

# The Physics of the Dense Kondo lattice

Z. Fisk, UC Irvine

KITP January 14, 2010

# Collaborators

Yi-feng Yang UC Davis

David Pines UC Davis

Sam Maquilon UC Davis

Long Pham UC Davis

J. D. Thompson LANL

E. Bauer LANL

H. Lee LANL

C. Capan UCI

D. Hurt UCI

A. Bianchi U Montreal

support: NSF-DMR- 0801253

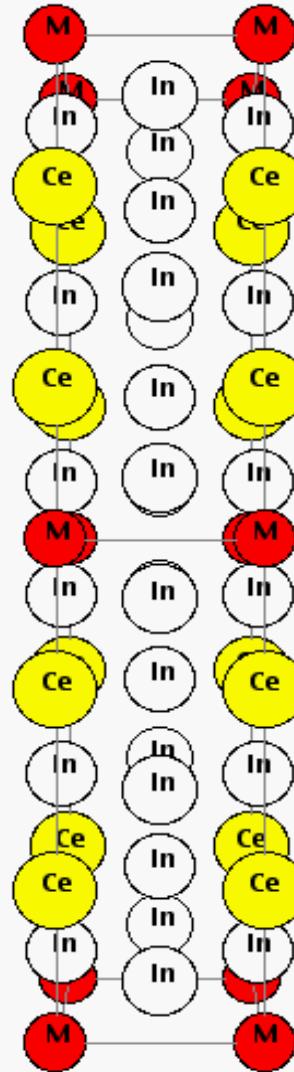
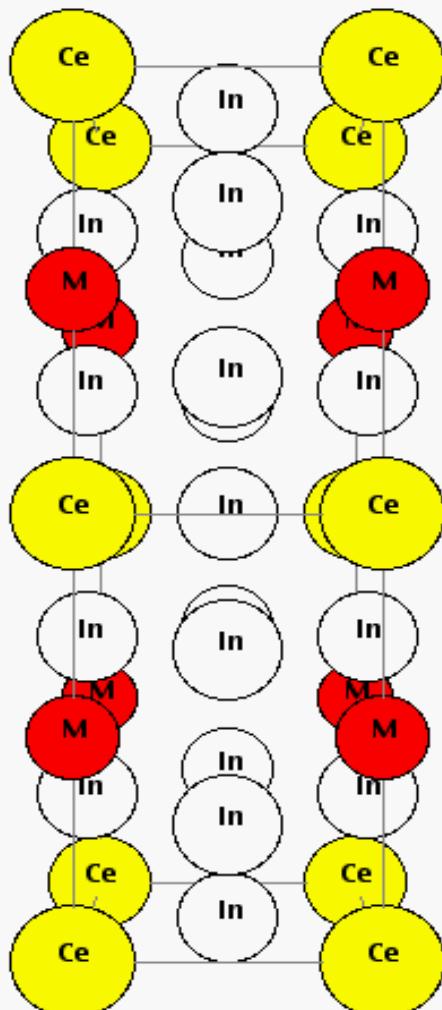
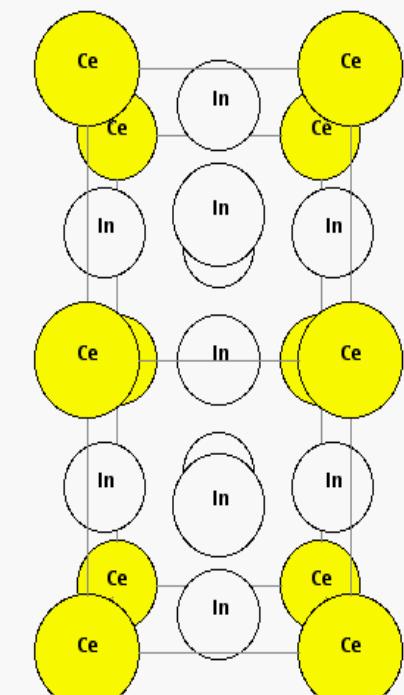
# Outline

- evolution of coherent lattice with doping in  $\text{Ce}_{1-x}\text{La}_x\text{CoIn}_5$
- comparison with  $\text{Yb}_{1-x}\text{Lu}_x\text{Rh}_2\text{Si}_2$
- scale for entropy development in these systems:  $T_K$  sets the lattice coherence scale
- using the sc condensation energy in  $\text{Ce}_{1-x}\text{La}_x\text{CoIn}_5$  to show inhomogeneity of doped dense Kondo liquid
- evidence for intrinsic dilute gas of free Kondo centers in pure  $\text{CeCoIn}_5$

# dilution studies of CeCoIn<sub>5</sub>

Cross over from single ion Kondo  
to  $C/T \propto \ln(T/T^*)$  near 2D  
percolation threshold

# Crystal Structures



$M = \text{Co, Rh, Ir}$  (isovalent)

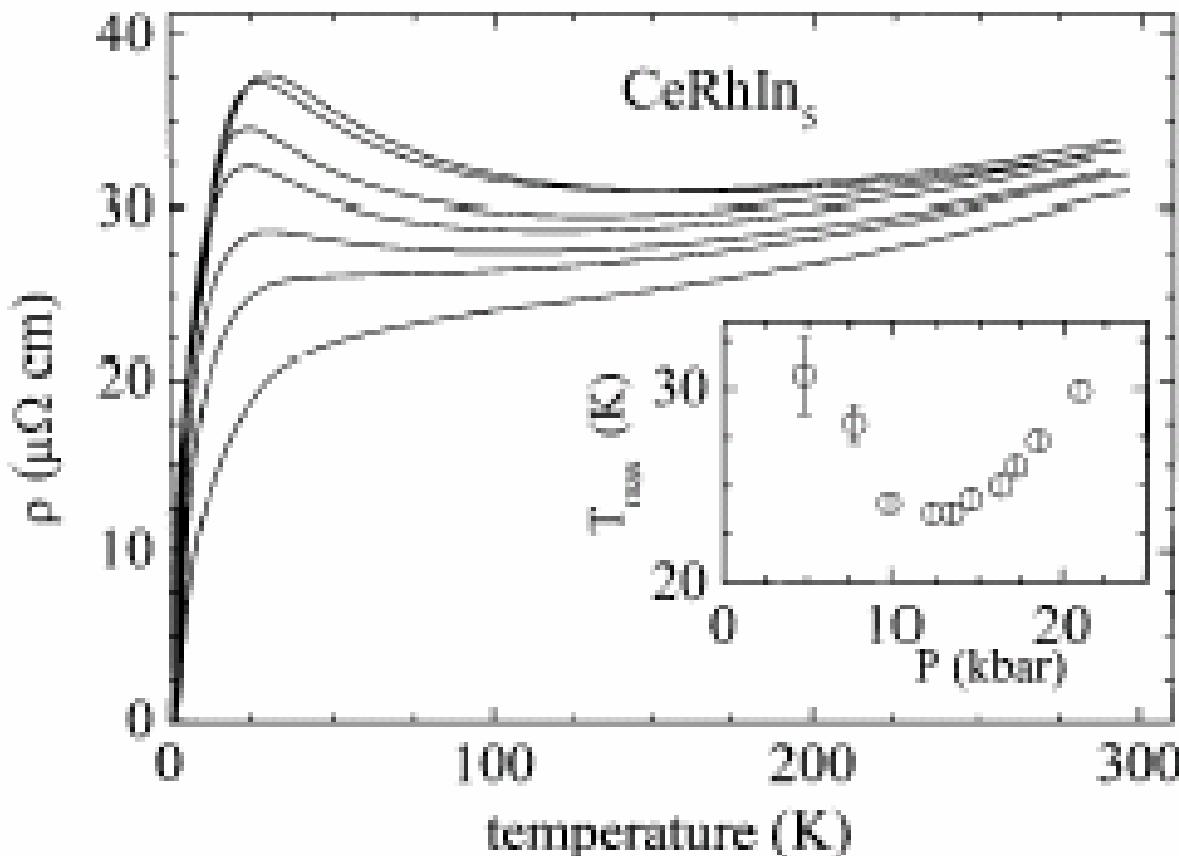
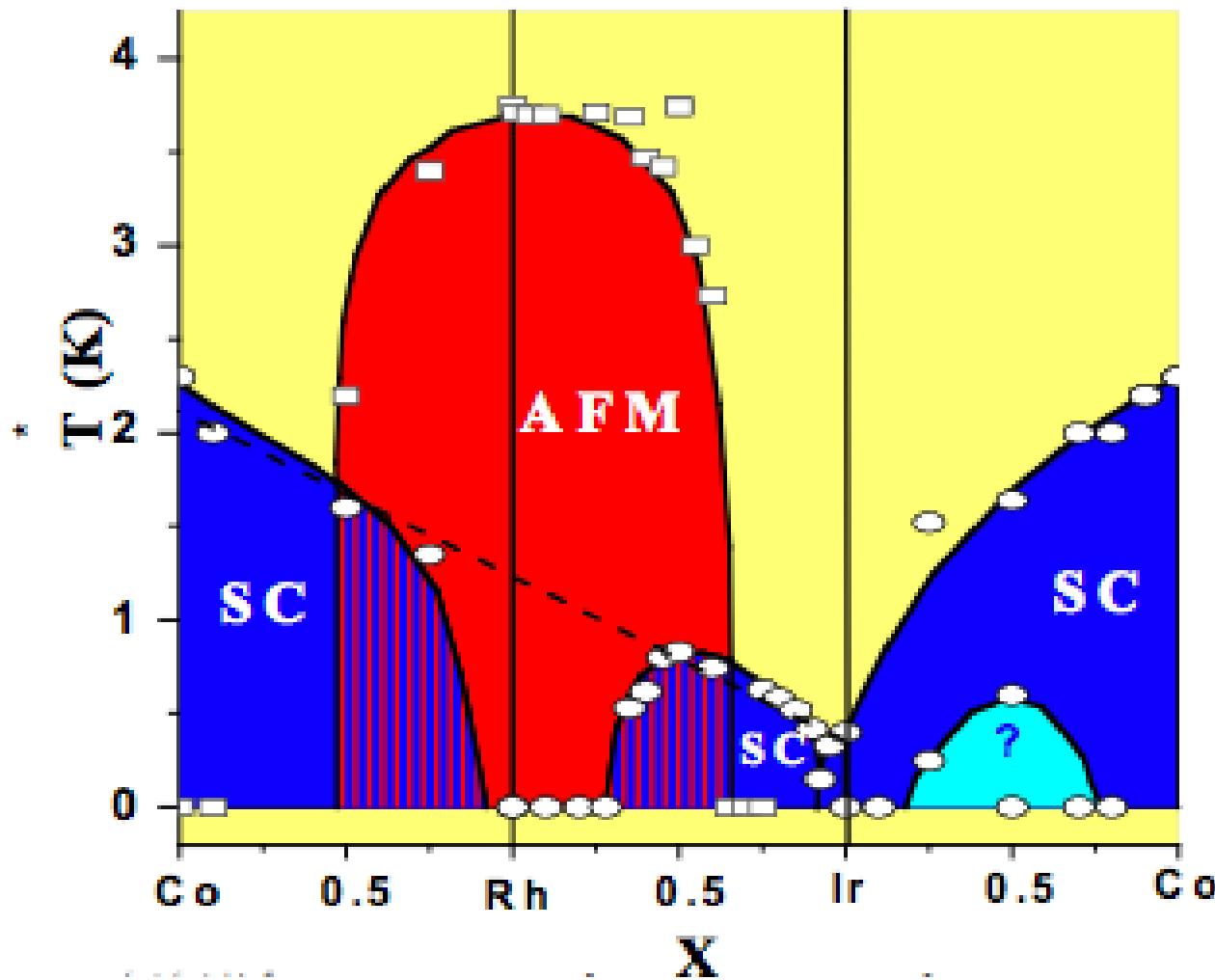
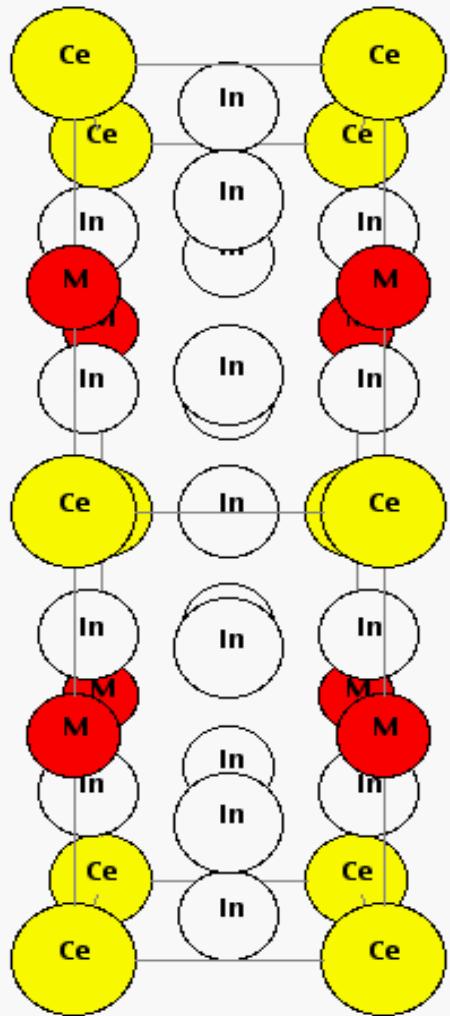


FIG. 2. Temperature dependence of the electrical resistivity of  $\text{CeRhIn}_5$  at representative applied pressures. Data shown correspond to pressures of 0.001, 4.8, 7.9, 12.2, 14.5, 18.5, and 21.0 kbar and are associated, respectively, with curves of increasing resistivity at 50 K. The inset is a plot of the pressure dependence of the temperature  $T_{\max}$  where the resistivity is a maximum.

# AF and Superconductivity in CeMIn<sub>5</sub> systems



# Heavy Fermion Superconductor CeCoIn<sub>5</sub>



M = Co

- Heavy Fermion Superconductor with  $T_c \approx 2.3$  K

(C. Petrovic et al. J. Phys.: Condensed Matter **13**, L337 (2001).)

- Quasi 2D electronic structure

(e.g. D. Hall et al., Phys. Rev. B **64**, 212508 (2001).)

- Unconventional SC state

Line nodes, most likely  $d(x^2 - y^2)$  symmetry

(e.g. R. Movshovich et al., Phys. Rev. Lett. **86**, 5152 (2001).)

Izawa et al., Phys. Rev. Lett. **87**, 057002 (2001))

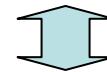
- Normal state

Non-Fermi-liquid behavior )

$$\Delta\rho \propto T, C_m/T \propto -\log T$$

probably due to strong AF fluctuations

(e.g. V.A. Sidorov et al., cond-mat/0202251,  
Shishido et al., J. Phys. Soc. Jpn. **71**, 162 (2002).)

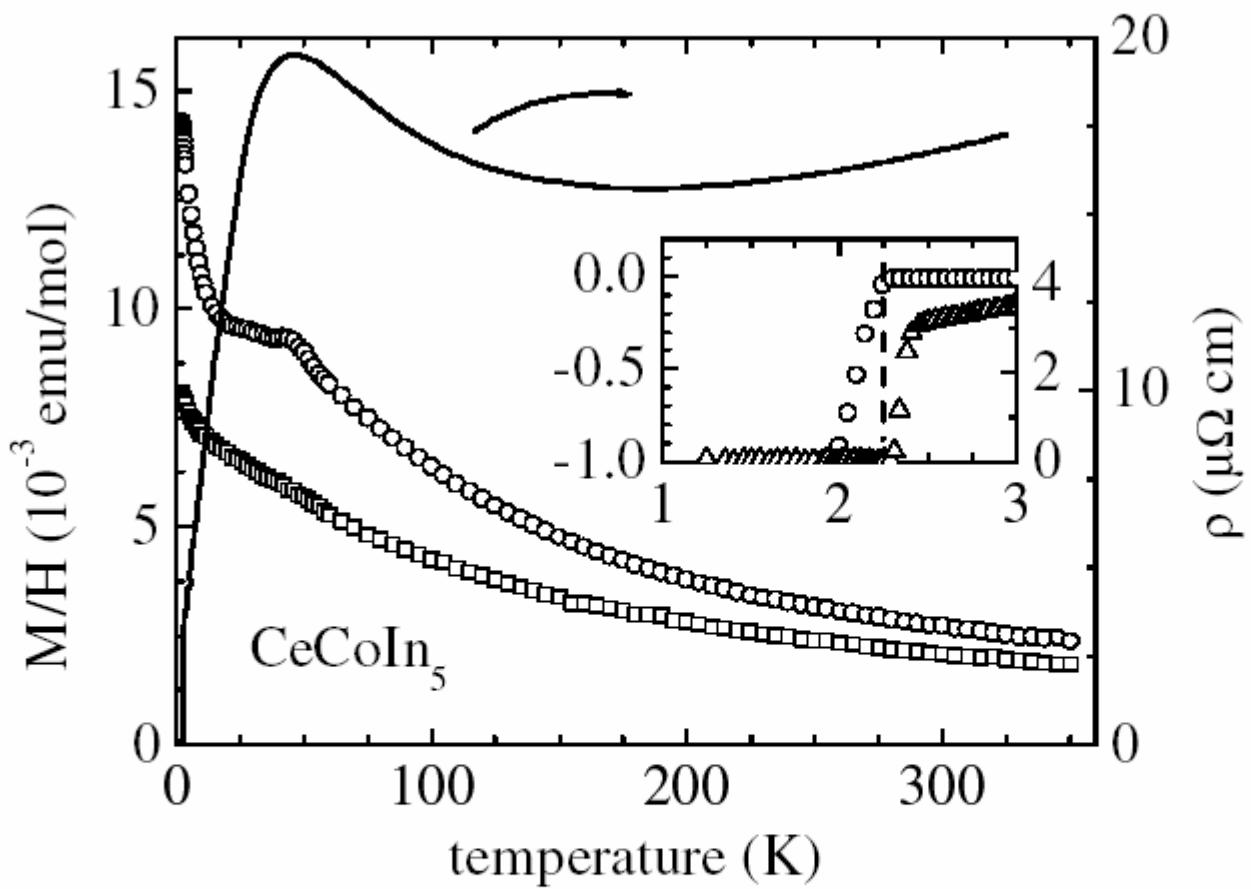


Theoretical expectations near 2D AF QCP,

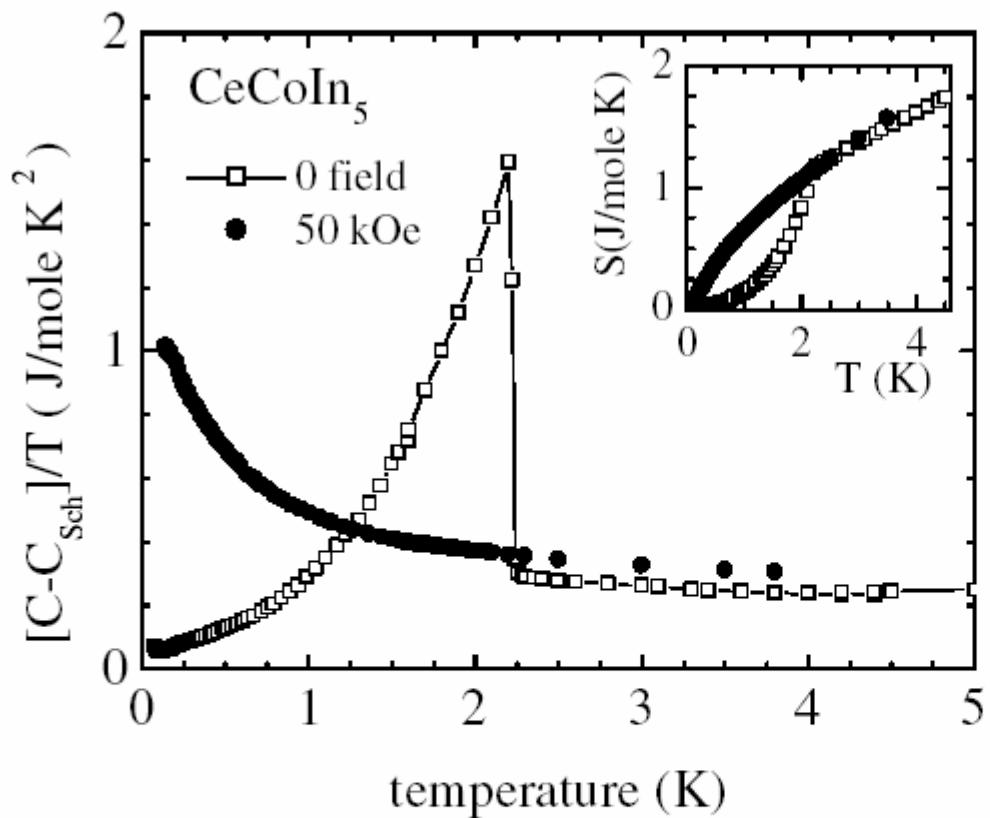
$$\Delta\rho \propto (T/T^{sf}), C_m/T \propto -\log (T/T^{sf})$$

$T^{sf}$ : a characteristic energy of spin-fluctuations

(e.g. T. Moriya and K. Ueda, Adv. Phys. **49**, 555 (2000).,  
G. R. Stewart, Rev. Mod. Phys. **73**, 797 (2001). )

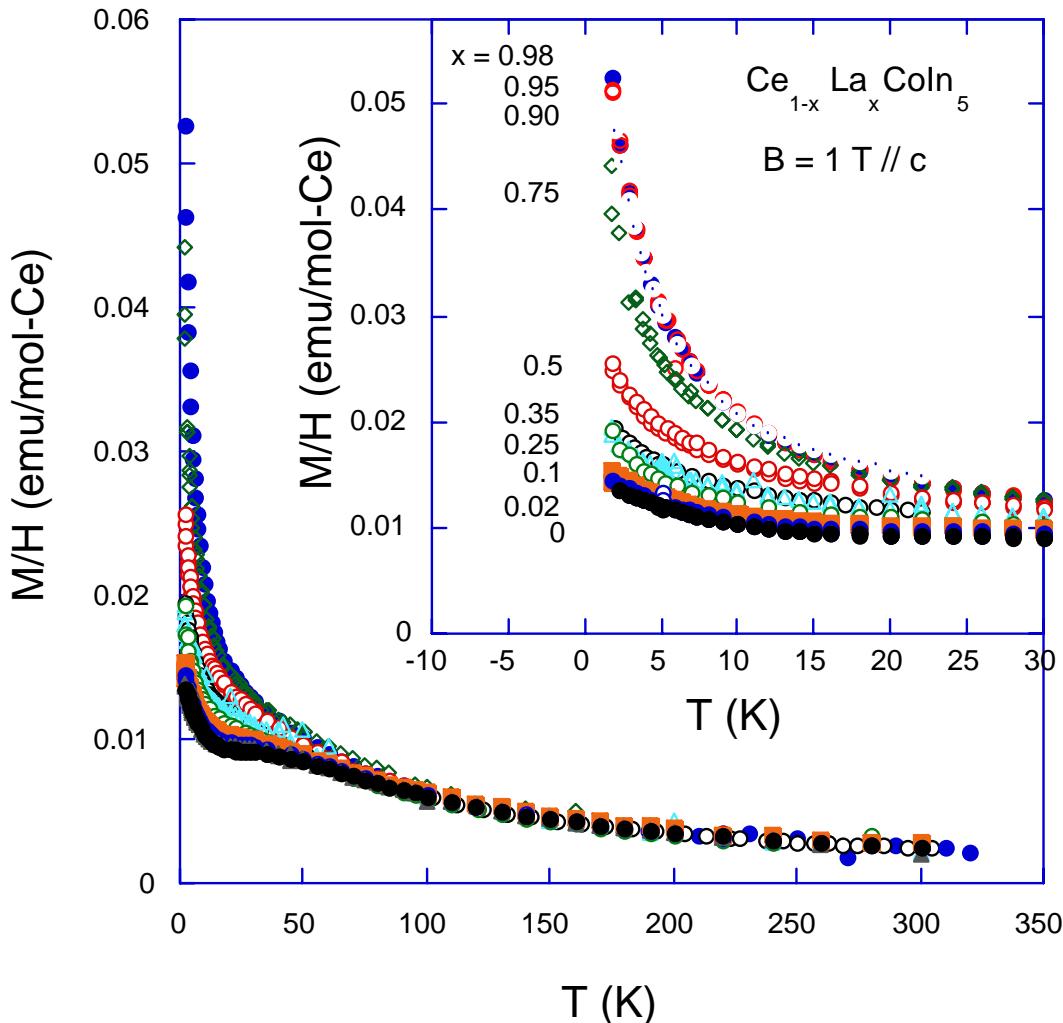


**Figure 1.** Magnetic susceptibility and electrical resistivity of CeCoIn<sub>5</sub>. Susceptibility is measured in a 1 kOe field applied parallel (circles) or perpendicular (squares) to the *c*-axis of CeCoIn<sub>5</sub> using a SQUID magnetometer. The inset shows zero-field-cooled magnetic susceptibility (circles) as a fraction of  $1/4\pi$  measured in 10 Oe and resistivity (triangles) in the vicinity of the superconducting transition.



**Figure 2.** Specific heat divided by temperature versus temperature for CeCoIn<sub>5</sub>. For both the zero-field (open squares) and 50 kOe (solid circles) data, a nuclear Schottky contribution, due to the large nuclear quadrupole moment of In, has been subtracted. The inset shows the entropy recovered as a function of temperature in the superconducting (open squares) and field-induced normal (solid circles) states.

# Systematic change in low $T$ susceptibility

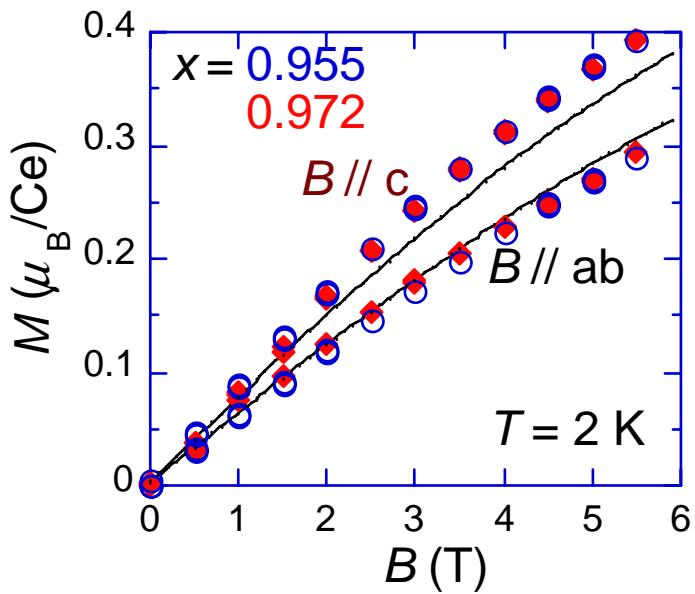
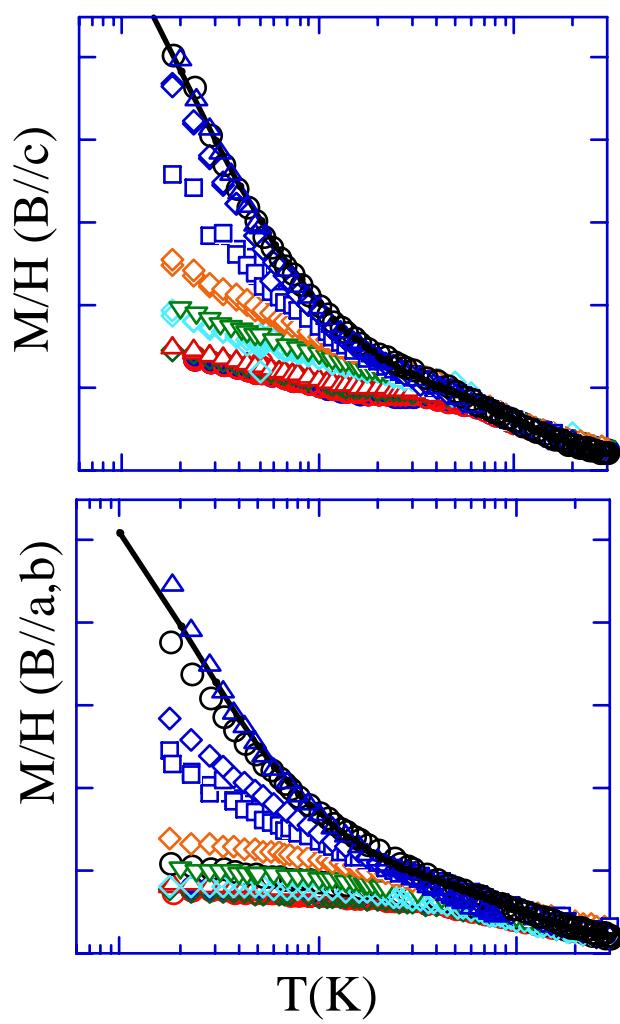


- Constant high temp.  $T_K$
- Single impurity limit:  
 $x(\text{La}) > 0.95$
- Systematic increase of  $M/H$  with La dilution at low temperatures

Possible origins:

- 1) Crystal field splitting
- 2) Kondo coupling  $T_K$
- 3) Intersite coupling

# Crystal field analyses for $\text{Ce}_{1-x}\text{La}_x\text{CoIn}_5$



197 K      $\overline{\quad}$   $\Gamma 6$       $|1/2\rangle$   
148 K      $\overline{\quad}$   $\Gamma 7^{(2)}$       $-|1/2\rangle$   
               $\overline{\quad}$   $\Gamma 7^{(1)}$

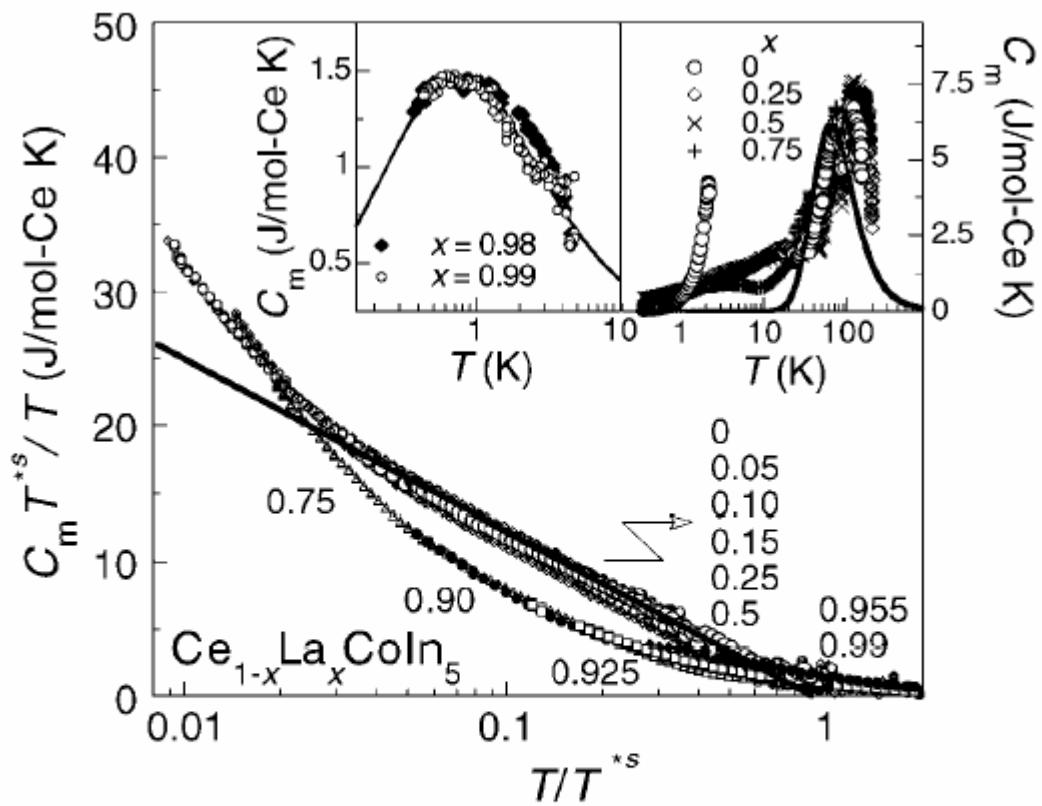


FIG. 3.  $C_m/T$  times  $T^{*s}$  vs  $T/T^{*s}$ . The solid line represents the  $-\ln T$  fit. Left inset:  $T$  dependence of  $C_m$  for  $x = 0.98$  and  $0.99$ . The solid curve is the fit to the  $S = 1/2$  Kondo impurity limit with  $T_K = 1.7$  K. Right inset:  $T$  dependence of  $C_m$ . The solid curve is the fit based on our CEF scheme.

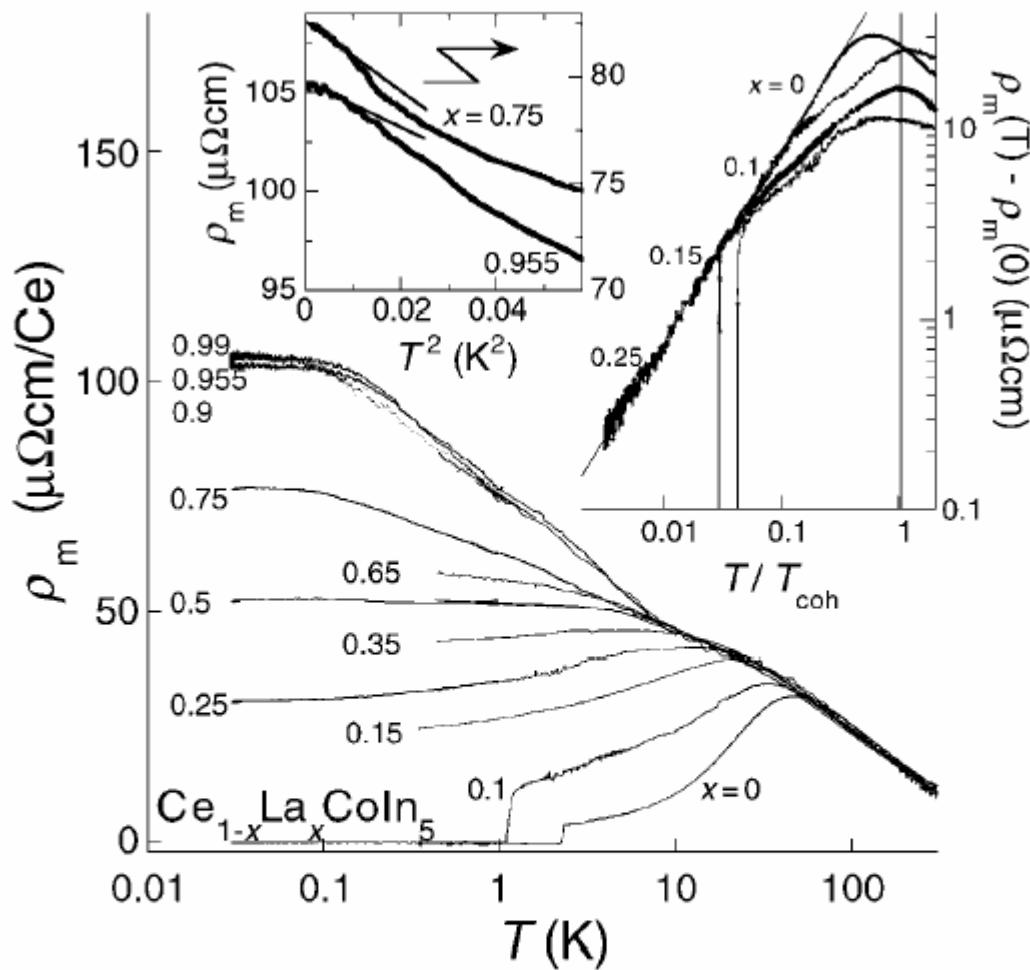
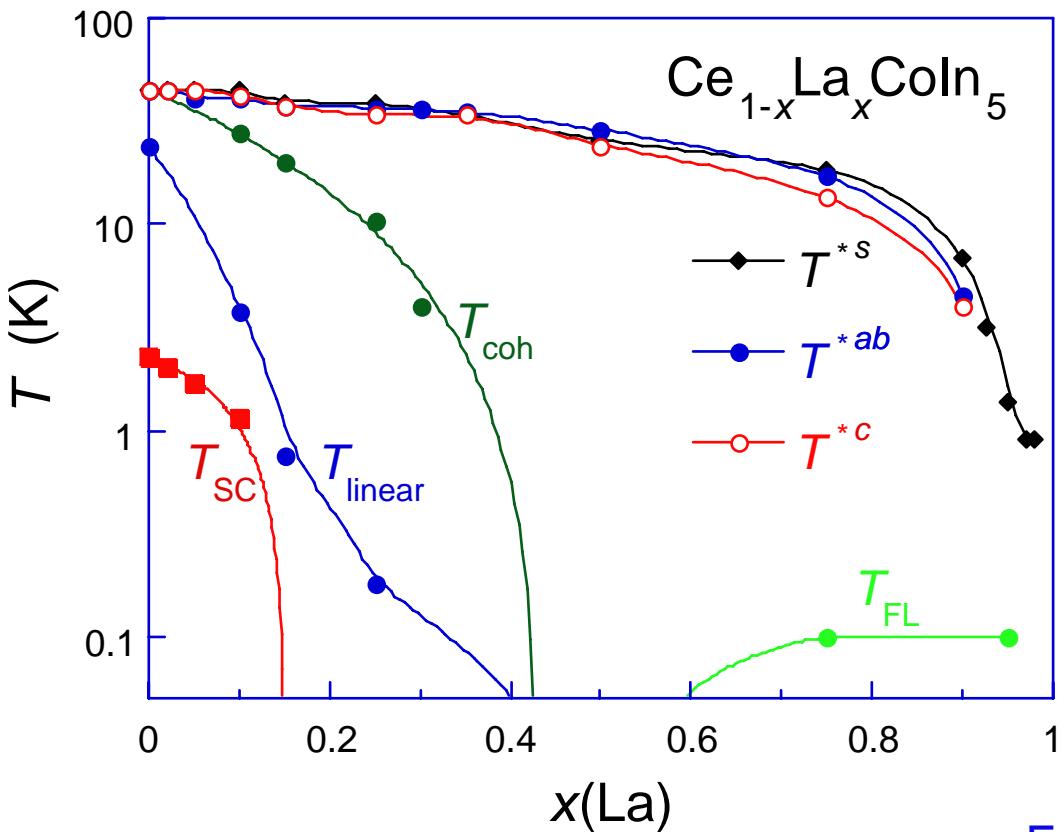


FIG. 1. Magnetic in-plane resistivity  $\rho_m$  for various  $x$  of  $\text{Ce}_{1-x}\text{La}_x\text{CoIn}_5$ . Right inset: The log-log plot for the inelastic part of  $\rho_m$  vs  $T/T_{\text{coh}}$ ; the solid line is the  $T$  linear fit and the vertical lines mark the onset of superconductivity. Left inset:  $\rho_m$  vs  $T^2$  for the incoherent regime.

# Energy scale diagram of $\text{Ce}_{1-x}\text{La}_x\text{CoIn}_5$



- 1)  $T^{*ab}$ ,  $T^{*c}$ ,  $T^{*s}$  are essentially identical.
- 2)  $T^*$  originates from the single-ion  $T_K$  at  $x \rightarrow 1$  limit.
- 3) The systematic increase should arise from intersite correlation.  
 $T_{\text{coh}} \rightarrow T^*$  at  $x \rightarrow 0$  limit.
- 4) Change in the ground state properties at around  $x = 0.5$ .

Evolution of intersite AF fluctuations similar to RVB with energy scale of  $T^*$  and correlation length of several  $a$

Basis of our analysis:  $T_K \ll T^*$  (intersite)  $\ll \Delta$  (crystal field)

1 K

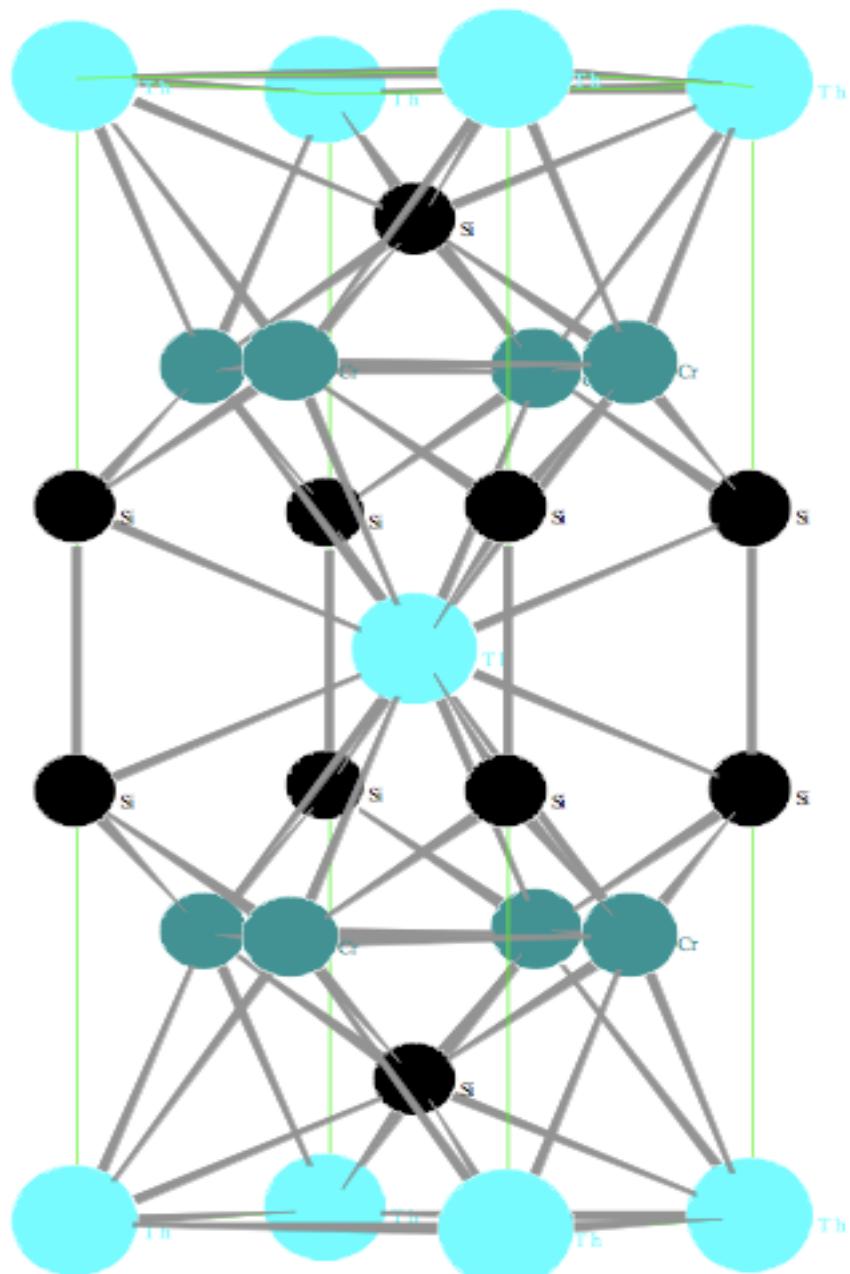
50 K

200 K

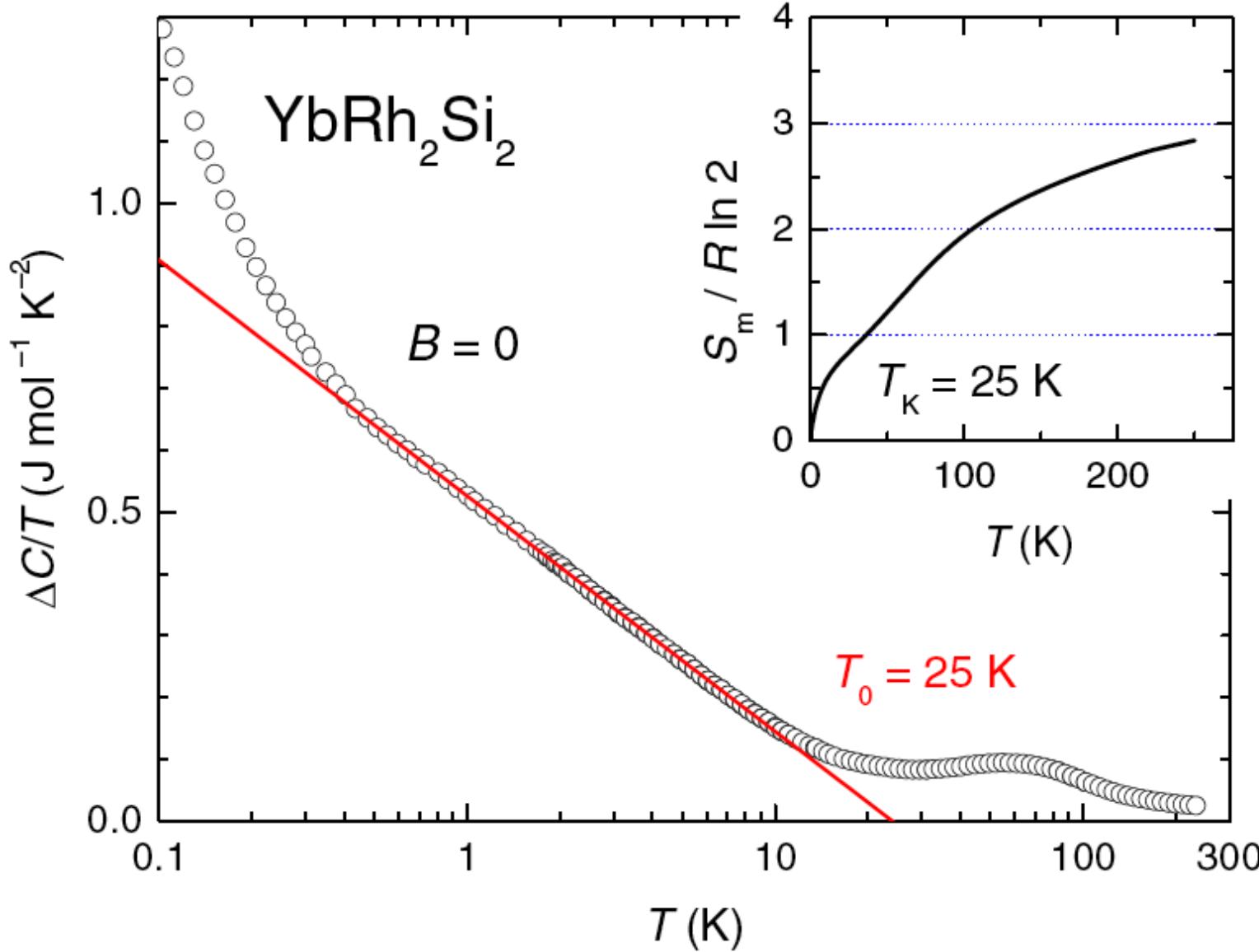
dilution in  $\text{YbRh}_2\text{Si}_2$

same trends as seen in  $\text{CeCoIn}_5$

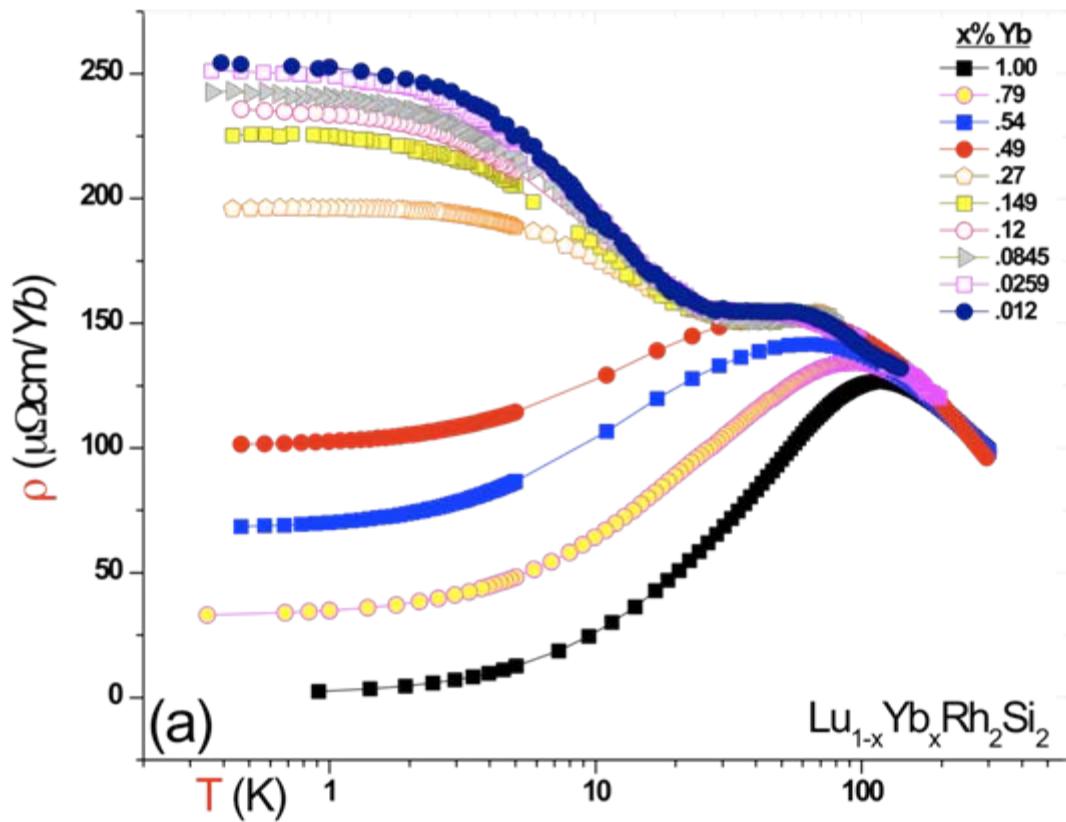
# ThCr<sub>2</sub>Si<sub>2</sub> Prototype Structure

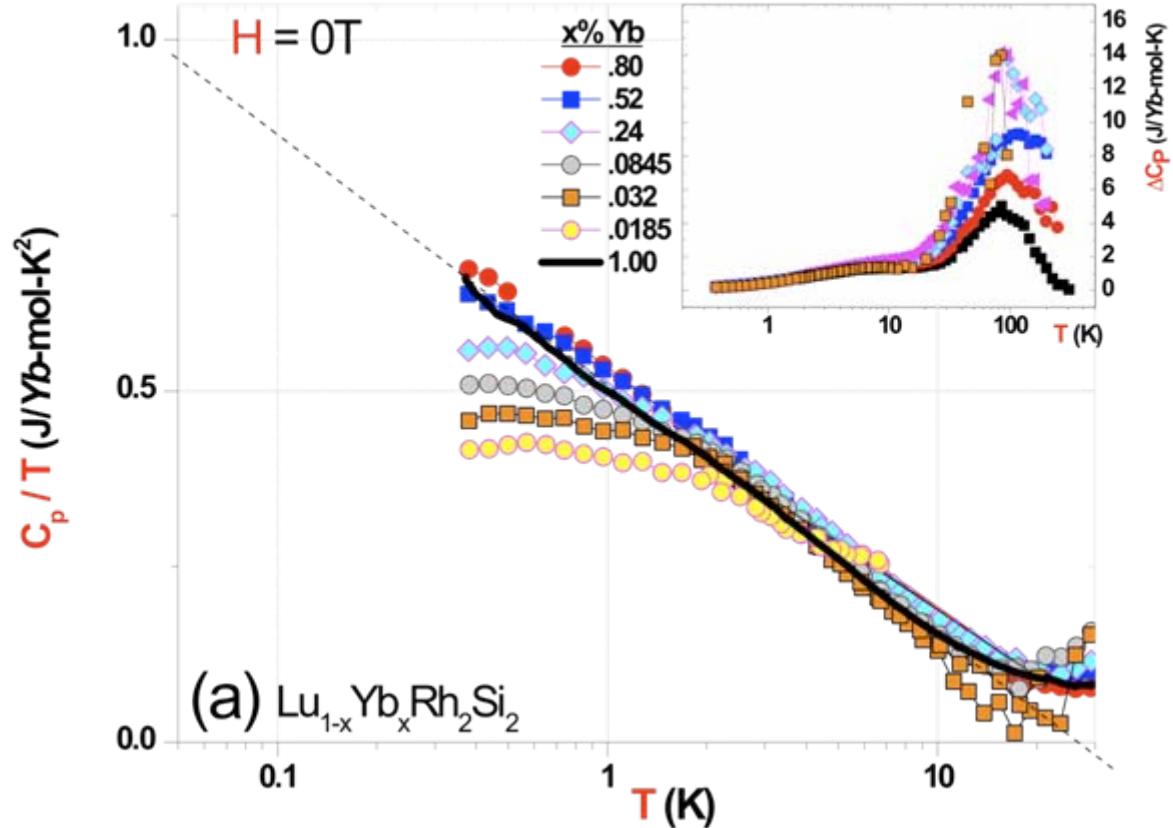


# Sommerfeld coefficient – Kondo lattice?

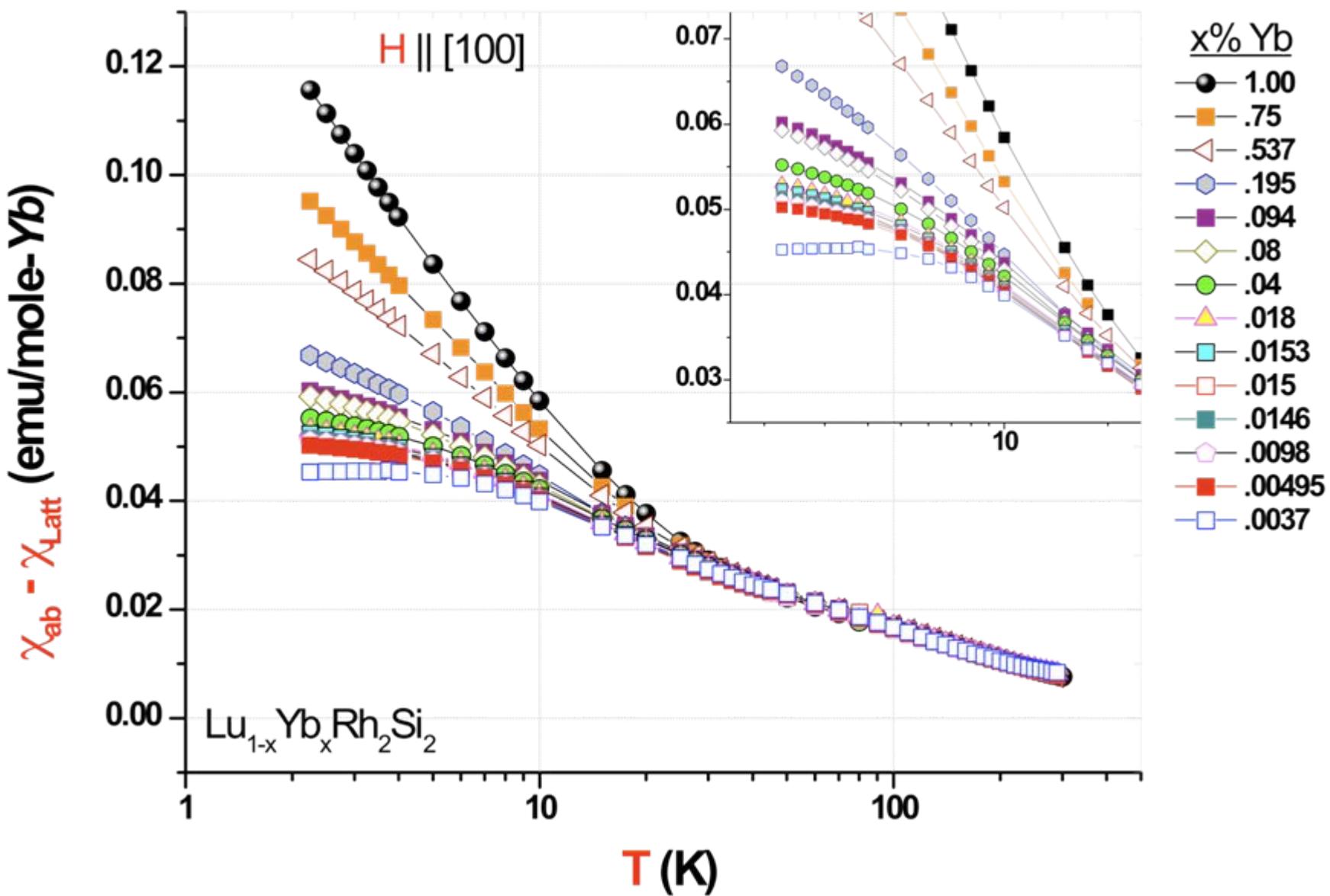


P. Gegenwart *et al.*, New J. Phys. **8**, 171 (2006).





more than 1 plate/mass



# Entropy development in quantum critical regime

$$C/T \propto \ln T$$

Typically:  $C/T = (R \ln 2 / T^*) \ln(T^*/T)$   
and  $S(T^*) = R \ln 2$

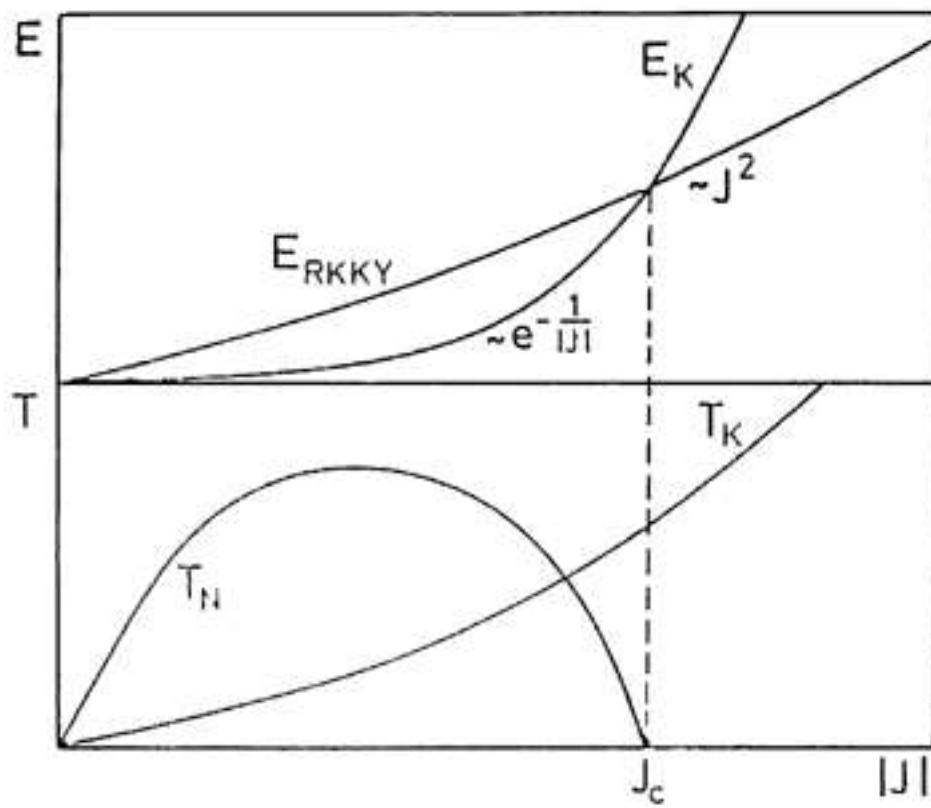
$T^*$  sets the scale for heavy Fermion physics

For heavy Fermion superconductors:

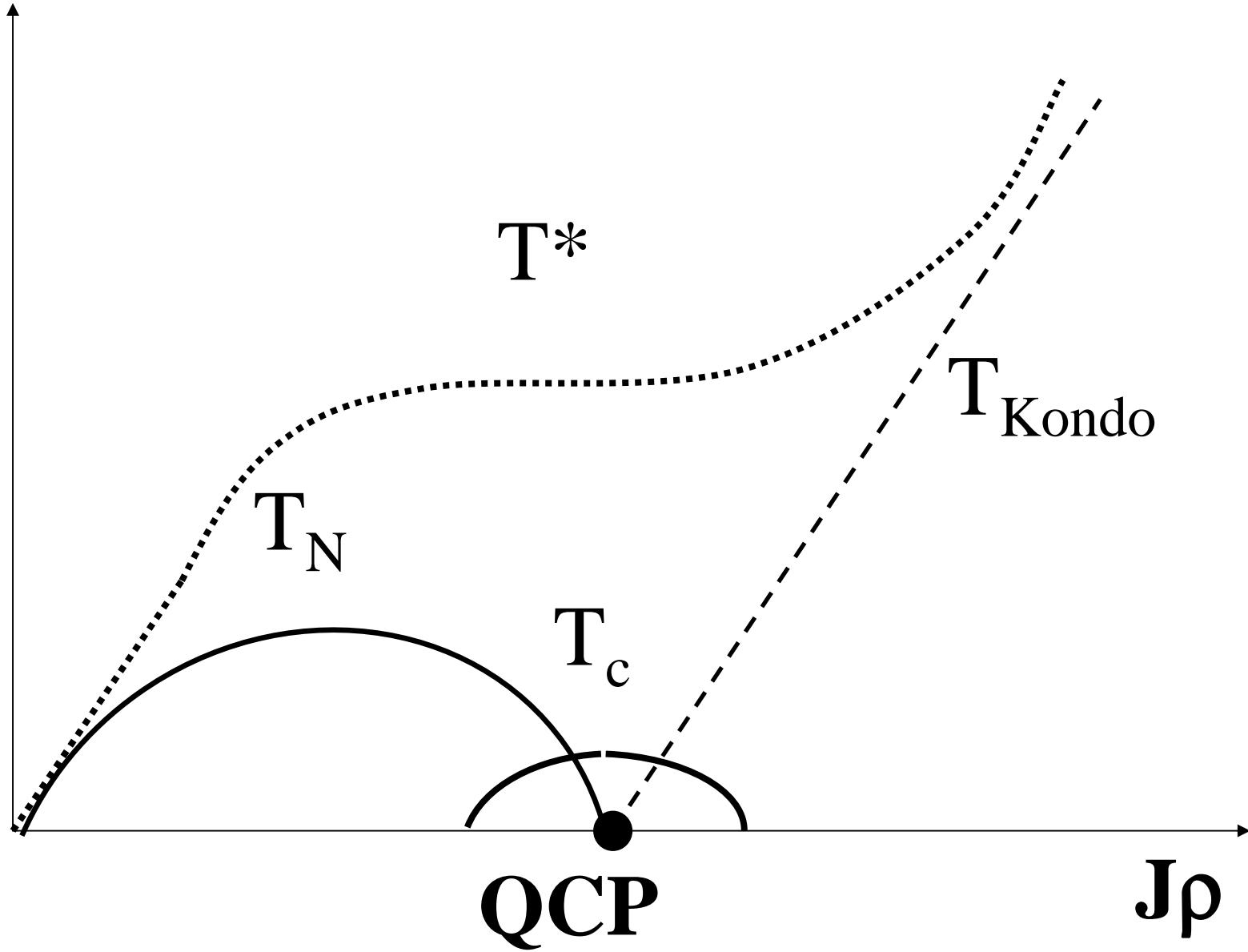
$$S(T_c) \sim 10\text{-}20\% R \ln 2 \leftrightarrow T_c/T^* \sim 1/20$$

# Source of coherence scale in dense Kondo lattice

Kondo coupling parameter ( $\rho J$ )  
determines both  $T_K$  and  $T^*$



*top - Dependences of the characteristic energies connected to the Kondo effect and the RKKY interactions as function of the coupling constant  $J$ .  
 below - Connected "phase diagram".*



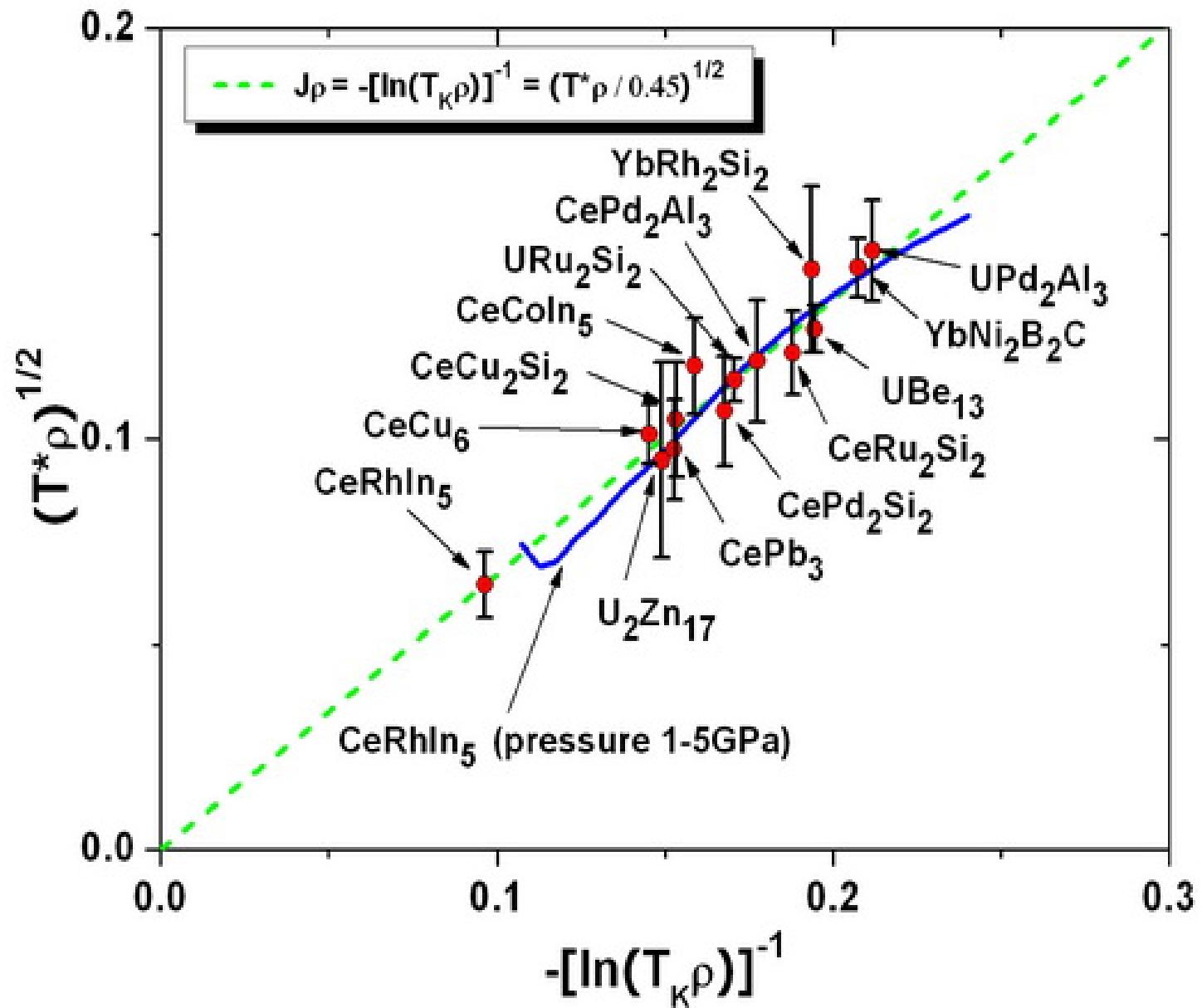
$$\text{Kondo scale: } T_K = \rho^{-1} e^{-1/J\rho}$$

$$\text{RKKY scale: } T^* = c J^2 \rho$$

$$J\rho = -1/\ln(T_K \rho) = \sqrt{c^{-1} T^* \rho}$$

**Table I. Experimental  $T^*$ ,  $T_K$  and  $\gamma$  for a variety of Kondo lattice compounds.**

Compound	$T^*$ (K)	$T_K$ (K)	$\gamma$ (mJ/mol K <sup>2</sup> )	$J\rho$	$c$	Reference
CeRhIn <sub>5</sub>	20	0.15	5.7	0.10	0.45	5,7,(H.L.)
CeCu <sub>6</sub>	35	3.5	8	0.15	0.49	8,9
U <sub>2</sub> Zn <sub>17</sub>	20	2.7	12.3	0.15	0.41	10,11,12
CeCu <sub>2</sub> Si <sub>2</sub>	75	10	4	0.15	0.47	5,13,14
CePb <sub>3</sub>	20	3	13	0.15	0.41	15,16
CeCoIn <sub>5</sub>	50	6.6	7.6	0.16	0.55	3,5,6
CePd <sub>2</sub> Si <sub>2</sub>	40	9	7.8	0.17	0.41	17,18
URu <sub>2</sub> Si <sub>2</sub>	55	12	6.5	0.17	0.45	5,19,20
CePd <sub>2</sub> Al <sub>3</sub>	40	10	9.7	0.18	0.45	21,22,23
CeRu <sub>2</sub> Si <sub>2</sub>	60	20	6.68	0.19	0.42	24,25
UBe <sub>13</sub>	55	20	8	0.19	0.43	26,27
YbRh <sub>2</sub> Si <sub>2</sub>	70	20	7.8	0.19	0.53	(Z.F.)
YbNi <sub>2</sub> B <sub>2</sub> C	50	20	11	0.21	0.47	28
UPd <sub>2</sub> Al <sub>3</sub>	60	25	9.7	0.21	0.48	23,29

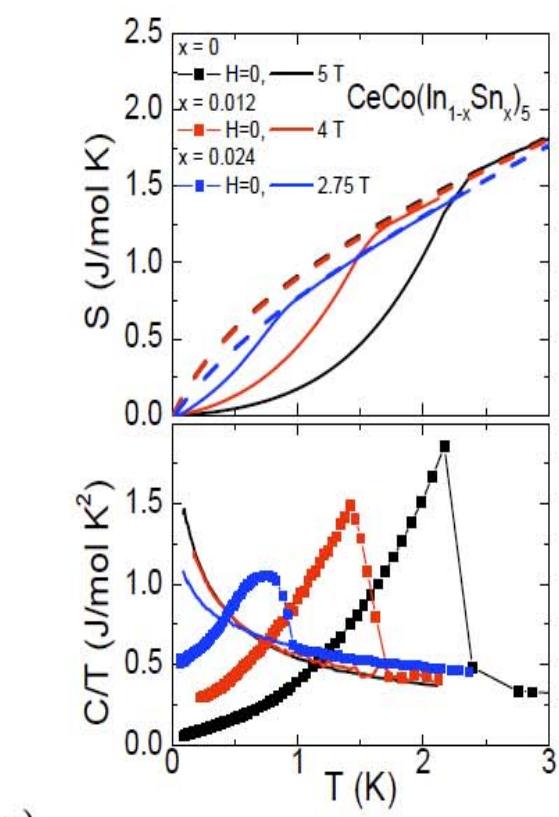
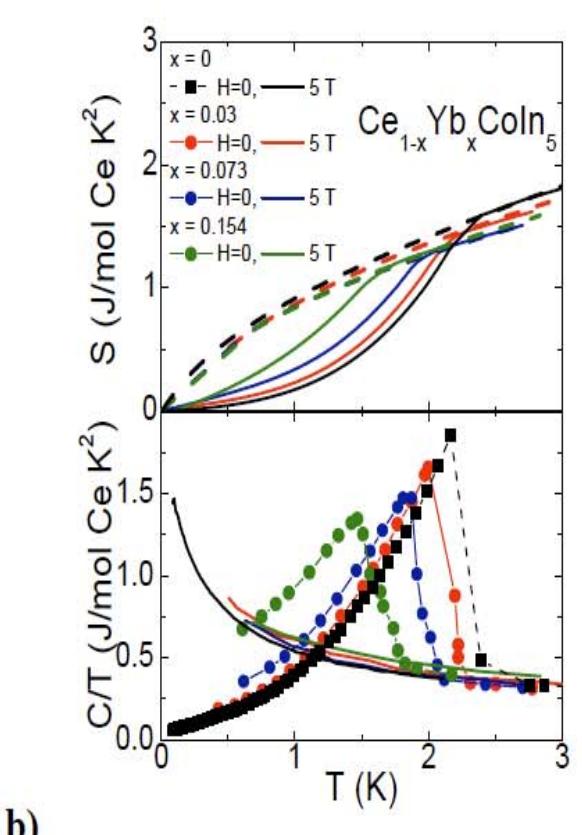
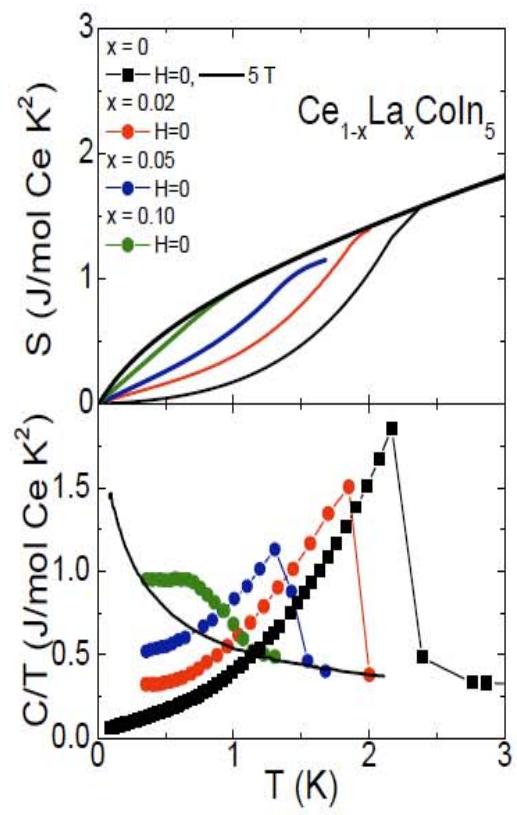


# Electronic inhomogeneity in doped dense Kondo lattice

normalized condensation energy  
in doped heavy Fermion  
superconductors shows linear  
decrease with doping

# Electronic inhomogeneity in doped dense Kondo lattice

normalized condensation energy  
in doped heavy Fermion  
superconductors shows linear  
decrease with doping



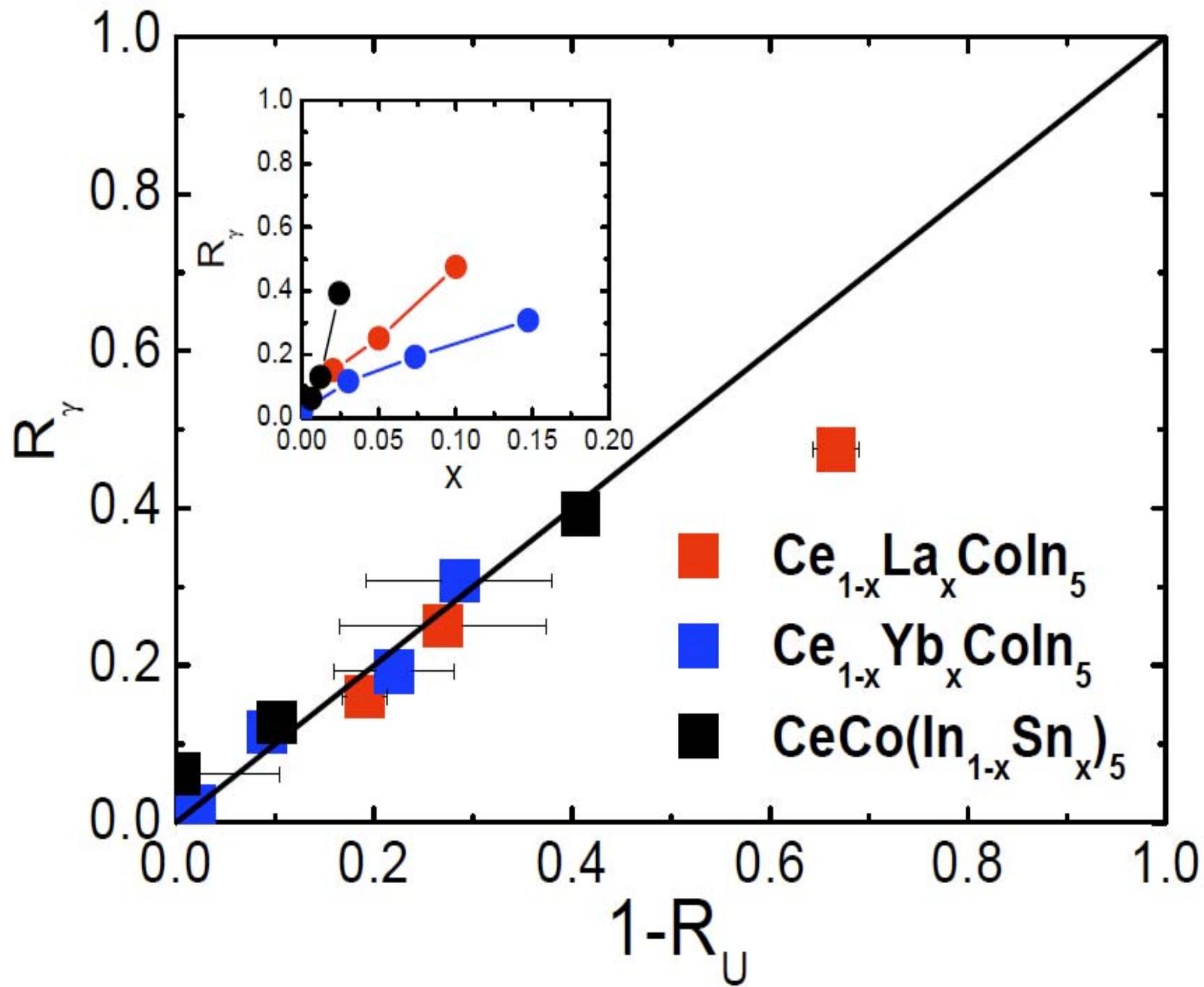
# Superconducting condensation energy

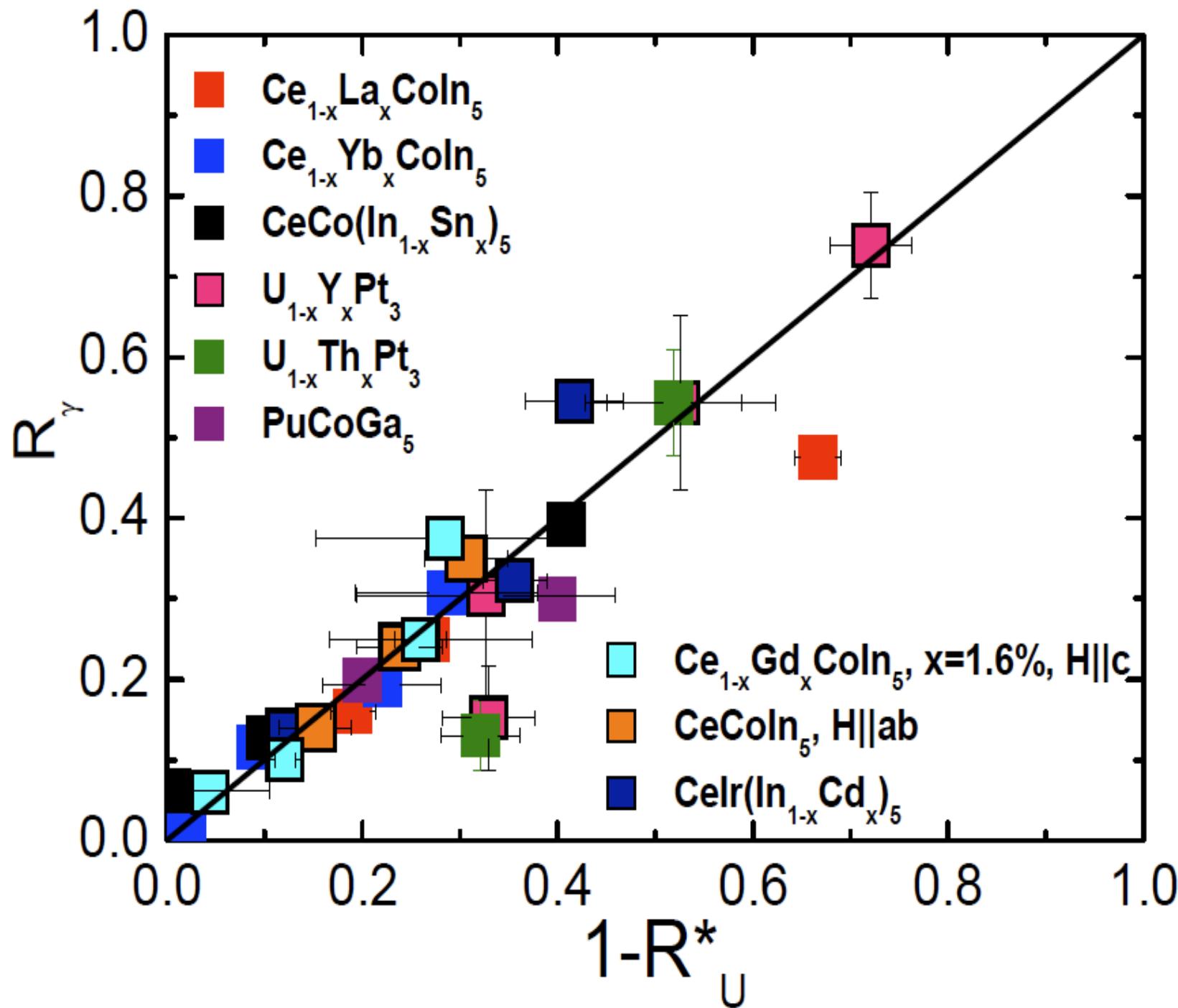
$$U_{sc} = \int (S_N - S_{sc}) dT$$

expect  $U_{sc} \propto T_c^2$

$$R_U = [U_{sc}(x)/T_c^2(x)]/[U_{sc}(0)/T_c^2(0)]$$

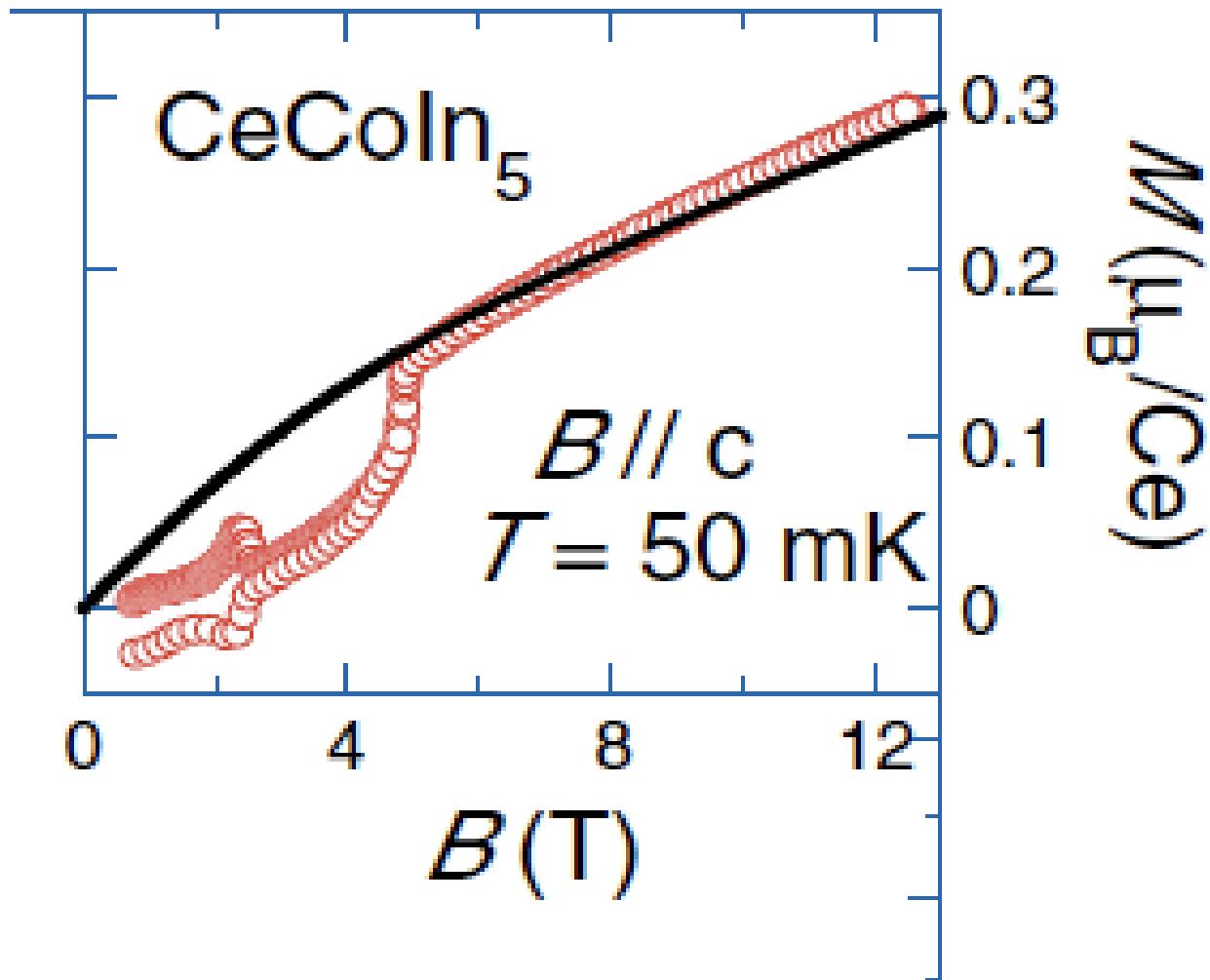
$$R_\gamma = \gamma_0/\gamma_N$$

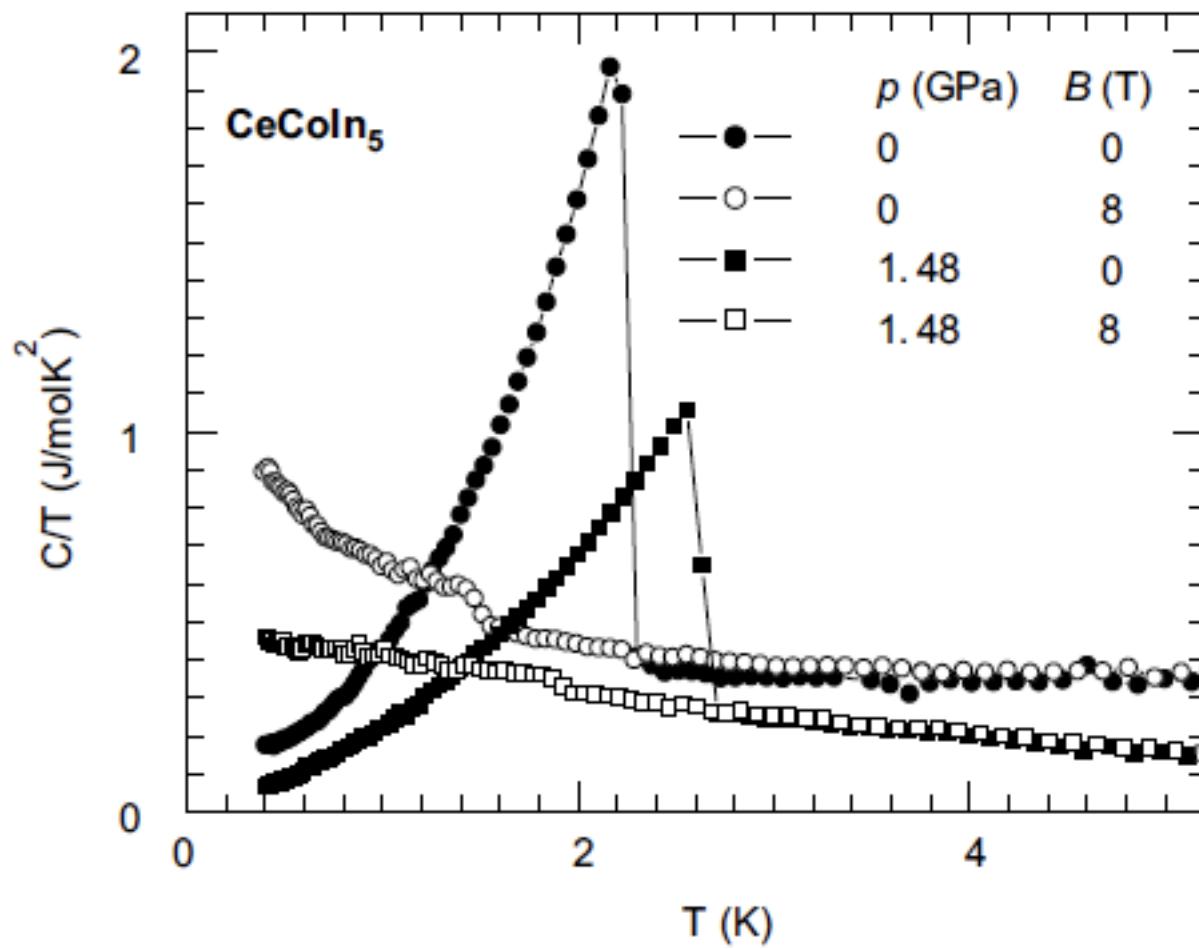


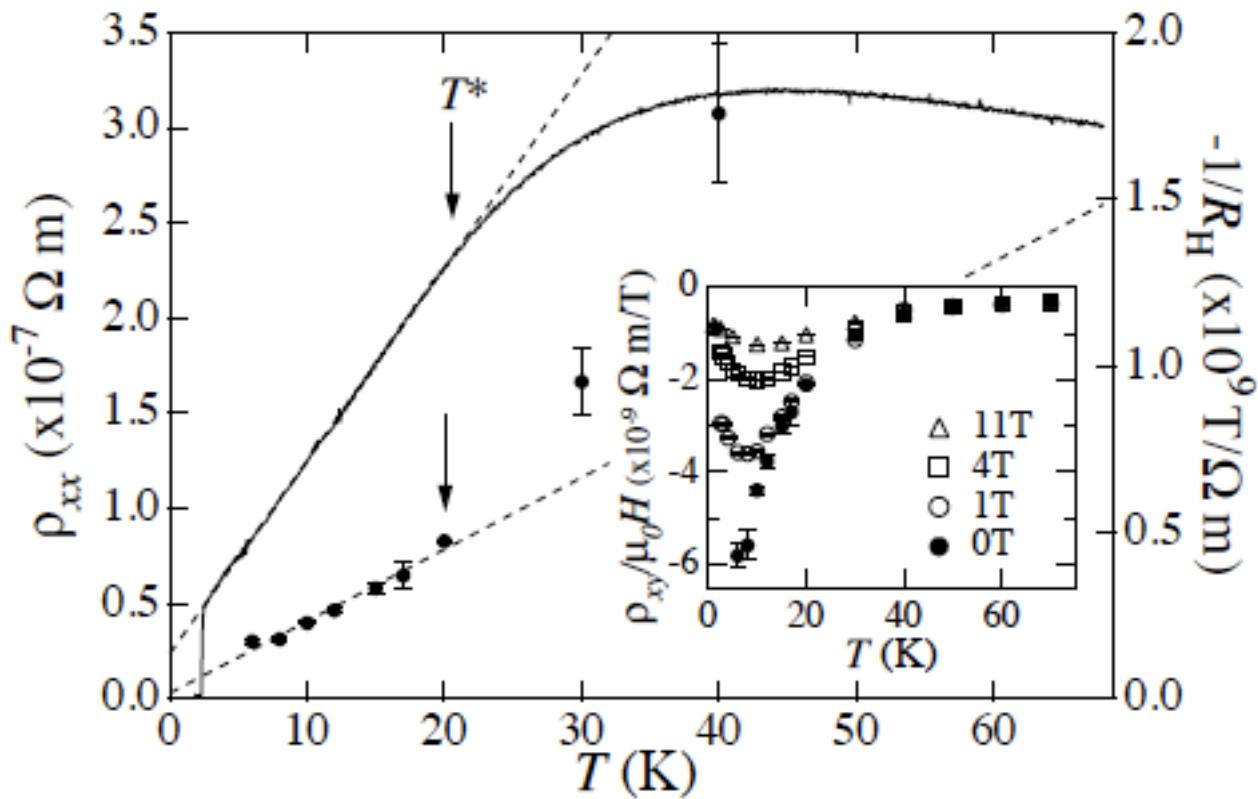


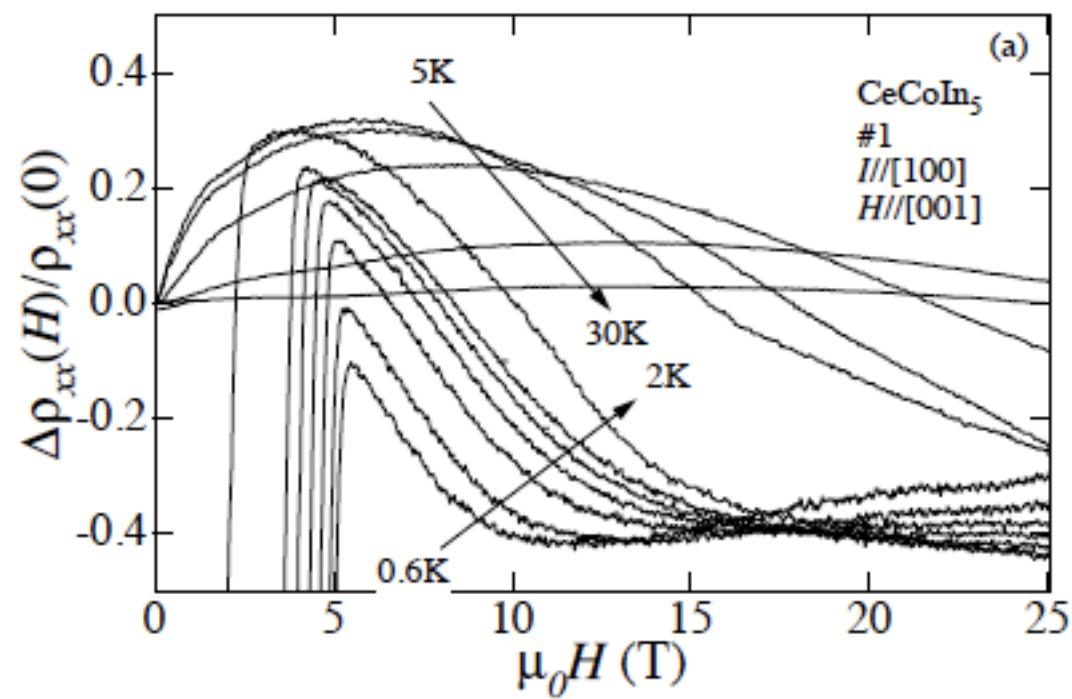
# **intrinsic Kondo impurities in pure CeCoIn<sub>5</sub>**

**low T properties consistent with  
~ 10% free Kondo centers**









# conclusions

- dense Kondo lattice scale set by Kondo single ion scale
- Kondo liquid state disrupted by percolative non-Kondo component
- similarity between doped dense Kondo and cuprate superconductors: Swiss cheese
- residual Kondo gas in stoichiometric systems