

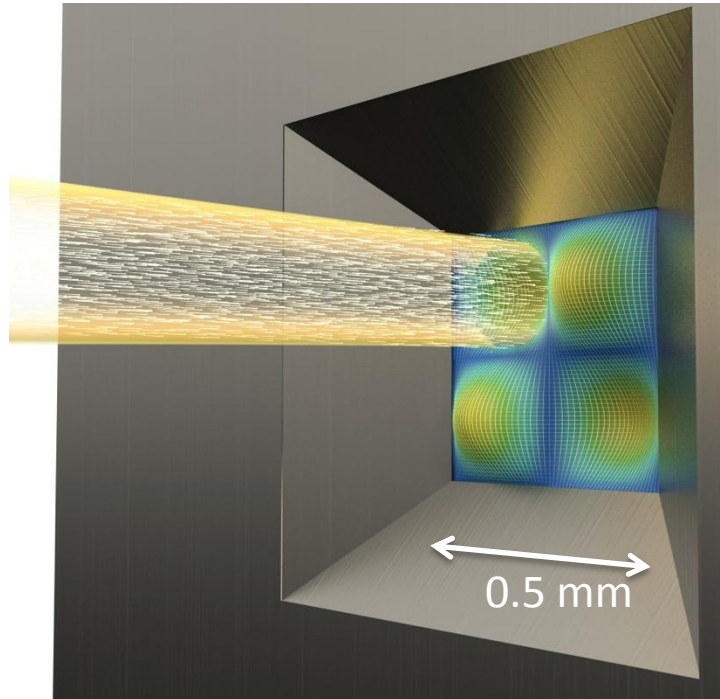
Observing Radiation Pressure Shot Noise on a Solid Object

Cindy Regal
Tom Purdy
Bob Peterson
Ben Yu

KITP, QuControl, 2013

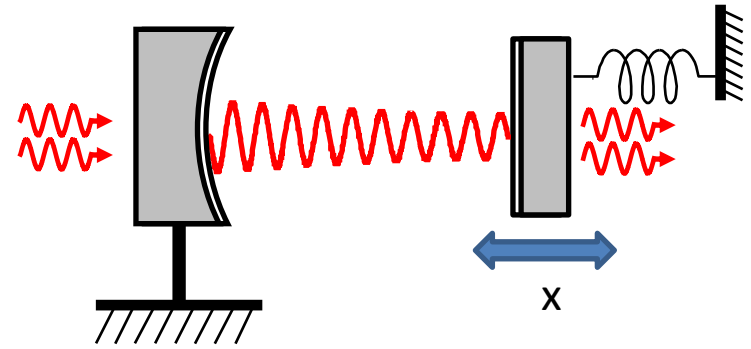


Boulder, CO, USA



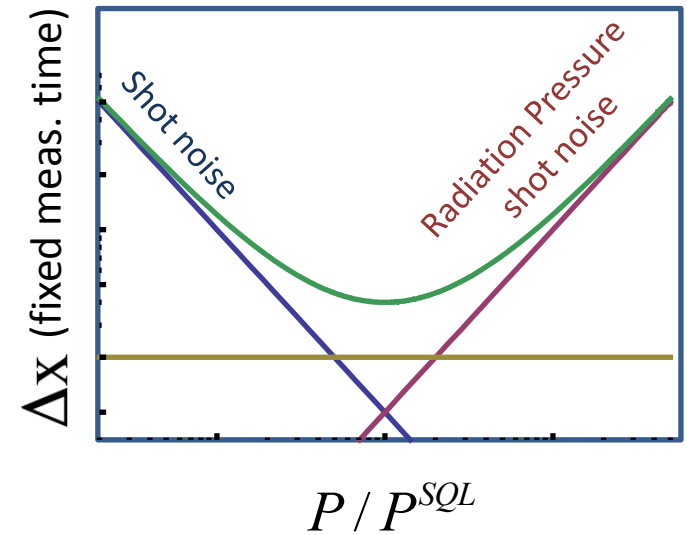
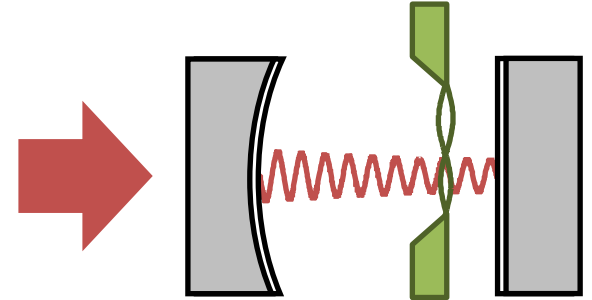
Orientation and outline

- (Quantum) **Cavity Optomechanics**
Measure and control motion of objects in interferometers near quantum limits
 - One degree of freedom
 - larger – size, mass
 - complex?



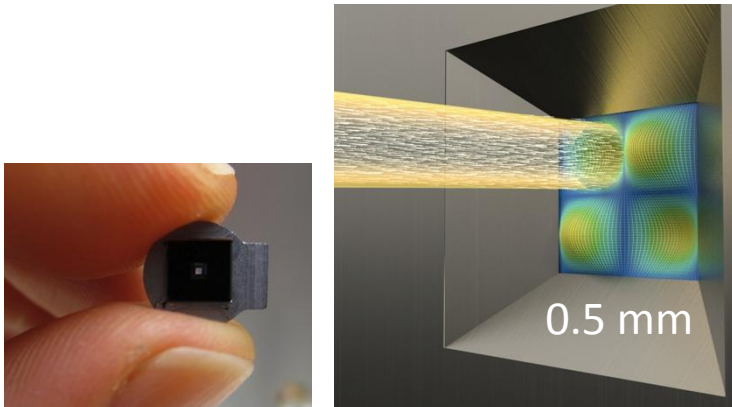
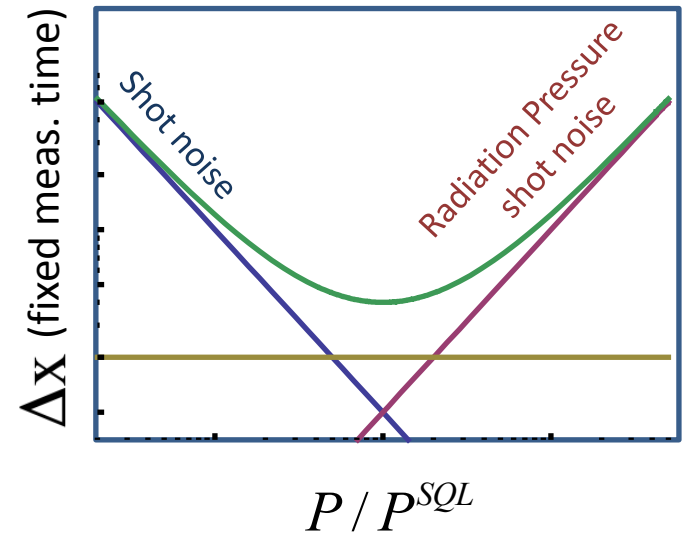
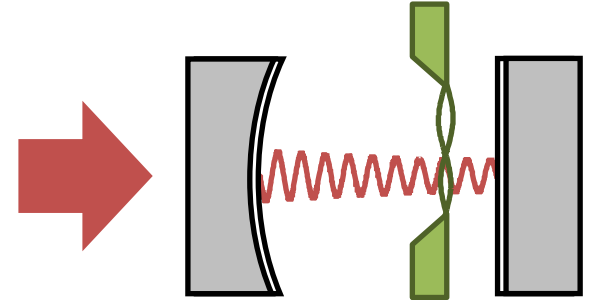
Outline

- (Quantum) **Cavity Optomechanics**
Measure and control motion of objects in interferometers near quantum limits
- Experiment presented: Observation of radiation pressure shot noise (RPSN)
 - Backaction branch of quantum-limited continuous position measurement



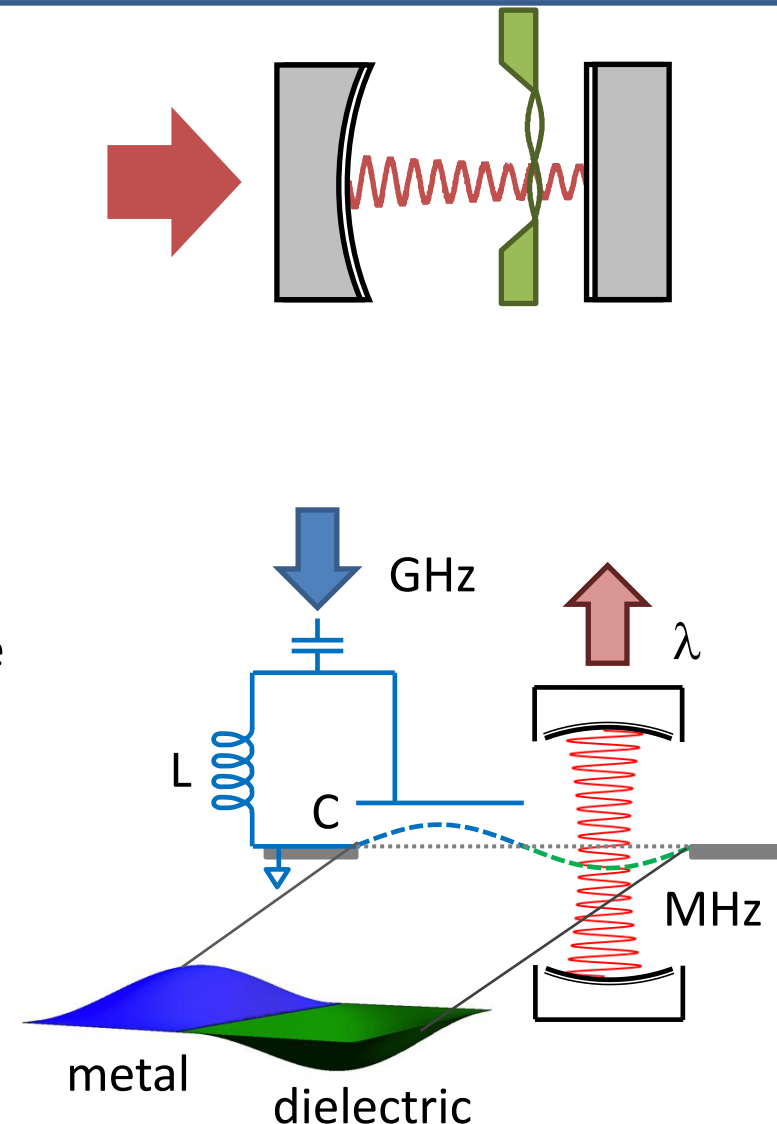
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 - Si_3N_4 (50 nm by mm-scale)



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- Physical object: Very thin vibrating membrane
 - Si_3N_4 (50 nm by mm-scale)
- Quantum information applications
 - Mechanically mediated interactions
 - Microwave - Optical



Introduction

Heisenberg uncertainty and precision measurement



Free mass limit

Measure to Δx at time t

Momentum uncertain to
 $\Delta p \geq \hbar / 2\Delta x$

At later time...

$$\Delta x(t') = \Delta x(t) + \frac{\hbar(t' - t)}{2m\Delta x(t)}$$

Heisenberg Microscope: Always some physical origin

Heisenberg's book, 1930...

a) *Determination of the position of a free particle.*—As a first example of the destruction of the knowledge of a particle's momentum by an apparatus determining its position, we consider the use of a microscope.¹ Let the particle be moving at such a distance from the microscope that the cone of rays scattered from it through the objective has an angular opening ϵ . If λ is the wave-length of the light illuminating it, then the uncertainty in the measurement of the

x -co-ordinate (see Fig. 5) according to the laws of optics governing the resolving power of any instrument is:

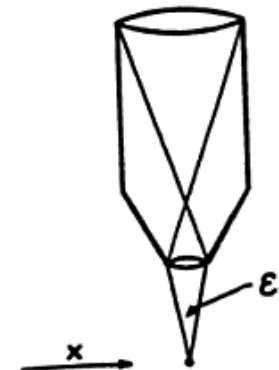
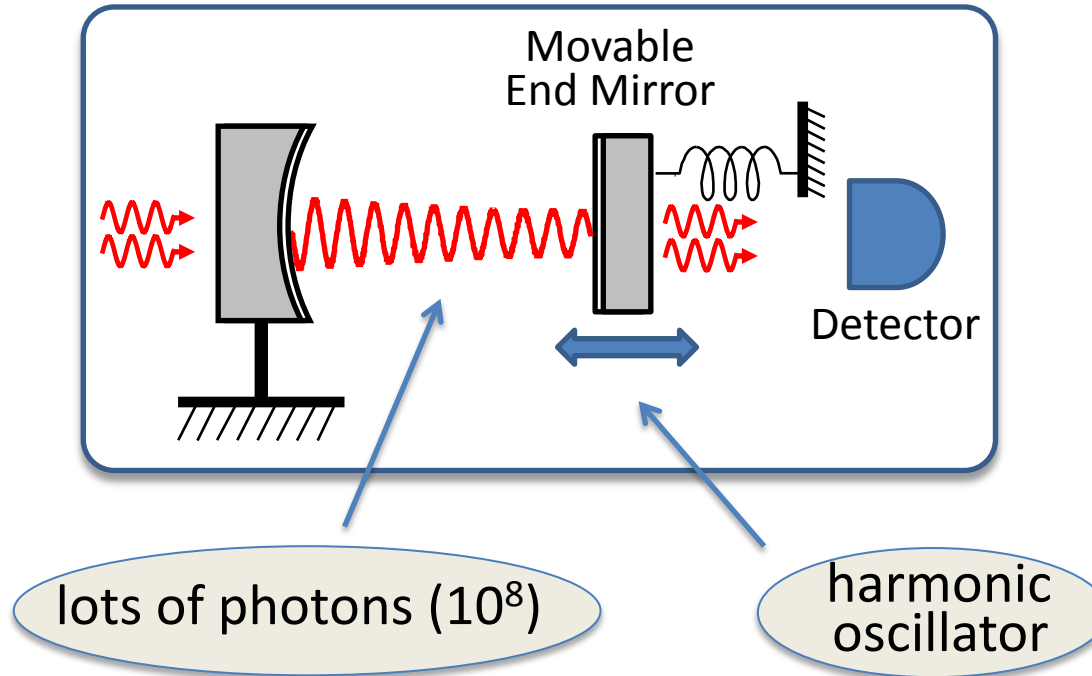


FIG. 5

governing the resolving power of any instrument is:

$$\Delta x = \frac{\lambda}{\sin \epsilon}. \quad (16)$$

Our version



Shot noise \sqrt{N}

Shot noise of radiation pressure drives up mirror

PHYSICAL REVIEW
LETTERS

VOLUME 45

14 JULY 1980

NUMBER 2

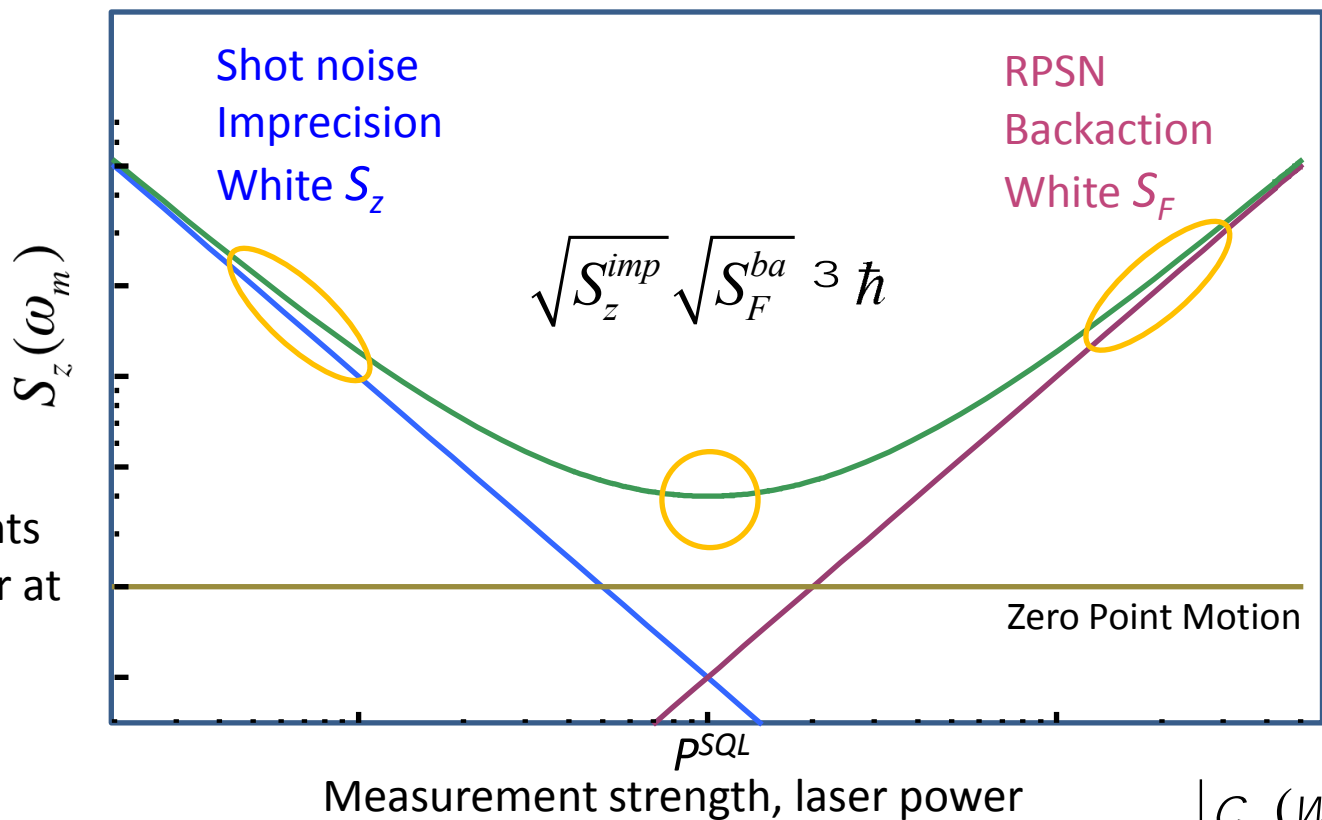
Quantum-Mechanical Radiation-Pressure Fluctuations in an Interferometer

Carlton M. Caves

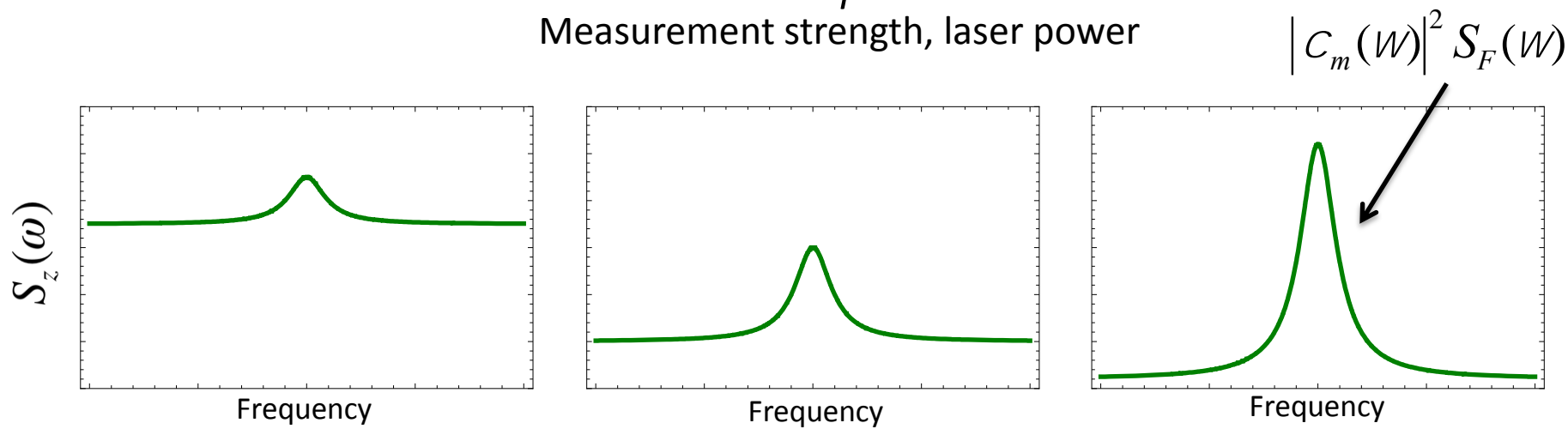
W. K. Kellogg Radiation Laboratory, California Institute of Technology, Pasadena, California 91125
(Received 29 January 1980)

The interferometers now being developed to detect gravitational waves work by measuring small changes in the positions of free masses. There has been a controversy whether quantum-mechanical radiation-pressure fluctuations disturb this measurement. This Letter resolves the controversy: They do.

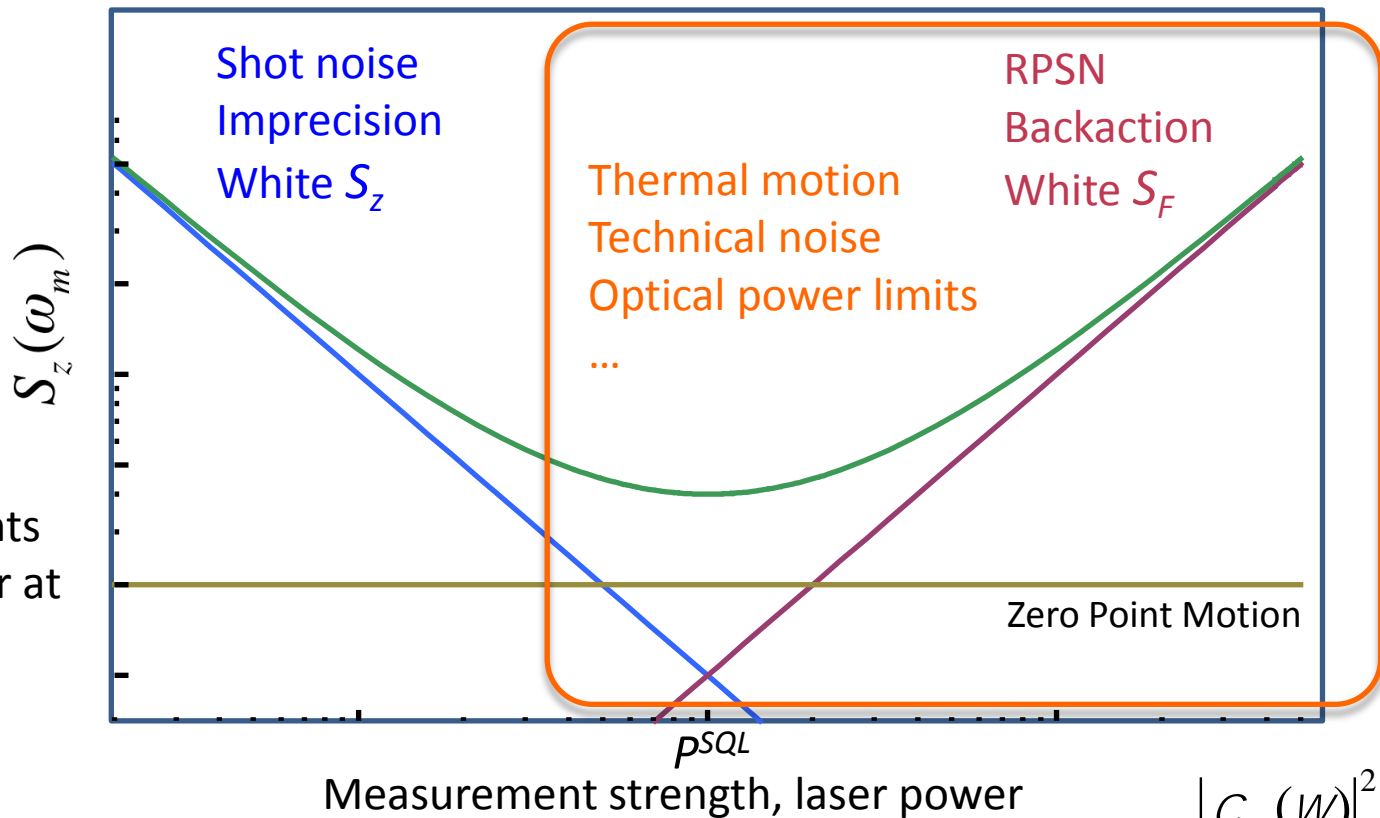
Standard Quantum Limit



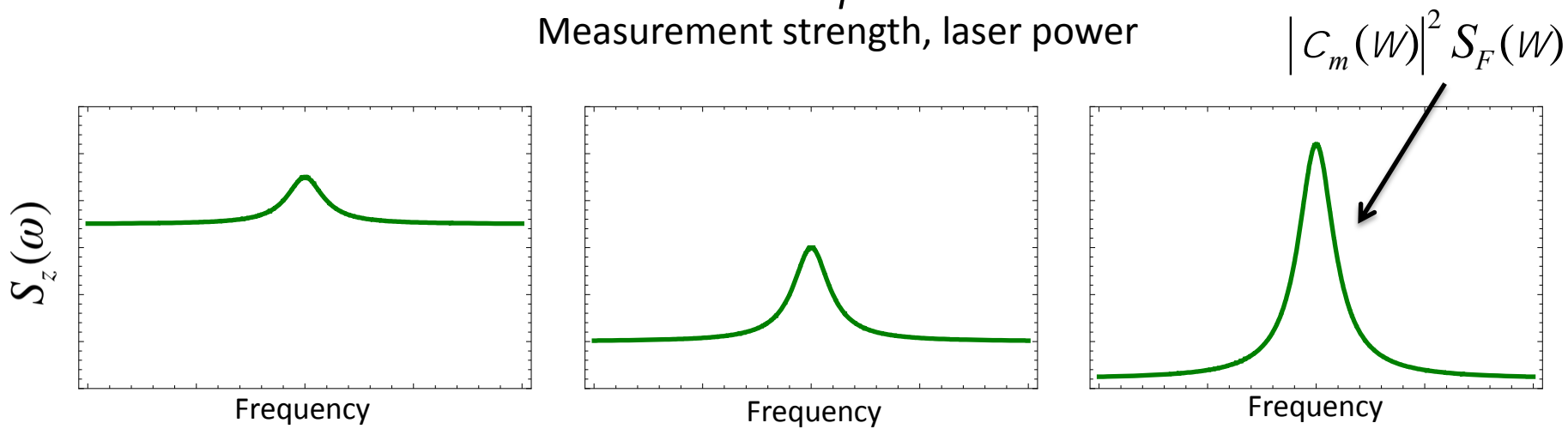
Our measurements focus on behavior at resonance ω_m



Standard Quantum Limit



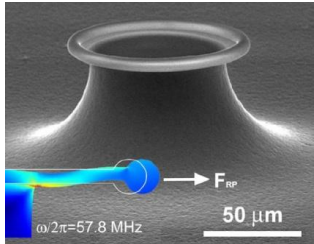
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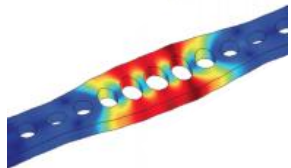
Subset of spectrum of optomechanics experiments

Optomechanics

Effectively moving mirrors



Kippenberg, EPFL

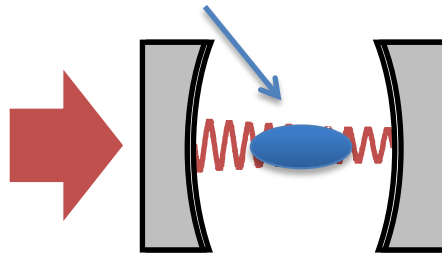


Painter, Caltech

Gravitational wave detectors

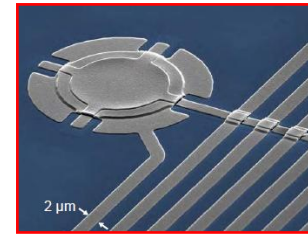


trapped atoms



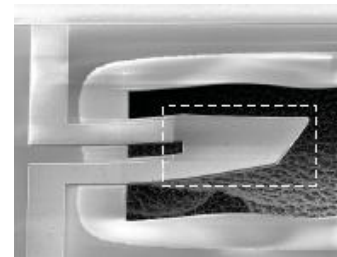
Electromechanics

Moving capacitor plate



Lehnert/Simmonds, Boulder

Piezoelectrics

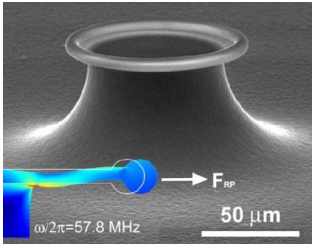


Cleland/Martinis
UCSB

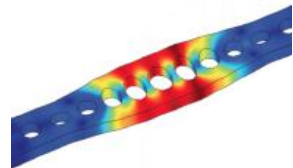
Closely related optomechanics experiments

Optomechanics

Effectively moving mirrors



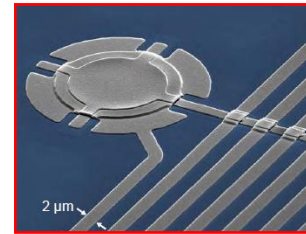
Kippenberg, EPFL



Painter, Caltech

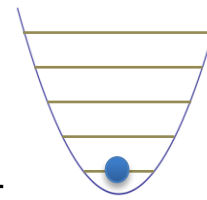
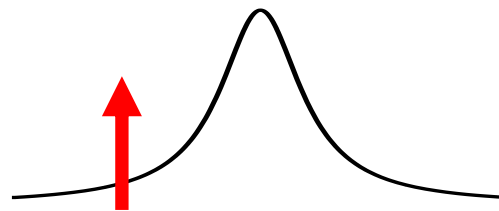
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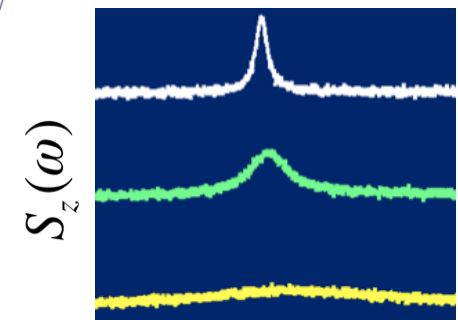


Lehnert/Simmonds, Boulder

“Laser” cooling to near the mechanical ground state
(combined with cryogenic cooling)

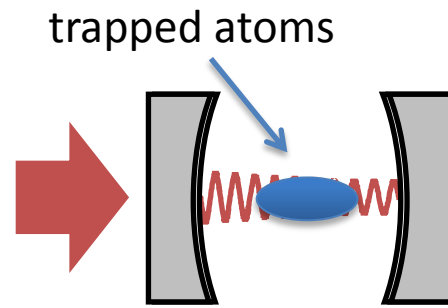


Observation of sideband asymmetry, Painter group



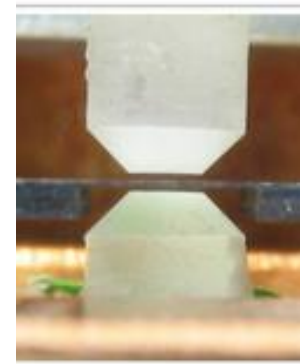
Frequency

Closely related optomechanics experiments



Observation of RPSN heating with atom gas
And ponderomotive squeezing

Stamper-Kurn group, Berkeley

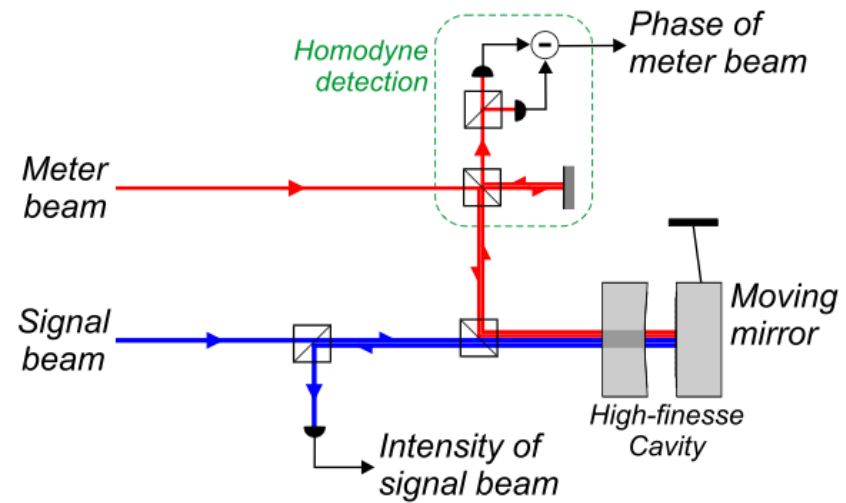


Closely related optomechanics experiments

Gravitational wave detectors

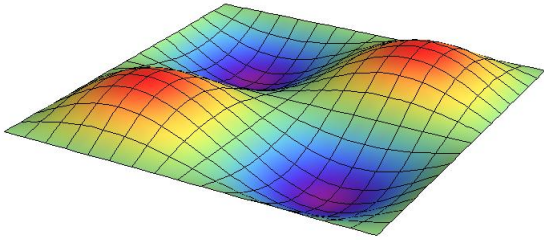


Experimental studies of classical analogs:
Heidmann group, Paris



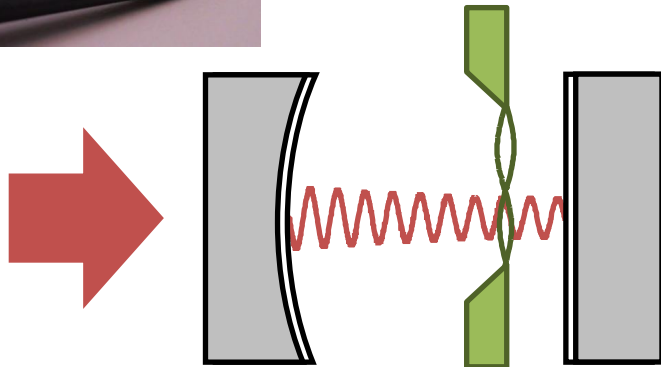
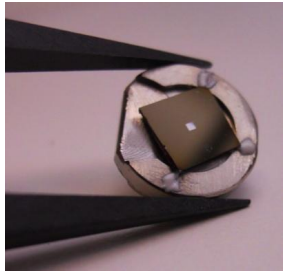
Our optomechanical device

(2,2) drum mode

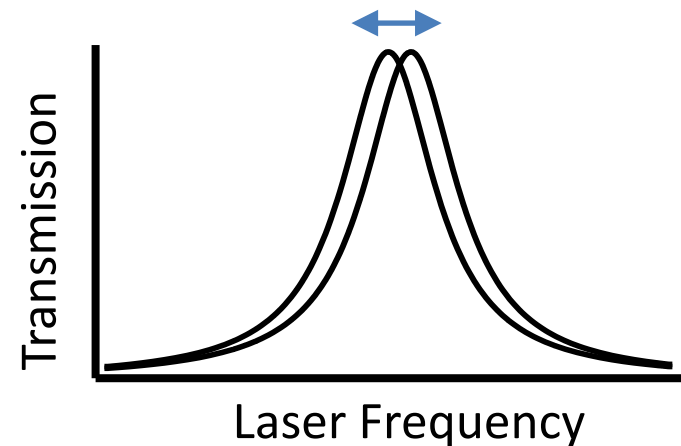


- Stoichiometric **silicon nitride*** sits in optical standing wave near end of cavity
- 50 nm thick drum - highly stressed, $\nu_m = 1$ MHz
- Increases oscillator energy compared to thermal scales while keeping dissipation similar

$$Q \sim 10^6 - 10^7$$



Cavity resonance shifts with membrane position

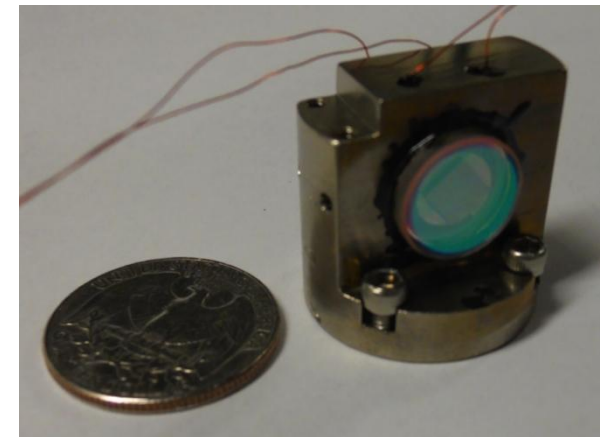
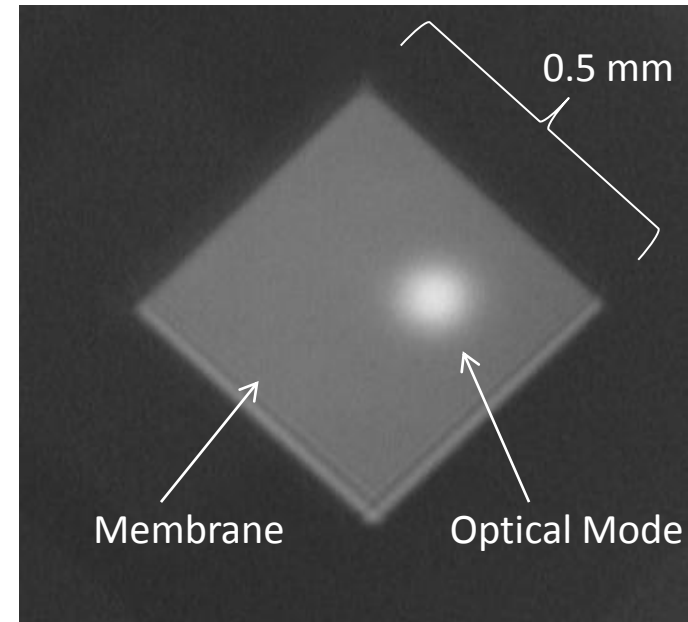
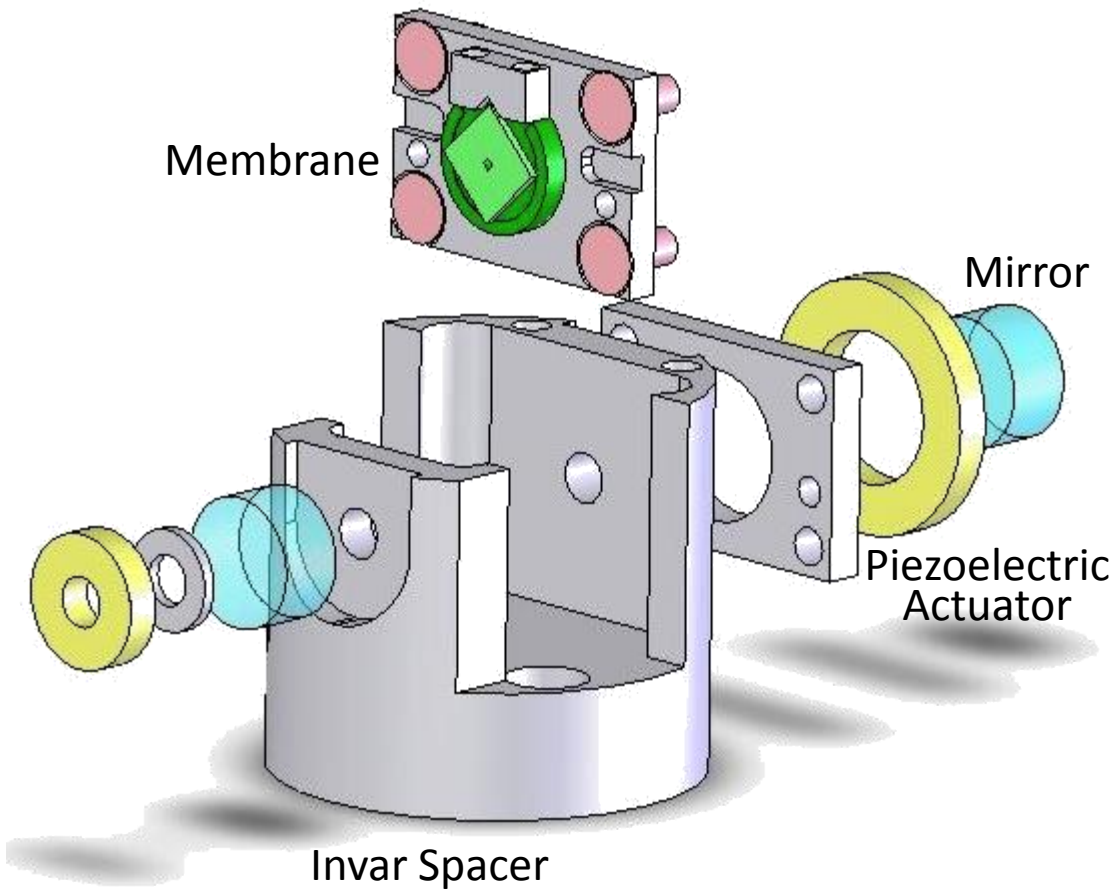


*Introduced to optomechanics: Harris group at Yale, Thompson et al. Nature 2008

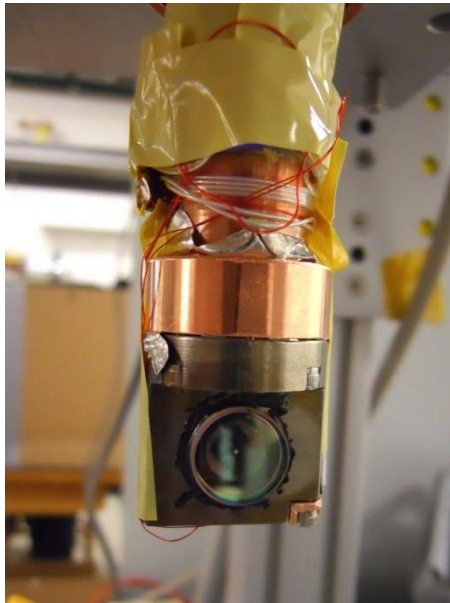
A cryogenic, three-element Fabry-Perot cavity

Challenge:

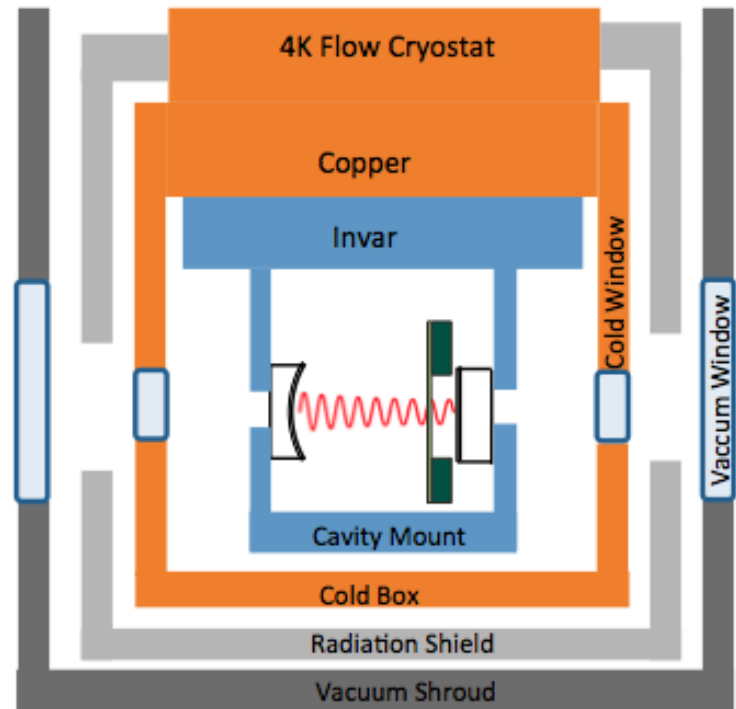
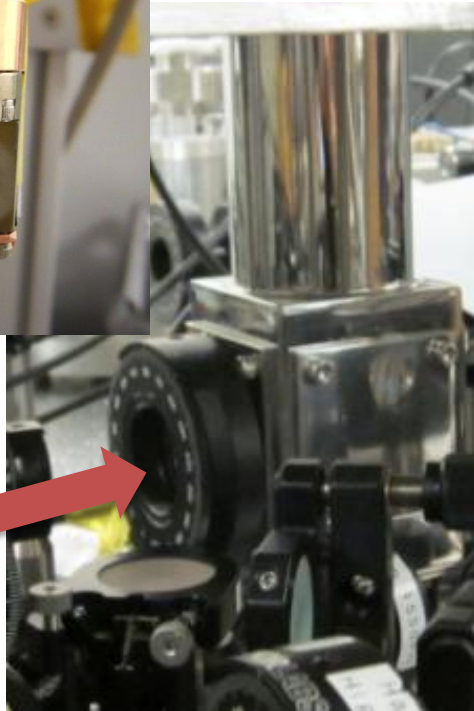
- Stability and alignment of cryogenic device



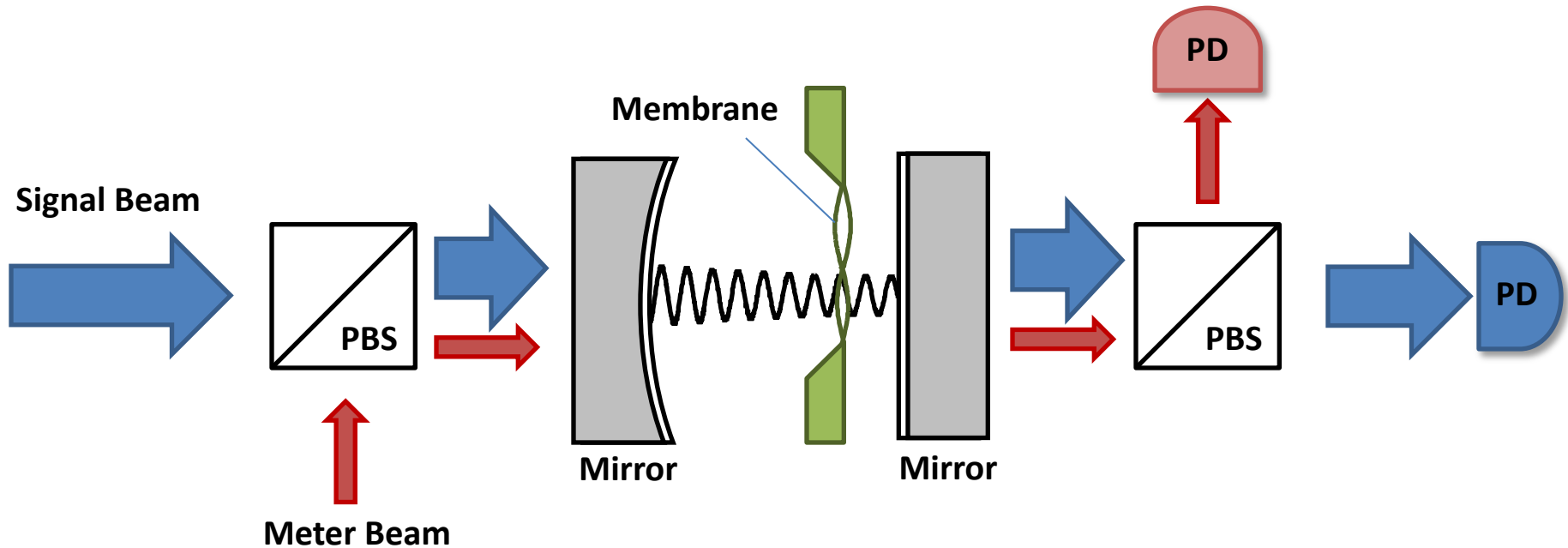
Cryogenic optomechanical device



Experiment at 4 kelvin – simple in many ways



RPSN experiment setup

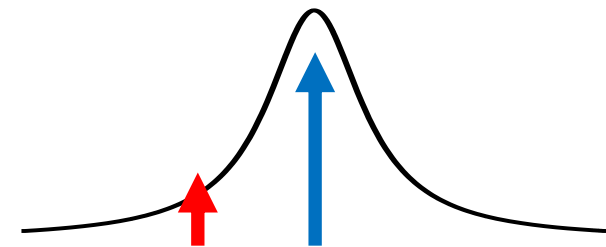


“Signal Beam (S)”

- High Power
- On resonance
- RPSN
- Optical force readout

“Meter Beam (M)”

- Low Power
- Red detuned
- Optical damping/cooling
- Displacement readout



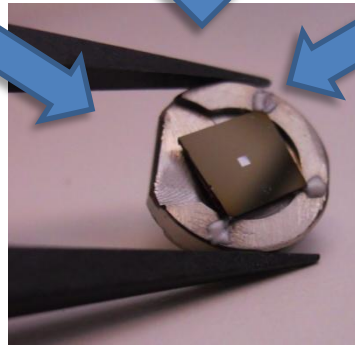
Observing radiation pressure shot noise heating

^4He Cryostat
 $T_0 = 5 \text{ K}$
 $G_0 = 0.5 \text{ Hz}$

Meter Beam
Dominant damping
 $G_M = 1.4 \text{ kHz}$

Signal Beam
RPSN

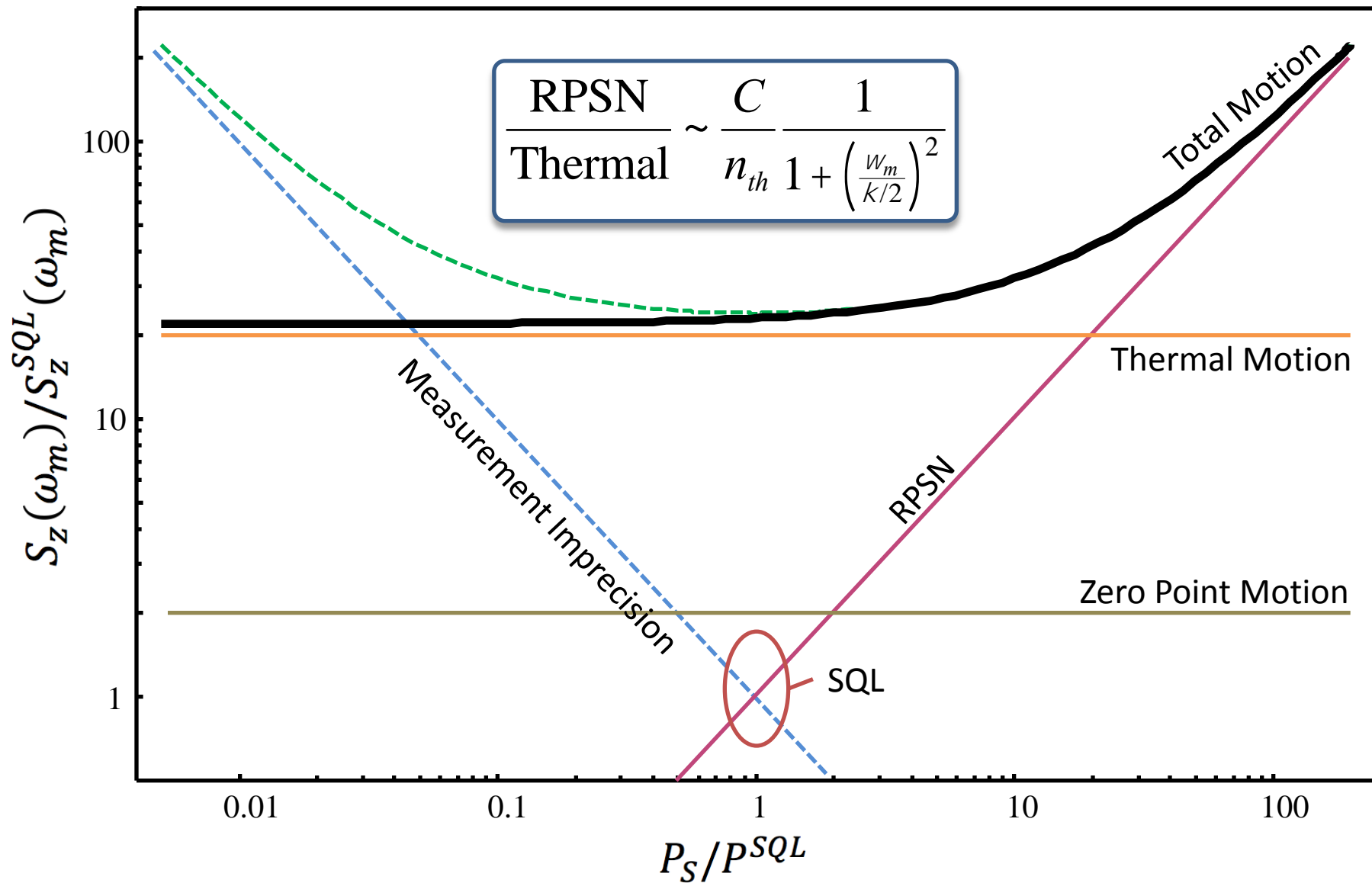
Three heat baths at different temperatures coupled to the resonator with differing strengths



$$T_{eff} = \frac{T_0 G_0 + T_M G_M + T_S G_S}{G_0 + G_M + G_S}$$

Equilibrium Temperature

Radiation pressure shot noise heating



Parameters for seeing RPSN heating

$$\frac{\text{RPSN}}{\text{Thermal}} \sim \frac{C}{n_{th}} \frac{1}{1 + \left(\frac{W_m}{k/2}\right)^2}$$

Cooperativity

$$C = \frac{4Ng^2}{kG_0}$$

cavity
damping

mechanical
damping

photon number
coupling

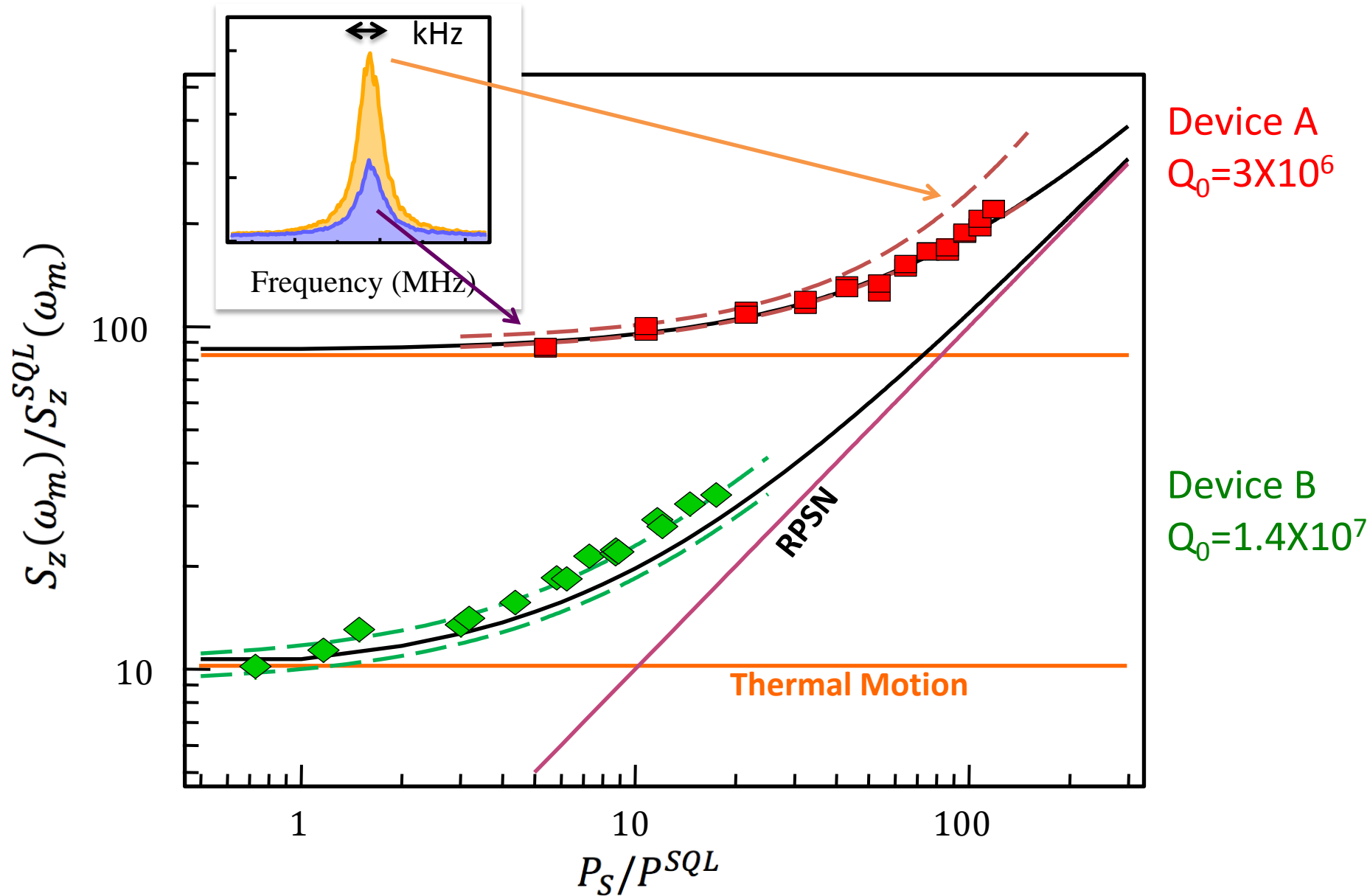
Thermal phonons (4 K bath)

$$n_{th} = \frac{k_b T_0}{\hbar W_m}$$

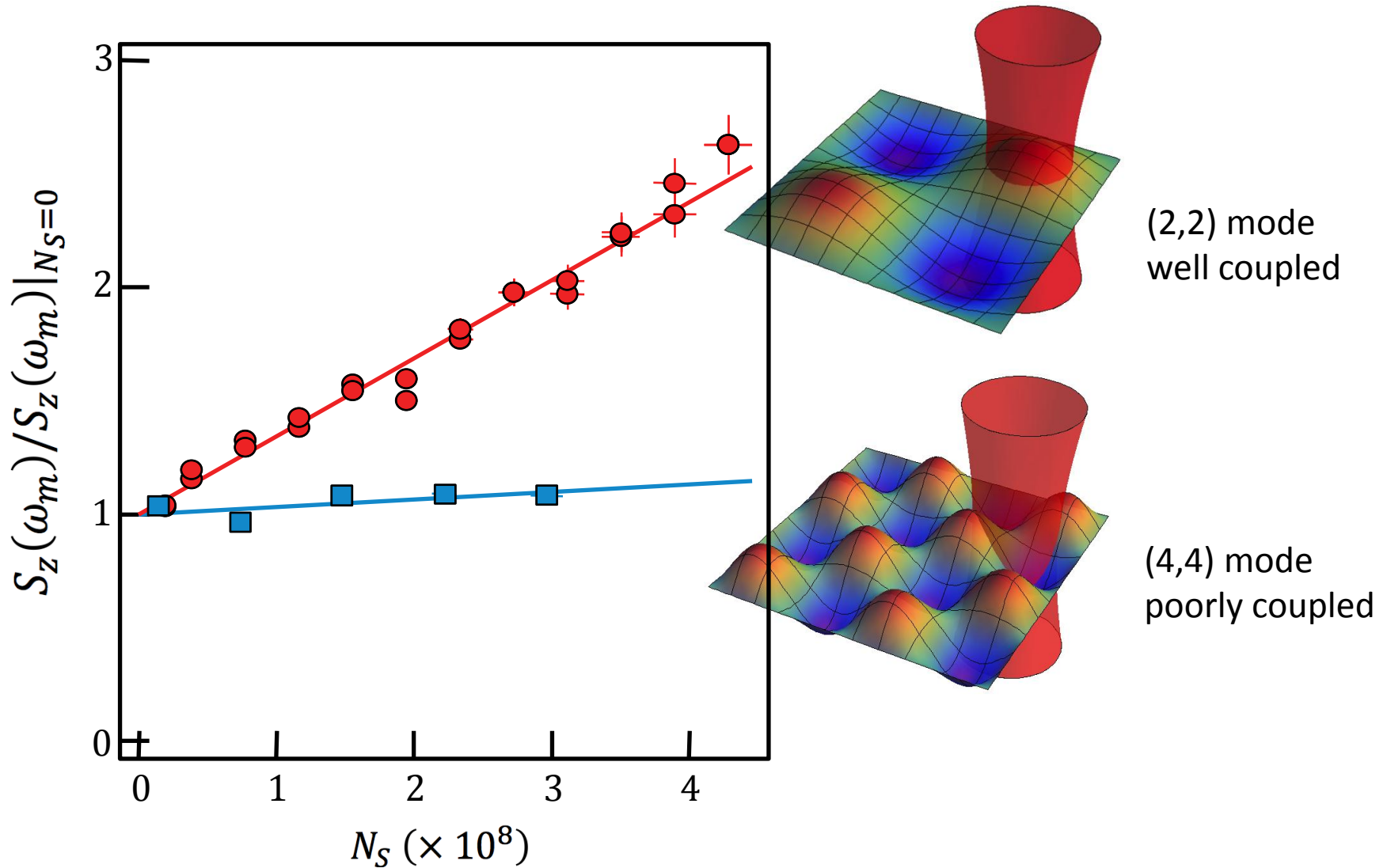
Meter beam damping:

- Plays no role in this ratio
- (Very important) convenience

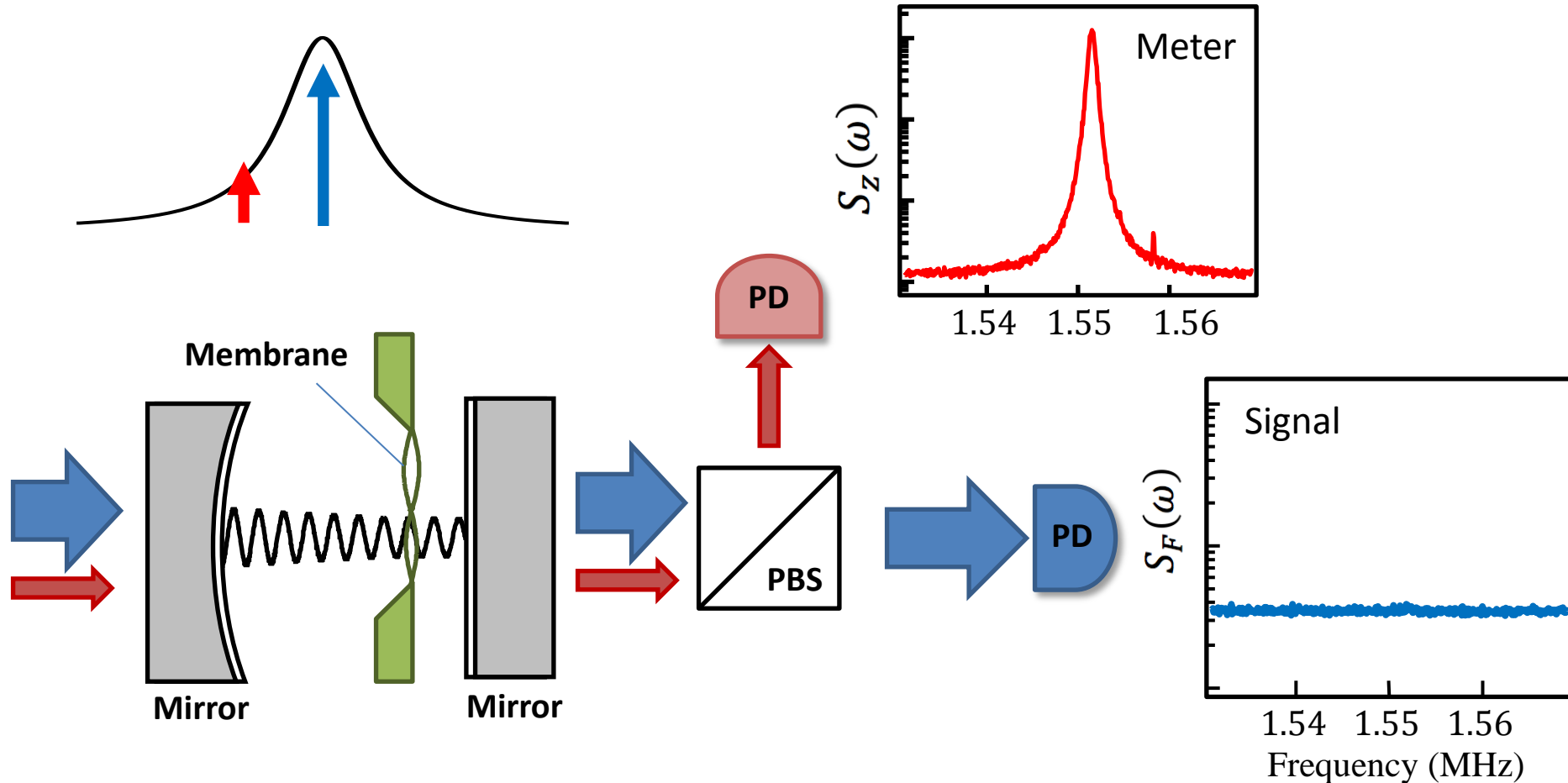
Radiation pressure shot noise heating



Check for physical heating



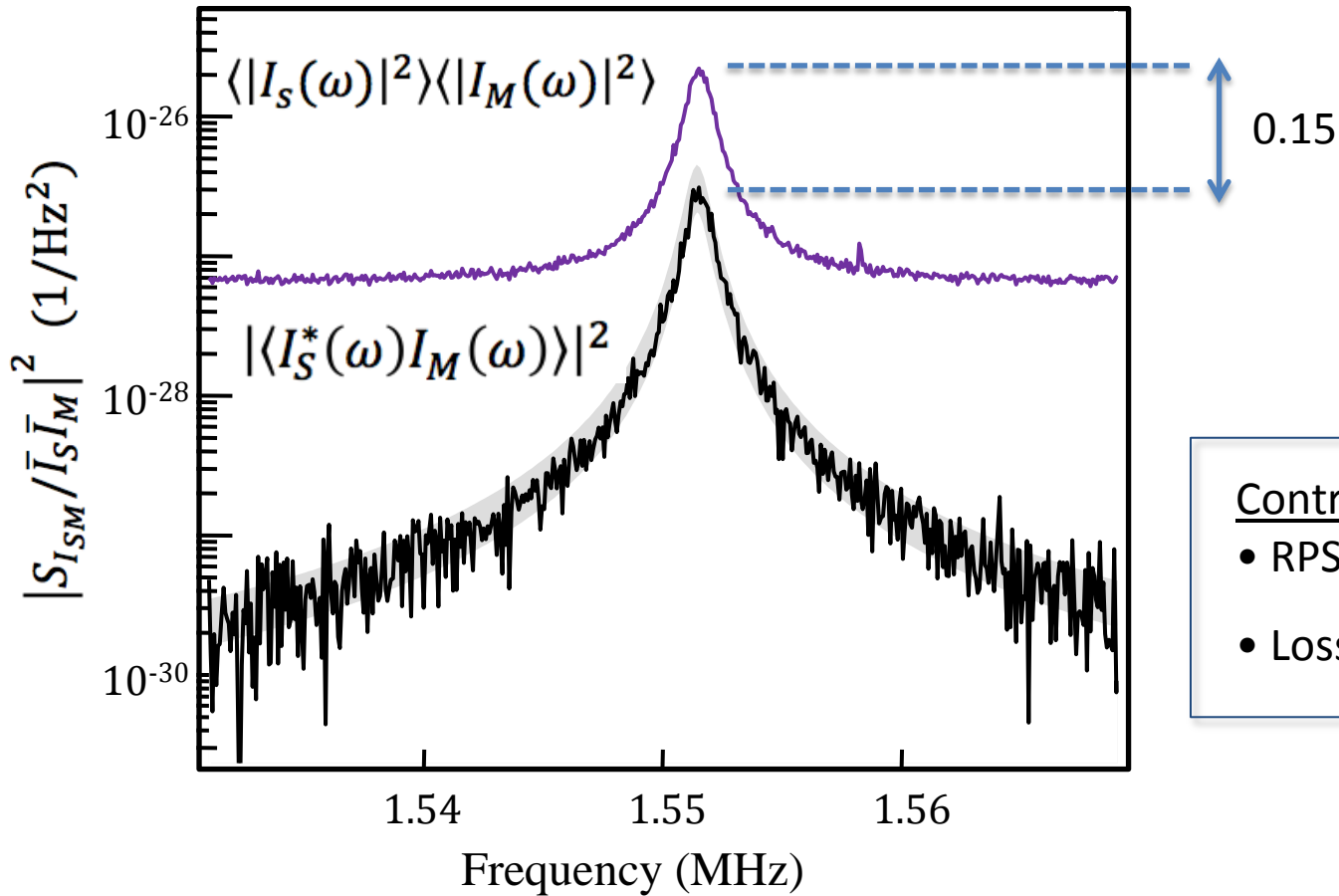
Signal beam: Record of optical force



- AM quadrature - shot noise intensity fluctuations - record of the optical force on the resonator

Two beam cross correlation

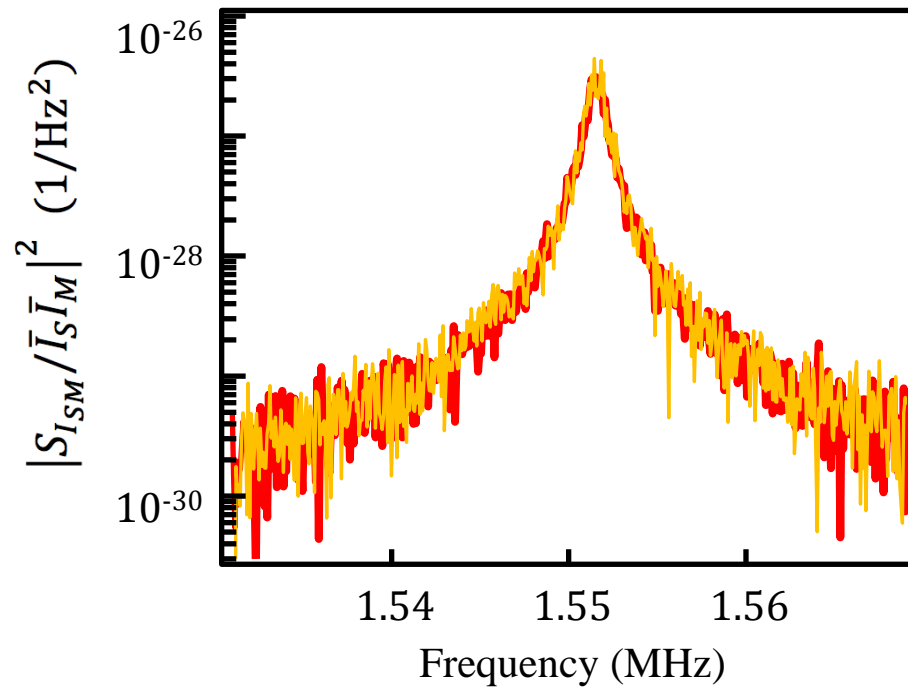
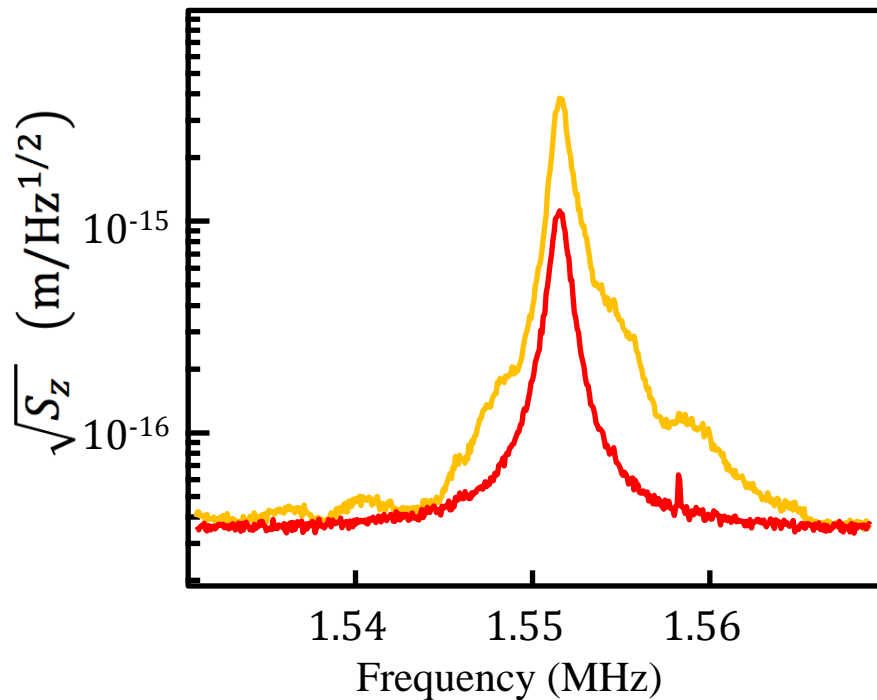
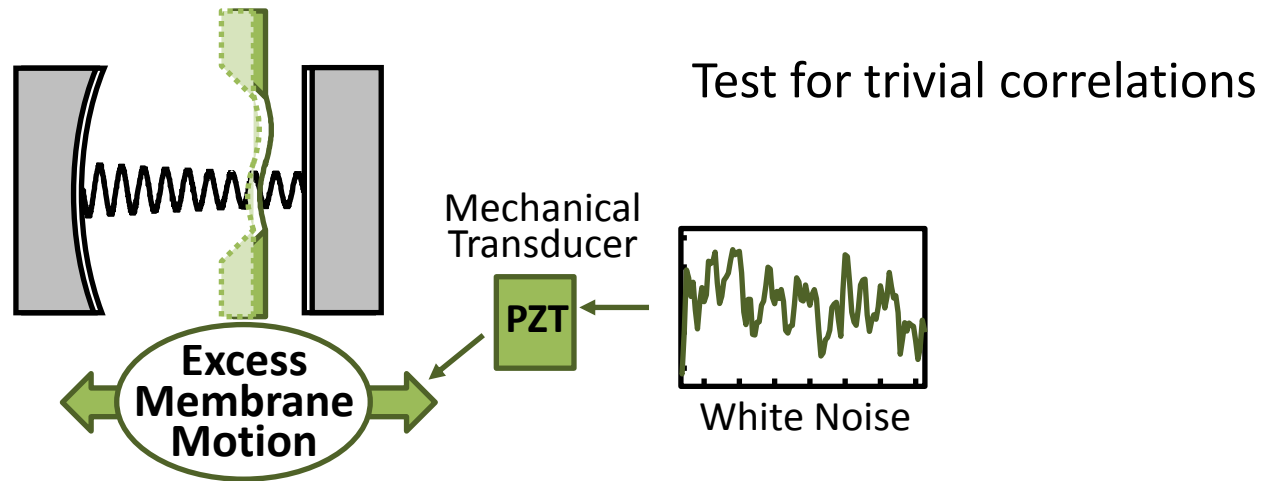
Cross correlation between
meter & signal



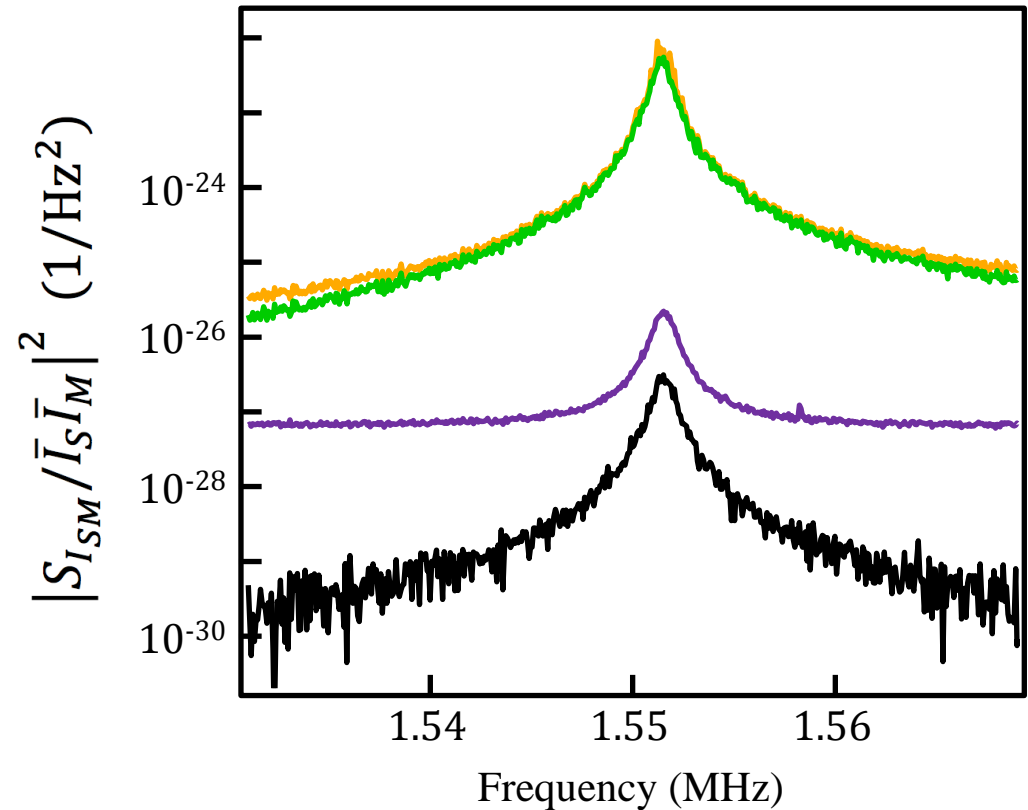
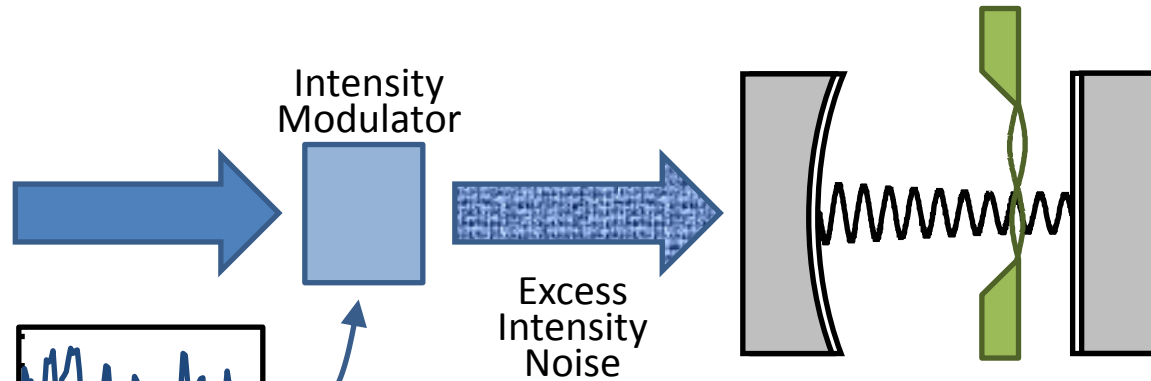
Contributions:

- RPSN to thermal 40%
- Loss (ports, path, QE) 40%

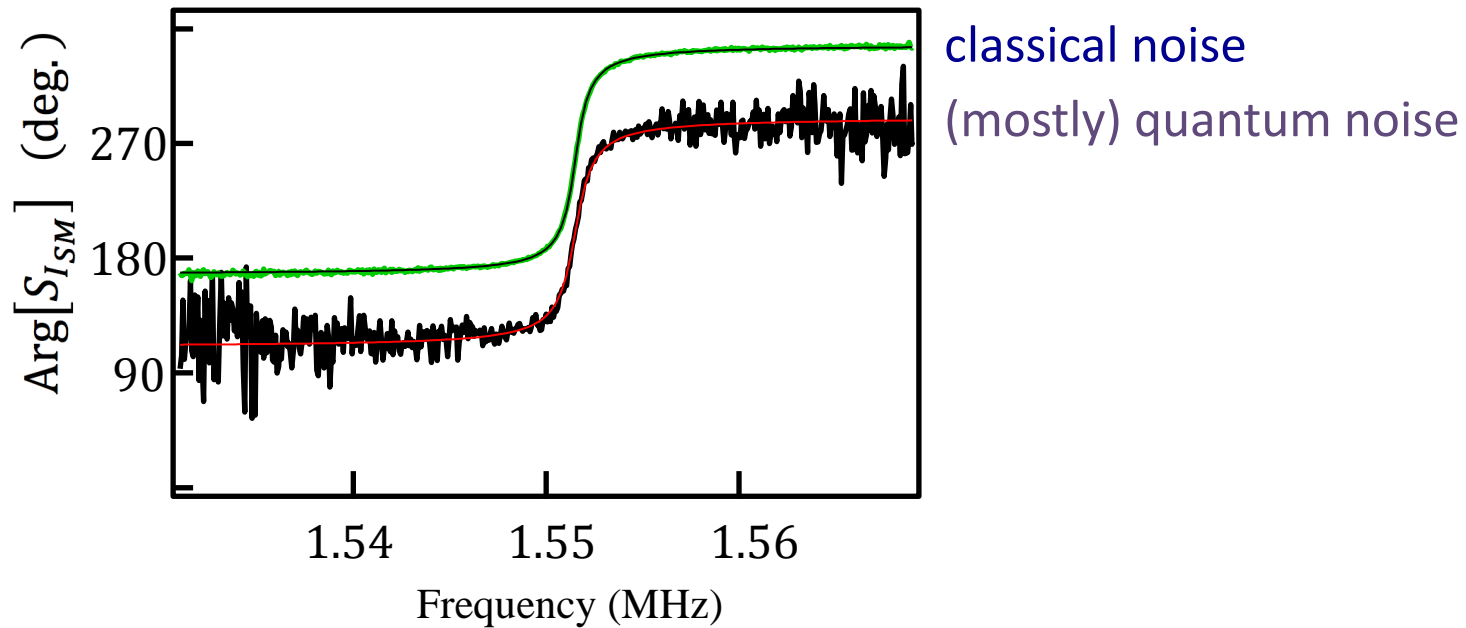
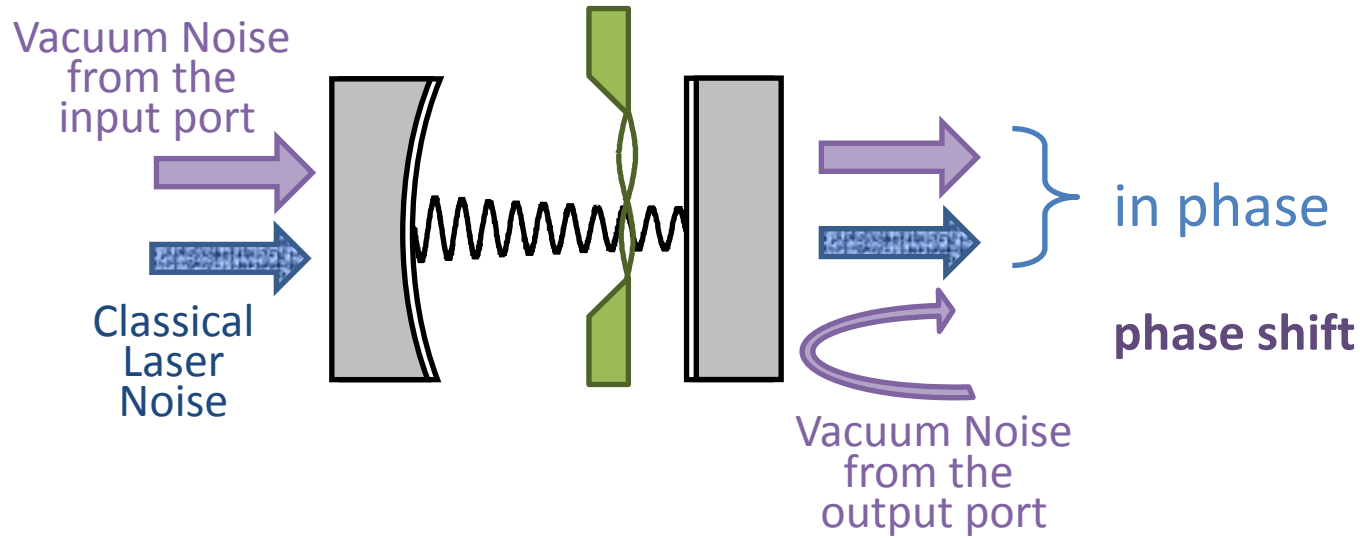
Two beam cross correlation



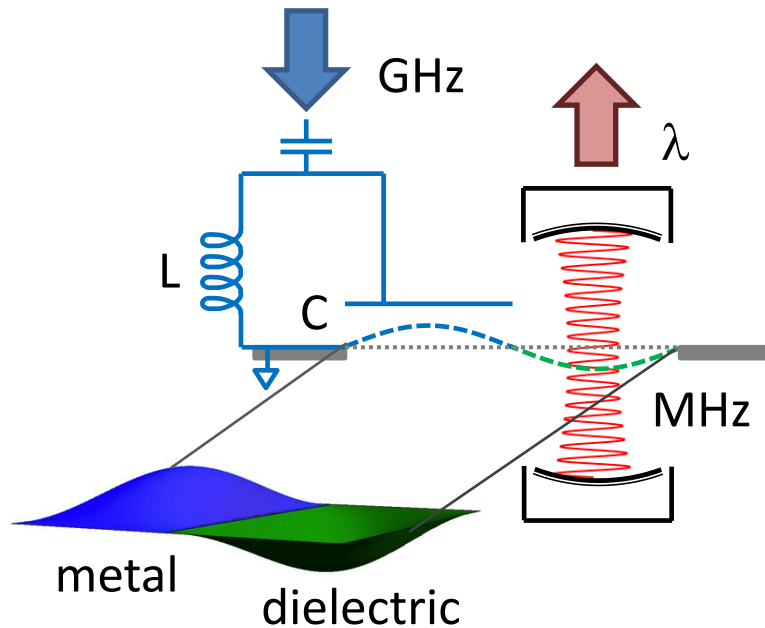
Classical intensity noise limit



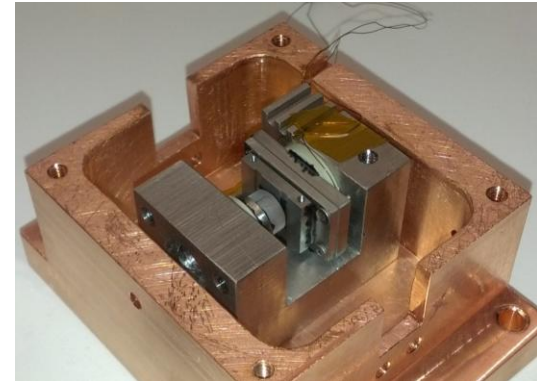
Consistency with quantum noise



Microwave to optical quantum link



Electromechanics: Lehnert Group (JILA)



$$C = \frac{4Ng^2}{kG_0} > n_{th}$$

Transfer rate between phonons and (itinerant) photons exceeds rate at which single phonon leaves to environment

Analogous experiments: UCSB

See for ideas:

J. Zhang...S. L. Braunstein, PRA (2003)

C. A. Regal and K. W. Lehnert, J. Phys. Conf. Series (2011)

A. Safavi-Naeini...O. Painter, New J. Phys. (2011)

J. Taylor et al., PRL (2011)

T. Palomaki...K. W. Lehnert, Nature in press (2013)

Conclusions and directions

- To do – Standard quantum limit for continuous position measurement
- There is a lot of quantum optics to pursue in these systems, optical squeezing, backaction evasion,...
- Elucidating to study these with physical object in interferometer driven by quantum noise

Group members: Optomechanics



Thomas Purdy

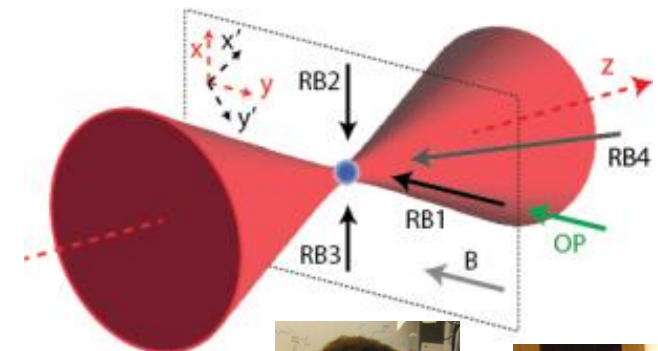


Bob Peterson



Ben Yu

Single neutral atoms



Adam Kaufman



Brian Lester

Collaborators:

Konrad Lehnert Group, JILA
Ray Simmonds Group, NIST