

Topological phases in pyrochlore iridate thin films

Gregory A. Fiete
University of Texas at Austin



Chief Collaborators on Iridate Films



Andreas Ruegg



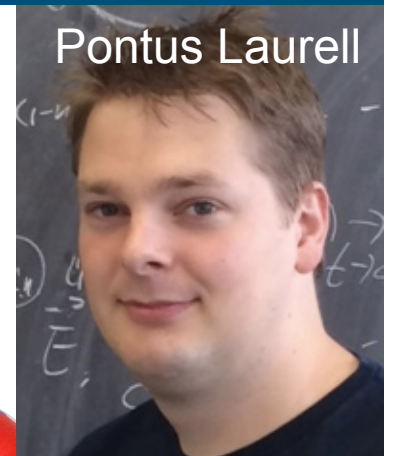
Xiang Hu



Zhicheng Zhong



Qi Chen



Pontus Laurell

X. Hu, A. Ruegg, *GAF Phys. Rev. B* **86**, 235141 (2012) [Editor's Suggestion]

X. Hu, Z. Zhong, *GAF Sci. Rep.* **5**, 11072 (2015).

Q. Chen, H.-H. Hung, X. Hu, *GAF Phys. Rev. B* **92**, 085145 (2015)

P. Laurell, *GAF (In preparation)*

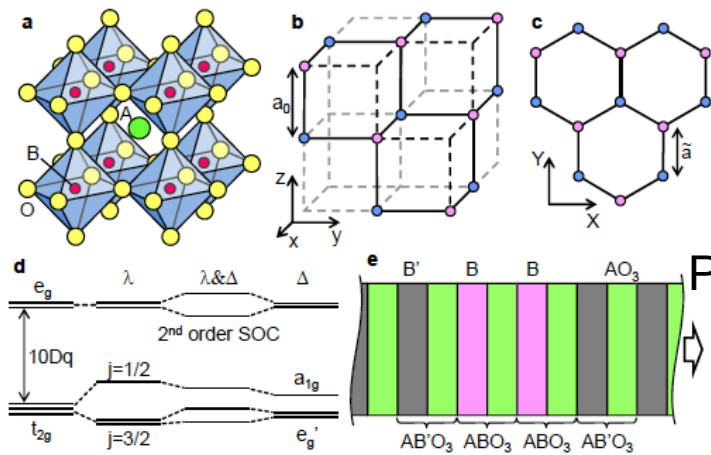
Mini-topical review: GAF and A. Ruegg *J. Appl. Physics* **117**, 172602 (2015).
"Topological Phases in Oxide Heterostructures with Light and Heavy Transition Metal ions"

Talk Outline

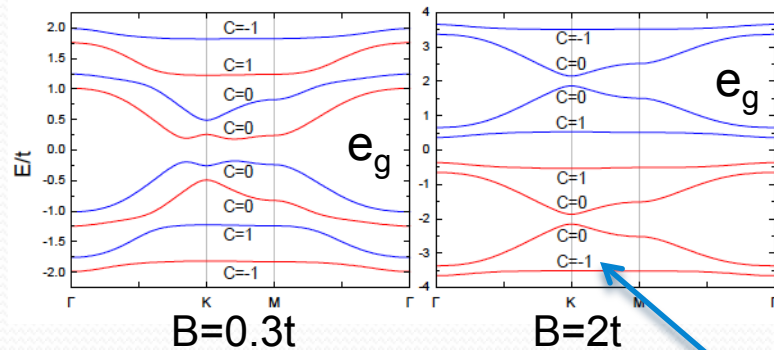
- Film geometry
 - Bilayer films along $[111]$ direction
 - Trilayer films along $[111]$ direction
- Weak coupling
 - Model Hamiltonian+Hartree-Fock
 - Model Hamiltonian+DMFT
 - First-principles+Hartree-Fock
- Strong coupling
 - Spin-wave analysis

An interesting direction for topological phases: oxide heterostructures along [111]: ABO_3 example

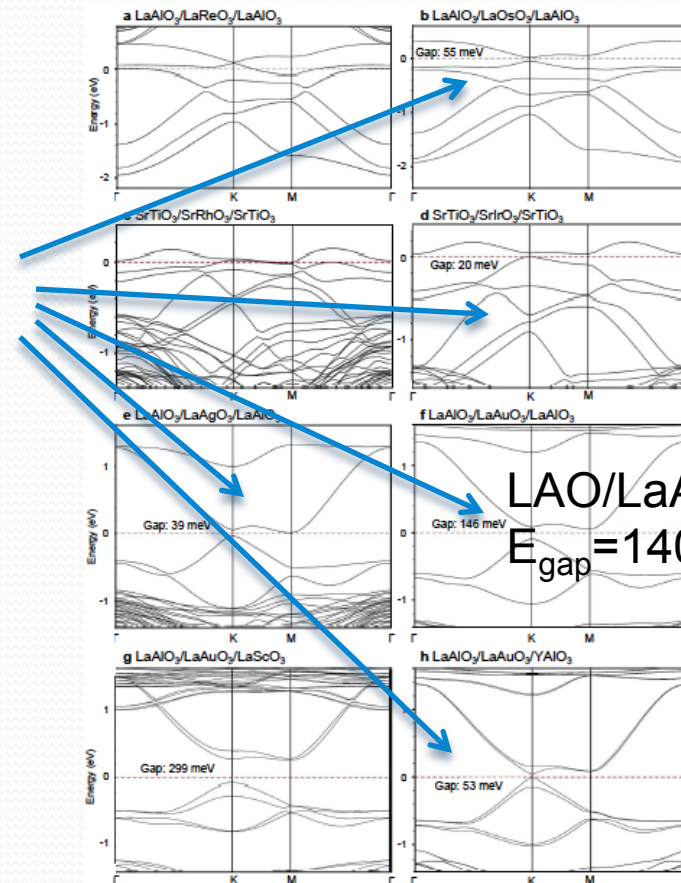
D. Xiao, W. Zhu, Y. Ran, N. Nagaosa, and S. Okamoto Nat. Comm. (2011)



Potential TI



Potential fractional quantum Hall states



$LAO/LaAuO_3/LAO$
 $E_{gap} = 1400 K$

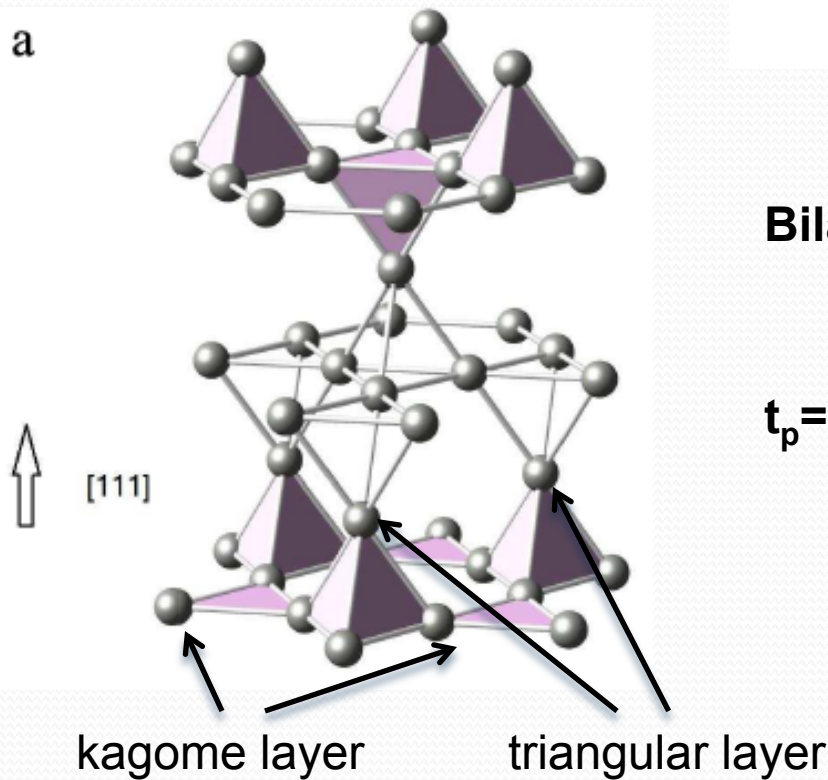
Topological phases in bilayer and trilayer pyrochlore systems along (111): $A_2Ir_2O_7$

Hu, Ruegg, Fiete PRB (2012) Editors' Suggestion

B.-J. Yang and N. Nagaosa, PRL (2014)

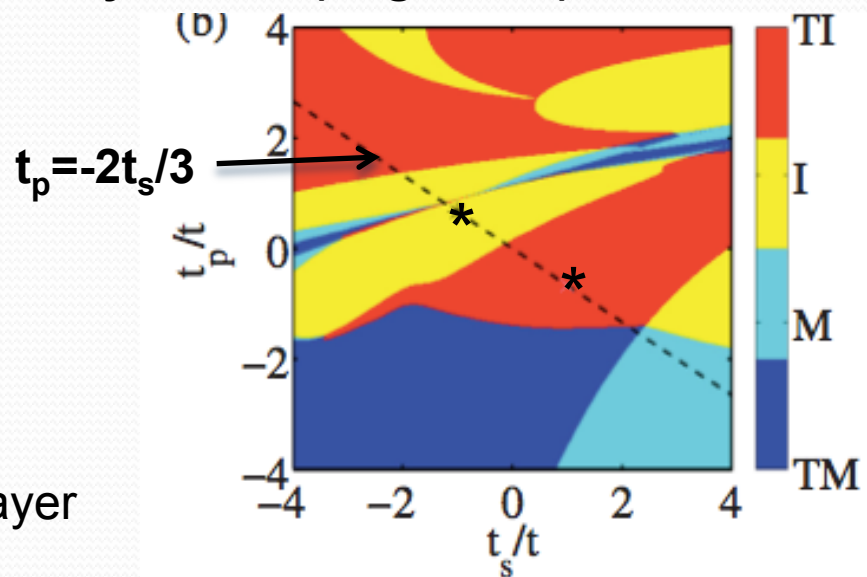
$$H_0 = \sum_{\langle i,j \rangle, \alpha, \beta} t_{i\alpha, j\beta} c_{i\alpha}^\dagger c_{j\beta} - \lambda \sum_i \mathbf{l}_i \cdot \mathbf{s}_i$$

$$t_{i\alpha, j\beta} = t_{i\alpha, j\beta}^{\text{in}} + t_{i\alpha, j\beta}^{\text{dir}}$$



Bilayer, $\lambda=4t$ (large SOC)

$J_{\text{eff}}=1/2$ only!



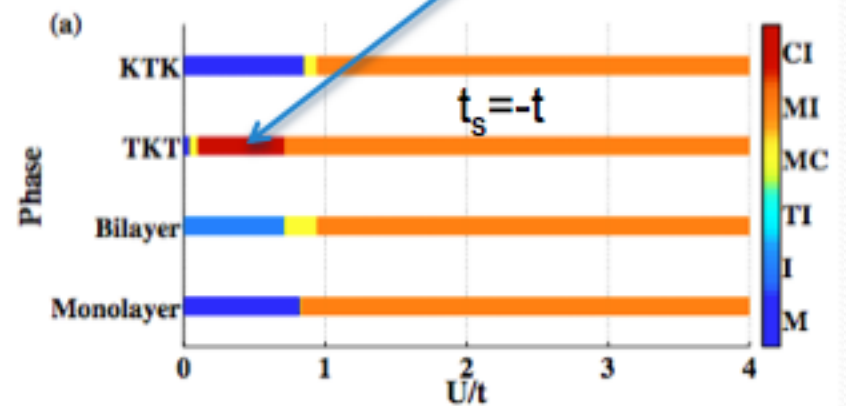
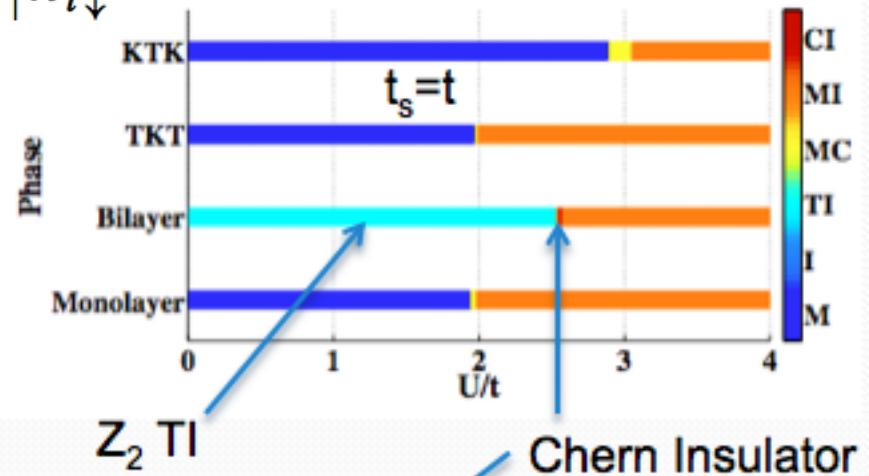
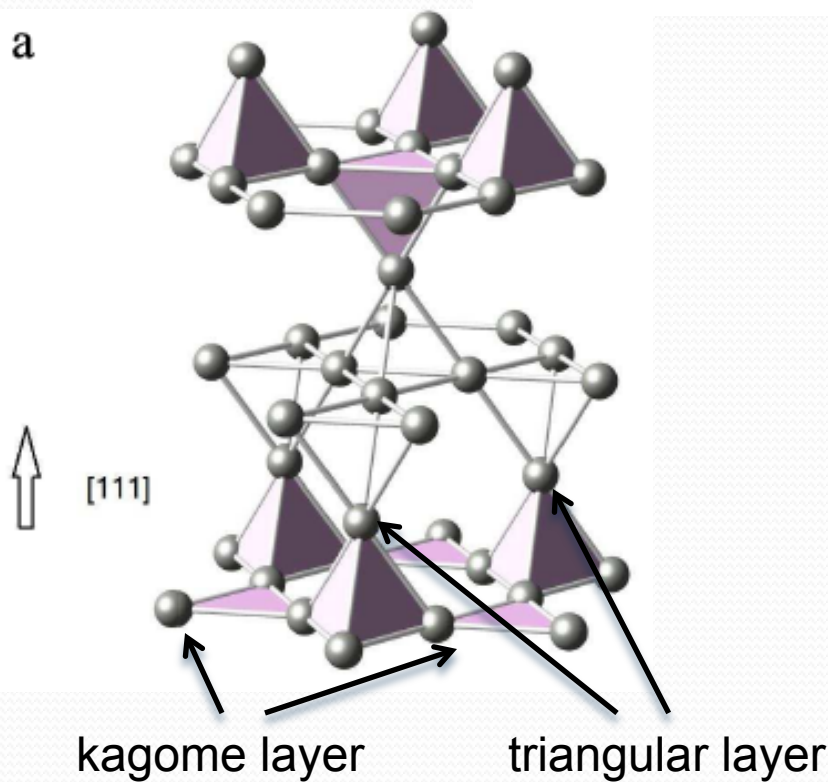
Topological phases in bilayer and trilayer pyrochlore systems along (111): $A_2Ir_2O_7$

Hu, Ruegg, Fiete PRB (2012) Editors' Suggestion

$J_{\text{eff}}=1/2$ only!

$$H_U = U \sum n_{i\uparrow} n_{i\downarrow}$$

Hartree-Fock Phase Diagram

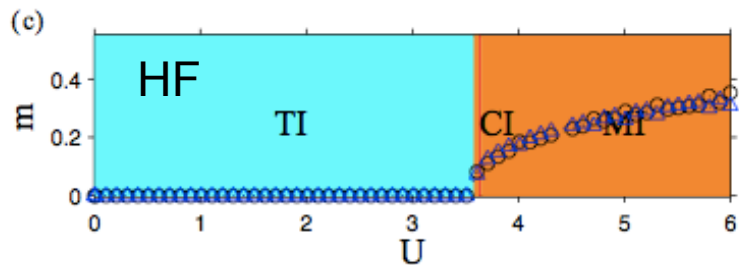
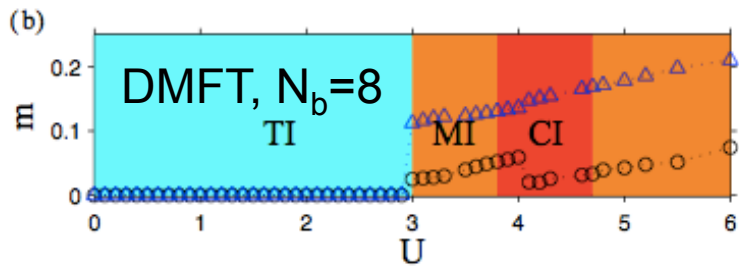
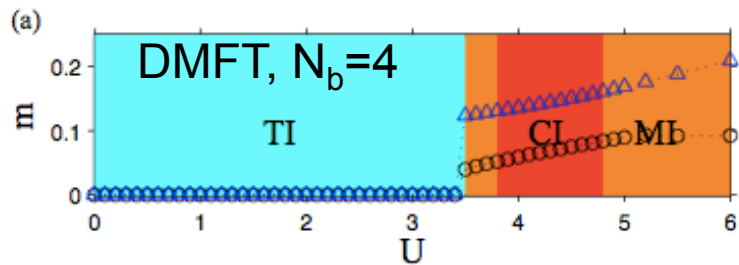


Comparison of DMFT and HF Phase Diagrams

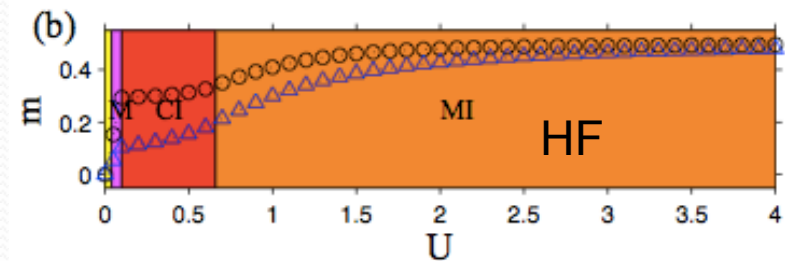
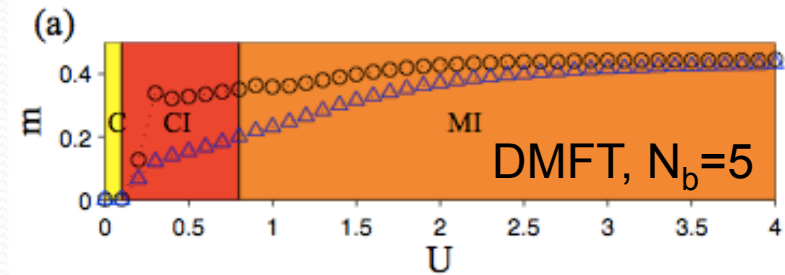
Chen, Hung, Hu, *GAF Phys. Rev. B* **92**, 085145 (2015)

$J_{\text{eff}}=1/2$ only!

Bilayer Film



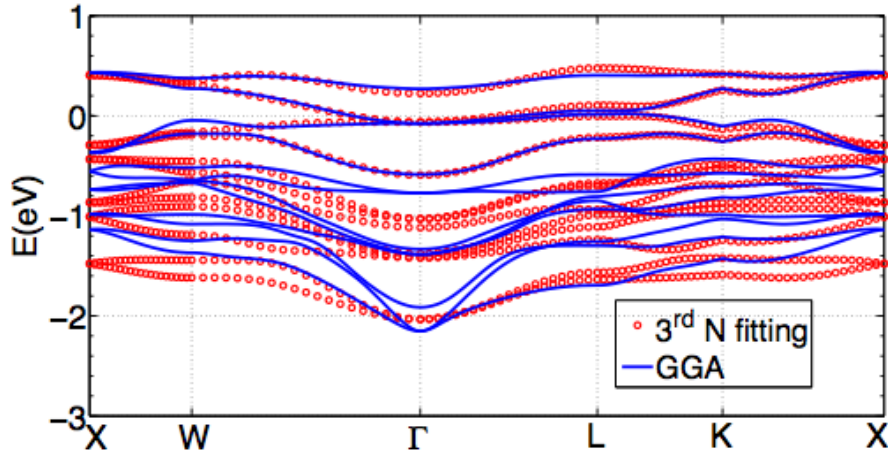
Trilayer Film



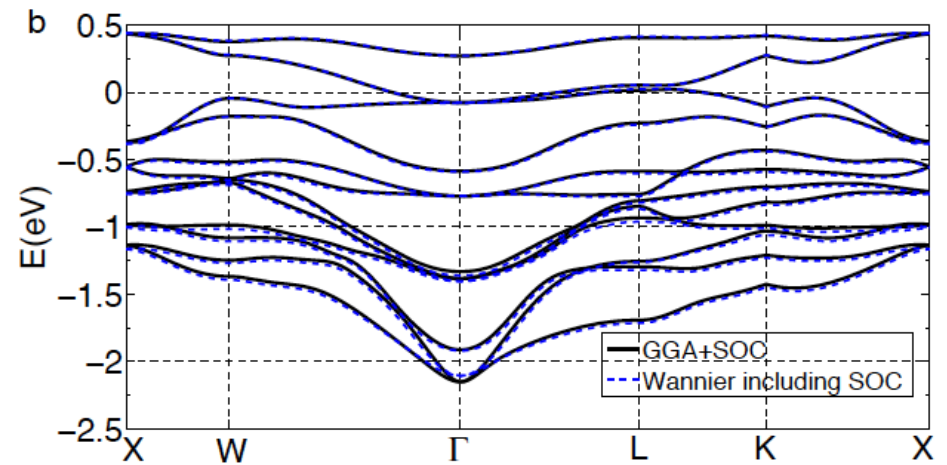
Overall, fairly good agreement. Appears quantum fluctuations may help stabilize CI in bilayer.

First Principles Study of $Y_2Ir_2O_7$: Fitting the band (bulk) band structure

Hu, Zhong, Fiete Sci. Rep. (2015)



Tight-binding fit

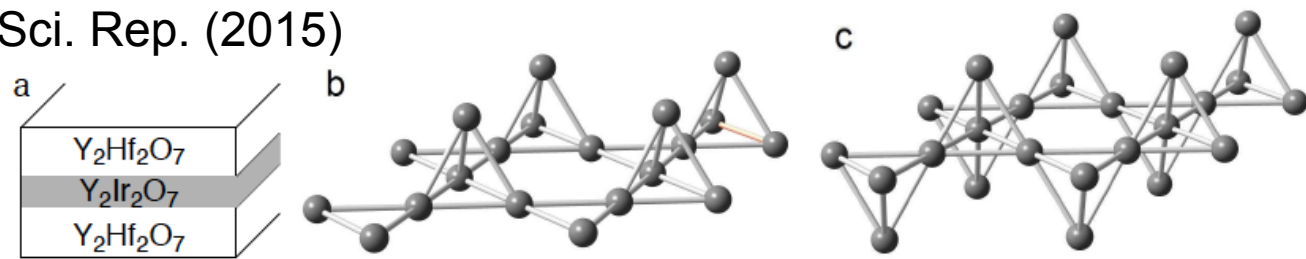


Wannier Fit

More extended 5d-orbitals are not well fit by tight binding!

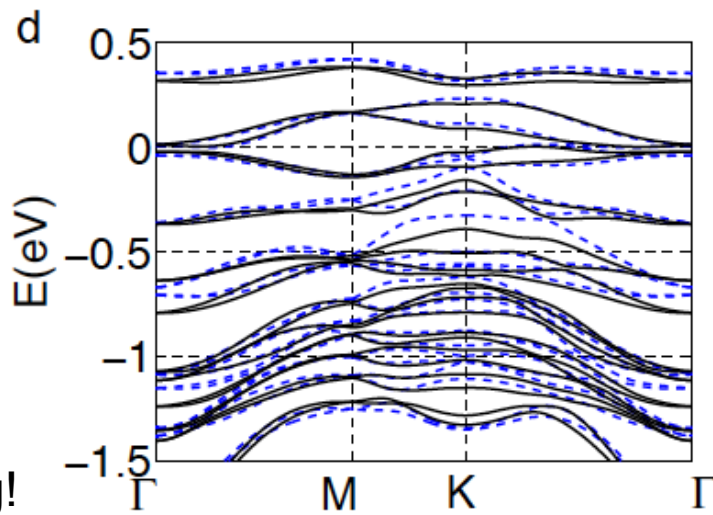
First Principles Study of $Y_2Ir_2O_7$: Fitting the band *thin-film* band structure \rightarrow Hartree-Fock study

Hu, Zhong, Fiete Sci. Rep. (2015)

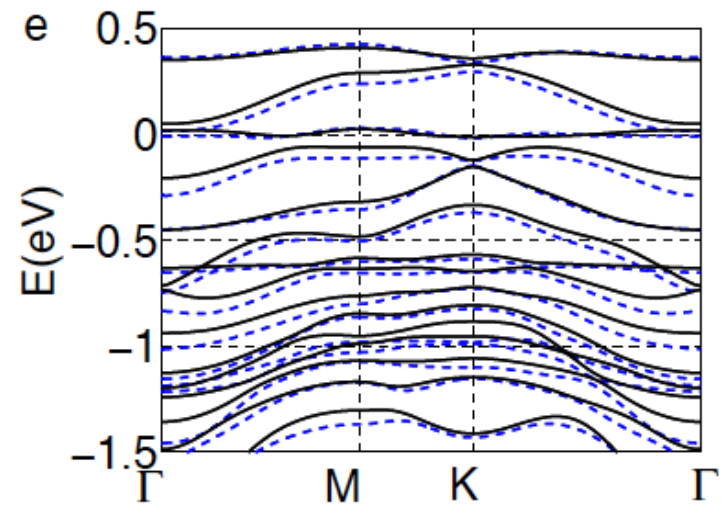


Wannier fits

No clear $j=1/2$ & $j=3/2$ splitting!



bilayer



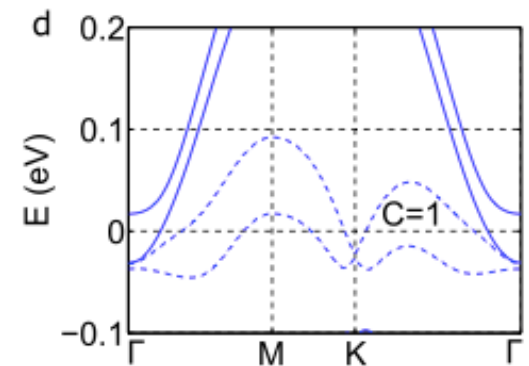
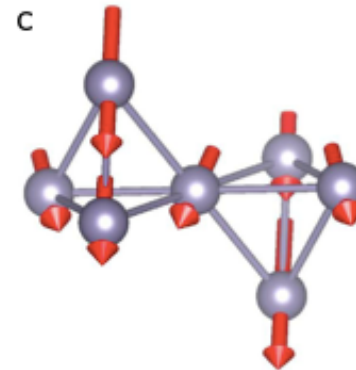
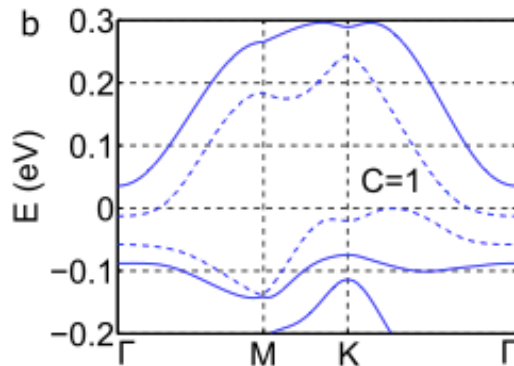
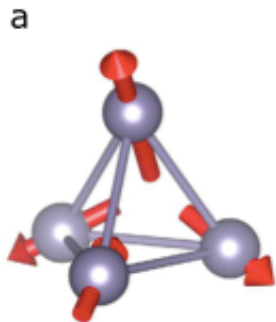
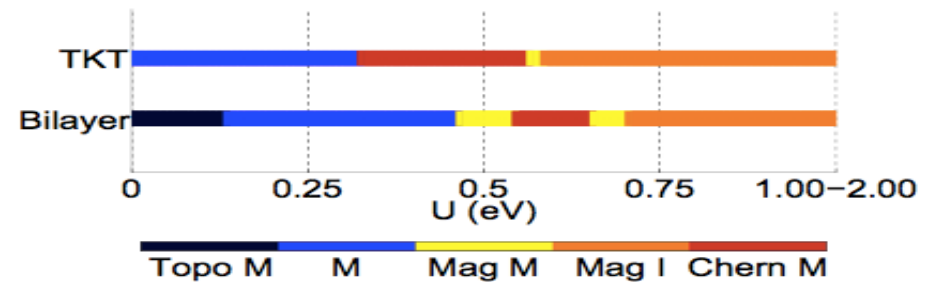
TKT trilayer

Hartree-Fock study of [111] bilayer and trilayer $\text{Y}_2\text{Ir}_2\text{O}_7$

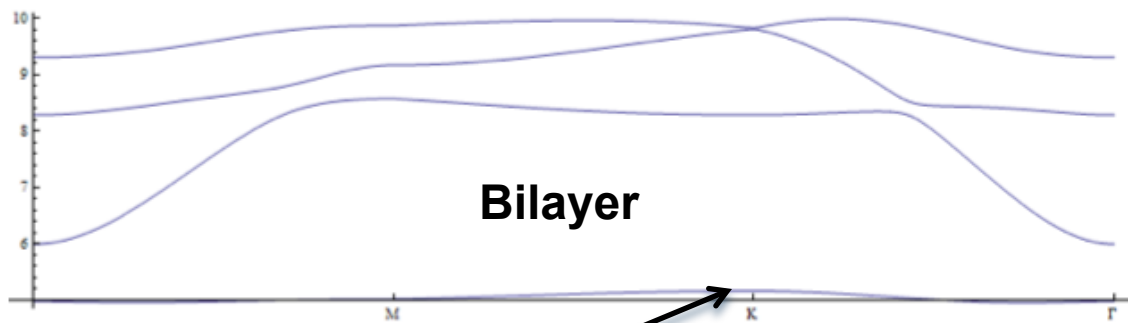
Hu, Zhong, Fiete Sci. Rep. (2015)

$$H = \sum_{i,j,\alpha,\beta} \tilde{t}_{i\alpha,j\beta} c_{i\alpha}^\dagger c_{j\beta} + \frac{U}{2} \sum_i \left(\sum_\alpha \hat{n}_{i\alpha} - 5 \right)^2 \quad \leftarrow \text{Full } t_{2g} \text{ manifold}$$

Hartree-Fock Phase Diagram:



Magnetic excitations in the strong coupling limit: Flat Magnon Bands with Chern number=1

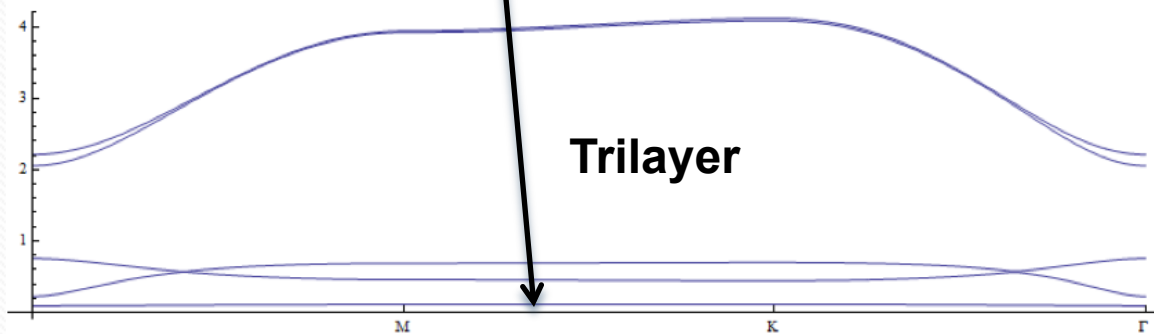


$$H = \sum_{ij} \left[R_i^T \Lambda_{ij} R_j \right]^{ab} \tilde{S}_i^a \tilde{S}_j^b$$

$$\equiv \sum_{ij} \tilde{\Lambda}_{ij}^{ab} \tilde{S}_i^a \tilde{S}_j^b.$$

$$\Lambda_{ij}^{ab} = J \delta^{ab} + \epsilon^{abc} D_{ij}^c + \Gamma_{ij}^{ab}$$

Flat bands



$$J = \frac{4}{U} \left(t^2 - \frac{|\mathbf{v}|^2}{3} \right),$$

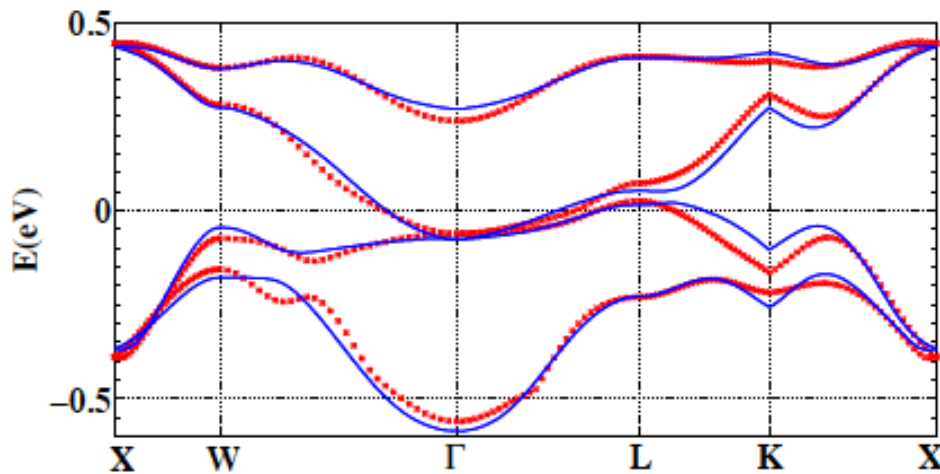
$$D_{ij} = \frac{8}{U} t v_{ij},$$

$$\Gamma_{ij}^{ab} = \frac{8}{U} \left(v_{ij}^a v_{ij}^b - \delta^{ab} \frac{|\mathbf{v}|^2}{3} \right)$$

Summary

- Studied thin film iridates from both weak and strong coupling limits.
- Topological phases (Chern insulators and Chern metals are possible)
- Magnetic excitations may also show topological properties and interesting interaction effects.

Pyrochlore Iridate $\text{Y}_2\text{Ir}_2\text{O}_7$ ($\text{La}_2\text{Ir}_2\text{O}_7$) Thin Films



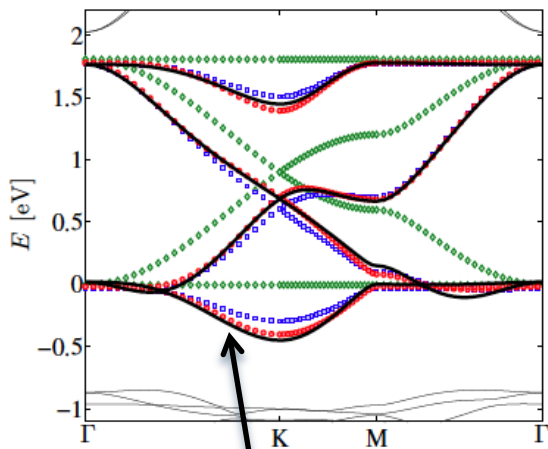
GGA Bandstructure (bulk)

3rd Neighbor tight-binding fit—
need further range hoppings

In the end, we did Wannier fits,
which are indistinguishable to the
eye from DFT.

Extended Phase Diagram for LaNiO₃ Bilayer

Ruegg, Mitra, Demkov, Fiete PRB 85, 245131 (2012)



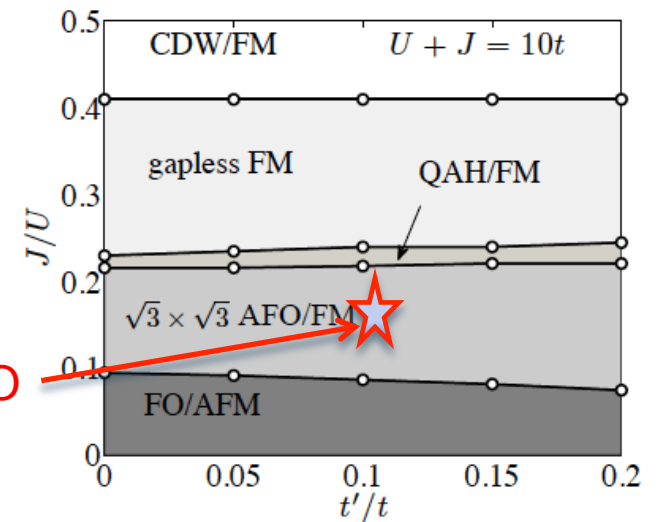
DFT result
(LDA)

1st neighbor 2nd neighbor

fFt	t (eV)	t' (eV)	Δ (eV)	t_δ (eV)	E_F (eV)
A	0.603	0	0	0	-0.701
B	0.600	0.058	0	0	-0.693
C	0.598	0.062	-0.023	0	-0.693
D	0.598	0.062	-0.023	-0.007	-0.693

$$\begin{aligned}
 H_{\text{int}} = \sum_r \left[& U \sum_\alpha n_{r\alpha\uparrow} n_{r\alpha\downarrow} + (U' - J) \sum_{\alpha>\beta,\sigma} n_{r\alpha\sigma} n_{r\beta\sigma} \right. \\
 & + U' \sum_{\alpha\neq\beta} n_{r\alpha\uparrow} n_{r\beta\downarrow} + J \sum_{\alpha\neq\beta} d_{r\alpha\uparrow}^\dagger d_{r\beta\uparrow} d_{r\beta\downarrow}^\dagger d_{r\alpha\downarrow} \\
 & \left. + I \sum_{\alpha\neq\beta} d_{r\alpha\uparrow}^\dagger d_{r\beta\uparrow} d_{r\alpha\downarrow}^\dagger d_{r\beta\downarrow} \right] \cdot \begin{matrix} U=U'+2J \\ I=J \end{matrix}
 \end{aligned}$$

(LNO)



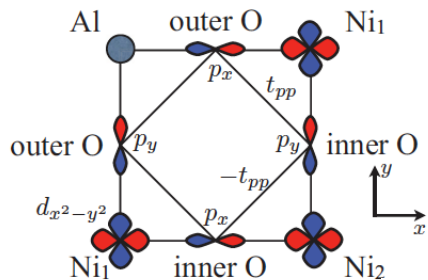
Charge-transfer physics in LaNiO₃ Bilayer (Explicitly retain O *p*-orbitals)

Ruegg, Mitra, Demkov, Fiete PRB 85, 245131 (2012)

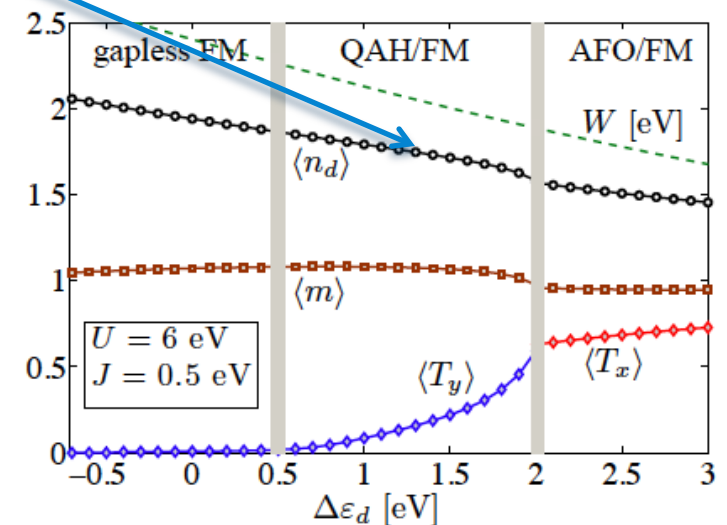
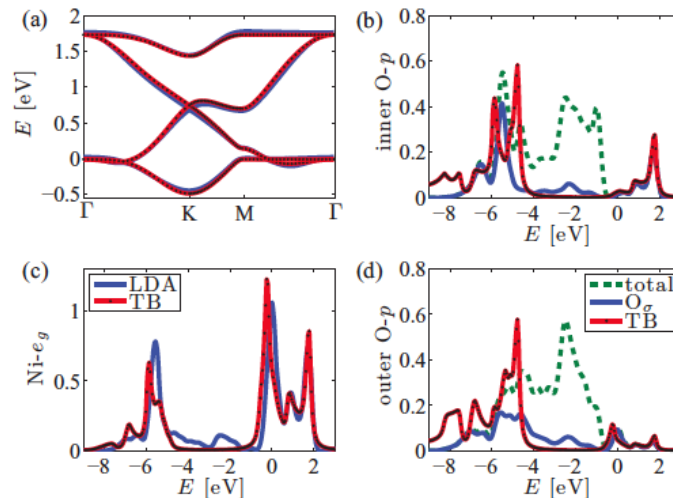
Mean-field (HF)

$$H = \sum_{i\sigma} \epsilon_{pi} p_{i\sigma}^\dagger p_{i\sigma} + \sum_{i\alpha\sigma} \epsilon_d d_{i\alpha\sigma}^\dagger d_{i\alpha\sigma} + H_p + H_{\text{hyb}} + H_{\text{int}} + H_{\text{DC}}$$

$$H_{\text{hyb}} = \sum_{\langle i,j \rangle} (V_{ij}^\alpha p_{i\sigma}^\dagger d_{j\alpha\sigma} + \text{H.c.})$$



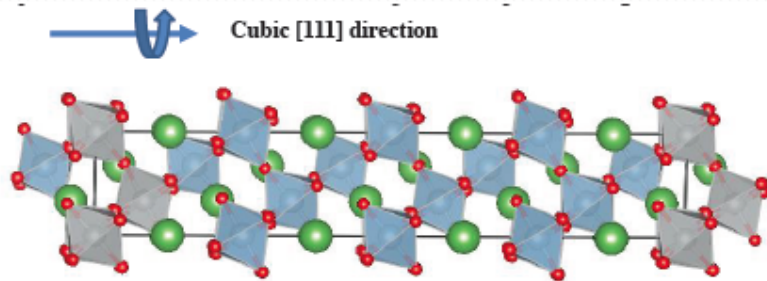
Charge-transfer physics



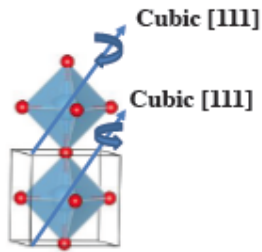
Related work:
Andy Millis Group
(explicit *p*-orbital)

Lattice Strain Effects: Internal

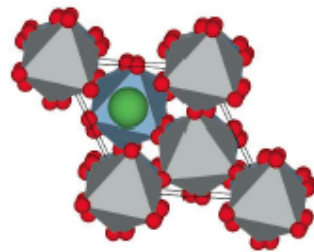
Ruegg, Mitra, Demkov, Fiete PRB (2013)



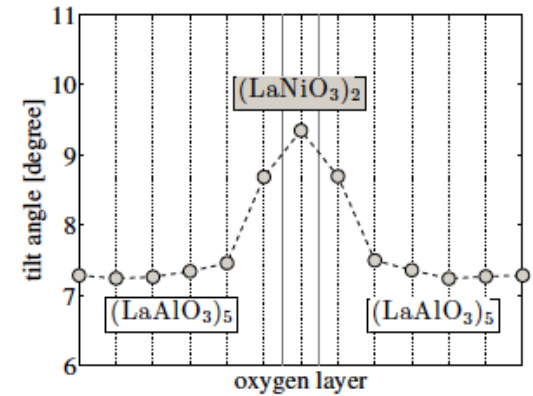
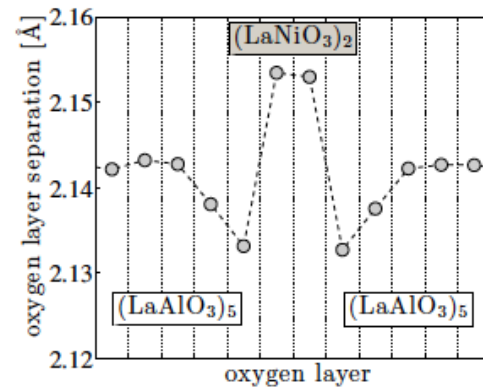
(a) Supercell



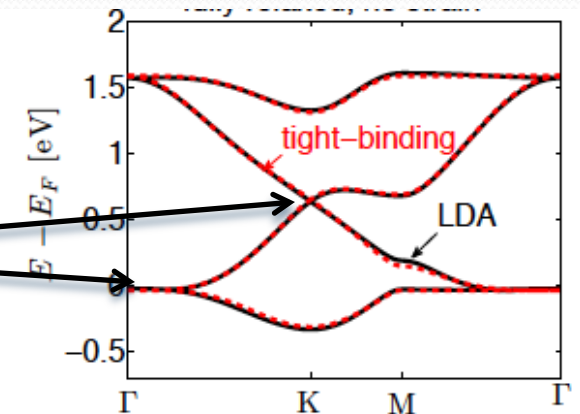
(b) Octahedral tilts



(c) View along [111]



QBCP & Dirac point intact



Internal lattice strain leaves unstrained picture essentially unchanged, even quantitatively!

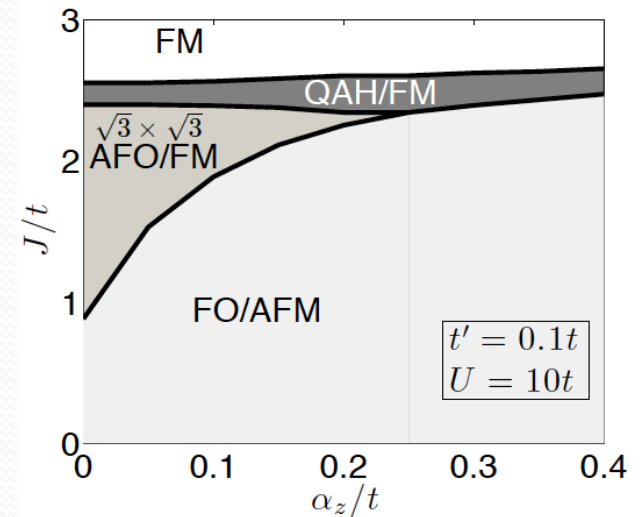
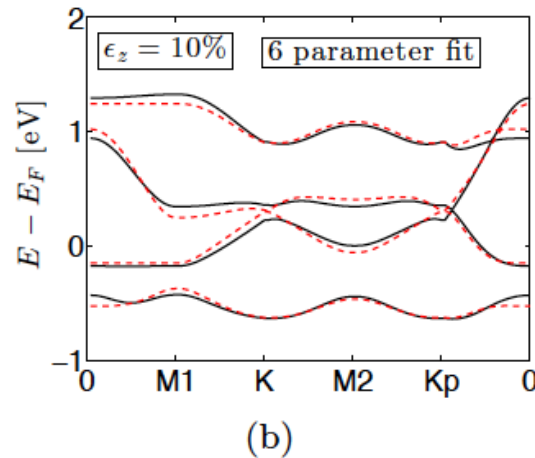
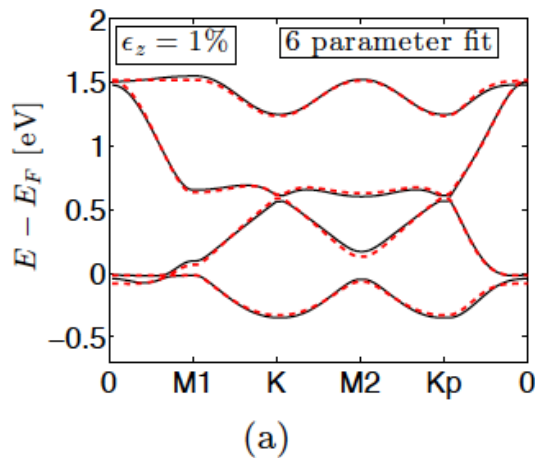
fit	t [eV]	t' [eV]	Δ [eV]	E_F [eV]
unrelaxed	0.598	0.062	-0.023	-0.693
fully relaxed	0.541	0.045	-0.017	-0.641

Lattice Strain Effects: External

Ruegg, Mitra, Demkov, Fiete *Phys. Rev. B* (2013)

Apply symmetry-breaking strain along the [001] cubic direction:

$$\begin{aligned} \mathbf{a}_1 &= a_0(1 - \mu x)\mathbf{i}, \\ \mathbf{a}_2 &= a_0(1 - \mu x)\mathbf{j}, \\ \mathbf{a}_3 &= a_0(1 + x)\mathbf{k}, \end{aligned}$$



Dominant effect is orbital splitting:
$$H_z = \alpha_z \sum_{\mathbf{r}} (n_{\mathbf{r},x^2-y^2} - n_{\mathbf{r},z^2})$$

Externally imposed strain along [001] favors FO/AFM order.
Topological phase unaffected.

Predictions for topological phases in pyrochlore iridates (partial)

- $A_2Ir_2O_7$ (undistorted): D. Pesin, L. Balents, Nat. Phys. (2010)
“Topological Mott Insulator” (TMI)
- $A_2Ir_2O_7$ (distorted): B-J. Yang, Y.-B. Kim, PRB (2010)
Single-particle type TI in non-interacting model
- $A_2Ir_2O_7$ (distorted+interaction): M. Kargarian, J. Wen, GAF PRB (2011)
“Weak Topological Mott Insulator” (WTMI)
- $Y_2Ir_2O_7$ (magnetically ordered): Wan *et al.* PRB (2011)
Weyl semi-metal
- $A_2Ir_2O_7$: Go, Witczak-Krempa, Jeon, Park, Y.-B. Kim PRL (2012)
Axion insulator (found via cellular DMFT)
- $A_2Ir_2O_7$: M. Kargarian, GAF PRL (2013)
Topological crystalline insulator, TCMI
- $A_2Ir_2O_7$: J. Maciejko, V. Chua, GAF PRL (2014)
TI*, SM*

Minimal model for $A_2Ir_2O_7$?

- Key energy scales:

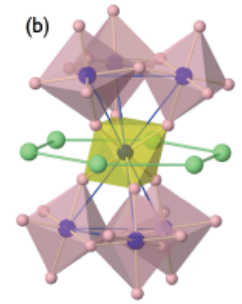
$$W \sim 1.5 \text{ eV}, E_{\text{SOC}} \sim 0.5 \text{ eV}, U \sim 2 \text{ eV}, E_{t_{2g}-e_g} \sim 2 \text{ eV}$$

$$\Delta \sim 0.3-0.5 \text{ eV}, J_H \sim 0.5 \text{ eV}$$

Moreover, extended 5d orbitals may feel significant crystal fields beyond the local oxygen environment, e.g., Hozio *et al.*, arXiv:1212.4009

Elements of minimal not entirely clear at present.

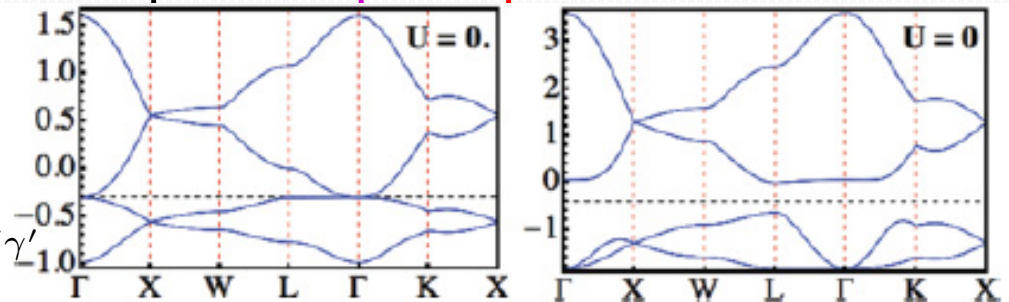
W. Witczak-Krempa, G. Chen, Y.-B. Kim, L. Balents arxiv:1305.2193



- A central issue for topological physics is the $j=1/2$ band structure, namely **order of degeneracies** at the Γ point: **2-4-2** vs **4-2-2**.

$$H_0 = \sum_{\langle ij \rangle} (T_{o,ij}^{\gamma\gamma'} + T_{d,ij}^{\gamma\gamma'}) d_{i\gamma}^\dagger d_{j\gamma'}$$

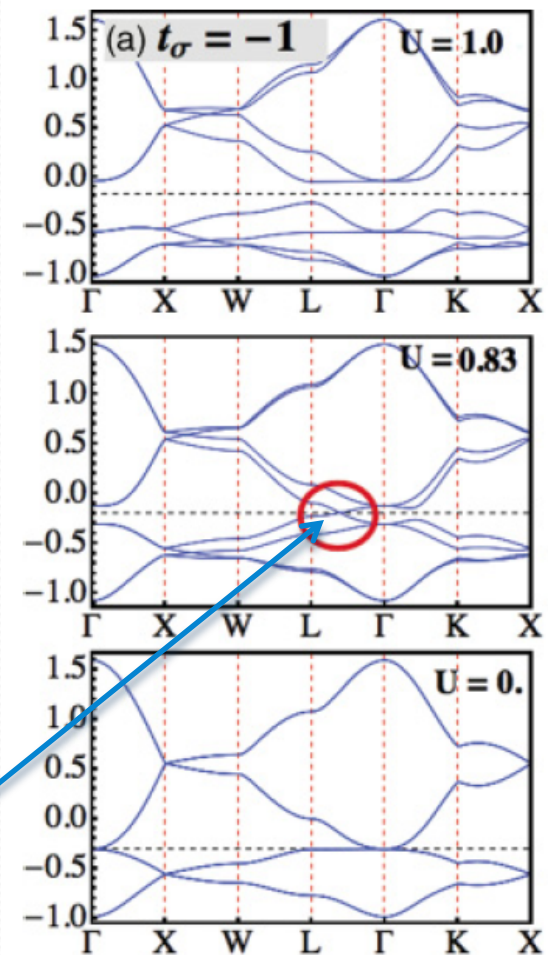
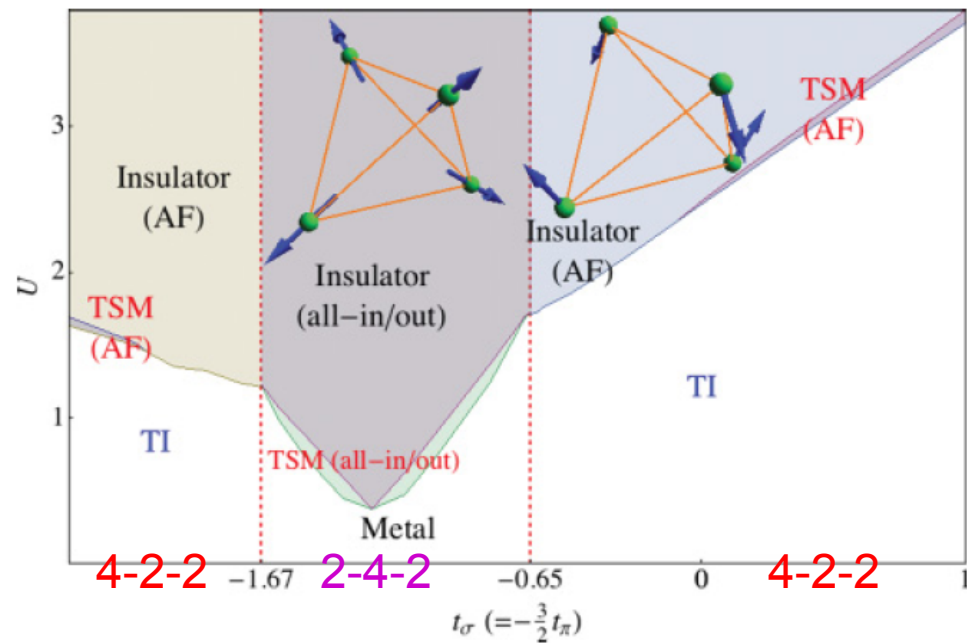
$$= \sum_{\langle ij \rangle} (t_1 \delta_{\gamma\gamma'} + it_2 \mathbf{d}_{ij} \cdot \vec{\sigma}_{\gamma\gamma'}) d_{i\gamma}^\dagger d_{j\gamma'}$$



W. Witczak-Krempa and Y.-B. Kim, PRB (2012)

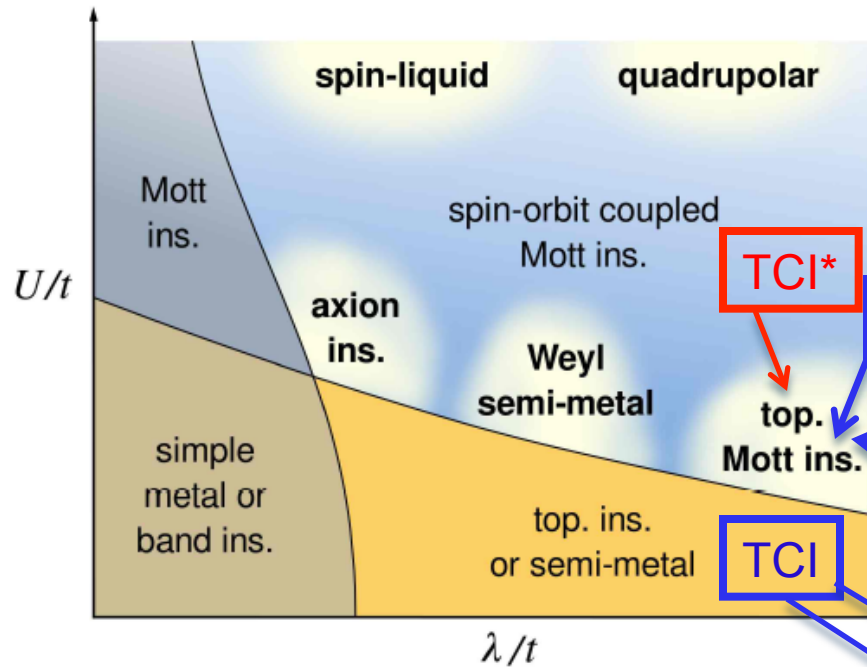
Topological phases in pyrochlore Iridate systems: $A_2Ir_2O_7$ Hartree-Fock Calculations for $j=1/2$

Witczak-Krempa and Kim, PRB (2012)



$$H = H_{d-d} + H_{d-o-d} + H_U \quad \text{Weyl point}$$

Summary



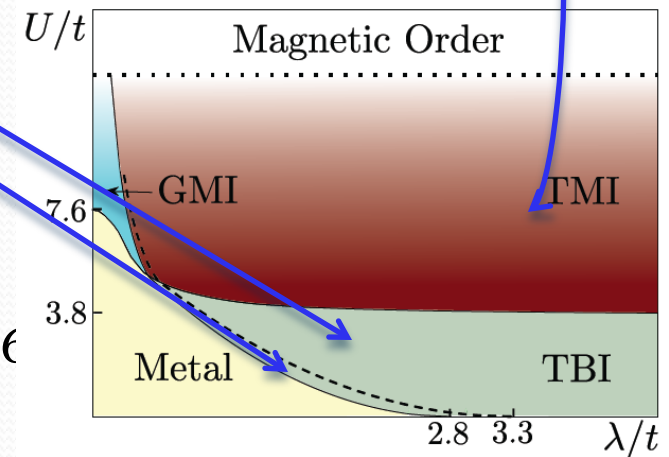
W. Witczak-Krempa, G. Chen,
Y.-B. Kim, L. Balents arxiv:1305.2193

TCI*

TCMI

TI*, SM*

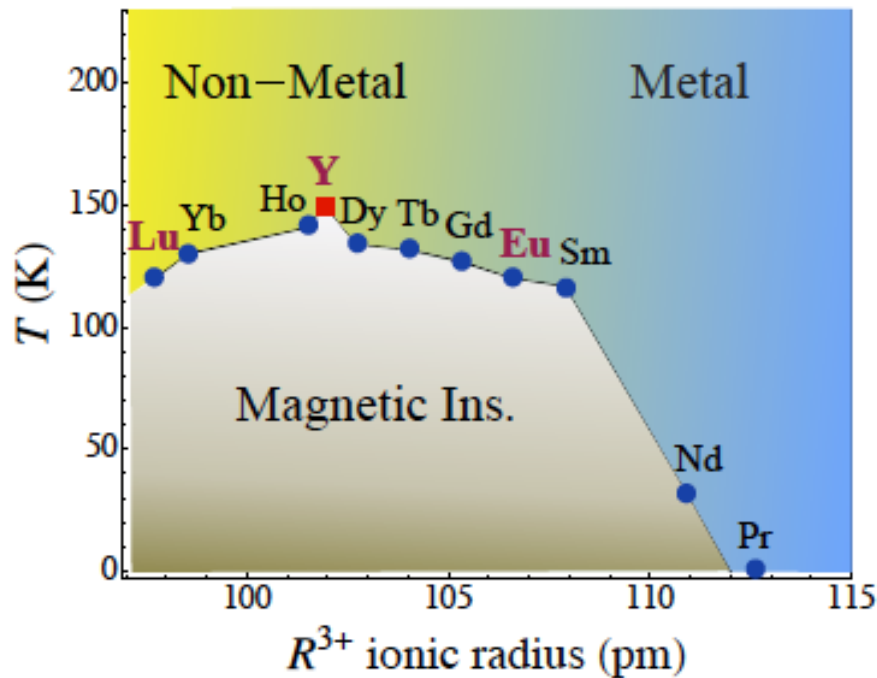
TCI



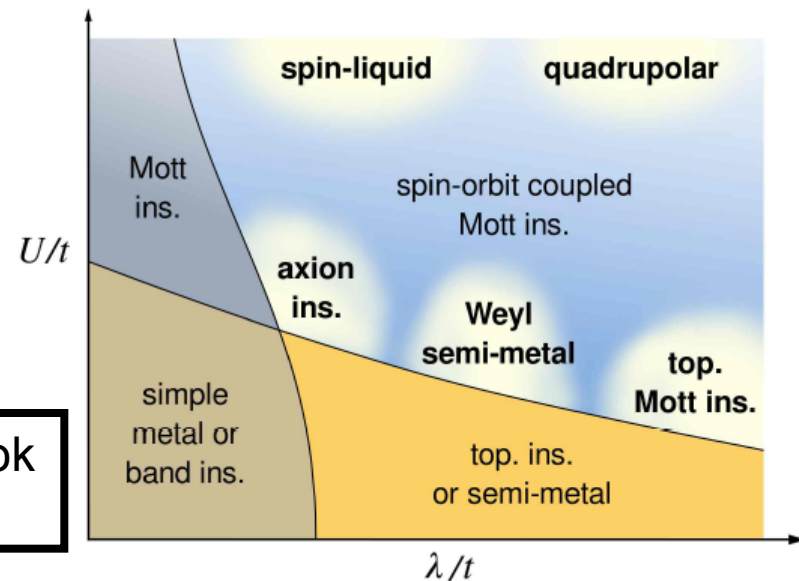
Pesin, Balents Nat. Phys. (2010)

- $A_2Ir_2O_7$: M. Kargarian, GAF PRL (2013)
Topological crystalline insulator, TCM I 4-2-2
- $A_2Ir_2O_7$: J. Maciejko, V. Chua, GAF arXiv:1307.5566
TI* 4-2-2, SM* 2-4-2

Experimental Phase Diagram for Bulk Pyrochlore Iridates

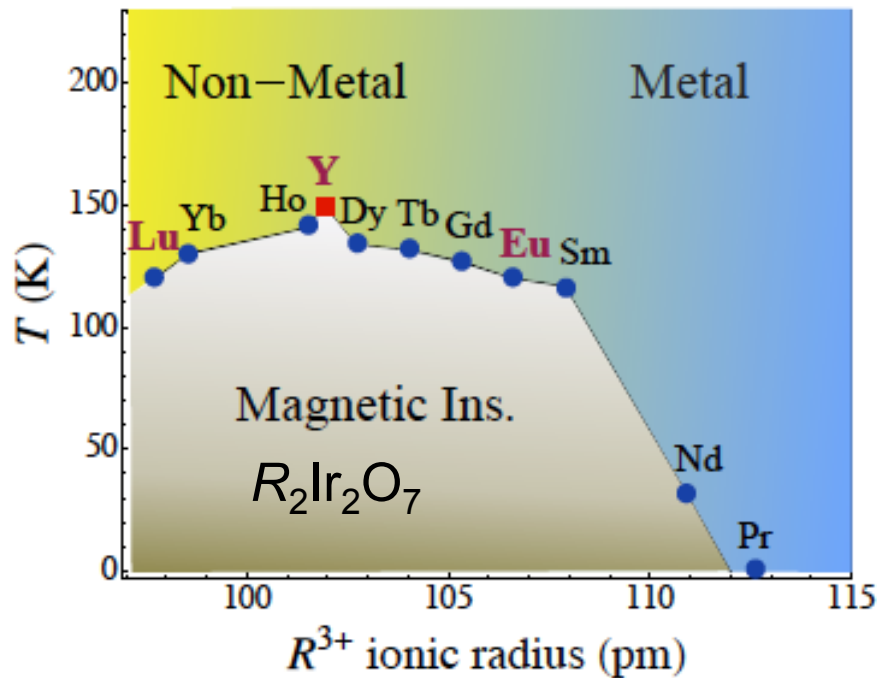


W. Witczak-Krempa, G. Chen,
Y.-B. Kim, L. Balents arxiv:1305.2193

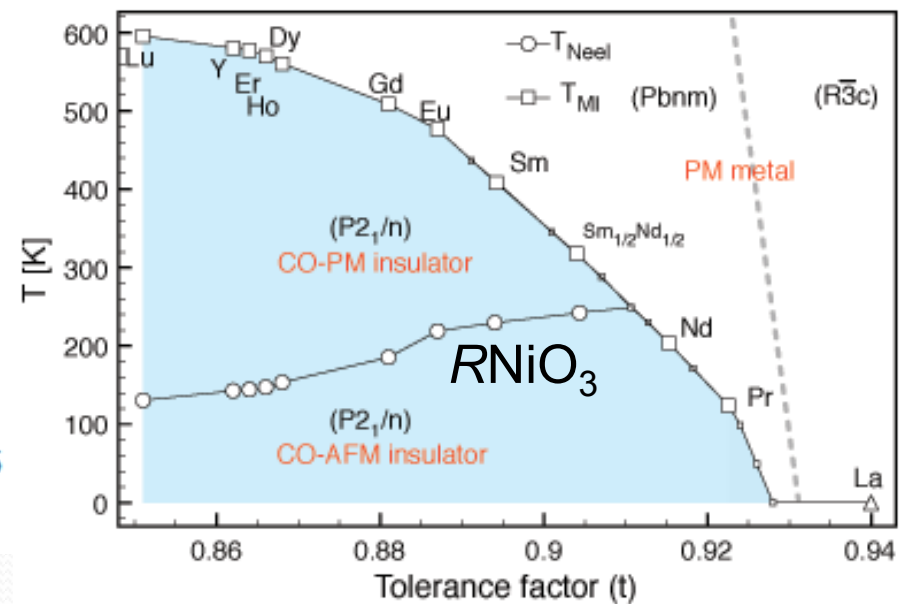


Overall, these particular materials do not look promising for topological phases.

Experimental Phase Diagram for Bulk Pyrochlore Iridates and Bulk Perovskite Nickelates



W. Witczak-Krempa, G. Chen,
Y.-B. Kim, L. Balents arxiv:1305.2193

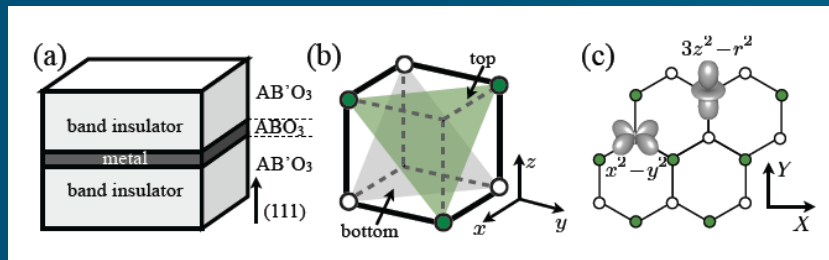


Overall, these particular materials do not look promising for topological phases.

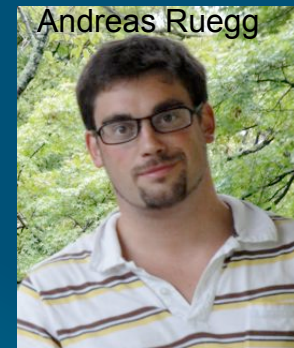
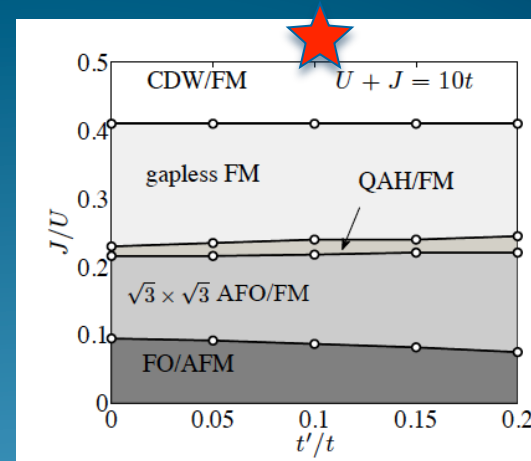
From Triscone Group Website

But thin films are a different story!

Topological Phases in Perovskite Heterostructures



LaAlO₃/LaNiO₃/LaAlO₃



- Ruegg, Fiete *Phys. Rev B (Rapid)* **84**, 201103 (2011)
- Ruegg, Mitra, Demkov, Fiete *Phys. Rev. B* **85**, 245131 (2012)
- Ruegg, Mitra, Demkov, Fiete *Phys. Rev. B* **88**, 115146 (2013)