

Axial Higgs Mode from Geometry + Intensity Wave



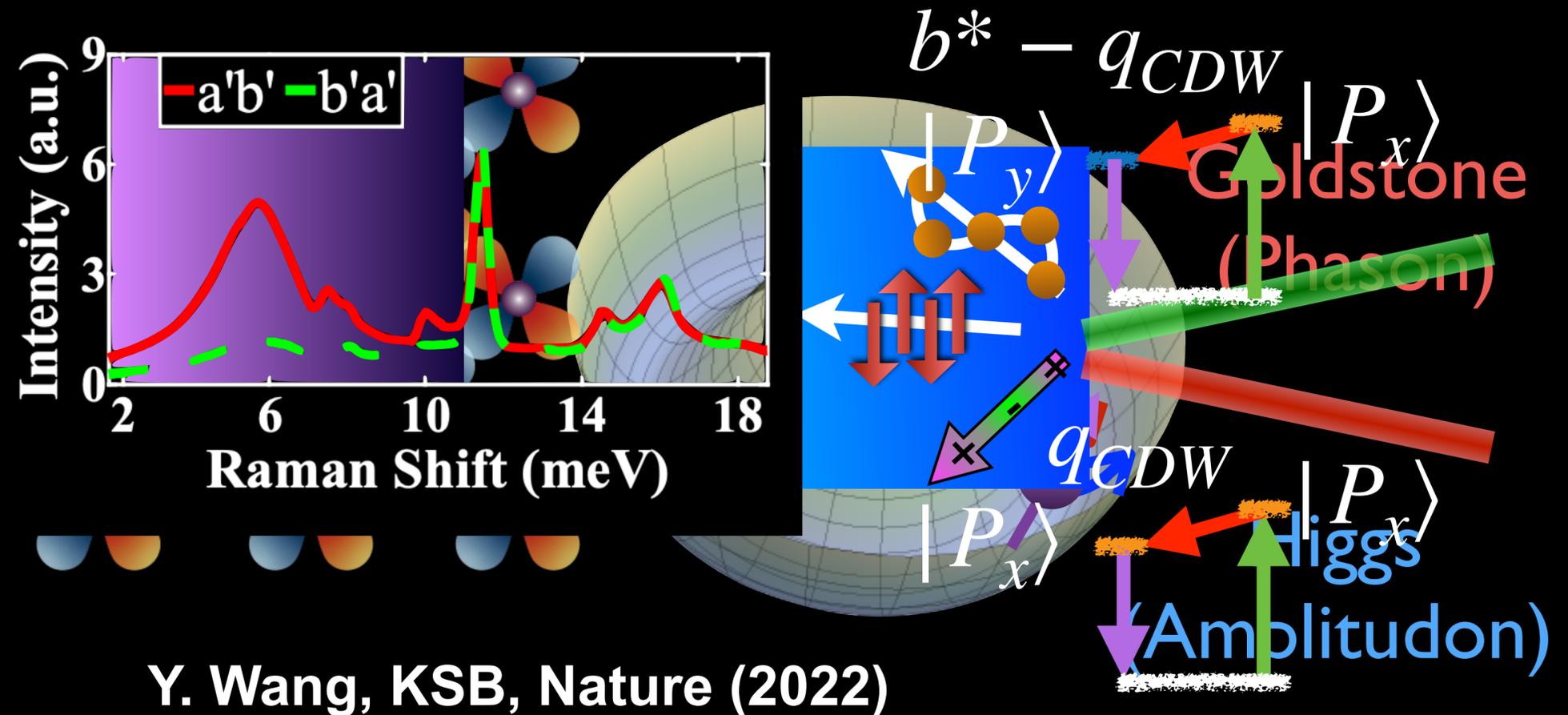
et al Nature (2022)

Fun



Axial Higgs Mode via Q.G. + C.D.W.

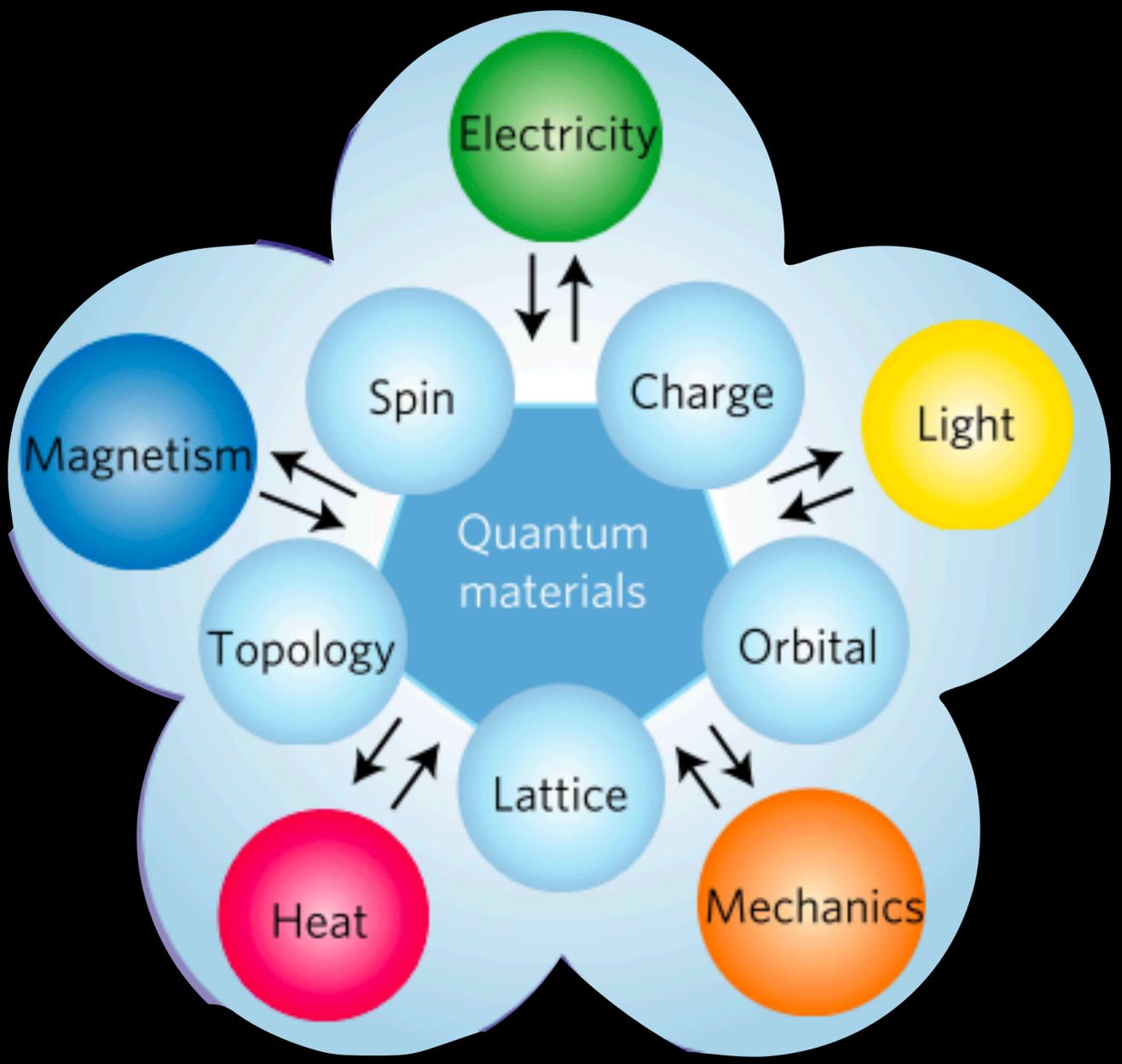
- **Higgs**
- **Square Scattering**
- **Interference**
- **Highlights**



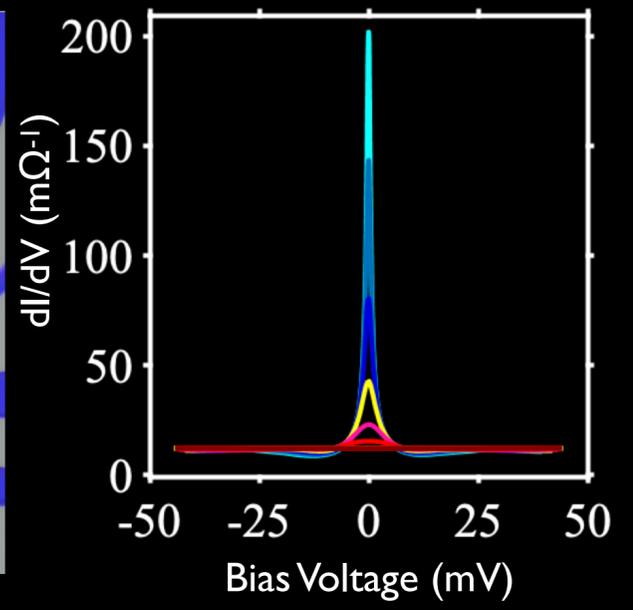
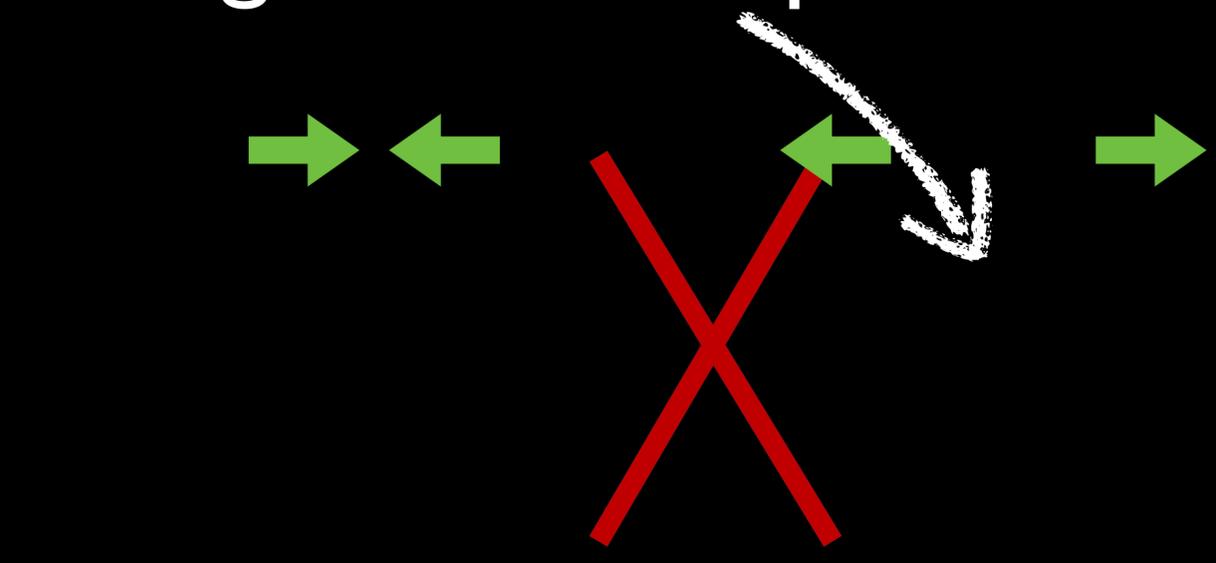
Funding:



Magnetic Monopole



Y. Tokura et al., Nature Physics (2017)

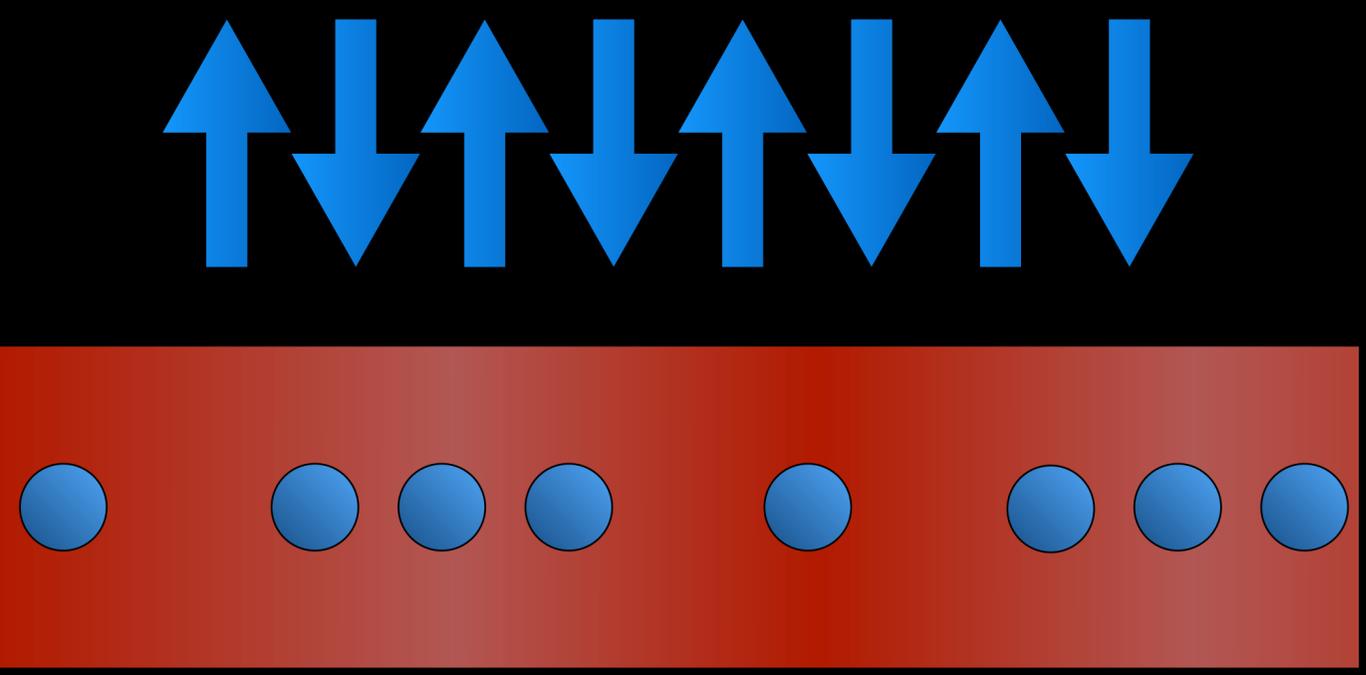


M. Gray, KSB et al, Nanoletters (2019)

Symmetry Breaking

$$\Psi(r, t) = |\Psi(r, t)| e^{i\phi(r, t)}$$

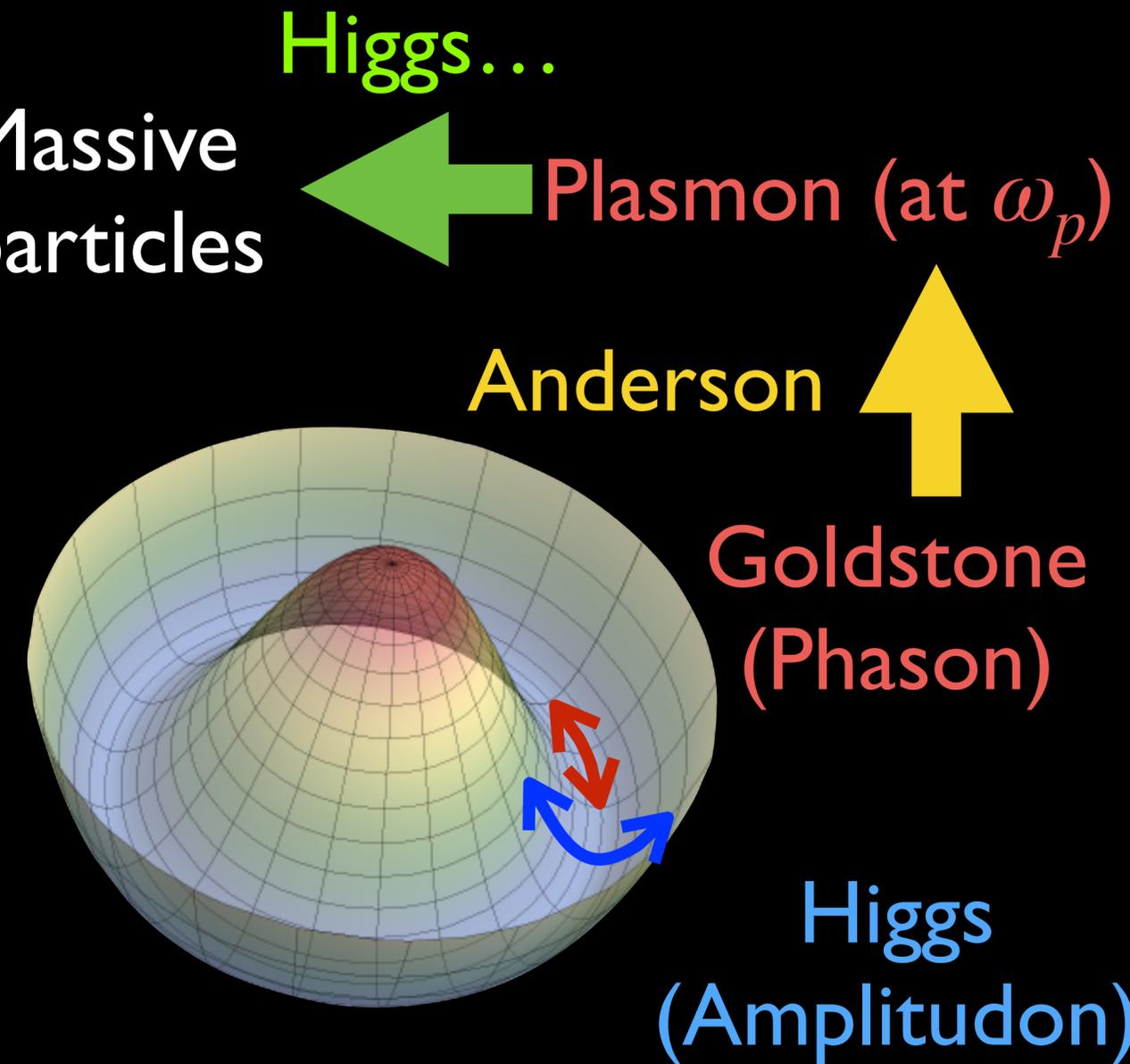
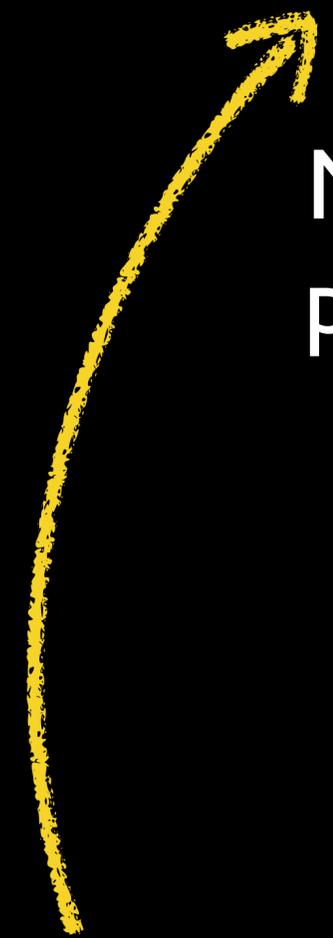
$$S = -\alpha \Psi^* \Psi + \beta (\Psi^* \Psi)^2 + \gamma (\nabla \Psi^* \nabla \Psi)$$



Gauge?

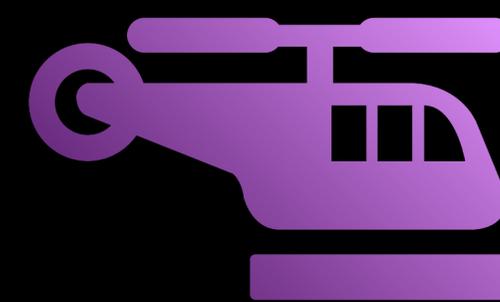
$$\nabla \rightarrow |\nabla - i(e/c)A|$$

D. Pekker and C. Varma Annu. Rev. CMP (2015)



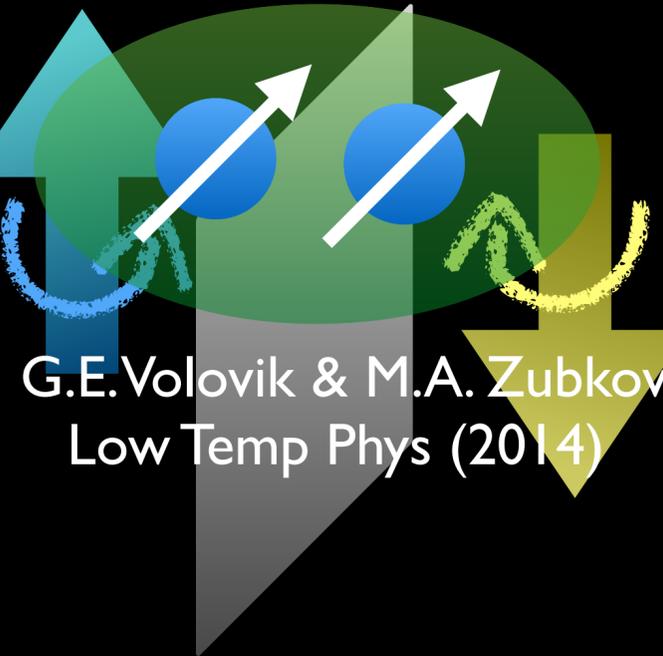
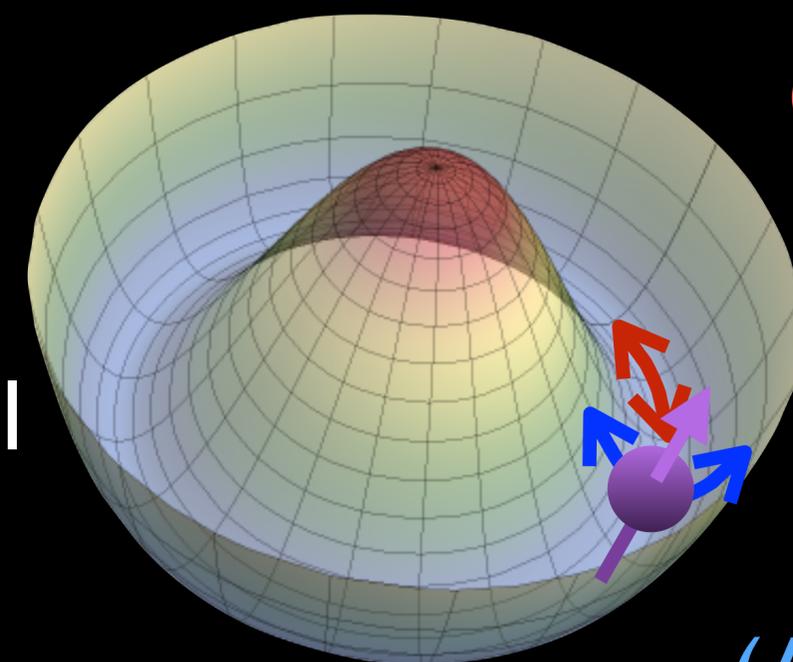
“It is worth noting that an essential feature of this type of theory ... is the prediction of an incomplete multiplet of **scalar** and **vector** bosons”

Superfluid ^3He Axial Multiple Symmetry Breaking?



Goldstone (Phason)

Higgs (Amplitudon)

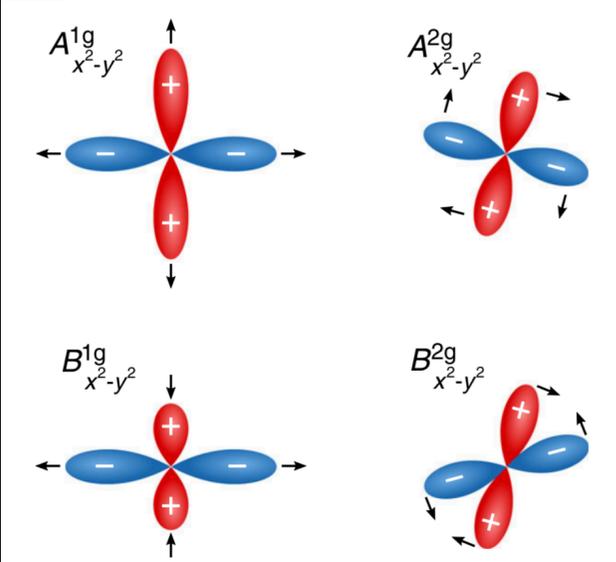


- Mirror
- Time Reversal
- 180°

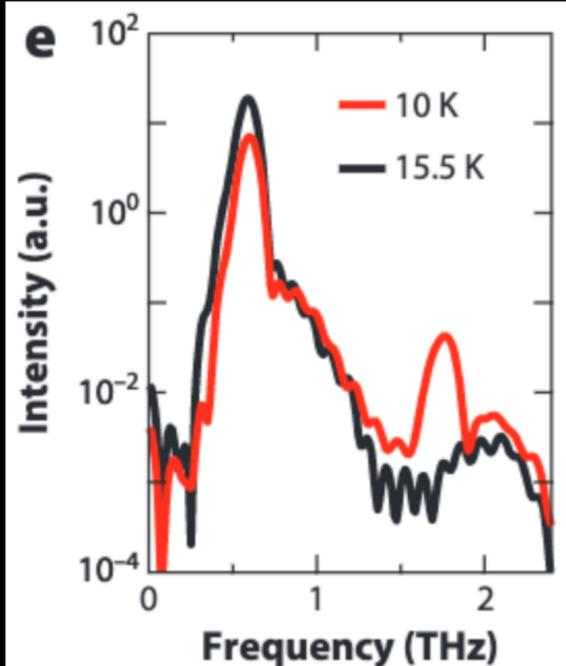
nature physics LETTERS
 PUBLISHED ONLINE: 27 MARCH 2017 | DOI: 10.1038/NPHYS4077

Higgs mode and its decay in a two-dimensional antiferromagnet

A. Jain^{1,2†}, M. Krautloher^{1†}, J. Porras^{1†}, G. H. Ryu^{1‡}, D. P. Chen¹, D. L. Abernathy³, J. T. Park⁴, A. Ivanov⁵, J. Chaloupka⁶, G. Khaliullin¹, B. Keimer^{1*} and B. J. Kim^{1,7*}



Nat. Comm 2020

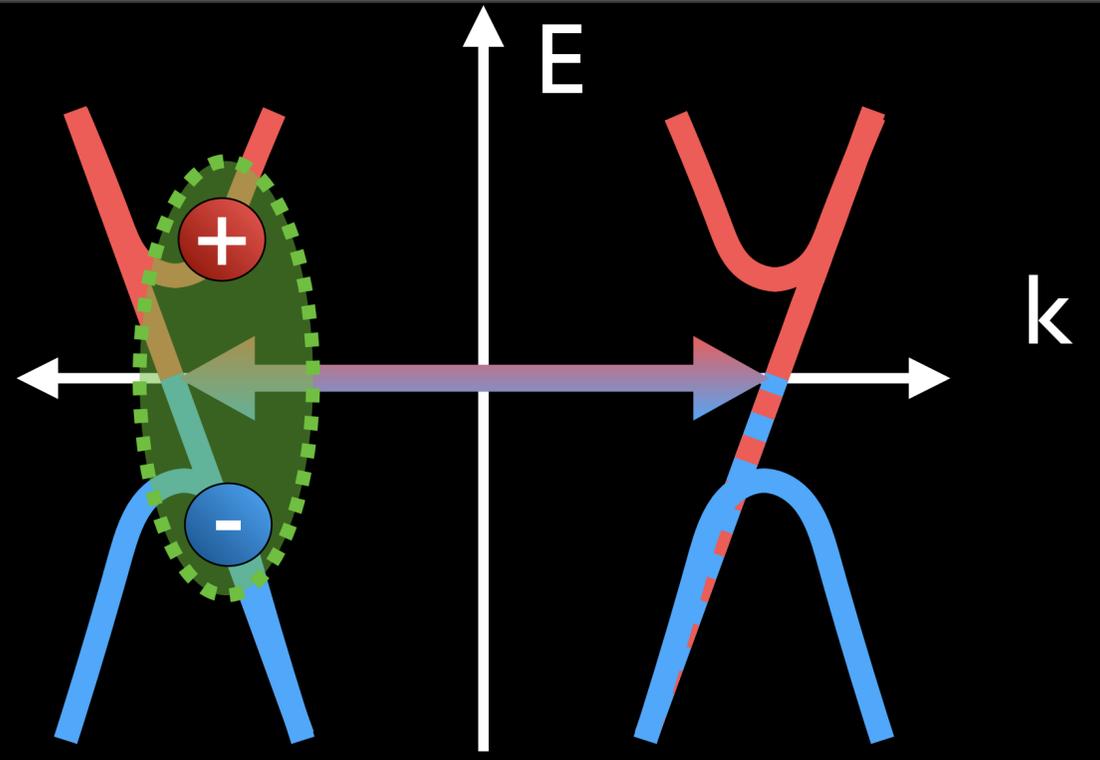
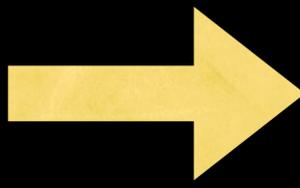
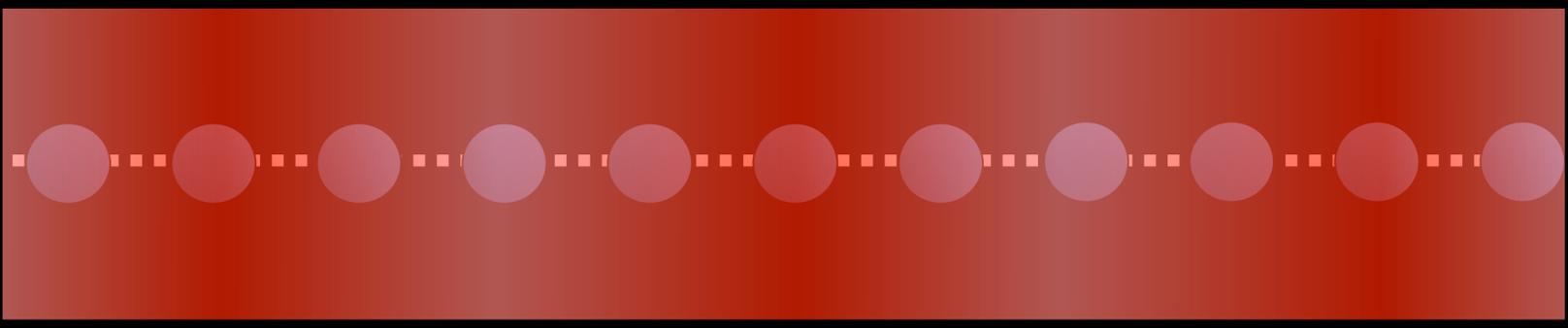


Science 345, 1145 (2014)

Square Scattering

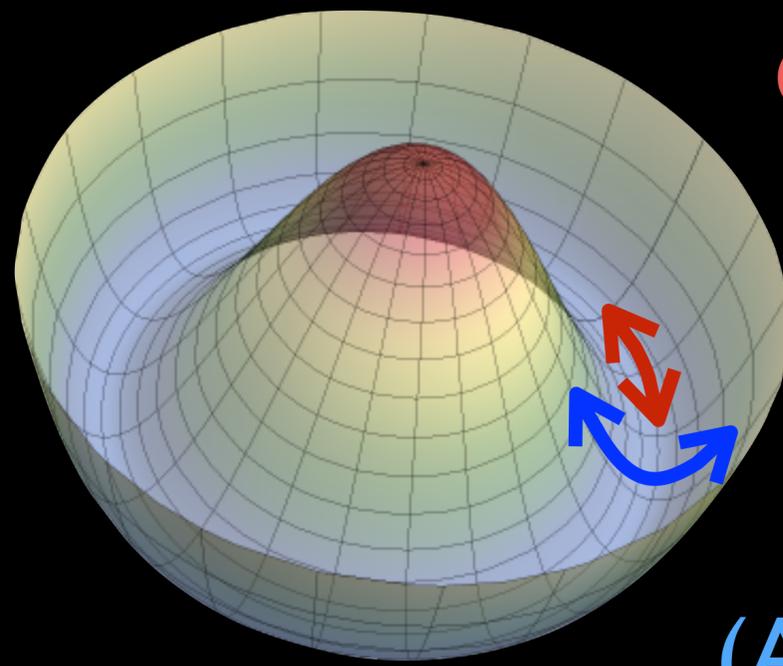
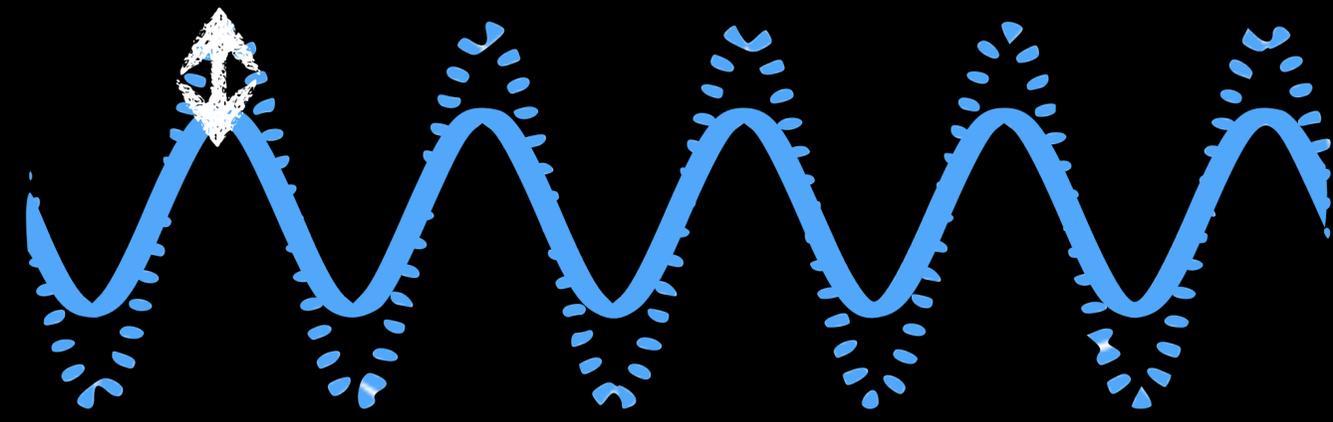
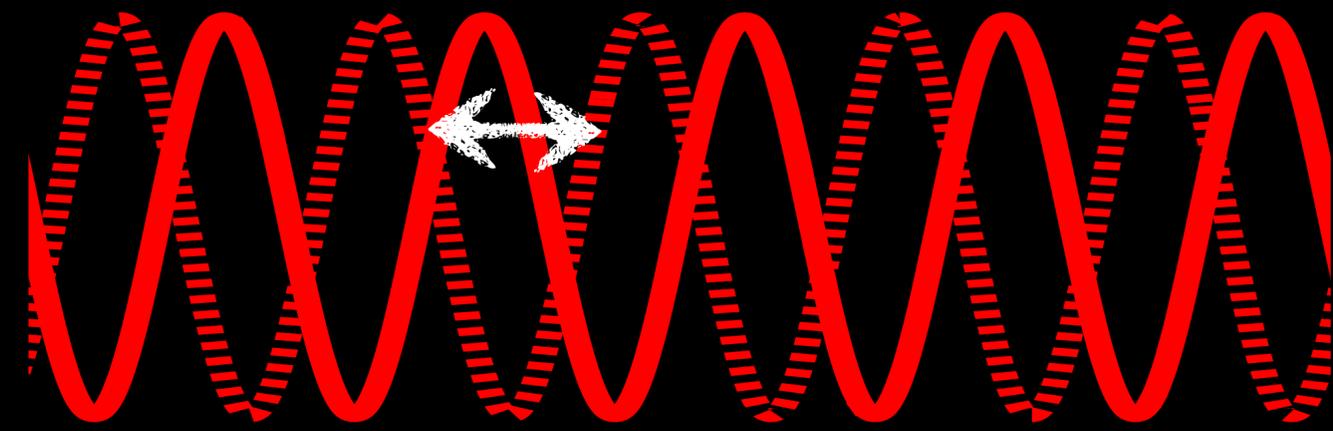
Charge Density Waves

Fröhlich (1954) and Peierls (1955)



G. Gruner, RMP (1988)

M.D Johannes, I. Mazin PRB 2008



Goldstone (Phason)

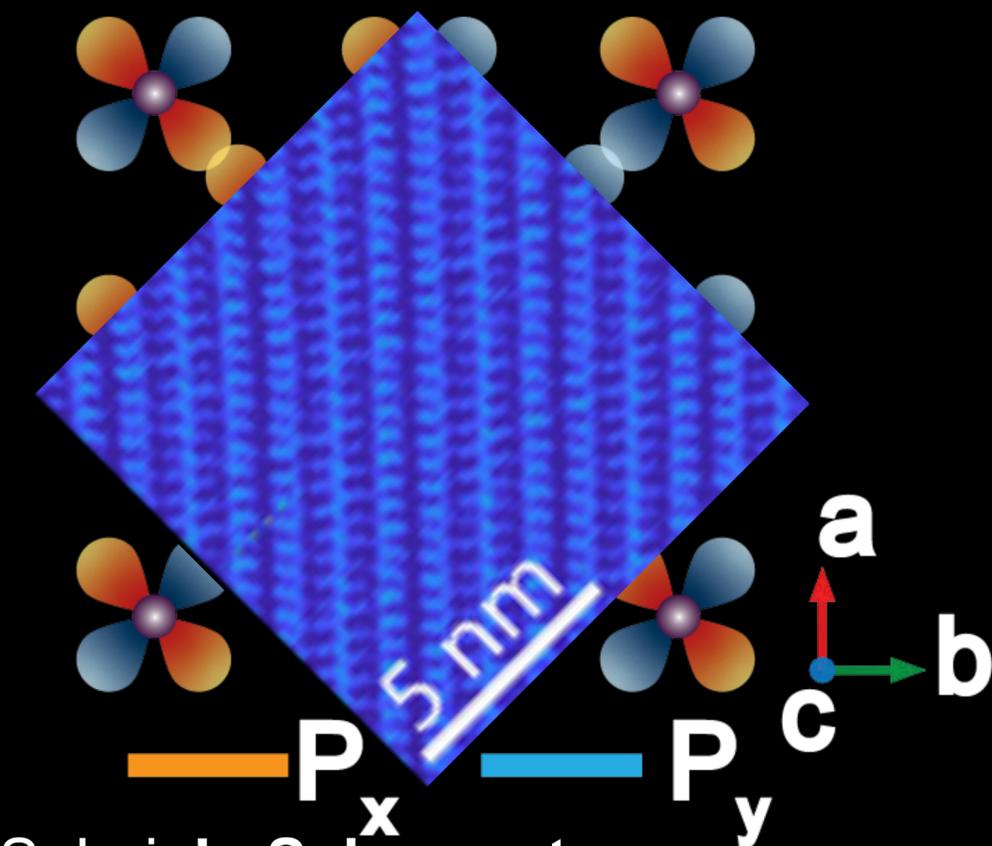
Higgs (Amplitudon)

- Particle-Hole

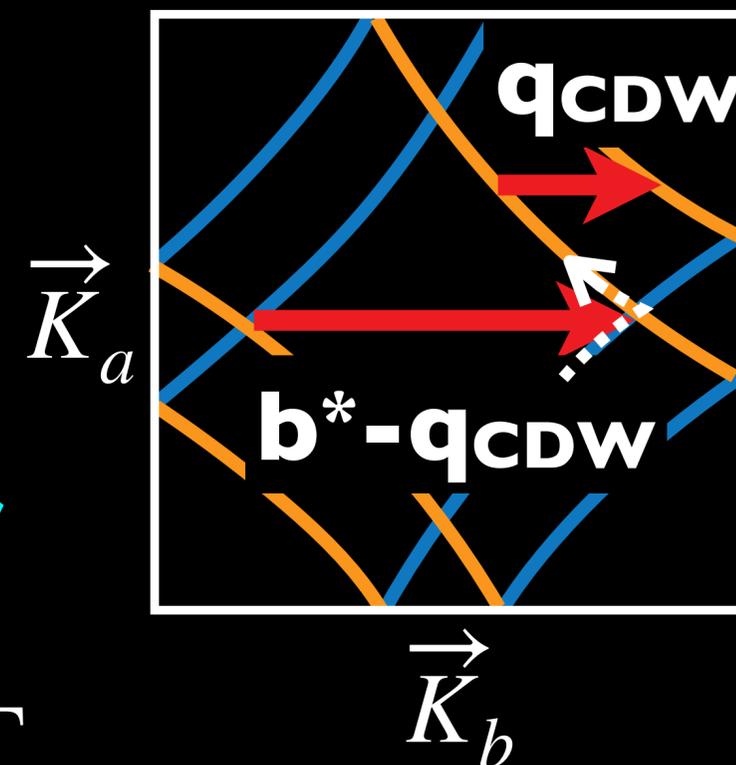
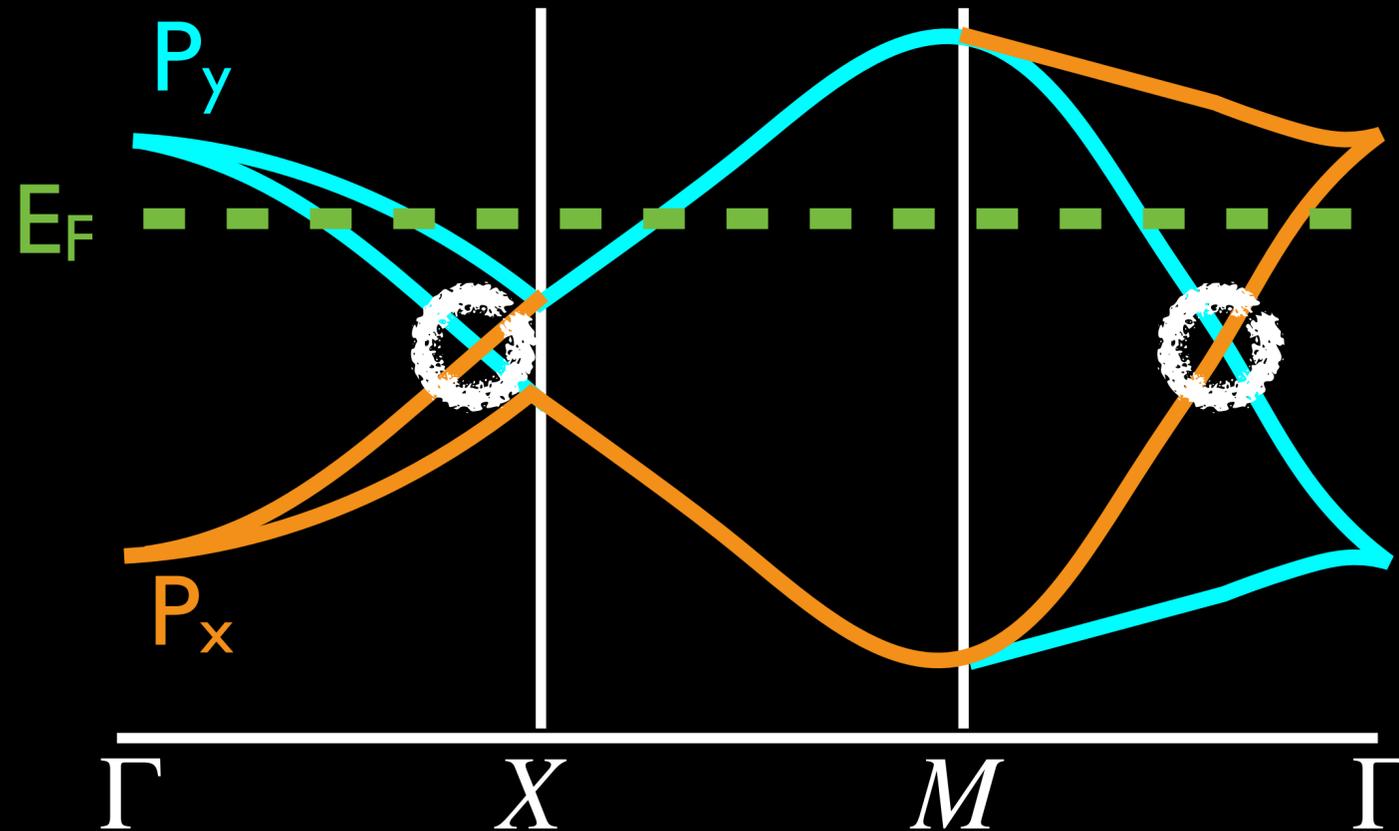
- High T/E

- Applications

A. Balandin, et al,
 APL (2021)



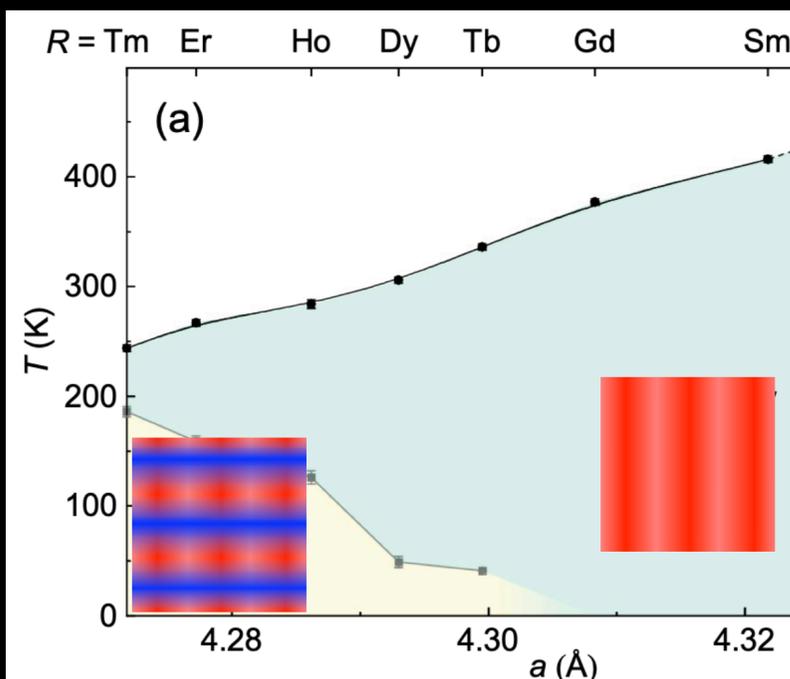
S. Lei, L. Schoop et al
 Sci. Adv. (2020)



S. Klemenz, J. Cano, L. Schoop et al
 JACS (2020)

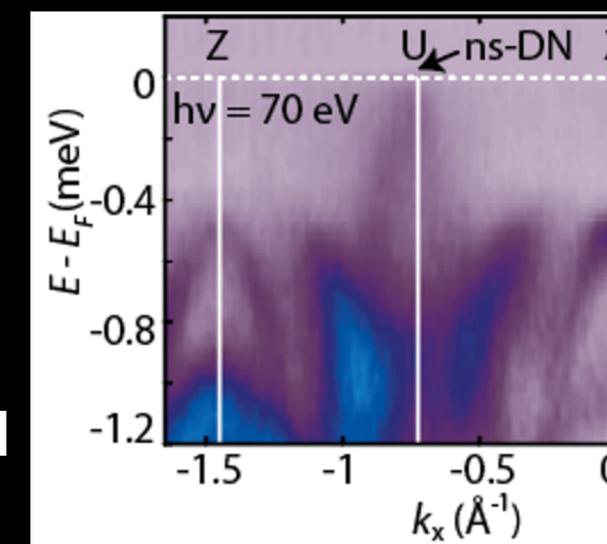
LnTe₃

P. Walmsley,
 I. Fisher et al,
 PRB 102, 045150
 (2020)



LnSb_xTe_{2-x}

S. Lei, L. Schoop et al
 Adv. Materials (2021)



A Postpandemic Tool

$$\vec{P} = \alpha \vec{E} = \left(\alpha_0 + \frac{d\alpha}{d\hat{O}} \delta \hat{O} \right) \vec{E}$$

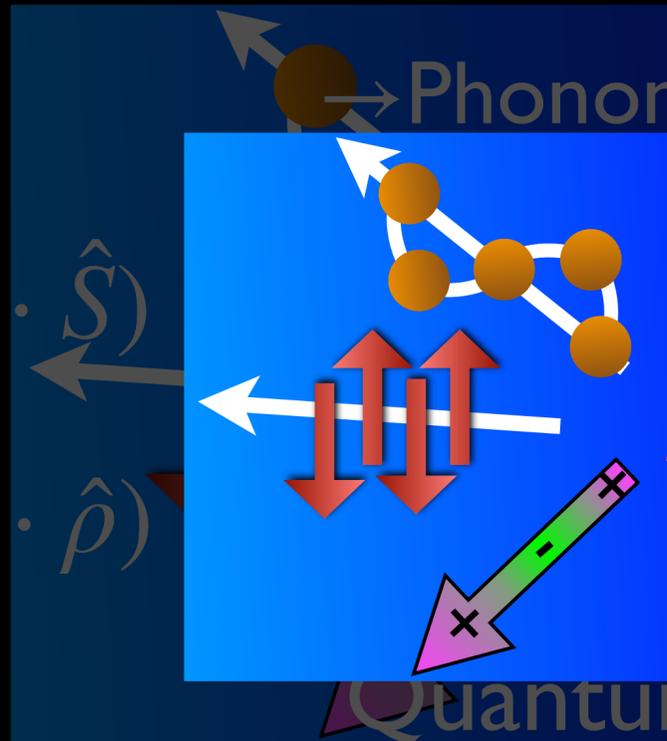
Absorption/Reflectance

$$I_{ij}(\omega) = |\hat{e}_i \cdot R_{ij} \cdot \hat{e}_j|^2 \rightarrow \text{Symmetry}$$

$$\hat{O} = \hat{a} \rightarrow \text{Phonon}$$

$$\hat{O} = f(\hat{S} \cdot \hat{S})$$

$$\hat{O} = f(\hat{\rho} \cdot \hat{\rho})$$



1918-1920: Spanish Flu

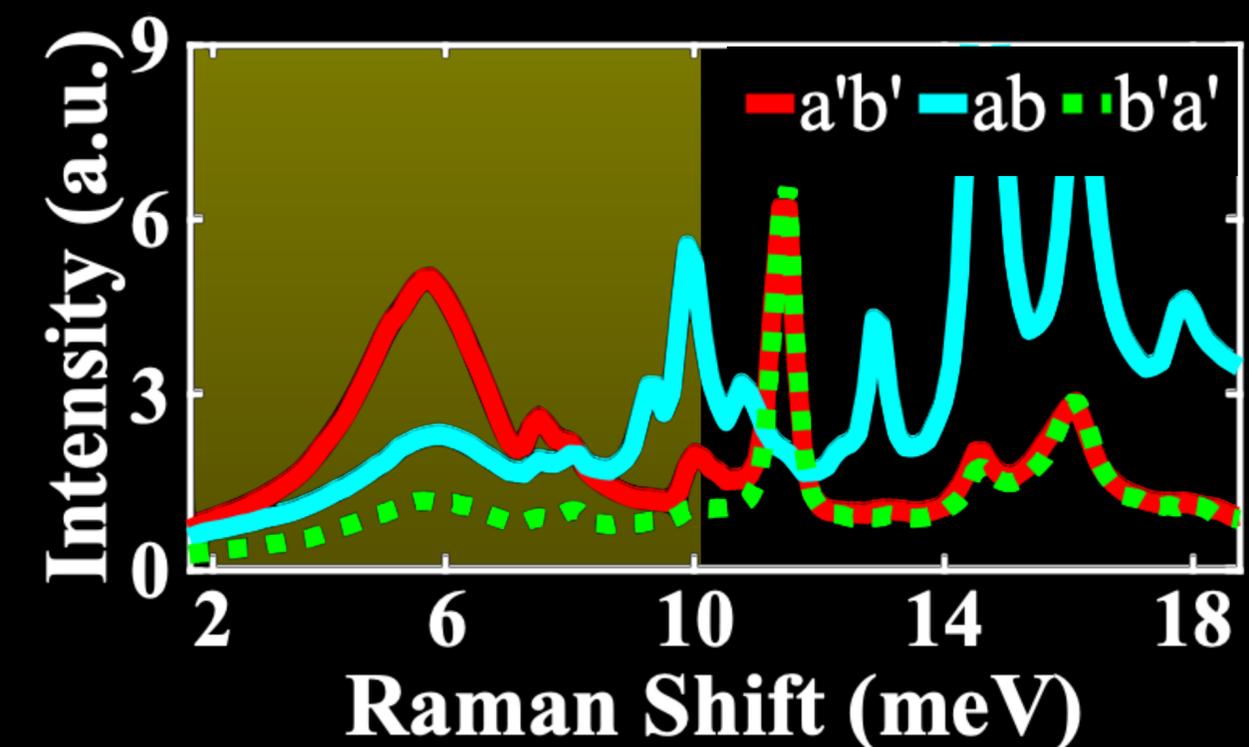
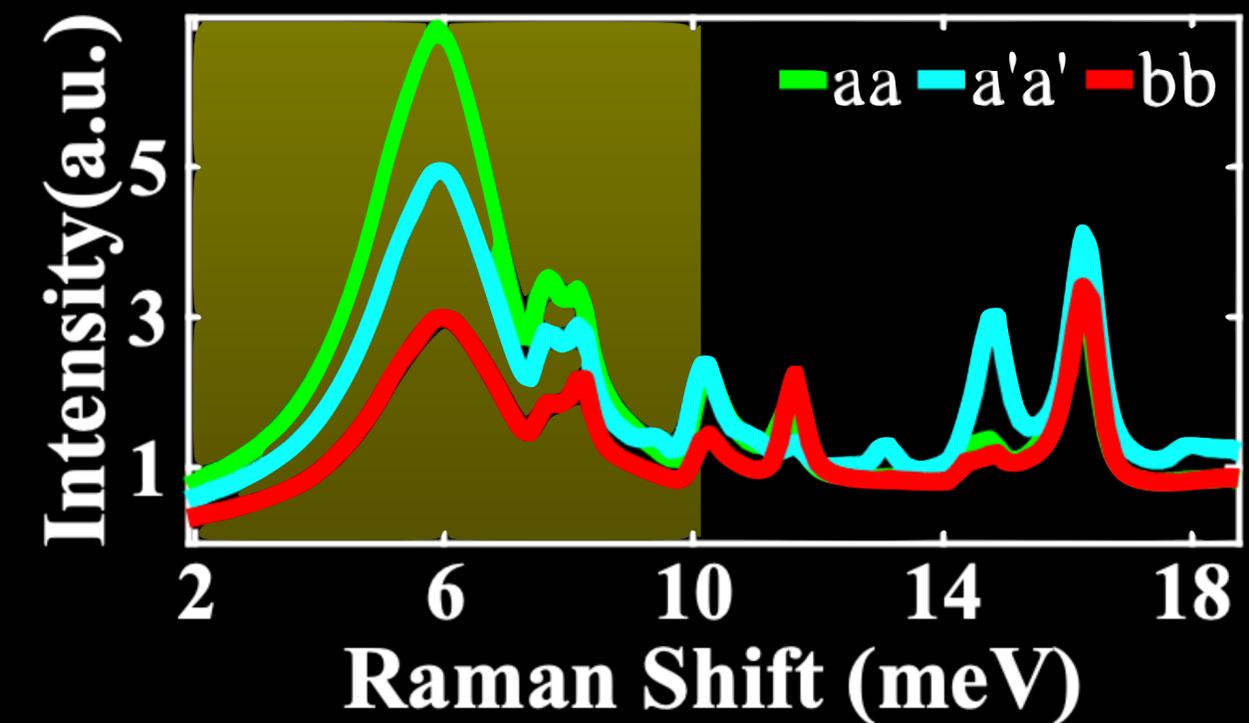
1922: Raman to Mediterranean

Peer Pressure in the Lab



PRB 13, 169 (1976)
 Proc. Phys. Soc. 86, 699 (1965)
 T. Devereaux Rev. Mod Phys. 79, 175 (2007)

Interference



Phonons

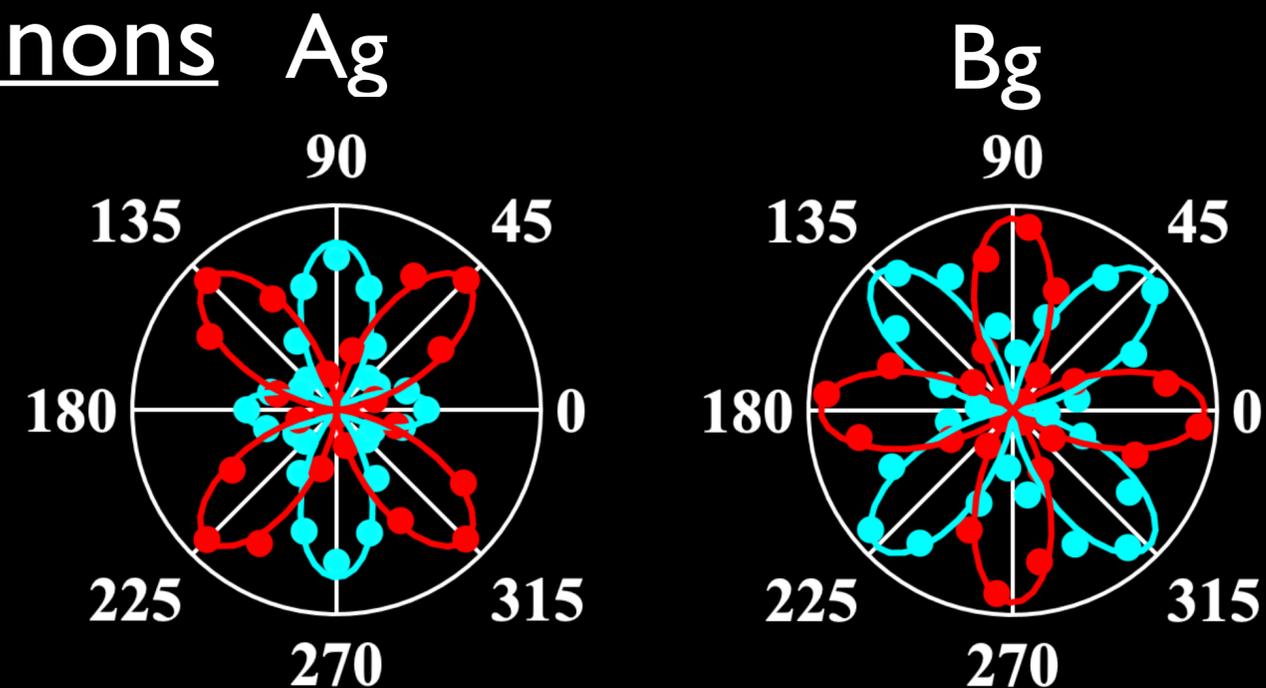
$$\hat{e}_i \parallel \hat{e}_s$$

$$\hat{e}_i \perp \hat{e}_s$$

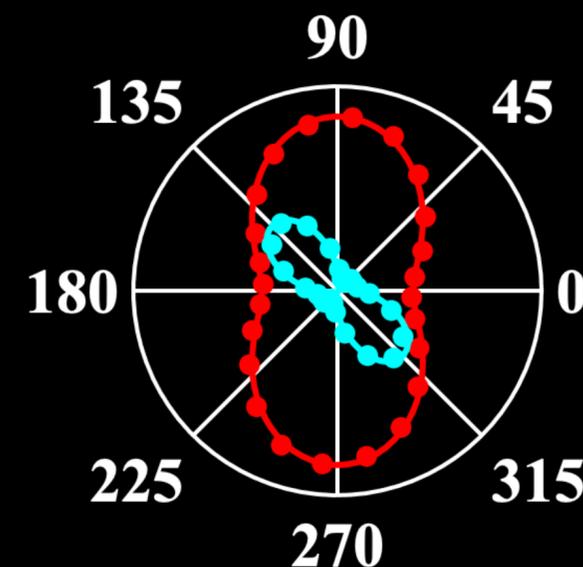
a'



Y. Wang, L. Schoop, KSB et al
 (Nature - 2022)



Amplitude Mode



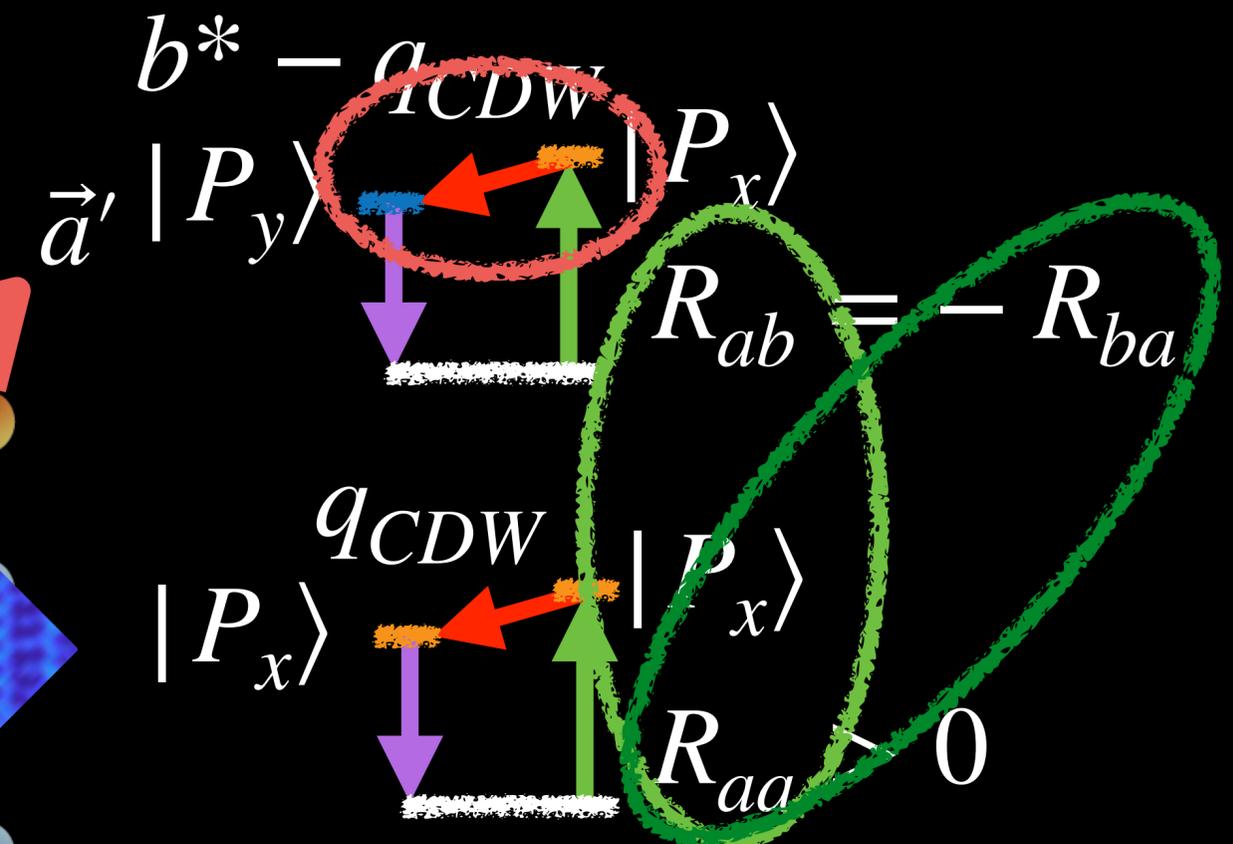
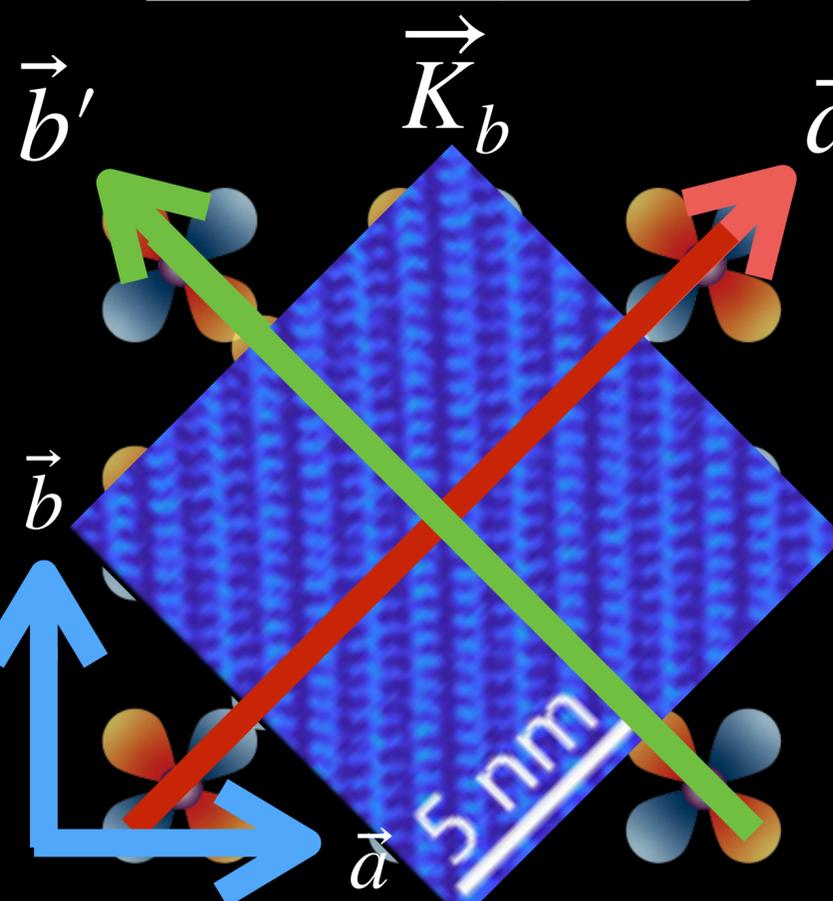
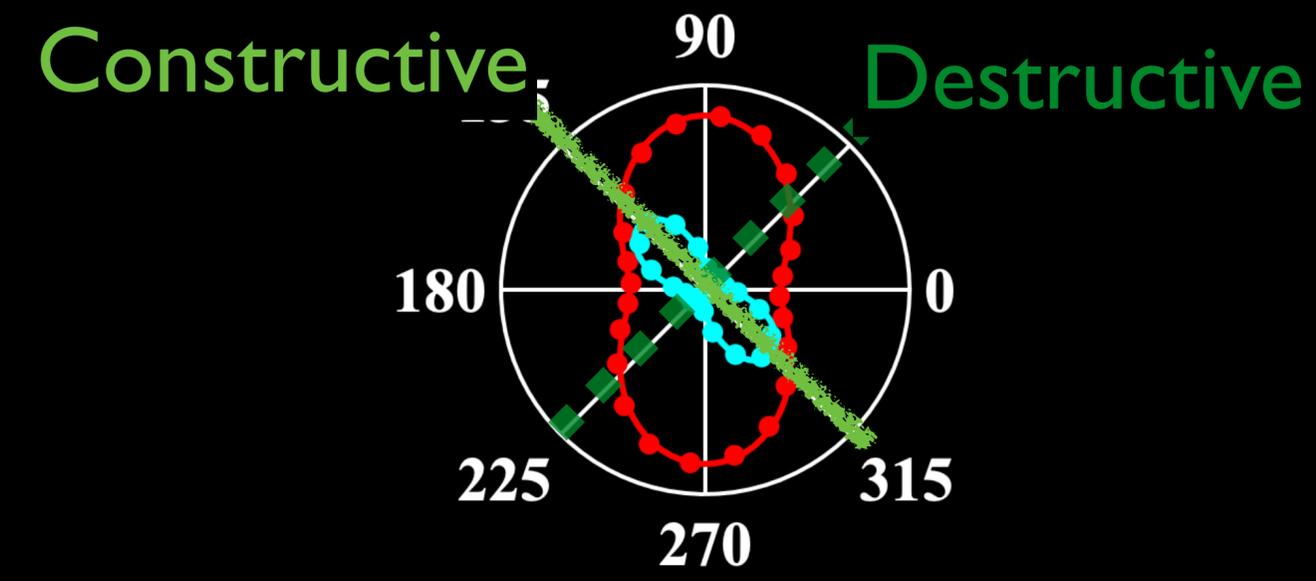
XX vs. YY:
 H.-M. Eiter, T. Devereaux, L. Degiorgi et al (PNAS - 2013)

Amplitude Mode



$$\hat{e}_i \parallel \hat{e}_s$$

$$\hat{e}_i \perp \hat{e}_s$$



Room T
in LaTe₃ & GdTe₃

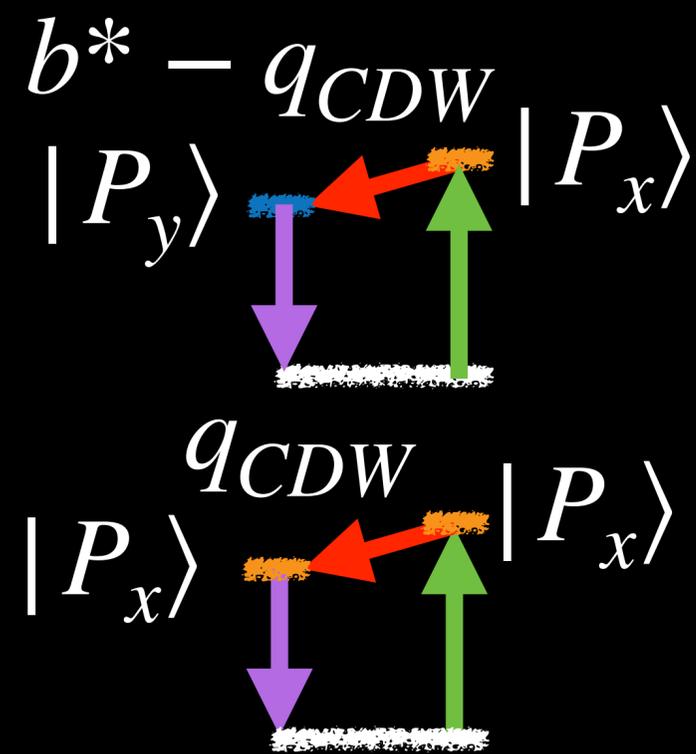
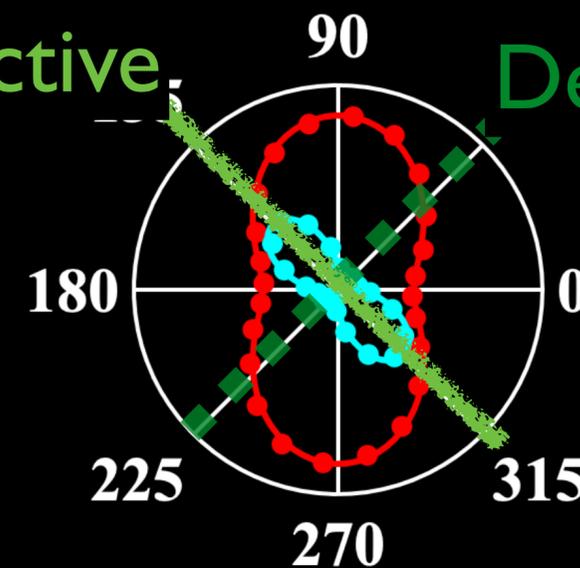
Y. Wang, L. Schoop, KSB et al
 (Nature - 2022)

Highlights

- What microscopically sets the phase?
- Unconventional CDW?
- CDW & Quantum Geometry?
- Sliding CDW + Topology?
- Quantum Optics for Quantum Materials?

Amplitude Mode

Constructive Destructive

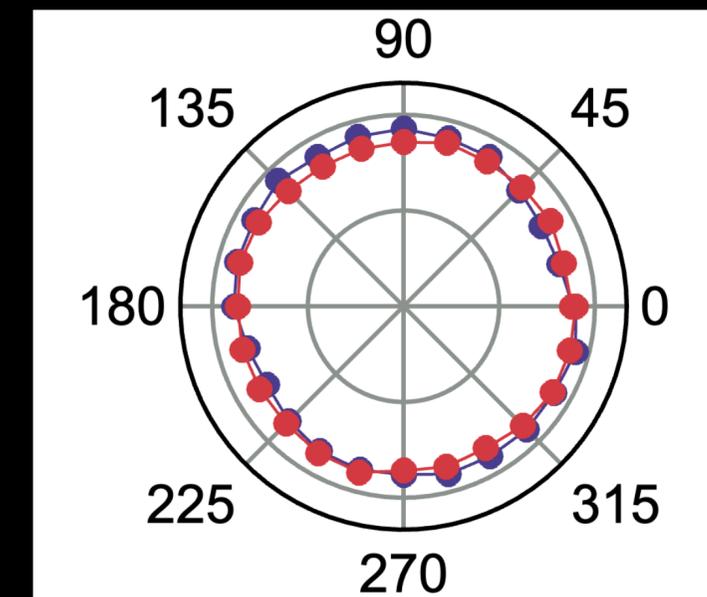
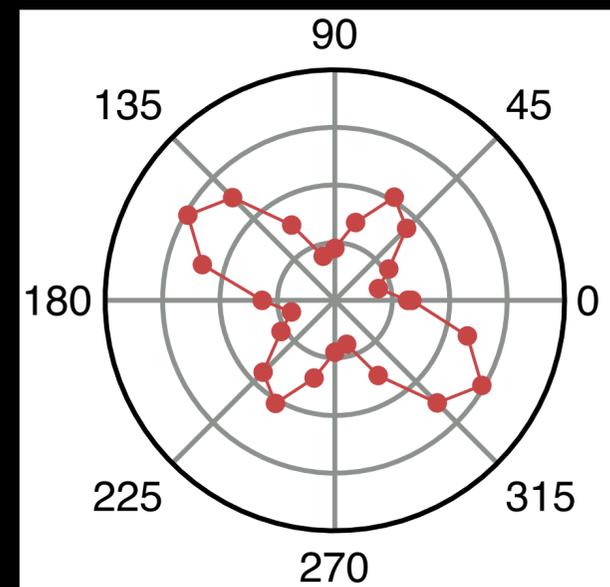
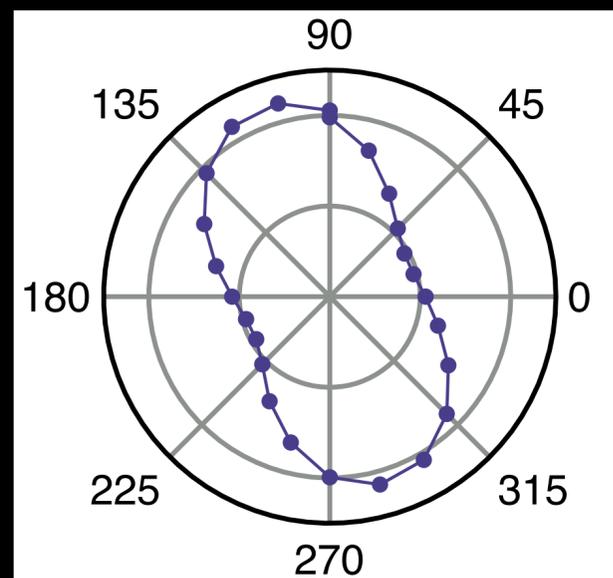
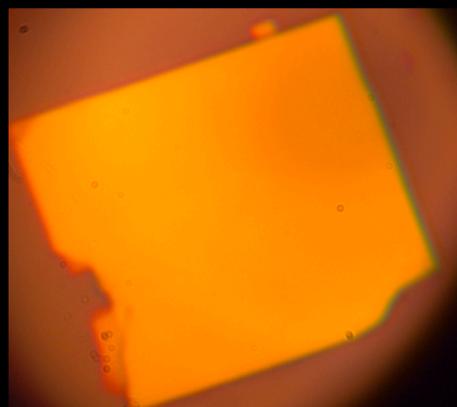
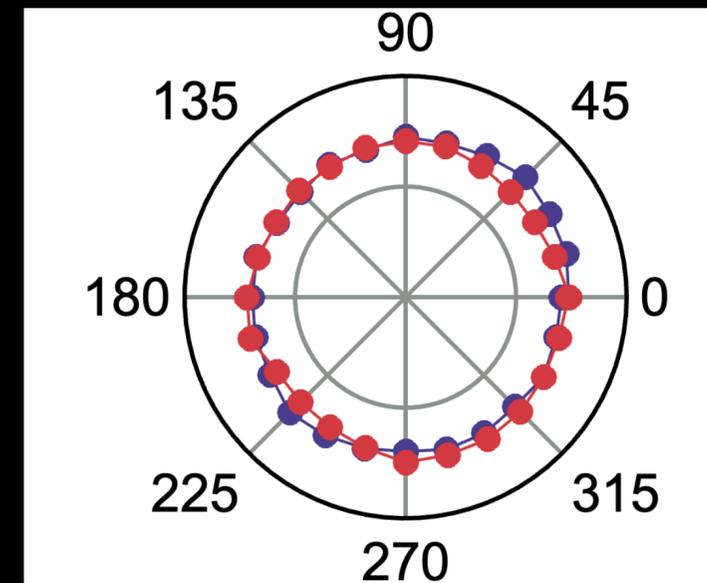
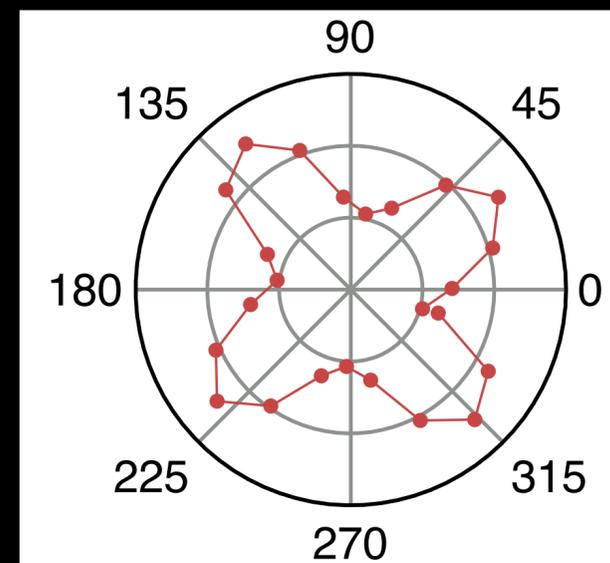
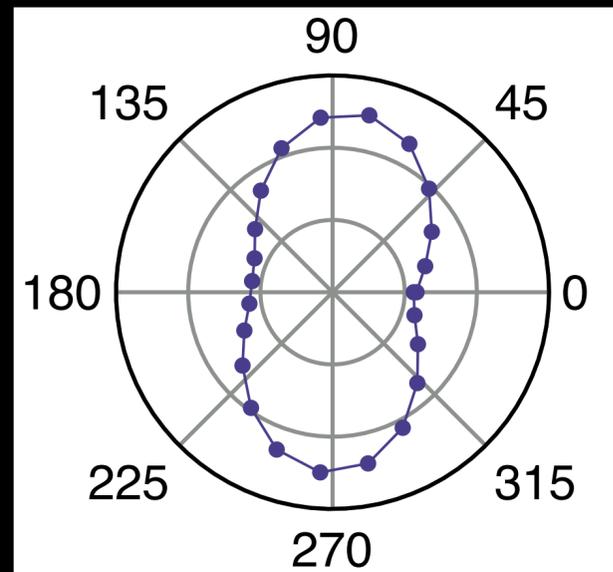
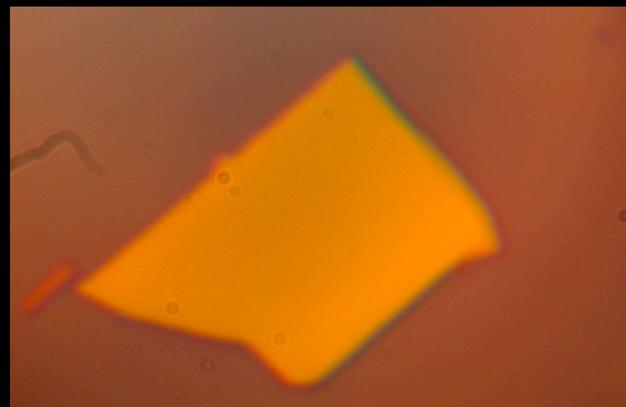


Domains?

$$\hat{e}_i \parallel \hat{e}_s$$

$$\hat{e}_i \perp \hat{e}_s$$

$$\sigma^+ \sigma^- \quad \sigma^- \sigma^+$$

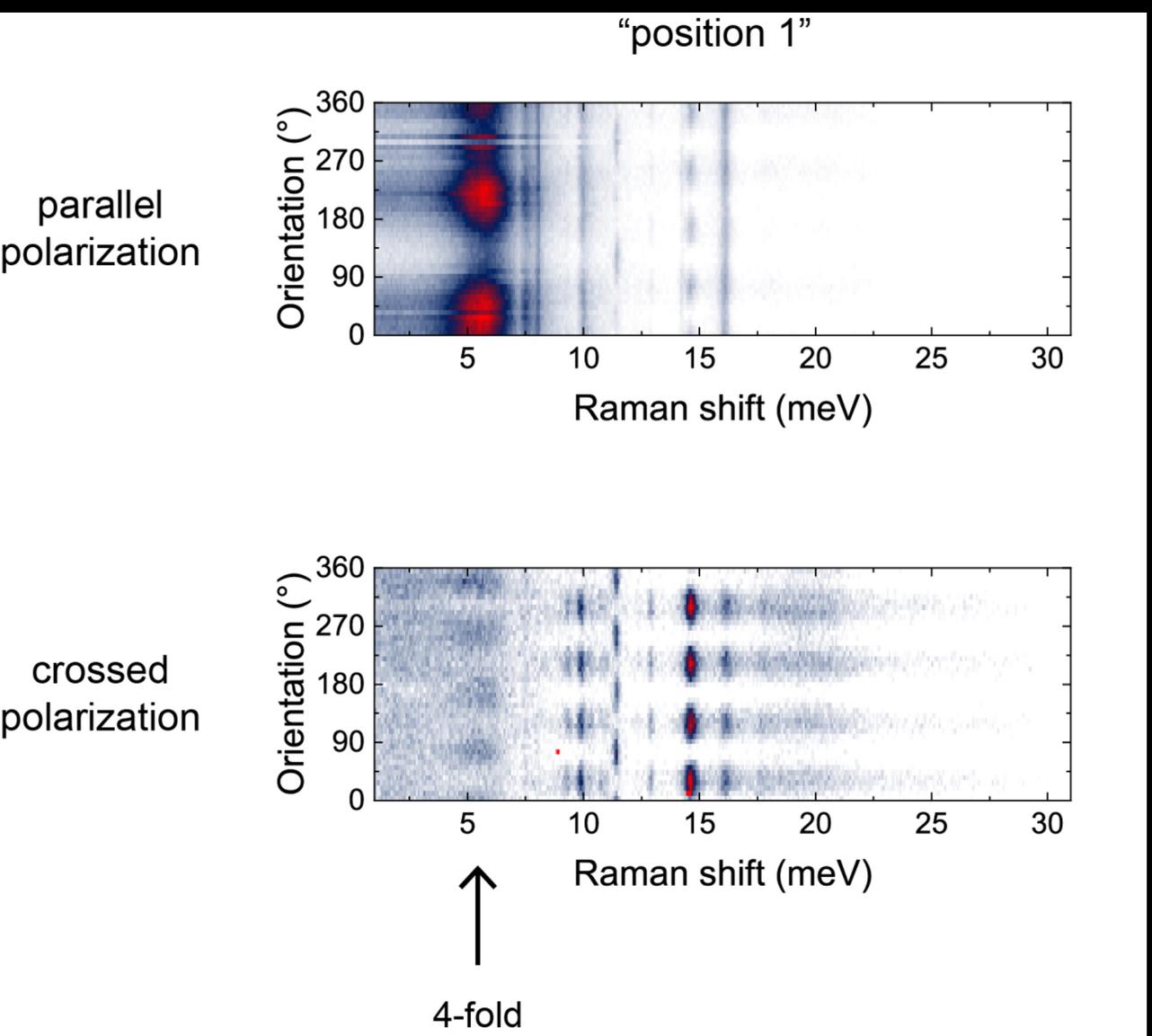


● Higgs

● Square Scattering

● Interference

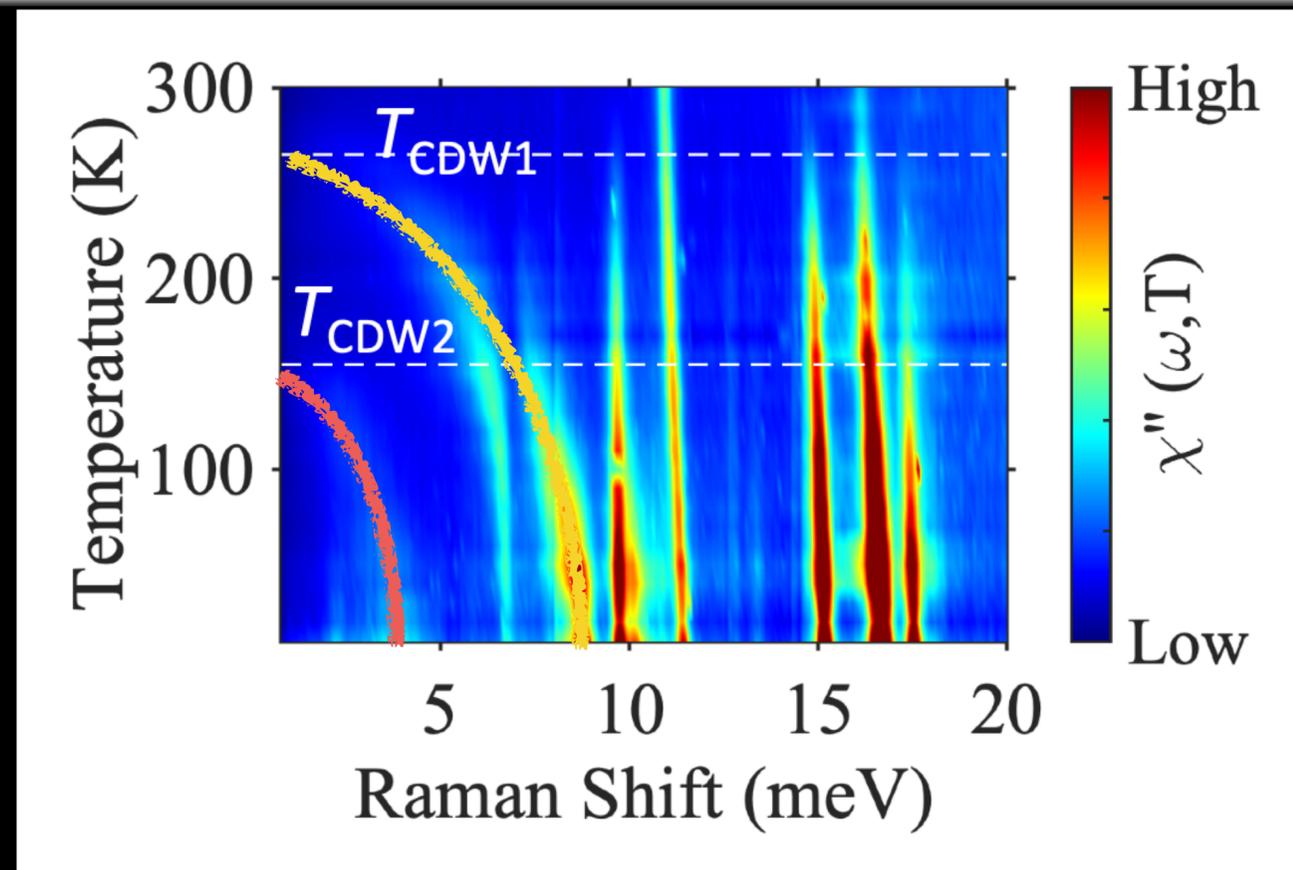
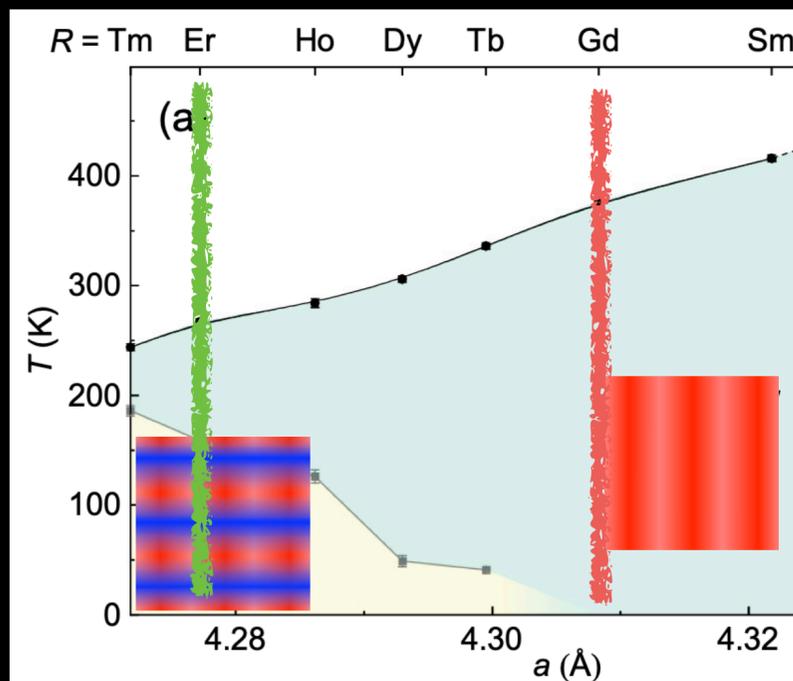
● Highlights



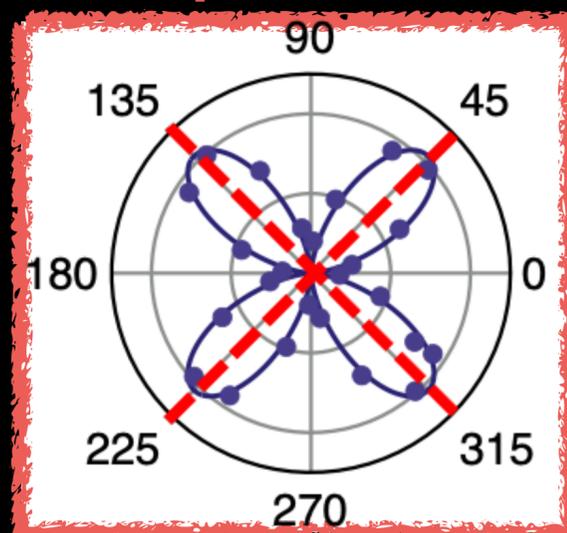
Dirk Wulferding and Changyoung Kim (SNU)

LnTe₃

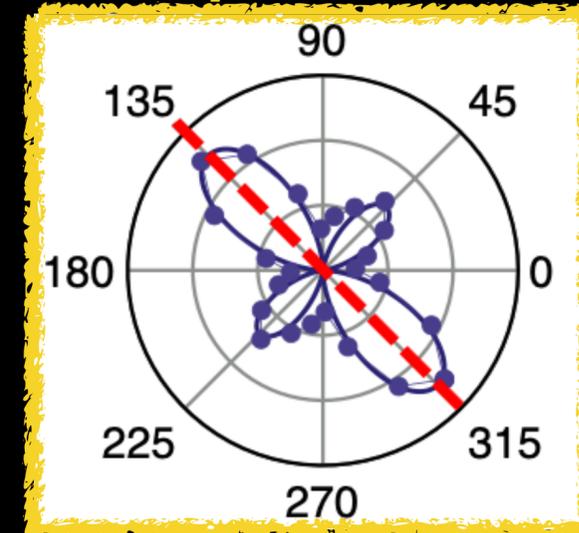
P. Walmsley,
 I. Fisher et al,
 PRB 102, 045150
 (2020)



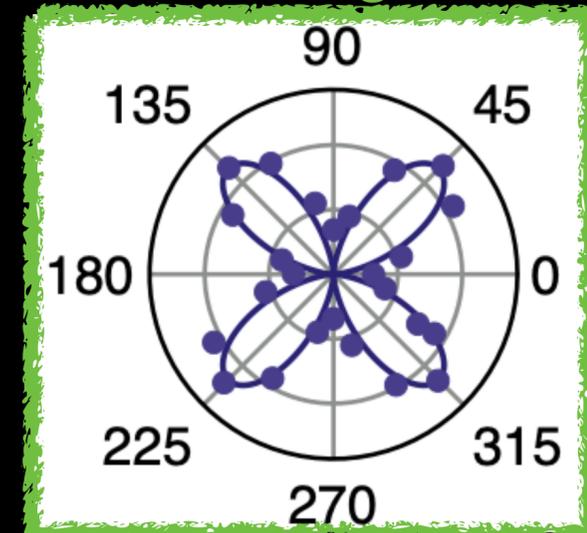
Amplitude 2



Amplitude 1



A_g



LASE Team

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B. Singh

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M. Romanelli (UIUC)

M. Hosen (Intel)

N. Kumar (Giner)

M. Gray (Resonant)

R. O'Connor (Tufts)

E. Sheridan (AFRL)



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LnTe₃

S. Lei (Rice)

L. Schoop (Princeton)

Theory:

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P. Narang (UCLA)

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J. Hart

J.J. Cha

Raman (UMass):

Y.C. Wu

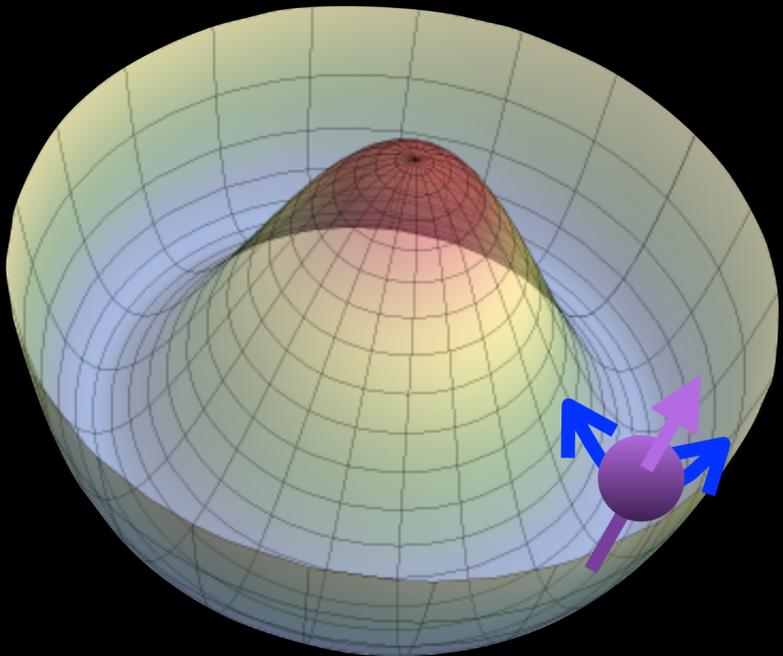
J. Yan



Higgs

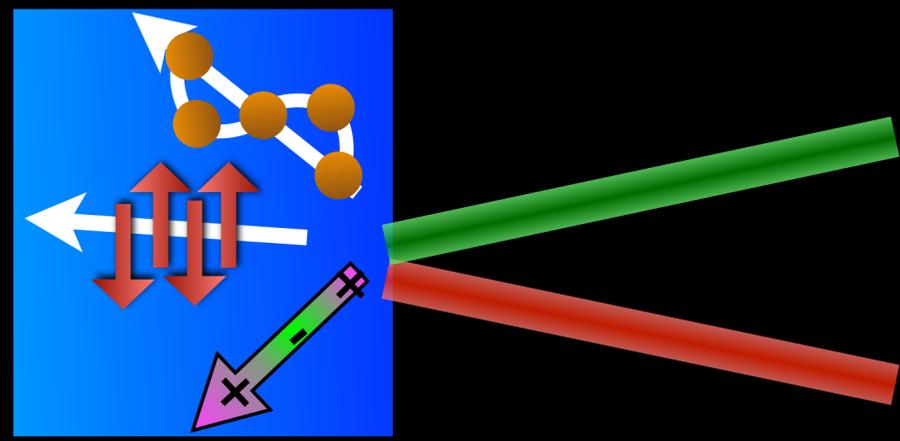
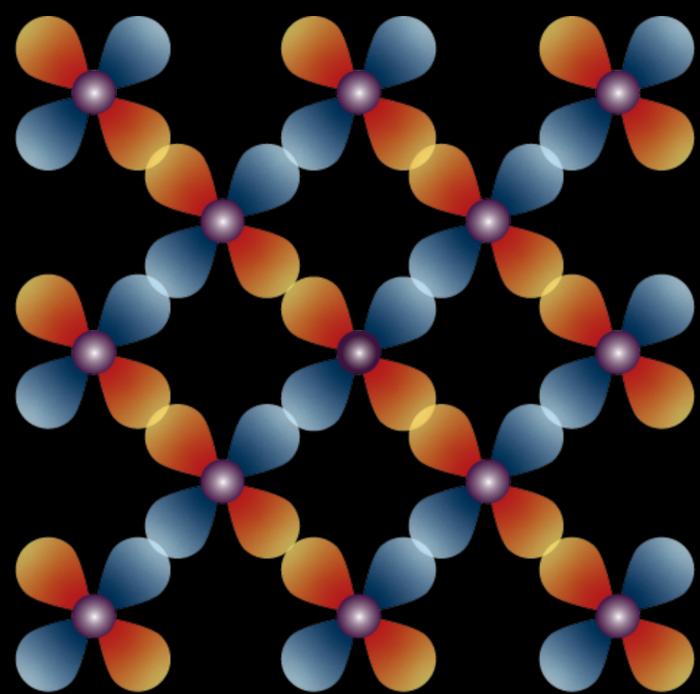


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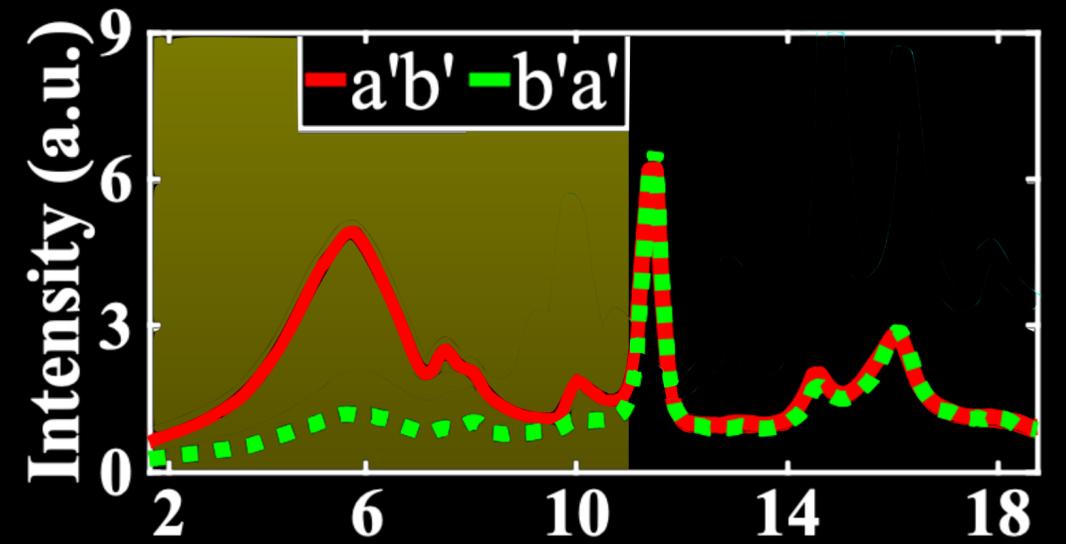
ks.burch@bc.edu
@Burch_Lab

Summary

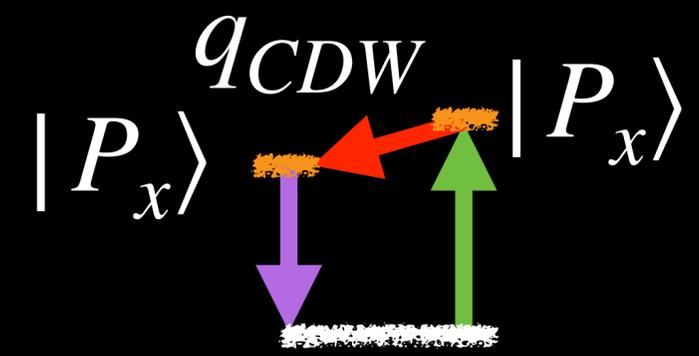
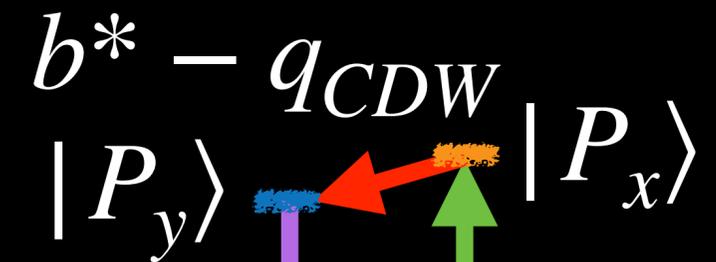


Square Scattering

Interference



Raman Shift (meV)



Y. Wang, KSB et al, Nature (2022)

Interference effects: A key to understanding forbidden Raman scattering by LO phonons in GaAs

José Menéndez and Manuel Cardona

Max-Planck-Institut für Festkörperforschung, Heisenbergstrasse 1, D-7000 Stuttgart 80, Federal Republic of Germany

(Received 22 October 1984)

$$\vec{\mathbf{R}}_{\text{DP}} = \begin{pmatrix} 0 & a_{\text{DP}} & 0 \\ a_{\text{DP}} & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}. \quad (1)$$

In addition, the forbidden LO-phonon Raman scattering tensor is given (via the Fröhlich interaction) by

$$\vec{\mathbf{R}}_F = \begin{pmatrix} a_F & 0 & 0 \\ 0 & a_F & 0 \\ 0 & 0 & a_F \end{pmatrix}. \quad (2)$$

The scattering efficiency is therefore proportional to

$$\frac{dS}{d\Omega}$$

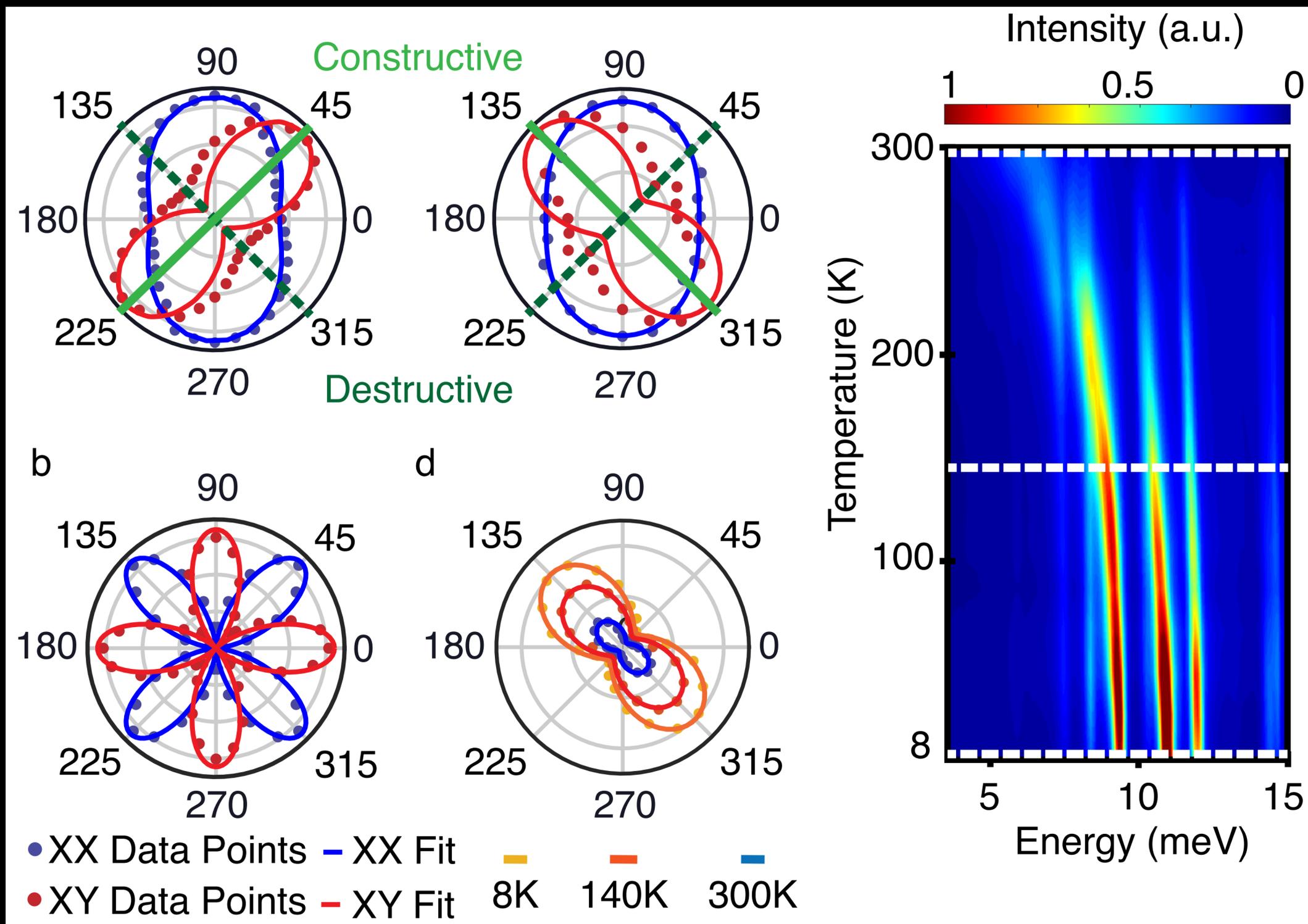
$$\propto \begin{cases} |a_F + a_{\text{DP}}|^2 & \text{for the } z(x',x')\bar{z} \text{ configuration,} & (3a) \\ |a_F - a_{\text{DP}}|^2 & \text{for the } z(y',y')\bar{z} \text{ configuration,} & (3b) \\ |a_F|^2 & \text{for the } z(x,x)\bar{z} \text{ configuration.} & (3c) \end{cases}$$

MOLECULAR STRUCTURE

Experimental Observation of an Antisymmetric Raman Scattering Tensor

Trivalent Lanthanides Electronic Raman

J.A. Koningstein et al, *Nature* (1968);
J. Chem. Phys. 48, 3971 (1968)

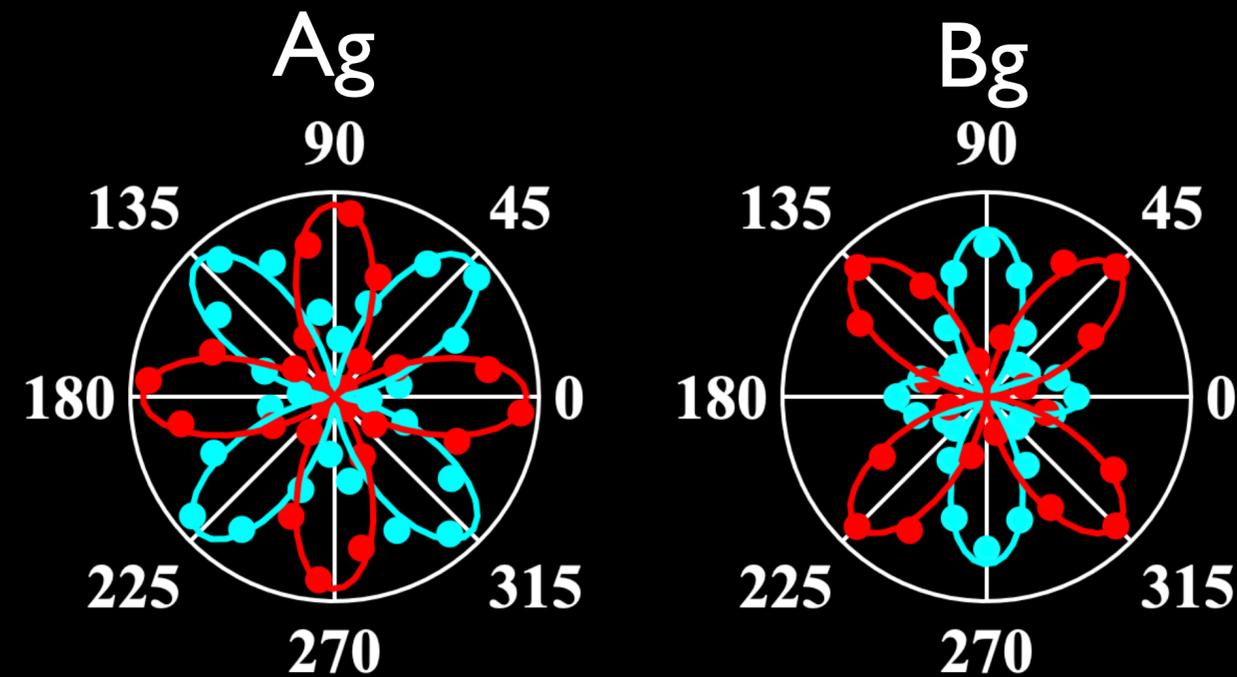
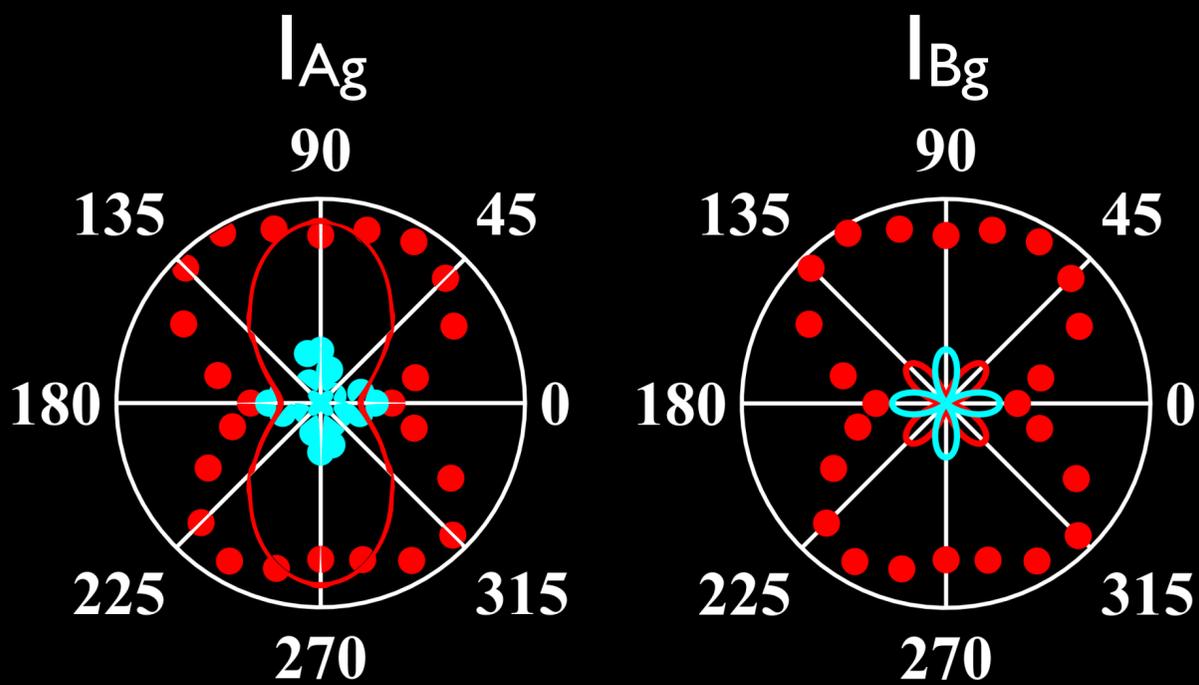


Interference vs Degeneracy

Phonons

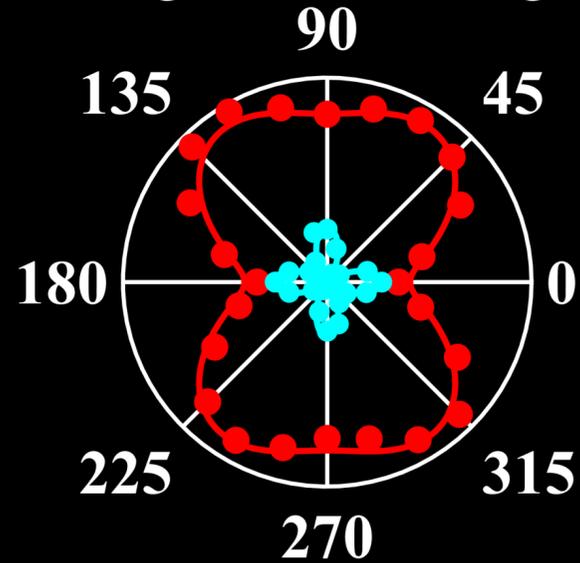
$$\hat{e}_i \parallel \hat{e}_s$$

$$\hat{e}_i \perp \hat{e}_s$$

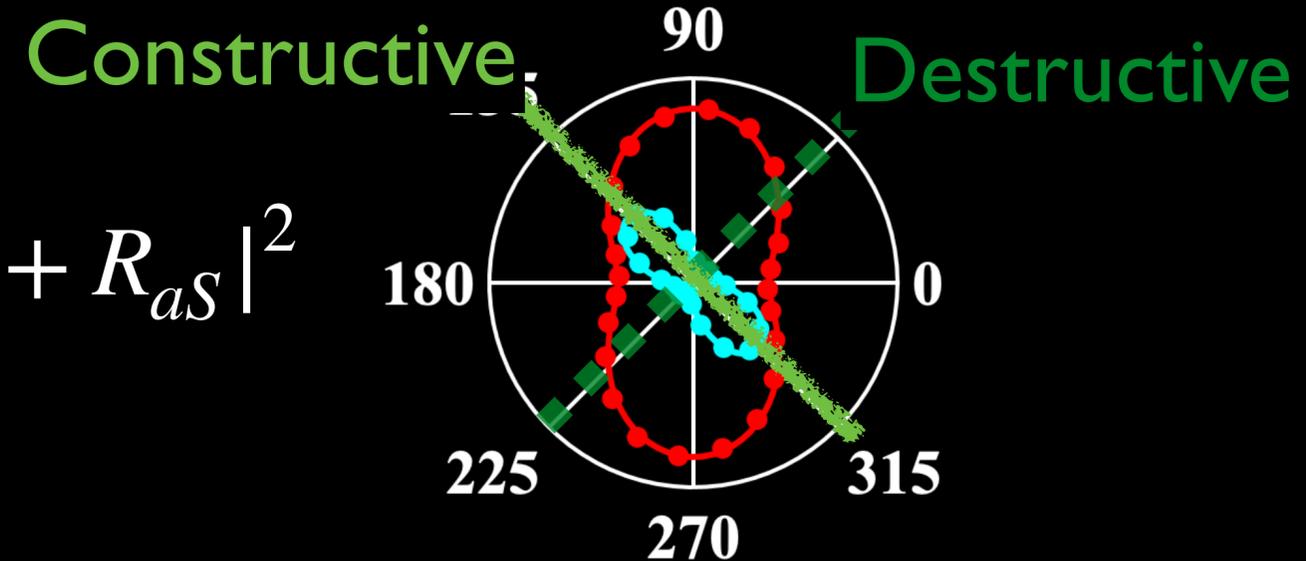


Amplitude Mode

$$I = |R_{Ag}|^2 + |R_{Bg}|^2$$



$$I = |R_{Ag} + R_{aS}|^2$$



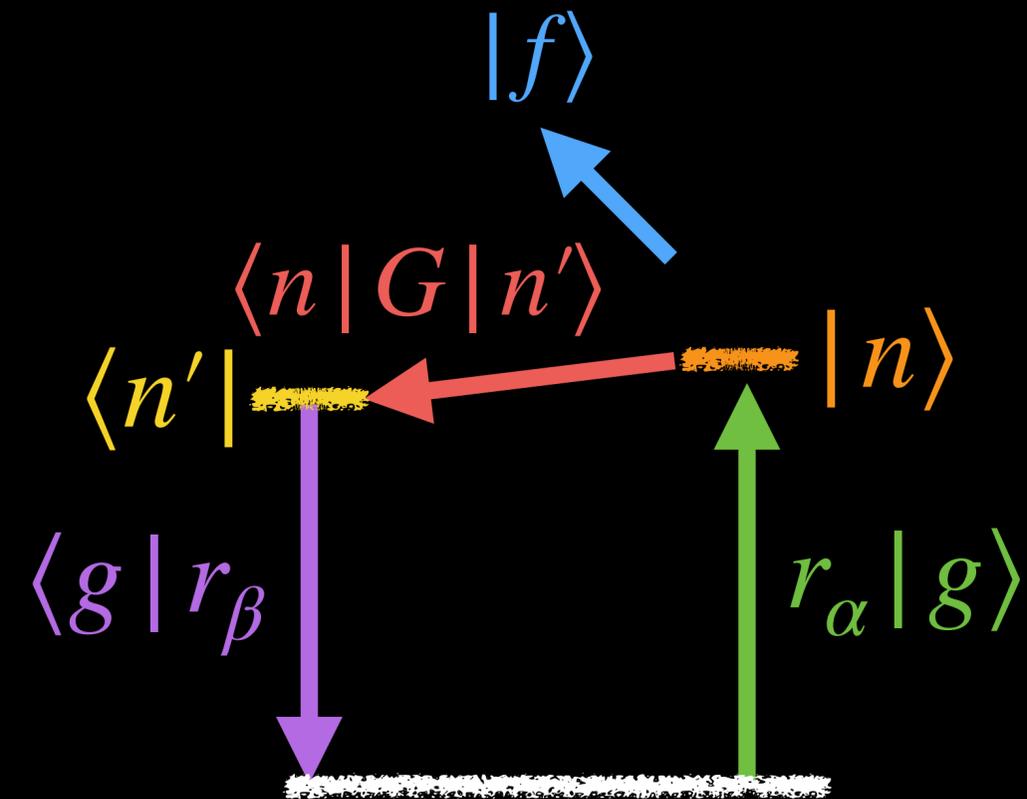
Y. Wang, L. Schoop,
 KSB et al (Nature - 2022)

Interference in Raman

$$\vec{P} = \alpha \vec{E} = \left(\alpha_0 + \frac{d\alpha}{d\hat{O}} \delta \hat{O} \right) \vec{E}$$

$$I_{ij}(\omega) = |\hat{e}_i \cdot R_{ij} \cdot \hat{e}_j|^2$$

$$R_{\alpha\beta} = \sum_{n,n'=1}^2 \langle f | \langle g | e r_\alpha | n \rangle \langle n | G | n' \rangle \langle n' | e r_\beta | g \rangle | i \rangle$$



→ 2 states uncoupled double slits in electronic space

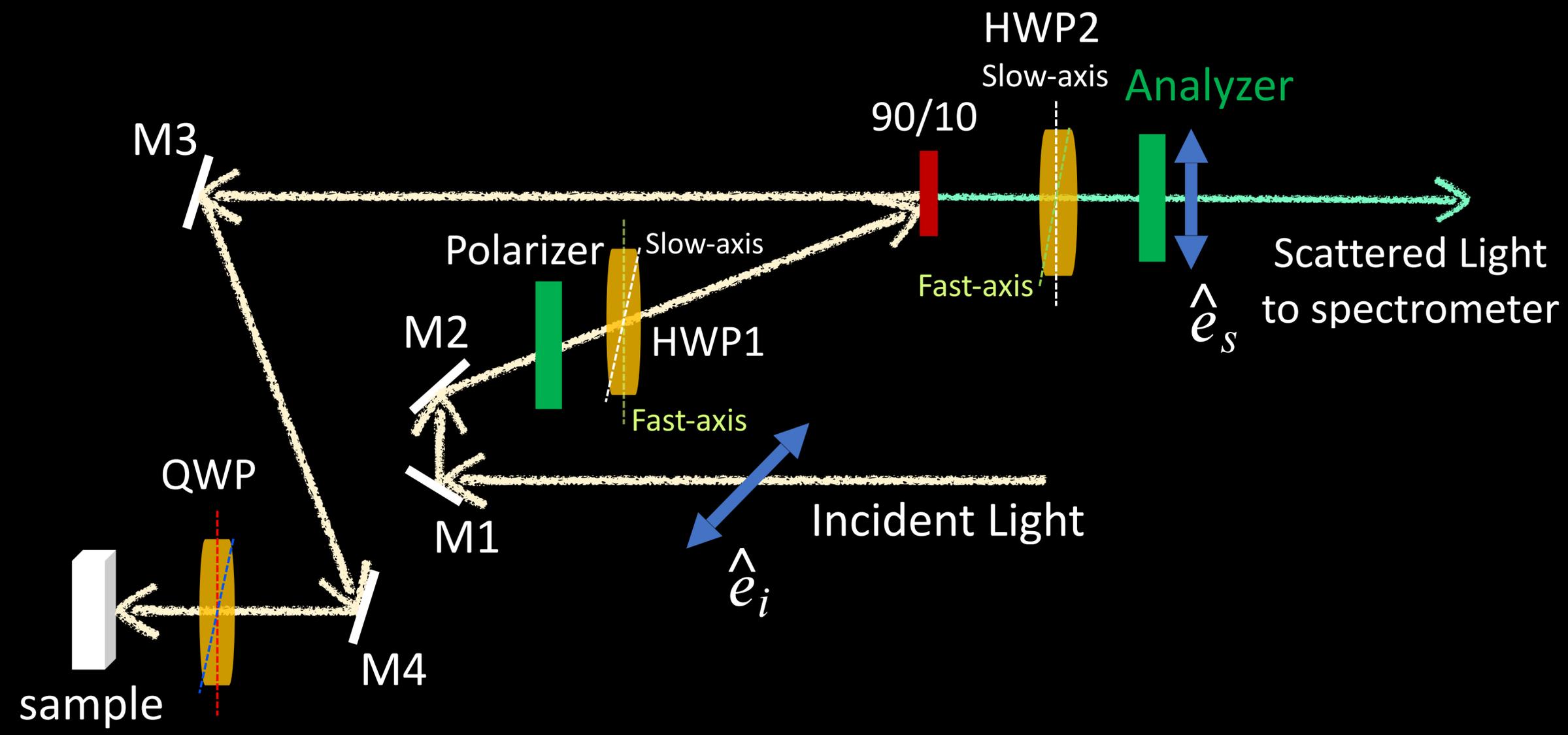
$$G_{nn'} = \delta_{nn'} G_n$$

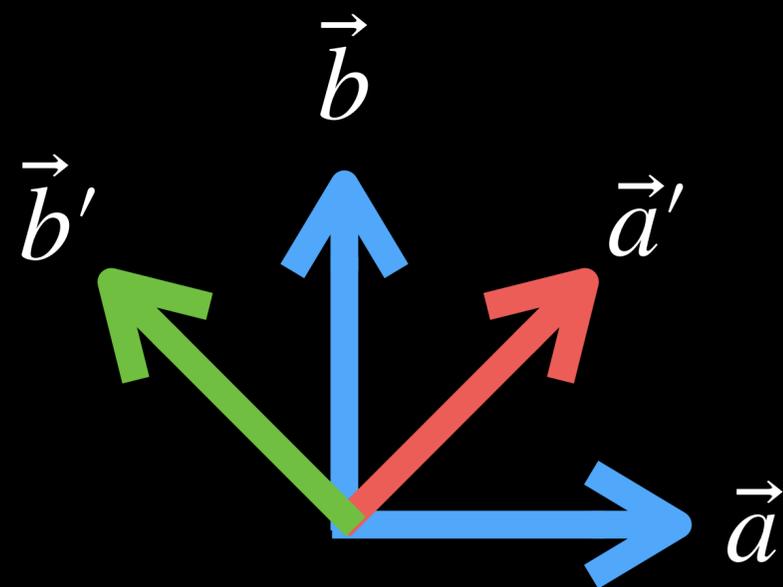
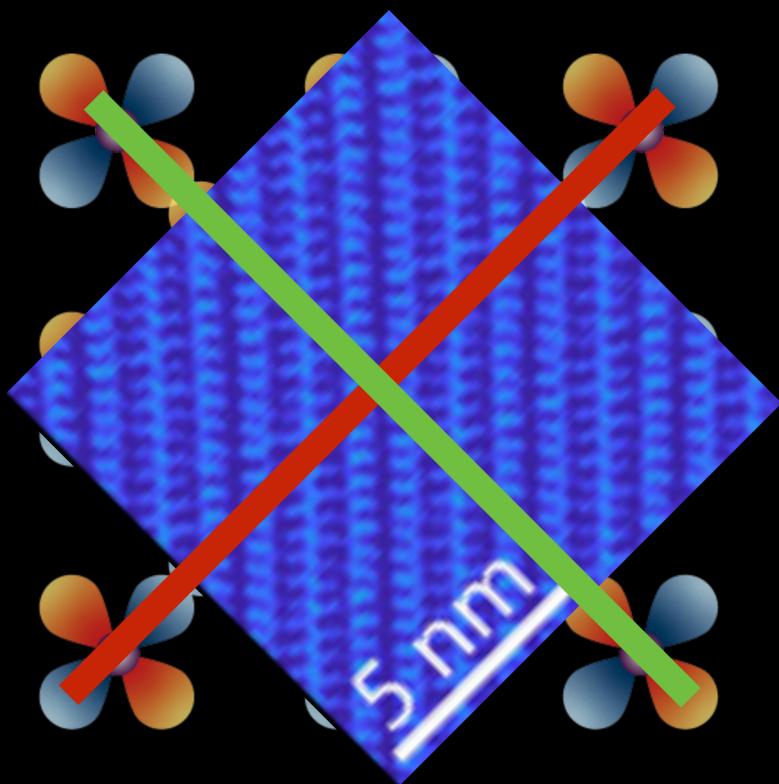
reverse process looks same
 Can tell which path (commute?)

No interference

no coupling between states: $R_{\alpha\beta} = R_{\beta\alpha}$

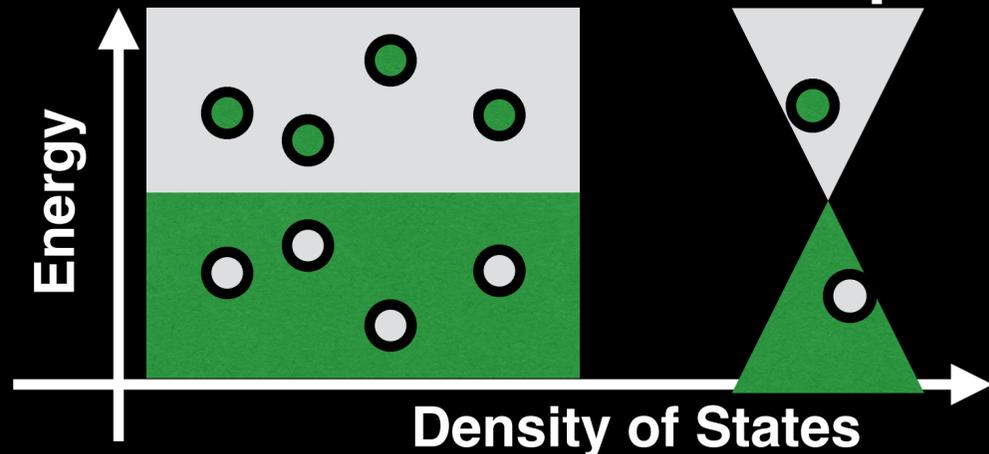
R.A. Harris et al, J. Chem Phys. 96, 15 1992





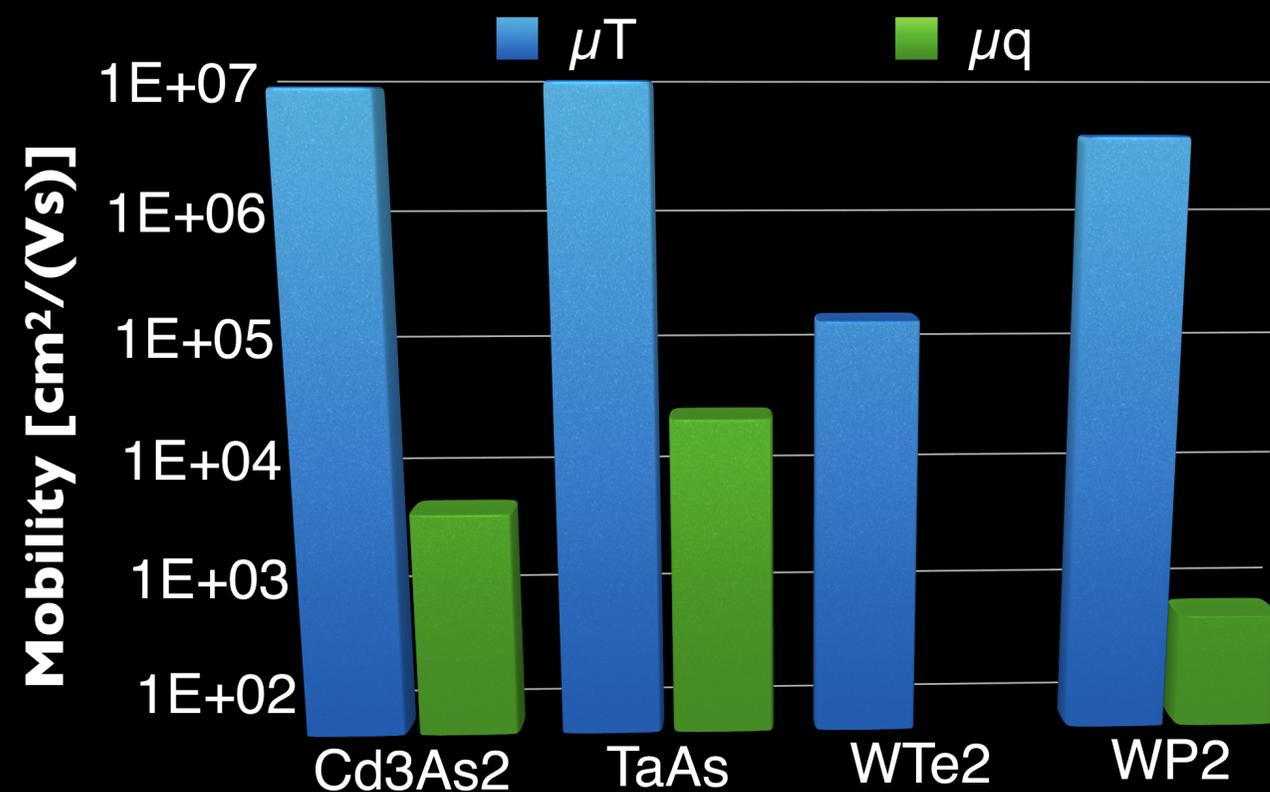
$$R_{ab} = -R_{ba}$$

Reduced Phase Space



“Protected” by Symmetry?

“Protected” by Topology?

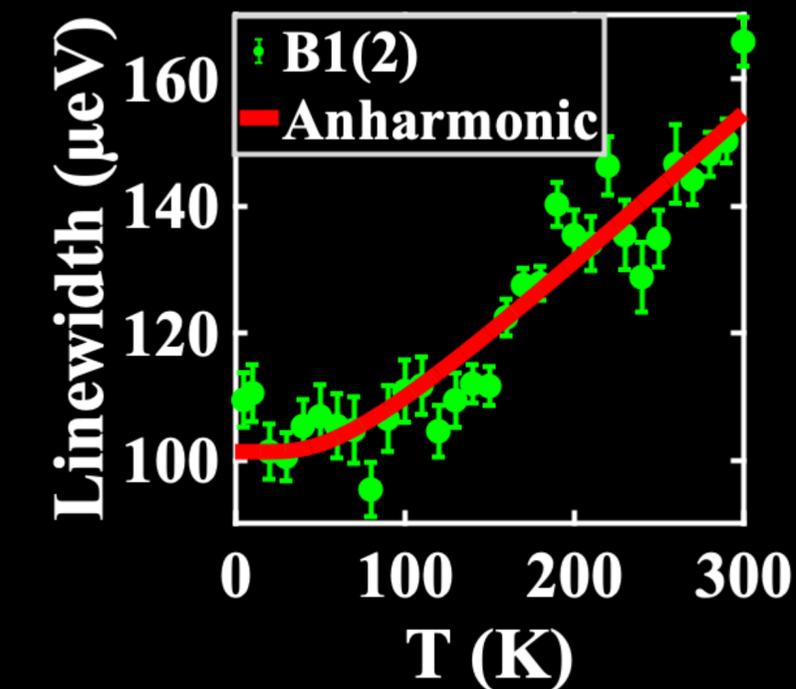


N. Kumar et al., Nat. Comm. 8, 1 (2017);

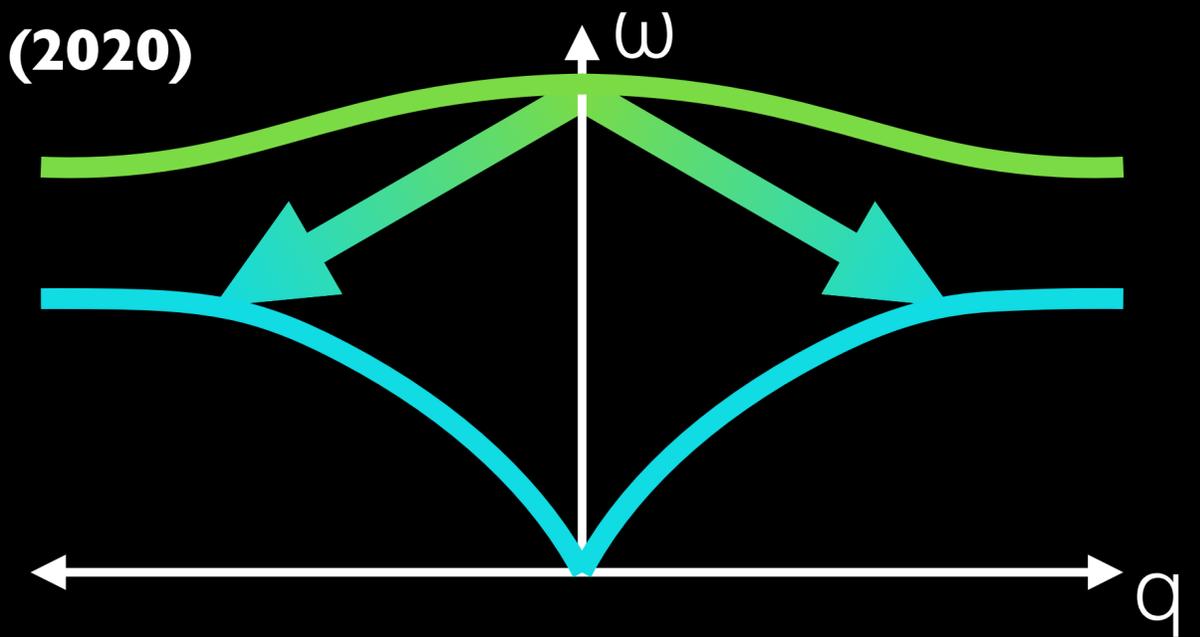
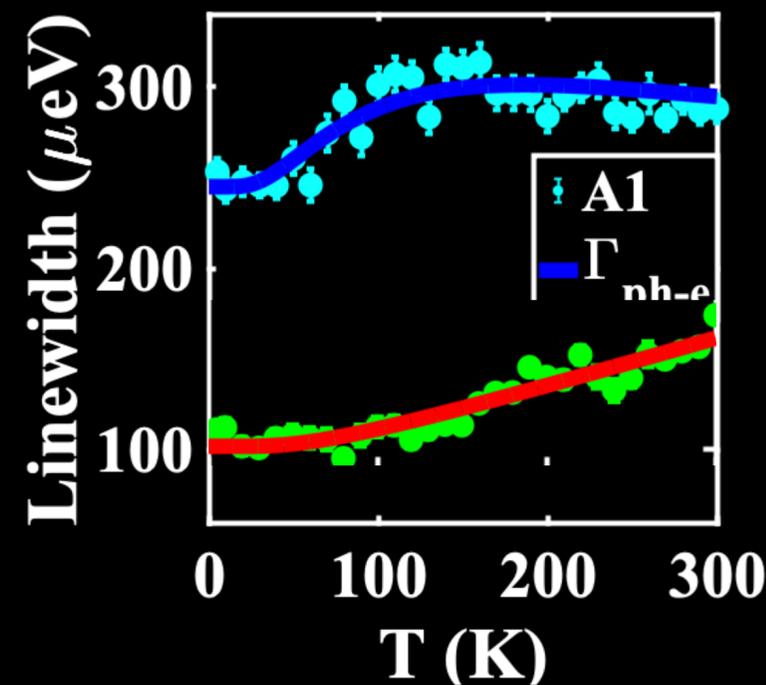
J. Hu et al., Ann. Rev. 49, 207 (2019);

T.O. Wehling et al., Adv. Phys. 63, 1 (2014)

(Ta,Nb)As



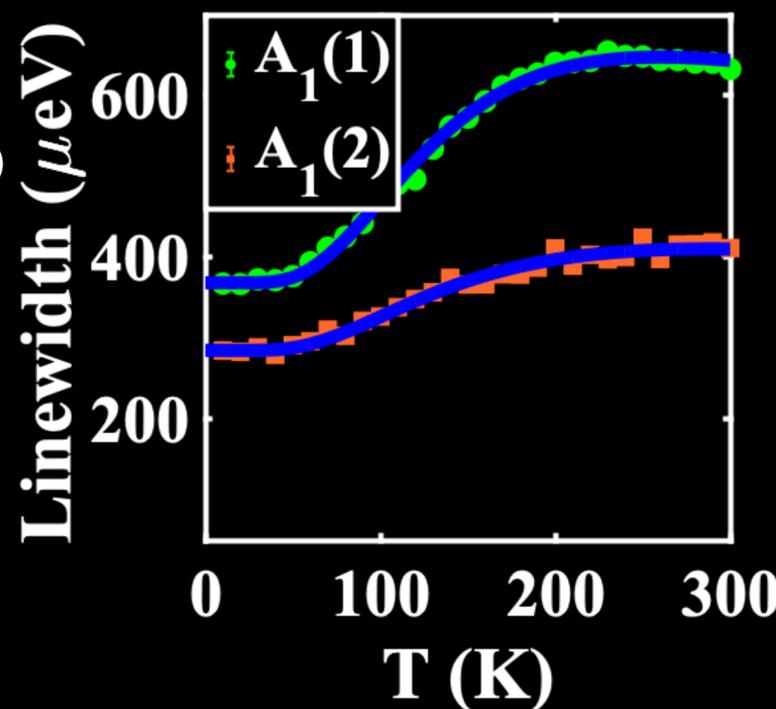
G. Osterhoudt, KSB Phys. Rev. B (2020)



Phys. Rev. 148, 845 (1966).; PRB, 29, 2051 (1984)

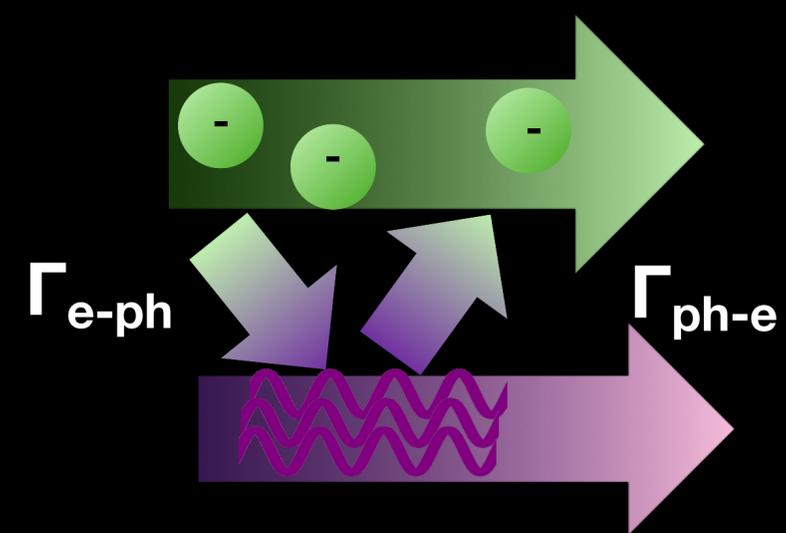
WP₂

G. Osterhoudt, KSB PRX (2021)

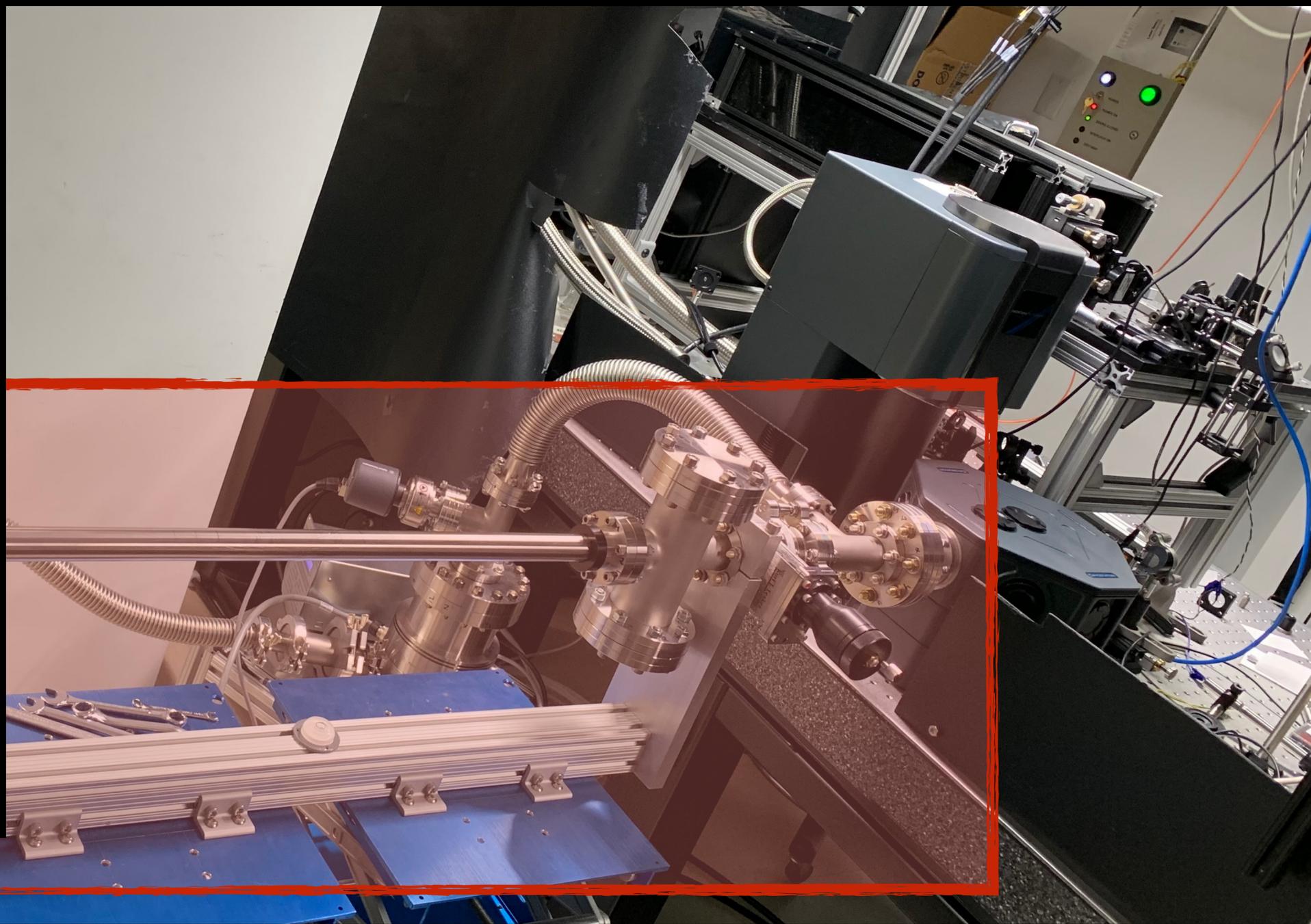
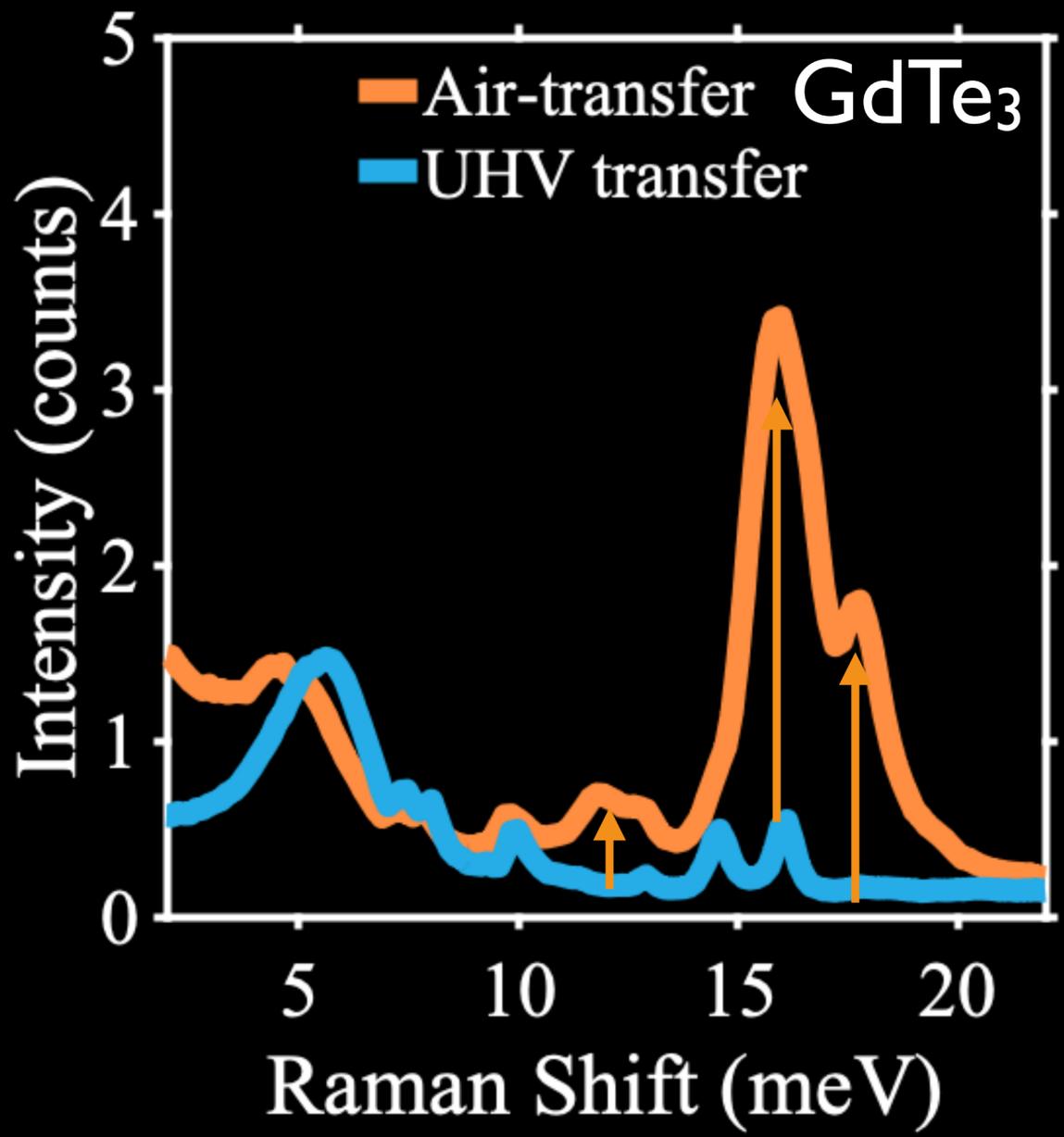


NbGe₂

H.-Y. Yang, KSB, Tafti Nature Comm (2021)

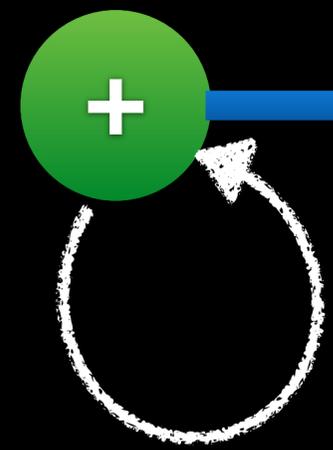


Our Postpandemic Tool



Y. Tian, KSB, et al Rev. Sci. Inst. 87, 4 (2016); M.Gray, KSB et al, RSI (2020)

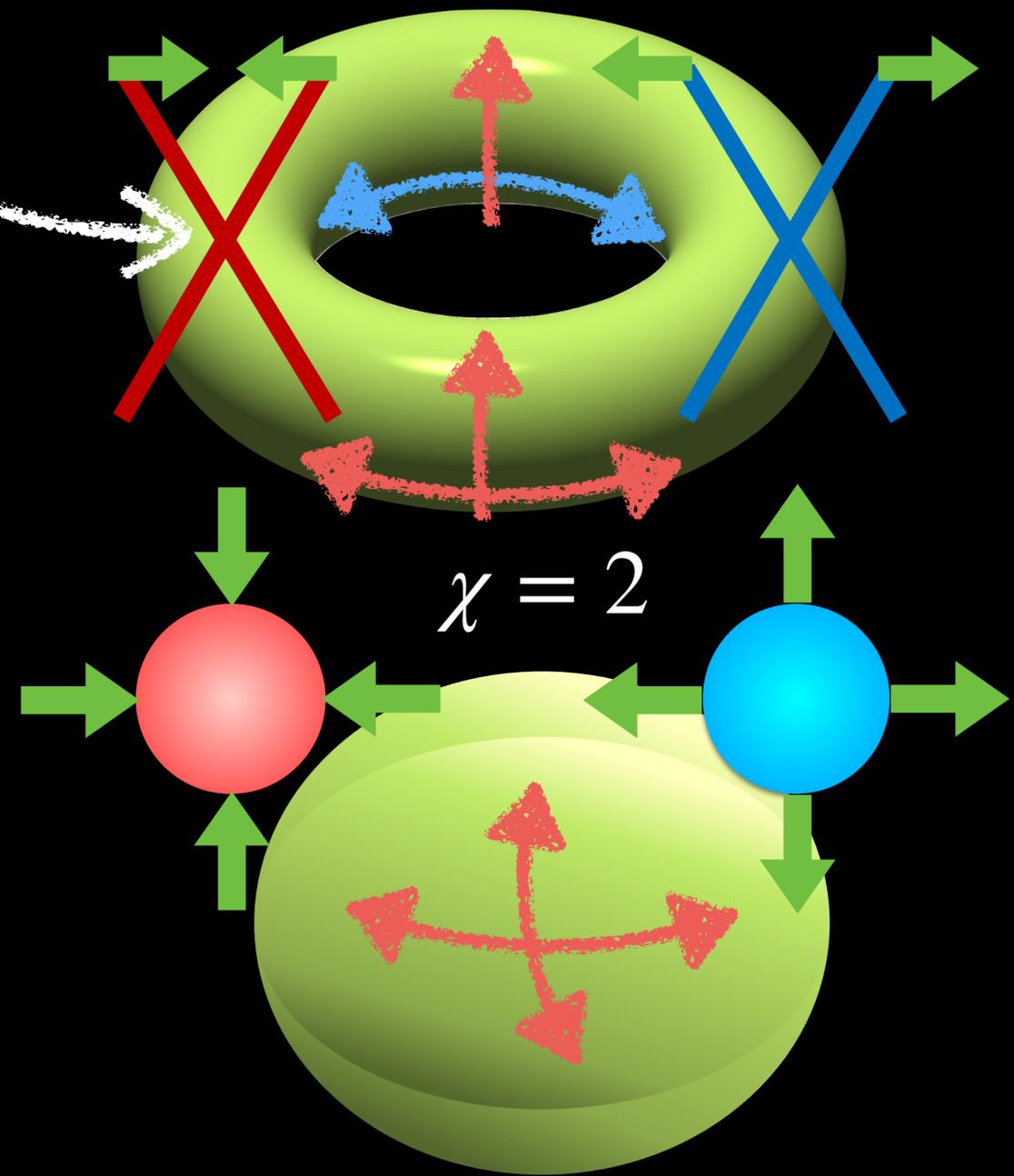
M. Berry



$$\psi(0) \rightarrow \psi(0)e^{i\gamma}$$

Magnetic Monopole

$$\Omega(k), \chi_{A(k)}^0 \rightarrow \infty$$



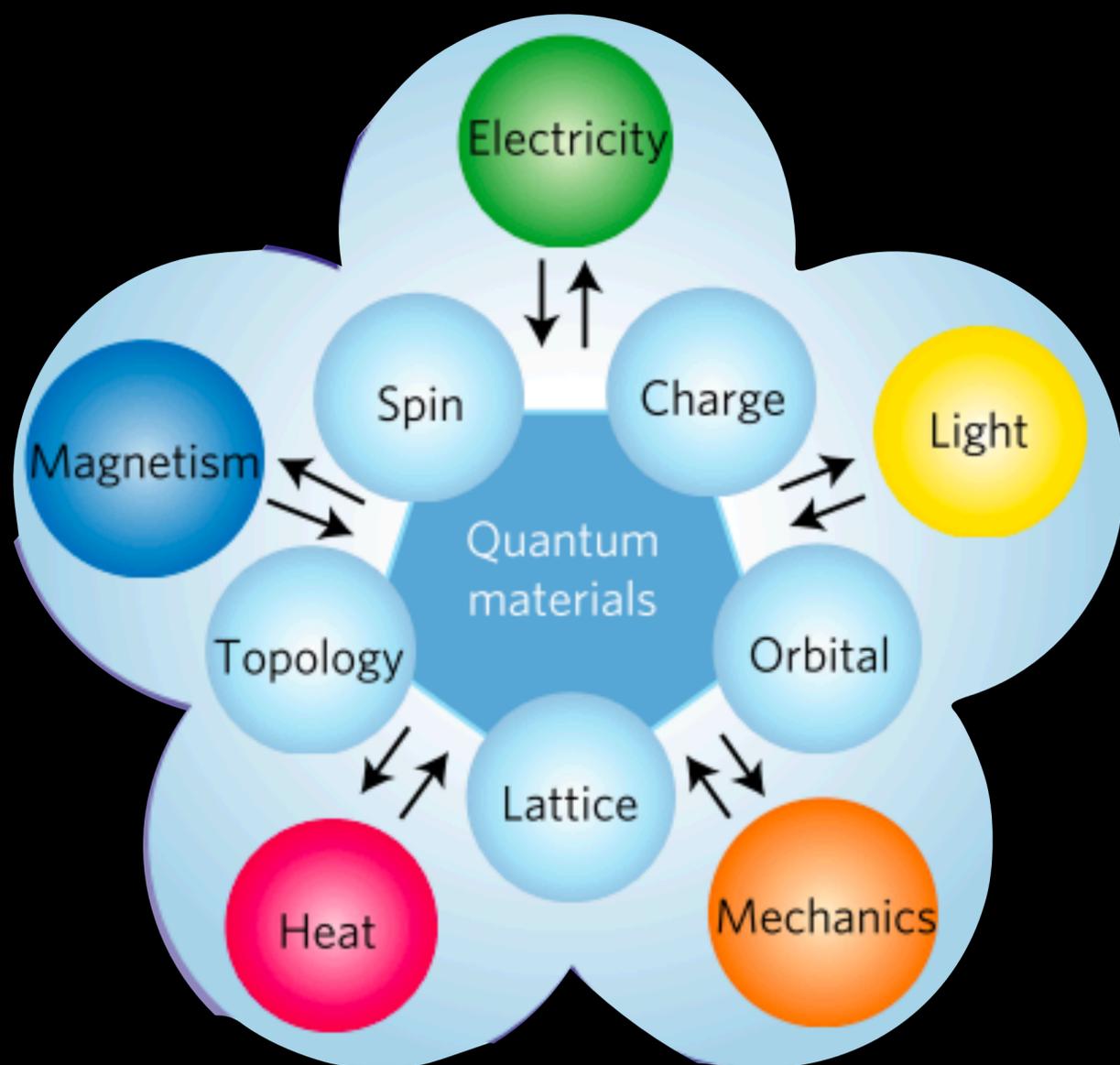
Phase:

$$\gamma = \oint_C dk \cdot A(\vec{k}) = \iint_S dk^2 \cdot \Omega(\vec{k}) \approx \text{invariant}$$

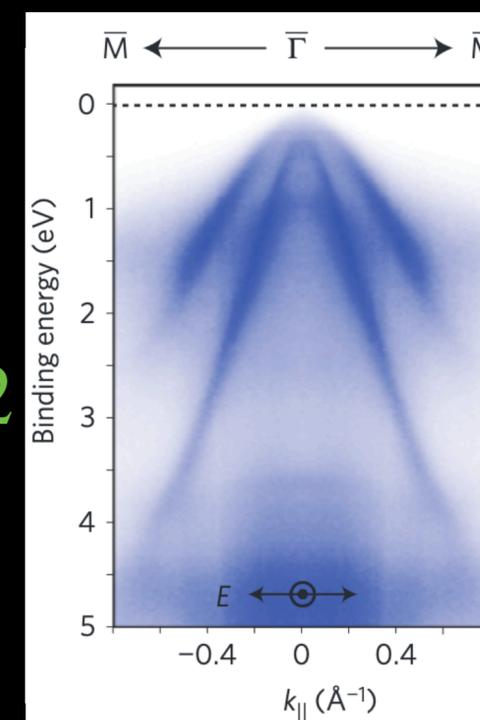
Curvature: $\Omega(\vec{k}) = \nabla_k \times A(\vec{k}) \approx \vec{B}(\vec{k})$

Connection: $A(\vec{k}) = \langle \psi(\vec{k}) | i \nabla_k | \psi(\vec{k}) \rangle \approx \text{Potential}$
 $= \langle | \hat{r} | \rangle$

D. Xiao, et al. RMP 82, 1959 (2010)



Y. Tokura et al., Nature Physics (2017)



Nat. Materials 13, 677 (2014)

NANO LETTERS

pubs.acs.org/NanoLett

Letter

Modulation Doping via a Two-Dimensional Atomic Crystalline Acceptor

[Yiping Wang](#), [Jesse Balgley](#), [Eli Gerber](#), [Mason Gray](#), [Narendra Kumar](#), [Xiaobo Lu](#), [Jia-Qiang Yan](#), [Arash Fereidouni](#), [Rabindra Basnet](#), [Seok Joon Yun](#), [Dhavala Suri](#), [Hikari Kitadai](#), [Takashi Taniguchi](#), [Kenji Watanabe](#), [Xi Ling](#), [Jagadeesh Moodera](#), [Young Hee Lee](#), [Hugh O. H. Churchill](#), [Jin Hu](#), [Li Yang](#), [Eun-Ah Kim](#), [David G. Mandrus](#), [Erik A. Henriksen](#),* and [Kenneth S. Burch](#)*

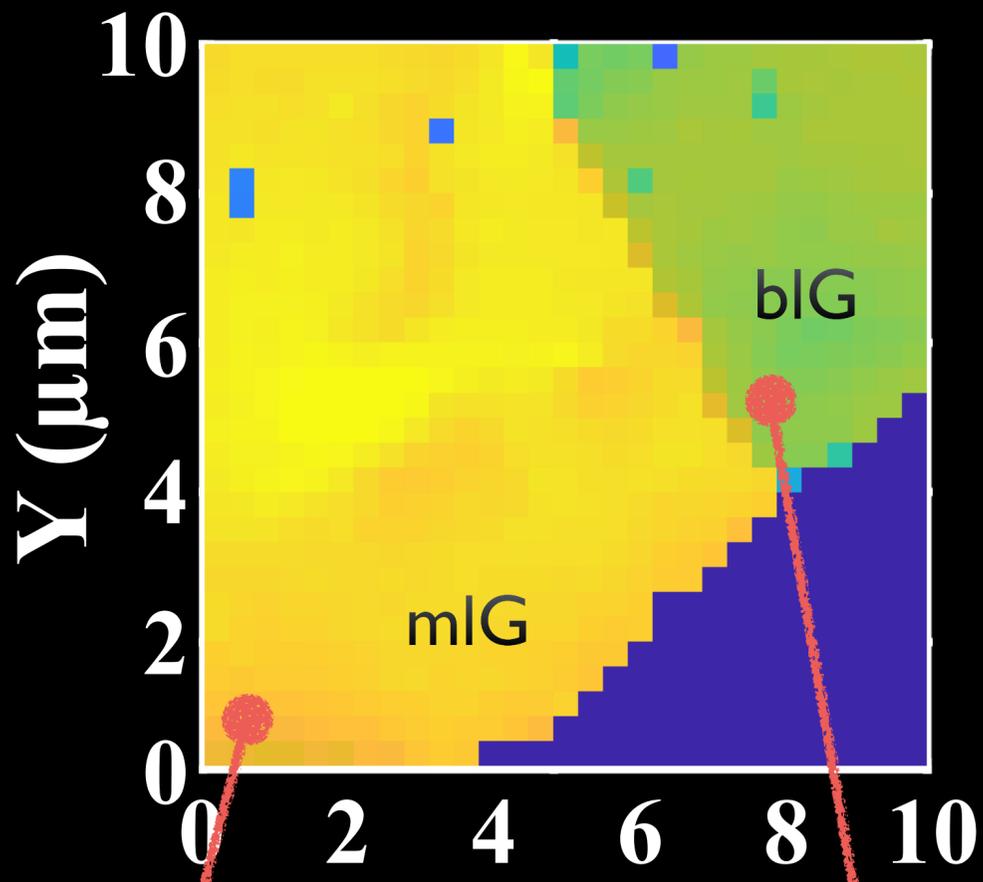
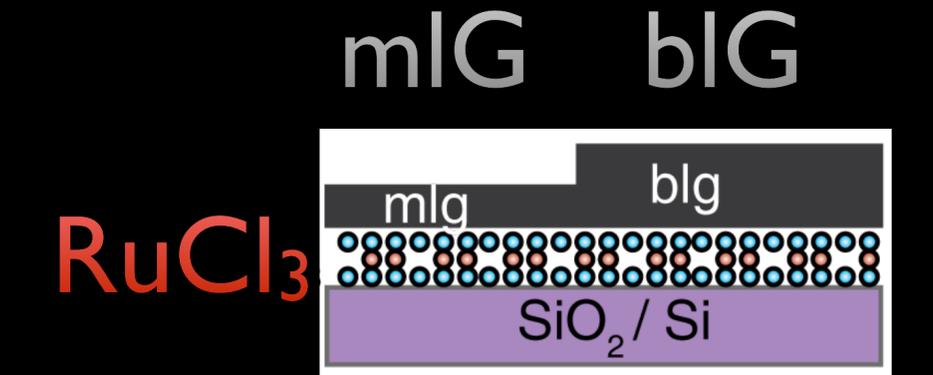
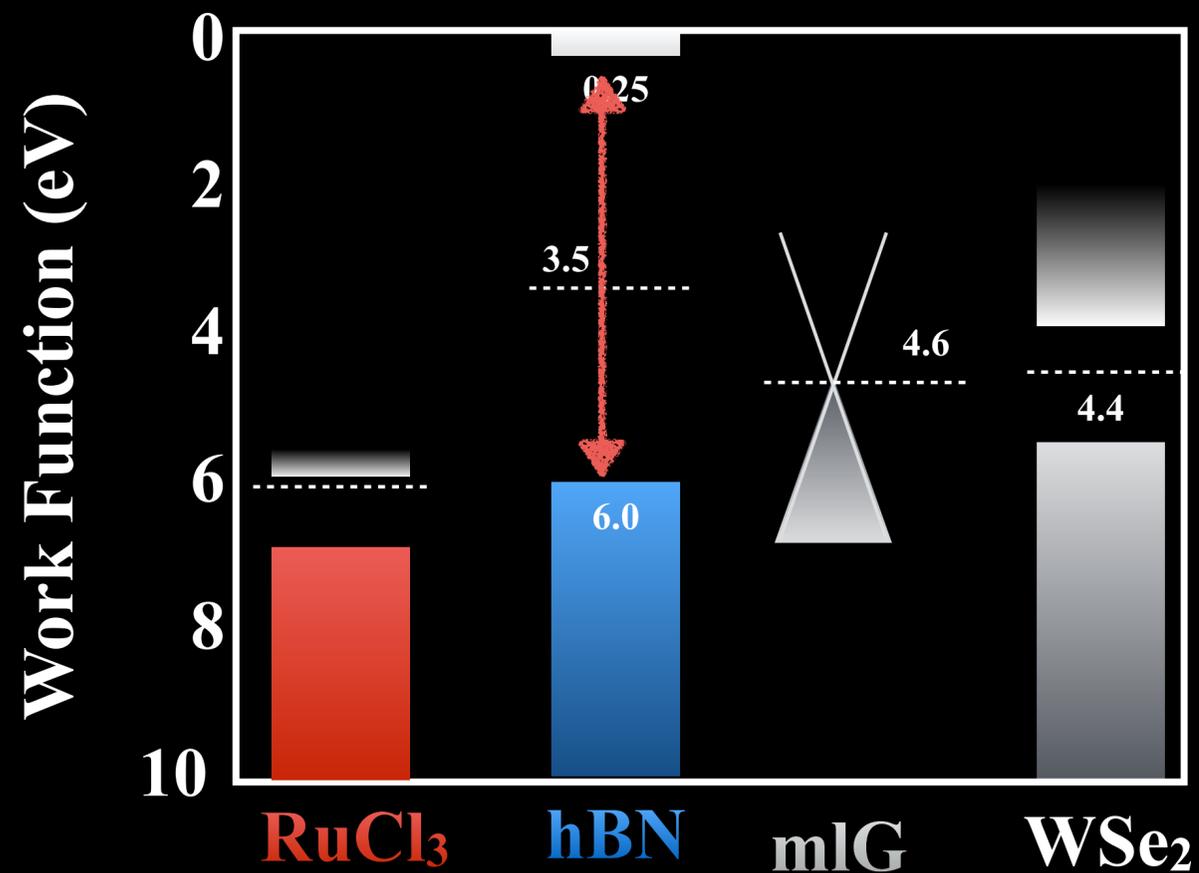


Cite This: *Nano Lett.* 2020, 20, 8446–8452

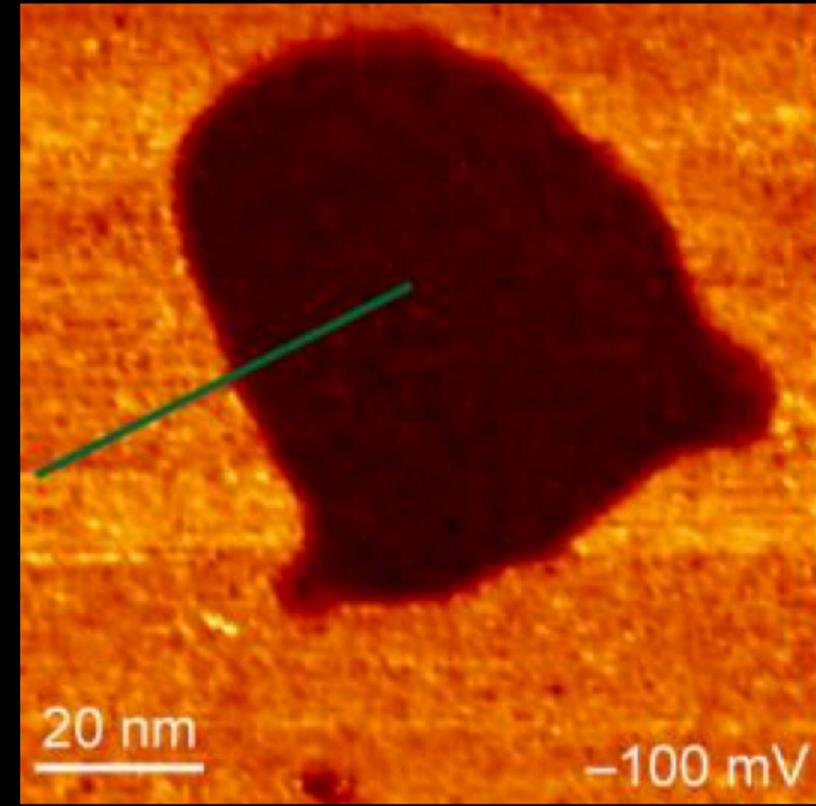


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Modulation Doping



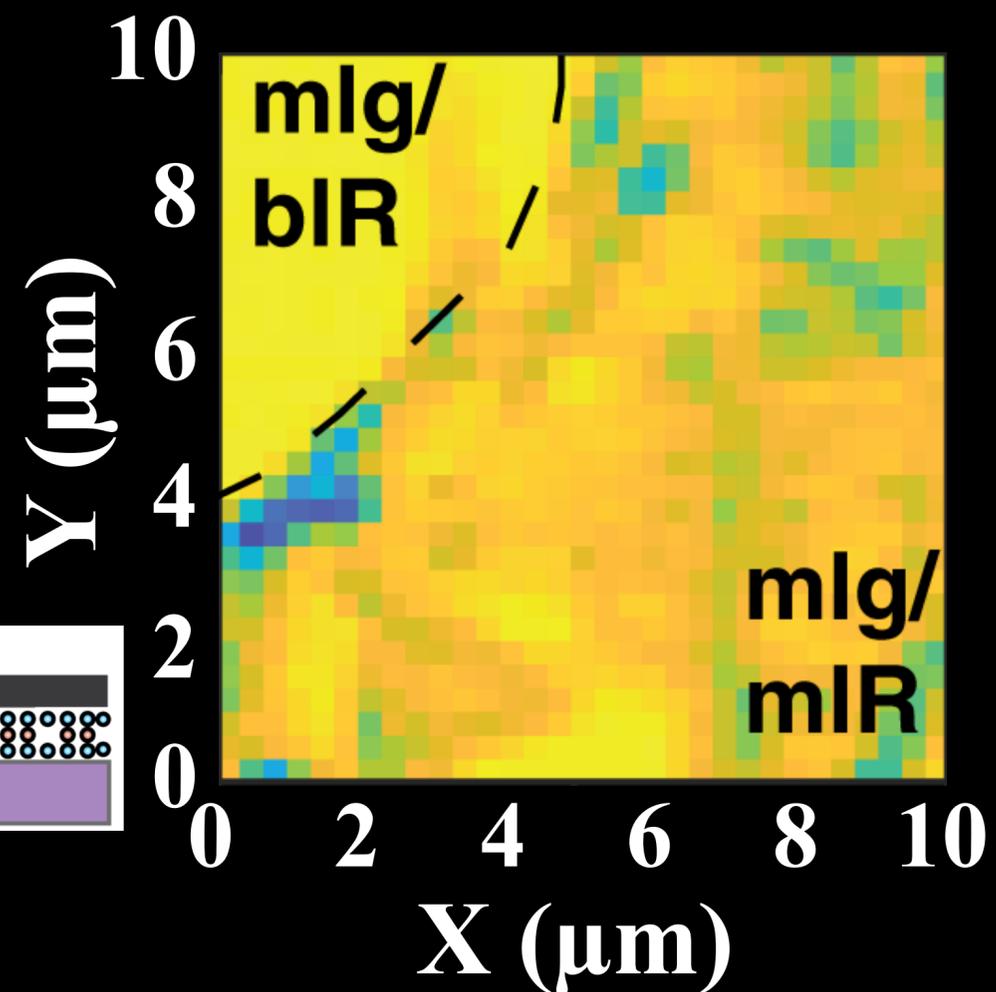
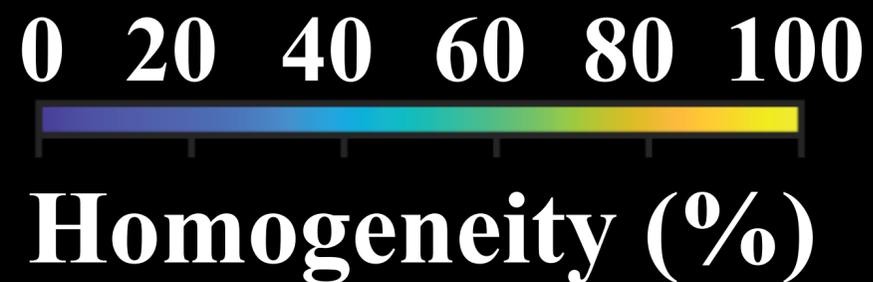
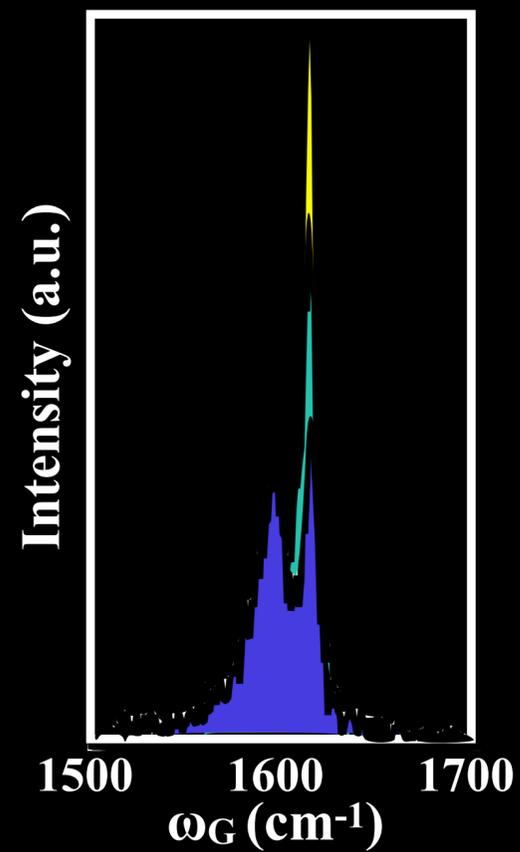
$\sim 3 \times 10^{13} \text{cm}^{-2}$ $E_F \sim 600 \text{meV}$ $\sim 6 \times 10^{13} \text{cm}^{-2}$



D. Rizzo et al, Nanoletters (2022)
 J. Bagley et al, Nanoletter (2022)

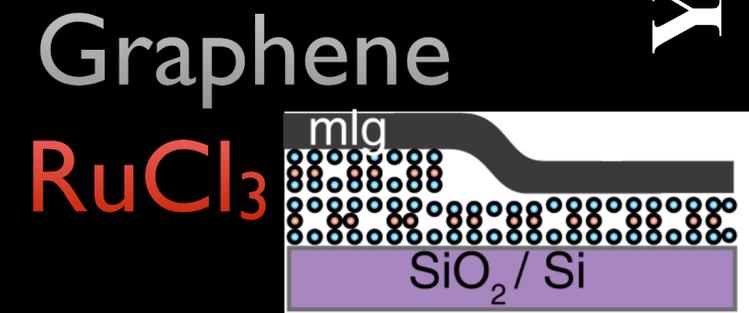
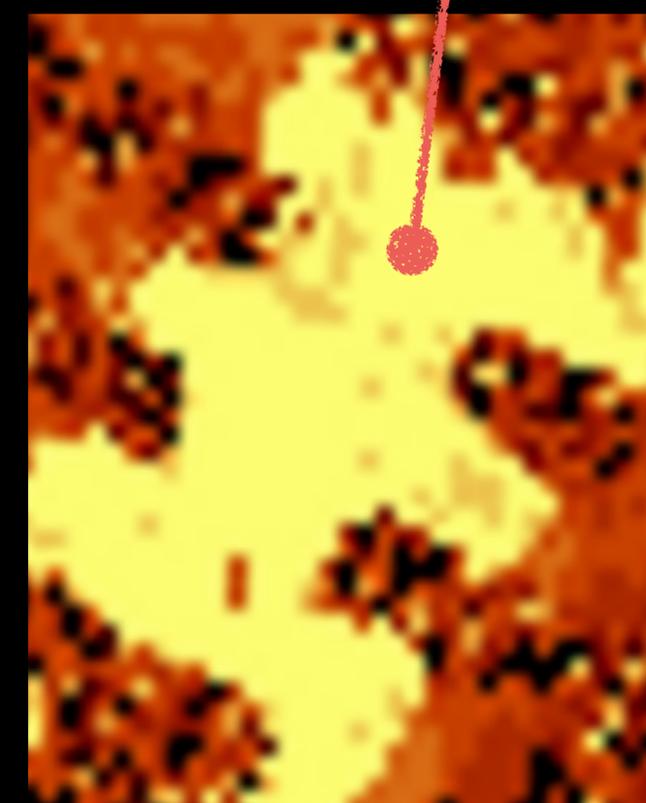
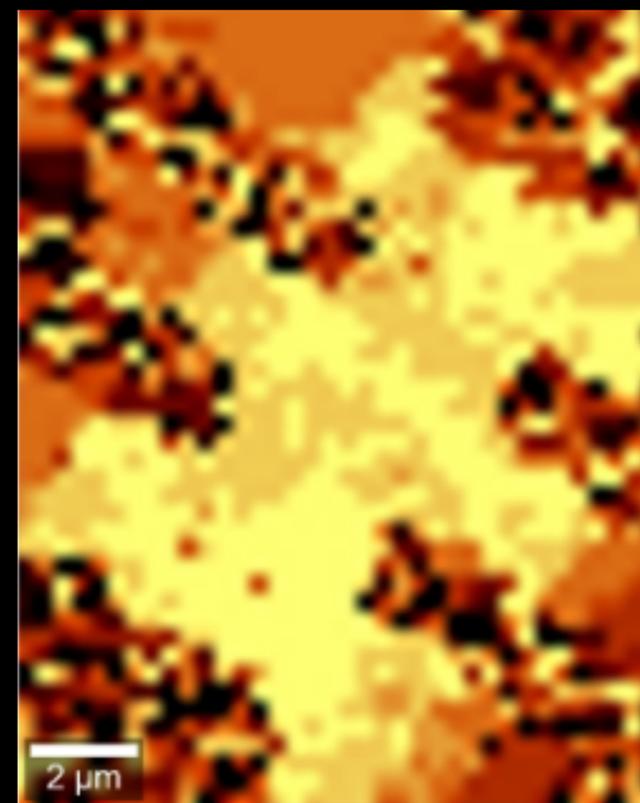
Y. Wang, KSB et al, Nanoletters (2020)

Optimal Modulation Doping



- ✓ Twist Agnostic
- ✓ Sweeping
- ✓ Annealing

$\sim 1.5 \times 10^{14} \text{cm}^{-2}$
 $E_F \sim 1.2 \text{ eV}$



Nonlinear

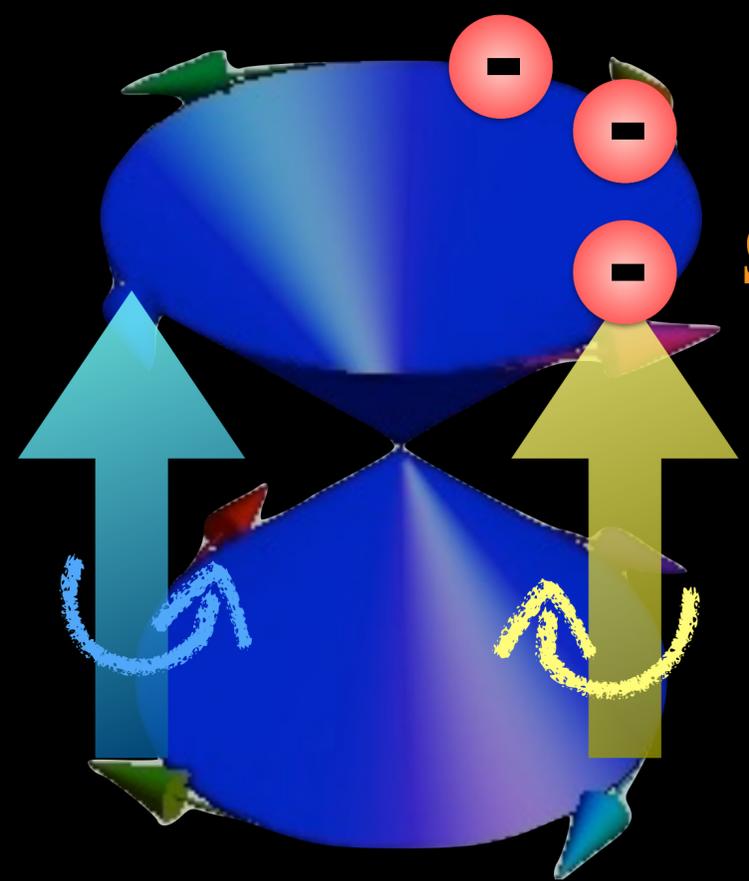
$$\vec{\Omega}(\vec{k}) = \nabla_{\vec{k}} \times A(\vec{k}) \approx \vec{B}(\vec{k})$$

$$A(\vec{k}) = \langle \psi(\vec{k}) | i \nabla_{\vec{k}} | \psi(\vec{k}) \rangle$$

$$= \langle | \hat{r} | \rangle$$

Injection Current

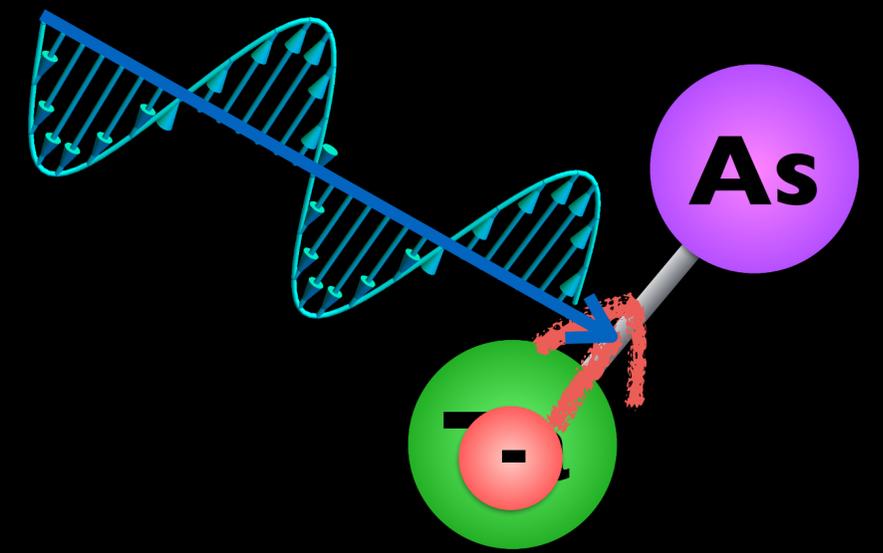
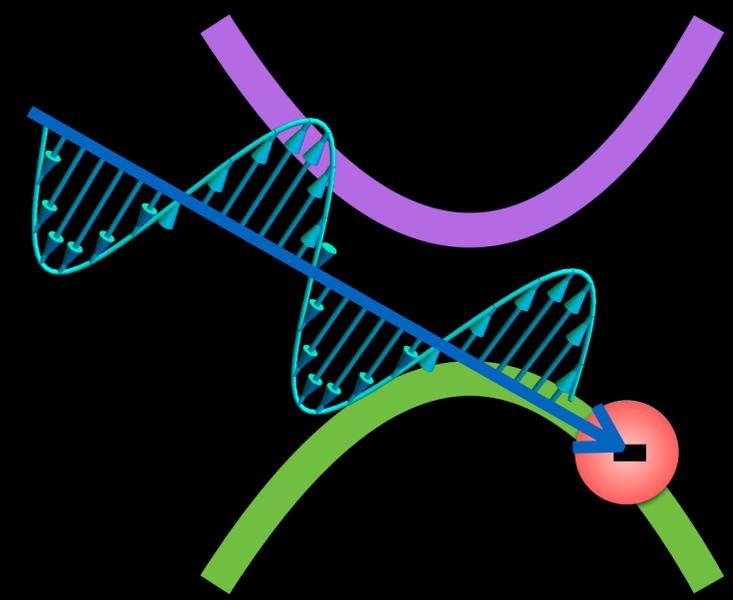
$$J_{inj} \propto \frac{dJ}{dt} \tau$$



$$\Omega(k_x) = B_0 \hat{y}$$

Shift Current

$$\frac{d\vec{P}}{dt} = \vec{J}$$

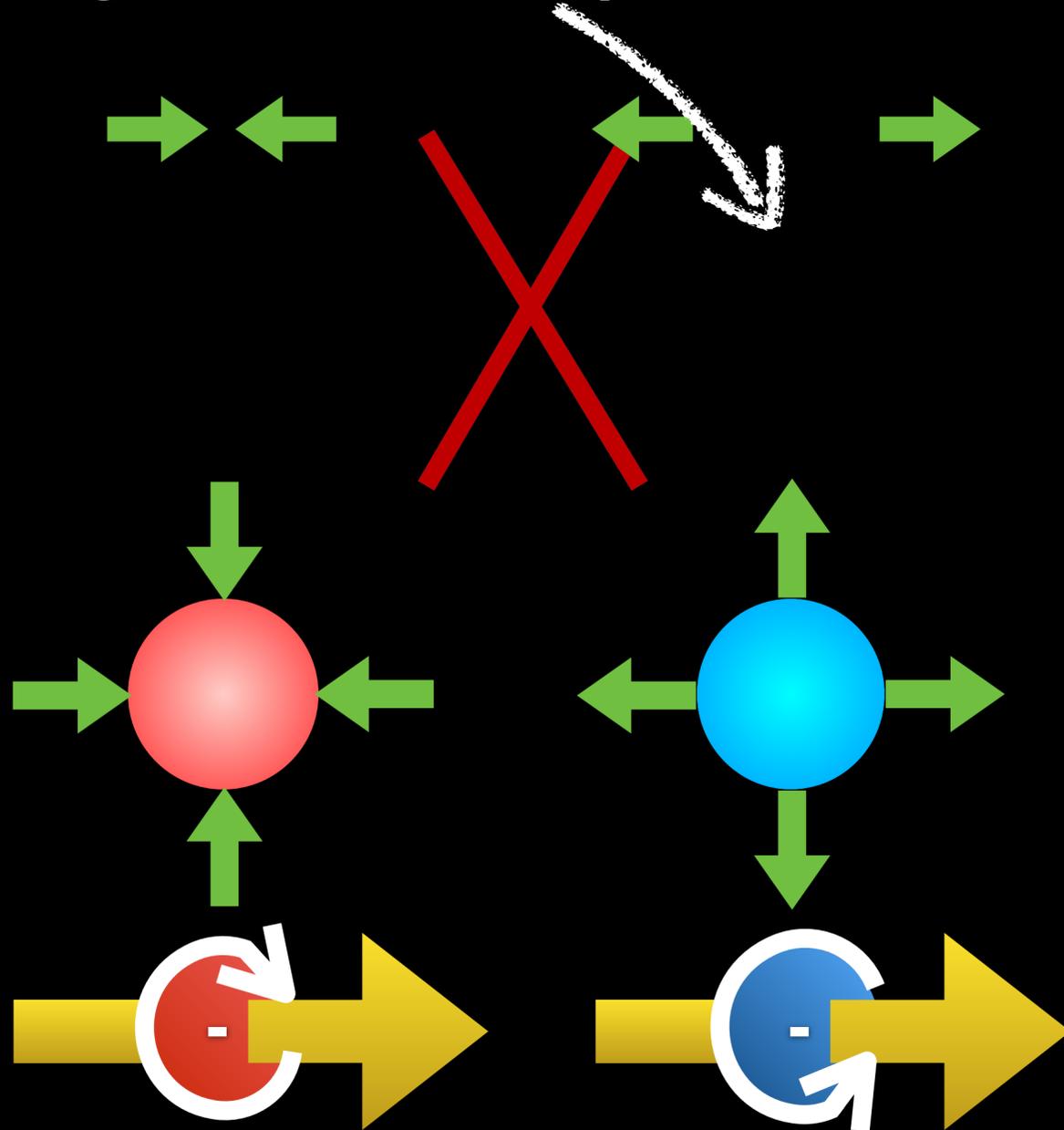


J.E. Sipe, & I. Shkrebtii, PRB 61, 5337 (2000)
 T. Morimoto & N. Nagaosa, Sci. Adv. 2, 150524 (2016)
 L.Z. Tan et al., NPJ Comp. Mat. 2, 16026 (2016)

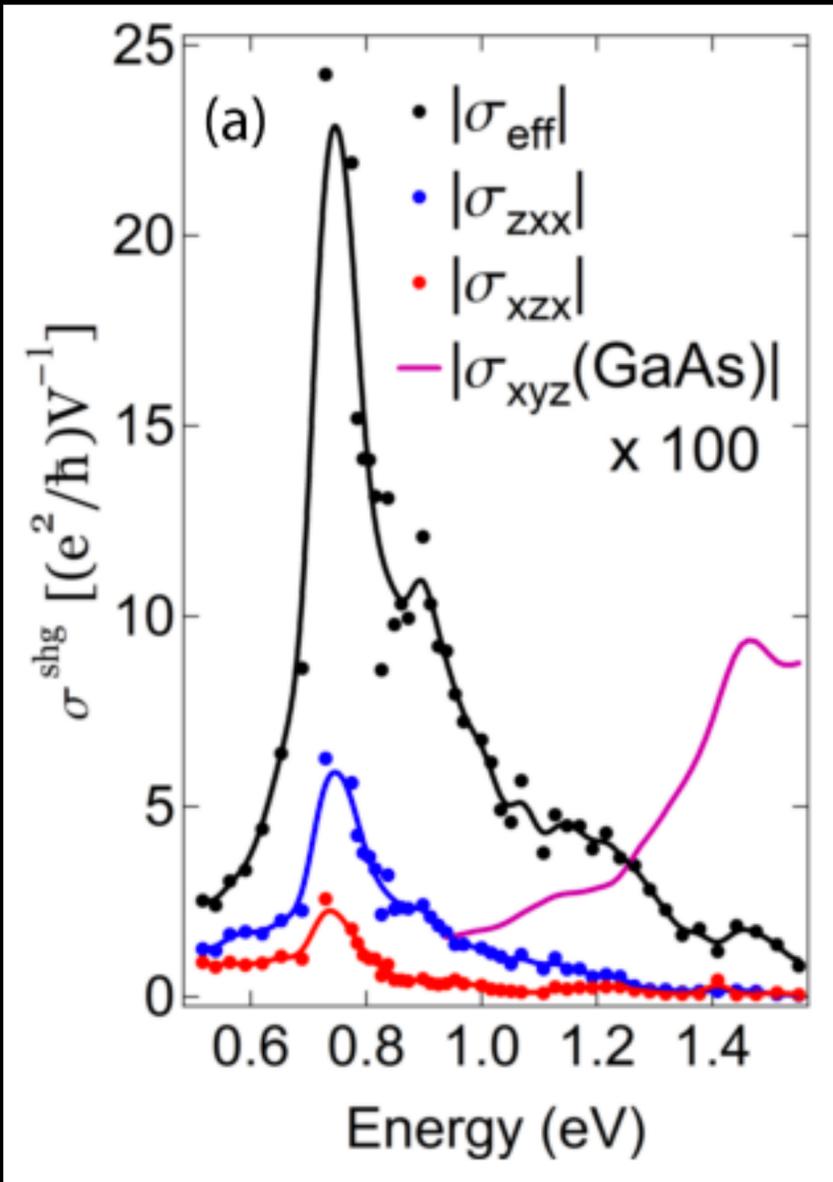
Magnetic Monopole $\rightarrow \Omega(k), A(k) \rightarrow \infty$

2nd harmonic

L.Wu et al, Nature Physics (2017)

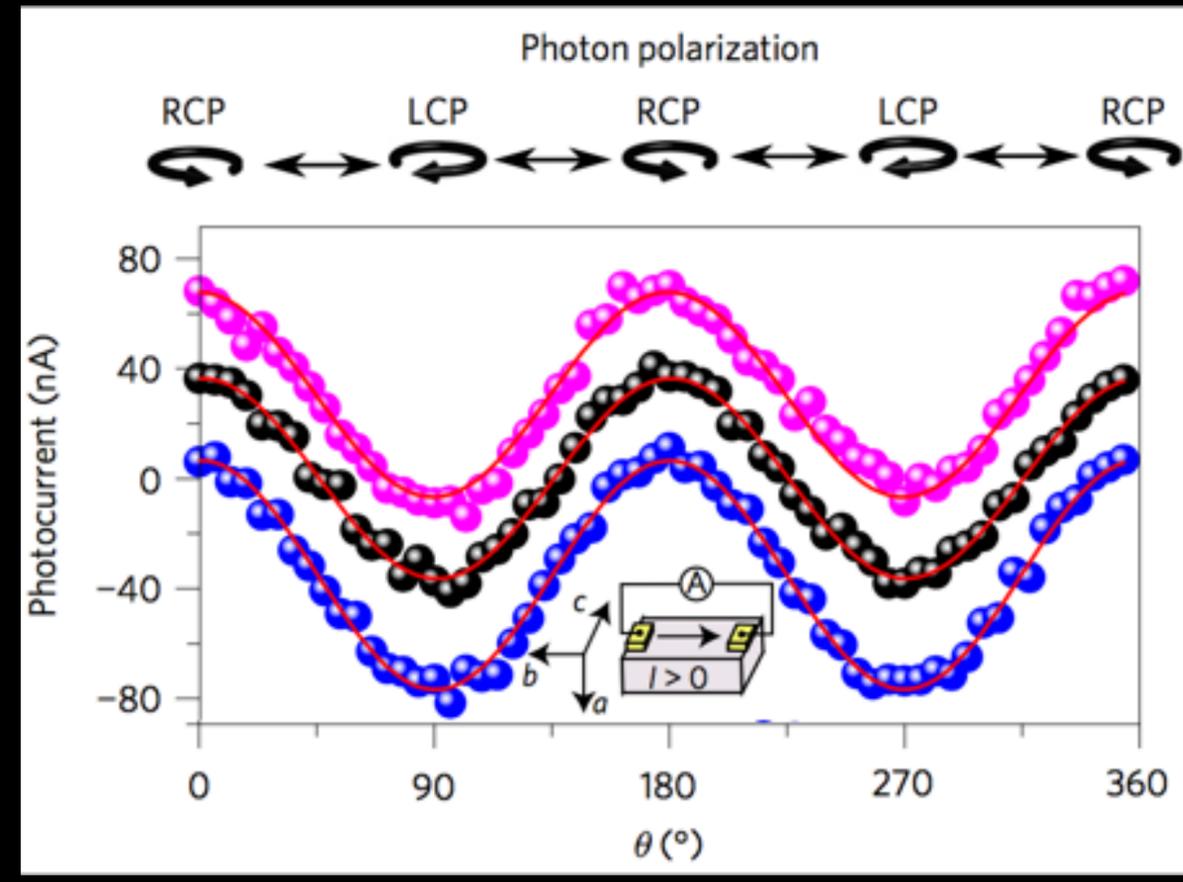
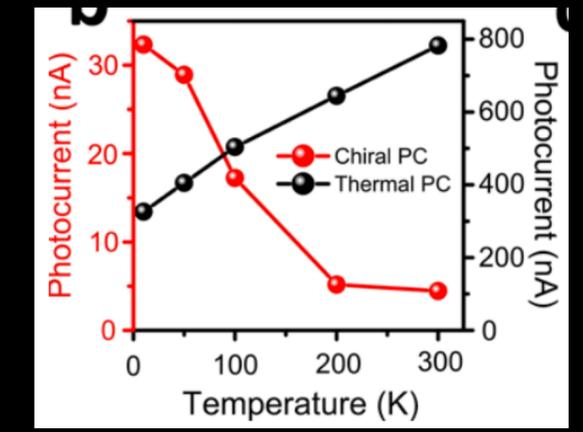
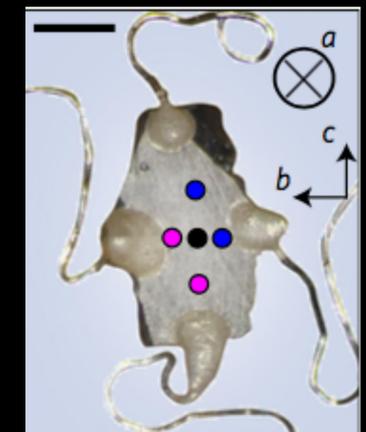


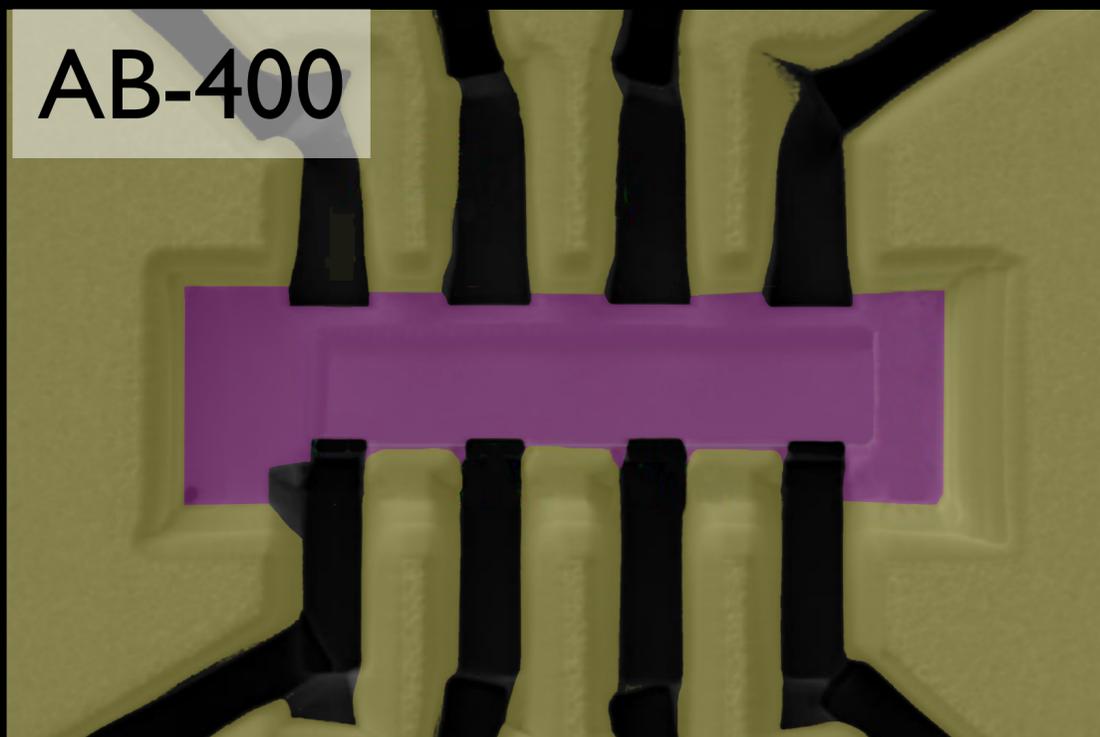
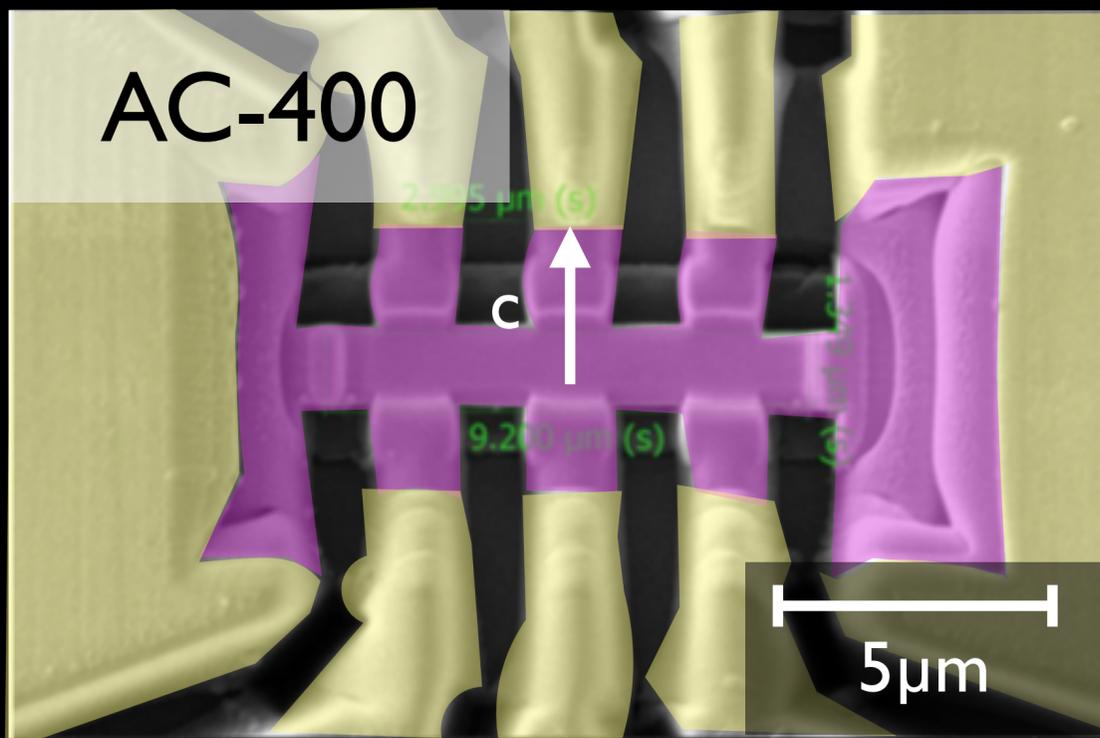
X.Yang et al., arxiv 1712.09363
 C.K. Chan et al., PRB 95, 41104



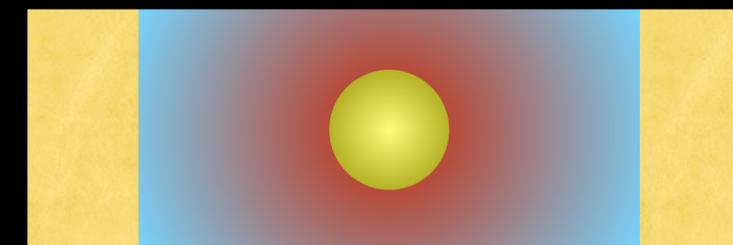
Injection Current

Q. Ma et al, Nature Physics (2017)



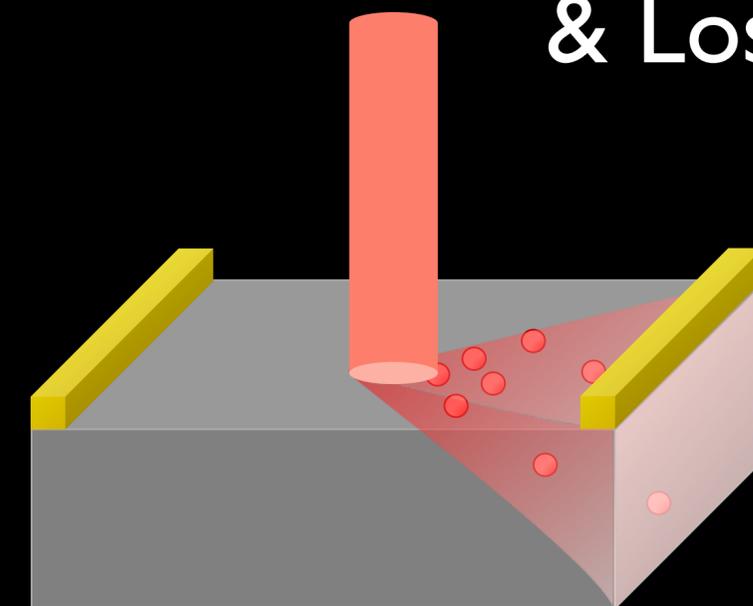


Seebeck



Symmetry

Penetration
& Loss



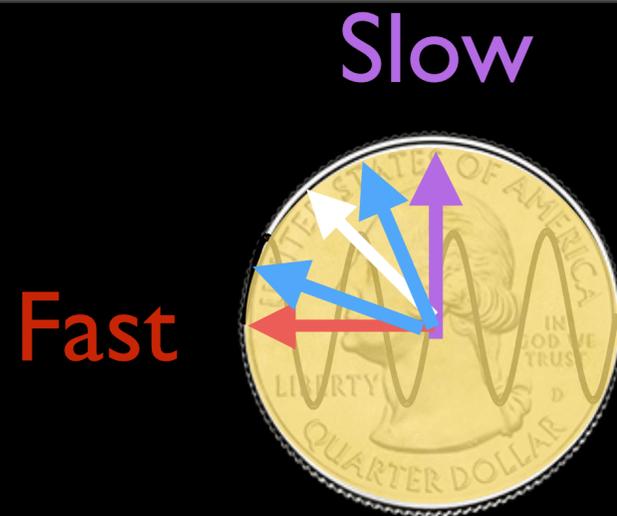
● Higgs

● Square Scattering

● Interference

● Highlights

Nature Materials (2019)

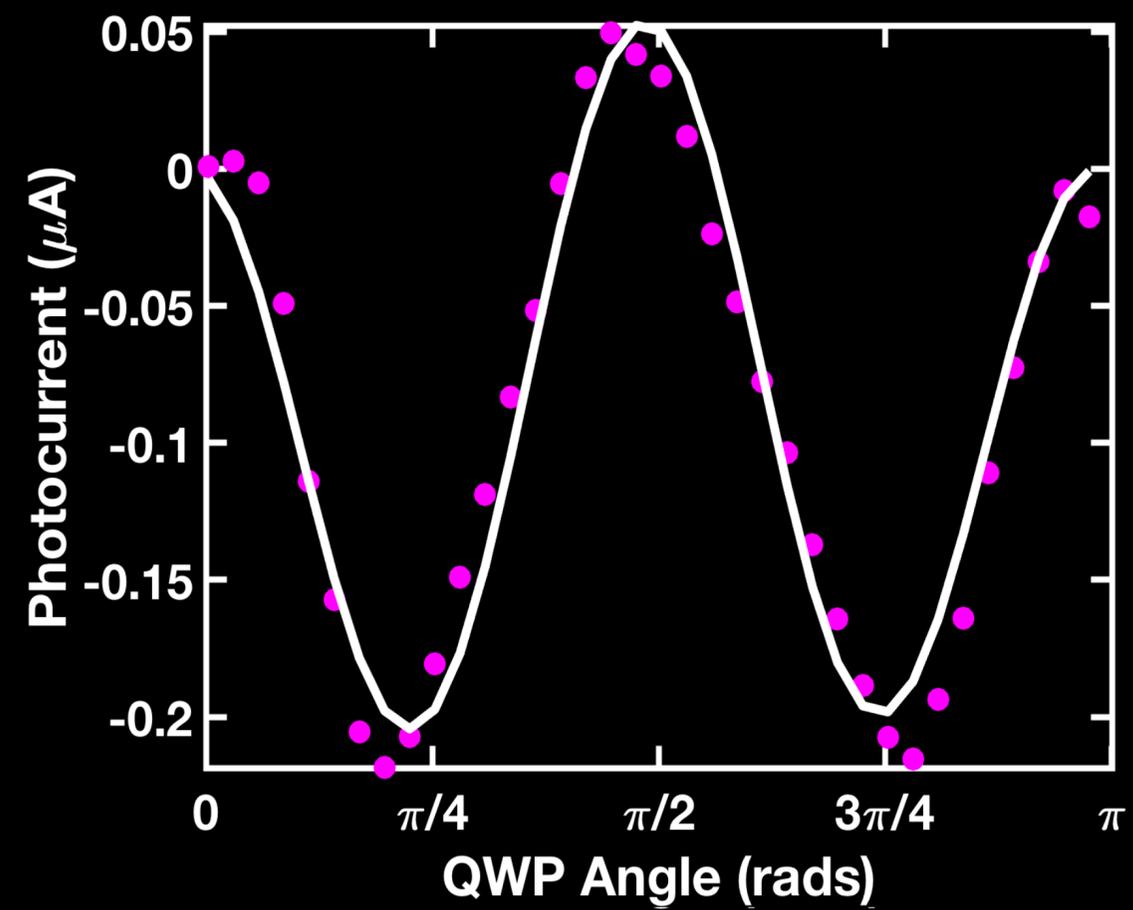


Circular: $S_2 \sin(2\theta)$

$E_x E_y$: $S_4 \sin(4\theta)$

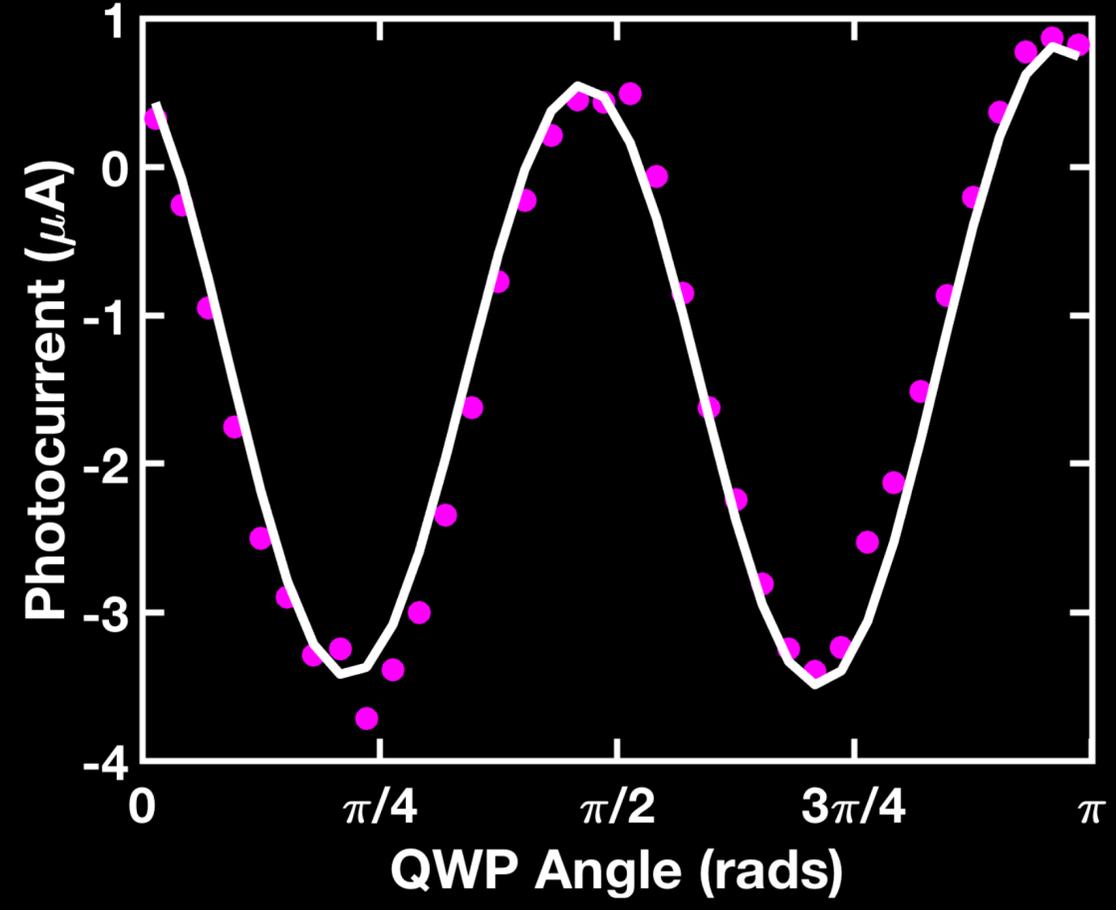
$|E_x|^2 + |E_y|^2$: $D + C_2 \cos(2\theta) + C_4 \cos(4\theta)$

AC-400



$C_4 = 0.11$
 $S_4 = -0.02$

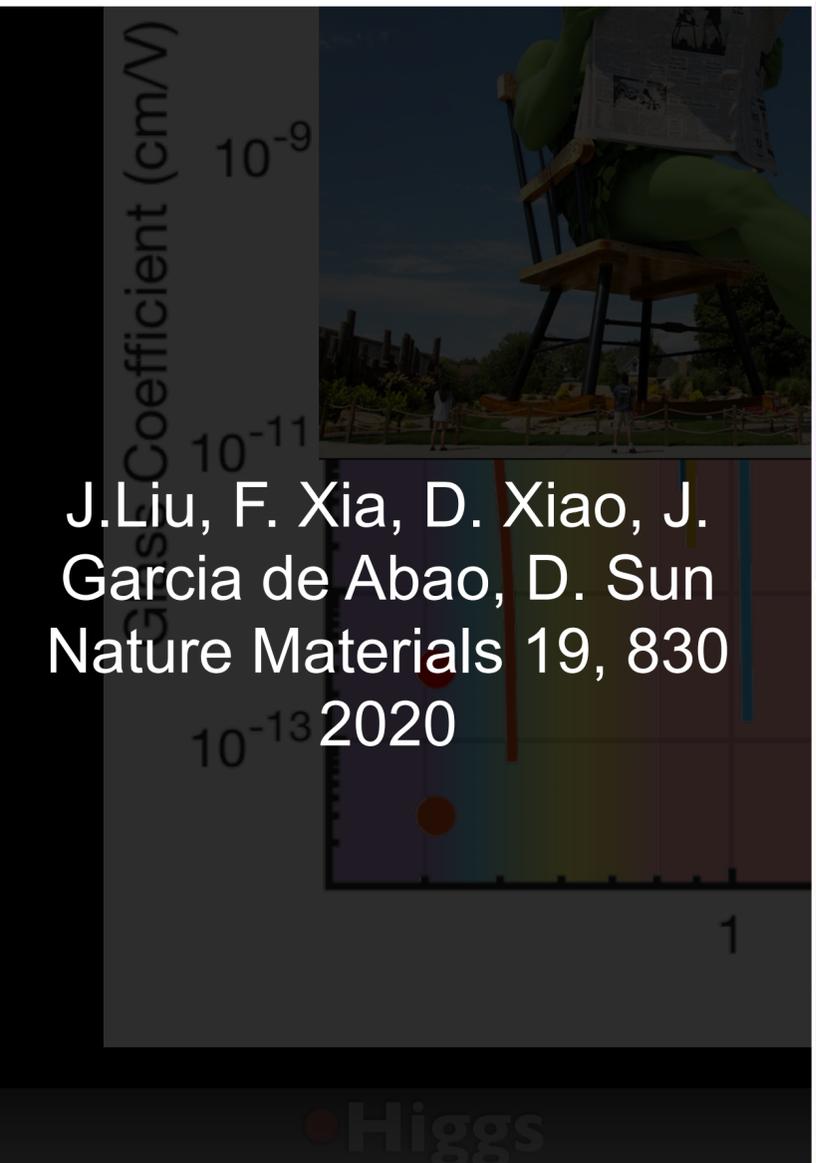
AB-400



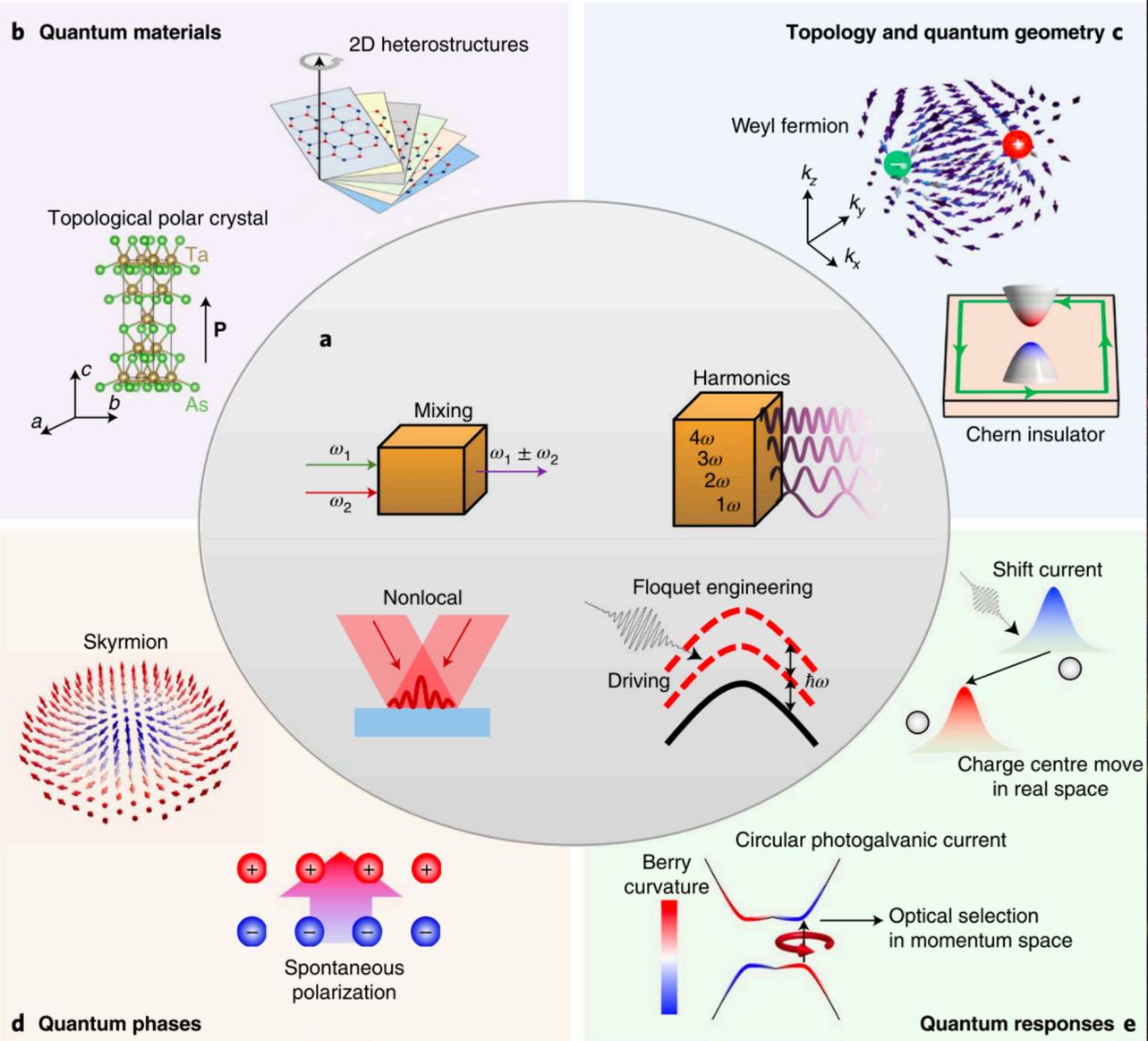
$\Phi = -13^\circ$
 $C_4 = 1.86$
 $S_4 = -0.89$

Topology and geometry under the nonlinear electromagnetic spotlight

Qiong Ma^{1,2}, Adolfo G. Grushin³ and Kenneth S. Burch²✉



J. Liu, F. Xia, D. Xiao, J. Garcia de Abao, D. Sun
 Nature Materials 19, 830
 2020



nature materials
 MAY 2019 VOL 18 NO 5
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