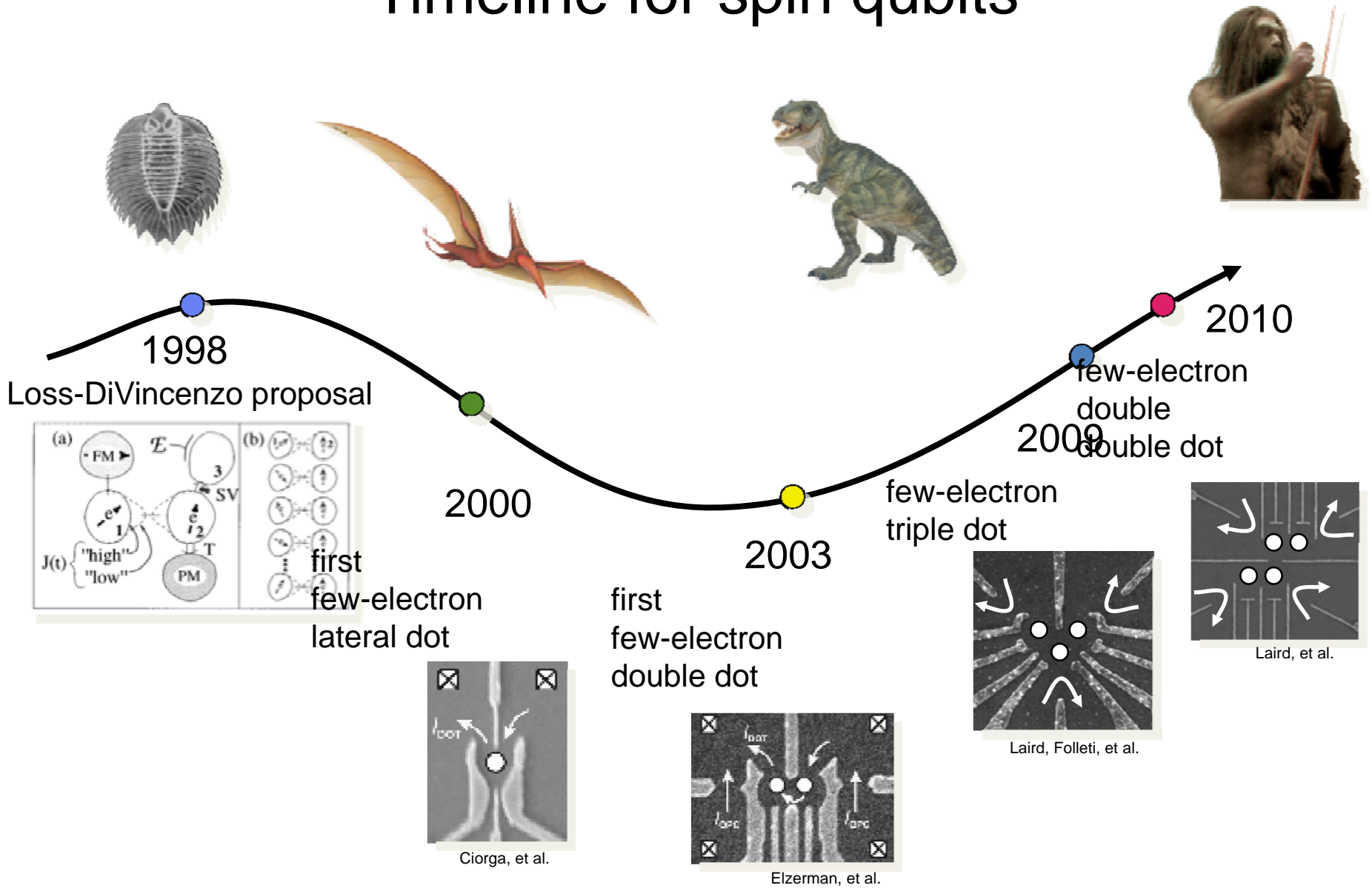




Timeline for spin qubits



Quantum computation with quantum dots

Daniel Loss^{1,2,*} and David P. DiVincenzo^{1,3,†}

¹*Institute for Theoretical Physics, University of California, Santa Barbara, Santa Barbara, California 93106-4030*

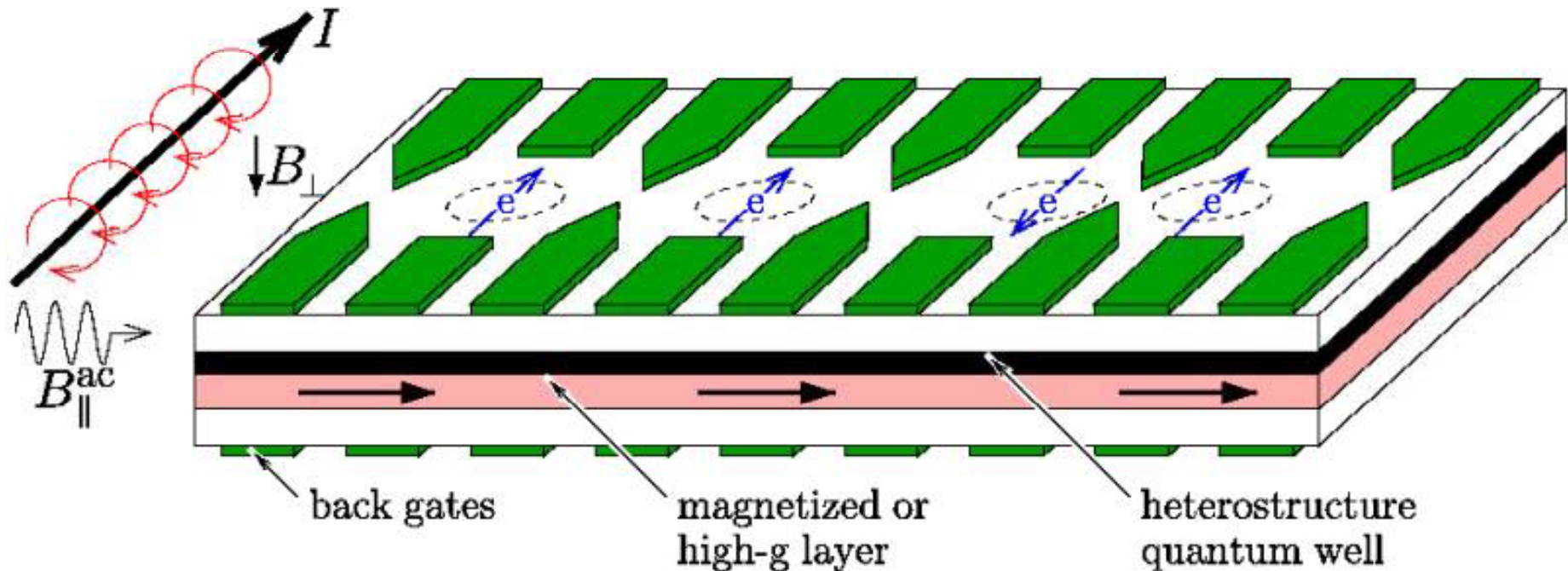
²*Department of Physics and Astronomy, University of Basel, Klingelbergstrasse 82, 4056 Basel, Switzerland*

³*IBM Research Division, T.J. Watson Research Center, P.O. Box 218, Yorktown Heights, New York 10598*

(Received 9 January 1997; revised manuscript received 22 July 1997)

We propose an implementation of a universal set of one- and two-quantum-bit gates for quantum computation using the spin states of coupled single-electron quantum dots. Desired operations are effected by the gating of the tunneling barrier between neighboring dots. Several measures of the gate quality are computed within a recently derived spin master equation incorporating decoherence caused by a prototypical magnetic environment. Dot-array experiments that would provide an initial demonstration of the desired nonequilibrium spin dynamics are proposed. [S1050-2947(98)04501-6]

PACS number(s): 03.67.Lx, 89.70.+c, 75.10.Jm, 89.80.+h



OXIDE NANOELECTRONICS

Jeremy Levy
University of Pittsburgh

qinfo2009
KITP

9 December 2009



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| | |
|--|---------------------|
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| Kris Andersen | Northern Arizona U. |
| C. Stephen Hellberg | NRL |

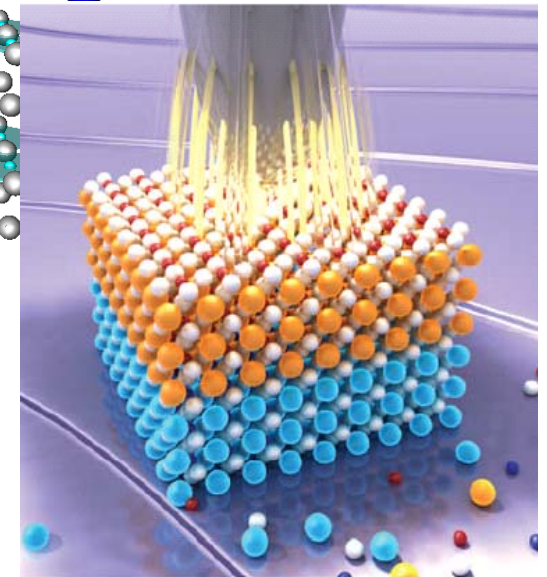
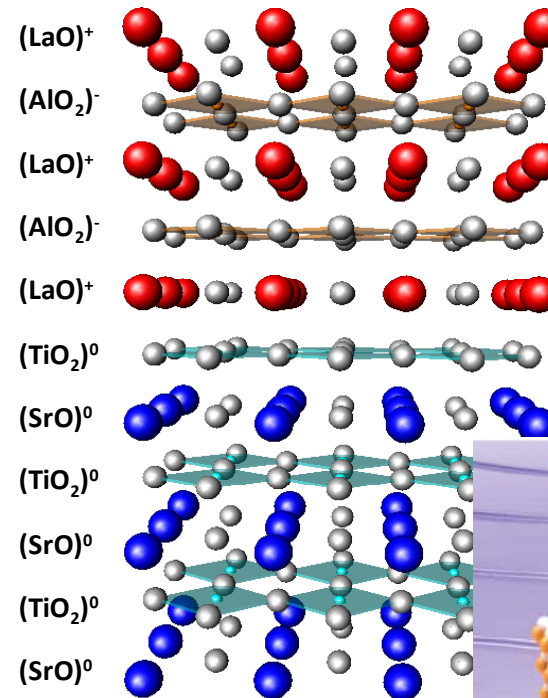
Support:



Emergent Phenomena at Oxide Interfaces

- High-mobility 2DEG
 - Ohtomo and Hwang, *Nature* (2004)
- Metal-insulator transition
 - Thiel et al, *Science* (2006)
- Superconductivity
 - Reyren et al, *Science* (2007);
Cavaglia, *Nature* (2008)
- Magnetism
 - Brinkman et al, *Nature Materials* (2007)
- Nanostructures
 - Cen et al, *Nature Materials* (2008)
- Nanodevices
 - Cen et al, *Science* (2009)

LaAlO₃/SrTiO₃

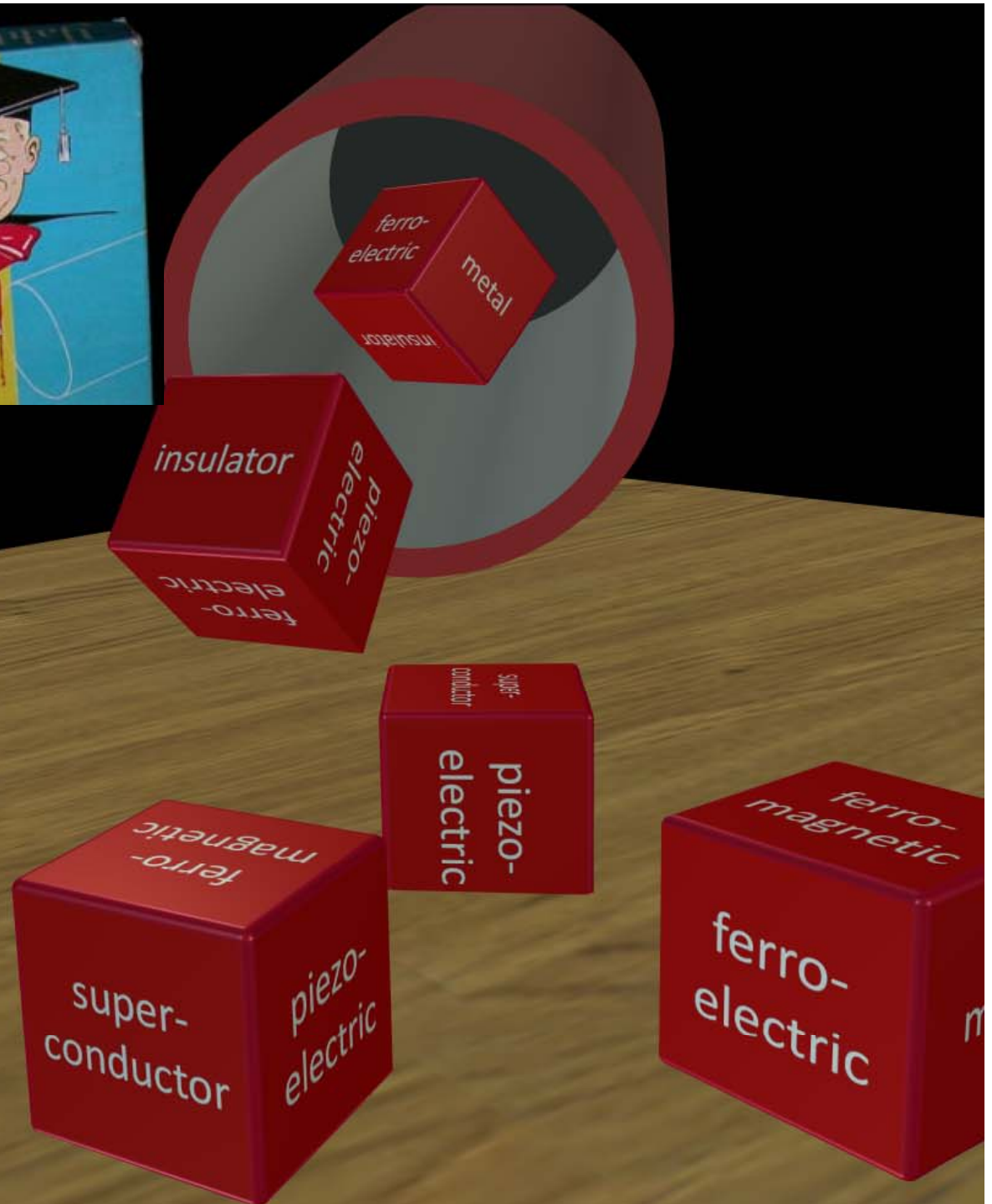


SrTiO₃
Edition!

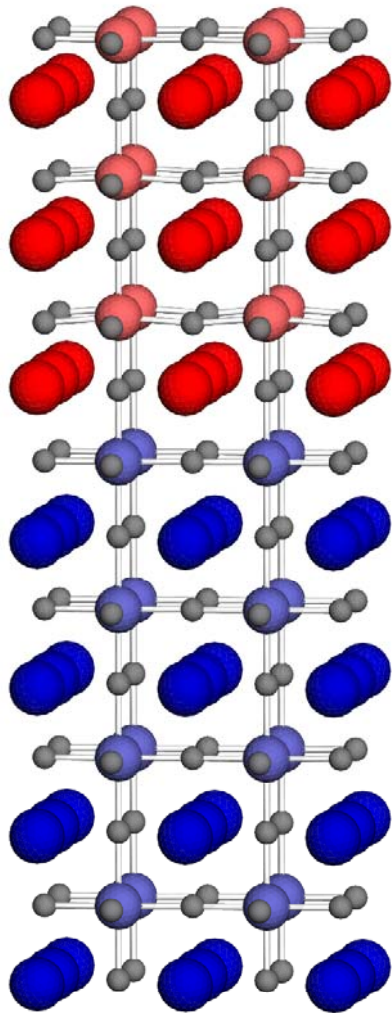


"The complexities of the crystal structure, lattice waves, band structure, transport properties, impurity electrons and superconductivity have inspired the comment: 'If SrTiO₃ had magnetic properties, a complete study of this material would require a thorough knowledge of all of solid state physics.'"

Marvin L. Cohen, in *Superconductivity* vol. 1, Robert Parks, Ed. (New York, 1969).

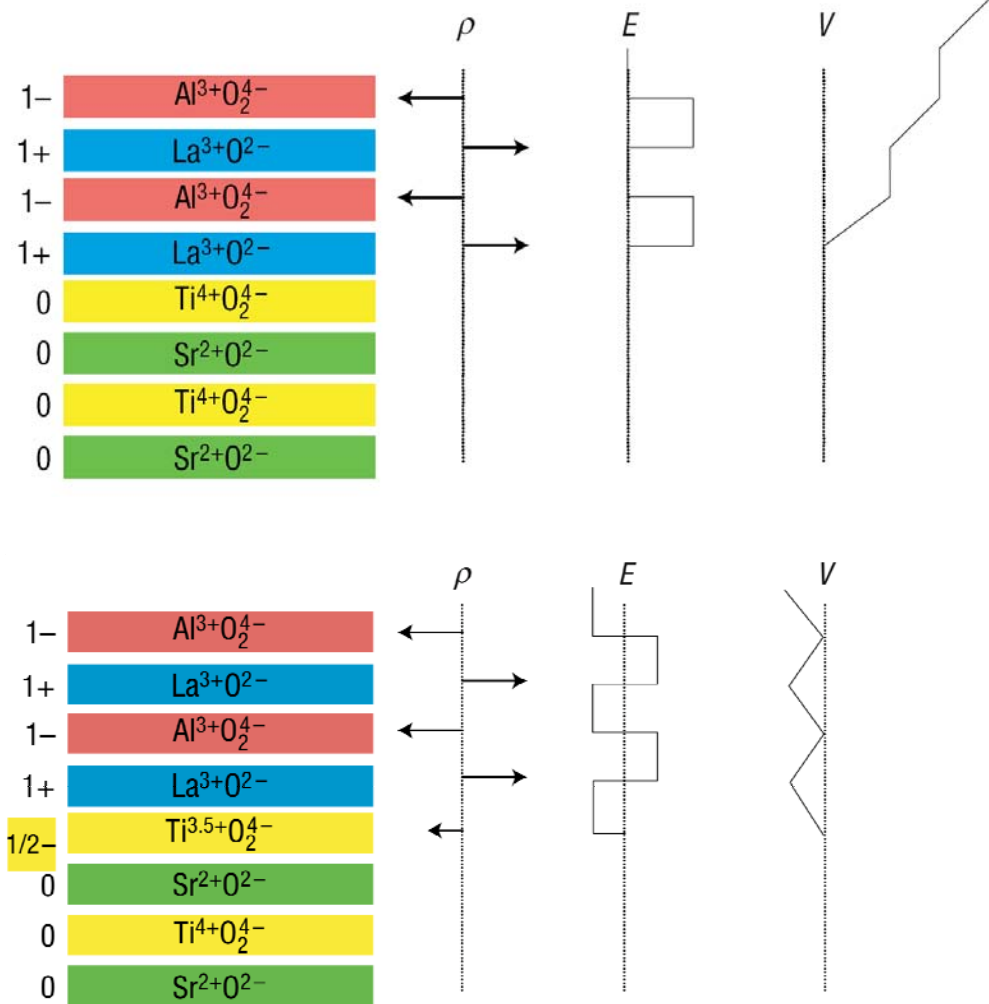


Polar Discontinuity: $\text{LaAlO}_3 / \text{SrTiO}_3$



LaAlO_3

SrTiO_3



Nakagawa, Hwang, and Muller, *Nature Materials* **5**, 204 (2006)

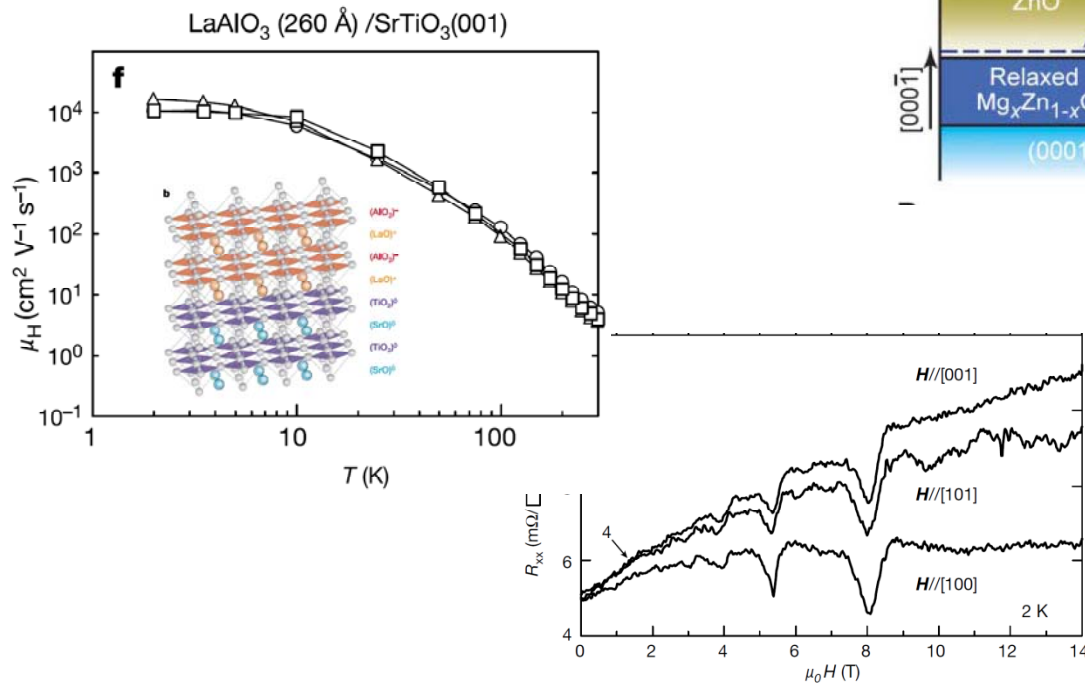
High-Mobility 2DEGs at Oxide Interfaces

A high-mobility electron gas at the $\text{LaAlO}_3/\text{SrTiO}_3$ heterointerface

A. Ohtomo^{1,2,3} & H. Y. Hwang^{1,3,4}

¹Bell Laboratories, Lucent Technologies, Murray Hill, New Jersey 07974, USA
²Institute for Materials Research, Tohoku University, Sendai, 980-8577, Japan
³Japan Science and Technology Agency, Kawaguchi, 332-0012, Japan
⁴Department of Advanced Materials Science, University of Tokyo, Kashiwa, Chiba, 277-8651, Japan

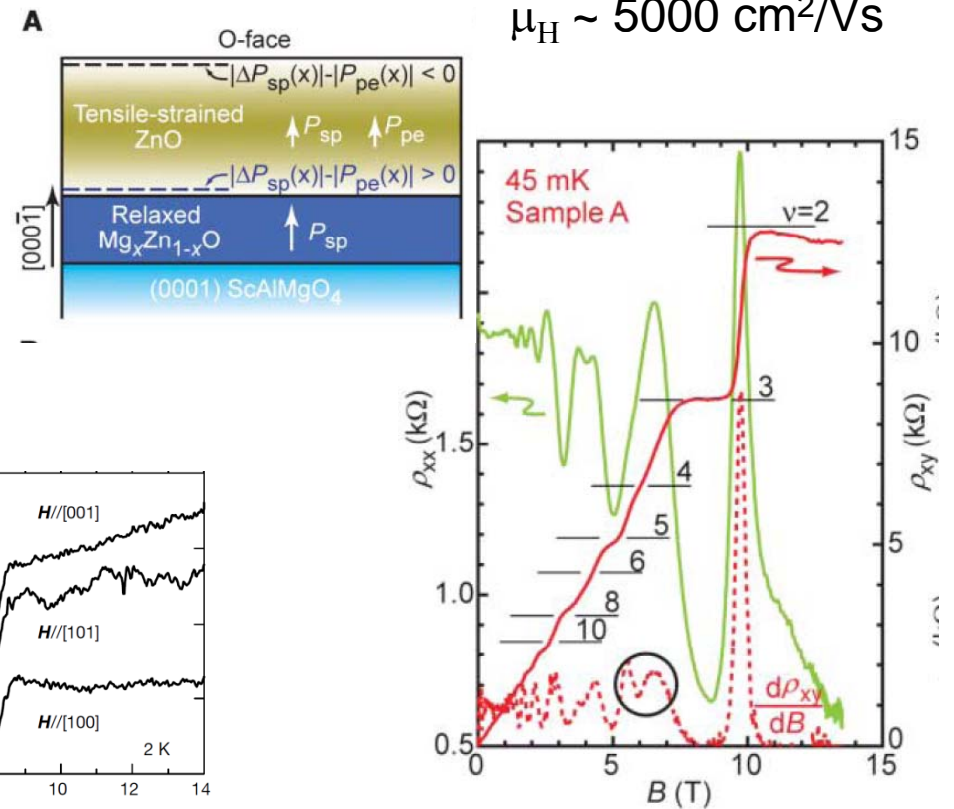
NATURE | VOL 427 | 29 JANUARY 2004 | www.nature.com/nature



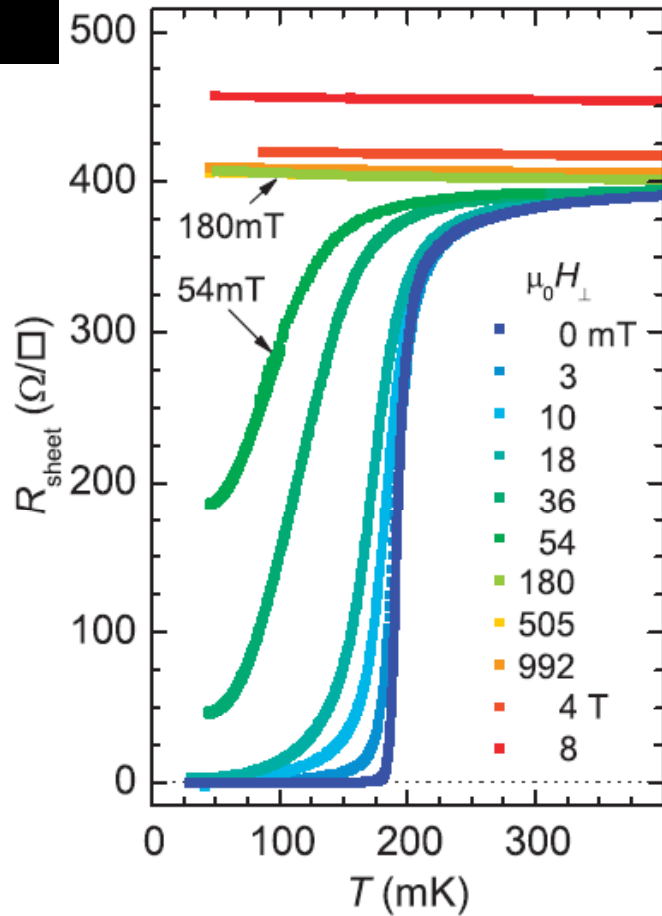
Quantum Hall Effect in Polar Oxide Heterostructures

A. Tsukazaki,¹ A. Ohtomo,^{1,2*} T. Kita,^{3,4} Y. Ohno,⁴ H. Ohno,^{3,4} M. Kawasaki^{1,5*}

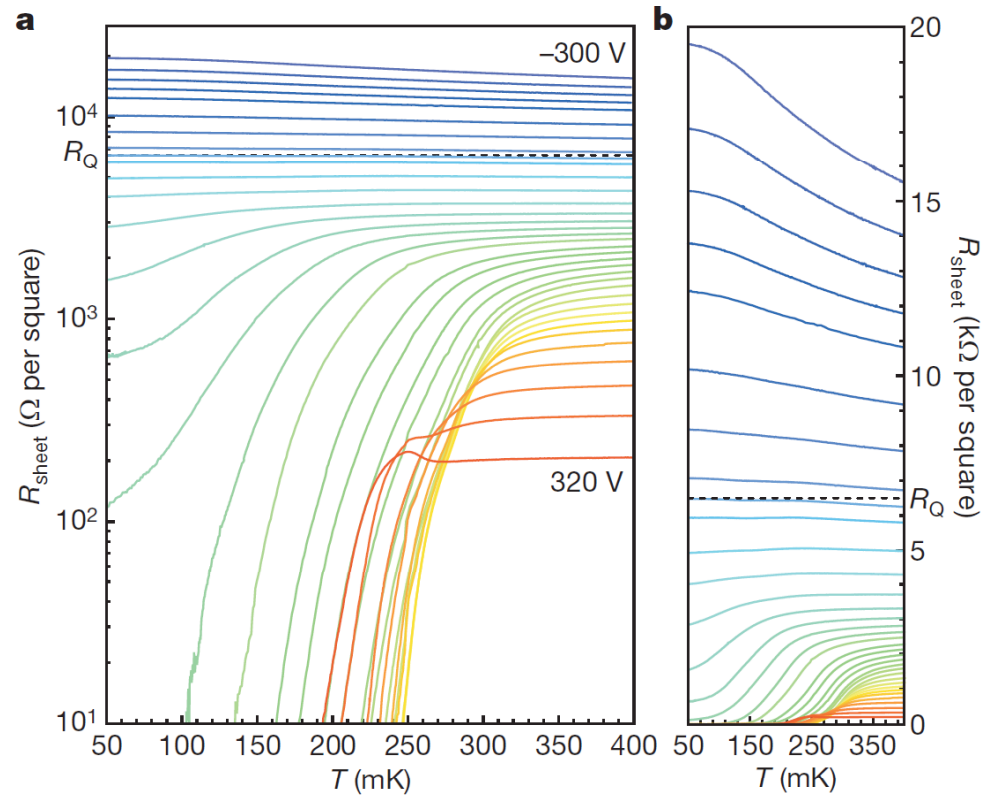
9 MARCH 2007 VOL 315 SCIENCE www.sciencemag.org



Superconductivity at the LaAlO₃/SrTiO₃ Interface



Superconducting Interfaces Between Insulating Oxides
 N. Reyren, *et al.*
Science **317**, 1196 (2007);
 DOI: 10.1126/science.1146006



LETTERS

nature Vol 456 | 4 December 2008 | doi:10.1038/nature07576

Electric field control of the LaAlO₃/SrTiO₃ interface ground state

A. D. Caviglia¹, S. Gariglio¹, N. Reyren¹, D. Jaccard¹, T. Schneider², M. Gabay³, S. Thiel⁴, G. Hammerl⁴, J. Mannhart⁴ & J.-M. Triscone¹

Magnetism at the LaAlO₃/SrTiO₃ Interface

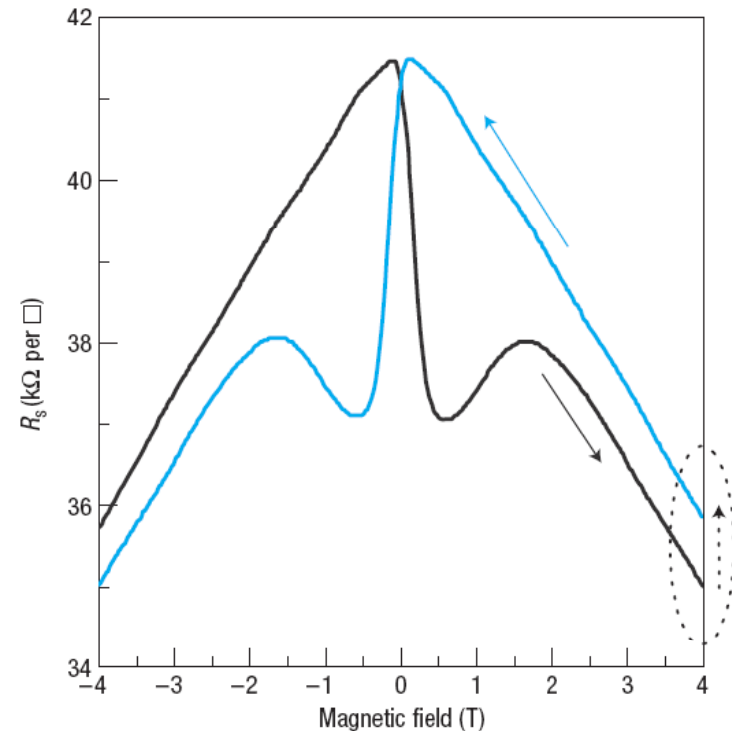
LETTERS

Magnetic effects at the interface between non-magnetic oxides

A. BRINKMAN^{1*}, M. HUIJBEN^{1†}, M. VAN ZALK¹, J. HUIJBEN¹, U. ZEITLER², J. C. MAAN², W. G. VAN DER WIEL³, G. RIJNDERS¹, D. H. A. BLANK¹ AND H. HILGENKAMP¹

Published online: 3 June 2007; doi:10.1038/nmat1931

- Magnetoresistance independent of field direction
- Long time scale (~10 sec)



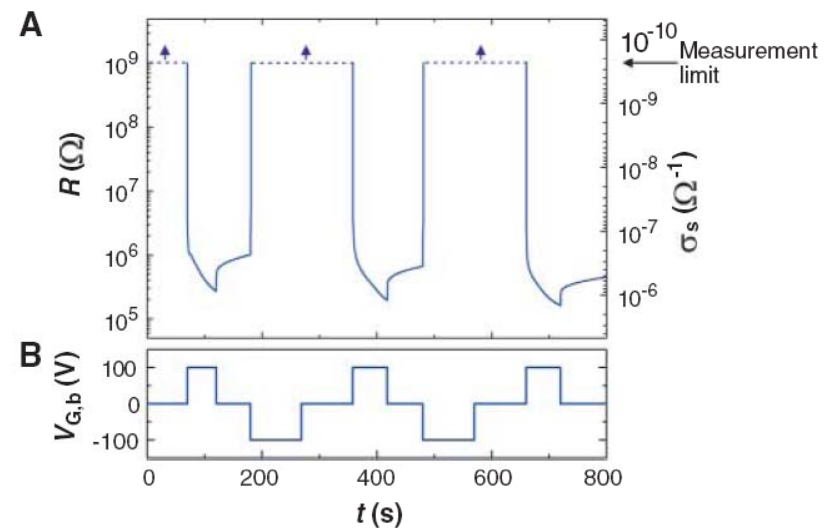
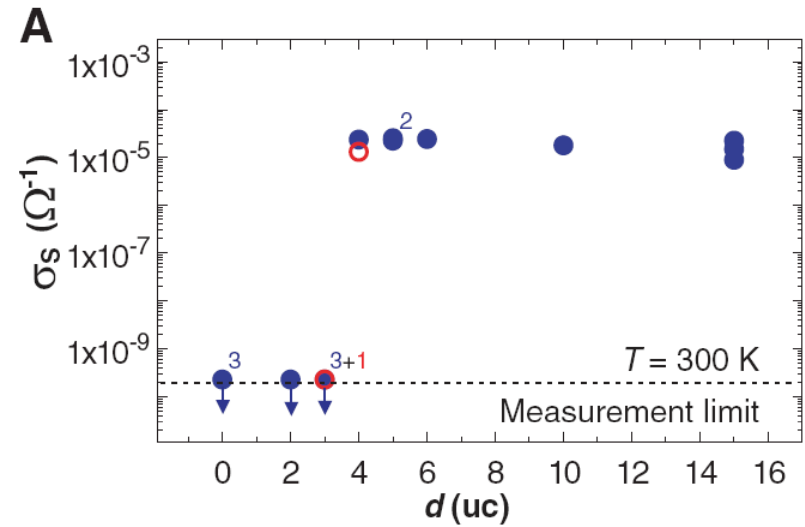
Metal-Insulator Transition

Tunable Quasi-Two-Dimensional Electron Gases in Oxide Heterostructures

S. Thiel,¹ G. Hammerl,¹ A. Schmehl,² C. W. Schneider,¹ J. Mannhart^{1*}

29 SEPTEMBER 2006 VOL 313 SCIENCE www.sciencemag.org

- Electric-field driven phase transition
- Voltage applied across SrTiO₃ substrate
- Critical thickness
 - ~ 3 unit cells LaAlO₃



LaAlO₃/SrTiO₃

Etch-a-Sketch Nanoelectronics

Toy →



(b)

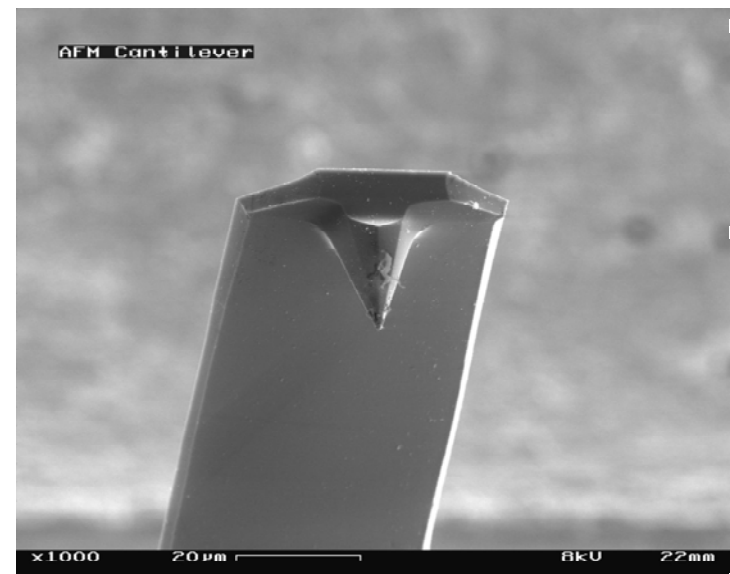


(c)

Tool →

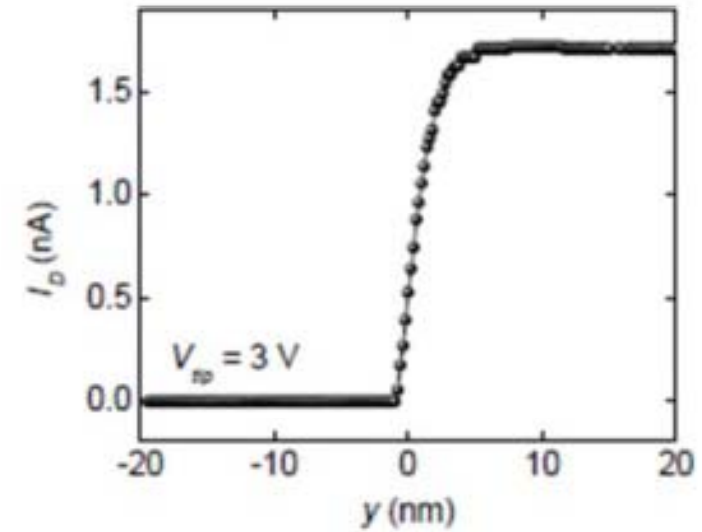
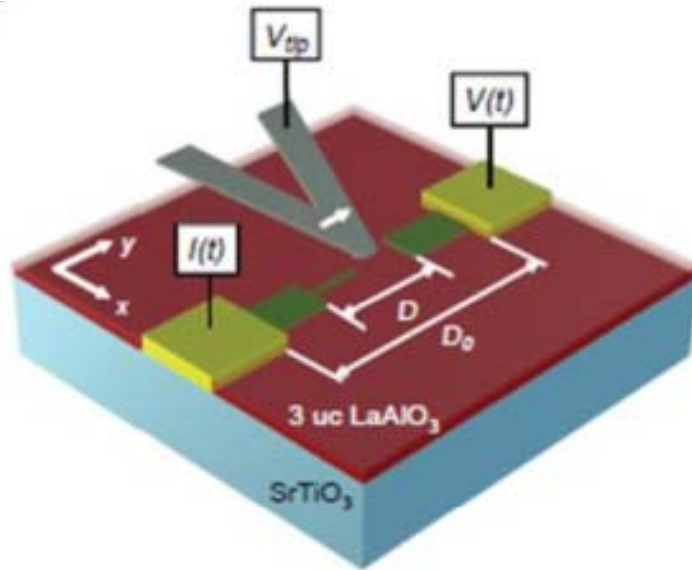


(d)

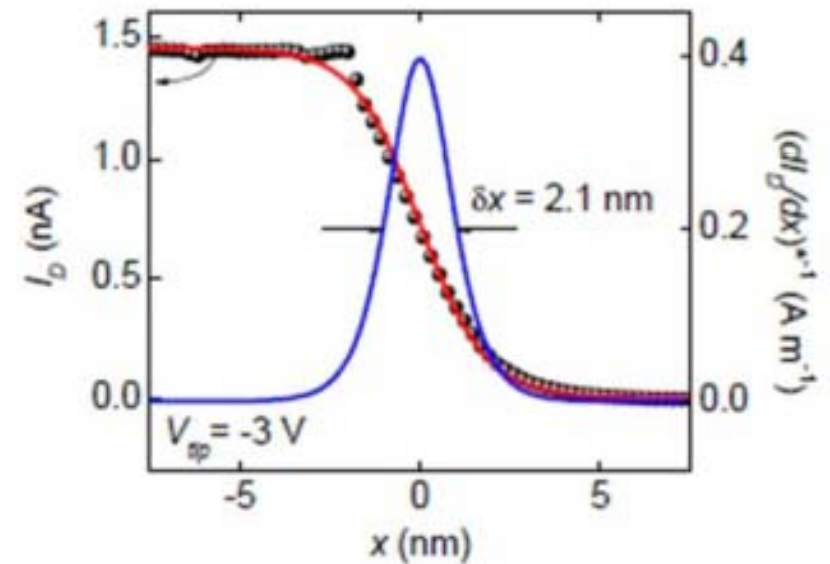
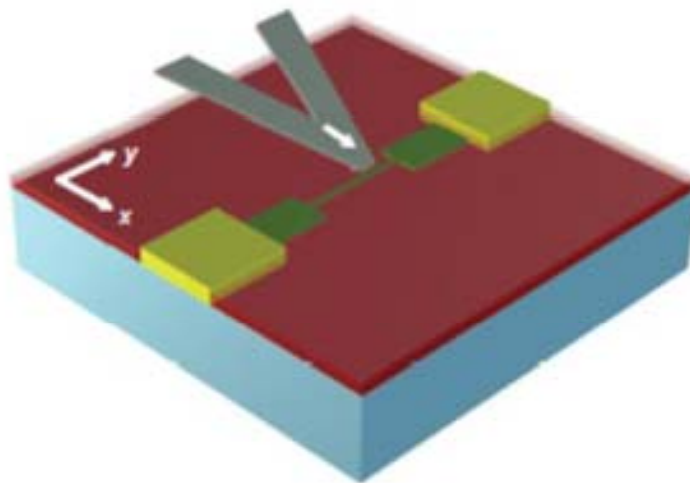


Conducting AFM Lithography of LaAlO₃/SrTiO₃

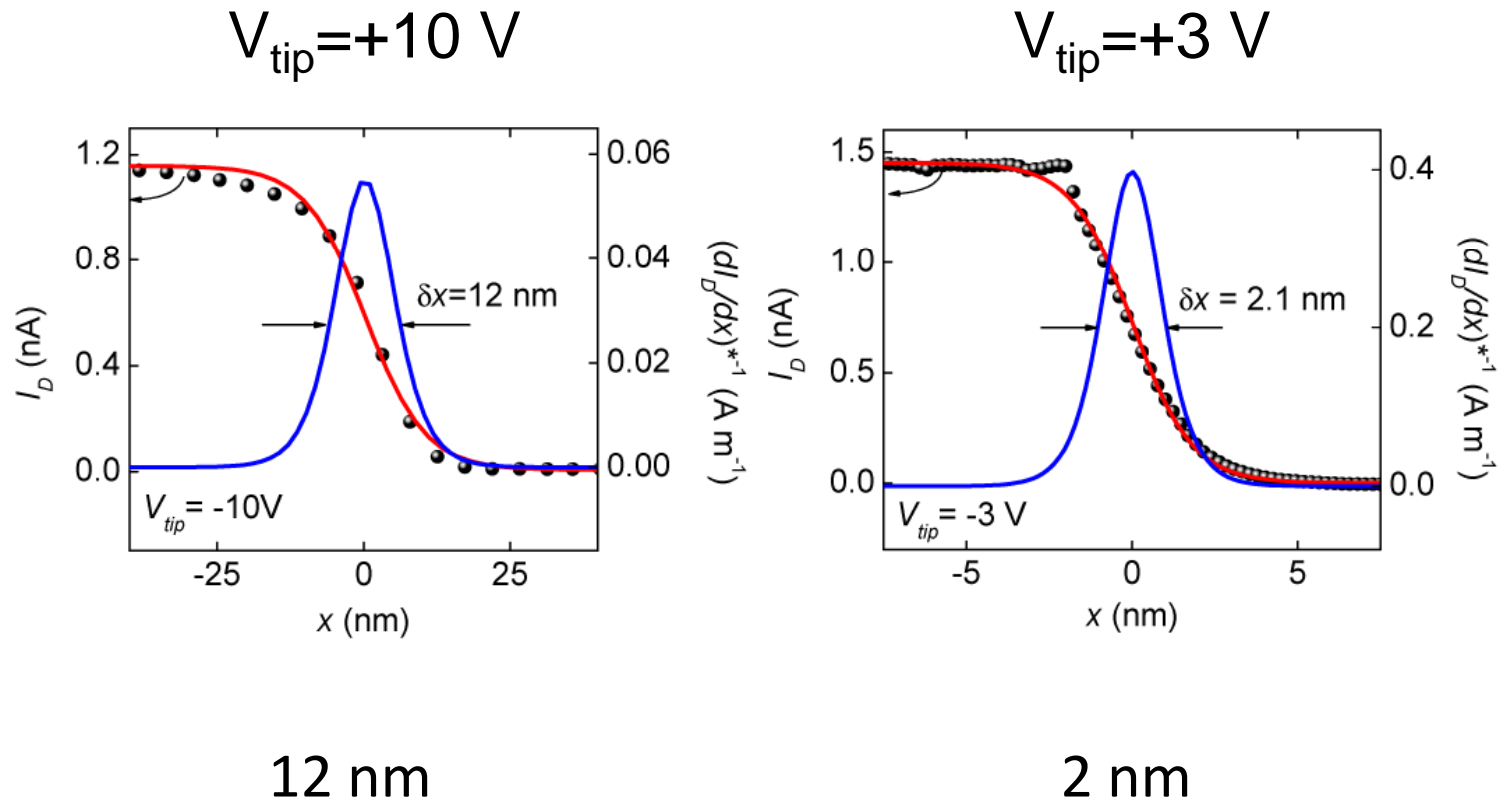
Writing



Erasing



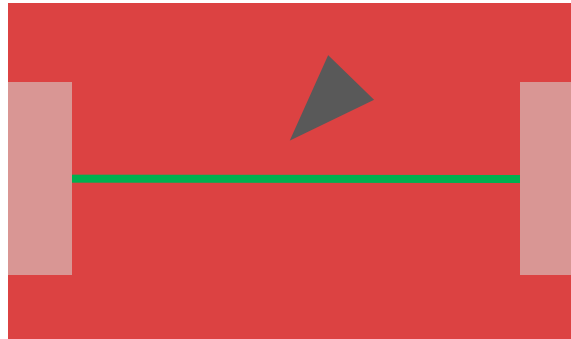
Ultranarrow Wires



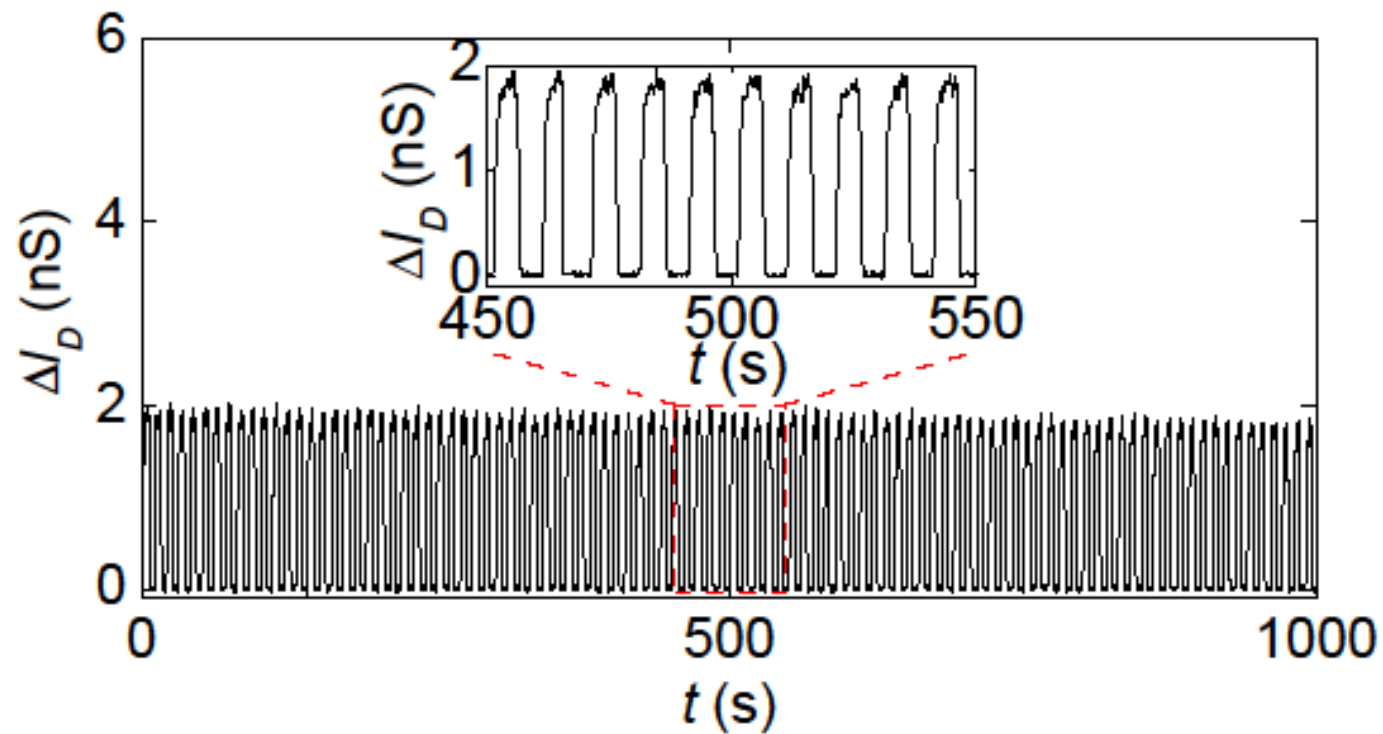
C. Cen, S. Thiel, J. Mannhart, and J. Levy, *Science* **323**, 1026 (2009).

Multiple Write/Erase

Write with $V_{\text{tip}} > 0$



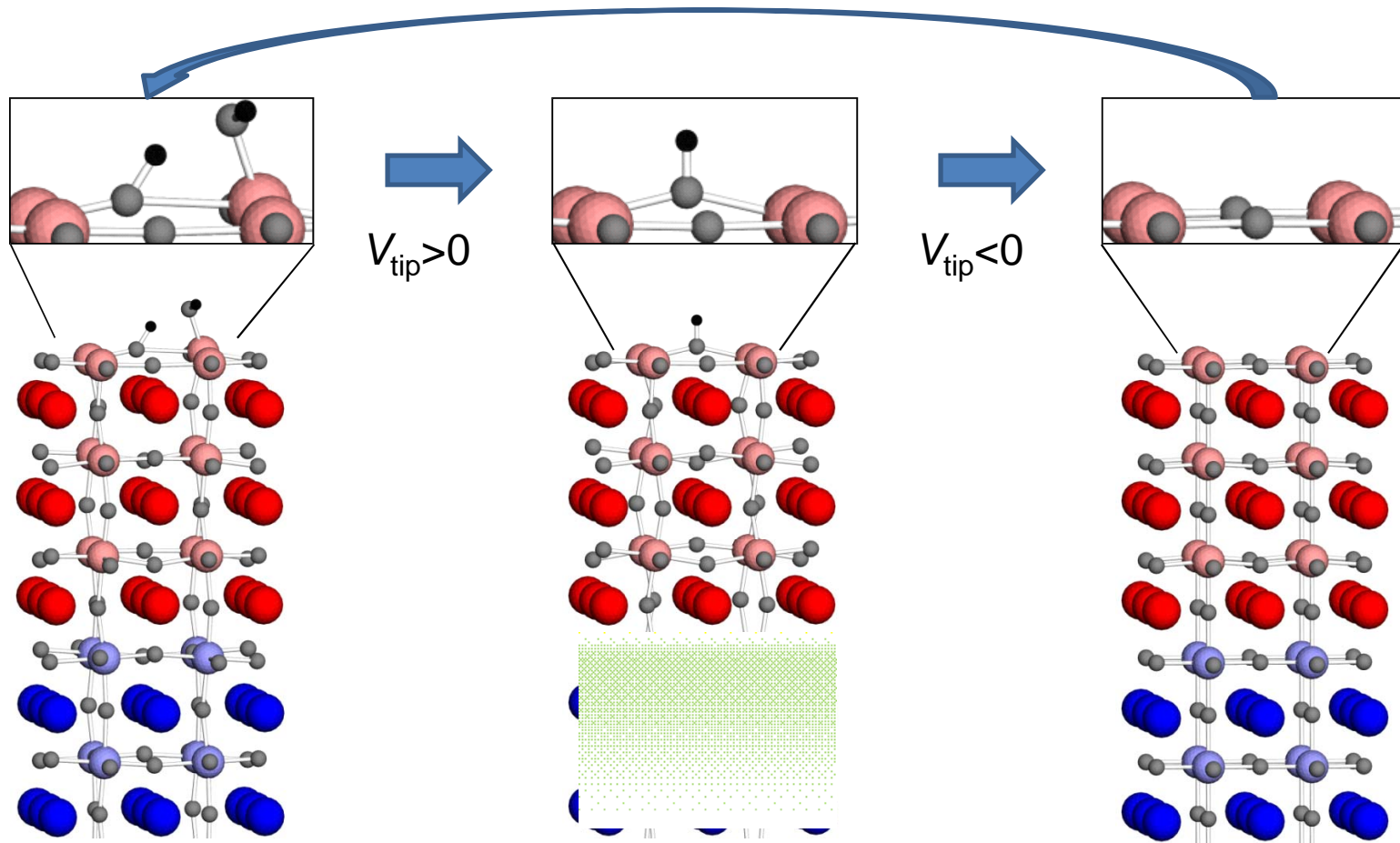
Erase with $V_{\text{tip}} < 0$



C. Cen, S. Thiel, J. Mannhart, and J. Levy, *Science* **323**, 1026 (2009).

Possible Mechanism: “Water Cycle”

(C. S. Hellberg, unpublished)

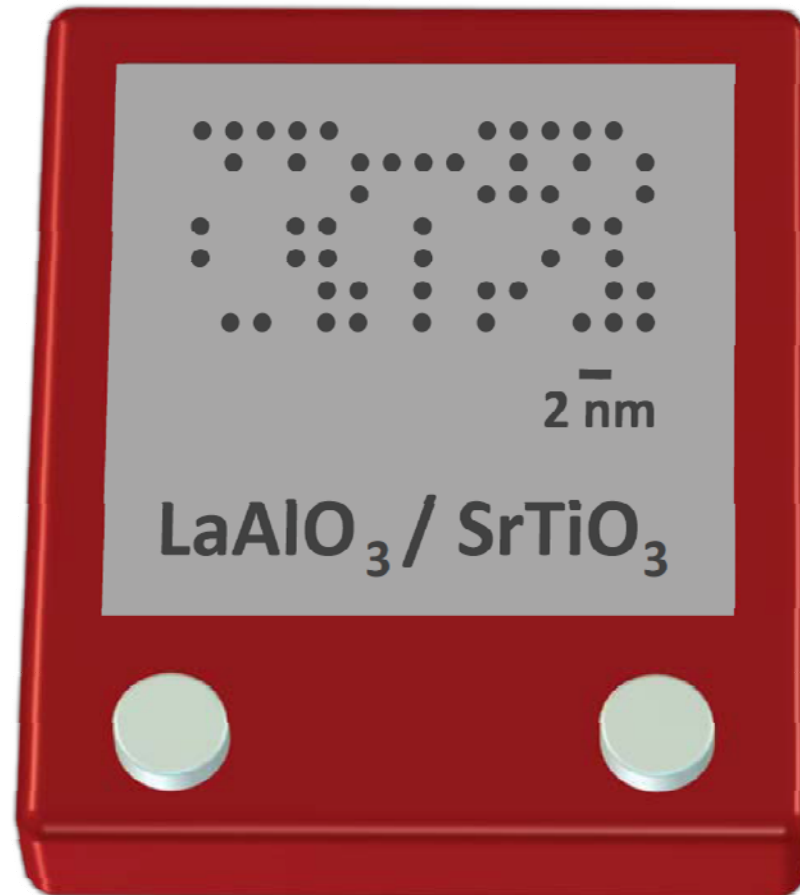


H₂O adsorbs, dissociates on LaAlO₃ surface

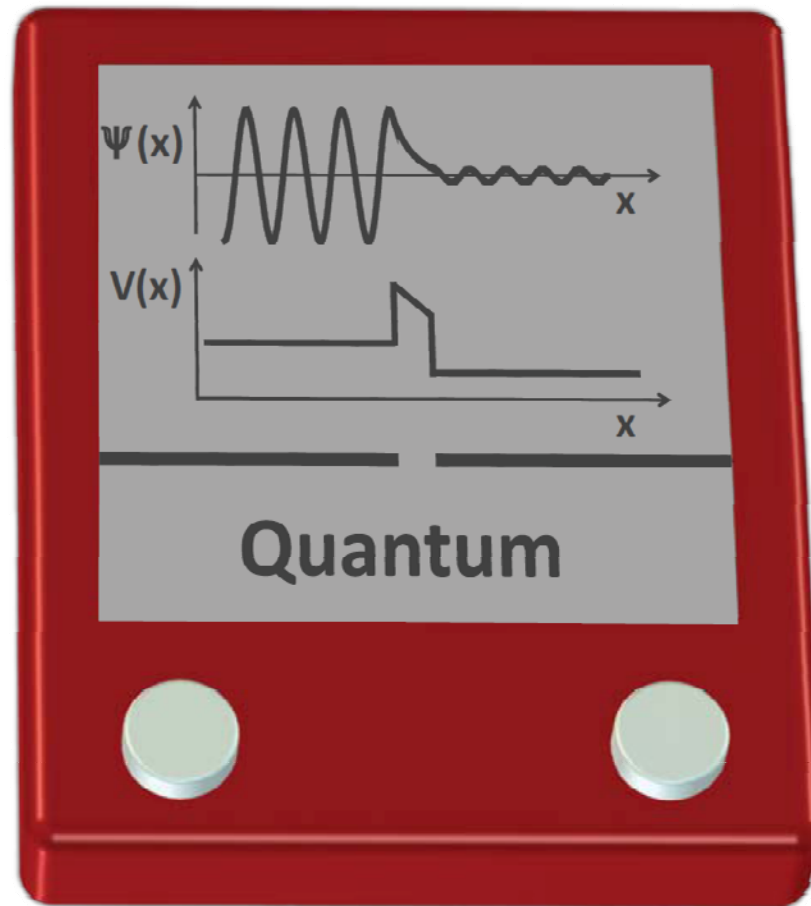
Positive tip removes OH⁻, leaving H⁺ on surface and producing conducting interface

Positive tip removes H⁺, restoring insulating state.

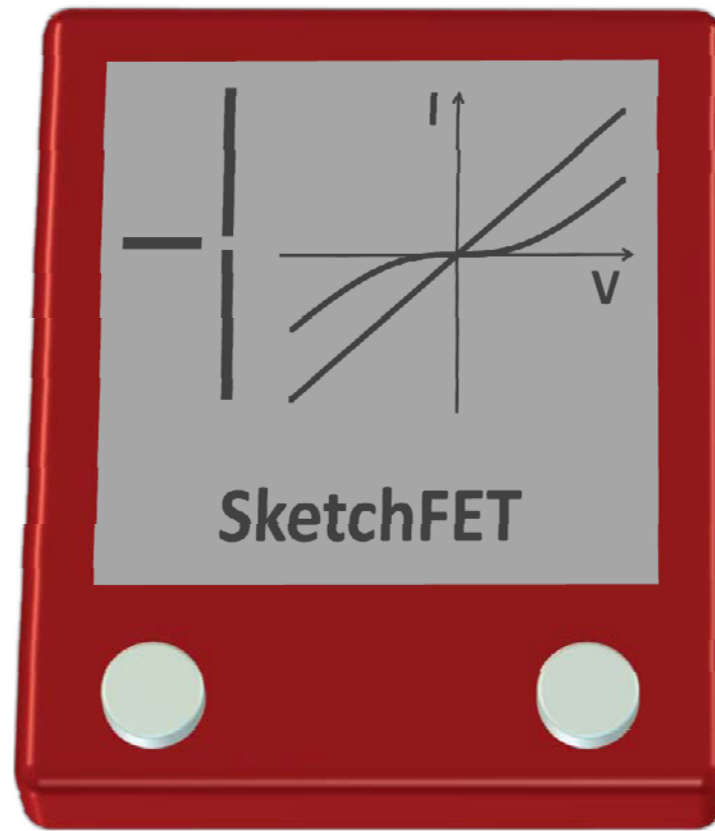
Ultrahigh Density Memory



Quantum Mechanics On-The-Fly



Transistor



Sketch-based Electronic Transport within Complex-oxide
Heterostructure Field-Effect Transistor

QUANTUM TRANSPORT AT LOW TEMPERATURES

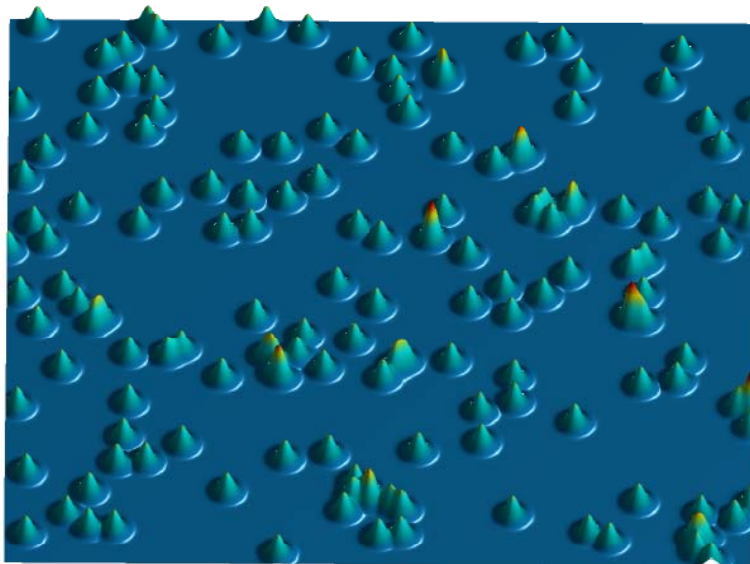
- Spin-Orbit (Rashba) Coupling
- Quantum Coherence
- Quantum Hall states

Experiments performed at:



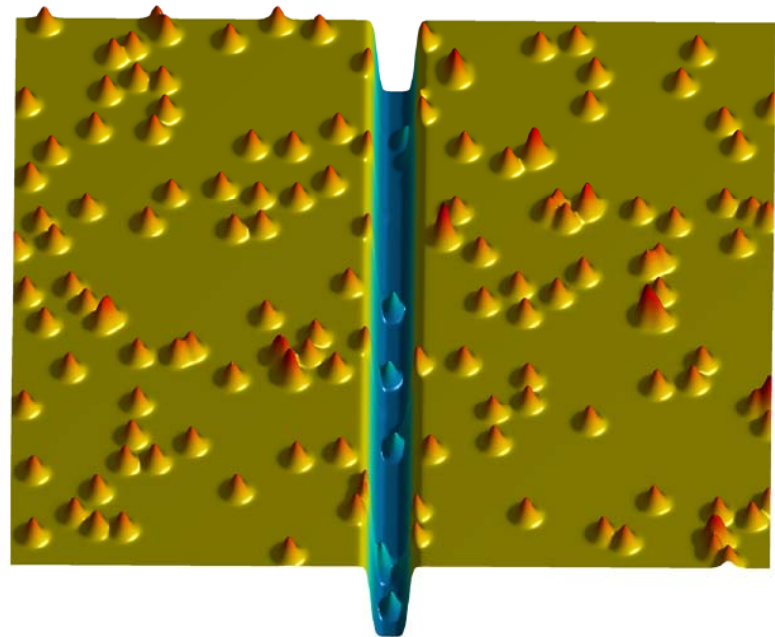
Effect of Dimensionality on Transport

Two Dimensions



100 nm

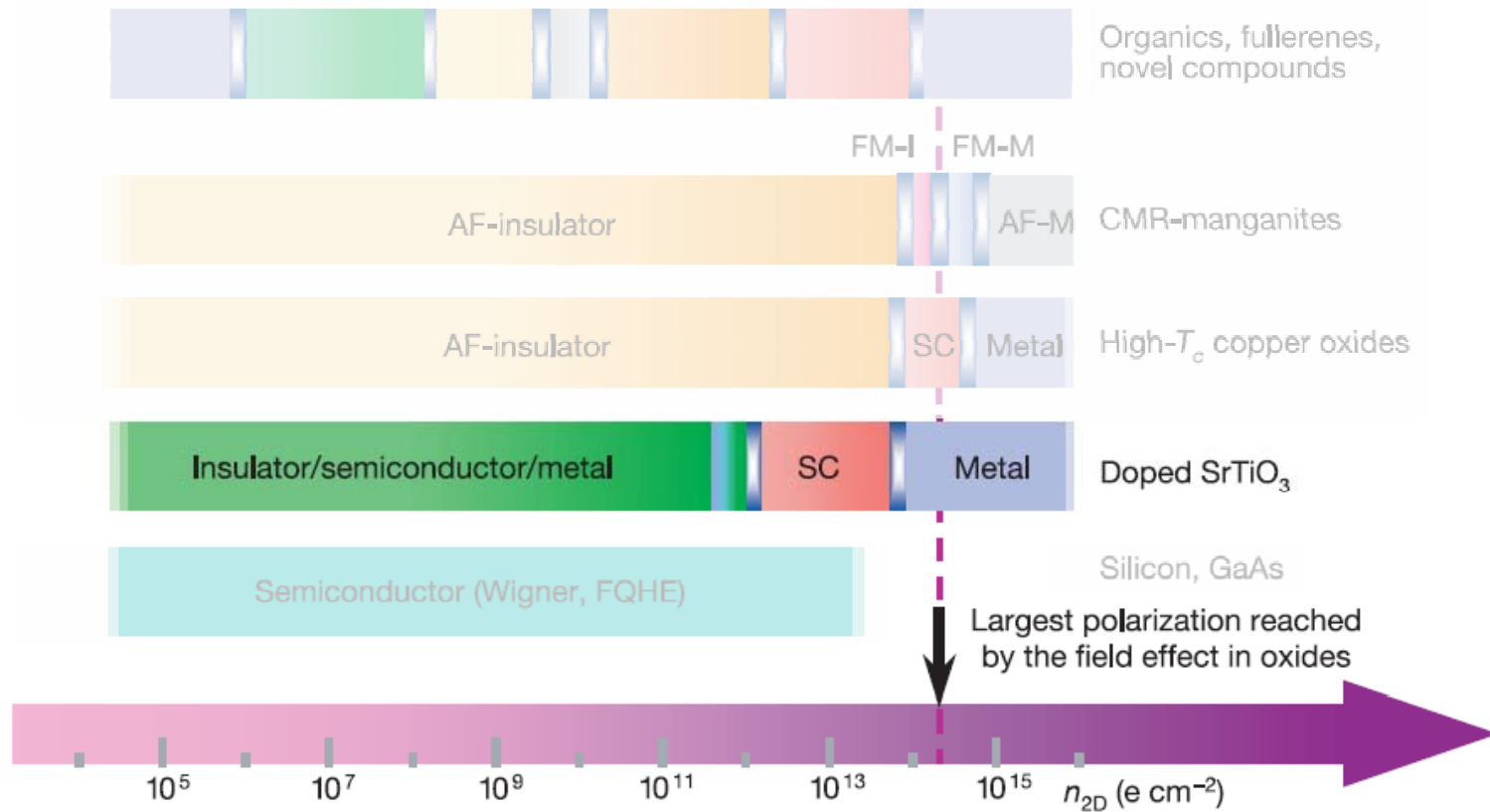
One Dimension



100 nm

Mean free path ~ 16 nm (mobility ~ 1000 cm²/Vs at low temp)
Quasi-1D confinement may help to suppress scattering in 1d

Effect of Carrier Density on Transport



C. H. Ahn, J. M. Triscone, J. Mannhart, Nature **424**, 1023 (2003)

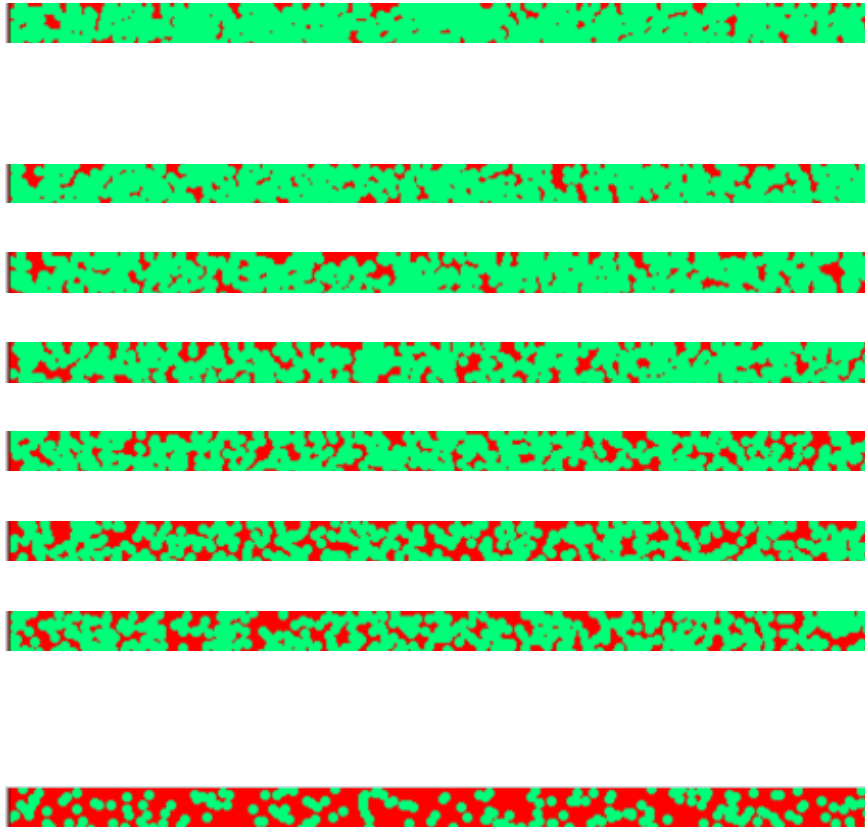
Transport Parameters

TABLE I Electronic properties of the 2DEG in GaAs-AlGaAs heterostructures and Si inversion l

| | | GaAs(100) | Si(100) | LaAlO ₃ /SrTiO ₃ | Units |
|---------------------------------------|-------------------------------------|---------------|-----------|--|---|
| Effective Mass | m | 0.067 | 0.19 | 4.5 | $m_e = 9.1 \times 10^{-28}$ g |
| Spin Degeneracy | g_s | 2 | 2 | 2 | |
| Valley Degeneracy | g_v | 1 | 2 | 1 | |
| Dielectric Constant | ϵ | 13.1 | 11.9 | 300–30K | $\epsilon_0 = 8.9 \times 10^{-12}$ Fm ⁻¹ |
| Density of States | $\rho(E) = g_s g_v (m/2\pi\hbar^2)$ | 0.28 | 1.59 | 20 | 10^{11} cm ⁻² meV ⁻¹ |
| Electronic Sheet Density ^a | n_s | 4 | 1–10 | 8–800 | 10^{11} cm ⁻² |
| Fermi Wave Vector | $k_F = (4\pi n_s / g_s g_v)^{1/2}$ | 1.58 | 0.56–1.77 | 2–20 | 10^6 cm ⁻¹ |
| Fermi Velocity | $v_F = \hbar k_F / m$ | 2.7 | 0.34–1.1 | 0.06–0.6 | 10^7 cm/s |
| Fermi Energy | $E_F = (\hbar k_F)^2 / 2m$ | 14 | 0.63–6.3 | 0.4–4 | meV |
| Electron Mobility ^a | μ_e | $10^4 - 10^6$ | 10^4 | 6–1000 | cm ² /Vs |
| Scattering Time | $\tau = m\mu_e / e$ | 0.38–38 | 1.1 | 3 | ps |
| Diffusion Constant | $D = v_F^2 \tau / 2$ | 140–14000 | 6.4–64 | 0.4–4 | cm ² /s |
| Resistivity | $\rho = (n_s e \mu_e)^{-1}$ | 1.6–0.016 | 6.3–0.63 | 7–0.07 | kΩ |
| Fermi Wavelength | $\lambda_F = 2\pi / k_F$ | 40 | 112–35 | 28 | nm |
| Mean Free Path | $l = v_F \tau$ | $10^2 - 10^4$ | 37–118 | 15–150 | nm |
| Phase Coherence Length ^b | $l_\phi = (D\tau_\phi)^{1/2}$ | 200–... | 40–400 | | nm(T/K) ^{-1/2} |
| Thermal Length | $l_T = (\hbar D / k_B T)^{1/2}$ | 330–3300 | 70–220 | 1–18 | nm(T/K) ^{-1/2} |
| Cyclotron Radius | $l_{cycl} = \hbar k_F / eB$ | 100 | 37–116 | 15–150 | nm(B/T) ⁻¹ |
| Magnetic Length | $l_m = (\hbar / eB)^{1/2}$ | 26 | 26 | 26 | nm(B/T) ^{-1/2} |
| | $k_F l$ | 15.8–1580 | 2.1–21 | 3–300 | |
| | $\omega_c \tau$ | 1–100 | 1 | 0.1 | (B/T) |
| | $E_F / \hbar \omega_c$ | 7.9 | 1–10 | 17 | (B/T) ⁻¹ |

Metal-Insulator Transition in SrTiO₃ Nanowires

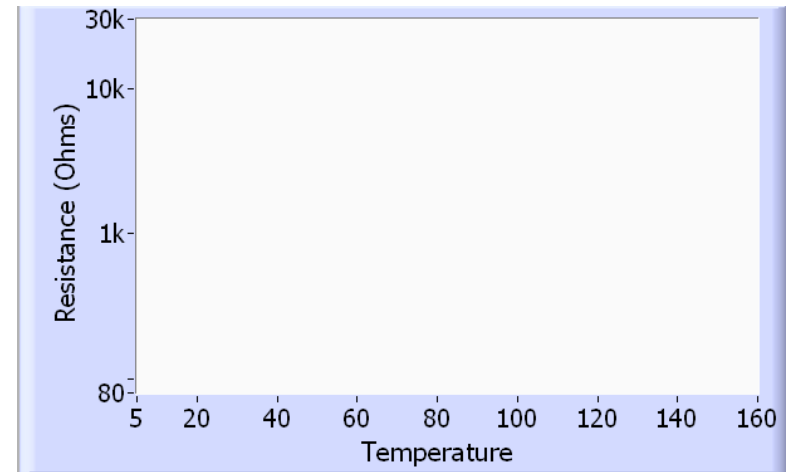
Metal



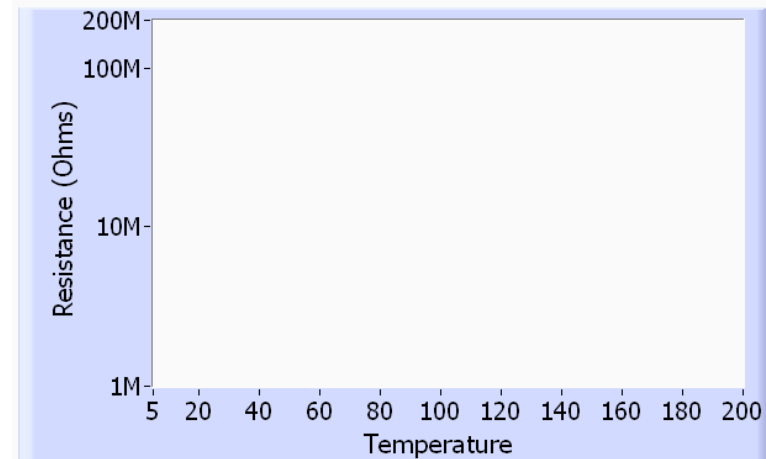
Insulator

Fluctuations enhanced in 1d

$n=8 \times 10^{13} \text{ cm}^{-2}$



$n=8 \times 10^{11} \text{ cm}^{-2}$



Weak Antilocalization

SPIN-ORBIT COUPLING

Rashba Spin-Orbit Coupling Probed by the Weak Antilocalization Analysis in InAlAs/InGaAs/InAlAs Quantum Wells as a Function of Quantum Well Asymmetry

Takaaki Koga,* Junsaku Nitta, Tatsushi Akazaki, and Hideaki Takayanagi

*NTT Basic Research Laboratories, Nippon Telegraph and Telephone Corporation, 3-1 Morinosato-Wakamiya,
Atsugi, Kanagawa 243-0198, Japan*

(Received 3 October 2001; published 2 July 2002)

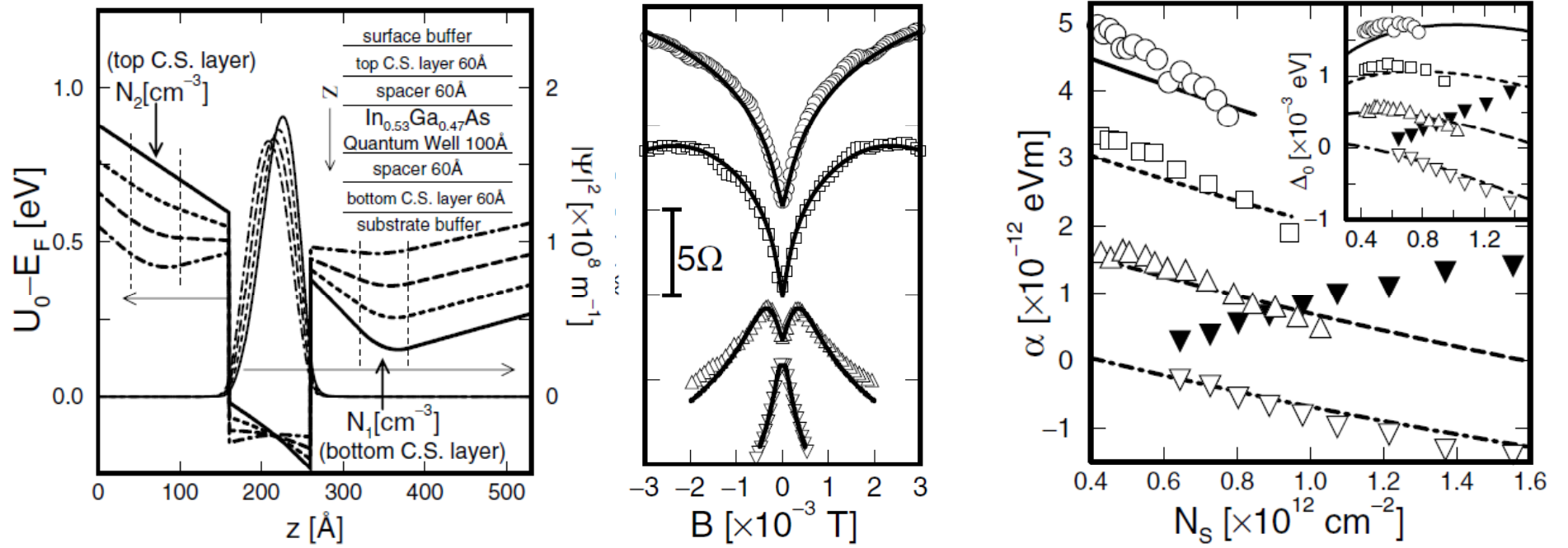
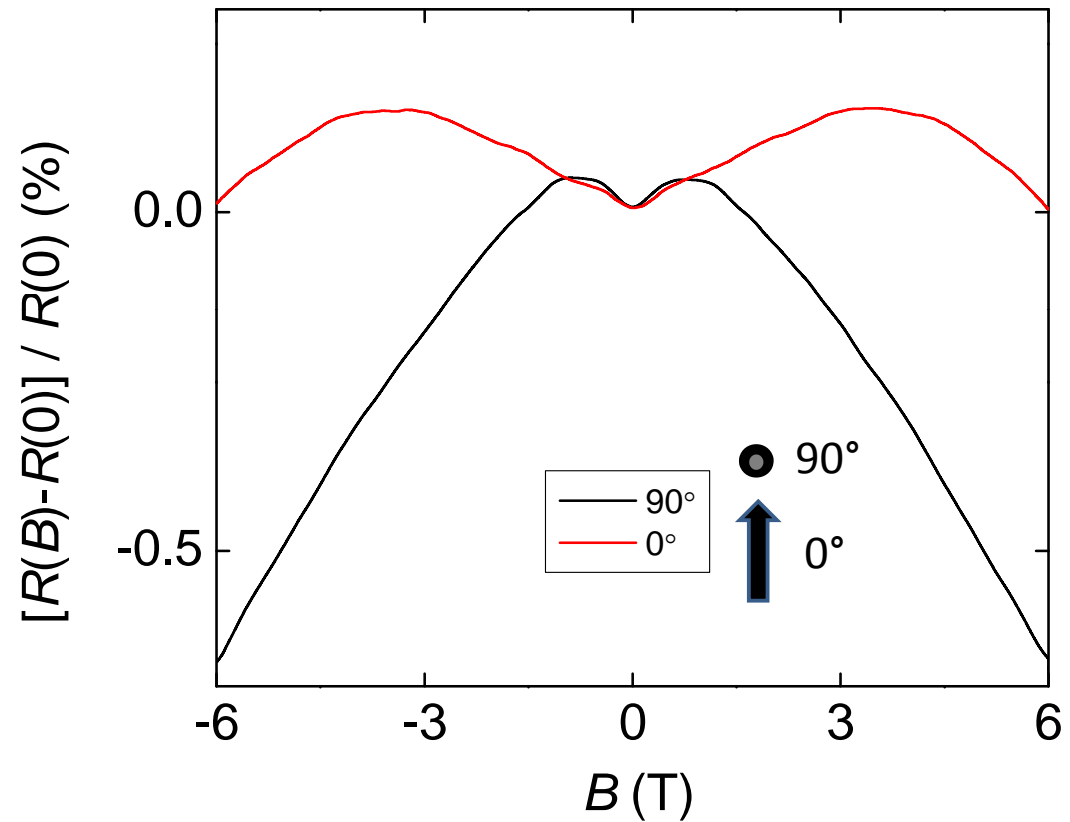
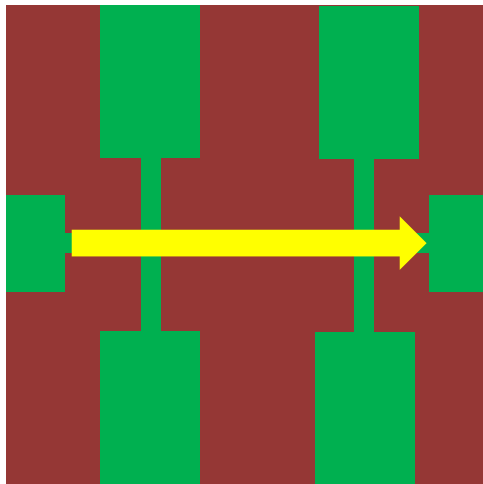


TABLE I. Impurity concentrations used in the present samples.

| | Sample 1 | Sample 2 | Sample 3 | Sample 4 |
|---------------------------|--------------------|--------------------|--------------------|--------------------|
| N_1 [cm ⁻³] | 4×10^{18} | 3×10^{18} | 2×10^{18} | 1×10^{18} |
| N_2 [cm ⁻³] | 0×10^{18} | 1×10^{18} | 2×10^{18} | 3×10^{18} |

Weak Antilocalization

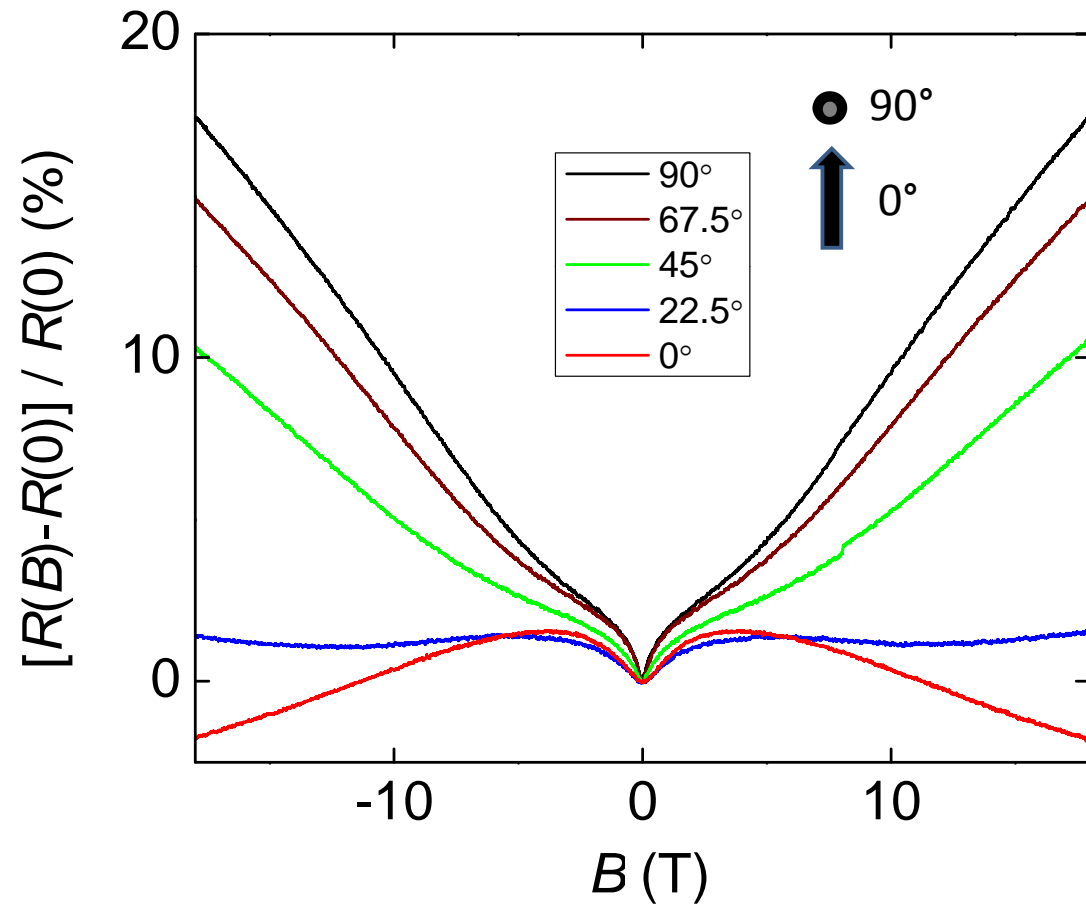
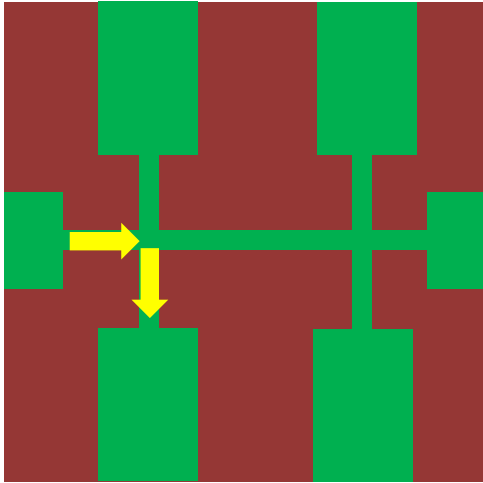
T=250 mK



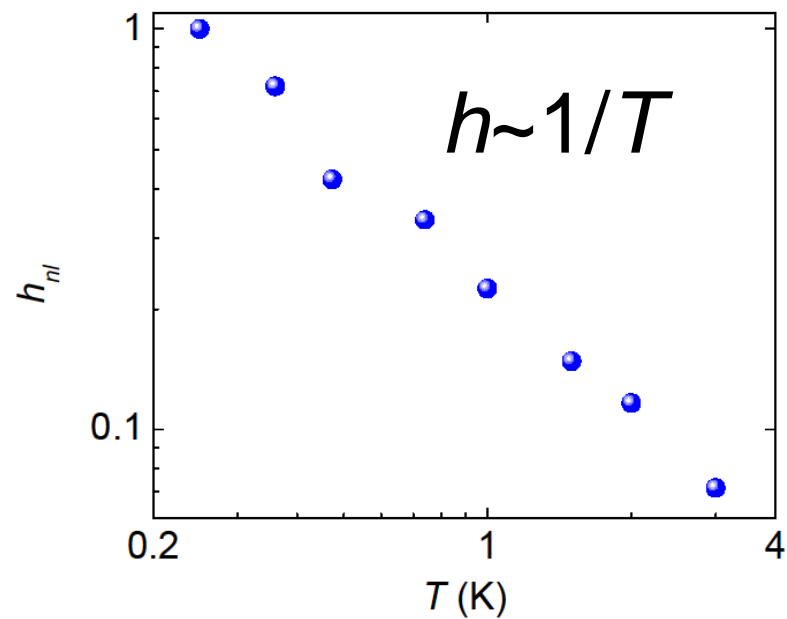
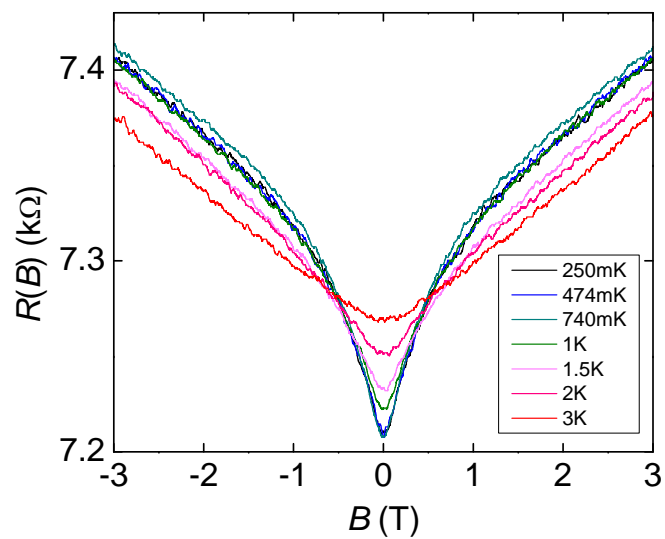
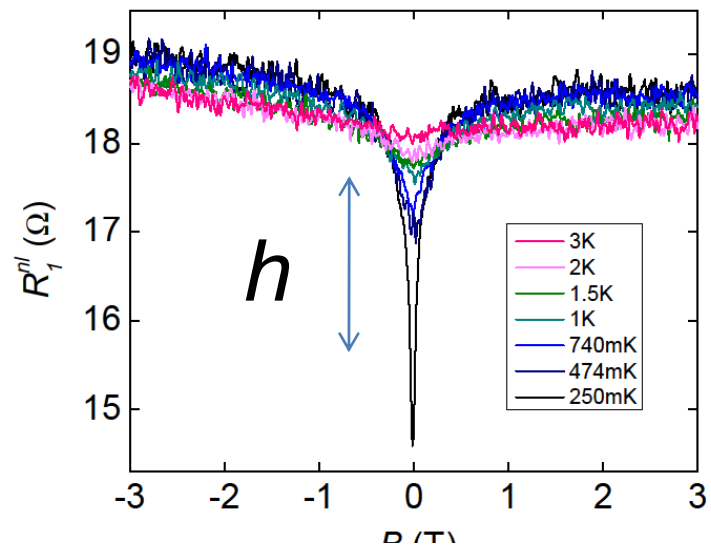
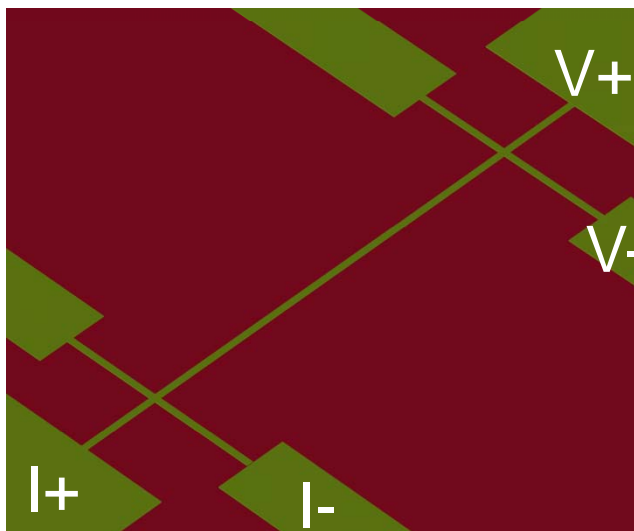
Evidence for spin-orbit coupling (Rashba)

Weak Antilocalization (I)

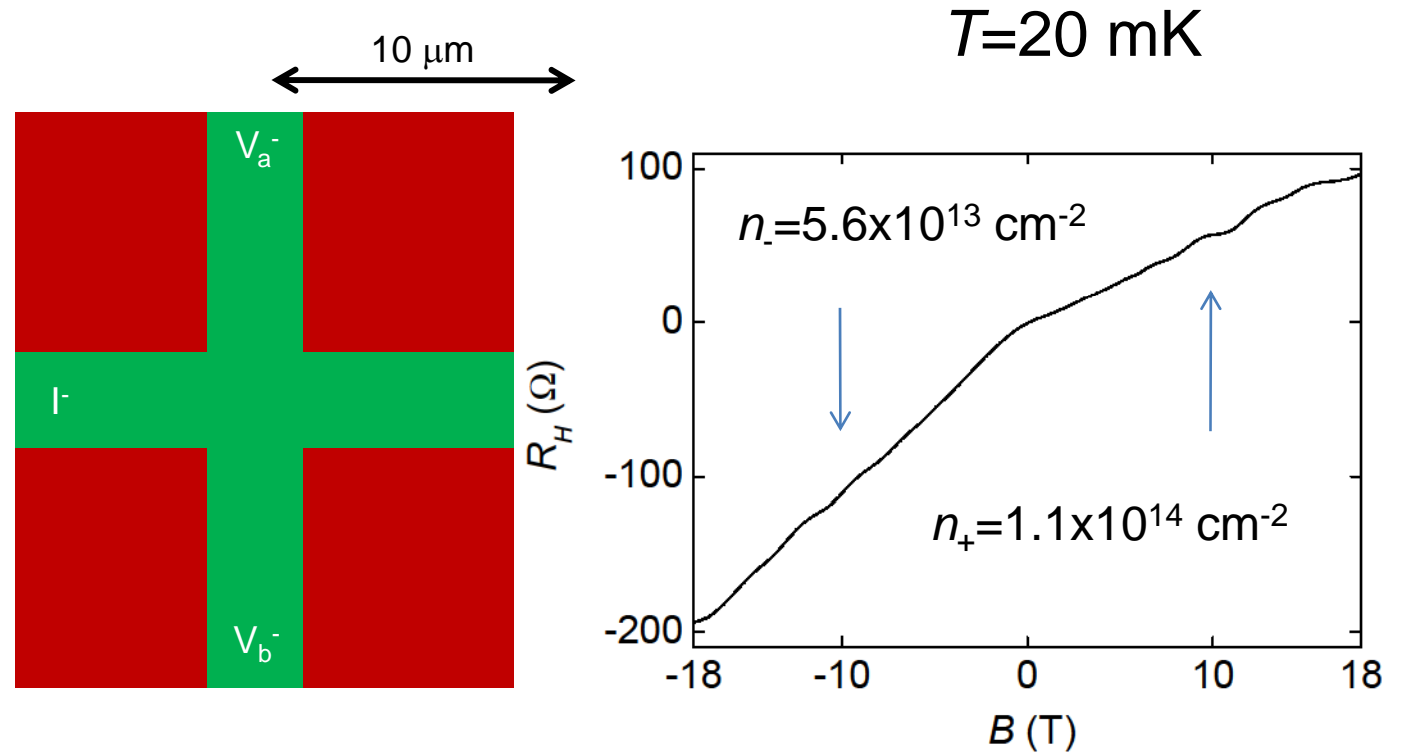
T=250 mK



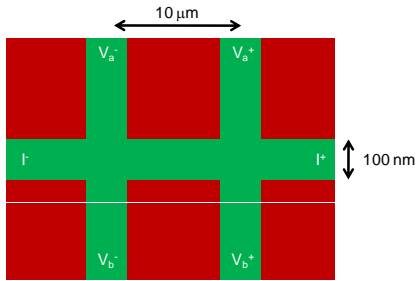
Non-Local Magnetoresistance



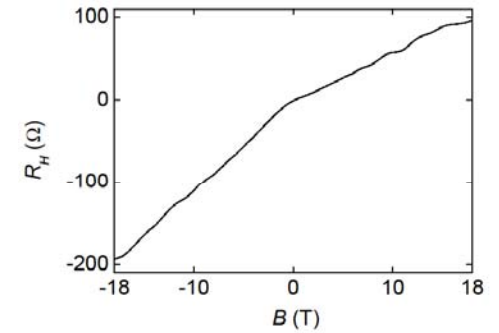
Hall Effect



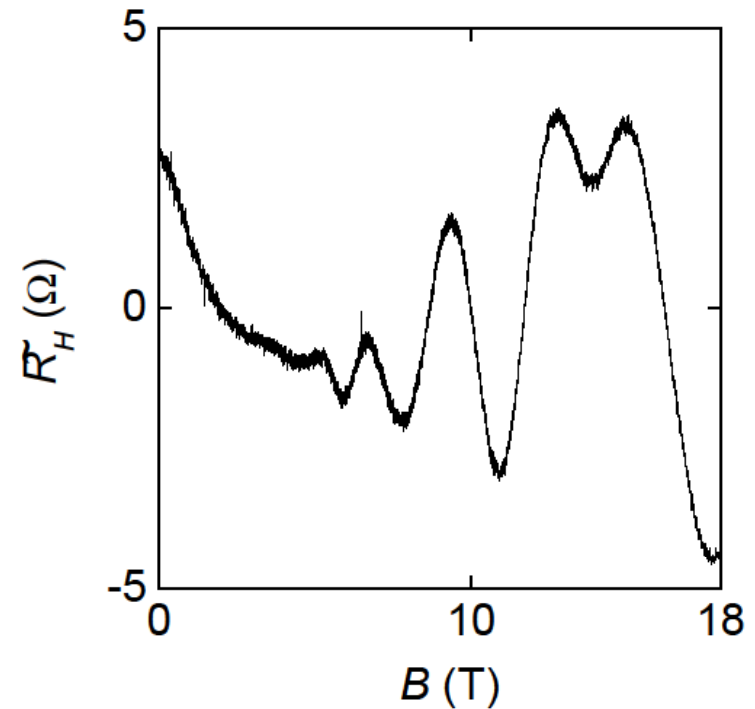
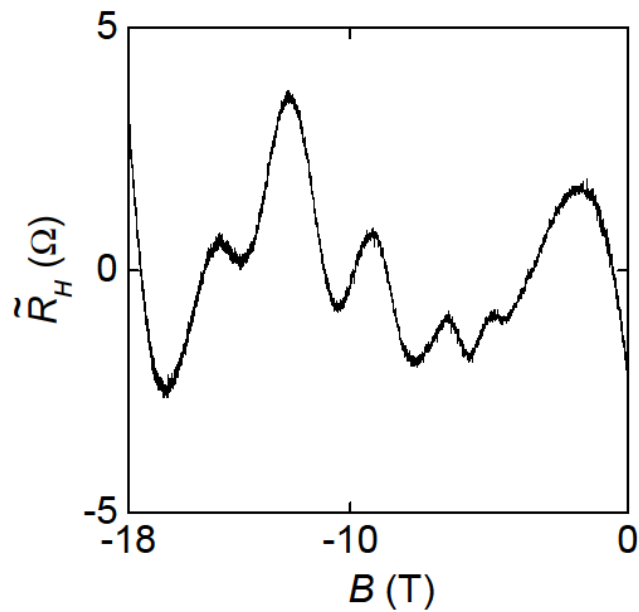
Symmetric component between $B > 0$ and $B < 0$



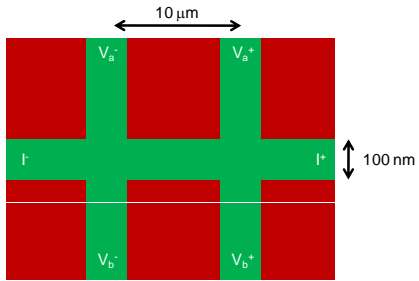
Hall Effect: Closeup



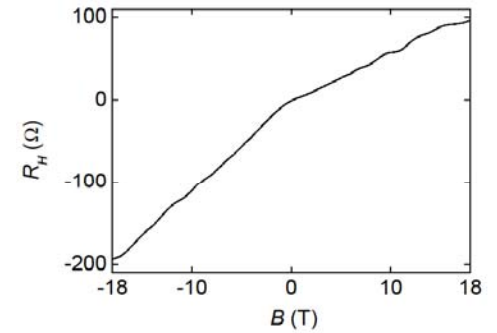
Subtract linear term



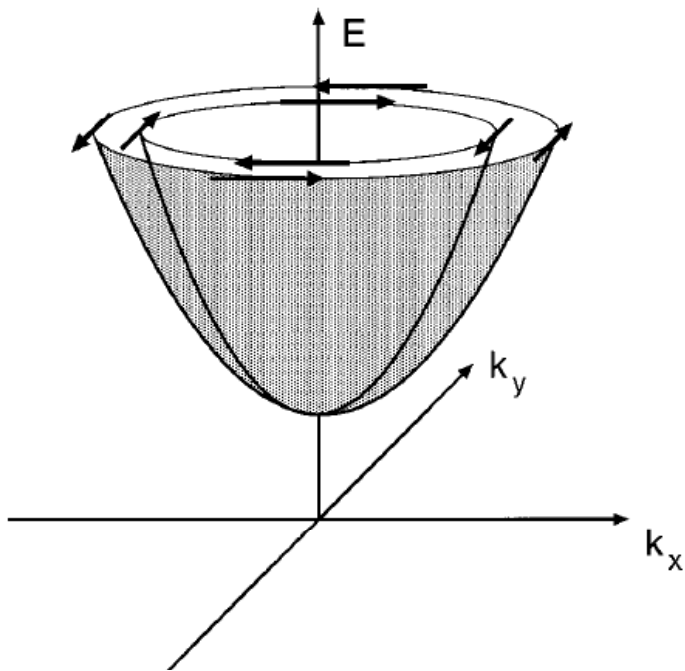
Shubnikov-de Haas oscillations (high ν)



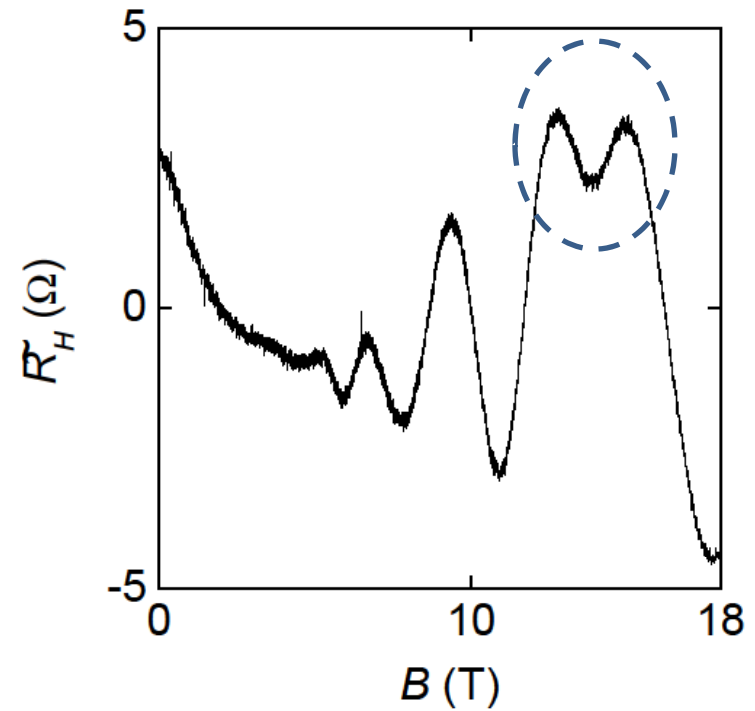
Hall Effect: Closeup



SdH beats \rightarrow Spin-Orbit coupling



J. Appl. Phys., Vol. 83, No. 8, 15 April 1998



Evidence for spin splitting in $\text{In}_x\text{Ga}_{1-x}\text{As}/\text{In}_{0.52}\text{Al}_{0.48}\text{As}$ heterostructures as $B \rightarrow 0$

B. Das, D. C. Miller, and S. Datta

School of Electrical Engineering, Purdue University, West Lafayette, Indiana 47907

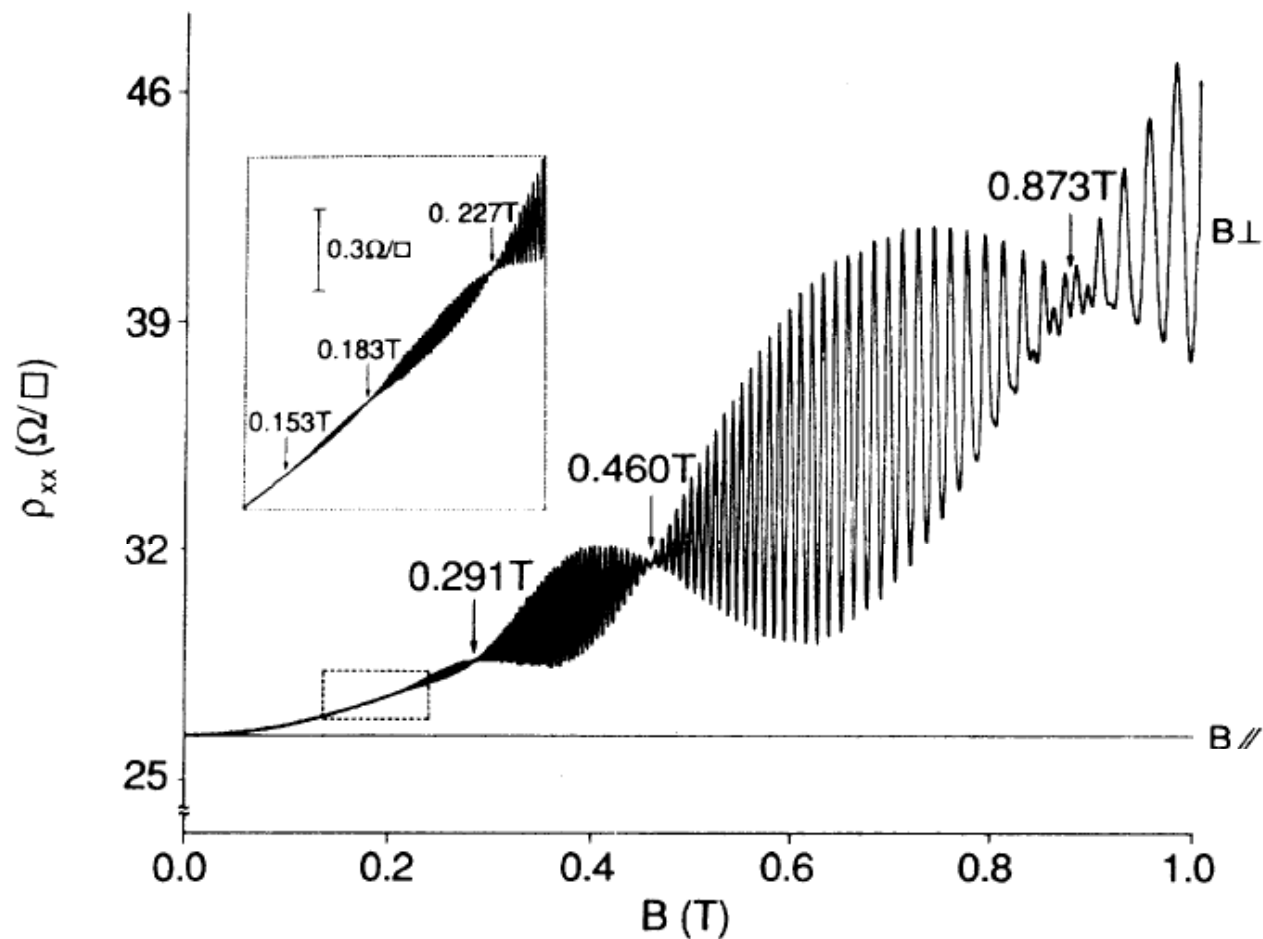
R. Reifenberger

Department of Physics, Purdue University, West Lafayette, Indiana 47907

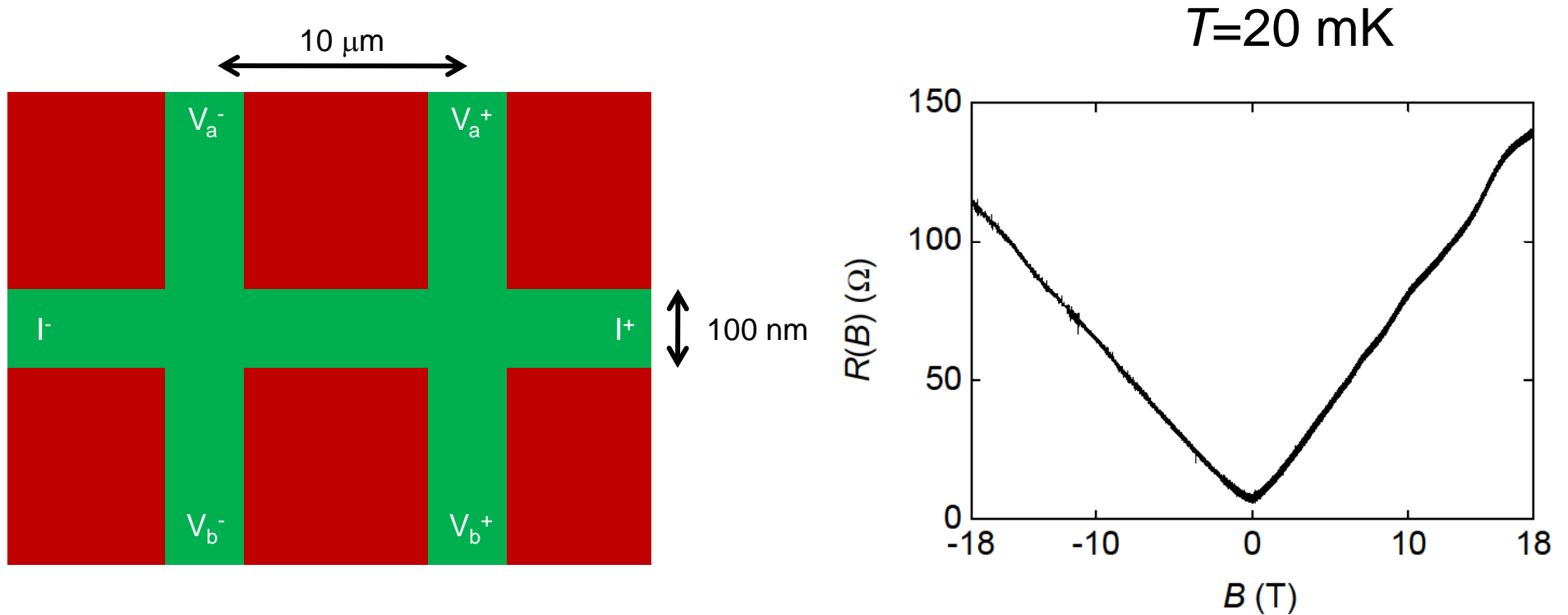
W. P. Hong, P. K. Bhattacharya, J. Singh, and M. Jaffe

*Department of Electrical Engineering and Computer Science, The University of Michigan,
Ann Arbor, Michigan 48109*

(Received 19 April 1988; revised manuscript received 30 September 1988)



Magnetoresistance



Large linear magnetoresistance for $|B| > 2\ \text{T}$
→ Asymmetry, possibly due to Hall coupling

Antisymmetric magnetoresistance of the SrTiO₃/LaAlO₃ interface

Snir Seri and Lior Klein

Department of Physics, Nano-magnetism Research Center, Institute of Nanotechnology and Advanced Materials, Bar-Ilan University, Ramat-Gan 52900, Israel

(Received 24 August 2009; revised manuscript received 24 September 2009; published 12 November 2009)

The longitudinal resistance R_{xx} of the SrTiO₃/LaAlO₃ interface with magnetic fields applied perpendicular to the interface has an antisymmetric term [namely, $R_{xx}(H) \neq R_{xx}(-H)$] which increases with decreasing temperature and increasing field. We argue that the origin of this phenomenon is a nonhomogeneous Hall effect with clear contribution of an extraordinary Hall effect, suggesting the presence of nonuniform field-induced magnetization.

Anisotropic magnetotransport at the SrTiO₃/LaAlO₃ interface

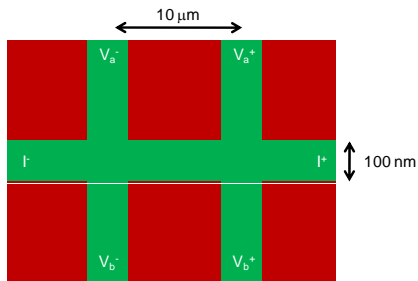
M. Ben Shalom,¹ C. W. Tai,^{2,*} Y. Lereah,² M. Sachs,¹ E. Levy,¹ D. Rakhmilevitch,¹ A. Palevski,¹ and Y. Dagan^{1,†}

¹*Raymond and Beverly Sackler School of Physics and Astronomy, Tel-Aviv University, Tel Aviv 69978, Israel*

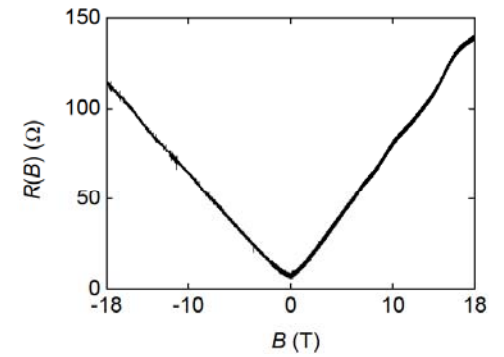
²*Department of Physical Electronics, School of Electrical Engineering, The Iby and Aladar Fleischman Faculty of Engineering, Tel-Aviv University, Tel Aviv 69978, Israel*

(Received 7 August 2009; published 8 October 2009)

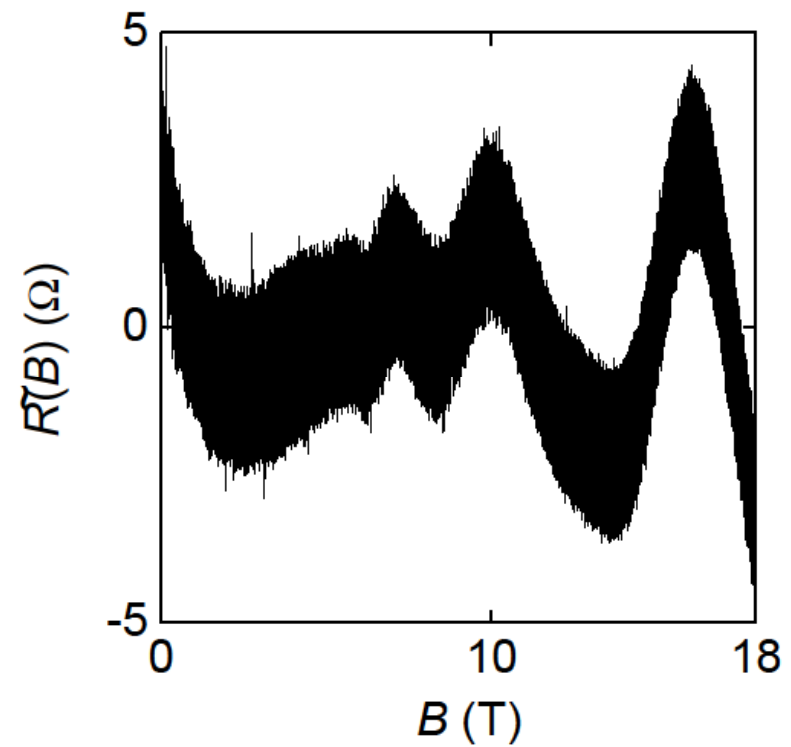
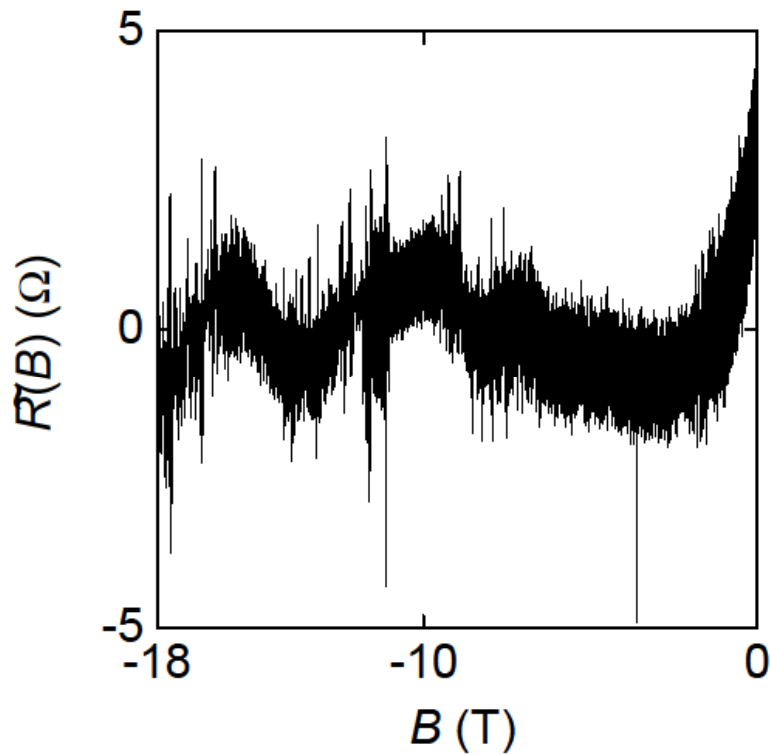
The sheet resistance as a function of temperature, magnetic field and its orientation for atomically flat SrTiO₃/LaAlO₃ interfaces with carrier densities of $\sim 3 \times 10^{13} \text{ cm}^{-2}$ is reported. At low magnetic fields superconductivity is observed below 130 mK. The temperature dependence of the high field magnetoresistance and its strong anisotropy suggest possible magnetic ordering below 35 K. The origin of this ordering and its possible relation to superconductivity are discussed.



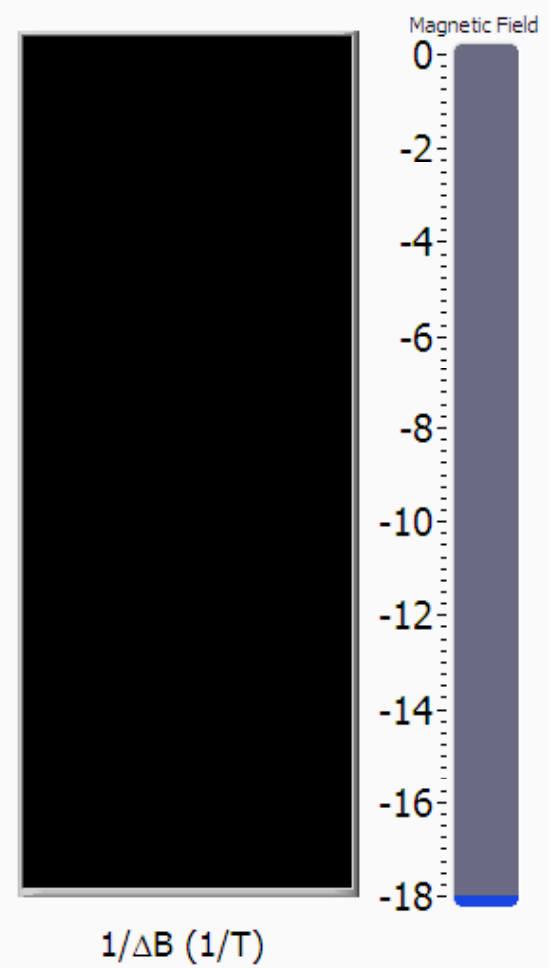
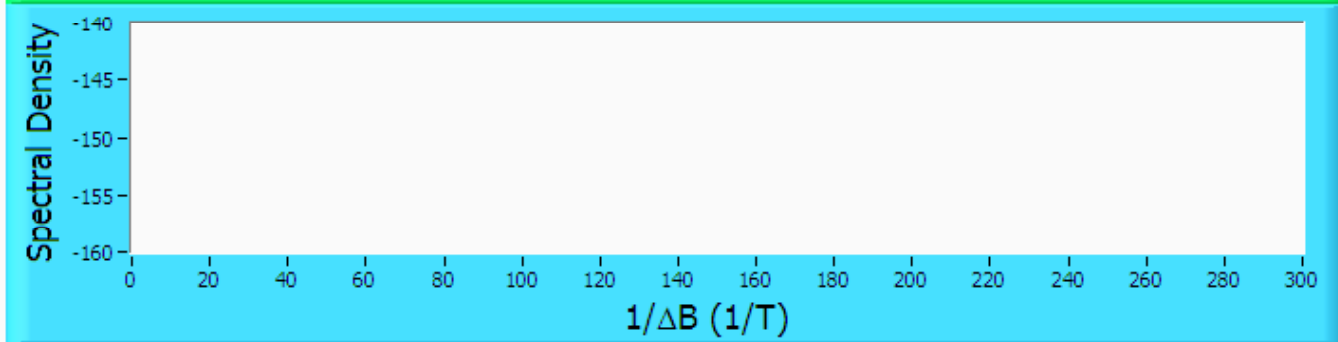
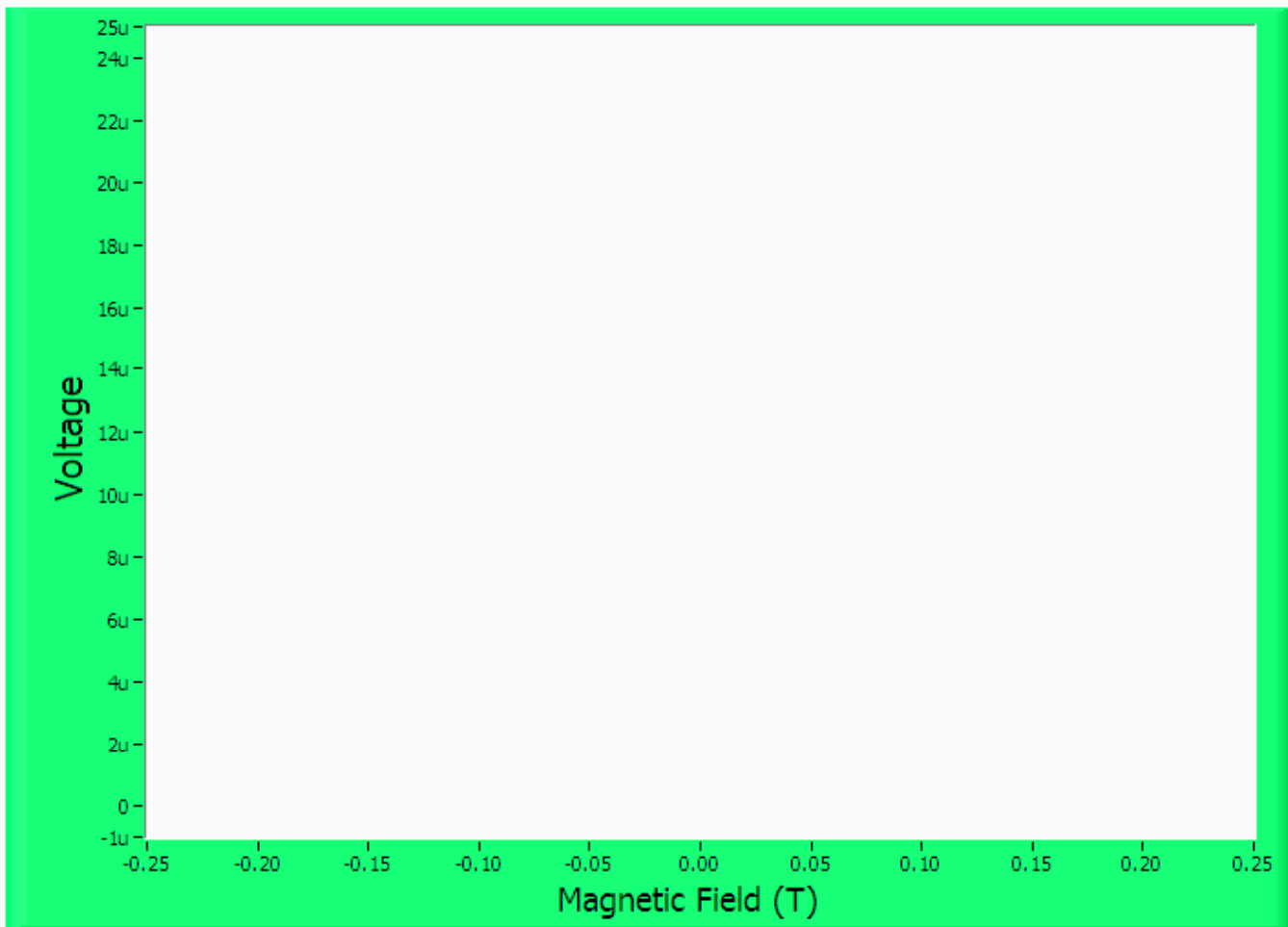
Magnetoresistance: close-up

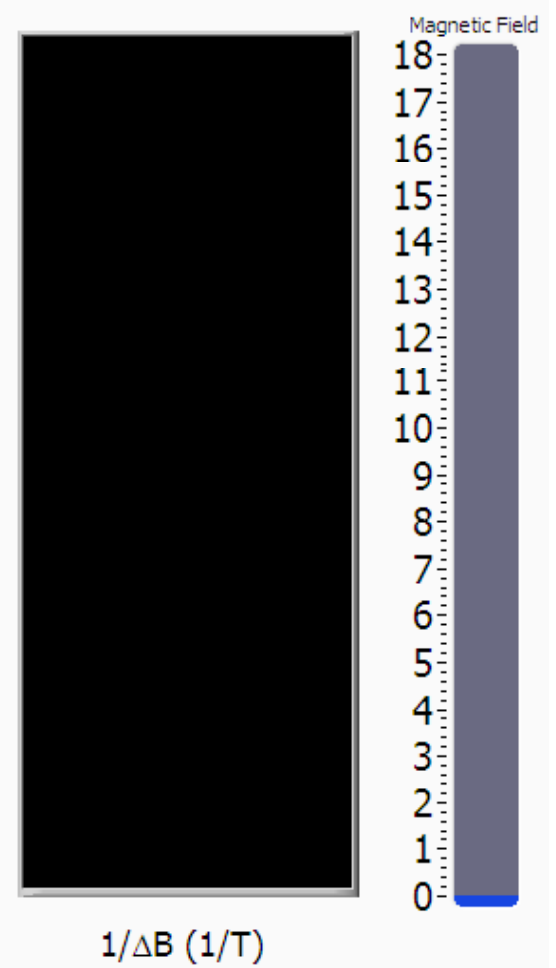
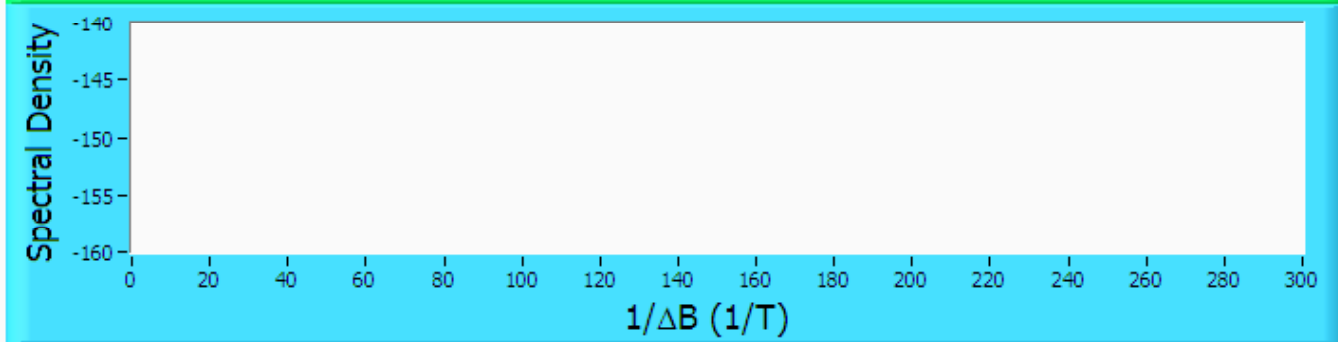
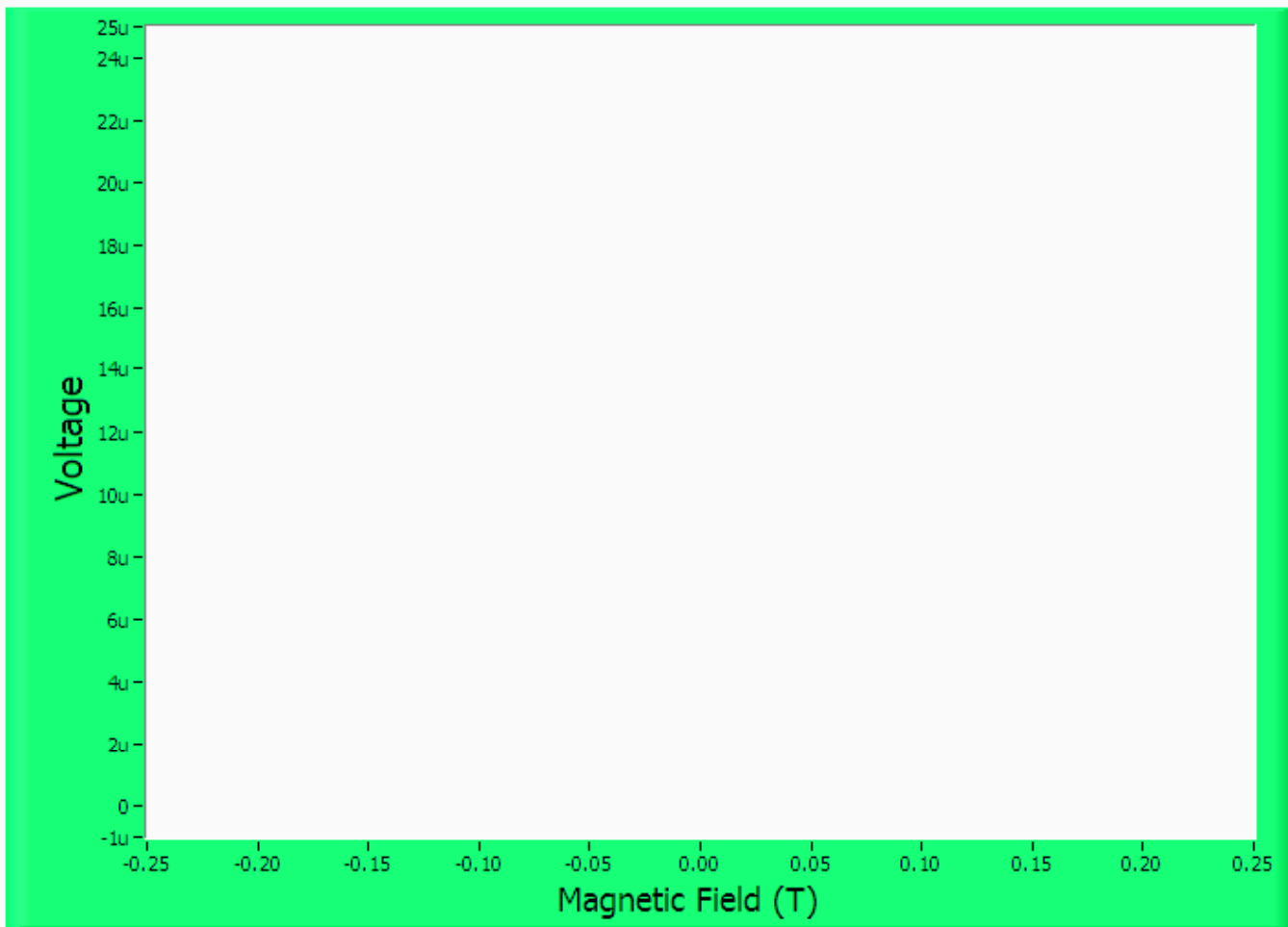


Subtract linear term

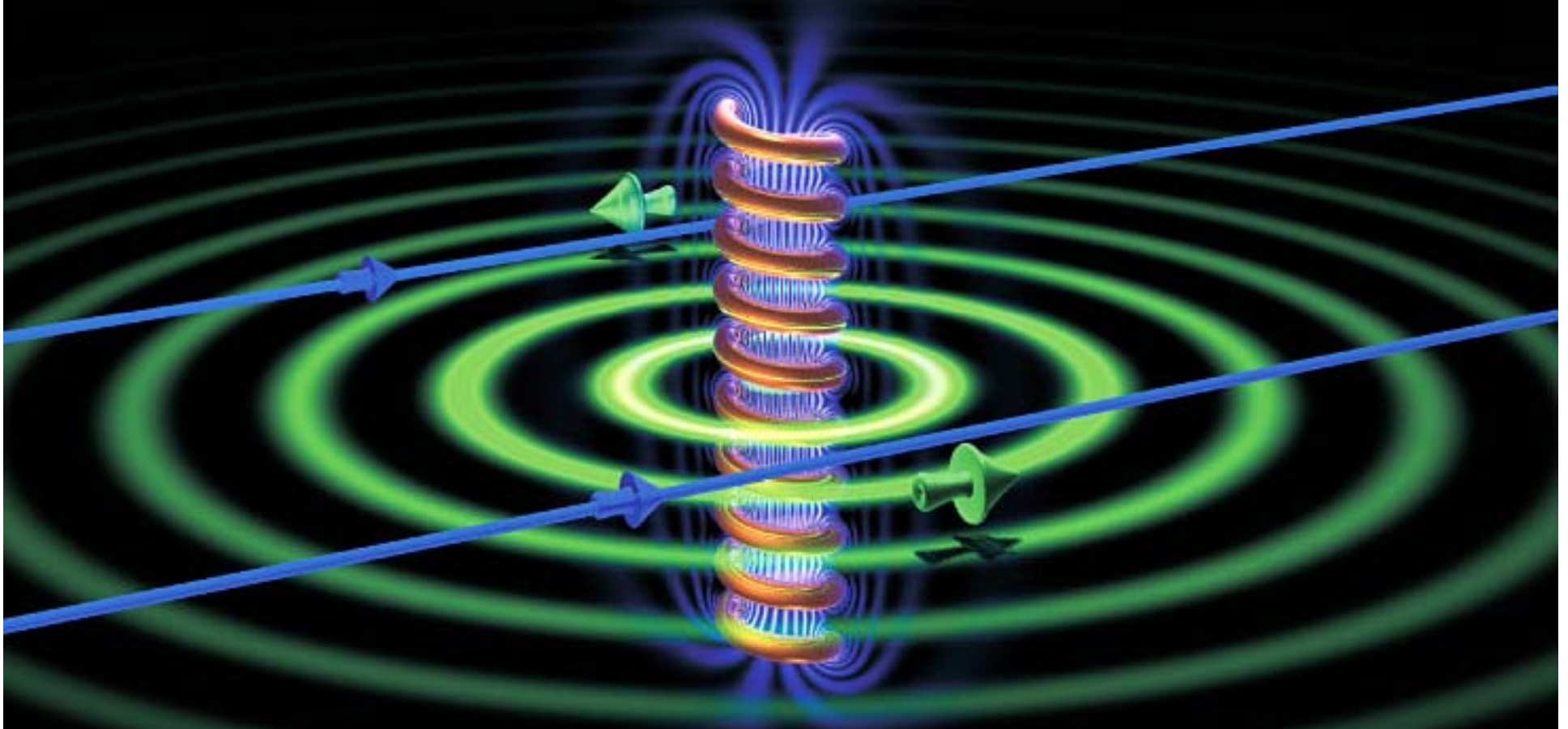


Shubnikov de Haas oscillations
→ Noisy!





Aharonov-Bohm Effect



$$\Delta\varphi = e/\hbar \int \vec{A} \cdot d\vec{l} = e/\hbar \int \vec{B} \cdot d\vec{a} = (e/\hbar)\Phi$$

Illustration: H. Batelaan and A. Tonomura, *Physics Today* 9, 38 (2009).

Observation of h/e Aharonov-Bohm Oscillations in Normal-Metal Rings

R. A. Webb, S. Washburn, C. P. Umbach, and R. B. Laibowitz
IBM Thomas J. Watson Research Center, Yorktown Heights, New York 10598
 (Received 27 March 1985)

Magnetoresistance oscillations periodic with respect to the flux h/e have been observed in submicron-diameter Au rings, along with weaker $h/2e$ oscillations. The h/e oscillations persist to very large magnetic fields. The background structure in the magnetoresistance was *not* symmetric about zero field. The temperature dependence of both the amplitude of the oscillations and the background are consistent with the recent theory by Stone.

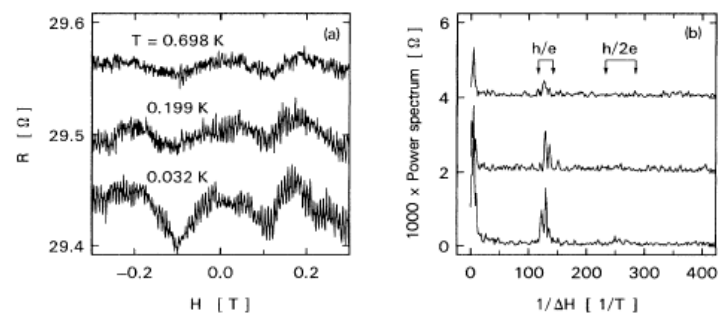
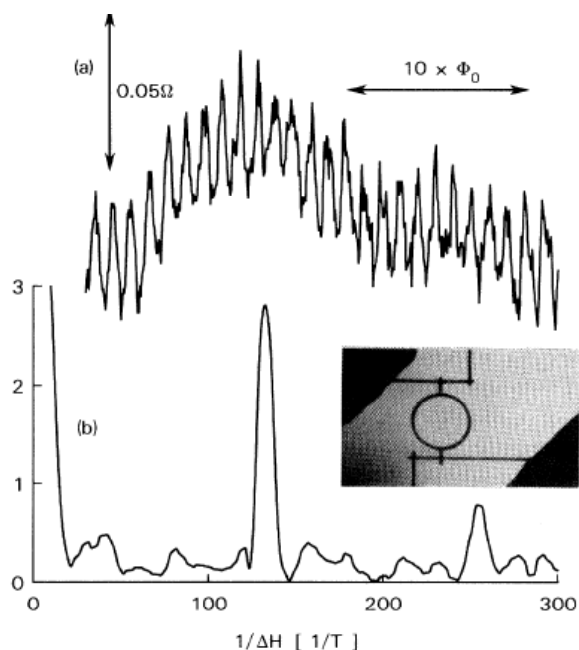
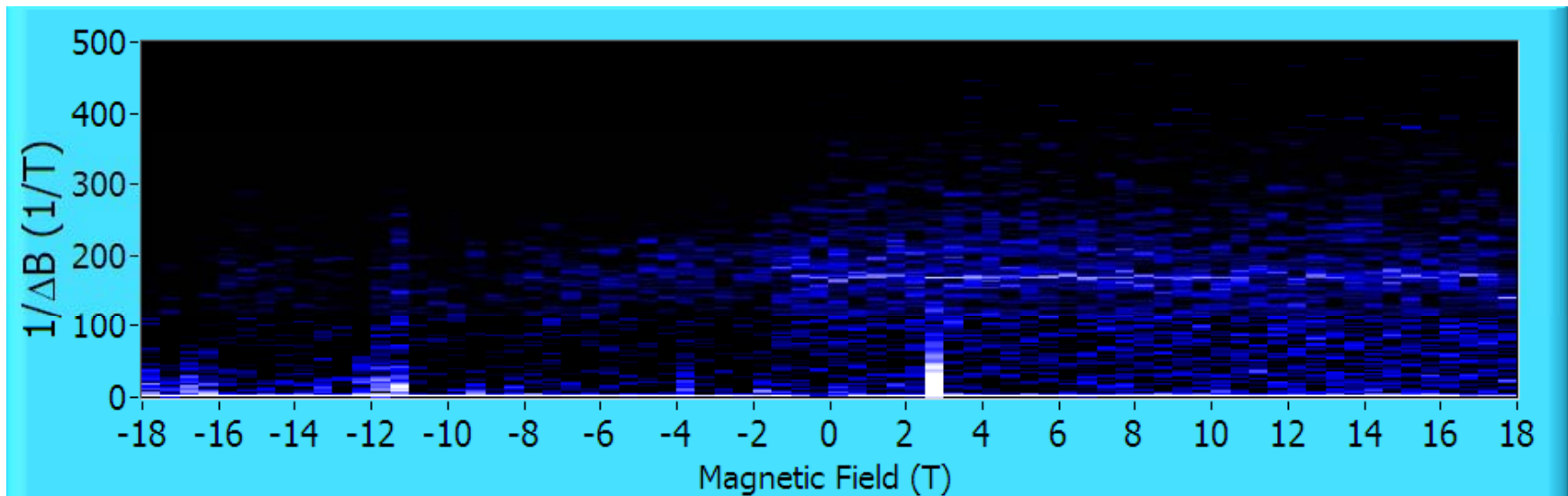
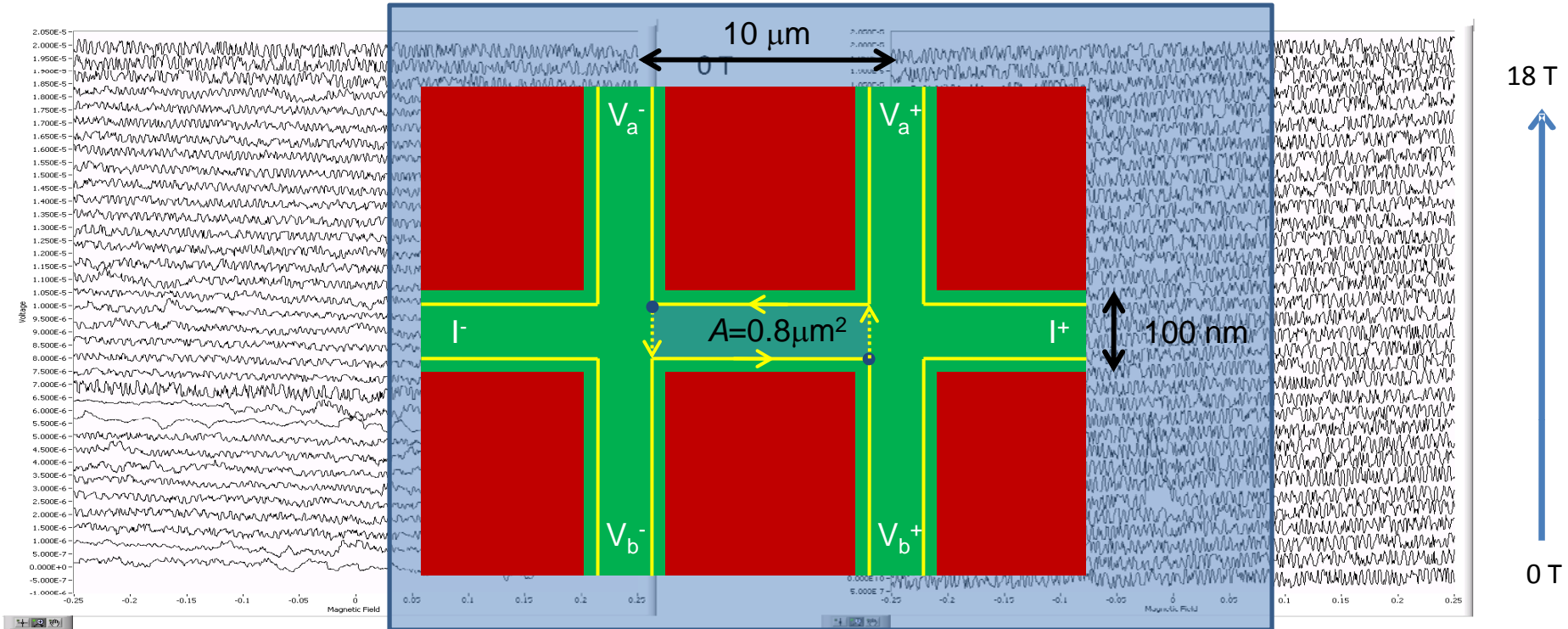


FIG. 2. (a) Magnetoresistance data from the ring in Fig. 1 at several temperatures. (b) The Fourier transform of the data in (a). The data at 0.199 and 0.698 K have been offset for clarity of display. The markers at the top of the figure indicate the bounds for the flux periods h/e and $h/2e$ based on the measured inside and outside diameters of the loop.

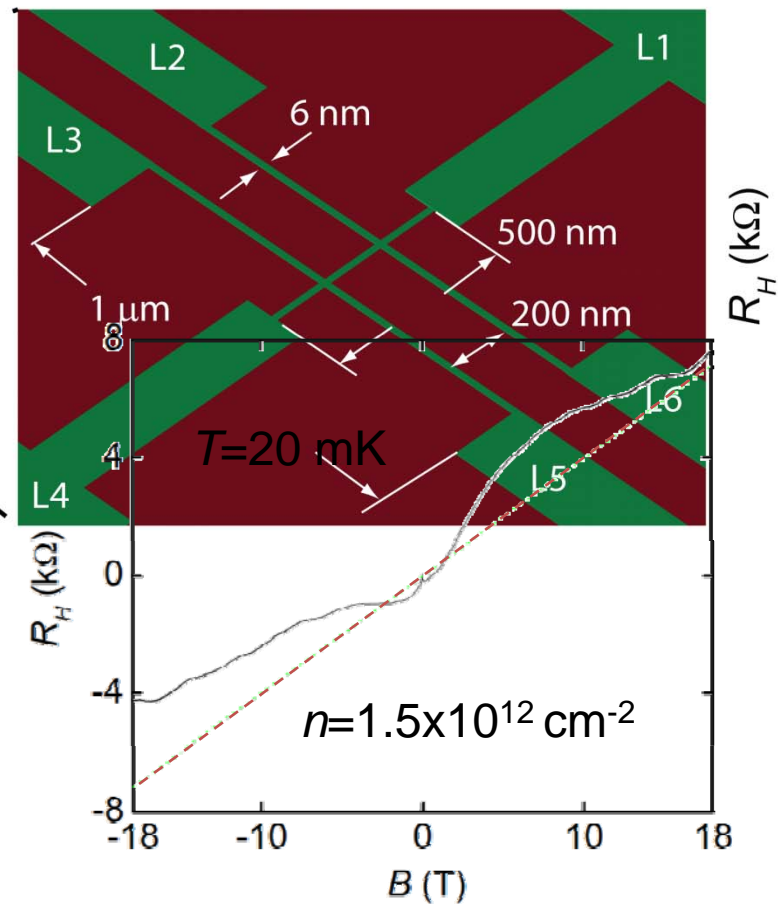
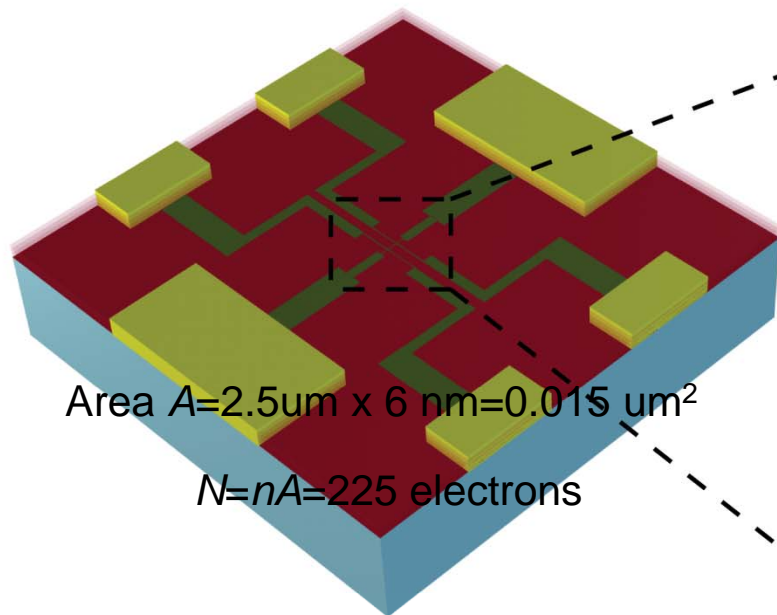
larger than the oscillations observed in normal-metal cylinders and networks of loops.^{8,10,11}

Figure 2(a) contains resistance data for three tem-

Aharonov-Bohm Oscillations

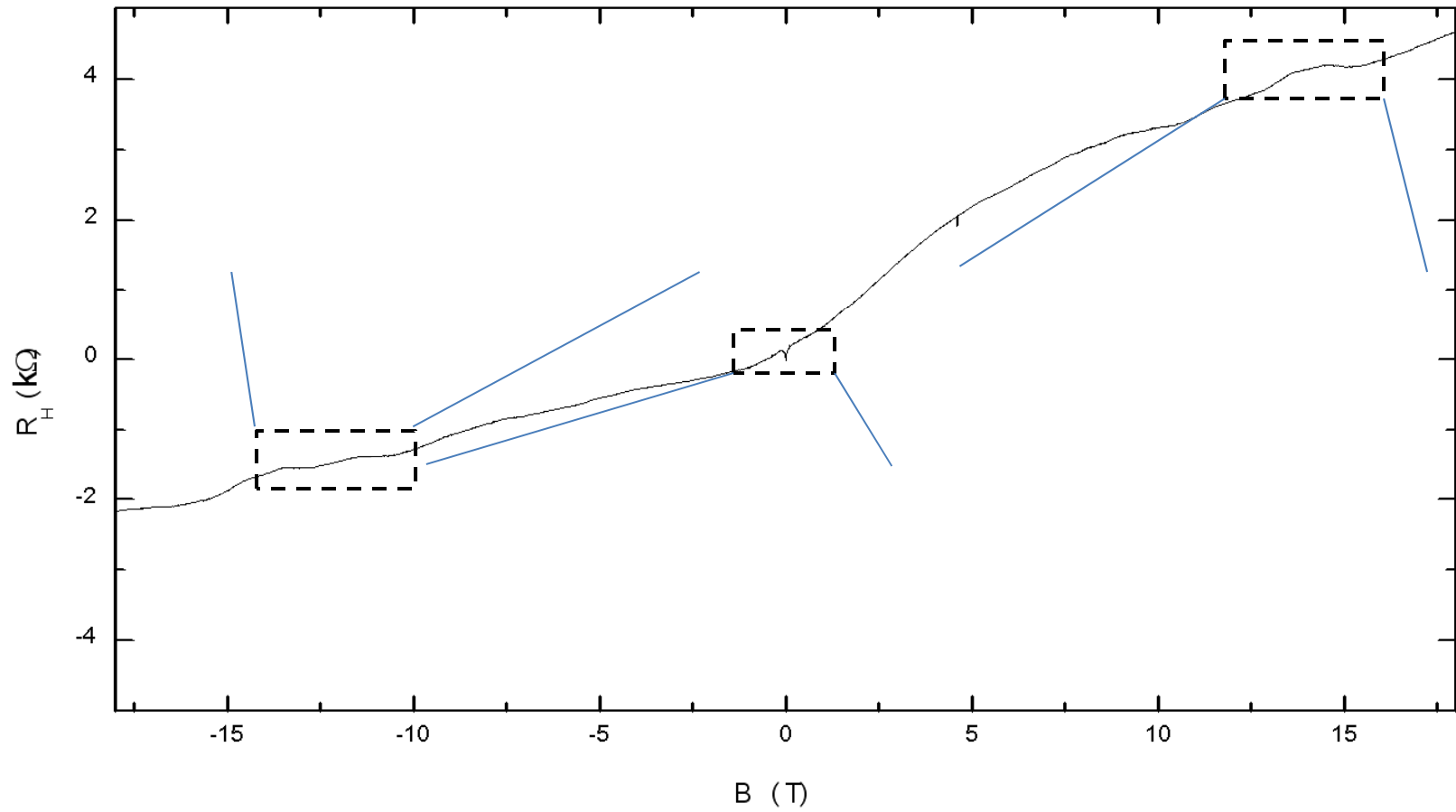


60 Å Hall cross

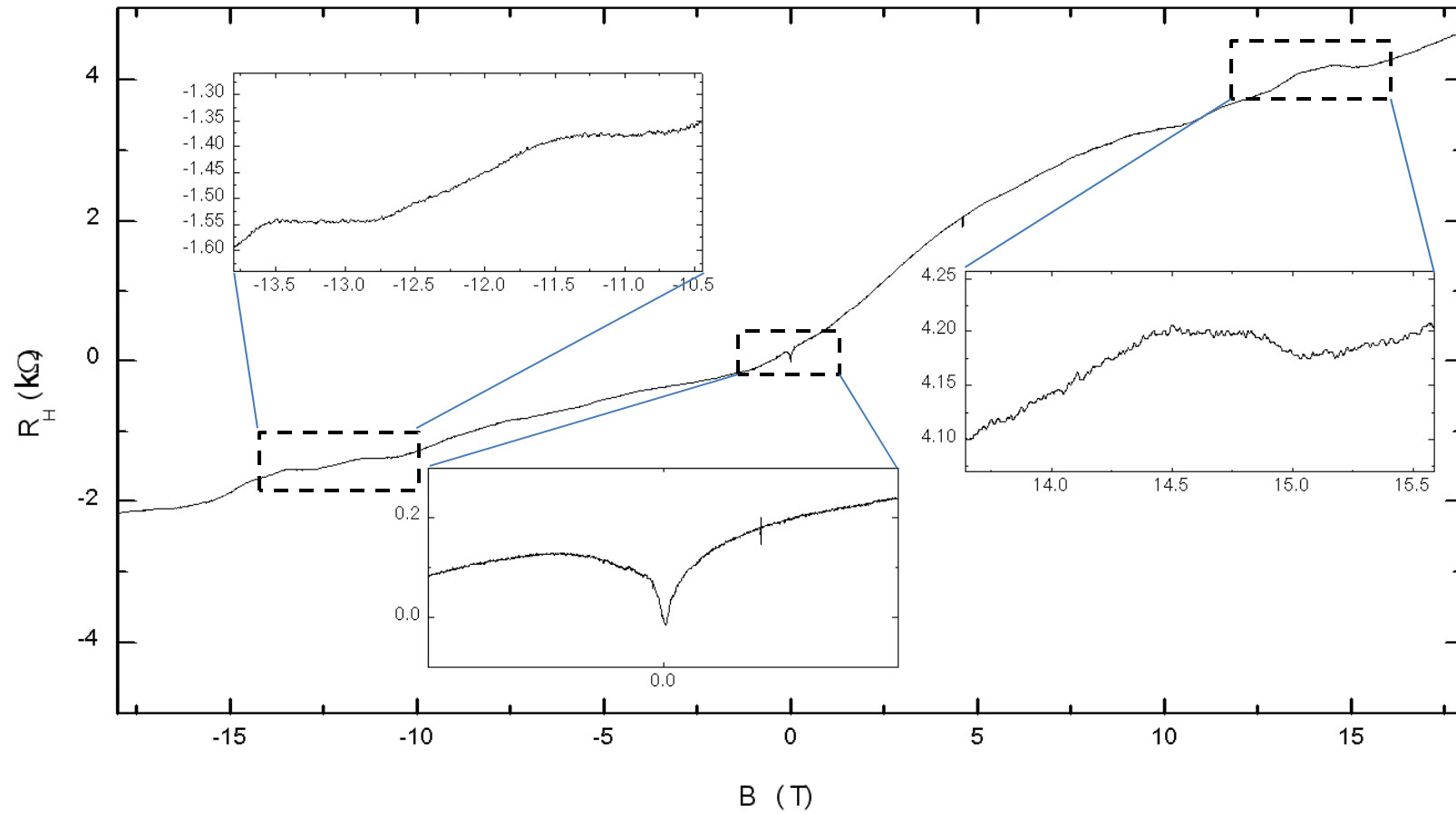


- Anomalous Hall response for $|B| < 2$ T
- Plateaus for $|B| > 10$ T

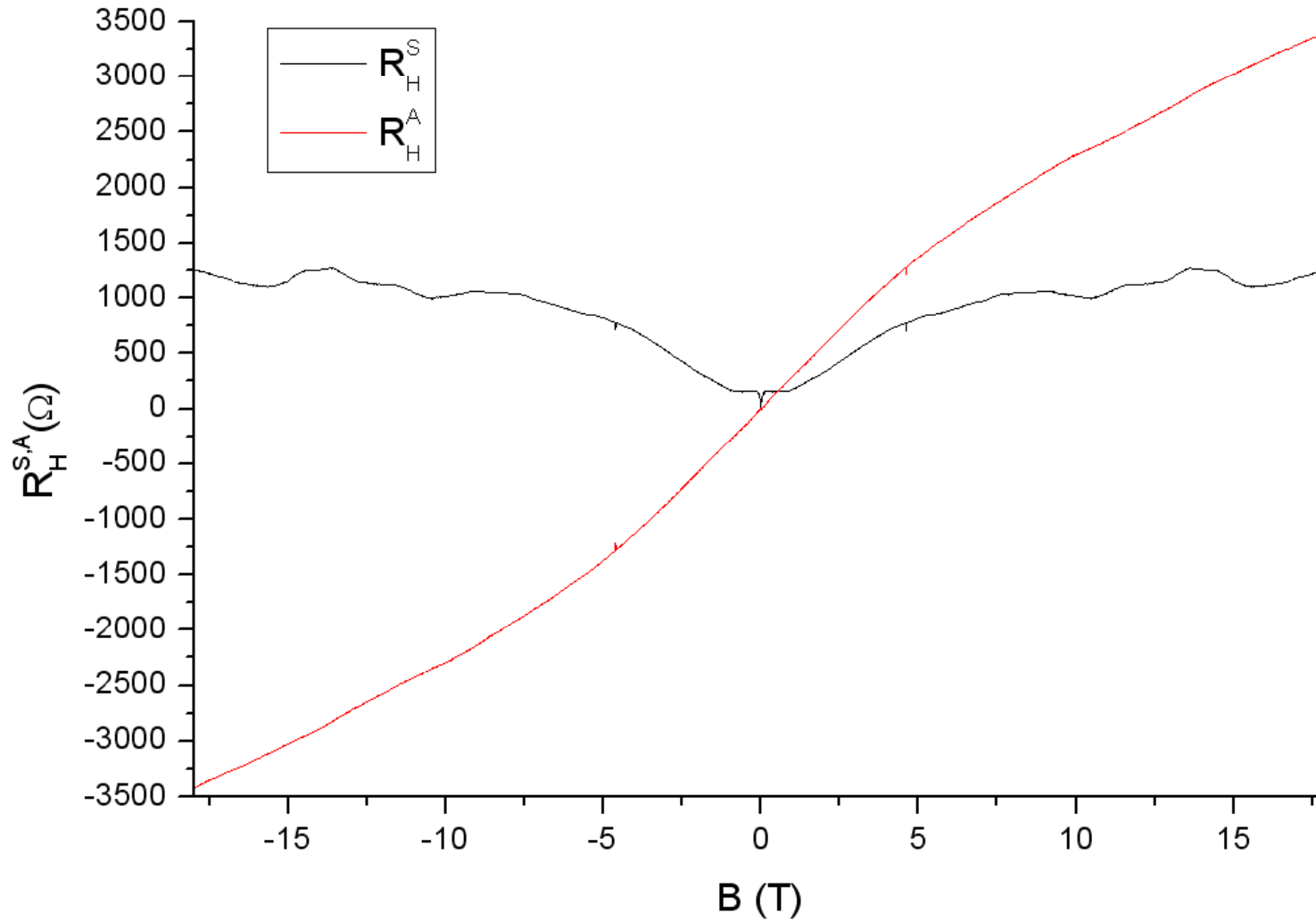
Hall Resistance



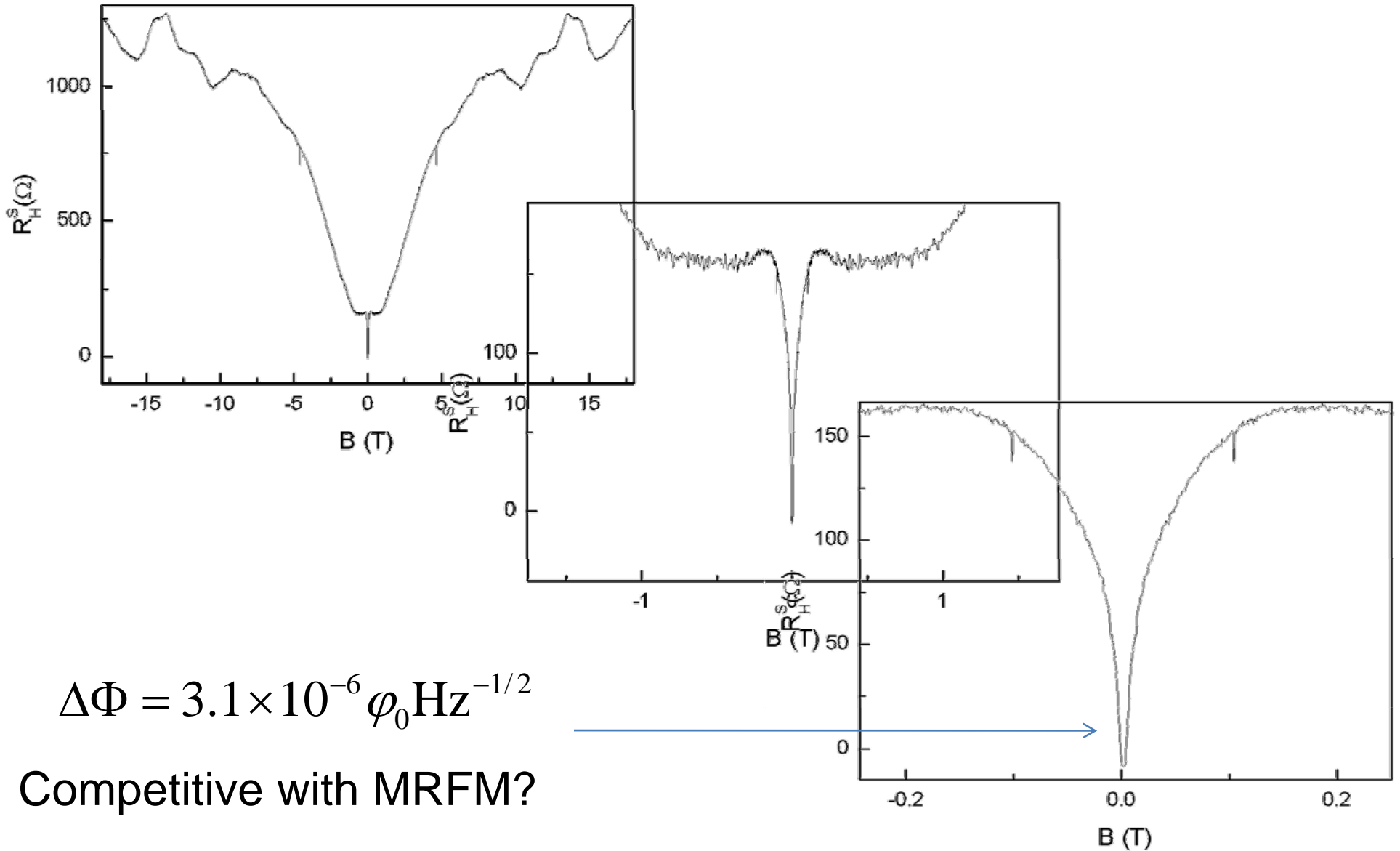
Hall Resistance



Symmetric and Antisymmetric Components



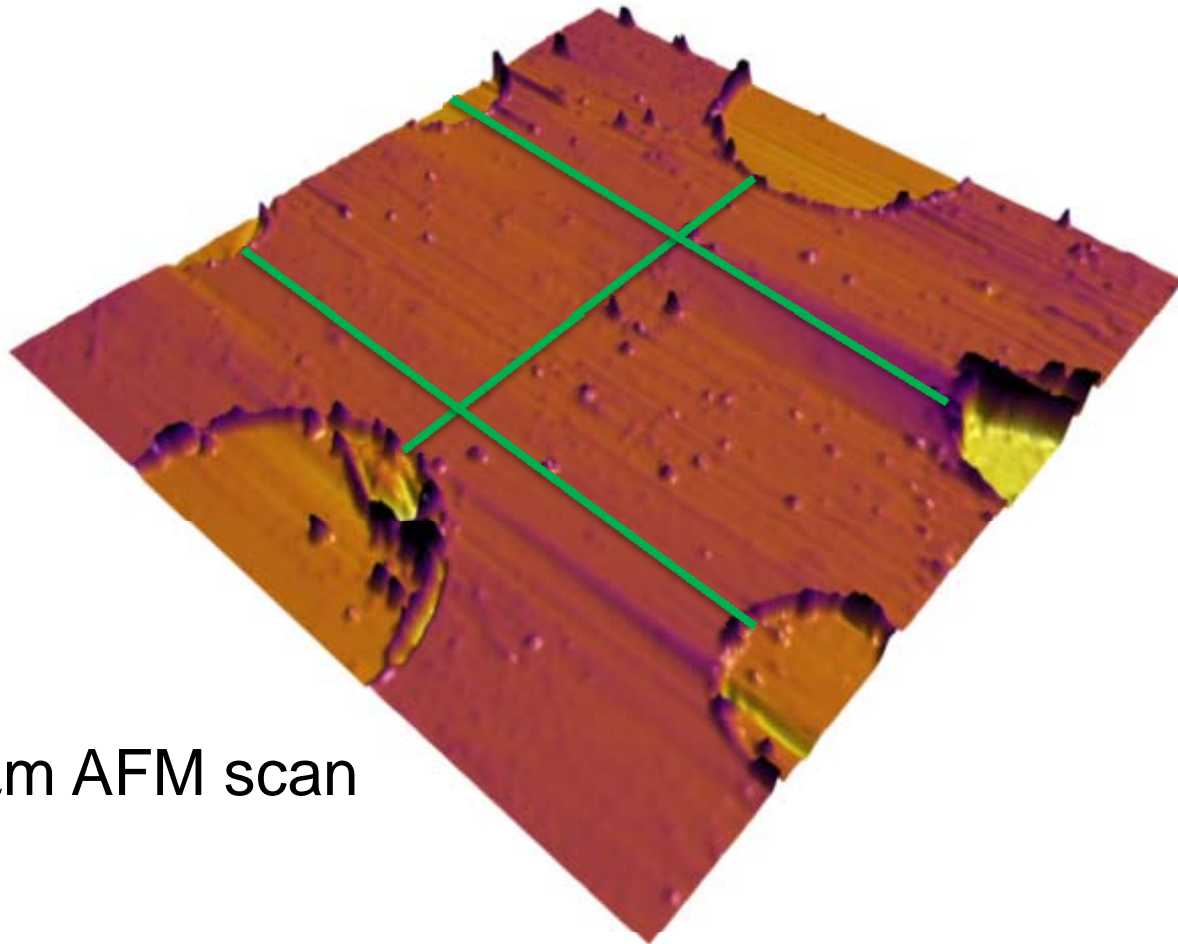
Ultrasensitive (spin?) Hall Nanosensor



$$\Delta\Phi = 3.1 \times 10^{-6} \varphi_0 \text{Hz}^{-1/2}$$

Competitive with MRFM?

Low-Density Nanostructure

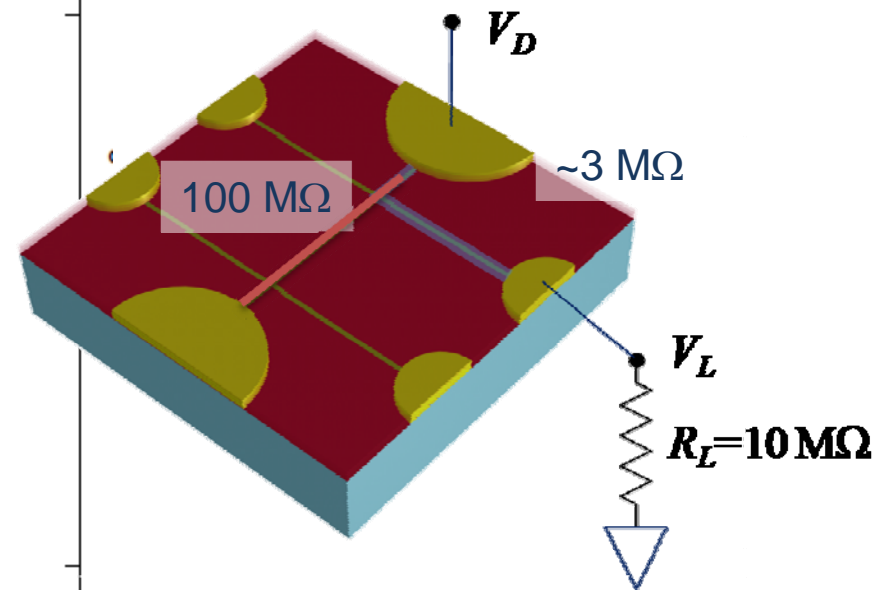
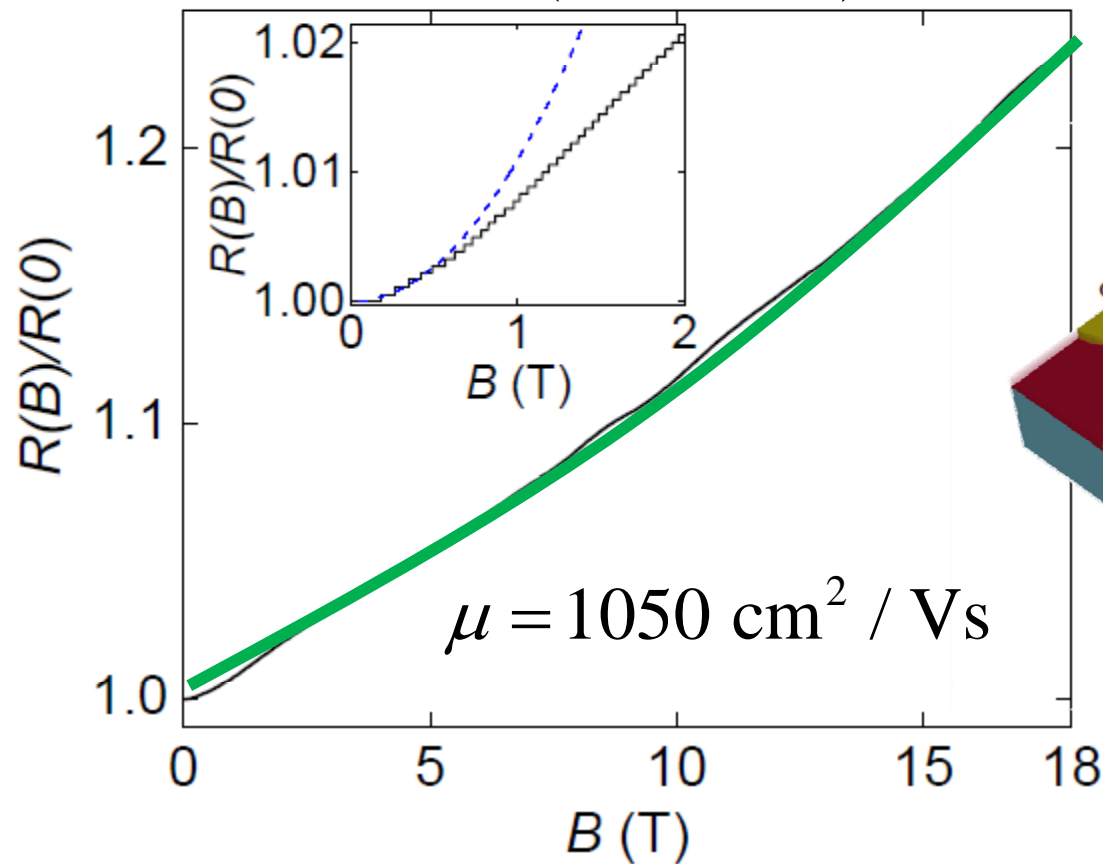


50 μ m x 50 μ m AFM scan

Magnetoresistance @ 250 mK

$$R(B) \approx R(0) \left(1 + (\mu_0 B)^2 \right)$$

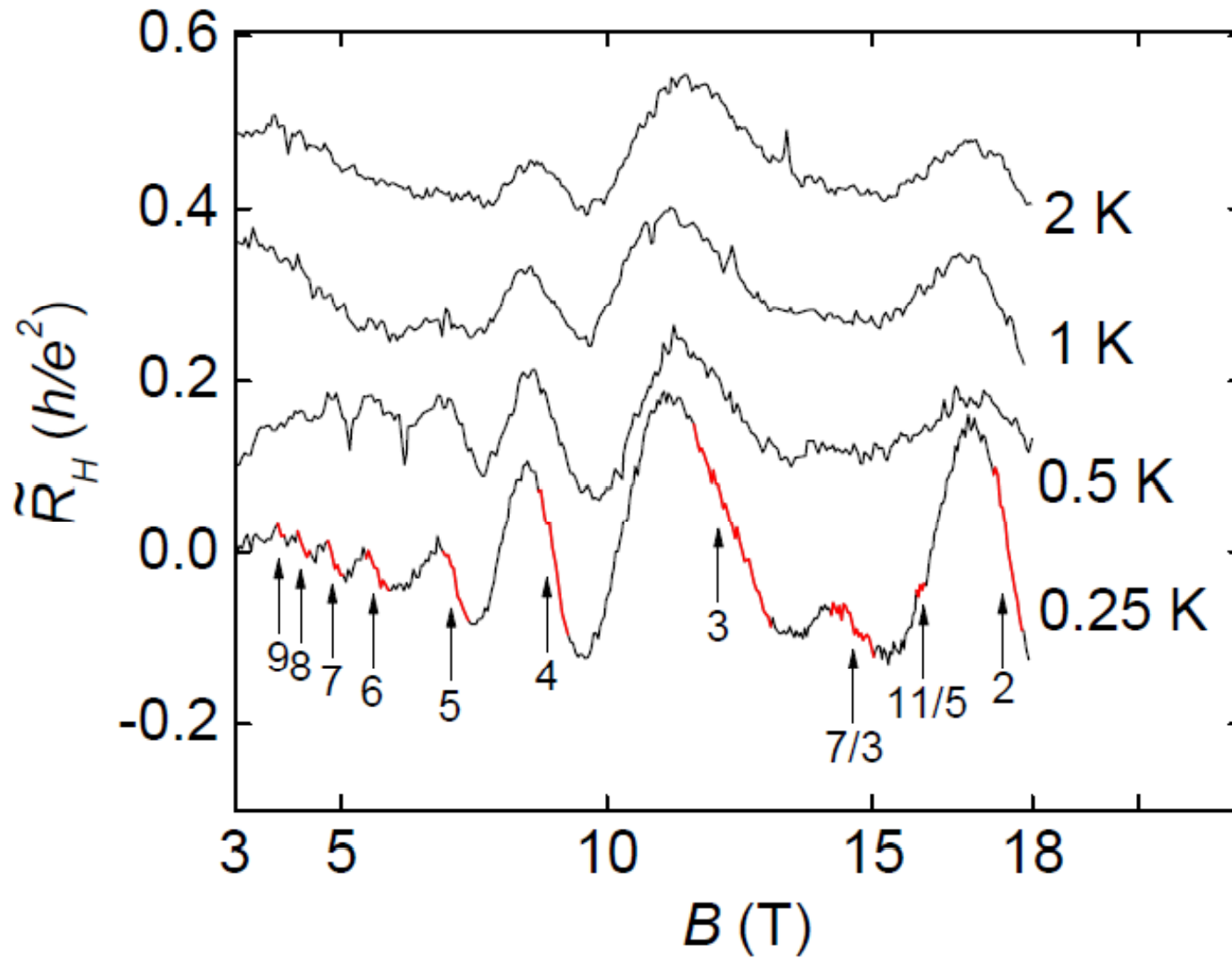
Hall leads -> insulating



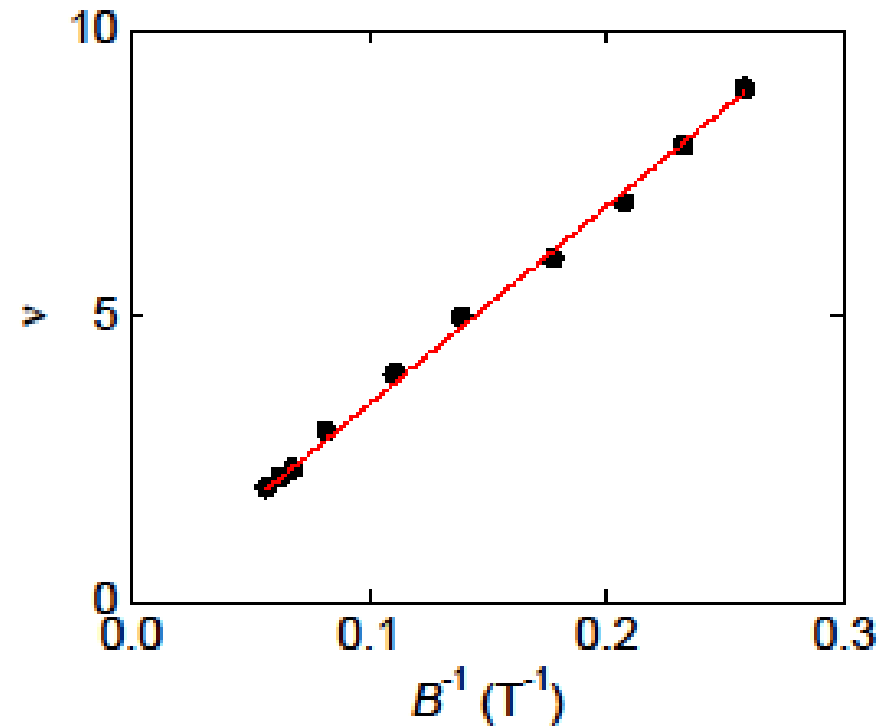
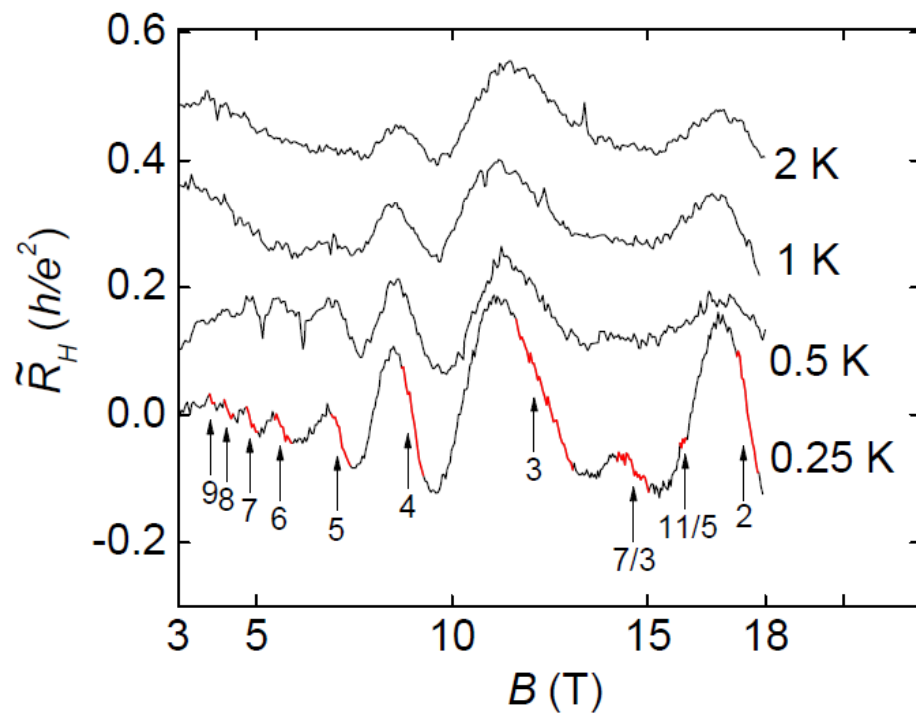
Subtract linear (+ weak parabolic) background...

$$R_C(B) = R(0) \left(1 + C_1 B + C_2 B^2 \right)$$

Magnetoresistance Plateaus

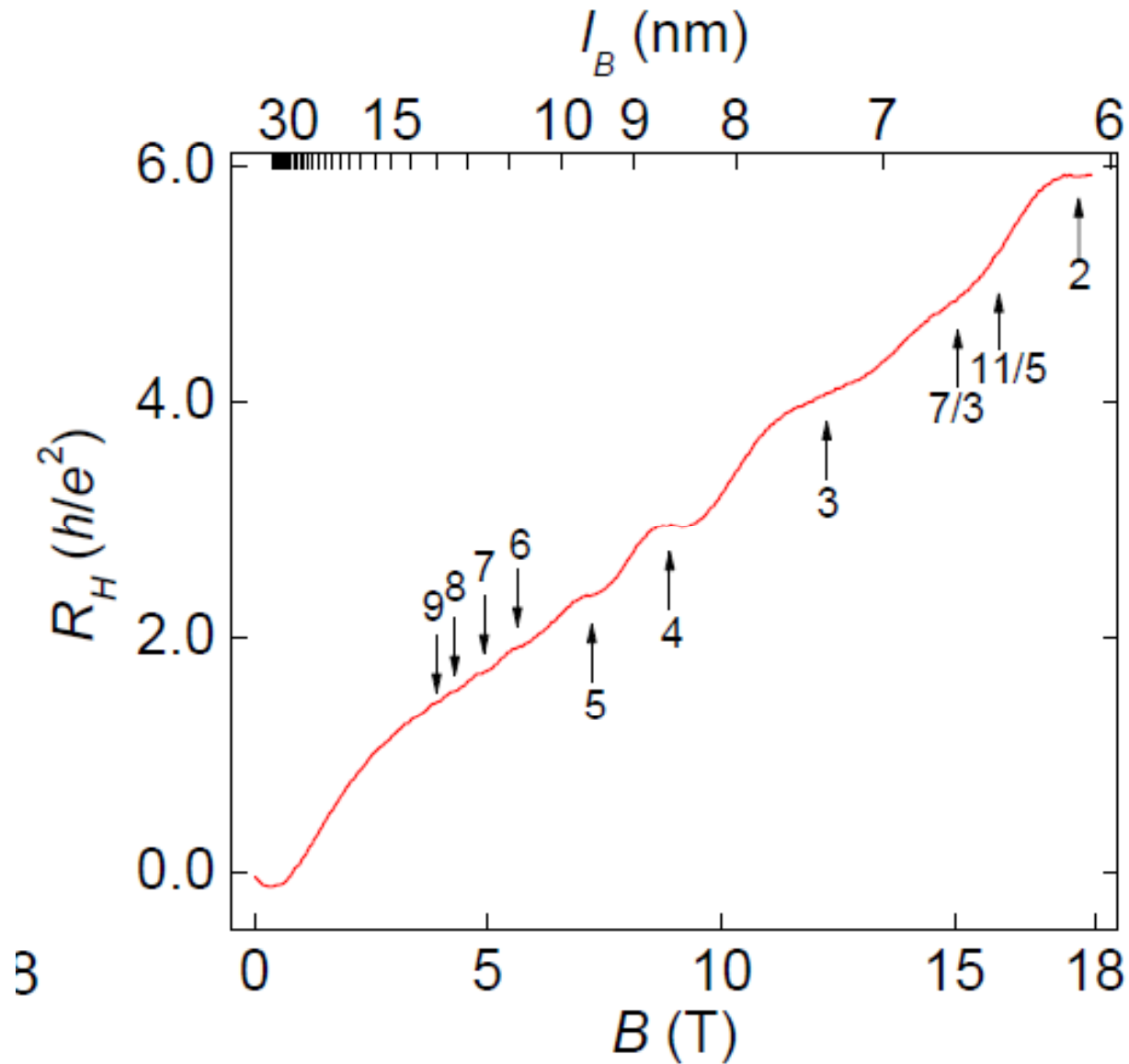


Landau Levels (integer and fractional)



$$n = 8 \times 10^{11} \text{ cm}^{-2}$$

Magnetoresistance Plateaus



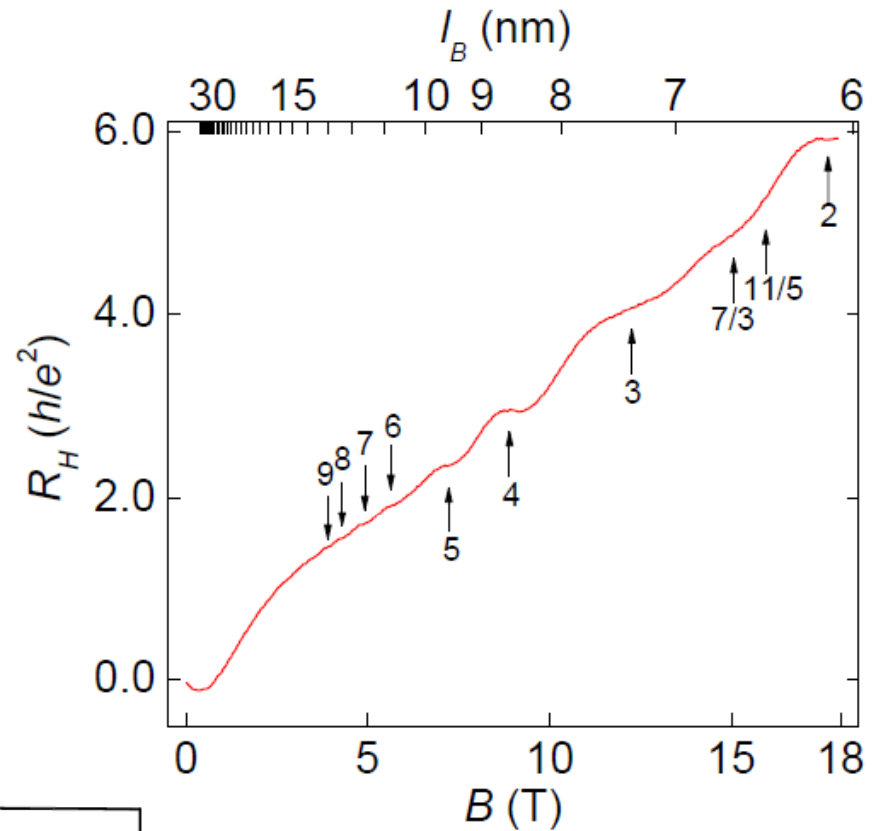
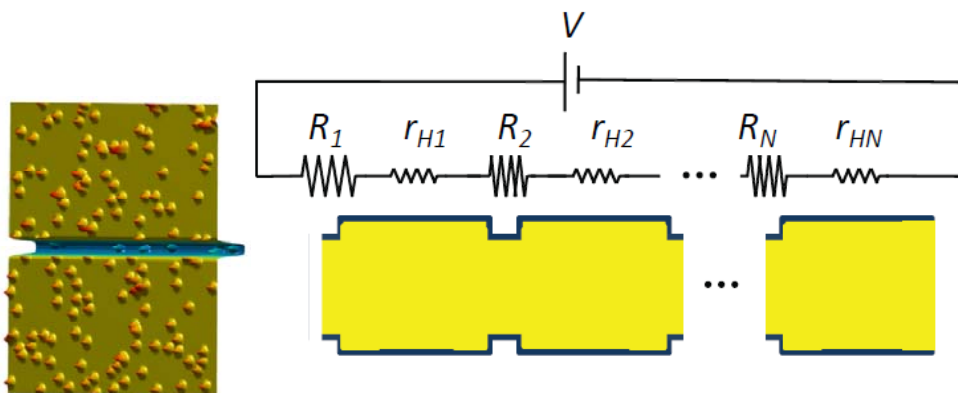
Edge State Picture

Density is below metal-insulator transition

Two-terminal Landauer-Buttiker formalism: absence of back-scattering from edge states in QH regime

$$R = R_H + R_C$$

$$R_H = \sum_{k=1}^N r_{Hk} = \frac{Nh}{ve^2}$$

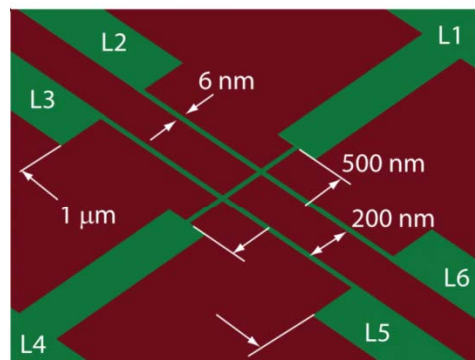
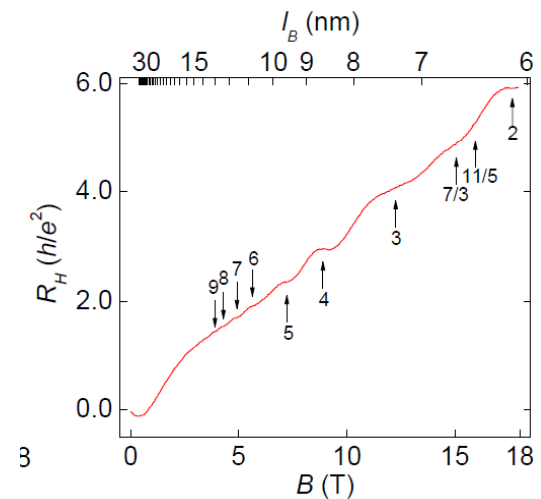
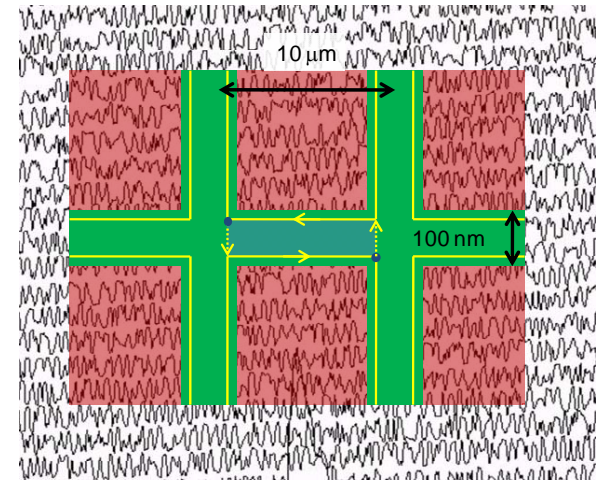


$$N = 12 \pm 2$$

FUTURE DIRECTIONS

Summary and Future Directions

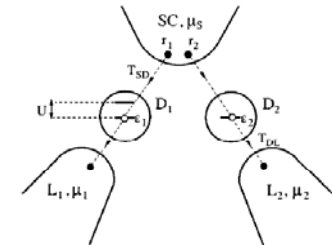
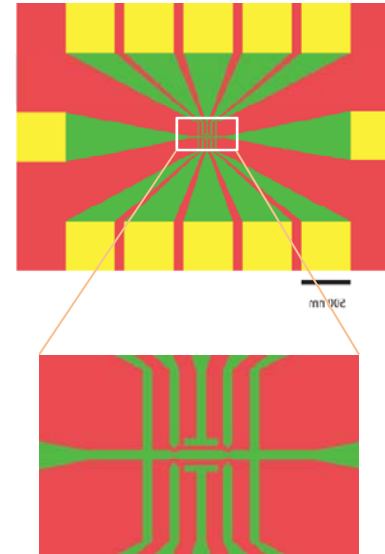
- Oxides replay “Physics Hits of the ’80s”
 - Aharonov-Bohm oscillations
 - Integer and fractional quantum Hall
 - Reduced dimensionality/edge states (1d) plays critical role



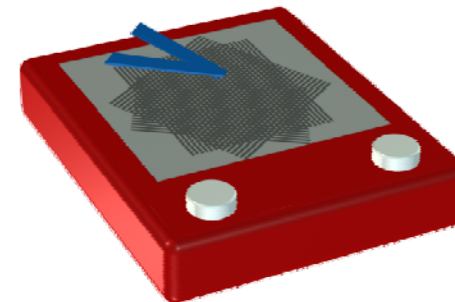
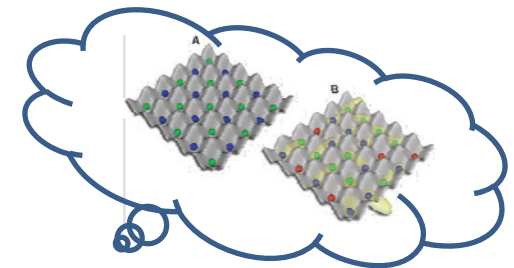
Summary and Future Directions

- Oxides replay “Physics Hits of the ’80s”
 - Aharonov-Bohm oscillations
 - Integer and fractional quantum Hall
 - Reduced dimensionality/edge states (1d) plays critical role
- Future directions
 - Superconducting nanostructures
 - Topological quantum computation
 - Hubbard simulators
 - ...

Topological quantum bit



Andreev Entangler
(Recher and Loss, 2001)



Oxide Nanoelectronic
Hubbard Simulator