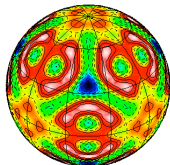


# Iridates

## The New Frontier

Mike Norman

Materials Science Division  
Argonne National Laboratory



KITP, Feb. 12, 2010

Spin Liquids are insulators that have large Curie-Weiss temperatures, but do not order or show spin glass behavior. Particularly relevant are those with  $S=1/2$ .

PHYSICS

## An End to the Drought of Quantum Spin Liquids

Patrick A. Lee

After decades of searching, several promising examples of a new quantum state of matter have now emerged.

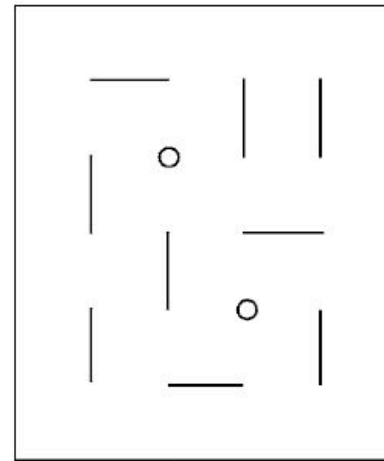
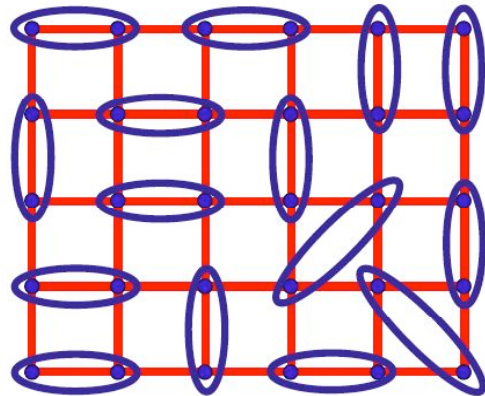
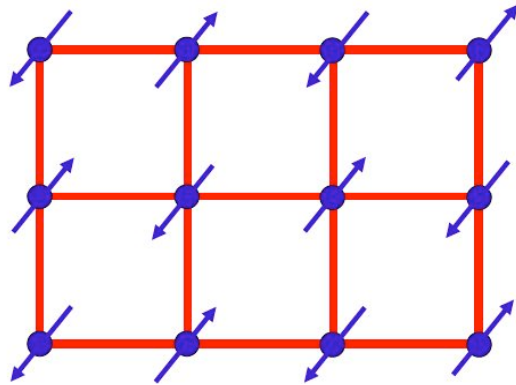


Science 321, 1306 (2008)

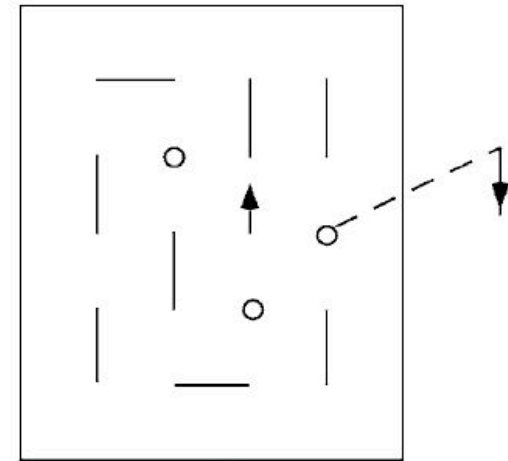
- $\kappa$ -(BEDT-TTF)<sub>2</sub>Cu<sub>2</sub>(CN)<sub>3</sub> (triangular)
- ZnCu<sub>3</sub>(OH)<sub>6</sub>Cl<sub>2</sub> (kagome)
- Na<sub>4</sub>Ir<sub>3</sub>O<sub>8</sub> (hyper-kagome)

(See also article in Physics Today by Barbara Goss Levi, page 16, February 2007)

## RVB - a liquid of spin singlets



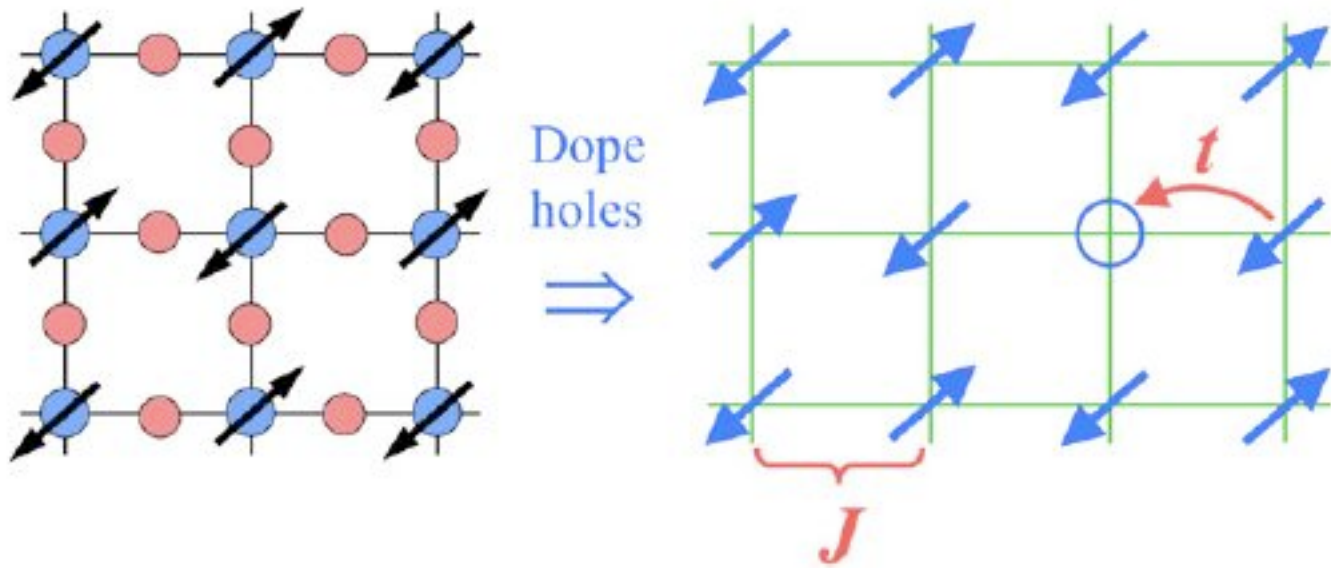
(a)



(b)

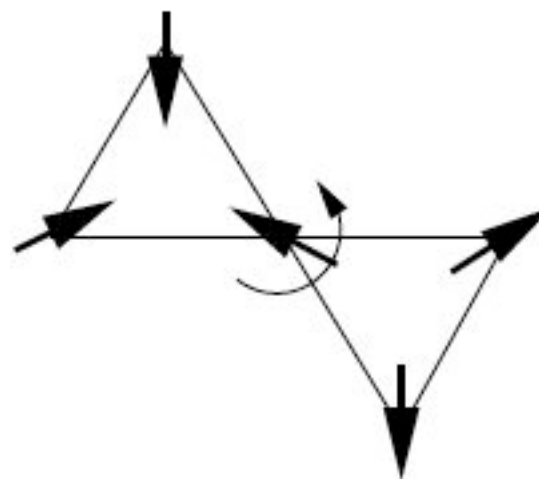
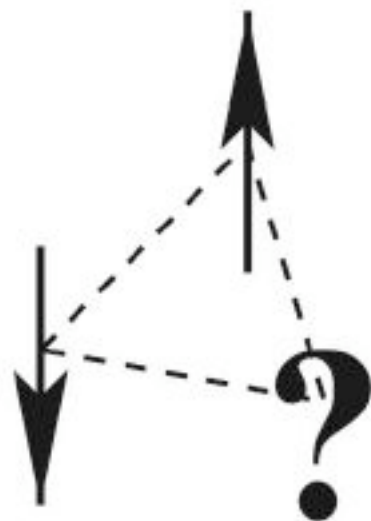
In the uniform RVB state, the  $S=1/2$  excitations (spinons) possess a zero energy Fermi surface (Anderson, 1987)

## Square Lattice (Anderson, 1987)



$J \mathbf{S} \cdot \mathbf{S}$  where  $J = 2 t^2/U$   
for  $S=1/2$   
Neel -  $J/4$  per bond -  $S_z S_z$   
Singlet -  $3J/4$  per bond -  $S(S+1)$

## Frustration on the Triangular Lattice (Anderson, 1973)



$$\chi^{-1} = \mathbf{T} - \Theta_{\text{CW}}$$

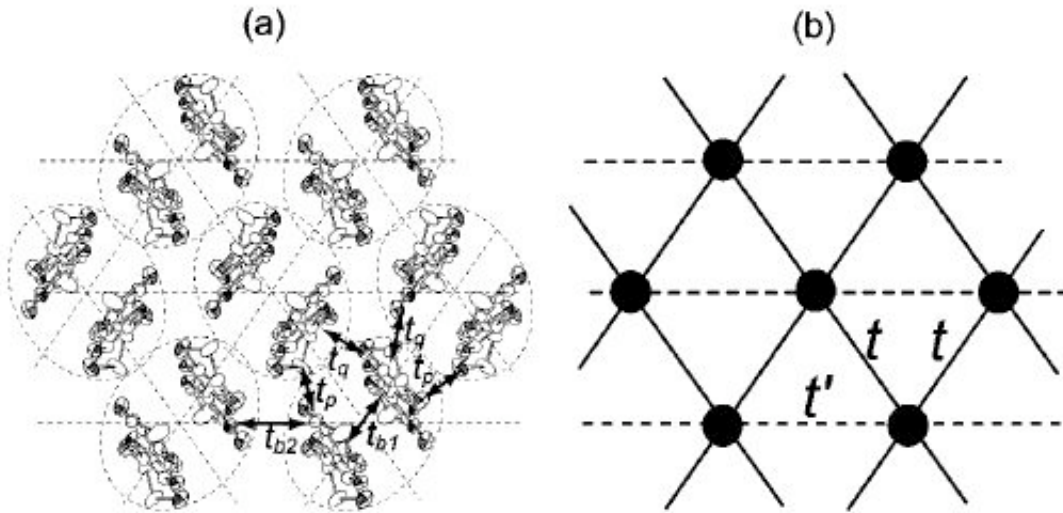
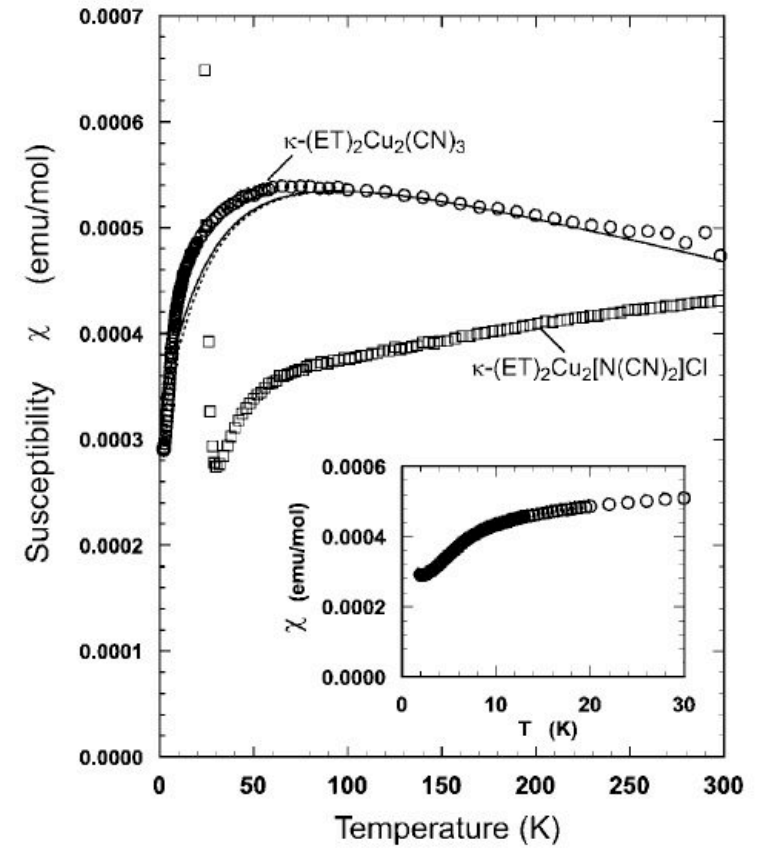
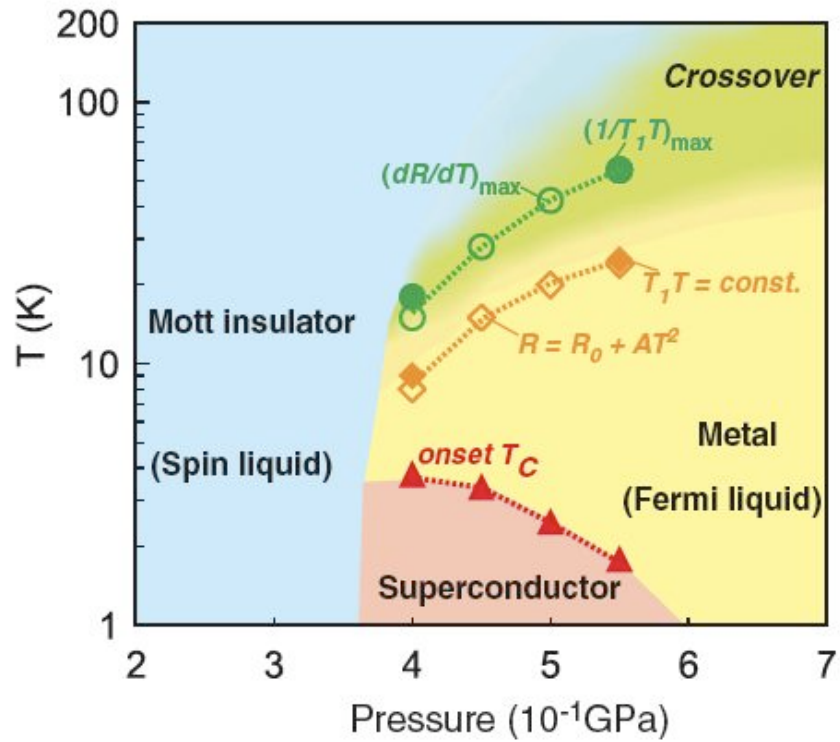


FIG. 1. (a) Crystal structure of an ET layer of  $\kappa\text{-(ET)}_2\text{Cu}_2(\text{CN})_3$  viewed along the long axes of ET molecules

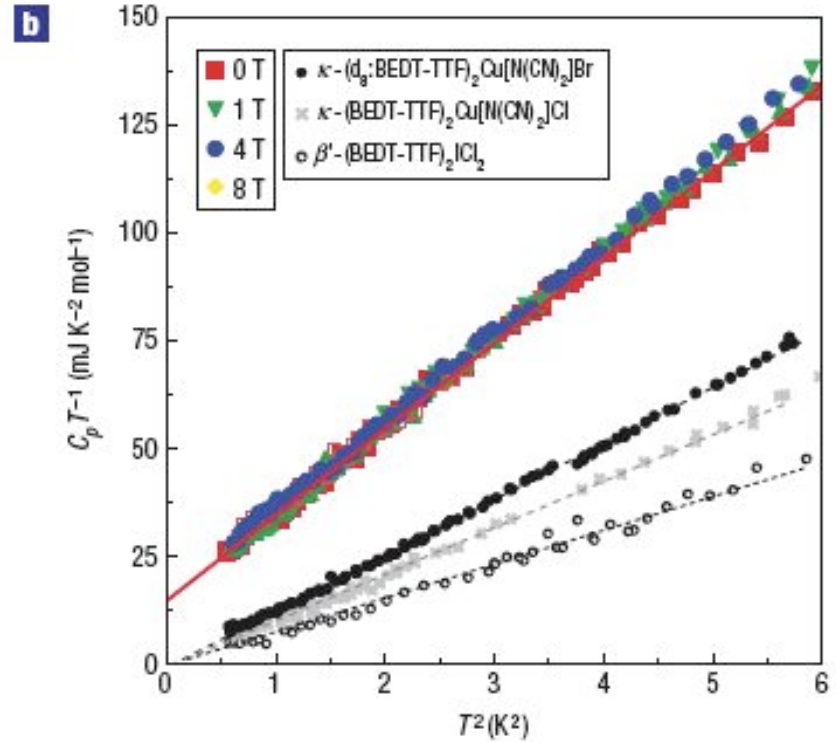
Geiser *et al.*, Inorg. Chem. 30, 2586 (1991)



Shimizu *et al.*, PRL 91, 107001 (2003)

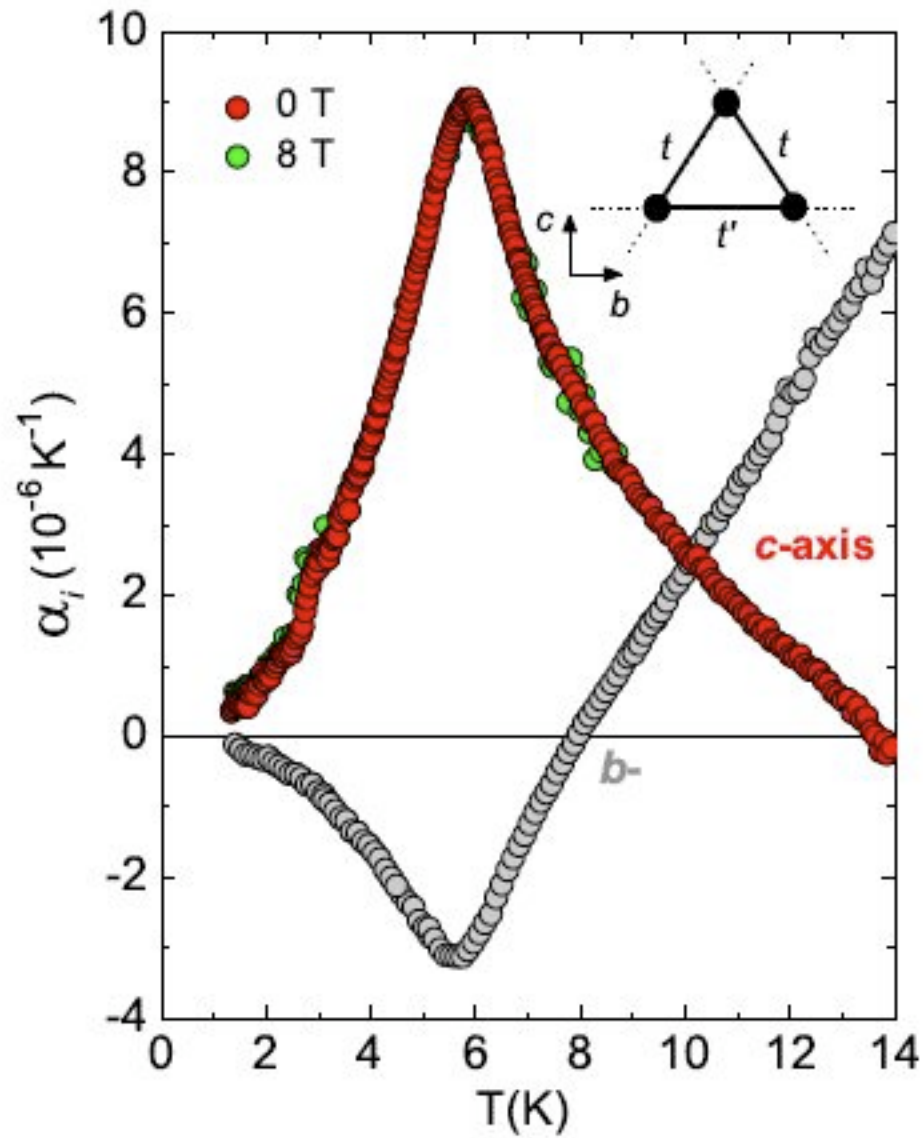


Kurosaki *et al.*, PRL 95, 177001 (2005)



Yamashita *et al.*, Nat. Phys. 4, 459 (2008)

## Ordering at 6 K?





# The Universe is a String-Net Liquid



Herbertsmithite

Zeeya Merali, New Scientist (15 March 2007)

# Herbertsmithite $\text{ZnCu}_3(\text{OH})_6\text{Cl}_2$

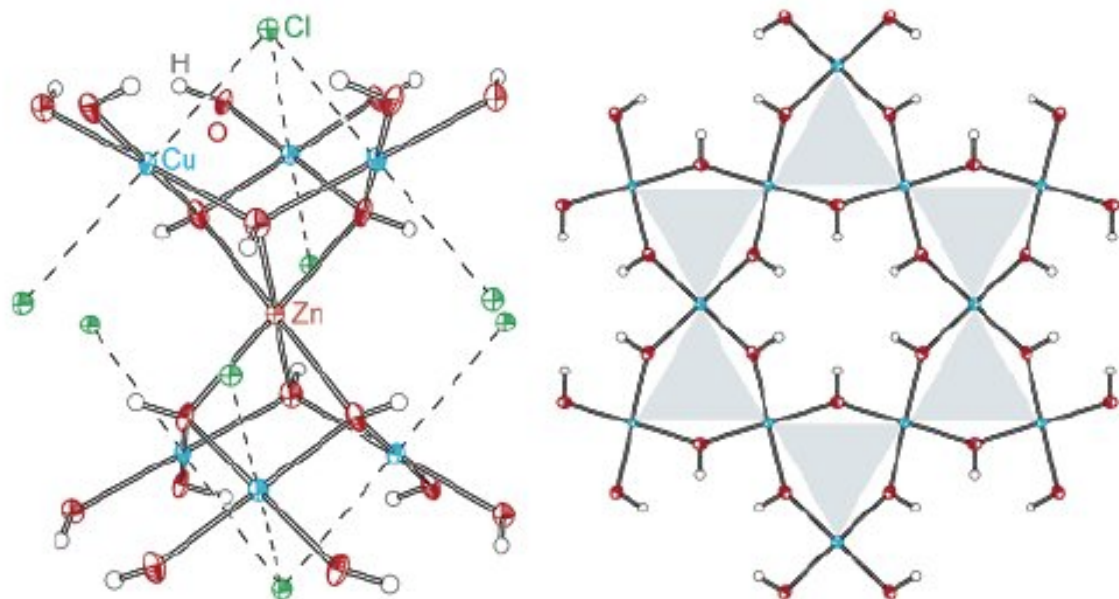
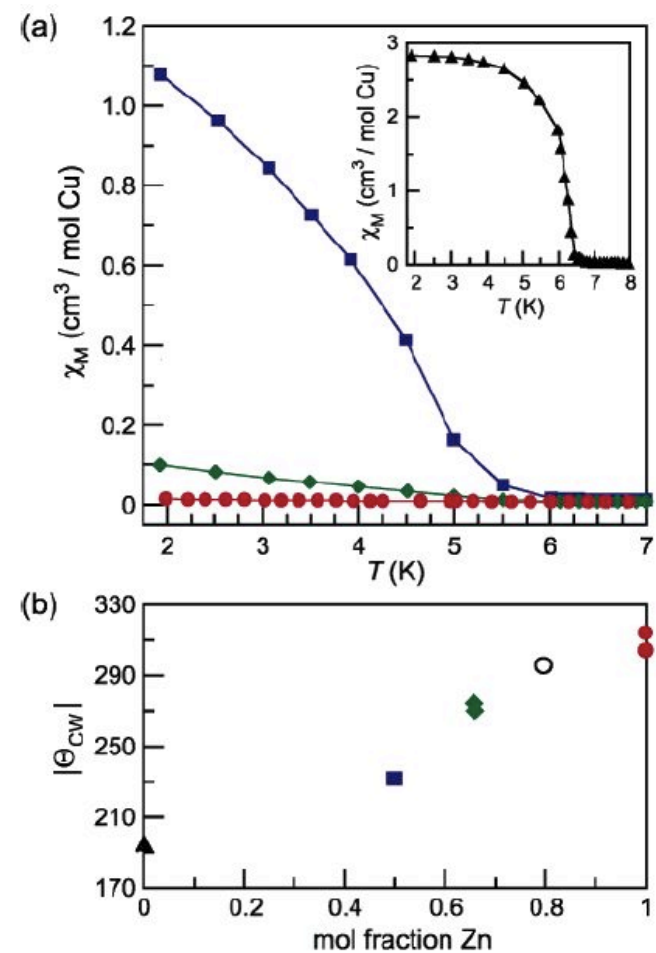
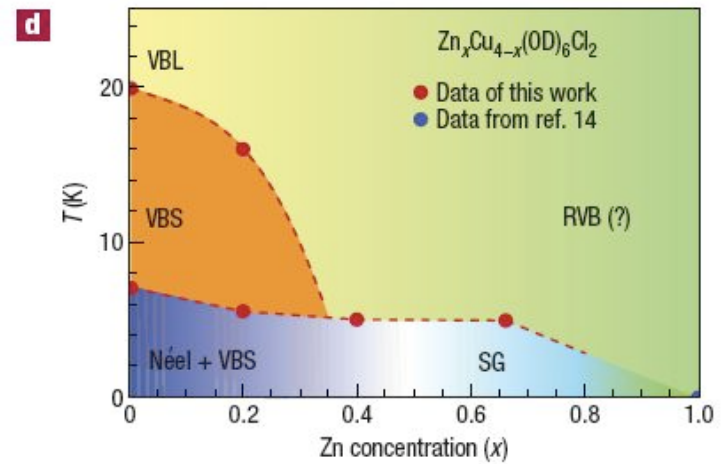
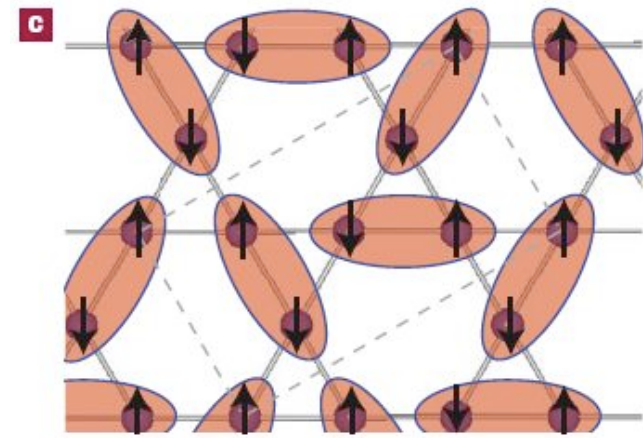
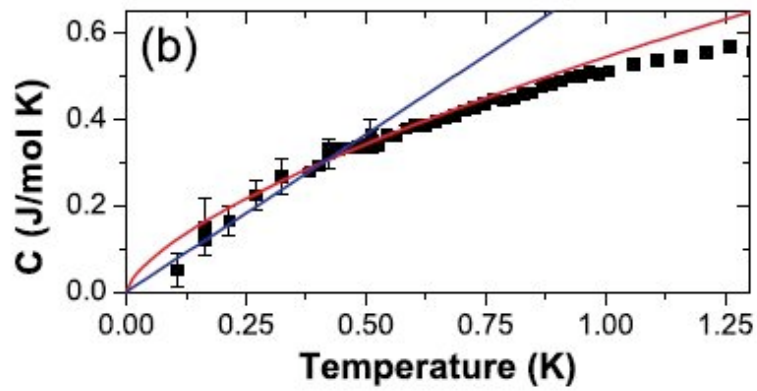
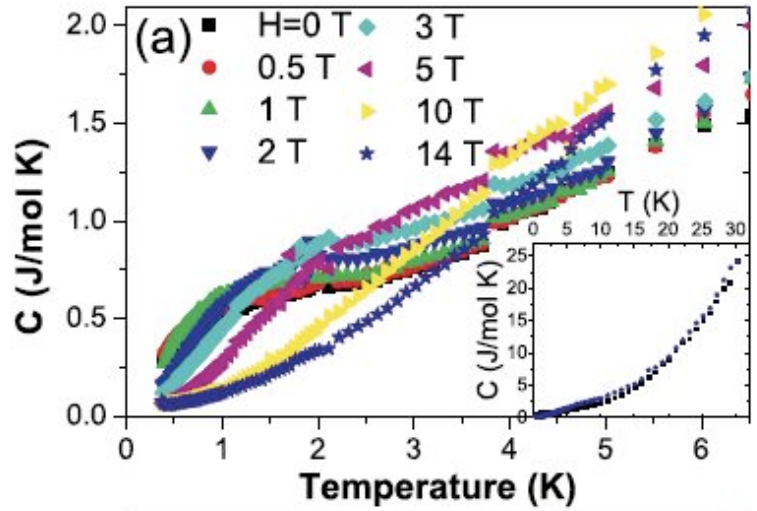


Figure 1. Crystal structure of Zn-paratacamite (I),  $\text{Zn}_{0.33}\text{Cu}_{3.67}(\text{OH})_6\text{Cl}_2$ .



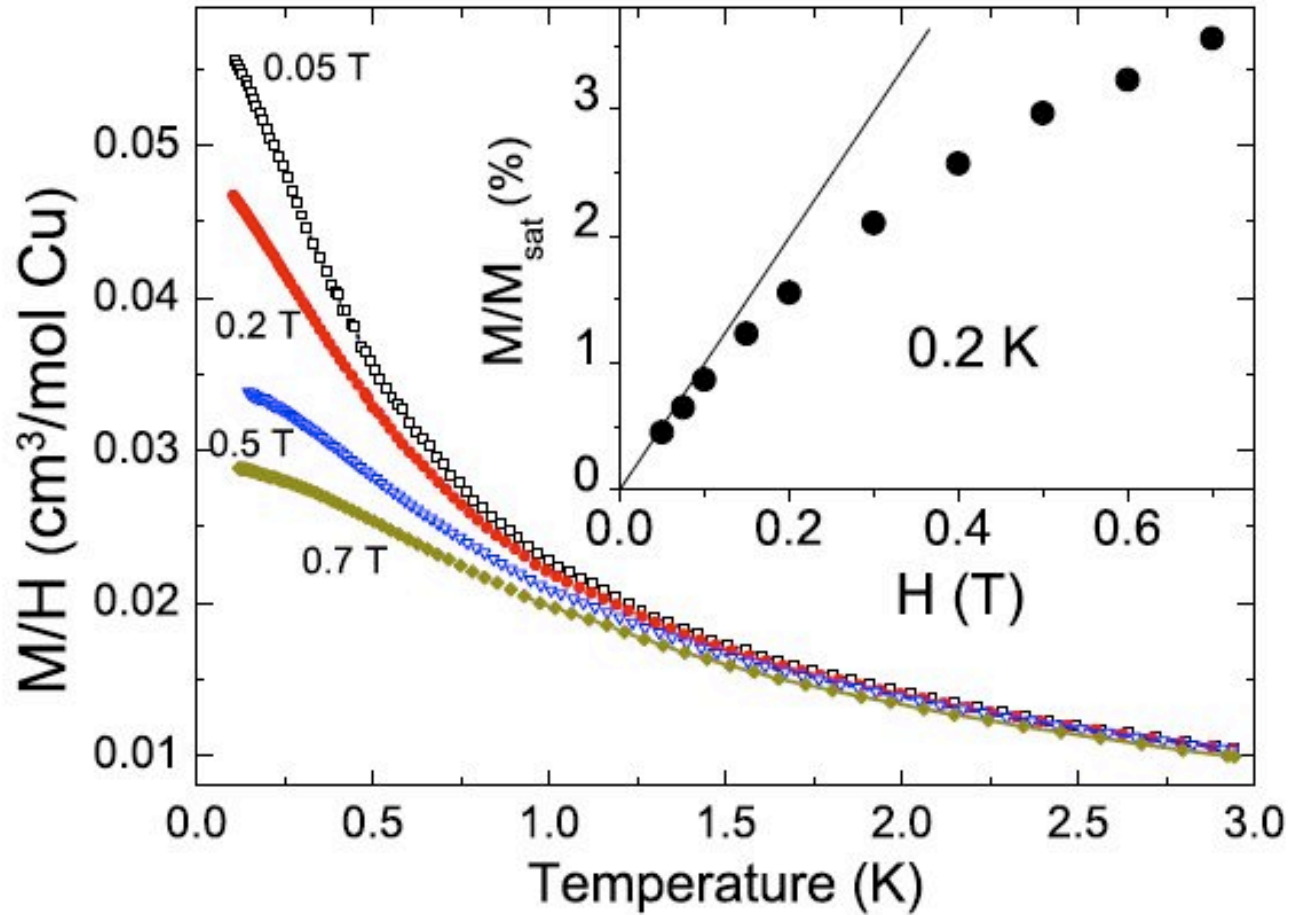
Shores *et al.*, JACS 127, 13462 (2005)



Helton *et al.*, PRL 98, 107204 (2007)

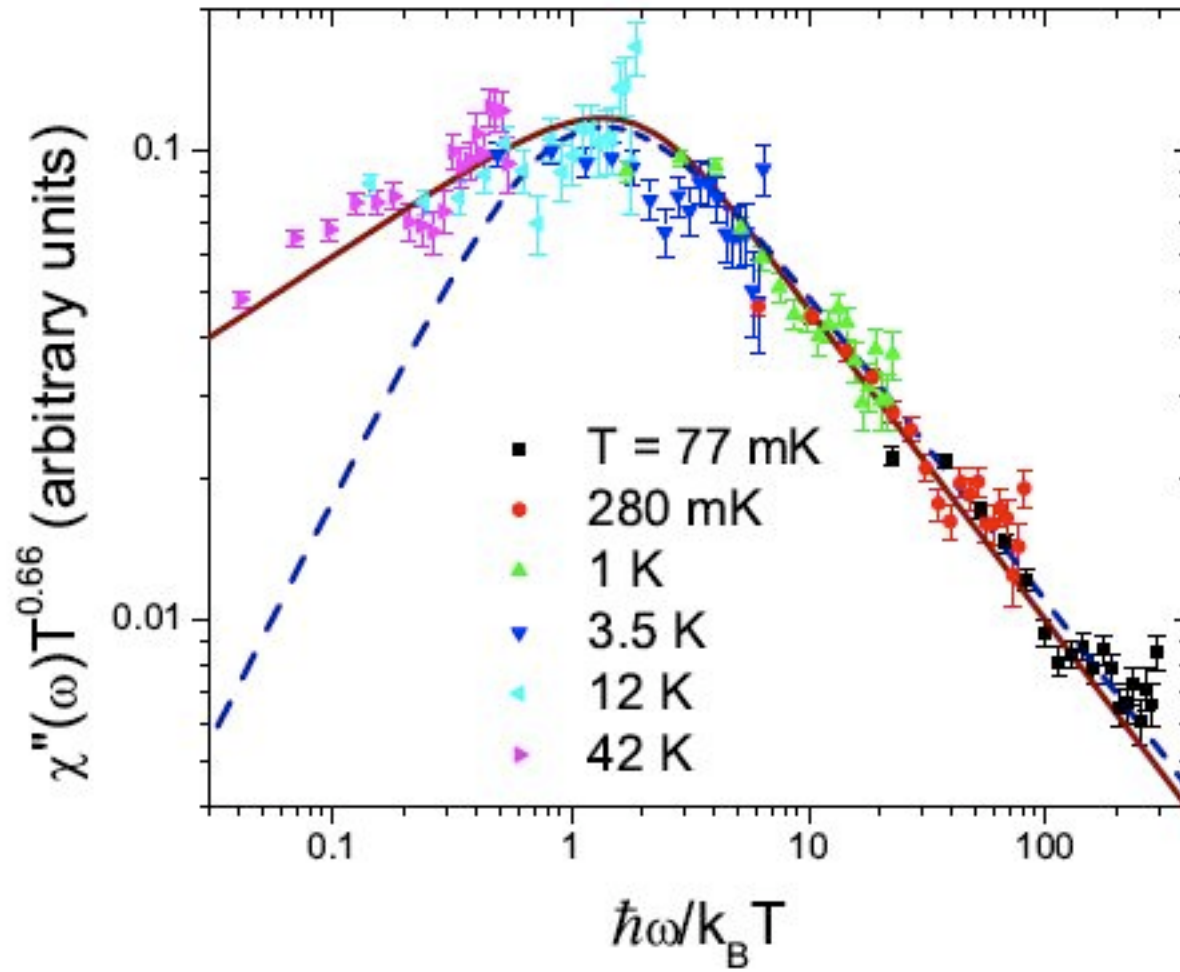
Lee *et al.*, Nat. Matls. 6, 853 (2007)

But, there is a large defect concentration (Cu - Zn)



Bert *et al.*, PRB 76, 132411 (2007)

# $\omega/T$ scaling





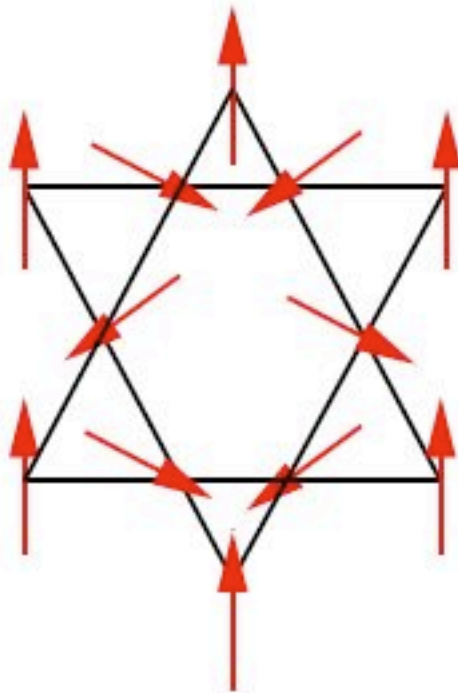
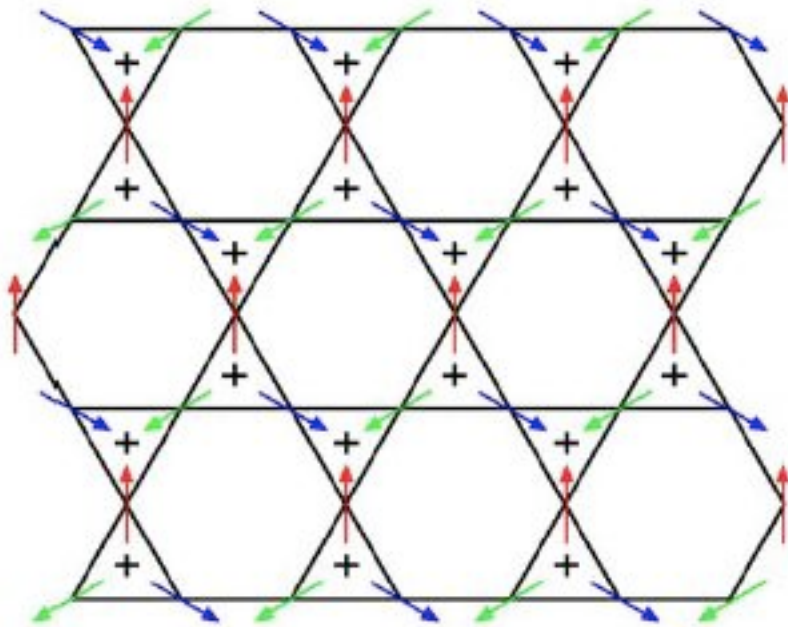


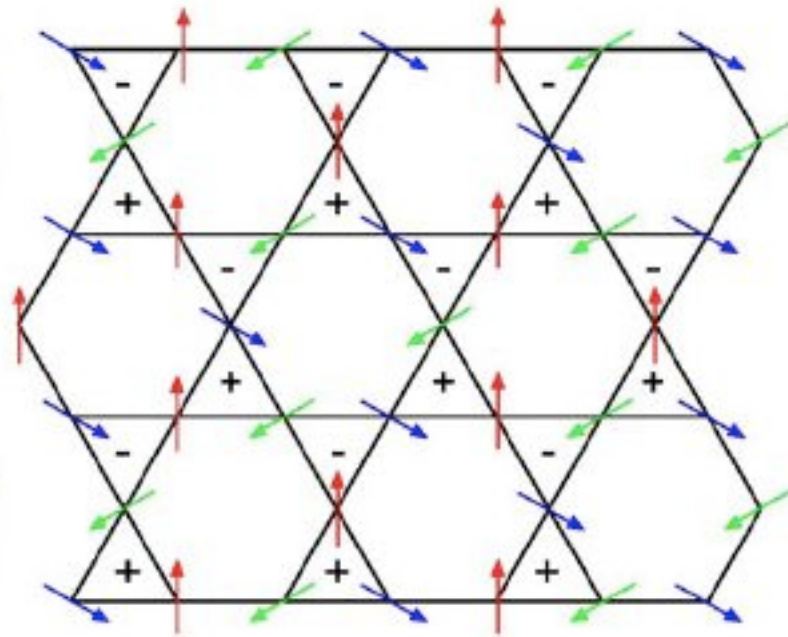
Fig. 1.5. Illustration of how ground state degrees of freedom arise for the Heisenberg model on the kagome lattice: spins on the central hexagon may be rotated together through any angle about the axis defined by the outer spins, without leaving the ground state.

# Classical Kagome Ground States

$$q=0$$

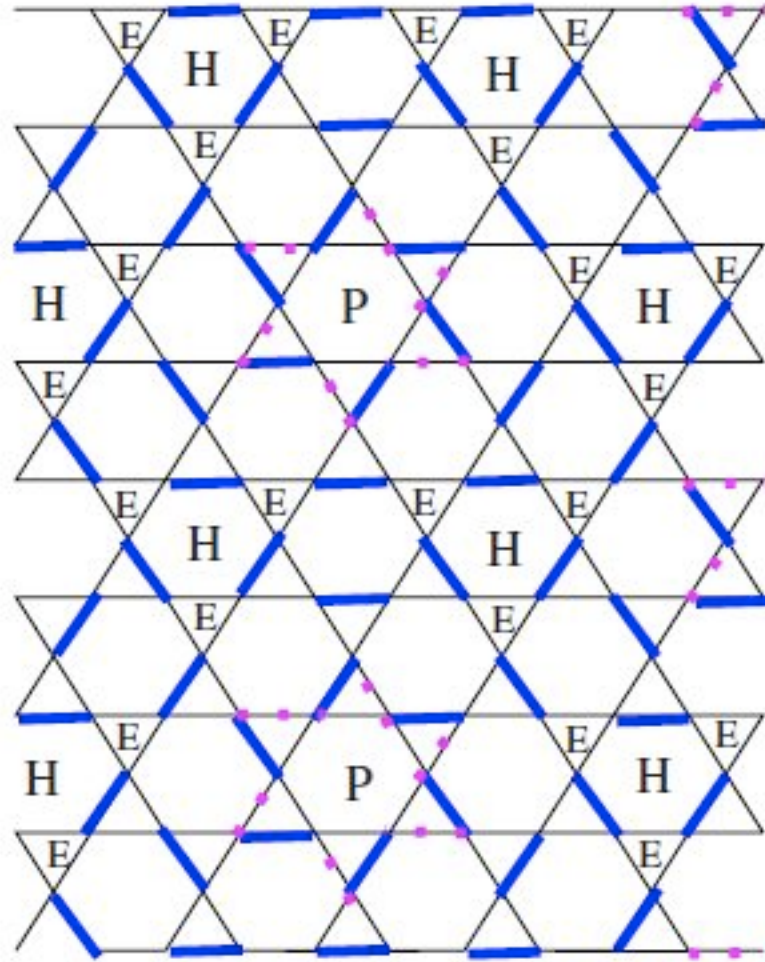


$$\sqrt{3} \times \sqrt{3}$$



Ryu *et al.*, PRB 75, 184406 (2007)

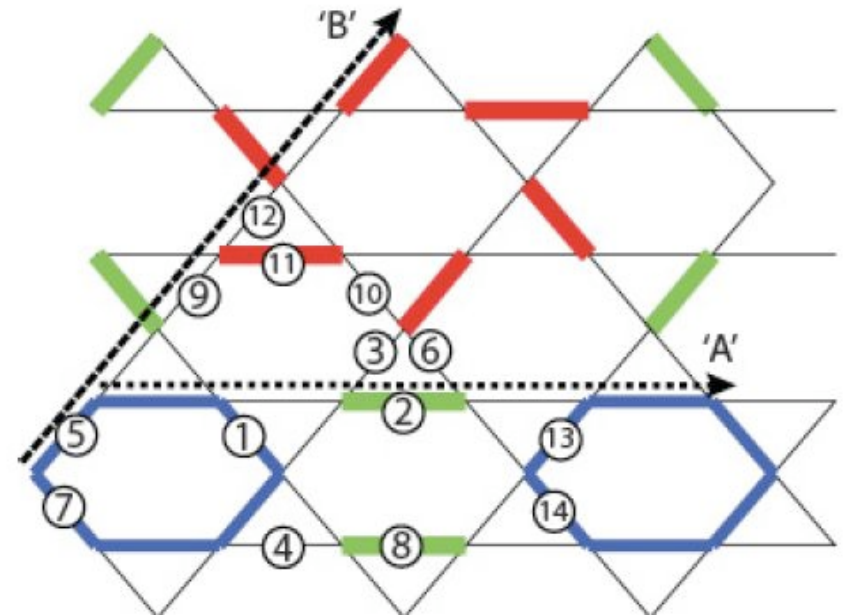
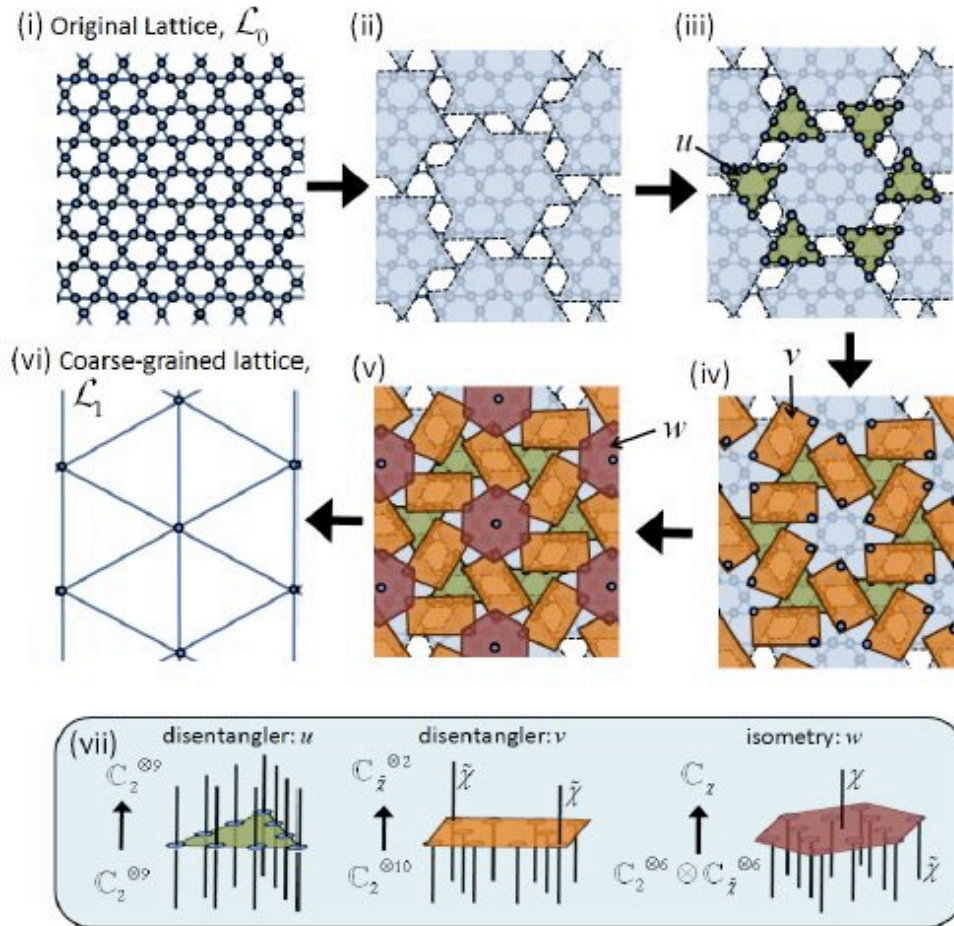
# Valence Bond Ground State for Kagome?



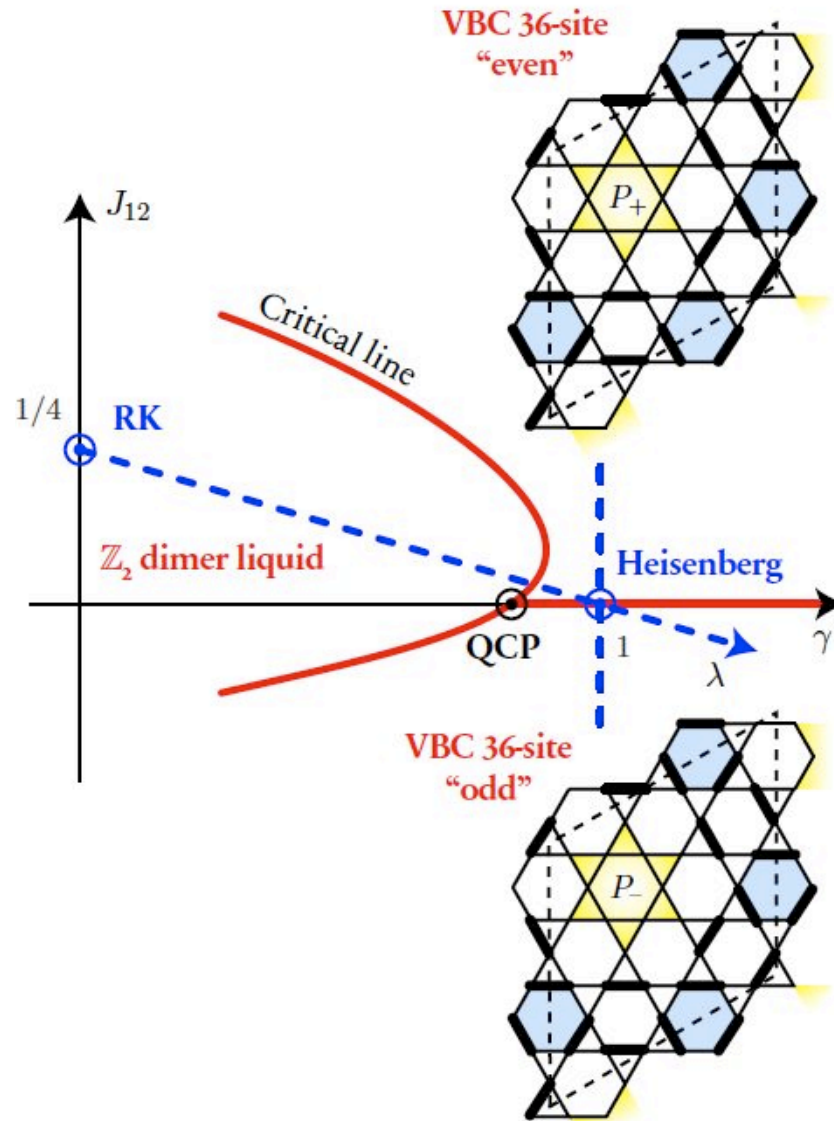
Singh & Huse, PRB 76, 180407 (2007)



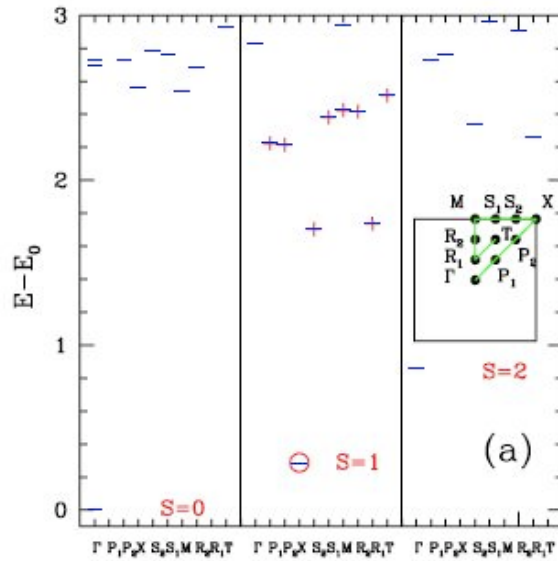
# Multi-scale entanglement renormalization ansatz (MERA)



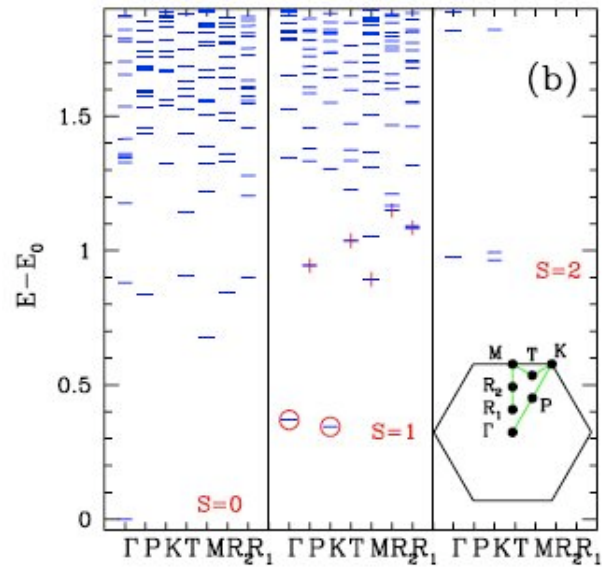
# Close to a Quantum Critical Point?



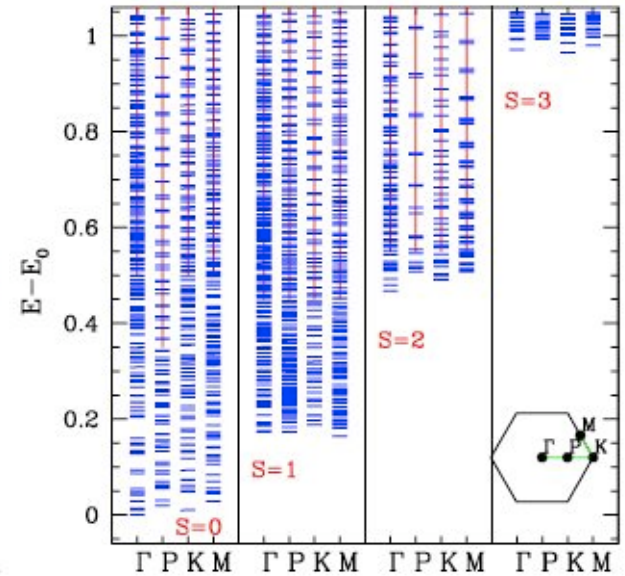
# Exact Diagonalization (36 sites)



square



triangular

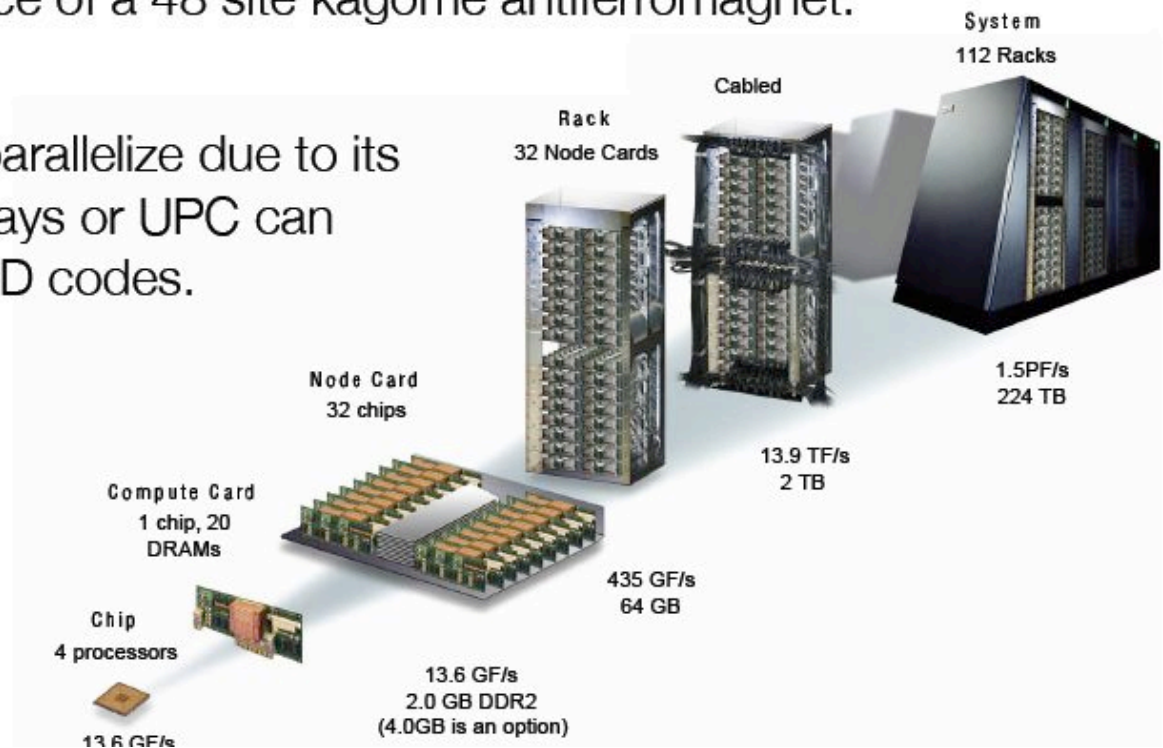


Kagome



# Parallelization: How to harness the petaflop computers ?

- Cutting edge petaflop systems have a huge number of core, but only a moderate amount of node-local memory.
- Next generation ED codes need to be developed in order to attack e.g. the 80 billion Hilbert space of a 48 site kagome antiferromagnet.
- Problem remains difficult to parallelize due to its all-to-all structure. Global Arrays or UPC can help developing distributed ED codes.





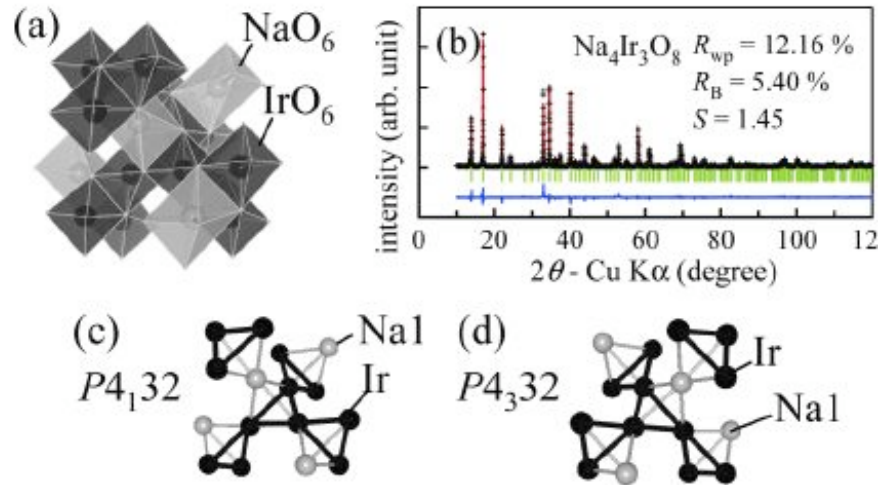
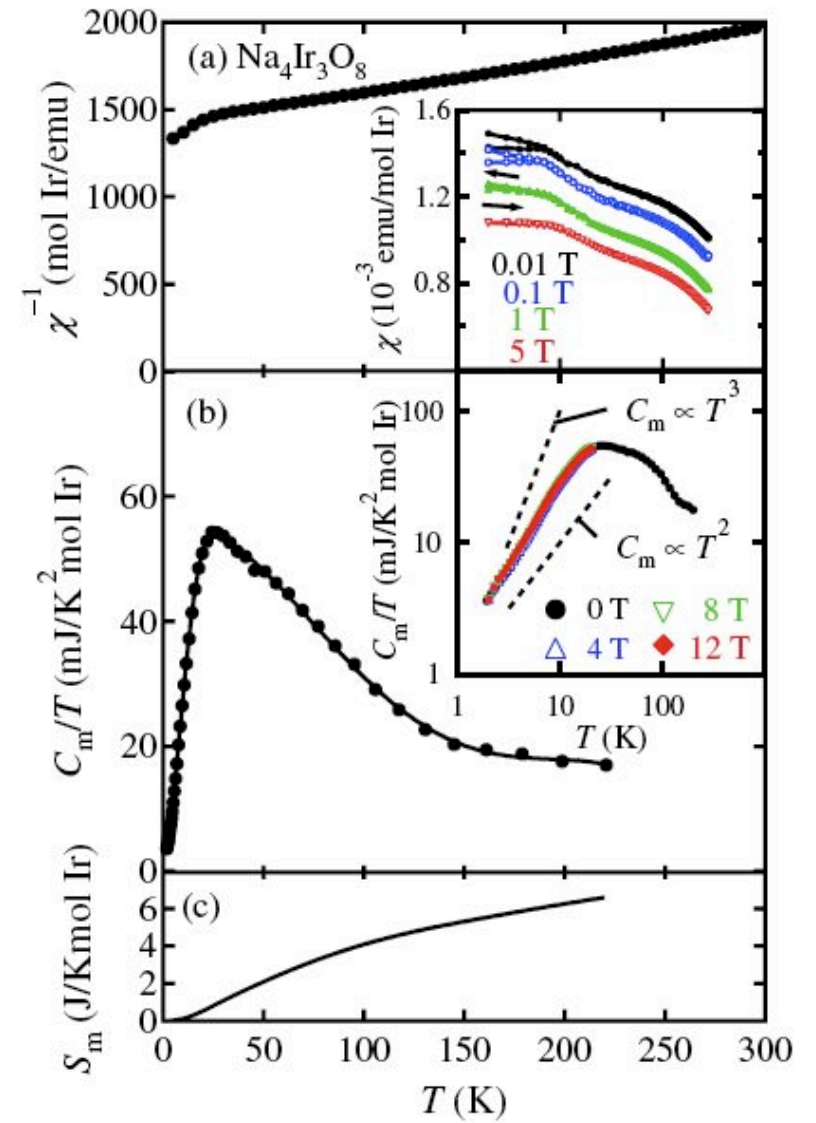


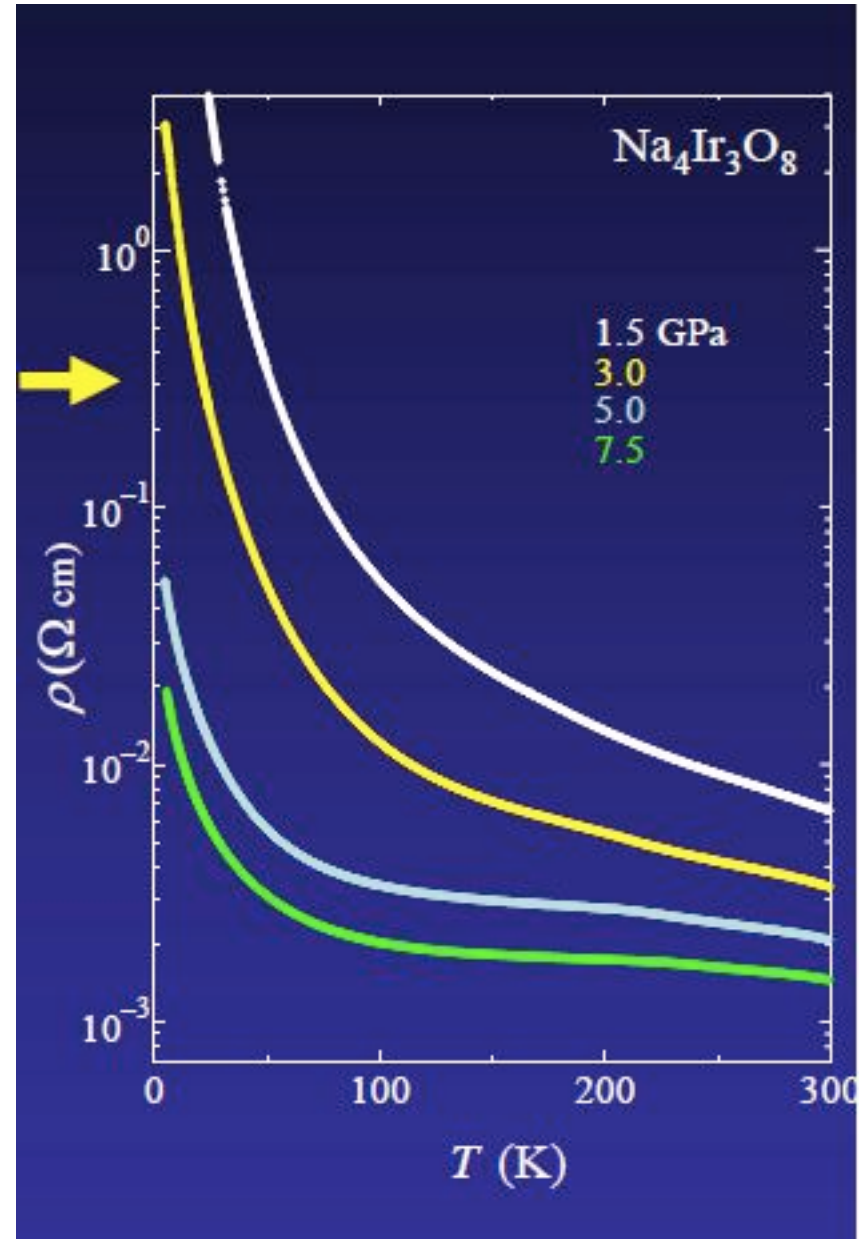
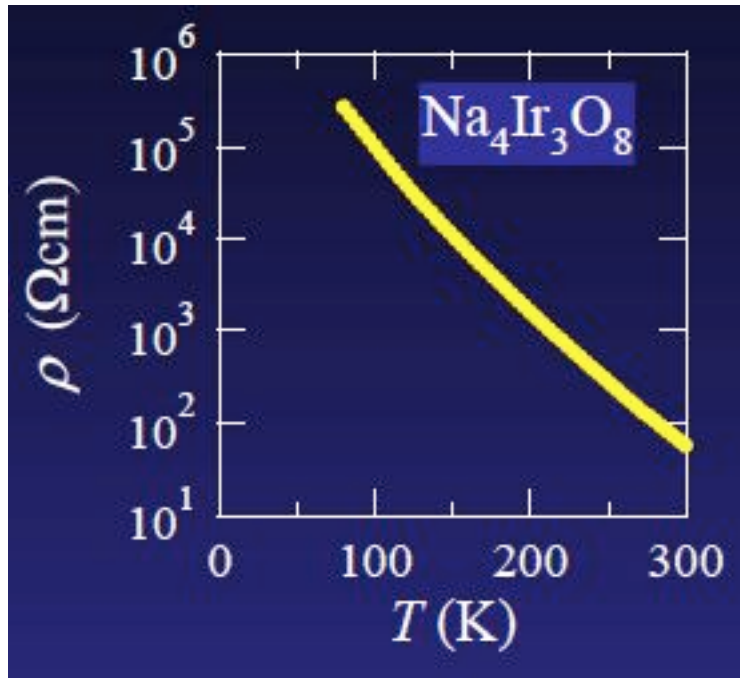
FIG. 1 (color online). (a) Crystal structure of  $\text{Na}_4\text{Ir}_3\text{O}_8$

$$\Theta_{\text{CW}} \sim -650 \text{ K}, \mu_{\text{eff}} \sim 2 \mu_{\text{B}}$$



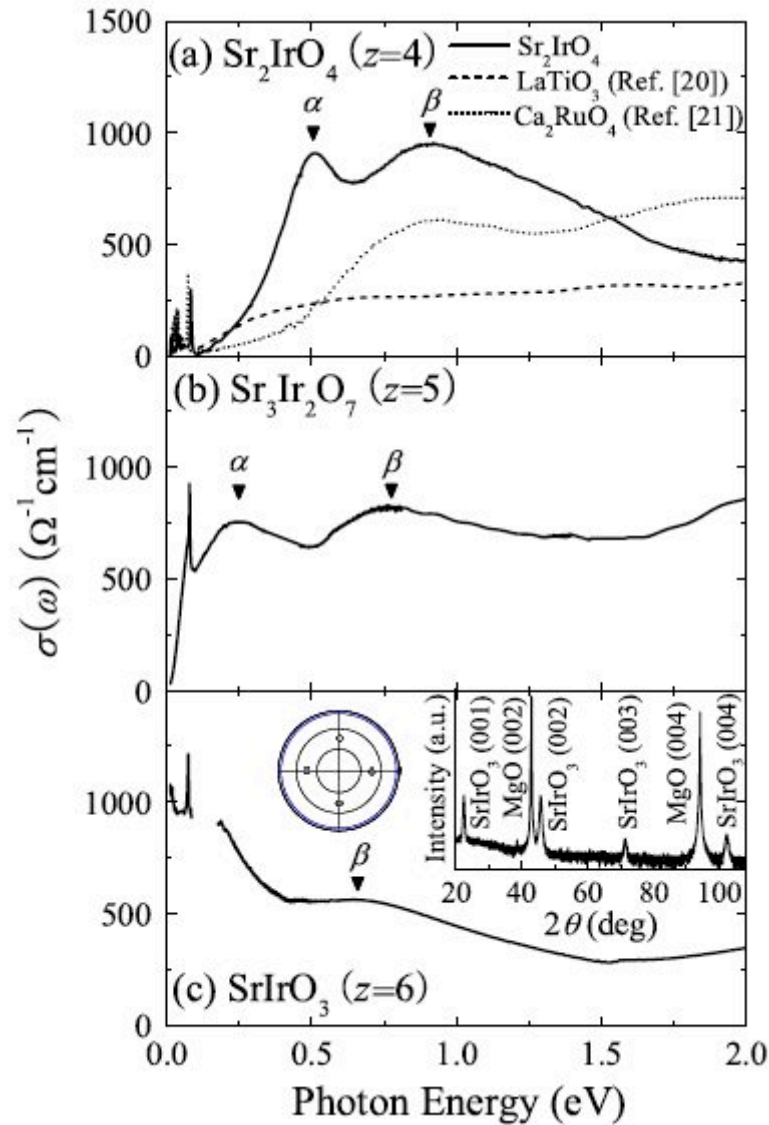
Okamoto *et al.*, PRL 99, 137207 (2007)

## Mott Insulator?



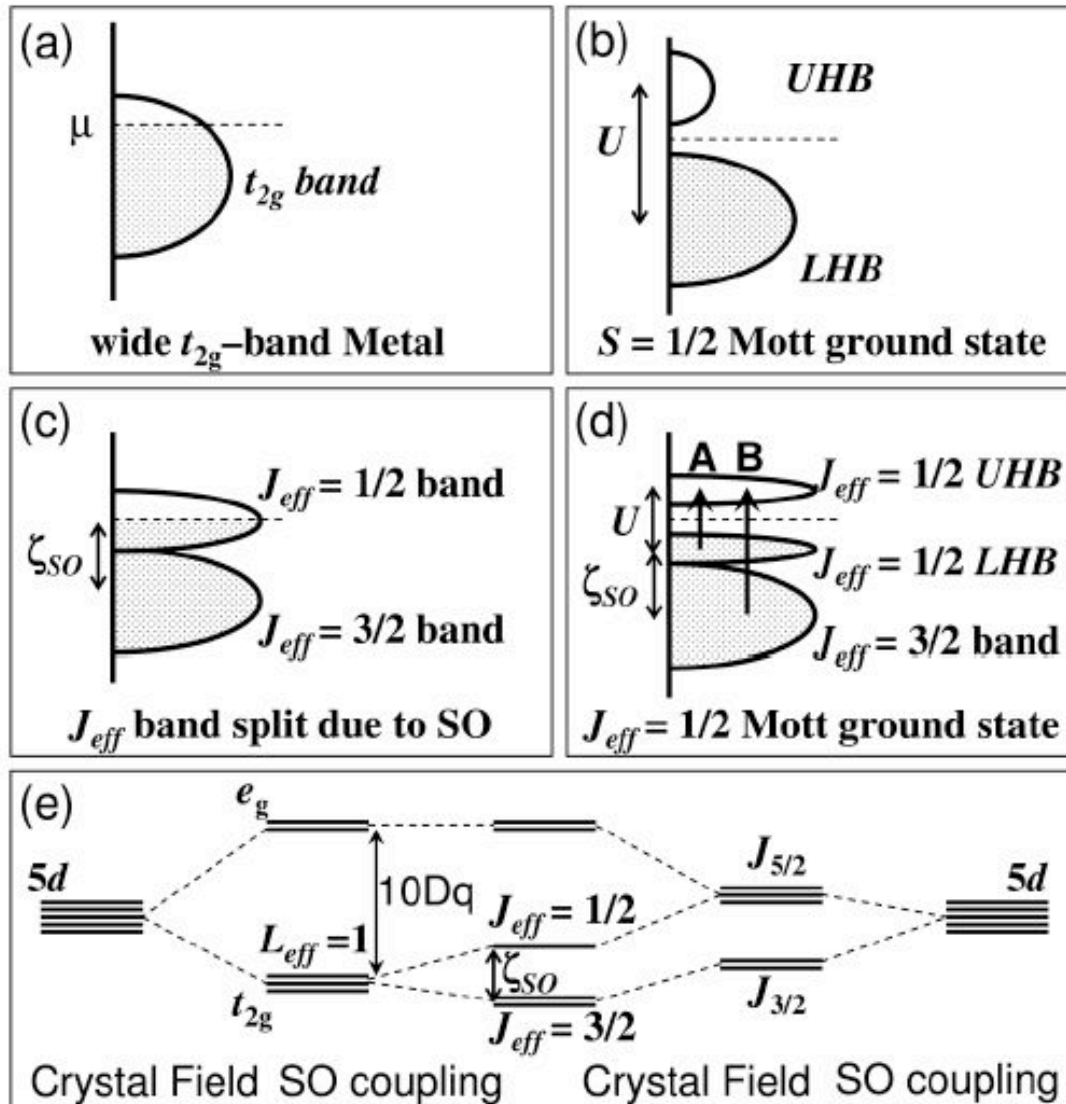
H. Takagi, unpublished

$\text{Sr}_2\text{IrO}_4$  ( $\text{La}_2\text{CuO}_4$  analogue) appears to be a Mott insulator



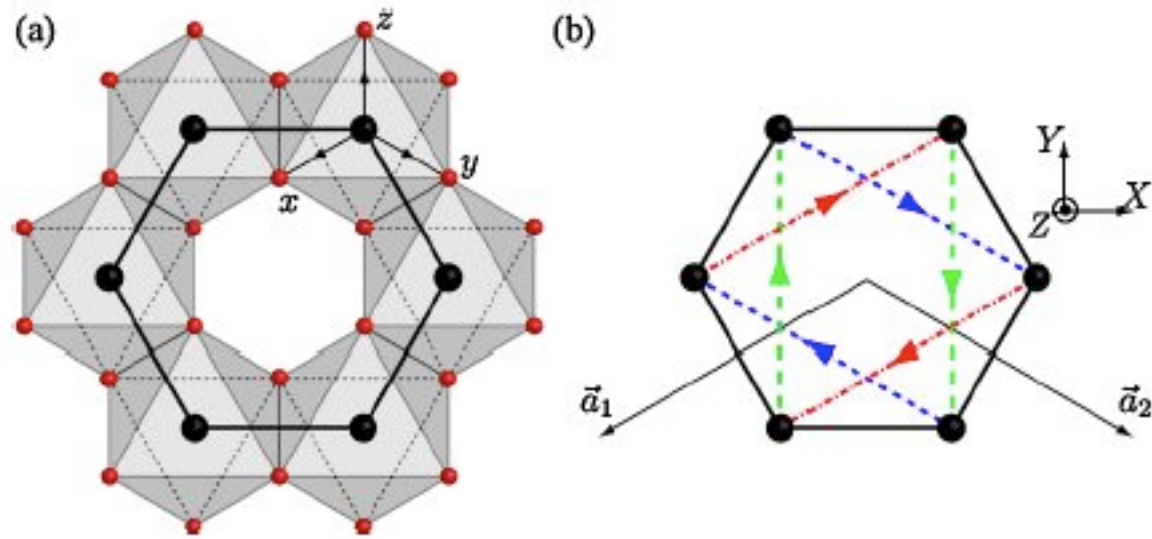
Moon *et al.*, PRL 101, 206402 (2008)

# Spin-orbit plus $d^5$ configuration leads to a half filled doublet



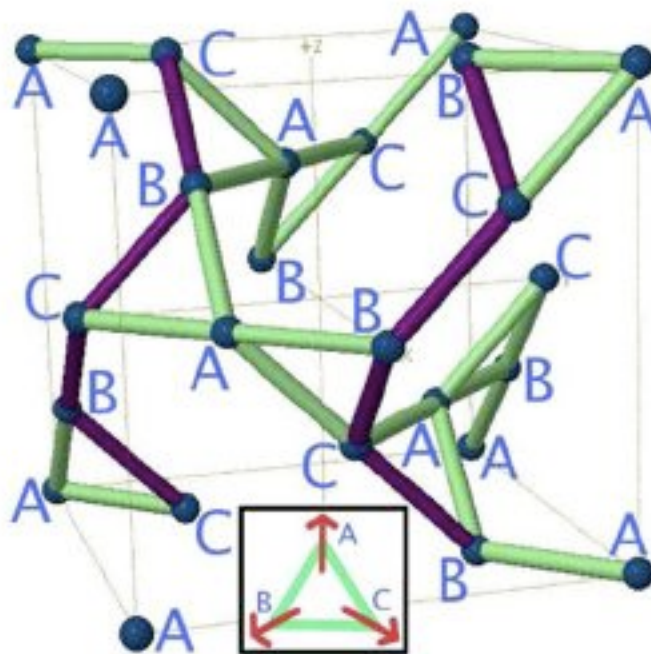


# Quantum Spin Hall Effect in $\text{Na}_2\text{IrO}_3$ ?



Shitade *et al.*, PRL 102, 256403 (2009)

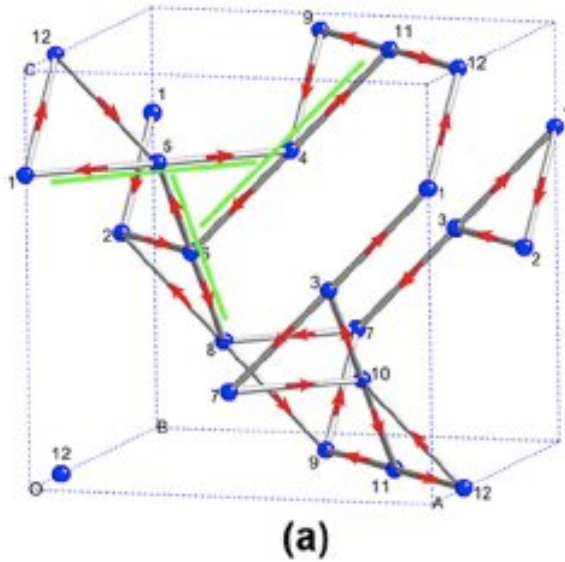
$\text{Na}_4\text{Ir}_3\text{O}_8$  - Ir ions form a network of corner sharing triangles



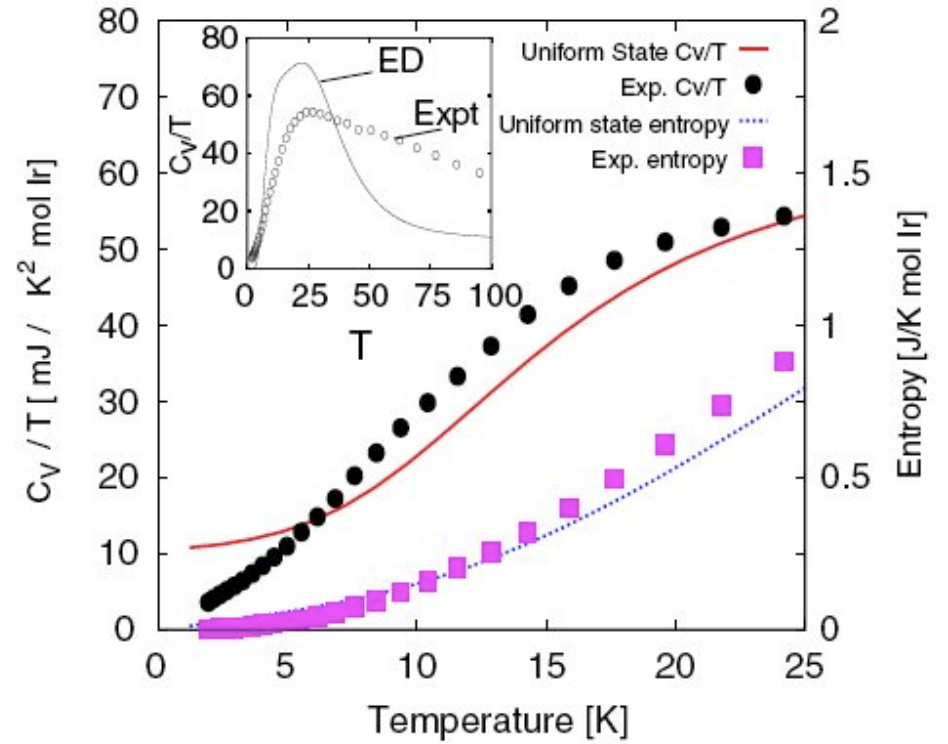
Semiclassical - J S·S

Lawler *et al.*, PRL 100, 227201 (2008)

# 10 site loops



Zhou *et al.*, PRL 101, 197201 (2008)



Lawler *et al.*, PRL 101, 197202 (2008)

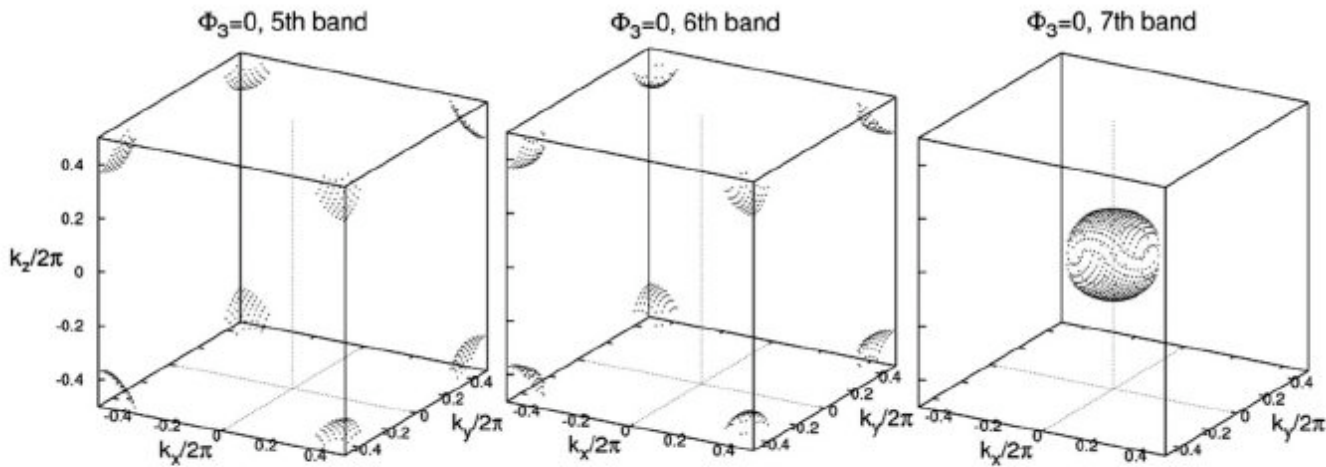
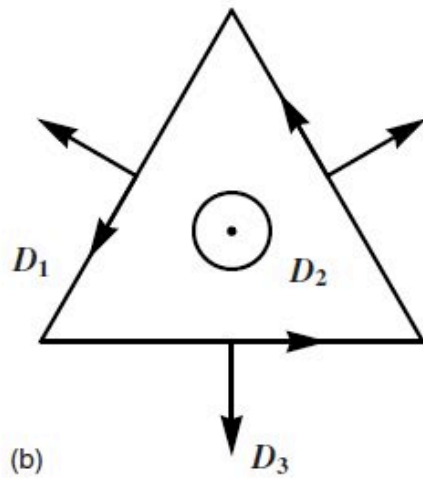
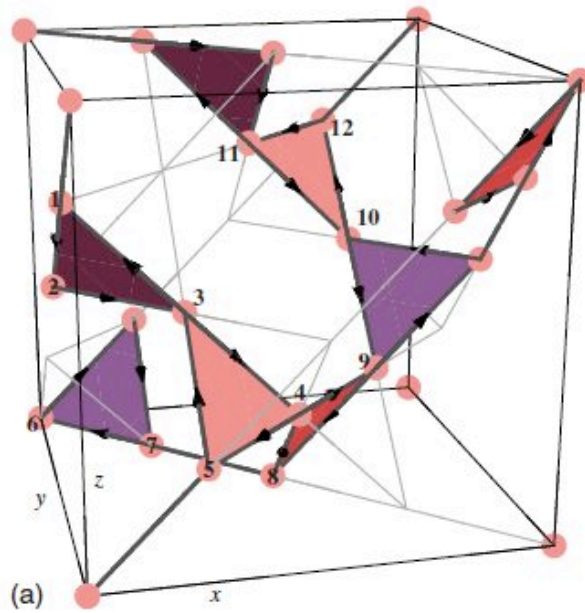


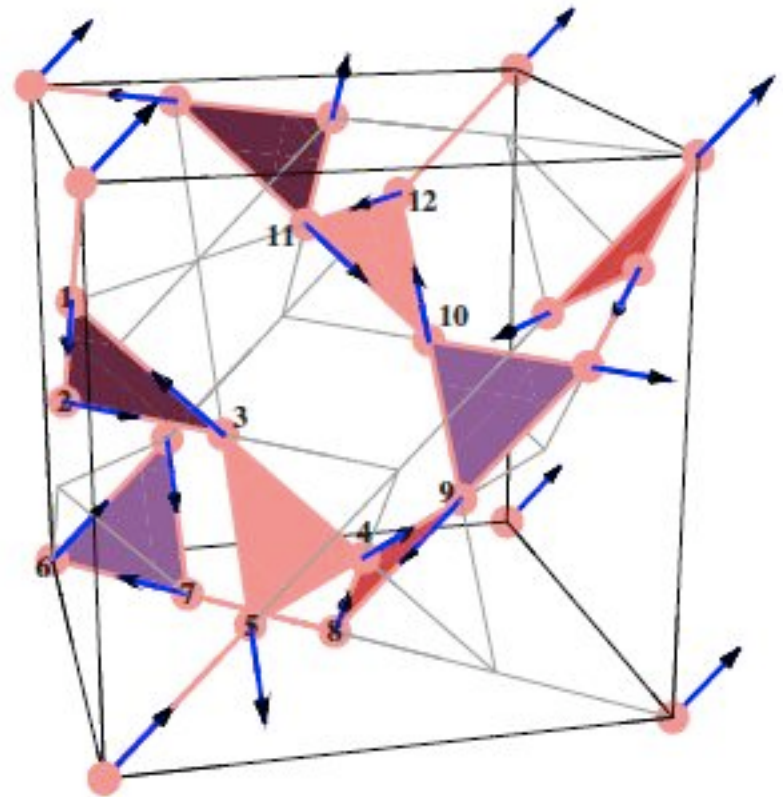
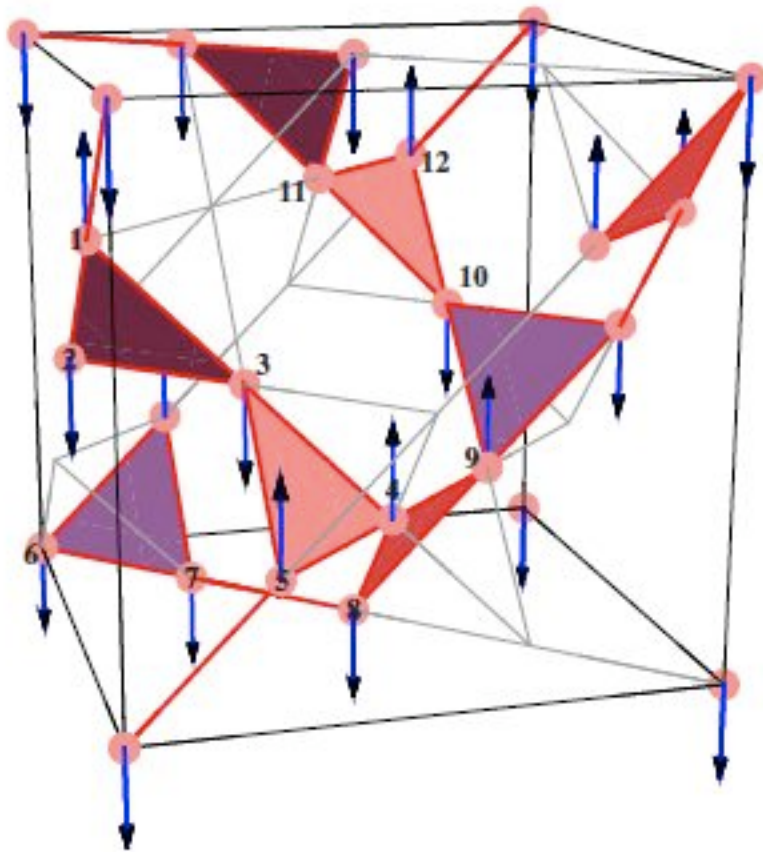
FIG. 2. Fermi surfaces of the zero flux state at half-filling.

# $\text{Na}_4\text{Ir}_3\text{O}_8$ - anisotropy important due to spin-orbit coupling



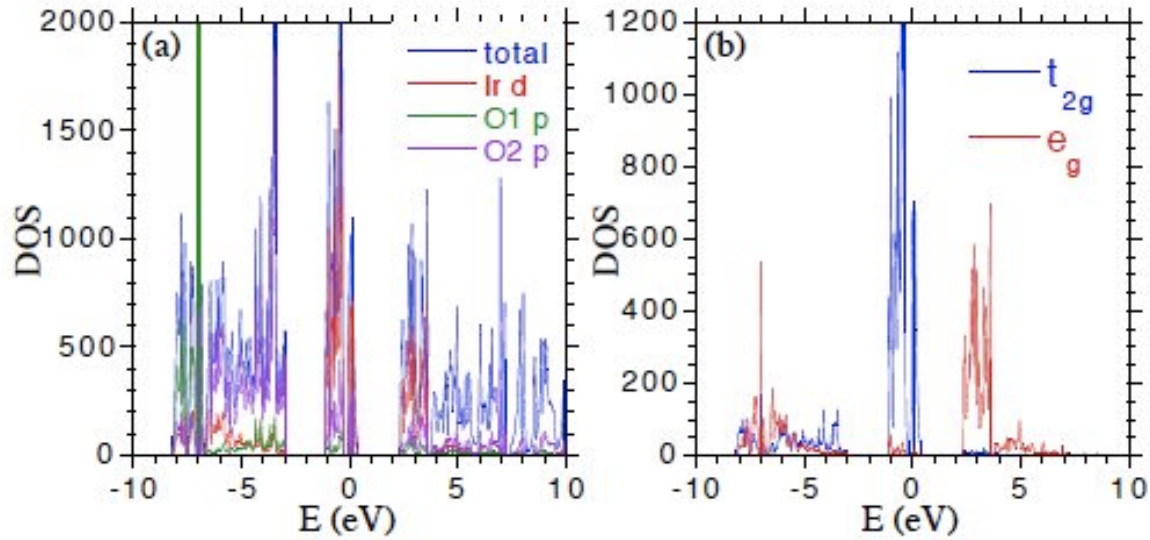
Chen & Balents, PRB 78, 094403 (2008)

# Possible ground states in the presence of anisotropy

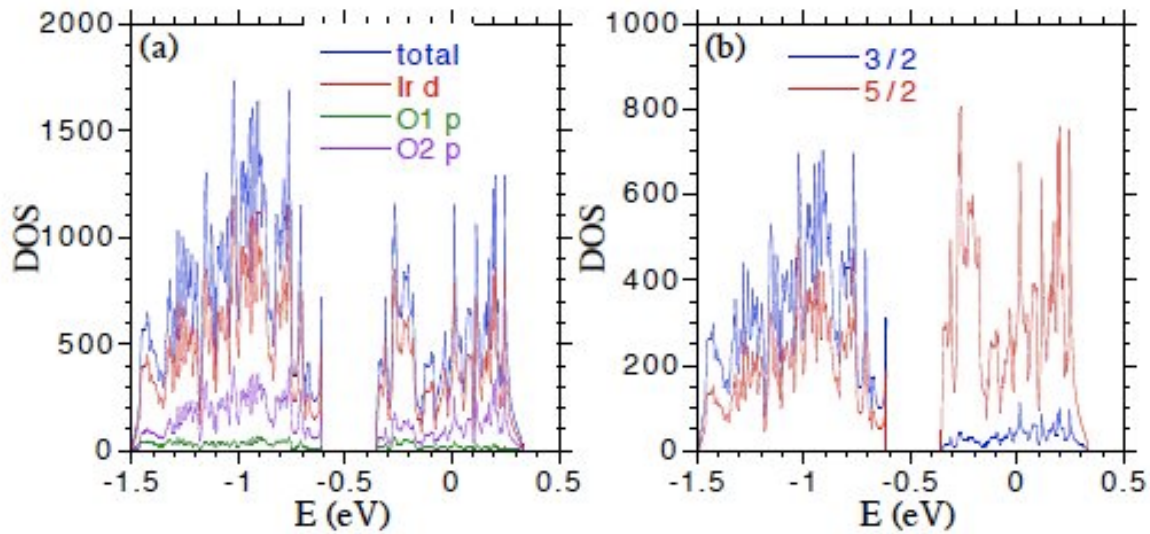




# LDA



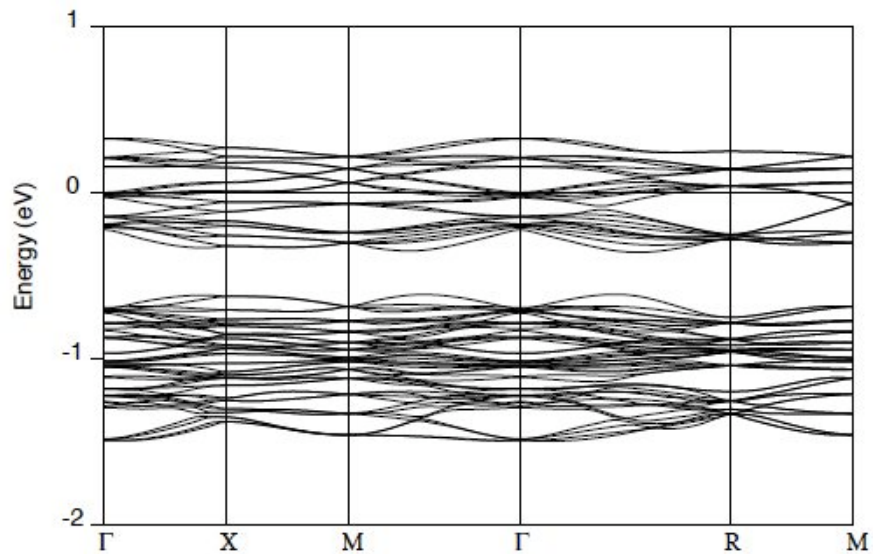
No spin-orbit



Spin-orbit

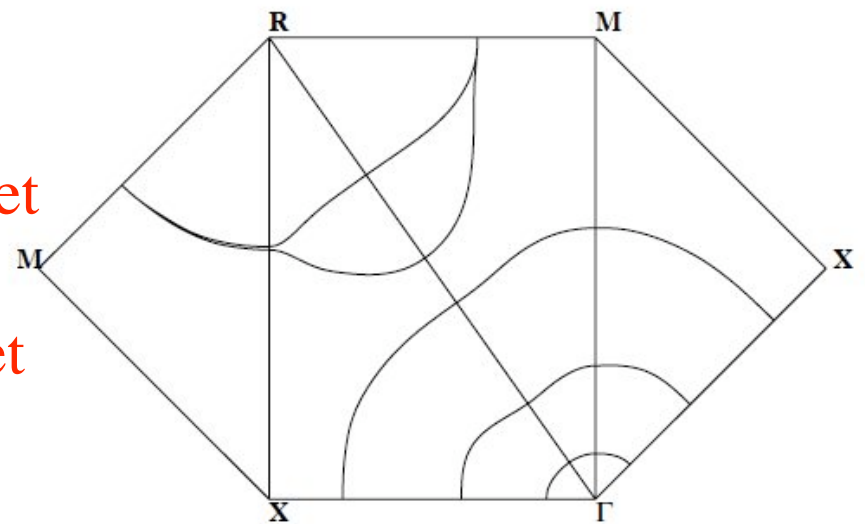
Norman & Micklitz, PRB 81, 024428 (2010)

## LDA (spin-orbit)

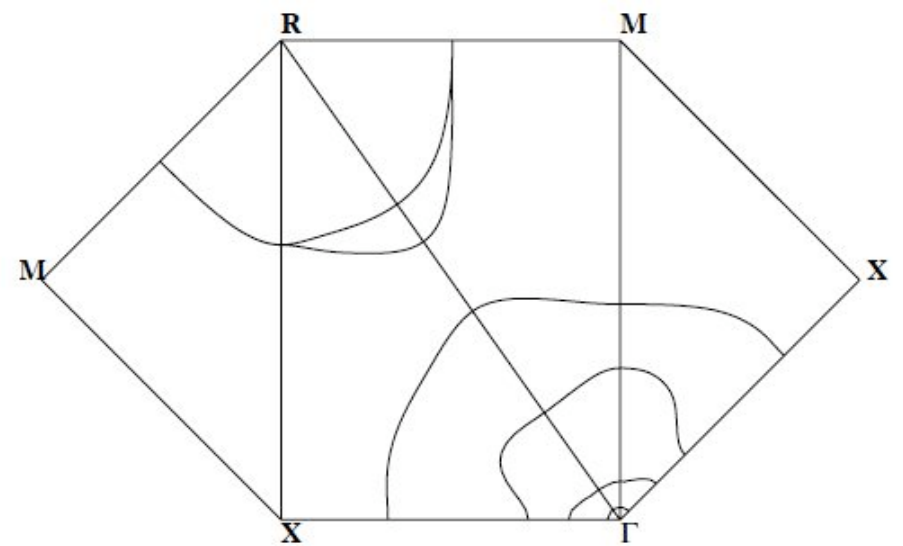
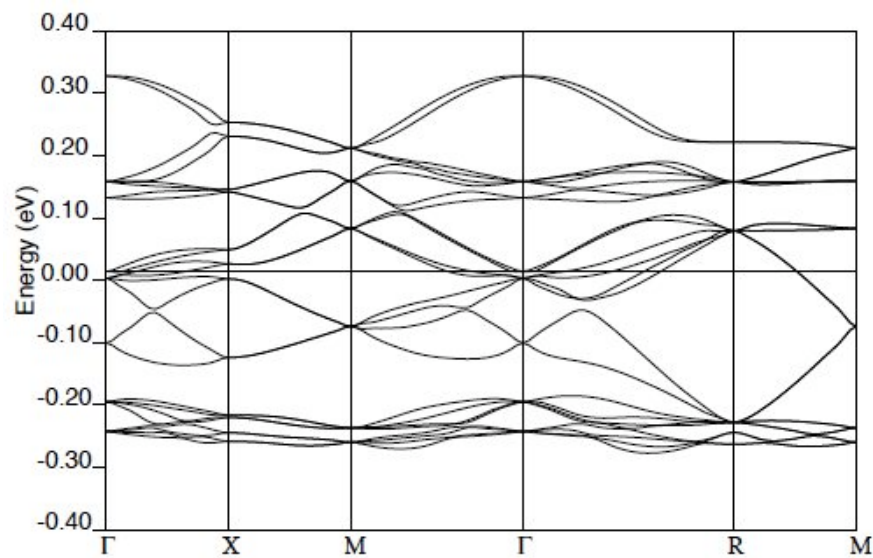


doublet

quartet



## Tight Binding Fit



## Direct Ir-Ir Exchange is Isotropic!

$$J = 4 t^2/U$$

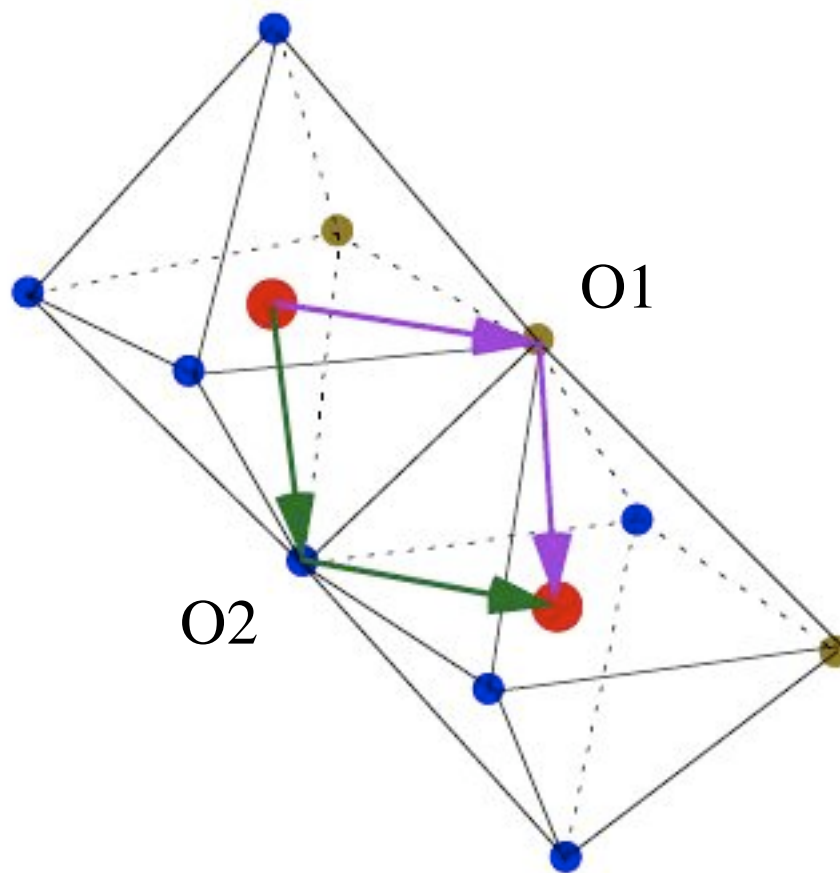
where

$$t = \frac{1}{4} t_{dd}^{\sigma} + \frac{1}{3} t_{dd}^{\pi} + \frac{5}{12} t_{dd}^{\delta}$$

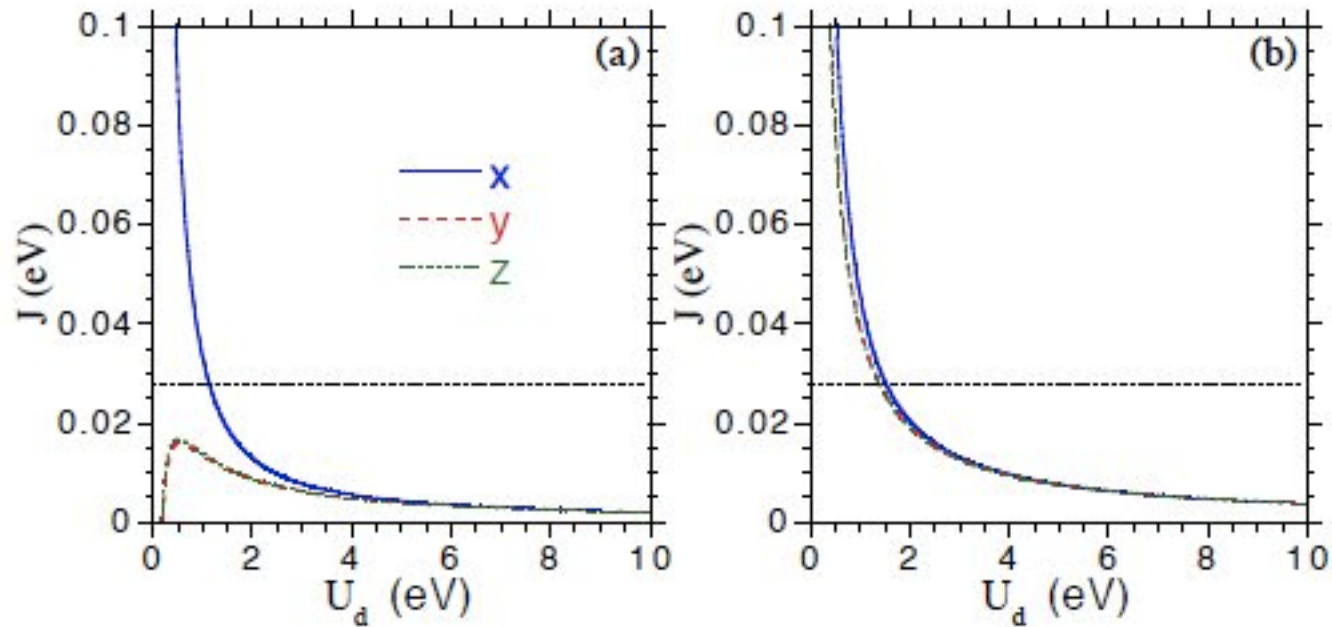
But superexchange is present which should give rise to anisotropic exchange plus Dzyaloshinskii-Moriya



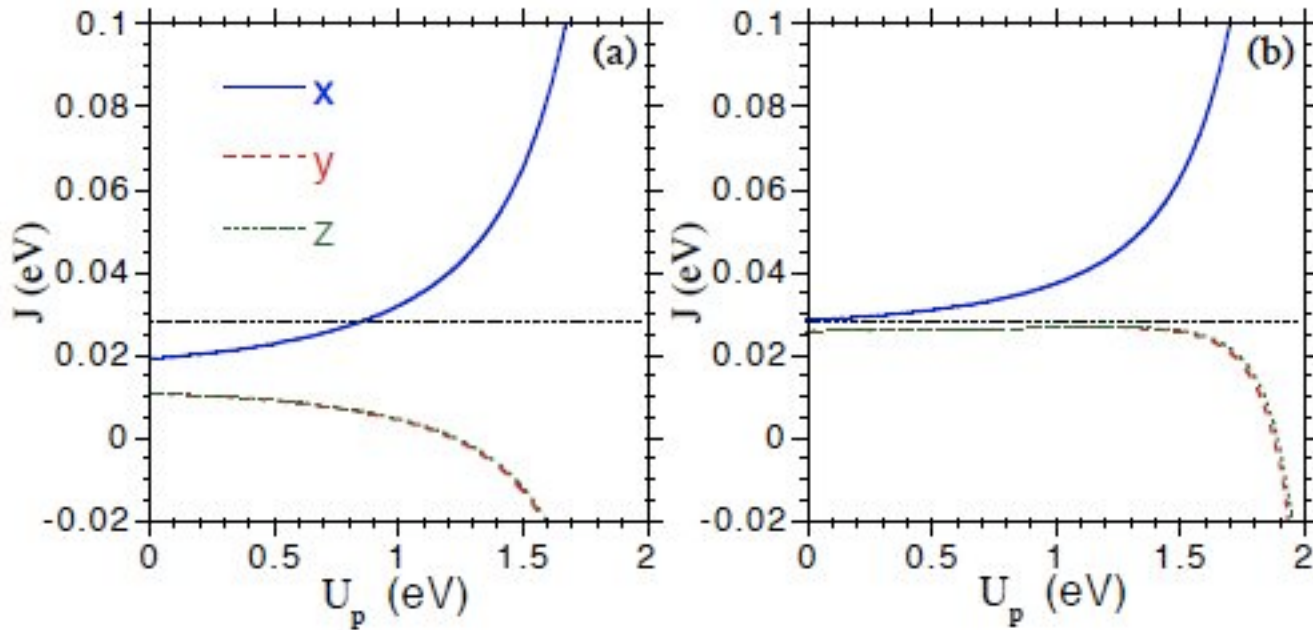
# Superexchange



# Total Exchange versus $U_d$ and $U_p$ for two tight binding fits



<- exp.



# How to Detect a Spinon Fermi Surface

Norman & Micklitz, PRL 102, 067204 (2009)

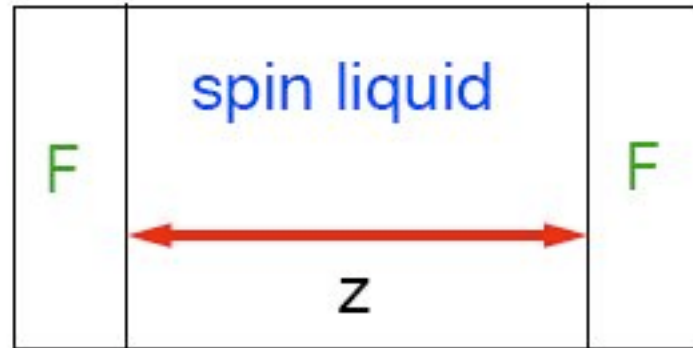


FIG. 1: (Color online) The proposed experiment involves two ferromagnetic layers (F) with a spin liquid spacer of variable thickness,  $z$ . Depending on the sign of the oscillatory coupling, the two ferromagnets will be aligned or anti-aligned.

Parkin *et al.*, PRL 64, 2304 (1990)

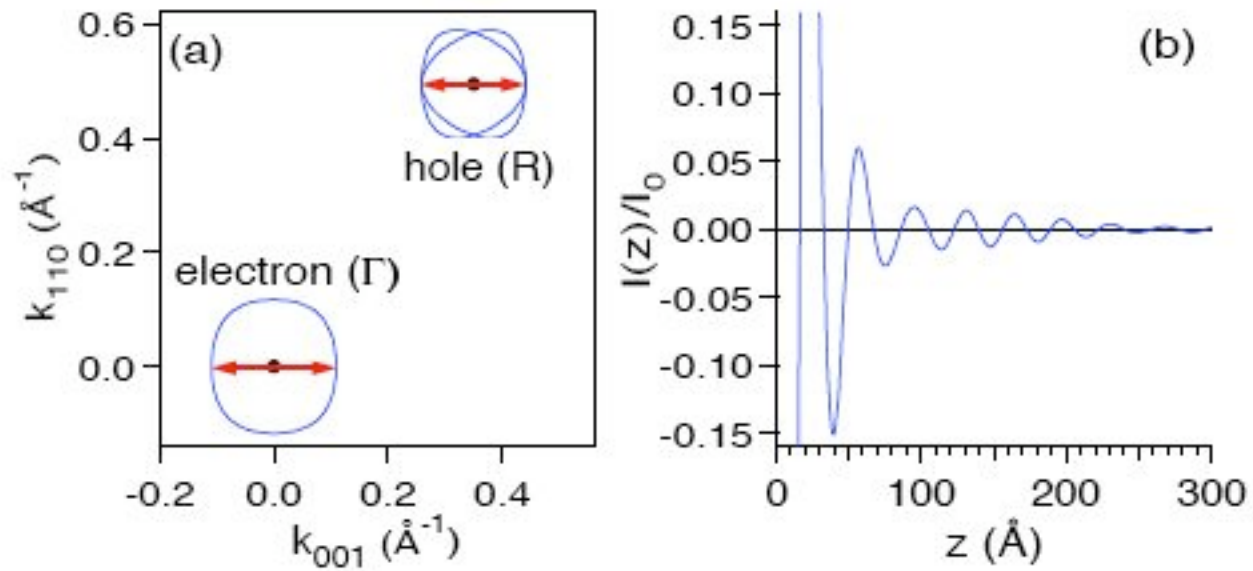


FIG. 3: (Color online) (a) Spinon Fermi surface for  $\text{Na}_4\text{Ir}_3\text{O}_8$  ( $a=8.985\text{\AA}$ ). Spanning vectors are indicated by arrows. (b) Calculated oscillatory response from Eq. 7.

$$I(z) = I_0 \left(\frac{d}{z}\right)^2 \sum_n \frac{m_n^*}{m} \sin(2k_{F_n} z)$$

Cuprates are Mott insulators characterized by  
a half filled band and have a large  $J$

So are iridates!

Can iridates be doped, and if so, will they  
become high temperature superconductors?