

Publications of the Speaker to the Topic

Publications used in this talk

T. Skinner, T. Reiss, B. Luy, N. Khaneja, S. J. Glaser, "Application of Optimal Control Theory to the design of broadband excitation pulses for high resolution NMR ", *J. Magn. Reson.* **163**, 8-15 (2003).

T. E. Skinner, T. O. Reiss, B. Luy, N. Khaneja, S. J. Glaser, "Reducing the duration of broadband excitation pulses using optimal control with limited RF amplitude", *J. Magn. Reson.* **167**, 68-74(2004).

K. Kobzar, T. E. Skinner, N. Khaneja, S. J. Glaser, B. Luy, "Exploring the limits of broadband excitation and inversion pulses", *J. Magn. Reson.* **170**, 236-243 (2004).

T. E. Skinner, T. O. Reiss, B. Luy, N. Khaneja, S. J. Glaser, " Tailoring the optimal control cost function to enable shorter broadband excitation pulses ", *J. Magn. Reson.* **172**, 17-23 (2005).

K. Kobzar, Luy, B., N. Khaneja, S. J. Glaser, "Pattern pulses: design of arbitrary excitation pulses as a function of pulse amplitude and offset", *J. Magn. Reson.* **173**, 229-235.

B. Luy, K. Kobzar, T. E. Skinner, N. Khaneja, S. J. Glaser, "Construction of universal rotations from point to point transformations", *J. Magn. Reson.* **176**, 179-186 (2005).

T. E. Skinner, K. Kobzar, B. Luy, R. Bendall, W. Bermel, N. Khaneja, S. J. Glaser, "Optimal control design of constant amplitude phase-modulated pulses: application to calibration-free broadband excitation", *J. Magn. Reson.* **179**, 241-249 (2006).

K. Kobzar, T.E. Skinner, N. Khaneja, S. J. Glaser, B. Luy, "Exploring the limits of broadband excitation and inversion pulses II: RF-power optimized pulses", *J. Magn. Reson.* **194**, 58-66 (2008).

Other related OCT publications

N. Khaneja, T. Reiss, B. Luy, S. J. Glaser, "Optimal Control of Spin Dynamics in the Presence of Relaxation", preprint quant-ph/0208050 (2002), *J. Magn. Reson.* **162**, 311-319 (2003).

N. Khaneja, B. Luy, S. J. Glaser, "Boundary of Quantum Evolution under Decoherence", preprint: quant-ph/0302060, *Proc. Natl. Acad. Sci. USA* **100**, 13162-13166 (2003).

N. Khaneja, J.S. Li, C. Kehlet, B. Luy, S. J. Glaser, "Broadband relaxation-optimized polarization transfer in magnetic resonance", *Proc. Natl. Acad. Sci. USA* **101**, 14742-14747 (2004).

N. I. Gershenson, K. Kobzar, B. Luy, S. J. Glaser, T. E. Skinner, "Optimal control design of excitation pulses that accomodate relaxation", *J. Magn. Reson.* **188**, 330-336 (2007).

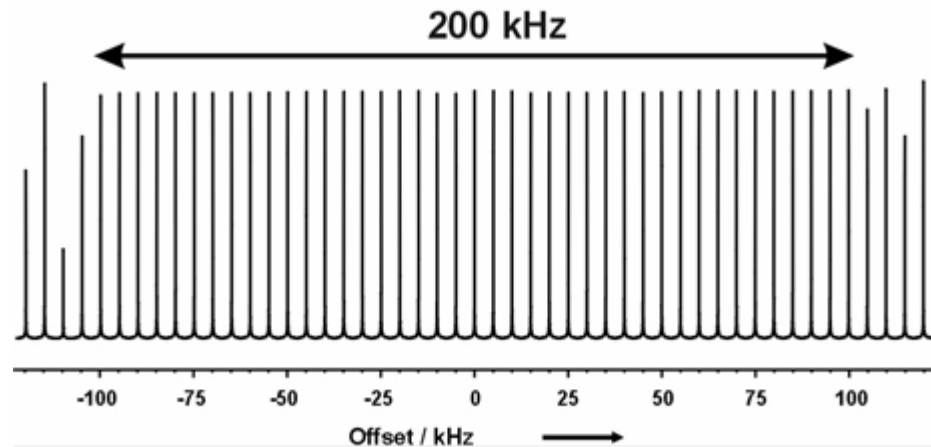
N. I. Gershenson, T. E. Skinner, B. Brutscher, N. Khaneja, M. Nimbalkar, B. Luy, S. J. Glaser, "Linear phase slope in pulse design: Application to coherence transfer", *J. Magn. Reson.* **192**, 235-243 (2008).

Related Publications

T. Untidt, T. Schulte-Herbrüggen, B. Luy, S. J. Glaser, C. Griesinger, O. W. Sørensen, N. C. Nielsen, "Design of NMR Pulse Experiments with Optimum Sensitivity. Coherence-Order-Selective Transfer in I_2S and I_3S Spin Systems", *Molecular Physics*, **95**, 787-796 (1998).

A. Enthart, J. C. Freudenberger, J. Furrer, H. Kessler, B. Luy, "The CLIP/CLAP-HSQC: Pure absorptive spectra for the measurement of one-bond couplings", *J. Magn. Reson.* **192**, 314-322 (2008).

NMR Pulse Design by OCT: Introduction, Applications and What we can learn from it



Kyryl Kobzar, Naum Gershenzon, Tom Skinner,
Navin Khaneja, Steffen Glaser, Burkhard Luy



Why bother with NMR spectroscopy?

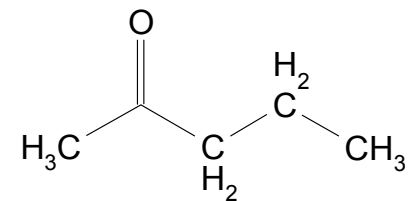
Broadband 'State-To-State' Pulses

Broadband 'Universal Rotation' Pulses

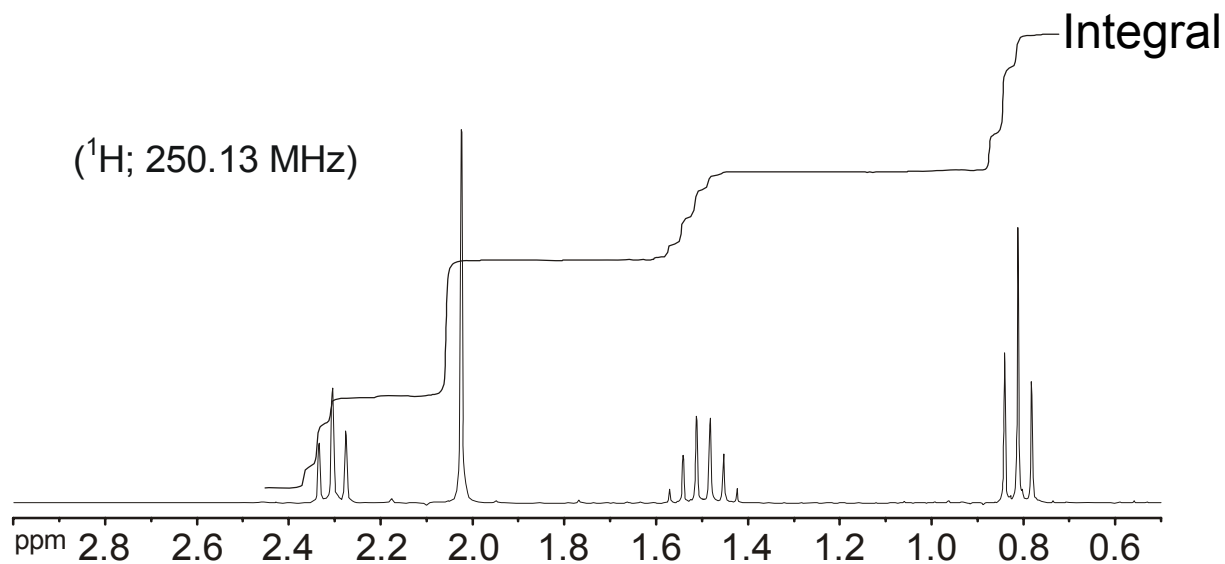
Ultrabroadband Excitation

Pattern Pulses

Simple ^1H -1D Spectrum



**Pentan-2-on,
Methylpropylketon**



Chemical Shift

Intensity

J-Couplings

Drift Hamiltonians

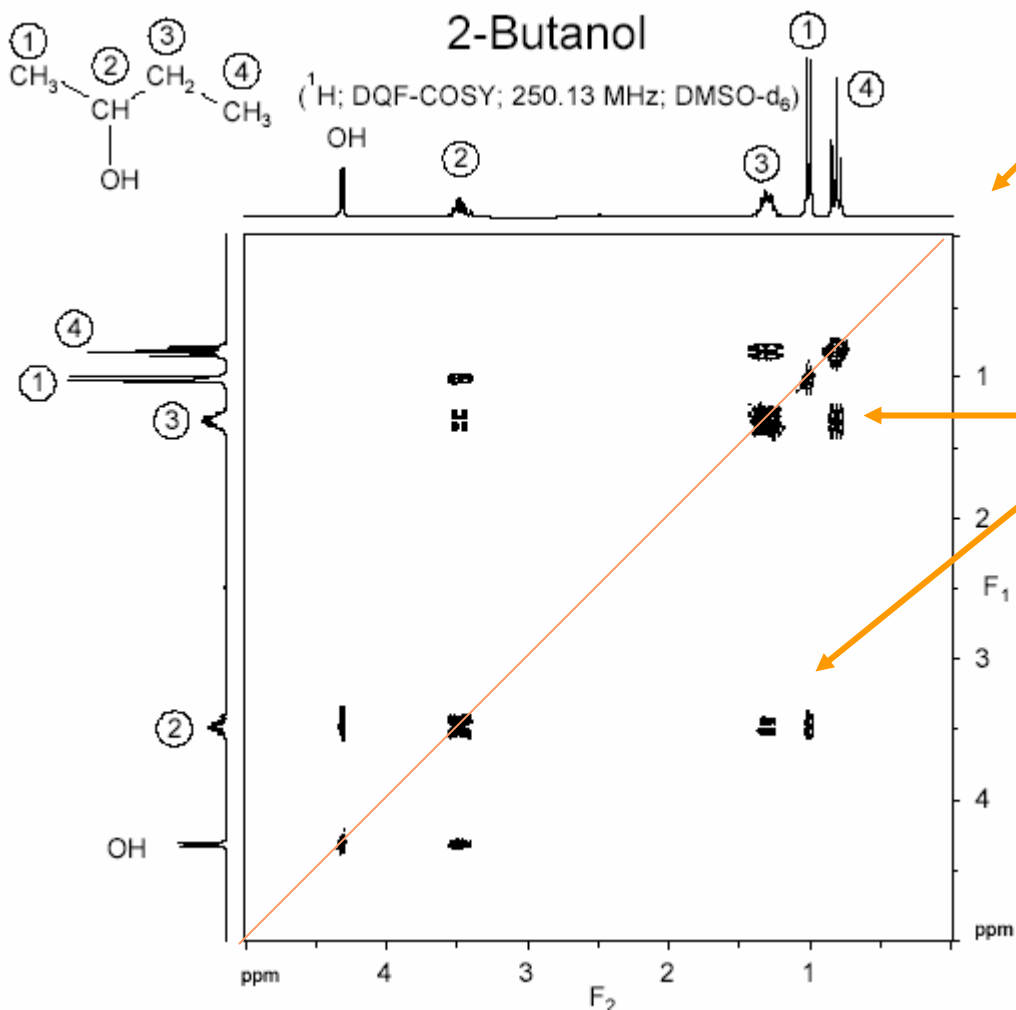
chemical shift: $H_{\text{CS}} = \omega_I I_z$

hom. J-coupl.: $H_{\text{iso}} = 2\pi J_{12} (I_{1x}I_{2x} + I_{1y}I_{2y} + I_{1z}I_{2z})$

het. J-coupl.: $H_{\text{long}} = 2\pi J_{IS} I_z S_z$

(no relaxation considered)

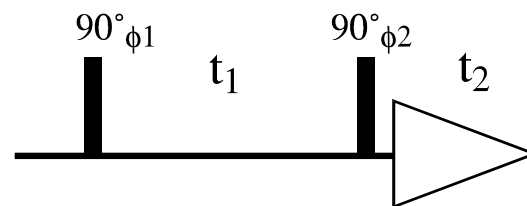
Correlation via J-Couplings: COSY



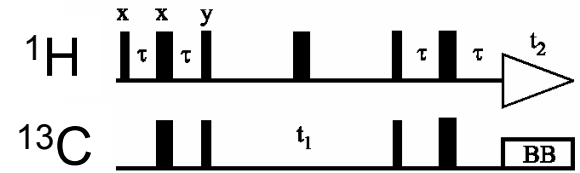
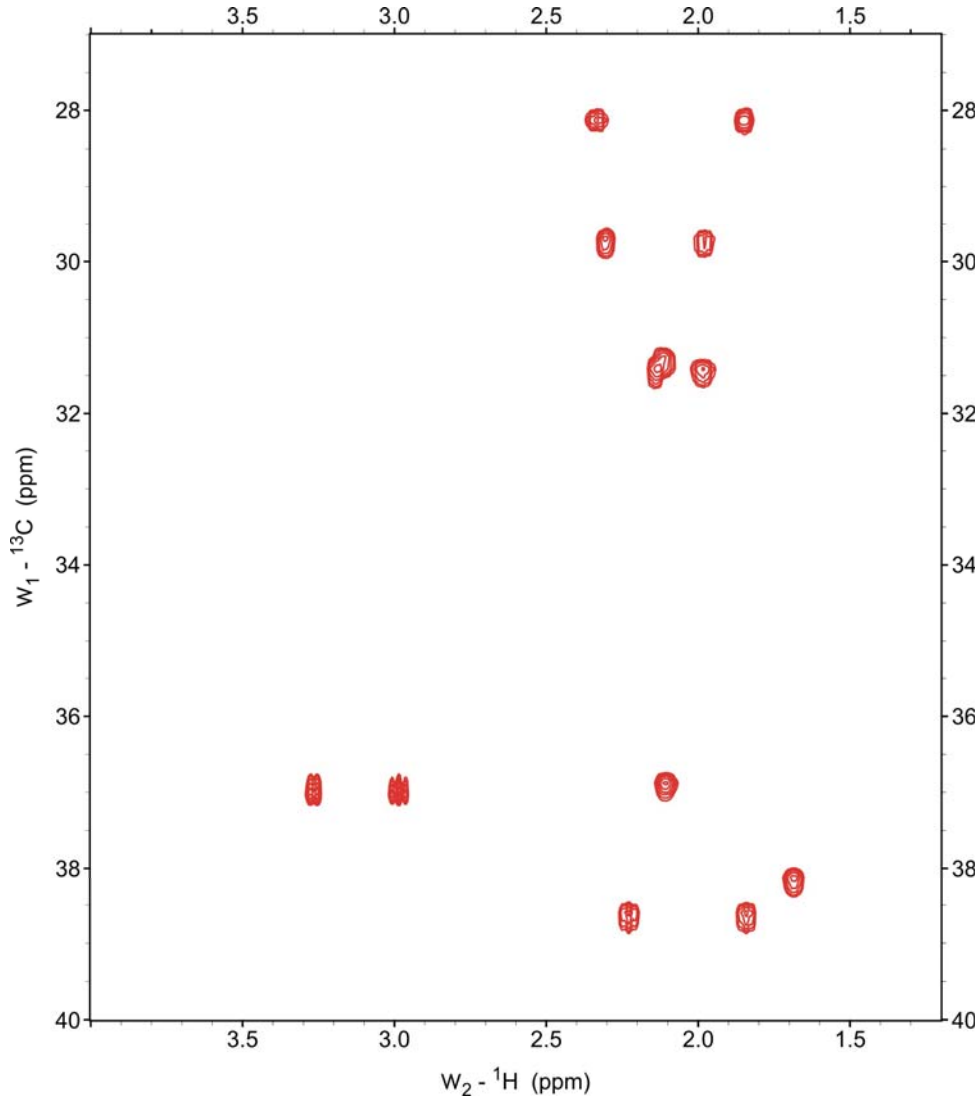
Diagonal

Cross peaks:

J-couplings between neighboring protons



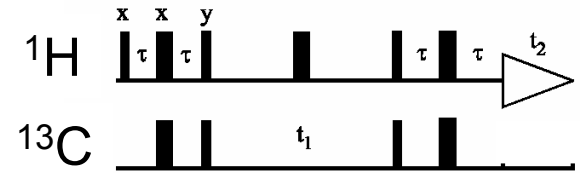
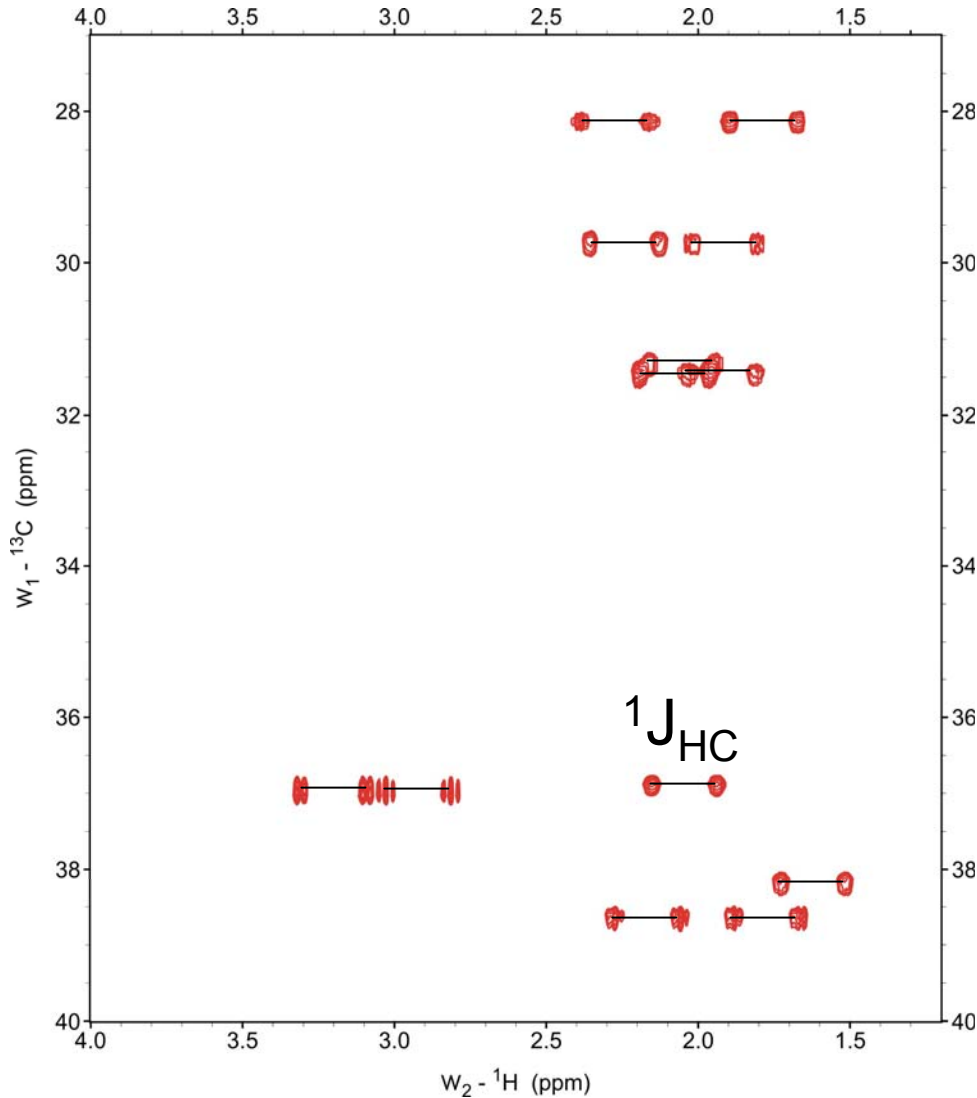
Heteronuclear Correlations: HSQC



Correlation of protons
to directly attached
 ^{13}C -atoms

with decoupling

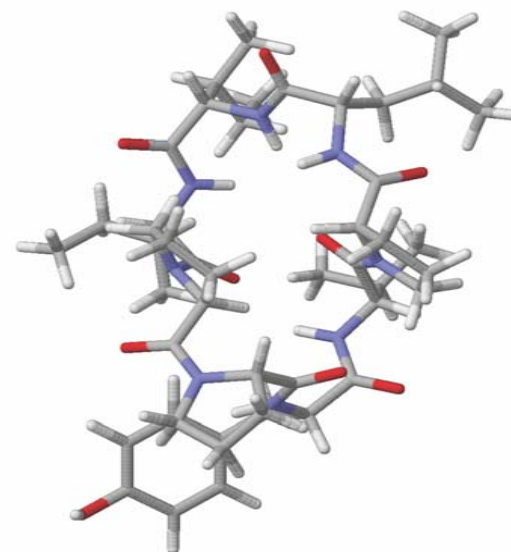
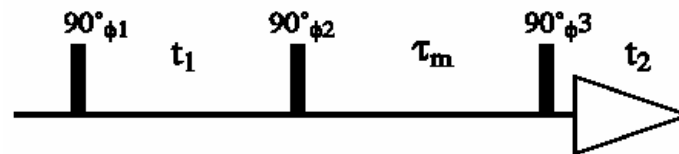
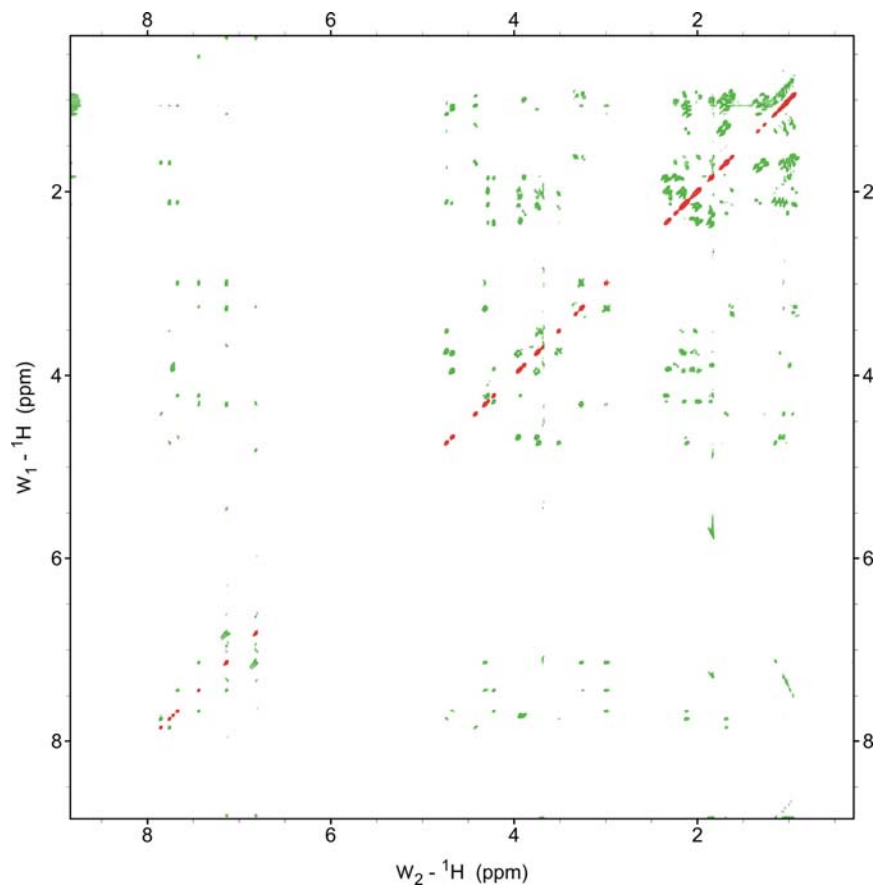
Heteronuclear Correlations: HSQC



Correlation of protons
to directly attached
 ^{13}C -atoms

without decoupling

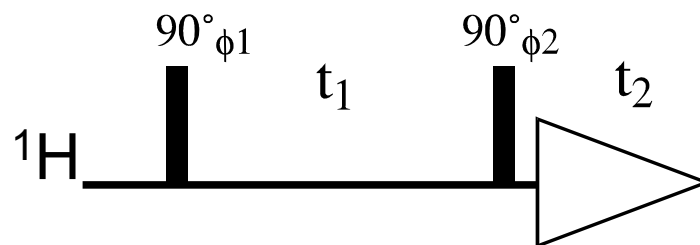
Dipole-Dipole-Relaxation: NOESY



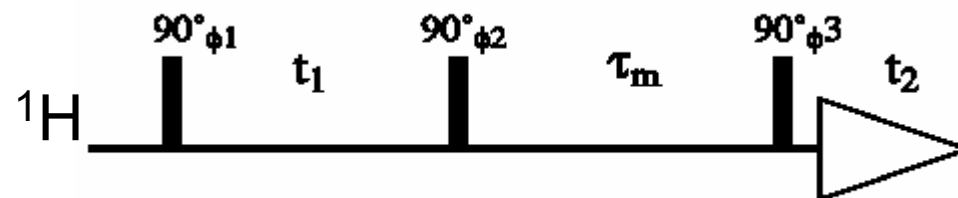
NOESY: relaxation-based transfer $\sim 1/r^6$
=> Structure calculations

Common Scheme: Coherence/Polarization Transfer

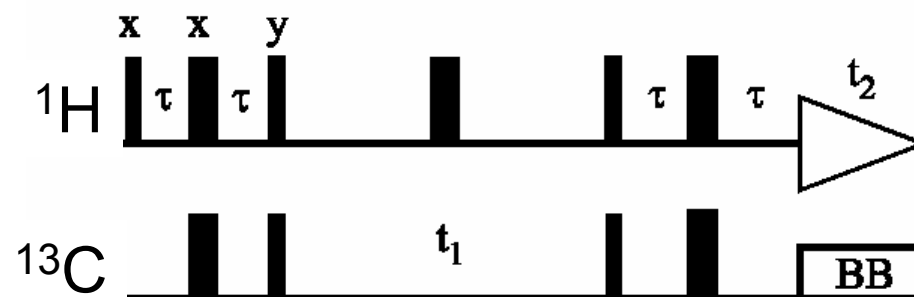
COSY



NOESY



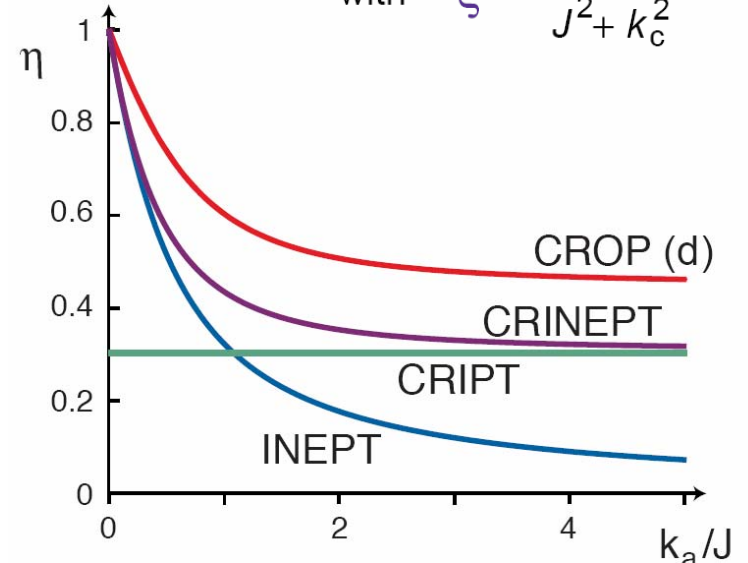
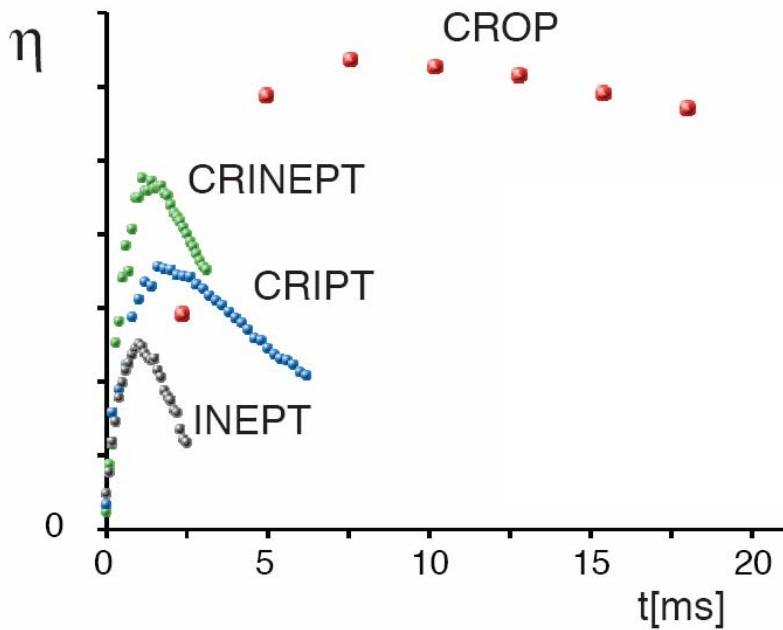
HSQC



Future Transfer Building Block: CROP

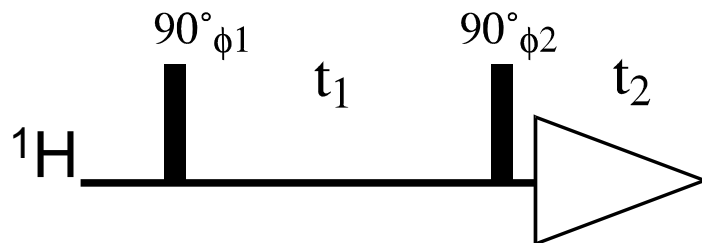
$$\eta = \sqrt{1 + \xi^2} - \xi$$

with $\xi^2 = \frac{k_a^2 - k_c^2}{J^2 + k_c^2}$

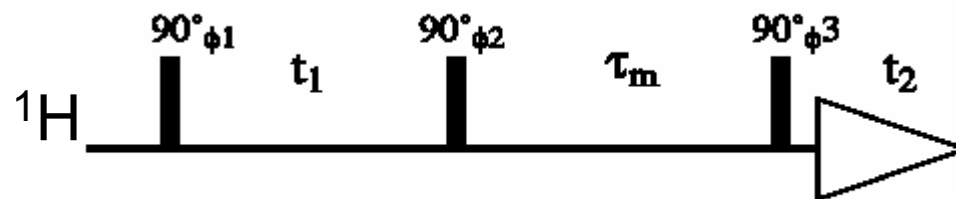


90° and 180° Pulses: Today's Work Horses

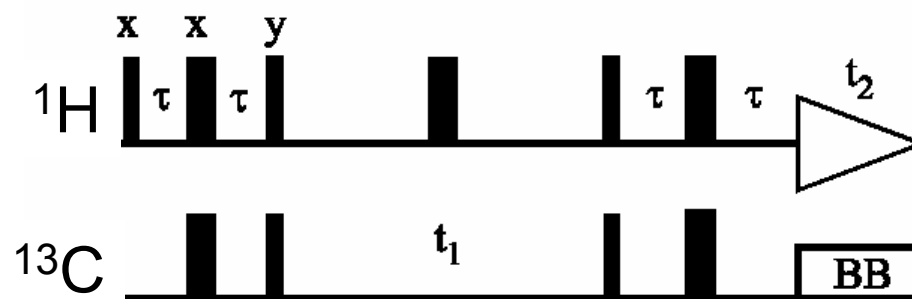
COSY



NOESY



HSQC



Why bother with NMR spectroscopy?

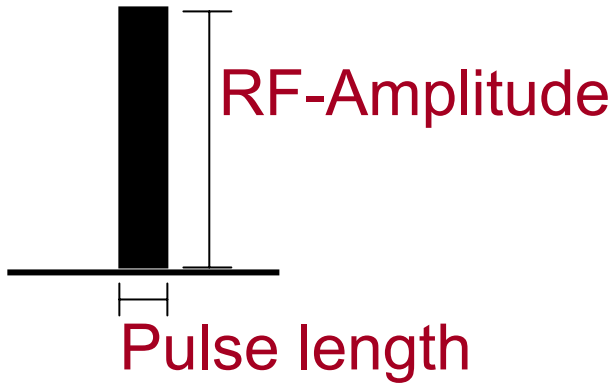
Broadband 'State-To-State' Pulses

Broadband 'Universal Rotation' Pulses

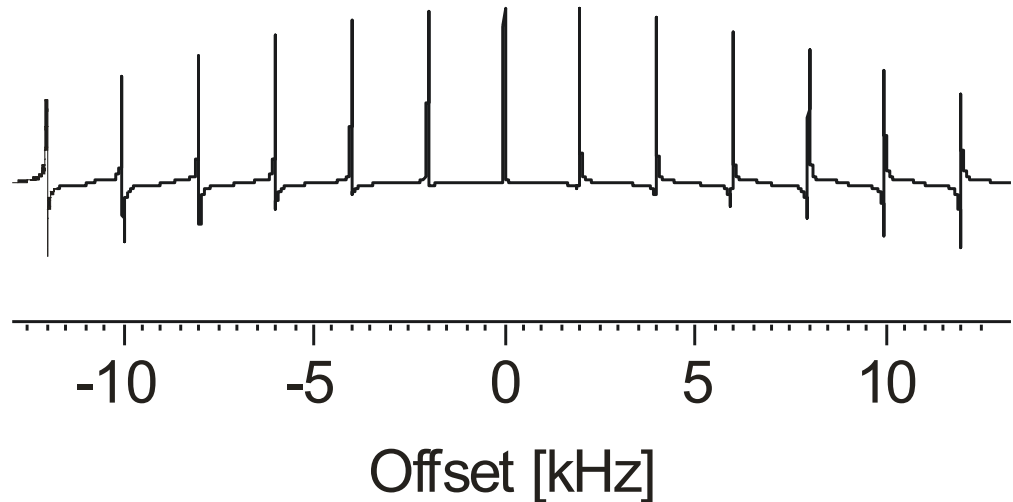
Ultrabroadband Excitation

Pattern Pulses

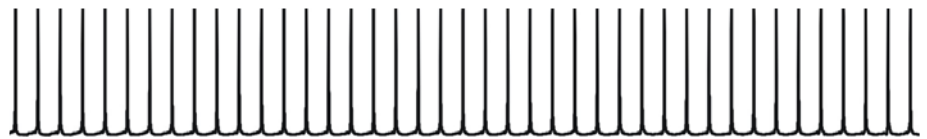
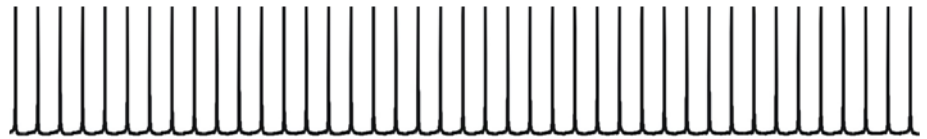
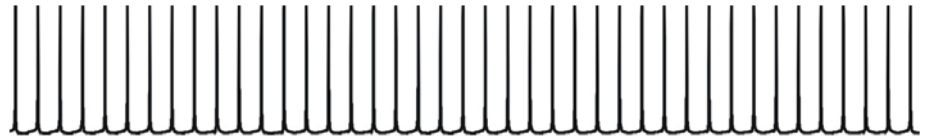
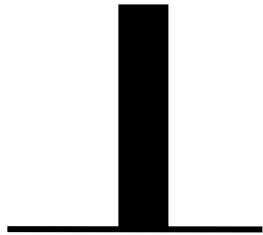
Offset-Dependence of RF-Pulses



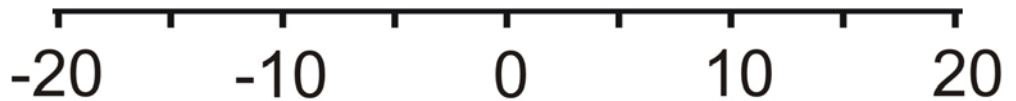
Phase distortions
and loss of signal
due to offset
(e.g. ^{13}C , ^{19}F)



„The Ideal Pulse“



Same flip angle for all offsets and RF-amplitudes



Optimization Setup

Approximation: pulse length is short
=> J-coupling / relaxation is neglected

$$H_{\text{CS}} = \omega_{\text{offs}} I_z$$

$$H_{\text{ctrl}} = \omega_{\text{RF}} = \omega_1 (\cos \varphi I_x + \sin \varphi I_y)$$

Goal: Same transfer for all $\omega_{\text{RF}} \pm \sigma_{\text{RF}}$ and ω_{offs}

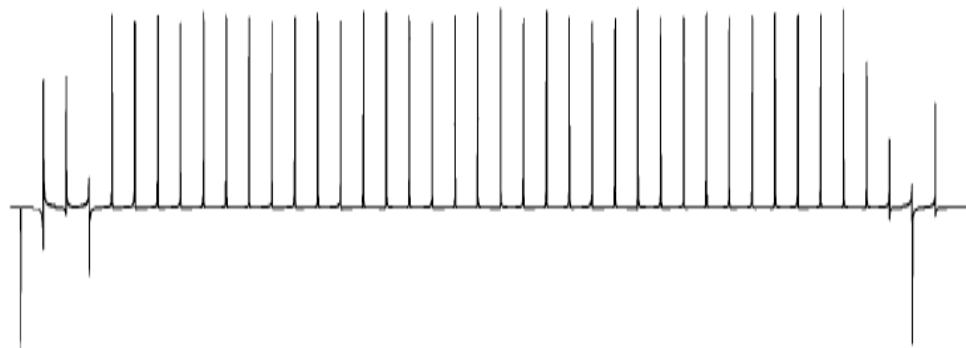
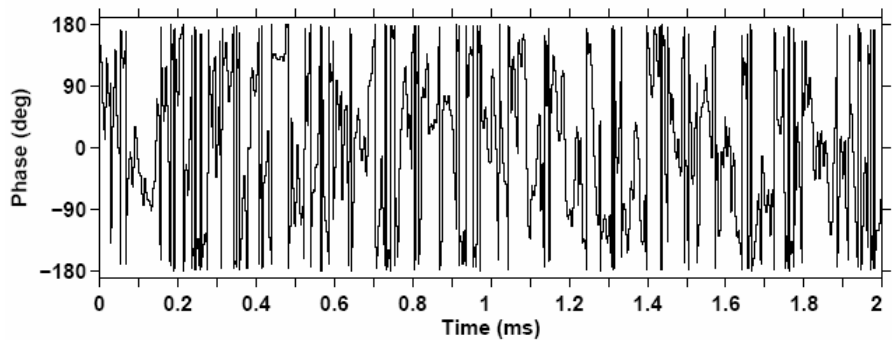
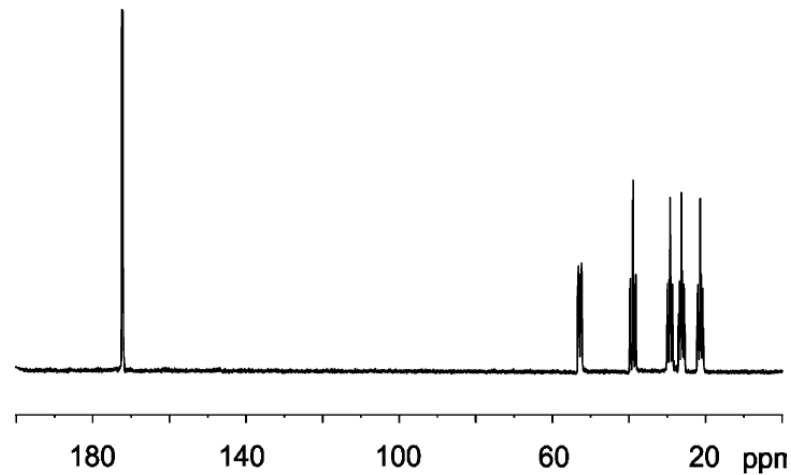
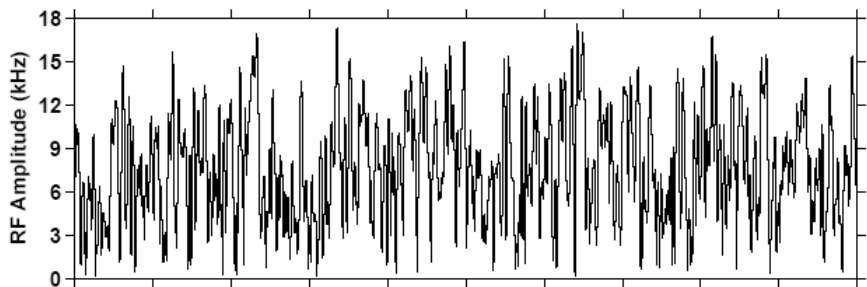
Optimization Algorithm

1. Choose an initial rf sequence $\omega_{\text{rf}}^{(0)}$.
2. Evolve \mathbf{M} forward in time starting from $\mathbf{M}(t_0)$.
3. Calculate $\Gamma(t_p) = \mathbf{M}(t_p) \times \mathbf{F}$ for all offsets and scaled rf-amplitudes and evolve it backwards in time.
4. $\omega_{\text{rf}}^{(k+1)}(t) \rightarrow \omega_{\text{rf}}^{(k)}(t) + \epsilon \cdot \overline{\Gamma(t)}$.
- 5.
- 6.
7. Repeat steps 2–6 until a desired convergence of Φ is reached.

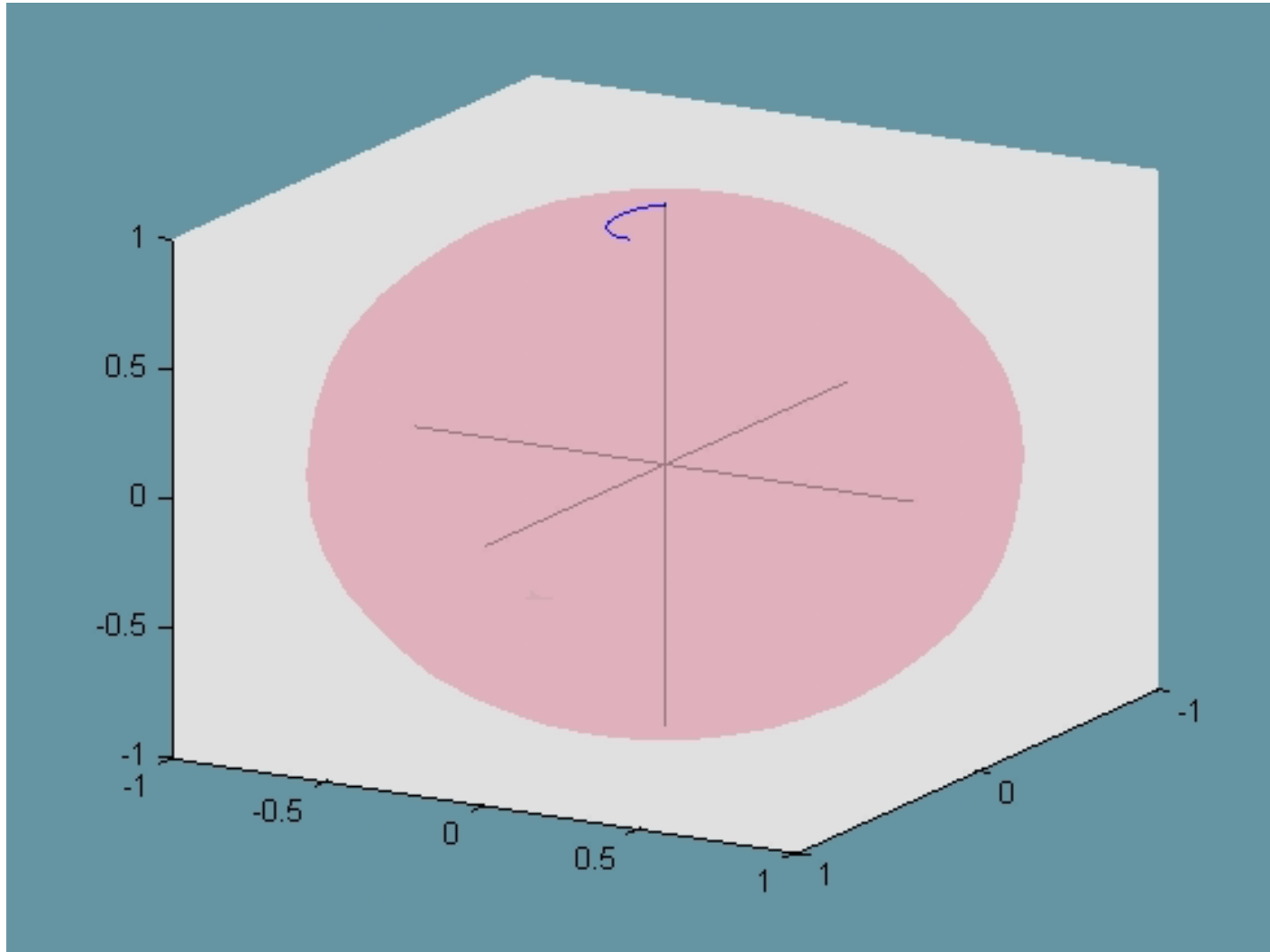
$$\mathbf{M} = (I_x, I_y, I_z)$$

$$\Gamma = \text{Gradient}$$

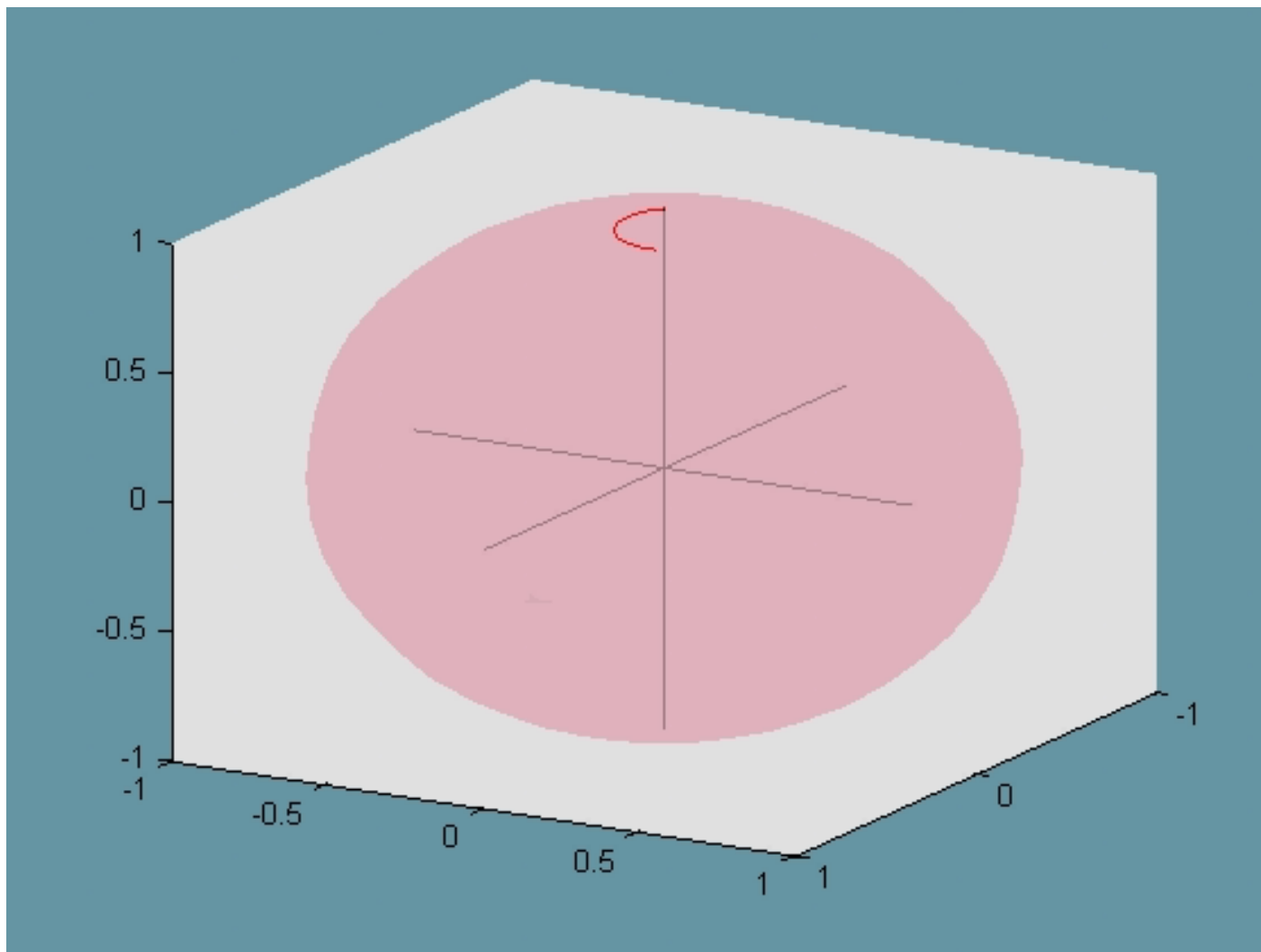
2 ms BEBOP no RF-constraints



Trajectory (0 Hz Offset)

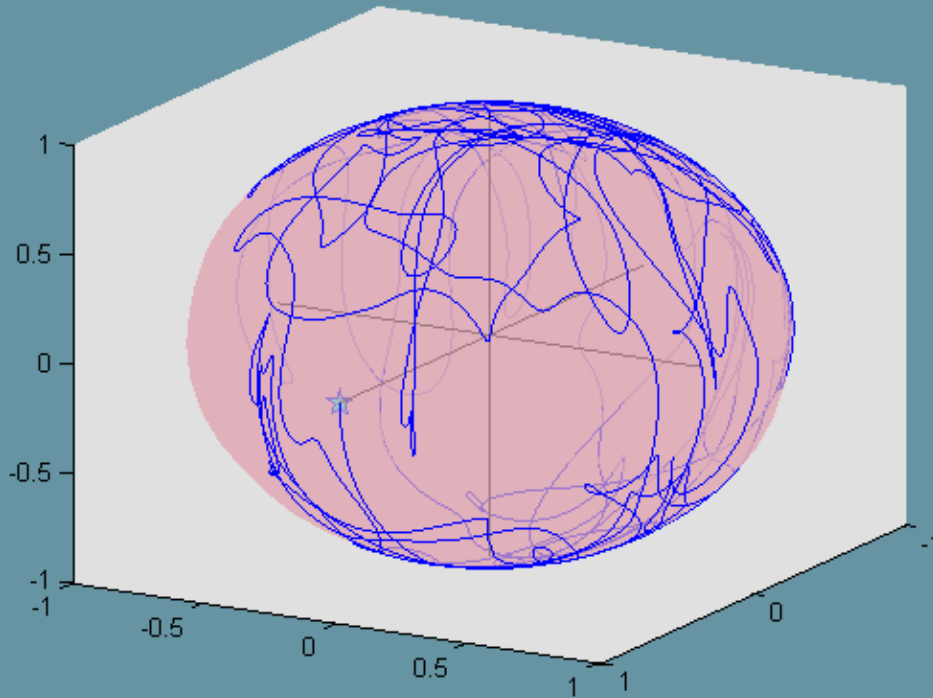


Trajectory (16 kHz Offset)



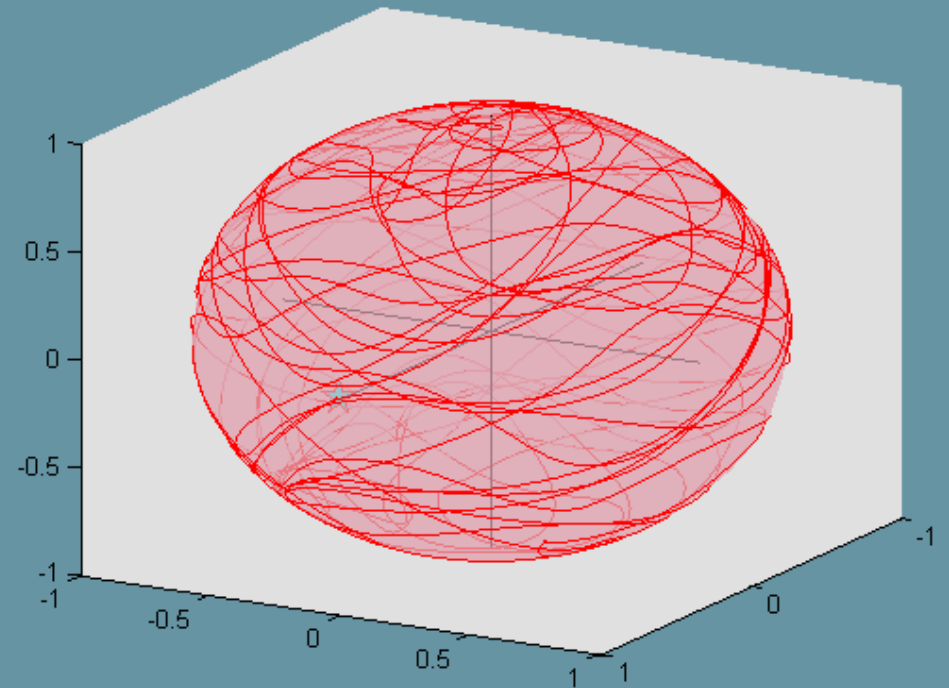
Pulse-Trajectories

$$\omega_1 = 0 \text{ Hz}$$



despite different
trajectories final
magnetization in x

$$\omega_1 = 16 \text{ kHz}$$



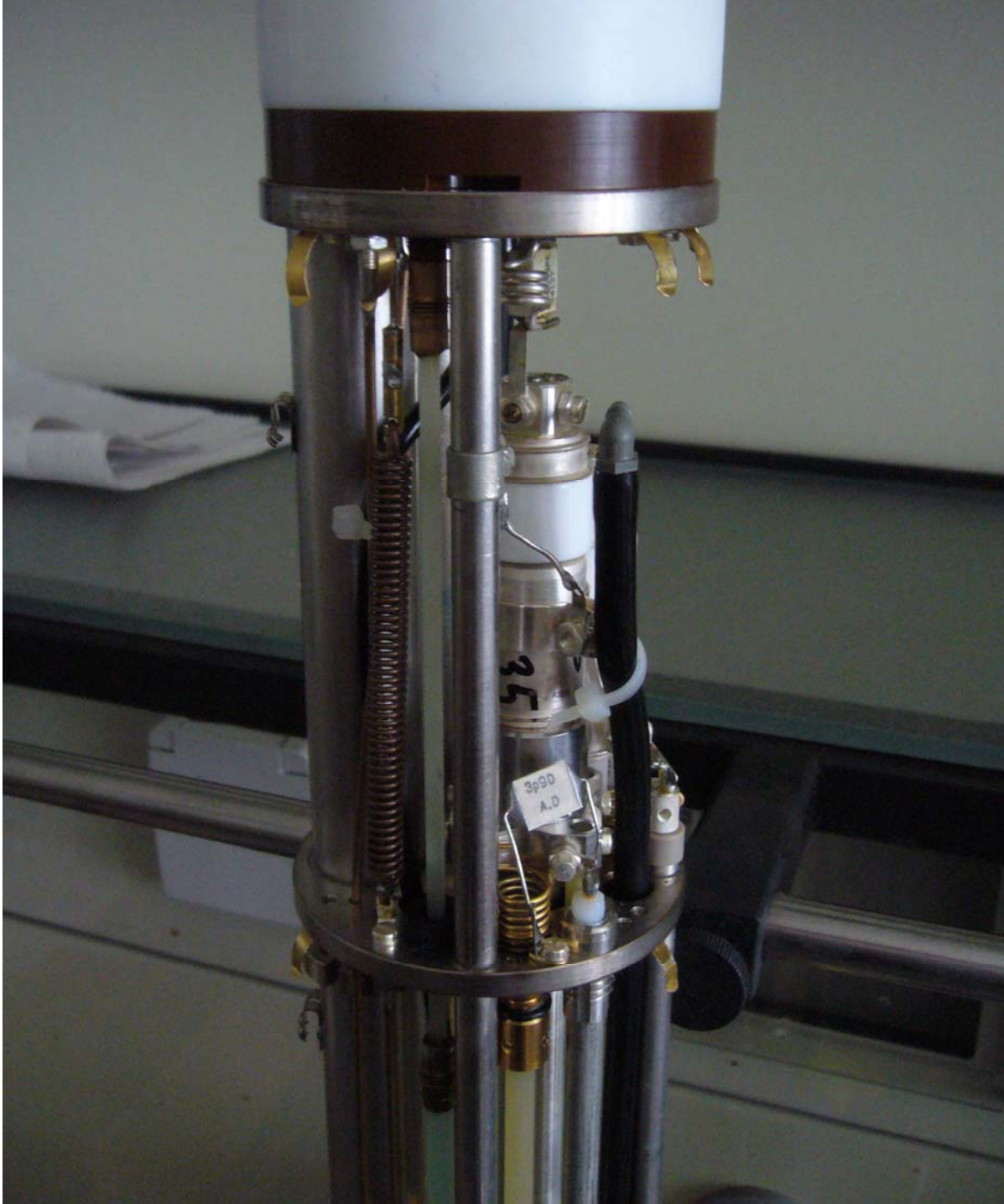
Shorter Pulses ?

Shorter Pulses: RF-constraints Needed in Optimization

Max. RF-amplitude !

&

Max. RF-energy !



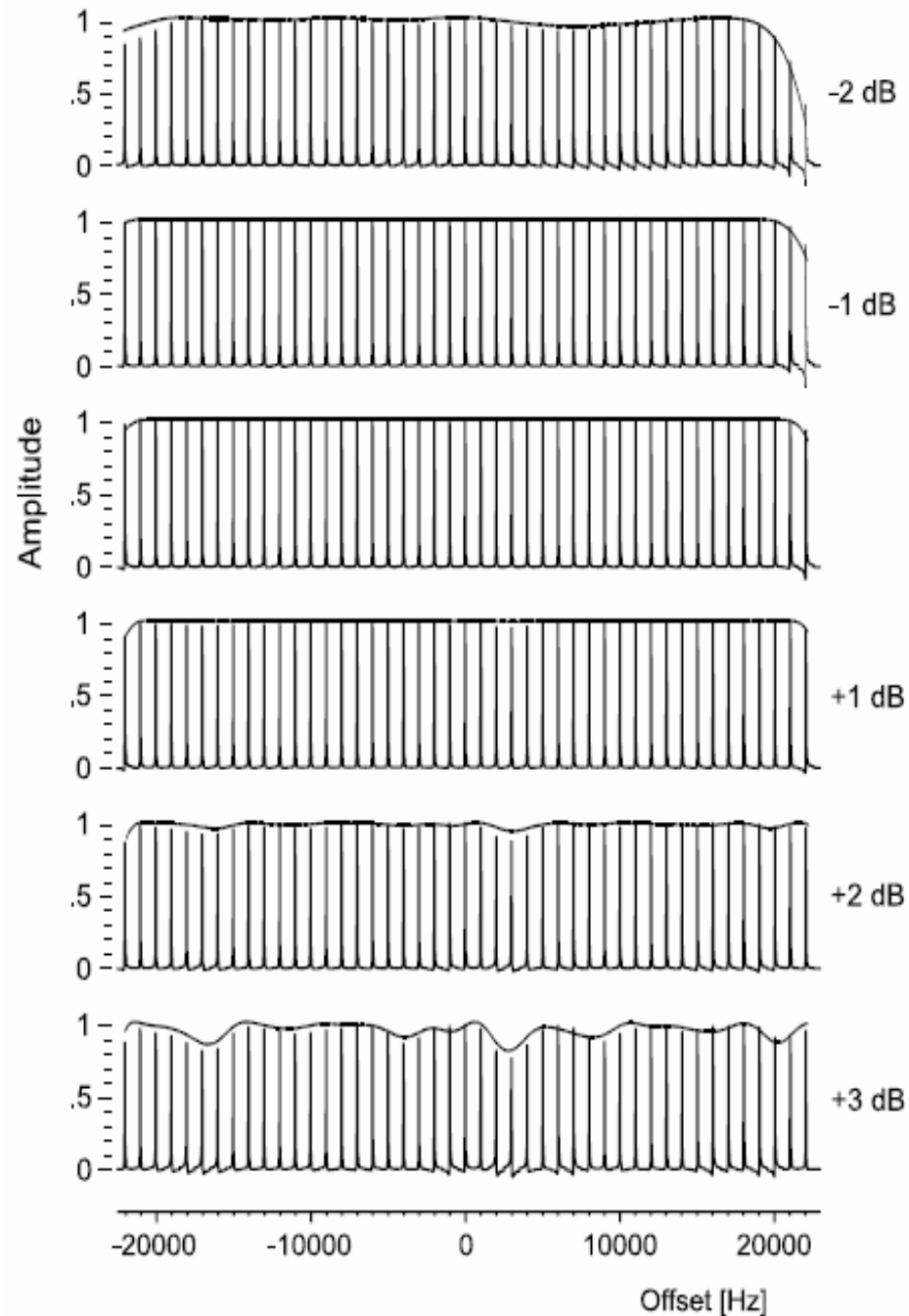
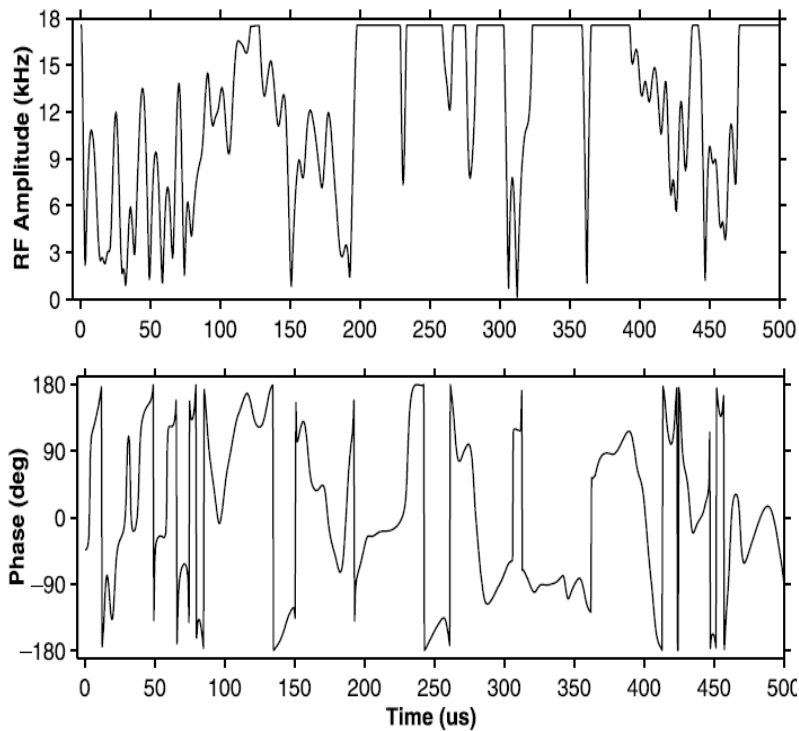
Modified Algorithm

1. Choose an initial rf sequence $\omega_{\text{rf}}^{(0)}$.
2. Evolve \mathbf{M} forward in time starting from $\mathbf{M}(t_0)$.
3. Calculate $\Gamma(t_p) = \mathbf{M}(t_p) \times \mathbf{F}$ for all offsets and scaled rf-amplitudes and evolve it backwards in time.
4. $\omega_{\text{rf}}^{(k+1)}(t) \rightarrow \omega_{\text{rf}}^{(k)}(t) + \epsilon \cdot \overline{\Gamma}(t)$.
5. Calculate $\bar{P} = \frac{1}{t_p} \int_{t_0}^{t_p} dt (\omega_1(t))^2$.
6. If $\bar{P} > P_{\text{max}}$, set $\omega_1(t) \rightarrow \omega_1(t) \cdot \sqrt{\frac{P_{\text{max}}}{\bar{P}}}$.
7. Repeat steps 2–6 until a desired convergence of Φ is reached.

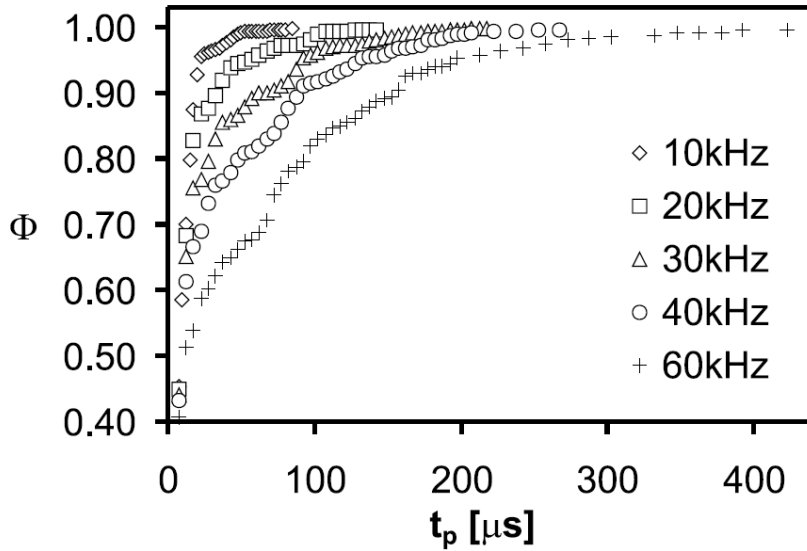
or for max. RF-amplitude:

5./6. If $\omega_1(t) > \omega_{\text{max}}$ set $\omega_1(t) = \omega_{\text{max}}$

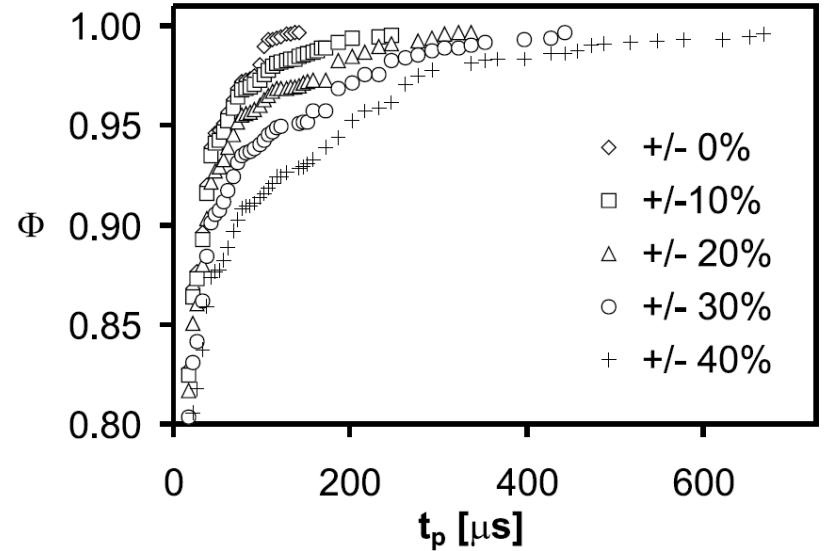
500 μ s BEBOP with max. Ampl.



Limits of Excitation



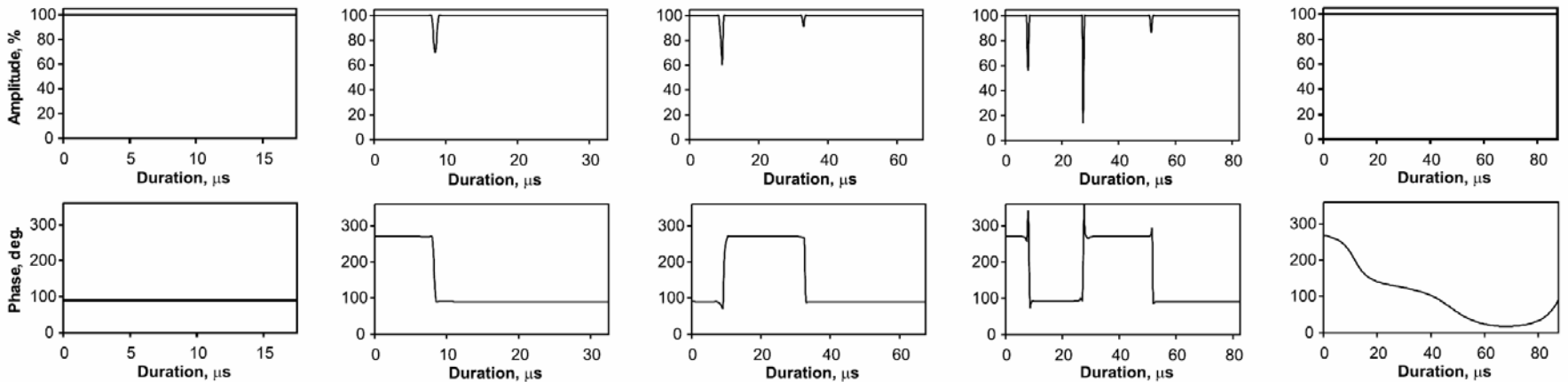
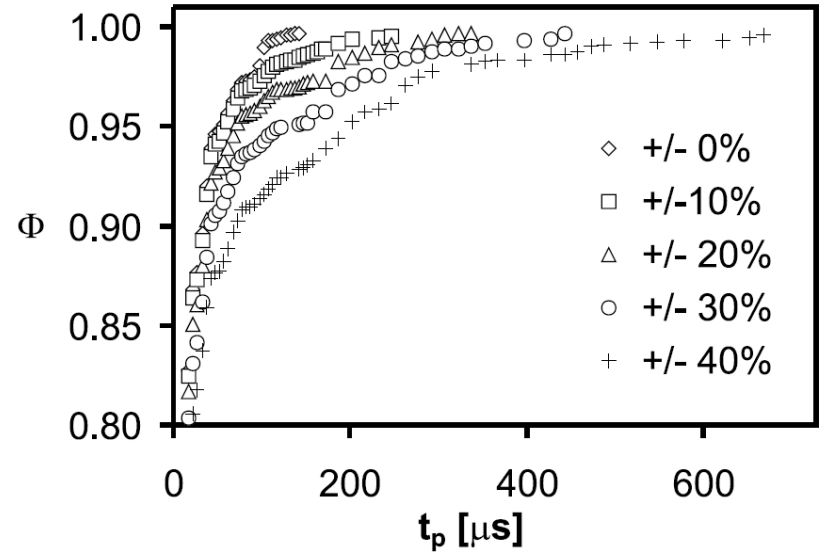
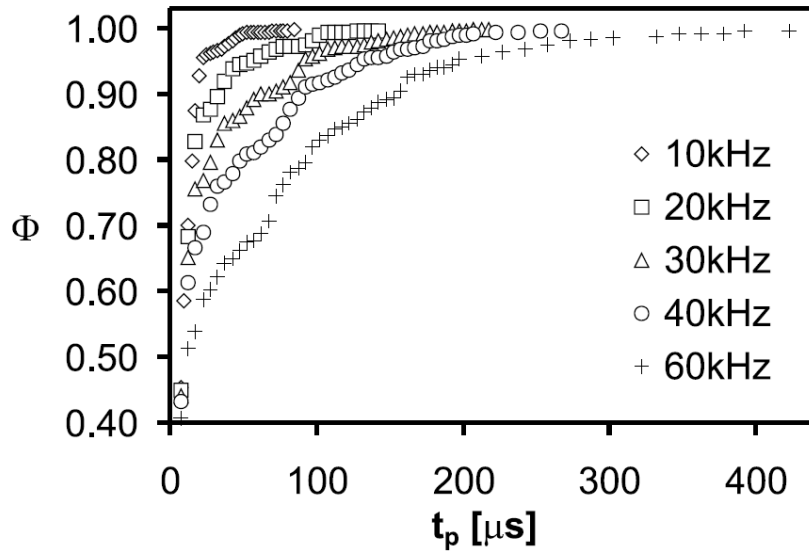
Offset



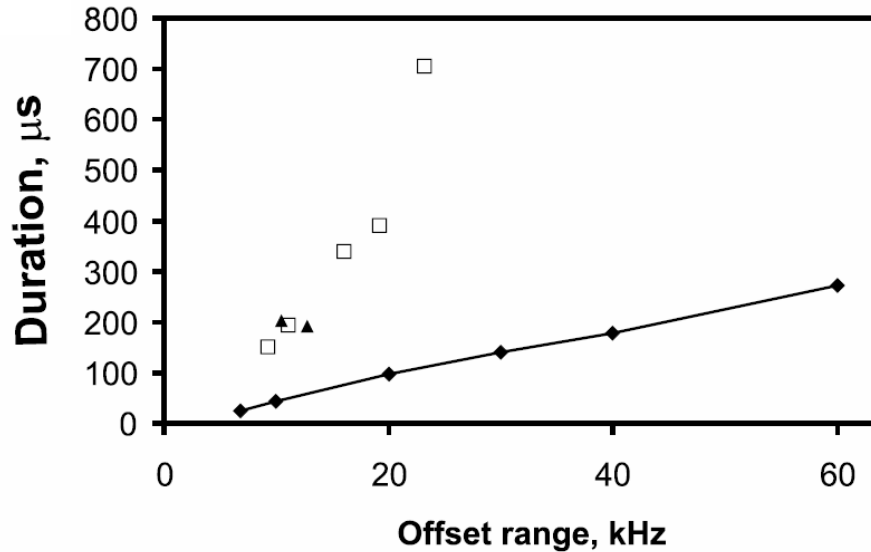
B_1 -Inhomogeneity

RF-Limit: 10 kHz

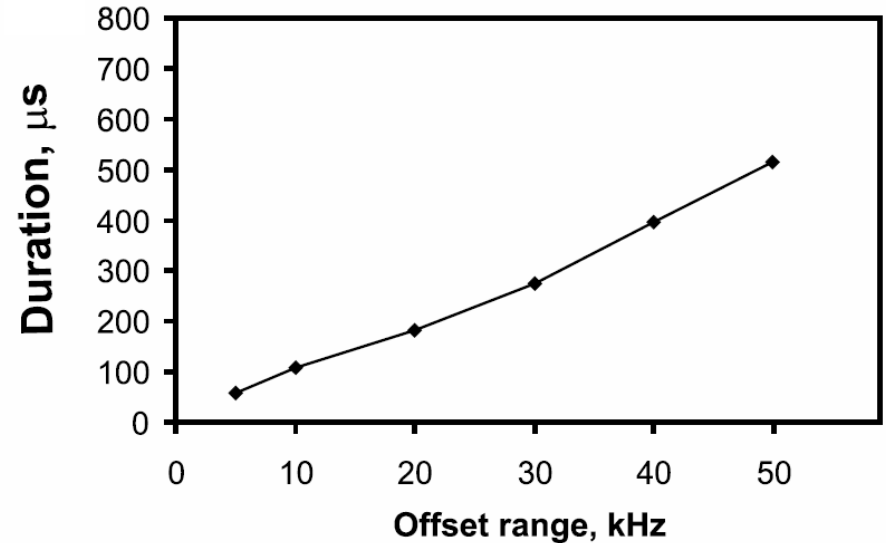
Limits of Excitation



Limits of Excitation



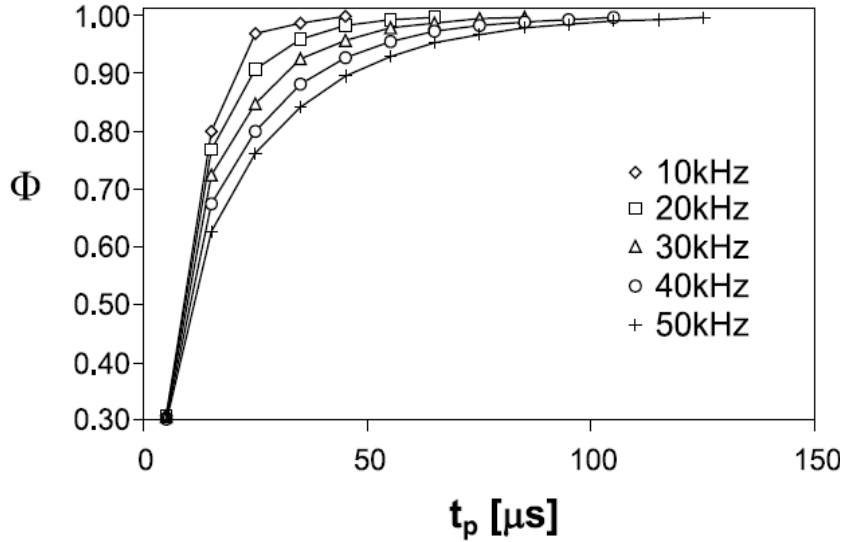
$\pm 0\% B_1$



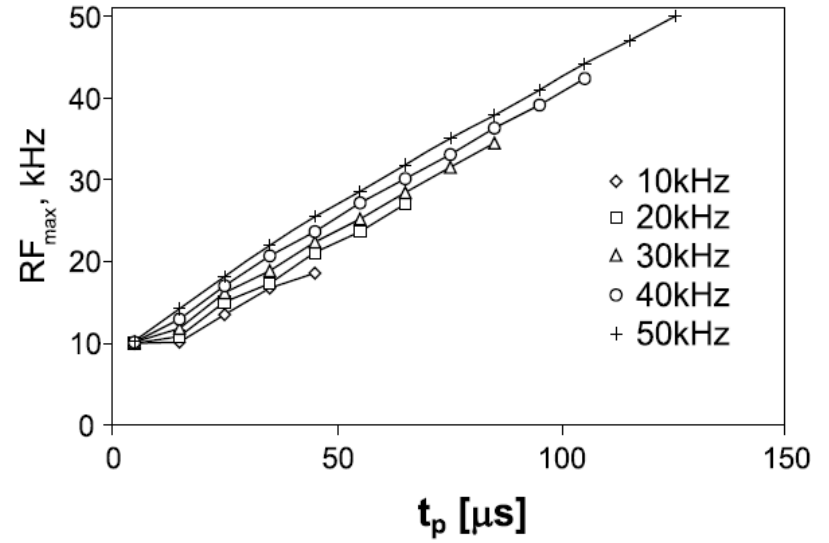
$\pm 20\% B_1$

Comparison with other excitation pulses

RF-Energy Limits of Excitation



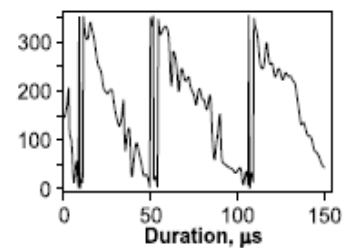
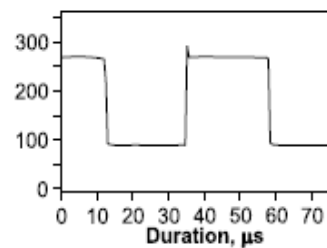
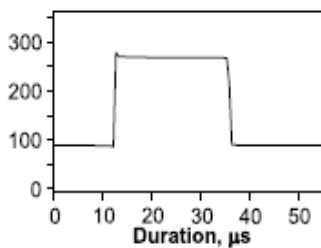
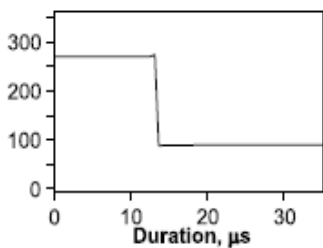
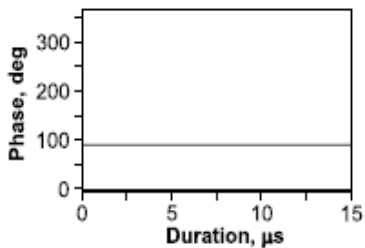
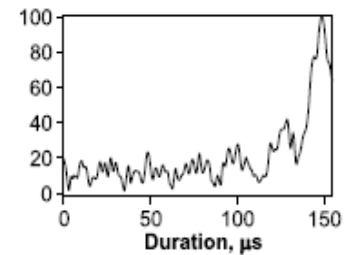
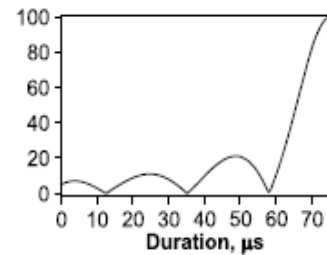
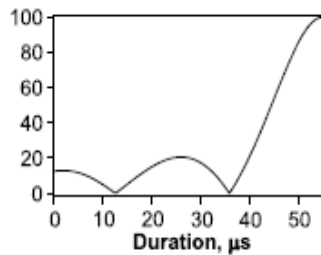
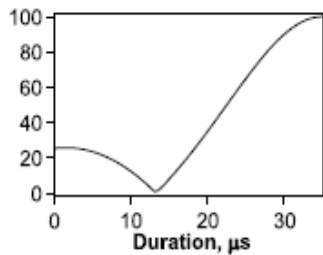
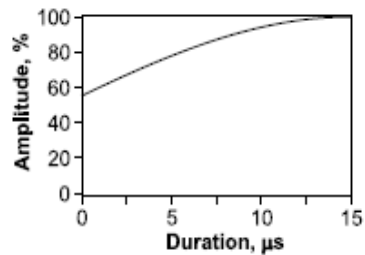
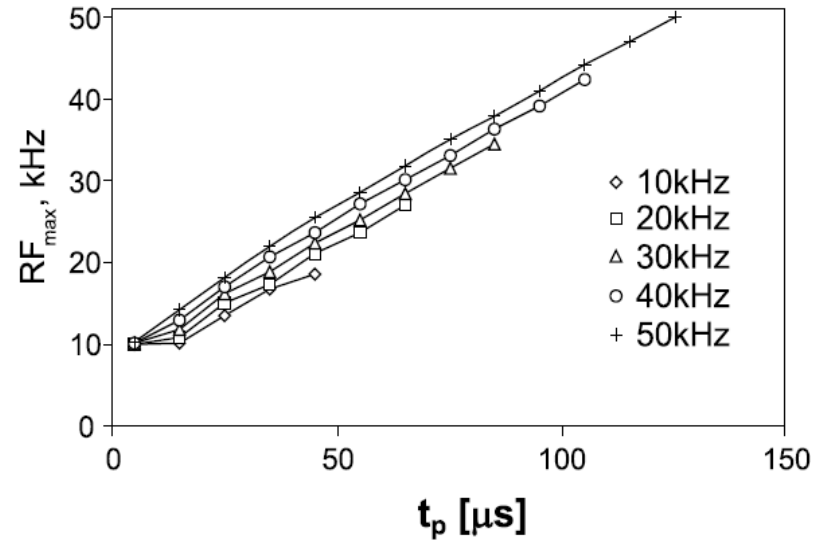
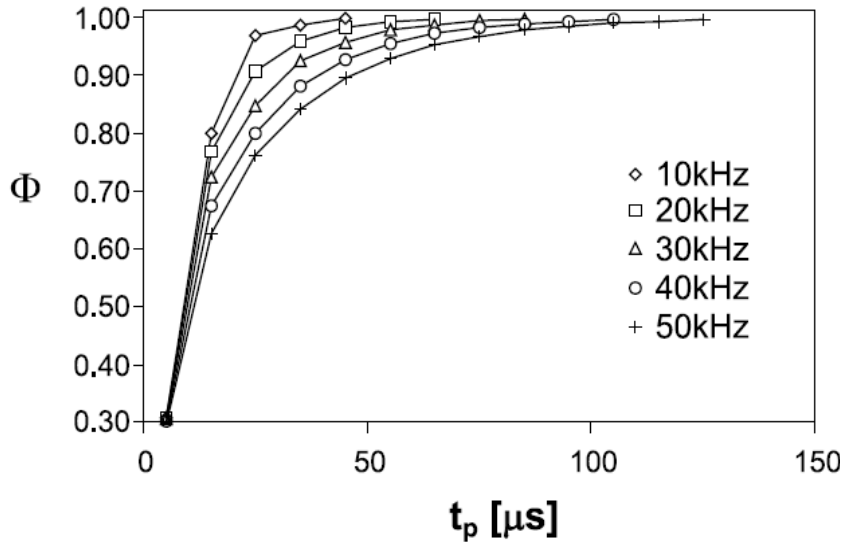
Offset



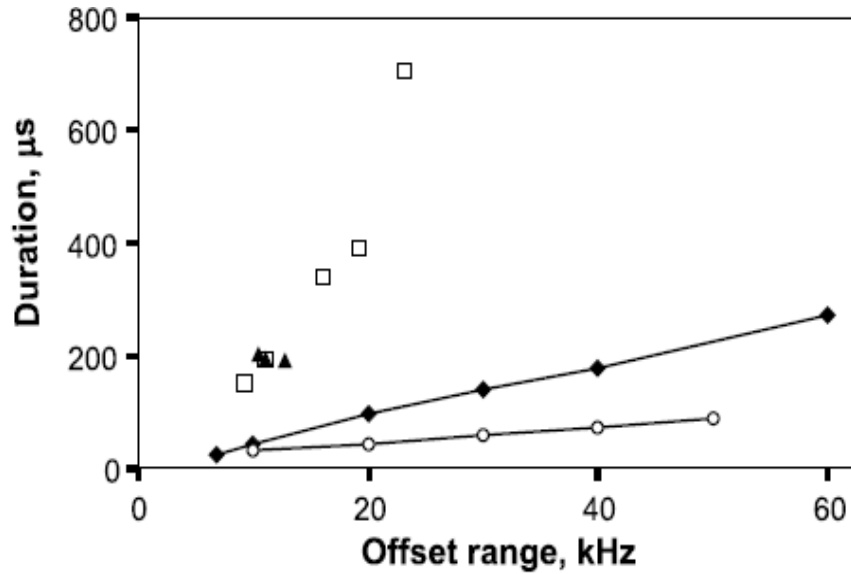
max. ampl.

restricted to RF-energy of const. ampl. 10 kHz pulse

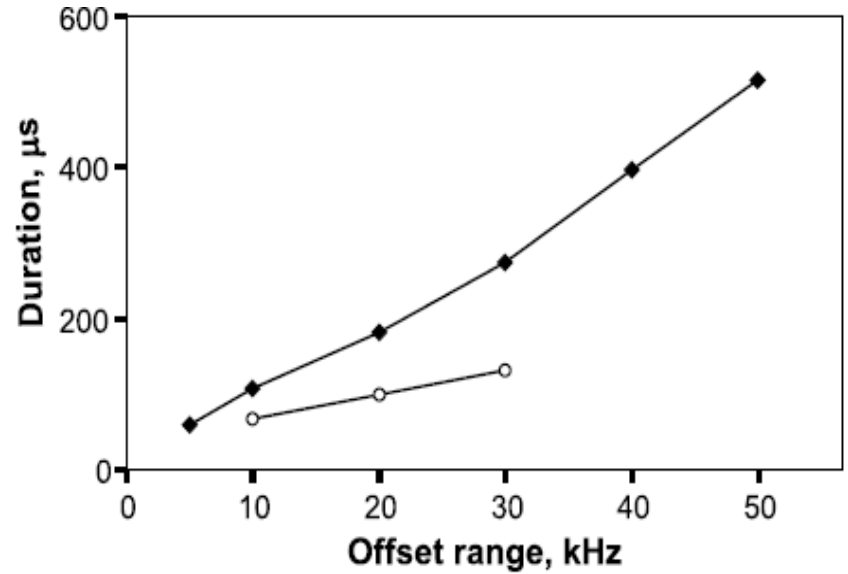
RF-Energy Limits of Excitation



RF-Energy Limits of Excitation

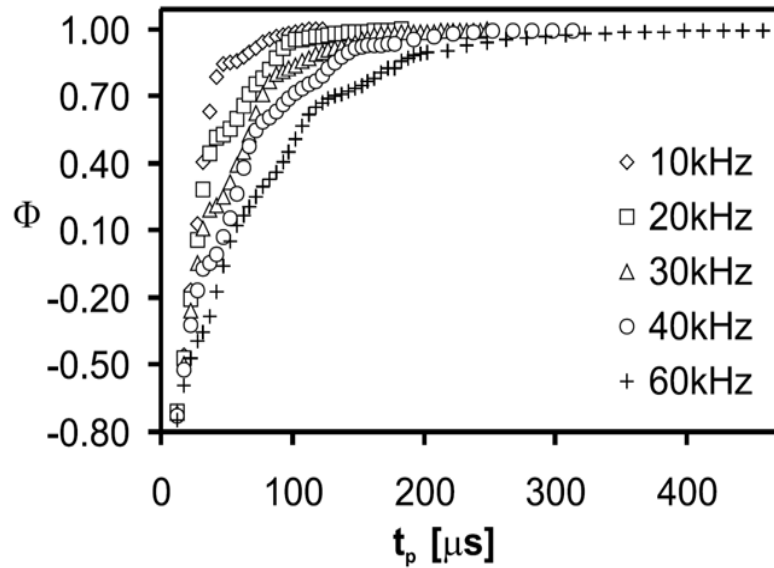


$\pm 0\% B_1$

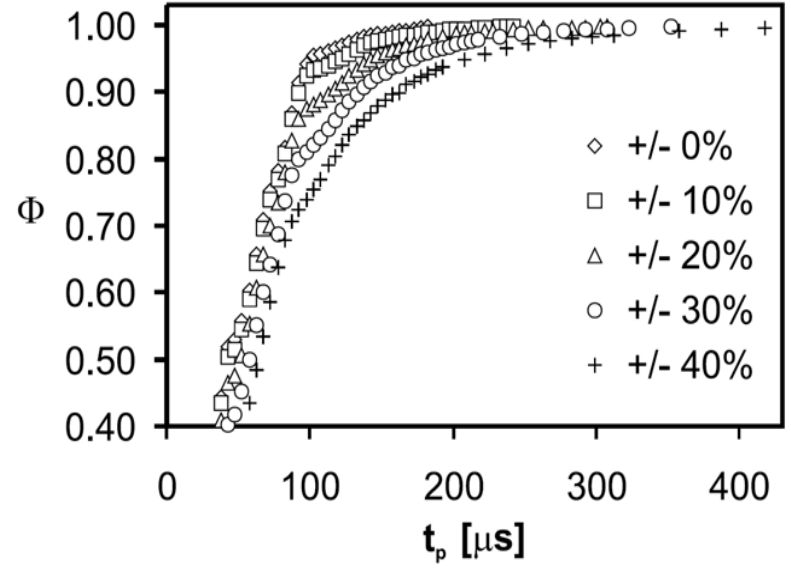


$\pm 20\% B_1$

Limits of Inversion



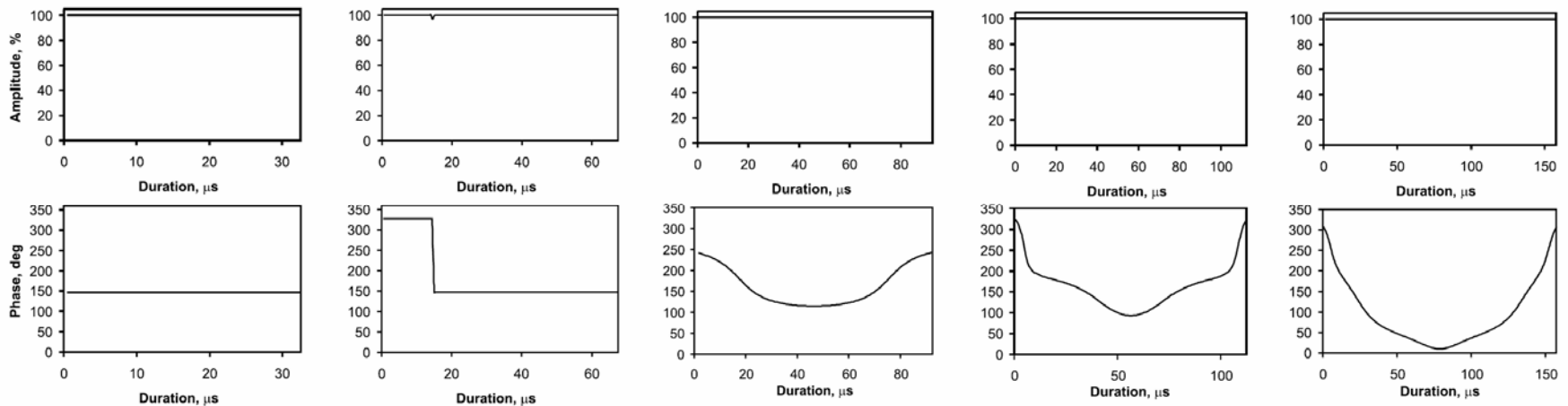
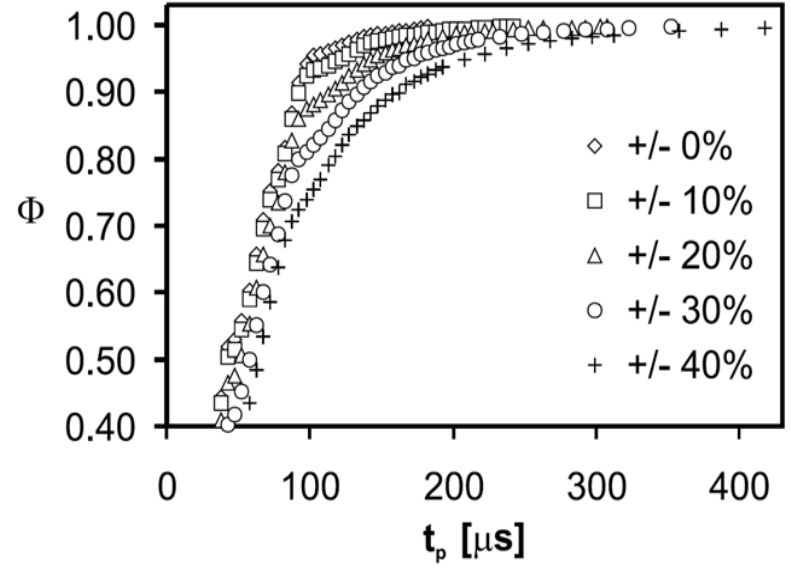
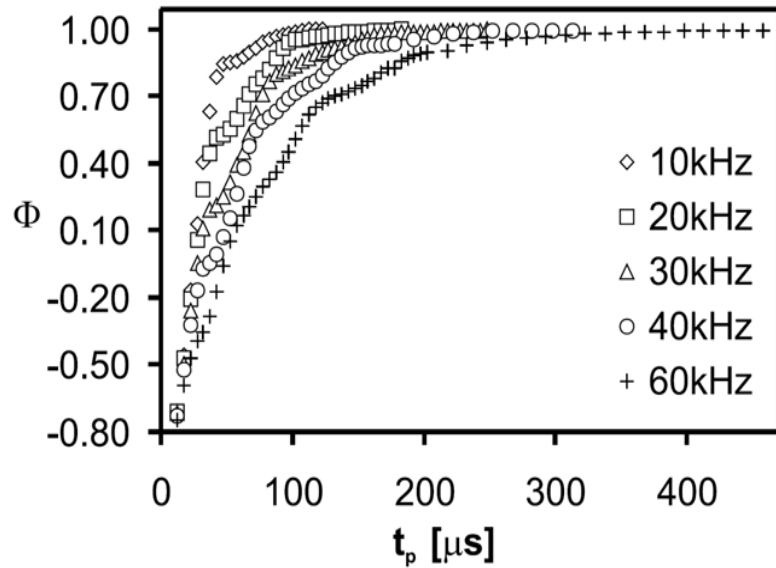
Offset



B_1 -Inhomogeneity

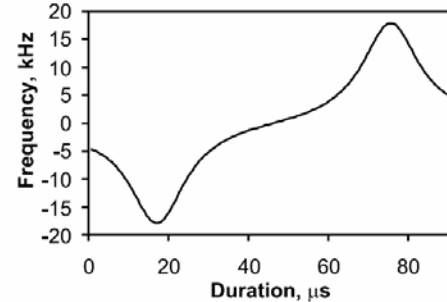
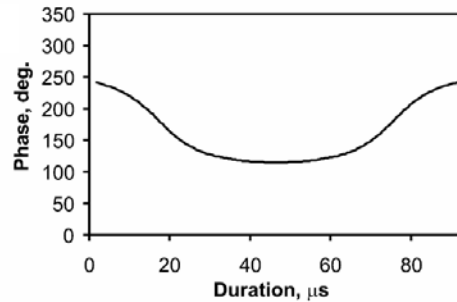
RF-Limit: 10 kHz

Limits of Inversion

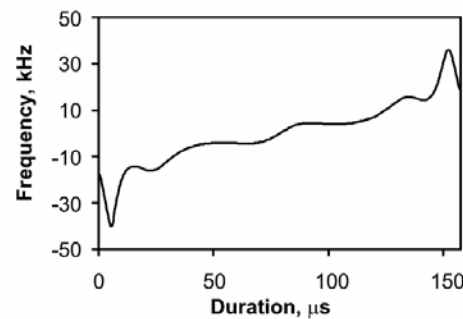
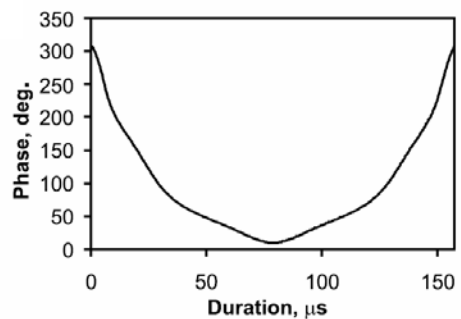
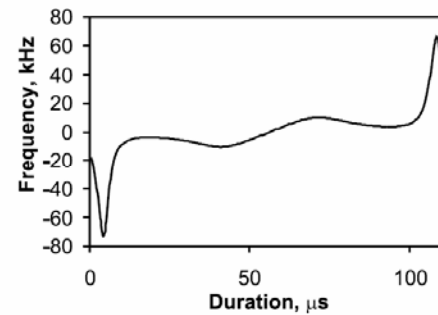
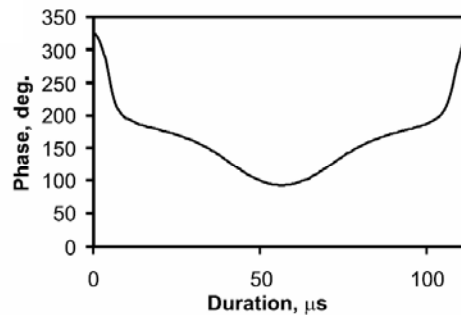


„Half-adiabatic“ Inversion Pulses

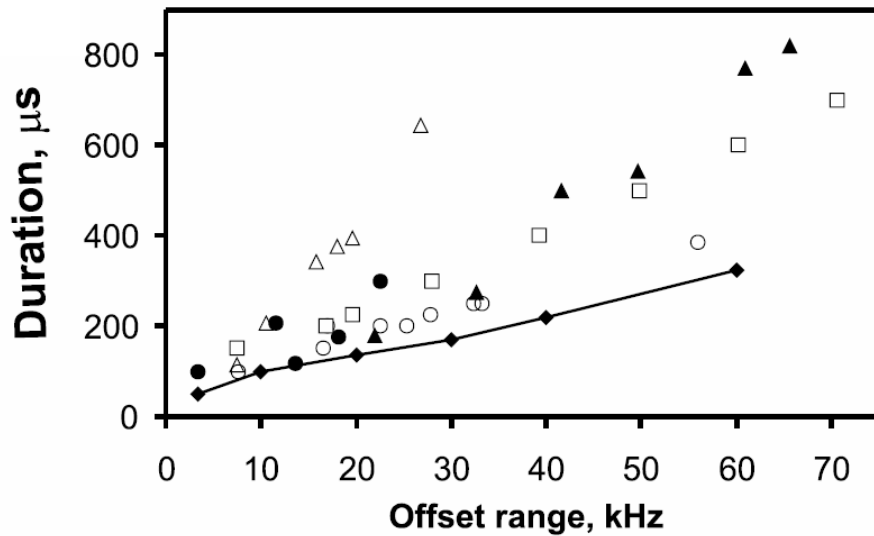
Phase



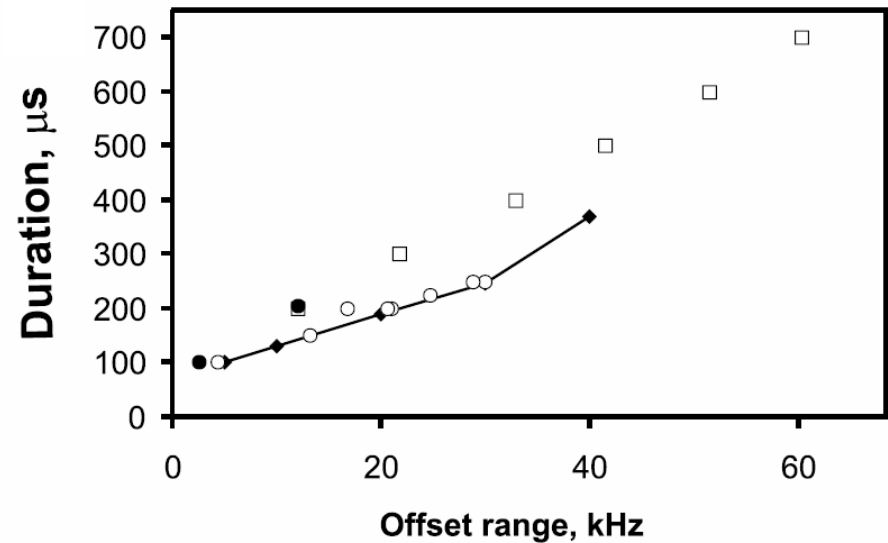
Frequency



Limits of Inversion



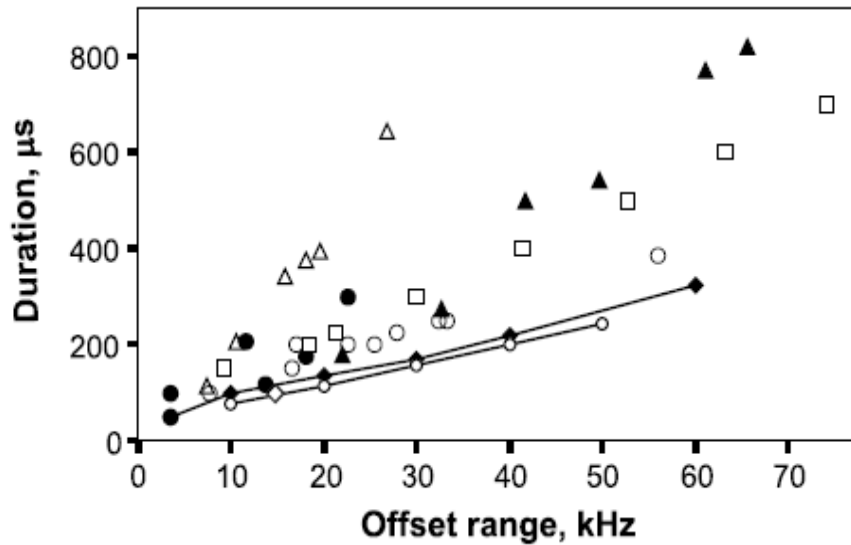
$\pm 0\% B_1$



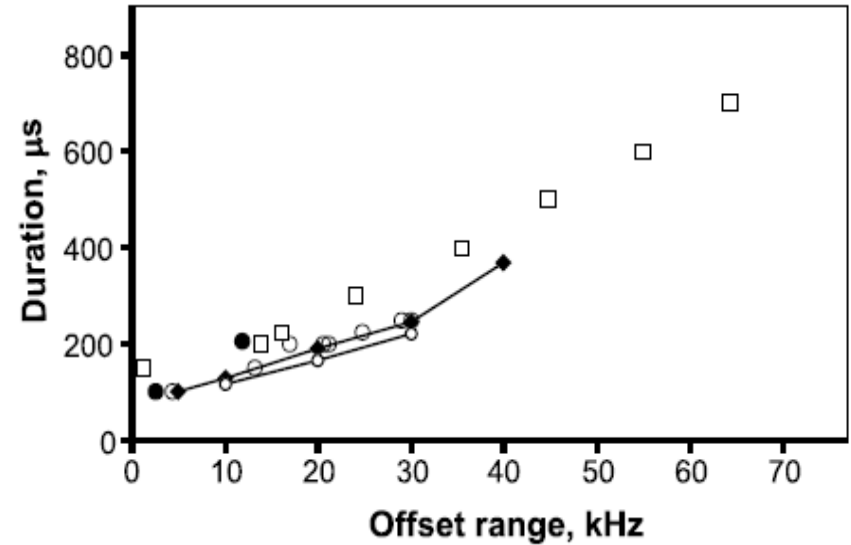
$\pm 20\% B_1$

Comparison with other inversion pulses

Limits of Inversion



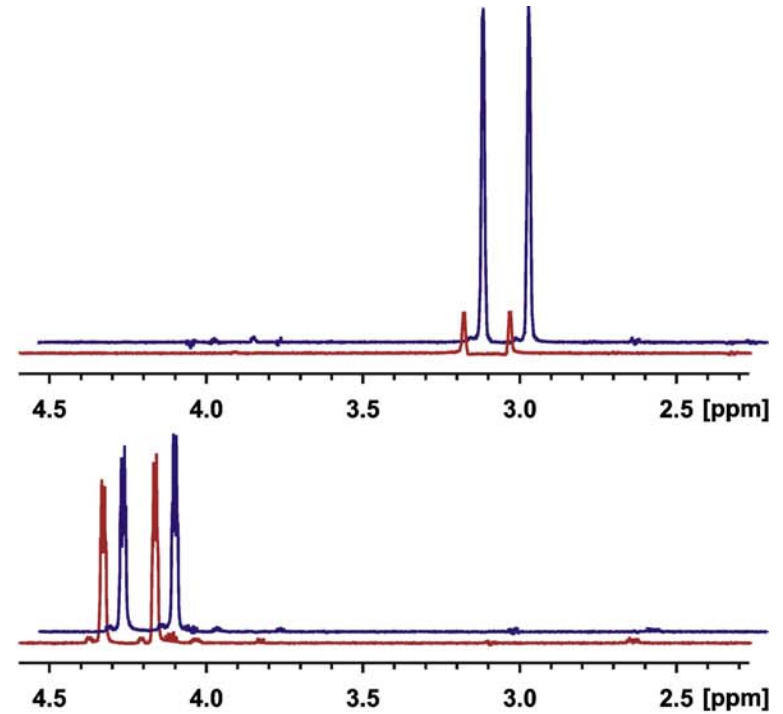
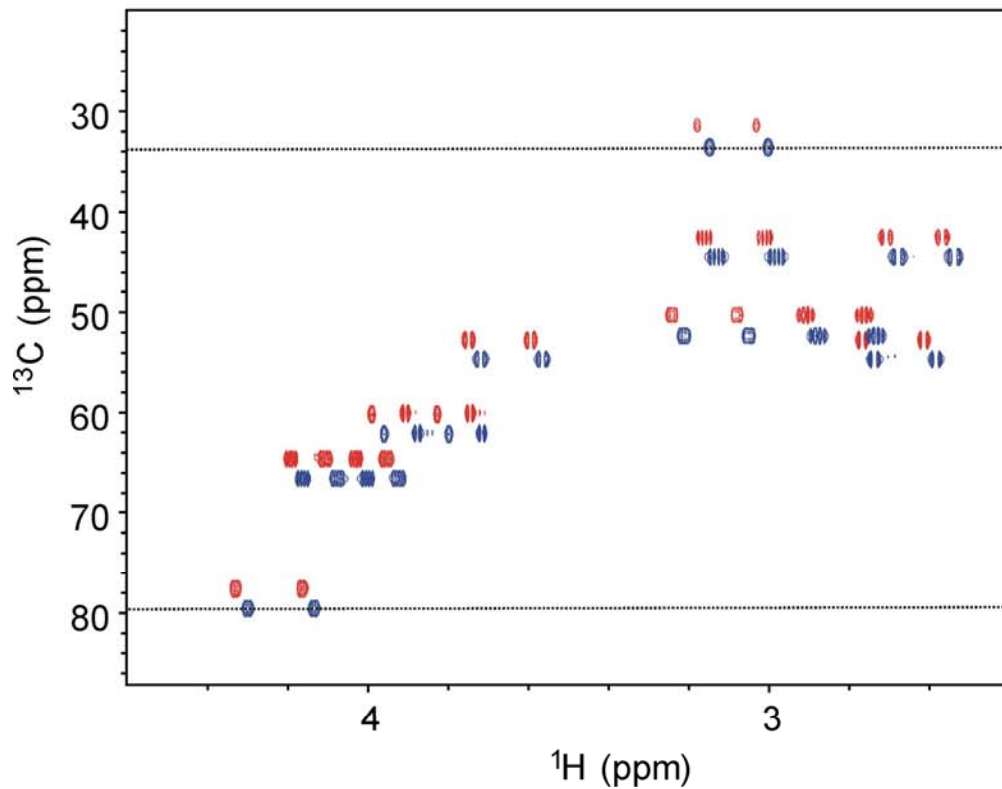
$\pm 0\% B_1$



$\pm 20\% B_1$

Comparison with other inversion pulses

BEBOP/BIBOP and hard Pulses



CLIP-HSQC (900MHz) **with** and **without** BEBOP/BIBOP on ^{13}C

Why bother with NMR spectroscopy?

Broadband 'State-To-State' Pulses

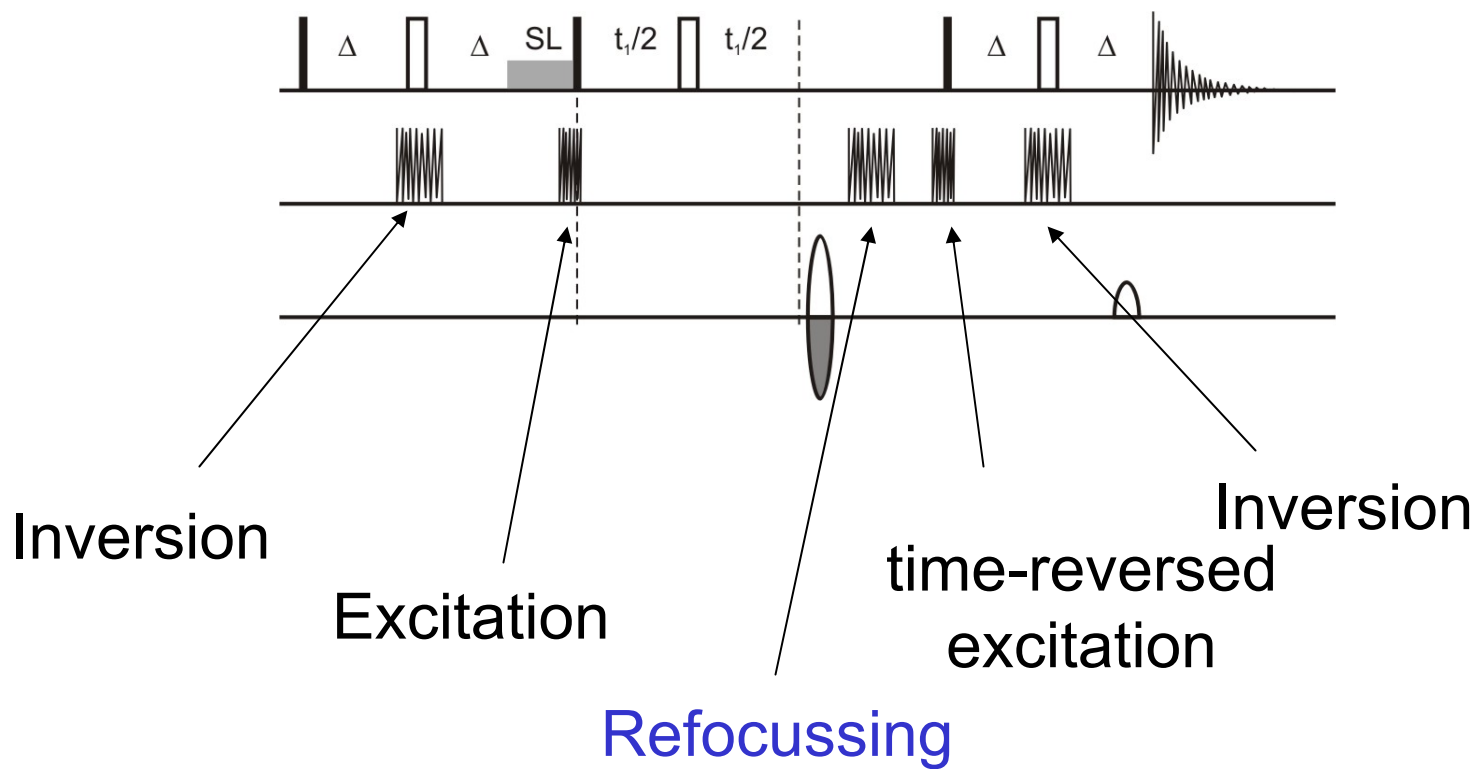
Broadband 'Universal Rotation' Pulses

Ultrabroadband Excitation

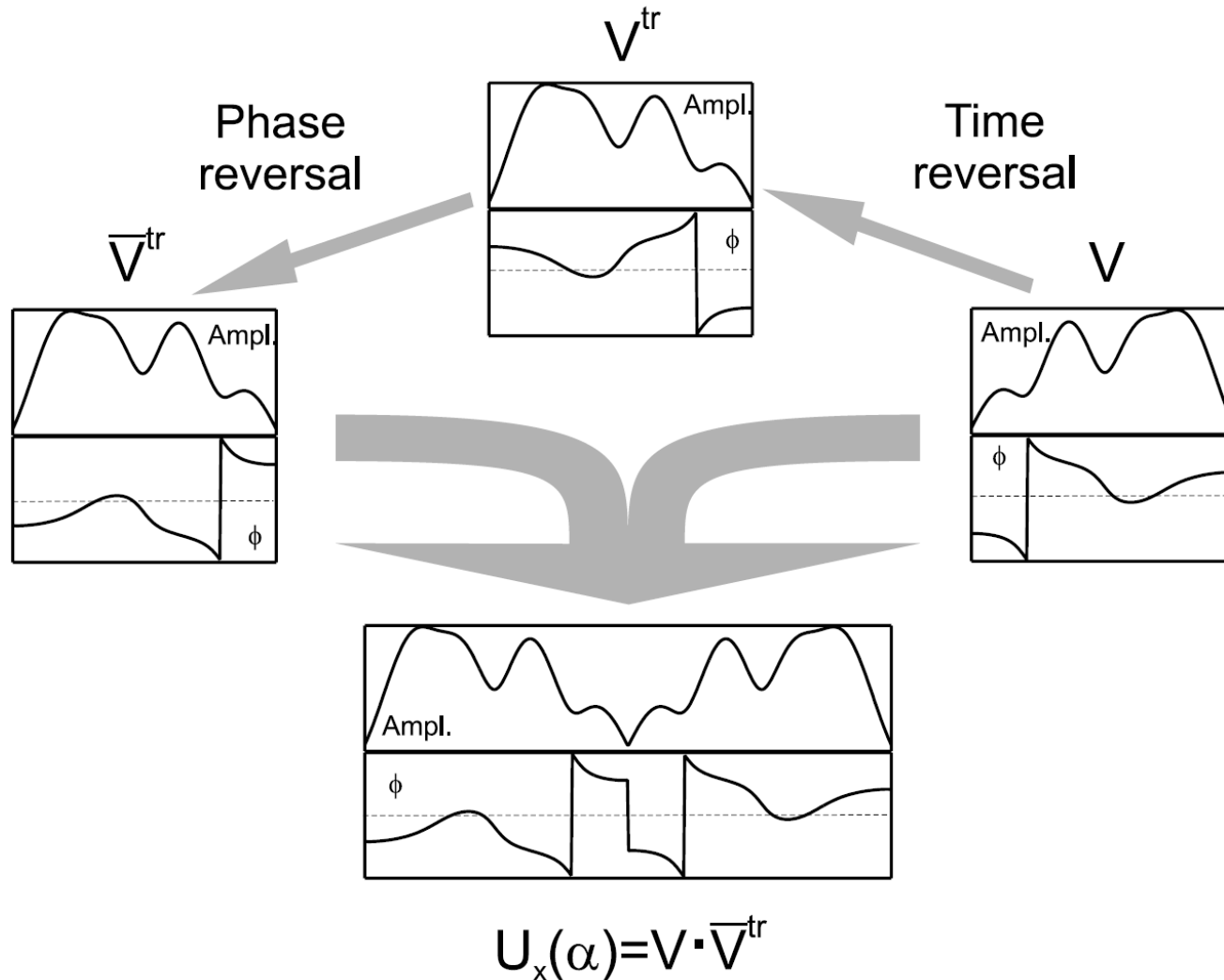
Pattern Pulses

UR-Pulses

HSQC with ^{13}C -BEBOP/BIBOP

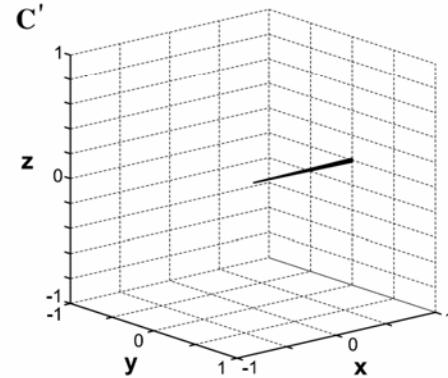
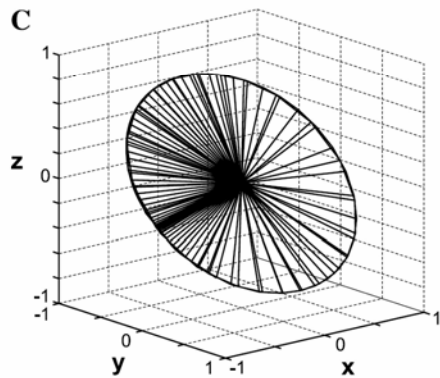
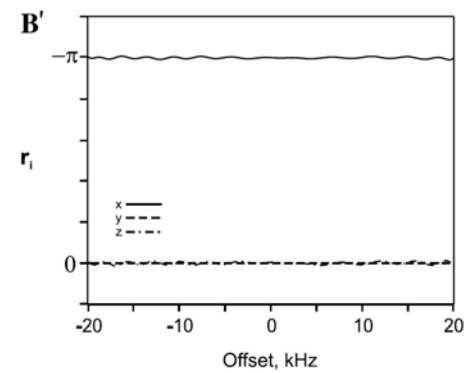
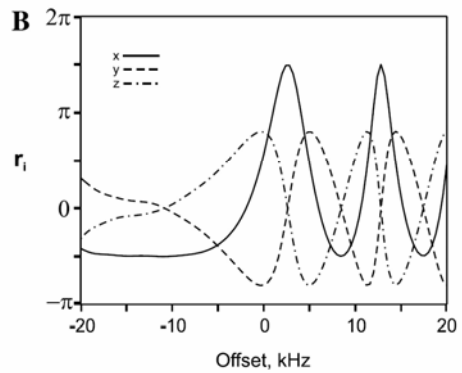
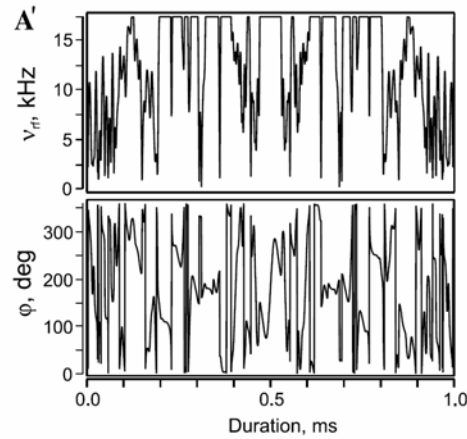
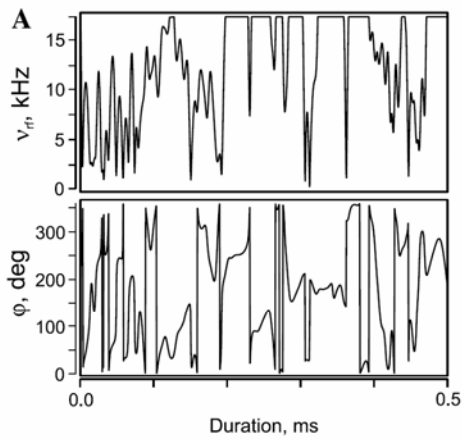


Construction Principle for UR Pulses



V = State-to-State Pulse
 half flip angle α from I_y

Example: Refocussing from 2 x BEBOP



BEBOP

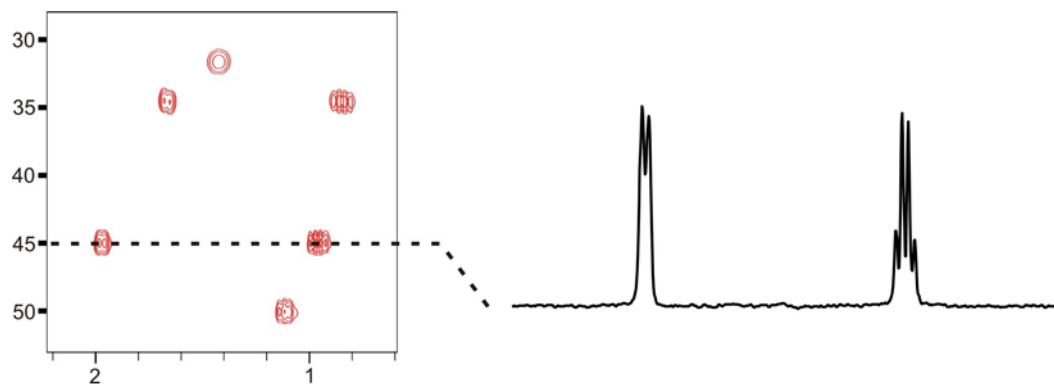
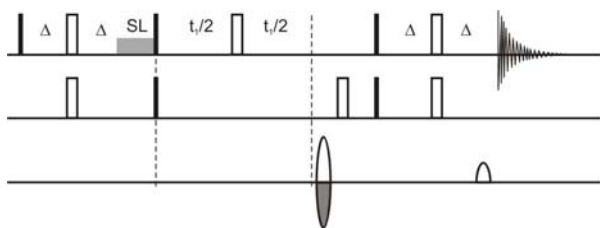
BURBOP-180°

rotational axes

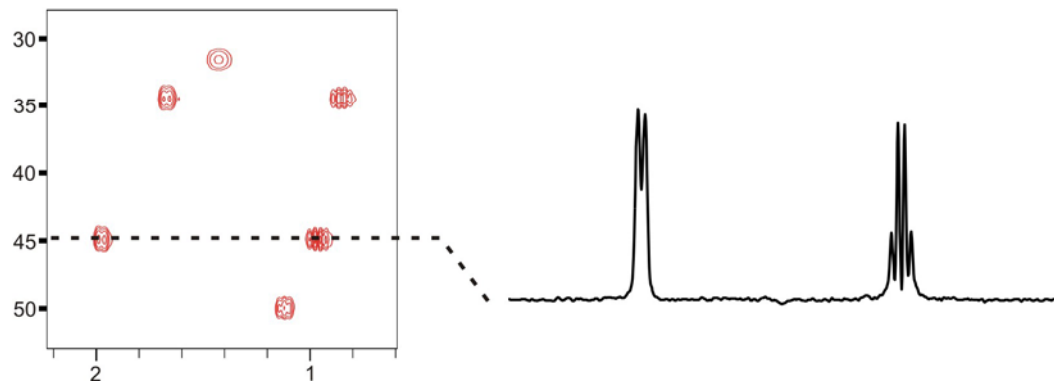
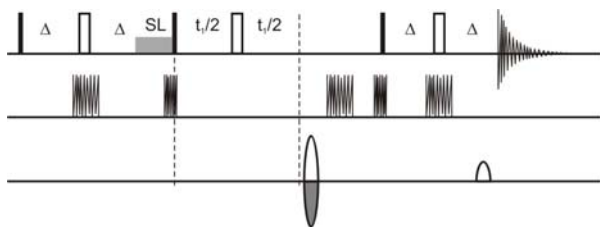
B. Luy et al., JMR 176, 179 (2005).

Almost Calibration-free 90°- and 180°- Pulses: HSQC of Menthol

conventional HSQC



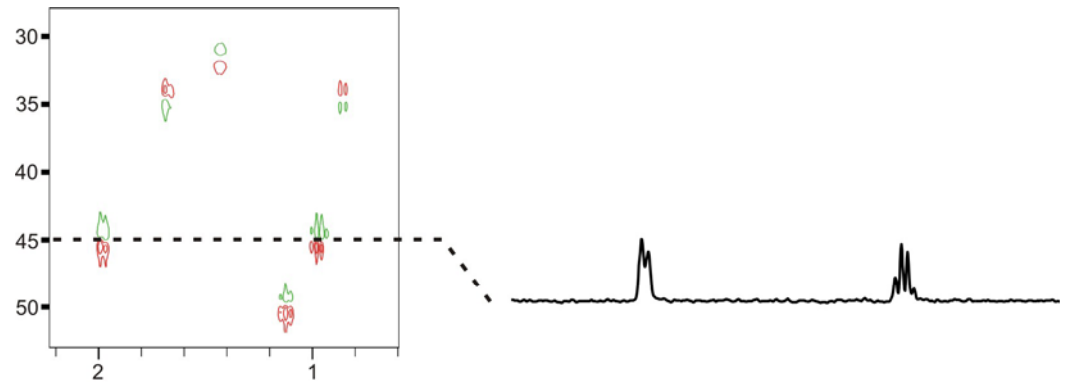
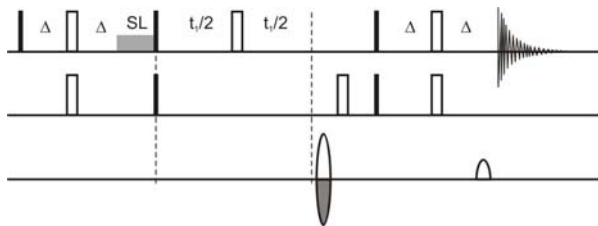
HSQC with ^{13}C -BEBOP



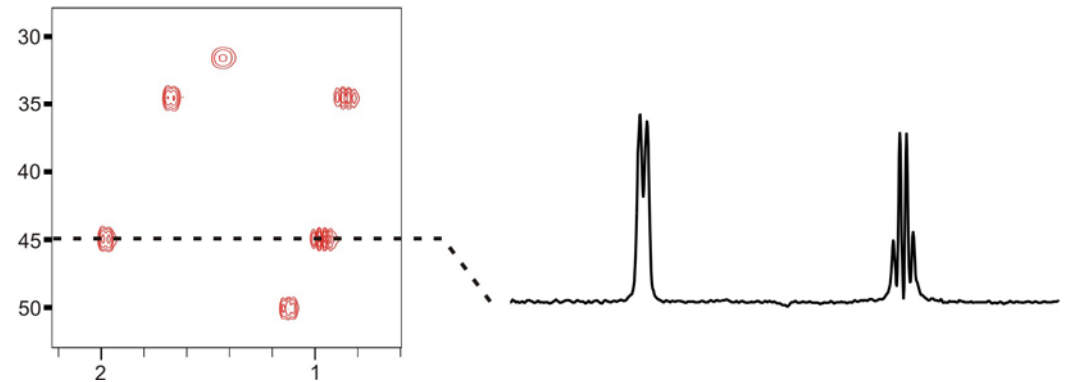
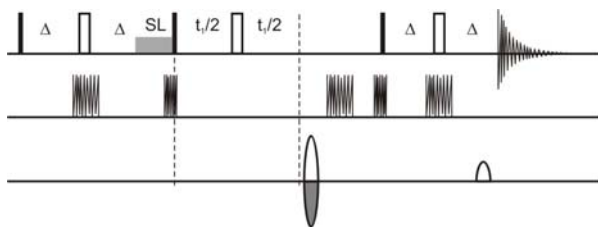
calibrated, no Offset

Almost Calibration-free 90°- and 180°- Pulses: HSQC of Menthol

conventional HSQC



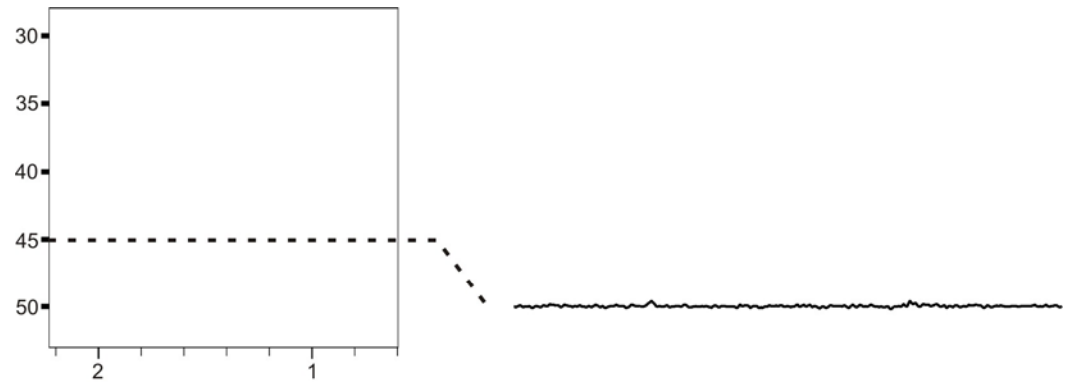
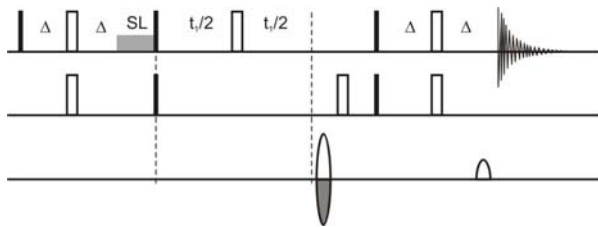
HSQC with ^{13}C -BEBOP



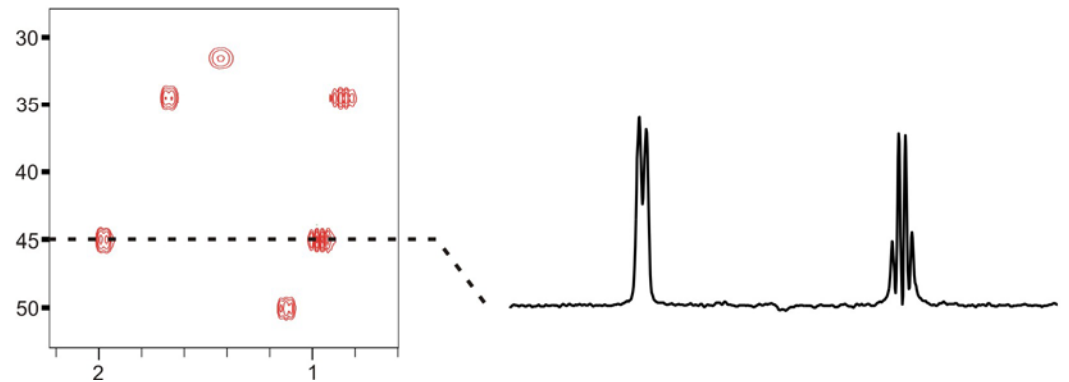
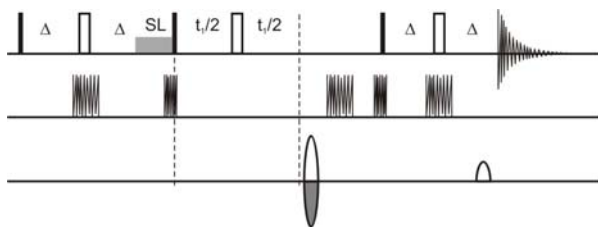
3dB miscalibrated, 8kHz Offset

Almost Calibration-free 90°- and 180°- Pulses: HSQC of Menthol

conventional HSQC

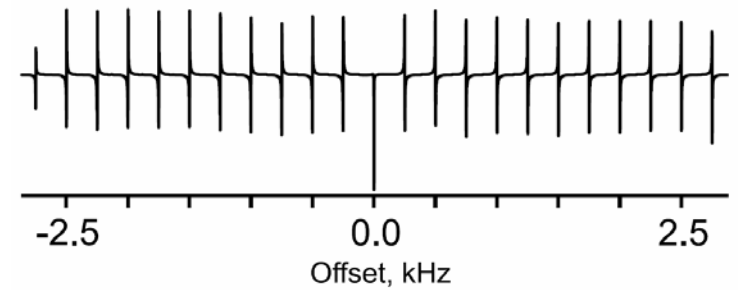
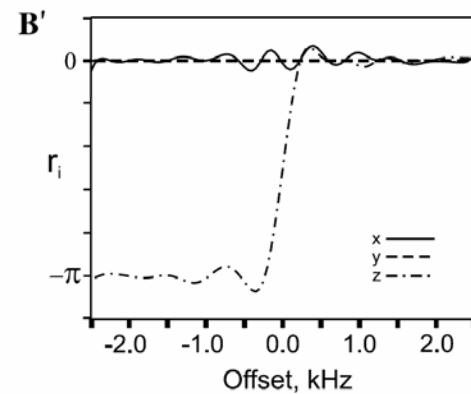
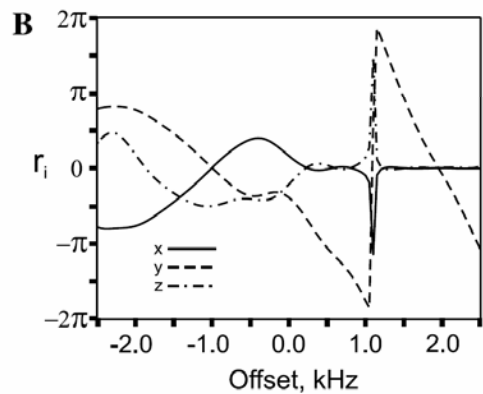
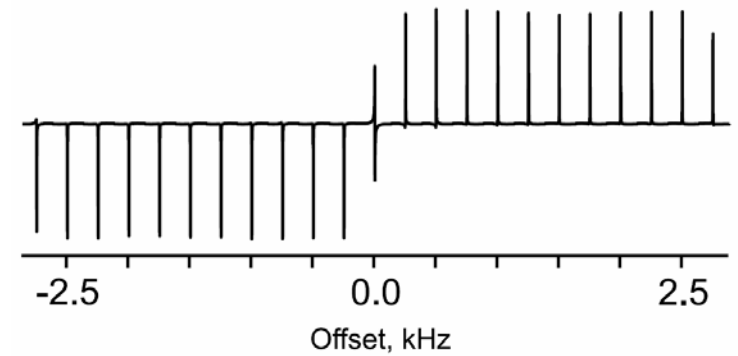
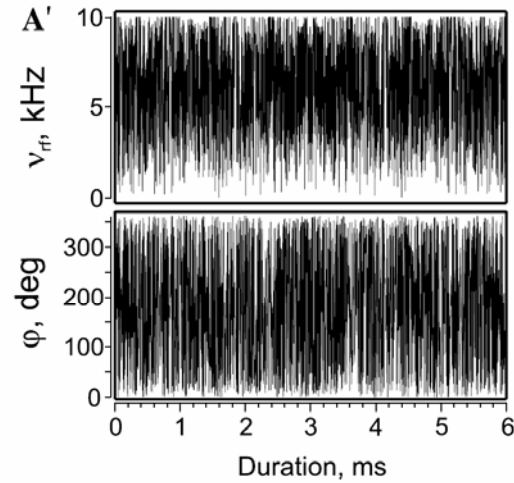
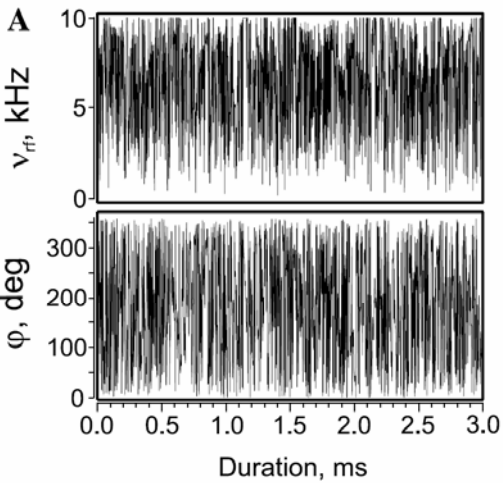


HSQC with ^{13}C -BEBOP



3dB miscalibrated, 16kHz Offset

Example: Construction of 180° z-Rotation

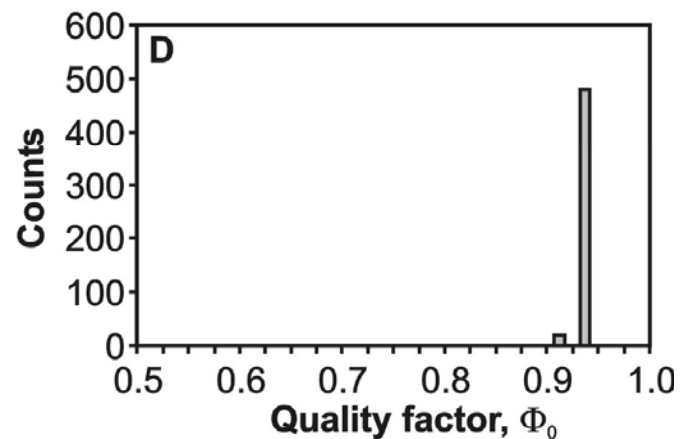
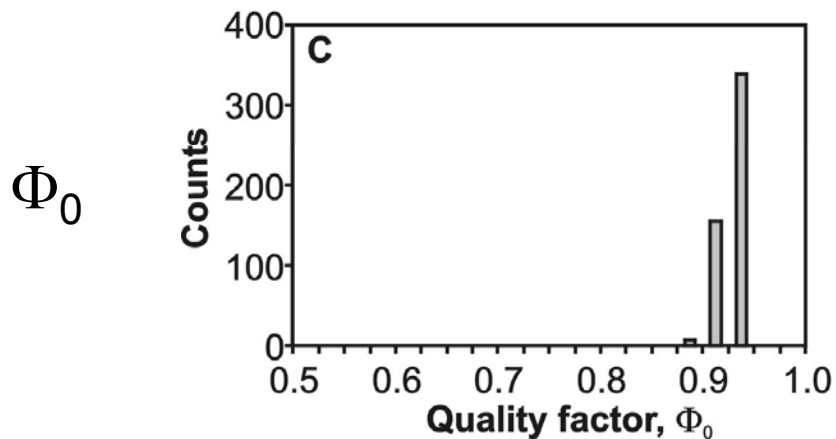
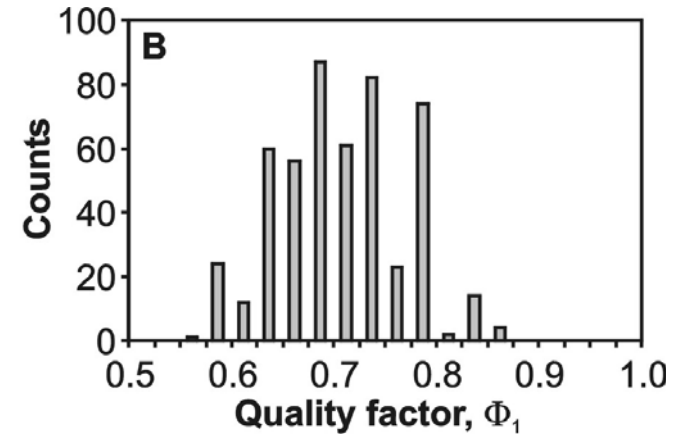
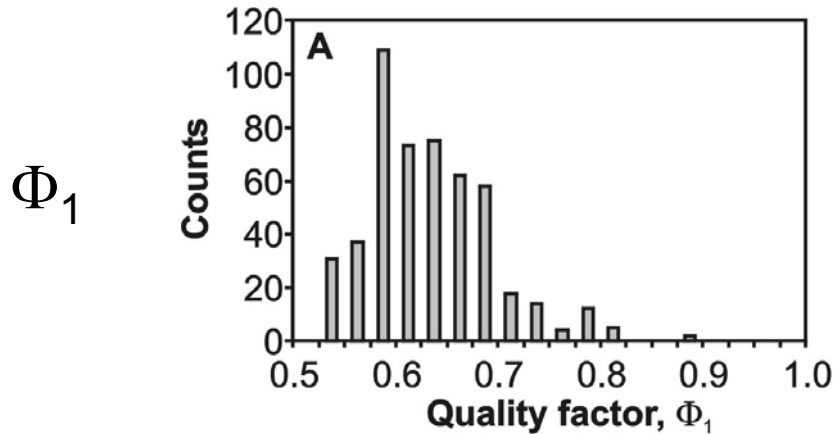


Optimization of UR-Pulses from Scratch

$$\Phi_1 = |\langle \uparrow | U_F | U(T) \uparrow \rangle|^2$$

$$\Phi_0 = \text{Re} \{ \langle \uparrow | U_F | U(T) \uparrow \rangle \}$$

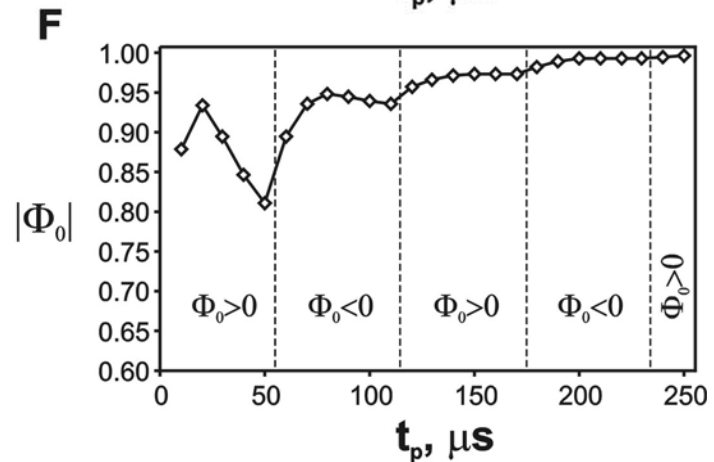
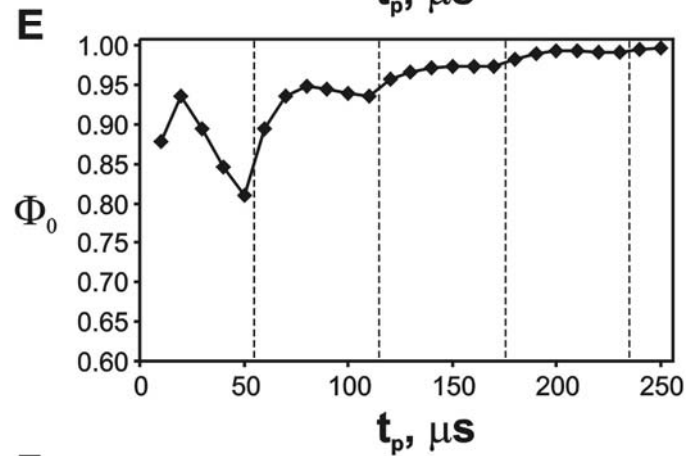
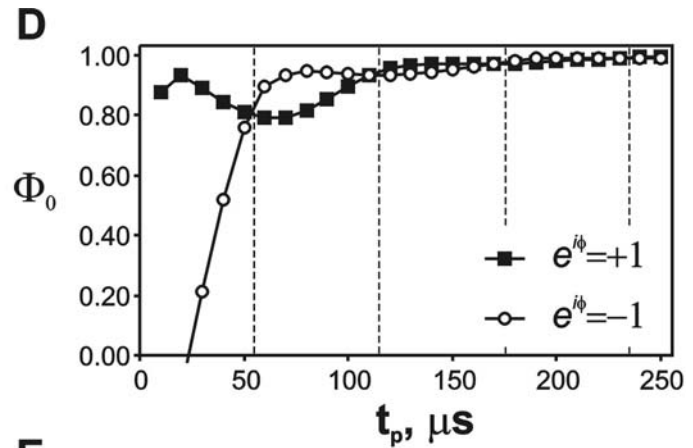
Comparison of Convergence



90°, 40kHz BW

180°, 40kHz BW

Comparison of Results for Φ_1 / Φ_0



90° UR-Pulse
20 kHz BW

(several unpublished slides have been removed. Please contact Burkhard.Luy@ch.tum.de if interested)

Why bother with NMR spectroscopy?




Broadband 'State-To-State' Pulses

Broadband 'Universal Rotation' Pulses

Ultrabroadband Excitation

Pattern Pulses

Chemical Shift Ranges (600 MHz)

^1H		~15 ppm / 9kHz
^{13}C (org.)		~250 ppm / 37kHz
^{15}N (org.)		~600 ppm / 36kHz

Chemical Shift Ranges (600 MHz)

^1H



~15 ppm / 9kHz

^{13}C (org.)

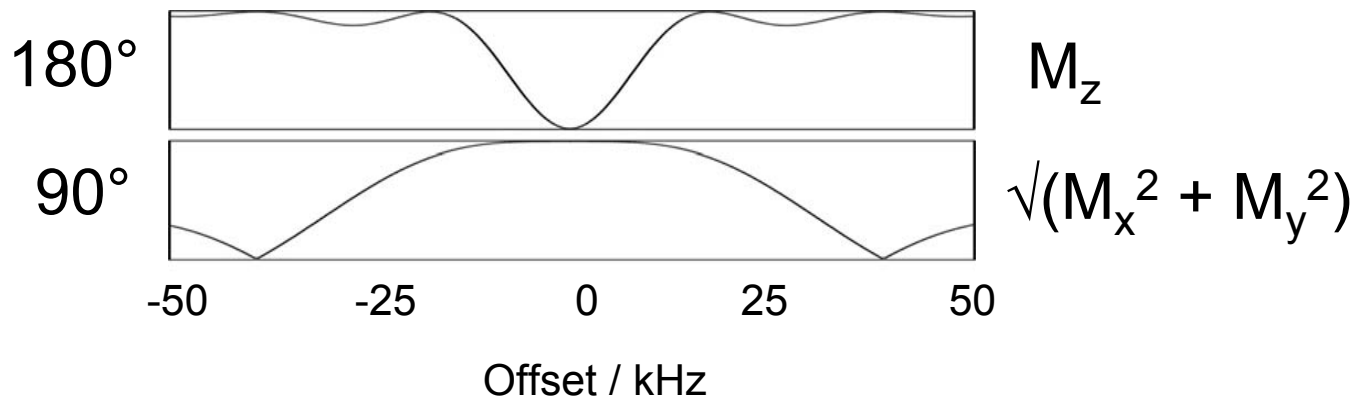


~250 ppm / 37kHz

^{15}N (org.)



~600 ppm / 36kHz



Chemical Shift Ranges (600 MHz)

^1H



~15 ppm / 9kHz

^{13}C (org.)

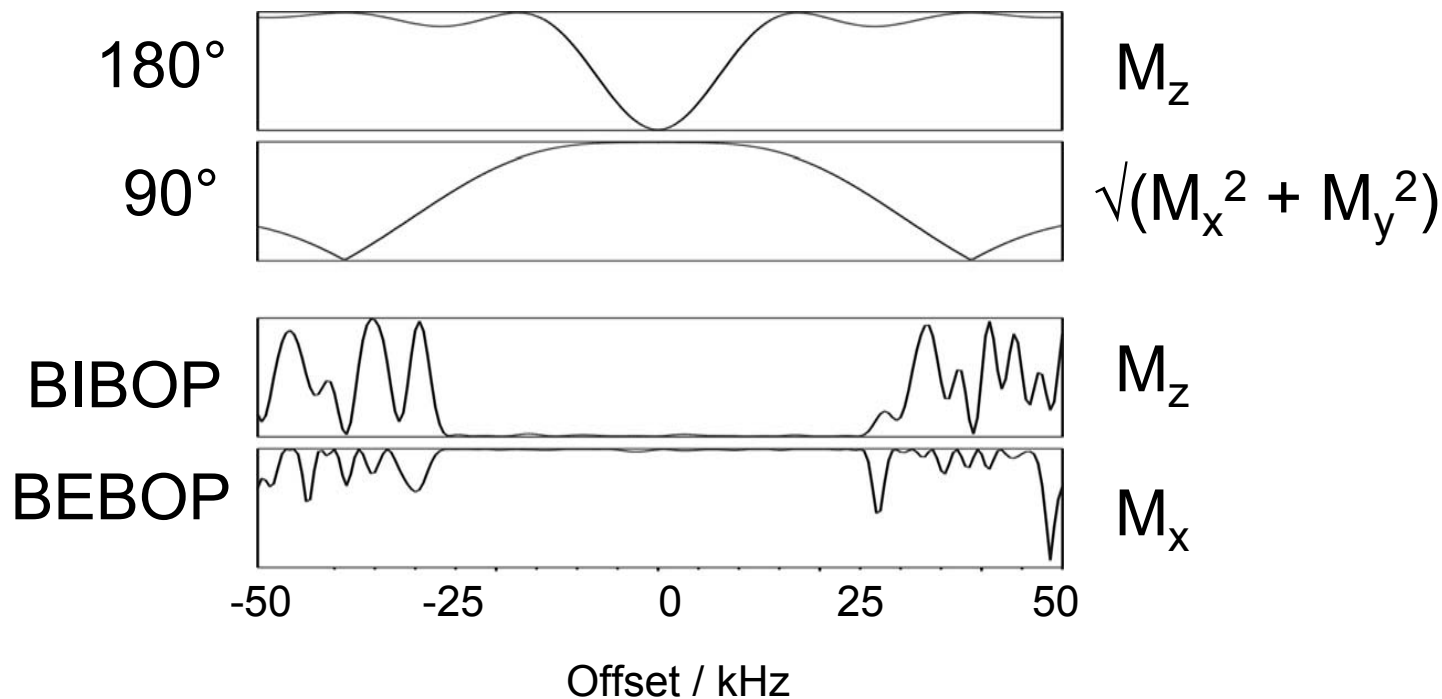


~250 ppm / 37kHz

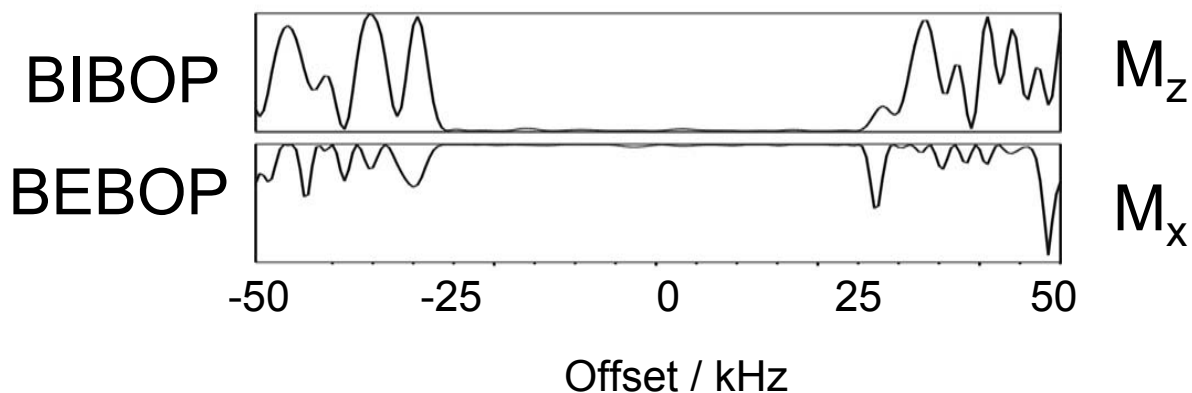
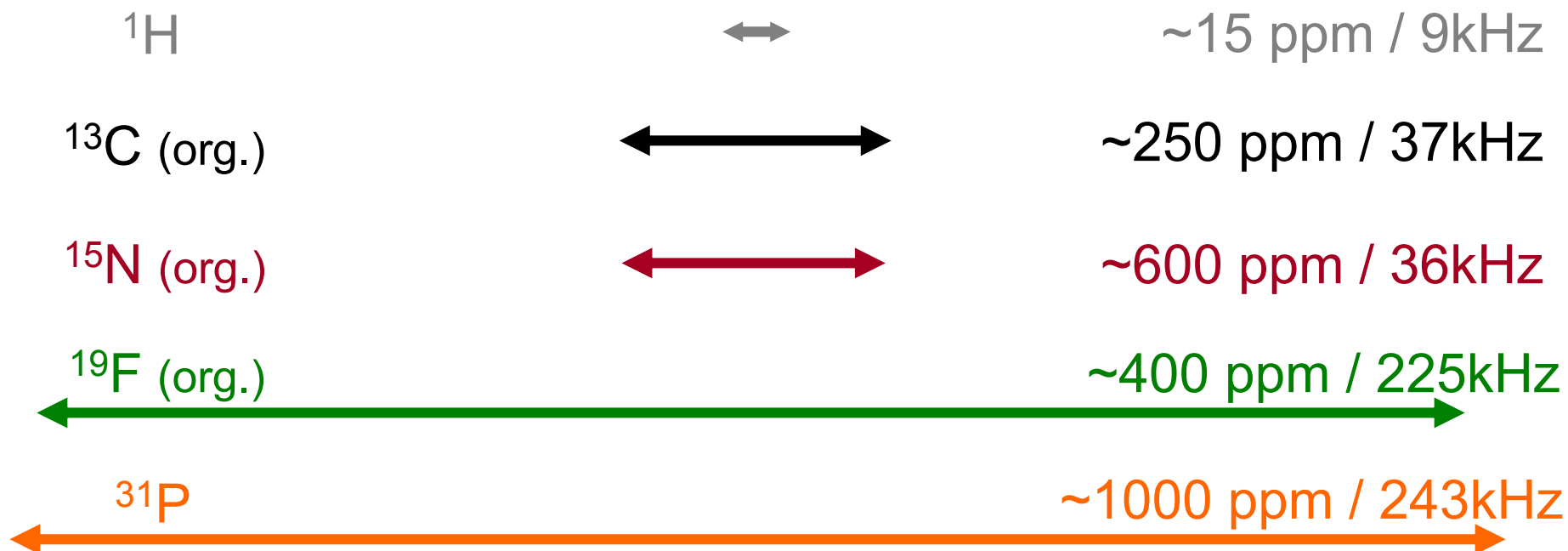
^{15}N (org.)



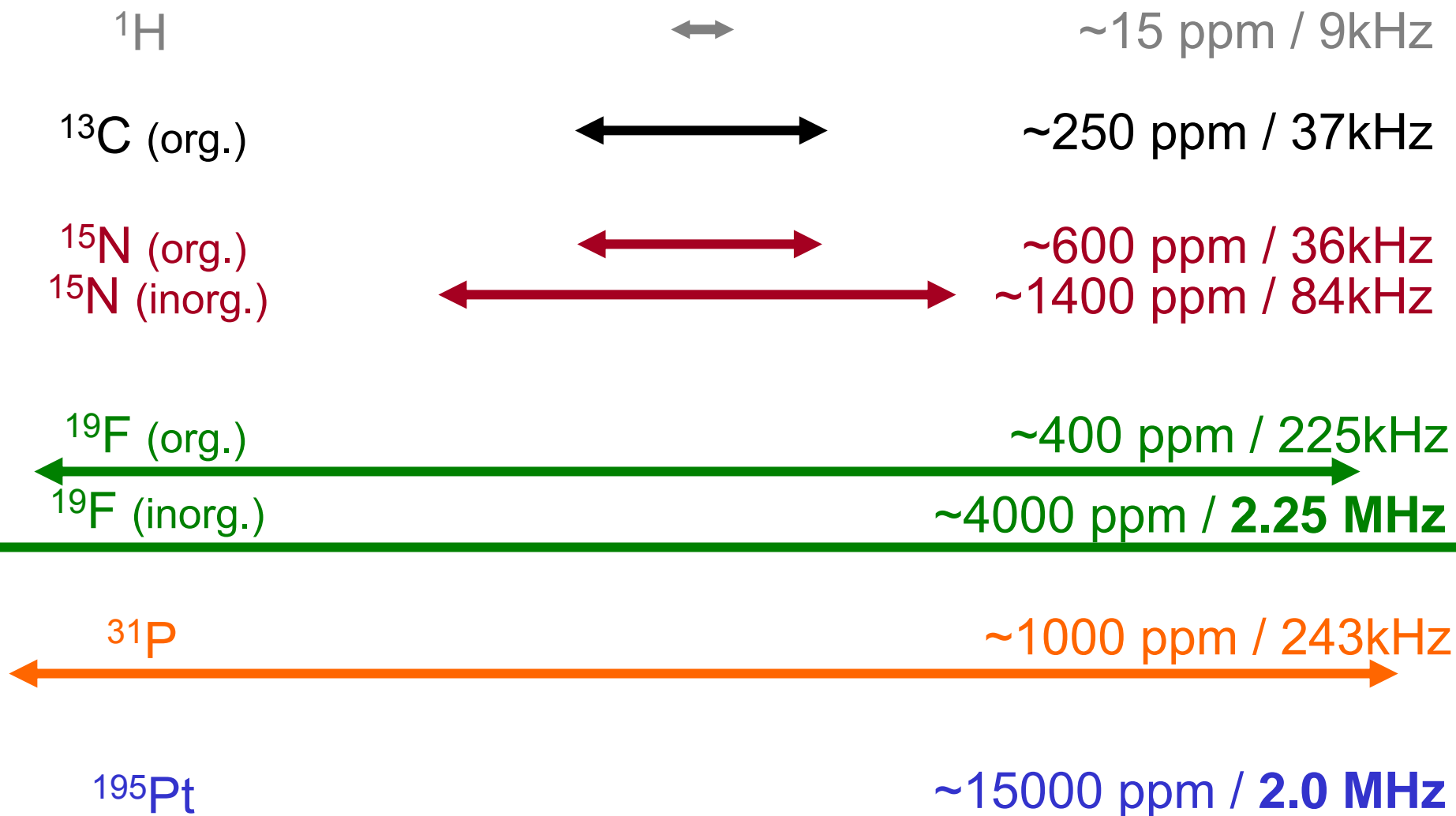
~600 ppm / 36kHz



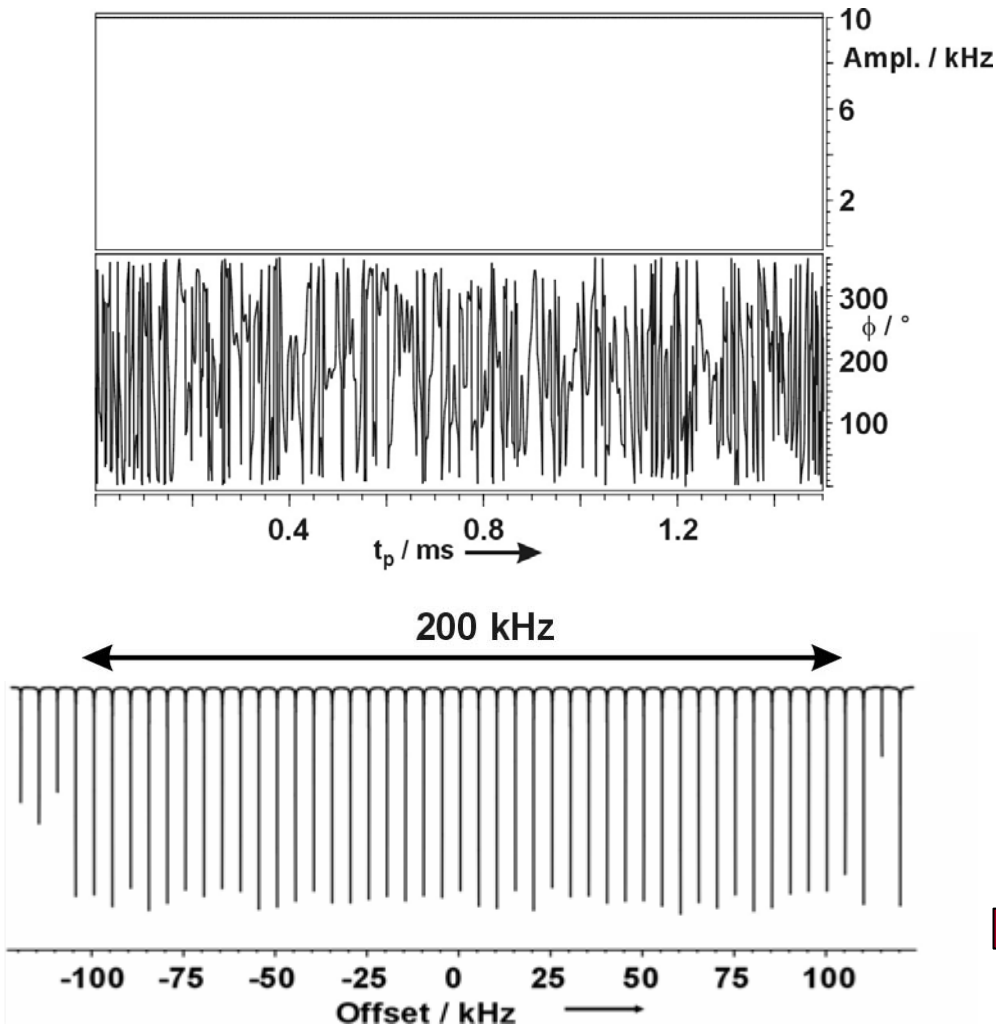
Chemical Shift Ranges (600 MHz)



Chemical Shift Ranges (600 MHz)



Situation at 200 kHz Bandwidth



For 10 kHz RF-amplitude:

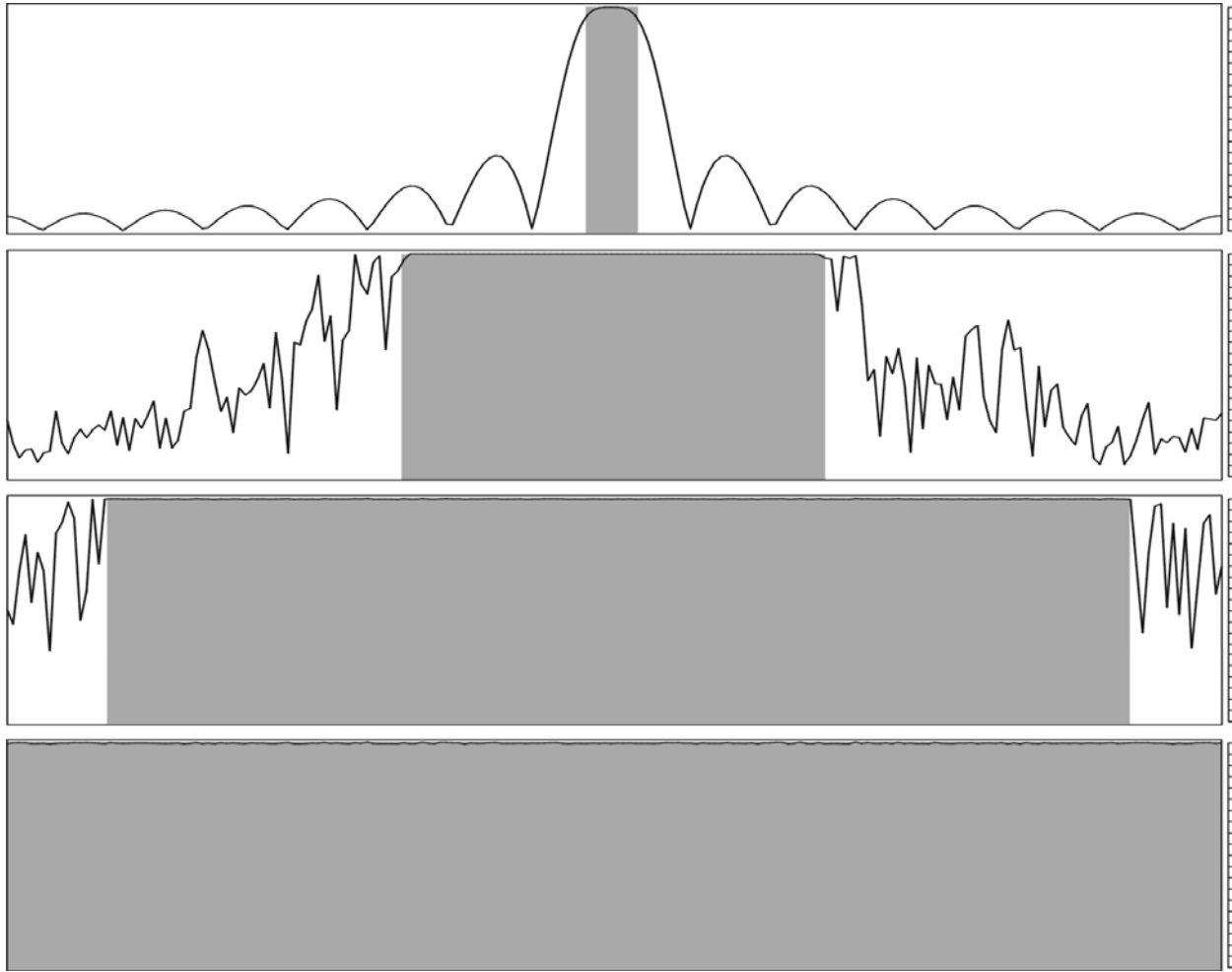
- BIBOP inversion pulse 1.5 ms duration
- **no** excitation pulse ● 2 ms
- **no** refocussing pulse ● 2 ms



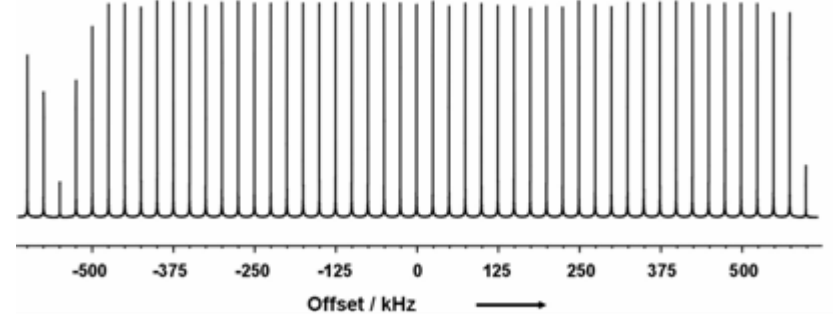
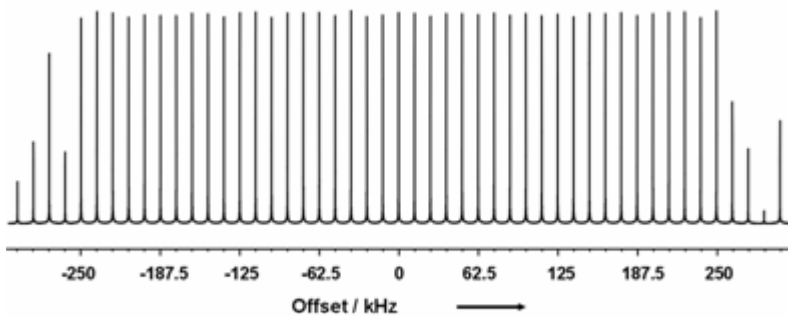
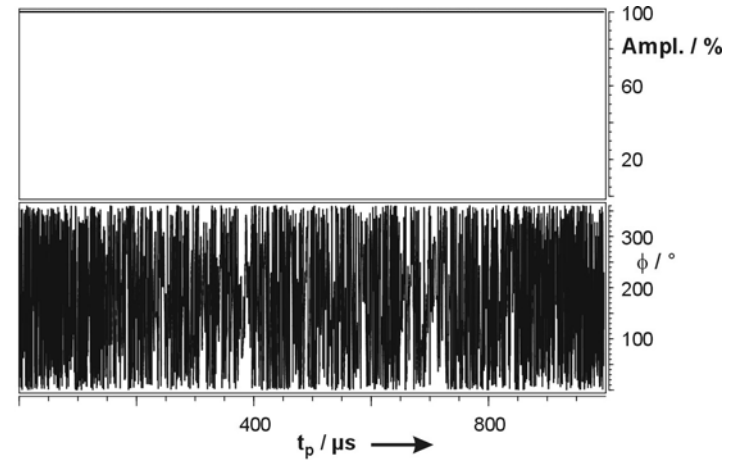
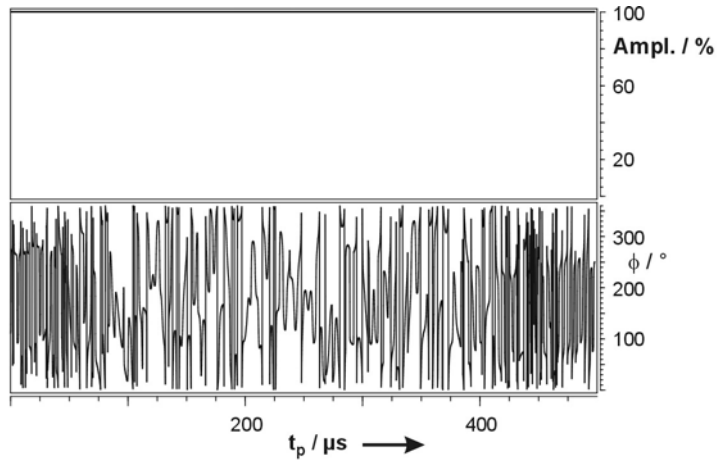
no conventional NMR possible !

(several unpublished slides have been removed. Please contact Burkhard.Luy@ch.tum.de if interested)

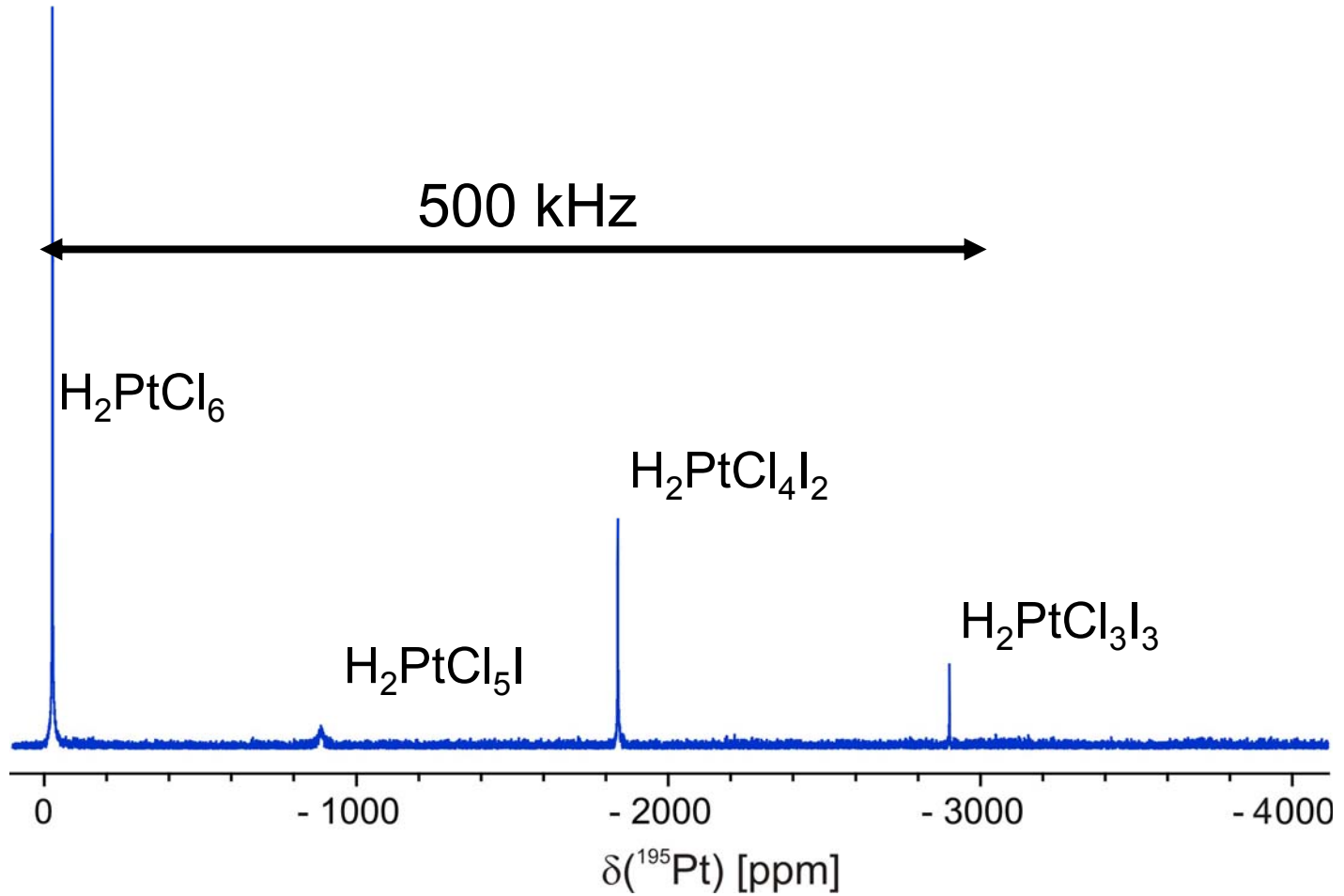
Even Larger Bandwidths ?



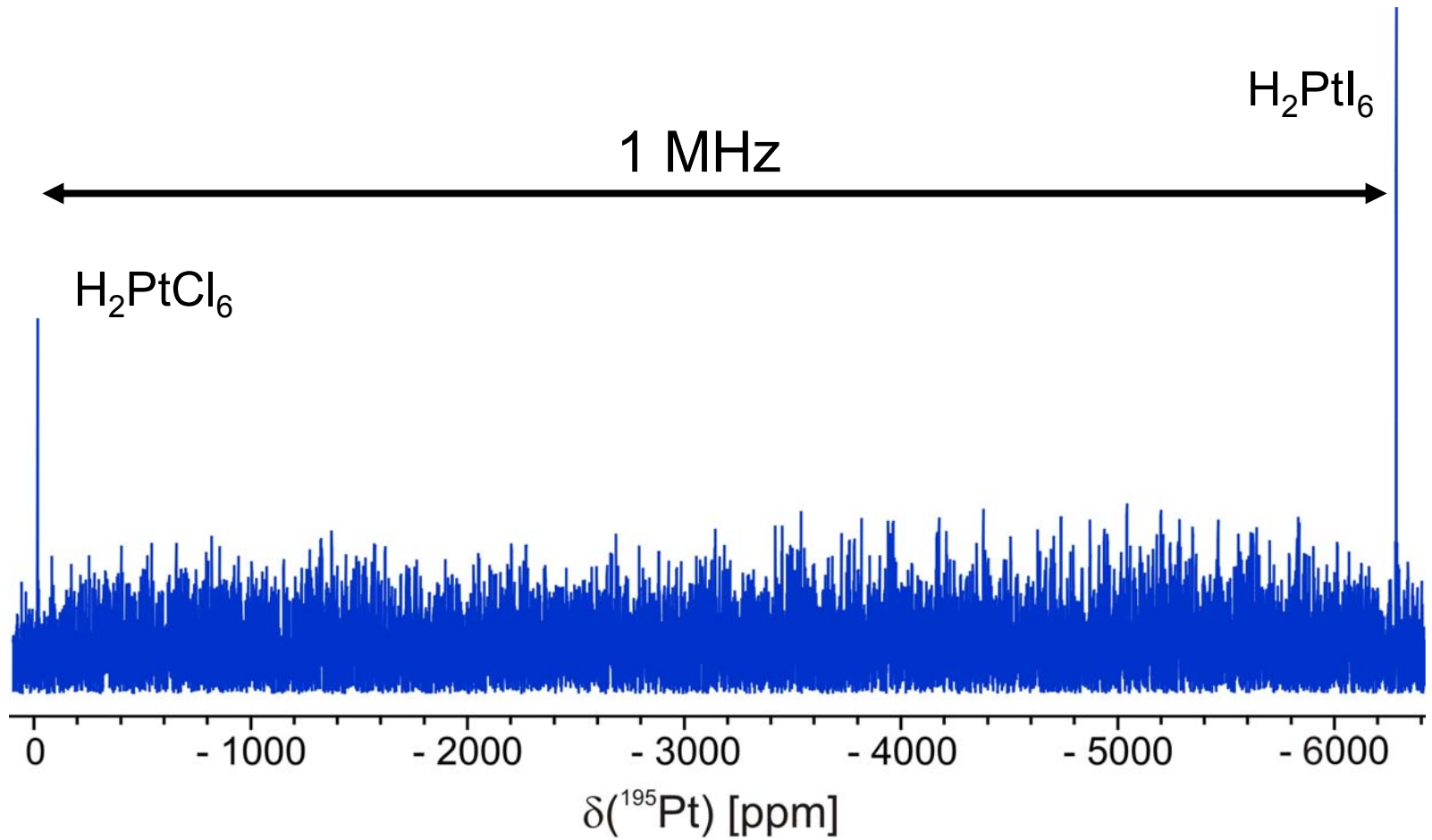
Reaching the MHz ...



^{195}Pt -Spectra



^{195}Pt -Spectra



Why bother with NMR spectroscopy?

Broadband 'State-To-State' Pulses

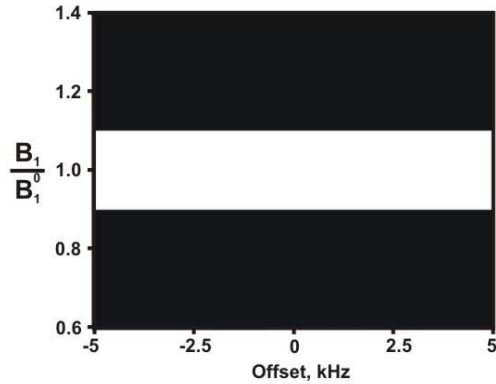
Broadband 'Universal Rotation' Pulses

Ultrabroadband Excitation

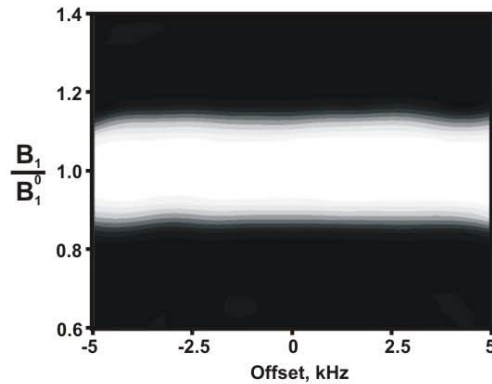
Pattern Pulses

Pattern Pulses

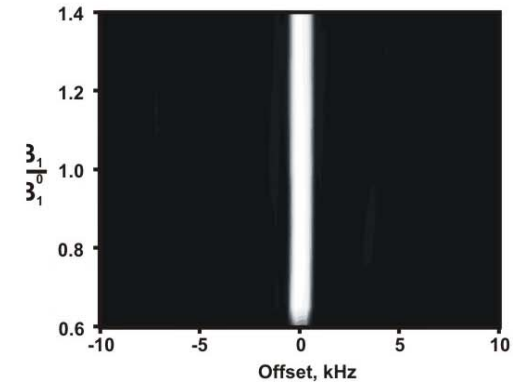
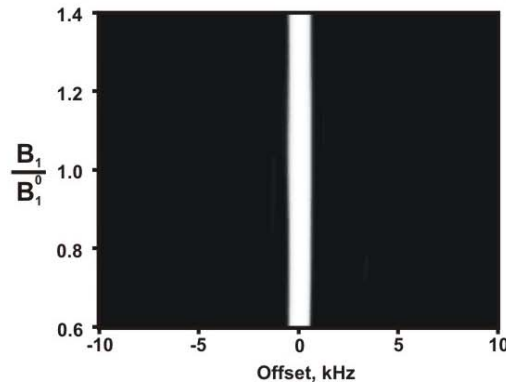
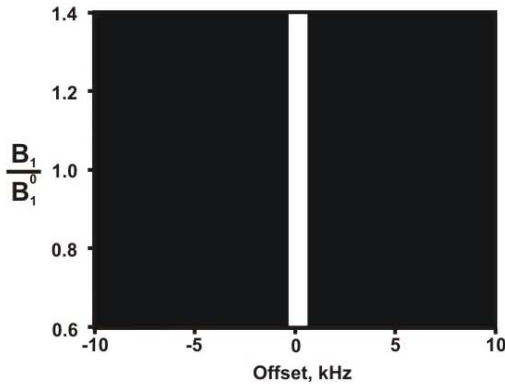
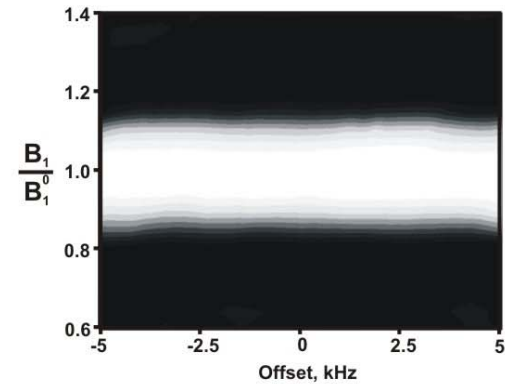
Target



Theoretical



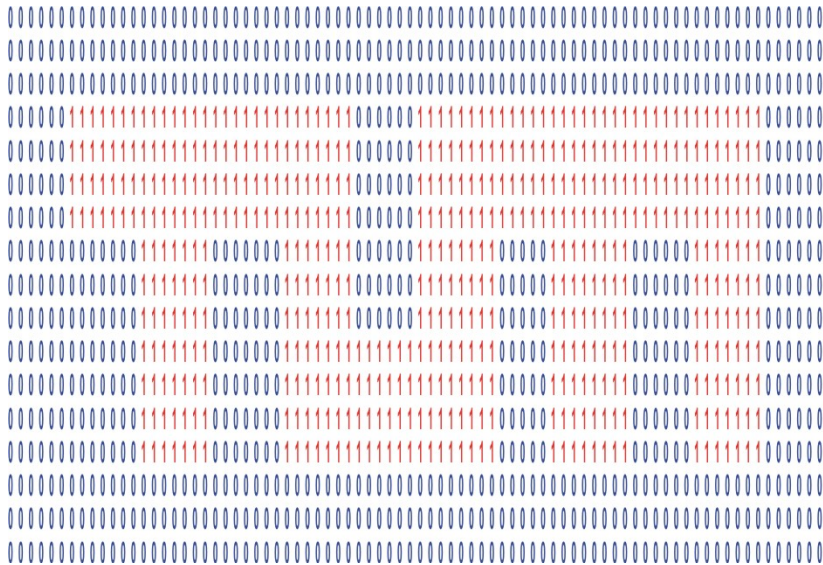
Experimental



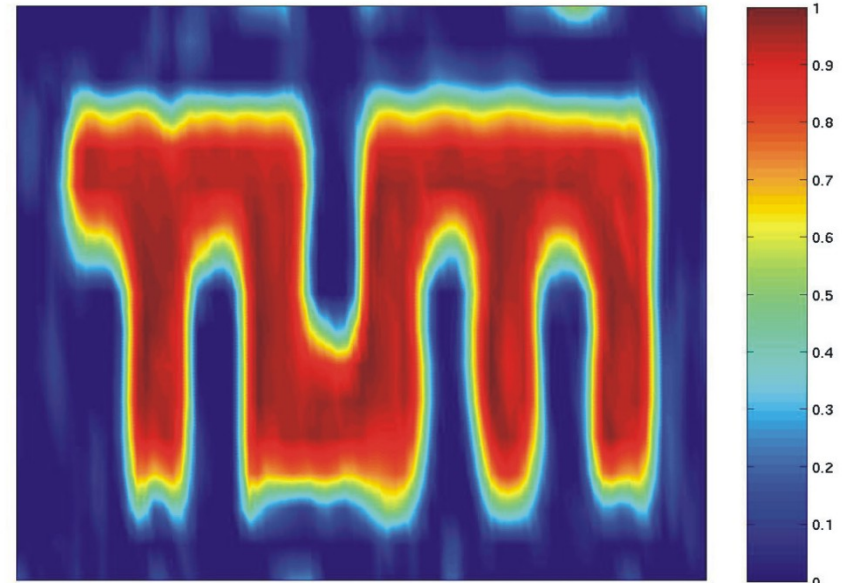
RF- and offset-selective pulses

Pattern Pulses

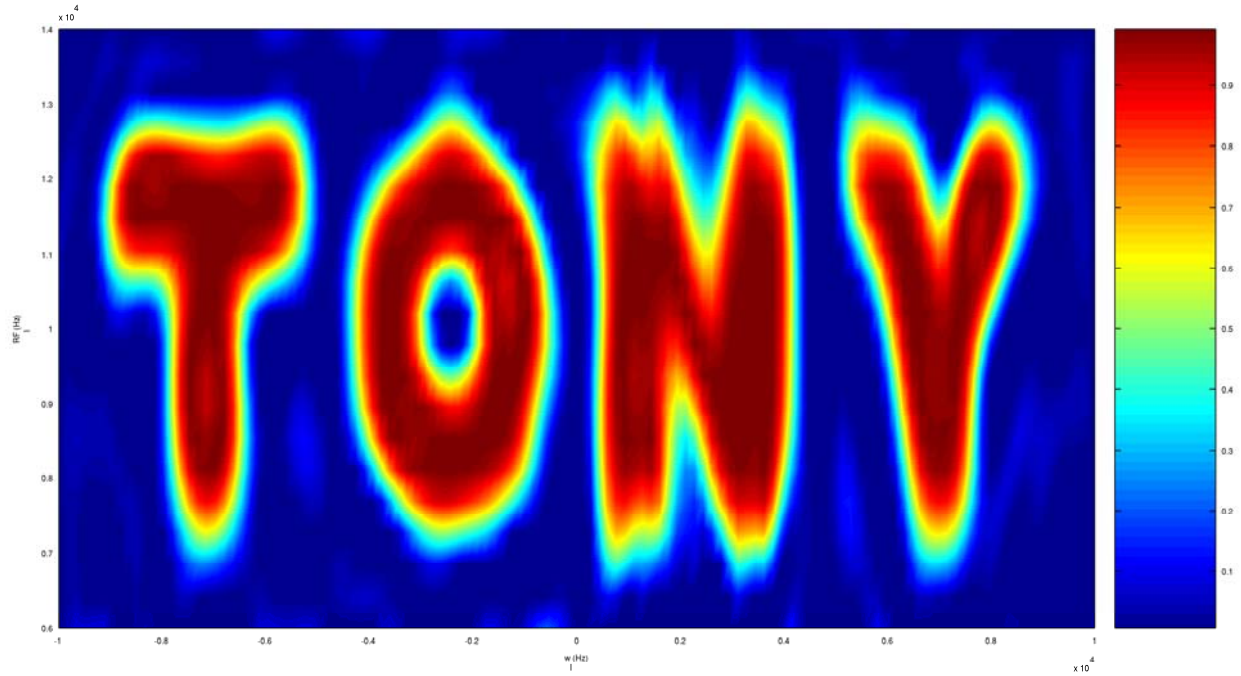
Target



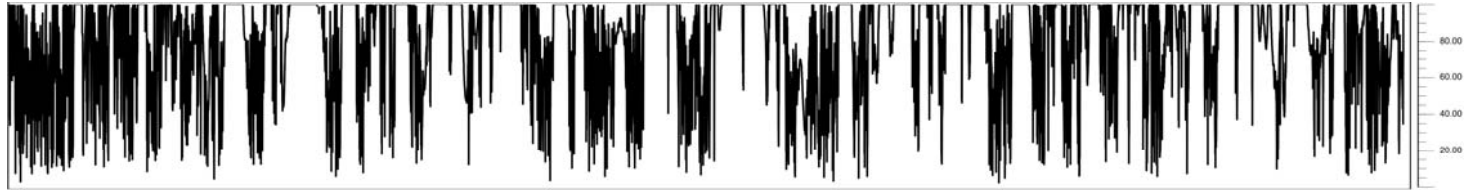
Experiment



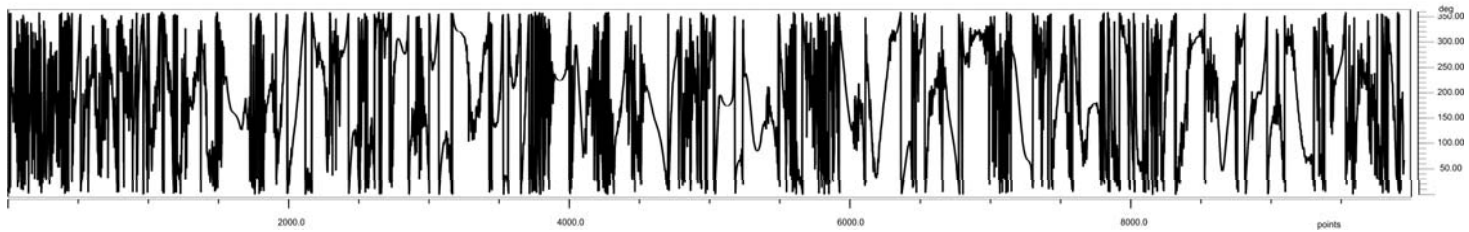
Almost arbitrary RF- and Offset dependence possible for excitation profile



Ampl.

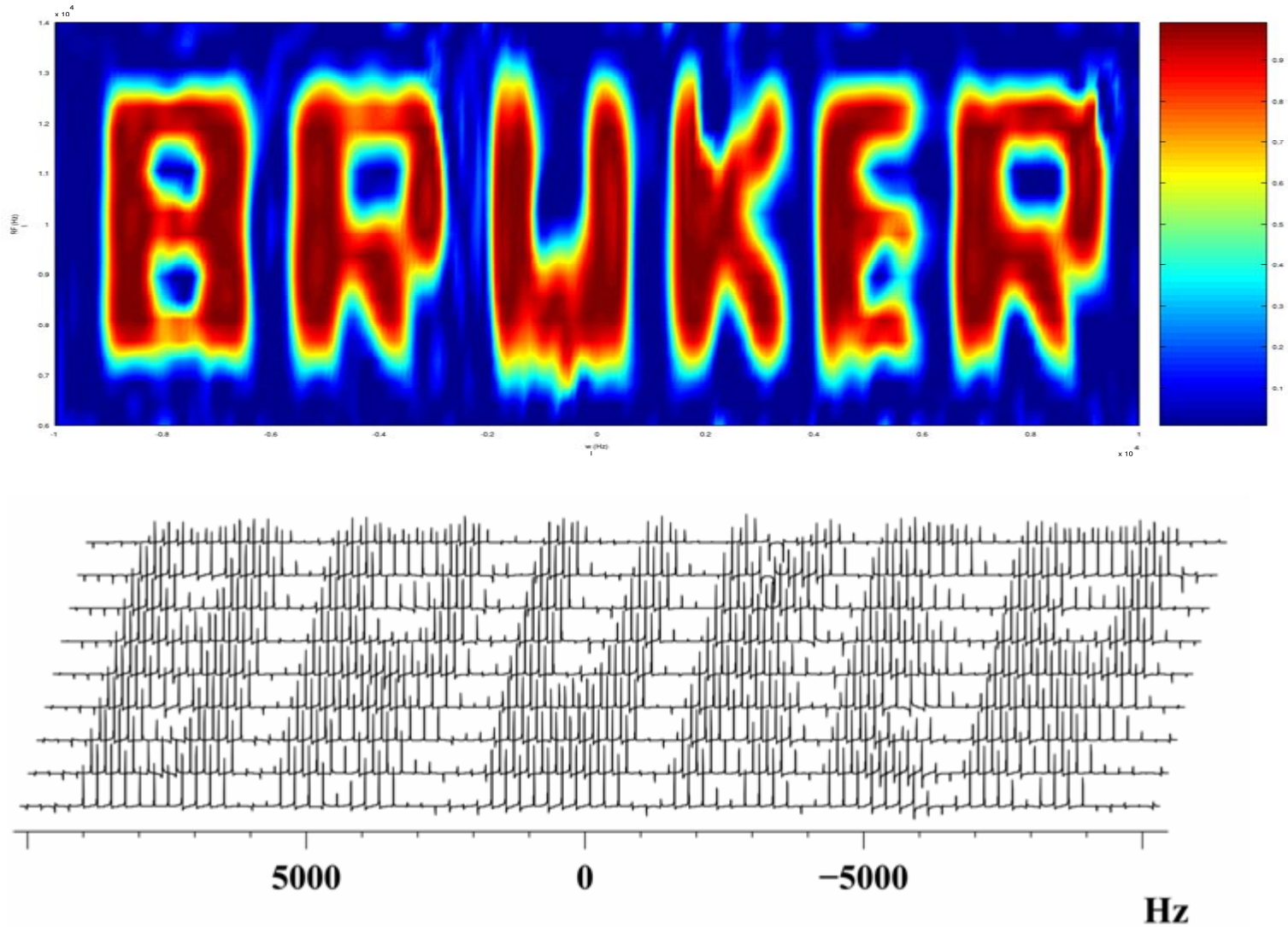


ϕ



Kyryl Kobzar, Burkhard Luy, unveröffentlicht.

Pattern Pulses



Kyryl Kobzar, Markus Wälchli, Burkhard Luy, unpublished.



BRUKER
900
UltraStabilized™