



Modeling Nanoparticles in Solution

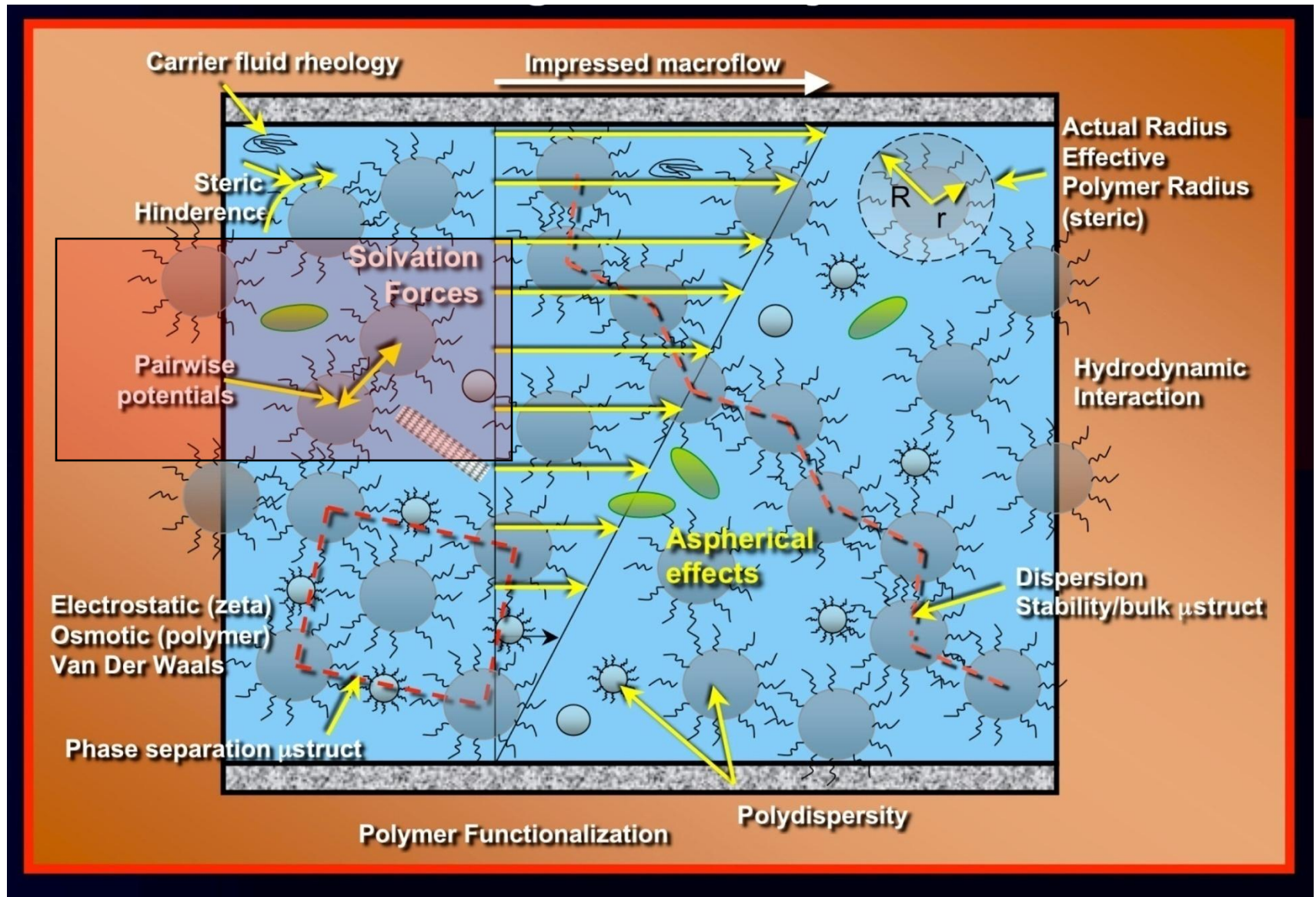
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Center for Integrated Nanotechnology

Albuquerque, NM

Rich Physical Phenomena



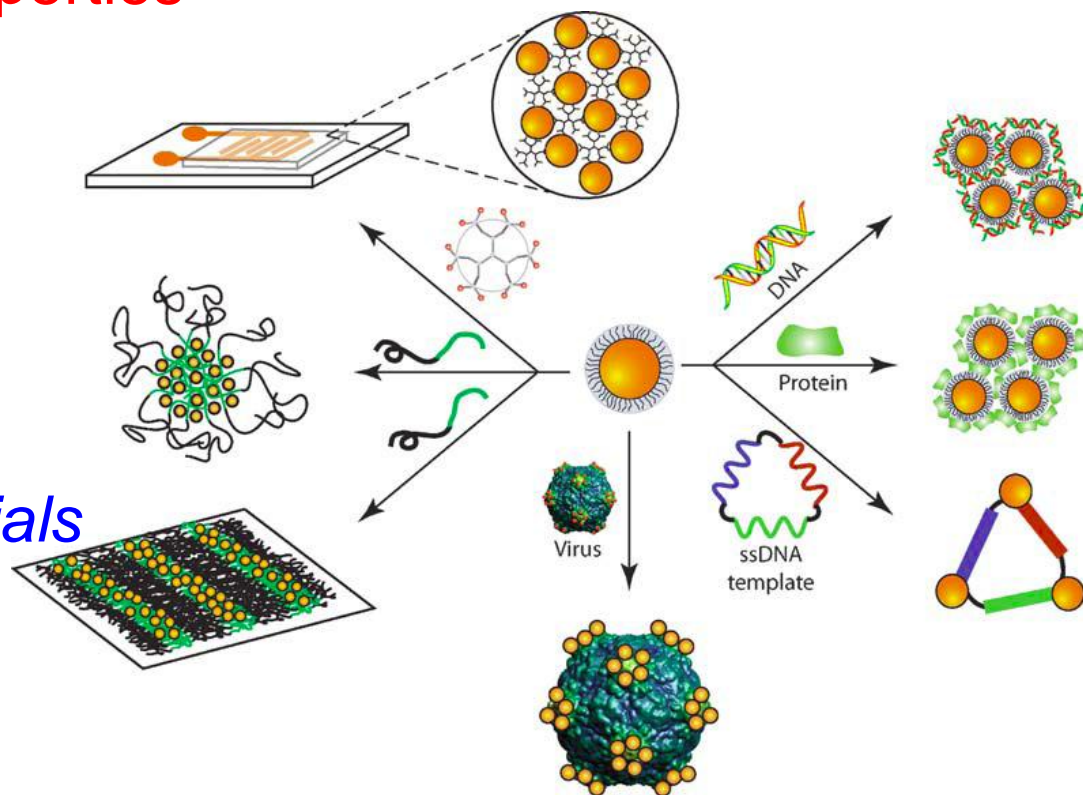
Polymer Nanoparticle Complexes

Controlled Designed Properties

- Mechanical, Thermal
- Optical
- Electronic
- Transport

High performance materials
Plasmonic devices
Sustainable energy

Protein Recognition
Drug and Gene Carriers



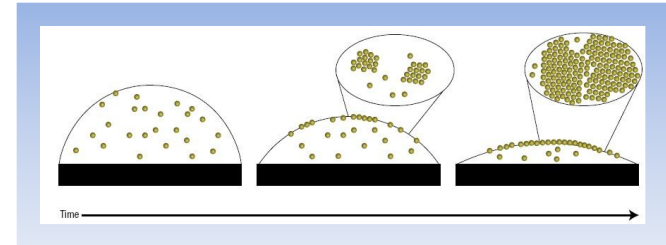
Polymer-mediated assembly of Au NP

Y. Ofir, B. Samanta and V. M. Rotello,
Chem. Soc. Rev. 37, 1814 (2008)

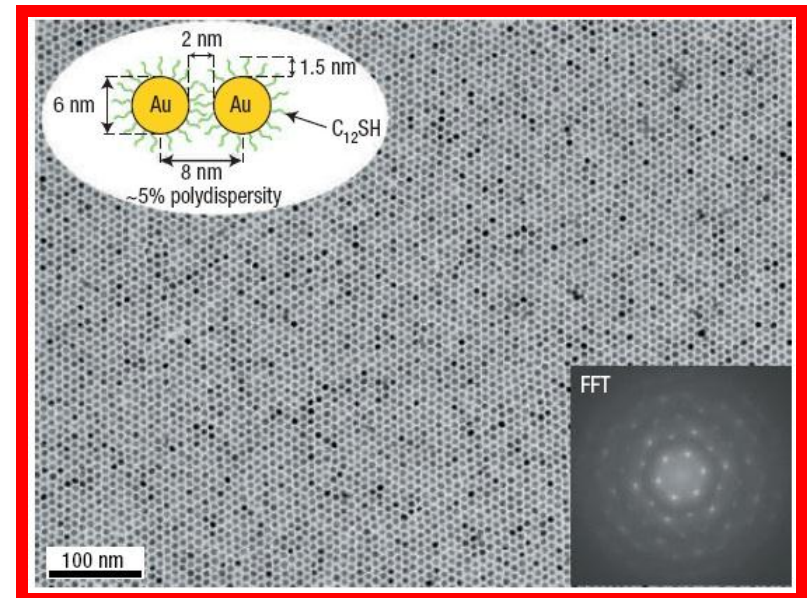
Nanoparticle Assembly Challenges

- **Synthesis of nanoparticles**
well defined size,
uniform, stable coating
- **Tailored properties**
optical, electrical, and
magnetic
- **Assemble nanoparticles**
retaining unique
properties **without**
acting like a bulk metal

-long range order is possible, only some times desirable, but often not necessary

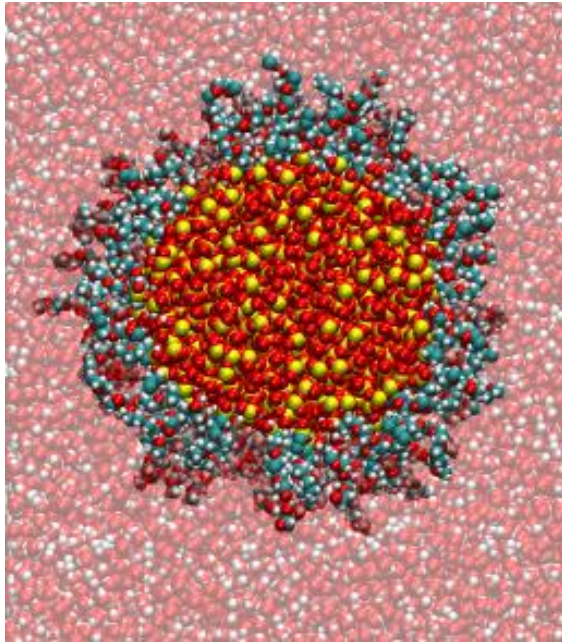


Slow evaporation of solvent



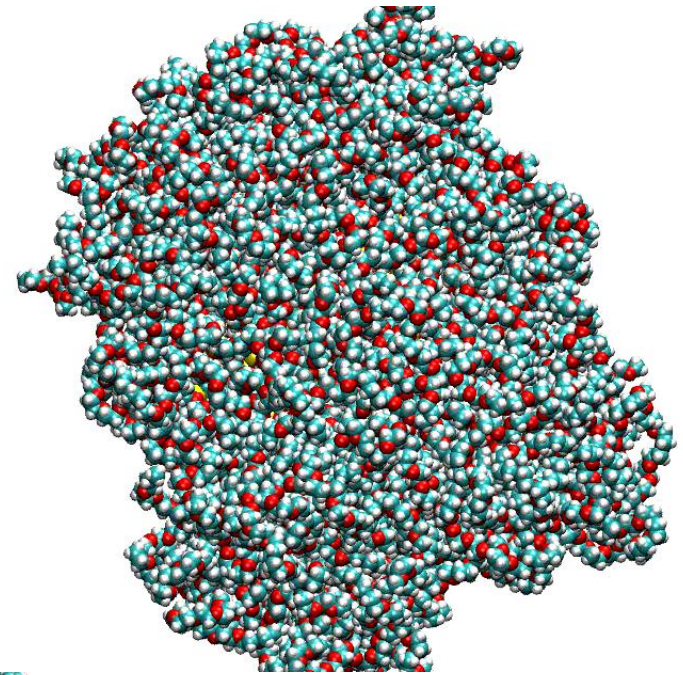
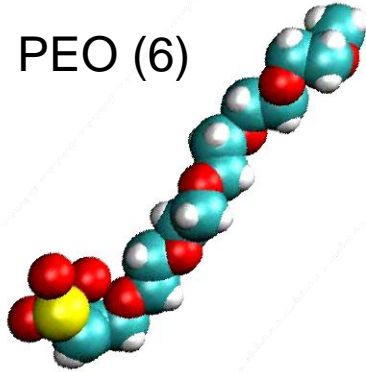
Bigioni *et al*, Nature Mat.5, 265 (2006)

Coated Nanoparticles

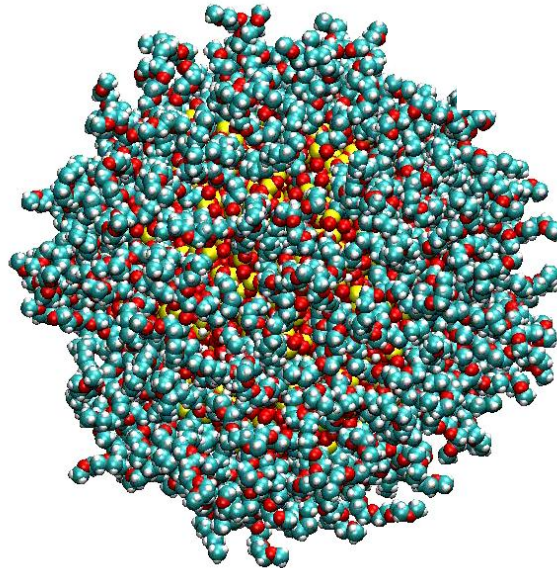


Polyethylene PEO(6) coated
5nm silica nanoparticle in
water (3.1 chains/nm²)

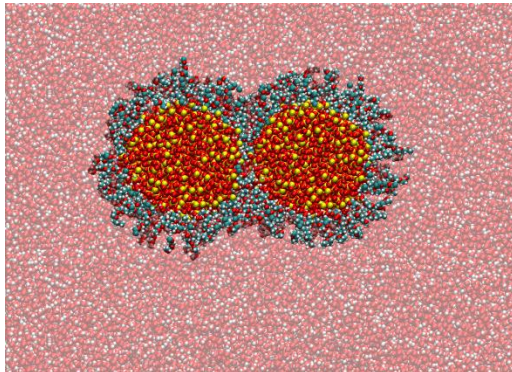
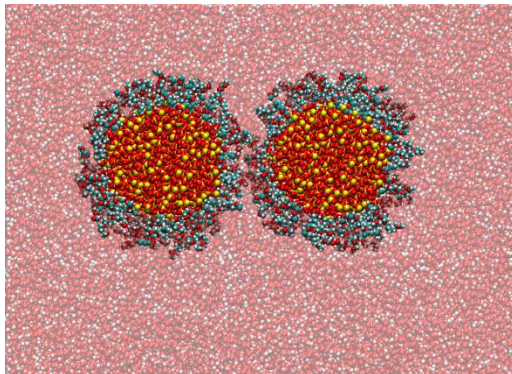
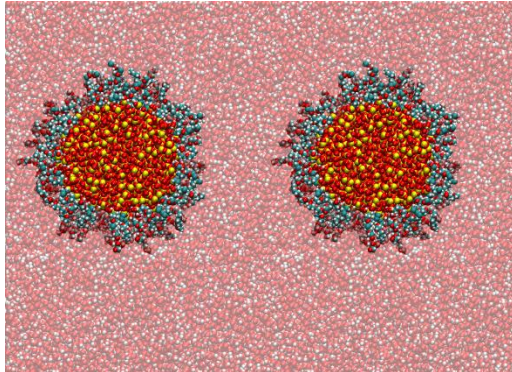
PEO (6)



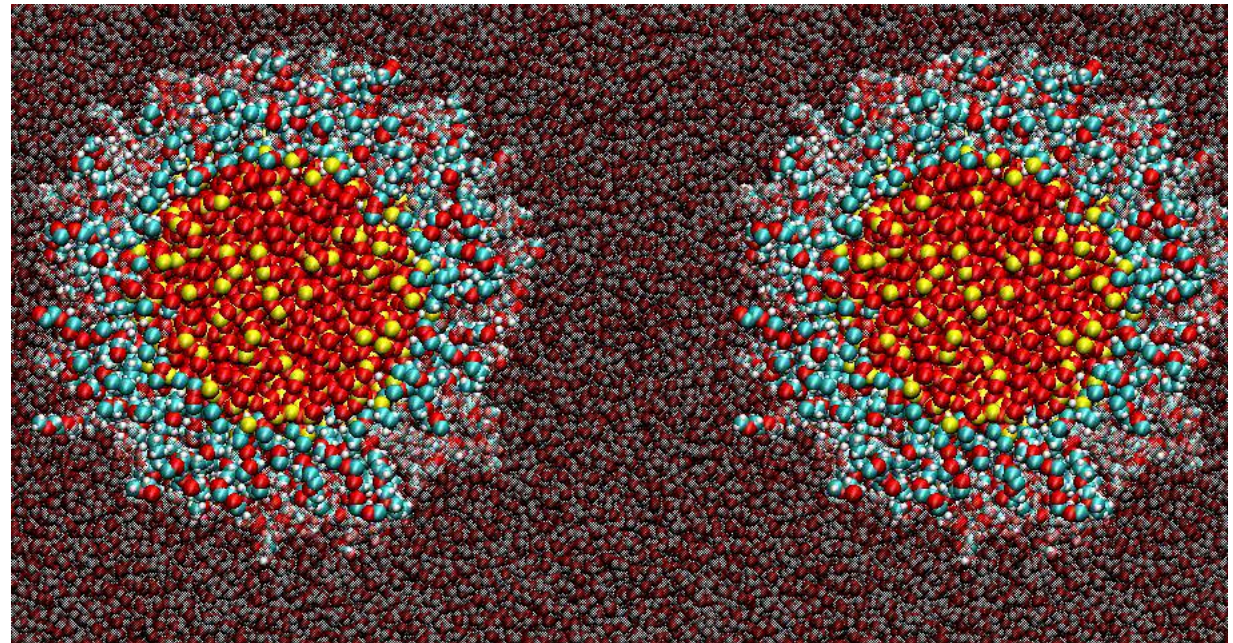
PEO(100)
0.5 chains/nm²
Aspherical Shape



Interactions between Nanoparticles

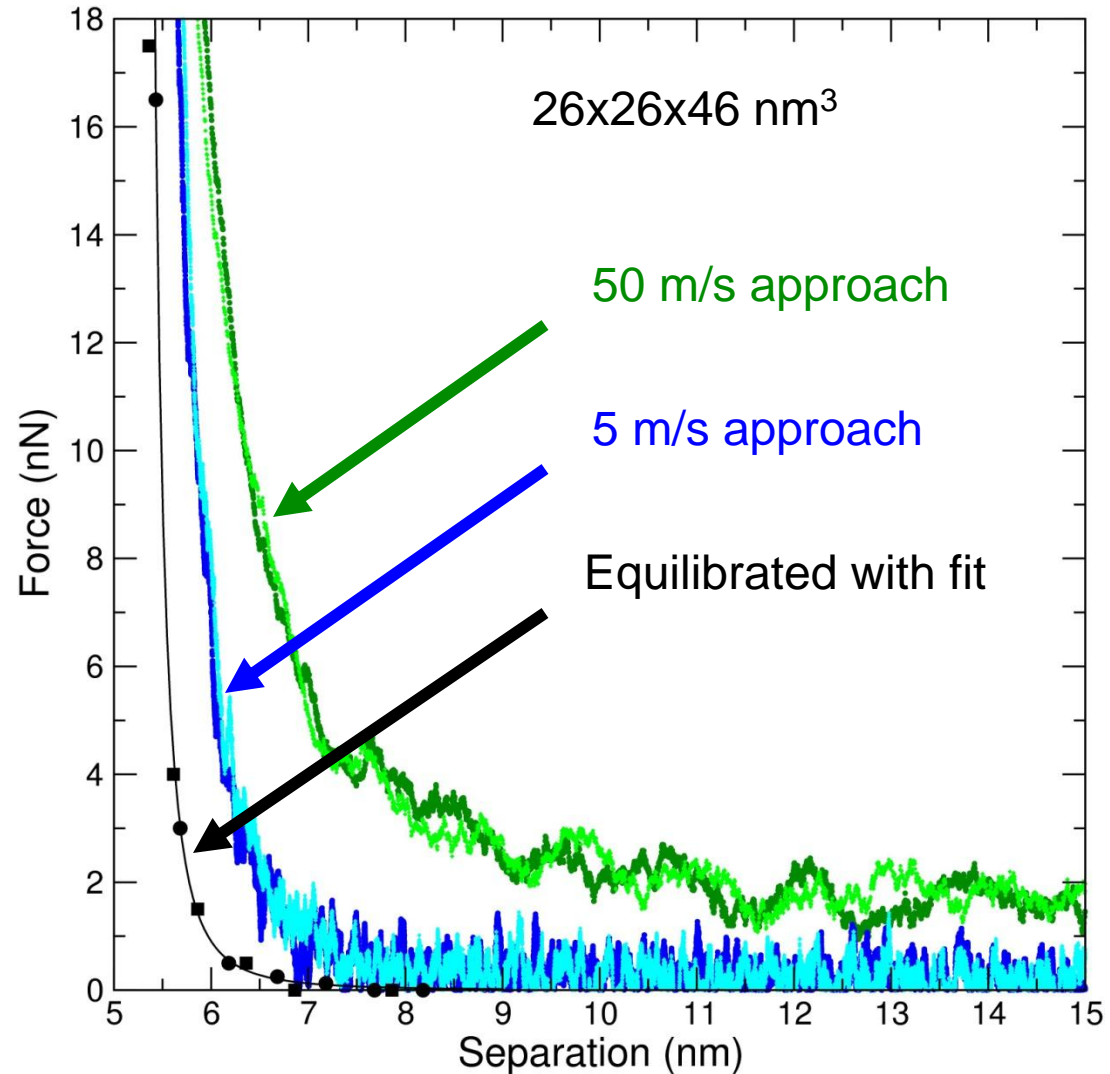
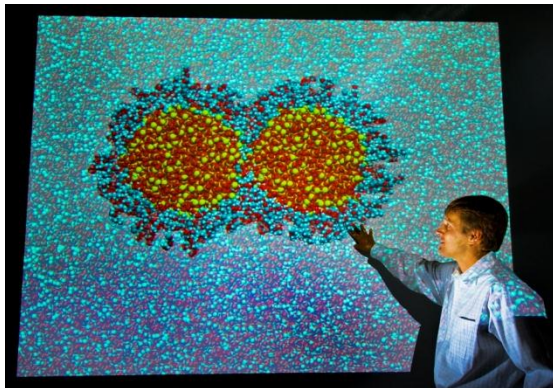


- Determine velocity independent (solvation) and velocity dependent (lubrication) forces
 - chain length, nanoparticle size/shape, coverage
- Integrate into coarse-grained model



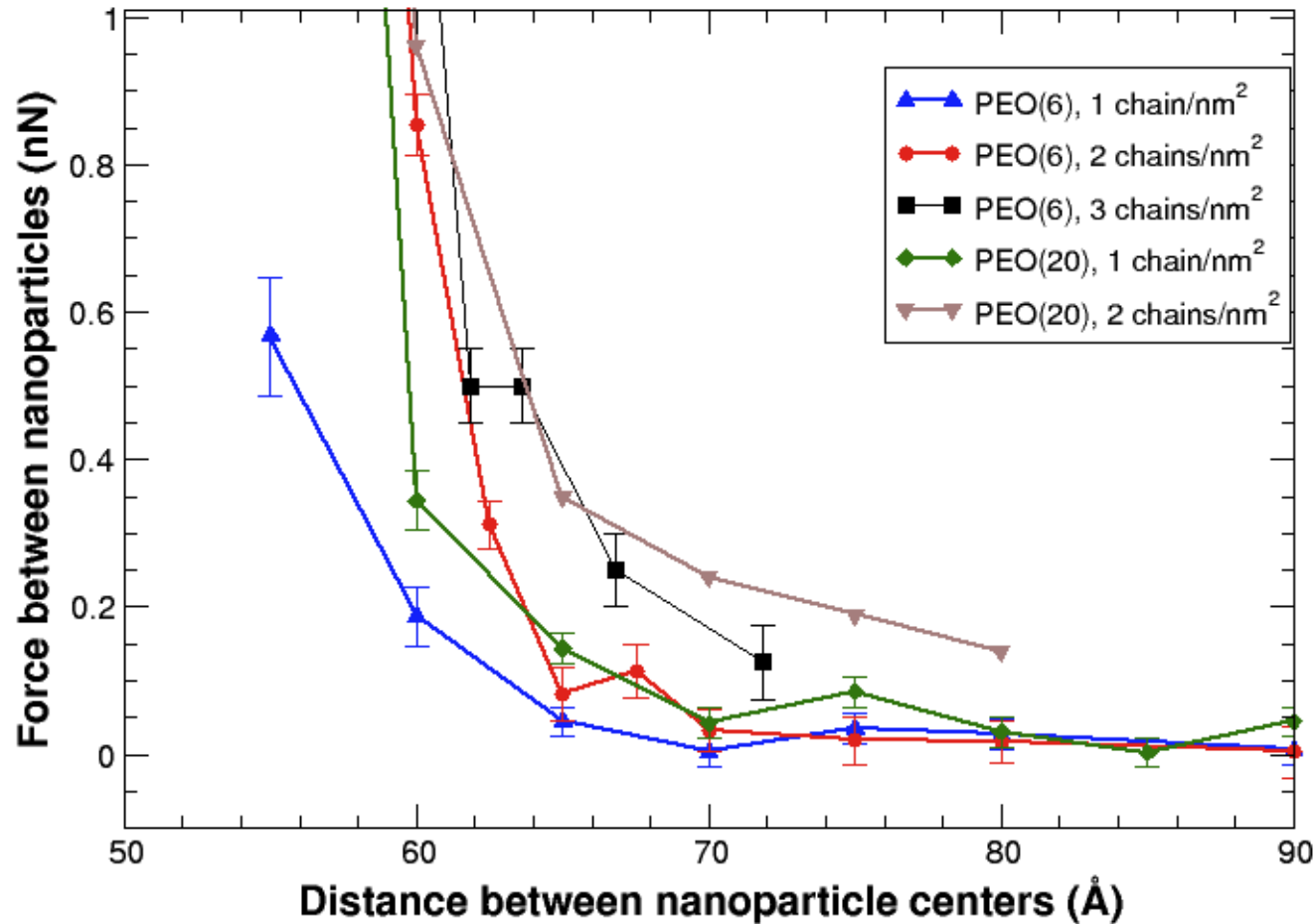
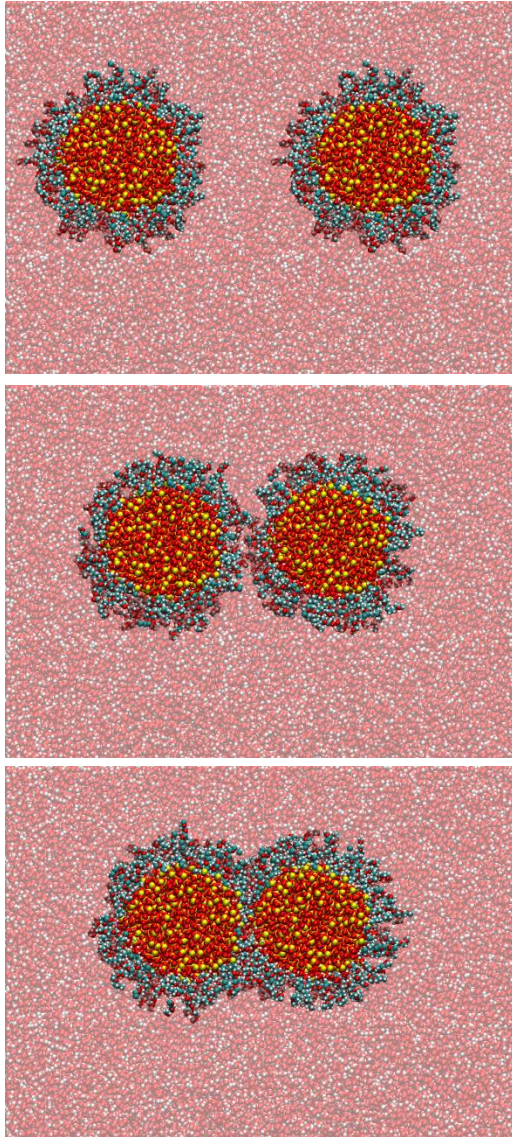
Force between Silica Nanoparticles

- Stokes drag at large separation with linear velocity scaling
- Complex mixed response in the separation range of interest (near contact)
- No oscillations in force



5 nm PEO(6) coated silica NP – 3 chains/nm²

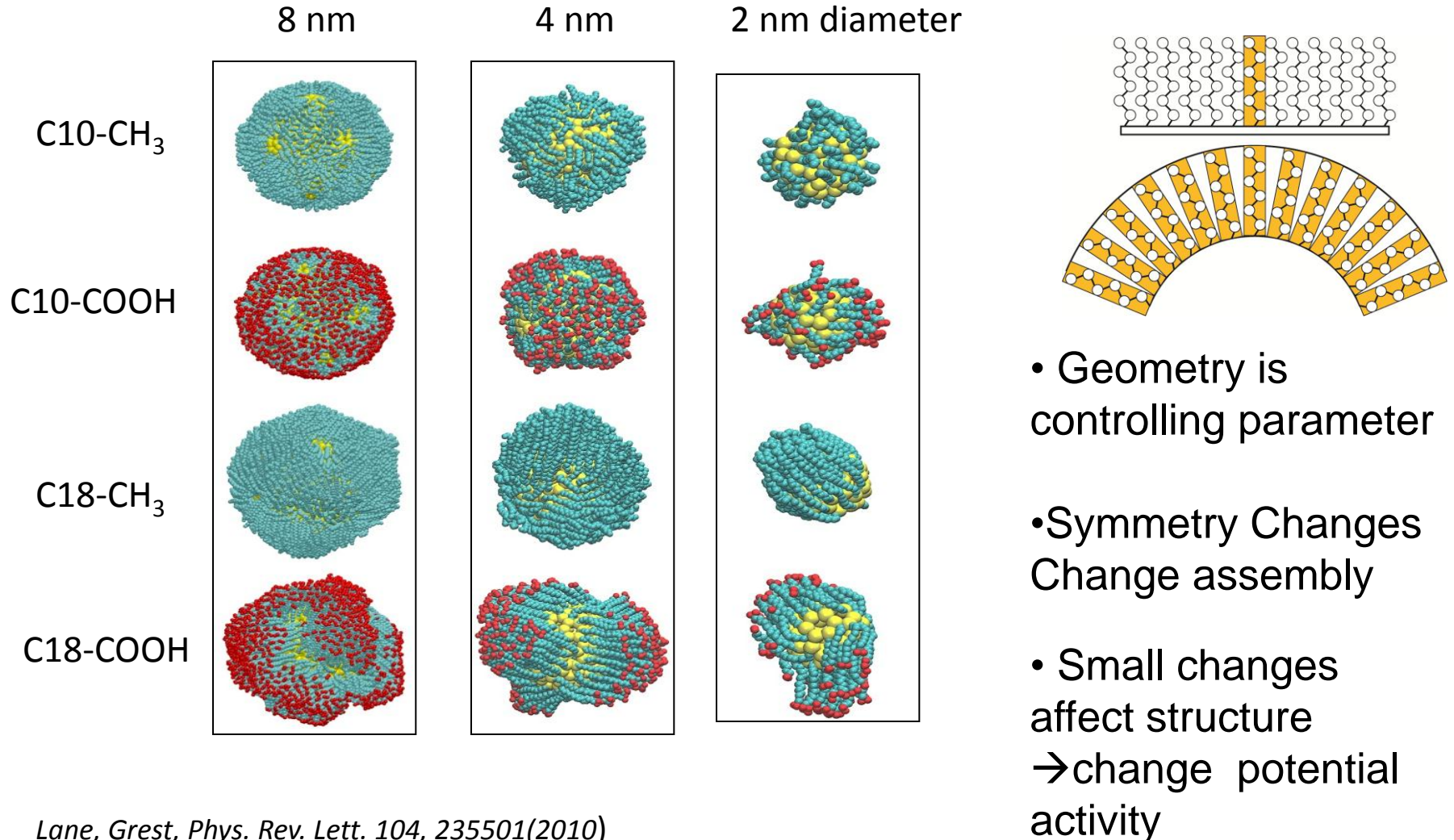
Interactions between Nanoparticles



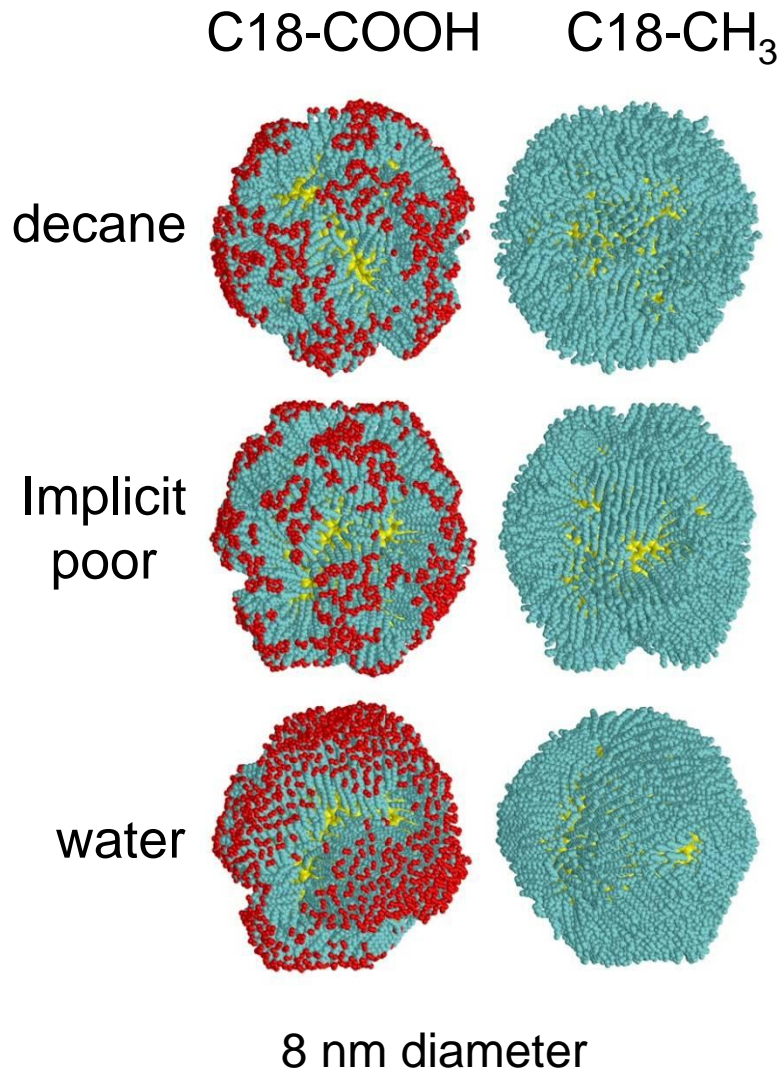
- 300K, thermal fluctuations corresponds to forces < 1 nN

Alkanethiol Coated Au Nanoparticles in Water

Symmetric Coating Leads to Asymmetric Shapes



Different Solvents



- CH₃ terminated chains behave largely as expected to solvent changes based on hydrophilic/phobic interactions
- COOH terminated chains form small tight bundles unless solvated
- Implicit solvent captures, some but not all features of explicit solvent

Coated Nanoparticles at a Water/Vapor Interface

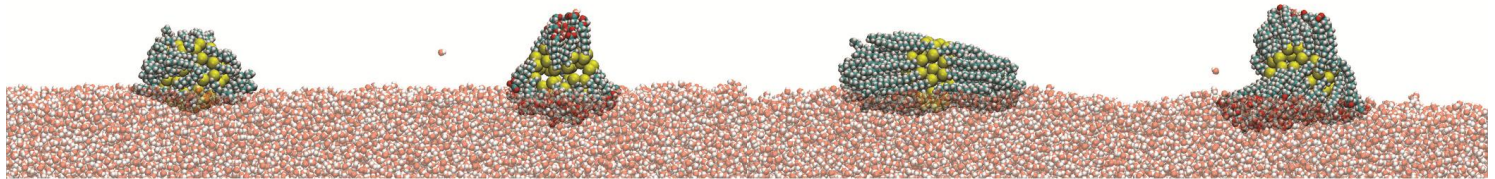
C10 - CH₃

C10 - COOH

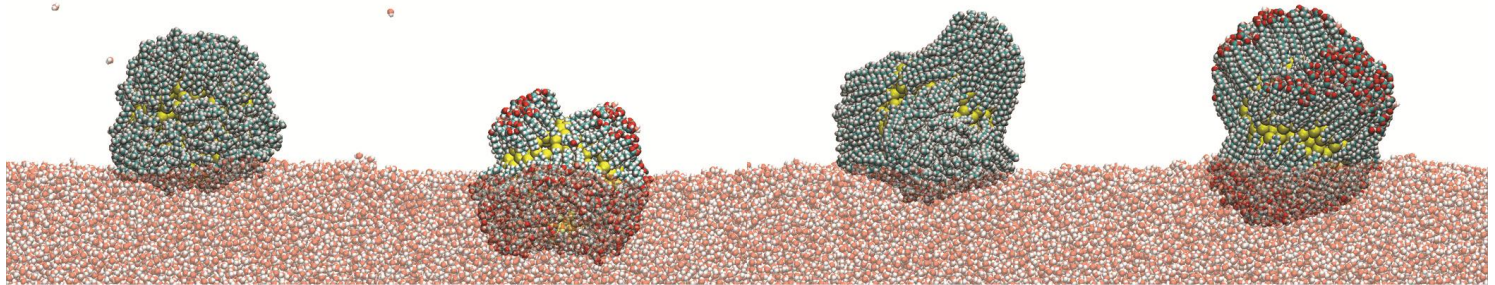
C18 - CH₃

C18 - COOH

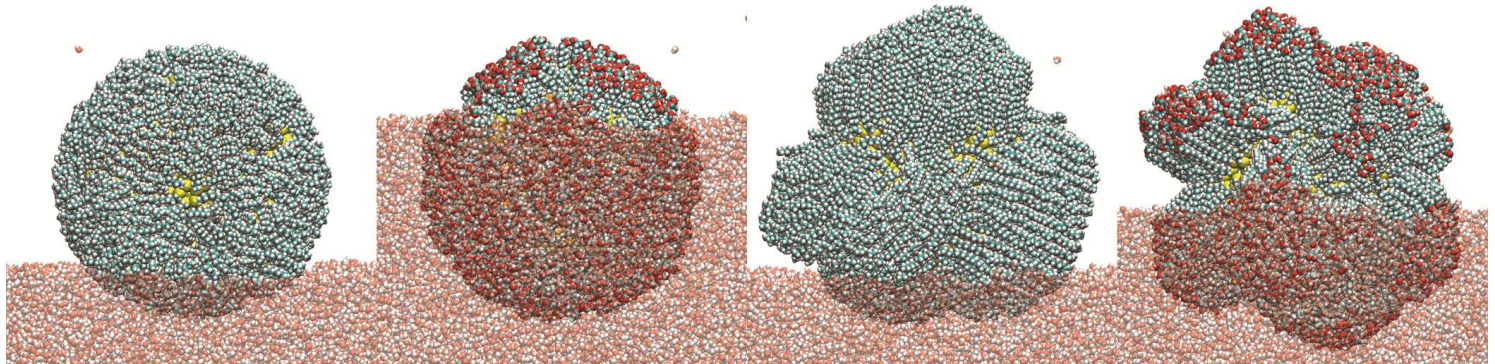
2 nm
diameter



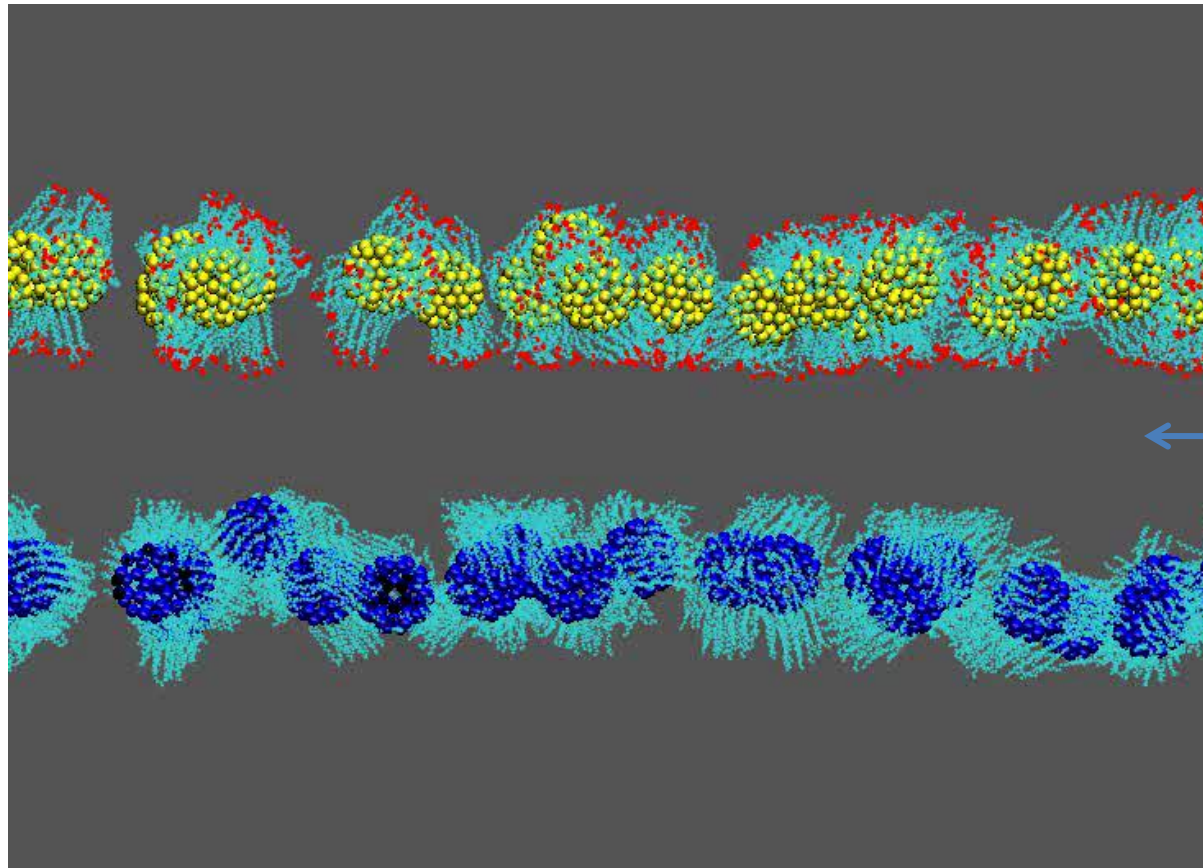
4 nm
diameter



8 nm
diameter



Surface Aggregation and Self-Assembly

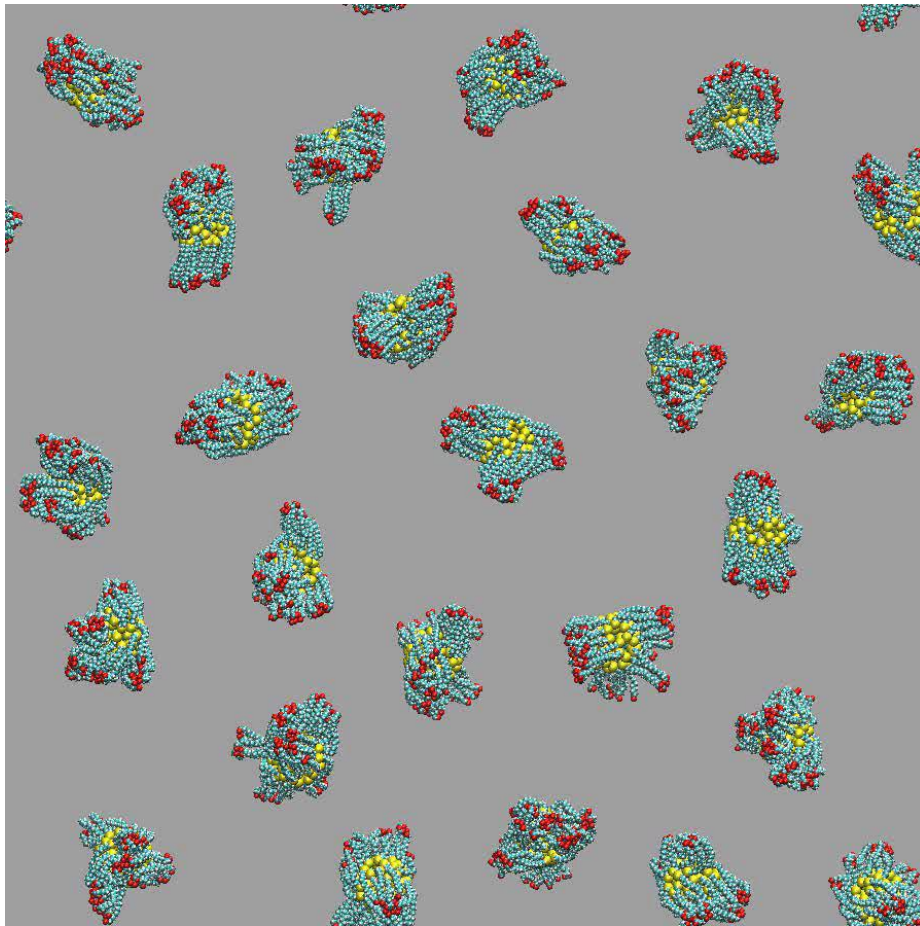


Water (not shown)

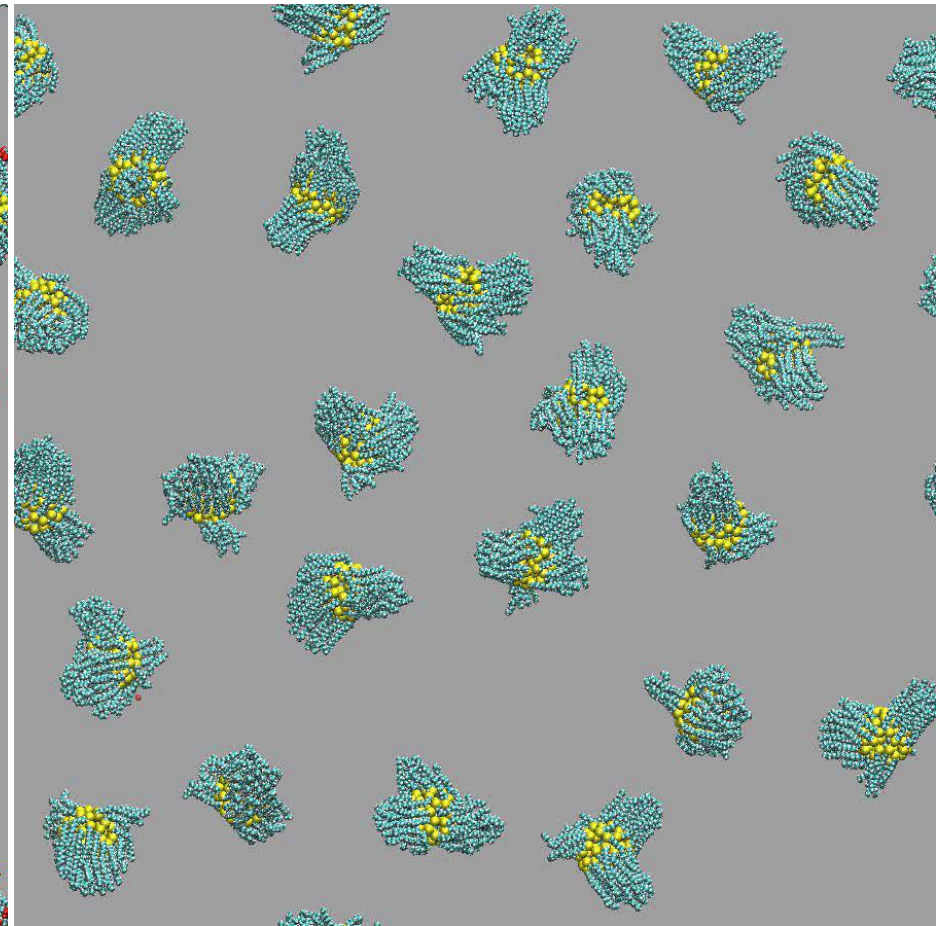
*COOH terminal group
(top)*

*CH₃ terminal group
(bottom)*

Surface Aggregation and Self-Assembly



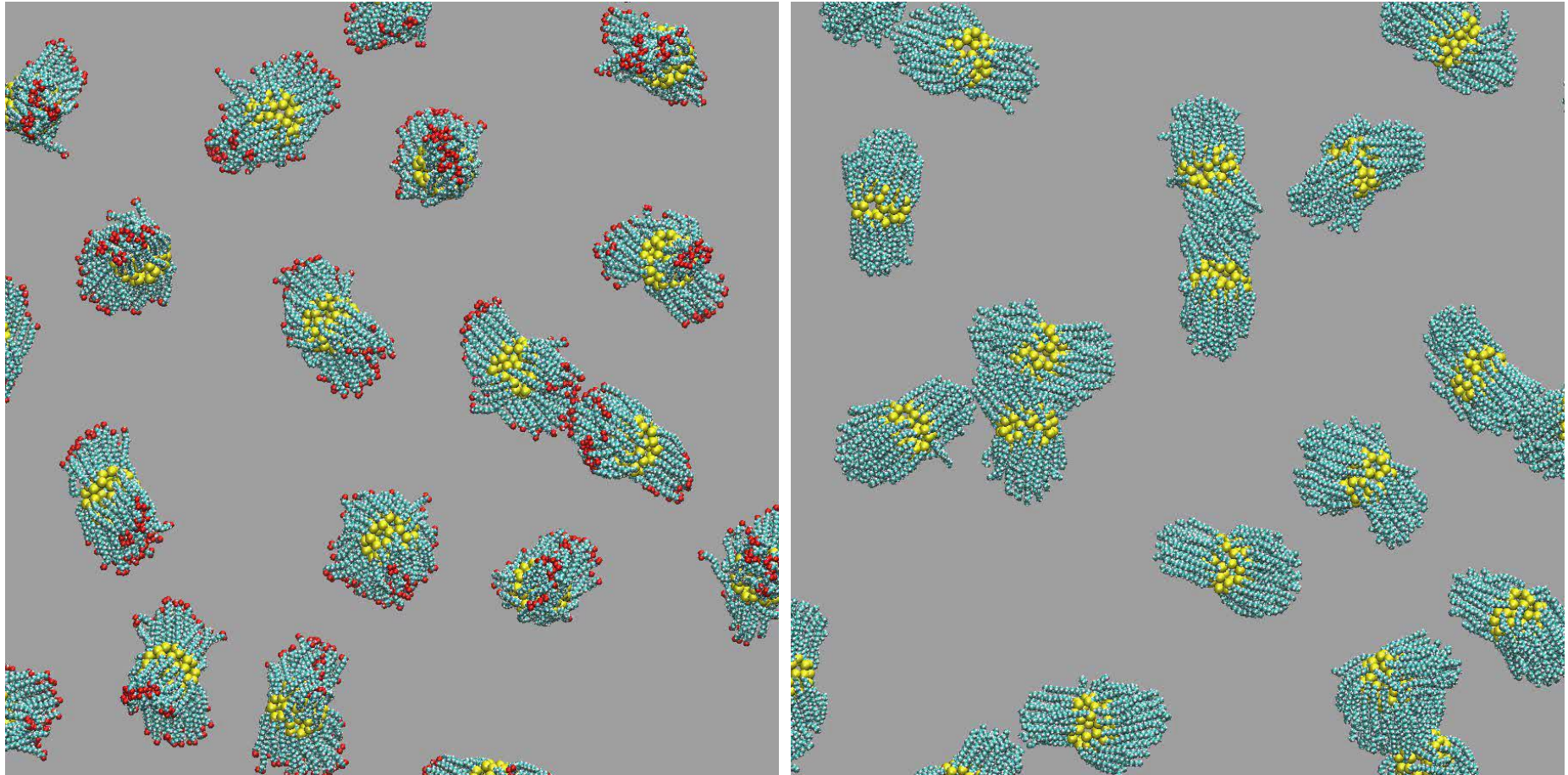
COOH terminal group



CH₃ terminal group

1,200,000 atoms ~ 1.1 ns/day on 1152 cores (Red Sky)
~ 2.2 million core hours for 90 ns

Surface Aggregation and Self-Assembly



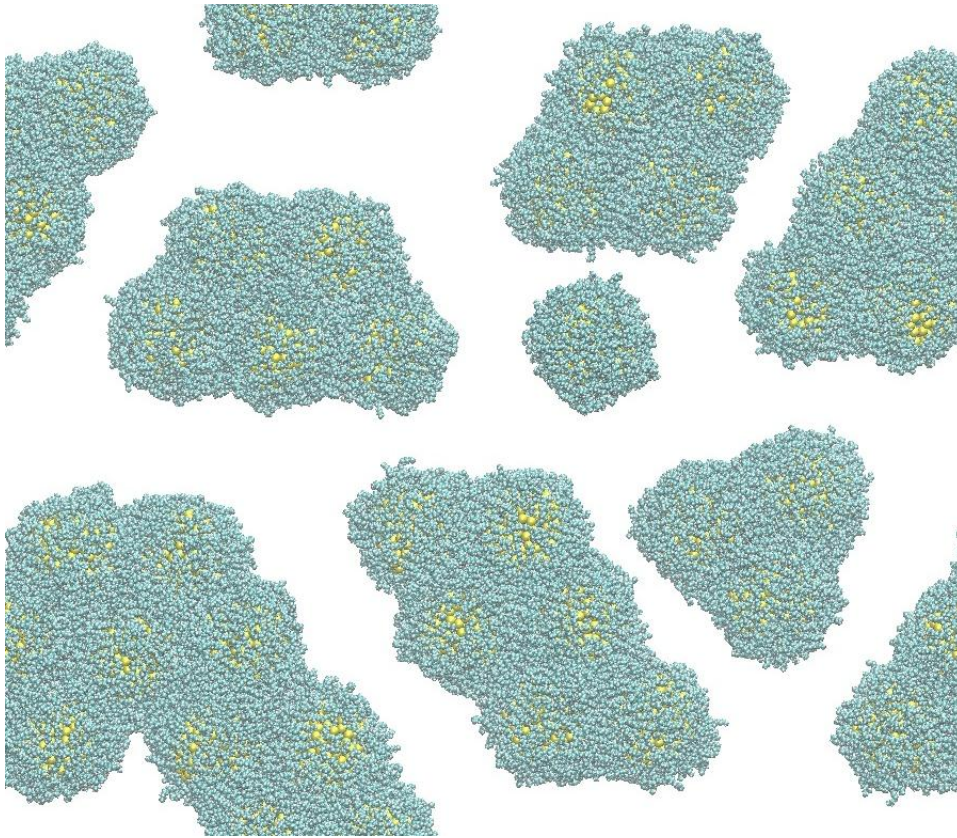
COOH terminal group

90 ns

CH₃ terminal group

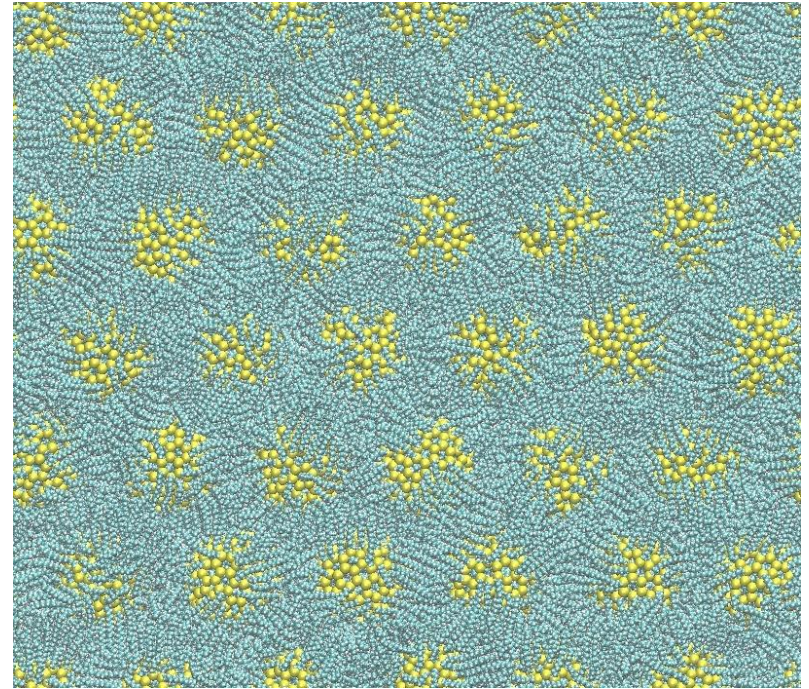
0.8 ns/day on 1920 cores Cray XE6 (Hopper), 1.1 ns/day on 1152 cores Red Sky

4 nm Diameter Alkanethiol Nanoparticles



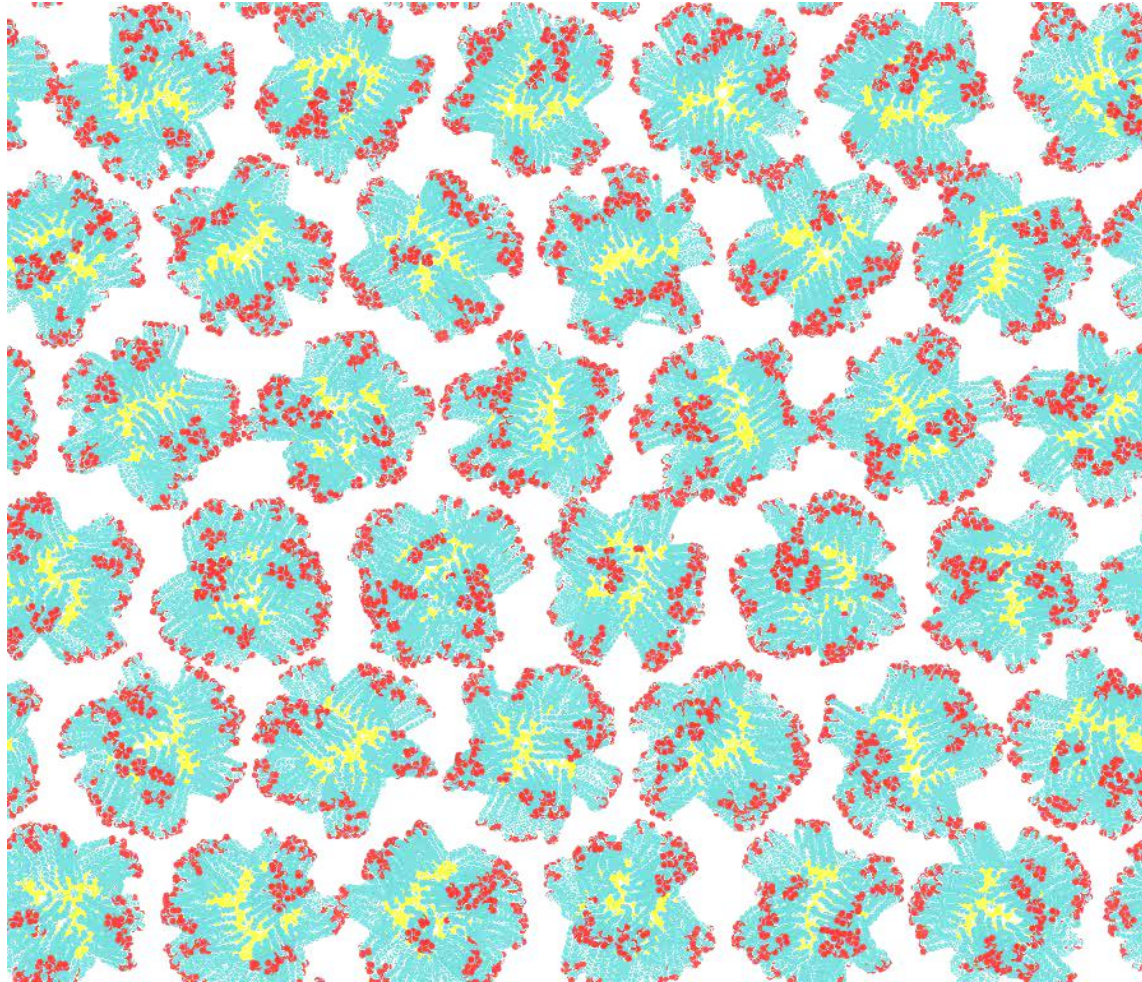
36 Nanoparticles – Hexagonal Lattice
4 ns – initial lattice spacing 80Å

CH₃ terminal group



Equilibrium 65 Å

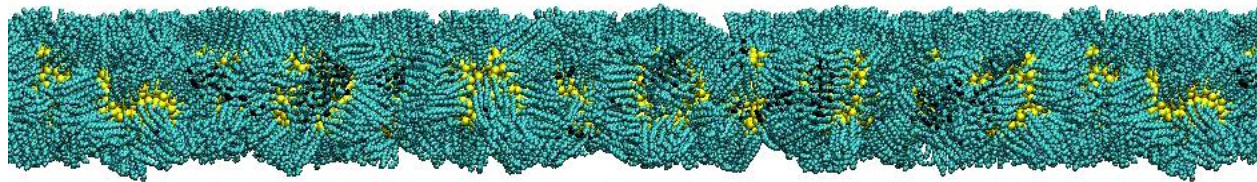
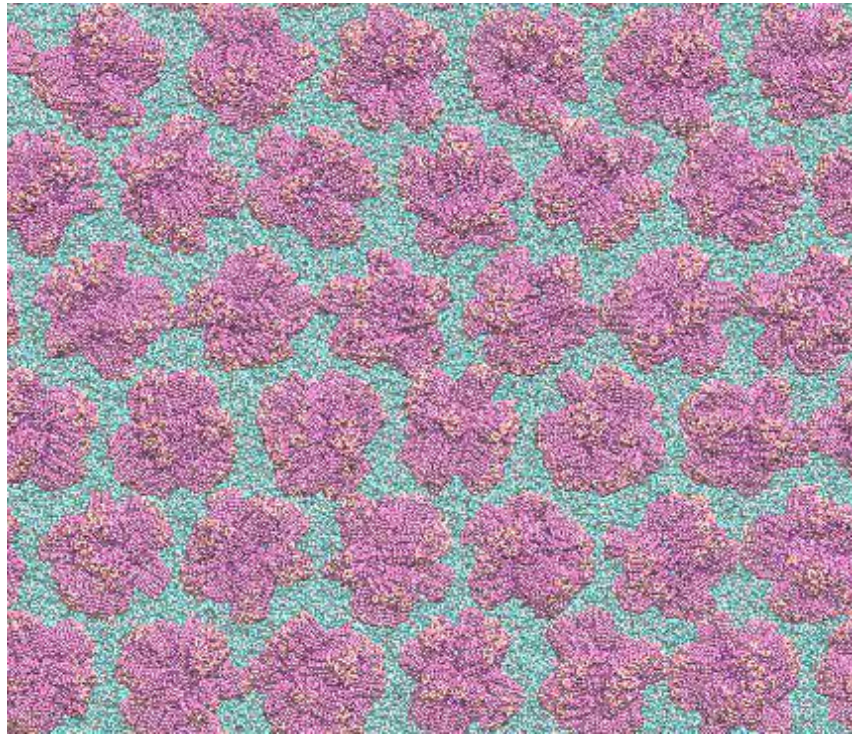
4 nm Diameter Alkanethiol Nanoparticles



COOH terminal group

36 Nanoparticles – Hexagonal Lattice
6.2 ns – initial lattice spacing 90Å

4 nm Diameter Alkanethiol Nanoparticles

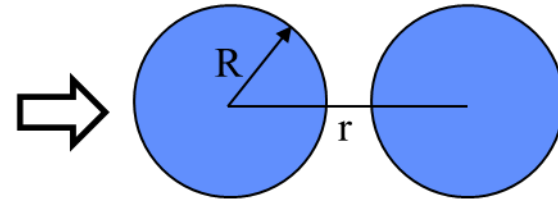
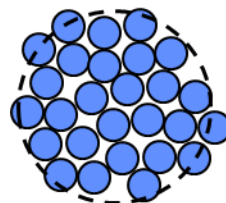


COOH terminal group

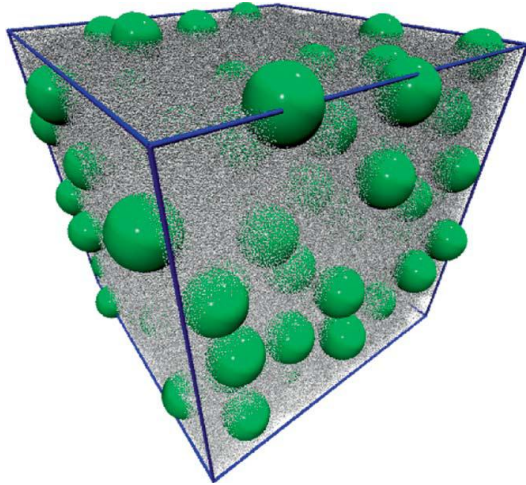
36 Nanoparticles – Hexagonal Lattice
12 ns – initial lattice spacing 90Å

Coarse Graining - Nanoparticle Solutions

- Natural length scale of solvent is comparable to size of NP
- Effective Potential
 - Integrated NP potential
 - Potential of Mean Force
- Solvent representation
 - Implicit - easy/ignores hydrodynamics
 - Explicit - number increases as volume of nanoparticle
NP diameter 20-25 x solvent diameter
 - Dissipative Particle Dynamics (DPD)
 - Stokesian Dynamics
 - Lattice Boltzmann
 - Multi-Particle Collision Dynamics

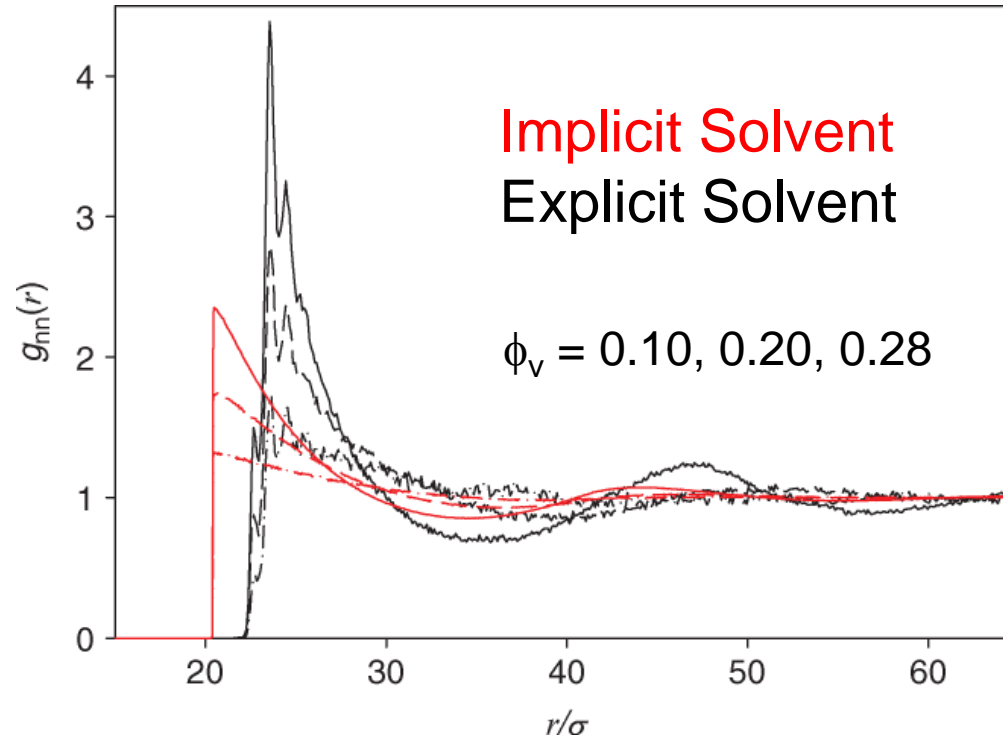


Minimal Model for NP in Suspension



- 167 NP of diameter 20σ in 1.8 million LJ monomers
- Integrated interaction between NP
- Most models treat large colloidal particles as hard spheres
 - not suitable for modeling NPs in an explicit solvent
 - hard spheres strongly phase separate even for relatively small differences in size
- To solvate NPs in an explicit solvent critical to include attractive component of the interaction between NP and solvent
- Solvent layer surrounding NP forms increases the effective radii of NP

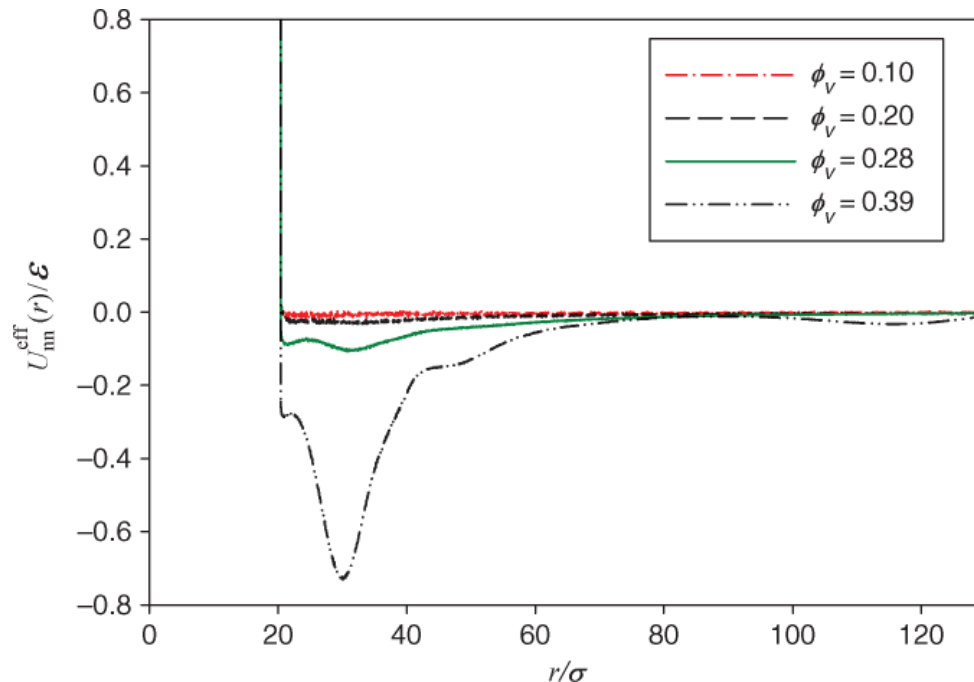
NP/NP Pair Correlation Function



- First peak is higher and shifted to larger separations for the explicit solvent
- Solvent forms a layer near NP
 - two NPs cannot approach as closely as for implicit solvent

Effective Potential between Nanoparticles

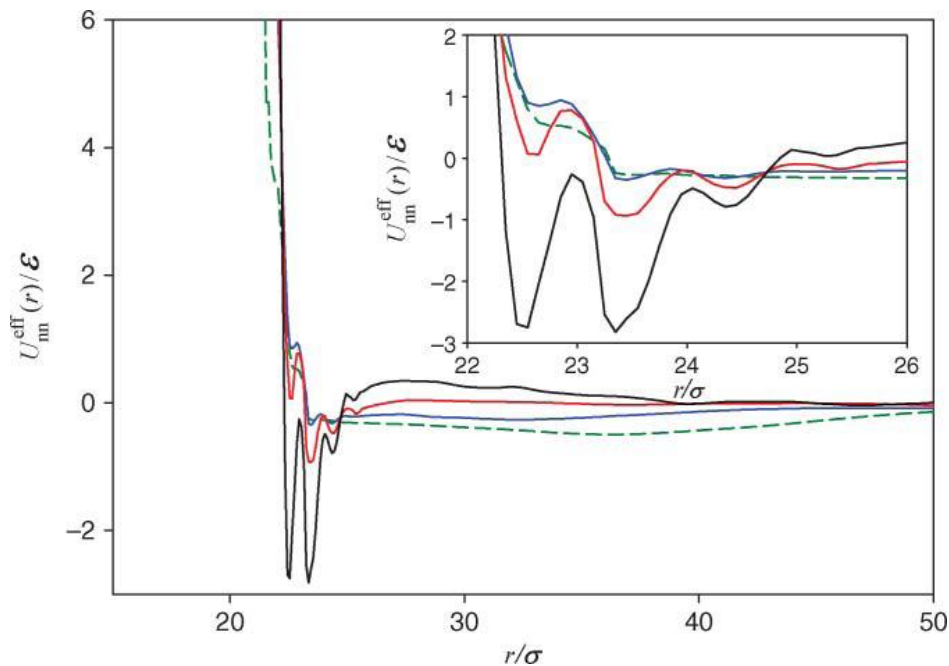
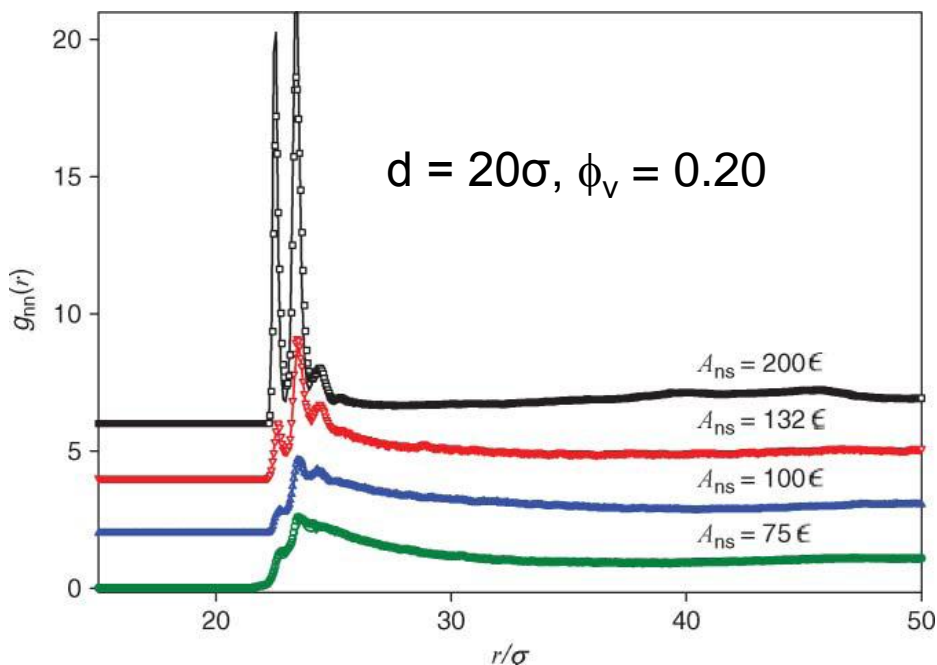
- Ornstein–Zernike equation with the Percus–Yevick closure approximation*
- Pure repulsive NP potential in implicit solvent recovered only for $\phi_v < 0.30$



*Behrens and Grier, PRE 64, 050401 (2001);
Rajagopalan and Rao, PRE 55, 4423 (1997);
Wang et al, PRE 81, 061204 (2010)

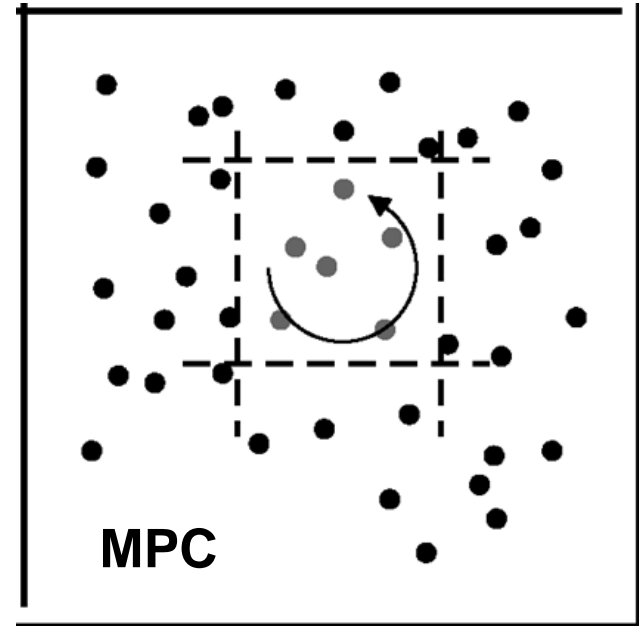
Effective Potential between Nanoparticles

- Effective Potential between NPs for varying strength of NP/solvent interaction



Multi-Particle Collision Dynamics

- Point particle based fluid
 - fluid interacts through collision operations
- Conserves linear momentum
- Produces fluctuating hydrodynamic behavior
- Computational efficient
 - No pair wise potential
 - Rotation does not limit time step
- Density/viscosity can be mapped to LJ fluid, water, ...*



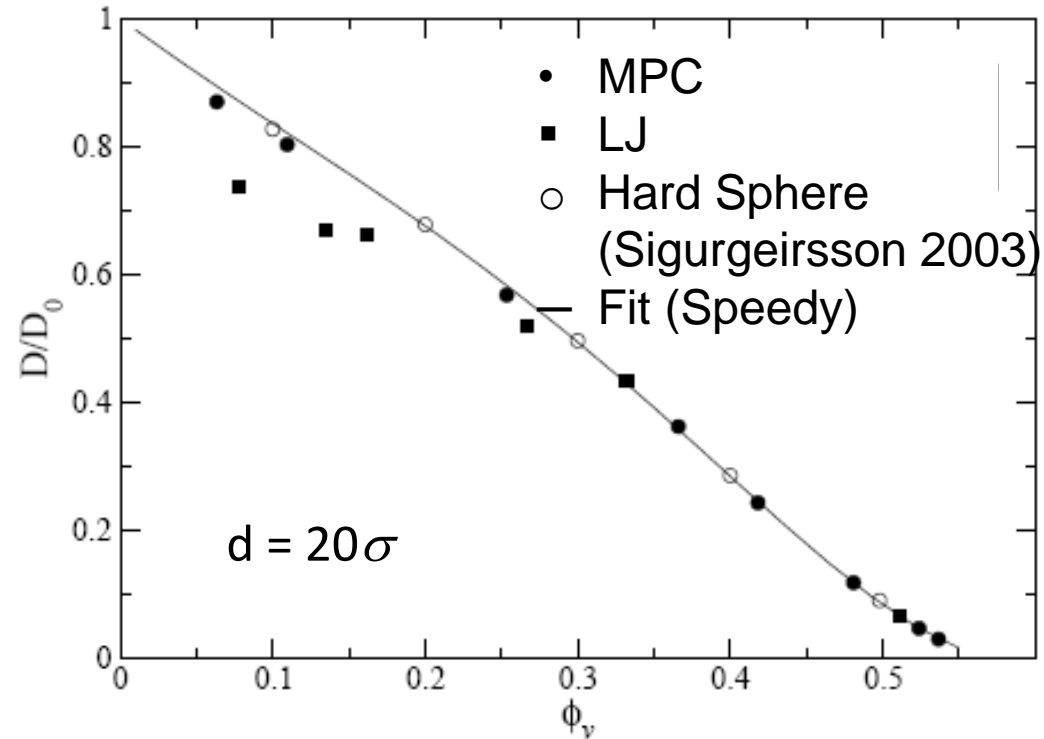
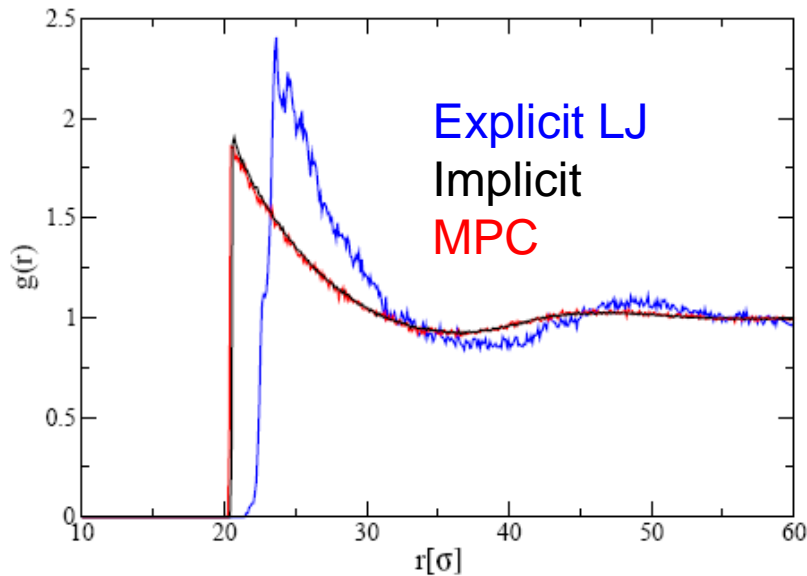
Malevanets and Kapral, J. Phys. Chem. 110, 8605 (1999).

Gompper et al, Adv. Polym. Sci. 221, 1 (2009)

*Petersen, JCP 132, 174106 (2010).

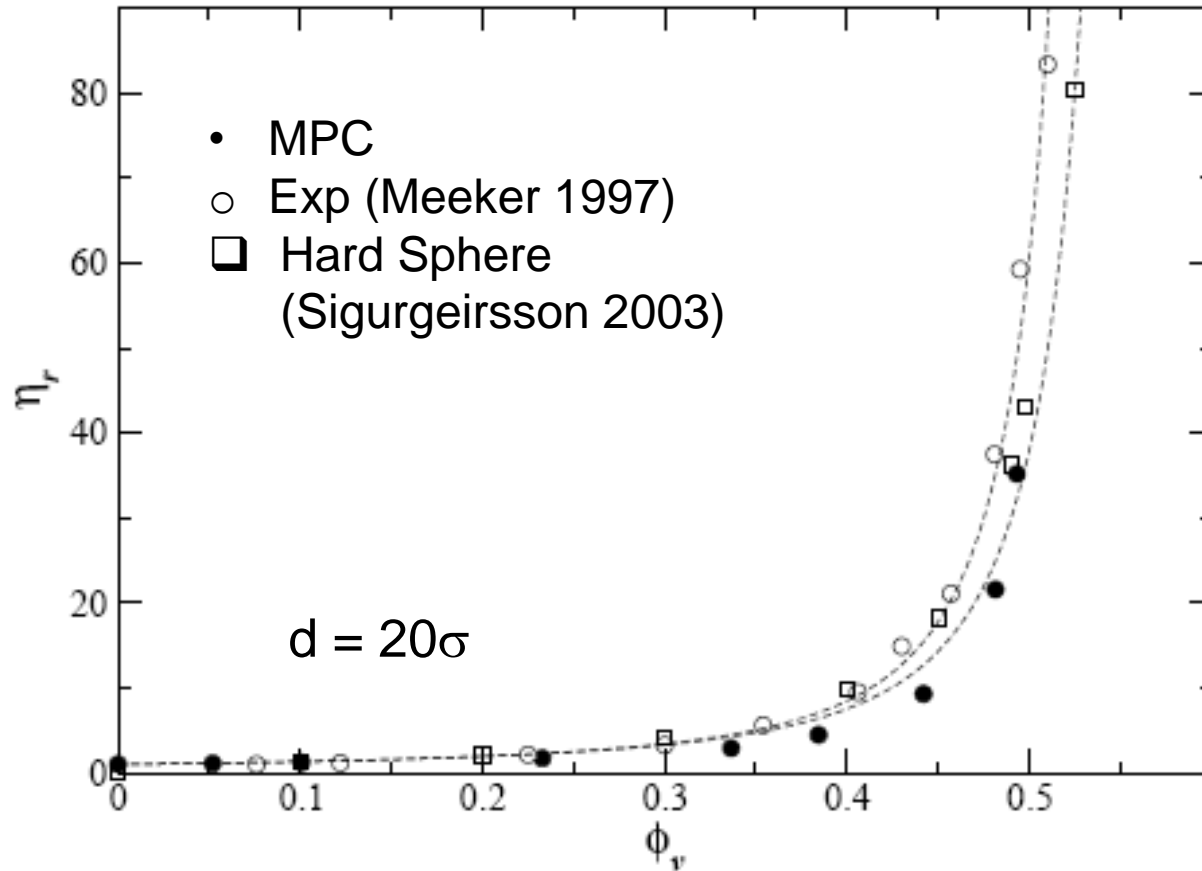
Equilibrium: Nanoparticle Diffusion

- Select MPC parameters to map to LJ viscosity and density
 - MPC have ideal gas pressure
- Implicit/MPC give identical $g(r)$



- MPC results agree with hard sphere experiments on micron size colloids
- Deviations for low ϕ_v for LJ solvent due to solvation shell around NP

Zero Shear-Rate Viscosity



- MPC results in good agreement with hard sphere simulations and experiment

Summary and Conclusions

- For small particles asymmetric coatings are the norm even for perfectly uniform grafting at full coverage
 - Geometric properties dictate when a coatings' spherical symmetry will be unstable.
 - Chain end group and the solvent play a secondary role in determining the properties of surface patterns.
- Water/vapor interface significantly distorts and orients the particle coatings
- Mapping to Coarse Grained Models captures some but not all the important details of Nanoparticles in Solution

Acknowledgements

Collaborators:

- J. Matthew Lane, Michael Chandross, Steve Plimpton, Mark Stevens (Sandia National Laboratories)
- Ahmed Ismail (Universität Aachen)
- Christian Lorenz (King's College)
- Qifei Wang, David J. Keffer (University of Tennessee)

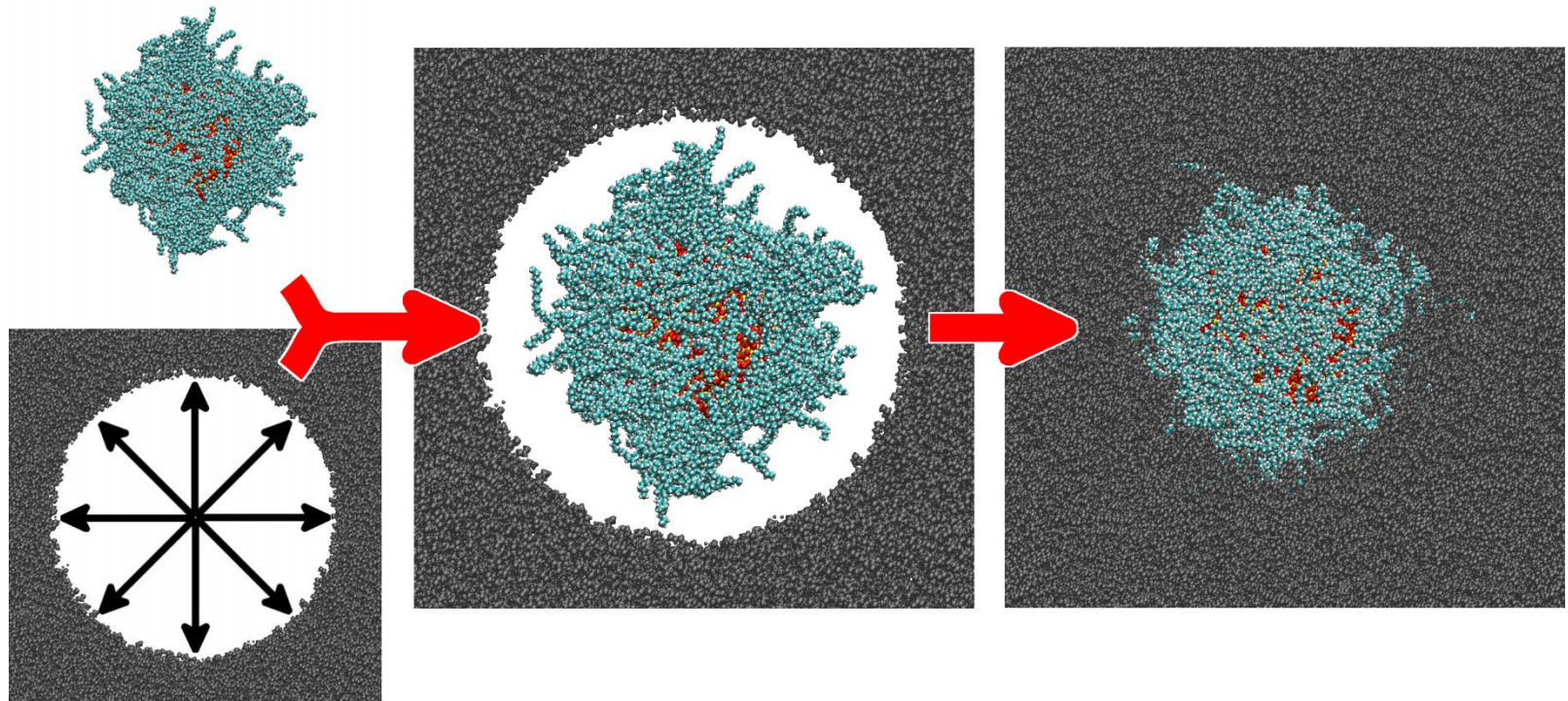
Funding:

- Center for Integrated Nanotechnology (CINT)
- DOE – ALCC grant 40 million core hours on NERSC/ORNL

Computers:

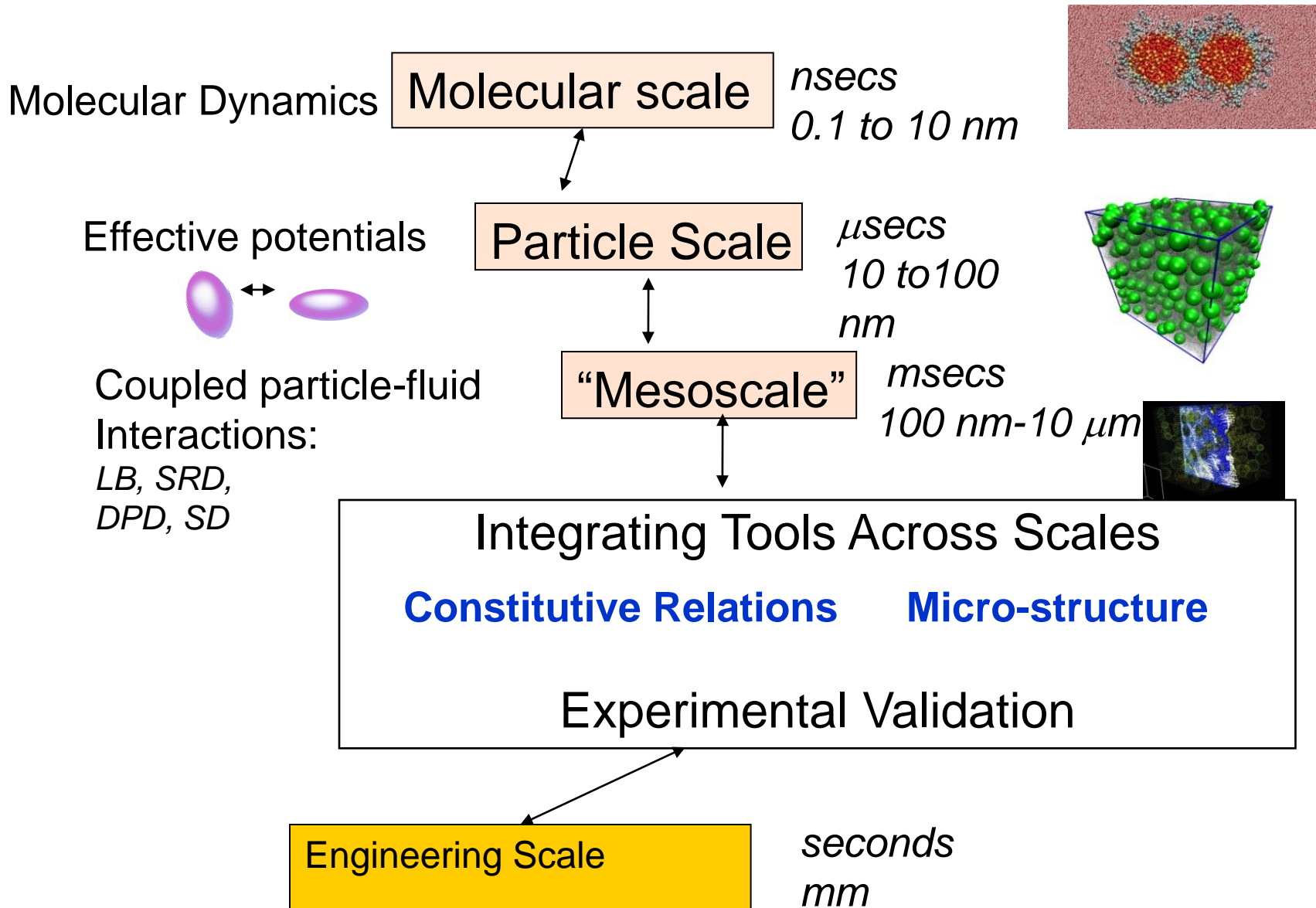
- Sandia's Red Sky/Red Mesa
- NERSC Hopper XE6
- ORNL Jaguar Cray XE6

How Systems are Build



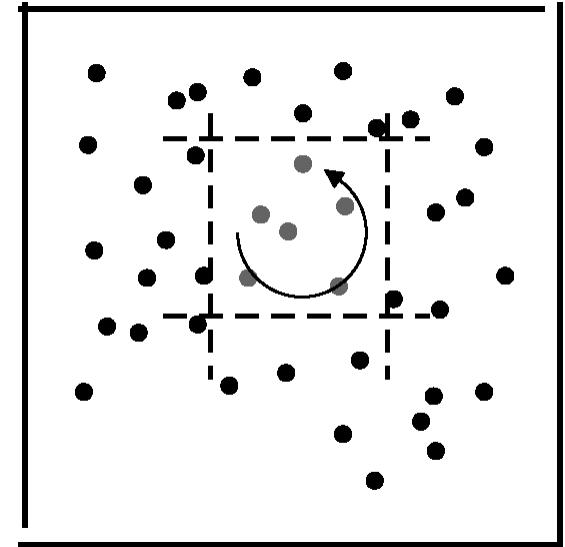
- Ligands attached to nanoparticle, equilibrated in implicit solvent
- Spherical cavity is grown in melt – NPT
- Nanoparticle inserted into melt, equilibrated - NPT
- System run for 2-10 ns - NVT

Integrated Hierarchical Approach



Multi-Particle Collision Dynamics

- Simulation cell divided up into cubic cells of side
 - On average, M SRD particles with mass m_f are placed in each cell of volume a^3
- Two simulation steps
 - Particle streaming
 - particles move according to Forward Euler $v_i t$
 - Velocity update (coarse-grained collision)
 - Apply rotation about randomly chosen axis to fluctuating part of the velocity



$$\mathbf{v}_i(t + \tau) = \mathbf{u}(\xi_i(t + \tau)) + \omega(\xi_i(t + \tau))(\mathbf{v}_i(t) - \mathbf{u}(\xi_i(t + \tau)))$$

- Or can have $U(r_{coll} - r_{SRD})$

$$m_f \frac{d\mathbf{v}_i}{dt} = \mathbf{f}_i$$

$$\frac{d\mathbf{r}_i}{dt} = \mathbf{v}_i$$

Coupling to Colloids

- MPC particles collide with colloids
 - Solvent coarse-grained so assume no-slip via stochastic rule
 - SRD particle receives a new random velocity magnitude

$$P(v_n) \propto v_n \exp(-\beta v_n^2)$$

$$P(v_t) \propto \exp(-\beta v_t^2)$$

- Difference in new and old velocity is momentum transferred to colloid
- Generalized slip conditions or pair-interaction, $U(r_{coll}-r_{SRD})$ possible

