

*KITP Nonequilibrium14, Sept. 22 – Dec. 12, 2014*

# **Bridging the Mesoscale Gap**

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**Workshop: Dislocations and Plasticity**  
**ITP – UCSB, March 27-29, 1997**



**Explore commonalities of different problem --  
connecting a few dots ( → JSL talks)**

*avalanches, intermittency, non-linear, non-equilibrium response*

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**primary example:**

*shear viscosity of supercooled liquids*

**additional examples:**

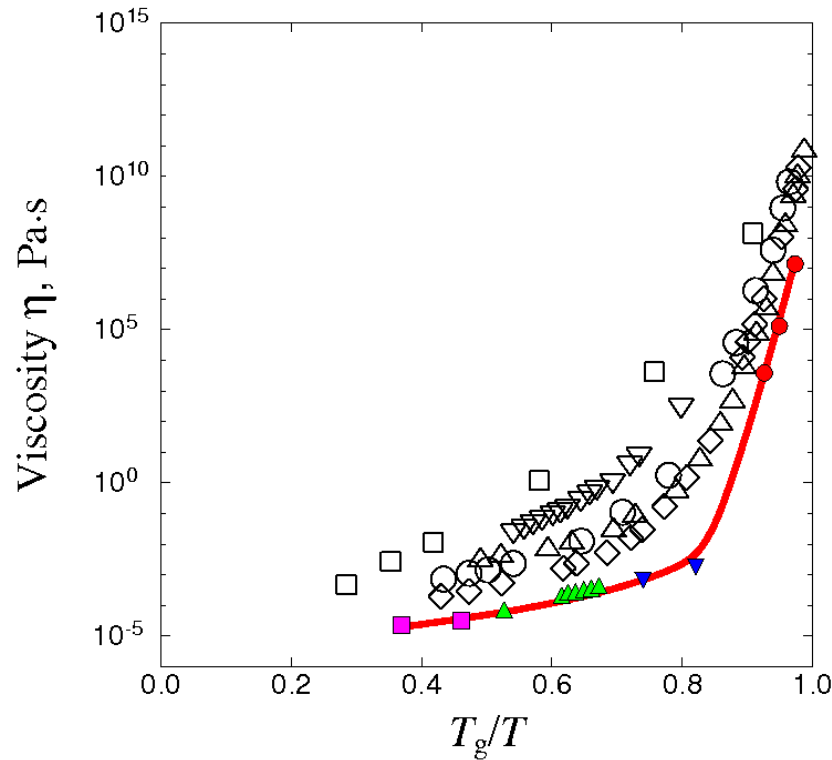
*yielding, creep, corrosion, cement*

**MSS Frontier (bridging the mesoscale gap)**

*predicting macro behavior using micro input*

## Fragile behavior of glass formers

(sharp increase in shear viscosity arounds  $T_x$  )



molecular-level understanding of macro behavior:

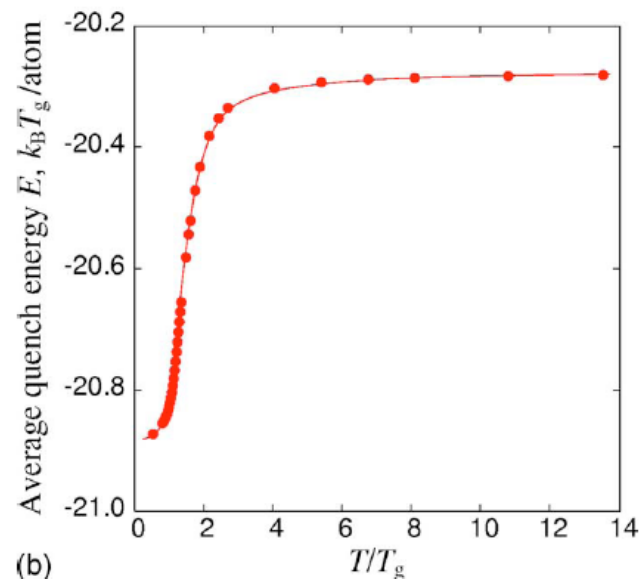
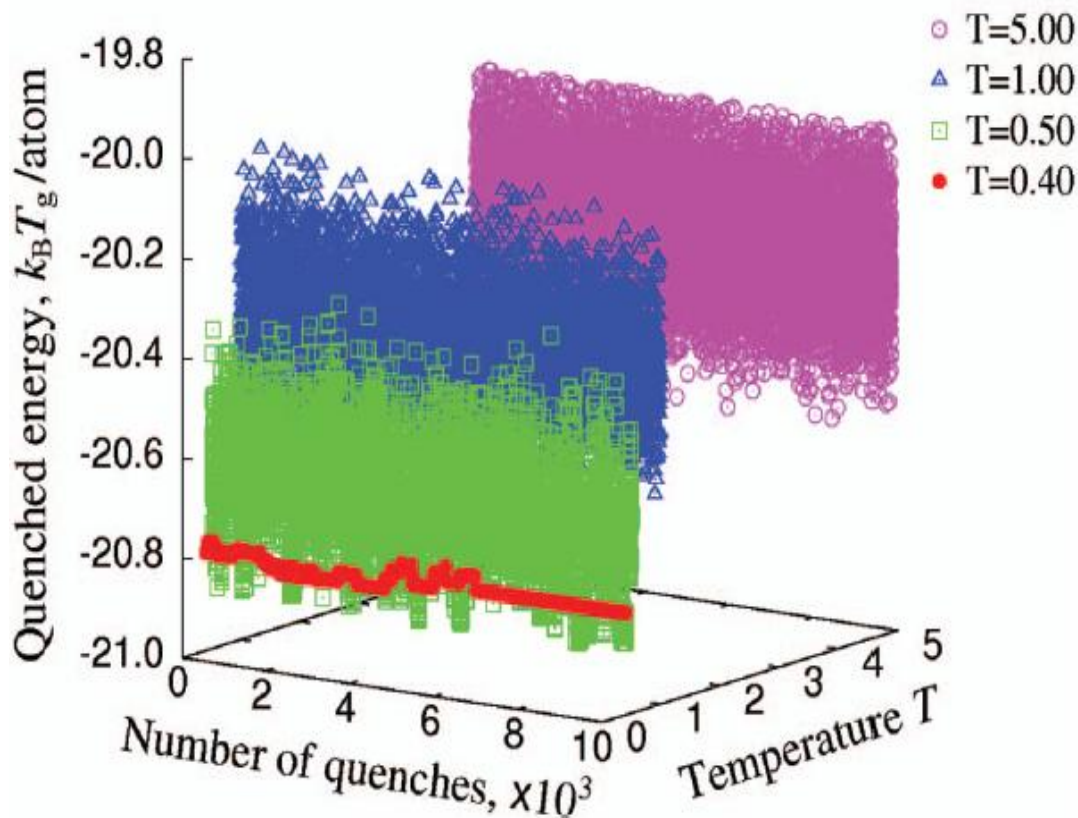
Energetics and atomic configurations of supercooled states **(1)**

Transition-state (reaction) pathway sampling **(2)**

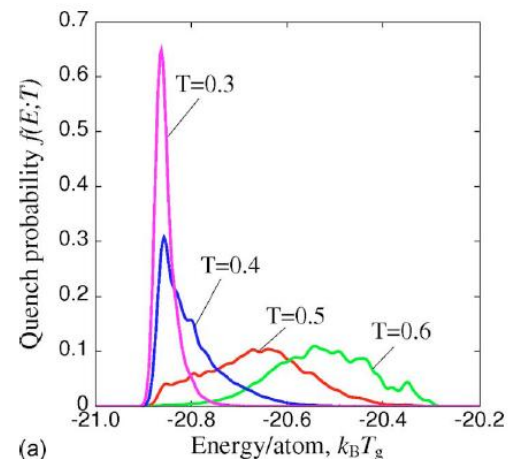
*Linear response theory of transport* **(3)**

# 1

## Inherent Structure of Supercooled Liquids



(b)

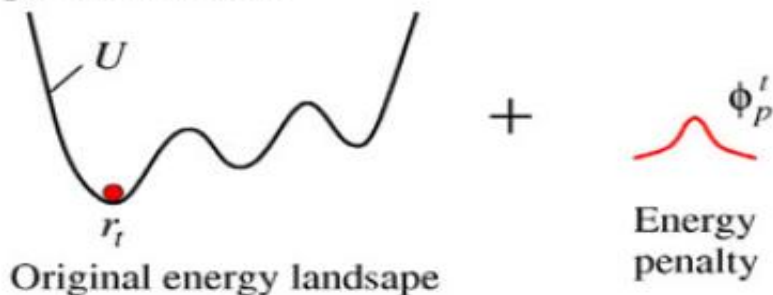


(a)

## 2

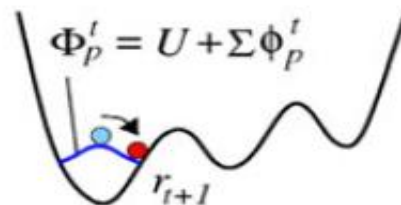
## Transition State Pathway Sampling – metadynamics (ABC)

Step 1: Activation



Step 2: Relaxation

Original energy landscape with cumulative penalties

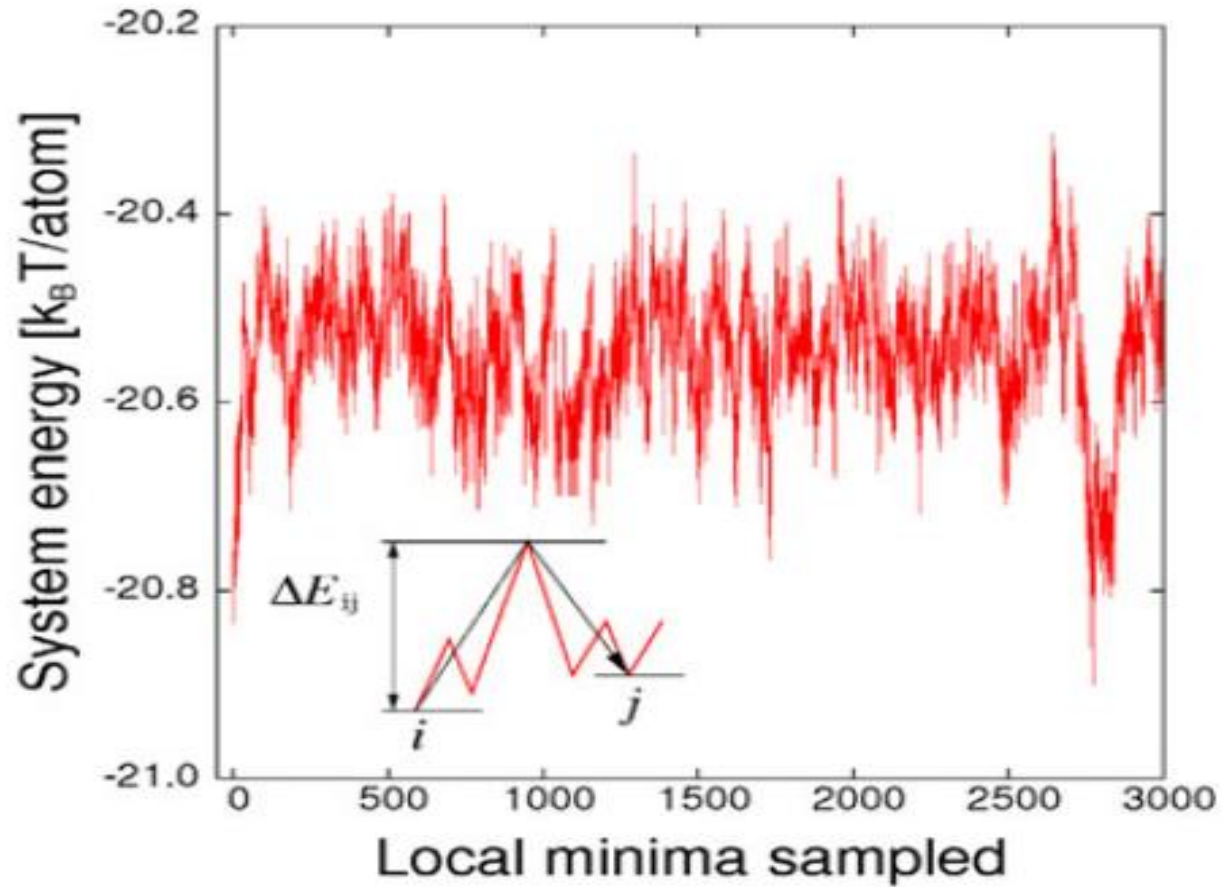


Repeat steps 1 and 2 to explore energy landscape



2

## Transition State Pathway sampled at $T = 1.35 T_g$

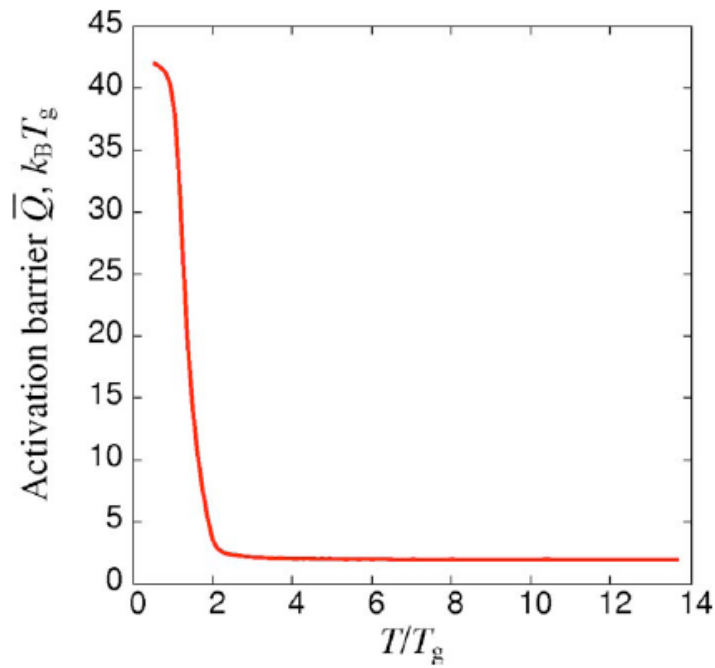


- (a) Extract effective activation barrier in the spirit of TST
- (b) Direct input into a network model (Green-Kubo calc.

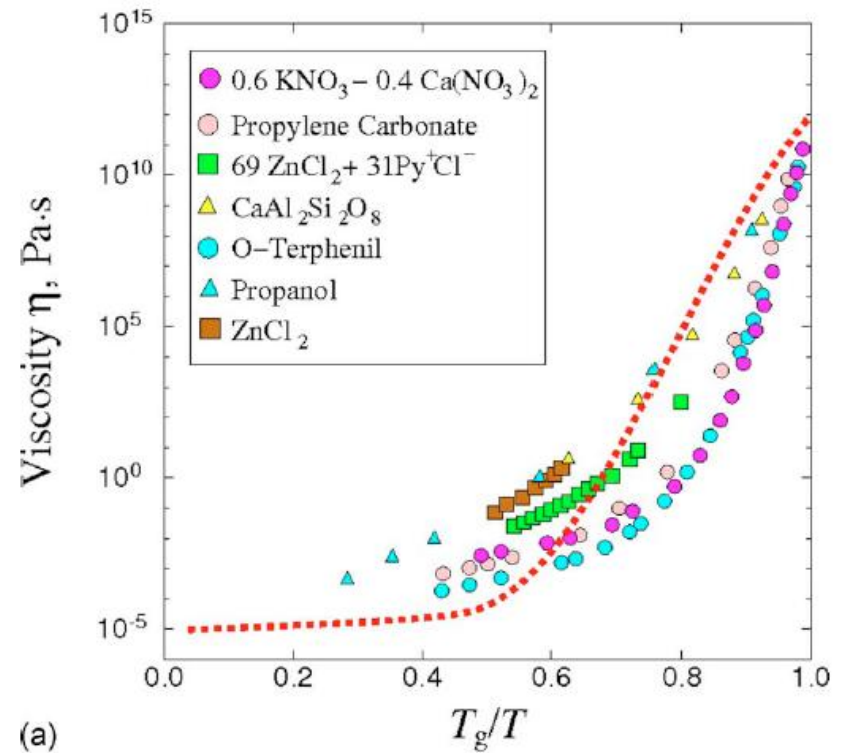
Kushima JCP 2009

# 3

## activation barrier analysis (heuristic model)



$$\eta(T) = \eta_0 \exp[Q(T)/k_B T]$$



(a)



# 3

## Linear Response (Green-Kubo) theory with network model

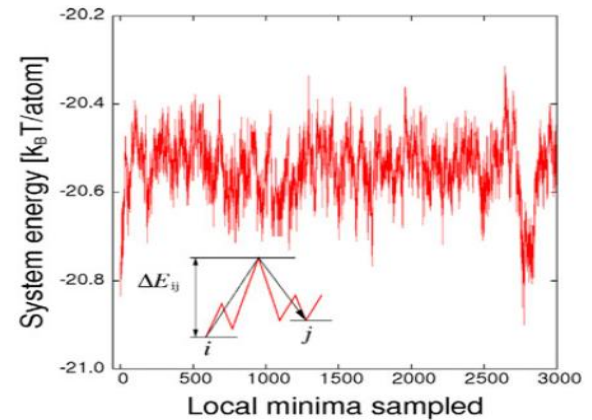
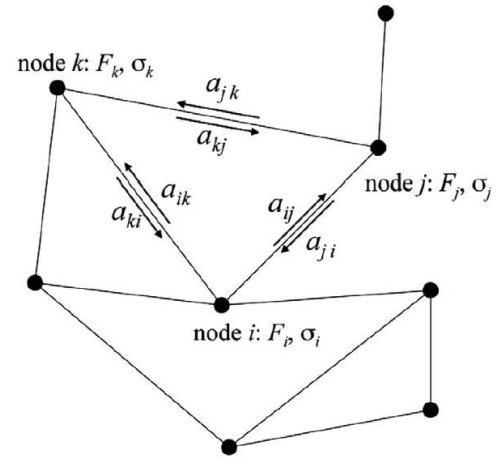
$$\eta(T) = \frac{V}{3k_B T} \int_0^\infty \left\langle \sum_{x < y} \tau^{xy}(t) \tau^{xy}(0) \right\rangle dt$$

$$\langle \sigma(t) \sigma(t+\tau) \rangle = \sum_i P_i \sigma_i g_i(\tau)$$

$$g_i(\tau) = \sum_j \int_0^\tau d\tau' a_{ij} s_i(\tau') g_j(\tau - \tau') + s_i(\tau) \sigma_i$$

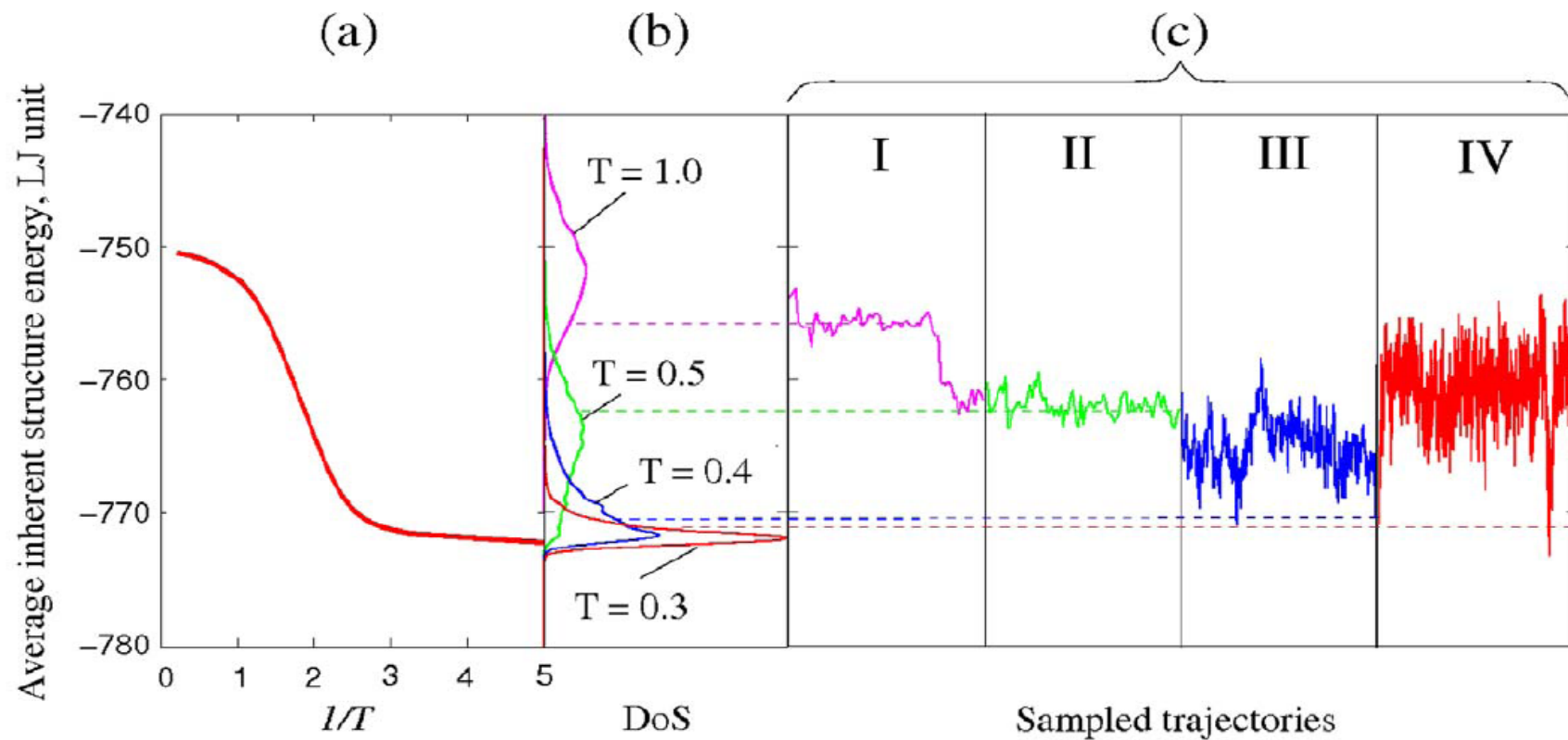
$$a_{ij}(T) = v_0 \exp(-q_{ij}/k_B T)$$

$$s_i(\tau) = \exp(-\tau a_i), \quad a_i \equiv \sum_j a_{ij}, \quad a_{ii} = 0.$$



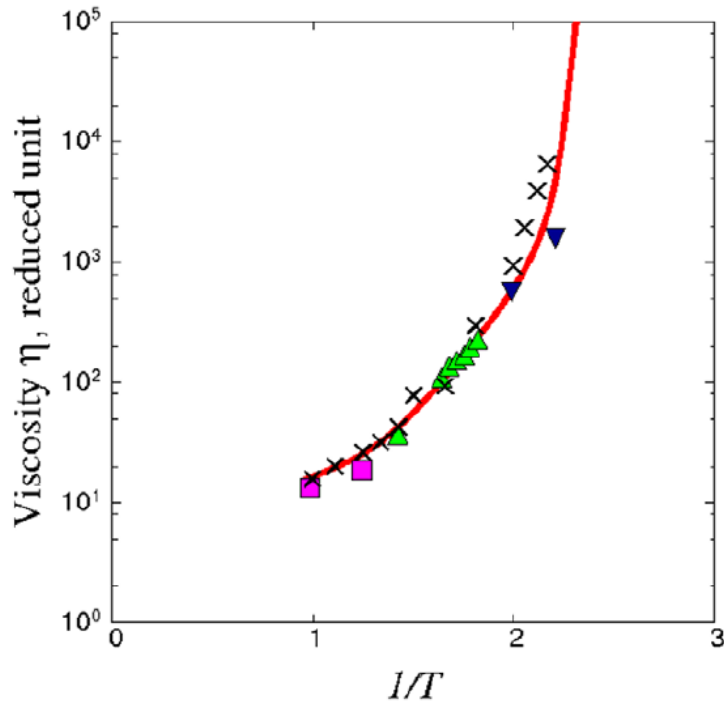
Li, PLoS ONE 2011

### 3 Analysis divided into 4 temperature ranges

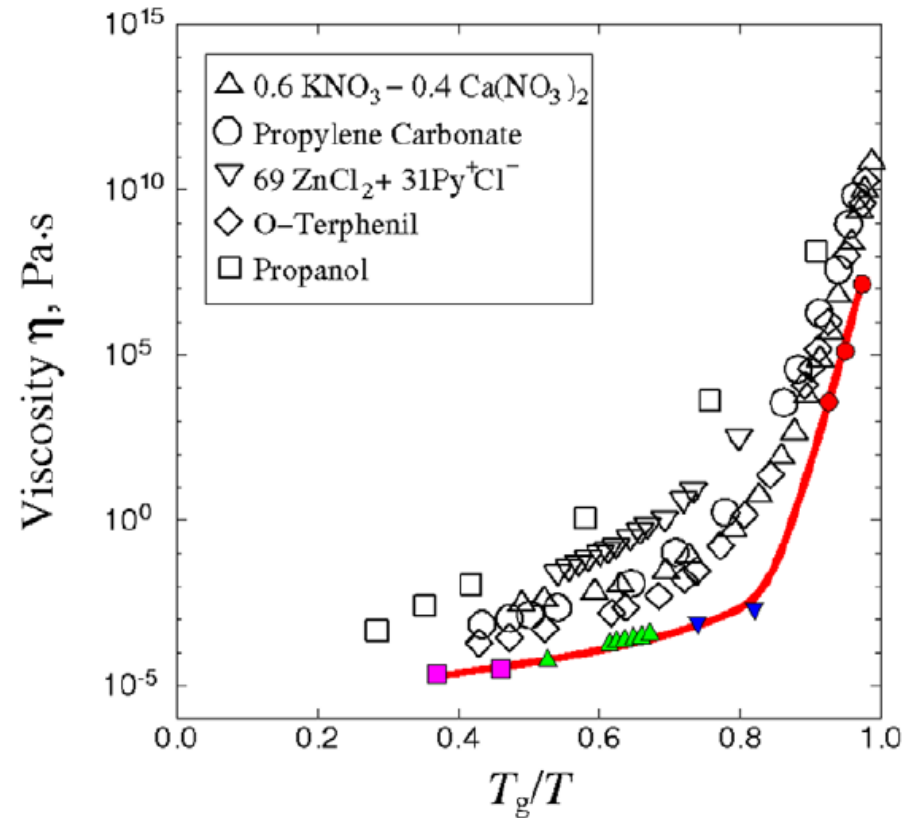


# 3

## Validation against MD and experiments



MD validation at low-moderate viscosity



Experimental comparison

*Issues to ponder (connecting a few dots)*

**“Fragility” as a consequence of energy landscape?**

**Relevance of TSP (mobility/transport) is essential**

**Challenge to simulation methodology**

**Challenge to theoretical approaches**

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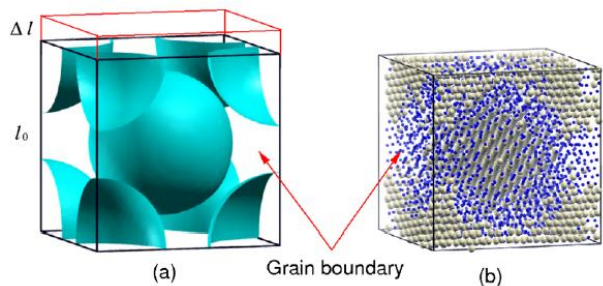
**JSL talk on Oct. 16**

**Applicable to deformation under stress?**

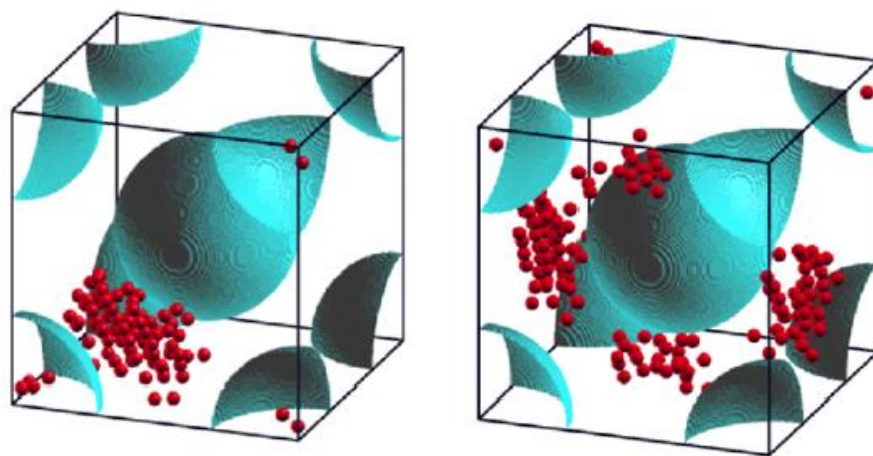
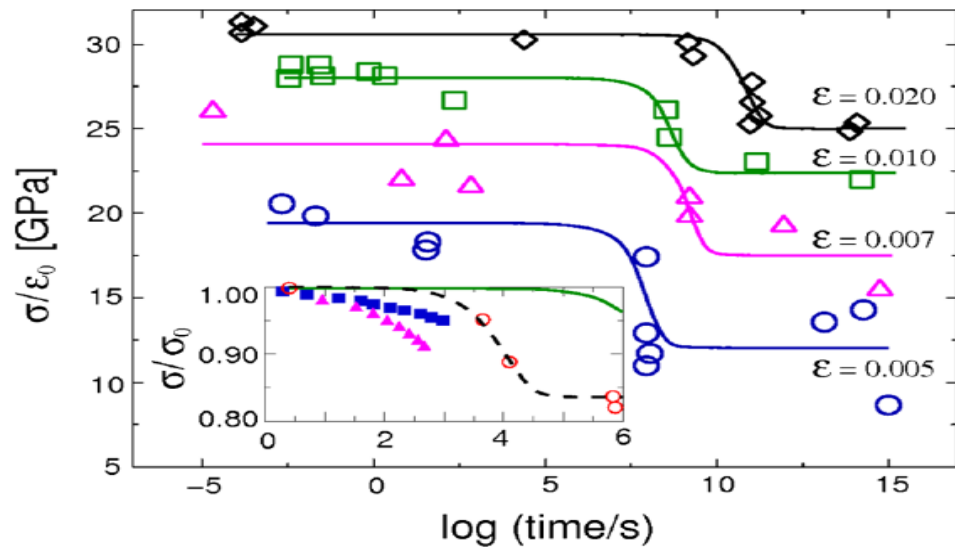
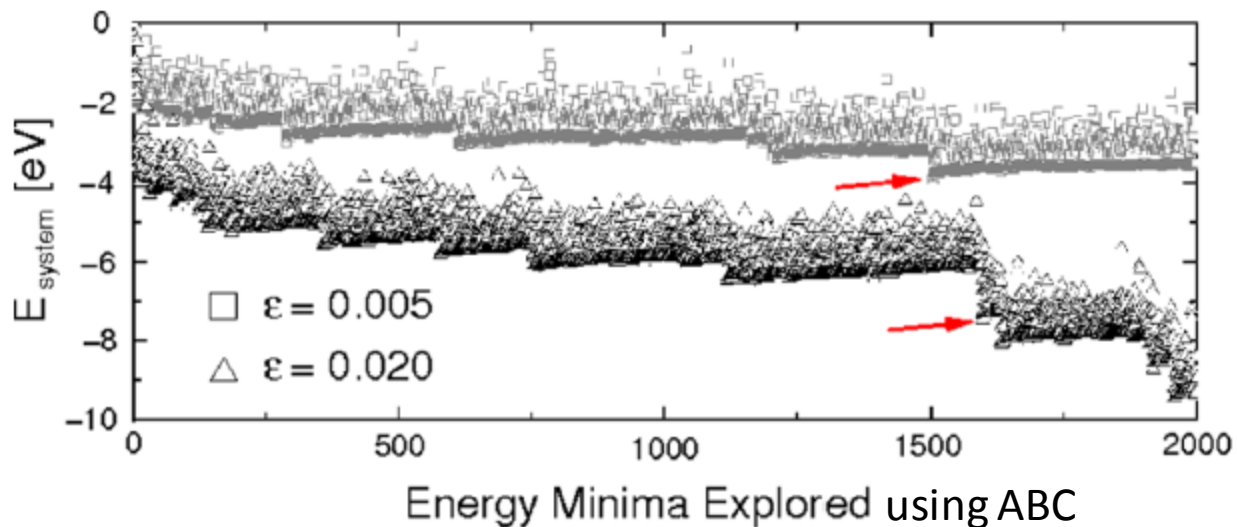
**Using TSP sampling (ABC) to study time evolution of a solid  
under deformation at finite T**

# Stress relaxation in uniaxially strained nanocrystal –

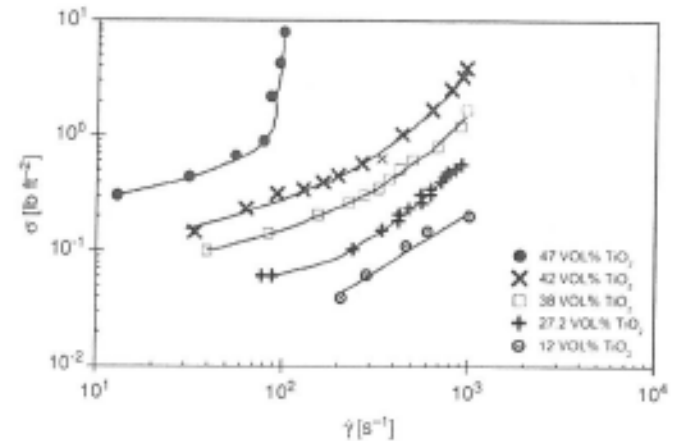
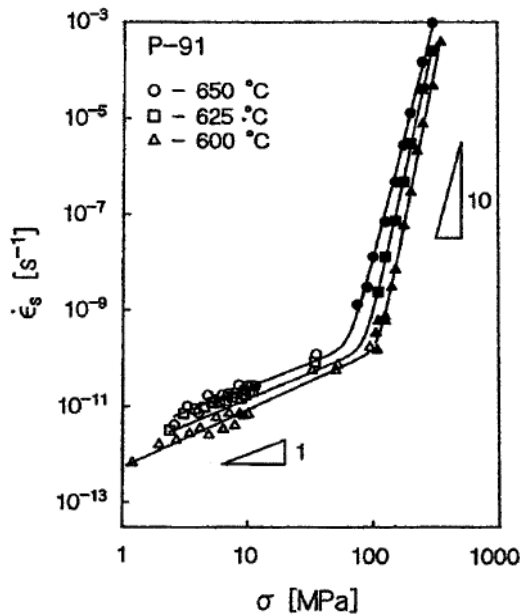
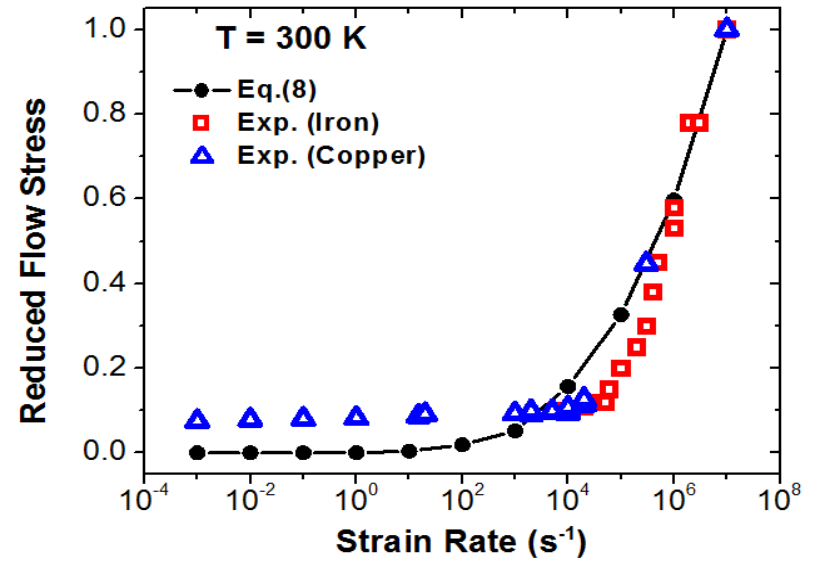
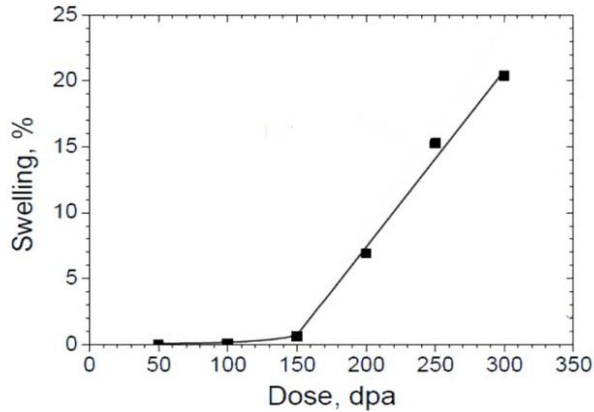
Lau, PRL 2010



$$\Delta t = \left[ \nu_0 \exp\left(-\frac{\Delta U}{k_B T}\right) \right]^{-1}$$

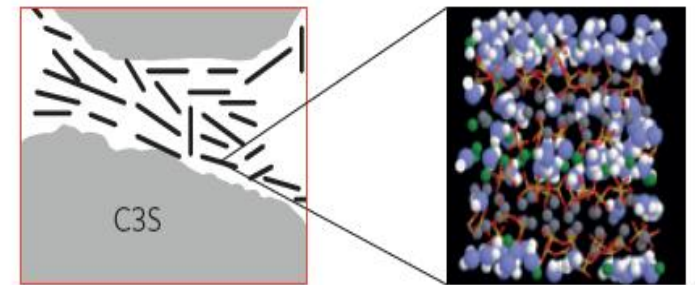
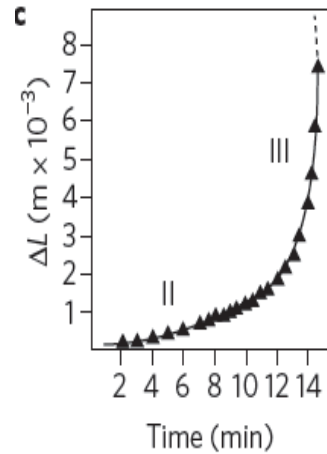
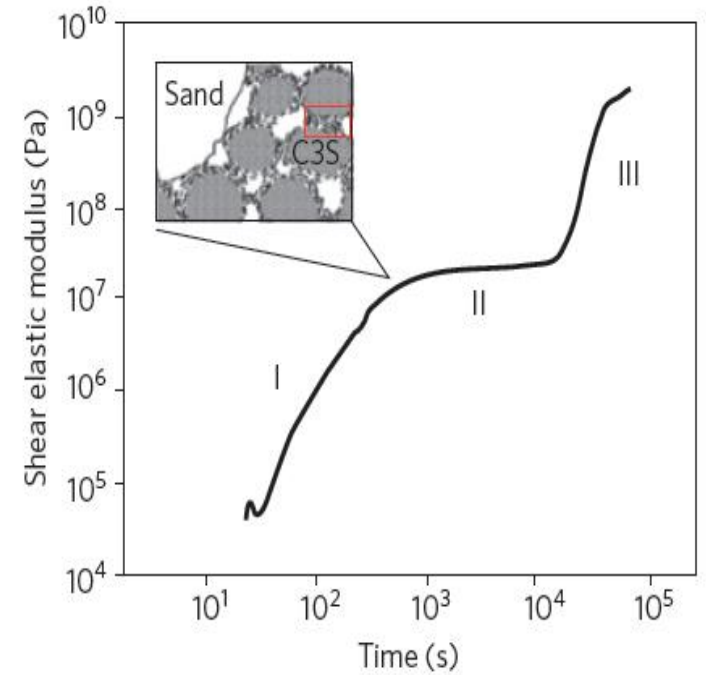
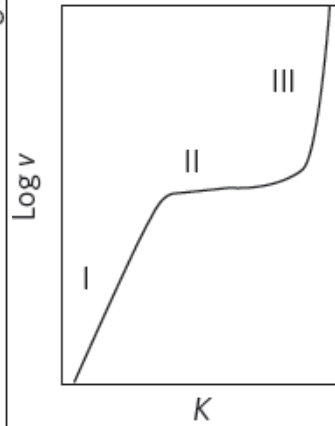
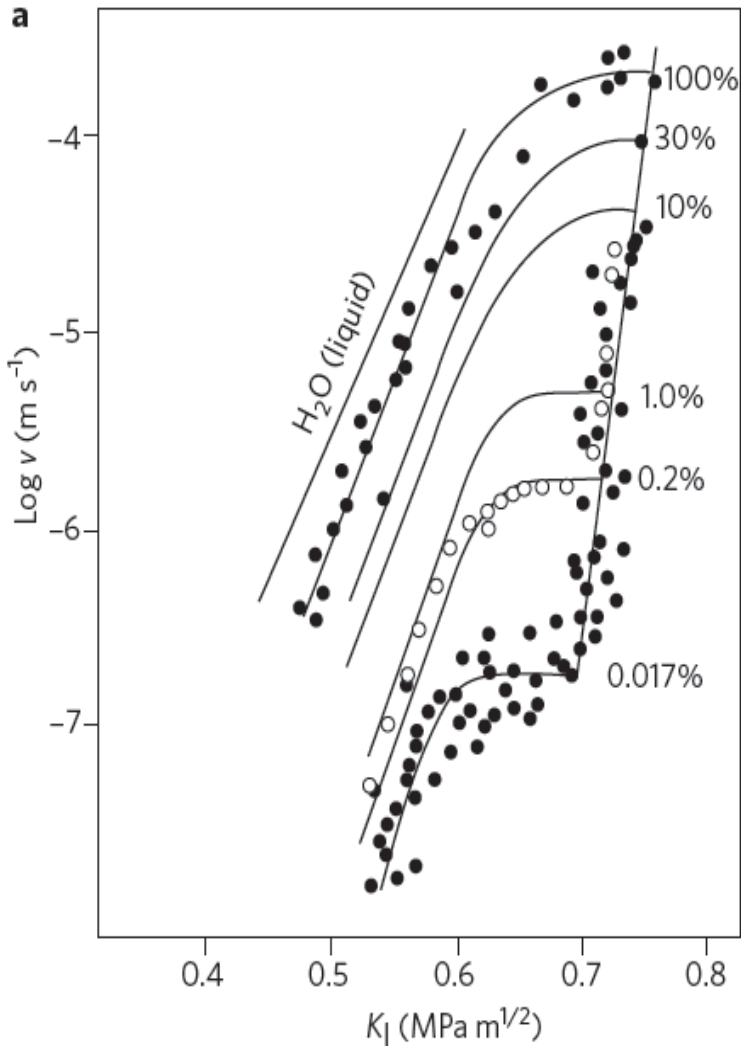


# additional phenomena showing upturn/crossover behavior (macroscale)



Shear thickening in a dense suspension

# 3-stage responses – stress corrosion cracking and cement setting



NMAT 2013



## **Collaborators**

**Akihiro Kushima (MIT)**

**Xi Lin (BU)**

**Ju Li (MIT)**

**Xiaofeng Qian (MIT/TAMU)**

**Jacob Eapen (NCSU)**

**John Mauro (Corning)**

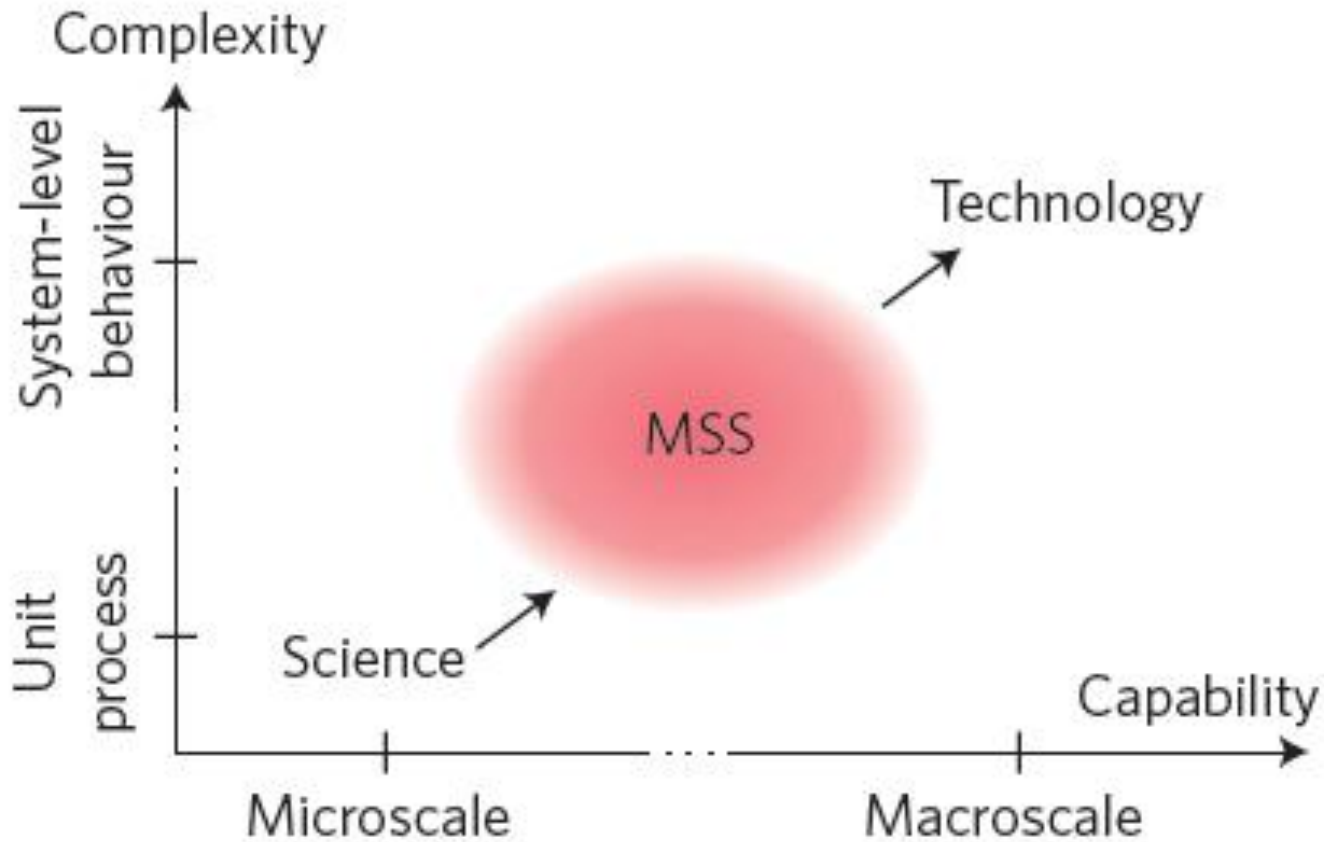
**Tim Lau (MIT)**

**Yue Fan (ORNL)**

**Bilge Yildiz (MIT)**

**Mike Short (MIT)**

# The Mesoscale Science (MSS) Frontier



NMAT 2013

*Science push w/ technology pull*