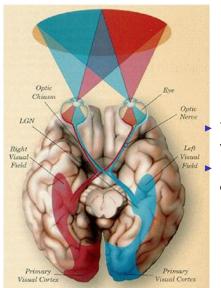
# & "normalizing" nonlinearities in visual cortex: A simple unified circuit model

Ken Miller Dan Rubin Jun Zhao Brendan Murphy Evan Schaffer

Experiments: Hirofumi Ozeki, Ian Finn, David Ferster

October 22, 2010

# Primary visual cortex (V1)

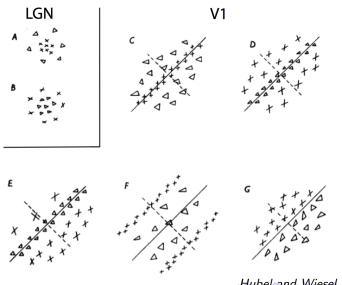


The first area of cortex to receive visual information (from LGN)

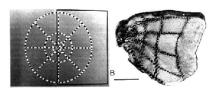
Neurons respond selectively to oriented visual stimuli

### LGN and V1 Receptive Fields

LGN RFs are circularly symmetric; V1 RFs are orientation-tuned



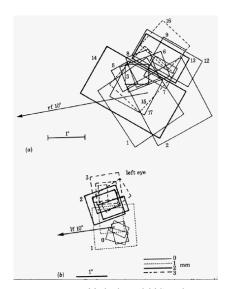
# V1 has a retinotopic map



Tootell et al., 1988; scalebar= 1cm

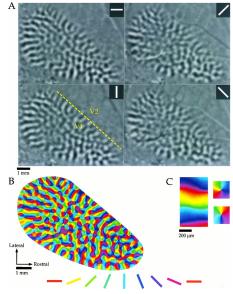
#### Right:

- ► TOP: RFs recorded in vertical penetration (⊥ to surface). Positions stay ~constant.
- ▶ BOTTOM: RFs recorded in horizontal penetration ( $\parallel$  to surface). 1mm movement  $\Rightarrow$  RFs  $\sim \frac{1}{2}$ -overlapping.



Hubel and Wiesel, 1977

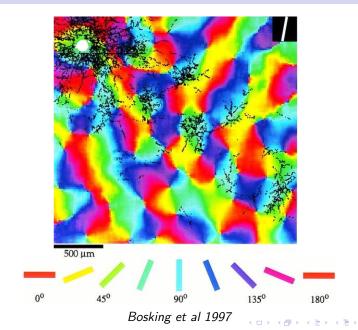
# V1 has a map of orientation preference



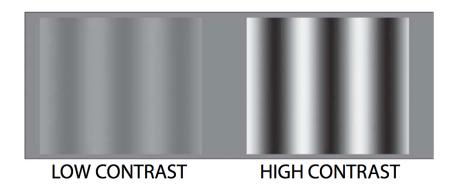
Bosking et al 1997

- Preferred orientation is
   constant from top to
   bottom of cortex at a given point
- Preferred orientation varies periodically with movement across the V1 surface
- ▶ Period ~1 mm: all orientations represented within a 1 mm<sup>2</sup> "functional unit"

### Long-range V1 connections are orientation-tuned



### Stimulus Contrast



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  - ► Auditory stimuli transduced punctate in frequency and time ⇒ perceive sounds of different objects
- ▶ Similarly on motor side: we experience high-level motor plans/intentions ("grasp my pen") invariant to, yet dependent on, detailed implementation.

- How are objects knit together?
  - ► Long-range (contextual) interactions within one cortical area
  - ▶ Hierarchical feedforward/feedback between areas: larger invariant structures emerge gradually (small steps per area; e.g. V2, but not V1, responds to illusory contours)

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  - ► Selectivity *e.g.* for orientation, position largely or entirely created by arrangement of feedforward inputs onto layer 4 cells
  - ► Context, attention appear to modulate **gain** of response

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- ► Largely ignore laminar structure; imagine we are modeling interactions within layers 2/3
- Only consider "excitatory" and "inhibitory" neurons, without further divisions into subtypes

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 Response suppression – by context or competing stimuli – has been assumed to arise from activation of inhibitory neurons that in turn suppress the other neurons;

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- Instead, all of this can arise from simple, generic network dynamics, in which the entire network – both E and I cells – undergo the suppression, or loss of amplification;

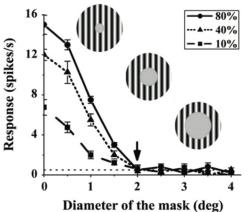
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- ▶ Instead, all of this can arise from simple, generic network dynamics, in which the entire network both E and I cells undergo the suppression, or loss of amplification;
- ► An expansive input-output cellular nonlinearity (which can be identical for E and I cells) automatically leads to the two regimes: a low-contrast "facilitative" regime and a high contrast "suppressive" regime

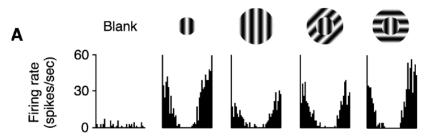
# Surround Suppression

Classical Receptive Field (CRF or "center"): region in which appropriate visual stimuli elicit spikes:

**Extra-Classical Receptive Field (ECRF or "surround")**: region surrounding CRF; visual stimuli do not elicit spikes:



### Surround Suppression



Ozeki, Finn, Schaffer, Miller and Ferster (2009) Stimulus: 2 degree center, 20 degree surround, drifting grating

- Surround stimuli suppress responses to CRF stimuli
- Suppression is tuned for surround orientation, relative to center
- ▶ Found in  $\sim 1/2$  of V1 cells in layers 2-4



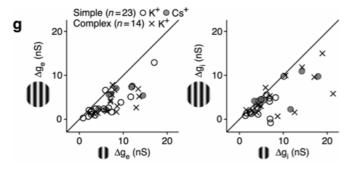
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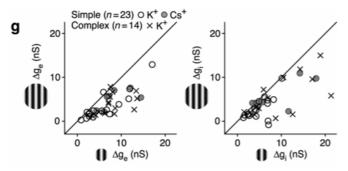
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- ► This evokes excitatory, orientation-tuned input into local region via long-range connections
- To cause suppression, this input must preferentially drive inhibitory cells (so these inhibitory cells would not be surround suppressed)
- ► Expectation: cells should receive increased inhibition when they undergo suppression

# During Suppression, Both the Inhibition and Excitation That Cells Receive *Decrease*



Ozeki, Finn, Schaffer, Miller and Ferster (2009)

# During Suppression, Both the Inhibition and Excitation That Cells Receive *Decrease*



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- Interpretation: During suppression, both excitatory and inhibitory cells are suppressed (lower their firing rates)
- Has been confirmed directly (Song and Li, 2008)



A: This will happen iff

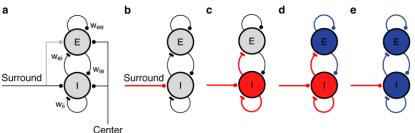
- ► Excitatory recurrence alone is strong enough to be unstable
- ▶ Network is stabilized by feedback inhibition (Tsodyks et al., 1997, *J. Neurosci.*)

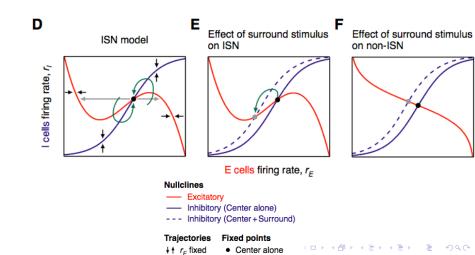
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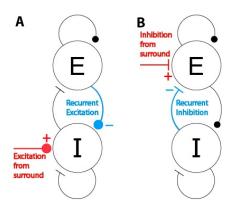
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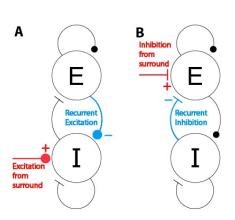




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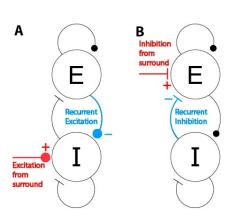


#### Common principle:

If E unstable

 Reduction in recurrent E is too large for reduction in E firing rate

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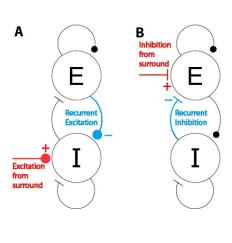


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#### If E stable:

► In new steady state, E must receive *more* inhibition and/or *less* external excitation (can rule out the latter scenarios)

#### Predictions of the ISN Model

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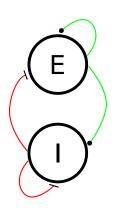
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Both verified (Ozeki et al. 2009)

#### Surround Suppression and the ISN Model: Conclusion

- ▶ Surround suppression is not inhibition it is de-amplification:
  - Responses are normally amplified by recurrent excitation in balanced network ("balanced amplification")
  - ► Surround stimulus adds bias toward inhibition ⇒ turns down gain for both E and I responses

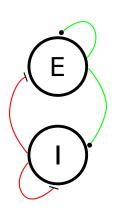
#### **Balanced Amplification**



Because of separation of excitatory and inhibitory neurons, synaptic connectivity matrices are *non-normal*:  $\mathbf{W}\mathbf{W}^T \neq \mathbf{W}^T\mathbf{W}$ .

$$\mathbf{r} = \left( \begin{array}{c} \mathbf{r}_E \\ \mathbf{r}_I \end{array} \right) \qquad \mathbf{W} = \left( \begin{array}{cc} \mathbf{W}_{EE} & -\mathbf{W}_{EI} \\ \mathbf{W}_{IE} & -\mathbf{W}_{II} \end{array} \right)$$
 
$$\mathbf{W}_{XY} \geq \mathbf{0}$$

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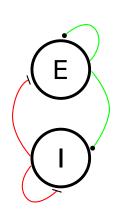


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 $\mathbf{W}\mathbf{W}^{T} = \begin{pmatrix} + & + \\ + & + \end{pmatrix} \qquad \mathbf{W}^{T}\mathbf{W} = \begin{pmatrix} + & - \\ - & + \end{pmatrix}$ 

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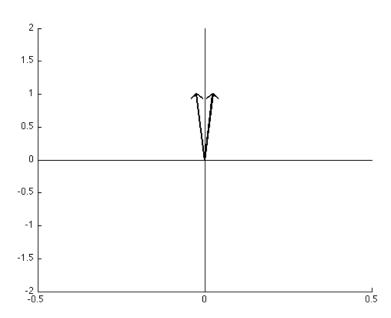


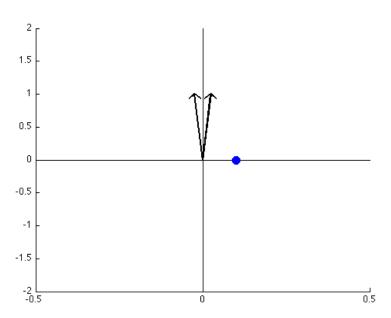
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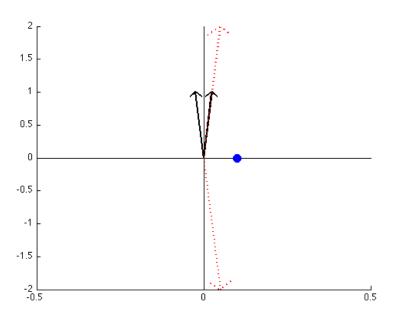
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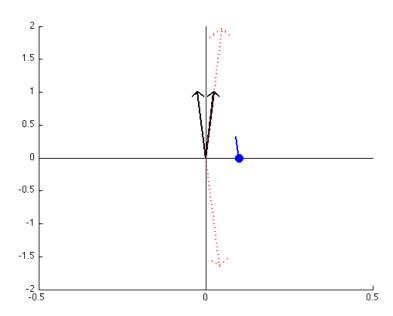
Non-normal  $\iff$  Eigenvectors are not orthogonal

⇒ can have large amplification – large transient responses to small perturbations – not predicted by eigenvalues: well known in fluid mechanics (see book by Trefethen and Embree, 2005)

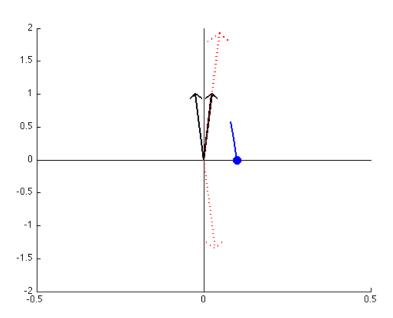


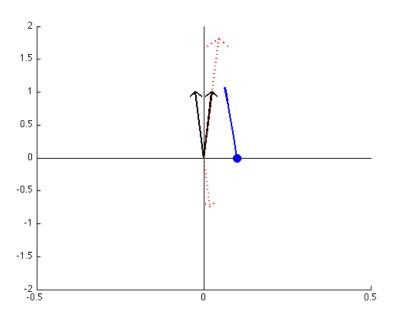


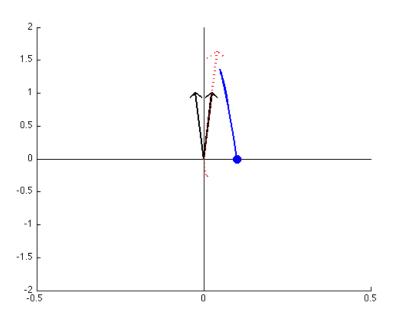


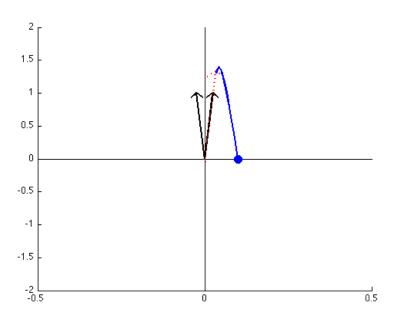




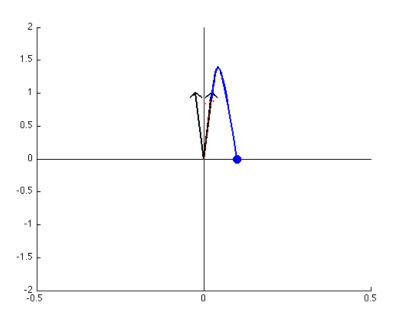


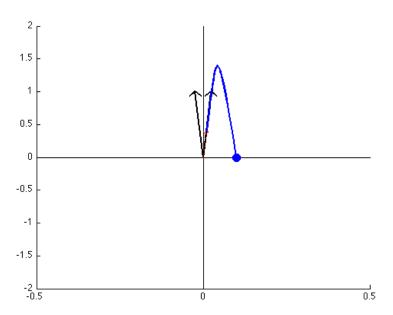












#### Balanced amplification: Effective Feedforward Connections

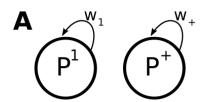
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  - ► Network activity is growing and then shrinking, but in eigenvector basis it appears to be monotonically shrinking
- ▶ Best simplification with a unitary (non-distorting) transformation: Schur decomposition:
  - Eigenvalues on diagonal
  - Upper diagonal nonzero = "Feedforward weights"; lower diagonal zero.

#### Balanced Amplification vs. Eigenvector Picture

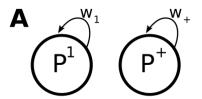
Eigenvector picture:

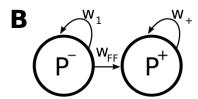


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Eigenvector picture:

Schur picture:





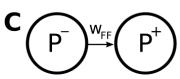
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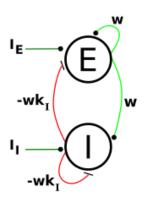
Eigenvector picture:

Schur picture:

 $\mathbf{B} \xrightarrow{\mathbf{P}^{-}} \mathbf{W}_{\mathsf{FF}} \xrightarrow{\mathbf{P}^{+}} \mathbf{P}^{\mathsf{W}_{\mathsf{F}}}$ 

Schur picture with small eigenvalues ("balanced"):

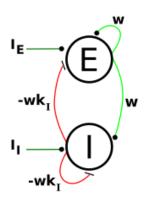




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Linear dynamics in terms of  $r_E$  and  $r_I$ :

$$\tau \frac{dr_E}{dt} = -r_E + wr_E - k_I wr_I$$
  
$$\tau \frac{dr_I}{dt} = -r_I + wr_E - k_I wr_I$$



$$w_{\mathrm{FF}} \equiv w(k_I + 1)$$
  
 $w_+ \equiv w(k_I - 1)$ 

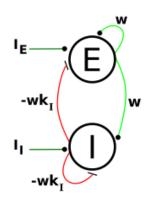
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$$au rac{dr_{+}}{dt} = -r_{+} - w_{+}r_{+} + w_{\mathrm{FF}}r_{-} \\ au rac{dr_{-}}{dt} = -r_{-}$$



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 $w_{+} \equiv w(k_{I}-1)$ 
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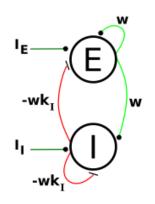
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 $W_{\text{FF}} \bullet (E+I)$ 

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Small E/I imbalances drive large balanced responses (e.g., surround suppression)