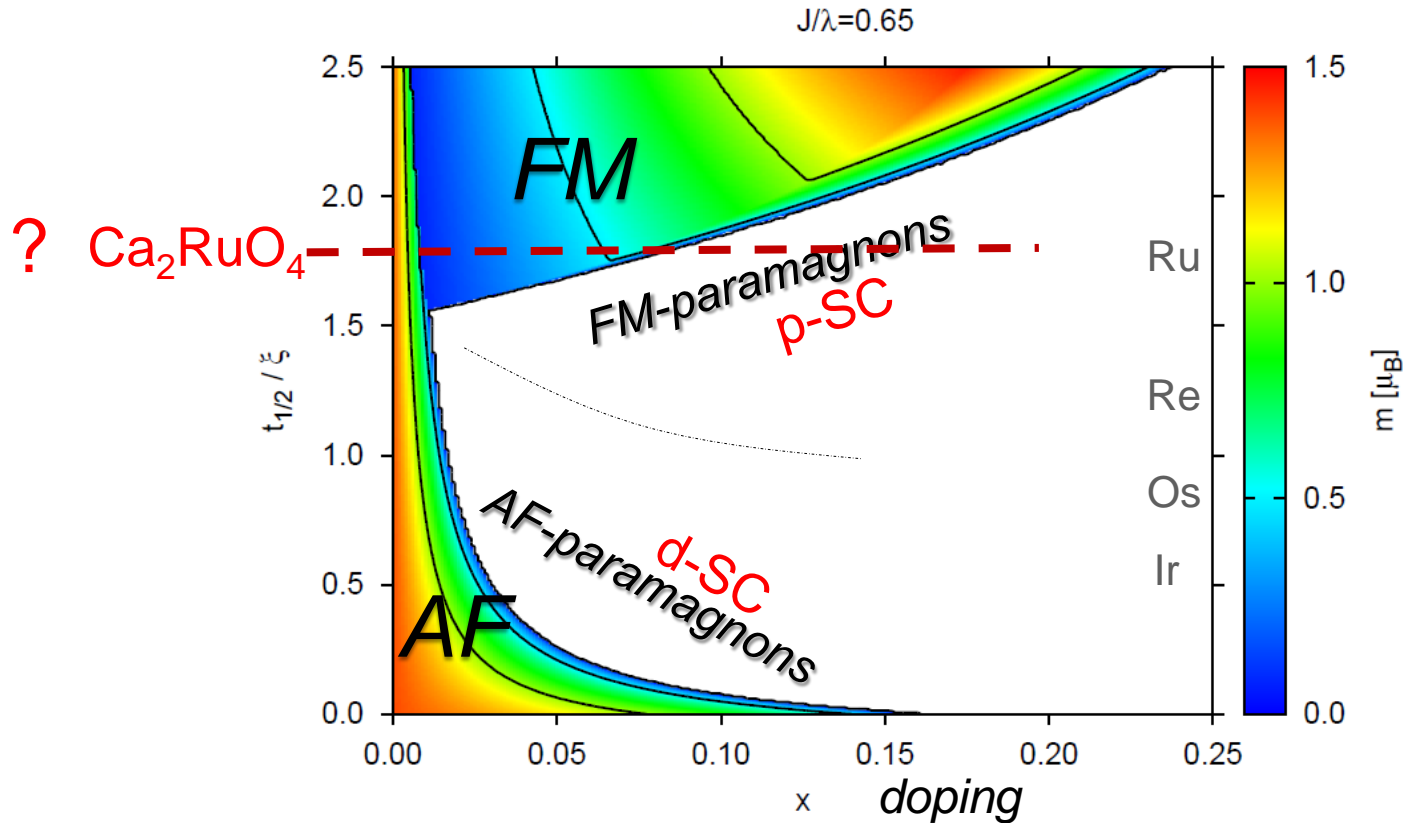
...all emerging out of the „nonmagnetic $J=0$ “ state

Doping of „nonmagnetic“ d^4 Mott insulators



„Paramagnon-gluе“: *triplet or singlet SC-pairing*

Doping of „nonmagnetic“ d⁴ Mott insulators



„Sample“



t_{2g}^4 ions: Re^{3+} , Ru^{4+} , Os^{4+} , Ir^{5+}

Mott insulator to start with, better 2D
Spin-orbit comparable to hopping t

Singlet-triplet model $H_{eff}(90^\circ)$

GKh (2013)

(triangular, honeycomb, kagome...)

c-bond:

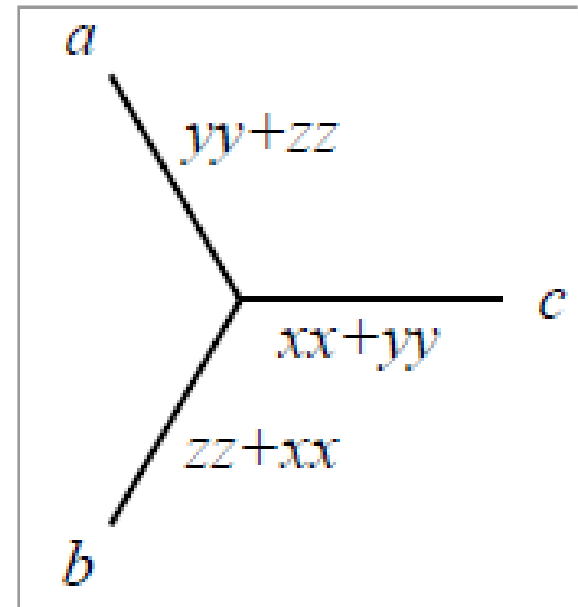
$$\frac{2}{3}(T_{ix}^\dagger T_{jx} + T_{iy}^\dagger T_{jy}) - \frac{5}{6}(T_{ix} T_{jx} + T_{iy} T_{jy}) + H.c.,$$

hopping

pair-generation

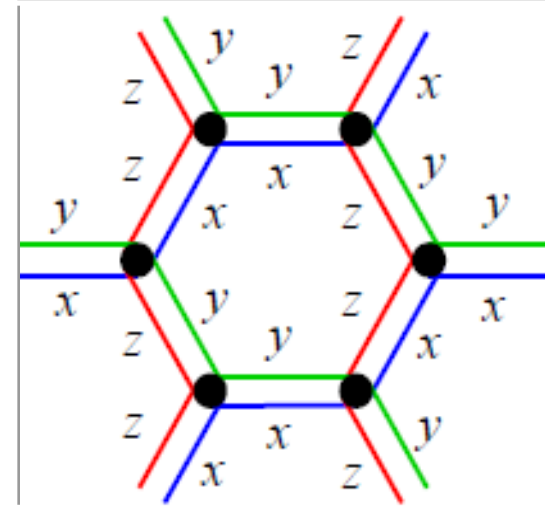
x and y type bosons only involved

Bond-dependent „xy-model“:



Honeycomb lattice: **FLAT BANDS**

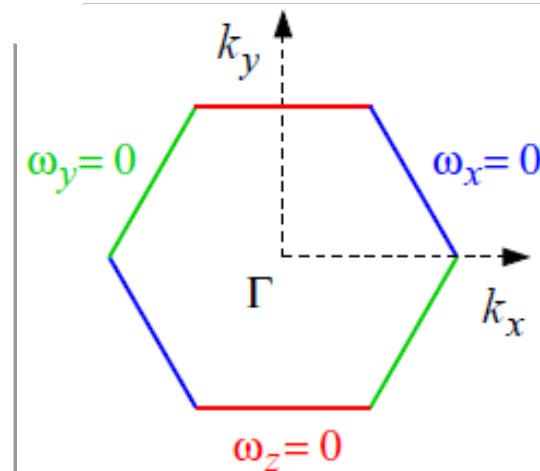
□ Each flavor T_x , T_y , T_z has its own zigzag to move along



□ **1D dispersion:**

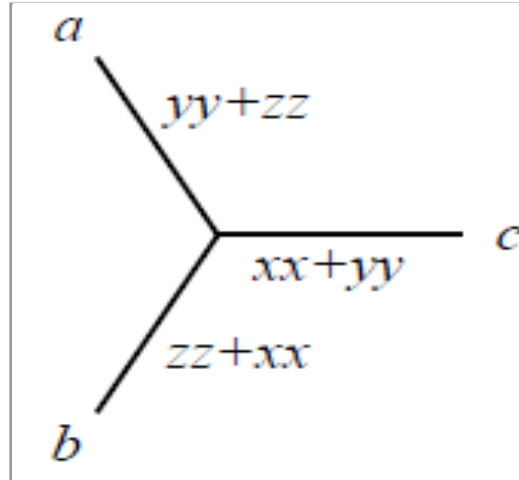
$$|\omega_z(\mathbf{k}) \equiv \omega_z(k_y) \simeq \lambda \sqrt{1 + (\kappa/\kappa_c)C_y}$$

□ $J=J_{\text{crit}}$: **zero-energy lines**

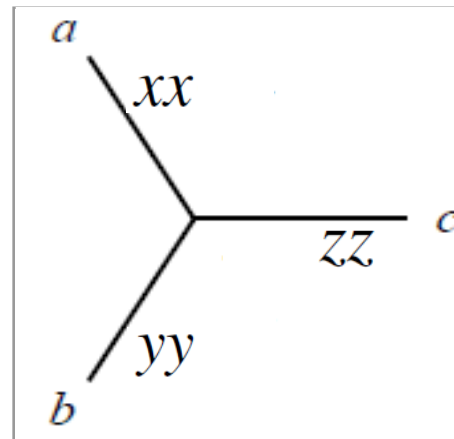


Boson exchange, two channels: t (via oxygen) vs t' (direct overlap)

Via oxygen t :
-bond-dependent „xy“



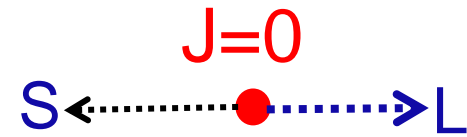
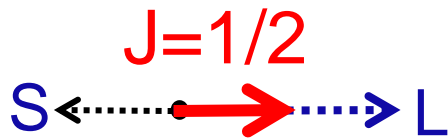
Direct overlap t' :
-bond-dependent „Ising“



Unusual $S=1$ boson models

VBS?
nematic?
superfluid?

Summary



$J=S+L$ inherits bond-dependent
& frustrated nature of orbitals

„nonmagnetic“ $J=0$
Mott insulators



unconventional magnetism



...unconventional SC?