



# Trapped Ions: Condensed Matter From The Bottom Up

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INSTITUTE

University of Maryland

Boris  
2005

## More Is Different

Broken symmetry and the nature of the hierarchical structure of science.

P. W. Anderson

The reductionist hypothesis may still be a topic for controversy among philosophers, but among the great majority of active scientists I think it is accepted without question. The workings of our minds and bodies, and of all the animate or inanimate matter of which we have any detailed knowledge, are assumed to be controlled by the same set of fundamental laws, which except under certain extreme conditions we feel we know pretty well.

planation of phenomena in terms of known fundamental laws. As always, distinctions of this kind are not unambiguous, but they are clear in most cases. Solid state physics, plasma physics, and perhaps also biology are extensive. High energy physics and a good part of nuclear physics are intensive. There is always much less intensive research going on than extensive. Once new fundamental laws are discovered, a large and ever increasing activity begins in order to apply the discoveries to hitherto unexplained phenomena. Thus, there are two dimensions to basic research. The frontier of science extends all

less relevance they seem to have to the very real problems of the rest of science, much less to those of society.

The constructionist hypothesis breaks down when confronted with the twin difficulties of scale and complexity. The behavior of large and complex aggregates of elementary particles, it turns out, is not to be understood in terms of a simple extrapolation of the properties of a few particles. Instead, at each level of complexity entirely new properties appear, and the understanding of the new behaviors requires research which I think is as fundamental in its nature as any other. That is, it seems to me that one may array the sciences roughly linearly in a hierarchy, according to the idea: The elementary entities of science X obey the laws of science Y.

X	Y
solid state or many-body physics	elementary particle physics
chemistry	many-body physics
molecular biology	chemistry
cell biology	molecular biology
•	•
•	•
•	•

**T**rapped Ion Spin Hamiltonian Engineering

**G**round states and Adiabatic Protocols

**D**ynamics

Many-Body Spectroscopy

Propagation of Excitations: Lieb-Robinson

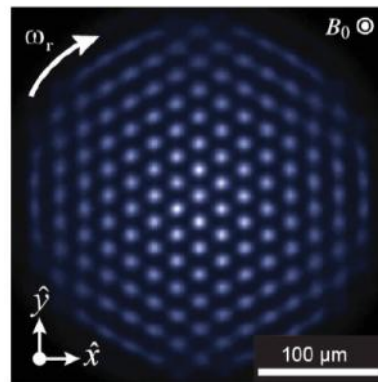
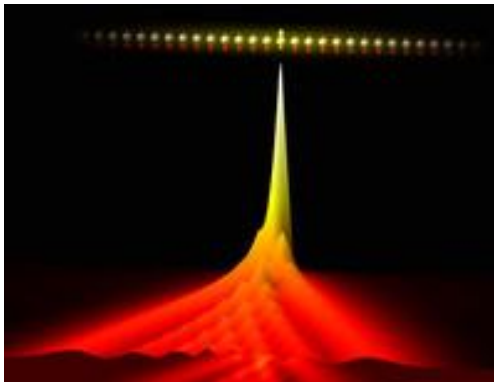
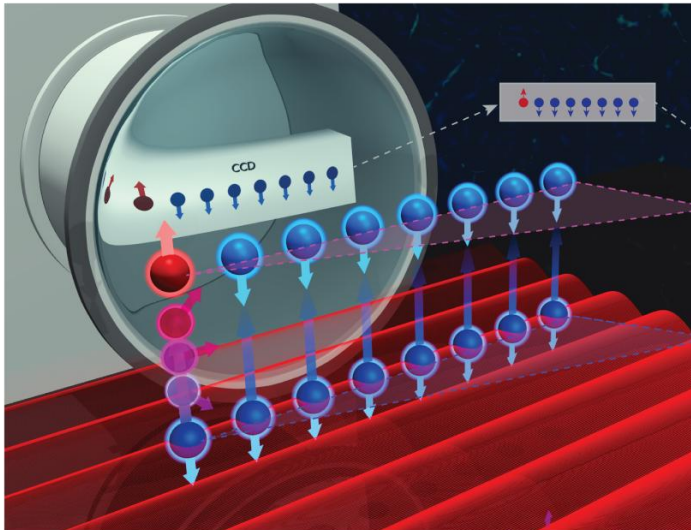
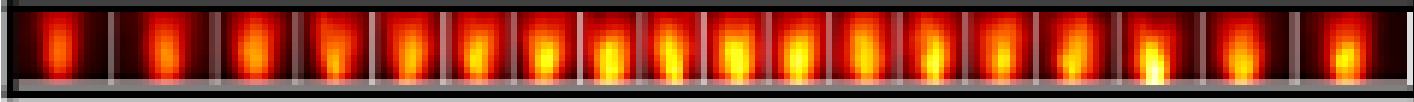
Prethermalization

Many-Body Localization

**S**pin-1

**E**xtending to  $N \sim 100$  spins and beyond

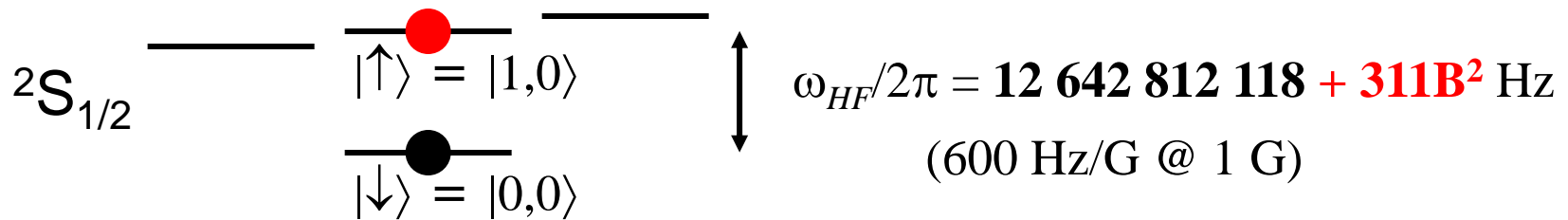
# Trapped Atomic Ions: Spin Models



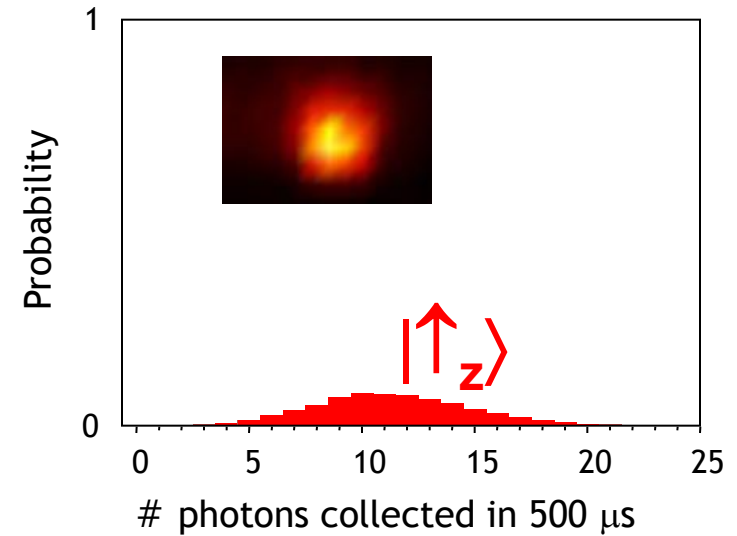
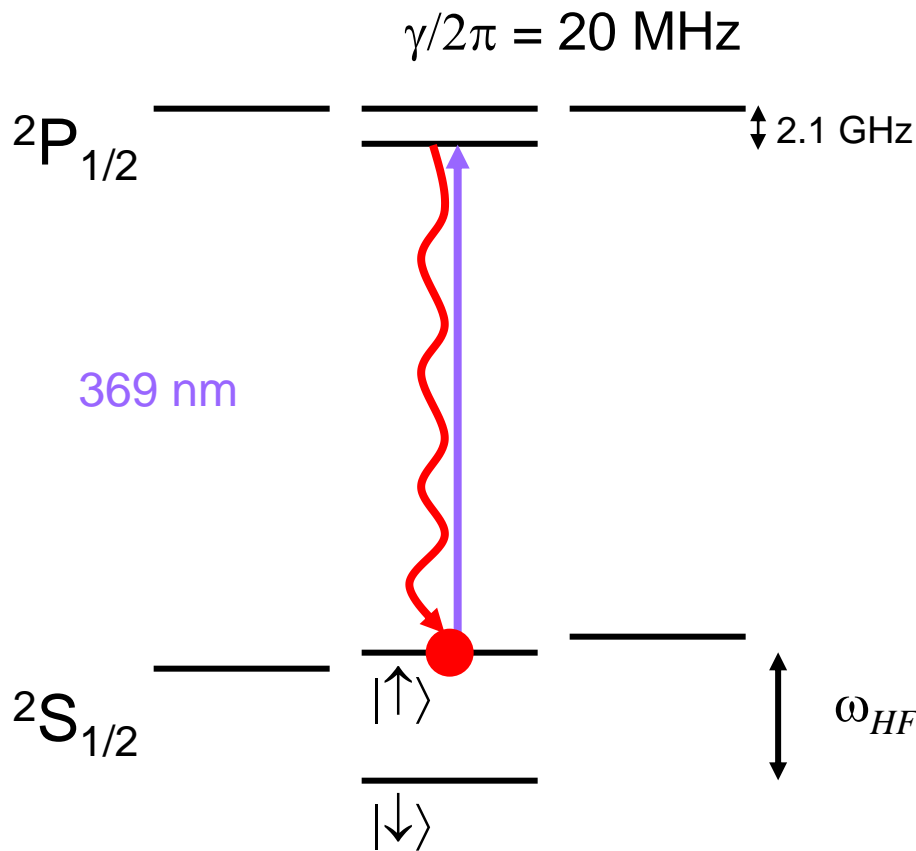
Porras and Cirac, PRL 92, 207901 (2004)  
Deng, Porras, Cirac, PRA 72, 063407 (2005)  
Taylor and Calarco, PRA 78, 062331 (2008)

- A. Friedenauer *et al.*, Nat. Phys. 4, 757 (2008)
- K. Kim *et al.*, PRL 102, 250502 (2009)
- K. Kim *et al.*, Nature 465, 590 (2010)
- E. Edwards *et al.*, PRB 82, 060412 (2010)
- J. Barreiro *et al.*, Nature 470, 486-491 (2011)
- R. Islam *et al.*, Nature Comm. 2, 377 (2011)
- B. Lanyon *et al.*, Science 334, 57 (2011)
- J. Britton *et al.*, Nature 484, 489 (2012)
- A. Khromova *et al.*, PRL 108, 220502 (2012)
- R. Islam *et al.*, Science 340, 583 (2013)
- P. Richerme *et al.*, PRL 111, 100506 (2013)
- P. Richerme *et al.*, PRA 88, 012334 (2013)
- P. Richerme *et al.*, Nature 511, 198 (2014)
- P. Jurcevic *et al.*, Nature 511, 202 (2014)
- C. Senko *et al.*, Science 345, 430 (2014)
- P. Jurcevic *et al.*, ArXiv 1505.02066 (2015)
- J. Smith *et al.*, ArXiv 1508.07026 (2015)

# $^{171}\text{Yb}^+$ hyperfine spin



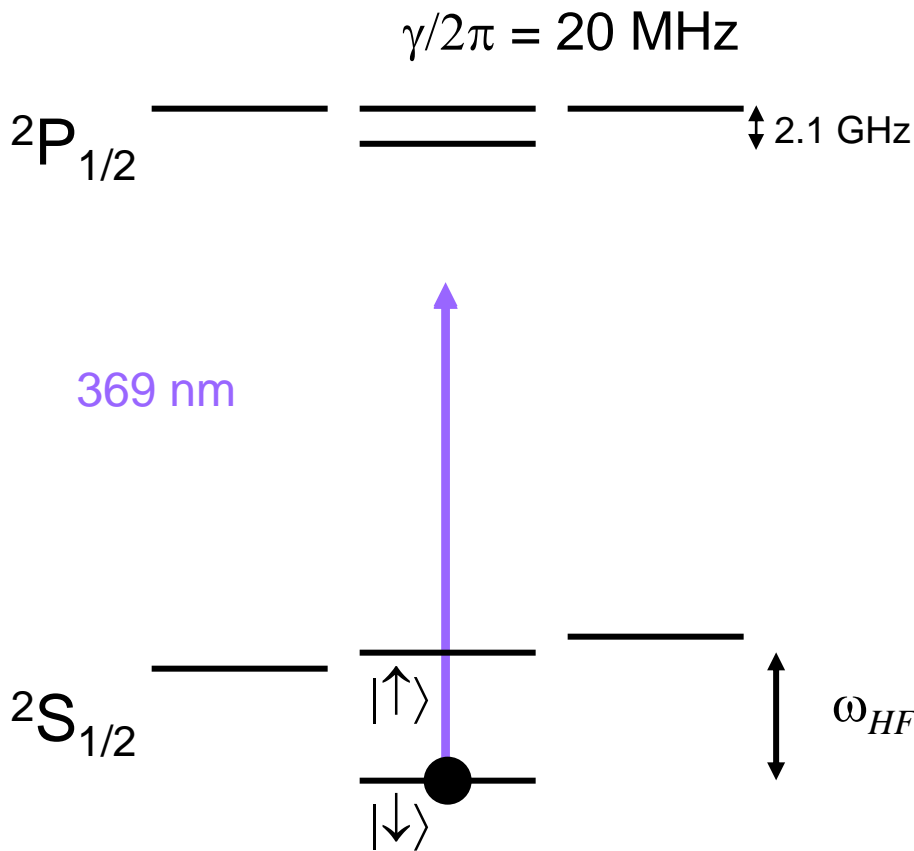
# $^{171}\text{Yb}^+$ spin detection



$$\omega_{HF}/2\pi = 12\,642\,812\,118 + 311B^2 \text{ Hz}$$

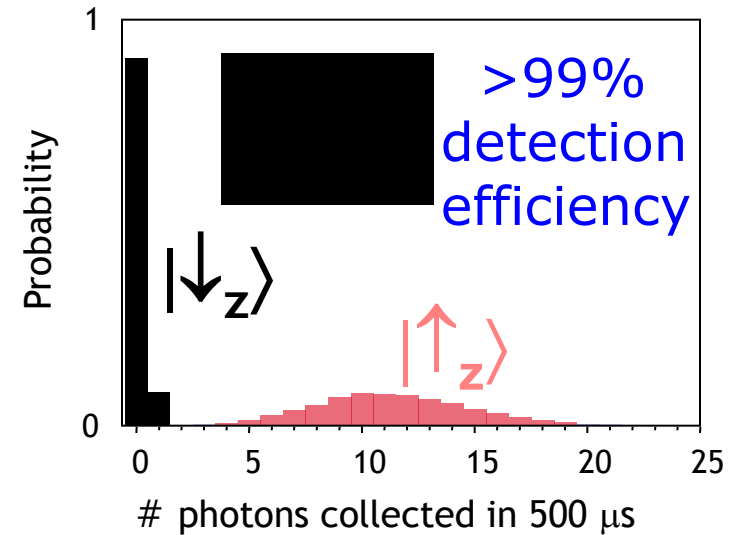
(600 Hz/G @ 1 G)

# $^{171}\text{Yb}^+$ spin detection



$$\omega_{HF}/2\pi = 12\,642\,812\,118 + 311B^2 \text{ Hz}$$

(600 Hz/G @ 1 G)



# $^{171}\text{Yb}^+$ spin manipulation

$^2\text{P}_{3/2}$   $\gamma/2\pi = 20 \text{ MHz}$

$^2\text{P}_{1/2}$   $\Delta = 33 \text{ THz}$

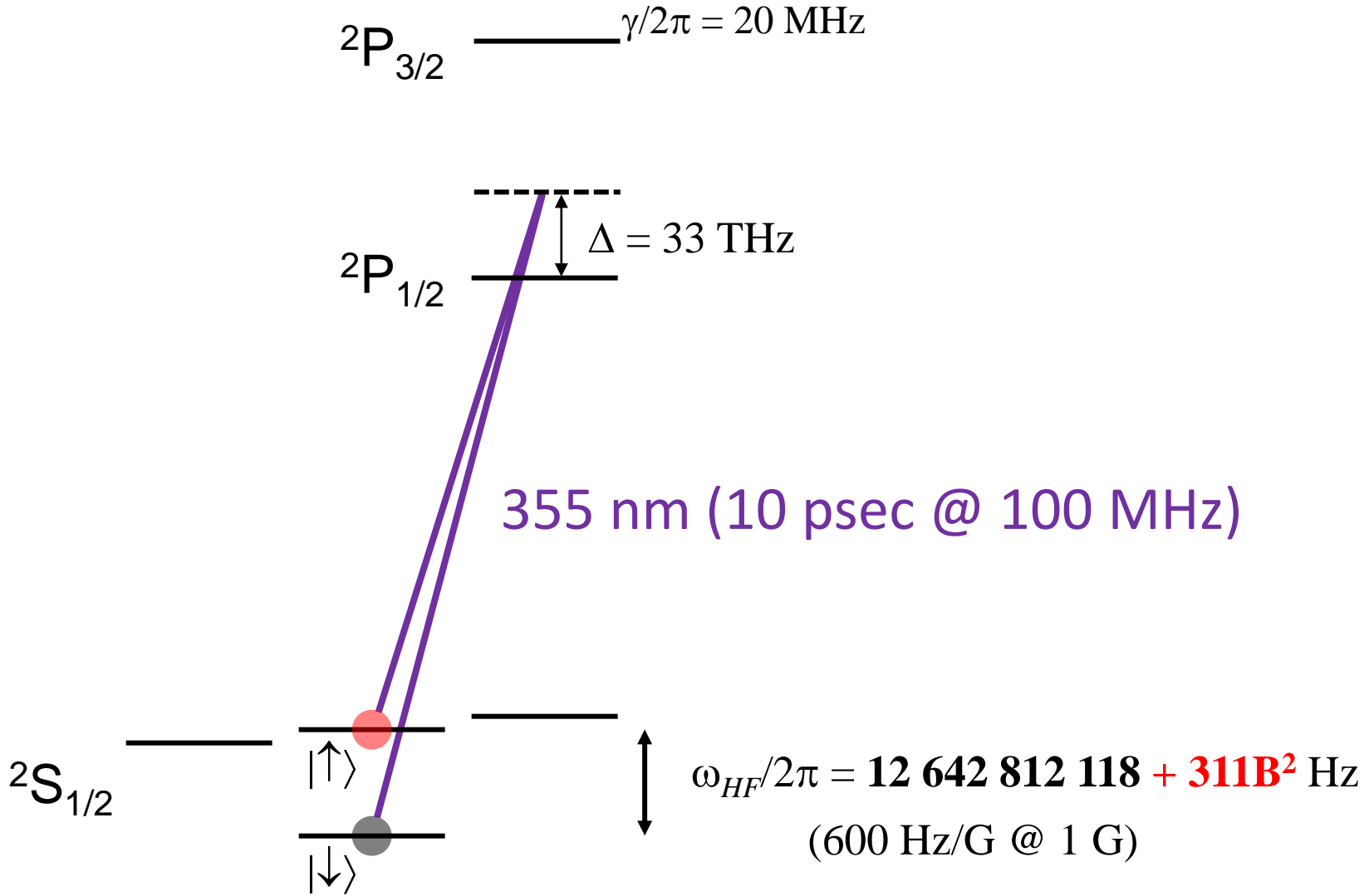
355 nm (10 psec @ 100 MHz)

$^2\text{S}_{1/2}$

$|\uparrow\rangle$

$|\downarrow\rangle$

$\omega_{HF}/2\pi = 12\,642\,812\,118 + 311B^2 \text{ Hz}$   
(600 Hz/G @ 1 G)





# Entangling Trapped Ion Spins



“dipole-dipole coupling”

$$\Delta E = \frac{e^2}{\sqrt{r^2 + \delta^2}} - \frac{e^2}{r} \approx -\frac{(e\delta)^2}{2r^3}$$

$\delta \sim 10 \text{ nm}$   
 $e\delta \sim 500 \text{ Debye}$

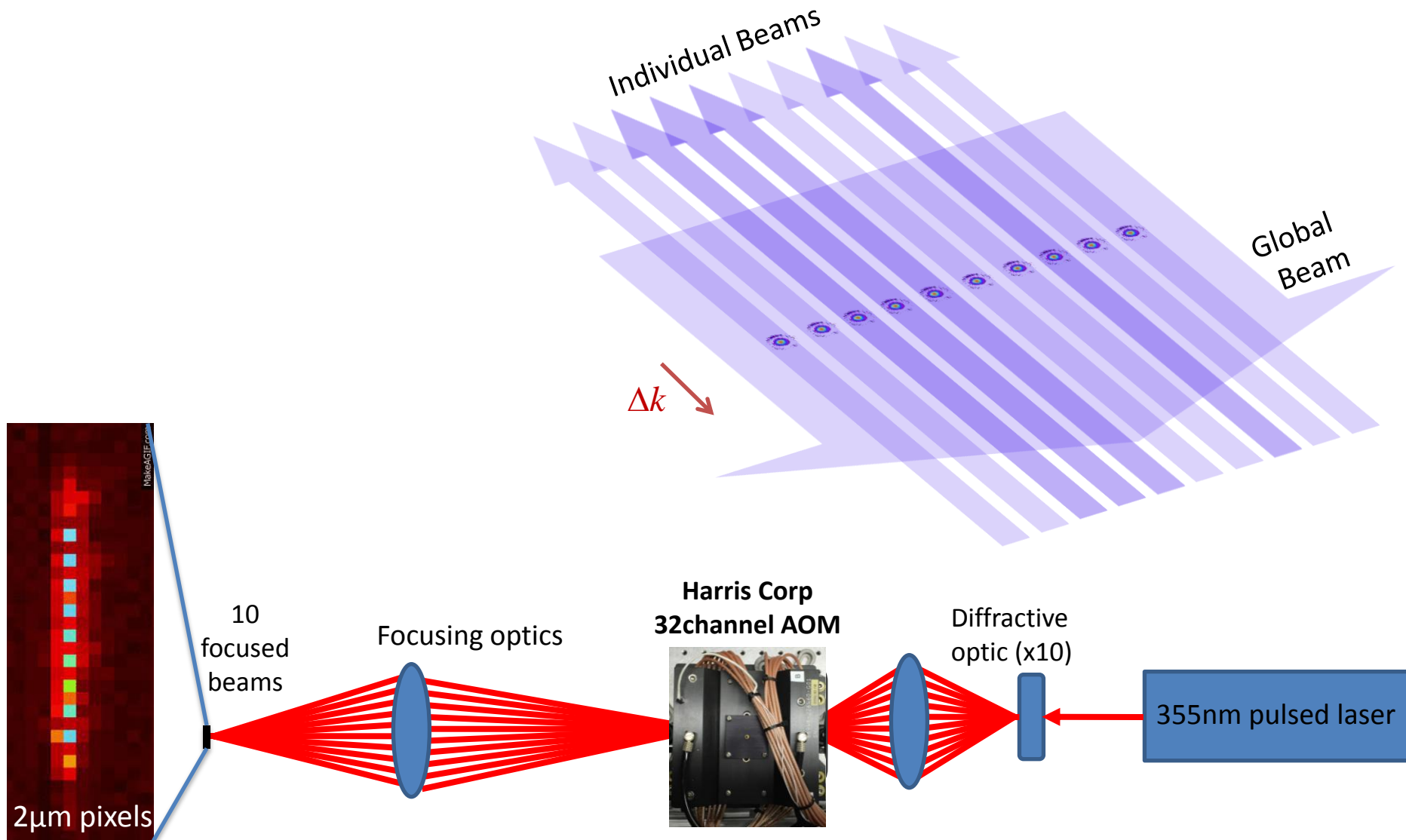
$$\begin{aligned} |\downarrow\downarrow\rangle &\rightarrow |\downarrow\downarrow\rangle \\ |\downarrow\uparrow\rangle &\rightarrow e^{-i\varphi} |\downarrow\uparrow\rangle \\ |\uparrow\downarrow\rangle &\rightarrow e^{-i\varphi} |\uparrow\downarrow\rangle \\ |\uparrow\uparrow\rangle &\rightarrow |\uparrow\uparrow\rangle \end{aligned}$$

$$\varphi = \frac{\Delta E t}{\hbar} = \frac{e^2 \delta^2 t}{2\hbar r^3} = \frac{\pi}{2}$$

for full  
entanglement

Cirac and Zoller (1995)  
 Mølmer & Sørensen (1999)  
 Solano, de Matos Filho, Zagury (1999)  
 Milburn, Schneider, James (2000)

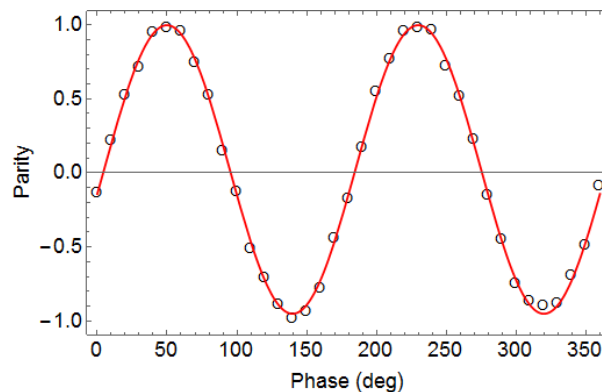
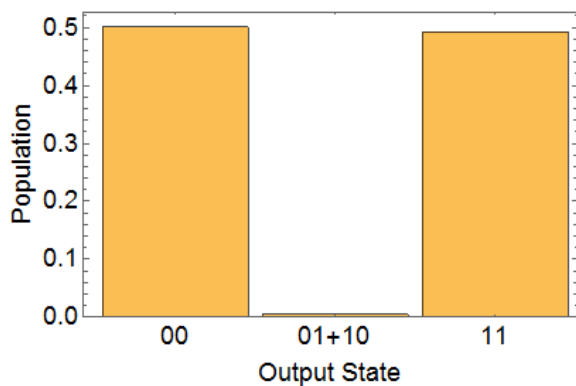
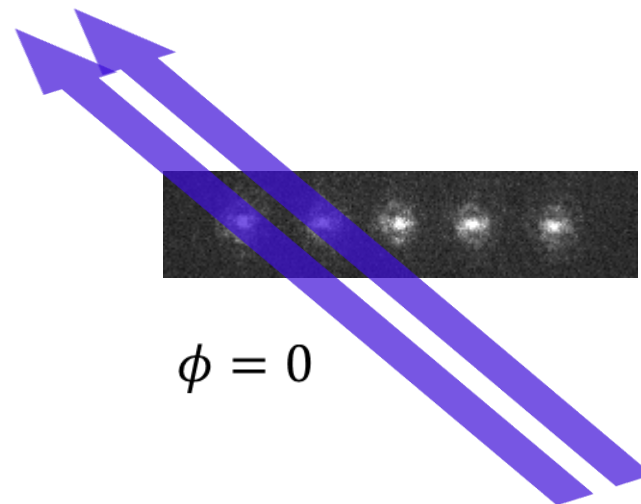
# Gates within a single crystal



T. Choi, et al., PRL 112, 19502 (2014)  
S. Debnath, et al., in preparation (2015)

# Ising (XX) gate [1,2]

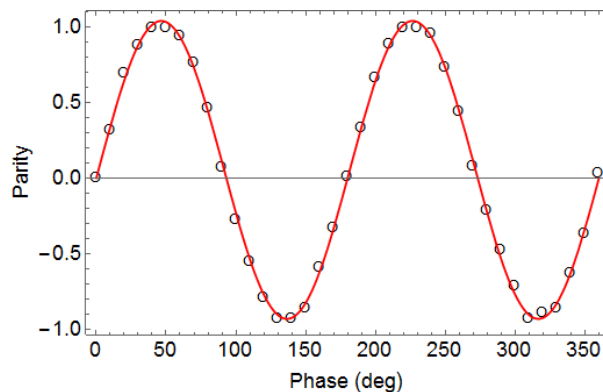
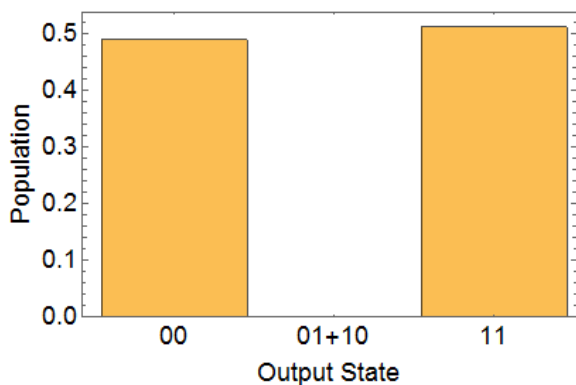
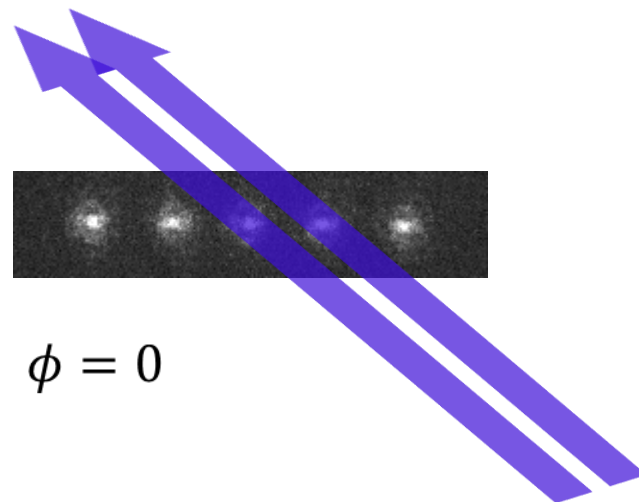
$$\begin{aligned} |0_1 0_2\rangle &\rightarrow |0_1 0_2\rangle - i|1_1 1_2\rangle e^{-i\phi} \\ |0_1 1_2\rangle &\rightarrow |0_1 1_2\rangle - i|1_1 0_2\rangle \\ |1_1 0_2\rangle &\rightarrow |1_1 0_2\rangle - i|0_1 1_2\rangle \\ |1_1 1_2\rangle &\rightarrow |1_1 1_2\rangle - i|0_1 0_2\rangle e^{i\phi} \end{aligned}$$



**F=0.983(4)**  
(excluding SPAM errors)

# Ising (XX) gate [3,4]

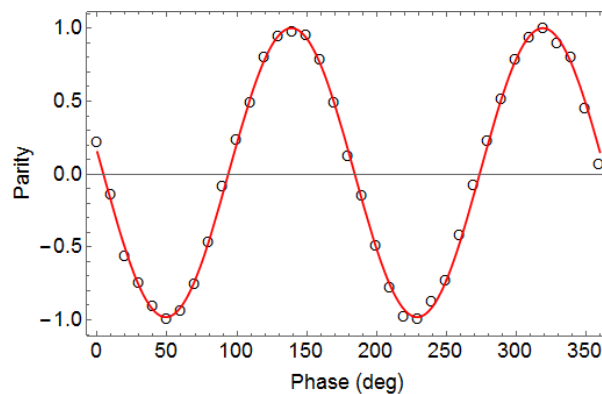
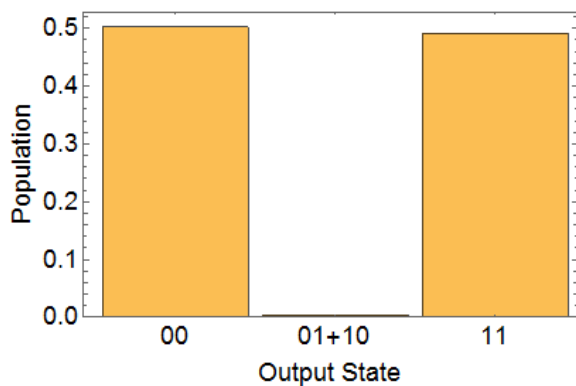
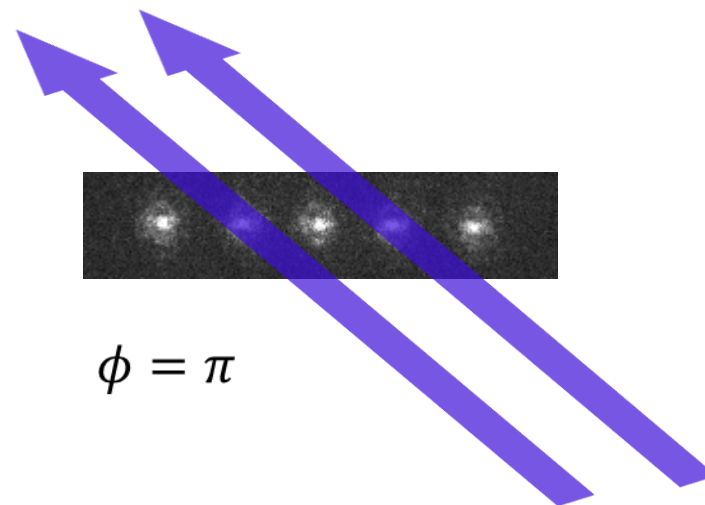
$$\begin{aligned} |0_3 0_4\rangle &\rightarrow |0_3 0_4\rangle - i|1_3 1_4\rangle e^{-i\phi} \\ |0_3 1_4\rangle &\rightarrow |0_3 1_4\rangle - i|1_3 0_4\rangle \\ |1_3 0_4\rangle &\rightarrow |1_3 0_4\rangle - i|0_3 1_4\rangle \\ |1_3 1_4\rangle &\rightarrow |1_3 1_4\rangle - i|0_3 0_4\rangle e^{i\phi} \end{aligned}$$



**F=0.992(3)**  
(excluding SPAM errors)

# Ising (XX) gate [2,4]

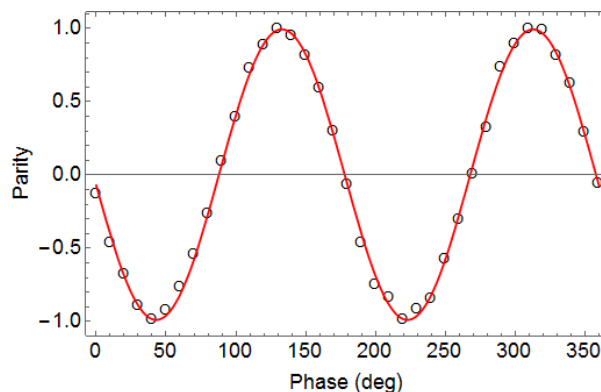
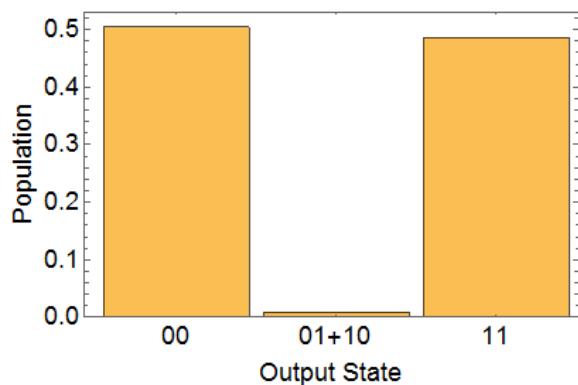
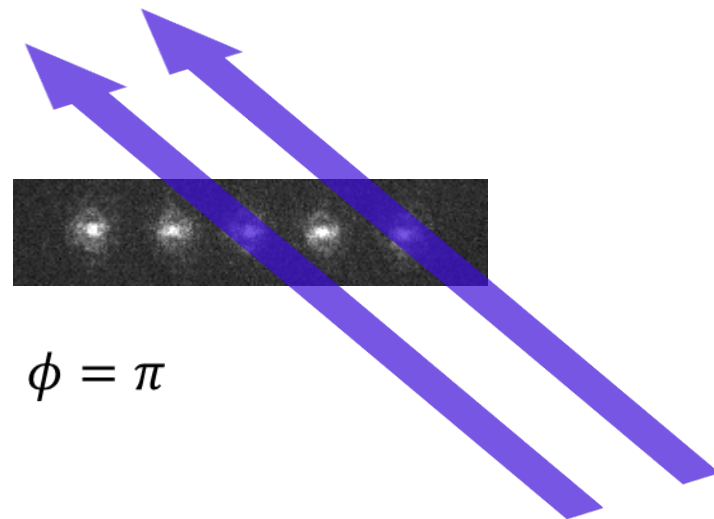
$$\begin{aligned}
 |0_2 0_4\rangle &\rightarrow |0_2 0_4\rangle - i|1_2 1_4\rangle e^{-i\phi} \\
 |0_2 1_4\rangle &\rightarrow |0_2 1_4\rangle - i|1_2 0_4\rangle \\
 |1_2 0_4\rangle &\rightarrow |1_2 0_4\rangle - i|0_2 1_4\rangle \\
 |1_2 1_4\rangle &\rightarrow |1_2 1_4\rangle - i|0_2 0_4\rangle e^{i\phi}
 \end{aligned}$$



**F=0.991(4)**  
(excluding SPAM errors)

# Ising (XX) gate [3,5]

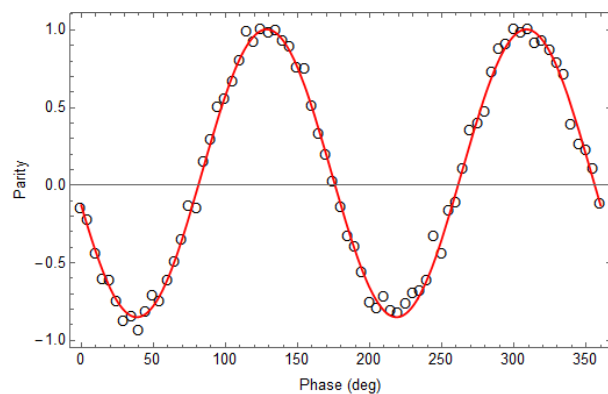
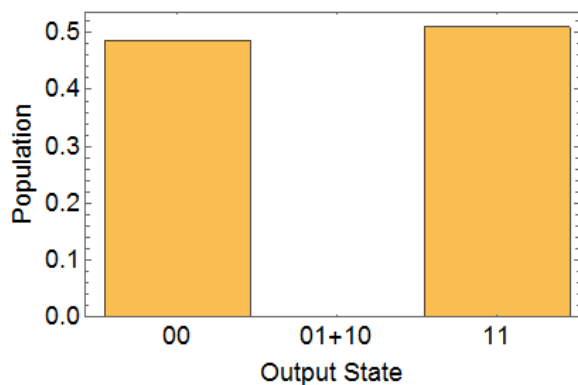
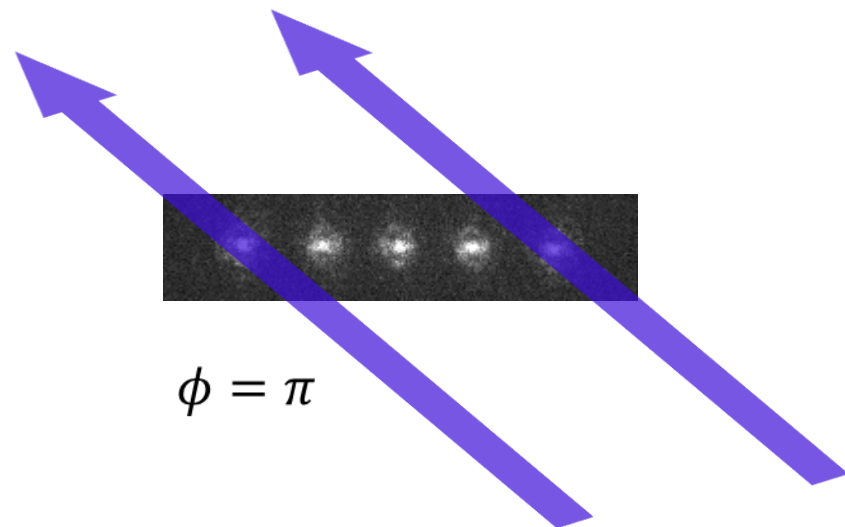
$$\begin{aligned}
 |0_3 0_5\rangle &\rightarrow |0_3 0_5\rangle - i|1_3 1_5\rangle e^{-i\phi} \\
 |0_3 1_5\rangle &\rightarrow |0_3 1_5\rangle - i|1_3 0_5\rangle \\
 |1_3 0_5\rangle &\rightarrow |1_3 0_5\rangle - i|0_3 1_5\rangle \\
 |1_3 1_5\rangle &\rightarrow |1_3 1_5\rangle - i|0_3 0_5\rangle e^{i\phi}
 \end{aligned}$$



**F=0.991(4)**  
(excluding SPAM errors)

# Ising (XX) gate [1,5]

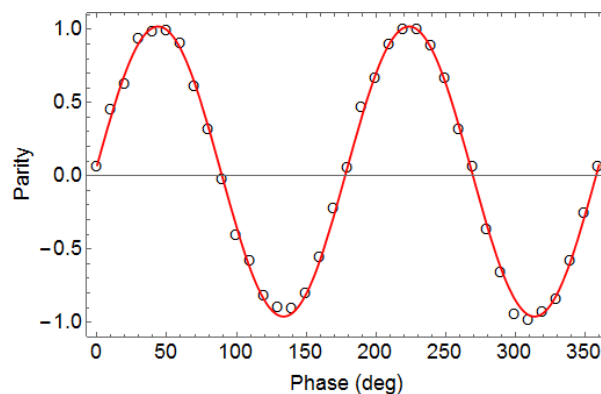
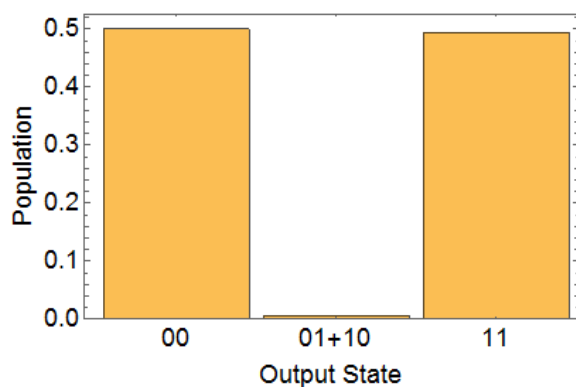
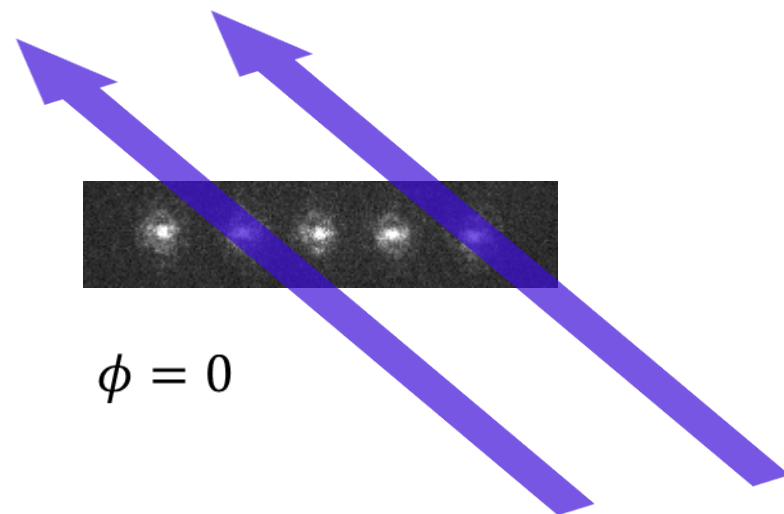
$$\begin{aligned} |0_1 0_5\rangle &\rightarrow |0_1 0_5\rangle - i|1_1 1_5\rangle e^{-i\phi} \\ |0_1 1_5\rangle &\rightarrow |0_1 1_5\rangle - i|1_1 0_5\rangle \\ |1_1 0_5\rangle &\rightarrow |1_1 0_5\rangle - i|0_1 1_5\rangle \\ |1_1 1_5\rangle &\rightarrow |1_1 1_5\rangle - i|0_1 0_5\rangle e^{i\phi} \end{aligned}$$



**F=0.961(5)**  
(excluding SPAM errors)

# Ising (XX) gate [2,5]

$$\begin{aligned} |0_2 0_5\rangle &\rightarrow |0_2 0_5\rangle - i|1_2 1_5\rangle e^{-i\phi} \\ |0_2 1_5\rangle &\rightarrow |0_2 1_5\rangle - i|1_2 0_5\rangle \\ |1_2 0_5\rangle &\rightarrow |1_2 0_5\rangle - i|0_2 1_5\rangle \\ |1_2 1_5\rangle &\rightarrow |1_2 1_5\rangle - i|0_2 0_5\rangle e^{i\phi} \end{aligned}$$



**F=0.992(4)**  
(excluding SPAM errors)



# Many ions: phonon modes

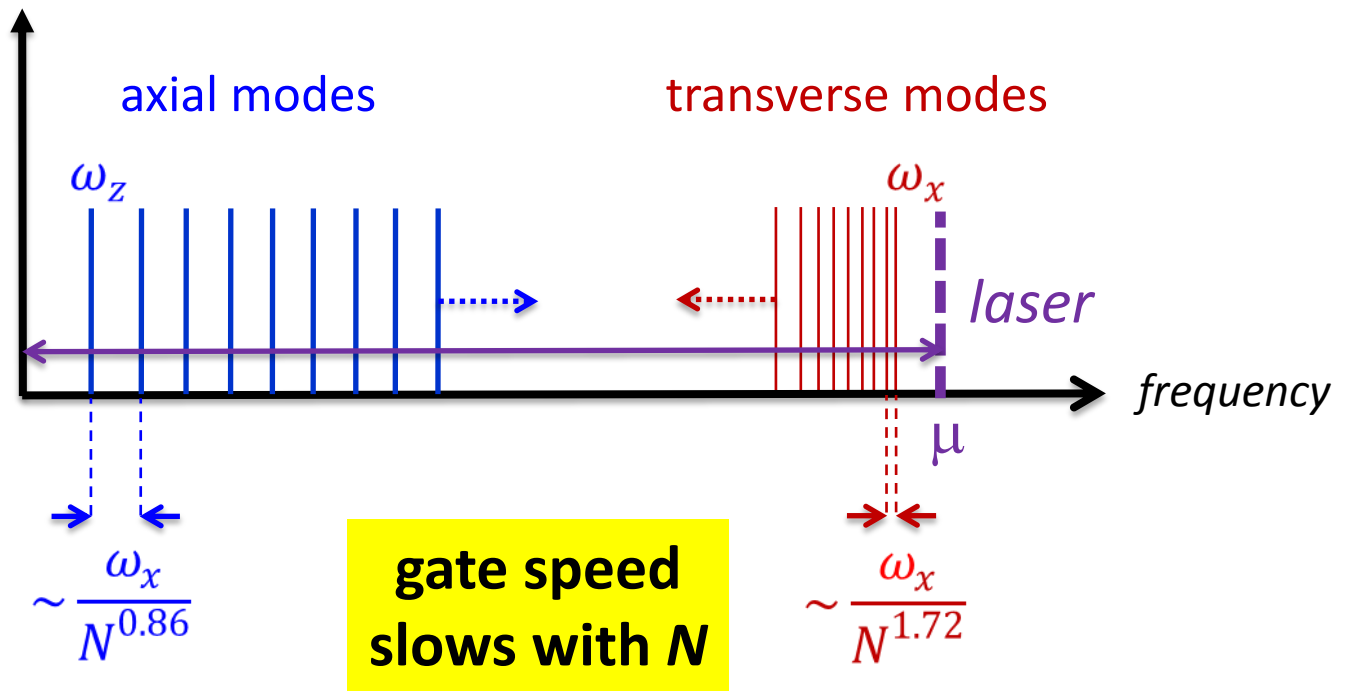
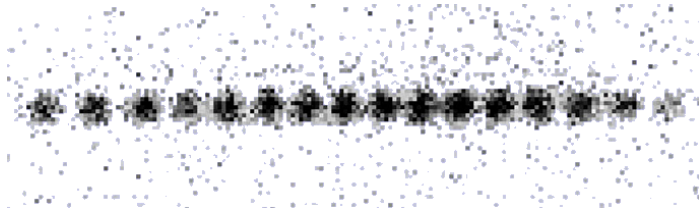
$N$  ions in a line

transverse trap frequency

$\omega_x =$  high as you can go

axial trap frequency

$$\omega_z < \frac{\omega_x}{N^{0.86}}$$

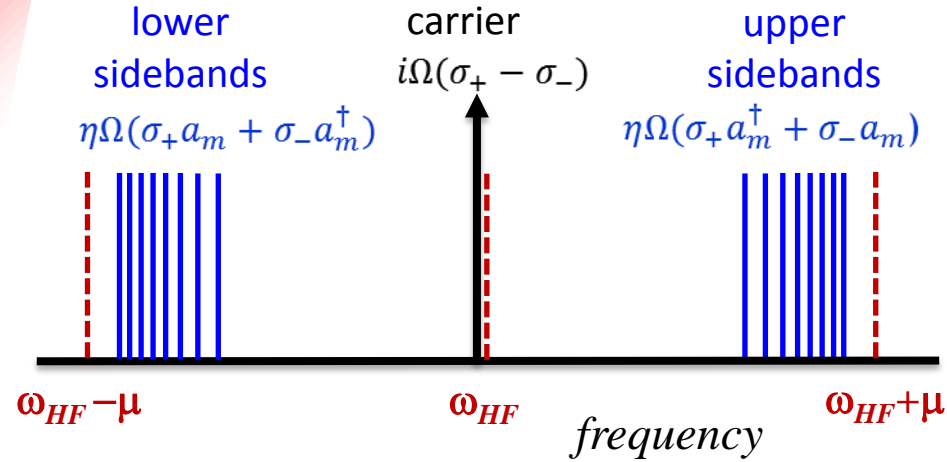
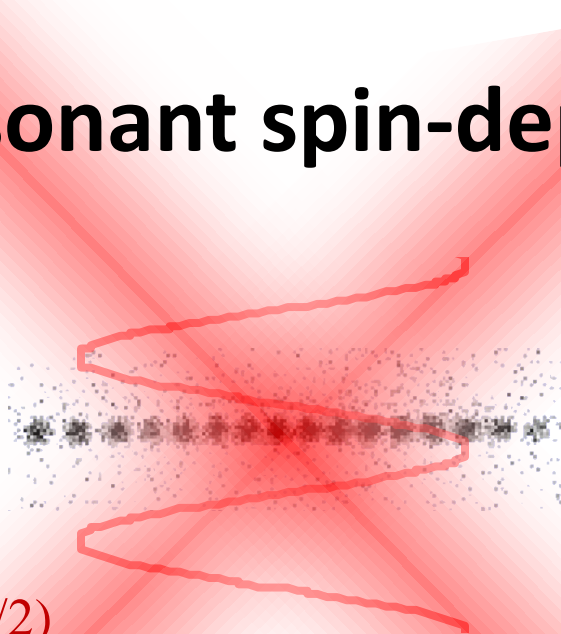


# Resonant spin-dependent force

Raman  
beatnotes:

$$\omega_{HF} \pm \mu$$

$$\omega_{HF} (\Delta\phi = \pi/2)$$



Lamb-Dicke limit:  $\Delta k \langle x \rangle = \eta \langle a + a^\dagger \rangle \ll 1$

RWA:  $\omega_{HF} \gg \mu, \omega_m \gg \eta\Omega$

$$H = \sum_{i,m} \eta_{im} \Omega \sigma_x^i \left[ a_m e^{-i(\mu - \omega)t} + a_m^\dagger e^{i(\mu - \omega)t} \right] \quad \eta_{im} = b_i^m \sqrt{\frac{\omega_{rec}}{\omega_m}}$$

normal mode eigenvectors  
ion  $i$  mode  $m$

Ad. eliminate phonons:  $|\mu - \omega_m| \gg \eta\Omega$

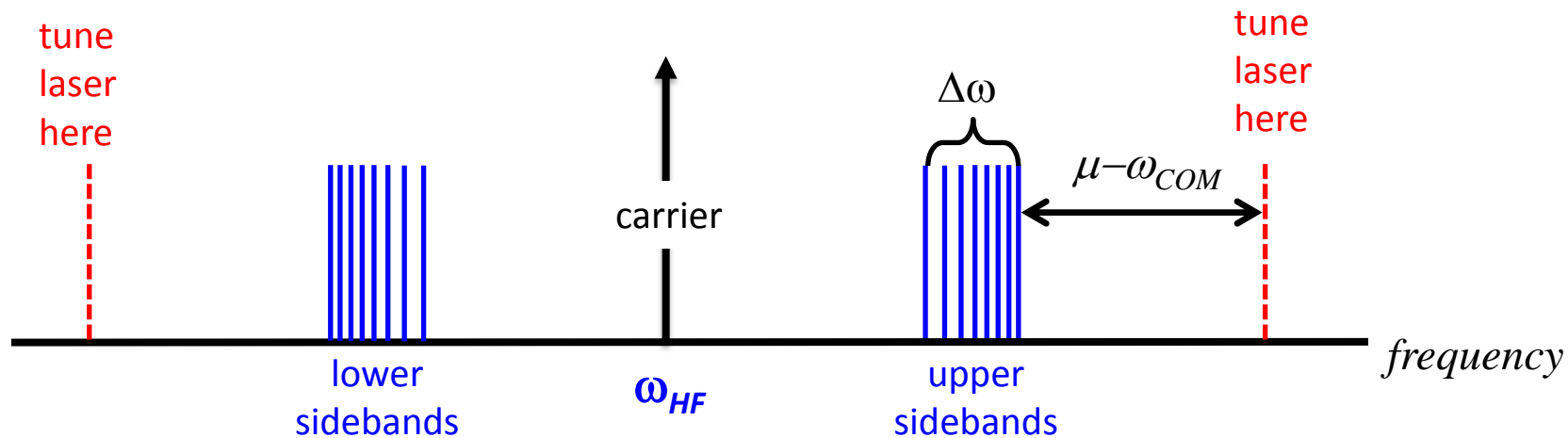
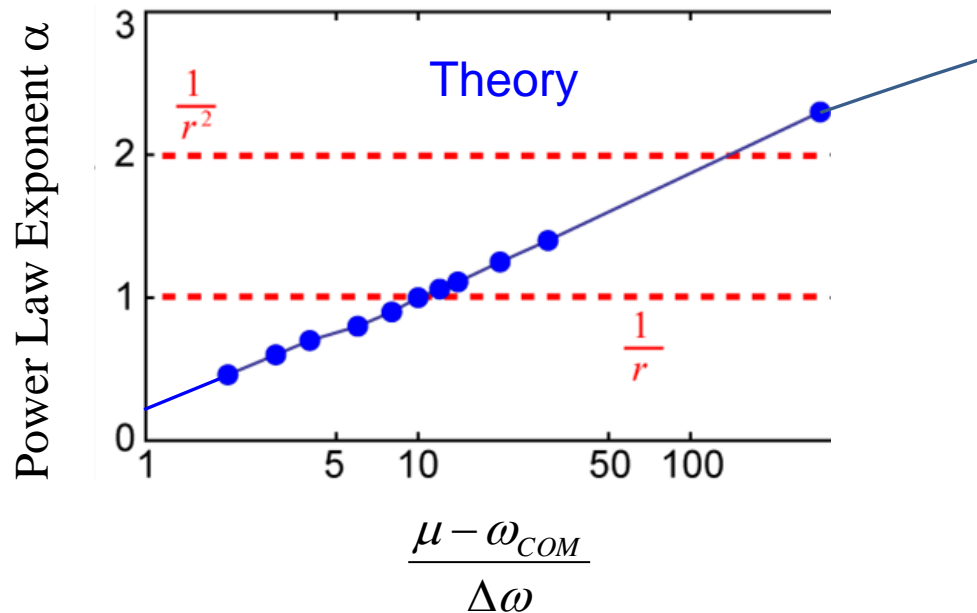
$$H = \sum_{i < j} J_{ij} \sigma_x^i \sigma_x^j + B \sum_i \sigma_y^i$$

$$J_{ij} = \omega_{rec} \Omega^2 \sum_m \frac{b_i^m b_j^m}{\mu^2 - \omega_m^2}$$

# Control of interaction range

$$J_{ij} = \omega_{rec} \Omega^2 \sum_m \frac{b_i^m b_j^m}{\mu^2 - \omega_m^2}$$

$$\sim + \frac{J_0}{|i - j|^\alpha}$$



# **T**rapped Ion Spin Hamiltonian Engineering

## **G**round states and Adiabatic Protocols

### **D**ynamics

Many-Body Spectroscopy

Propagation of Excitations: Lieb-Robinson

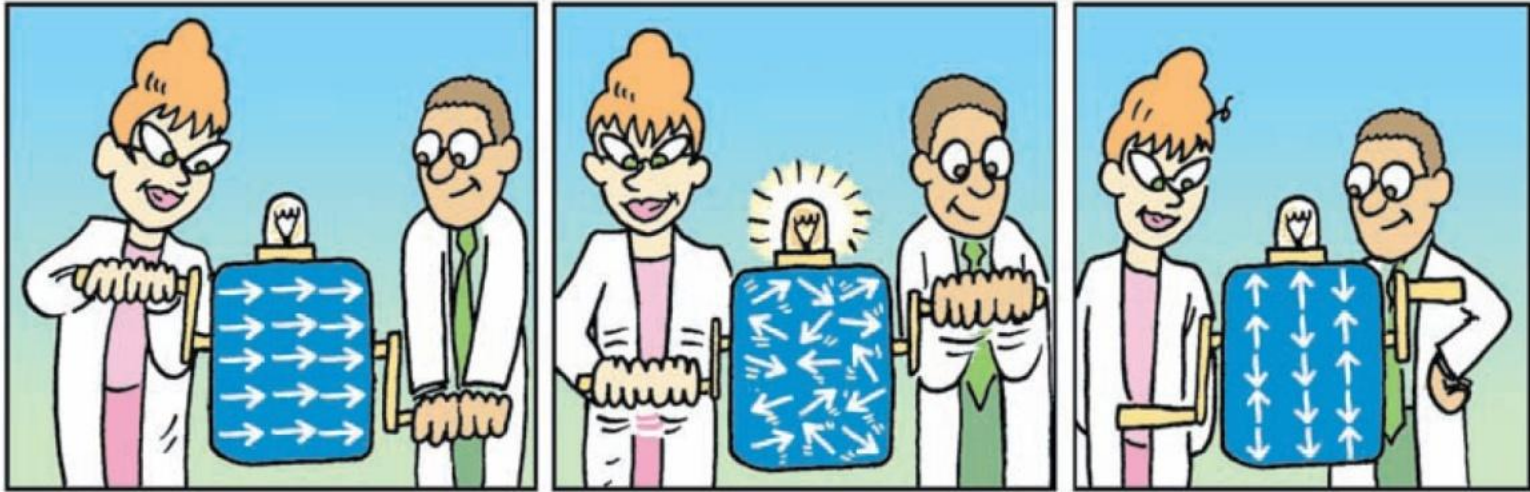
Prethermalization

Many-Body Localization

### **S**pin-1

### **E**xtending to $N \sim 100$ spins and beyond

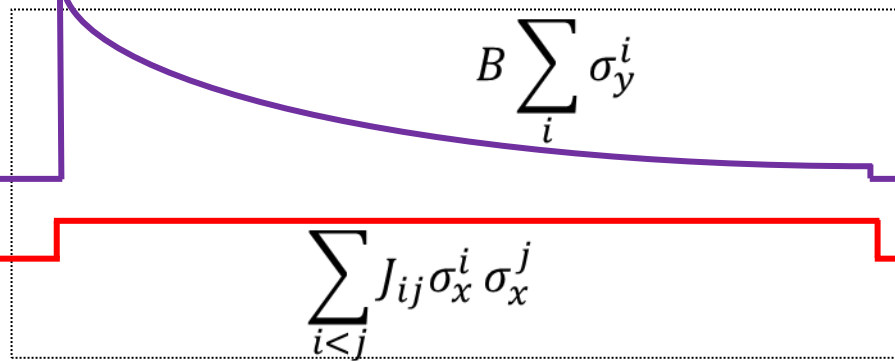
# Equilibrium: Adiabatic Quantum Simulation



from S. Lloyd, Science **319**, 1209 (2008)

$$H = \sum_{i < j} J_{ij} \sigma_x^i \sigma_x^j + B \sum_i \sigma_y^i$$

**Initialization:**  
spins along y

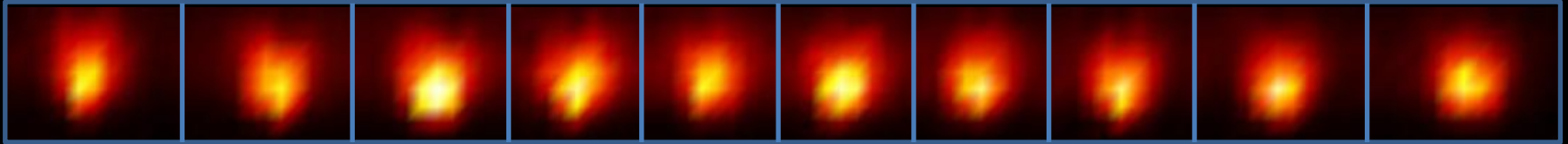


**Detection:**  
measure spins  
along x

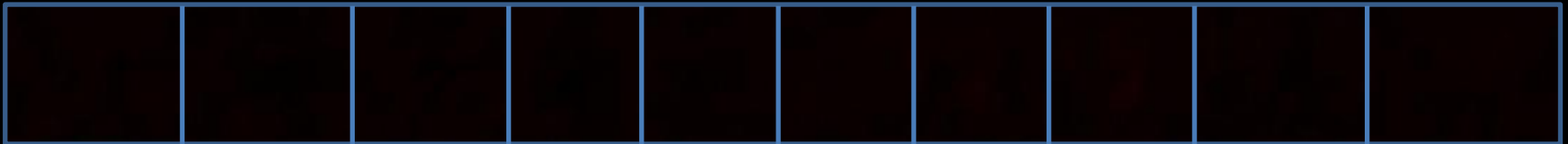
# Antiferromagnetic Néel order of N=10 spins

2600 runs,  $\alpha=1.12$

All in state  $\uparrow$

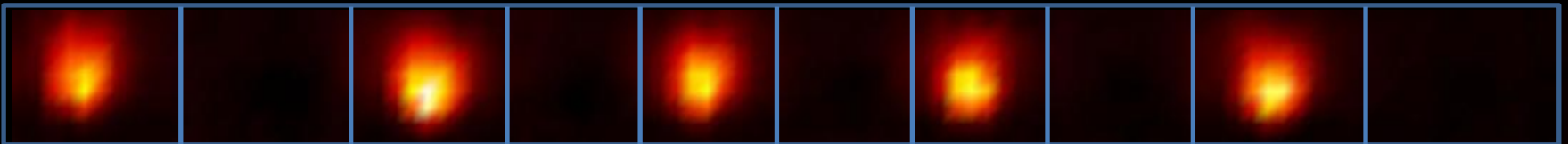


All in state  $\downarrow$

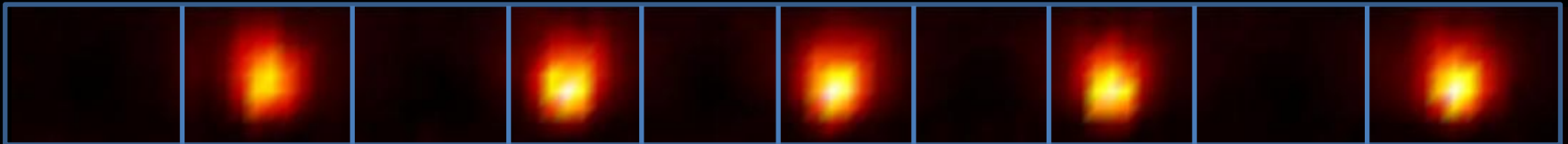


AFM ground state order

222 events



219 events



441 events out of 2600 = 17%

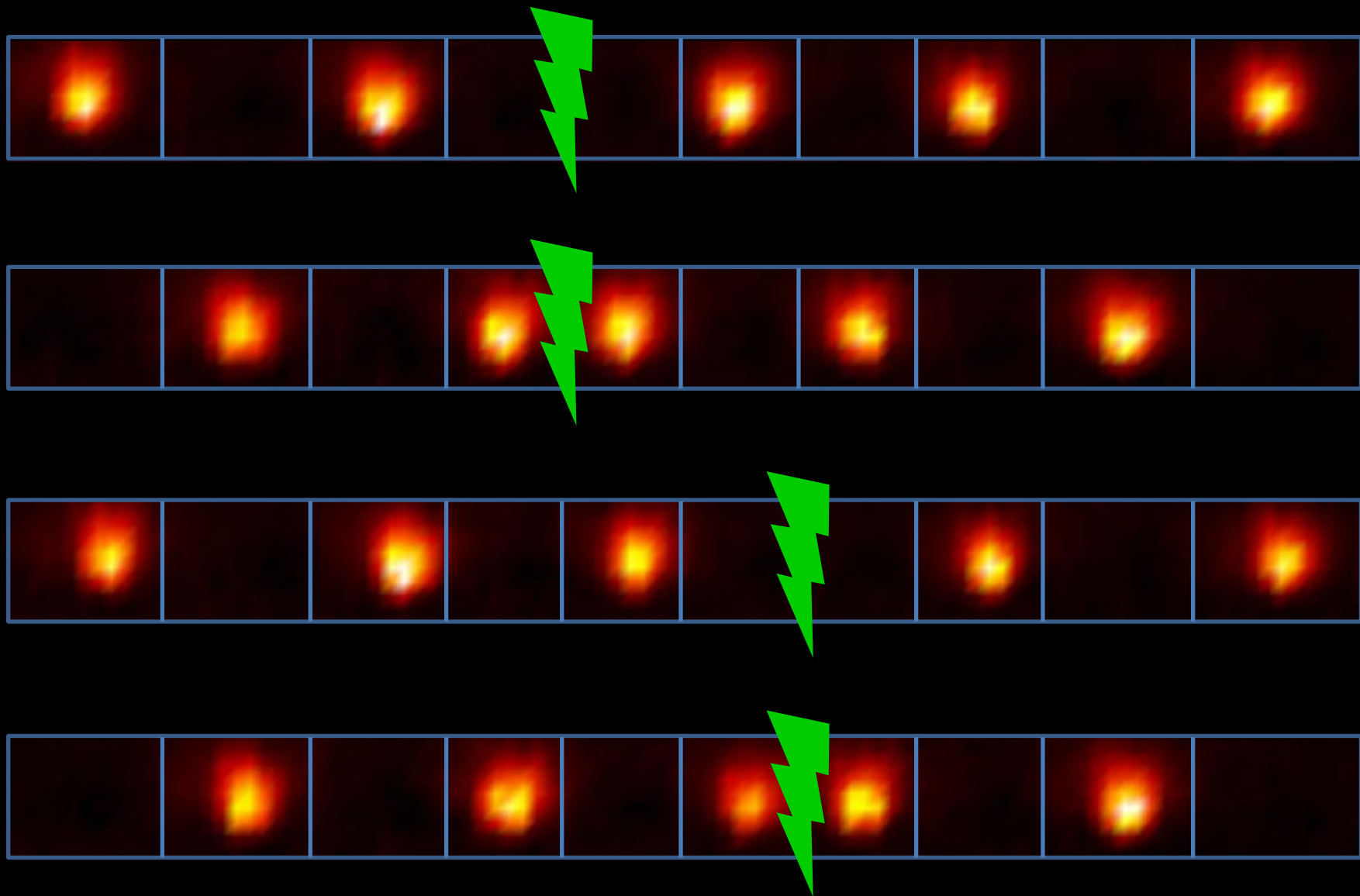
R. Islam et al., Science

Prob of any state at random =  $2 \times (1/2^{10}) = 0.2\%$

340, 583 (2013)

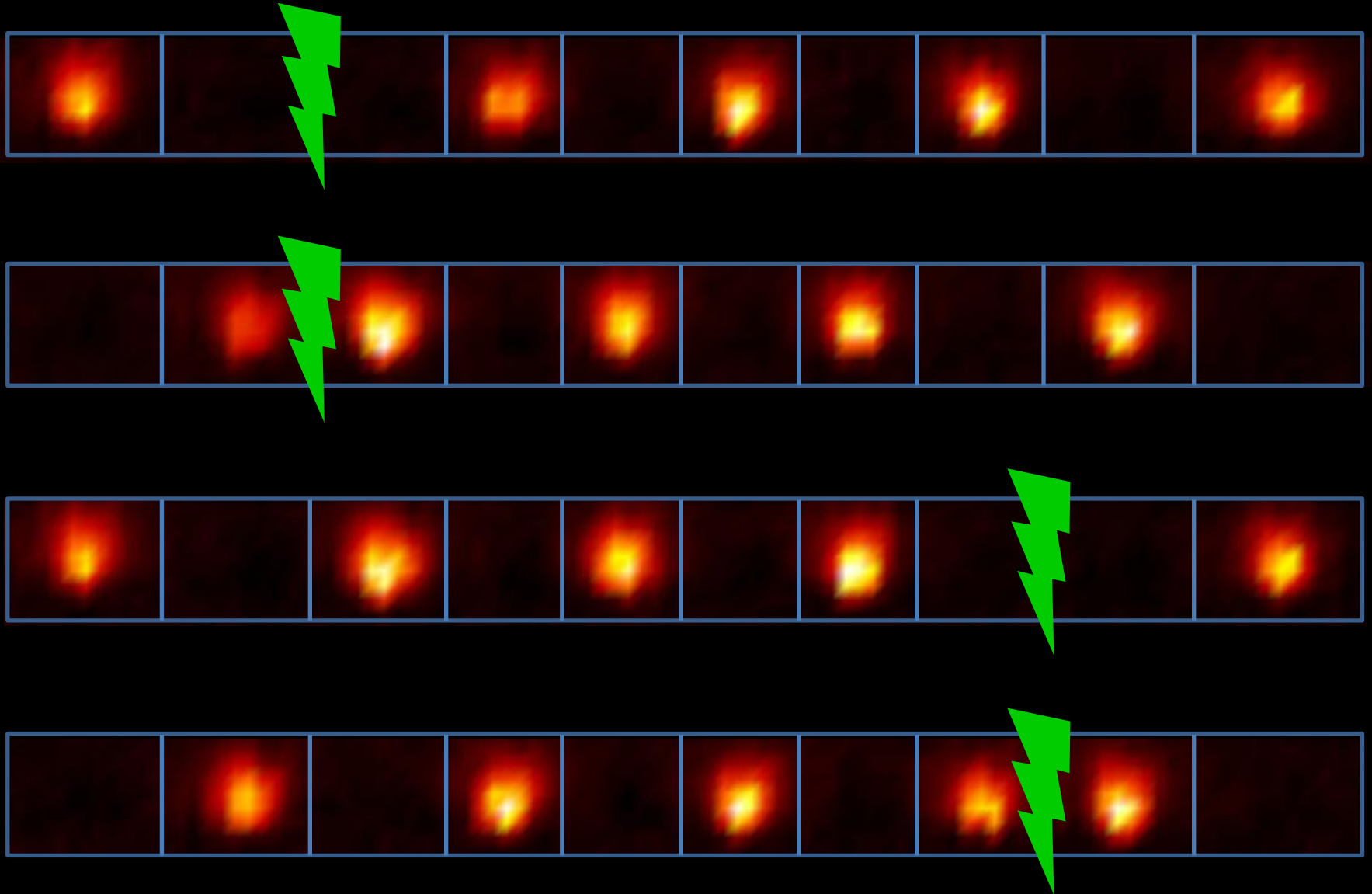
# First Excited States

(Pop. ~2% each)



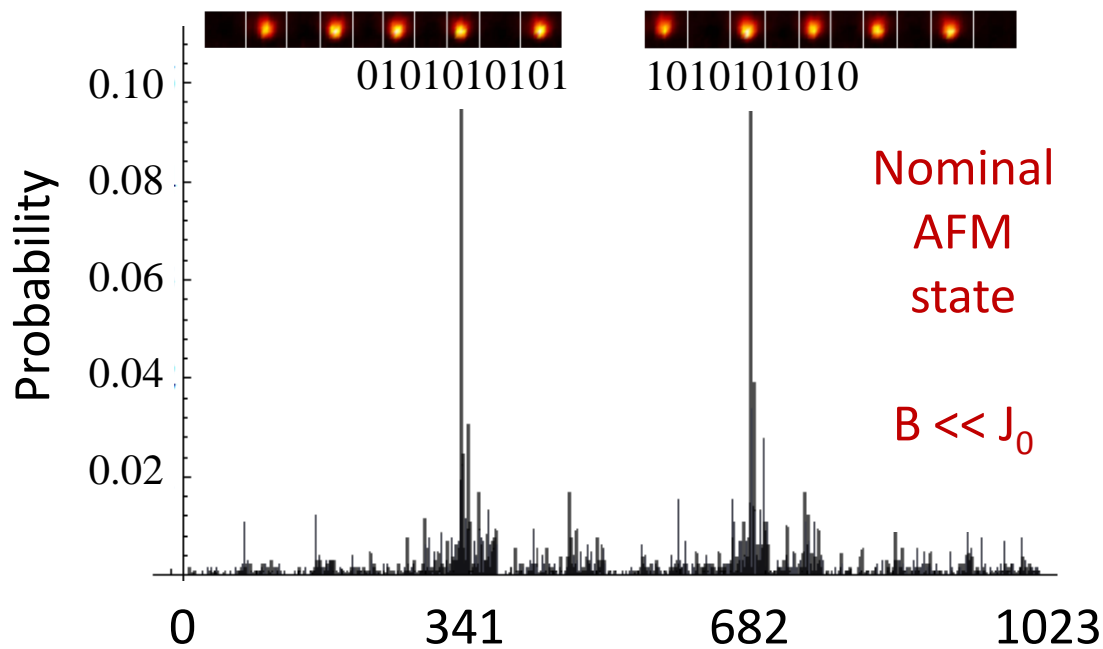
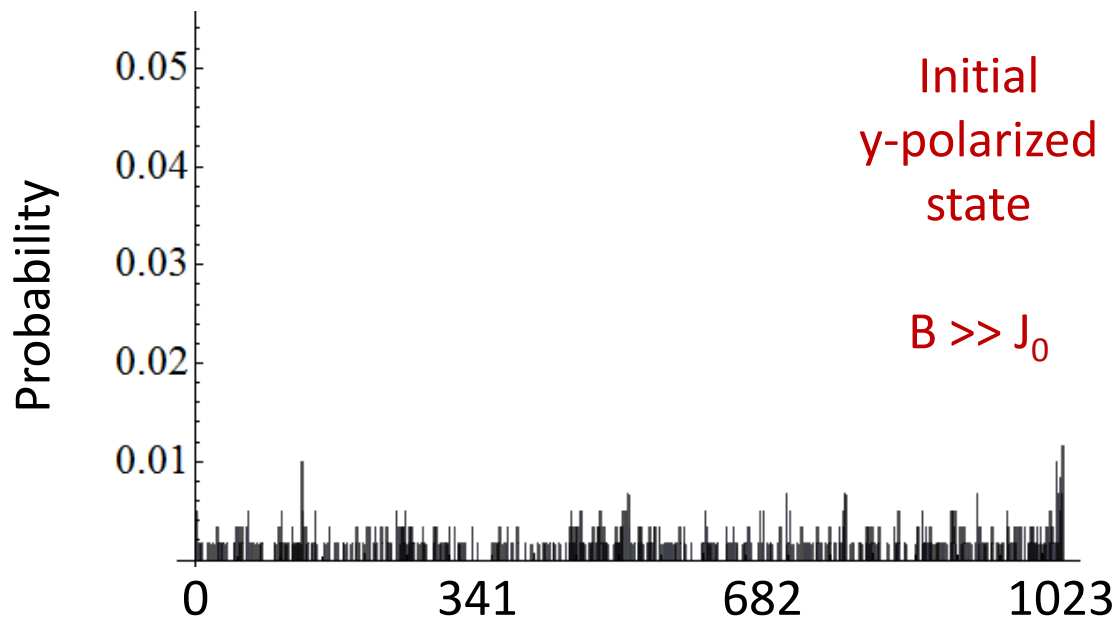
# Second Excited States

(Pop. ~1% each)

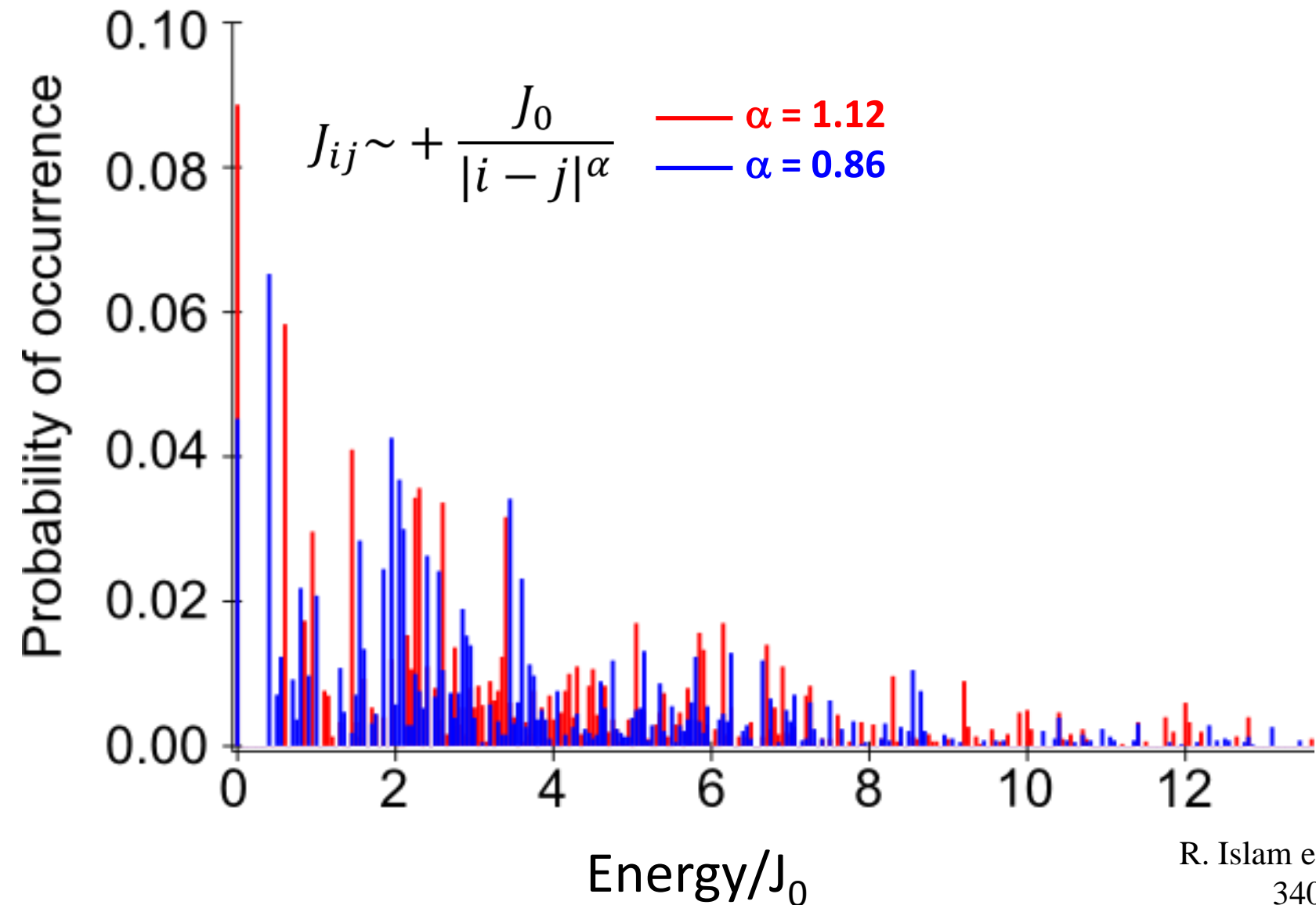




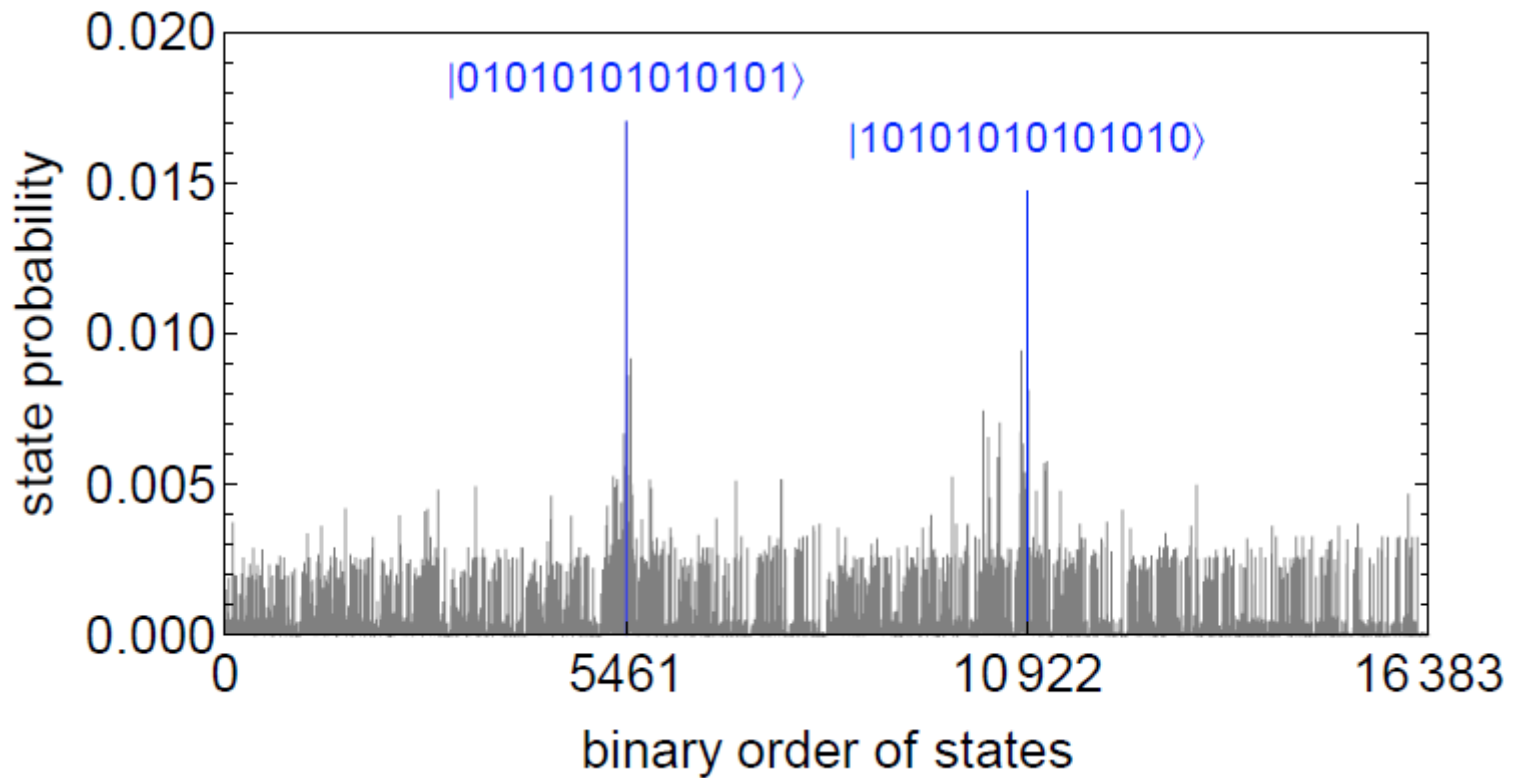
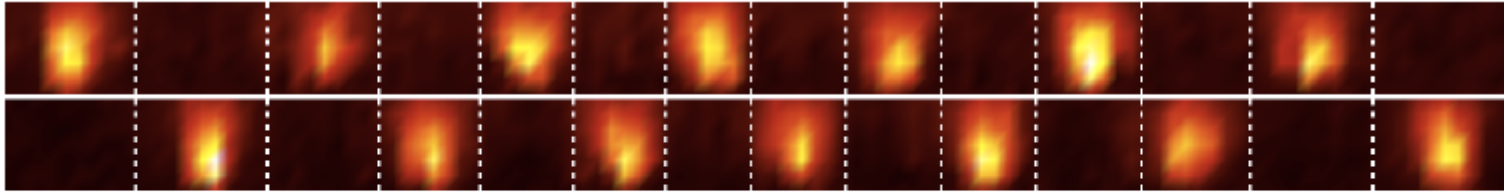
# Distribution of all $2^{10} = 1024$ states



# Distribution of states ordered by energy (N=10)



# AFM order of N=14 spins (16,384 configurations)



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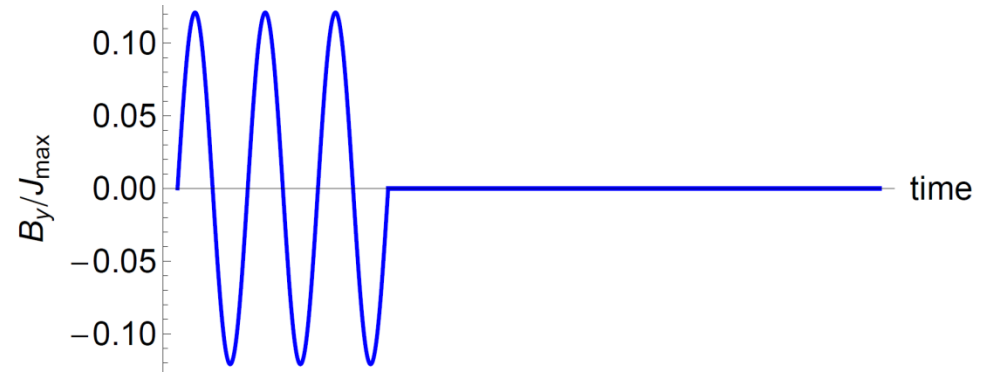
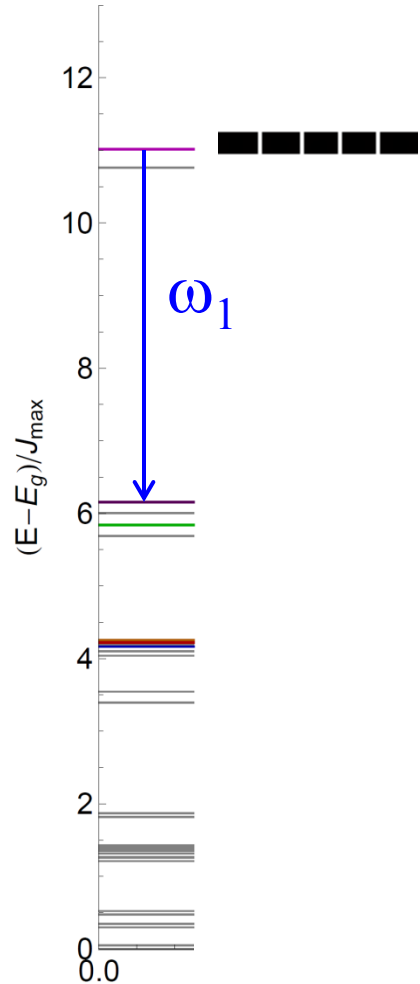
Many-Body Localization

**S**pin-1

**E**xtending to  $N \sim 100$  spins and beyond

# Coherent Imaging Spectroscopy (N=5 spins)

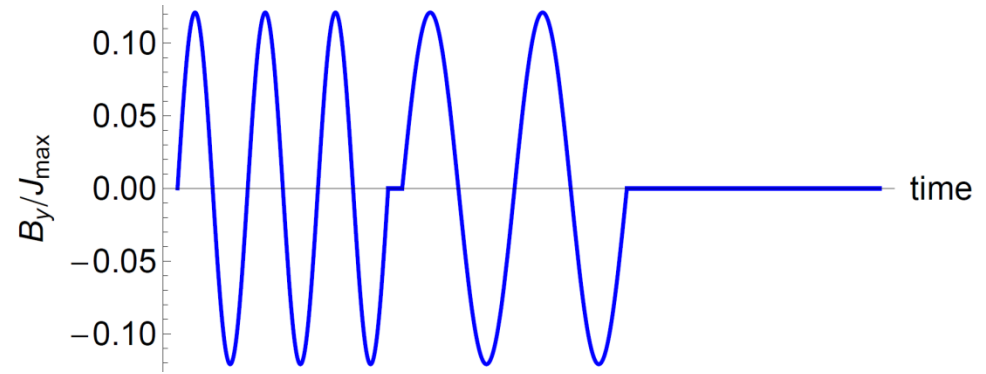
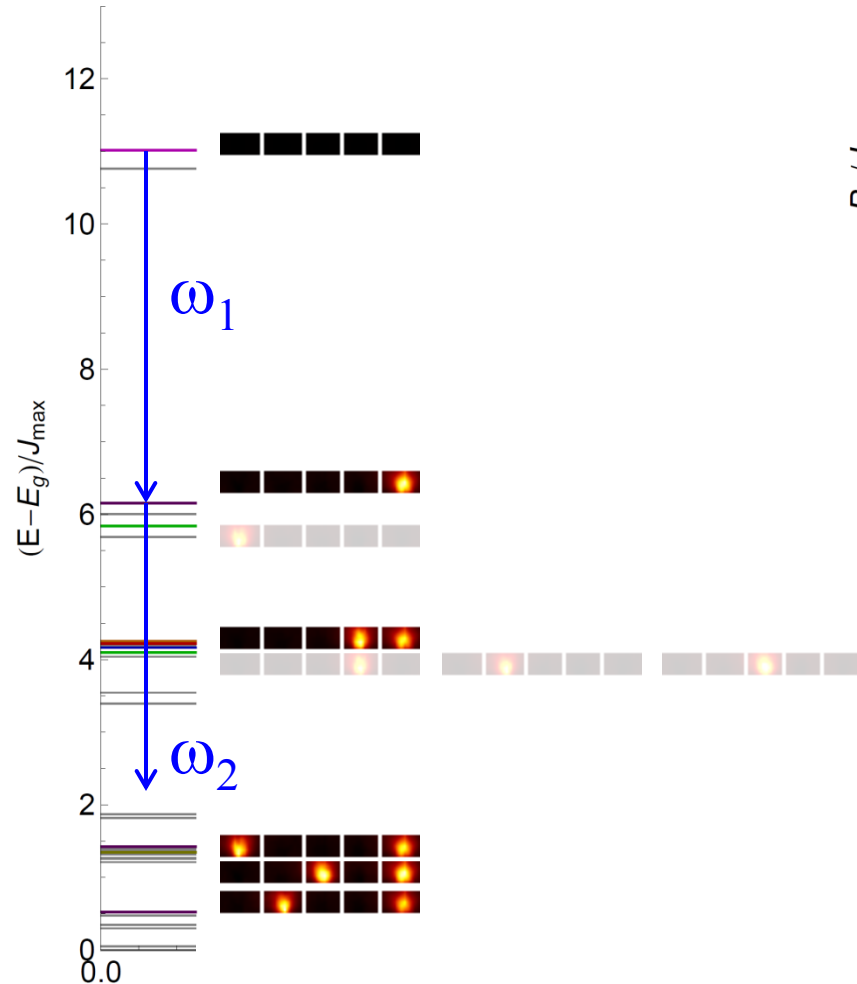
$$H = \sum_{i < j} J_{ij} \sigma_x^i \sigma_x^j$$



# Coherent Imaging Spectroscopy (N=5 spins)

$$H = \sum_{i < j} J_{ij} \sigma_x^i \sigma_x^j + B_y \sin(\omega t) \sum_i \sigma_y^i$$

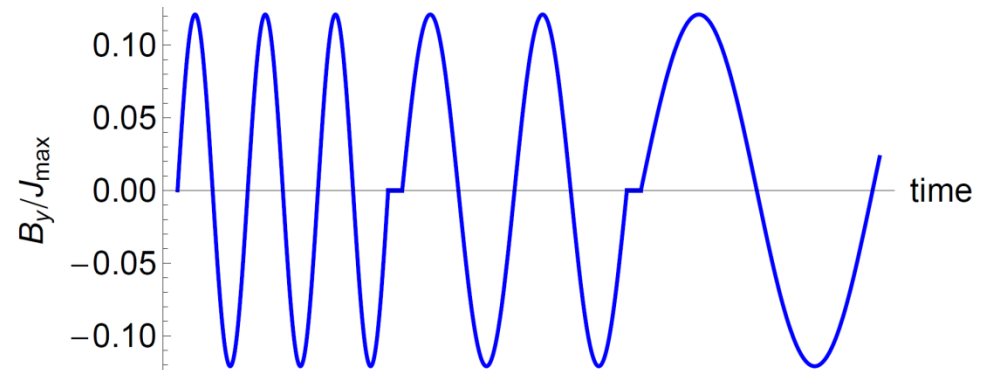
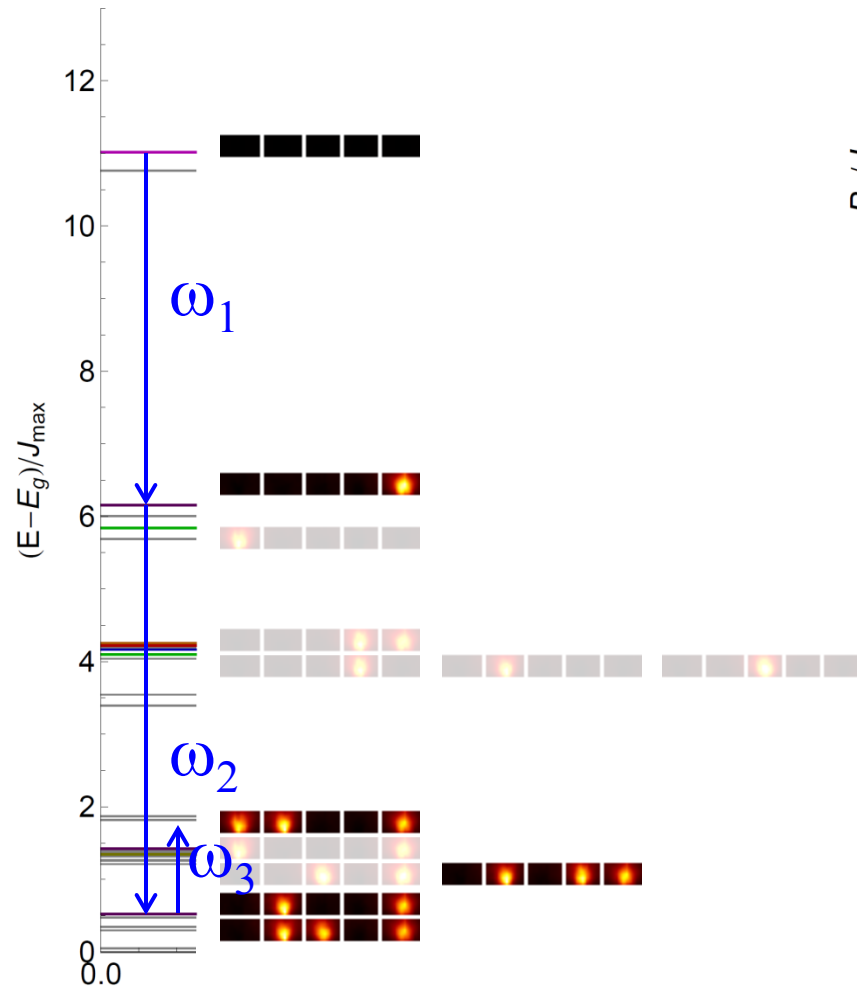
multiple frequencies



# Coherent Imaging Spectroscopy (N=5 spins)

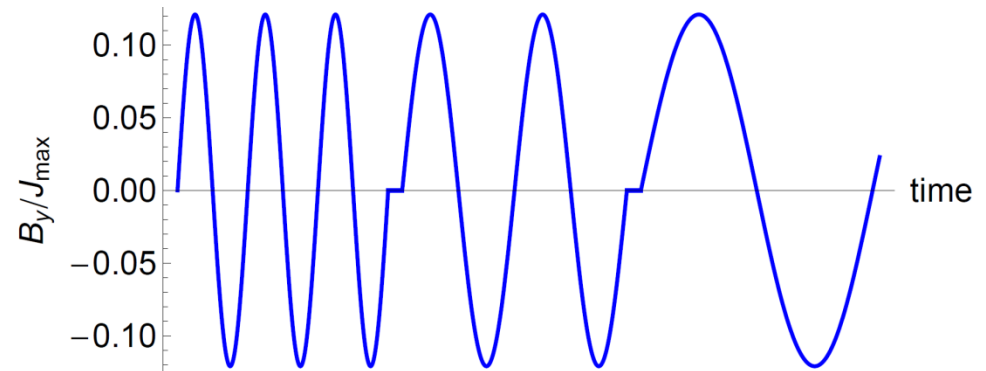
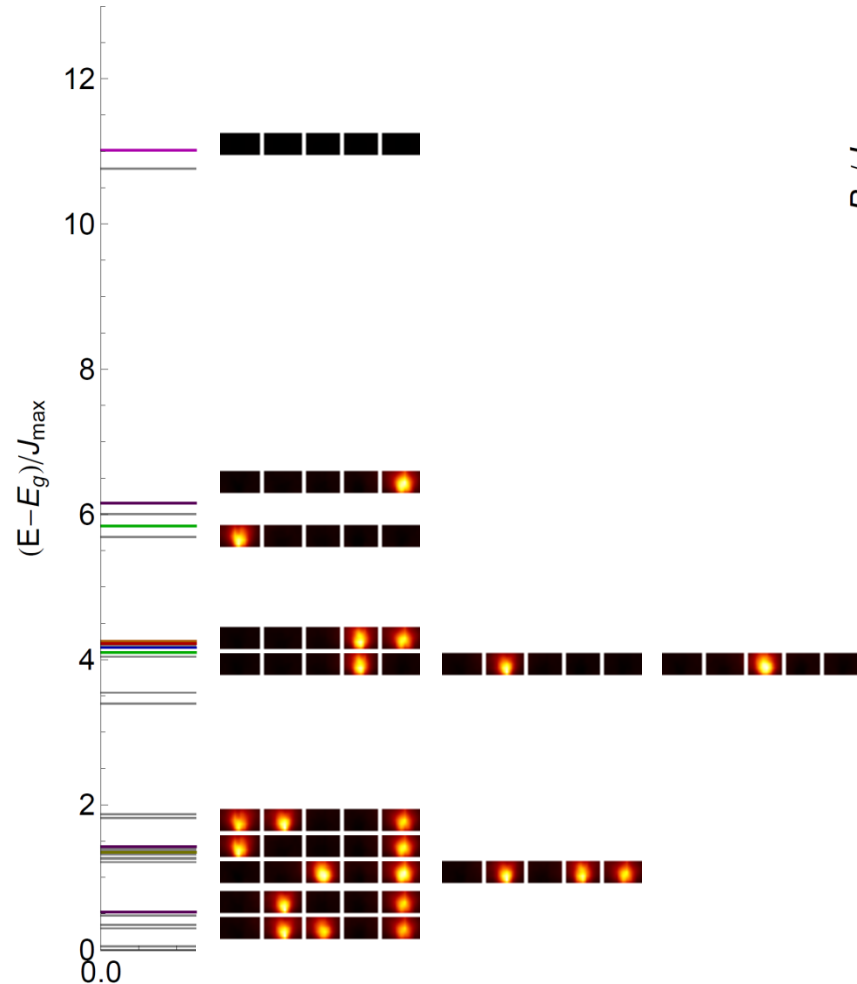
$$H = \sum_{i < j} J_{ij} \sigma_x^i \sigma_x^j + B_y \sin(\omega t) \sum_i \sigma_y^i$$

multiple frequencies



# Coherent Imaging Spectroscopy (N=5 spins)

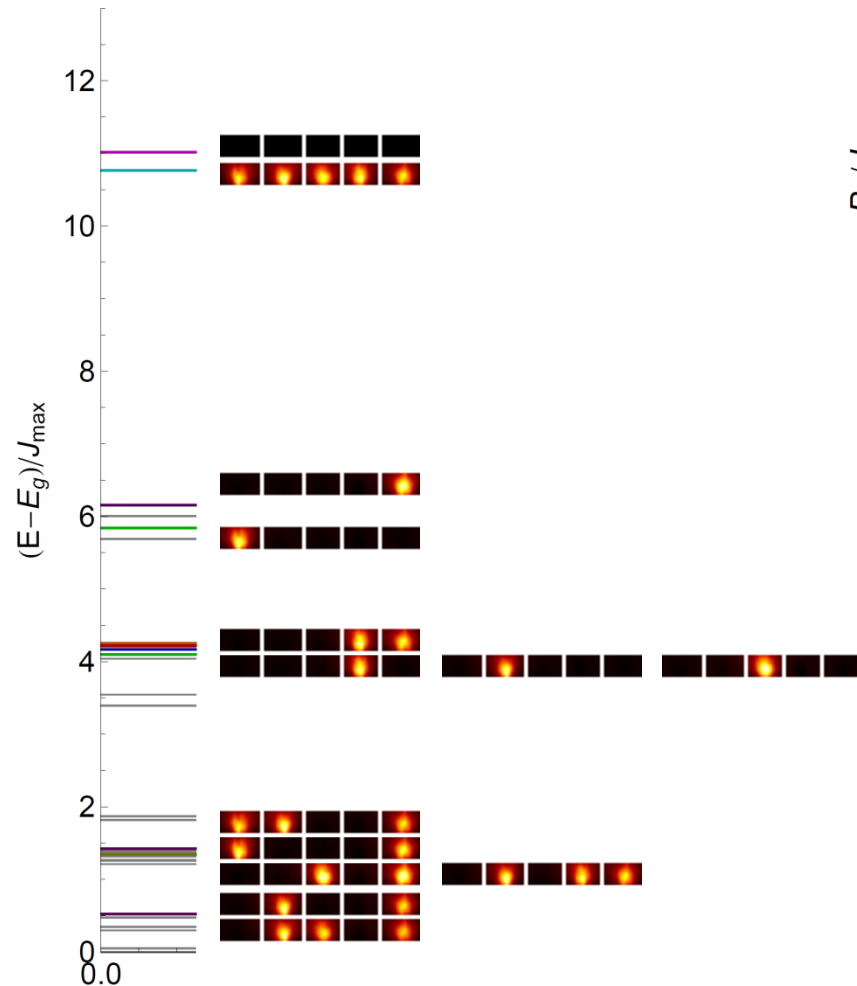
$$H = \sum_{i < j} J_{ij} \sigma_x^i \sigma_x^j + B_y \sin(\omega t) \sum_i \sigma_y^i$$





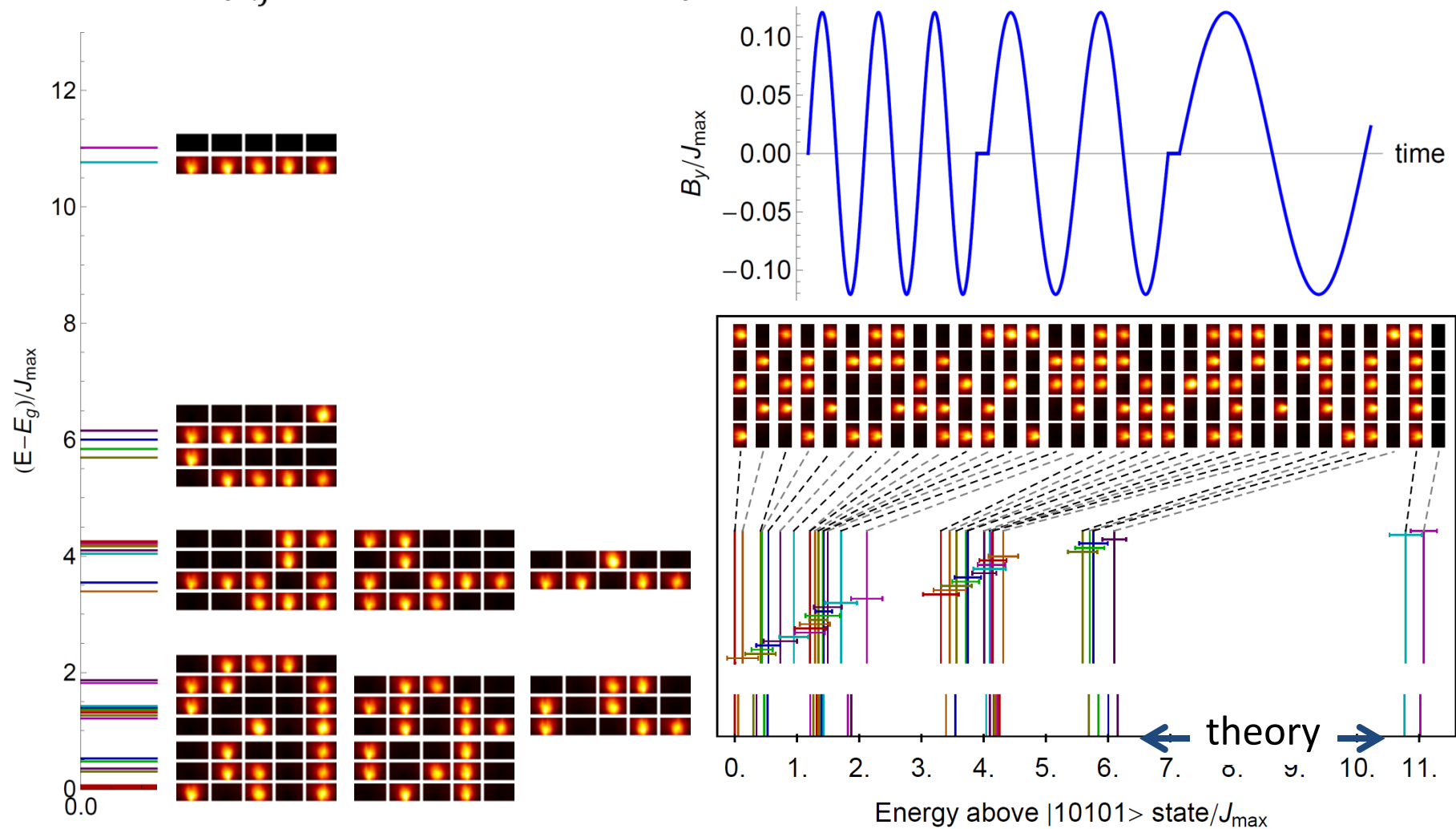
# Coherent Imaging Spectroscopy (N=5 spins)

$$H = \sum_{i < j} J_{ij} \sigma_x^i \sigma_x^j + B_y \sin(\omega t) \sum_i \sigma_y^i$$

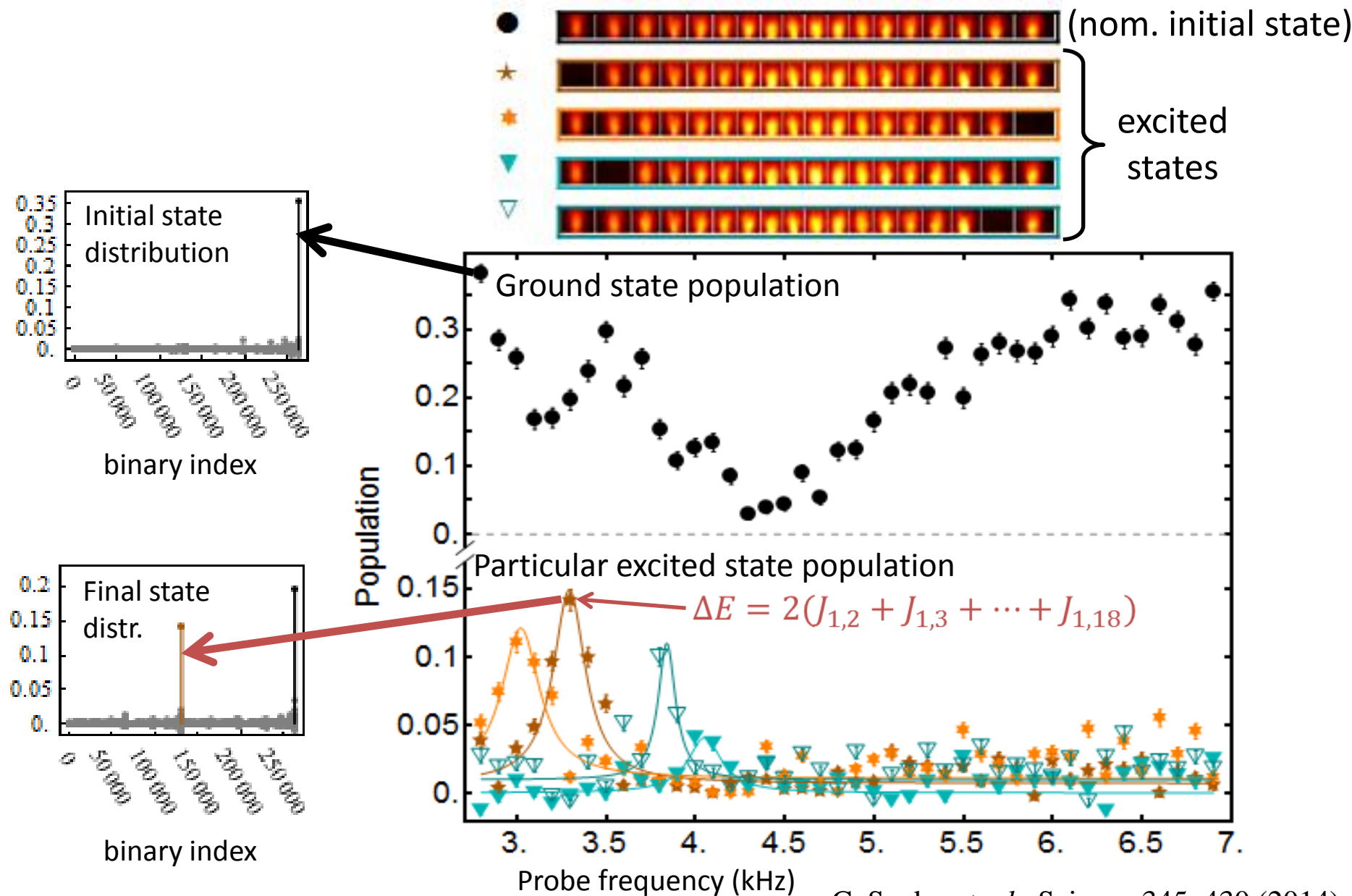


# Coherent Imaging Spectroscopy (N=5 spins)

$$H = \sum_{i < j} J_{ij} \sigma_x^i \sigma_x^j + B_y \sin(\omega t) \sum_i \sigma_y^i$$

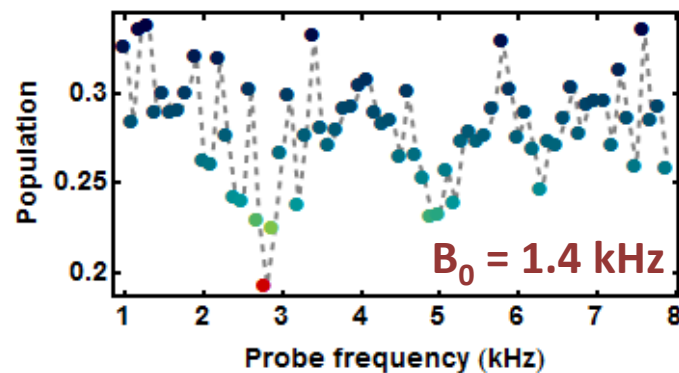
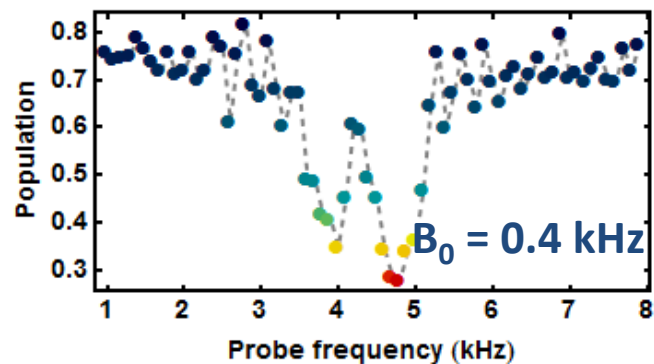
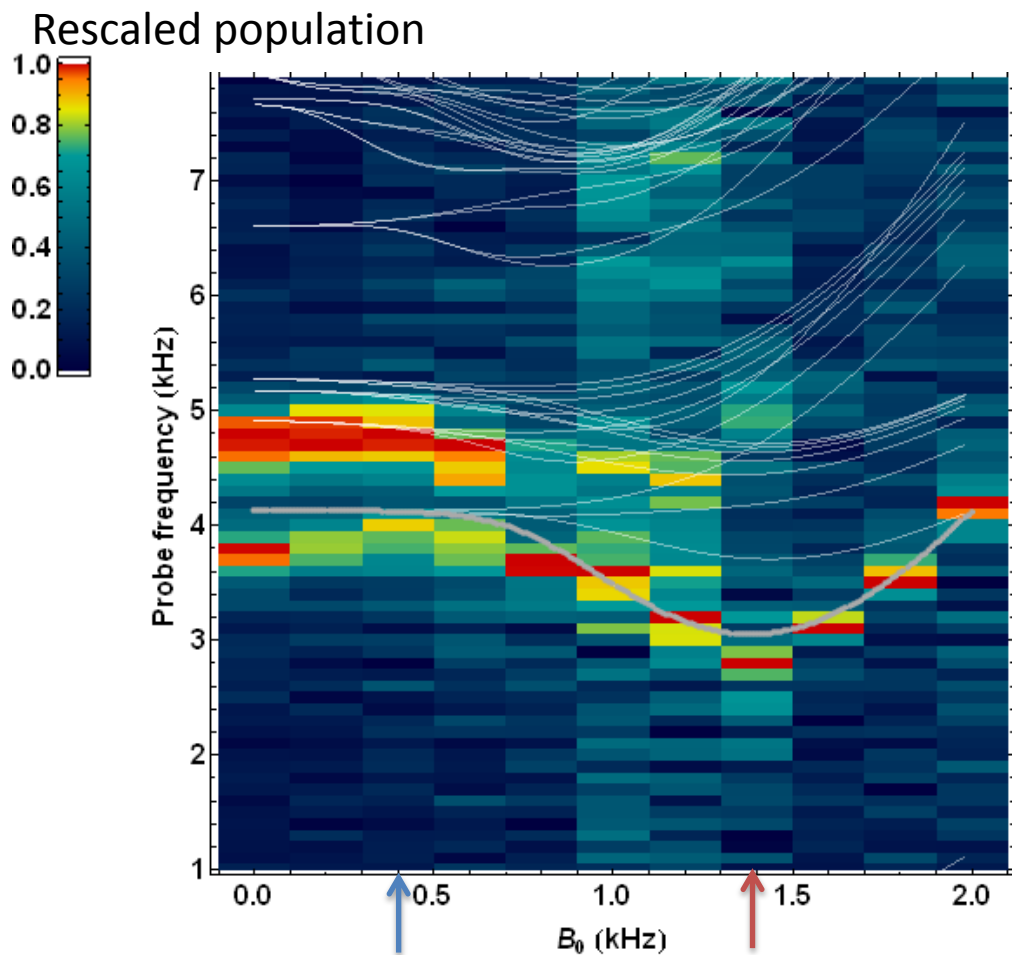


# Coherent Imaging Spectroscopy (N=18 spins)



# Coherent Imaging Spectroscopy: Critical Gap (N=8 spins)

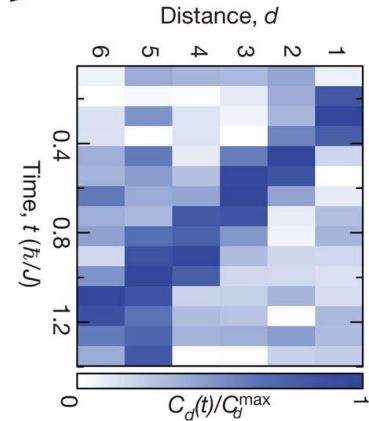
$$H = \sum_{i < j} J_{ij} \sigma_x^i \sigma_x^j + [B_0 + B_y \sin(\omega t)] \sum_i \sigma_y^i$$



# Dynamics: quantum quench

E.H. Lieb and D.W. Robinson, “*The finite group velocity of quantum spin systems,*”  
Commun. Math. Phys. 28, 251–257 (1972).

- M. Cheneau, et al., Nature 481, 484 (2012) →
- P. Hauke, et al., PRL 111, 207202 (2013)
- M. Knap, et al., PRL 111, 147205 (2013)
- Z.-X. Gong, et al., PRL 113, 030602 (2014)

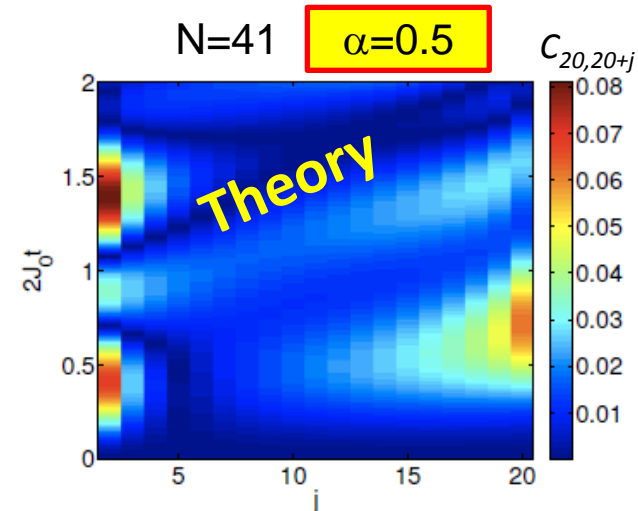
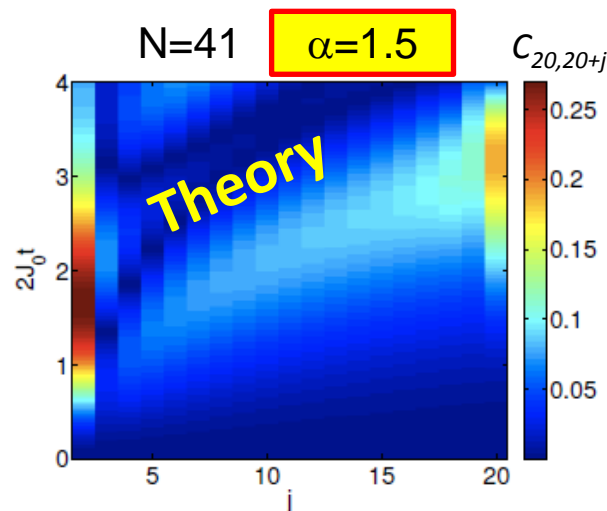
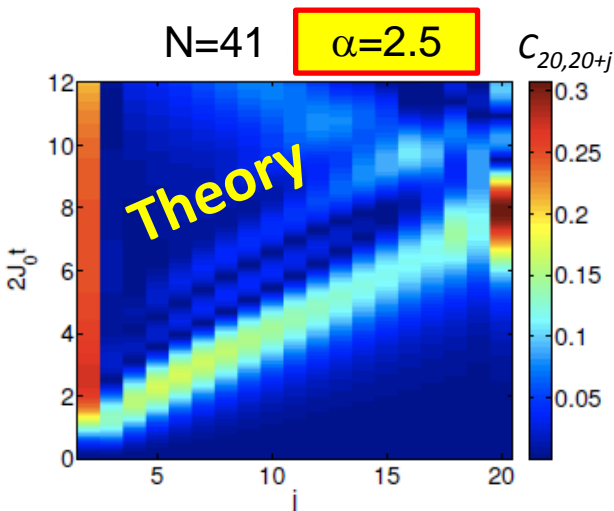


## “Global Quench”

- (a) Prepare  $(\downarrow_x + \uparrow_x)^{\otimes N}$  “ $kT = \infty$ ”
- (b) Turn on interactions
- (c) Measure correlations

$$C_{ij}^Z = \sum_{i,j} [\langle \sigma_i^Z \sigma_j^Z \rangle - \langle \sigma_i^Z \rangle \langle \sigma_j^Z \rangle]$$

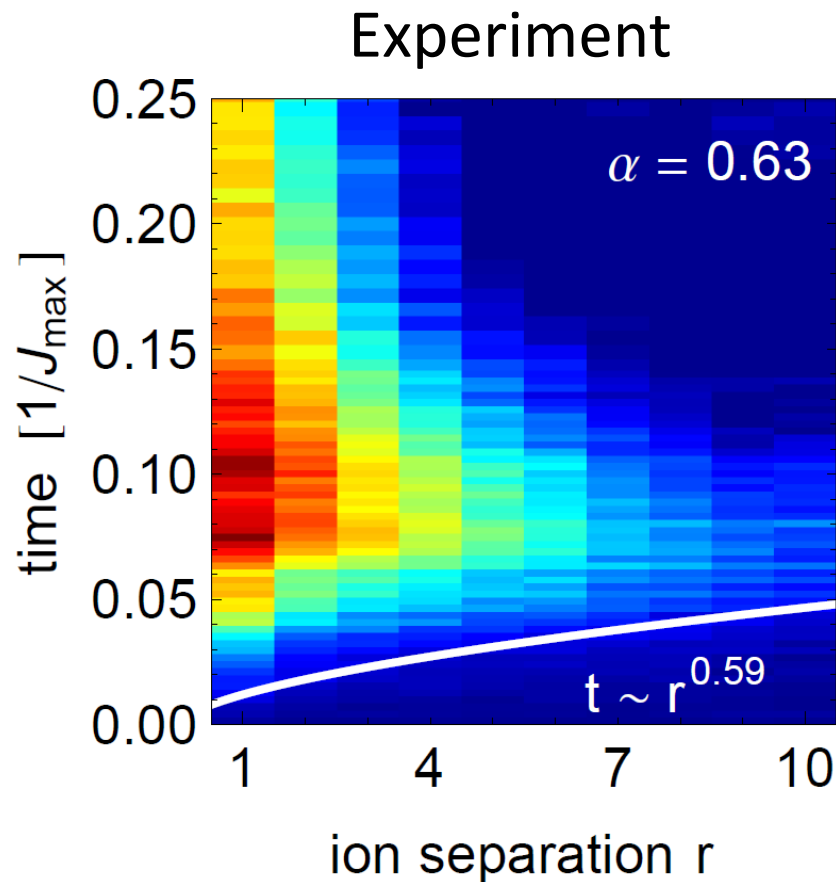
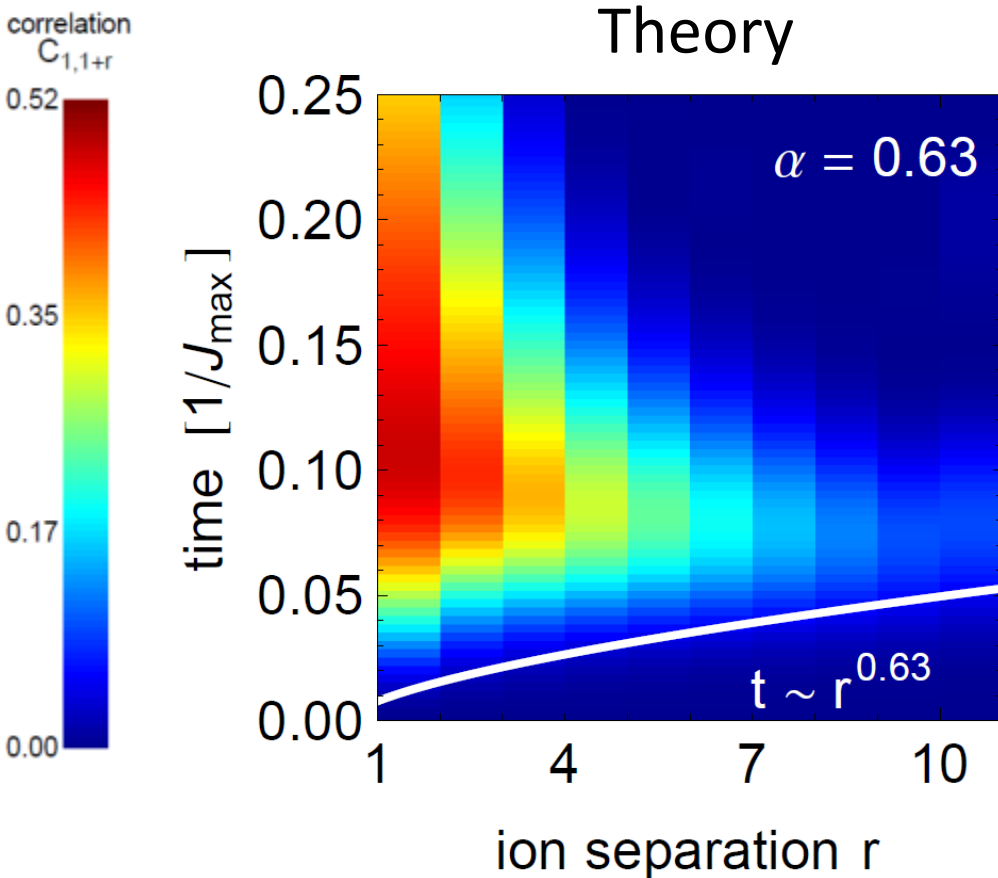
$$J_{i,j} = \frac{J_0}{|i-j|^\alpha}$$



# Long range “Light Cones” (Ising: N=11 spins)

$$H_{\text{Ising}} = \sum_{i < j} J_{ij} \sigma_x^i \sigma_x^j$$

$$J_{ij} \approx \frac{J_0}{r^\alpha}$$



P. Richerme et al., *Nature* **511**, 198 (2014)

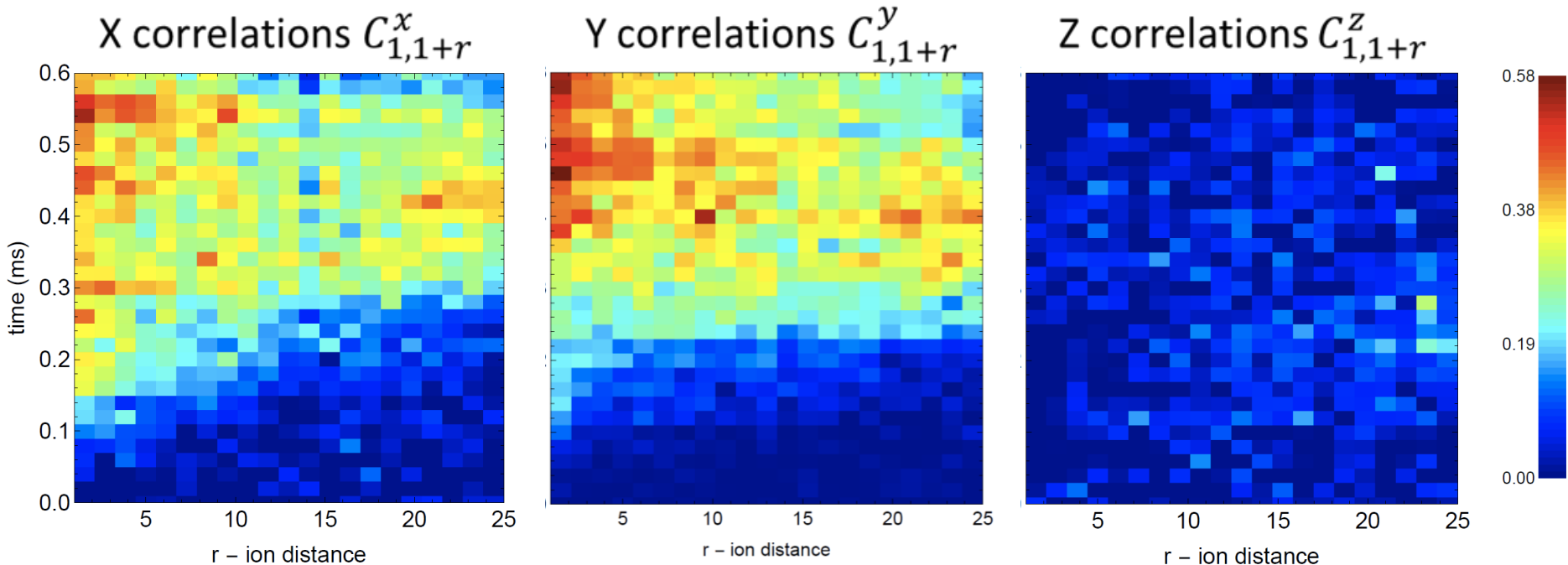
P. Jurcevic et al., *Nature* **511**, 202 (2014)

# Long range “Light Cones” (XY: N=25 spins)

$$H_{XY} = \sum_{i<j} J_{ij} (\sigma_x^i \sigma_x^j + \sigma_y^i \sigma_y^j) \quad J_{ij} \approx \frac{J_0}{r^\alpha} \quad \alpha = 1.3$$

## “Global Quench”

- (a) Prepare  $(\downarrow_z + \uparrow_z)^{\otimes N}$
- (b) Turn on interactions
- (c) Measure correlations in spacetime



P. Richerme *et al.*, *Nature* **511**, 198 (2014)

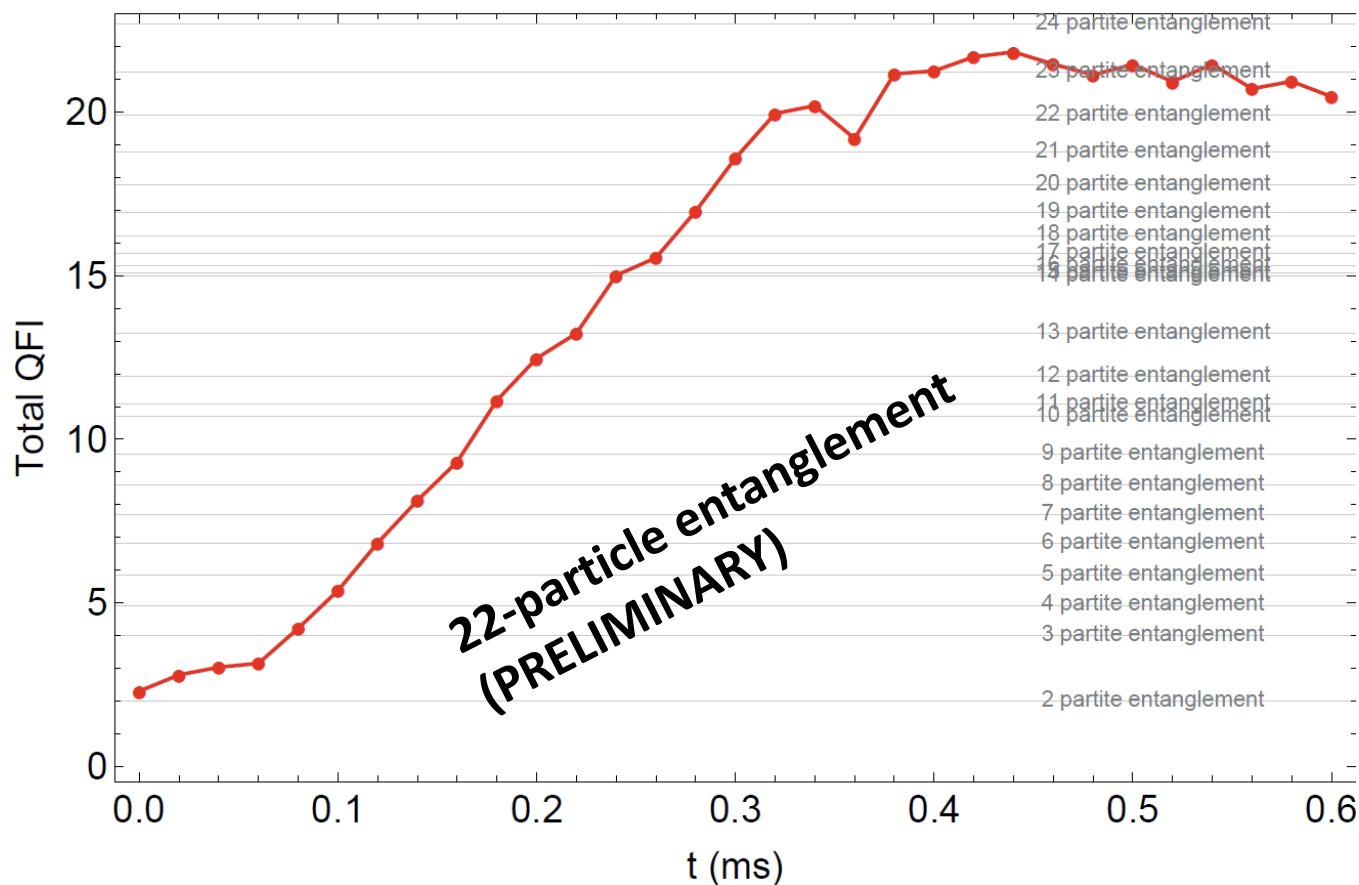
P. Jurcevic *et al.*, *Nature* **511**, 202 (2014)

# Quantum Fisher Information: characterizes system entanglement

$$F_Q = \sum_{i,j} C_{ij}^x + C_{ij}^y + C_{ij}^z \quad \text{is an entanglement witness operator}$$

Braunstein and Caves Phys. Rev. Lett. 72, 3439 (1994)

Hauke, Heyl, Tagliacozzo, Zoller, arXiv:1509.01739 (2015)





# Thermalization/Localization

How can quantum systems thermalize?

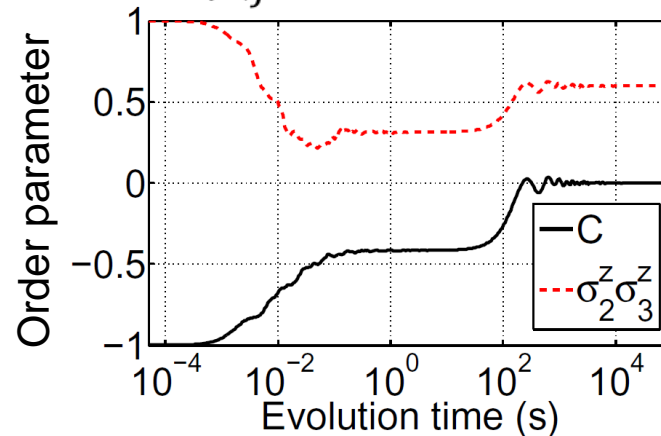
→ Eigenstate Thermalization Hypothesis (Rigol et al., *Nature* 2008)

How can quantum systems **fail** to thermalize?

Prethermalization

XY Model with inhomogeneous couplings

$$H_{XY} = \sum_{i < j} J_{ij} (\sigma_x^i \sigma_x^j + \sigma_y^i \sigma_y^j)$$



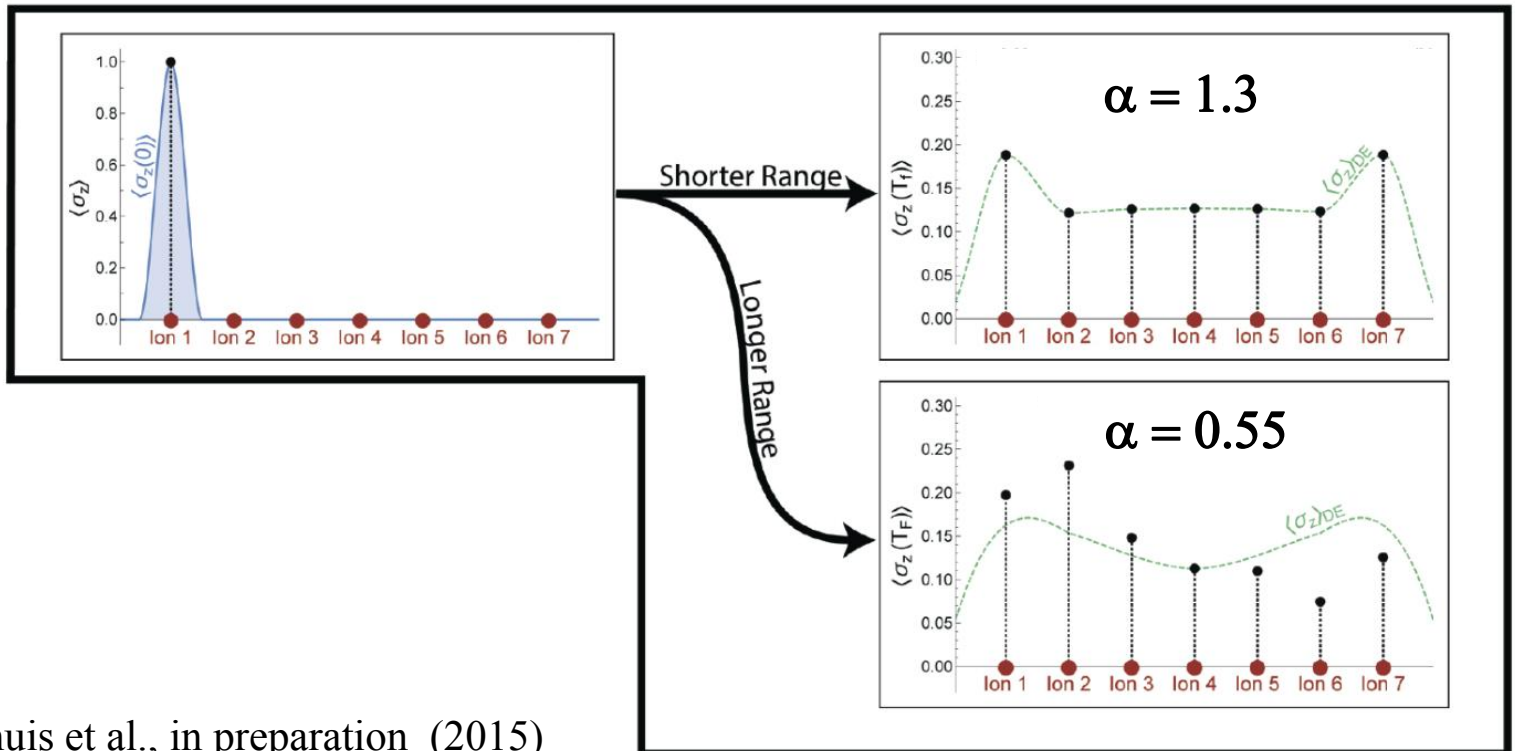
# Prethermalization

Step 1: Initialize with localized excitation 

Step 2: Evolve under variable-range XY model

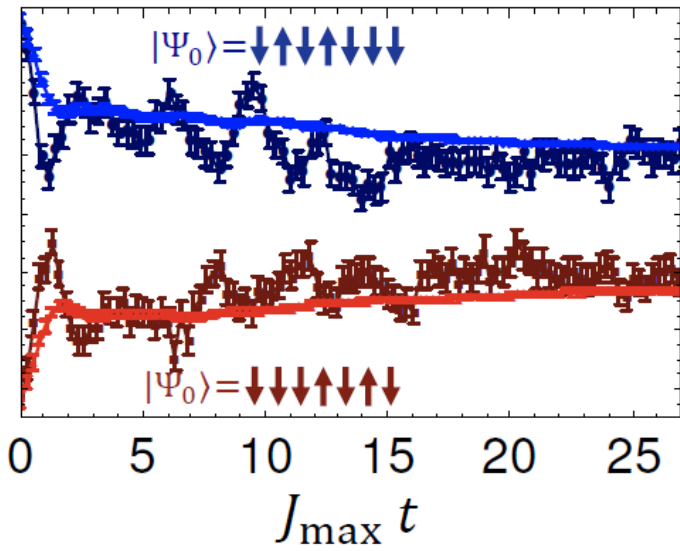
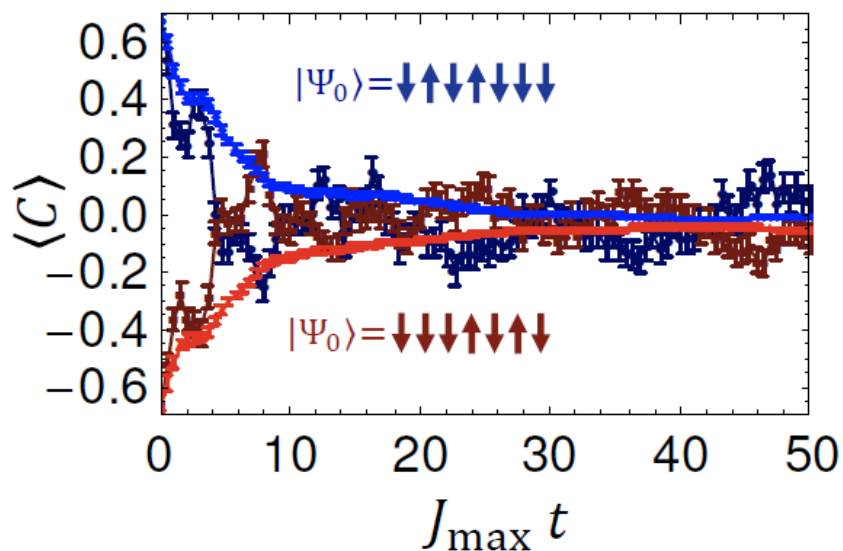
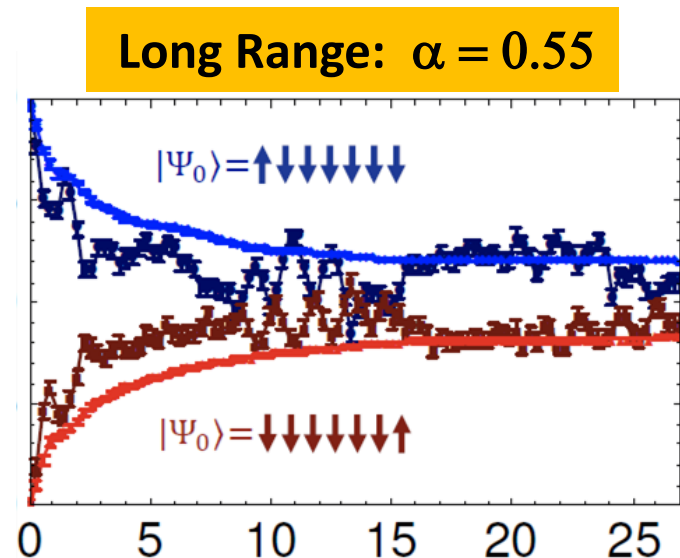
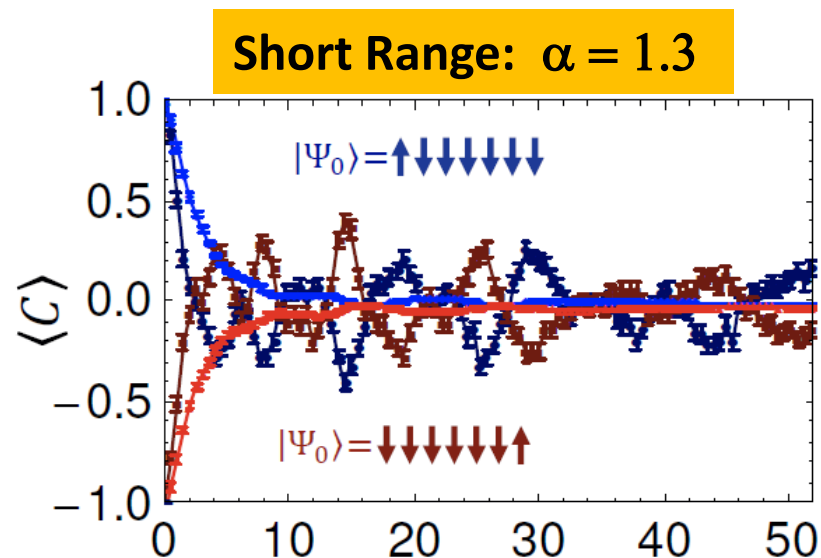
$$H_{XY} = \sum_{i < j} \frac{J_0}{|i - j|^\alpha} (\sigma_x^i \sigma_x^j + \sigma_y^i \sigma_y^j)$$

Step 3: Measure spins after time  $t$



Track “center” of spin excitation

$$C = \sum_{i=1}^N \left( \frac{2i - N - 1}{N - 1} \right) \frac{1 + \sigma_Z^i}{2}$$



# N=22 spins

$$H_{XY} = \sum_{i < j} \frac{J_0}{|i - j|^\alpha} (\sigma_x^i \sigma_x^j + \sigma_y^i \sigma_y^j) \quad \alpha = 0.6$$



state measured at  $J_0 t = 36$

# Thermalization/Localization

How can quantum systems thermalize?

→ Eigenstate Thermalization Hypothesis (Rigol et al., *Nature* 2008)

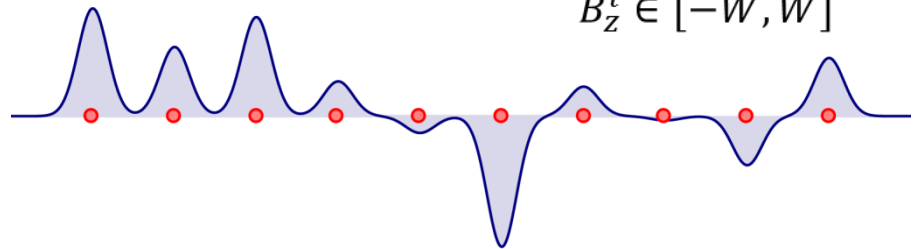
How can quantum systems **fail** to thermalize?

## Many-Body Localization

- Ising Model with random disorder

$$H_{MBL} = \sum_{i < j} J_{ij} \sigma_x^i \sigma_x^j + \sum_i \tilde{B}_Z^i \sigma_z^i$$

↓  
 $\tilde{B}_Z^i \in [-W, W]$



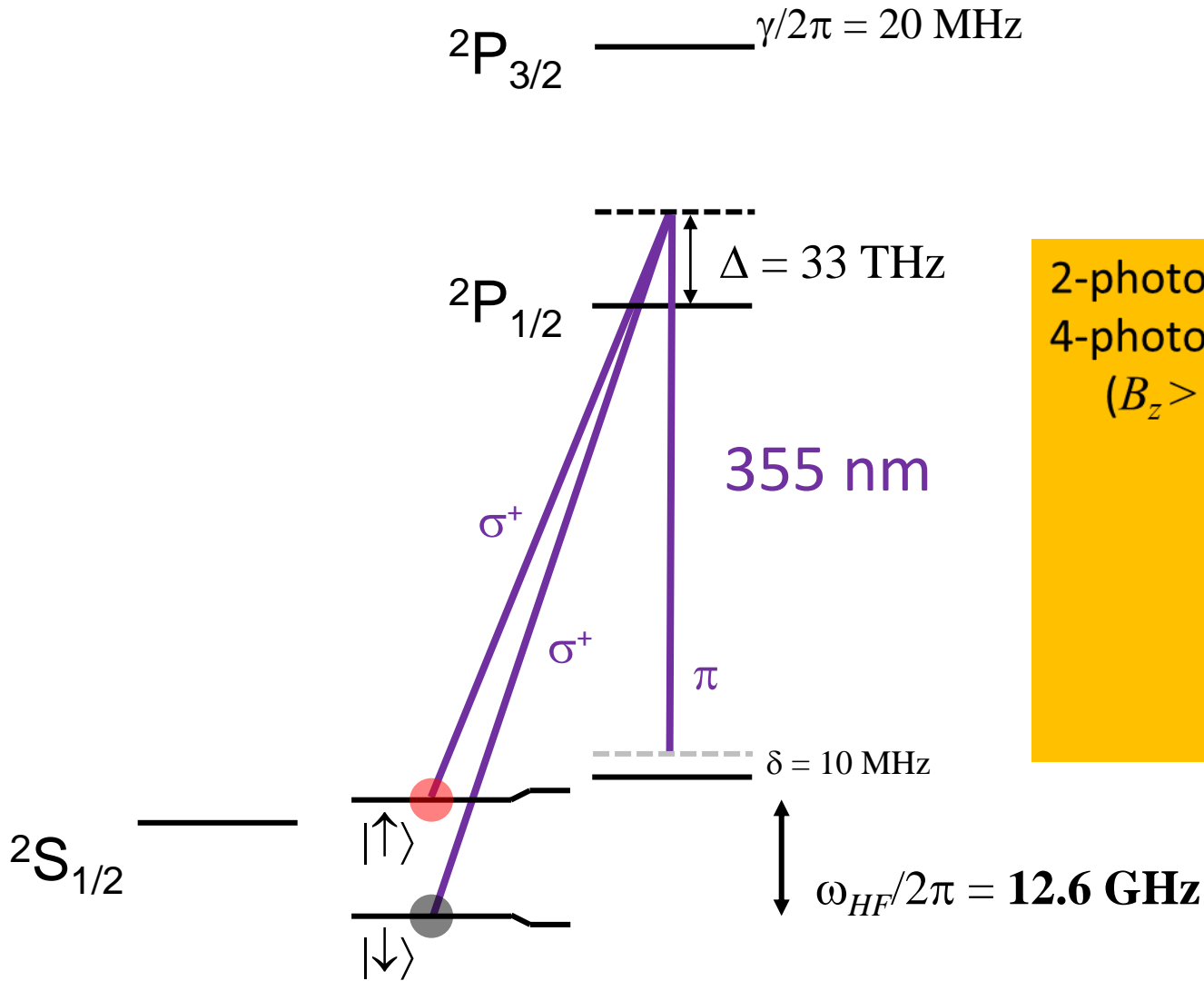
A. Polkovnikov et al., *Rev. Mod. Phys.* **83**, 863 (2011)

P. Hauke and M. Heyl, arXiv:1410.1491 (2014)

Exp: W. R. McGehee, et al., *PRL* 111, 145303 (2014)

Exp: M. Schreiber, et al., *Science* 349, 842 (2015)

# $^{171}\text{Yb}^+$ site-resolved field $\sigma_z$



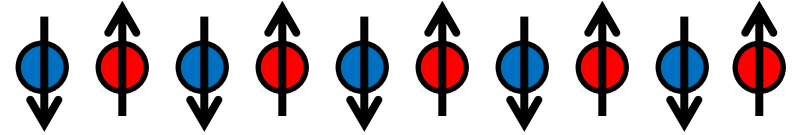
2-photon Stark shift  $\sim 100\text{Hz}$   
 4-photon Stark shift HUGE  
 ( $B_z > 1000 J$  possible)

$$J \sim \frac{\eta^2 g^4}{\omega_t \Delta^2}$$

$$B_z \sim \frac{g^4}{\delta \Delta^2}$$

# Many Body Localization (N=10)

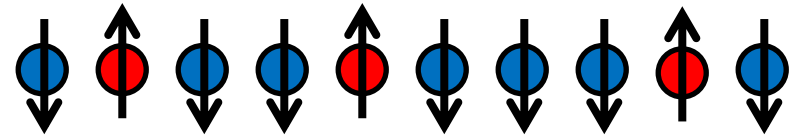
**Step 1:** Initialize spins staggered along z (“ $kT=\infty$ ”)



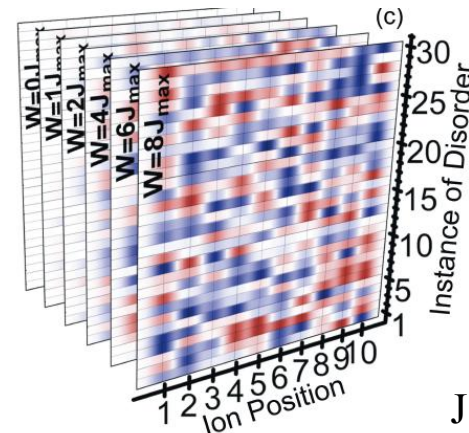
**Step 2:** Quench to transverse Ising model with random disorder

$$H_{MBL} = \sum_{i<j} J_{ij} \sigma_x^i \sigma_x^j + B \sum_i \sigma_z^i + \sum_i \tilde{B}_z^i \sigma_z^i \quad \tilde{B}_z^i \in [-W, W]$$

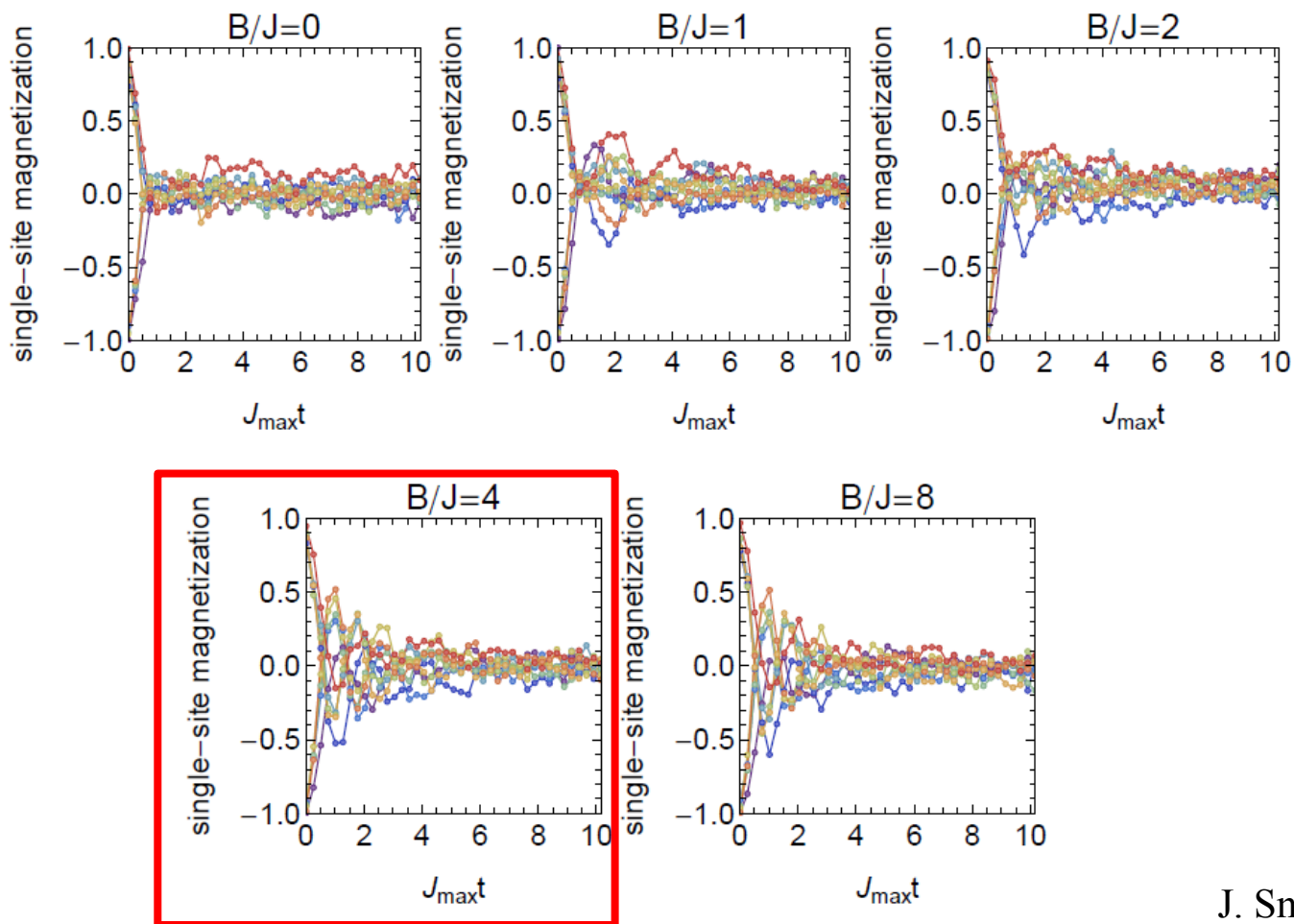
**Step 3:** Measure each spin along z after time  $t$



**Step 4:** Repeat for many different disorder instances and strengths



$$H = \sum_{i < j} J_{ij} \sigma_x^i \sigma_x^j + B \sum_i \sigma_z^i \quad (\text{no disorder})$$

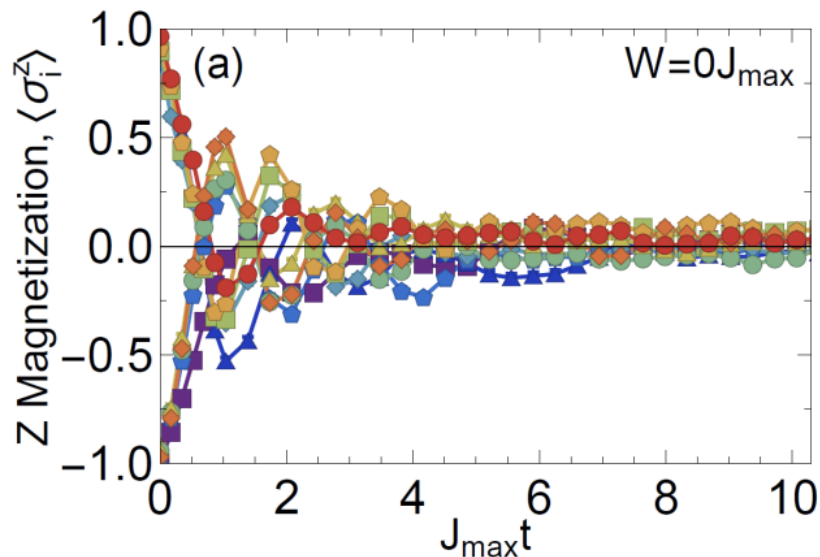




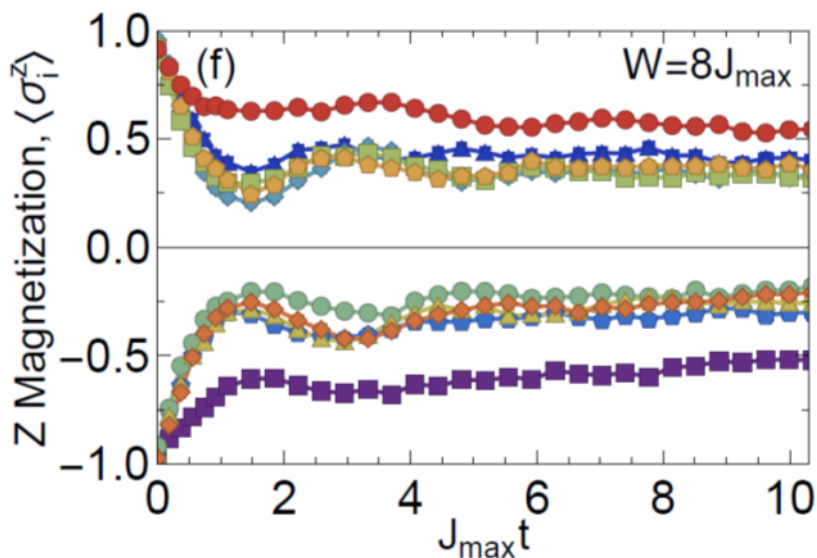
$$H = \sum_{i<j} J_{ij} \sigma_x^i \sigma_x^j + B \sum_i \sigma_z^i + \sum_i \tilde{B}_z^i \sigma_z^i \quad \tilde{B}_z^i \in [-W, W]$$

$$H = \sum_{i<j} J_{ij} \sigma_x^i \sigma_x^j + B_y \sin(\omega t) \sum_i \sigma_y^i$$

**No disorder**

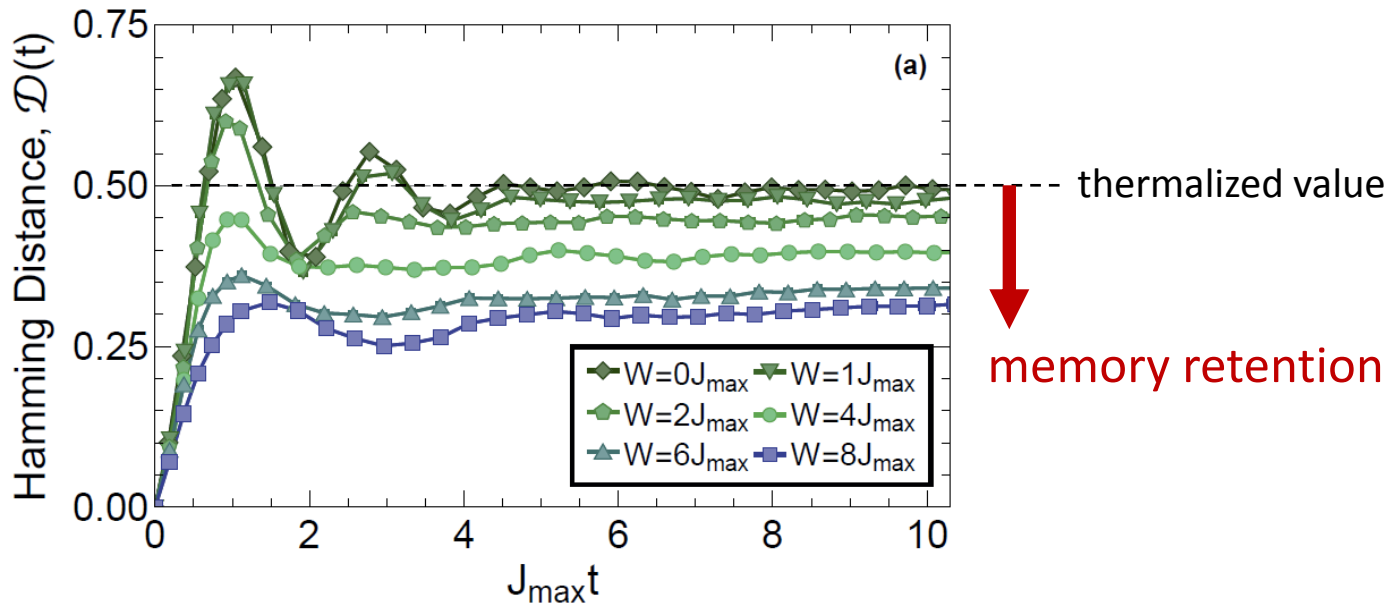


**Some disorder**



**Hamming distance**  
from initial state:

$$\mathcal{D}(t) = \frac{1}{2} - \frac{1}{2N} \sum_i \langle \psi_0 | \sigma_i^z(t) \sigma_i^z(0) | \psi_0 \rangle$$

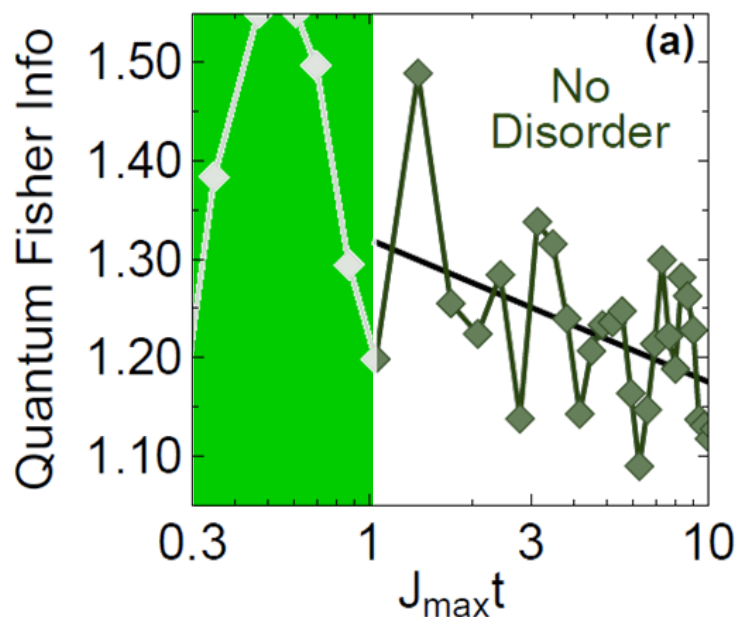


# Quantum Fisher Information: characterizes system entanglement

$$F_Q = 4N^2(\Delta\hat{D})^2 = \sum_{i,j} [(-1)^{i+j} \langle \sigma_i^z \sigma_j^z \rangle] - \left[ \sum_i (-1)^i \langle \sigma_i^z \rangle \right]^2$$

Braunstein and Caves Phys. Rev. Lett. 72, 3439 (1994)

Hauke, Heyl, Tagliacozzo, Zoller, arXiv:1509.01739 (2015)



**T**rapped Ion Spin Hamiltonian Engineering

**G**round states and Adiabatic Protocols

**D**ynamics

Many-Body Spectroscopy

Propagation of Excitations: Lieb-Robinson

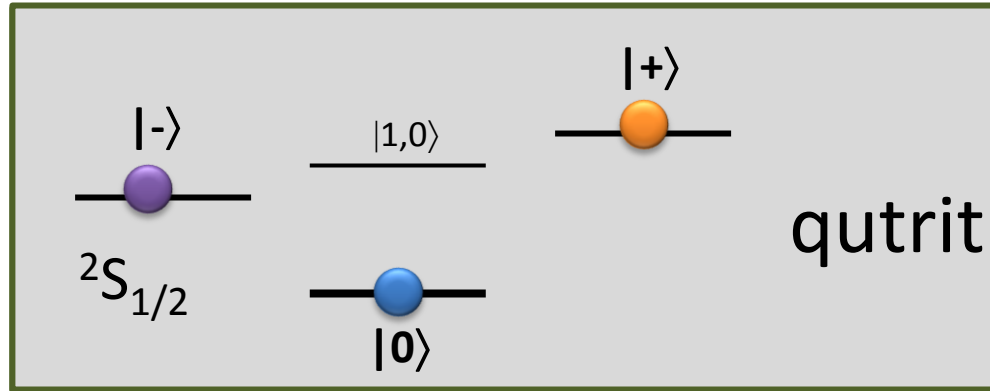
Prethermalization

Many-Body Localization

**S**pin-1

**E**xtending to  $N \sim 100$  spins and beyond

# Quantum simulations with Spin-1



rsb+bsb on  
both transitions

$$H = \sum_{i,j} J_{ij} S_x^i S_x^j$$

rsb  $|0\rangle \leftrightarrow |+\rangle$   
bsb  $|0\rangle \leftrightarrow |-\rangle$

$$H = \sum_{i,j} J_{ij} (S_+^i S_-^j + S_-^i S_+^j) + D \sum_i (S_z^i)^2 + \sum_{i,m} V_{im} (2\hat{n} + 1) S_z^i$$

$$J_{ij} \approx \frac{J_0}{r^\alpha}$$

Work in  $\langle S_z^i \rangle = 0$  subspace:  $\frac{3^N}{2\sqrt{N}}$  states

**T**rapped Ion Spin Hamiltonian Engineering

**G**round states and Adiabatic Protocols

**D**ynamics

Many-Body Spectroscopy

Propagation of Excitations: Lieb-Robinson

Prethermalization

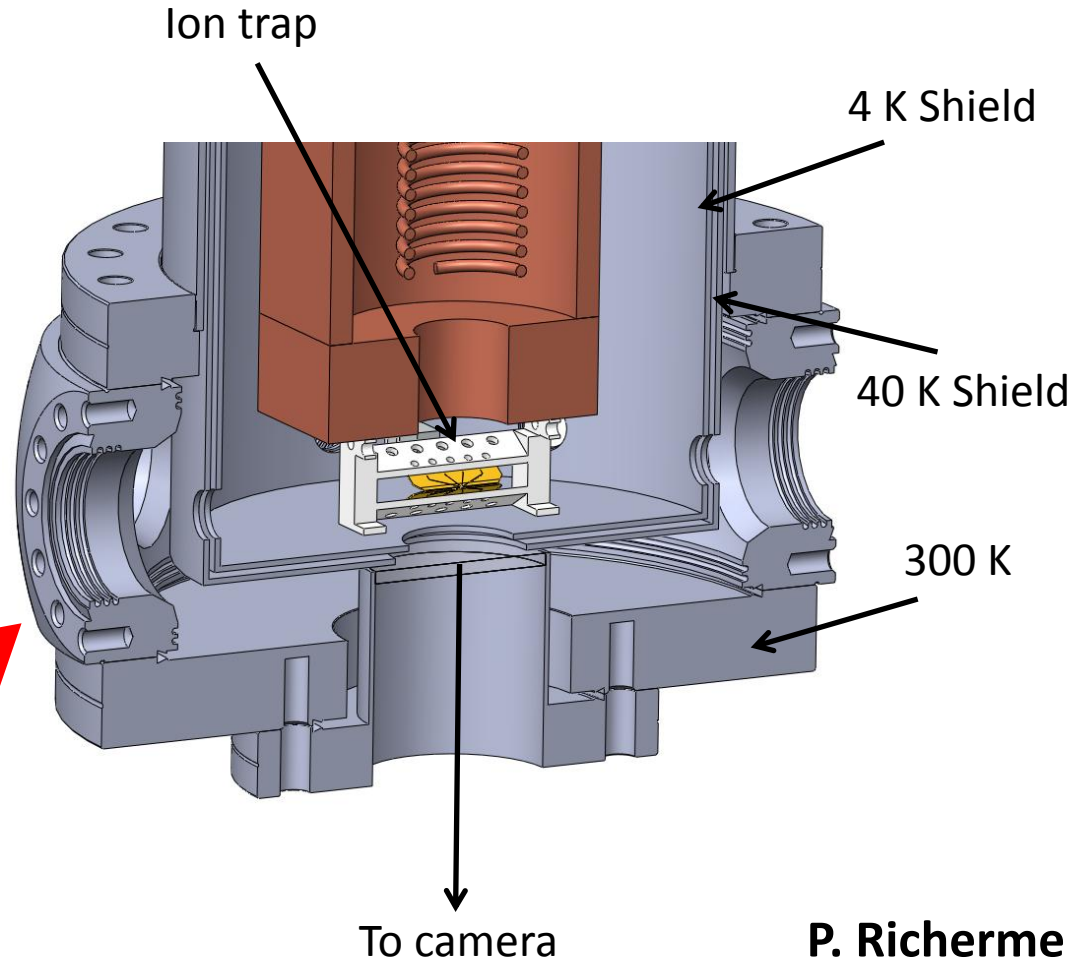
Many-Body Localization

**S**pin-1

**E**xtending to  $N \sim 100$  spins and beyond

# Scaling Up: 4K to get lower pressure

50-100 spins SOON



**P. Richerme**  
**P. Hess**

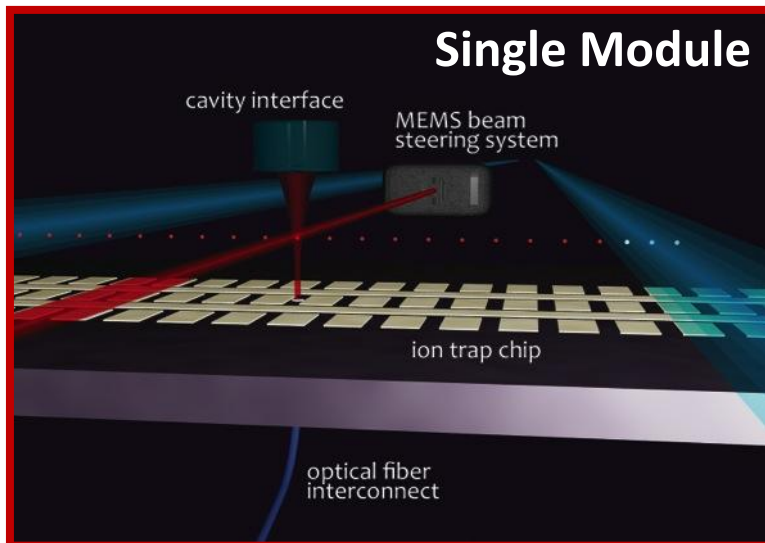
# Modular Scaling to $10^6$ qubits?

## Quantum Computation in Small Quantum Registers

- Linear ion chain with 20-100 ions (Elementary Logic Unit, or ELU)
- **Arbitrary quantum logic operation among the qubits in the chain**

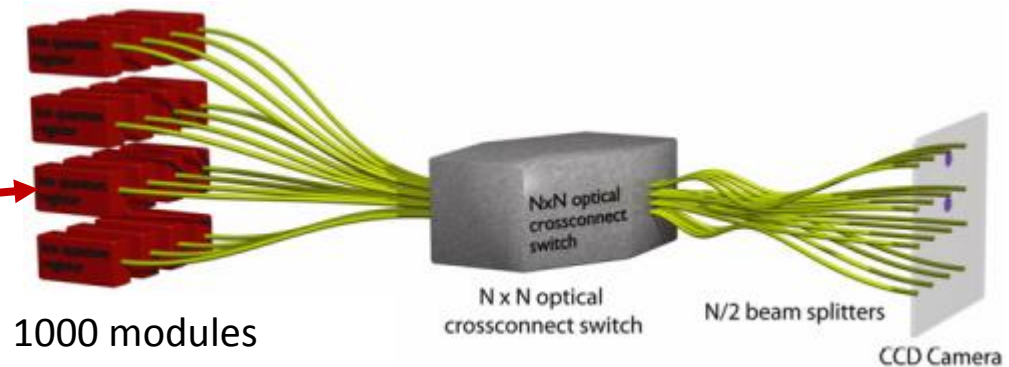
## Interconnect of Multiple Such Registers via Photonic Channel

- Reconfigurable interconnect using optical crossconnect switches
- **Efficient optical interface for remote entanglement generation**

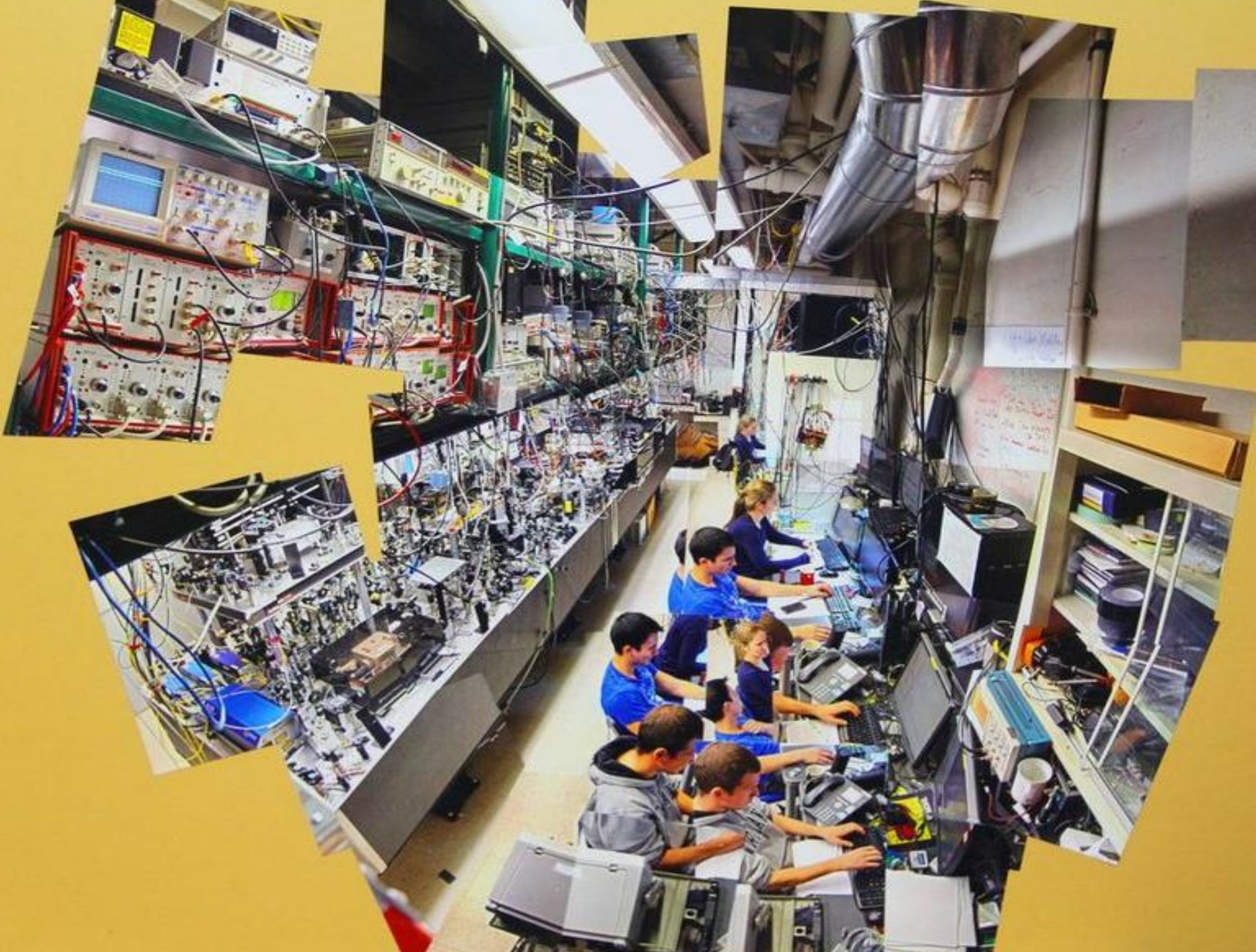


100 qubits / module

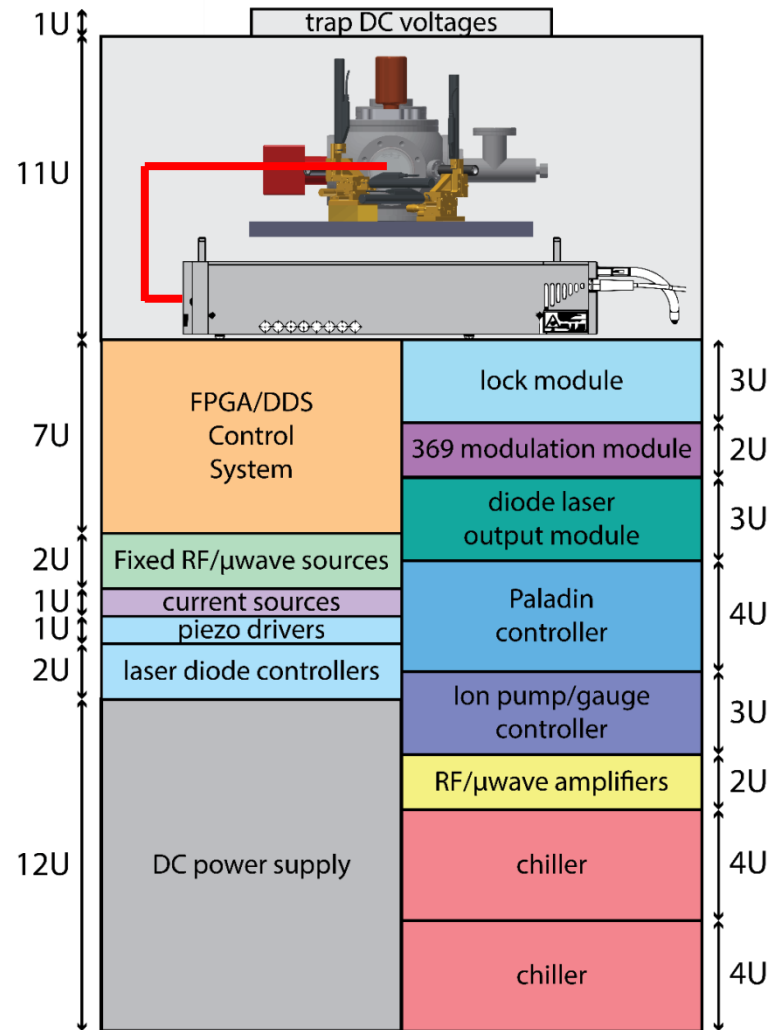
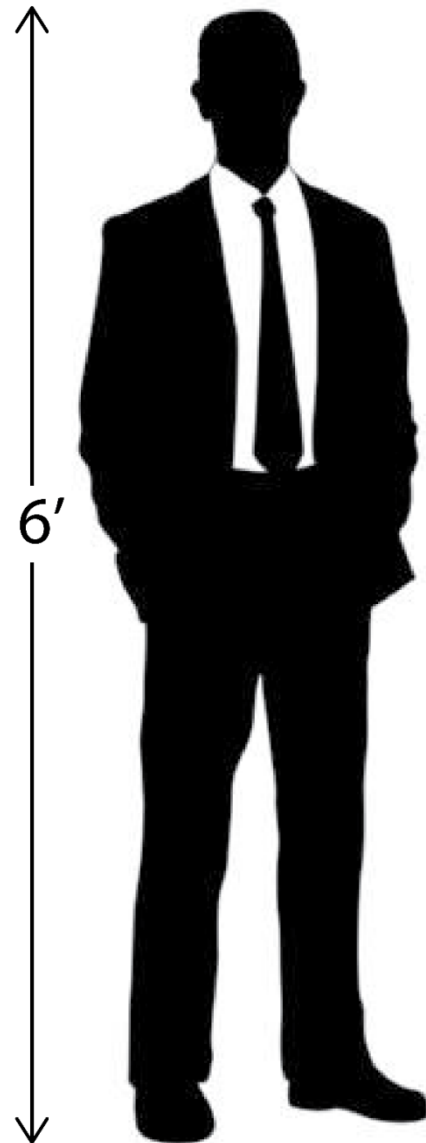
## 100,000 qubit quantum computer?





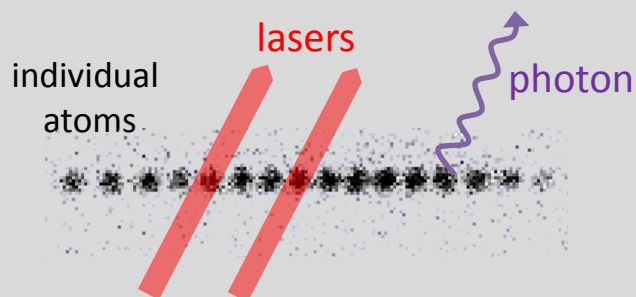


# Single Module ~100 spins on 2 × 19" Racks



# Leading Quantum Computer Hardware Candidates

## Trapped Atomic Ions



Atomic qubits connected through laser forces on motion or photons

### FEATURES & STATE-OF-ART

- very long ( $\gg 1$  sec) memory
- 5-20 qubits demonstrated
- **atomic qubits all identical**
- **connections reconfigurable**

### CHALLENGES

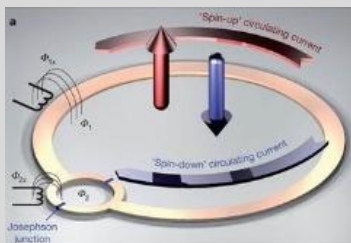
- lasers & optics
- high vacuum
- 4K cryogenics
- **engineering needed**

### Investments:

IARPA  
GTRI  
Sandia

Lockheed  
UK Gov't

## Superconducting Circuits



Superconducting qubit:  
right or left current

### FEATURES & STATE-OF-ART

- connected with wires
- fast gates
- 5-10 qubits demonstrated
- **printable circuits and VLSI**

### CHALLENGES

- short ( $10^{-6}$  sec) memory
- 0.05K cryogenics
- **all qubits different**
- **not reconfigurable**

### LARGE

### Investments:

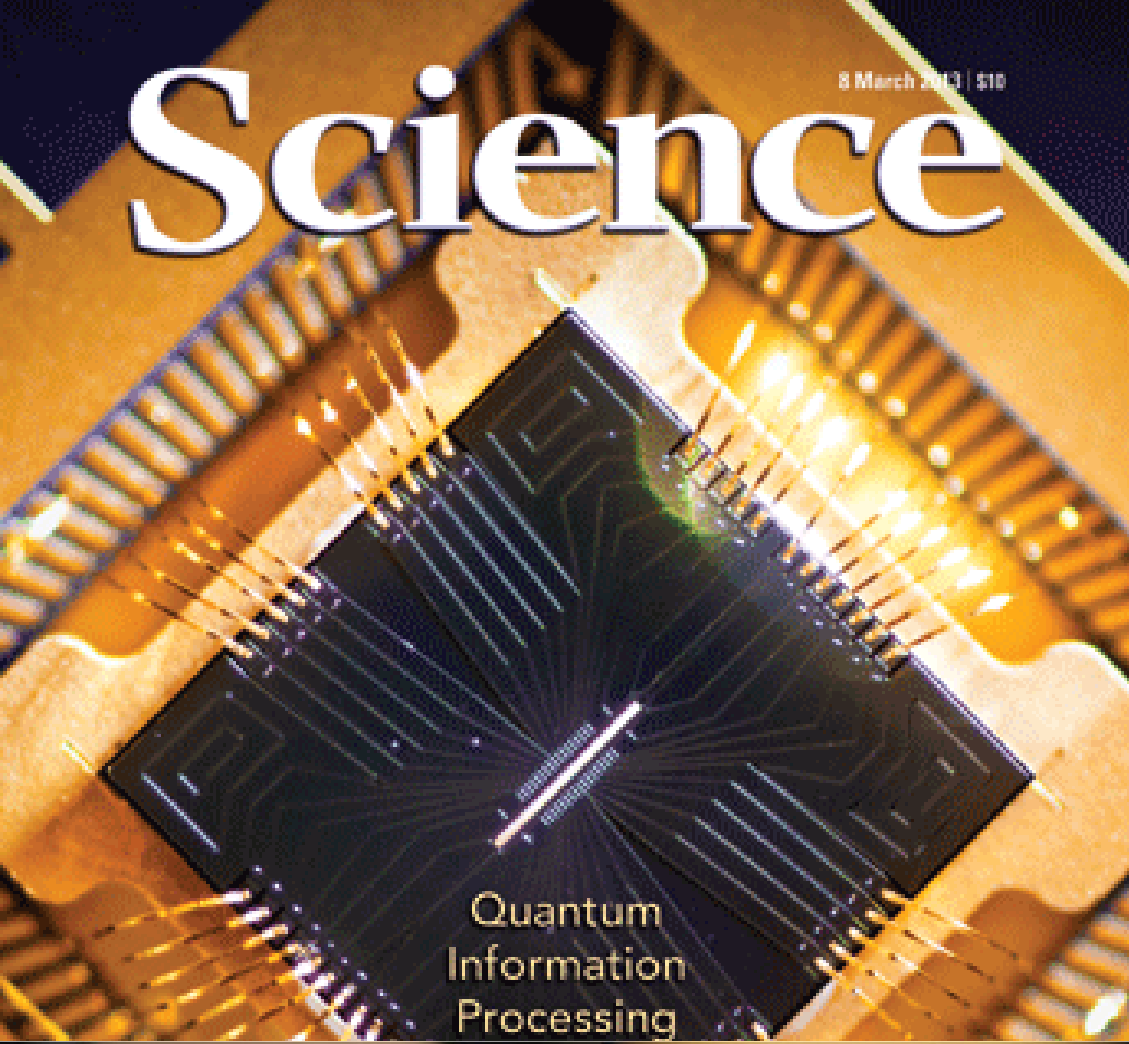
Google/UCSB    IBM  
Lincoln Labs    Intel/Delft

## Others: still exploratory

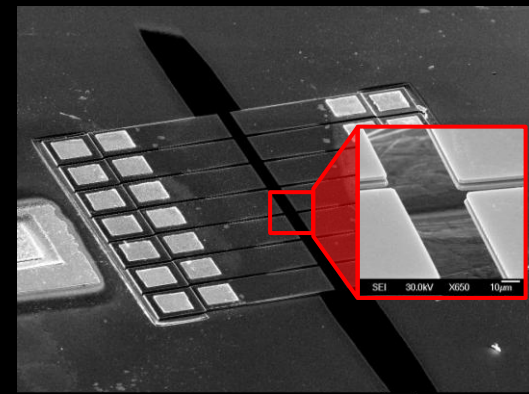
- NV-Diamond
- Semiconductor quantum dots
- Atoms in optical lattices

# Science

8 March 2013 | \$10



Quantum  
Information  
Processing



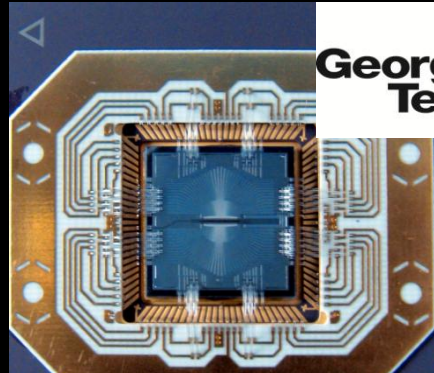
LPS SEI 30.0kV X80 100µm WD 29.2mm



Univ. of  
Maryland

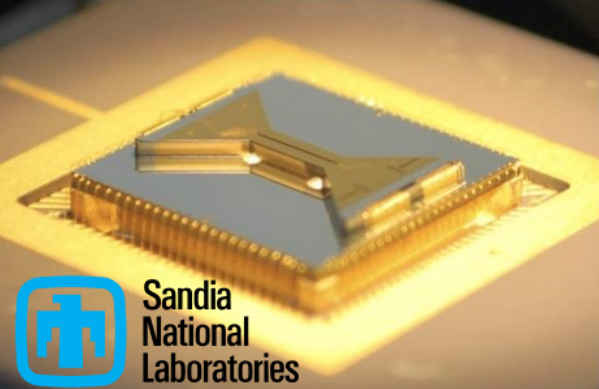
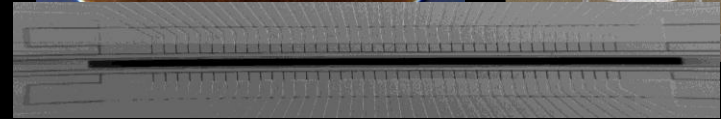


The Laboratory for Physical Sciences

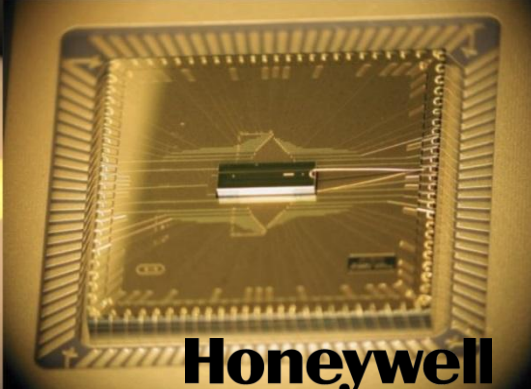


Georgia  
Tech

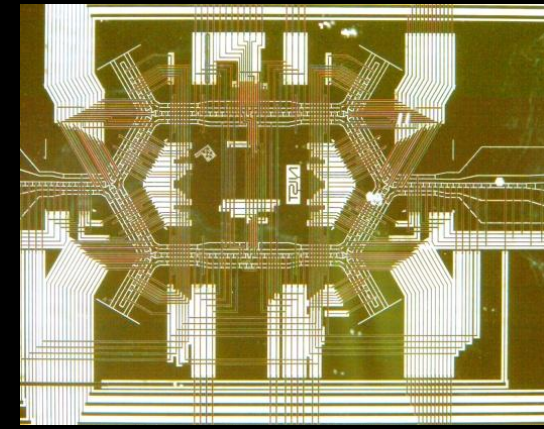
Research  
Institute



Sandia  
National  
Laboratories



Honeywell



NIST  
Boulder



# T1Q1 Trapped Ion Quantum Information



[www.iontrap.umd.edu](http://www.iontrap.umd.edu)

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**Crystal Senko (→ Harvard)**

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**Jake Smith**

Ken Wright

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**Jiehang Zhang**

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**Alexey Gorshkov (JQI/NIST)**

**Alex Retzker (Hebrew U)**



LPS/NSA



ARO

