MBL AND TENSOR NETWORKS

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Xiongjie Yu, Benjamin Corregea, David Luitz, David Pekker, Vadim Oganesyan, Gil Rafeal MBL in the language of tensor networks

Outline

You can efficiently encode all 2n eigenstates using 2n small matrices! Prescription to built 2ⁿ MPS out of these matrices

Using this language, you can choose the 'best' choice for I-bits

Generate I-bits, effective Hamiltonian Look at correlation lengths of different quantities... Two correlation lengths

We can find the MPS using two new algorithms

ES-DMRG: Modified DMRG sweeping* (same algorithm as DMRG-X)

SIMPS: Energy Targeting using (H-E)⁻¹

Entanglement SaturatesP(S)Local ExcitationsETH ViolatedMobility Edge

Beyond MPS: MERA and Huse-Elser states in 2D Scaling at the transition

Area Law MBL Eigenstates: Bauer, Nayak; Eisert

* Yu, Pekker, BKC; arxiv: 1509.01244

* Vedika, Pollmann, Sondhi; arxiv: 1509.00483

Two languages for many-body localization

Hamiltonian language: I-bits

$$H = \sum_{i} \alpha_{i} \tau_{i} + \sum_{i,j} \alpha_{ij} \tau_{i} \tau_{j} + \dots$$

Wave-function language: Tensor Networks

Want a language in which to describe the eigenstates

MPS Ground State:



$$G_1 \quad G_2 \quad G_3 \quad \dots \quad G_n$$

$$E_1 \quad E_2 \quad E_3 \quad \dots \quad E_n$$

All 2ⁿ eigenstates can be generated by all combinatorial combinations of the G, E matrices.



 G_1^{\uparrow}

Clark and Pekker: arxiv:1410.2224 Chandran, Carrasquilla, Kim, Abanin, Vidal: arxiv:1410.0687





 $UHU^{\dagger} = H_D$ $U: |i\rangle \to |e_i\rangle$

MPO takes I-bit space to physical space







Let's check this....

 $\hat{H} \longrightarrow \hat{U} \longrightarrow MPO$ What's the bond dimension? U maps product

states to eigenstates.

Many such mappings

Which one we pick is important!



Conserved quantum number: $\tau_i = U\sigma_z^i U^{\dagger}$ Hamiltonian: $H_D = UHU^{\dagger}$ From this you get α_{ij}

Many ways to represent au and H and $lpha_{ij}$ are all fixed by U

In U, you get to choose which product states match to which eigenstates and the phases of the eigenstates

D bipartite matching

jacobi rotation

U Wegner flow

 $\frac{dH}{dT} = [H, [H_0, V]]$







Acquiring Eigenstates



The evolution of two algorithms...

interesting to see how our two algorithms has evolved over the years





accurate.

Other Eigenstates

New Approach: For a site produce an effective Hamiltonian H' and choose the eigenstate of H' closest to the current energy

For a site produce an effective Hamiltonian H' and choose another eigenstate.



Getting a MPS are a good representation. How do we get them?



Typical DMRG: For a site produce an effective Hamiltonian H' and solve for the ground state of H'

Dresden: May 2014

Modified DMRG: For a site produce an effective Hamiltonian H' and choose the eigenstate of H' closest to the current energy of your state.



* Also time evolution variants of these; easier to 'analyze' but general experience is diagonalization approach tends to be more accurate.

Other Eigenstates

New Approach: For a site produce an effective Hamiltonian H' and choose the eigenstate of H' closest to the current energy

For a site produce an effective Hamiltonian H' and choose another eigenstate.



$(H-E)^2$ Entanglement Barrier



SIMPS $(H-E)^{-1}$





ES DMRG

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Modified DMRG: For a site produce an effective Hamiltonian H' and choose the eigenstate of H' closest to the current energy of your state.



Does it work?

N=30

W=4,5

P(S)

0.0

<u>ග</u> 0.100

0.010

0.001

 10^{-4}

0.0

0.2

10

The question: Do you get an eigenstate?

S

0.2



λ

S

How well does it work?



How does entanglement scale?





ETH













Is their any hope for two-dimensions?

Huse-Elser states



subadditivity







Conclusion

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We can find the MPS using two new algorithms ES-DMRG: Modified DMRG sweeping* (same algorithm as DMRG-X) SIMPS: Energy Targeting using (H-E)⁻¹

Beyond MPS: MERA and Huse-Elser states in 2D

Identifying the transition

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