

Many-Body Localization by DMRG and ED Studies

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KITP workshop

Research is supported by NSF

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CSUN)**

Preprints: [ArXiv1509.06786](https://arxiv.org/abs/1509.06786); [1510.08145](https://arxiv.org/abs/1510.08145)

Outline

Introduction: Many-body localization (MBL)
Numerical studies of MBL phase and transition
Different DMRG (MPS) for Ex-states

Our DMRG for Ex: A modified DMRG algorithm for accurately obtaining excited states

Nontrivial Distributions for MBL: for larger systems
N=24--72

Address and discuss open issues: intermediate (Griffiths) regime and phase transition-ED/DMRG

Mobility edge (large-N DMRG results and scaling)

—spin $\frac{1}{2}$ Heisenberg model in random fields

MBL phase and numerical studies

Reviews: Nandkishore & Huse (2015); Altman & Vosk (2015)

Many-body localization: an MBL at finite energy density exhibits Anderson localization

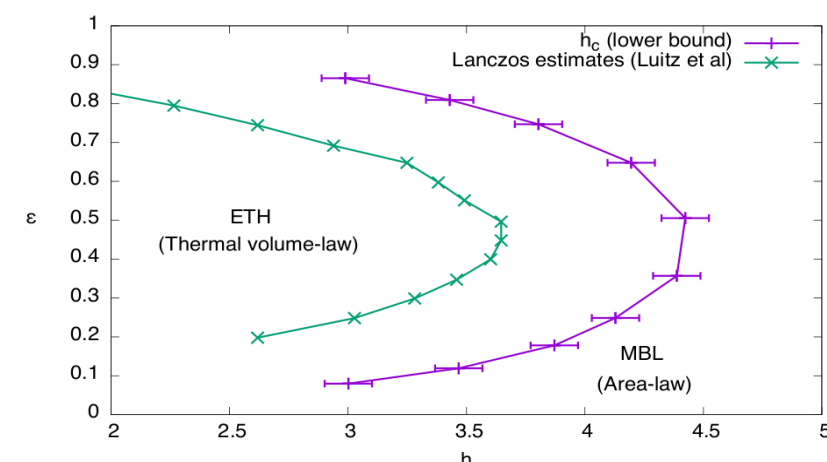
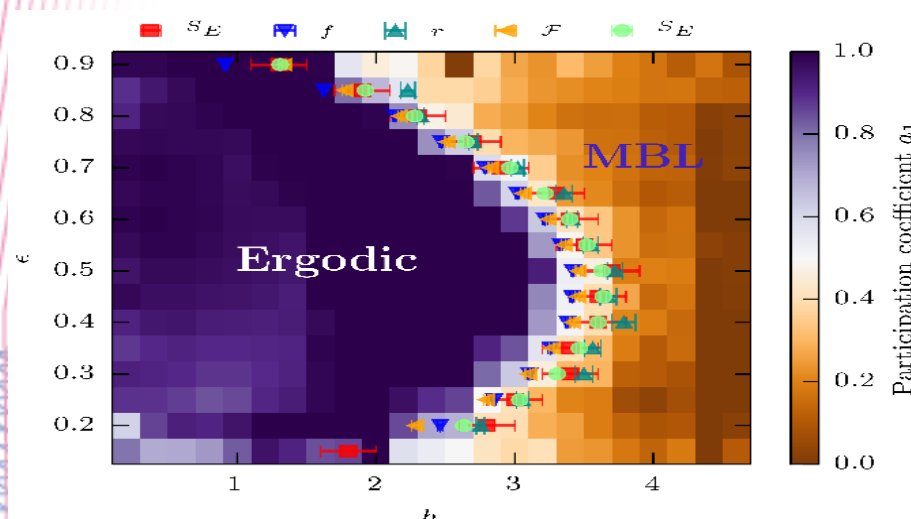
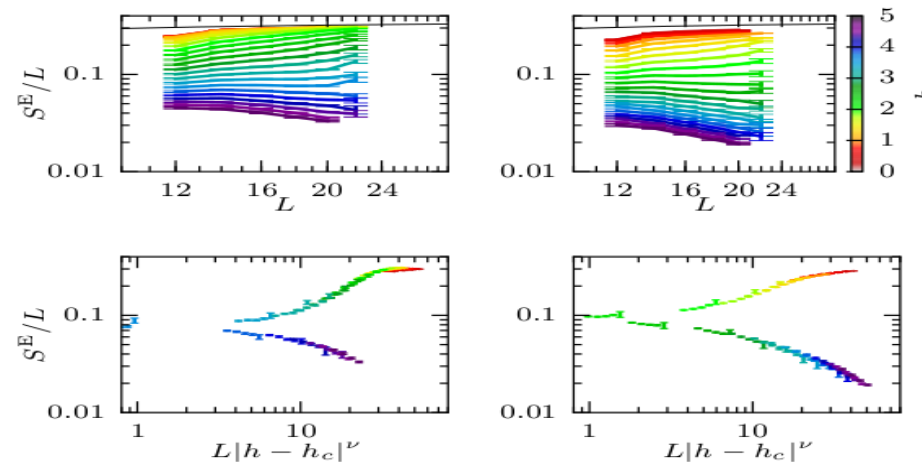
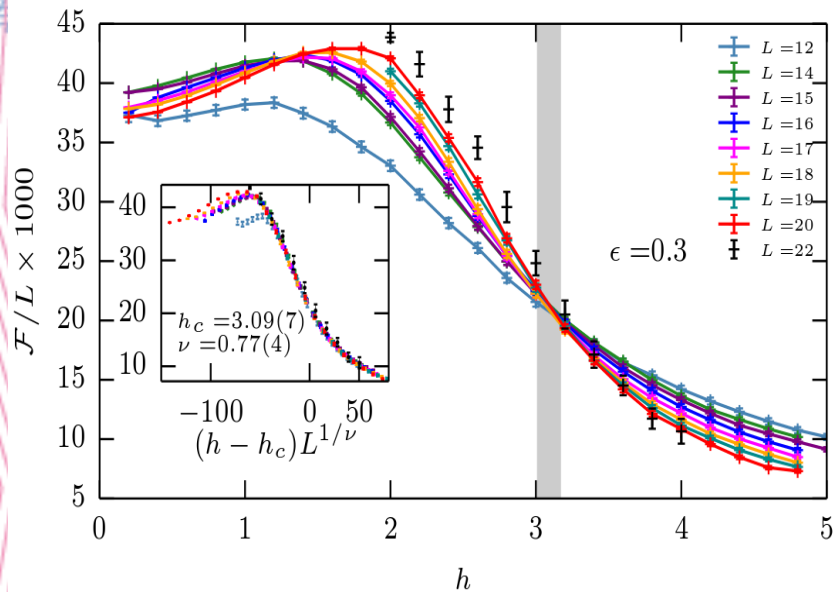
MBL cannot thermalize: this violates the interacting system “eigenstate thermalization hypothesis (ETH)”

MBL state has low entanglement ---allowing developing DMRG (MPS) related algorithms

Numerical studies of 1D models, 2-leg ladders---phases and transition. 1D: Luitz et al. (2015), Kjall et al (2014), Oganesyan & Huse (2007), Pal & Huse (2008); Monthus & Garel (2010), Iyer et al. (2013)
..... Agarwal et al, Gopalakrishnan et al, Vosk et al.,
Potter et al., Serbyn & Moore

ED studies of 1D $s=1/2$ model

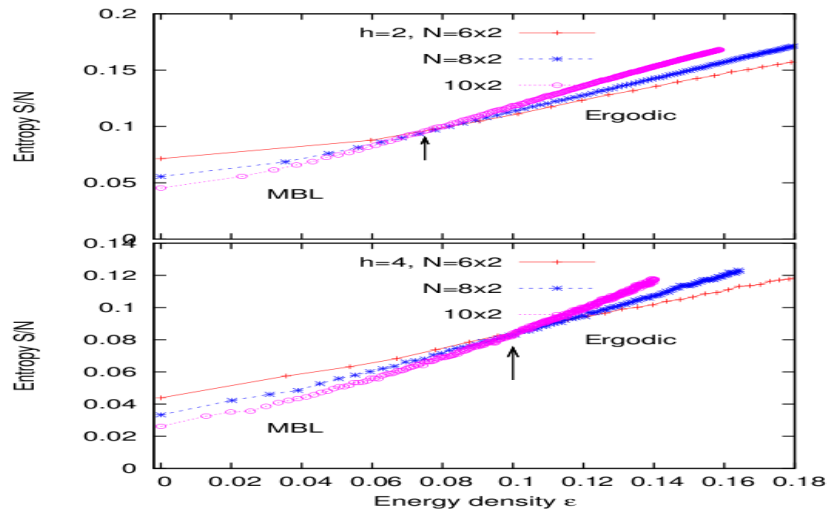
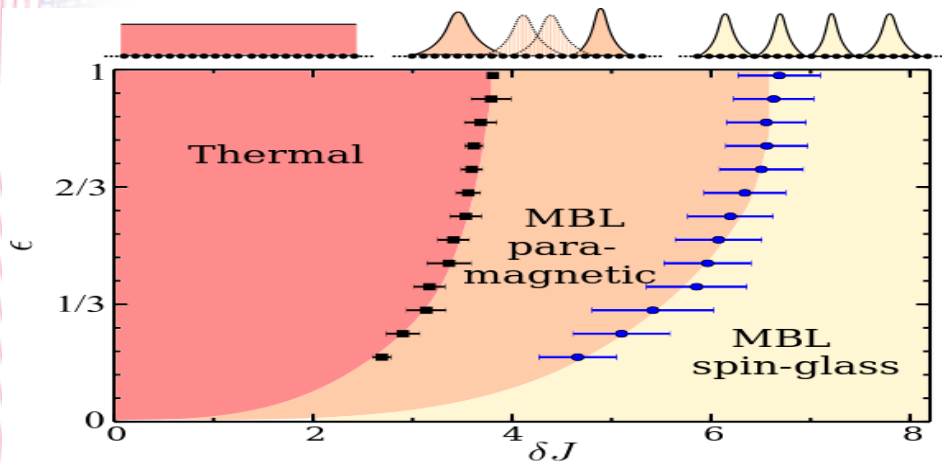
Luitz et al. 2015: Heisenberg model in random fields $N=12-22$



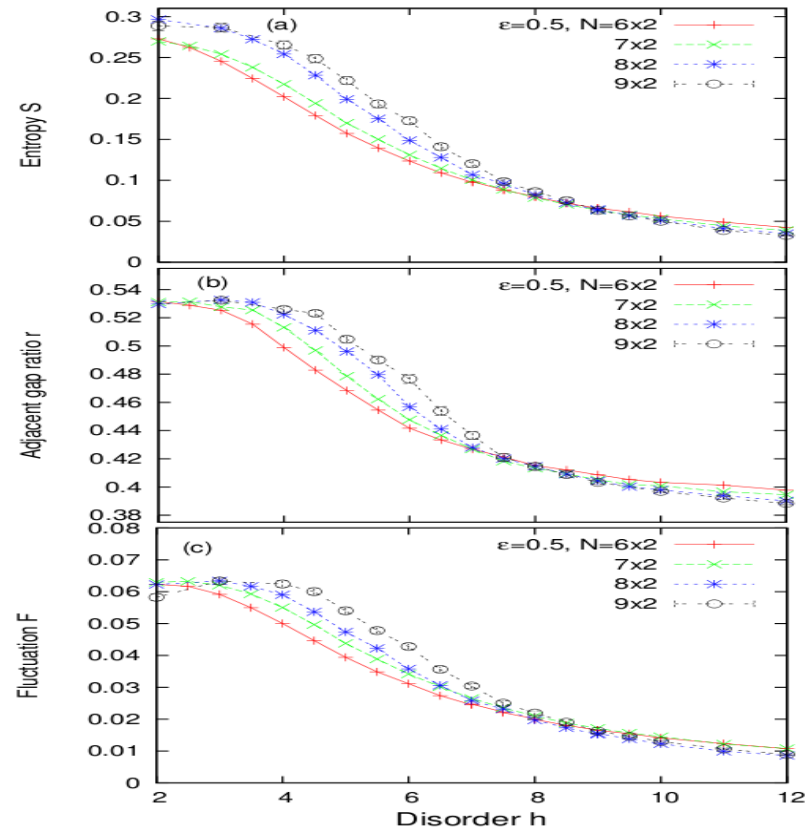
Devakul, Singh 2015: linked cluster expansion

Transitions in different models

Kjall et al (2014)

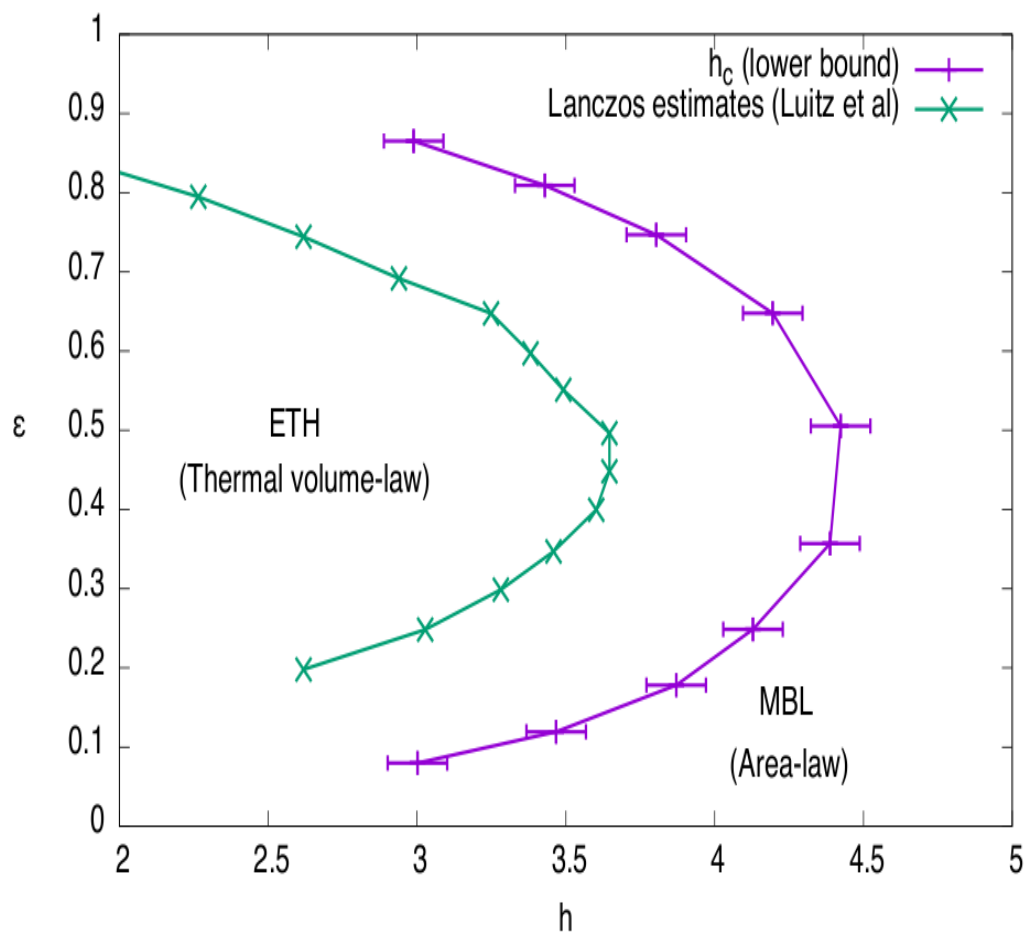


Baygan, Lim, DNS (2015)
N=12--20



Open issues about critical h_c and mobility edge may be resolved with larger system studies

Devakul, Singh 2015



Open issues regarding transition
Agarwal et al, Gopalakrishnan et al,
Vosk et al., Potter et al.,
Serbyn & Moore

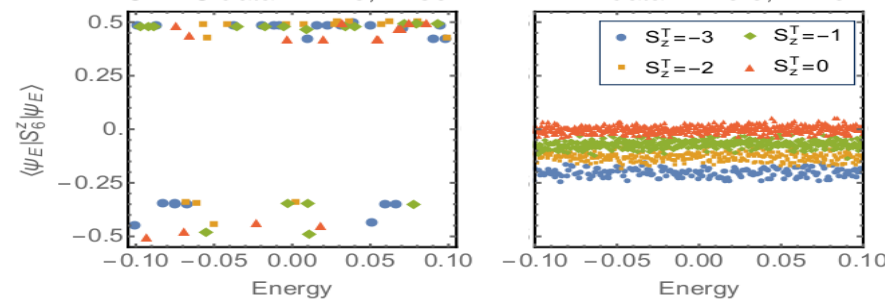
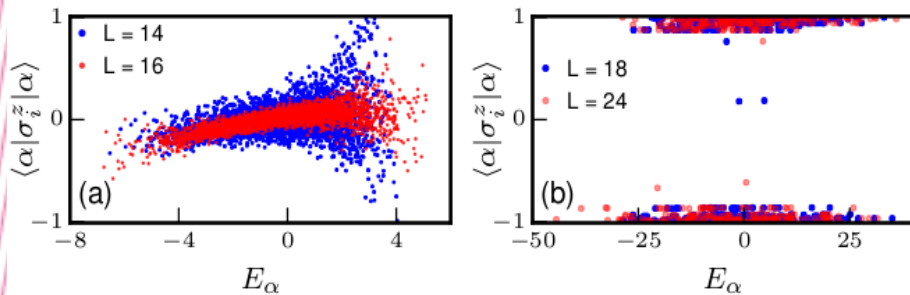
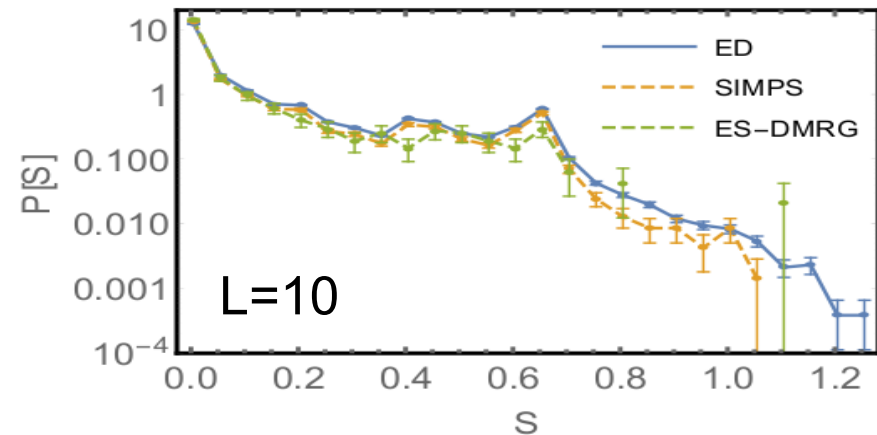
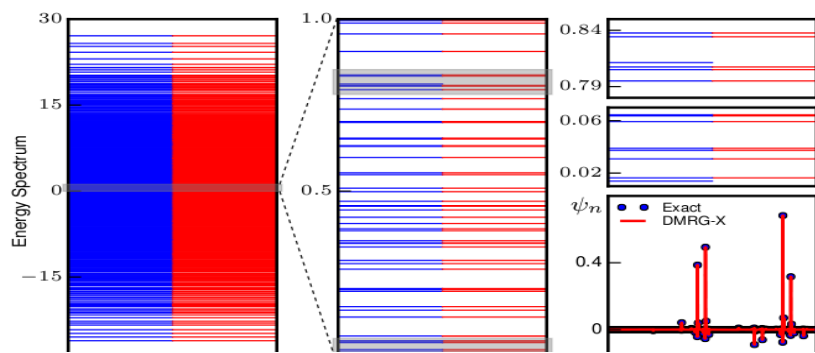
Mobility edge—role of rare
Regions

Laumann et al.
Huang
Vosk et al.
de Roeck et al.
Mondragon-Shem et al.
.....

Some DMRG methods for excited states

Khemani, Pollmann, Sondhi,
arXiv1509.00483

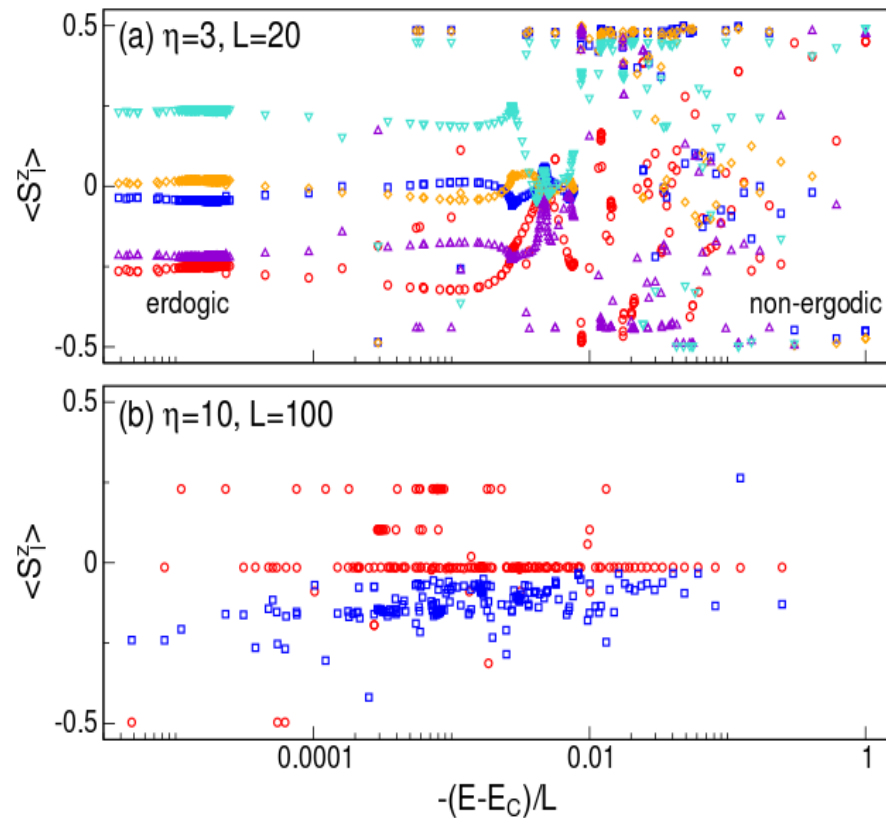
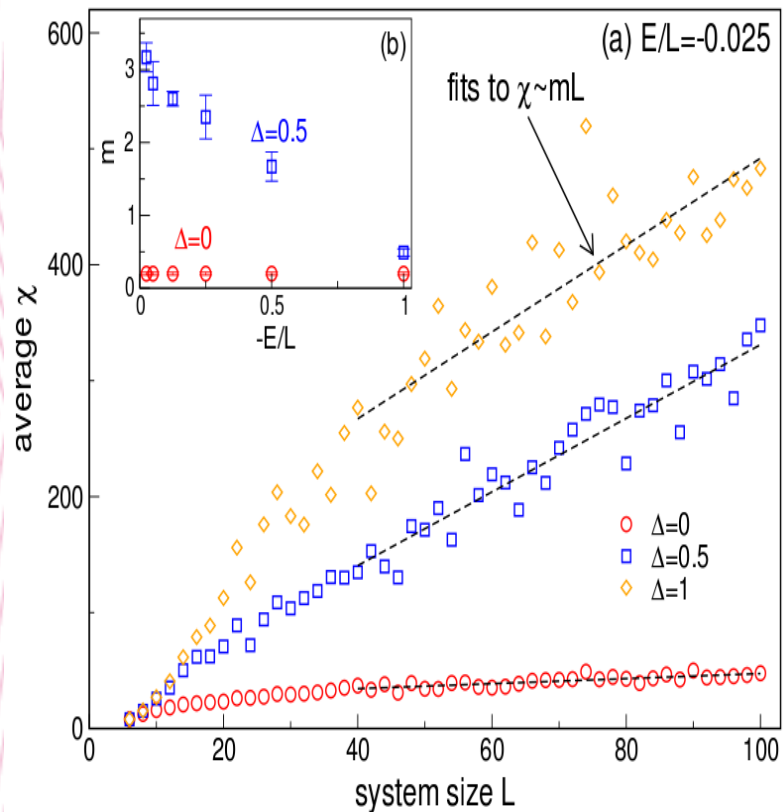
Yu, Pekker, Clark
arXiv1509.01244



There are also other developments: Pekker & Clark; Friesdorf et al.
Pollmann et al.; Chandran et al.
Kennes & Karrasch

Missing statistics for larger systems—different scope than our work

Kennes & Karrasch ---targeting superposition state



Entanglement DMRG (En-DMRG) for excited states

S. R. White 1992 DMRG



Initialization: larger M-bond dimension

Sweep: growing M to capture entanglement; targeting a couple of states to reduce frustration

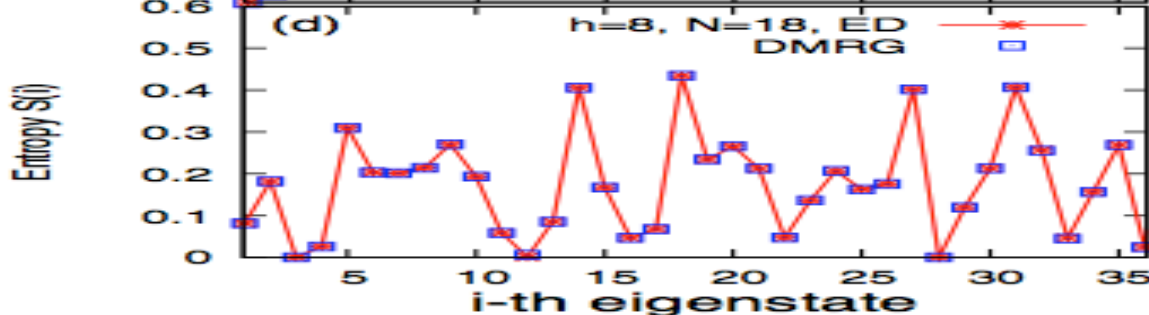
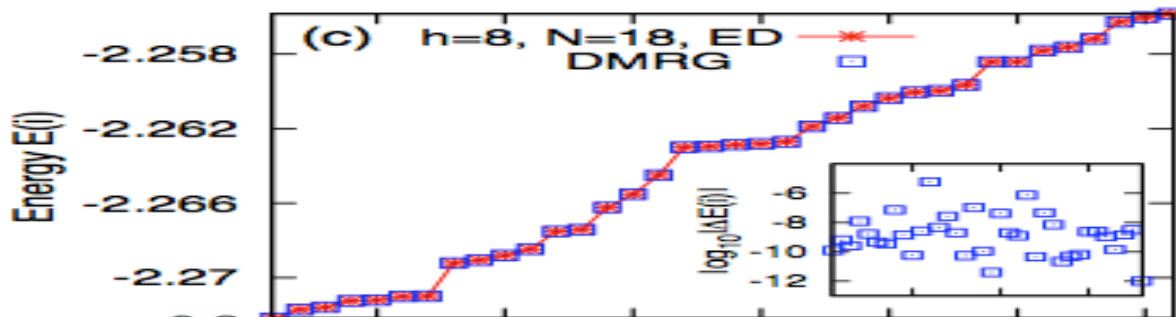
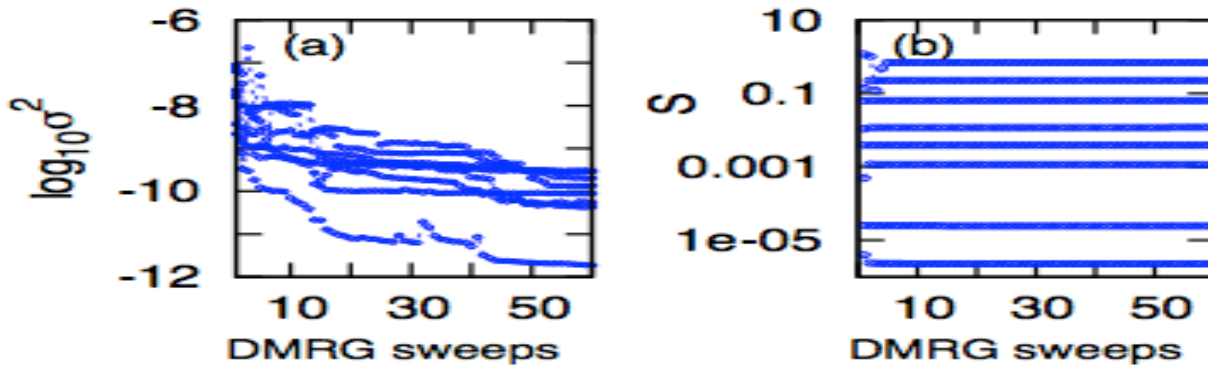
Lanczos: $H'=(H-Et)^2$ & H

Truncation error (auto)control: $<\sim 10^{(-8)}$

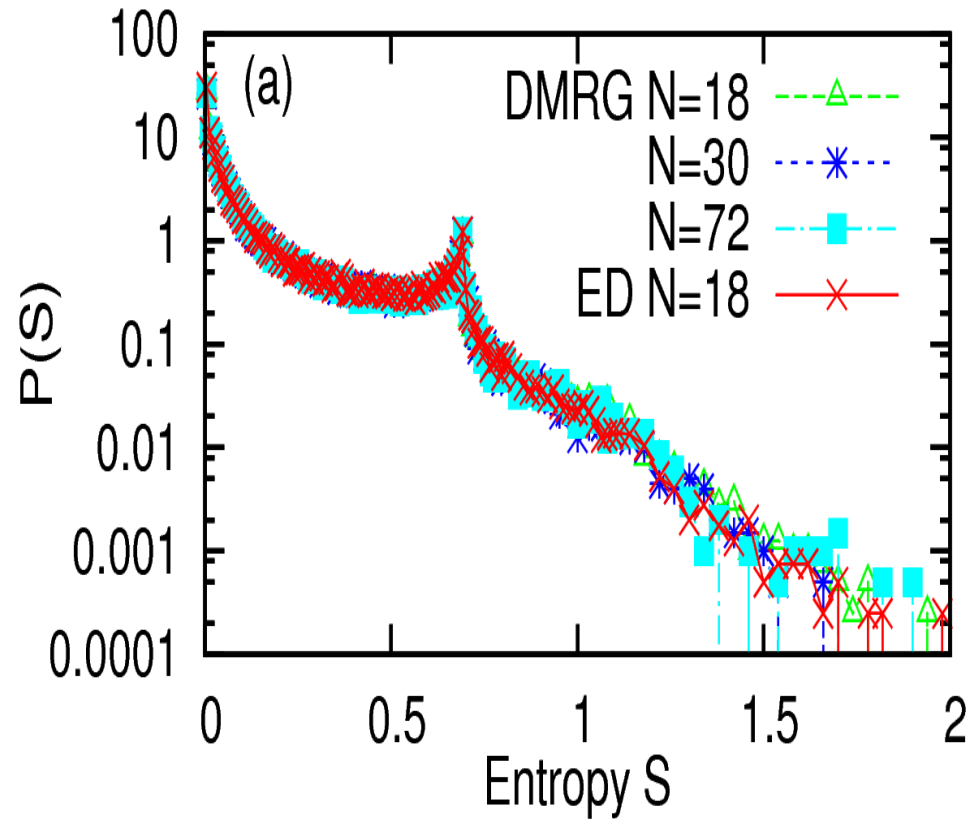
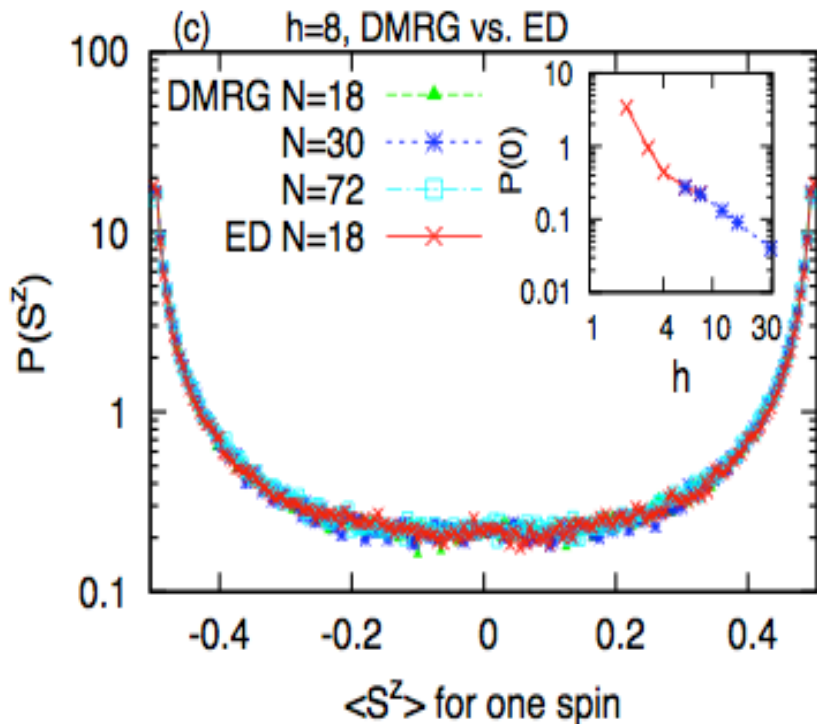
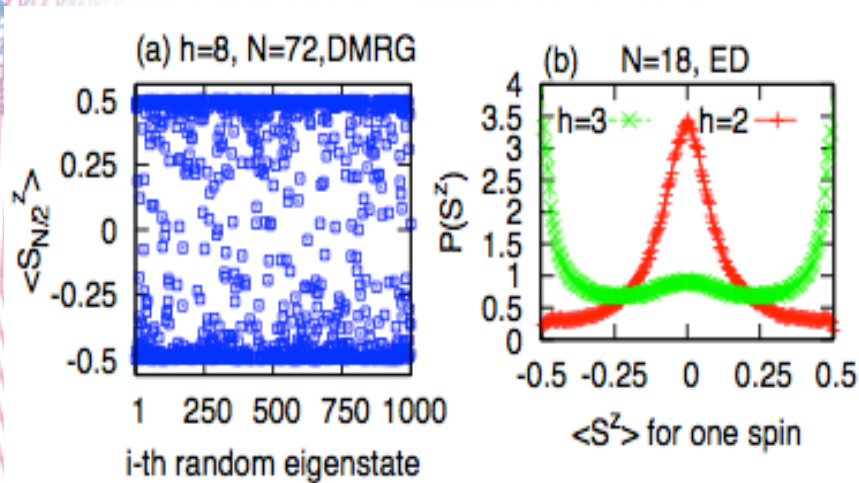
En-DMRG for excited states

$$H = \sum_{i=1}^{N-1} \vec{S}_i \cdot \vec{S}_{i+1} - \sum_i h_i S_i^z,$$

$h=8, N=72$



En-DMRG distributions functions for MBL

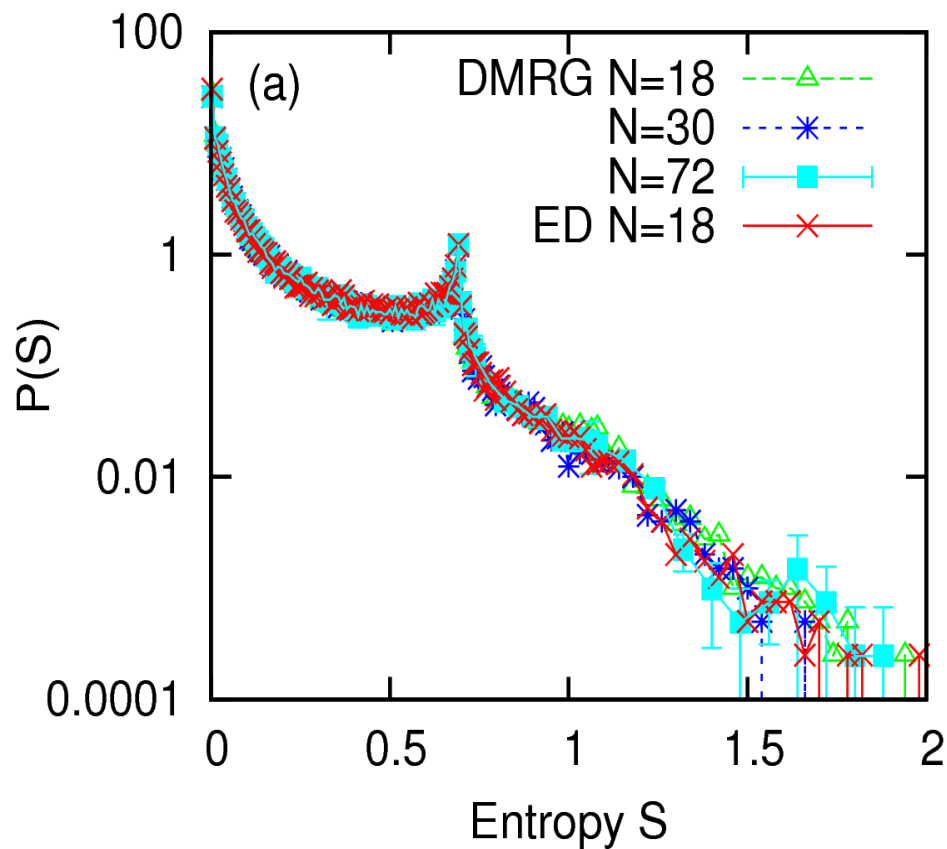
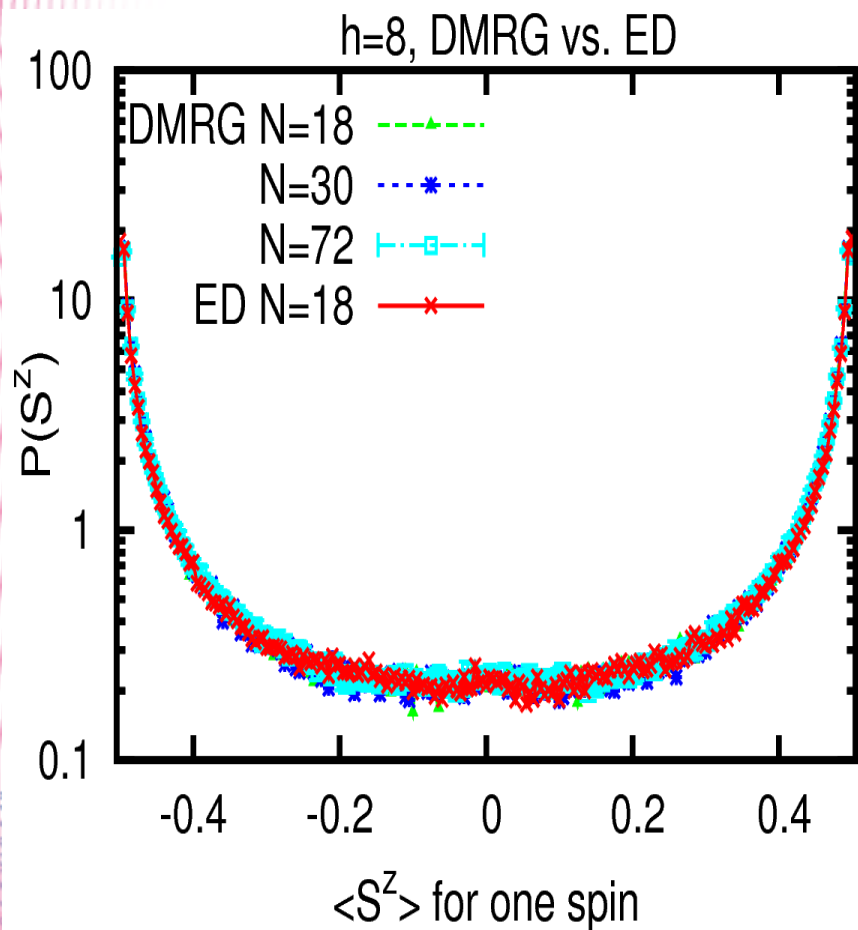


$H=8, M \sim 48-72$ (bond dim.)

Exponential decay of $P(S)$ on the larger S side

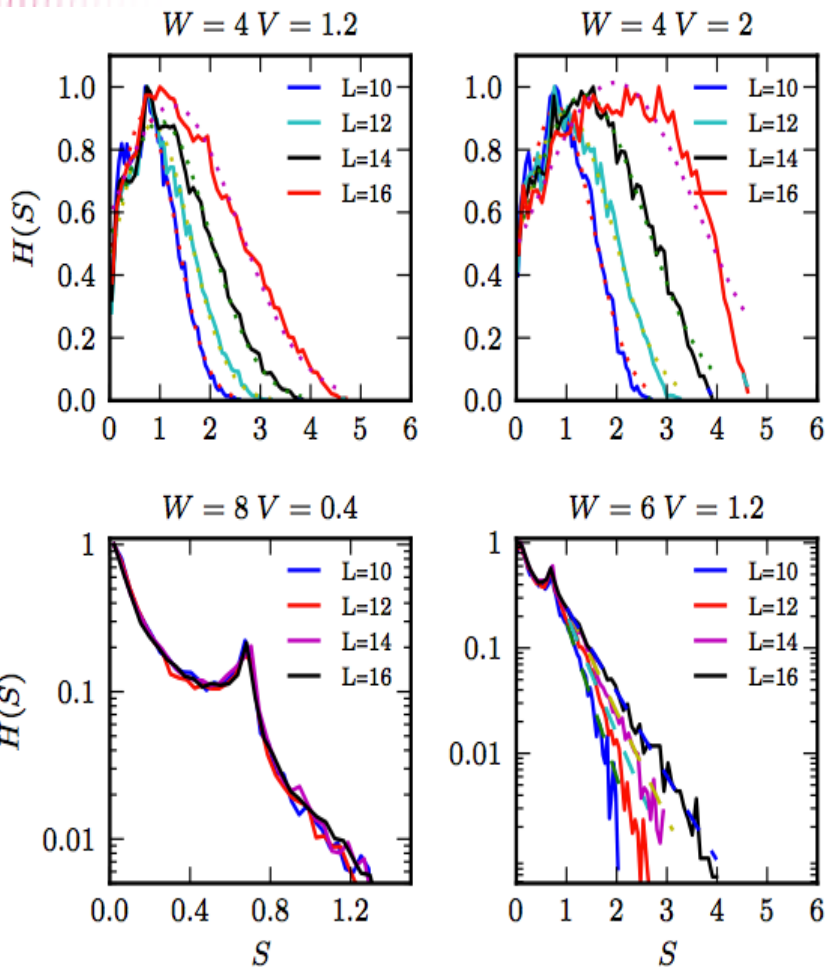
Bauer & Nayak (2013) ED

Error bar near the tail of $P(S)$ is large

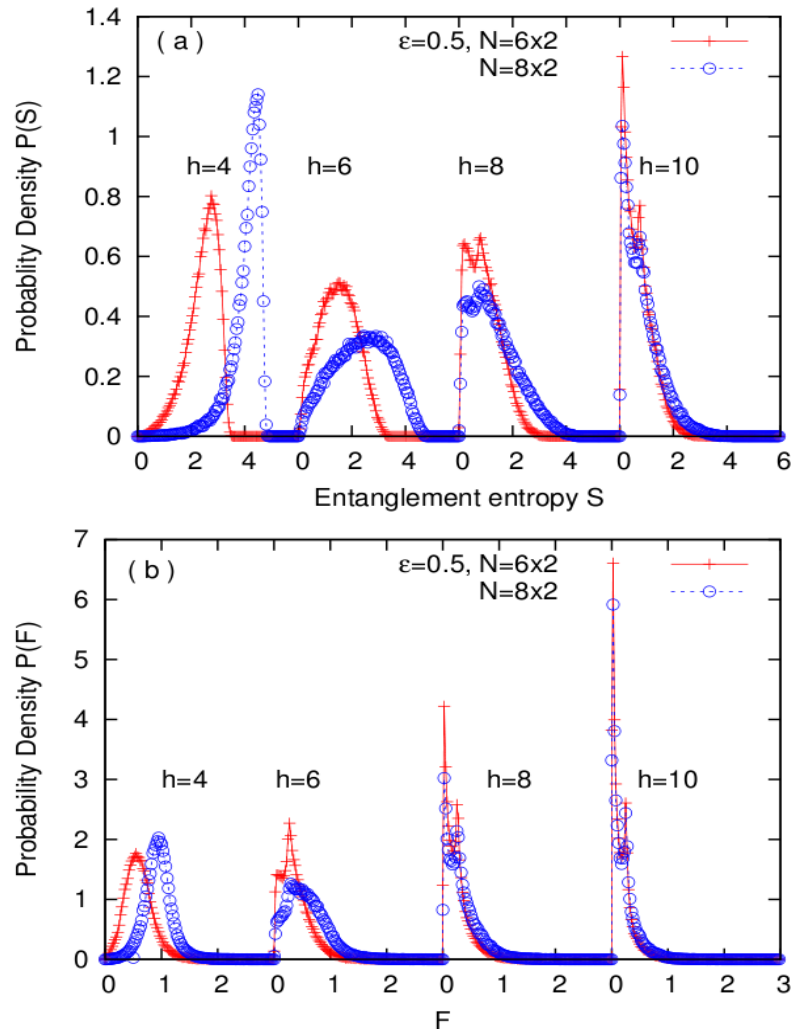


Similar distributions in 2-leg ladders

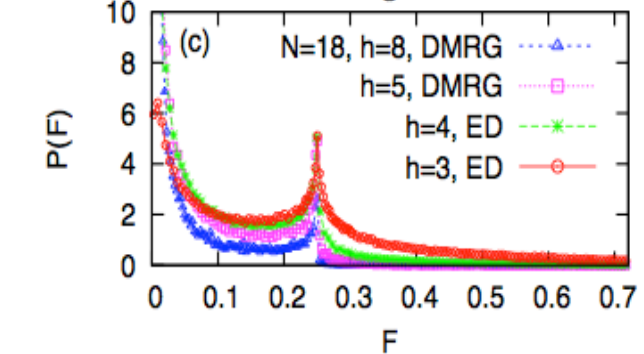
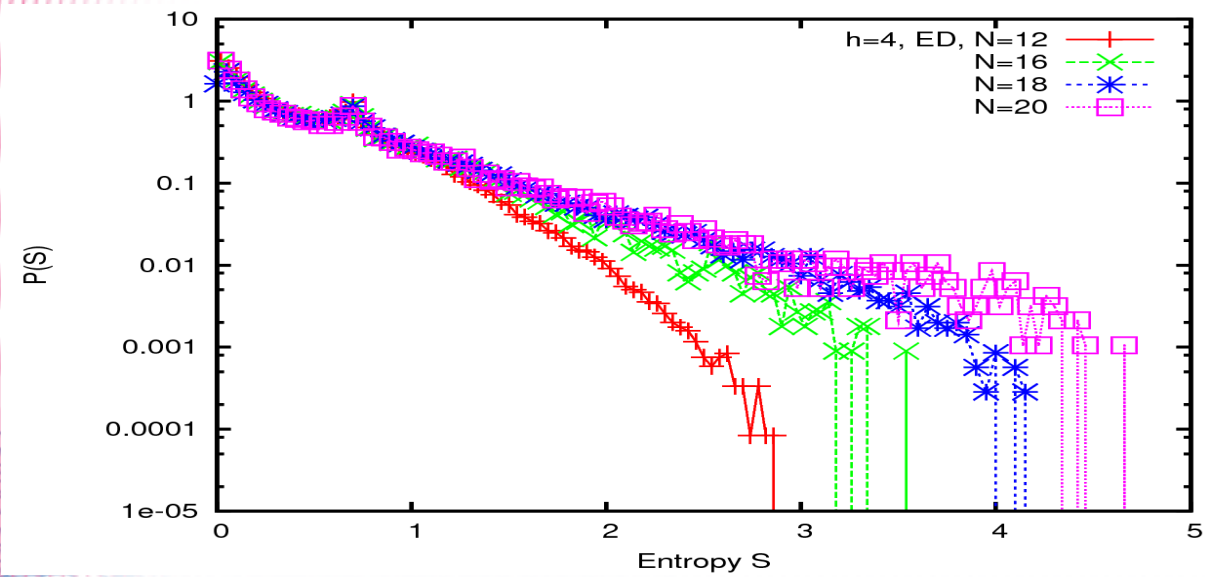
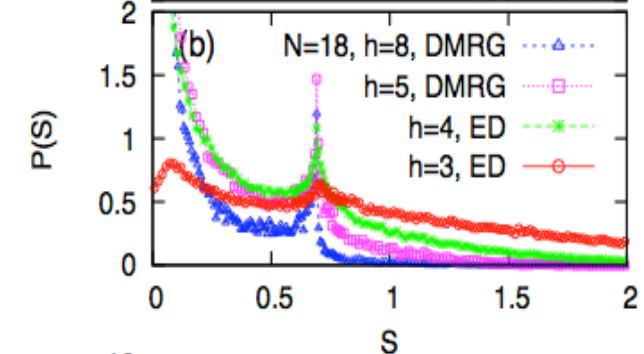
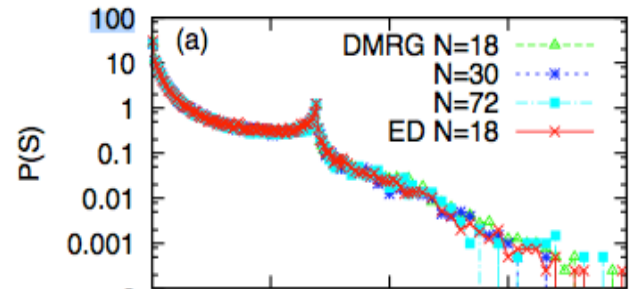
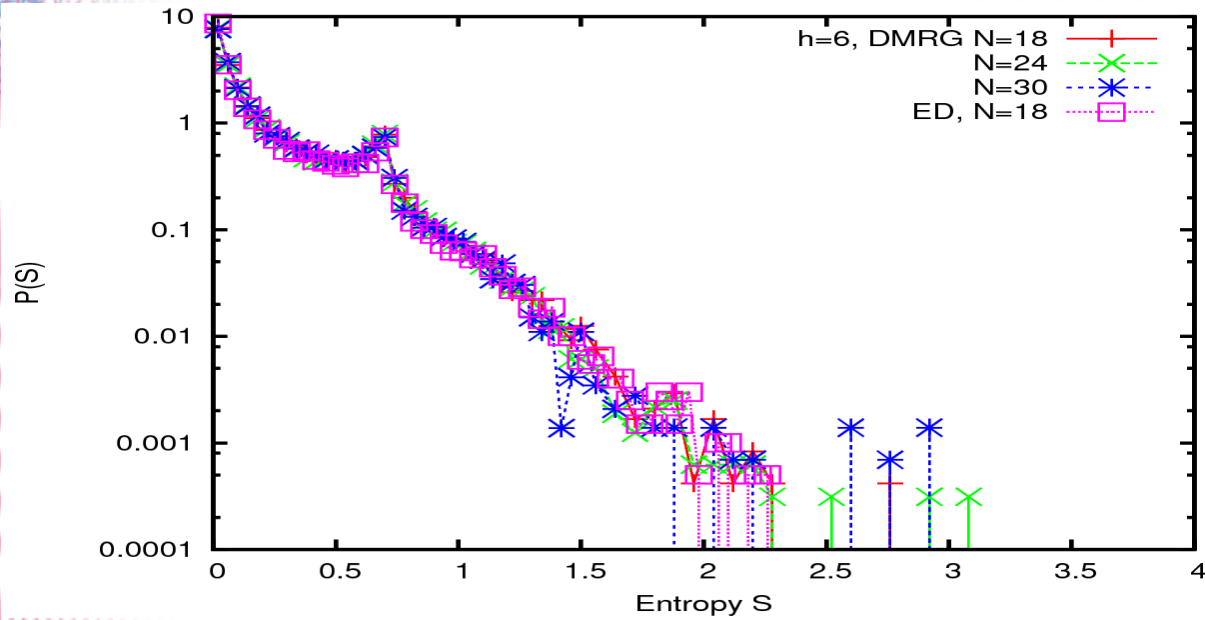
Bauer & Nayak (2013)



Baygan, Lim, DNS (2015)



Entropy distribution $P(S)$ reveals the evolution from MBL to delocalized phase

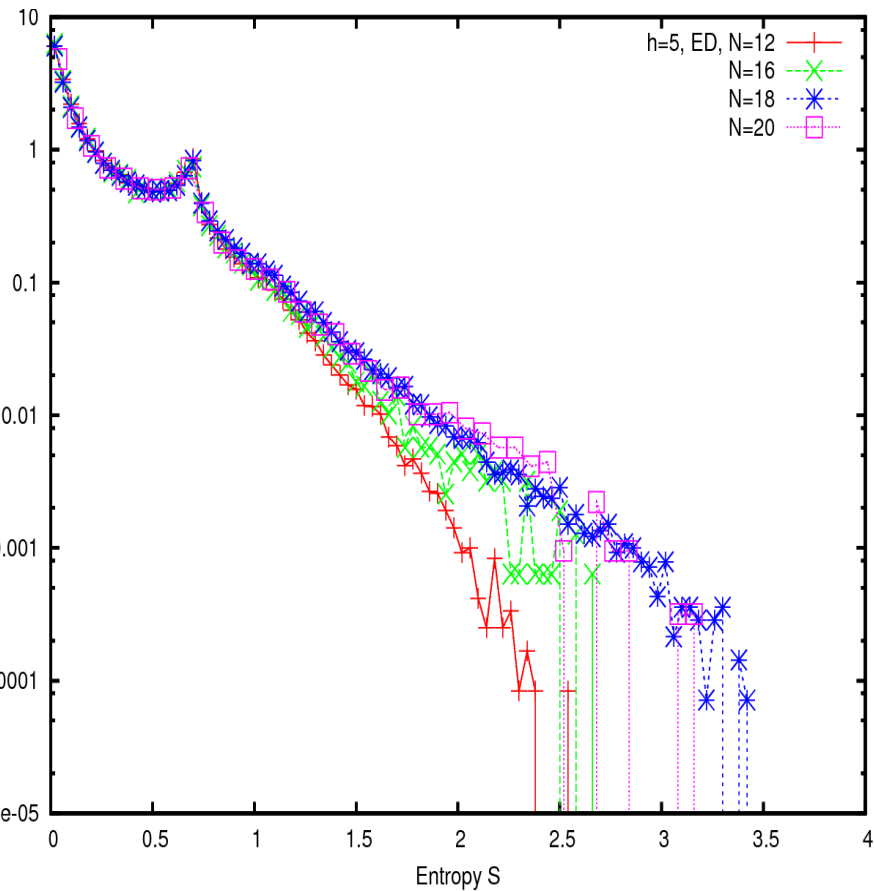
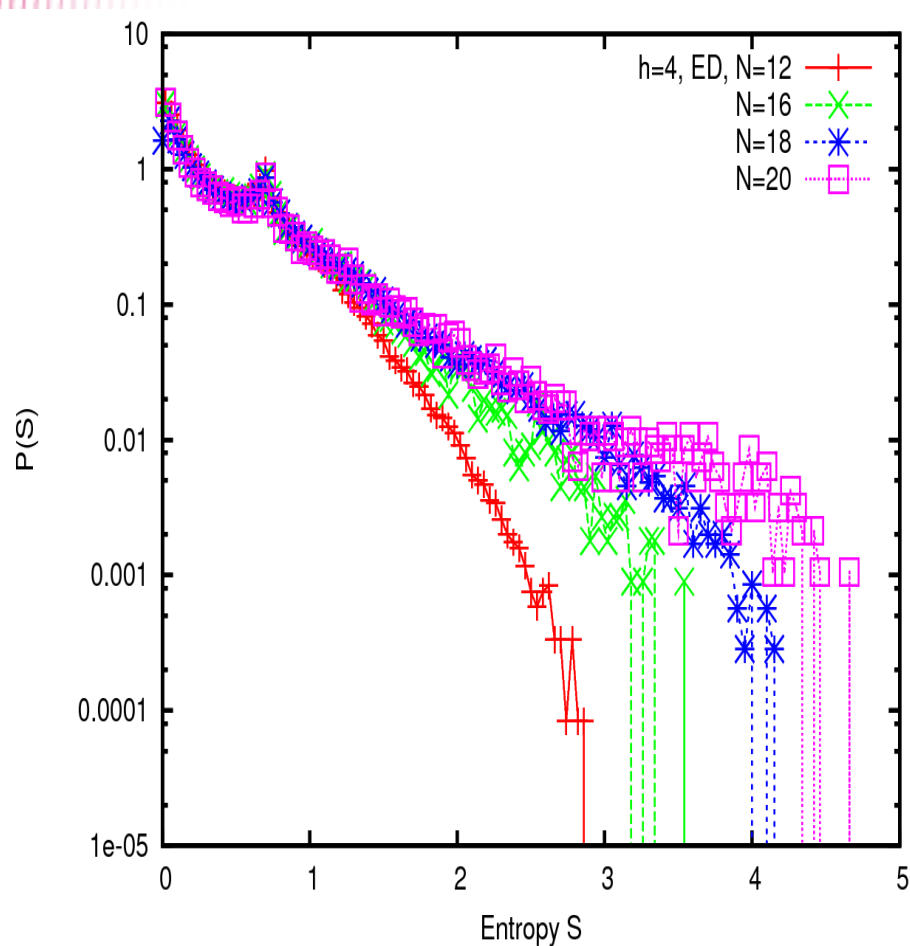


With reduced h , $P(S)$ grows from the tail for $h=4$ (ED)

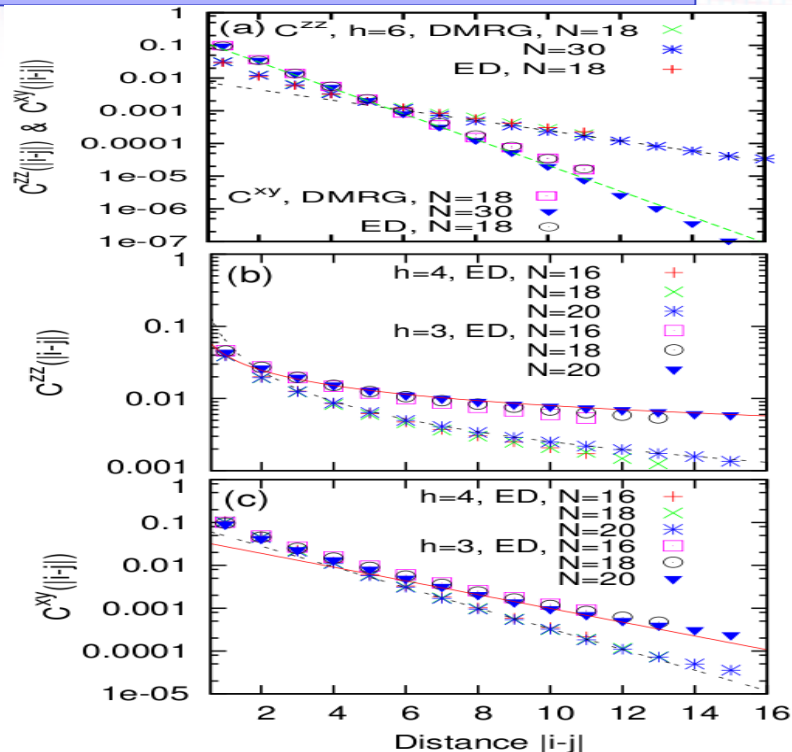
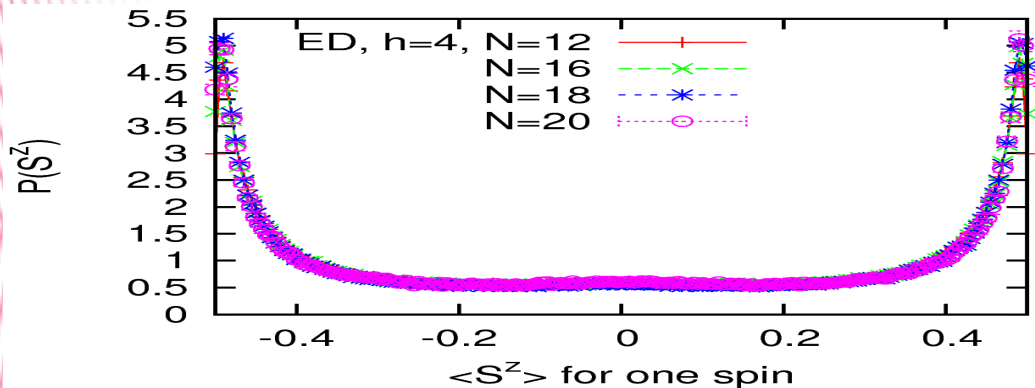
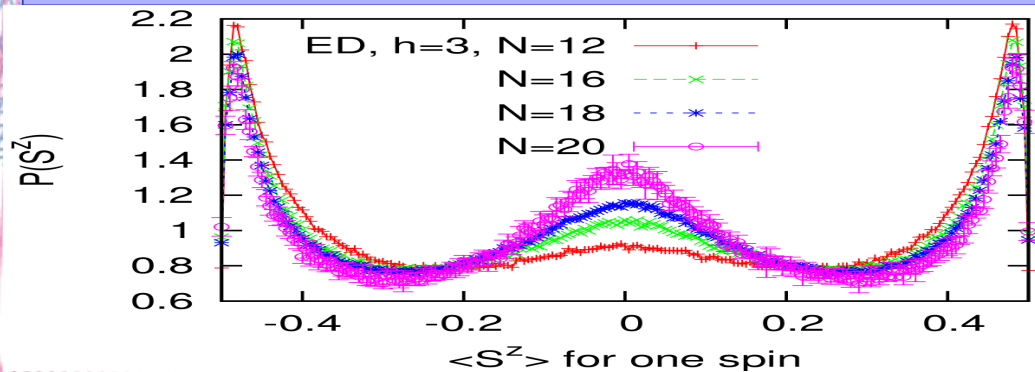
Entropy distribution $P(S)$ reveals the evolution from MBL to delocalized phase

$h=4$

$h=5$



DMRG-ED to study phase diagram



Deloc.

Critical
Regime

MBL

2.0

3.0

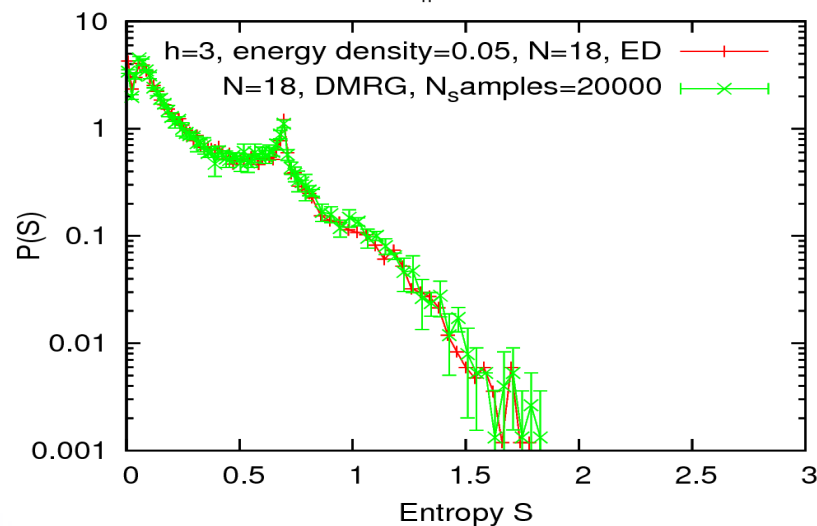
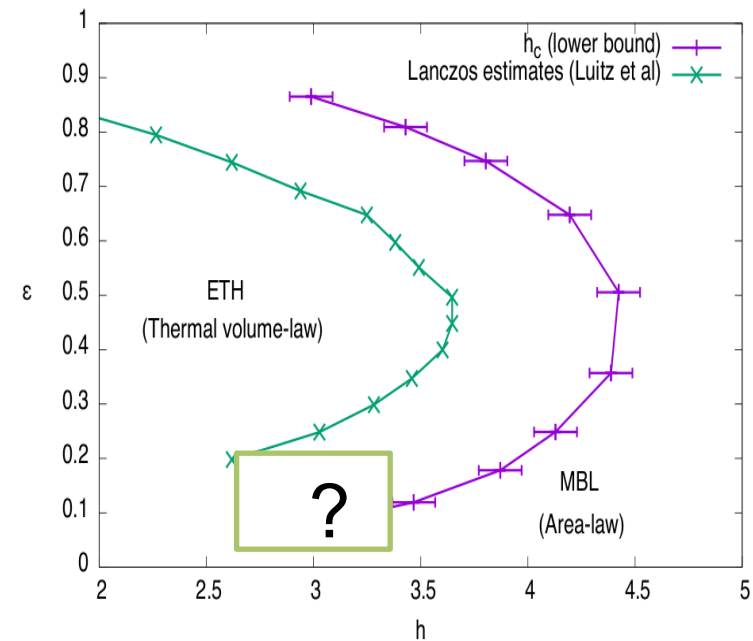
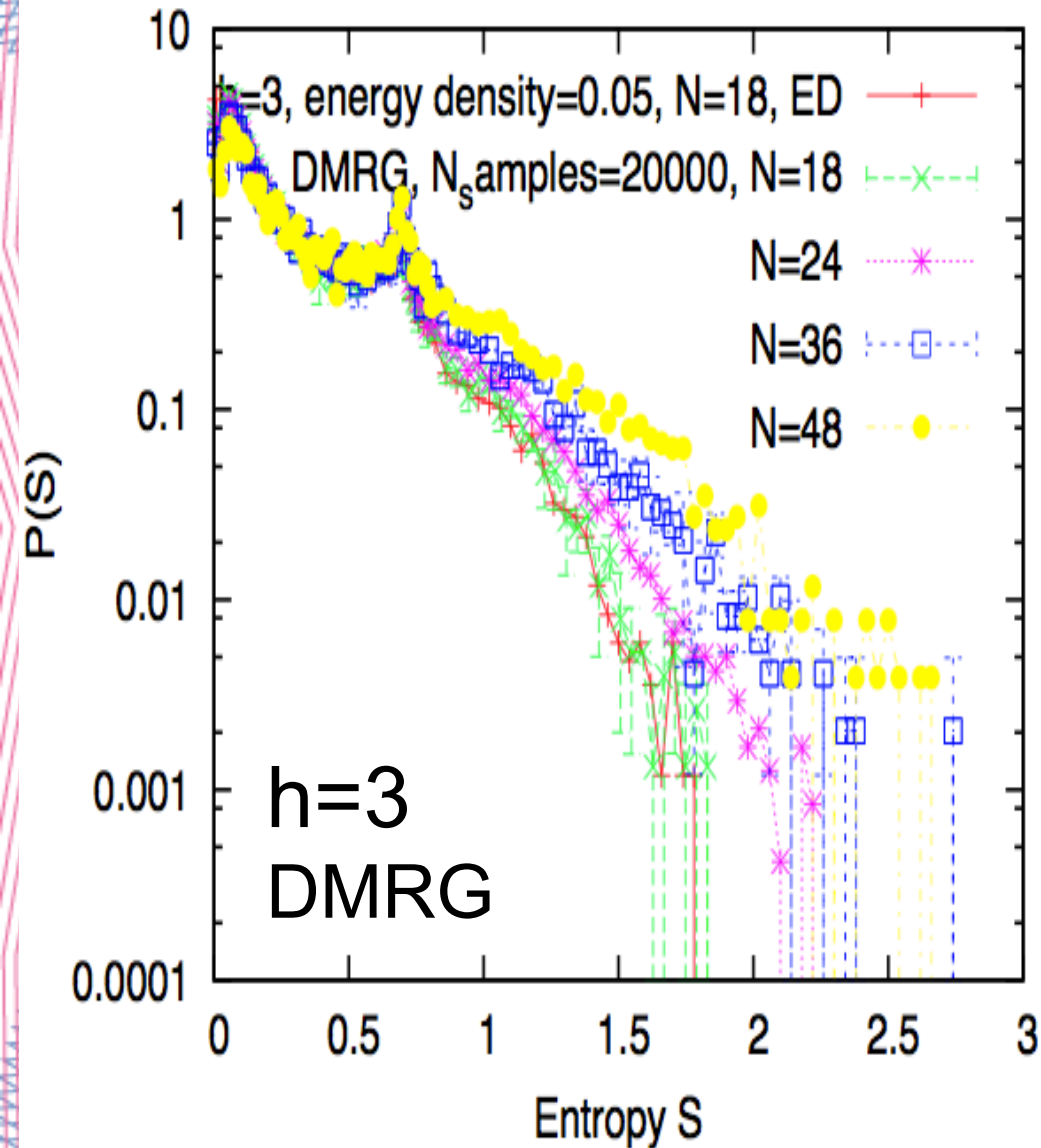
4.0

h

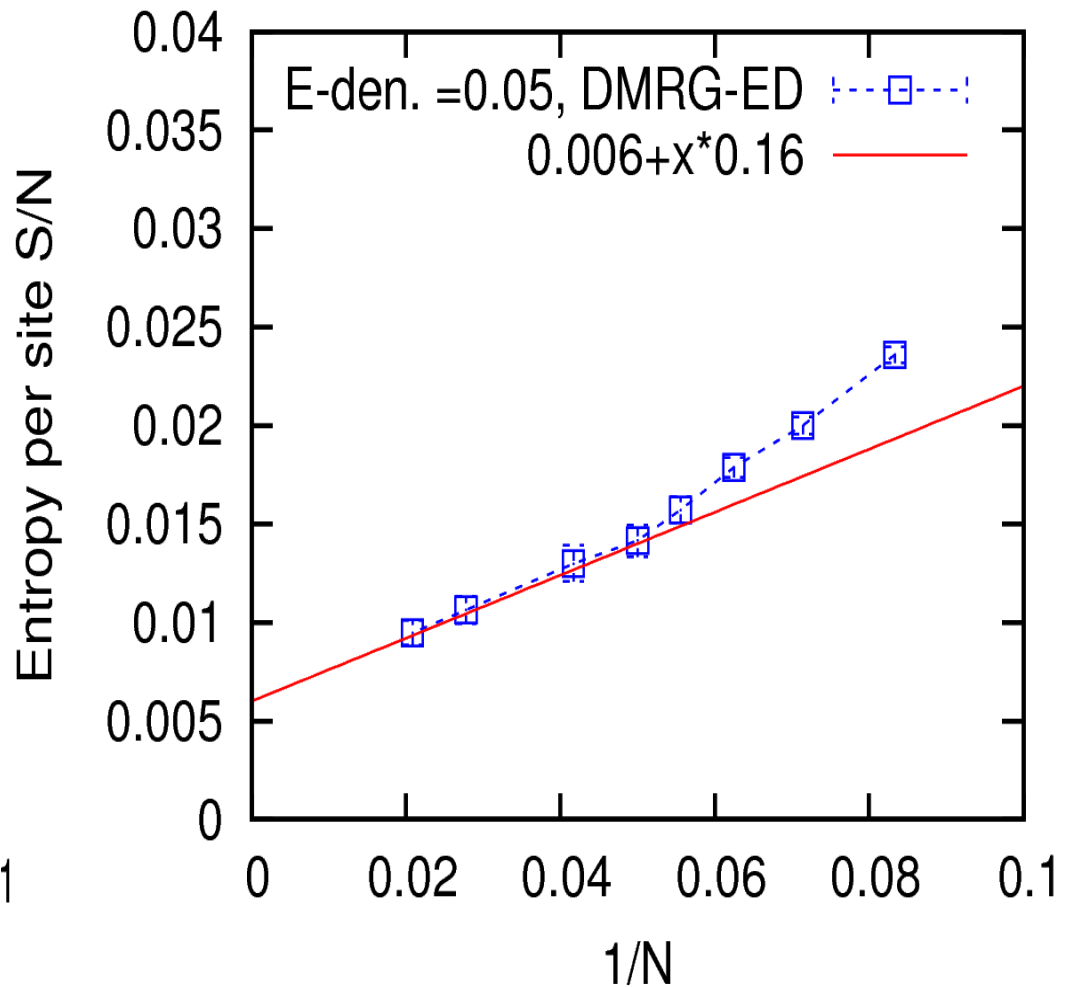
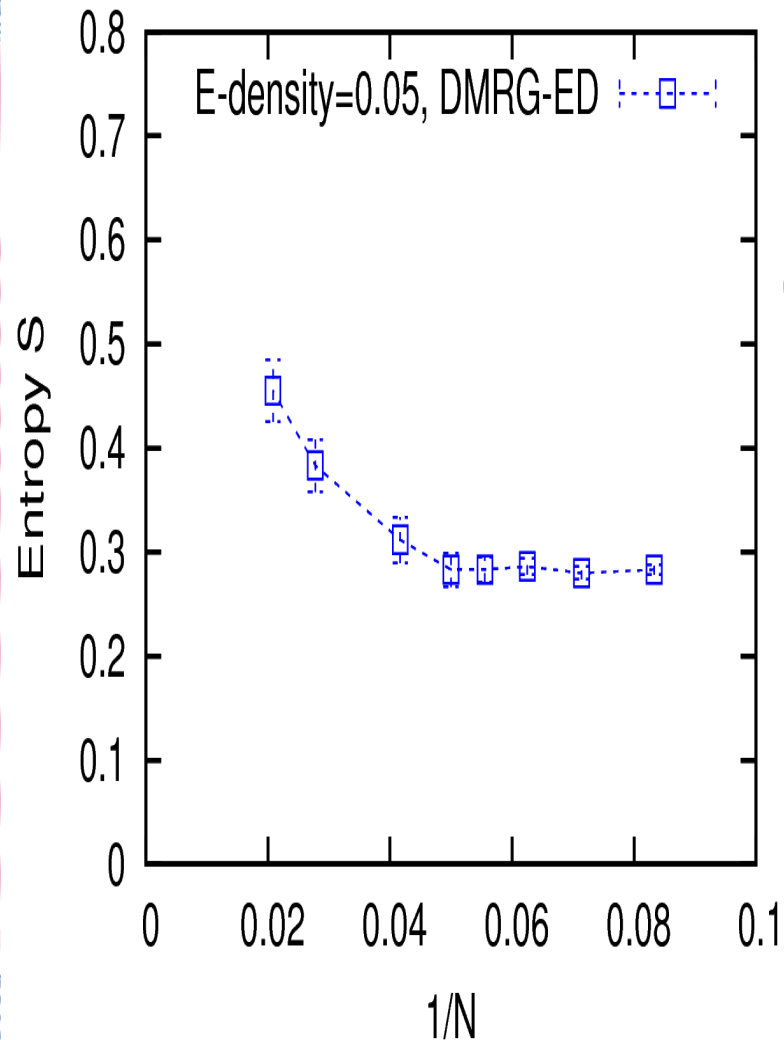
Serbyn & Moore
 Agarwal et al, Gopalakrishnan et al,
 Vosk et al., Potter et al.,

The critical regime may have strong size effect. Entropy grows with N slowly from the long tail of S (Griffiths regions).

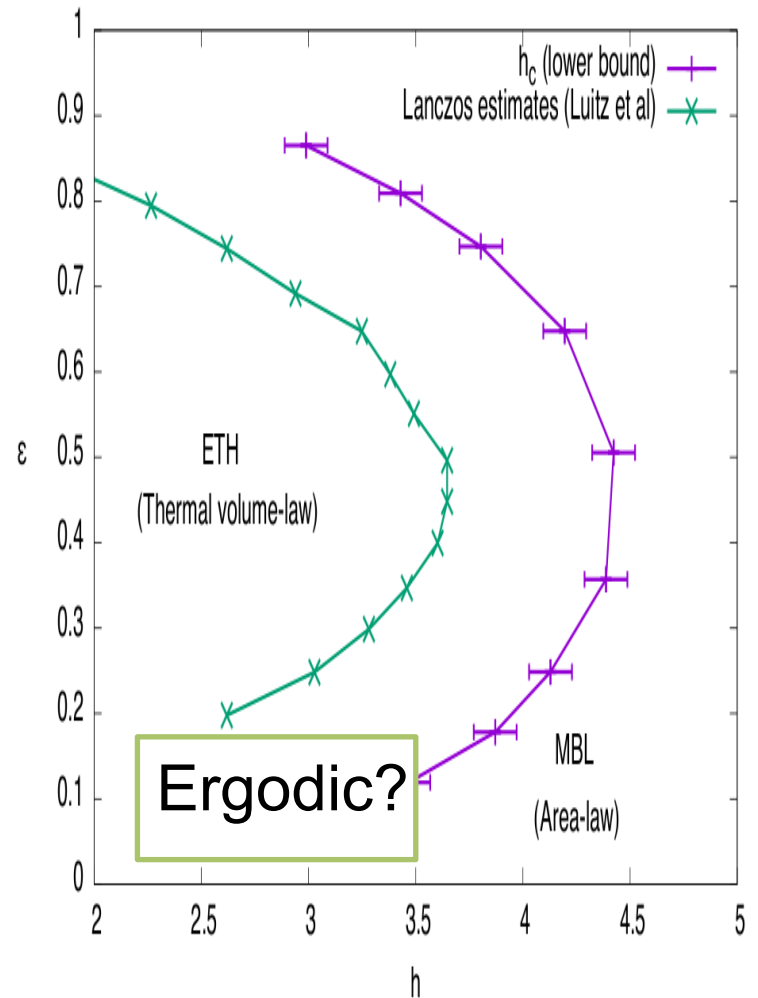
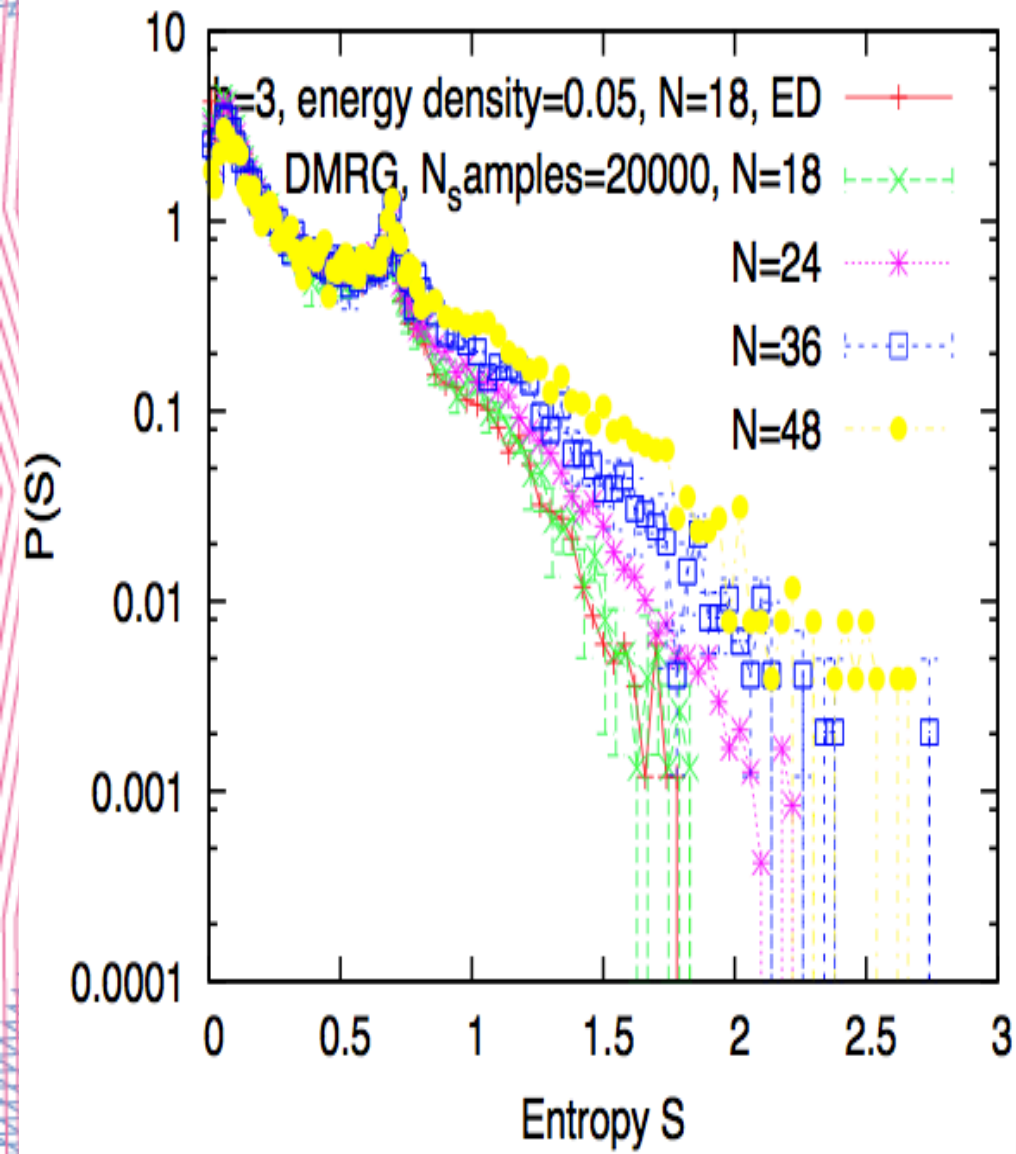
ED identified mobility edge and finite size effect



Entropy scaling for “the possible MBL phase below mobility edge”, S/N goes to constant



The lower energy “MBL phase” (ED) may be Ergodic phase



Summary

En-DMRG for excited states in MBL systems is highly accurate in obtaining statistical features of MBL phase.

Following the evolution of distribution functions, and combining DMRG-ED, we propose a phase diagram with an intermediate regime (thermal side) between delocalized ergodic and MBL phases.

Using DMRG to study lower energy excited states, we determine that the mobility edge “determined by ED” may be in Ergodic phase -----on going work.

The background features a complex, abstract pattern of thin, overlapping lines in blue and red. These lines form a grid-like structure that is distorted and warped, creating a sense of depth and movement. The lines are most prominent in the corners and fade towards the center, where the text is located.

Thank you