

# Field-Induced Metal-Insulator Transition in the Pyrochlore Iridate $\text{Nd}_2\text{Ir}_2\text{O}_7$

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# Rare-Earth Moments in Pyrochlore Iridates

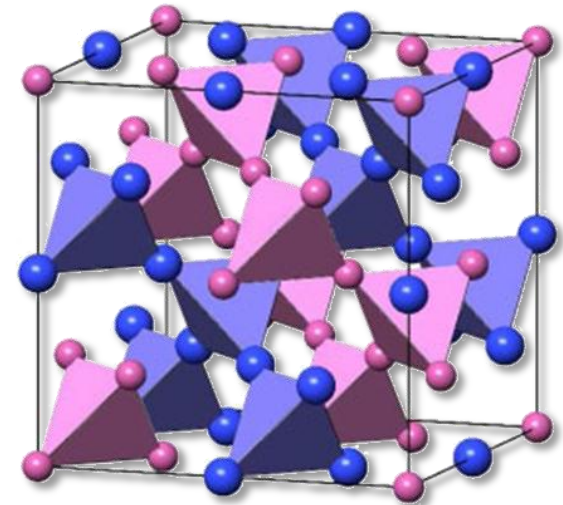
Does the rare-earth moments affect magnetic/transport properties?

## Iridium ions:

- Conduction electrons
- Moderately interacting
- Unique properties: quadratic band touching, Weyl semimetal, ...

## Rare-earth ions:

- Often form localized moment.
- **Ignored in most of theoretical studies.**

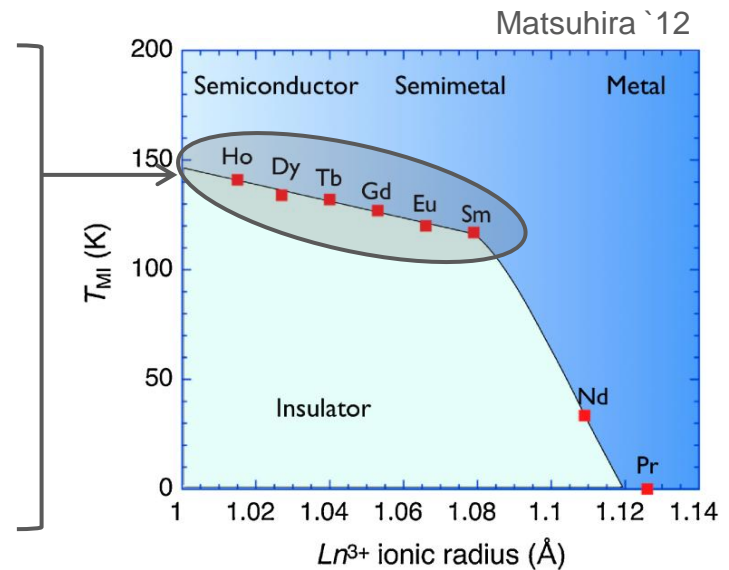


# Rare-Earth Moments in Pyrochlore Iridates

Does the rare-earth moments affect magnetic/transport properties?

## Ir pyrochlore ~ physics of Ir electrons?

- Band width  $W$  and Hubbard  $U \sim 1$  eV; much larger than expected Kondo coupling  $J_K \sim 10$  meV.
- MIT (mostly) takes place in the order of 100 K, and has weak dependence to  $Ln$  ions, magnetic or non-magnetic.

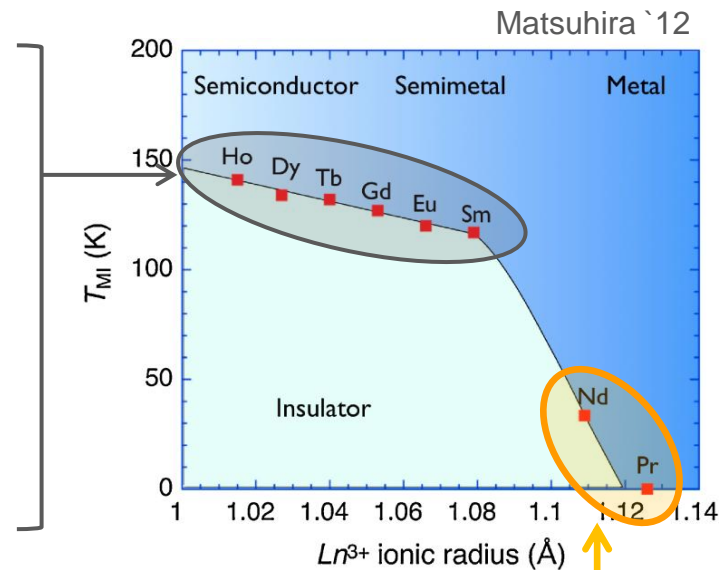


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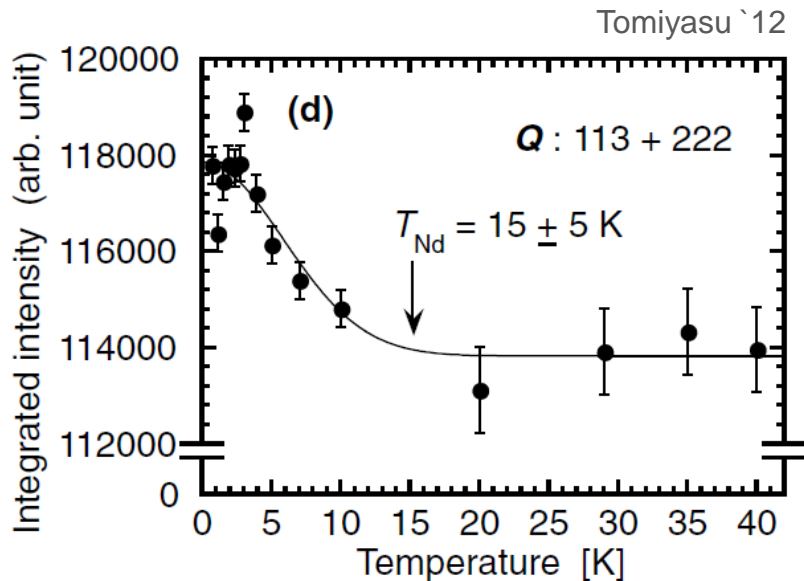
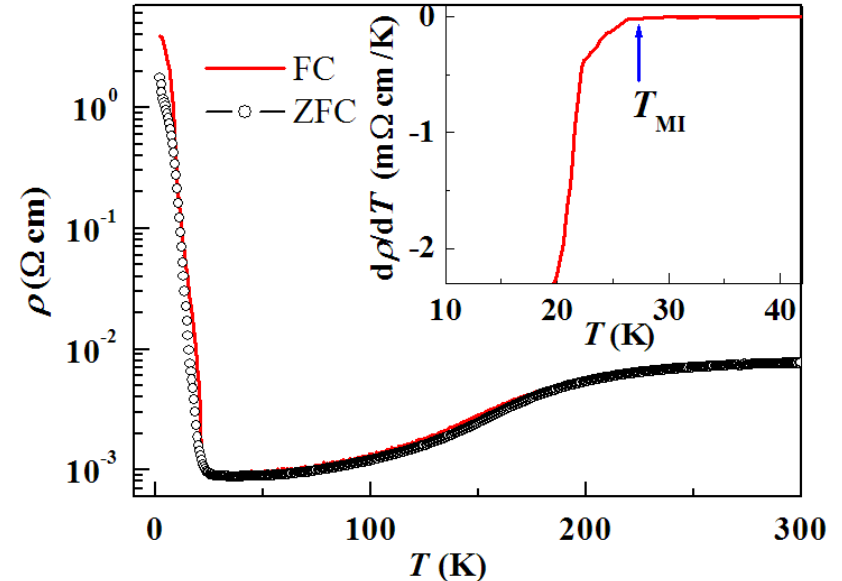
Kondo coupling may take important role if Ir electrons are at PM/AFM boundary.  
→  $Nd_2Ir_2O_7$  may be one such example.

# Field-Induced MIT in $\text{Nd}_2\text{Ir}_2\text{O}_7$

# Zero-Field MIT in $\text{Nd}_2\text{Ir}_2\text{O}_7$

## Resistivity Measurements:

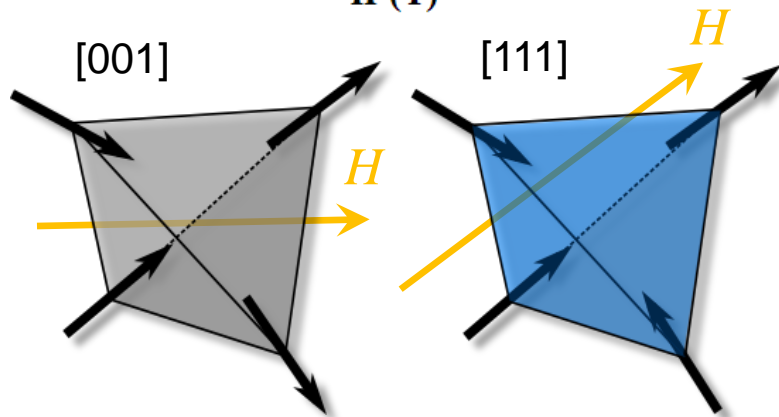
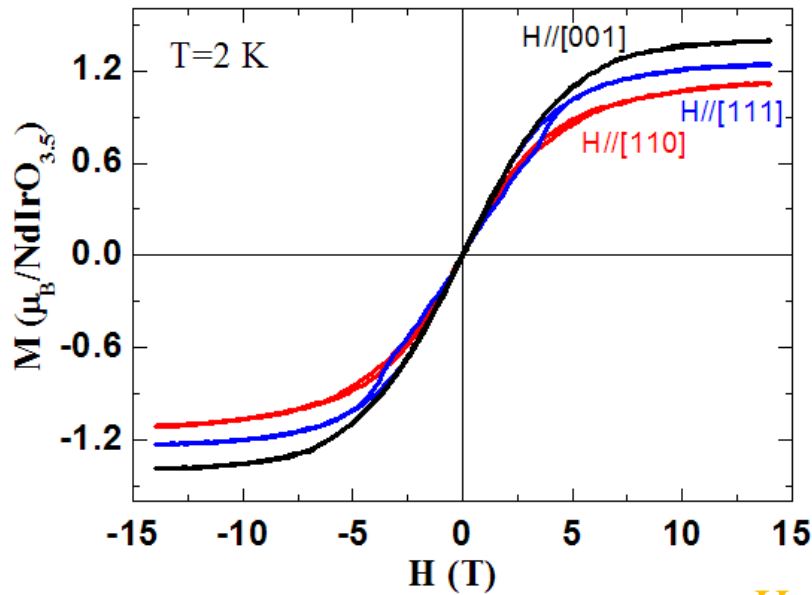
1. Metal-insulator transition takes place at  $T_{\text{MI}} \sim 30$  K.
2.  $T_{\text{MI}}$  associated with the onset of AIAO order (mainly on Ir sites).



## Neutron Diffraction:

1. Neutron being sensitive to Nd moments than the small Ir moments.
2. Onset of AIAO order on Nd sites ( $T_{\text{Nd}} \sim 15$  K) being lower than  $T_{\text{MI}} (\sim 30\text{K})$ ; ferromagnetic interactions between Nd moments?

# Magnetization Process



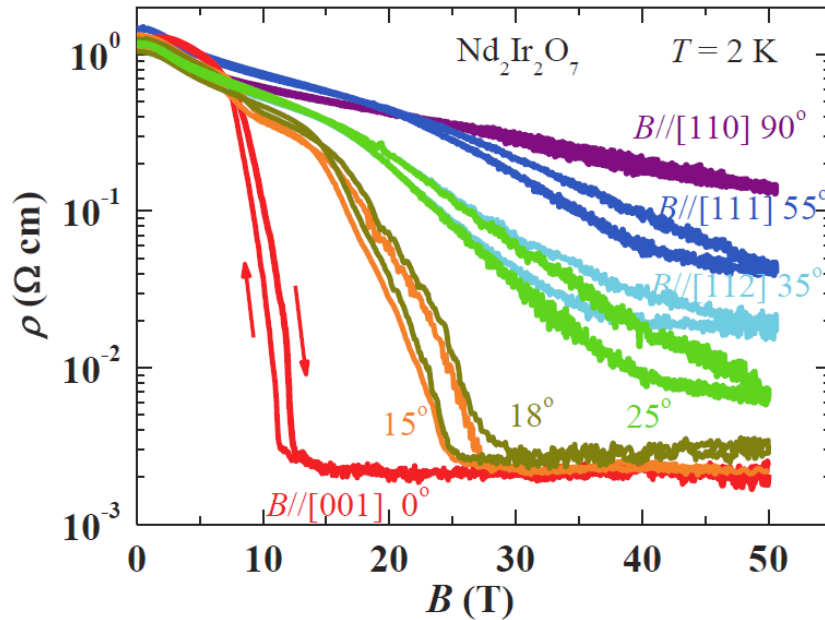
## Magnetization Curve:

1. Saturation at magnetic field  $H \sim 7$  T.
2. Hysteresis for field along  $\langle 111 \rangle$  while not for  $\langle 100 \rangle$ .
3. Contribution mainly from Nd moments; the magnetization at saturation consistent with single-ion moment for Nd:  $\mu_{\text{Nd}} \sim 2.4\mu_{\text{B}}$ .
4. The result is also consistent with the expected small moments for Ir electrons  $1/3 - 1/2\mu_{\text{B}}$ .

## Ising spins with local $\langle 111 \rangle$ axis (spin-ice):

1. AIAO for weak field.
2. 2-in 2-out for field along  $\langle 100 \rangle$ , while 3-in 1-out for field along  $\langle 111 \rangle$ .

# Field-Induced Metal-Insulator Transition

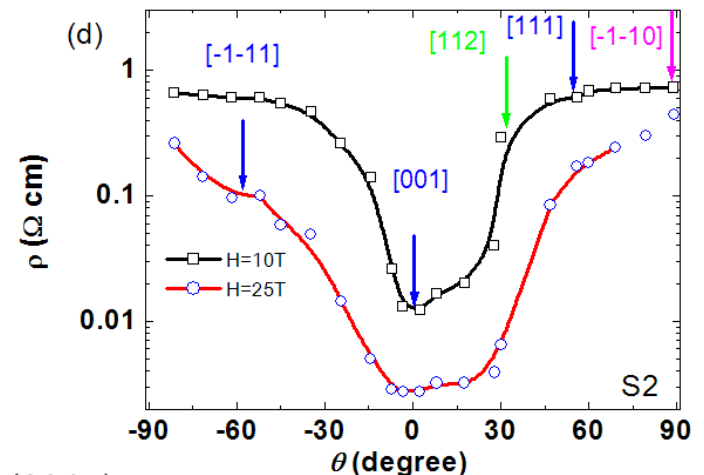


## Angle dependence of resistivity:

1. Large negative magneto-resistance observed only for field close to [001] direction.
2. **Highly anisotropic behavior, unusual for cubic magnets.**

## Metal-Insulator Transition

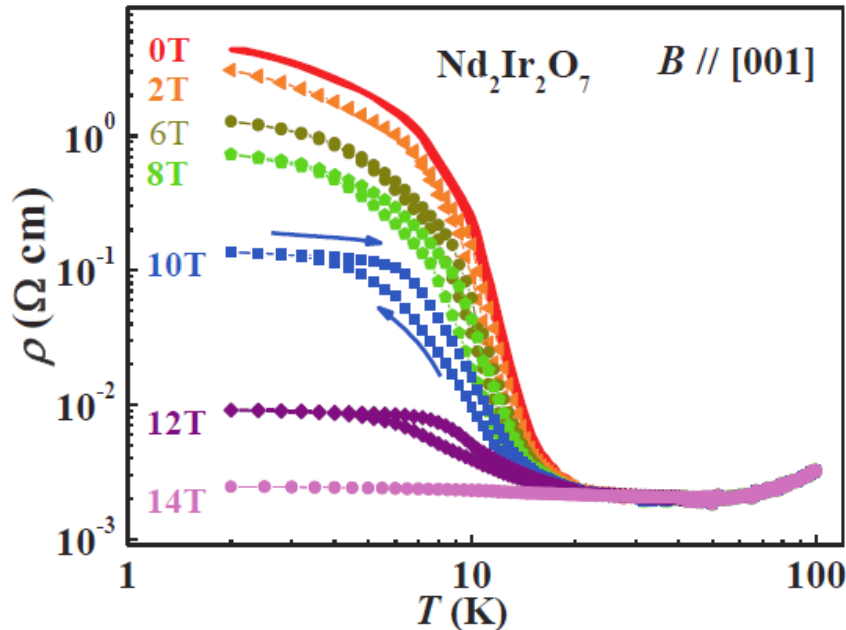
1. Sudden decrease of resistivity at  $B \sim 10$  T for field along [001].
2. Sharp metal-insulator transitions observed only for field close to [100] direction.
3. Hysteresis indicates 1<sup>st</sup> order transition.



Similar results: K. Ueda *et al.*, Phys. Rev. Lett. 115, 056402 (2015).



# Field-Induced Metal-Insulator Transition

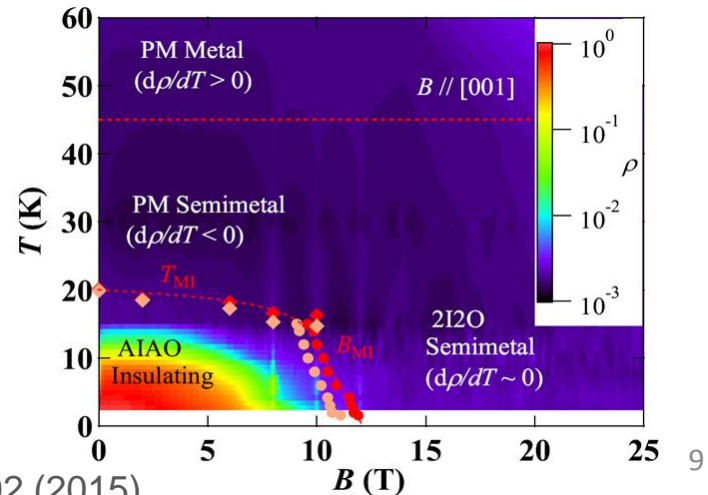


## Phase Diagram:

1. Ground state for low-field is a AIAO insulator.
2. High-field (semi)metal show very weak temperature dependence of  $\rho$ .

## Suppression of MIT with magnetic field:

1. Metal-insulator transition suppressed by application of external magnetic field.
2. Hysteresis observed for MIT under strong magnetic field (no hysteresis for  $B=0$ ); tricritical point at  $\sim 20$  K and 2-6 T?
3. Weak temperature dependence of  $\rho$  in the high field (semi)metal phase.



Similar results: K. Ueda *et al.*, Phys. Rev. Lett. 115, 056402 (2015).

# Effective Nd Spin Model

# Rare-Earth Moments in $Ln_2Ir_2O_7$

## Localized moments on $R$ ions:

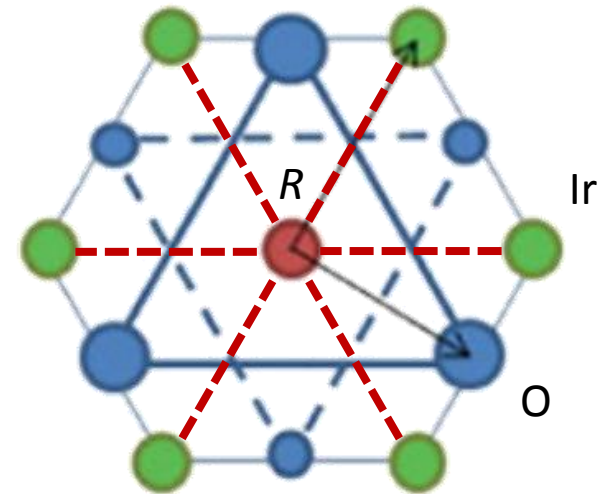
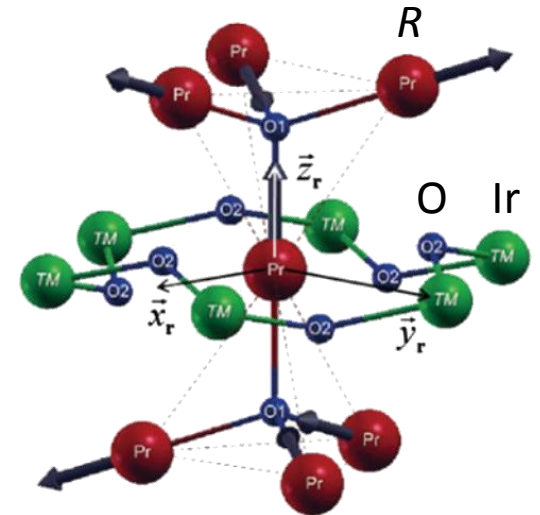
1.  $4f$  electrons on  $Ln$  ions form localized moments, often with large  $J$ :

$$\underline{J=4 \text{ for } Pr^{3+} \text{ and } J=9/2 \text{ for } Nd^{3+}}$$

2. Crystal field splits the degeneracy of moments.
3. May form pseudo-spins with multi-polar (quadrupolar/octupolar) moments with dipolar (magnetic) moments along the local  $z$  axis.

## Interaction with Ir electrons:

1. **6 nearest Ir sites** surrounding the  $Ln$  moments.
2. **Kondo coupling between Ir electrons and  $R$  moments may have unconventional form** due to the multi-polar nature of  $R$  moments.
3. Mediates RKKY interaction between Nd moments.



# Doublets of Nd Moments

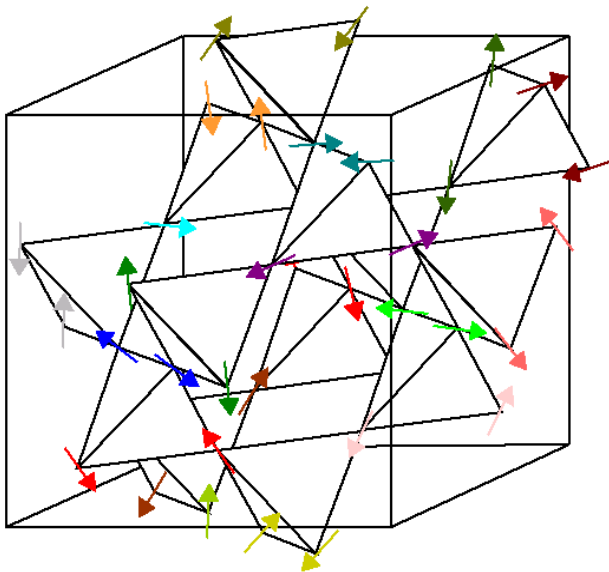
1. Due to the highly anisotropic crystal field, the  $J=9/2$  Nd moments split into 5 Kramers doublets.
2. The resultant ground state doublet is a **dipolar-octupolar doublet**.  
(Huang '14)
3. Investigated by neutron scattering measurement.

**Table 1.** Calculated CEF parameters, eigenenergies and eigenstates for  $\text{Nd}^{3+}$  ( $J = 9/2$ ). Ten coefficients with respect to  $|J_z\rangle$  are given for each eigenstates.

CEF parameters [meV]										
	$B_2^0$	$B_4^0$	$B_4^3$	$B_6^0$	$B_6^3$	$B_6^6$				
	-0.28(0)	$-0.95(9) \times 10^{-2}$	-0.33(9)	$-0.44(3) \times 10^{-3}$	$0.17(7) \times 10^{-2}$	$-0.45(7) \times 10^{-2}$				
eigenenergies [meV] and eigenstates										
$E_i$	$  -9/2 \rangle$	$  -7/2 \rangle$	$  -5/2 \rangle$	$  -3/2 \rangle$	$  -1/2 \rangle$	$  1/2 \rangle$	$  3/2 \rangle$	$  5/2 \rangle$	$  7/2 \rangle$	$  9/2 \rangle$
123	0	0	0.375	0	0	0.533	0	0	-0.758	0
123	0	-0.758	0	0	-0.533	0	0	0.375	0	0
57	0.135	0	0	-0.289	0	0	-0.772	0	0	0.550
57	0.550	0	0	0.772	0	0	-0.289	0	0	-0.135
42	0	0	-0.439	0	0	-0.617	0	0	-0.653	0
42	0	0.653	0	0	-0.617	0	0	0.439	0	0
26	0	0	0.816	0	0	-0.578	0	0	-0.003	0
26	0	0.003	0	0	0.578	0	0	0.816	0	0
0	-0.057	0	0	-0.286	0	0	-0.489	0	0	-0.822
0	-0.822	0	0	0.489	0	0	-0.286	0	0	0.057

# Model: Effective spin model for Nd moments

$$\mathcal{H}_{Nd}^{(\text{eff})} = \sum_{\langle i,j \rangle} J_z \tau_i^z \tau_j^z + J_y \tau_i^y \tau_j^y + J_x \tau_i^x \tau_j^x + J_{xz} (\tau_i^x \tau_j^z + \tau_i^z \tau_j^x) - A_H \sum_i \tau_i^z - g \sum_i \tau_i^z (\mathbf{a}_i \cdot \mathbf{h})$$

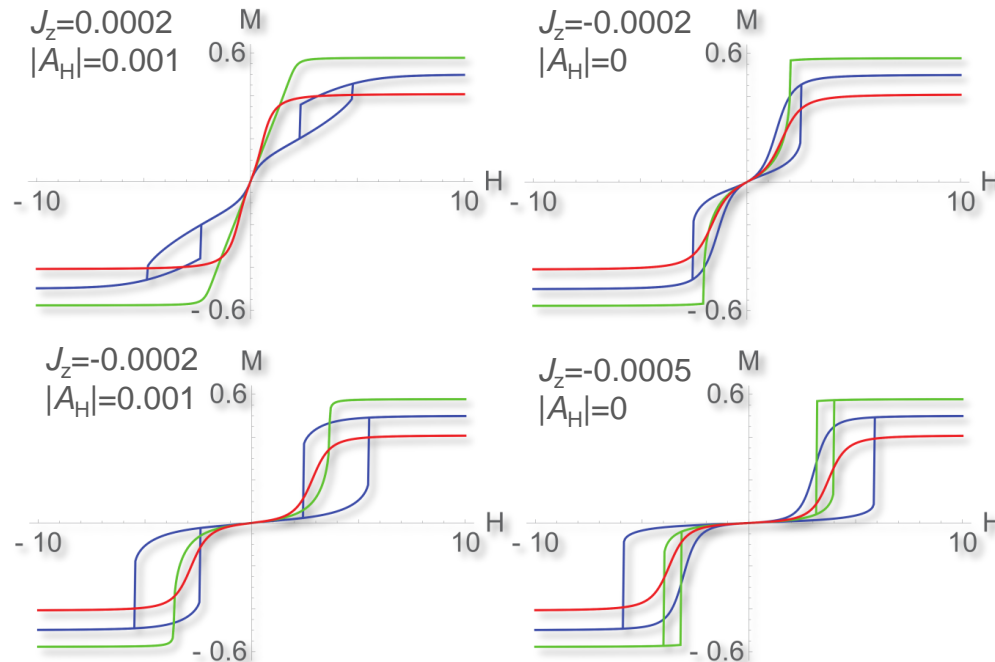


1. Spin model on a pyrochlore lattice with nearest-neighbor interactions.
2. The moments are dipolar-octupolar moments.
3. Interactions and Zeeman coupling terms allowed by symmetry.

# Magnetization Process

Parameters:

$$J_x=J_y=-0.0001, J_{xz}=0.0001, g=0.001$$



1. Magnetization process of Nd moments coupled to AIAO field from iridium ions ( $A_H$ ) with external field applied along  $\langle 100 \rangle$  (green),  $\langle 110 \rangle$  (red),  $\langle 111 \rangle$  (blue).
2.  $A_H$  is flipped at  $H=0$  to mimic the behavior of order parameter.
3. Ferromagnetic  $J_z$  reproduces hysteresis for  $\langle 111 \rangle$  at  $h \sim 0$ , while other terms ( $J_x, J_y, \dots$ ) contributes to smooth out the curves.

# Kondo Lattice Model

# Model: Ir Electrons + Nd Moments

Iridium Electrons:

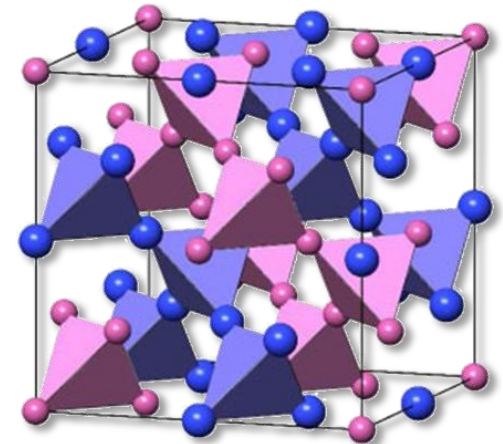
Tight-binding model for  $J_{\text{eff}}=1/2$  bands with 2<sup>nd</sup> neighbor hopping + onsite Hubbard  $U$ .

(Witczak-Krempa `13)

Kondo Coupling between Ir and Nd ions:

$$\mathcal{H}_K = J_K \sum_{ij} \Lambda_{ij}^{\mu\nu} S_i^\mu \tau_j^\nu \quad \mathcal{H}_h^{\text{Nd}} = -\gamma \sum_i (\mathbf{h} \cdot \mathbf{a}_i) \tau_i^z$$

$$\Lambda_{ij}^{\mu\nu} = \begin{cases} G_1^x \mathbf{a}_j \cdot \hat{\mathbf{e}}_\mu + G_2^x \mathbf{a}_j \bar{\times} (\mathbf{d}_{ij} \bar{\times} \mathbf{d}_{ij}) \cdot \hat{\mathbf{e}}_\mu & (\nu = x) \\ G^y \mathbf{a}_j \times (\mathbf{d}_{ij} \bar{\times} \mathbf{d}_{ij}) \cdot \hat{\mathbf{e}}_\mu & (\nu = y) \\ G_1^z \mathbf{a}_j \cdot \hat{\mathbf{e}}_\mu + G_2^z \mathbf{a}_j \bar{\times} (\mathbf{d}_{ij} \bar{\times} \mathbf{d}_{ij}) \cdot \hat{\mathbf{e}}_\mu & (\nu = z) \end{cases}$$



1. We consider effective Hamiltonian taking into account of the lowest energy doublets for Nd ions (dipolar-octupolar doublets).

(Huang `14)

2. We only consider coupling of Nd moments to Ir electrons (Kondo couplings) due to the highly localized nature of Nd 4f electrons.
3. We consider all types of couplings allowed by symmetry.

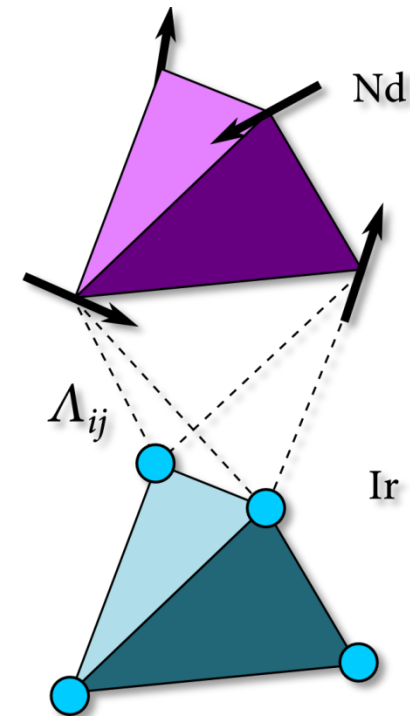


# Mean Field Theory

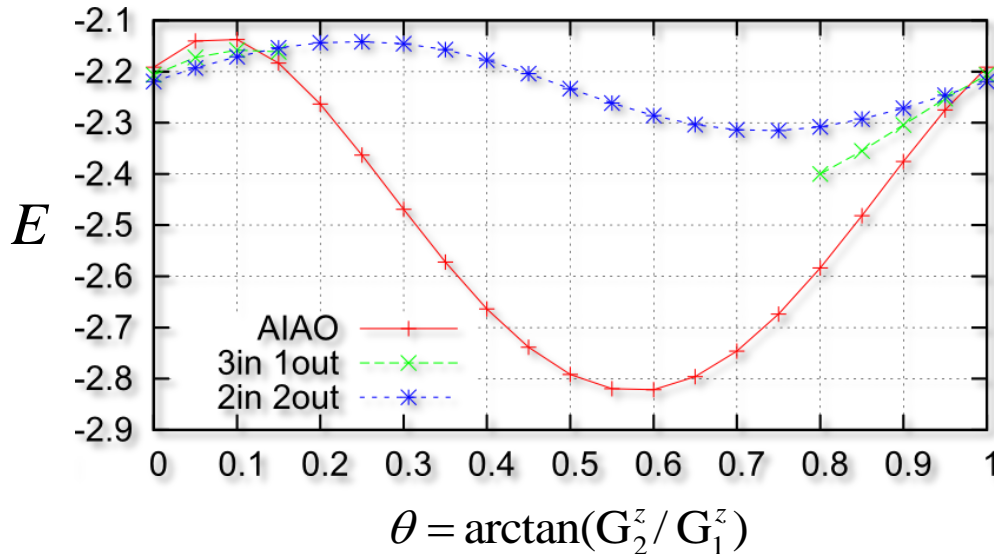
$$\mathcal{H}_U \simeq U \sum_{i\sigma} \langle c_{i\sigma}^\dagger c_{i\sigma} \rangle c_{i\bar{\sigma}}^\dagger c_{i\bar{\sigma}} - \langle c_{i\sigma}^\dagger c_{i\bar{\sigma}} \rangle c_{i\bar{\sigma}}^\dagger c_{i\sigma} - U \sum_i \langle c_{i\uparrow}^\dagger c_{i\uparrow} \rangle \langle c_{i\downarrow}^\dagger c_{i\downarrow} \rangle - \langle c_{i\uparrow}^\dagger c_{i\downarrow} \rangle \langle c_{i\downarrow}^\dagger c_{i\uparrow} \rangle$$

$$\begin{aligned} \mathcal{H}_K &\simeq J_K \sum_{ij} \Lambda_{ij}^{\mu\nu} [\langle S_i^\mu \rangle \tau_j^\nu + S_i^\mu \langle \tau_j^\nu \rangle - \langle S_i^\mu \rangle \langle \tau_j^\nu \rangle] \\ &= J_K \sum_{ij} \Lambda_{ij}^{\mu\nu} S_i^\mu \langle \tau_j^\nu \rangle. \end{aligned}$$

1. To take into account of the spacial correlation, we consider eight site cluster with four spins and four half-filled electron sites.
2. Mean-field expansion using unrestricted Hartree-Fock method for Ir electrons and mean-field treatment for localized Nd moments.

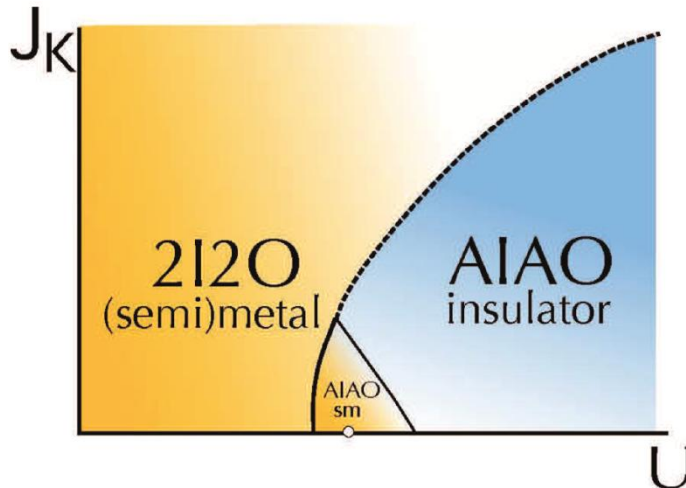
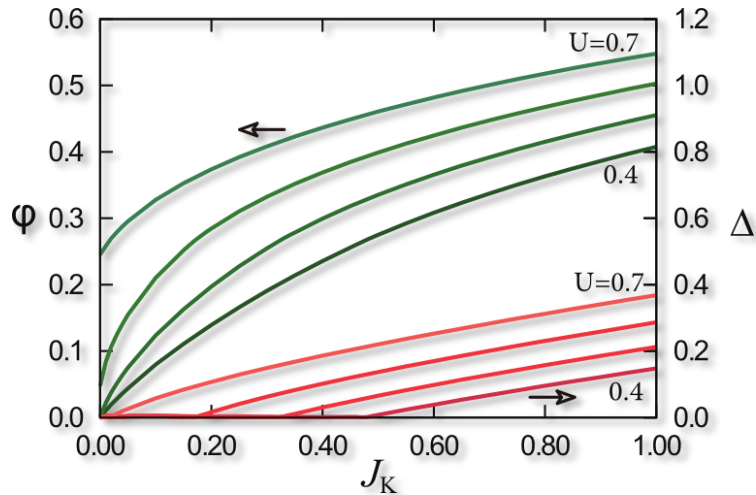


# Fermion-Mediated Interactions



1. We first look for the appropriate set of Kondo couplings with ferromagnetic nearest-neighbor interaction along  $z$  axis.
2. Ground state energy for (meta-)stable all-in all-out, two-in two-out, and three-in one-out states by mean-field calculation with different ratio of  $G_1^z$  and  $G_2^z$ .
3. All-in all-out become the ground state when  $G_2^z$  is dominant while two-in two-out is favored for  $G_1^z$ . This implies the nearest-neighbor interaction to be ferromagnetic when  $G_1^z$  is dominant while antiferromagnetic for  $G_2^z$ .
4. In the following, we consider  $|G_1^z| \gg |G_2^z|$ .

# Enhanced AIAO Order by Kondo Coupling



1. AIAO order parameter for Ir electrons (green) and the charge gap (red).
2. AIAO order being enhanced by the Kondo coupling, and AIAO order appears in weak U region where AIAO does not exist for  $J_K=0$ .
3. The charge gap induced by the Kondo coupling.
4. (below) Schematic phase diagram with  $J_K$  and  $U$ .

Parameters:

$$t_{oxy}=1, t_{\sigma}=-1.1, t_{\pi}=(2/3) t_{\sigma}, t'_{\pi,\sigma}=0.02 t_{\pi,\sigma}$$

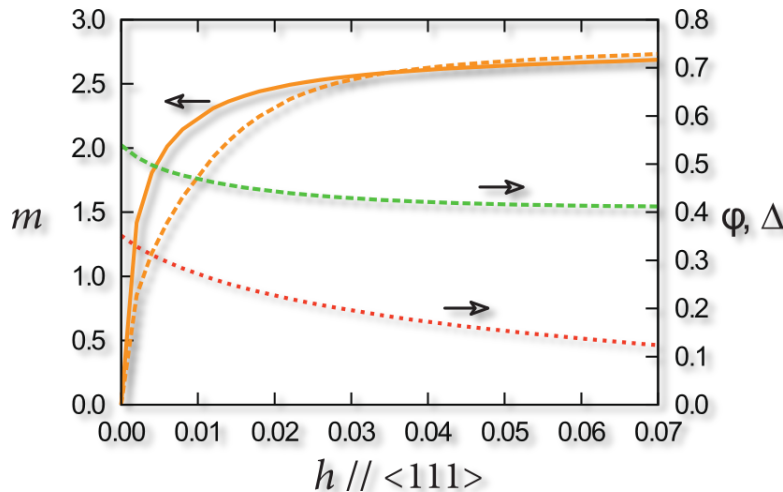
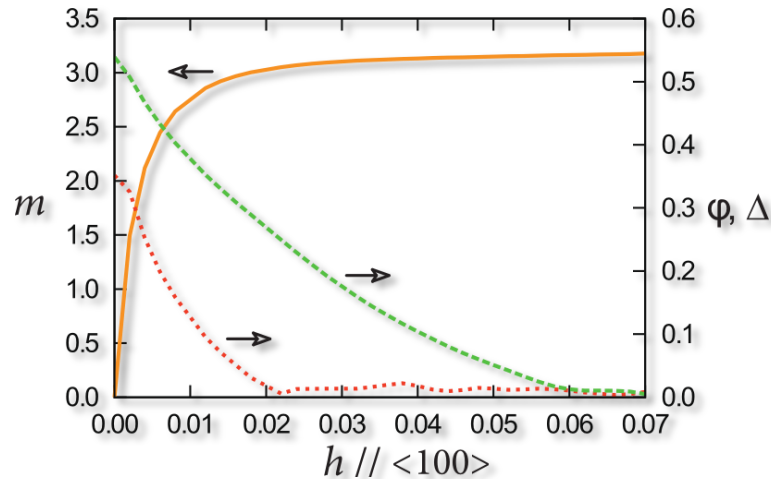
$$G_1^x=0.0, G_2^x=0.006, G^y=0.01, \\ G_1^z=-0.06, G_2^z=-0.02$$

# Magnetization Process

Parameters:

$$t_{\text{oxy}}=1, t_{\sigma}=-1.1, t_{\pi}=-\frac{2}{3} t_{\sigma}, t_{\pi,\sigma}=0.02 t_{\pi,\sigma}$$

$$G_1^x=0.0, G_2^x=0.006, G^y=0.01, \\ G_1^z=-0.06, G_2^z=-0.02, \gamma = 5.0$$



1. AIO order parameter for Ir electrons (green) , charge gap (red), and net magnetization along the external field (orange).
2. A metal-insulator transition occurs when the field is applied along <100> direction, while no transition for <111>. They are highly anisotropic.
3. The magnetization curve show hysteresis for field along <111>. This is due to the lifting of the degeneracy of two AIO ground states at  $h=0$ .
4. Very small critical  $h$  ( $\sim 0.01$ ) compared to  $U$  ( $\sim 1$ ), due to large  $\gamma$ .

# Summary

1. We studied magnetization process and metal-insulator transition in  $\text{Nd}_2\text{Ir}_2\text{O}_7$ .
2. We found a **field-induced metal-insulator transition**.
3. The **MIT is highly anisotropic**, unusual for cubic magnets.
4. The form of magnetization curves being strongly affected by the effective interaction between Nd localized moments.
5. The Kondo coupling between Nd moments and Ir electrons has significant effects over magnetic and electronic property of the material.
  - ✓ **Very low  $h_c$  compared to Hubbard  $U$ .**
  - ✓ **Highly anisotropic MIT with applied magnetic field.**
6. Anisotropic hysteresis in magnetization curve is a consequence of AIAO ground state.

