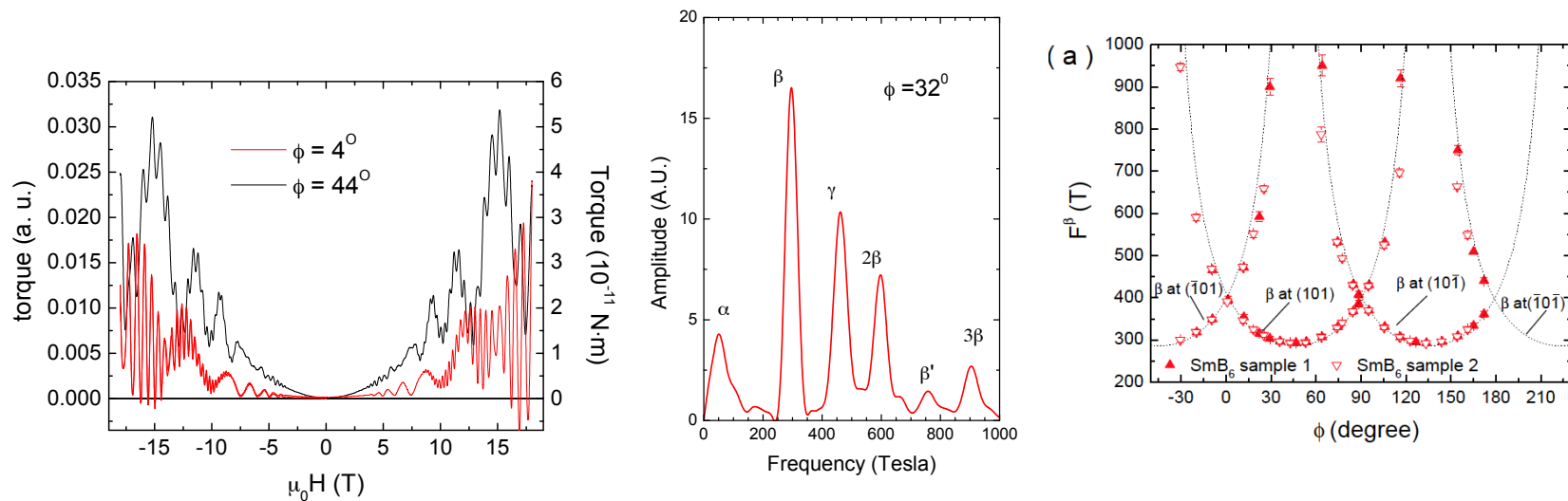


# Two-dimensional Fermi surfaces in Kondo Insulator $\text{SmB}_6$

*Lu Li*

*University of Michigan*



**G. Li, et al. Science 2014**

# Acknowledgement

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Yayu Wang, *Tsinghua Univ.*



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**ENERGY**

Office of  
Science

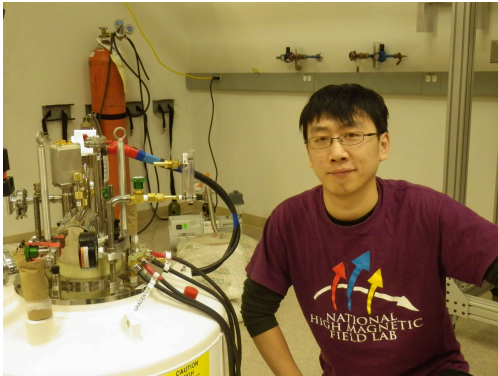
NSF

University of Michigan  
MCUBED project

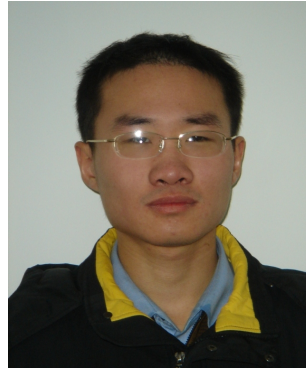


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Peng Cai

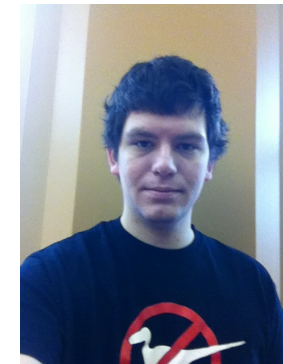


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Adam Berkley



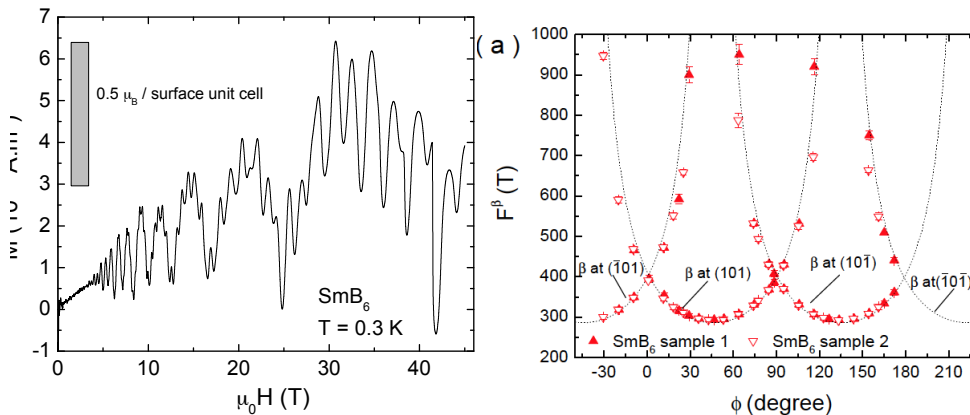
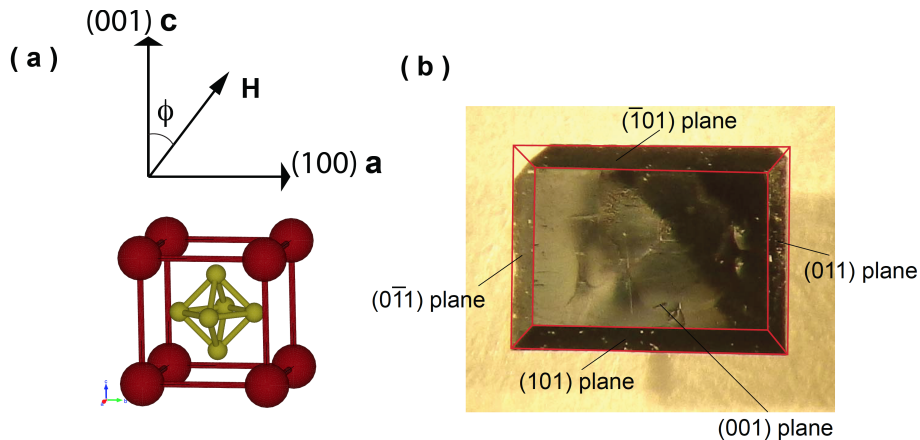
# Topological Kondo insulators $\text{SmB}_6$

1. **WHY?** Kondo Insulator  $\text{SmB}_6$

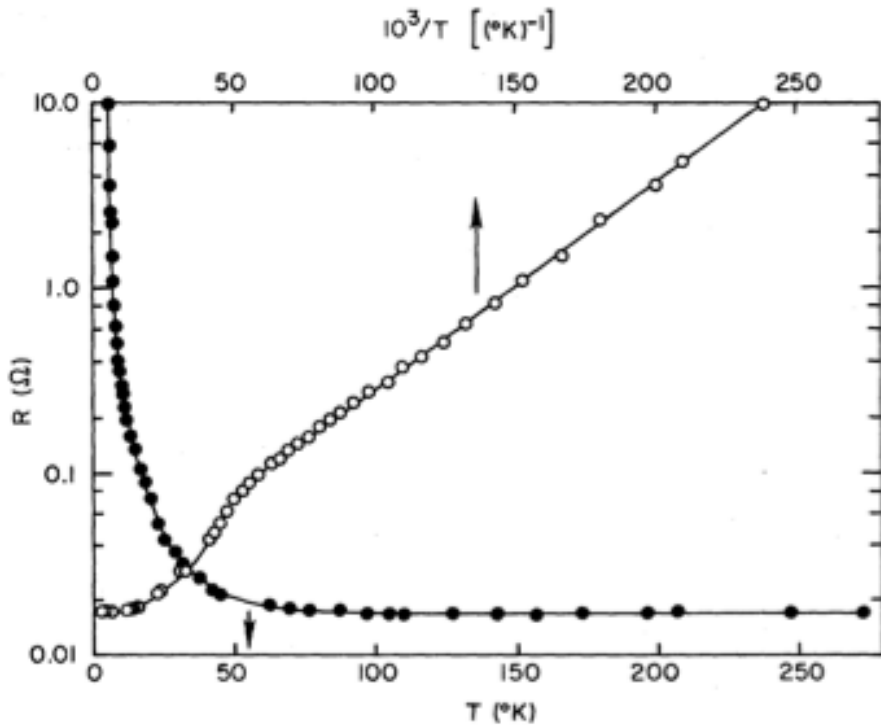
2. **HOW?** Torque magnetometry

3. **Result?**

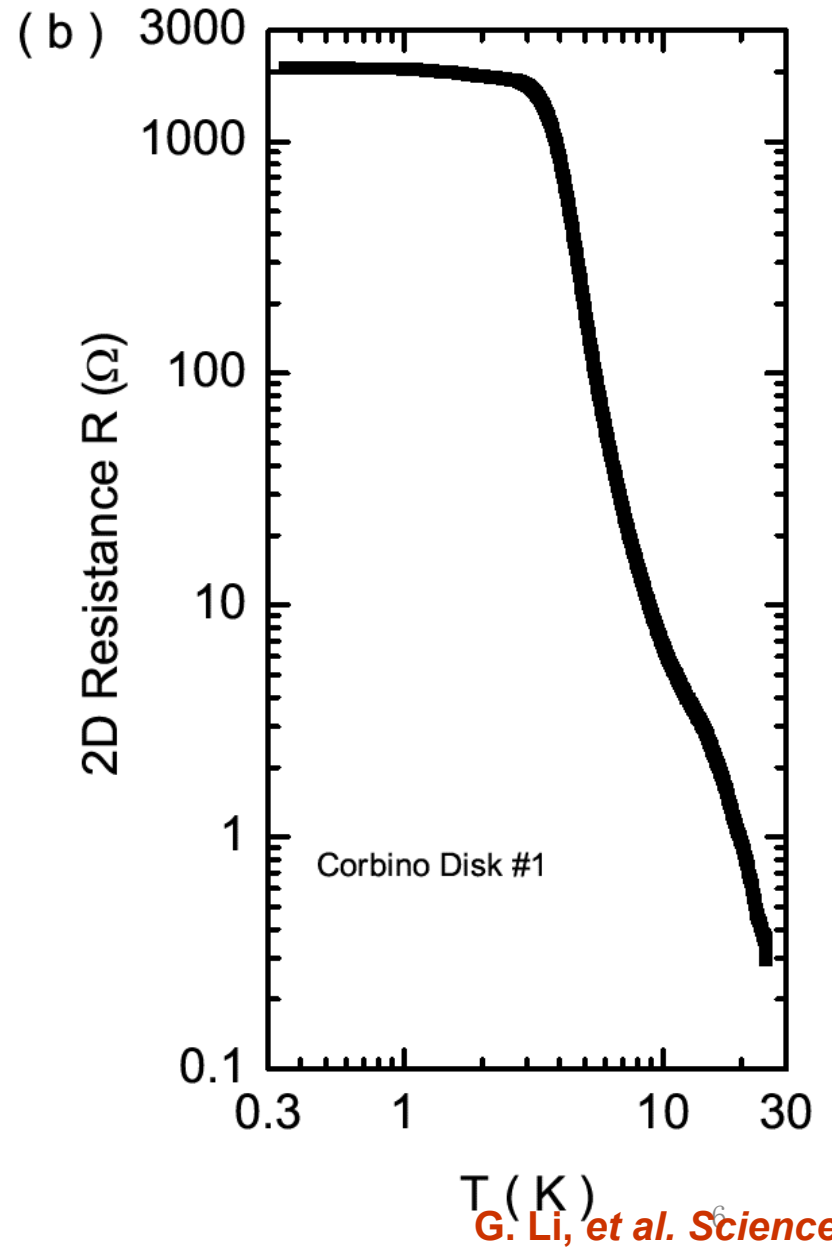
- Quantum oscillations in **M**
- 2 dimensional surface state  
 $F \sim 1 / \cos(\text{angle})$
- Landau Levels index plots  $\rightarrow$   
-1/2 Berry phase factor for Dirac dispersion
- Heavy Mass observed in  
Floating-zone samples



# Insulating above 4 K, but metallic at lower T



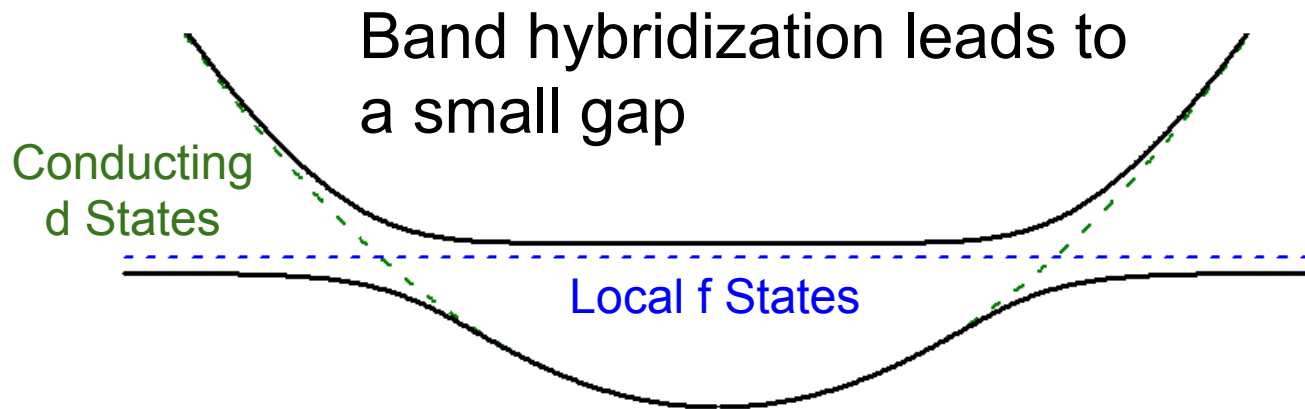
Menth, Buehler, Geballe, PR 1968



$T$  (K)  
G. Li, et al. Science

# Kondo Insulator $\text{SmB}_6$

- Mixed valence:  $\text{Sm}^{3+}$  and  $\text{Sm}^{2+}$  both present
- Kondo insulator
  - Metallic properties at low T
  - Non-magnetic insulator properties at low T
- Behavior is attributed to mixing of localized f states and conduction d states



# 3D Topological Kondo Insulators

Theoretical Kondo TI prediction:

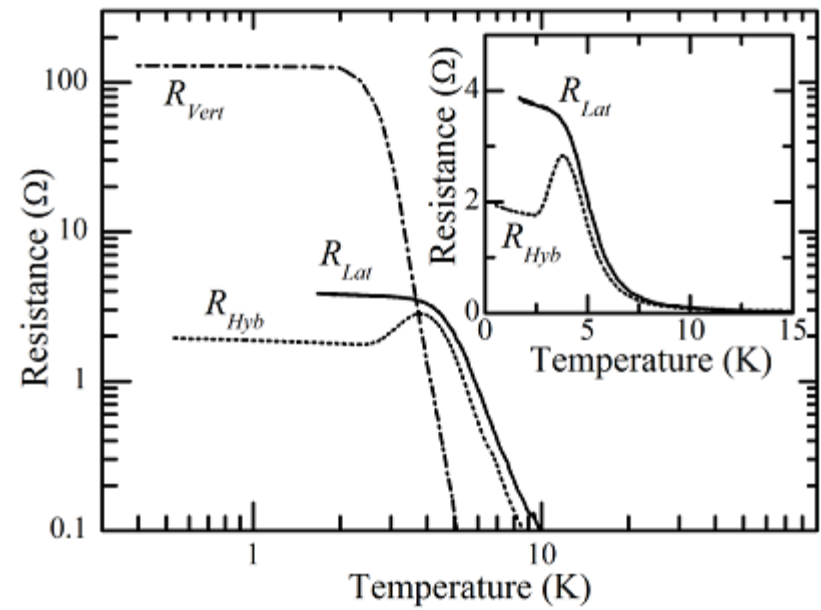
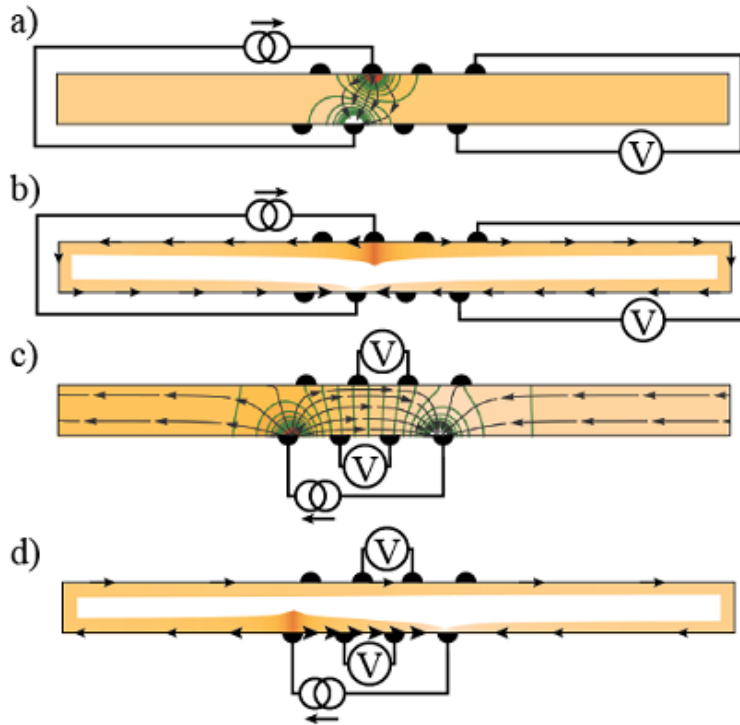
- $\text{SmB}_6$  Dzero, Sun, Galitski, Coleman, *PRL* 2010

Topological Insulator w weak interaction

- Robust (protected) surface state
- Insulating bulk
- Odd number of Dirac cones
- Helical spin structure

*Kane, Fu, Zhang, Xi, Moore, Balents ....*

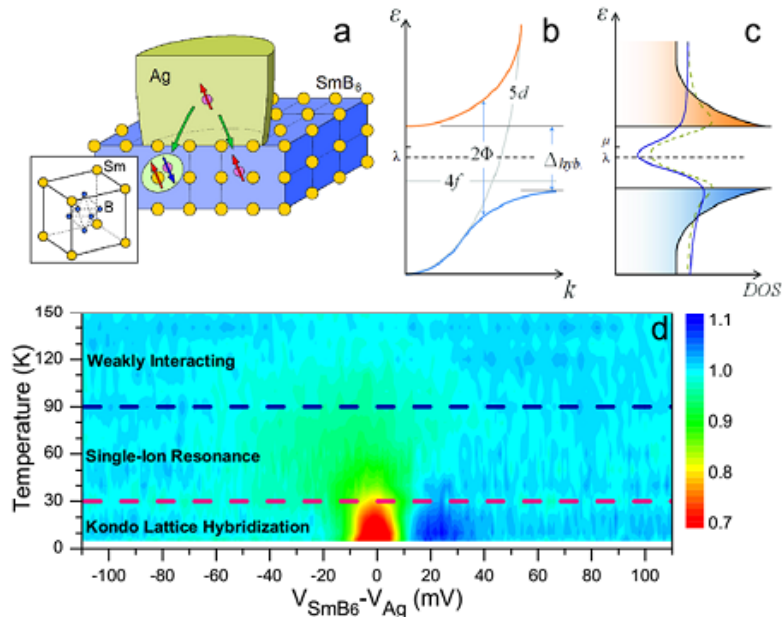
# Surface conductance



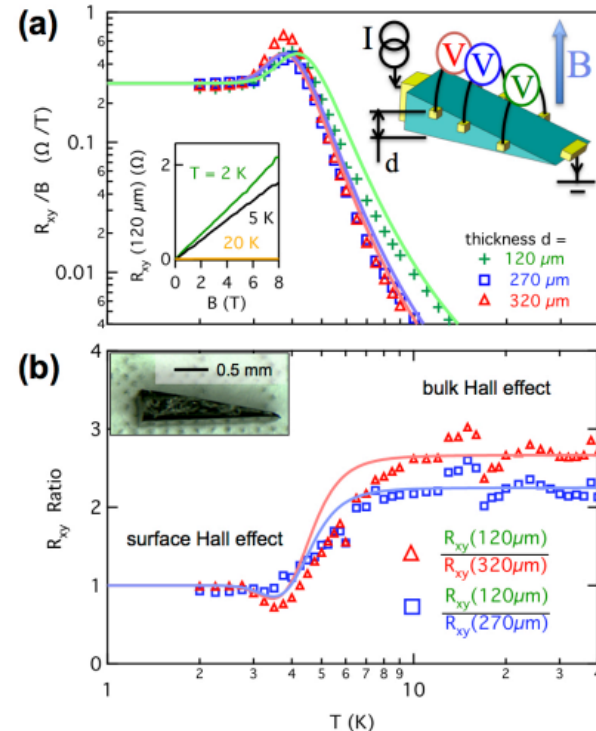
*Wolgast et.al.*  
*arxiv: 2012, PRB 2013*  
*Michigan*



# Surface conductance and bulk gap

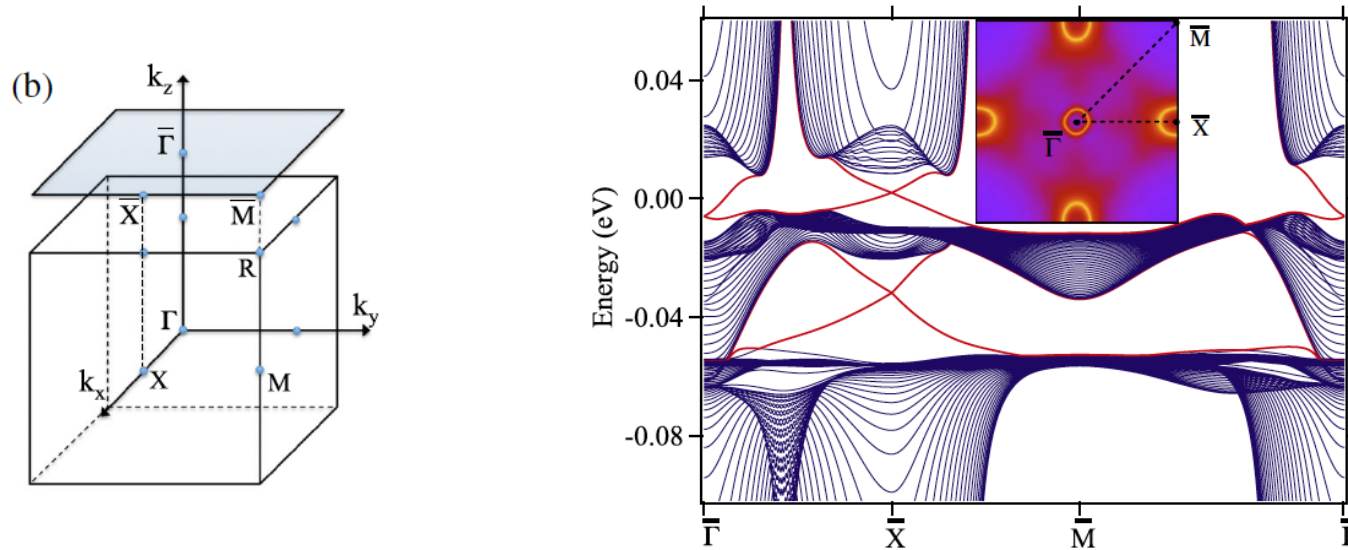


Zhang et al.  
 arxiv:1211.5532  
 PRX 2013  
 Maryland



Botimer et al.  
 arXiv:1211.6769  
 Scientific Report 2013  
 UCI

# Advanced Calculation shows possible surface state on the 100 cleavage plane



3 Dirac Cones, 2 Fermi Surface Areas

# Experimental approach demonstrating the topological surface state

## 1. ARPES *Hasan, Shen, ...*

- Dirac dispersion
- Helical spin structure

## 2. STM *Yazdani. ...*

## 3. Quantum oscillations *Ong, Ando, Fisher ...*

# Experimental approach demonstrating the topological surface state in $\text{SmB}_6$

## 1. ARPES shows Dirac dispersion

*N. Xu, et al., Phys. Rev. B. 88, 121102 (2013).*

*M. Neupane, et al., Nat. Commun.4, 2991 (2013).*

*J. Jiang, et al., Nat. Commun.4, 3010 (2013).*

*E. Frantzeskakis, et al., Phys. Rev. X. 3, 041024 (2013).*

*J. D. Denlinger, et al., arXiv:1312.6637 (2013).*

*Z.-H. Zhu et al., Phys. Rev. Lett. 111, 216402 (2013).*

## 2. STM *Yayu Wang, PRL 2014,*

*S. Wirth, PNAS 2014*

*Hoffman, arXiv:2013*

## 3. Quantum oscillations

*Gang Li & L. Li, Science 2014*

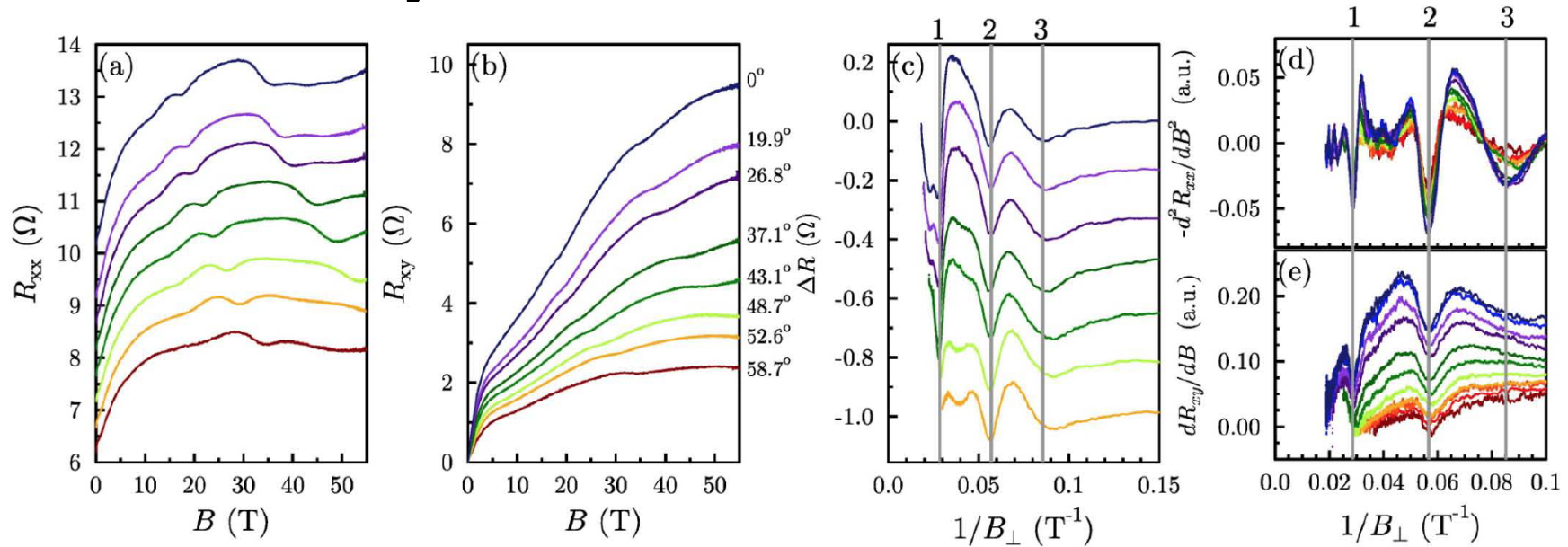
*J. Xia et al....*

*Sebastian et al... Science 2015*

# Quantum Oscillations reveal

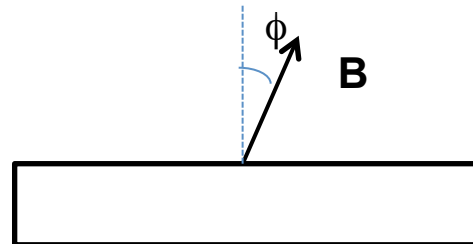
## 1. Dimensionality

$\text{Bi}_2\text{Se}_3$



Scale as  $1/B_{\text{perp}}$ ,

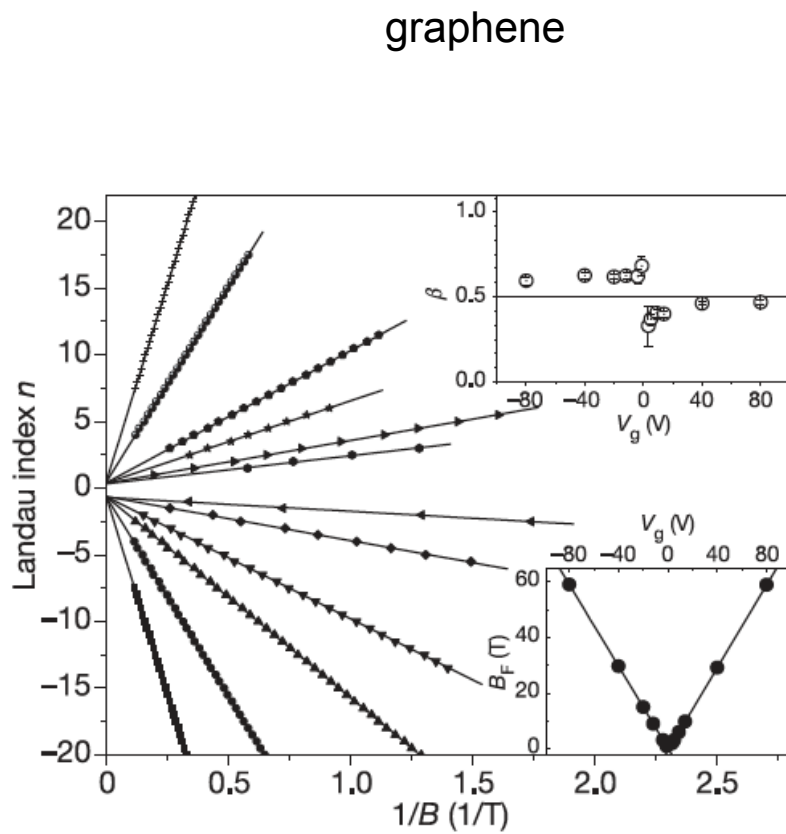
frequency  $\sim 1/\cos(\phi)$



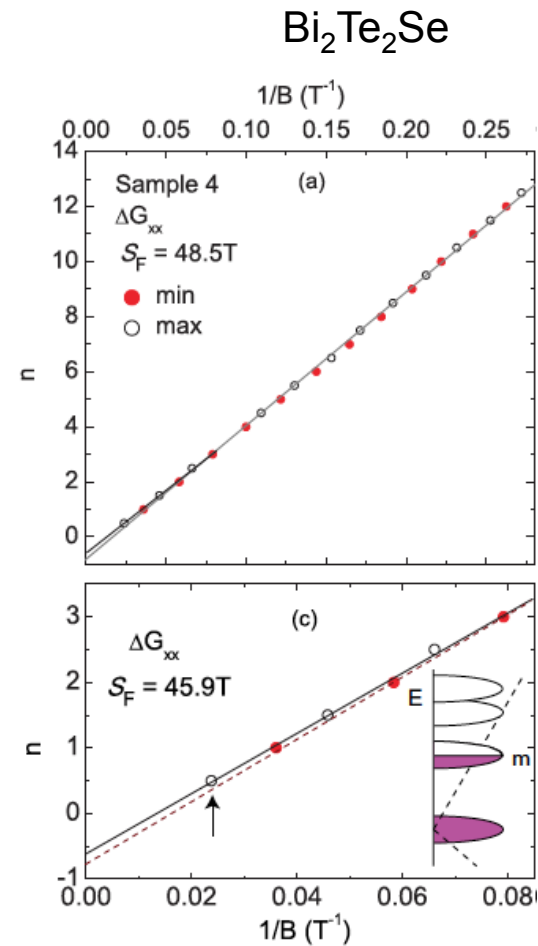
*Analytis et al. Nature Physics 2010*

# Quantum Oscillations reveal

## 2. Signature of Dirac dispersion in the Landau Levels index plot

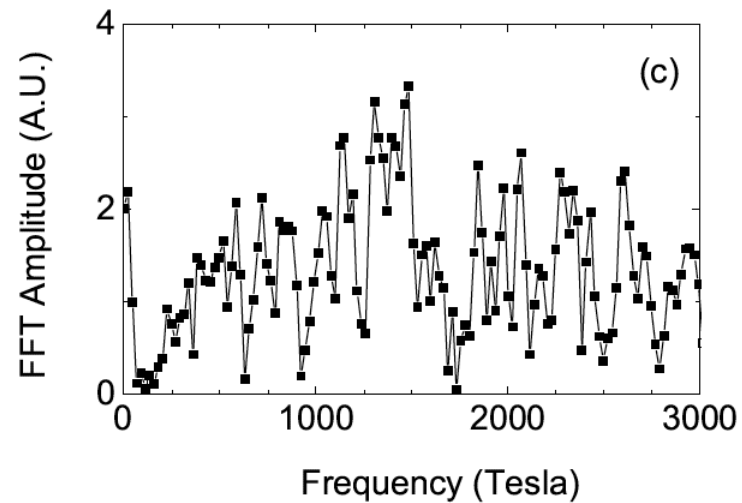
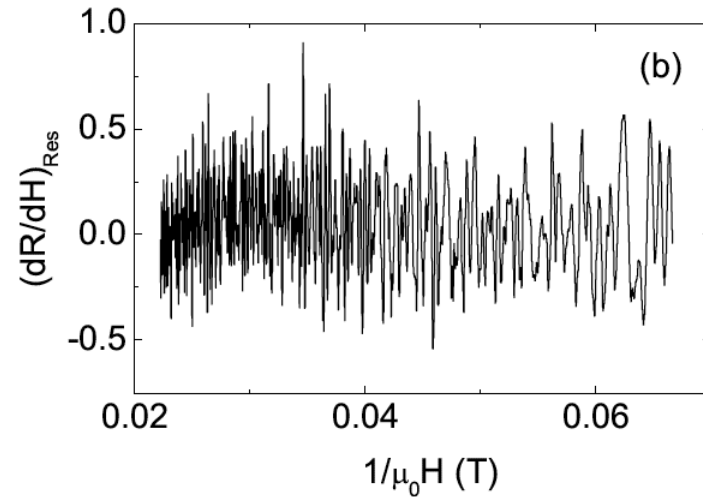
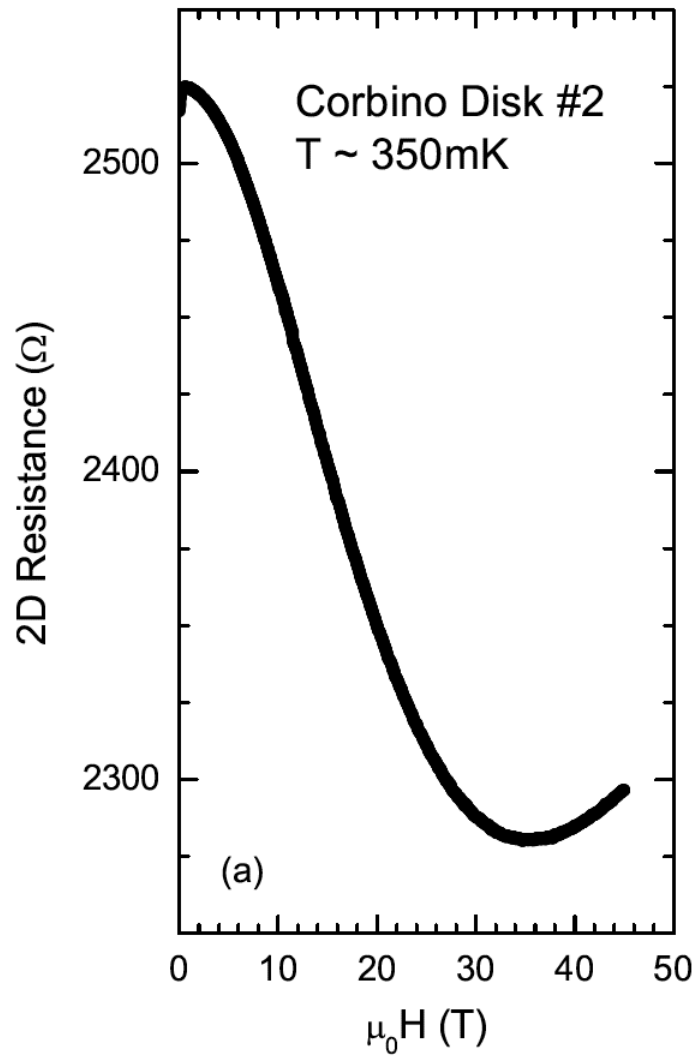


Zhang & Kim *Nature* (2005)



Xiong & Ong *PRB* (2012)

# Missing: quantum oscillation in magnetoresistance

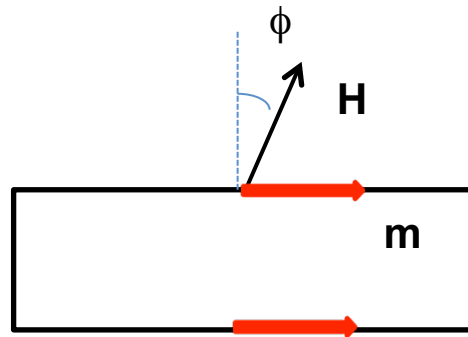


**G. Li, et al. Science 2014**

**Challenge: how to measure the magnetic moment  
of surfaces?**



# Challenge: how to measure the magnetic moment of surfaces?



Torque on moment:  $\tau = m \times B$

# Torque magnetometry

Torque on moment:  $\tau = \mathbf{m} \times \mathbf{B}$

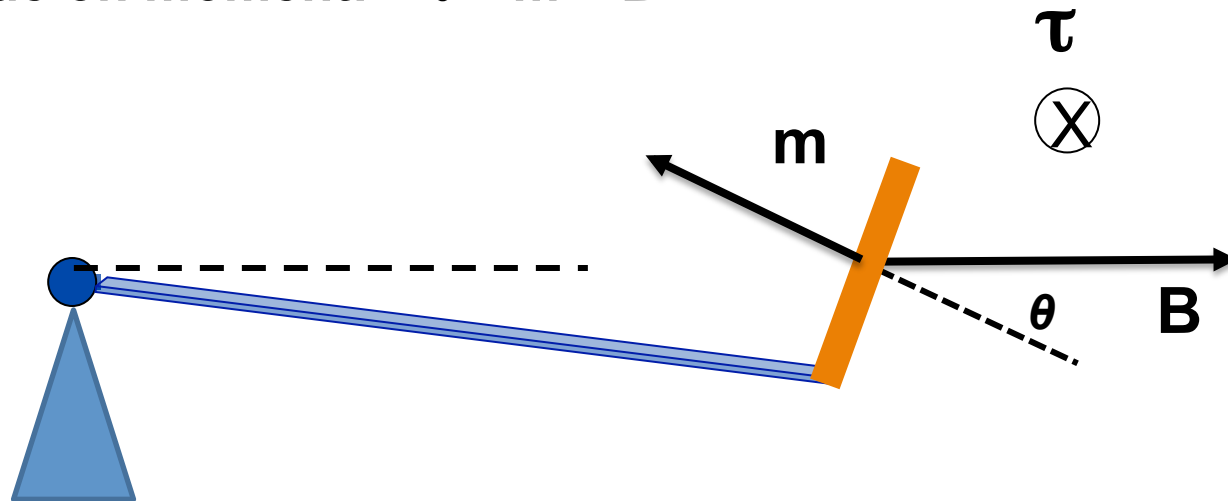


Deflection of cantilever:  $\tau = k \phi$

$$M_{\text{eff}} = \tau / \mu_0 H V \sin(\theta)$$

# Torque magnetometry

Torque on moment:  $\tau = m \times B$

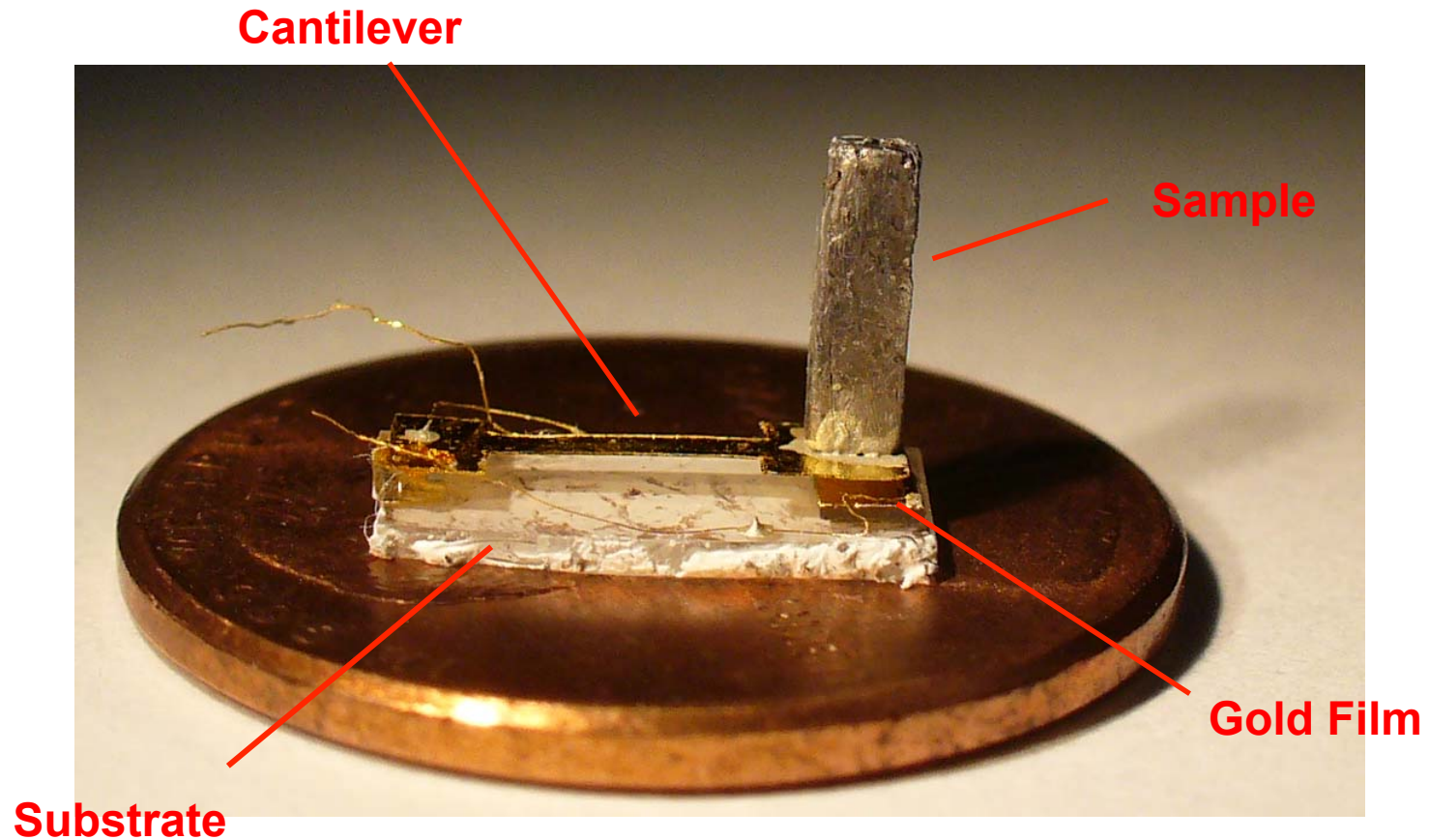


Deflection of cantilever  $\rightarrow$  torque  $\tau$

$$M_{\text{eff}} = \tau / \mu_0 H V \sin(\theta)$$

**Only sensitive to magnetic anisotropy**

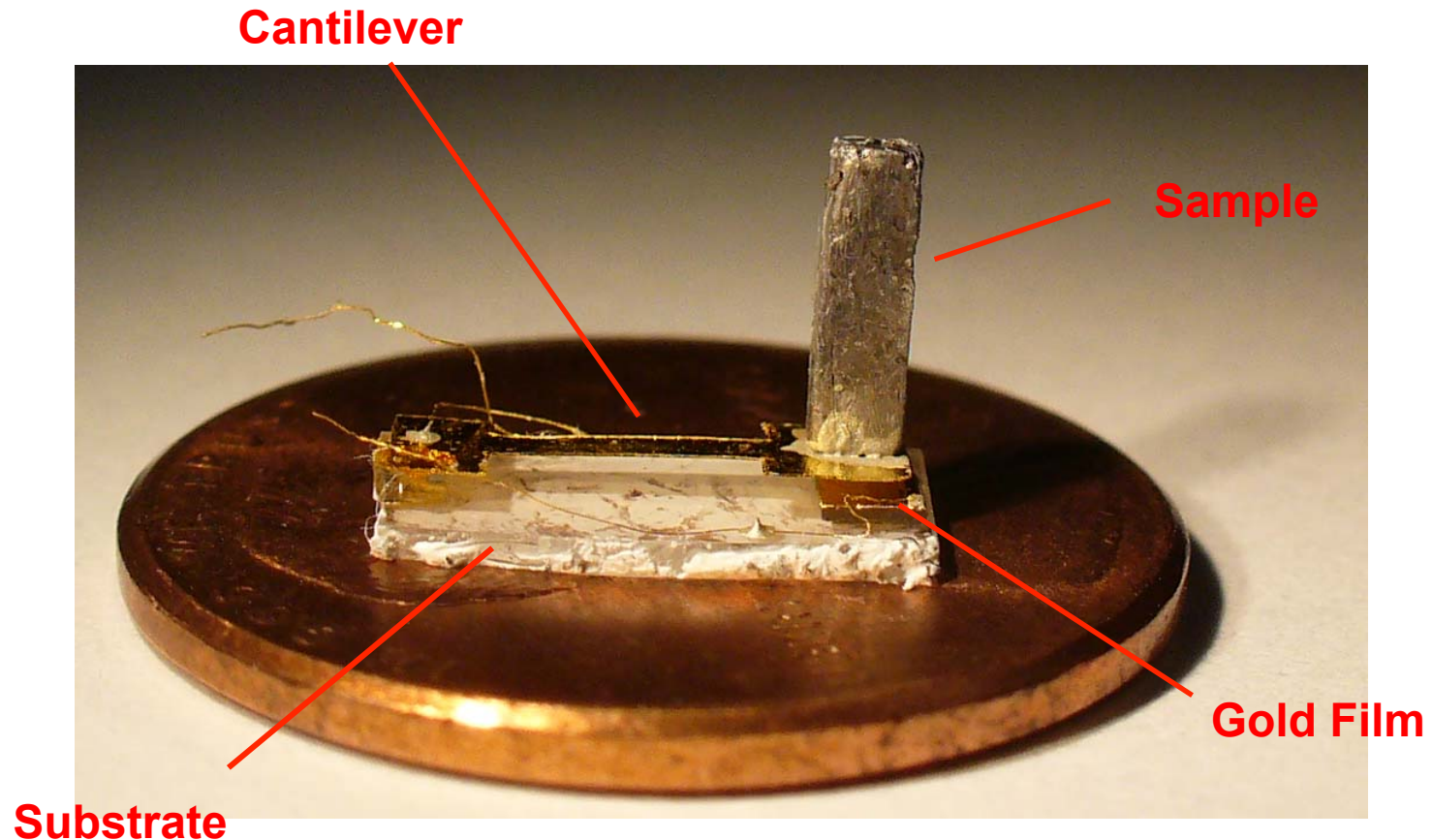
# Cantilever setup of bismuth



1. Magnetic moment  $\Delta m \sim 10^{-13} \text{ A.m}^2$  at 10 T (  $10^{10} \mu_B$  )  
( SQUID MPMS,  $\Delta m \sim 10^{-9} \text{ A.m}^2$  )
2. Works up to 45 Tesla, at 20 m K  $\sim$  300 K

*Li, Cava, Uher, Hebard, Ong ... Science (2008)*

# Cantilever setup of bismuth



Magnetic moment  $\Delta m \sim 10^{-13} \text{ A.m}^2$  at 10 T (  $10^{10} \mu_B$  )

For a 3 mm X 2 mm X 0.2 mm  $\text{SmB}_6$  crystal,

$$\Delta m \sim 10^{-4} \mu_B / \text{u.c.}$$

Susceptibility resolution (at 10 T )  $\Delta \chi \sim 10^{-6}$

# Laboratory

Dilution Refrigerator



18 mK – 40 K  
Magnetic field up to 8 T

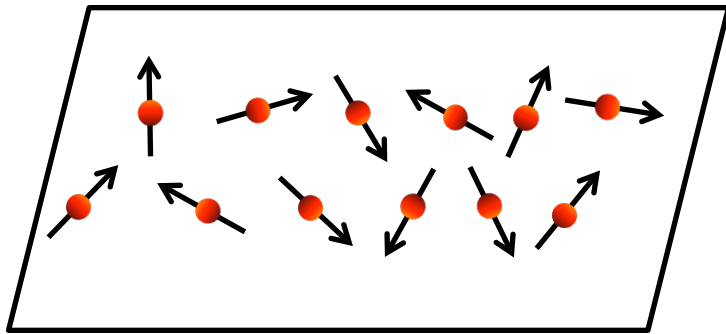
NHMFL Hybrid



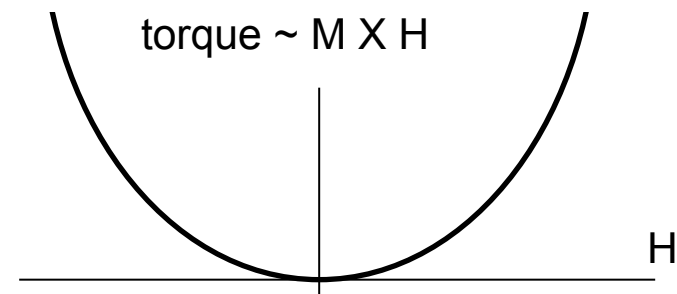
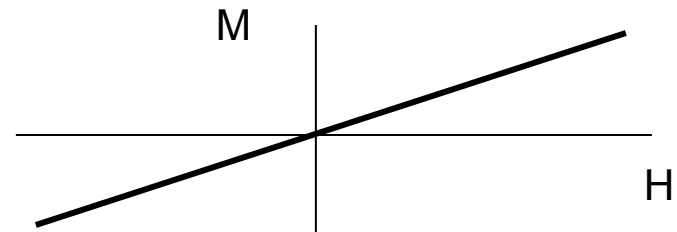
Magnetic field up to 45T

# Torque curve examples

Paramagnet

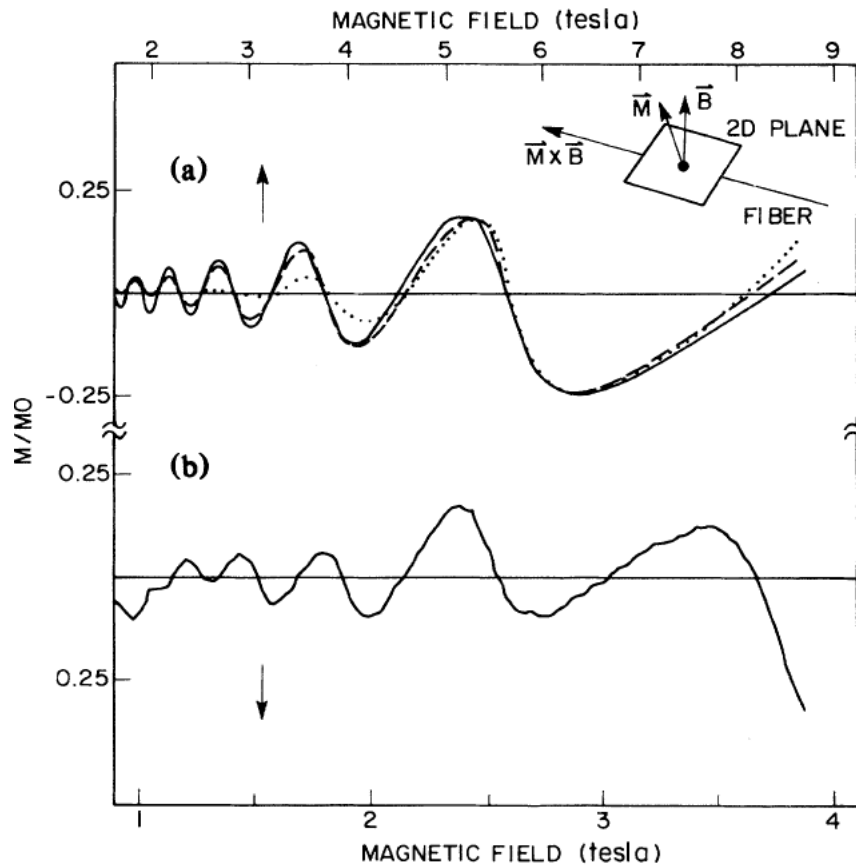


$M$  proportional to  $H$   
 $\text{torque} = M \times H \sim H^2$



# Torque curve examples

2D electronic system

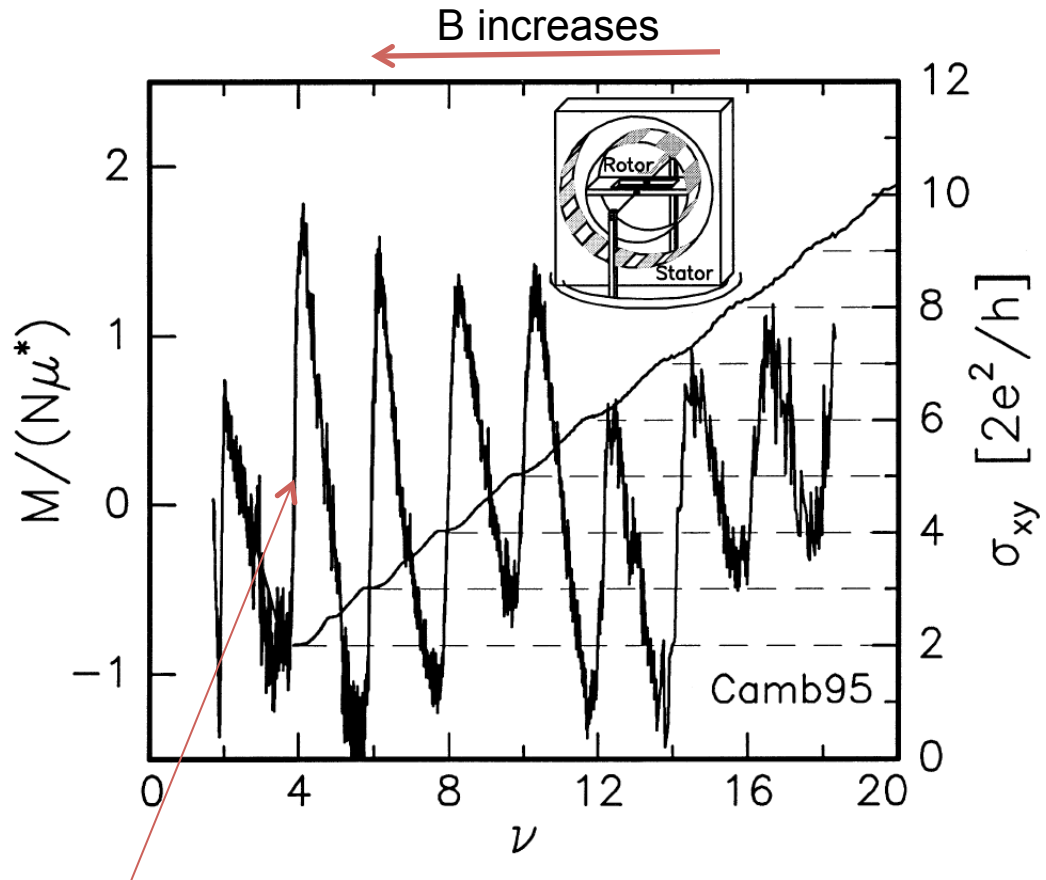


*Eisenstein et al. PRL 1985*



# Torque curve examples

2D electronic system



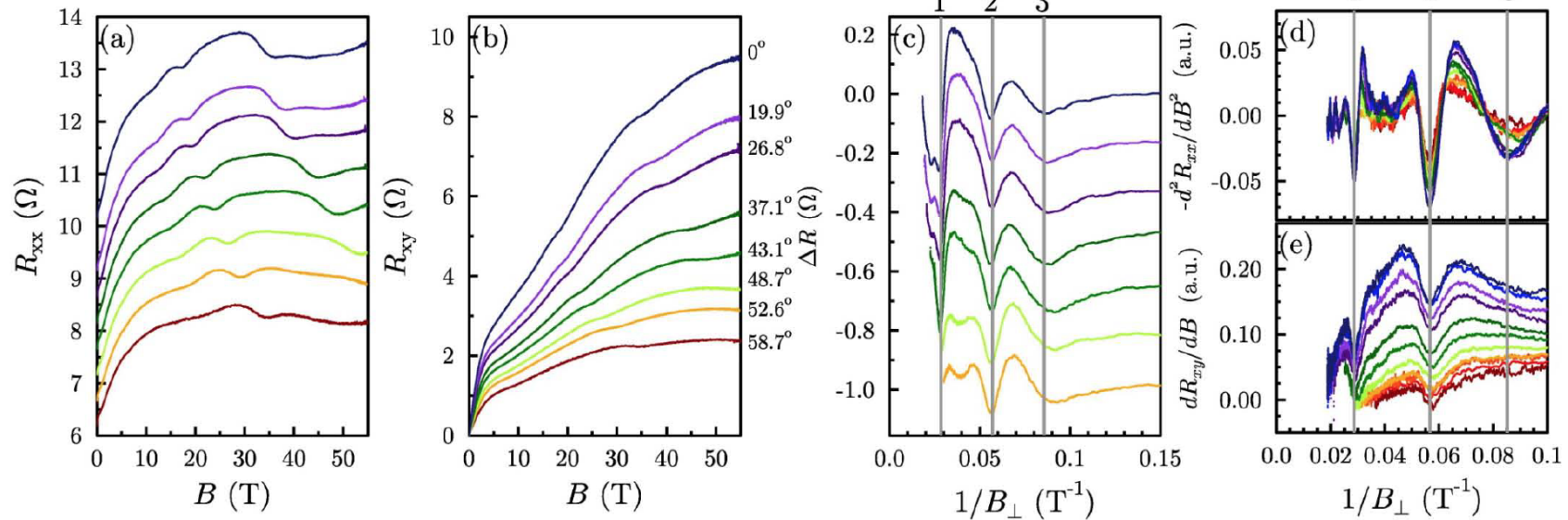
At integer  $\nu$  filling,  
 $M$  drops sharply,  
 $dM/dH$  is minimum

$2 \mu_B$  change at each LL

Wieggers et al. PRL 1997

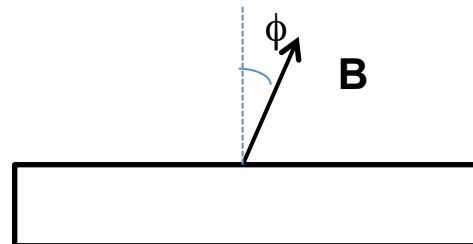
# 2DEG oscillation $F \sim 1/\cos(\phi)$

## 1. Dimensionality



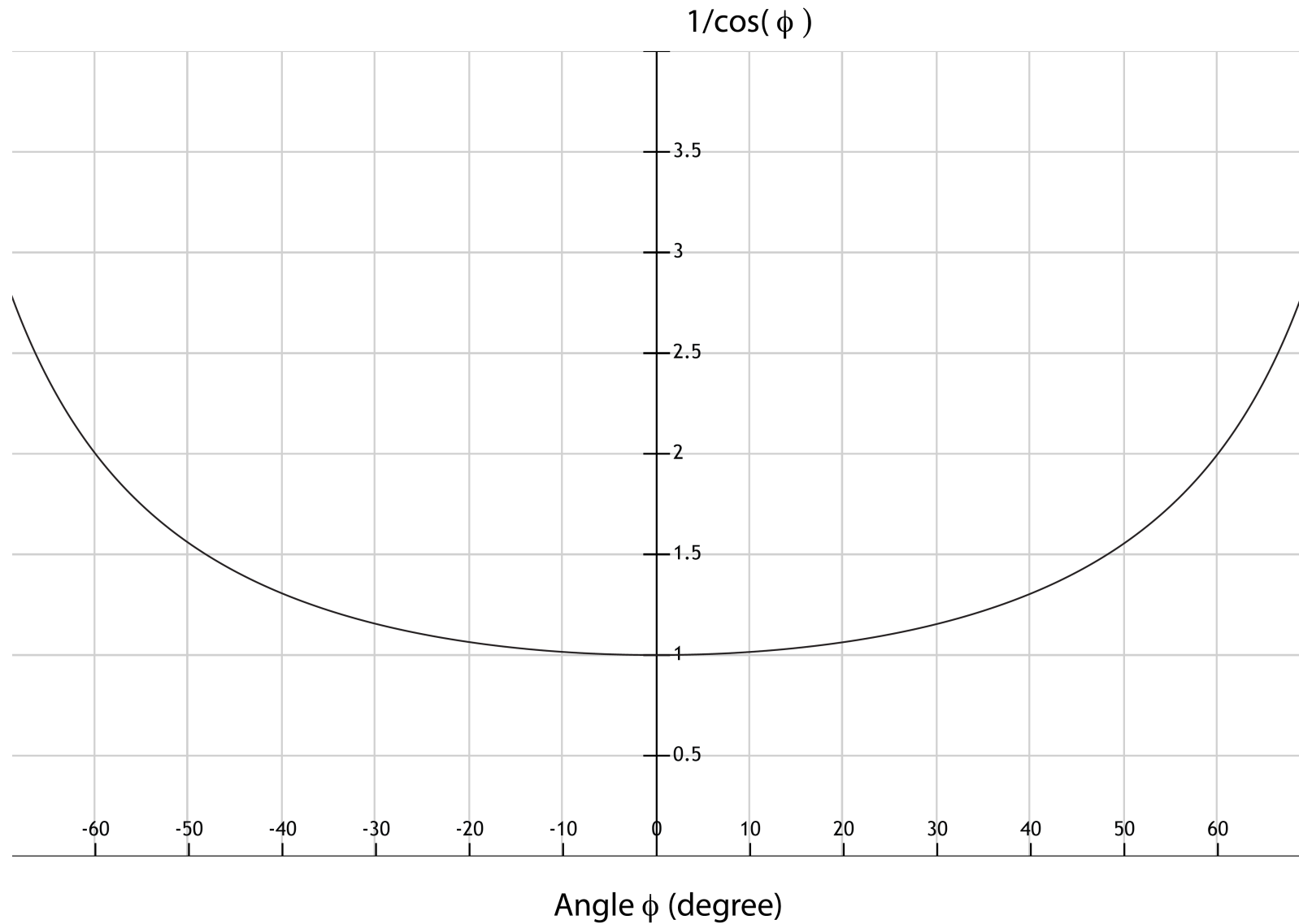
Scale as  $1/B_{\text{perp}}$ ,

frequency  $\sim 1/\cos(\phi)$

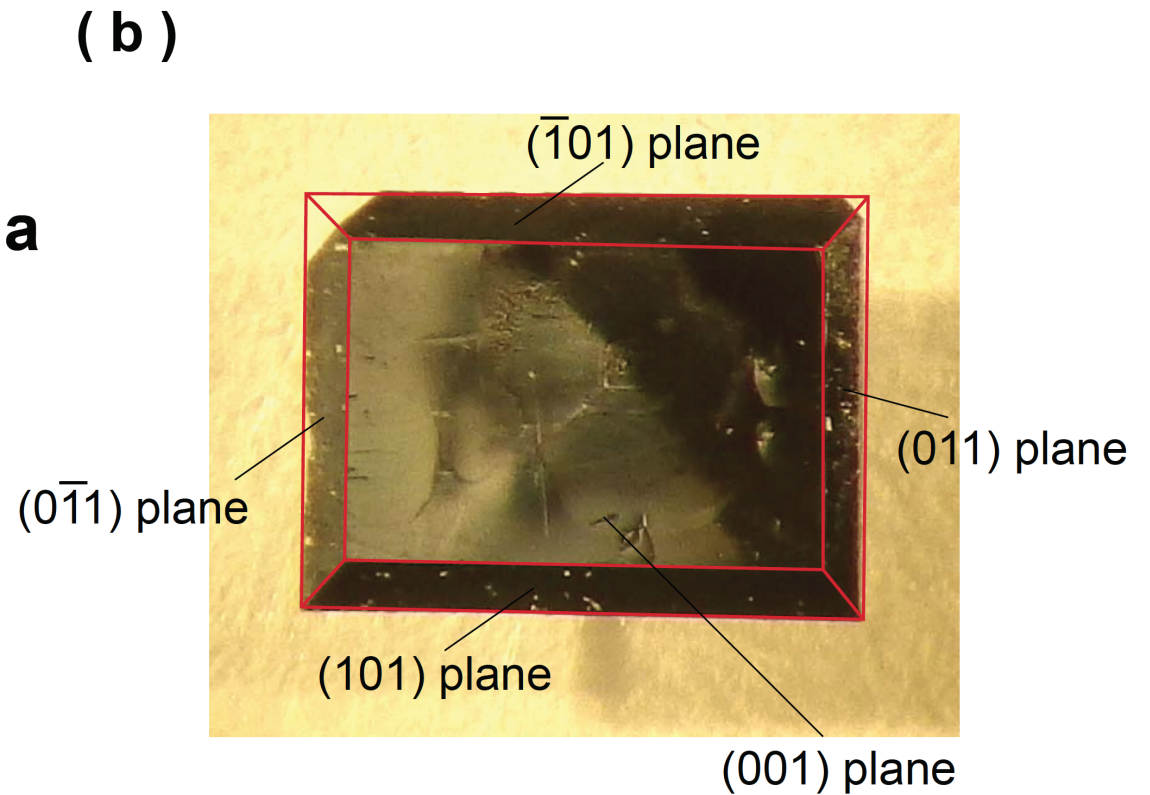
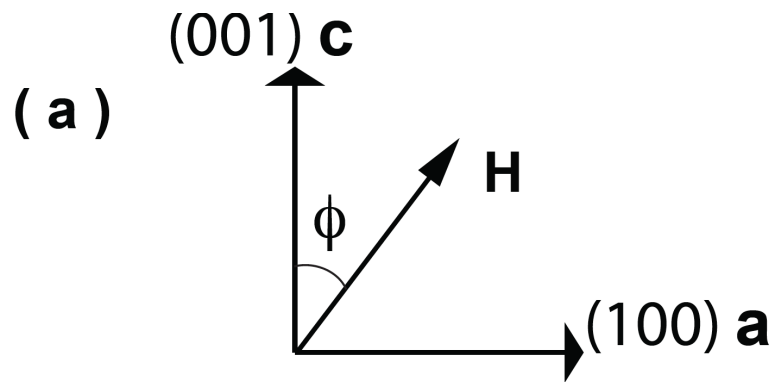


*Analytis et al. Nature Physics 2010*

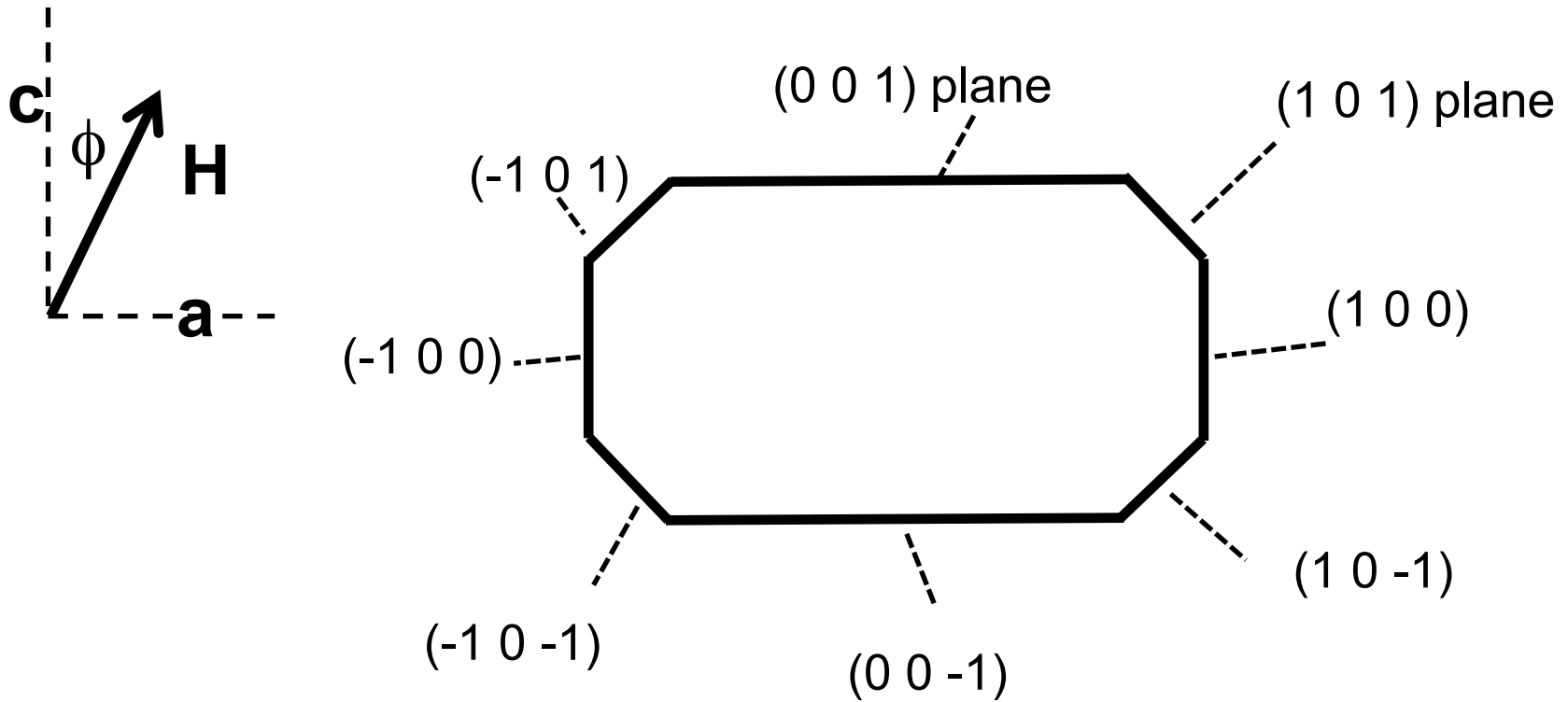
# 2DEG oscillation $F \sim 1/\cos(\phi)$



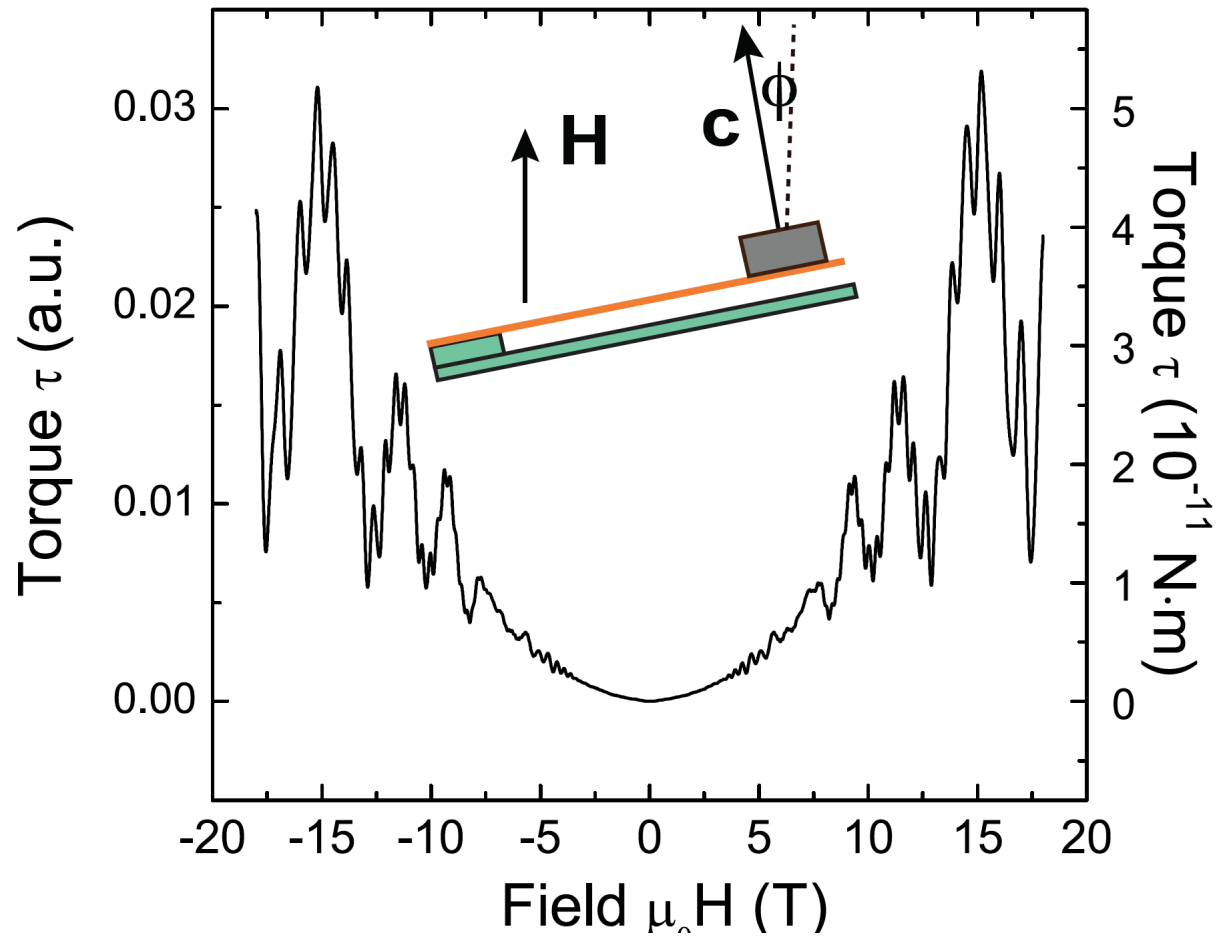
# SmB<sub>6</sub> samples



# Sketch Sample sideview

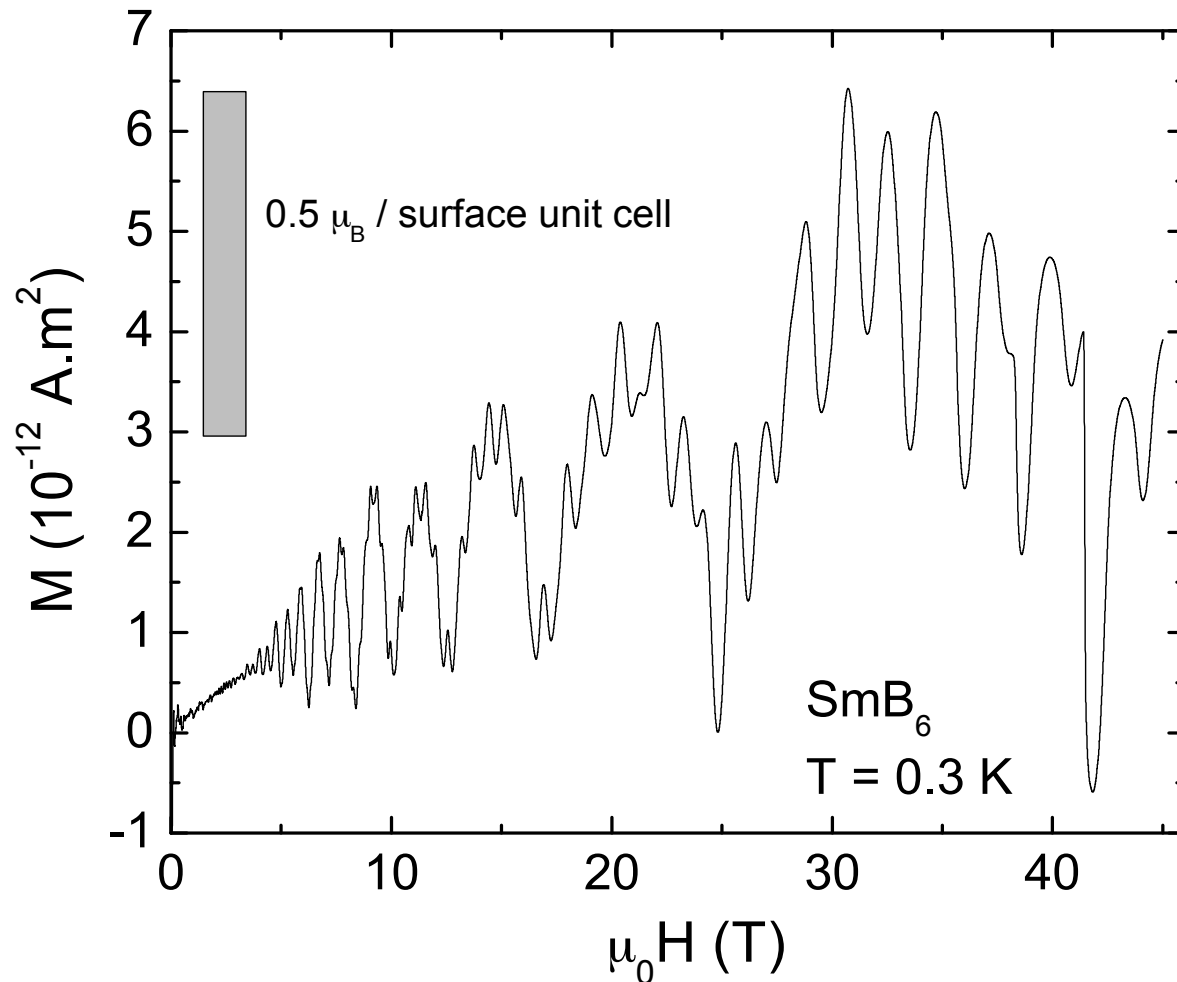


# Quantum oscillations in magnetic torque



G. Li, et al. *Science* 2014

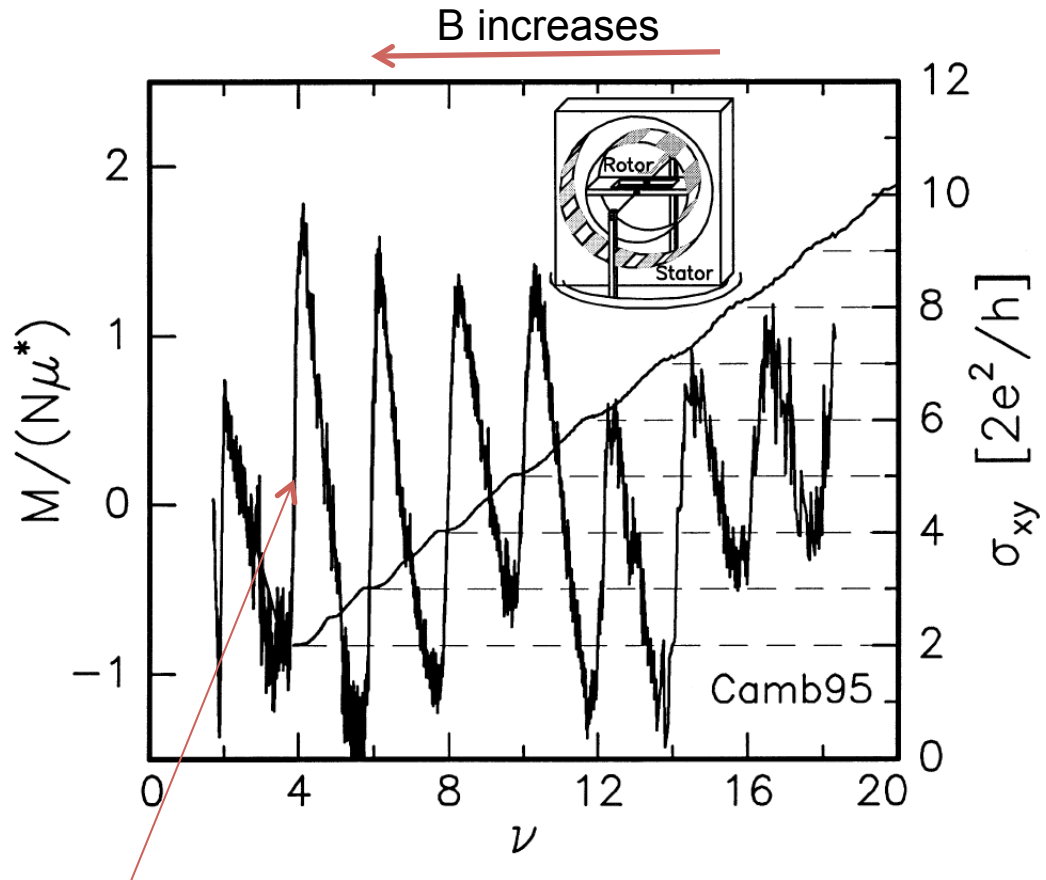
# Magnetization resolved for surfaces



For a 3 mm X 2 mm X 0.2 mm  $\text{SmB}_6$  crystal,  
resolution  $\Delta m \sim 10^{-4} \mu_B$  /u.c.

# Torque curve examples

2D electronic system



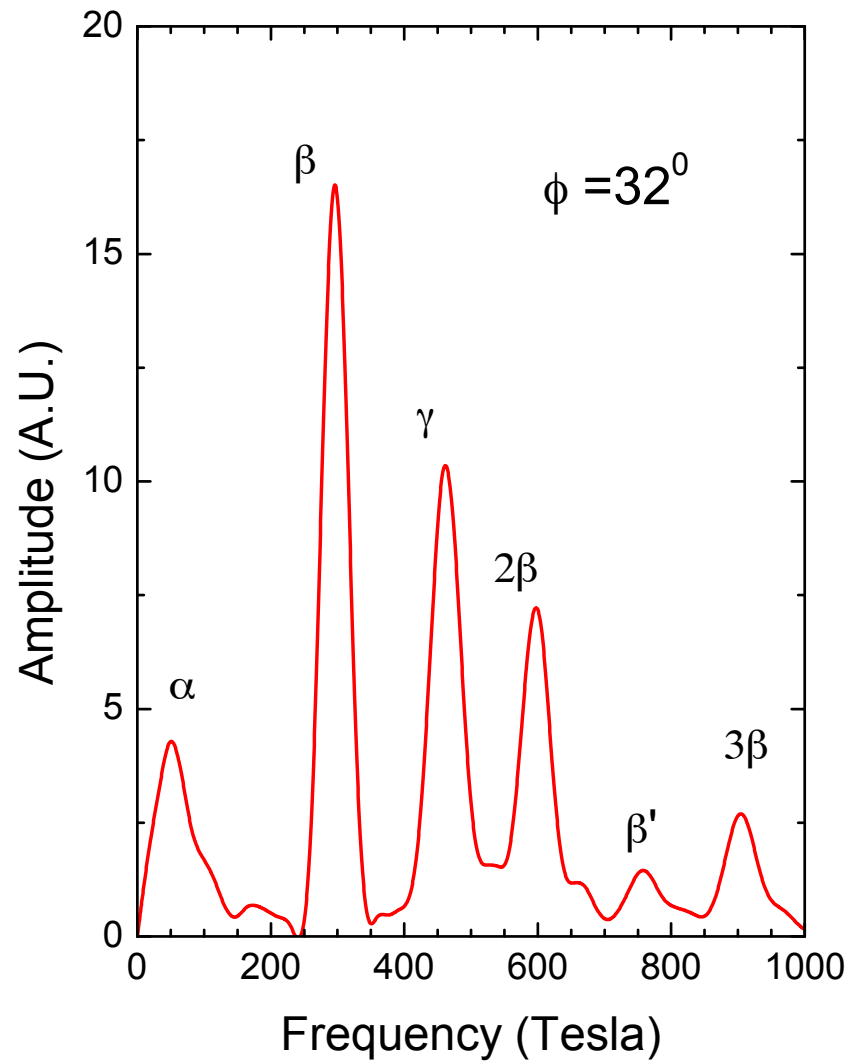
At integer  $\nu$  filling,  
 $M$  drops sharply,  
 $dM/dH$  is minimum

$2 \mu_B$  change at each LL

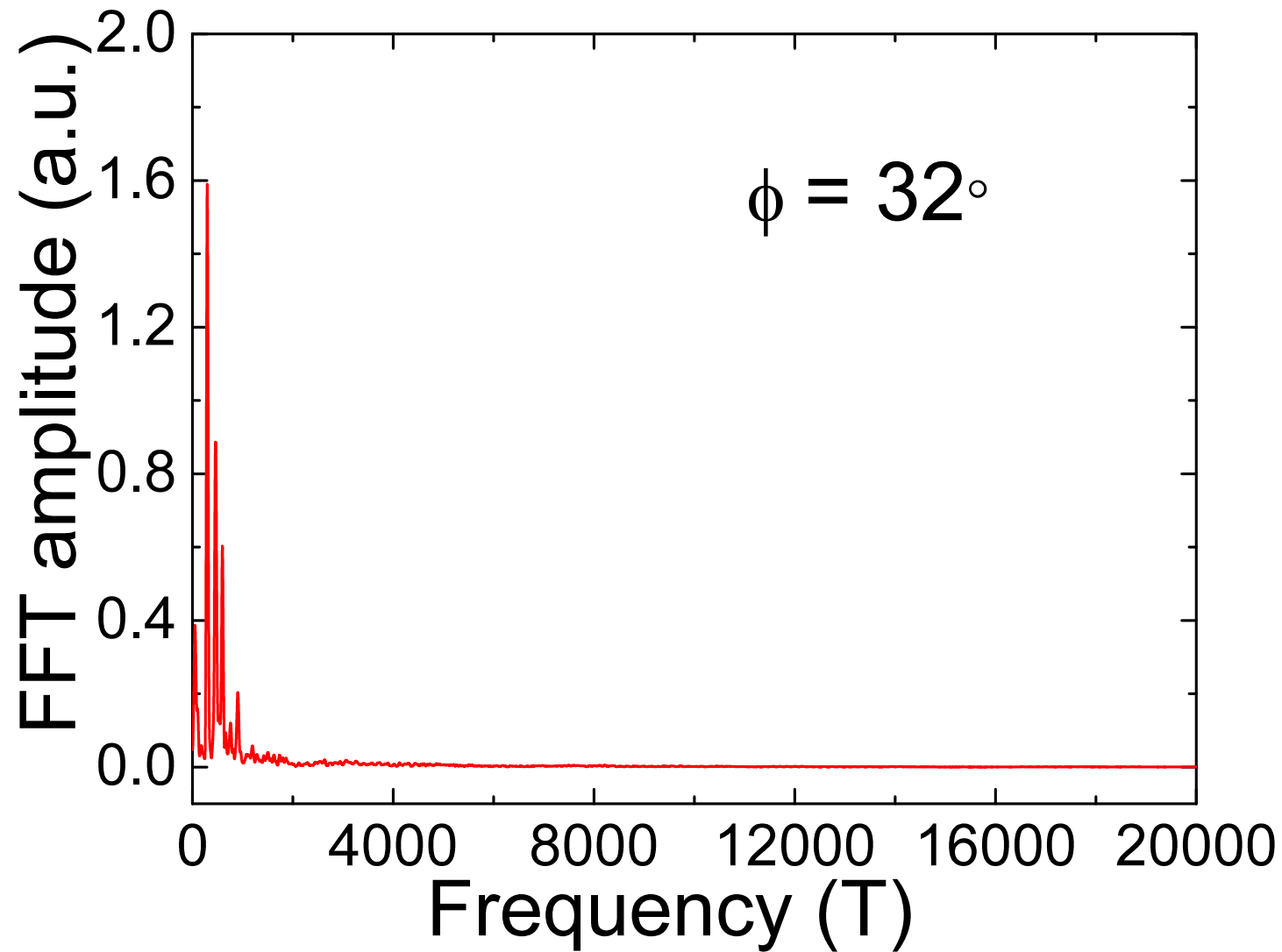
Wieggers et al. PRL 1997



# Fourier Transform shows oscillation frequencies



# No oscillation frequencies observed above 2 kT



# Topological Kondo insulators $\text{SmB}_6$

1. **WHY?** Kondo Insulator  $\text{SmB}_6$

2. **HOW?** Torque magnetometry

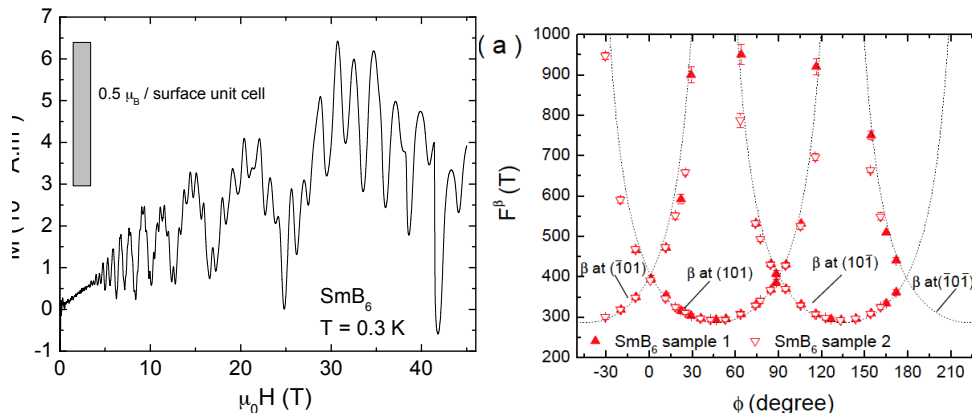
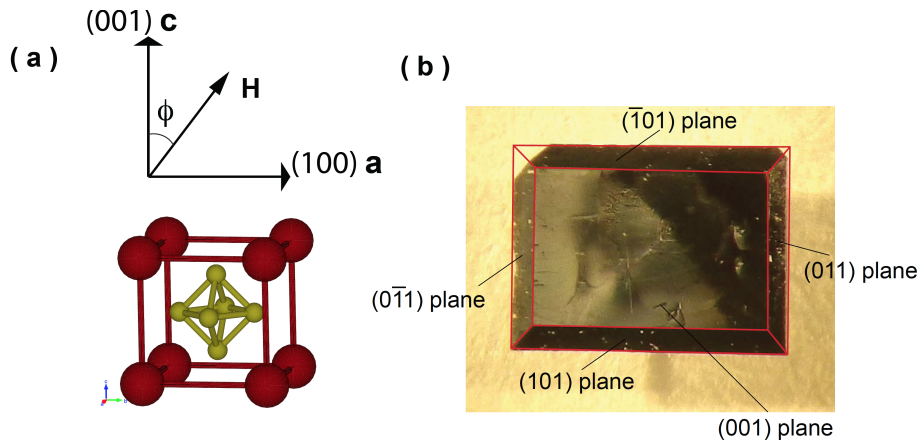
3. **Result?**

- Quantum oscillations in **M**

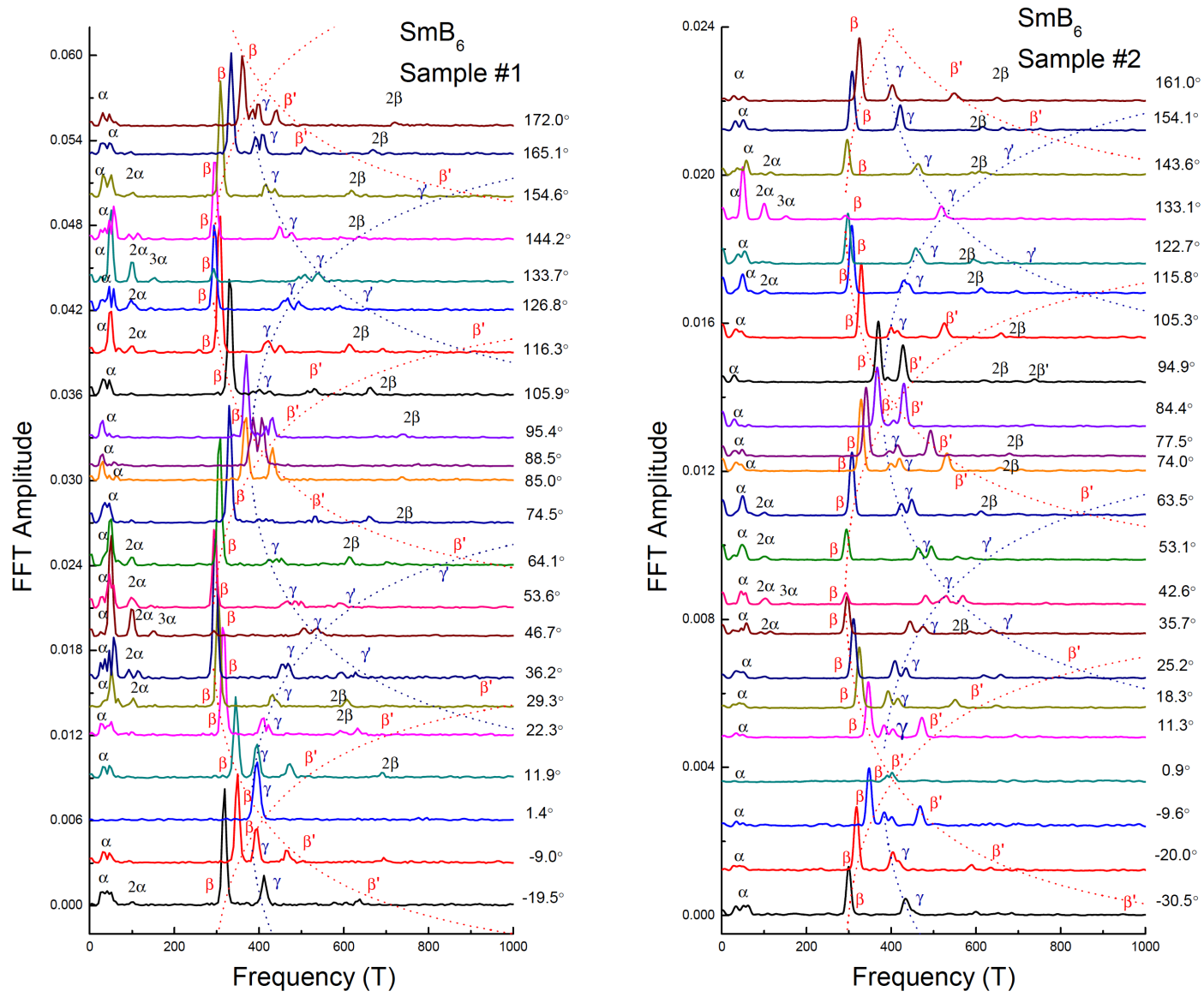
- **2 dimensional surface state  $F \sim 1 / \cos(\text{angle})$**

- Landau Levels index plots  $\rightarrow$   $-1/2$  Berry phase factor for Dirac dispersion

- **Heavy Mass observed in Floating-zone samples**

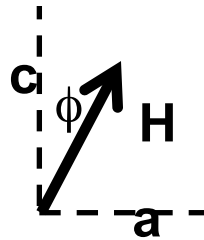
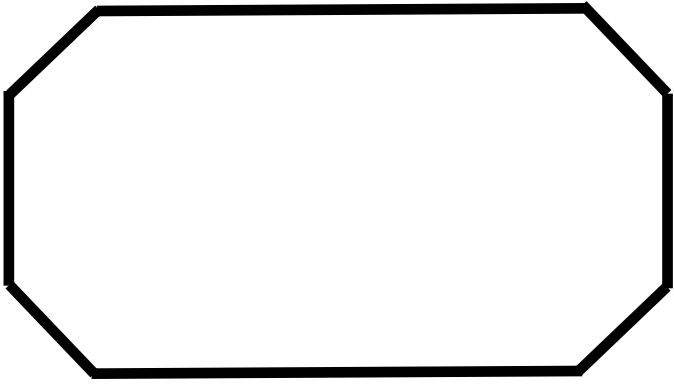


# Track the angular dependence of the frequency

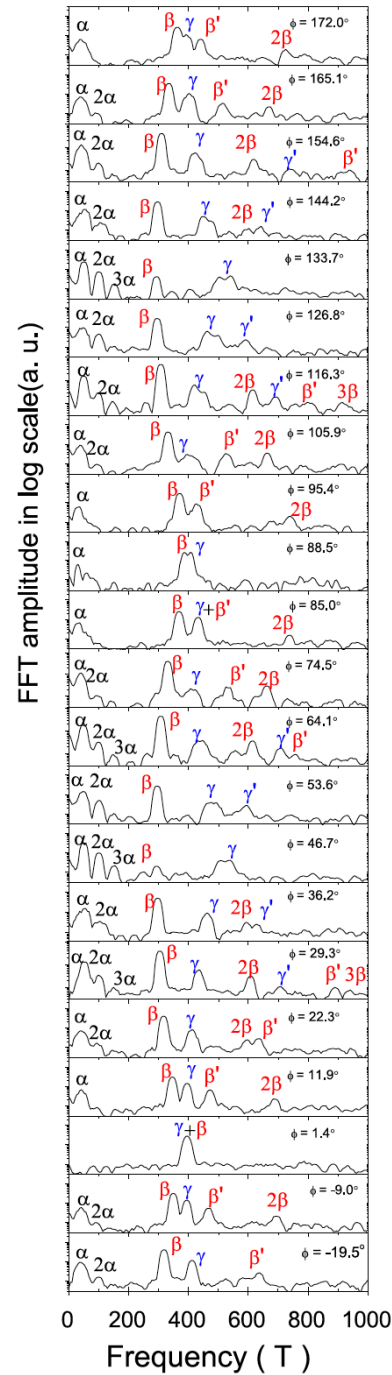


G. Li, et al. Science 2014

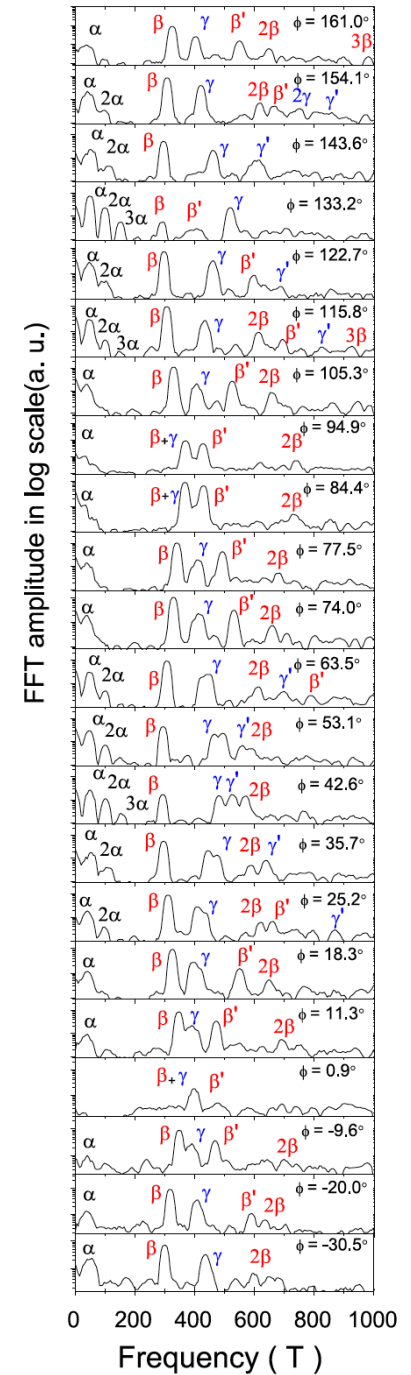
# FFT in logarithmic scale helps track F vs. angle



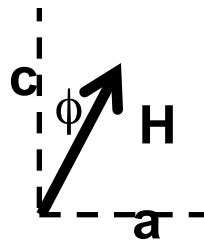
(a) SmB<sub>6</sub> Sample 1



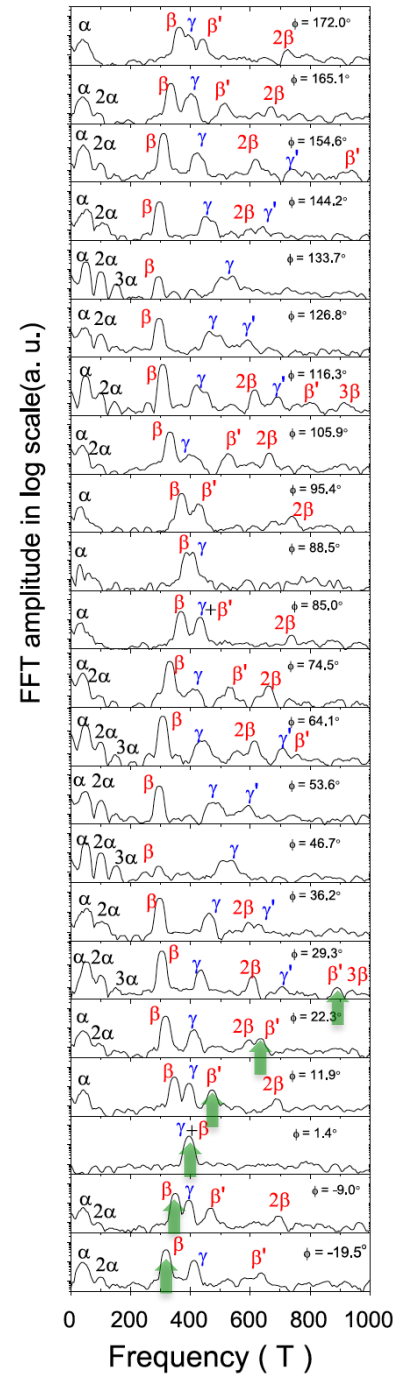
(b) SmB<sub>6</sub> Sample 2



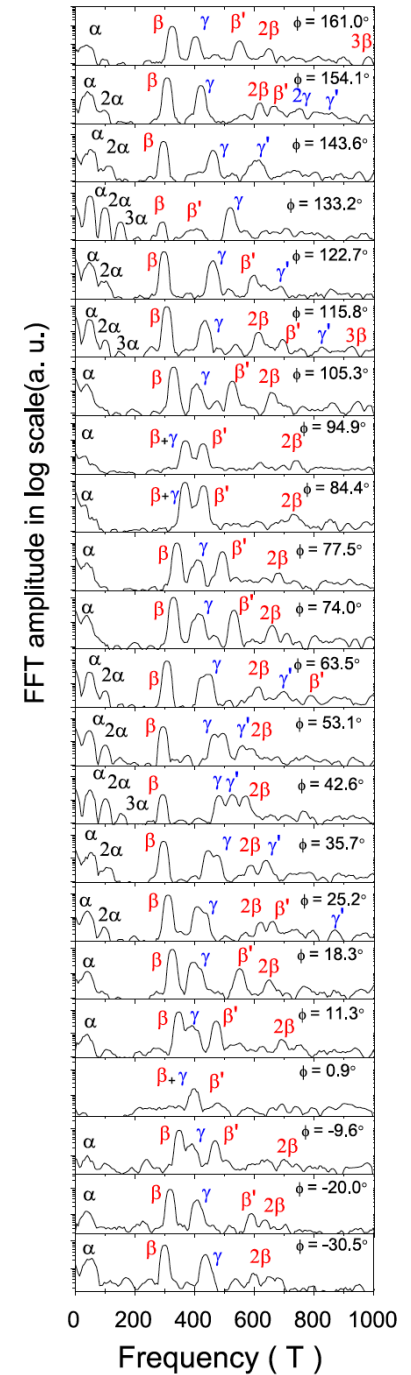
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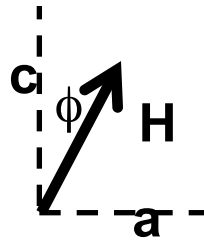
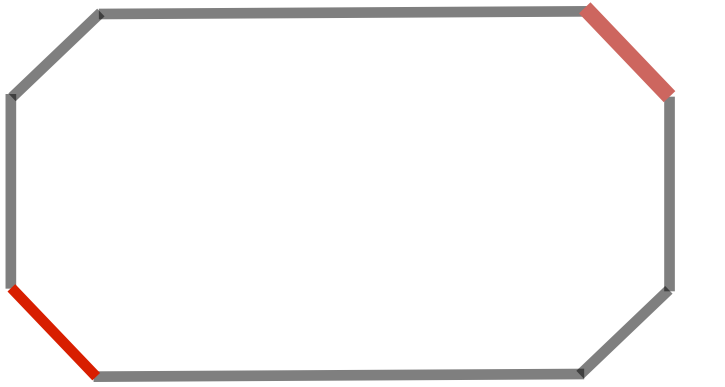
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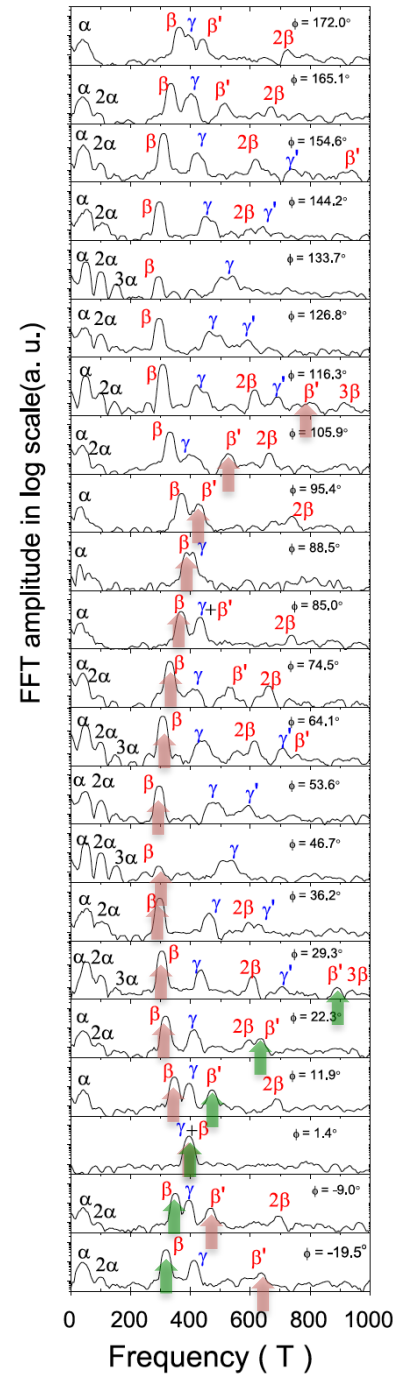
(b) SmB<sub>6</sub> Sample 2



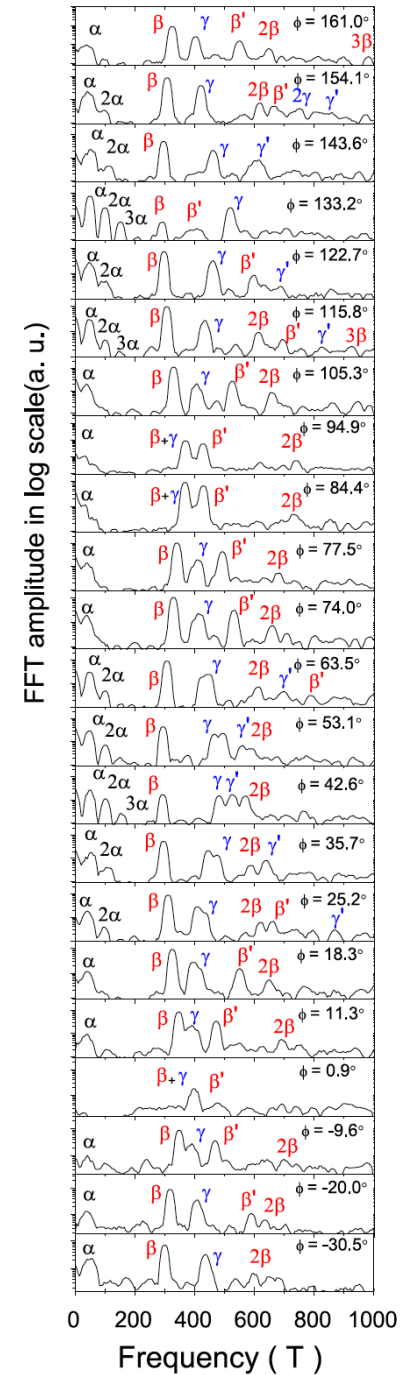
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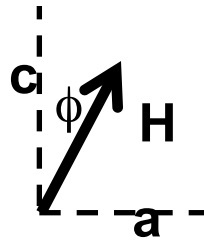
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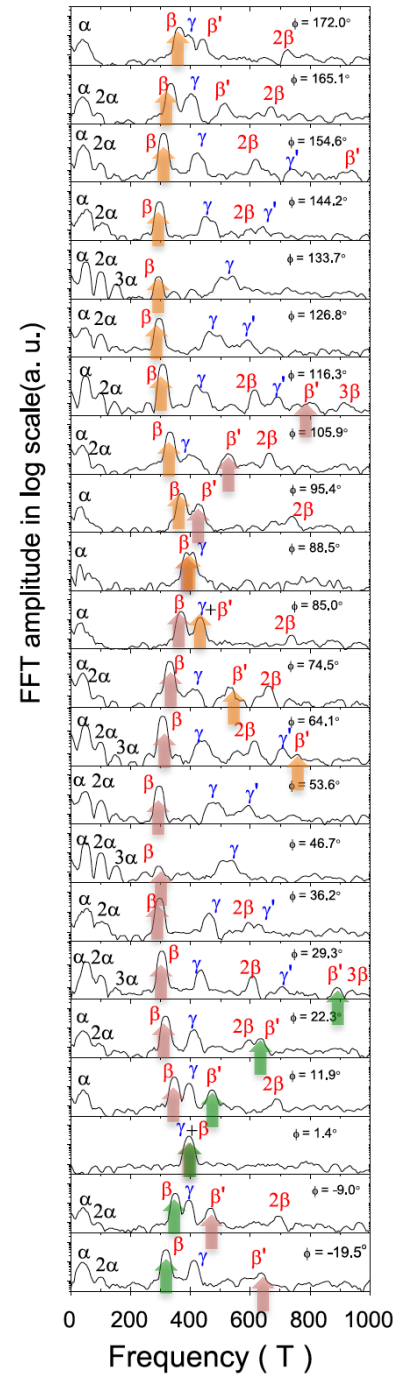
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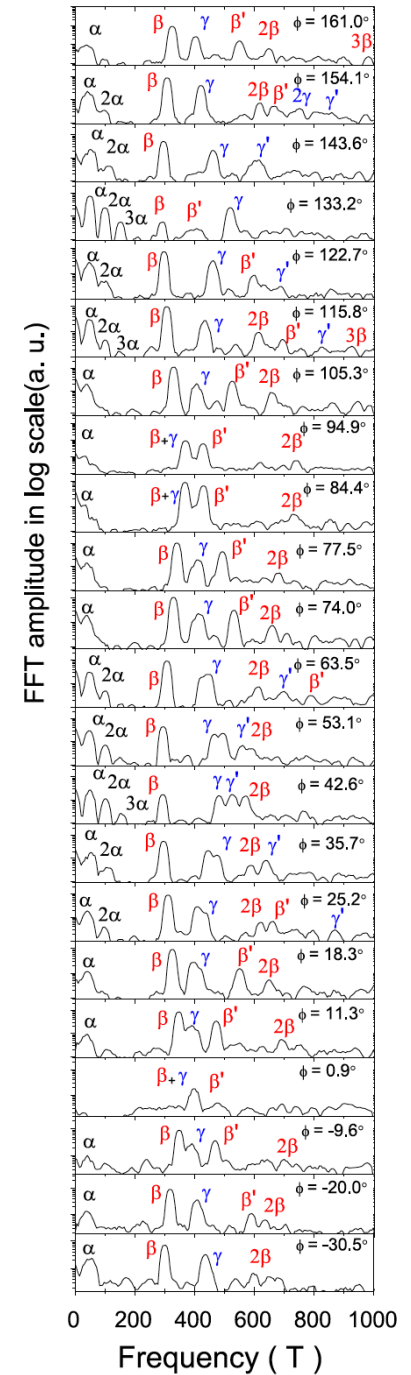
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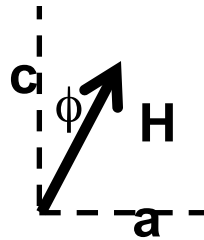


(b) SmB<sub>6</sub> Sample 2

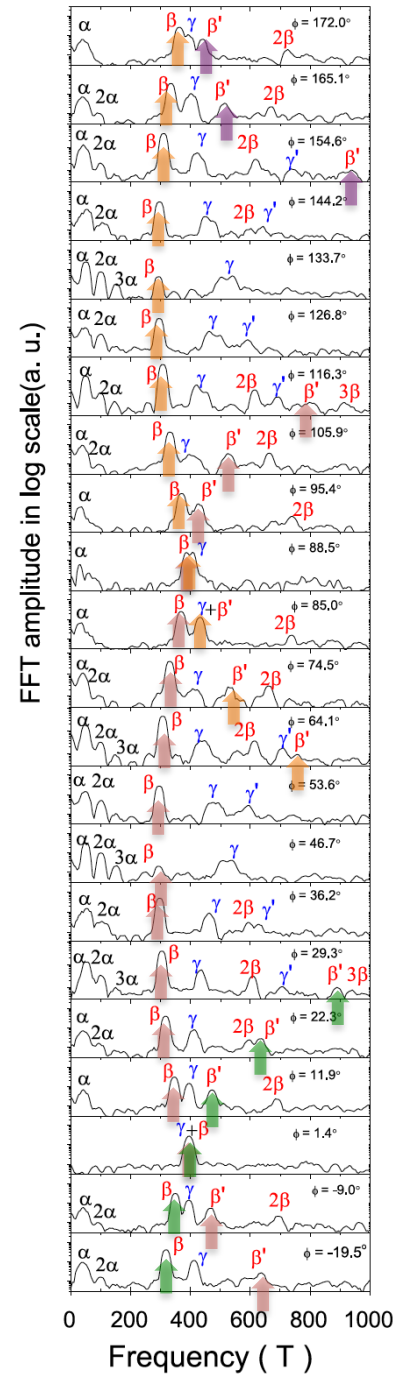




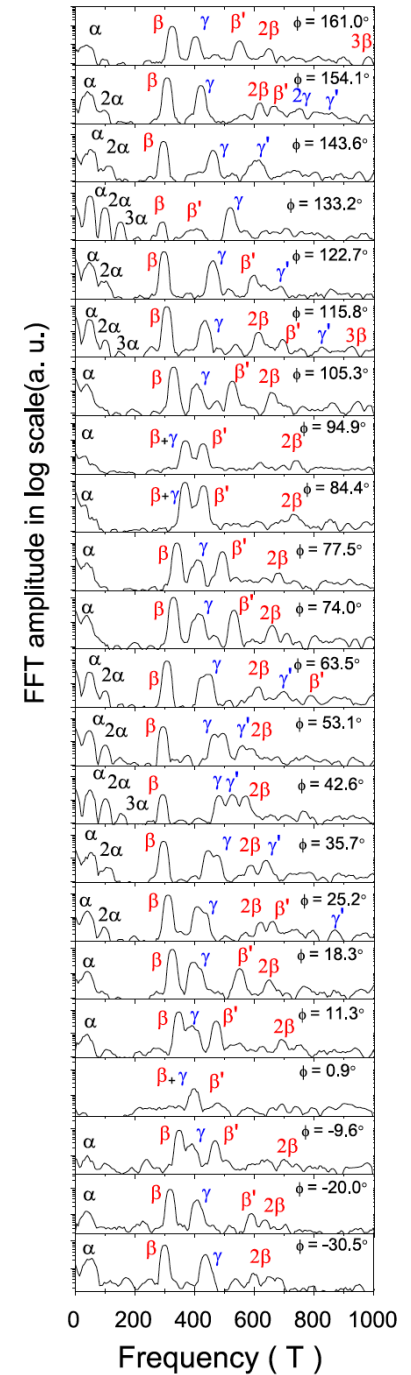
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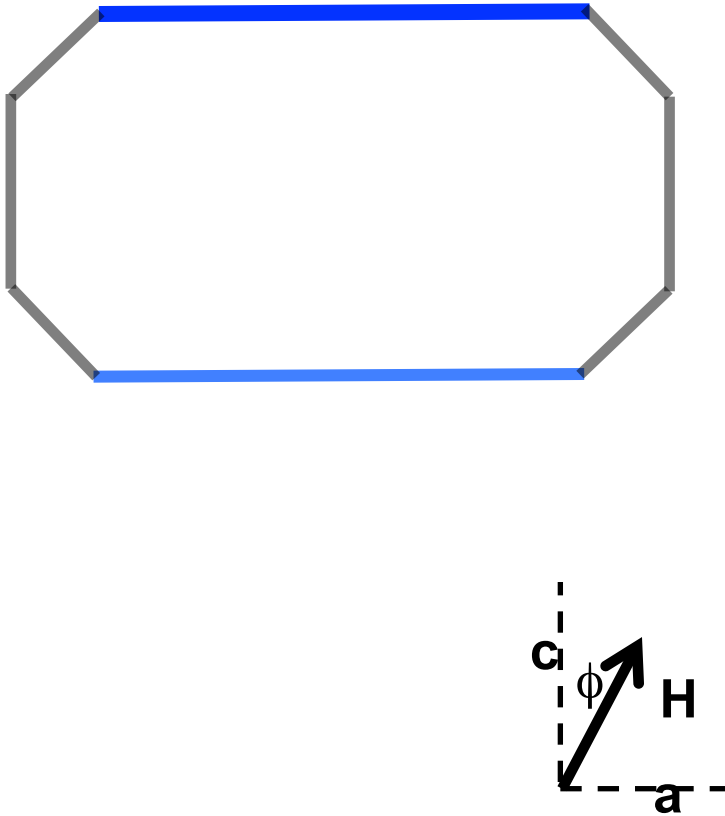
(a) SmB<sub>6</sub> Sample 1



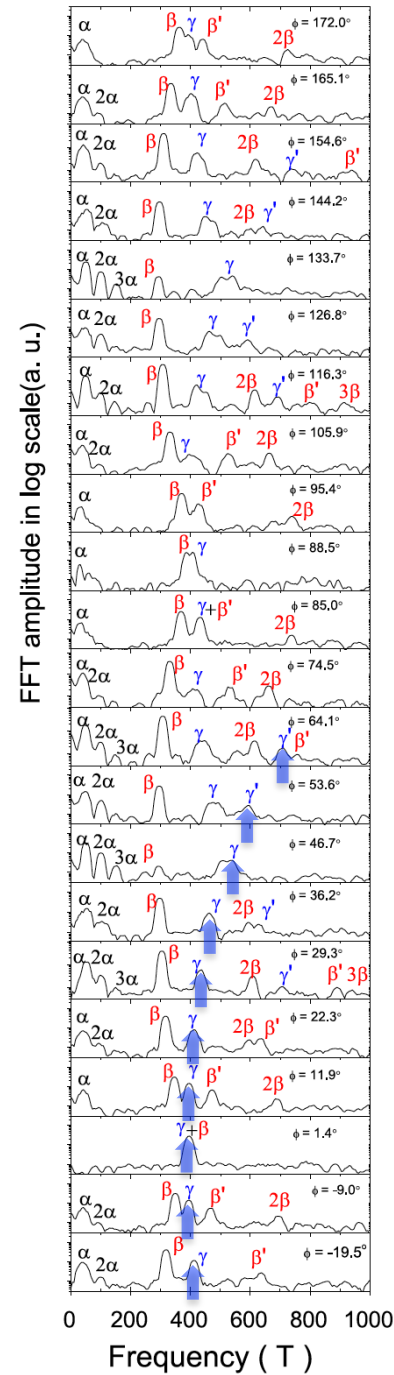
(b) SmB<sub>6</sub> Sample 2



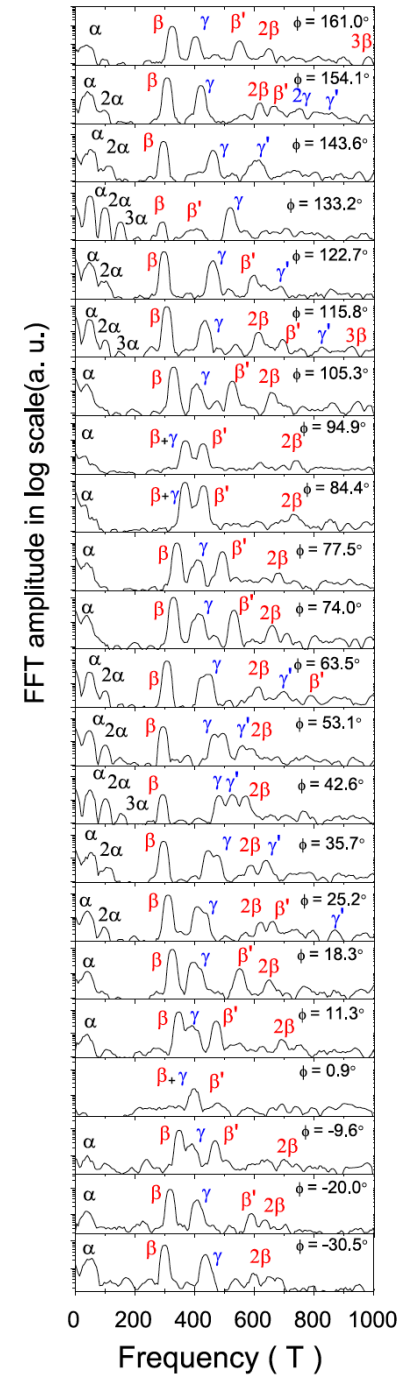
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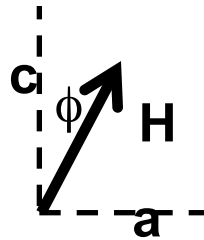
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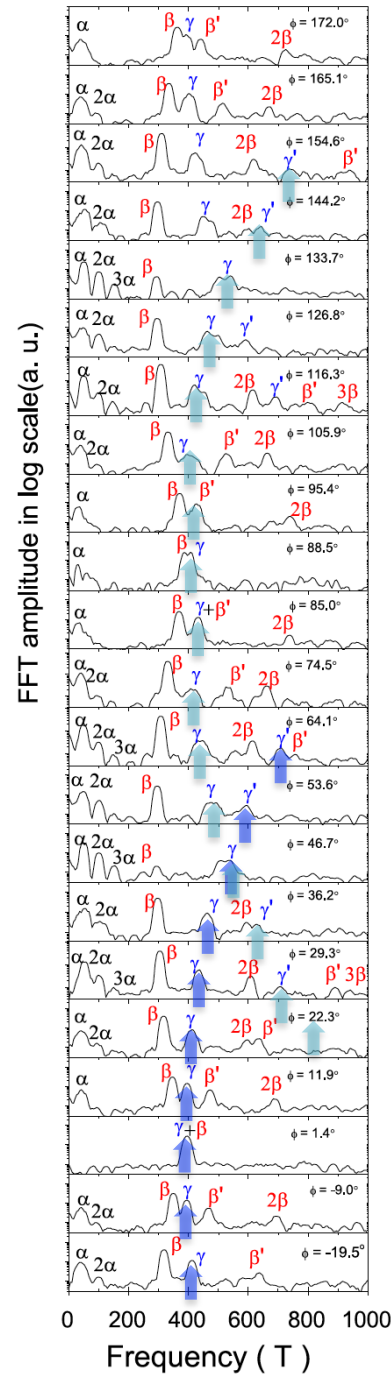
(b) SmB<sub>6</sub> Sample 2



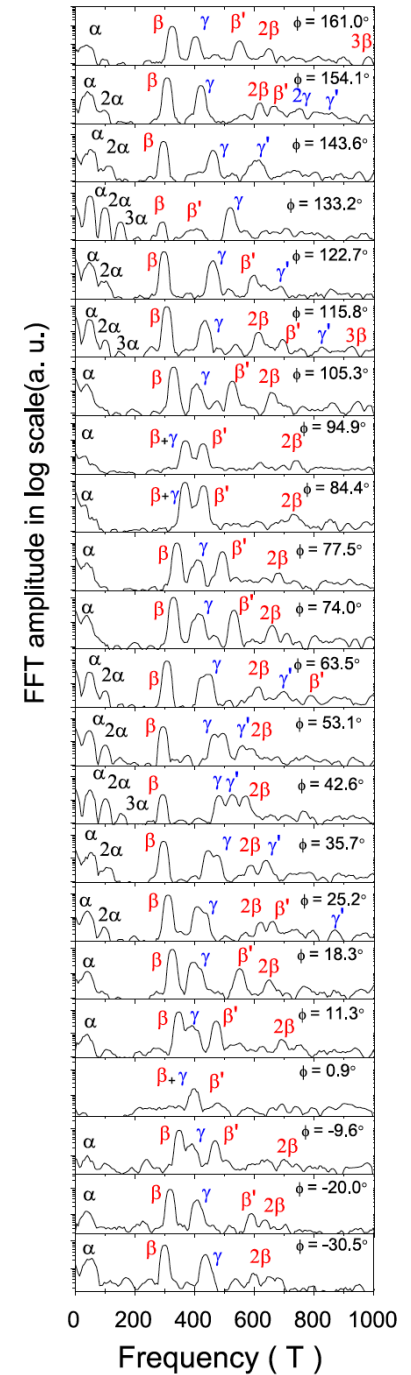
# FFT in logarithmic scale helps track F vs. angle



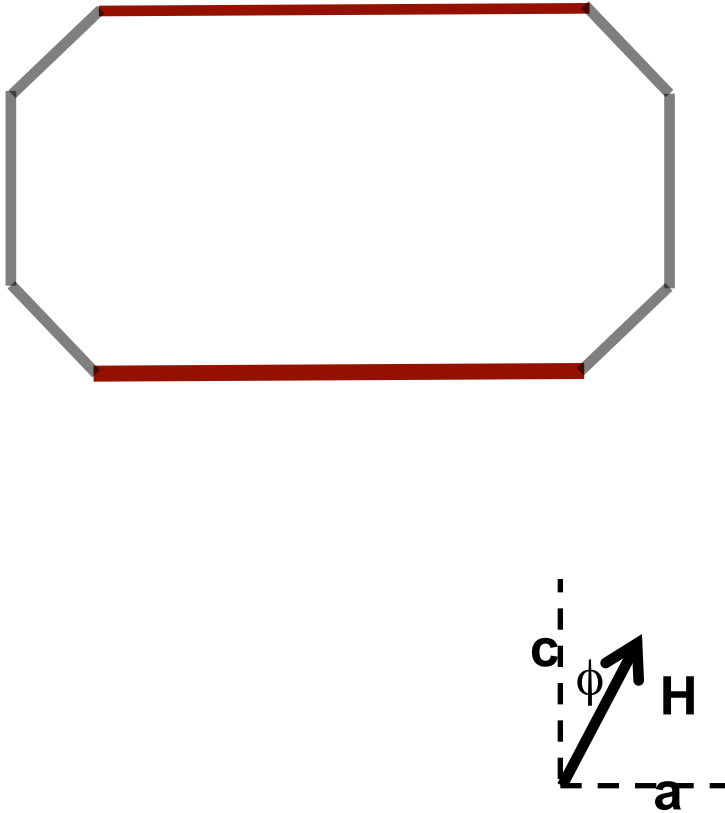
(a) SmB<sub>6</sub> Sample 1



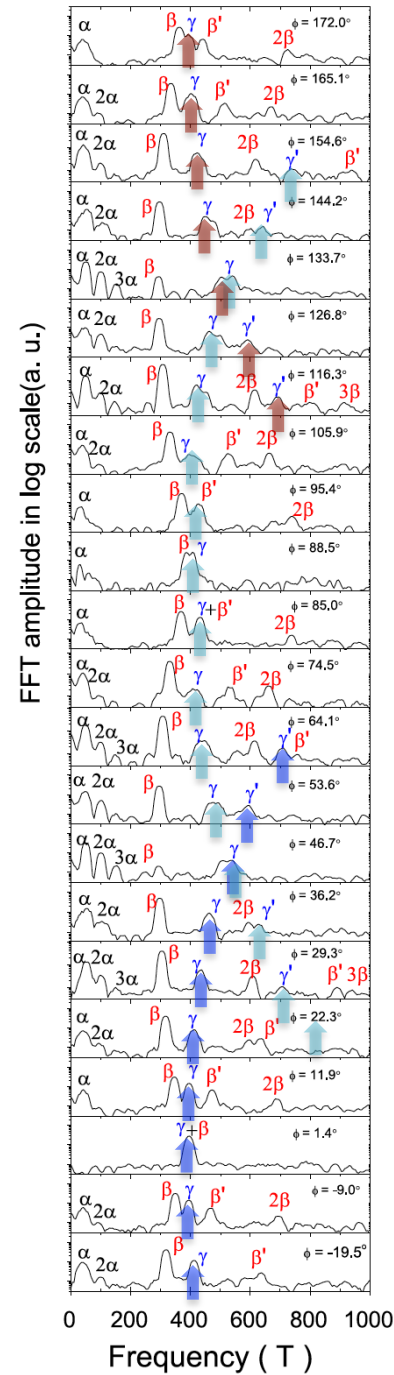
(b) SmB<sub>6</sub> Sample 2



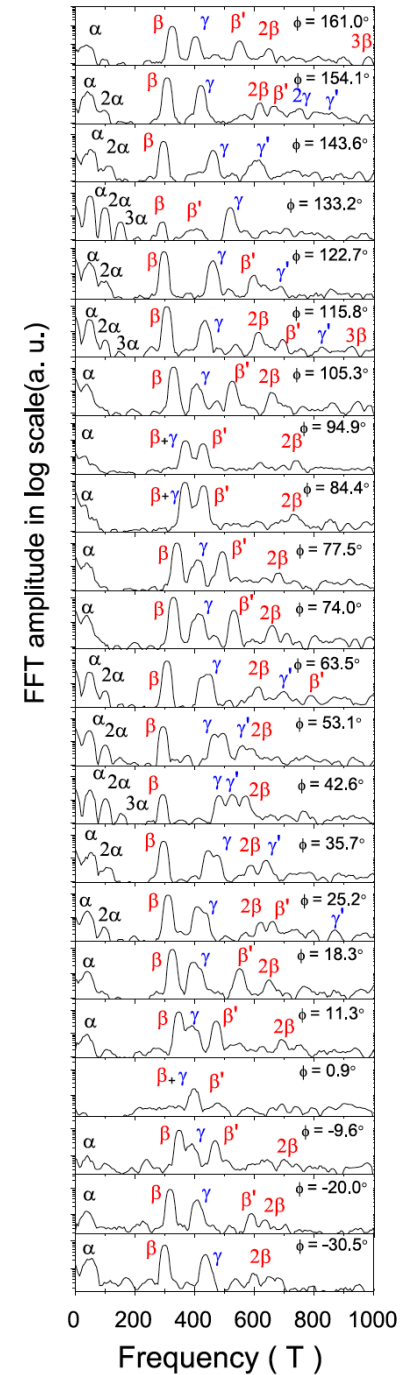
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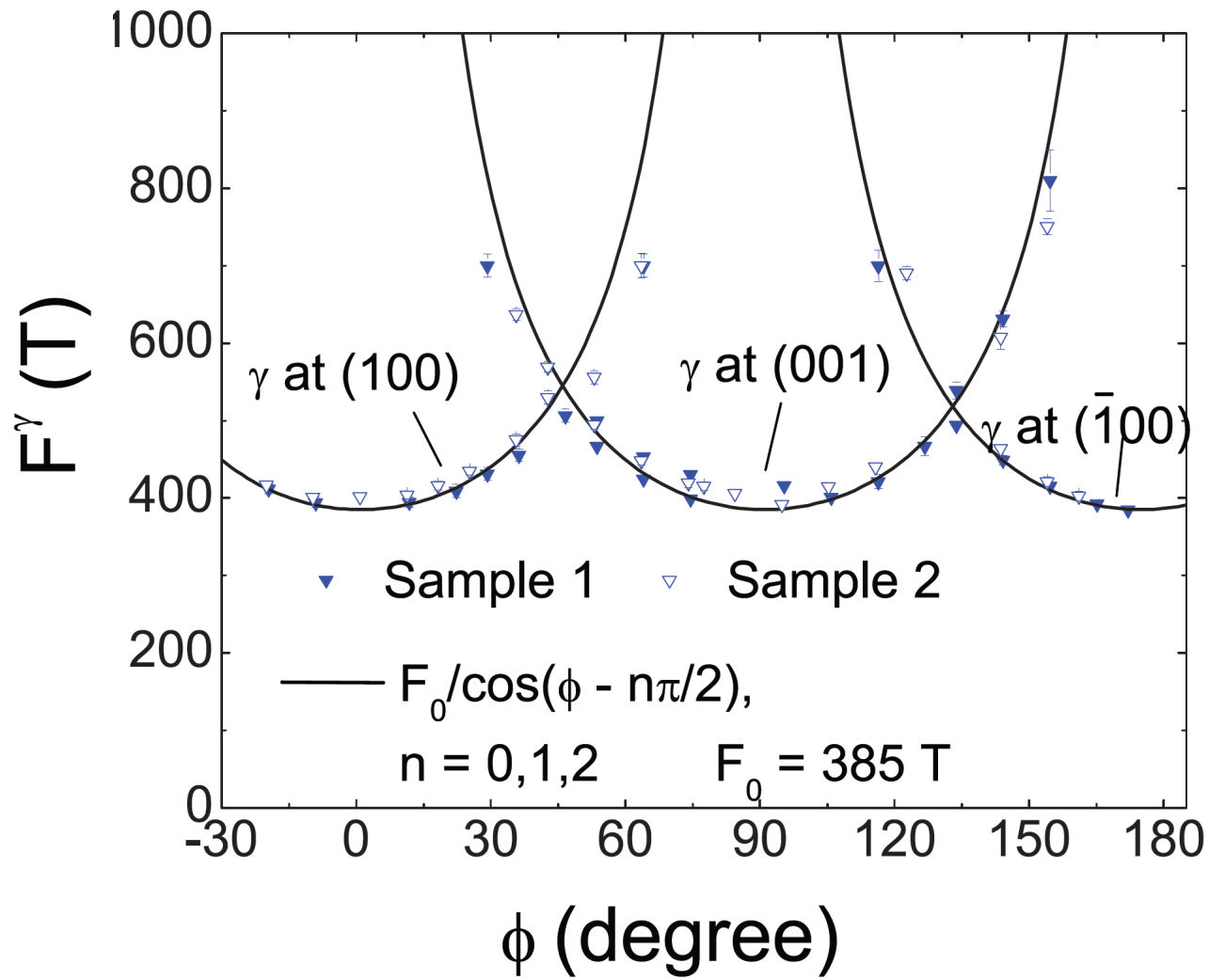
(a) SmB<sub>6</sub> Sample 1



(b) SmB<sub>6</sub> Sample 2

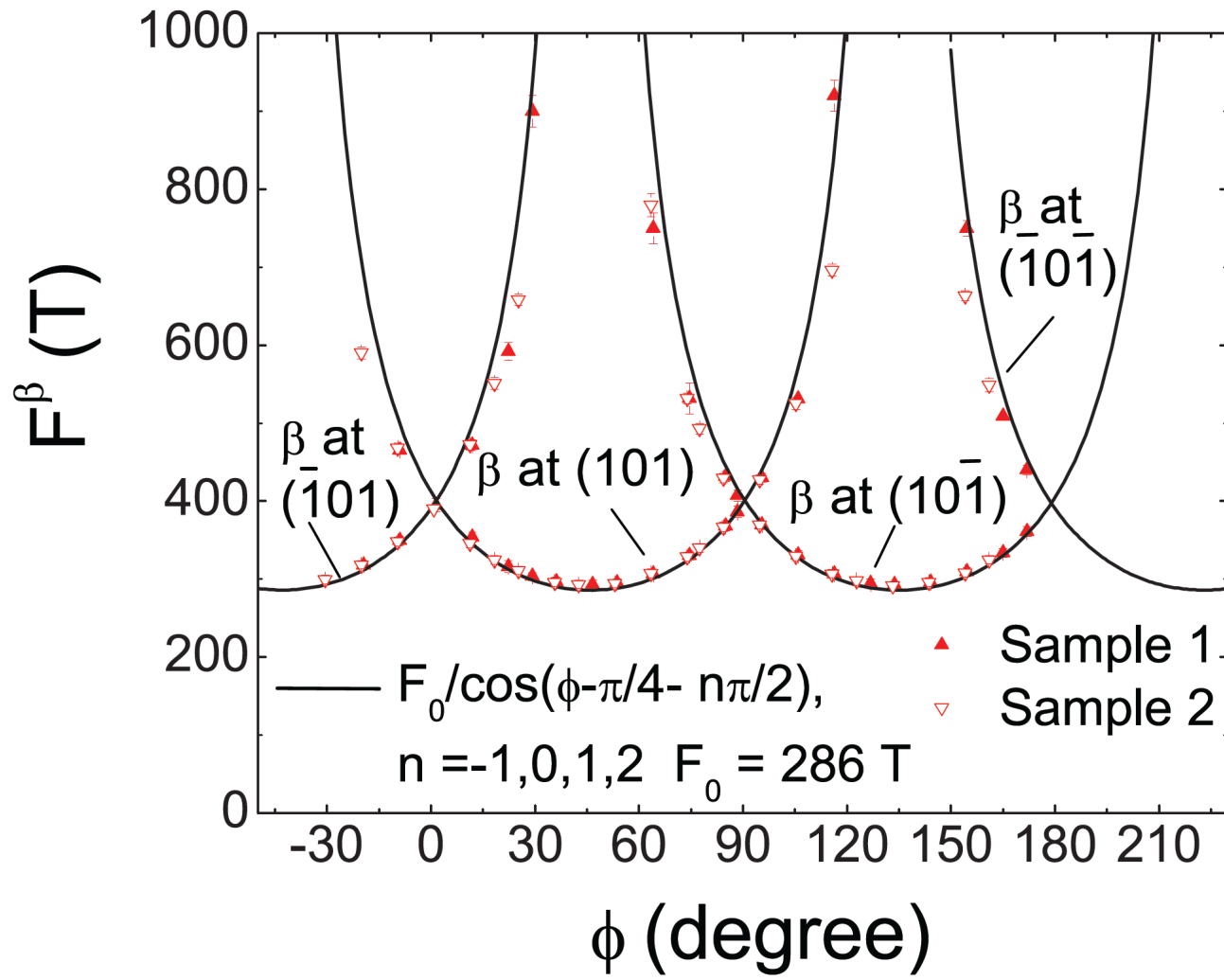


# Two-dimensional $\gamma$ pocket on (100) plane



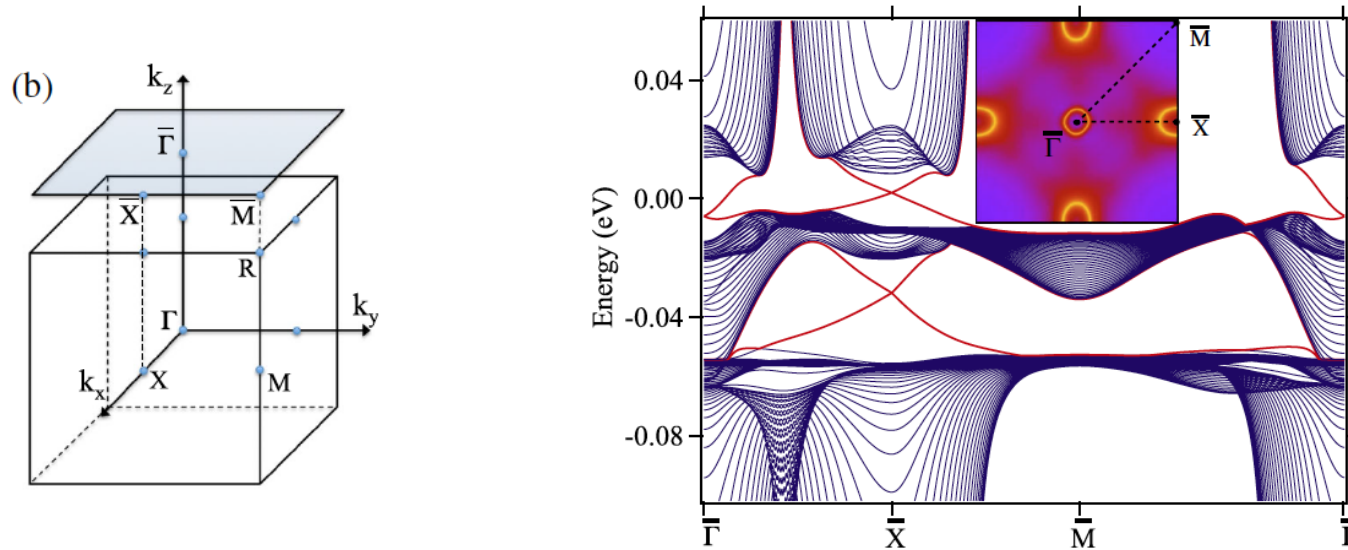
G. Li, et al. Science 2014

# Two-dimensional $\beta$ pocket on (101)



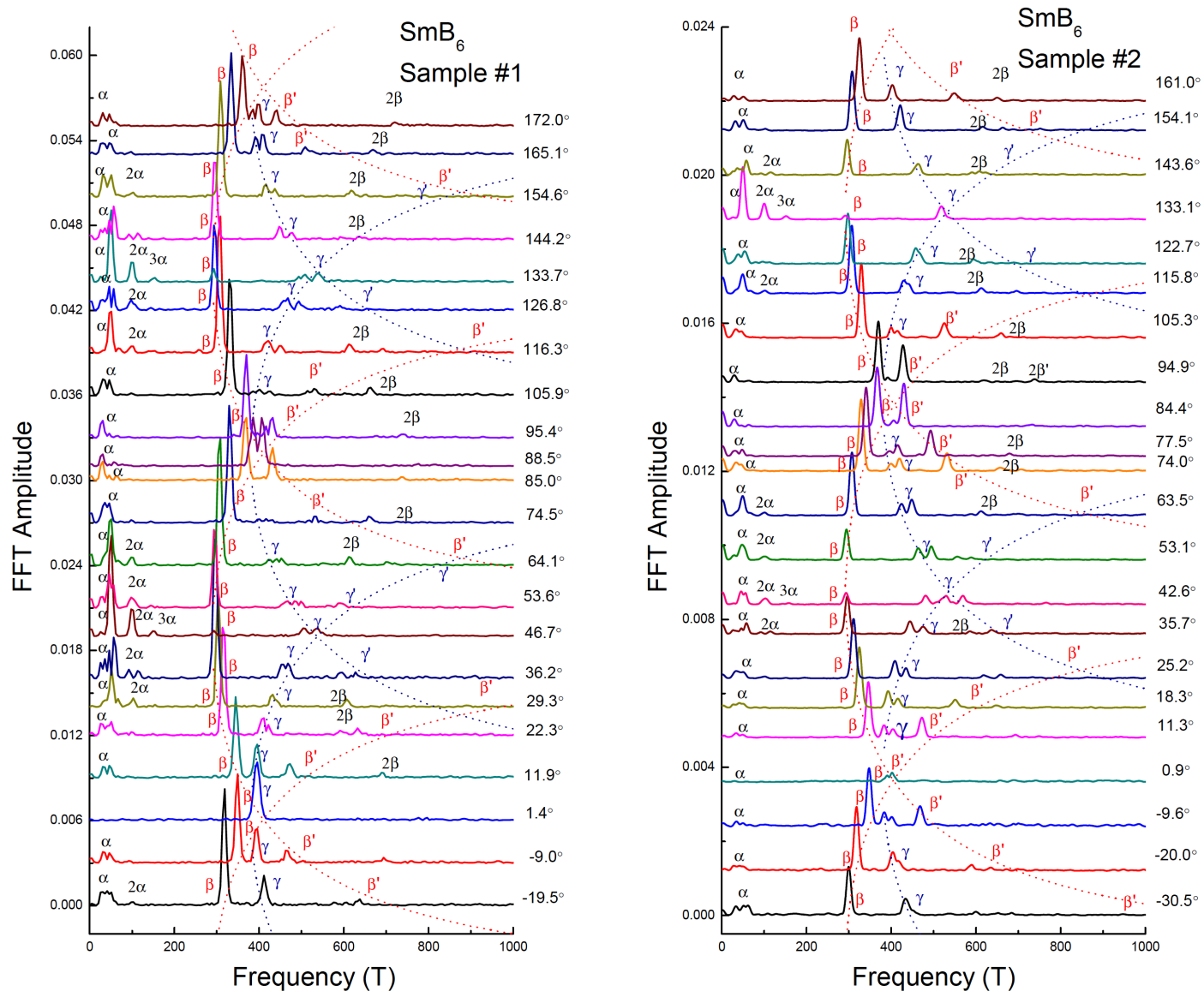
G. Li, et al. Science 2014

# Advanced Calculation shows possible surface state on the 100 cleavage plane



3 Dirac Cones, 2 Fermi Surface Areas

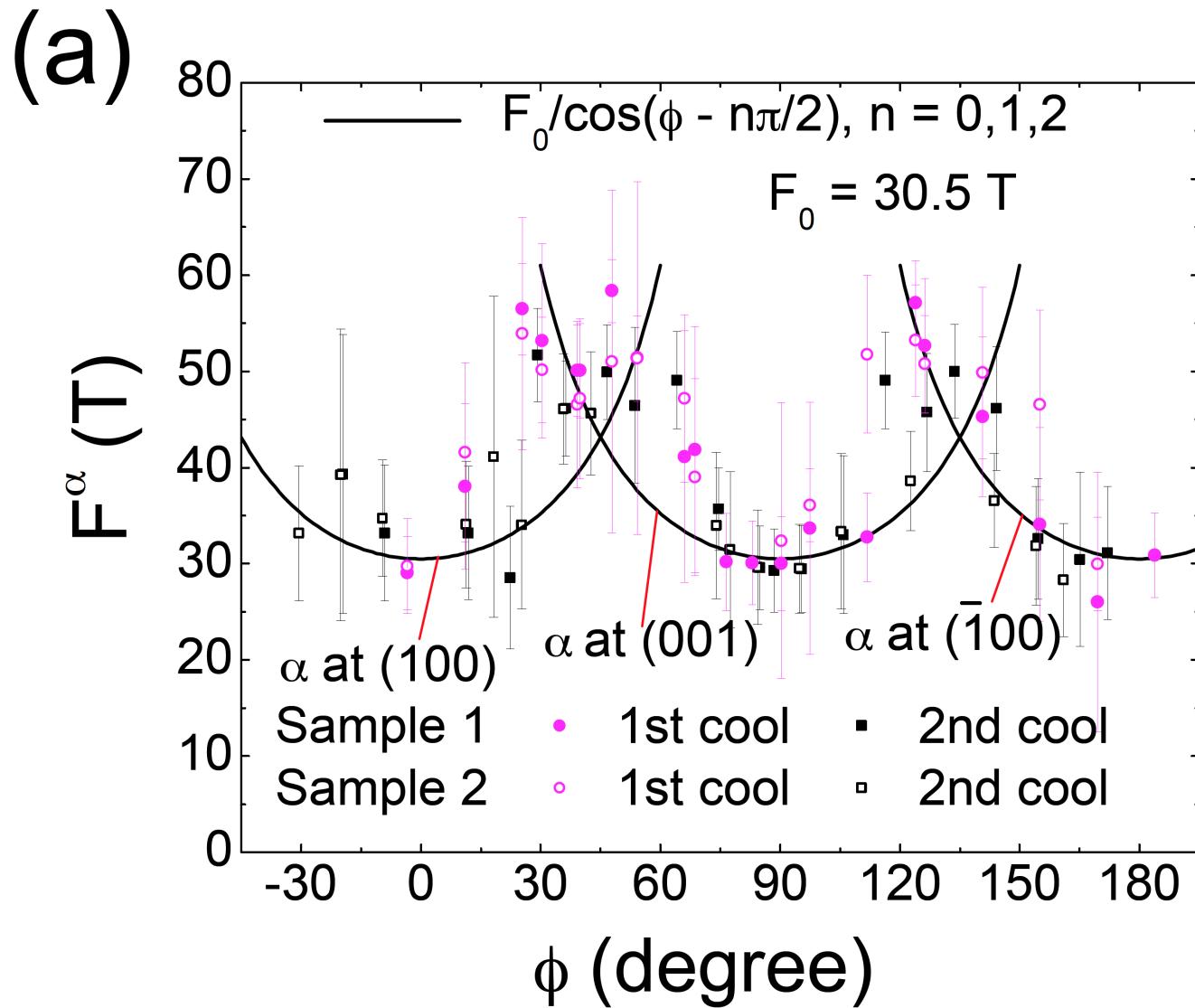
# Track the angular dependence of the frequency



~ 10 degree between each trace

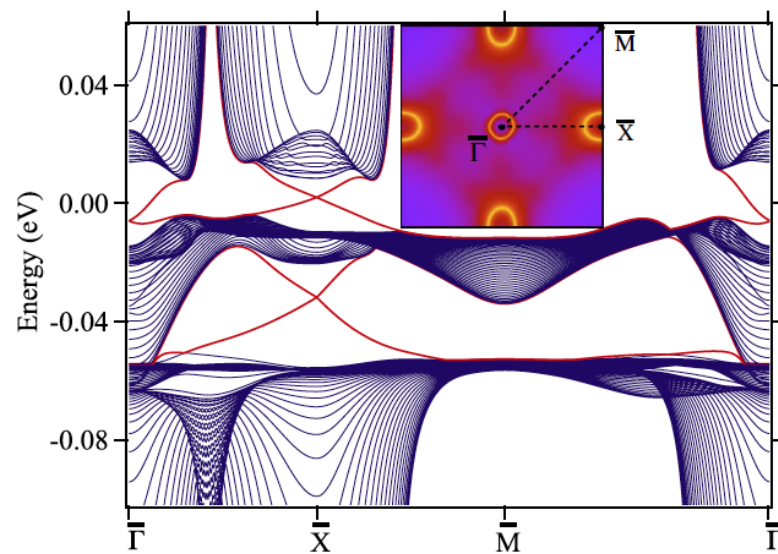
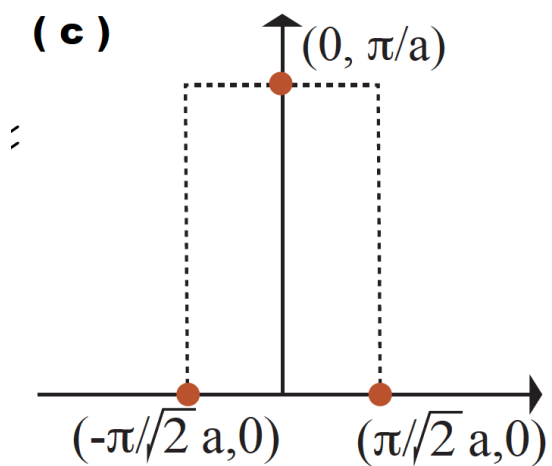
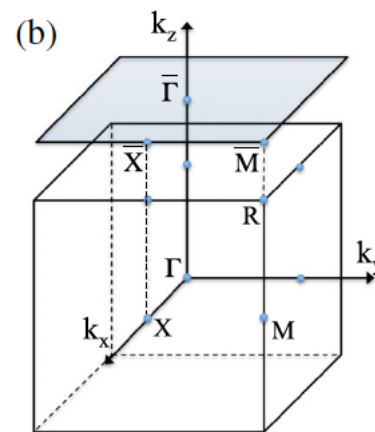
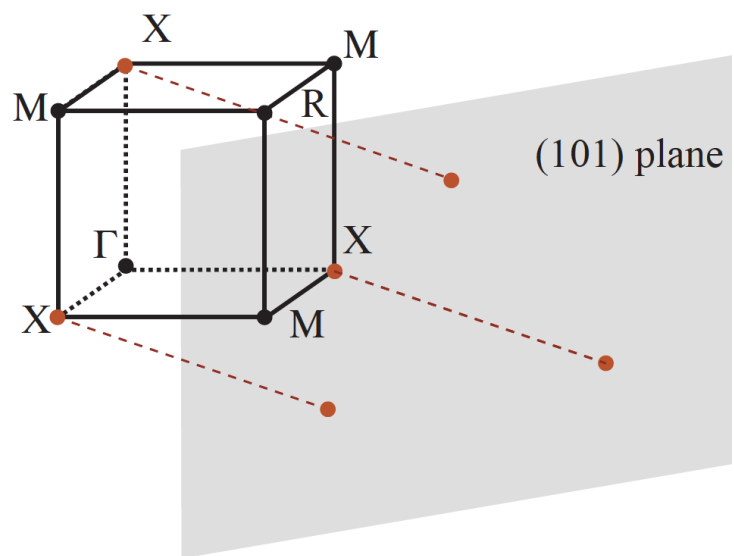


# Two-dimensional $\alpha$ pocket on (100) plane



G. Li, et al. Science 2014

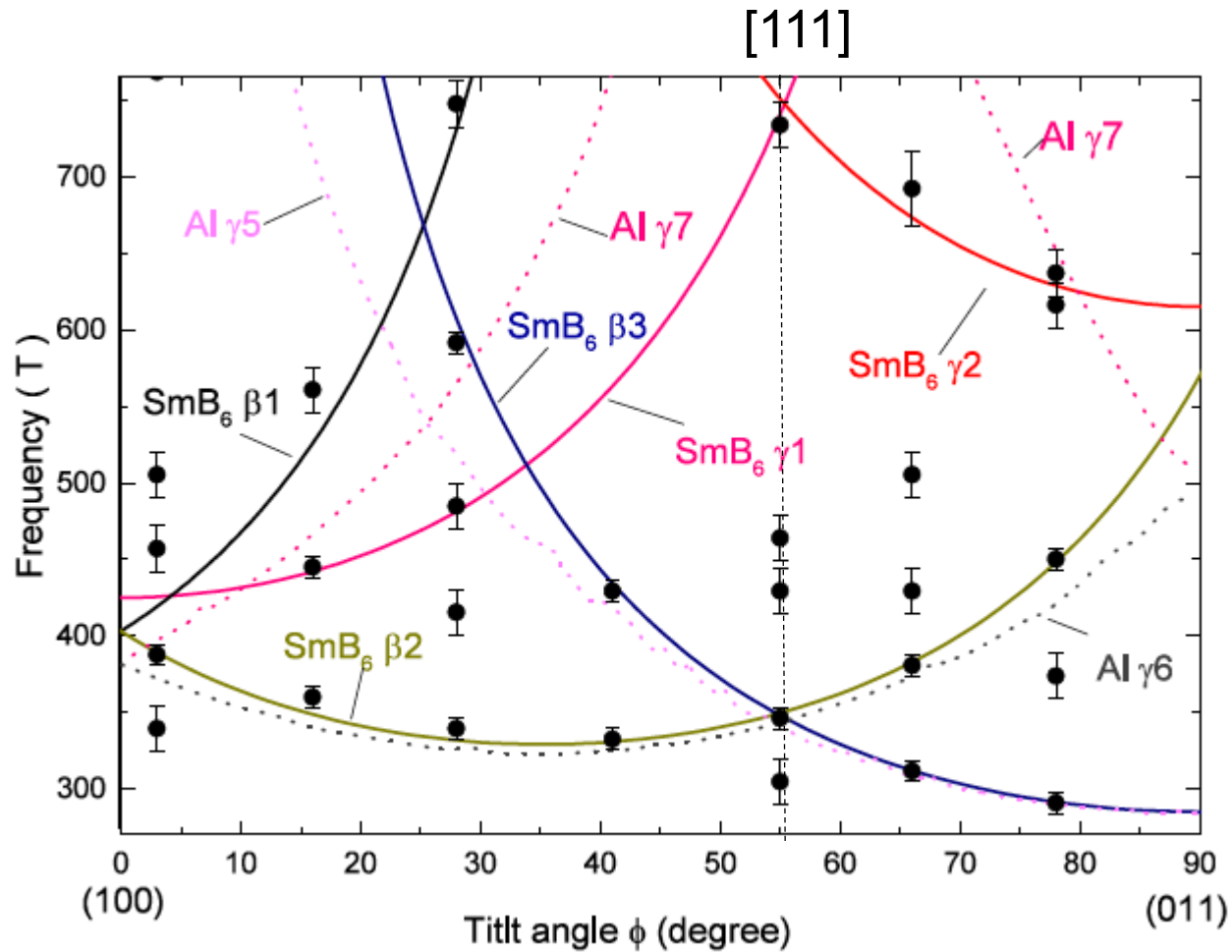
# Surface states



G. Li, et al. *Science* 2014

Lu, et al. *PRL* (2013)

# 2D nature rotating from 100 axis to 011 axis



G. Li, et al. Science 2014

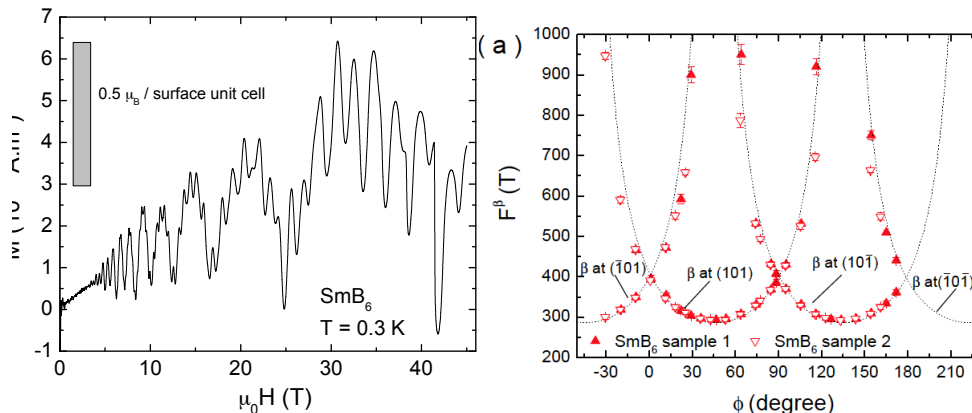
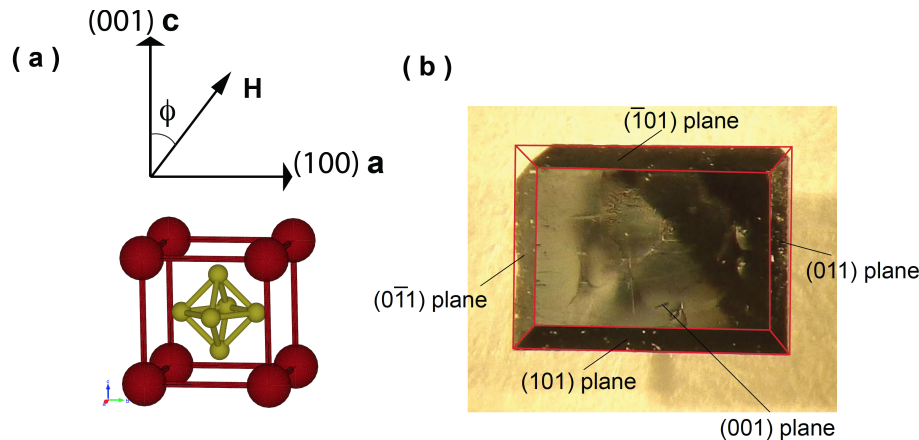
# Topological Kondo insulators $\text{SmB}_6$

1. **WHY?** Kondo Insulator  $\text{SmB}_6$

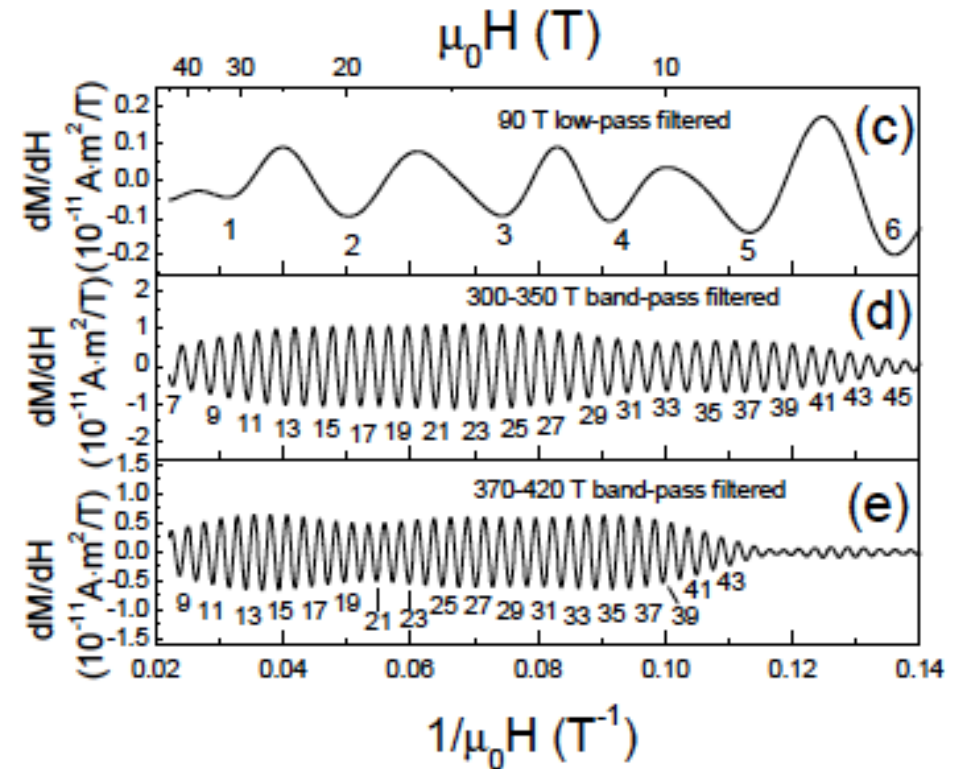
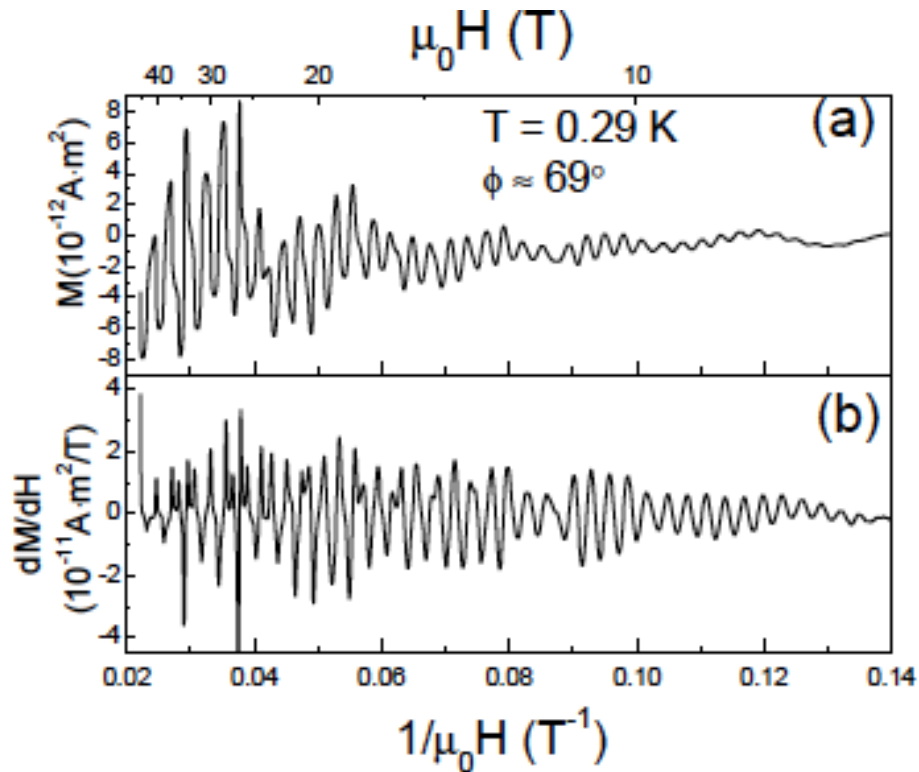
2. **HOW?** Torque magnetometry

3. **Result?**

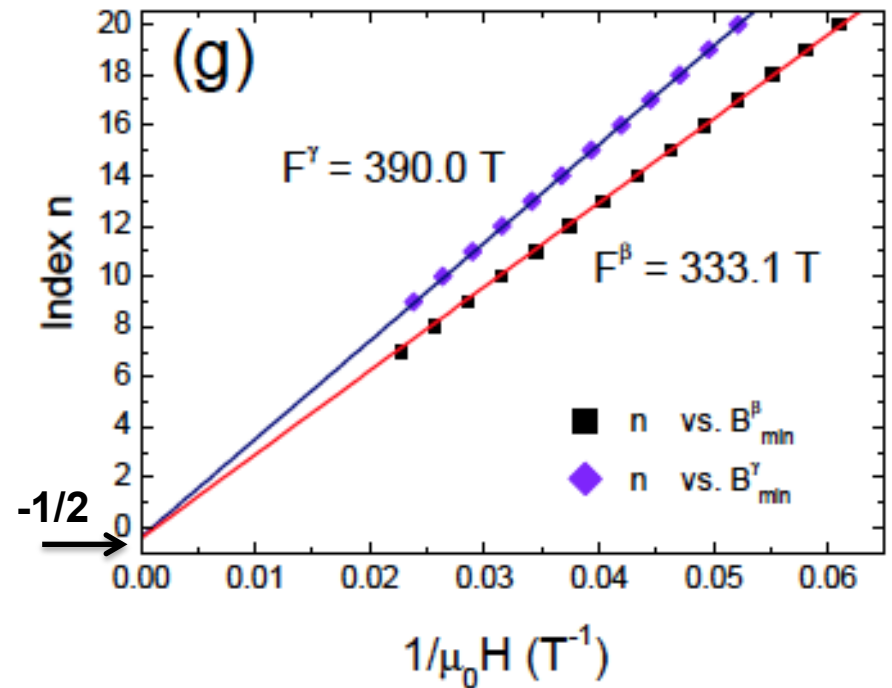
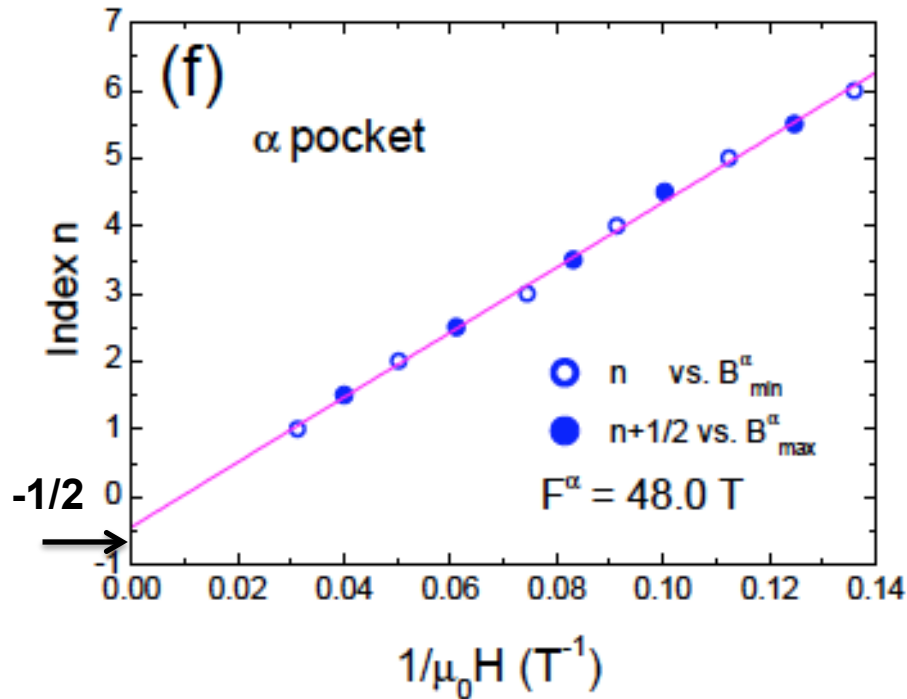
- Quantum oscillations in **M**
- 2 dimensional surface state  
 $F \sim 1 / \cos(\text{angle})$
- Landau Levels index plots  
 $\rightarrow -1/2$  Berry phase factor  
for Dirac dispersion
- Heavy Mass observed in  
Floating-zone samples



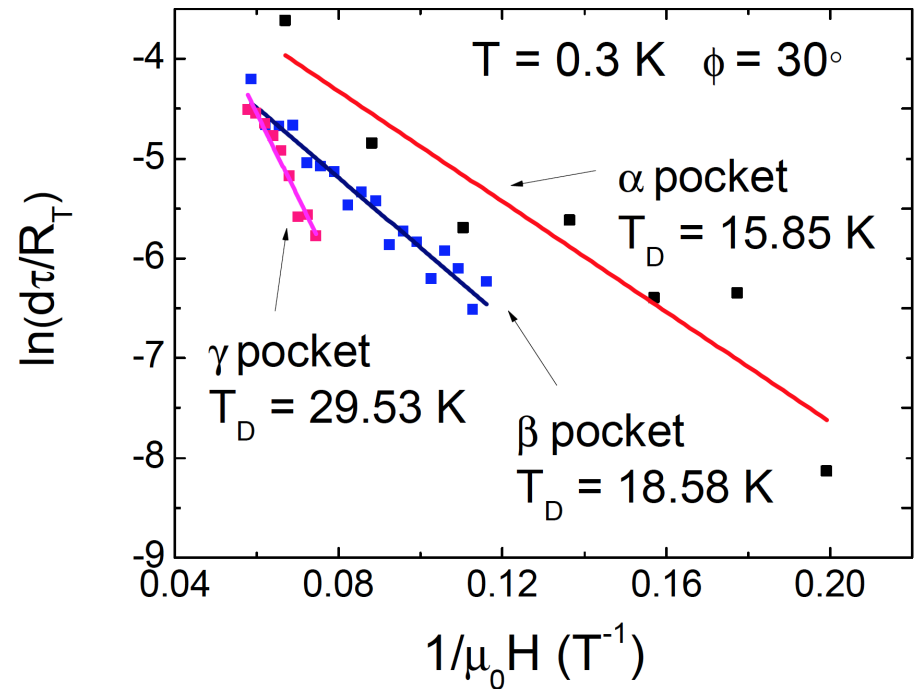
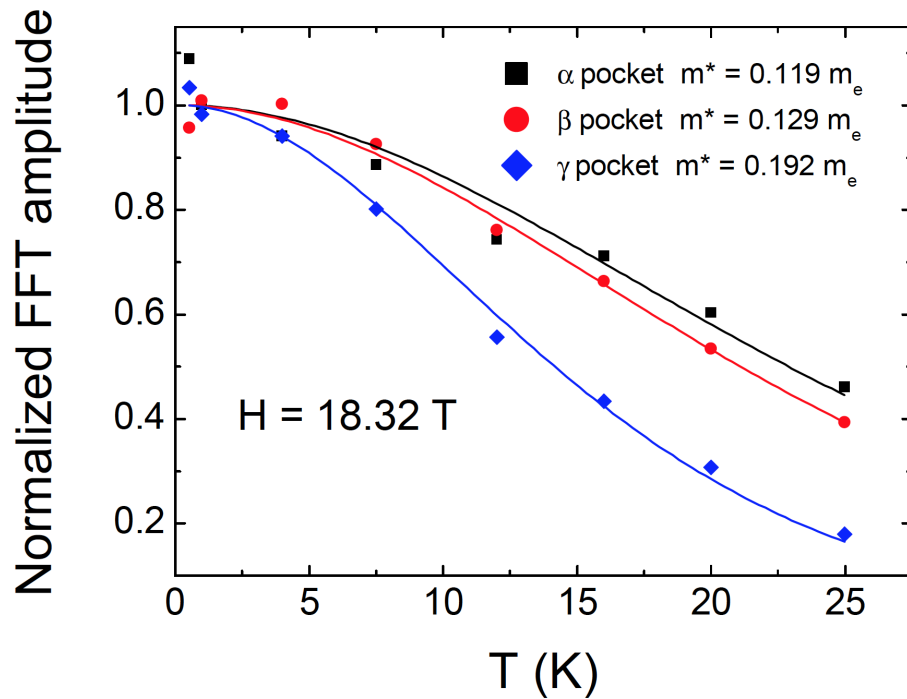
# Resolving Landau Levels



# Index plot $\rightarrow -1/2$ at infinite H limit



# Open question: Light effective mass

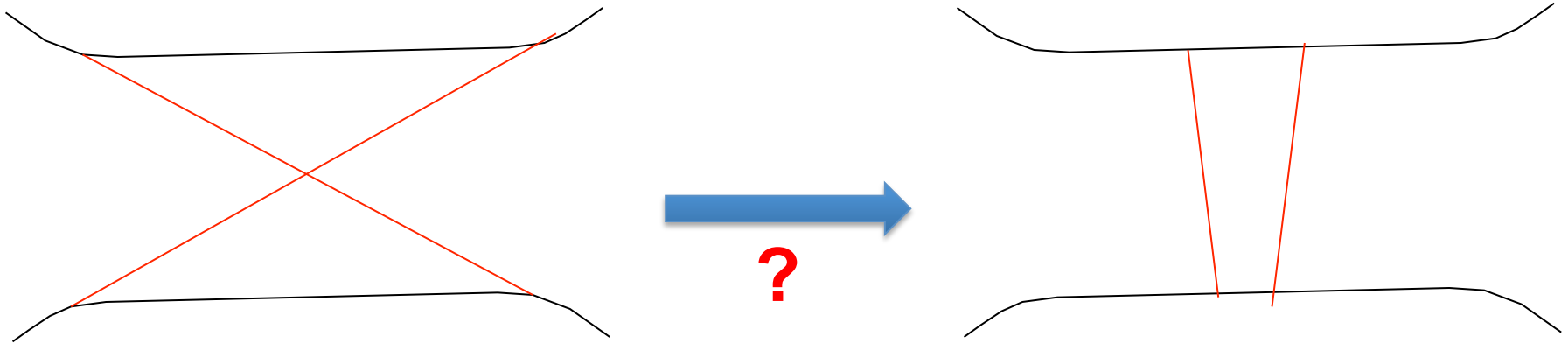


# Open question: Large Fermi Velocity

	$\alpha$	$\beta$	$\gamma$
$F$ ( T )	$29.3 \pm 4$	$292 \pm 5$	$383 \pm 5$
Crystalline Surface Origin	( 1 0 0 )	( 1 0 1 )	( 1 0 0 )
$k_F$ ( nm <sup>-1</sup> )	$0.28 \pm 0.04$	$0.941 \pm 0.008$	$1.08 \pm 0.01$
$\frac{m}{m_e}$	$0.119 \pm 0.007$	$0.129 \pm 0.004$	$0.192 \pm 0.005$
$v_F$ ( 10 <sup>5</sup> m s <sup>-1</sup> )	$2.9 \pm 0.4$	$8.45 \pm 0.33$	$6.50 \pm 0.21$
$l$ ( nm )	$22 \pm 8$	$55 \pm 7$	$27 \pm 4$
$\mu$ ( $\times 10^3$ cm <sup>2</sup> / V s )	$1.2 \pm 0.6$	$0.89 \pm 0.12$	$0.38 \pm 0.06$
$k_F l$	$6.2 \pm 3.1$	$52 \pm 7$	$29 \pm 4$
$\delta$	$-0.45 \pm 0.07$	$-0.44 \pm 0.06$	$-0.32 \pm 0.07$



# Open question: Large Fermi Velocity



Polar surface at 100 ? But non-polar on 101 surface

Interaction driven renormalization?

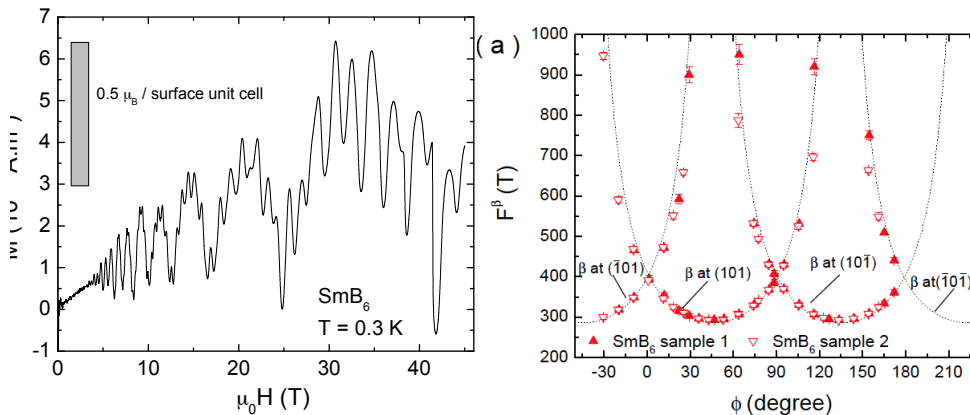
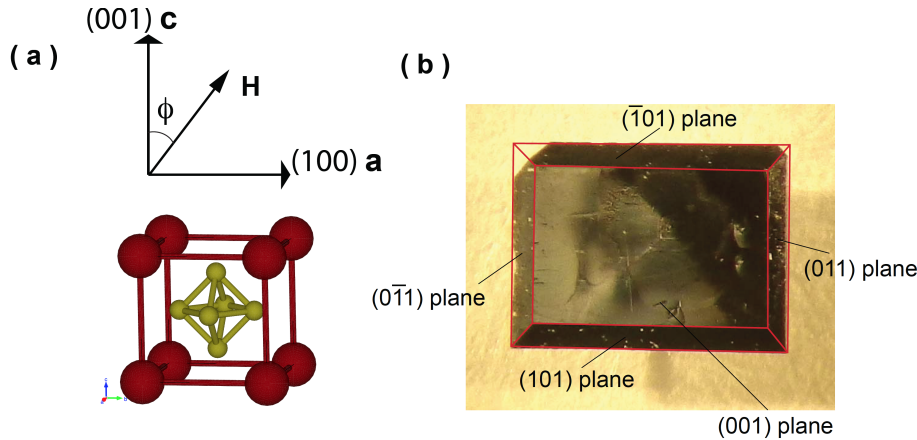
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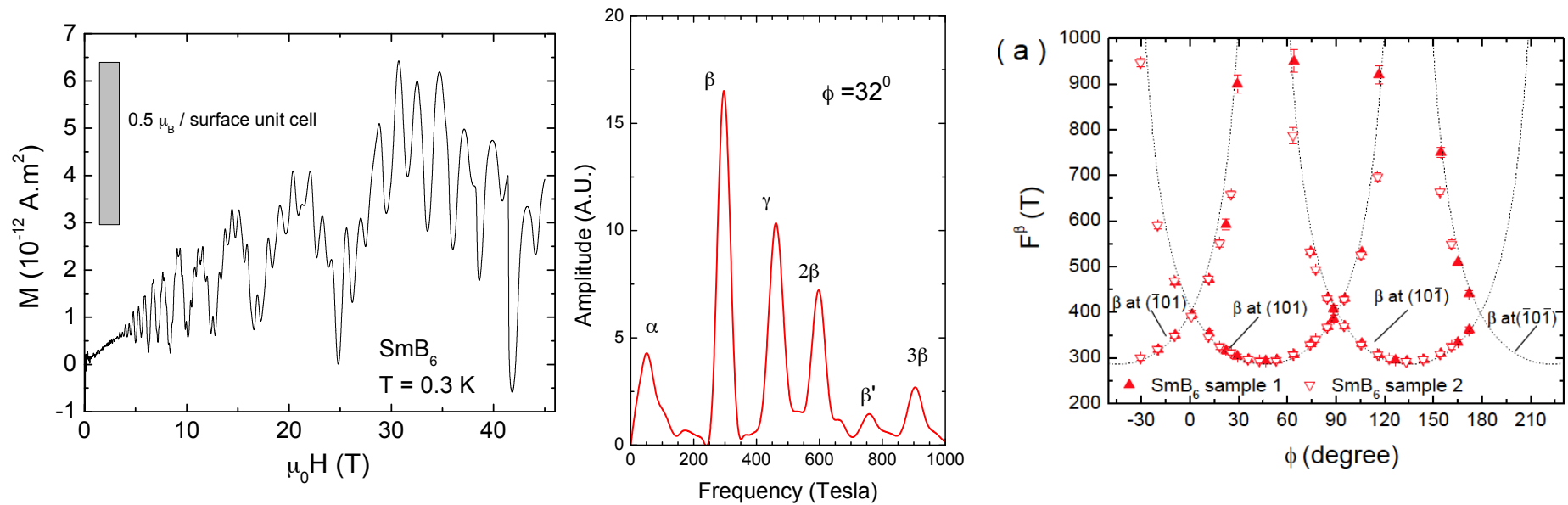
3. **Result?**

- Quantum oscillations in **M**
- 2 dimensional surface state  
 $F \sim 1 / \cos(\text{angle})$
- Landau Levels index plots  $\rightarrow$   
-1/2 Berry phase factor for Dirac dispersion
- **Heavy Mass observed in Floating-zone samples**



# Conclusion

## Surface states resolved at Kondo Insulator $\text{SmB}_6$



- Quantum oscillations in magnetization
- 2D surface state FS areas: 1 on  $(101)$  surface, 2 on  $(100)$  surface