

n - \bar{n} Transformations

Susan Gardner

Department of Physics and Astronomy
University of Kentucky
Lexington, KY 40506

gardner@pa.uky.edu

Based, in part, on...

SG and Xinshuai Yan (UK), Phys. Rev. D93, 096008 (2016) [arXiv:1602.00693];
and on work in collaboration with Xinshuai Yan (UK).



Why search for $n \rightarrow \bar{n}$?

The Standard Model (SM) leaves many questions unanswered. Most notably it cannot explain **the cosmic baryon asymmetry, dark matter, or dark energy.**

\mathcal{B} violation plays a role in at least one of these puzzles.

Although \mathcal{B} violation appears in the SM (sphalerons),

[Kuzmin, Rubakov, & Shaposhnikov, 1985]

we know nothing of its pattern at accessible energies.

Do processes occur with $|\Delta\mathcal{B}| = 1$ or $|\Delta\mathcal{B}| = 2$ or both?

The SM conserves $\mathcal{B} - \mathcal{L}$, but does Nature?

Severe limits on nucleon decay ($|\Delta\mathcal{B}| = 1$) exist, but the origin of $|\Delta\mathcal{B}| = 2$ processes can be completely distinct.

[Marshak and Mohapatra, 1980; Babu and Mohapatra, 2001 & 2012; Arnold, Fornal, and Wise, 2013]

If neutron-antineutron oscillations, e.g., are observed (a “background free” signal!), then $\mathcal{B} - \mathcal{L}$ is **broken**, and **we have discovered physics beyond the SM.**

$\mathcal{B} - \mathcal{L}$ violation and the neutrino mass

Elementary, charged fermions get their mass from the Higgs mechanism, but the origin of the neutrino mass is **not yet known**.

A massive neutrino could also be a **Dirac** particle, with its mass generated by the Higgs mechanism (N.B. enter the right-handed neutrino! Note Yukawa coupling $\sim 10^{-12}$!)

A massive neutrino could be a **Majorana** particle with its mass generated by the $d = 5$ operator $\lambda(v_{\text{weak}}^2/\Lambda)\nu_L^T C\nu_L$ (N.B. $\mathcal{B} - \mathcal{L}$ is broken!). [Weinberg, 1979]

A massive neutrino could also get its mass from terms of both types. Even if the Dirac mass were to dominate, the mass eigenstates would be Majorana.

[Gribov and Pontecorvo, 1969; Bilenky and Pontecorvo, 1983]

Although a Majorana mass term breaks $\mathcal{B} - \mathcal{L}$, other sources of $\mathcal{B} - \mathcal{L}$ violation could operate.

Nevertheless, the observation of neutrinoless $\beta\beta$ decay ($|\Delta\mathcal{L}| = 2$) would reveal that the neutrino is Majorana, that the neutrino is its own antiparticle.

[Schechter and Valle, PRD, 1982]

A bonus: if $\mathcal{B} - \mathcal{L}$ is broken, the “see-saw” mechanism rationalizes the smallness of the ν mass. [Minkowski, 1977; Gell-Mann, Ramond, & Slansky, 1979; Yanagida, 1980; Mohapatra

& Senjanovic, 1980]

Why the scale of $\mathcal{B} - \mathcal{L}$ violation also matters

If we establish that $\mathcal{B} - \mathcal{L}$ is broken (by neutrinos), then...

- Electric charge quantization can be compatible w/ nonzero ν mass

[Babu & Mohapatra, 1989, 1990; note review: Foot et al., 1993]

- Leptogenesis may exist (and explain the BAU)

[Fukugita & Yanagida, 1986; note review: Buchmüller et al., 2005]

Even so, we may still not know the **mechanism** of $\mathcal{B} - \mathcal{L}$ violation.

If it is generated by the Weinberg operator, then SM electroweak symmetry yields $m_\nu = \lambda v_{\text{weak}}^2 / \Lambda$. If $\lambda \sim 1$ and $\Lambda \gg v_{\text{weak}}$, then naturally $m_\nu \ll m_f$!

N.B. if $m_\nu \sim 0.2$ eV, then $\Lambda \sim 1.6 \times 10^9$ GeV!

Alternatively it could also be generated by higher dimension $|\Delta L| = 2$ operators, so that m_ν is small just because $d \gg 4$ and Λ need not be so large.

[EFTs: Babu & Leung, 2001; de Gouvea & Jenkins, 2008 and many models]

Can we establish the scale of $\mathcal{B} - \mathcal{L}$ violation in another way?

N.B. searches for same sign dilepton final states at the LHC also constrain the higher dimension (“short range”) operators. [Helo, Kovalenko, Hirsch, and Päs, 2013]

$\mathcal{B} - \mathcal{L}$ Violation and $n-\bar{n}$ Oscillations

It has long been thought that $n-\bar{n}$ oscillations could shed light on the mechanism of

- Baryogenesis [Kuzmin, 1967]
- Neutrino mass [Mohapatra and Marshak, 1980]

The observation of $n-\bar{n}$ transformations would reveal that $\mathcal{B} - \mathcal{L}$ is indeed broken.

Extracting the scale of $\mathcal{B} - \mathcal{L}$ breaking from such a result can be realized through a matrix element computation in lattice QCD. There has been much progress towards this goal.

[Buchhoff, Schroeder, and Wasem, 2012; Buchhoff and Wagman, 2016; Syritsen, Buchhoff, Schroeder, and Wasem, 2016]

In contrast to proton decay, $n-\bar{n}$ probes new physics at “intermediate” energy scales. The two processes can be generated by $\mathbf{d}=6$ and $\mathbf{d}=9$ operators, respectively.

Crudely, $\Lambda_{p\text{ decay}} \geq 10^{15} \text{ GeV}$ and $\Lambda_{n\bar{n}} \geq 10^{5.5} \text{ GeV}$.

$\mathcal{B}-\mathcal{L}$ violation at such intermediate energy scales can have rich implications; e.g., in left-right symmetric models, successful leptogenesis requires that $n-\bar{n}$ oscillations be unobservably small.

[e.g., Dev, Lee, Mohapatra, 2014]

The Challenges of Observing $n-\bar{n}$ Oscillations

A 2×2 effective Hamiltonian framework for $n-\bar{n}$ mixing

[Marshak and Mohapatra, PLB, 1980; Cowsik and Nussinov, PLB, 1981; Phillips II et al. [NNbar Collaboration], arXiv:1410.1100]

$$\mathcal{H} = \begin{pmatrix} M_n - \mu_n \mathbf{B} & \delta \\ \delta & M_n + \mu_n \mathbf{B} \end{pmatrix},$$

yields

$$P_{n \rightarrow \bar{n}}(t) \simeq \frac{\delta^2}{2(\mu_n \mathbf{B})^2} [1 - \cos(2\mu_n \mathbf{B}t)] \exp(-\lambda t)$$

so that unless $t \ll 1/(2\mu_n \mathbf{B})$, a nonzero \mathbf{B} “quenches” $n-\bar{n}$ oscillations.

There have been many studies of $n-\bar{n}$ in “elixir” magnetic fields, all in the 2×2 framework.

[Arndt, Prasad, Riazuddin, PRD 1983; Pusch, Nuov. Cim. 1983; Krstić, Komarov, Janen, Zenko, PRD 1988; Dubbers, NIM 1989; Kinkel, Z. Phys. C 1992]

Experimentally magnetic fields have been mitigated, yielding $P_{n \rightarrow \bar{n}}(t) \simeq \delta^2 t^2$ and $\tau_{n\bar{n}} \equiv 1/\delta$ with $\tau_{n\bar{n}} \geq 0.85 \times 10^8$ s at 90% C.L.

[Baldo-Ceolin et al., ZPC, 1994 (ILL)]

Matter effects act to the same end and must also be mitigated.

$n-\bar{n}$ Oscillations and Nuclear Stability

$n-\bar{n}$ oscillations can be studied in bound or free systems.

New limits on dinucleon decay in nuclei have also recently been established.

[Gustafson et al., Super-K Collaboration, arXiv:1504.0104.]

$^{16}\text{O}(pp) \rightarrow ^{14}\text{C} \pi^+ \pi^+$ has $\tau > 7.22 \times 10^{31}$ years at 90% CL.

$^{16}\text{O}(pn) \rightarrow ^{14}\text{N} \pi^+ \pi^0$ has $\tau > 1.70 \times 10^{32}$ years at 90% CL.

$^{16}\text{O}(nn) \rightarrow ^{14}\text{O} \pi^0 \pi^0$ has $\tau > 4.04 \times 10^{32}$ years at 90% CL.

Note $\tau_{NN} = T_{\text{nuc}} \tau_{n\bar{n}}^2$ with $T_{\text{nuc}} \sim 1.1 \times 10^{25} \text{s}^{-1}$

Large suppression factors appear in all such nuclear studies, making free searches more effective.

In the case of bound $n-\bar{n}$ the suppression is set by

$$\frac{\delta^2}{(V_n - V_{\bar{n}})^2}$$

the difference in nuclear optical potentials. [Dover, Gal, and Richard; Friedman and Gal, 2008]

Now $^{16}\text{O}(n-\bar{n})$ has $\tau > 1.9 \times 10^{32}$ years at 90% CL,

yielding $\tau_{n\bar{n}} > 2.7 \times 10^8 \text{s}$. [Abe et al., Super-K Collaboration, arXiv:1109.4227.]

Cf. free limit: $\tau_{n\bar{n}} \geq 0.85 \times 10^8 \text{s}$ at 90% C.L. [Baldo-Ceolin et al., ZPC, 1994 (ILL)]

with future improvements expected.

The nuclear suppression dwarfs that from magnetic fields.

$n-\bar{n}$ Oscillations: Why Spin Could Matter

The SM preserves $\mathcal{B} - \mathcal{L}$, so that the observation of either $n-\bar{n}$ oscillations ($|\Delta\mathcal{B}| = 2$) or of neutrinoless $\beta\beta$ decay ($|\Delta\mathcal{L}| = 2$) would reveal the existence of dynamics beyond the SM.

However, QCD is a gauge theory in $SU(3)$ color $\leftrightarrow \mathbf{3} \neq \mathbf{3}^*$.
Thus n is distinct from \bar{n} , and it has a significant magnetic moment.

Certainly the neutron's Dirac mass dominates its measured mass; note
 $\delta m = (\tau_{n\bar{n}})^{-1} \leq 6 \times 10^{-29} \text{ MeV}$.

[Baldo-Ceolin et al., ZPC, 1994 (ILL)]

A neutron thus best resembles a pseudo-Dirac neutrino, though its electromagnetic interactions are also well established....

In particular, the CPT theorem guarantees that the magnetic moment of a neutron and antineutron differ only in sign.

A 4×4 matrix describes \mathcal{H} in this case.

[SG and Jafari, 2015]

\mathcal{H}_{ij} with $i, j = 1, \dots, 4$ maps to $n(\mathbf{p}, +)$, $\bar{n}(\mathbf{p}, +)$, $n(\mathbf{p}, -)$, and $\bar{n}(\mathbf{p}, -)$.

Hermiticity and CPT invariance limit its form.

But what is the precise form of the CPT transformation in this case?

Recall from neutrino physics: the discrete symmetry transformations of a theory should not depend on whether it contains Dirac or Majorana fields.

[Kayser and Goldhaber, 1983; Kayser, 1984 — also Carruthers, 1971; Feinberg and Weinberg, 1959]

Consequently the CPT, CP, and C phases of Majorana fields or states are restricted.

[Kayser and Goldhaber, 1983; Kayser, 1984]

Generalizing this to theories of fermions with B-L violation, the phases associated with the discrete symmetry transformations must themselves be restricted.

[SG and Yan, 2016]

Majorana Phase Constraints

For any fermion field

$$\mathbf{C}\psi(x)\mathbf{C}^{-1} = \eta_c \mathbf{C}\gamma^0\psi^*(x) \equiv \eta_c i\gamma^2\psi^*(x) \equiv \eta_c \psi^c(x),$$

$$\mathbf{P}\psi(t, \mathbf{x})\mathbf{P}^{-1} = \eta_p \gamma^0\psi(t, -\mathbf{x}),$$

$$\mathbf{T}\psi(t, \mathbf{x})\mathbf{T}^{-1} = \eta_t \gamma^1\gamma^3\psi(-t, \mathbf{x}),$$

Thus $\mathbf{P}^2\psi(x)\mathbf{P}^{-2} = \eta_p^2\psi(x)$ but $\mathbf{C}^2\psi(x)\mathbf{C}^{-2} = \psi(x)$; $\mathbf{T}^2\psi(x)\mathbf{T}^{-2} = -\psi(x)$

The plane wave expansion of a general Majorana field ψ_m is

$$\psi_m(x) = \int \frac{d^3\mathbf{p}}{(2\pi)^{3/2}\sqrt{2E}} \sum_s \{ f(\mathbf{p}, s)u(\mathbf{p}, s)e^{-ip\cdot x} + \lambda f^\dagger(\mathbf{p}, s)v(\mathbf{p}, s)e^{ip\cdot x} \}$$

Applying \mathbf{C} and noting the Majorana relation,

$$i\gamma^2\psi_m^*(x) = \lambda^*\psi_m(x)$$

yields

$$\mathbf{C}\psi_m(x)\mathbf{C}^{-1} = \eta_c \lambda^*\psi_m(x)$$

$$\mathbf{C}f(\mathbf{p}, s)\mathbf{C}^{-1} = \eta_c \lambda^* f(\mathbf{p}, s) \text{ and } \mathbf{C}f^\dagger(\mathbf{p}, s)\mathbf{C}^{-1} = \eta_c \lambda^* f^\dagger(\mathbf{p}, s)$$

Since \mathbf{C} is a unitary operator, taking the adjoint shows $\eta_c^*\lambda$ is real.

Majorana Phase Constraints

Under CP, we find $\eta_p^* \eta_c^* \lambda$ is imaginary, or that η_p^* is imaginary.

Under T we find that $\eta_t \lambda$ is real, whereas

$$\mathbf{CPT} \psi_m(x) (\mathbf{CPT})^{-1} = -\eta_c \eta_p \eta_t \gamma^5 \psi_m^*(-x)$$

yielding

$$\mathbf{CPT} f(\mathbf{p}, s) (\mathbf{CPT})^{-1} = s \lambda^* \eta_c \eta_p \eta_t f(\mathbf{p}, -s)$$

$$\mathbf{CPT} f^\dagger(\mathbf{p}, s) (\mathbf{CPT})^{-1} = -s \lambda \eta_c \eta_p \eta_t f^\dagger(\mathbf{p}, -s)$$

Since **CPT** is antiunitary, $\mathbf{CPT} = K U_{\text{cpt}}$, where U_{cpt} denotes a unitarity operator.

We conclude $\eta_c \eta_p \eta_t$ is pure imaginary.

Since η_p is imaginary, $\eta_c \eta_t$ must also be real — but $\eta_c \eta_p$ itself is unconstrained.

Since the phases are unimodular, they impact the discrete symmetry transformation properties of \mathcal{B} - \mathcal{L} violating operators only.

Building a Majorana field from Dirac fields yields

$\psi_{m\pm}(x) = \frac{1}{\sqrt{2}}(\psi(x) \pm \mathbf{C}\psi(x)\mathbf{C}^{-1})$ and $\lambda = \pm\eta_c$; all our other conclusions emerge as well.

Theories of Dirac Fermions with $\mathcal{B} - \mathcal{L}$ Violation

The prototypical $\mathcal{B} - \mathcal{L}$ violating operator is of form

$$\psi^T C \psi + \text{h.c.}$$

Since C satisfies $(\sigma^{\mu\nu})^T C = -C \sigma^{\mu\nu}$, this operator is Lorentz invariant. Under **CPT**...

$$\mathcal{O}_1 = \psi^T C \psi + \text{h.c.} \quad \xrightarrow{\text{CPT}} -(\eta_c \eta_p \eta_t)^2$$

$$\mathcal{O}_2 = \psi^T C \gamma_5 \psi + \text{h.c.} \quad \xrightarrow{\text{CPT}} -(\eta_c \eta_p \eta_t)^2$$

$$\mathcal{O}_3 = \psi^T C \gamma^\mu \psi \partial^\nu F_{\mu\nu} + \text{h.c.} \quad \xrightarrow{\text{CPT}} +(\eta_c \eta_p \eta_t)^2$$

$$\mathcal{O}_4 = \psi^T C \gamma^\mu \gamma_5 \psi \partial^\nu F_{\mu\nu} + \text{h.c.} \quad \xrightarrow{\text{CPT}} -(\eta_c \eta_p \eta_t)^2$$

$$\mathcal{O}_5 = \psi^T C \sigma_{\mu\nu} \psi F^{\mu\nu} + \text{h.c.} \quad \xrightarrow{\text{CPT}} +(\eta_c \eta_p \eta_t)^2$$

$$\mathcal{O}_6 = \psi^T C \sigma_{\mu\nu} \gamma_5 \psi F^{\mu\nu} + \text{h.c.} \quad \xrightarrow{\text{CPT}} +(\eta_c \eta_p \eta_t)^2$$

The phase constraint $(\eta_c \eta_p \eta_t)^2 = -1$ only flips the sign of the eigenvalue!

The operators do not transform under CPT with definite sign!

Theories of Dirac Fermions with $\mathcal{B} - \mathcal{L}$ Violation

The operators

$$\mathcal{O}_3 = \psi^T \mathbf{C} \gamma^\mu \psi \partial^\nu F_{\mu\nu} + \text{h.c.} \quad \xrightarrow{\text{CPT}} +(\eta_c \eta_p \eta_t)^2$$

$$\mathcal{O}_5 = \psi^T \mathbf{C} \sigma_{\mu\nu} \psi F^{\mu\nu} + \text{h.c.} \quad \xrightarrow{\text{CPT}} +(\eta_c \eta_p \eta_t)^2$$

$$\mathcal{O}_6 = \psi^T \mathbf{C} \sigma_{\mu\nu} \gamma_5 \psi F^{\mu\nu} + \text{h.c.} \quad \xrightarrow{\text{CPT}} +(\eta_c \eta_p \eta_t)^2$$

become CPT odd once the phase constraint $(\eta_c \eta_p \eta_t)^2 = -1$ is applied.

They also vanish once the anticommuting nature of the fermion fields is taken into account.

That these operators do not contribute has long been recognized:

The vector, tensor, and axial tensor electromagnetic form factors of Majorana neutrinos vanish.

[Schechter and Valle, 1981; Nieves, 1982; Kayser, 1982; Shrock, 1982; Li and Wilczek, 1982; Davidson, Gorbahn, Santamaria, 2006]

Recall flavor-spin neutrino oscillations. The flavor-diagonal ν transition magnetic moment vanishes due to the antisymmetry of fermion exchange.

[Okun, Voloshin, and Vysotsky, 1986 & 1986; Lim and Marciano, 1988]

CP Transformation Properties

The surviving operators transform under CP as

$$\begin{aligned}\mathcal{O}_1 &= \psi^T C \psi + \text{h.c.} && \xrightarrow{\text{CP}} -(\eta_c \eta_p)^2 \\ \mathcal{O}_2 &= \psi^T C \gamma_5 \psi + \text{h.c.} && \xrightarrow{\text{CP}} -(\eta_c \eta_p)^2 \\ \mathcal{O}_4 &= \psi^T C \gamma^\mu \gamma_5 \psi \partial^\nu F_{\mu\nu} + \text{h.c.} && \xrightarrow{\text{CP}} -(\eta_c \eta_p)^2\end{aligned}$$

where we have left the phase dependence explicit.

Employing $\eta_p^2 = -1$, the CP transformation properties remain nevertheless indeterminate — because they are given by η_c^2 .

Prompted by the remark that $n^T C n + \text{h.c.}$ breaks CP,

[Berezhiani and Vainshtein, 2015]

explicit examples of the indeterminate CP of $n^T C n + \text{h.c.}$ employing

$\psi \rightarrow \psi' = e^{i\theta} \psi$, have also been noted.

[Fujikawa and Tureanu, 2015]

The noted phase rotation has the effect of changing $\eta_c \rightarrow e^{2i\theta} \eta_c$, $\eta_t \rightarrow e^{-2i\theta} \eta_t$, with η_p unchanged, in the C, T, and P transformations.

Implications of the CP Phases

Physically, too, the appearance of $n - \bar{n}$ oscillations cannot signal CP violation — only one operator mediates an low energy, *en vacuo* $n - \bar{n}$ transition, and it appears in the transition probability as $|\delta|^2$.

Thus this operator gives no failure of detailed balance: $P_{n \rightarrow \bar{n}} = P_{\bar{n} \rightarrow n}$

This is in contradistinction to case of a permanent EDM.

$$\mathcal{H} = -\frac{\mu}{S} \mathbf{S} \cdot \mathbf{B} - \frac{d}{S} \mathbf{S} \cdot \mathbf{E}$$

The appearance of nonzero d changes the splitting of spin states in a nonzero magnetic field, so that it is appreciable even if engendered by a single operator.

Nevertheless CP violation can appear in $n \leftarrow \bar{n}$ oscillations.

A failure of detailed balance can appear through absorptive effects.

[McKeen and Nelson, 2015]

Implications of the CPT Phases

Previously it had been suggested that spin-dependent SM effects involving transverse magnetic fields could help connect n and \bar{n} states of opposite spin and thus evade the need for magnetic field quenching.

[SG and Jafari, 2015]

The success of this suggestion is sensitive to the CPT phase constraint we have discussed.

Fixing the spin quantization axis with \mathbf{B}_0 and defining $\omega_0 \equiv -\mu_n B_0$ and $\omega_1 \equiv -\mu_n B_1$, the Hamiltonian matrix in the $|n(+)\rangle, |\bar{n}(+)\rangle, |\bar{n}(-)\rangle, |n(-)\rangle$ basis at $t > 0$ is of form

$$\mathcal{H} = \begin{pmatrix} M + \omega_0 & \delta & \omega_1 & 0 \\ \delta & M - \omega_0 & 0 & -\omega_1 \\ \omega_1 & 0 & M - \omega_0 & -\delta\eta_{cpt}^2 \\ 0 & -\omega_1 & -\delta\eta_{cpt}^2 & M + \omega_0 \end{pmatrix},$$

where M is the neutron mass and δ denotes a $n(+) \rightarrow \bar{n}(+)$ transition matrix element.

Previously $\eta_{cpt}^2 = 1$ was employed. [SG and Jafari, 2015]

But $\eta_{cpt}^2 = -1$ is needed. [SG and Yan, 2016] [Voloshin, priv. comm., 2015; Berezhiani and Vainshtein, 2015]

Upon including $\eta_{cpt}^2 = -1$

- No $n+ \rightarrow \bar{n}-$ or $n- \rightarrow \bar{n}+$ transitions
- Quenching of $n\bar{n}$ transitions irrespective of transverse magnetic fields

However, spin-dependent effects appear in $n-\bar{n}$ transitions. Consider

$$\mathcal{O}_4 = \psi^T C \gamma^\mu \gamma_5 \psi \partial^\nu F_{\mu\nu} + \text{h.c.}$$

$n(+)$ \rightarrow $\bar{n}(-)$ occurs directly because the interaction with the current flips the spin.

This is concomitant with $n(p_1, s_1) + n(p_2, s_2) \rightarrow \gamma^*(k)$, for which only $L = 1$ and $S = 1$ is allowed via angular momentum conservation and Fermi statistics. [Berezhiani and Vainshtein, 2015]

Here $e + n \rightarrow \bar{n} + e$, e.g., so that the experimental concept for “ $n\bar{n}$ conversion” would be completely different.

BSM theories that generate $n\bar{n}$ oscillations support $n\bar{n}$ conversion as well.

[SG and Yan, in preparation, 2016]

We have found that the employing phase constraint $(\eta_c \eta_p \eta_t)^2 = -1$ still yields CPT-odd operators. We emphasize that the operators are Lorentz invariant by construction.

The CPT theorem is not broken, however, because the wrong CPT operators do appear to vanish.

The stature of the proof that they do indeed vanish depends on whether the fermions are Majorana or Dirac. In the latter case, canonical quantization and a Fourier expansion of the fermion field is required, though fermion antisymmetry is still key.

To consider why it might be possible to write down a CPT-odd, Lorentz-invariant operator (even if it does vanish!), we recall theories of self-conjugate particles with half-integer isospin, which are non-local and have anomalous CPT properties. [Carruthers, 1967; Lee, 1967; Fleming and Kazes, 1967; Jin, 1967; Kantor, 1967; Steinmann, 1967; Zumino and Zwanziger, 1967; Carruthers, 1968 & 1968 & 1968 & 1968]

In attempting to rationalize the spectral pattern of the low-lying, light hadrons, Carruthers discovered a class of theories for which the CPT theorem does not hold. [Carruthers, 1967]

The pions form a self-conjugate isospin multiplet (π^+, π^0, π^-) , but the kaons form pair-conjugate multiplets (K^+, K^0) and (\bar{K}^0, K^-) .

Carruthers discovered that free theories of self-conjugate bosons with half-integer isospin are nonlocal, that the commutator of two self-conjugate fields with opposite isospin components do not vanish at space-like separations. [Carruthers, 1967]

Moreover, since weak local commutativity fails, CPT symmetry is no longer expected to hold, nor should the CPT theorem of Greenberg apply. [Carruthers, 1968; Streater and Wightman, 2000; Greenberg, 2002]

The neutron and antineutron are members of pair-conjugate $I = 1/2$ multiplets. The quark-level operators that generate $n - \bar{n}$ oscillations would also produce $p - \bar{p}$ oscillations under the isospin transformation $u \leftrightarrow d$, though the latter are removed by electric charge conservation....

Ergo $n - \bar{n}$ oscillations are problematic in pure QCD in the isospin limit.

[SG and Yan, 2016]

The study of $n-\bar{n}$ transitions provides insight into the nature of $\mathcal{B}-\mathcal{L}$ violation.

We have analyzed the C, P, and T transformations of fermions with $\mathcal{B} - \mathcal{L}$ violation and have found that the so-called arbitrary phases are not arbitrary. We find $\eta_{cpt}^2 = -1$, as well as $\eta_{ct}^2 = 1$ and $\eta_p^2 = -1$. These phase restrictions are only appreciable in $\mathcal{B} - \mathcal{L}$ violating operators and impact their interplay with SM effects.

A particular $n - \bar{n}$ transition operator coupled to an external electromagnetic current, made possible by the nucleon spin, looks promising for practical applications....

“The future ain’t what it used to be.” — Yogi Berra

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