

Dynamics of functionalised particles diffusing through reversible ligand-receptor bridges

Bortolo Matteo Mognetti

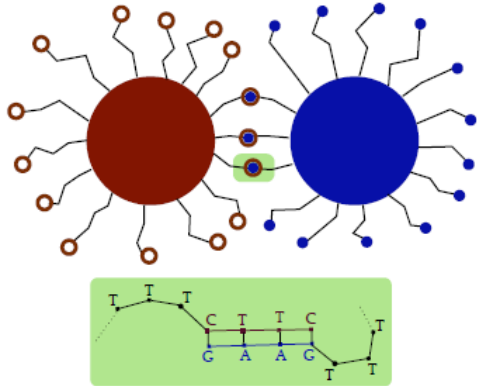
Université libre de Bruxelles, Interdisciplinary Center for Nonlinear Phenomena and Complex Systems, Belgium

Nanoparticle assemblies: 6 April 2023



Kavli Institute for
Theoretical Physics
University of California, Santa Barbara

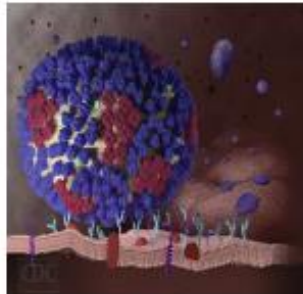
Ligand-receptor-mediated interactions



- Reversible supramolecular reaction (proteins, DNA/RNA, chemical complexes)
- Programmable self-assembly

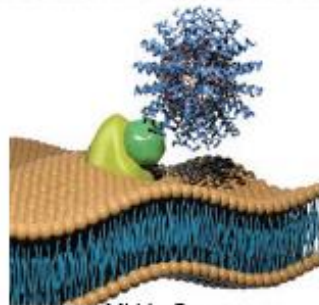
Mirkin *et al*, Nature **1996**
 Alivisatos *et al*, Nature **1996**

from biology to materials



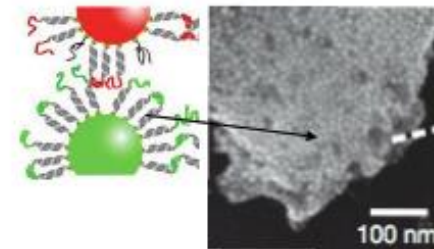
CDC website

viral infection
 cell signaling



Mirkin Group,
 Northwestern University

nanoparticles for
 drug delivery

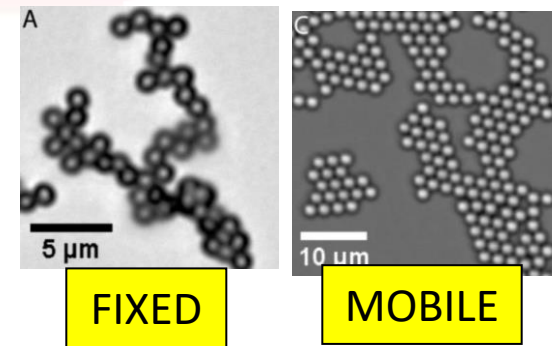
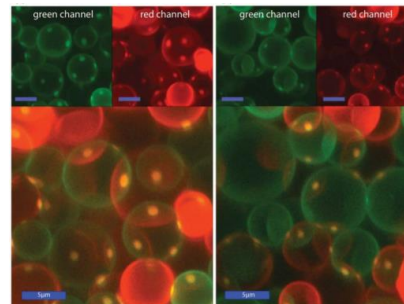
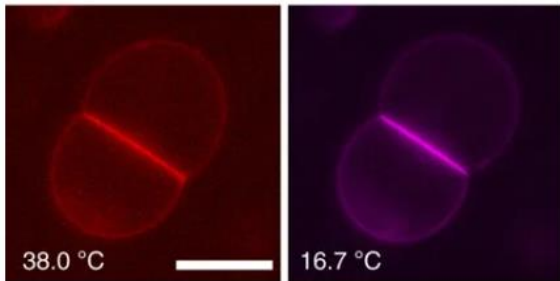
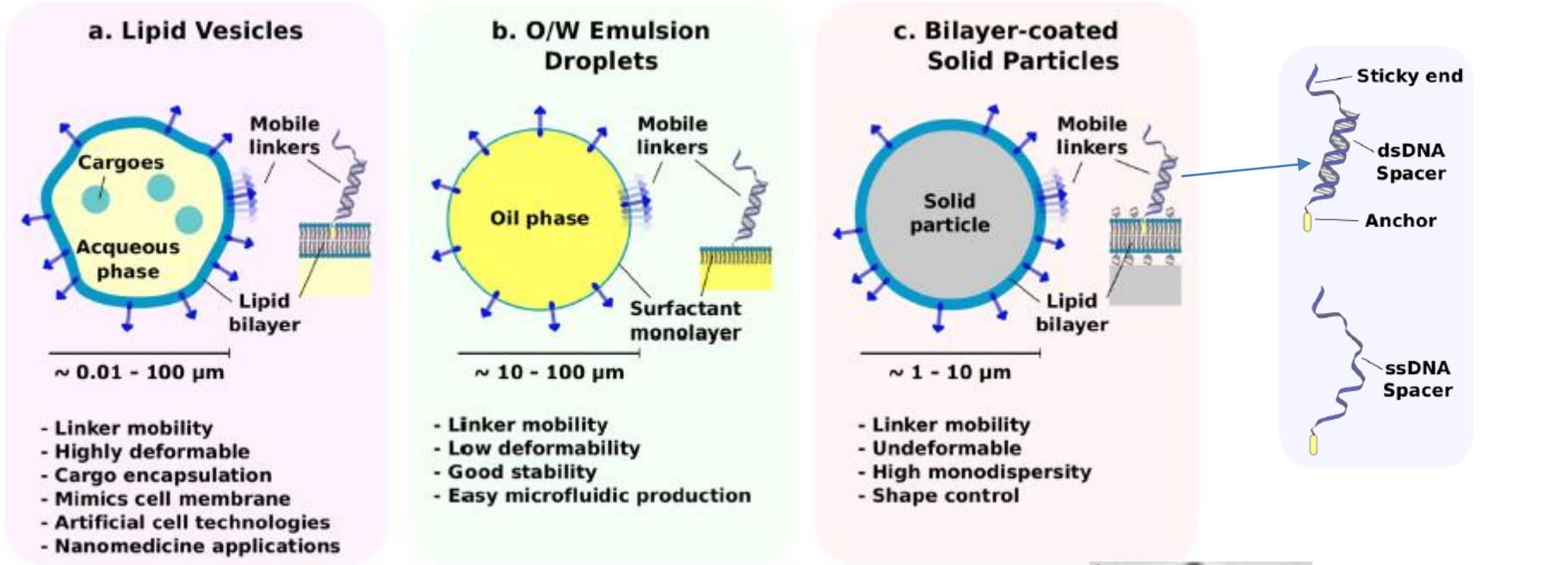


Nykypachuk *et al*,
 Nature 451 (2008)

Self-Assembly

Particles functionalized by mobile linkers

Mognetti *et al*, Rep. Progr. Phys. 2019



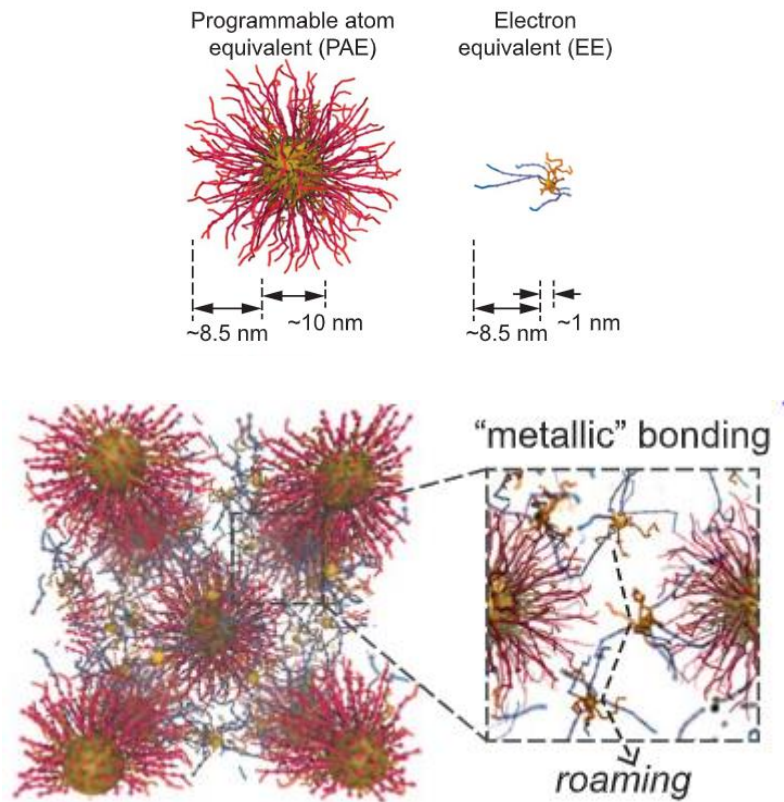
Parolini *et al*, Nat. Comm. 2015;
ACS Nano 2016
Bachmann *et al*, Soft Matter 2016

Feng *et al*, Soft Matter 2013
Zhang *et al*, Nat. Comm. 2018;
PNAS 2019

Van der Meulen *et al*, JACS 2013
Rinaldin *et al*, Soft Matter 2019

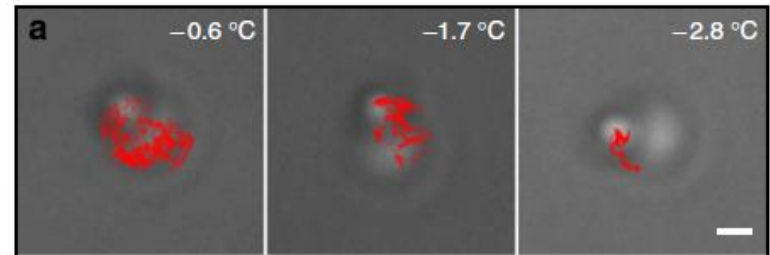
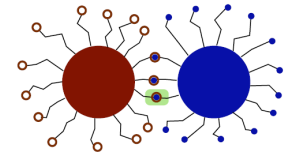
Building multivalent models

- Sticky ends continuously bind/unbind
- Particles acting as electrons



Girard *et al*, Science **2019**

- DNA coated colloids can roll without detaching



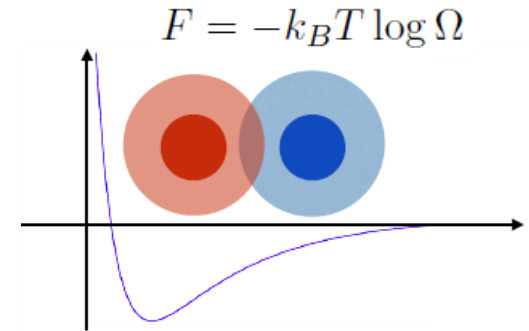
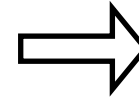
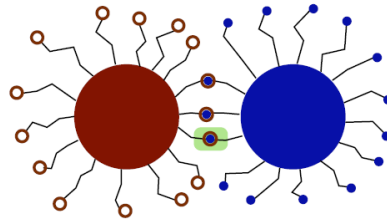
Wang *et al*, Nat. Commun. **2015**

- We need computational platforms capable of performing many reactions between sticky ends

Equilibrium models

- Effective interactions

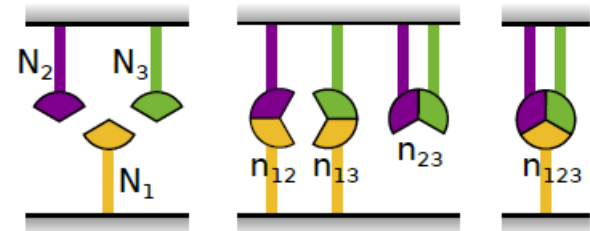
Bell *et al*, Biophys. J. **1984**



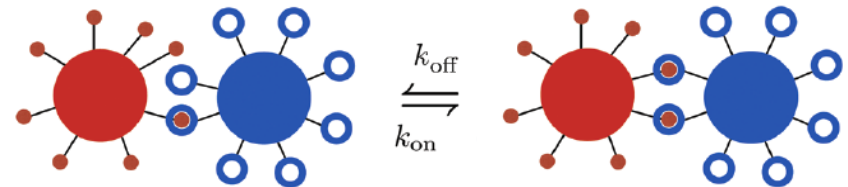
- Sampling over all possible ligand-receptor reactions

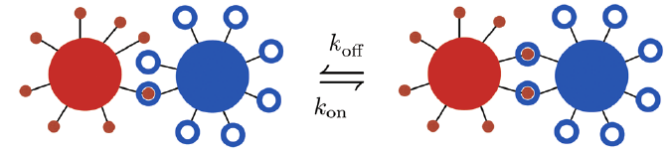
$$\frac{F}{k_B T} = \sum_i N_i \log \frac{\bar{n}_i}{N_i} + \sum_{i \leq j} \bar{n}_{ij} + 2 \sum_{i \leq j \leq k} \bar{n}_{ijk} + 3 \dots$$

Di Michele *et al*, J. Chem. Phys. **2016**; Angioletti-Uberti *et al*, J. Chem. Phys. **2013**; Varilly *et al*, J. Chem. Phys. **2013**



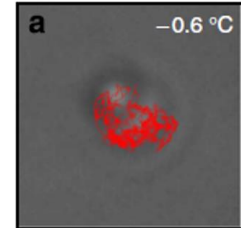
- Effective interactions based on the assumption that the reaction timescales are small





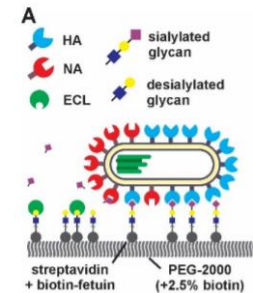
- Dynamics of particles moving through reversible ligand-receptor contacts

- Predicting the emerging diffusion constant D in reaction-limited conditions



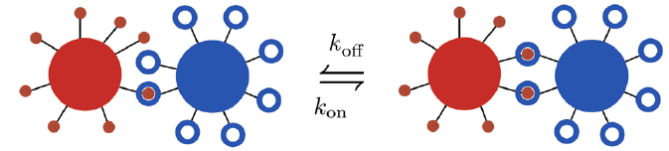
- Comparison with simulations and experiments

- Increasing the motility of the particles using enzymes (Influenza A Virus)



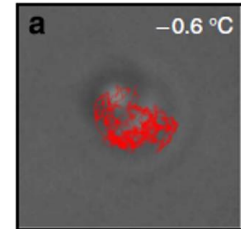
- Self-assembly dynamics

- Finite reaction rates alter the morphology of steady aggregates



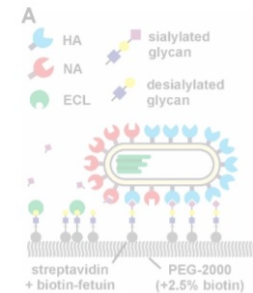
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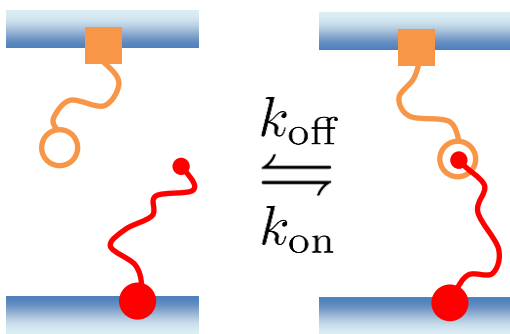
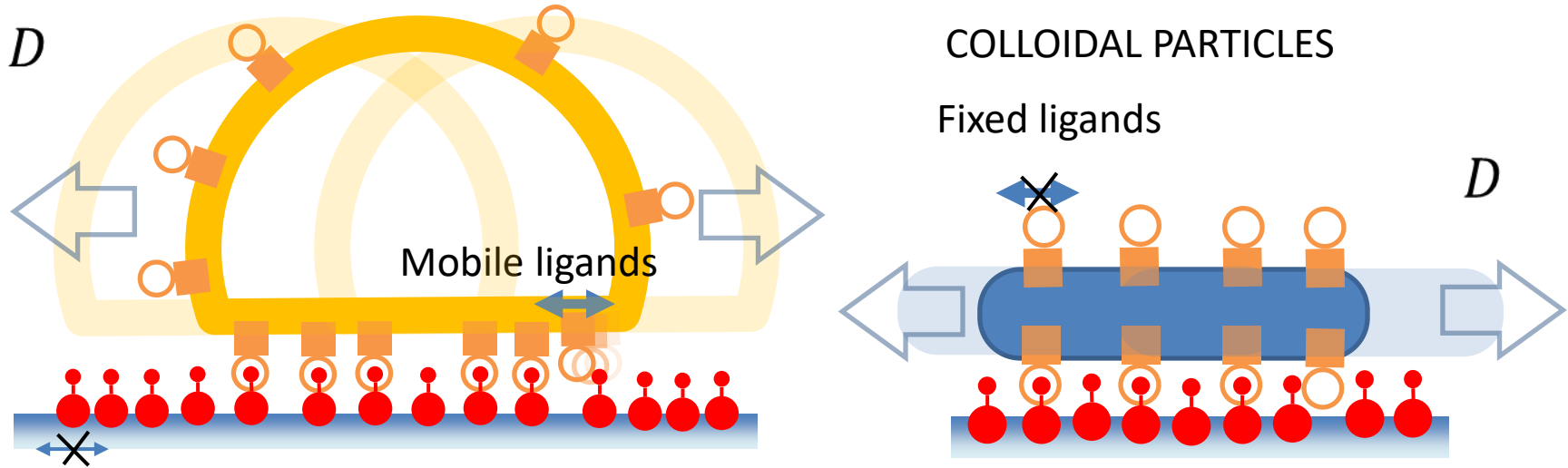
- Increasing the motility of the particles using enzymes (Influenza A Virus)



- Self-assembly dynamics

- Finite reaction rates alter the morphology of steady aggregates

Sliding across functionalised surfaces

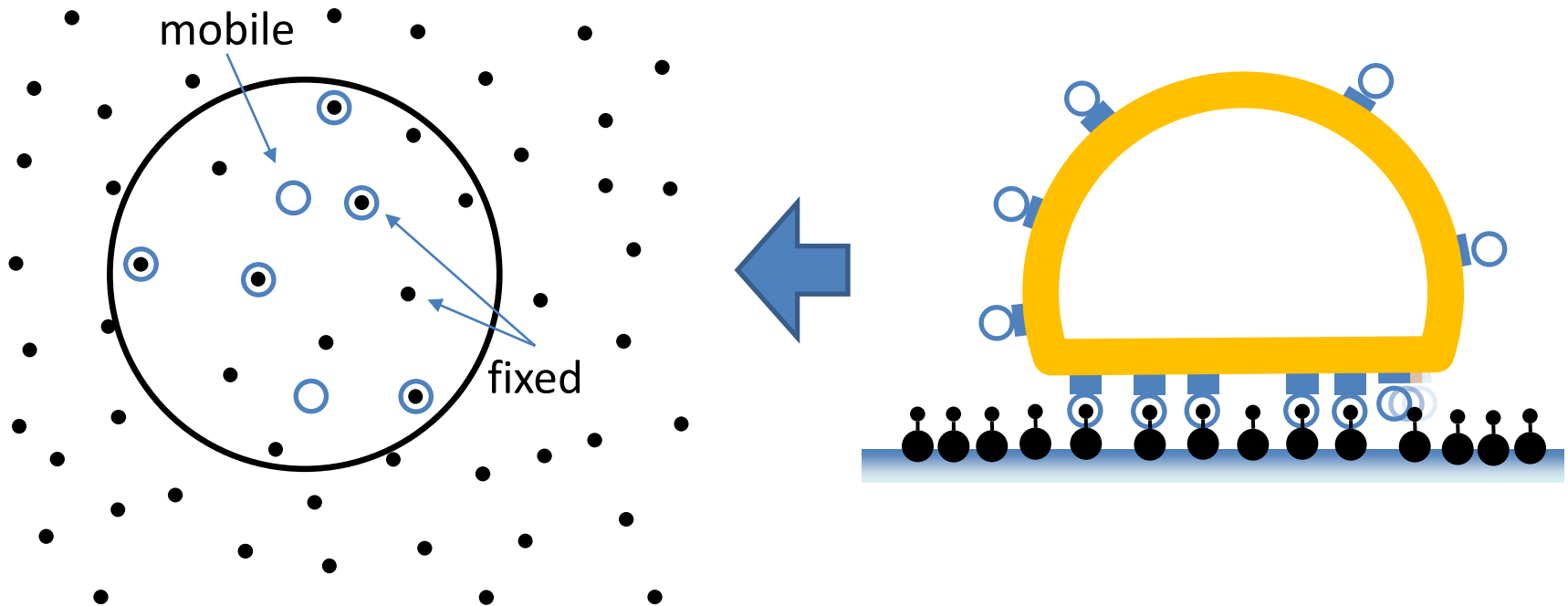


- We aim to predict the emerging diffusion constant of the particle, D , from the reaction rates, k_{on} and k_{off} , and the number of ligand-receptor bridges, n_b

Lowensohn, Stevens *et al.*, J. Chem. Phys. **2022**

Coarse-graining the diffusion dynamics

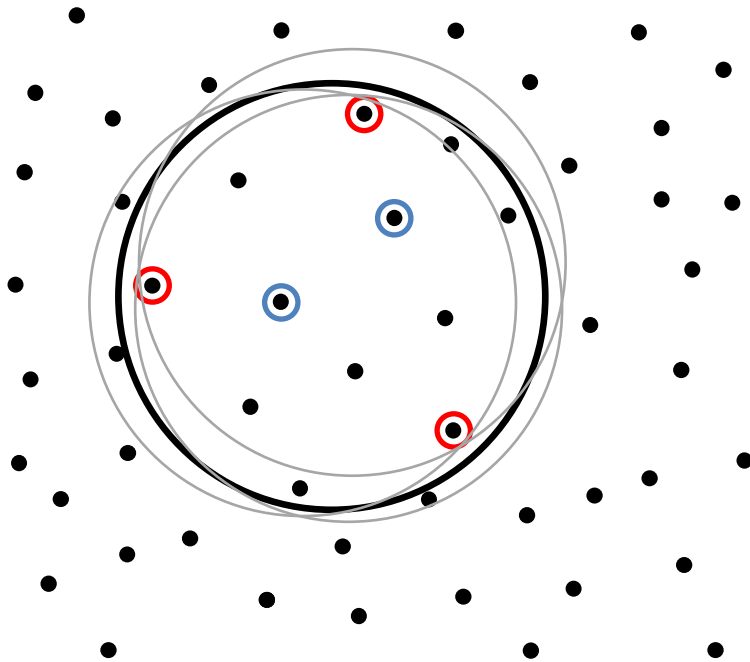
- 2D representation with fixed receptors and mobile ligands



- Receptors
- Ligand-receptor bridges
- Ligands

Coarse-graining the diffusion dynamics

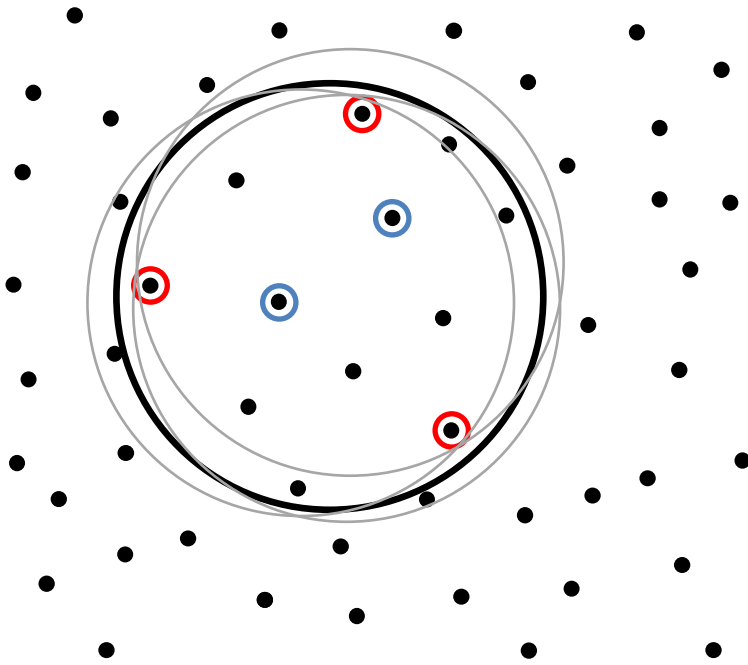
- Short timescales: the particle rattles around the current set of constraining bridges



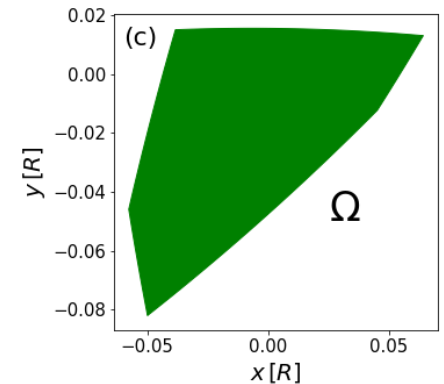
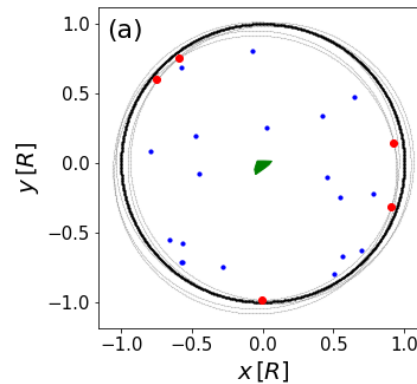
- Receptors
- ⊙ Ligand-receptor (non constraining) bridges
- ⊙ Constraining bridges (CBs)

Coarse-graining the diffusion dynamics

- Short timescales: the particle rattles around the current set of constraining bridges



- Ω : configurational region available to the particle's centre at a given set of CBs

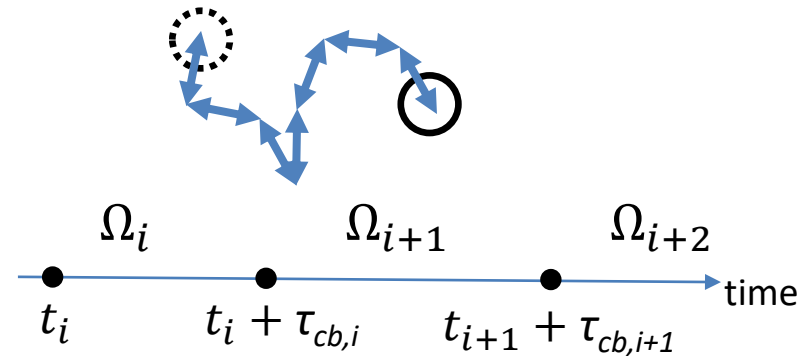
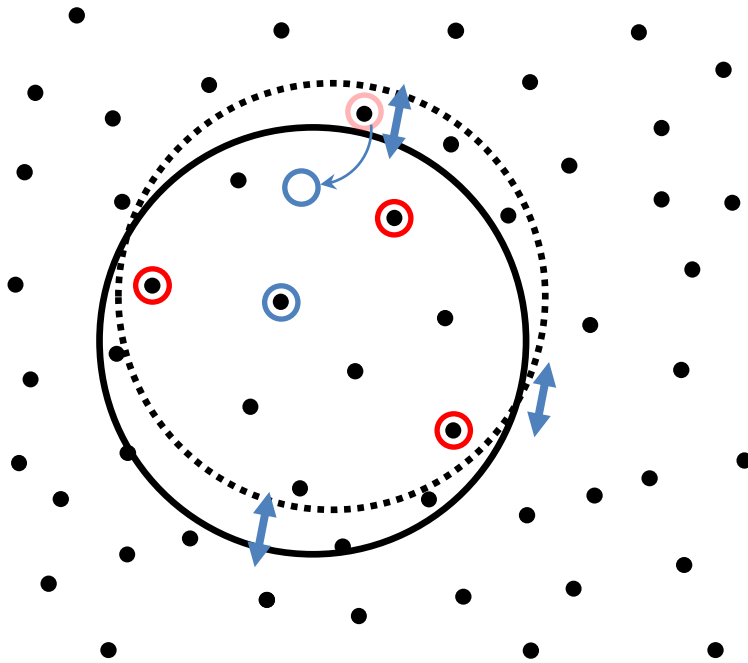


- Receptors
- ⊙ Ligand-receptor (non constraining) bridges
- ⊙ Constraining bridges (CBs)

Coarse-graining the diffusion dynamics

- Emerging diffusion controlled by the evolution of the set of CBs:

..., Ω_i, Ω_{i+1} ...



- Receptors

- Ligand-receptor bridges

- Constraining bridges (CBs)

- Time to update the set of CBs: τ_{cb}

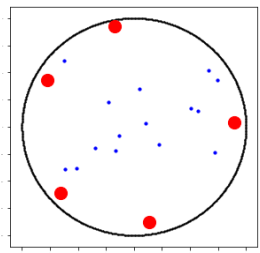
- Average displacement following an update of the CBs: δ_{cb}

- Emerging sliding diffusion constant, D

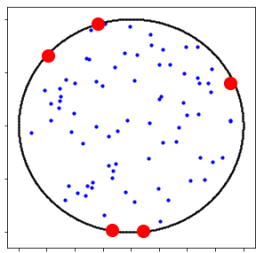
$$D = \frac{\langle \delta_{cb} \rangle^2}{2 \langle \tau_{cb} \rangle}$$

Constraining bridges

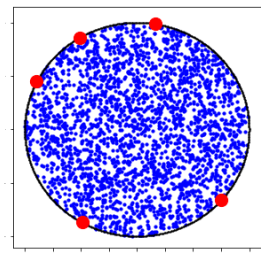
- The number of constraining bridges is finite



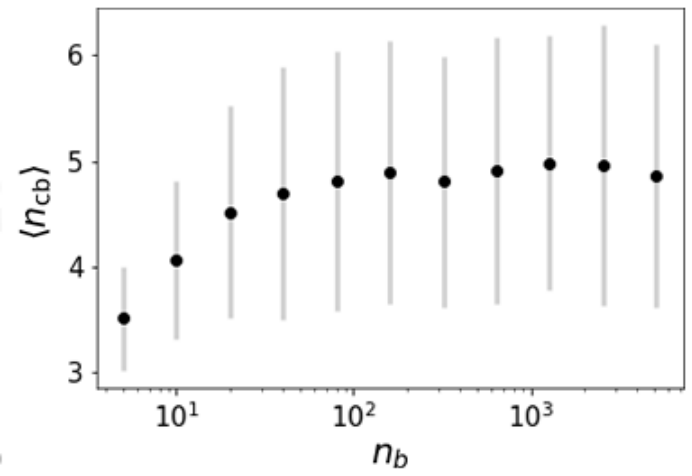
$\langle n_b \rangle = 20$



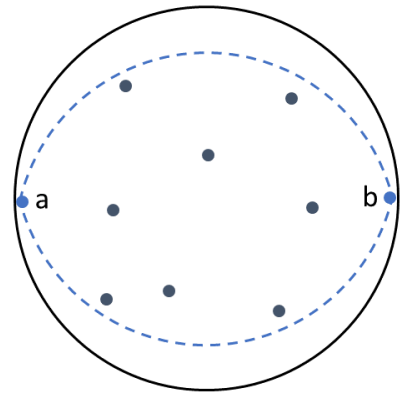
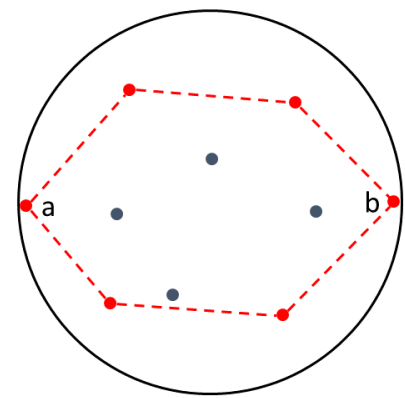
$\langle n_b \rangle = 80$



$\langle n_b \rangle = 2560$



- Not all bridges on the border of the particle (e.g., vertices of the convex hull) are CBs



Efron, Biometrika 1965

● - - - convex hull

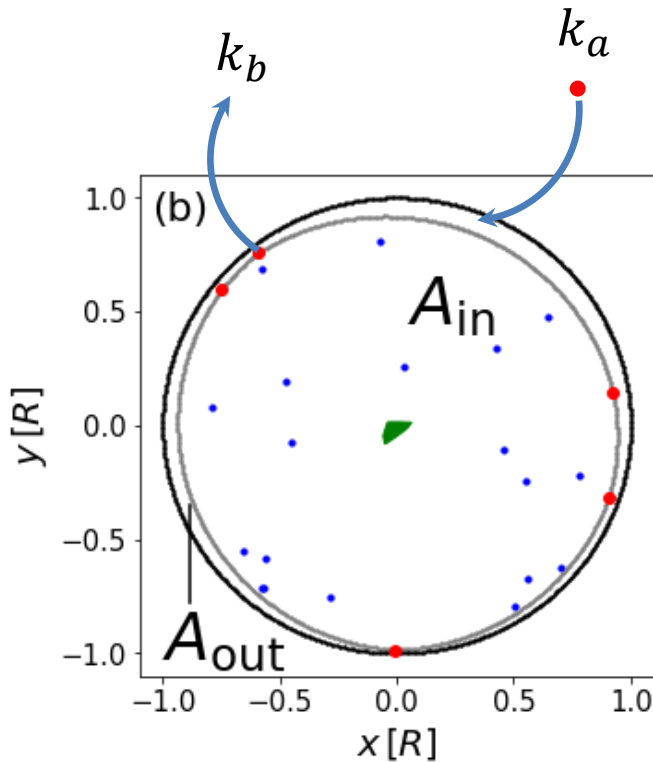
● - - - constraining bridges

$\langle n_{ch} \rangle \approx \log n_b$

$\langle n_{cb} \rangle \approx 4.9$

Updating sets of CBs: τ_{cb}

- Ω_i changes when (a) a bridge appears in A_{out} or (b) an existing CB is removed



- k_a : rate at which a bridge appears in A_{out}

$$k_a = n_L n_R k_{on} \frac{A_{out}}{\pi R^2}$$

- k_b : rate at which a constraining bridge is removed

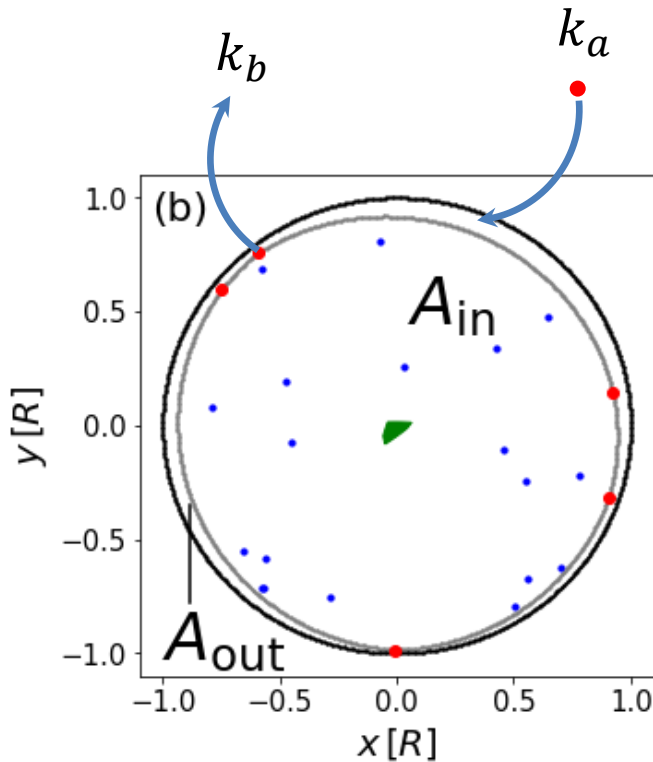
$$k_b = n_{cb} k_{off}$$

- In steady conditions, $\langle k_a \rangle = \langle k_b \rangle \rightarrow$

$$\langle \tau_{cb} \rangle = \frac{1}{\langle k_a \rangle + \langle k_b \rangle} = \frac{1}{2k_{off} \langle n_{cb} \rangle}$$

Updating sets of CBs: τ_{cb}

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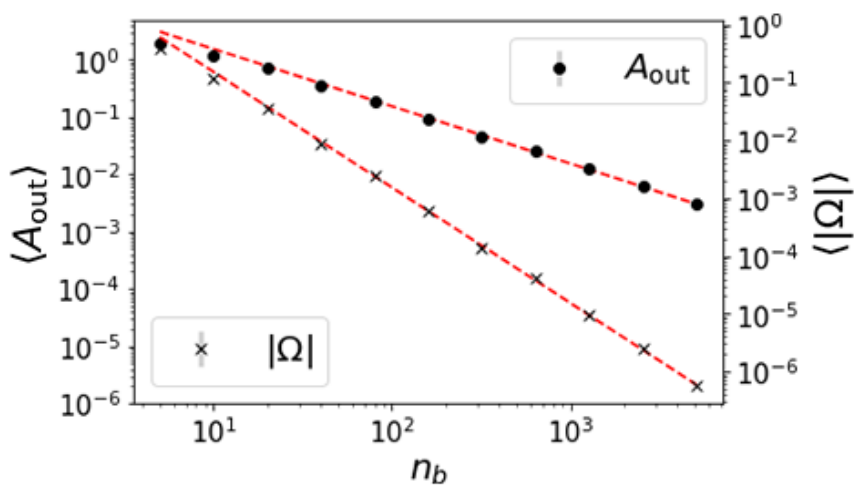
$$\langle \tau_{cb} \rangle = \frac{1}{\langle k_a \rangle + \langle k_b \rangle} = \frac{1}{2k_{off} \langle n_{cb} \rangle}$$

- In steady conditions, $\frac{d\langle n_b \rangle}{dt} = 0 \rightarrow$

$$\langle A_{out} \rangle = \pi \frac{R^2 \langle n_{cb} \rangle}{\langle n_b \rangle}$$

Updating sets of CBs: τ_{cb}

- Ω_i changes when (a) a bridge appears in A_{out} or (b) an existing CB is removed



- k_a : rate at which a bridge appears in A_{out}

$$k_a = n_L n_R k_{on} \frac{A_{out}}{\pi R^2}$$

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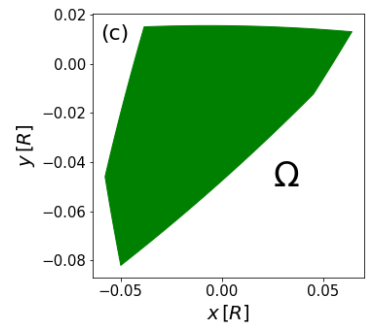
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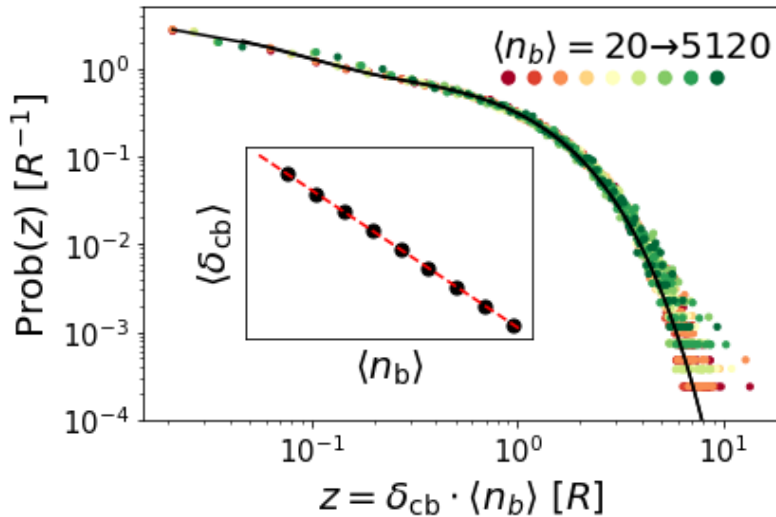
$$\langle |\Omega| \rangle = \frac{\langle A_{out} \rangle}{\langle n_b \rangle}$$

(fitted)



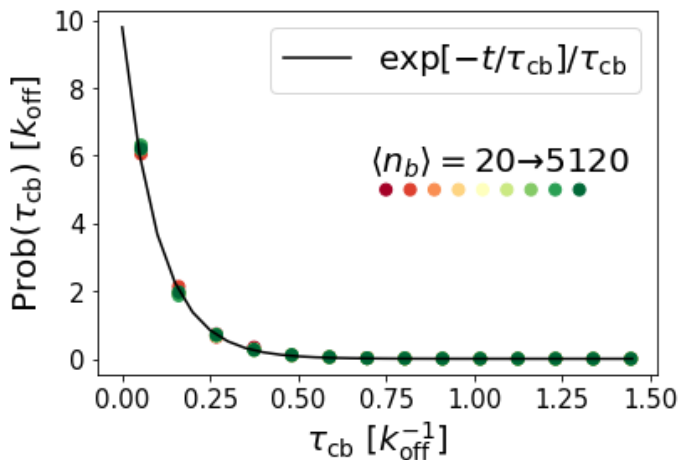
Updating sets of CBs: δ_{cb}

- Average displacement following an update of the CBs, δ_{cb}



$$\langle \delta_{cb} \rangle = \sqrt{\frac{\pi}{\langle n_{cb} \rangle} \frac{R}{\langle n_b \rangle}} \quad (\text{fitted})$$

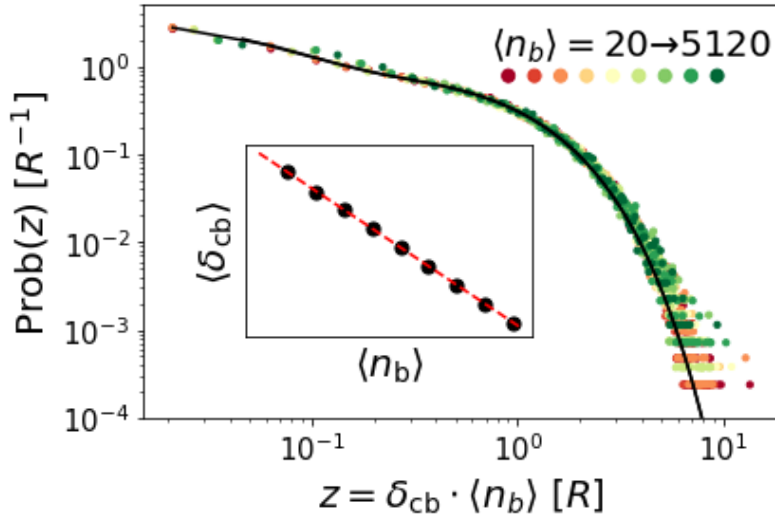
- δ_{cb} sampled using MC simulations in which we add/remove bridges while rattling the disk



- We verify that τ_{cb} follows the expected Poisson distribution

Updating sets of CBs: δ_{cb}

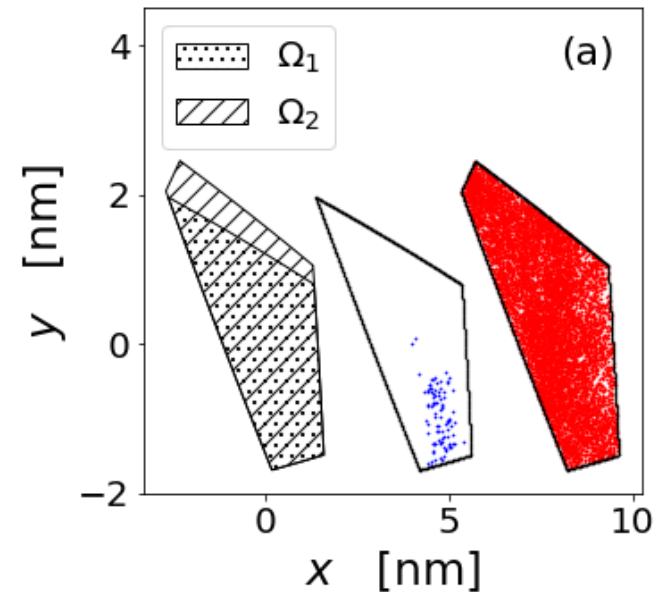
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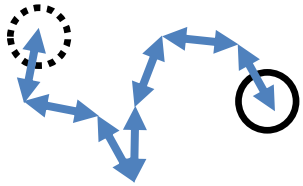
- δ_{cb} sampled using MC simulations in which we add/remove bridges while rattling the disk

- $\langle \delta_{cb} \rangle = \frac{\sqrt{\langle |\Omega| \rangle}}{\langle n_{cb} \rangle} \rightarrow$ Subsequent configurational spaces visited by the particle overlap $\Omega_i \cap \Omega_{i+1} \neq \emptyset$

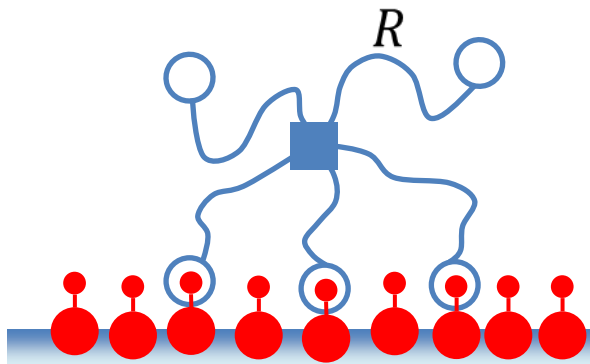


Emerging sliding diffusion constant

- Emerging diffusion constant, **mobile ligands**, $D = \frac{\langle \delta_{cb} \rangle^2}{2\langle \tau_{cb} \rangle} = \frac{\pi R^2 k_{off}}{\langle n_b \rangle^2}$



$$\langle \delta_{cb,i} \delta_{cb,i+1} \rangle = \langle \delta_{cb,i} \rangle \langle \delta_{cb,i+1} \rangle$$



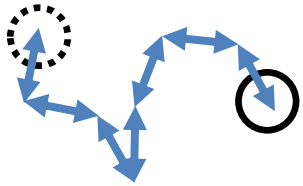
MOLECULAR WALKER

$$D = \frac{1}{2} \frac{k_{on} k_{off}}{k_{on} + k_{off}} \frac{R^2}{\langle n_b \rangle^2}$$

Kowalewski *et al*, J. Phys. Chem. B **125**, 6857 (2021)

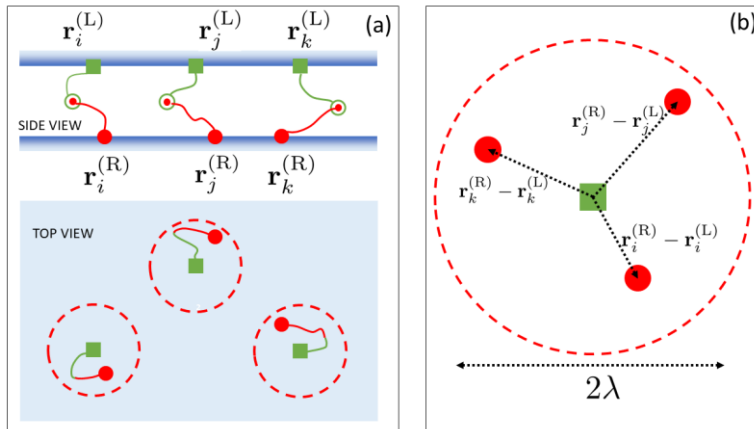
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$$\langle \delta_{cb,i} \delta_{cb,i+1} \rangle = \langle \delta_{cb,i} \rangle \langle \delta_{cb,i+1} \rangle$$

- Emerging sliding diffusion constant, **fixed ligands**, $D = \frac{\langle \delta_{cb} \rangle^2}{2\langle \tau_{cb} \rangle} = \frac{\pi \lambda^2 k_{\text{off}}}{\langle n_b \rangle^2}$



$$\langle \tau_{cb} \rangle = \frac{1}{2k_{\text{off}} \langle n_{cb} \rangle}$$

$$\langle \delta_{cb} \rangle = \sqrt{\frac{\pi}{\langle n_{cb} \rangle} \frac{\lambda}{\langle n_b \rangle}}$$

- λ : extensibility of a bridge

- **Mobile ligands:** $D = \frac{\langle \delta_{cb} \rangle^2}{2\langle \tau_{cb} \rangle} = \frac{\pi R^2 k_{\text{off}}}{\langle n_b \rangle^2}$
- **Fixed ligands:** $D = \frac{\langle \delta_{cb} \rangle^2}{2\langle \tau_{cb} \rangle} = \frac{\pi \lambda^2 k_{\text{off}}}{\langle n_b \rangle^2}$

○ Simulations (reaction-diffusion dynamics) validate the theory

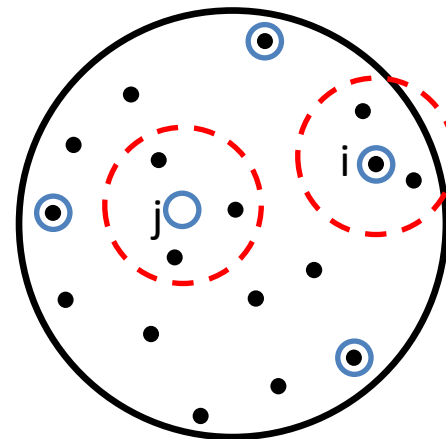
```

1:  $t \leftarrow 0$ 
2: while  $t < t_E$  do
3:   Fire Reactions( $\Delta t$ )
4:    $i_B = 0$ 
5:   while  $i_B < N_B$  do
6:     Brownian Diffusion( $\Delta t / N_B$ )
7:      $i_B \leftarrow i_B + 1$ 
8:   end while
9:    $t \leftarrow t + \Delta t$ 
10: end while

```

- The reaction algorithm (Gillespie) samples the type of reaction to be implemented and the time for it to happen t_{reac}

$$a_{\text{on}}^T = \sum_i a_{\text{on}}(i) \quad a_{\text{off}}^T = k_{\text{off}} n_b$$



$$a_{\text{on}}(i) = 0$$

$$a_{\text{on}}(j) = 3k_{\text{on}}$$

https://github.com/bmoggetti/SlidingDiffusionConstant_Mobile.git
https://github.com/StevensLaurie/Disk_Diffusion

- **Mobile ligands:** $D = \frac{\langle \delta_{cb} \rangle^2}{2\langle \tau_{cb} \rangle} = \frac{\pi R^2 k_{\text{off}}}{\langle n_b \rangle^2}$
- **Fixed ligands:** $D = \frac{\langle \delta_{cb} \rangle^2}{2\langle \tau_{cb} \rangle} = \frac{\pi \lambda^2 k_{\text{off}}}{\langle n_b \rangle^2}$

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$$a_{\text{on}}^T = \sum_i a_{\text{on}}(i) \quad a_{\text{off}}^T = k_{\text{off}} n_b$$

$$P(t_{\text{reac}}) = (a_{\text{on}}^T + a_{\text{off}}^T) e^{-(a_{\text{on}}^T + a_{\text{off}}^T) t_{\text{reac}}}$$

- If $t_r + t_{\text{reac}} < \Delta t$, we update the affinity lists, implement a reaction, and select a new t_{reac}

<https://github.com/bmoggetti/>

SlidingDiffusionConstant_Mobile.git

https://github.com/StevensLaurie/Disk_Diffusion

- **Mobile ligands:** $D = \frac{\langle \delta_{cb} \rangle^2}{2\langle \tau_{cb} \rangle} = \frac{\pi R^2 k_{\text{off}}}{\langle n_b \rangle^2}$
- **Fixed ligands:** $D = \frac{\langle \delta_{cb} \rangle^2}{2\langle \tau_{cb} \rangle} = \frac{\pi \lambda^2 k_{\text{off}}}{\langle n_b \rangle^2}$

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7:      $i_B \leftarrow i_B + 1$ 
8:   end while
9:    $t \leftarrow t + \Delta t$ 
10: end while

```

- Brownian Dynamics diffusion of the particle's position $r(t + \Delta t) = r(t) + \Delta r$

$$\Delta r = \frac{f D_0 \Delta t}{k_B T} + \delta r \quad \langle \delta r^2 \rangle = 2 D_0 \Delta t$$

$$\Delta \varphi = \frac{\tau D_0^R \Delta t}{k_B T} + \delta \varphi \quad \langle \delta \varphi^2 \rangle = 2 D_0^R \Delta t$$

- If a bridge becomes overstretched the BD update is rejected
- To limit the rejection rate, we divide the BD update into N_B sub-steps

<https://github.com/bmoggetti/>

[SlidingDiffusionConstant_Mobile.git](https://github.com/bmoggetti/SlidingDiffusionConstant_Mobile.git)

https://github.com/StevensLaurie/Disk_Diffusion

• **Mobile ligands:** $D = \frac{\langle \delta_{cb} \rangle^2}{2\langle \tau_{cb} \rangle} = \frac{\pi R^2 k_{\text{off}}}{\langle n_b \rangle^2}$ **Fixed ligands:** $D = \frac{\langle \delta_{cb} \rangle^2}{2\langle \tau_{cb} \rangle} = \frac{\pi \lambda^2 k_{\text{off}}}{\langle n_b \rangle^2}$

- Simulations (reaction-diffusion dynamics) validate the theory

```

1:  $t \leftarrow 0$ 
2: while  $t < t_E$  do
3:   Fire Reactions( $\Delta t$ )
4:   Static Update()
5:    $t \leftarrow t + \Delta t$ 
6: end while

```

- In the reaction-limited regime, we update the position of the particle by sampling Ω statically

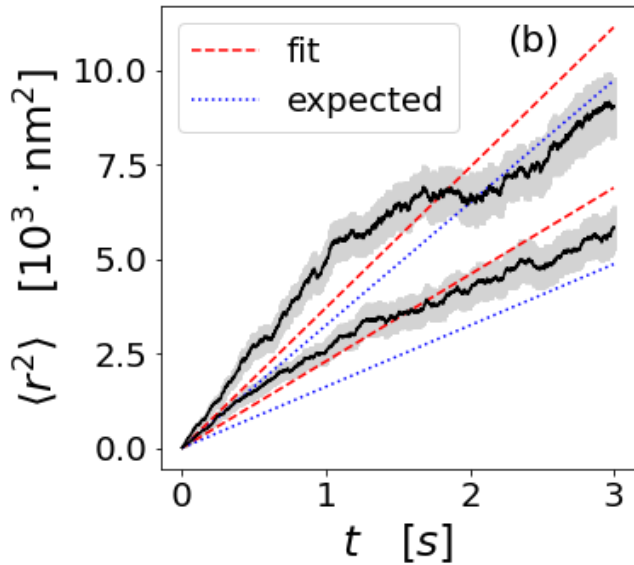
https://github.com/bmoggetti/SlidingDiffusionConstant_Mobile.git
https://github.com/StevensLaurie/Disk_Diffusion

Simulation validation

- Mobile ligands:** $D = \frac{\langle \delta_{cb} \rangle^2}{2\langle \tau_{cb} \rangle} = \frac{\pi R^2 k_{\text{off}}}{\langle n_b \rangle^2}$
- Fixed ligands:** $D = \frac{\langle \delta_{cb} \rangle^2}{2\langle \tau_{cb} \rangle} = \frac{\pi \lambda^2 k_{\text{off}}}{\langle n_b \rangle^2}$

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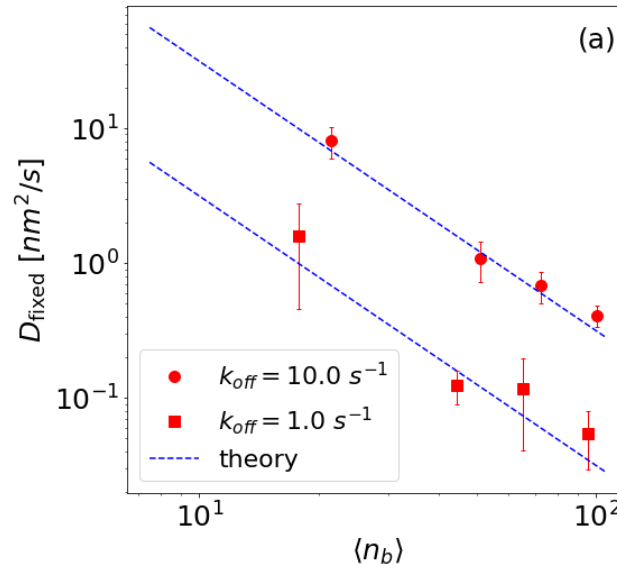
MOBILE



$$k_{\text{off}} = 318 \cdot \text{s}^{-1}; 636 \cdot \text{s}^{-1}$$

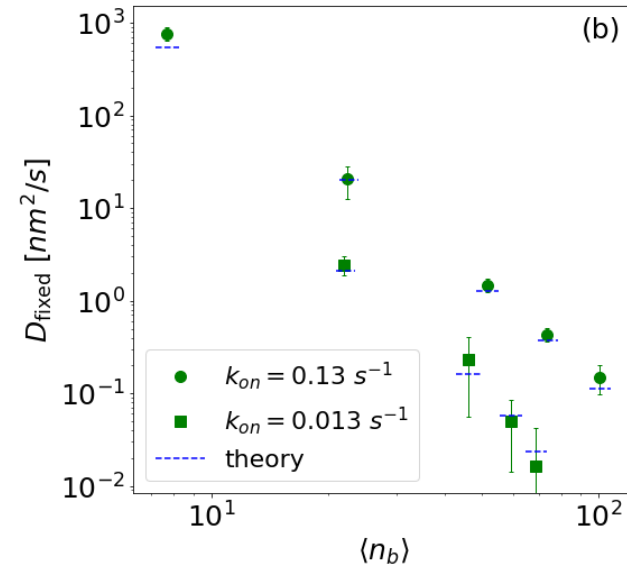
$$\langle n_b \rangle \approx 110$$

FIXED



- Different values of k_{on}

FIXED

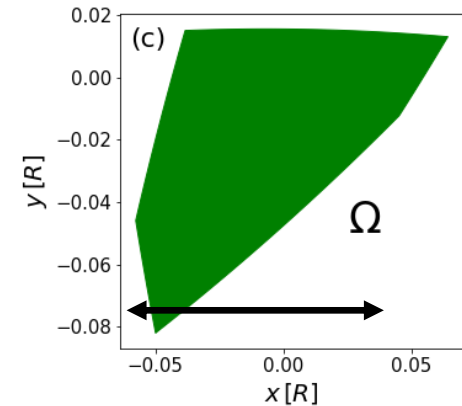
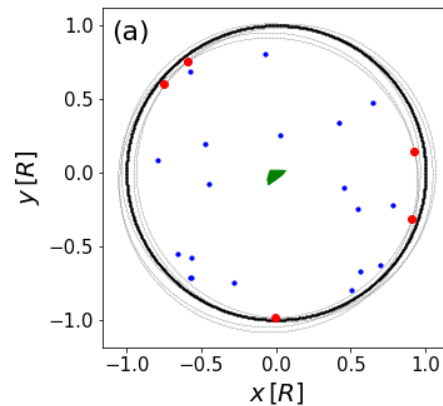
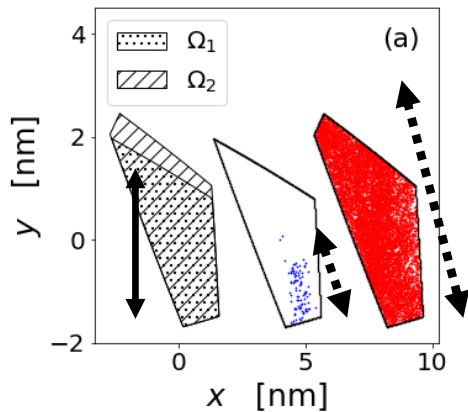


- Different values of k_{off}

Discussion: possible limitations

- **Mobile ligands:** $D = \frac{\langle \delta_{cb} \rangle^2}{2\langle \tau_{cb} \rangle} = \frac{\pi R^2 k_{\text{off}}}{\langle n_b \rangle^2}$ **Fixed ligands:** $D = \frac{\langle \delta_{cb} \rangle^2}{2\langle \tau_{cb} \rangle} = \frac{\pi \lambda^2 k_{\text{off}}}{\langle n_b \rangle^2}$

- The theory neglects that D may be limited by hydrodynamic friction. Predictions are reliable if $D_0 \langle \tau_{cb} \rangle \geq |\Omega|$ (reaction-limited diffusion)



- $\sqrt{D_0 \cdot \tau_{cb}}$: potential distance explored by the trajectory while rattling

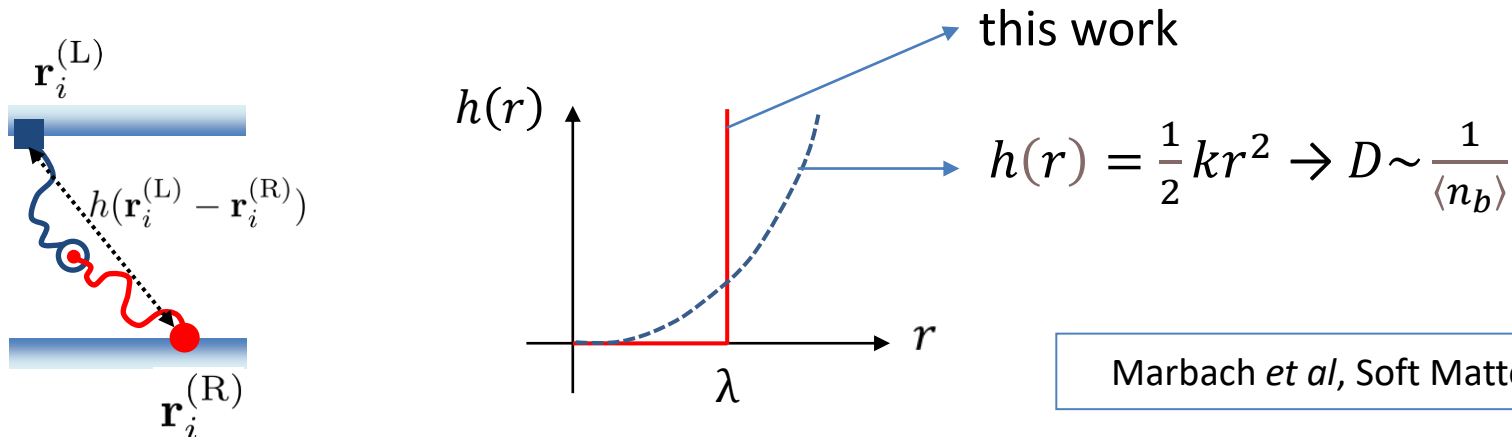
- $\sqrt{|\Omega|}$: typical linear extension of the configurational space
 $\sqrt{|\Omega|} \sim \frac{R}{\langle n_b \rangle}$ (mobile) $\sim \frac{\lambda}{\langle n_b \rangle}$ (fixed)

Discussion: possible limitations

- **Mobile ligands:** $D = \frac{\langle \delta_{cb} \rangle^2}{2\langle \tau_{cb} \rangle} = \frac{\pi R^2 k_{\text{off}}}{\langle n_b \rangle^2}$ **Fixed ligands:** $D = \frac{\langle \delta_{cb} \rangle^2}{2\langle \tau_{cb} \rangle} = \frac{\pi \lambda^2 k_{\text{off}}}{\langle n_b \rangle^2}$
- The theory neglects that D may be limited by hydrodynamic friction. Predictions are reliable if $D_0 \langle \tau_{cb} \rangle \geq |\Omega|$ (reaction-limited diffusion)
- Static and dynamic correlations between stochastic variables (e.g., $\langle A_{\text{out}} n_{cb} \rangle$, $\langle \delta_{cb} \cdot n_{cb} \rangle$, $\langle \delta_{cb,i} \cdot \delta_{cb,i+1} \rangle$, ...)

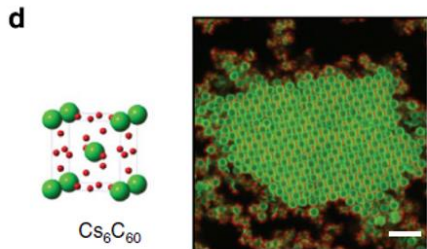
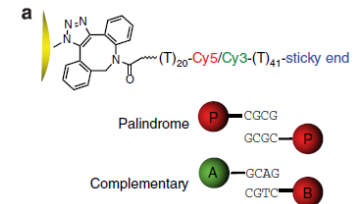
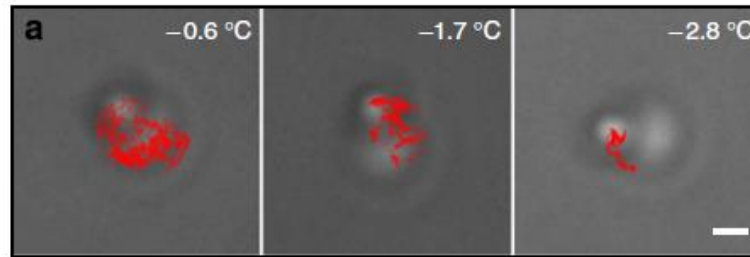
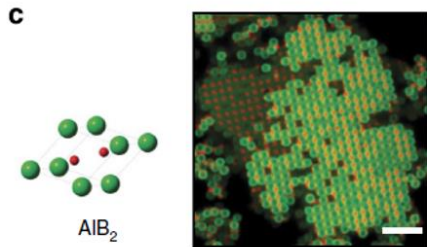
Discussion: possible limitations

- Mobile ligands:** $D = \frac{\langle \delta_{cb} \rangle^2}{2\langle \tau_{cb} \rangle} = \frac{\pi R^2 k_{\text{off}}}{\langle n_b \rangle^2}$
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- Results based on a particular choice of the bond potential $h(r)$



ULB Discussion: experimental predictions

- **Mobile ligands:** $D = \frac{\langle \delta_{cb} \rangle^2}{2\langle \tau_{cb} \rangle} = \frac{\pi R^2 k_{\text{off}}}{\langle n_b \rangle^2}$ **Fixed ligands:** $D = \frac{\langle \delta_{cb} \rangle^2}{2\langle \tau_{cb} \rangle} = \frac{\pi \lambda^2 k_{\text{off}}}{\langle n_b \rangle^2}$
- DNA coated colloids with a high grafting density crystallize



Wang *et al*, Nat. Commun. **2015**; Kim *et al*, Langmuir. **2006**

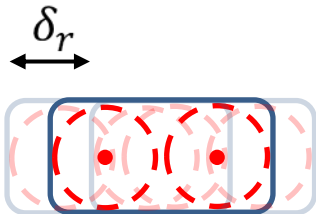
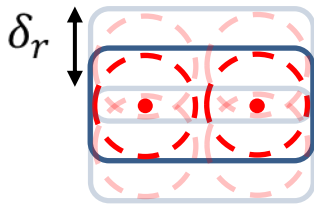
$$\langle n_b \rangle \sim \rho_R \rho_L e^{-\beta \Delta G(T)}$$

$$k_{\text{off}} \sim e^{\beta \Delta G(T)}$$

- Higher values of ρ_R or ρ_L will increase the value of the hybridisation free energy $\Delta G(T)$ (at a given $\langle n_b \rangle$) and therefore increase k_{off}

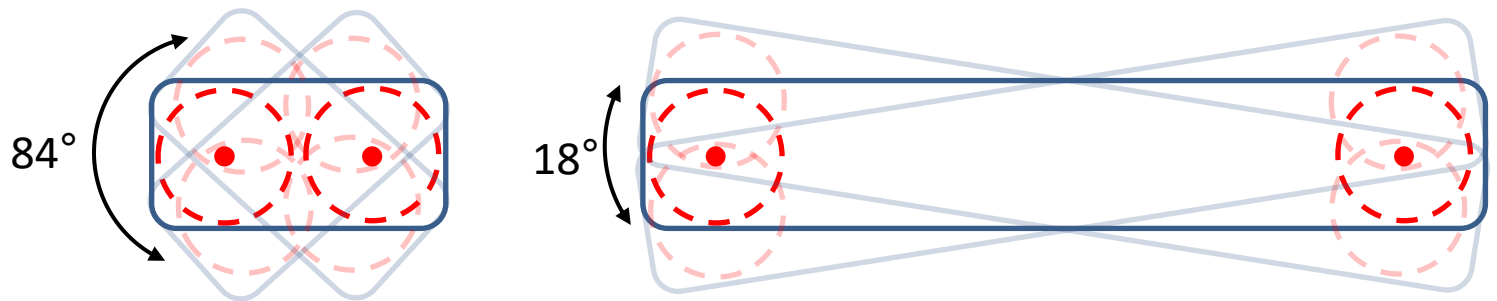
ULB Discussion: experimental predictions

- **Mobile ligands:** $D = \frac{\langle \delta_{cb} \rangle^2}{2\langle \tau_{cb} \rangle} = \frac{\pi R^2 k_{\text{off}}}{\langle n_b \rangle^2}$ **Fixed ligands:** $D = \frac{\langle \delta_{cb} \rangle^2}{2\langle \tau_{cb} \rangle} = \frac{\pi \lambda^2 k_{\text{off}}}{\langle n_b \rangle^2}$
 - DNA coated colloids with a high grafting density crystallize
 - The translational diffusion constant is not a function of the particle shape



Discussion: experimental predictions

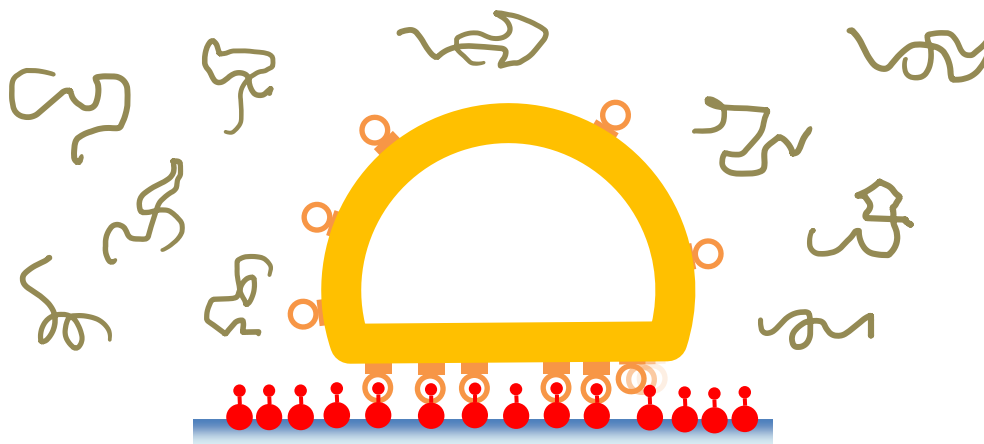
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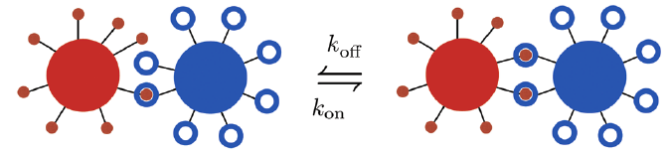
(the rotational diffusion constant is affected by the particle shape)

ULB Discussion: experimental predictions

- **Mobile ligands:** $D = \frac{\langle \delta_{cb} \rangle^2}{2\langle \tau_{cb} \rangle} = \frac{\pi R^2 k_{\text{off}}}{\langle n_b \rangle^2}$ **Fixed ligands:** $D = \frac{\langle \delta_{cb} \rangle^2}{2\langle \tau_{cb} \rangle} = \frac{\pi \lambda^2 k_{\text{off}}}{\langle n_b \rangle^2}$
 - DNA coated colloids with a high grafting density crystallize
 - The translational diffusion constant is not a function of the particle shape
 - The emerging mobility is not a function of the hydrodynamic friction

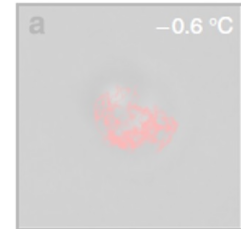


D is not affected by crowders



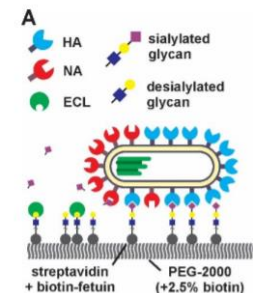
- Dynamics of particles moving through reversible ligand-receptor contacts

- Predicting the emerging diffusion constant D in reaction-limited conditions



- Comparison with simulations and experiments

- Increasing the motility of the particles using enzymes (Influenza A Virus)

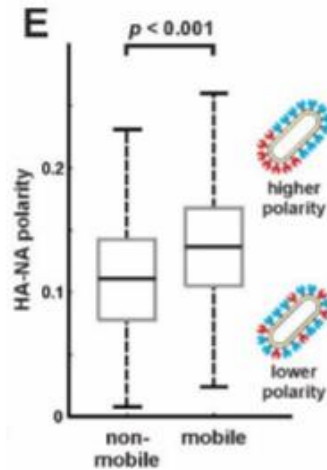
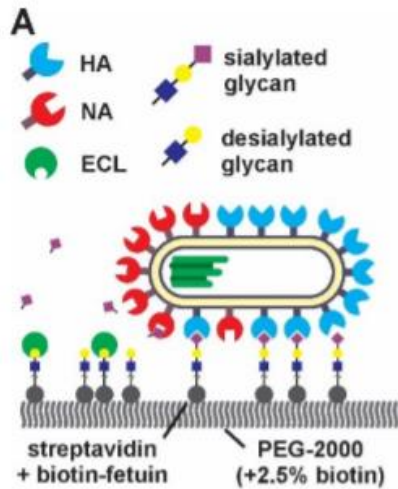


- Self-assembly dynamics

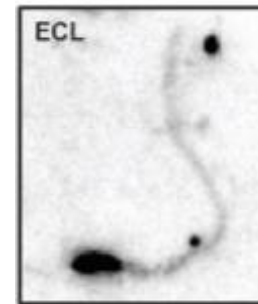
- Finite reaction rates alter the morphology of steady aggregates

Mobility of IAV virions

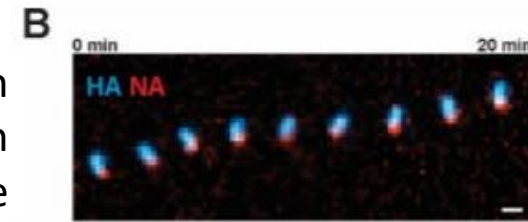
- IAV virions carry receptor-binding (HA) and receptor-cleaving (NA) proteins



persistent motion
towards the HA-rich
pole



trails of passivated
receptors

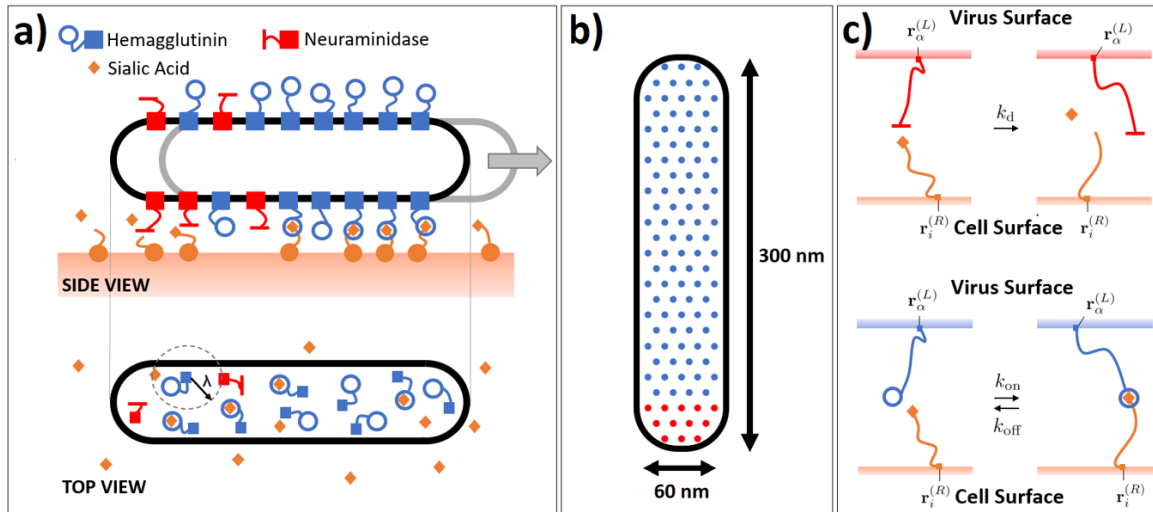


Vahey, Fletcher eLife 2019

- Hemagglutinin (HA) binds to receptors presenting sialic acid (SA) residues
- Receptor-cleaving protein neuraminidase (NA) passivates receptors
- The reduced number of HA-SA contact increases the motility of IAV virions

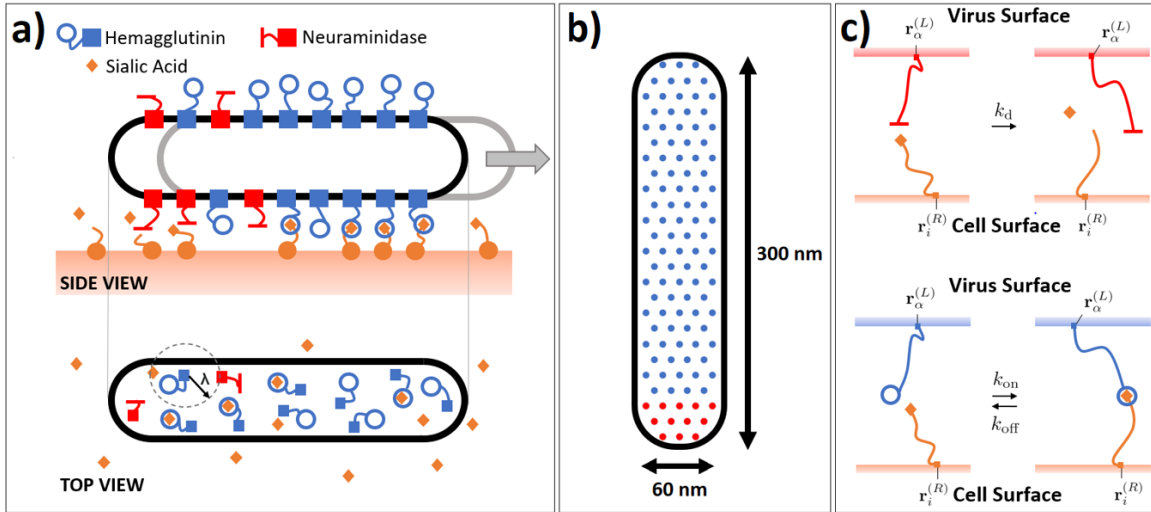
Mobility of IAV virions

- Polarised IAV virions (in which NA ligands are clustered)

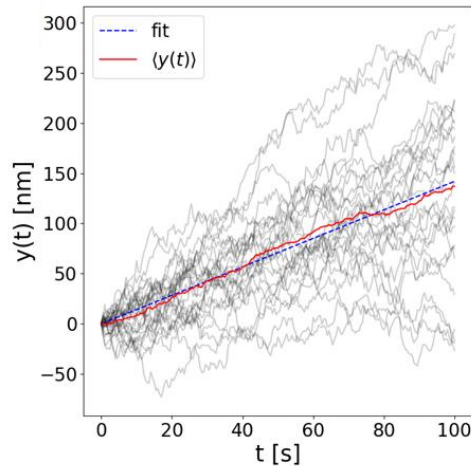
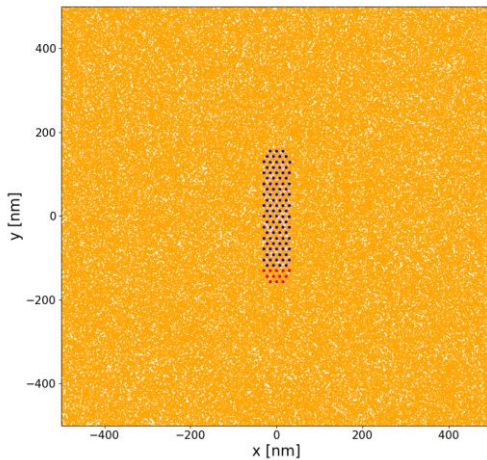


Mobility of IAV virions

- Polarised IAV virions (in which NA ligands are clustered)

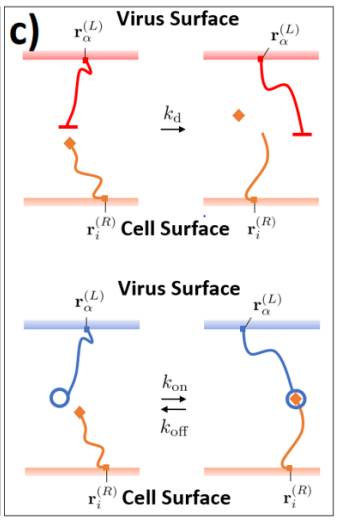
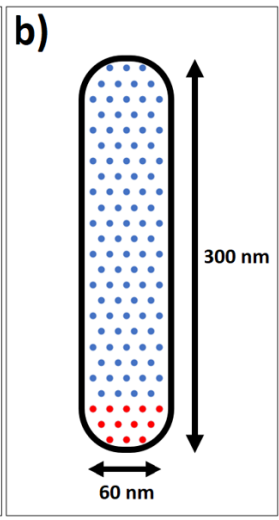
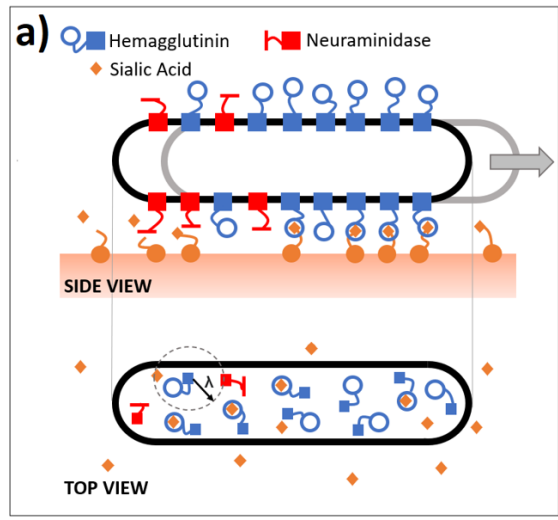


- At short timescales, the virion drifts in the direction opposite to the NA ligands

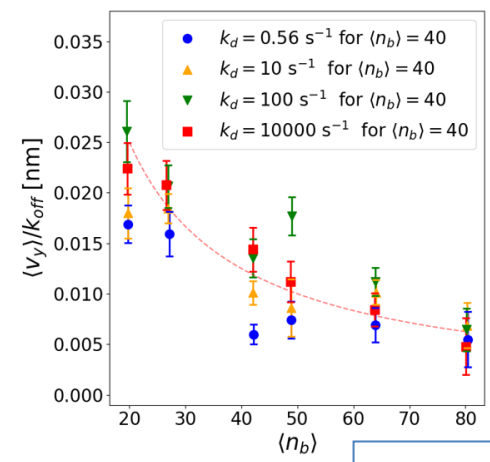
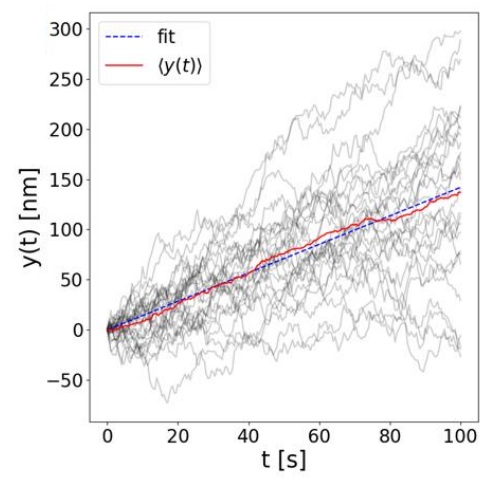
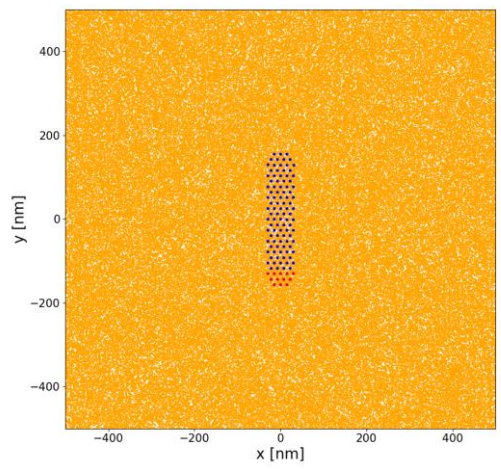


Mobility of IAV virions

- Polarised IAV virions (in which NA ligands are clustered)



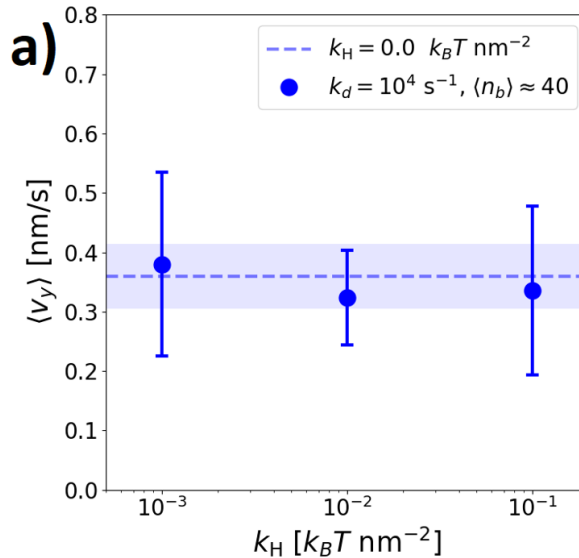
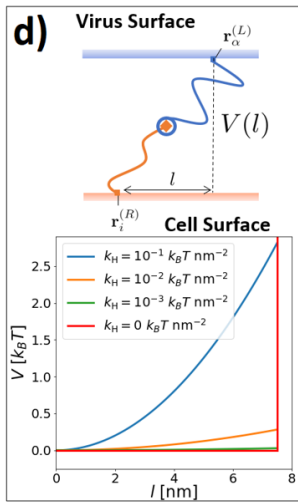
- At short timescales, the virion drifts in the direction opposite to the NA ligands
- The drifting velocity scales like $\langle v_y \rangle \sim 1/\langle n_b \rangle$ and is weakly affected by k_d



Mobility of IAV virions

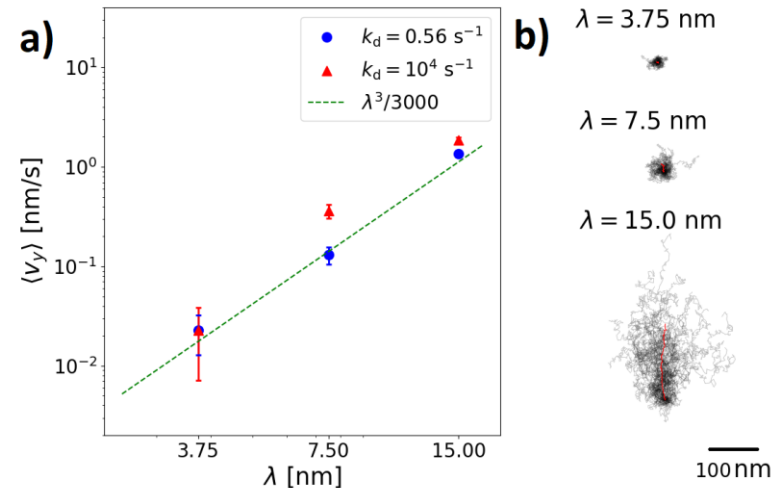
- IAV virions in which NA ligands are clustered

Stevens *et al*, submitted



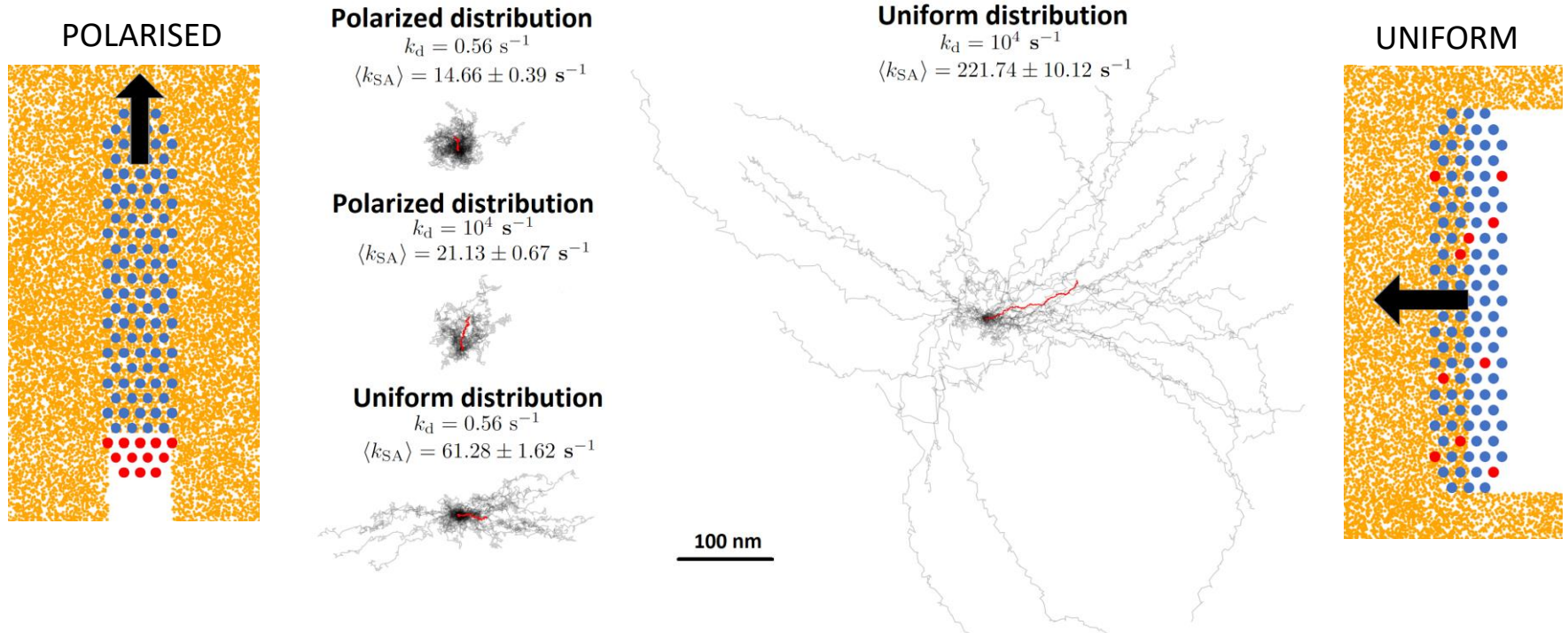
- Configurational forces do not affect v_y (consistent with reaction-limited dynamics)

- The maximal lateral distance at which a pair of ligand-receptor molecules can form a bridge (λ) greatly affects v_y



- Comparing different NA distributions

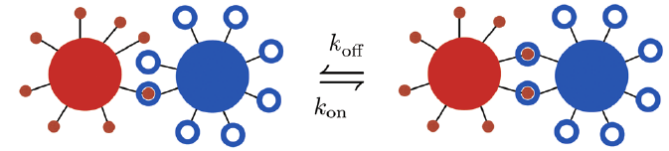
Stevens *et al*, submitted



- Virions with uniformly distributed NA ligands move orthogonally to the particle's axis

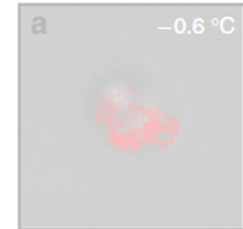
Sakai *et al*, J. Virol. **2018**; Bazrafshan *et al*, Angew. Chem. Int. Ed. **2020**

- The motility of virions with uniformly distributed ligands is more sensitive to variations in the catalytic rate (k_d)



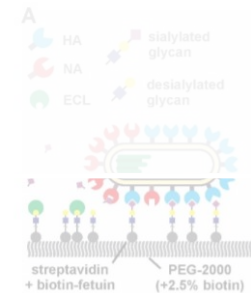
- Dynamics of particles moving through reversible ligand-receptor contacts

- Predicting the emerging diffusion constant D in reaction-limited conditions
- Comparison with simulations and experiments
- Increasing the motility of the particles using enzymes (Influenza A Virus)



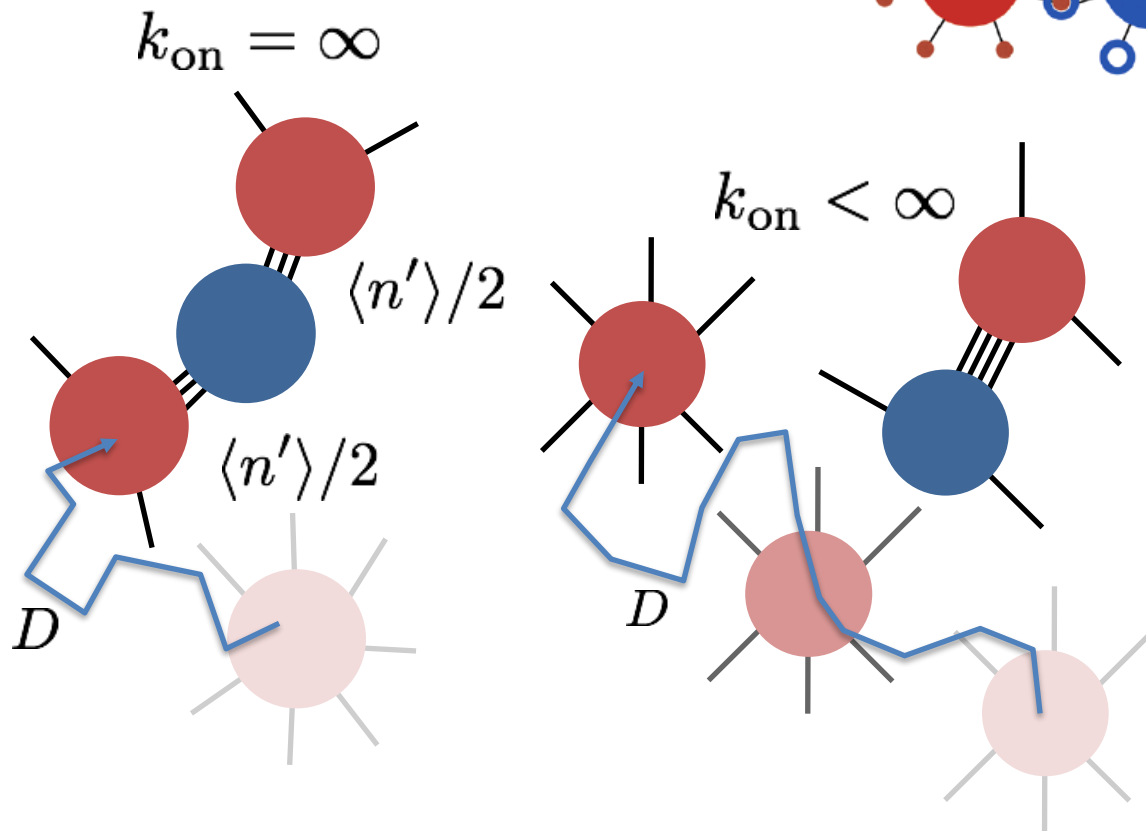
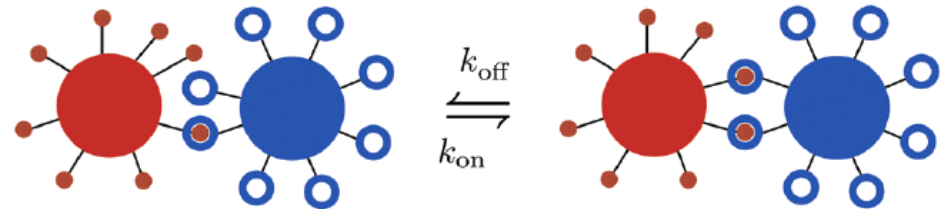
- Self-assembly dynamics

- Finite reaction rates alter the morphology of steady aggregates



Particles functionalized by mobile linkers

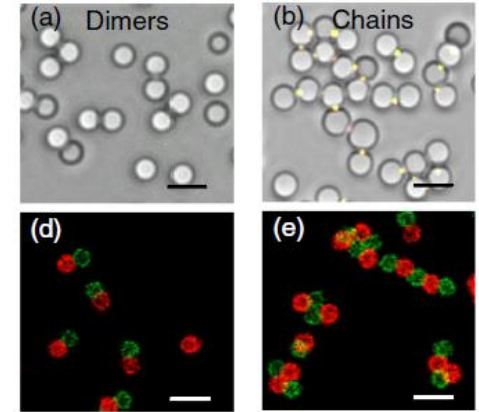
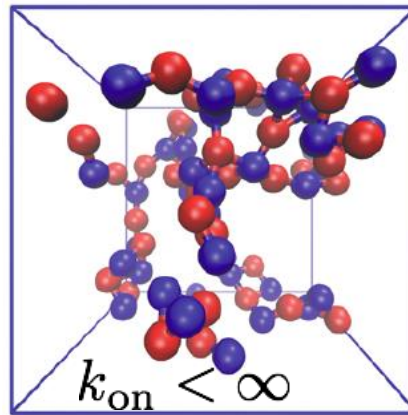
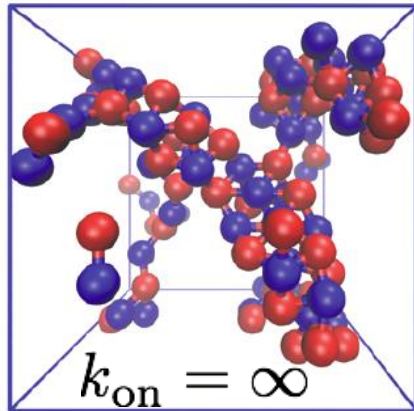
- Finite reaction rates drastically affect self-assembly



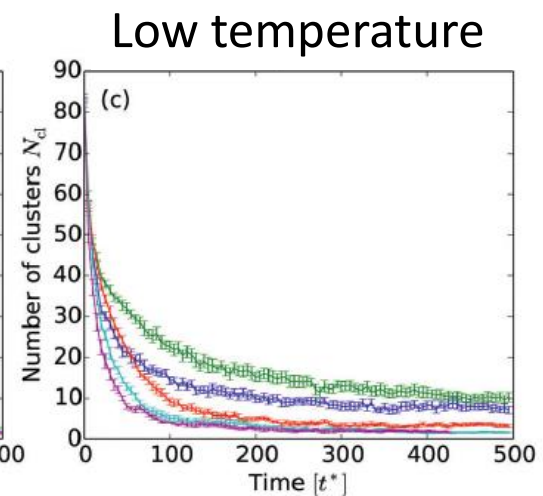
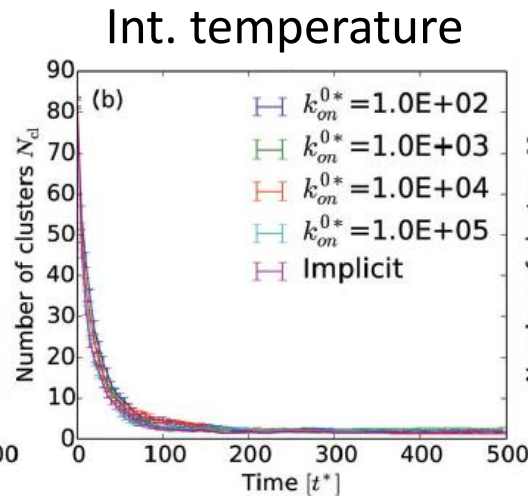
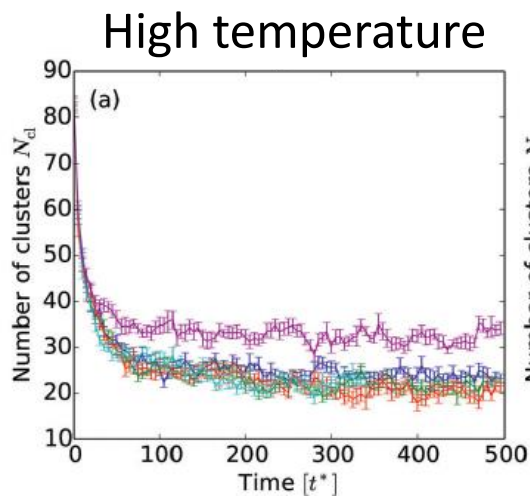
- Linkers segregate in the interaction patch
- Formation of new colloid-colloid contacts is limited by *on/off* reactions
- Kinetic control of the valency used to assemble *colloidomers*

Particles functionalized by mobile linkers

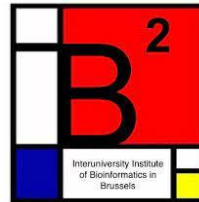
- Finite reaction rates drastically affect self-assembly



McMullen *et al*, Phys. Rev. Lett. **2019**;
Feng *et al*, Soft Matter **2013**



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 - Stephan Bachmann (BASF, Germany)
- Funding



- Computing

