

# Near the Superconducting Edge: Spin Confinement and Central Modes

**Bill Buyers**  
**National Research Council,**  
**Chalk River, Canada**

*Program on Quantum Phase Transitions*

*Kavli Institute for Theoretical Physics,*

*Santa Barbara January 25, 2005*

## **Collaborators:**

*National Research Council  
Chalk River Laboratories:*

- Zin Tun
- Zahra Yamani

*University of British  
Columbia:*

- Ruixing Liang
- Darren Peets
- Doug Bonn
- Walter N. Hardy

*University of Toronto:*

- Chris Stock
- Bob J. Birgeneau
- Paul S. Clegg

*ISIS:*

- Chris D. Frost

*Oxford:*

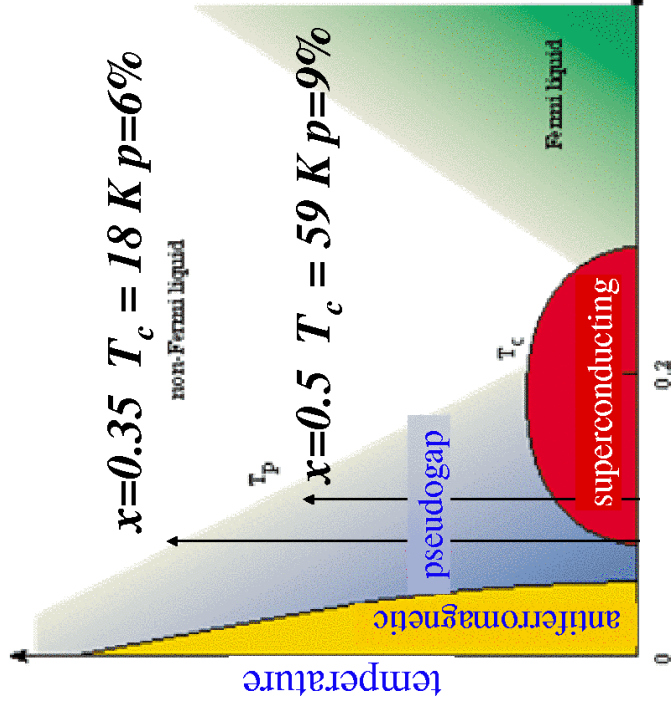
- Roger Cowley
- Radu Coldea
- *Johns Hopkins*
- Collin Broholm

YBCO<sub>6+x</sub>

No gap in normal spin response  
 Incommensurate spin modulations at low energy and resonance grow in for  $T < 2T_c$

Chris Stock et al  
 PRB **69**, 014502 '04  
 PRB **71**, Jan 1 '05

**Cuprate Phase Diagram:**

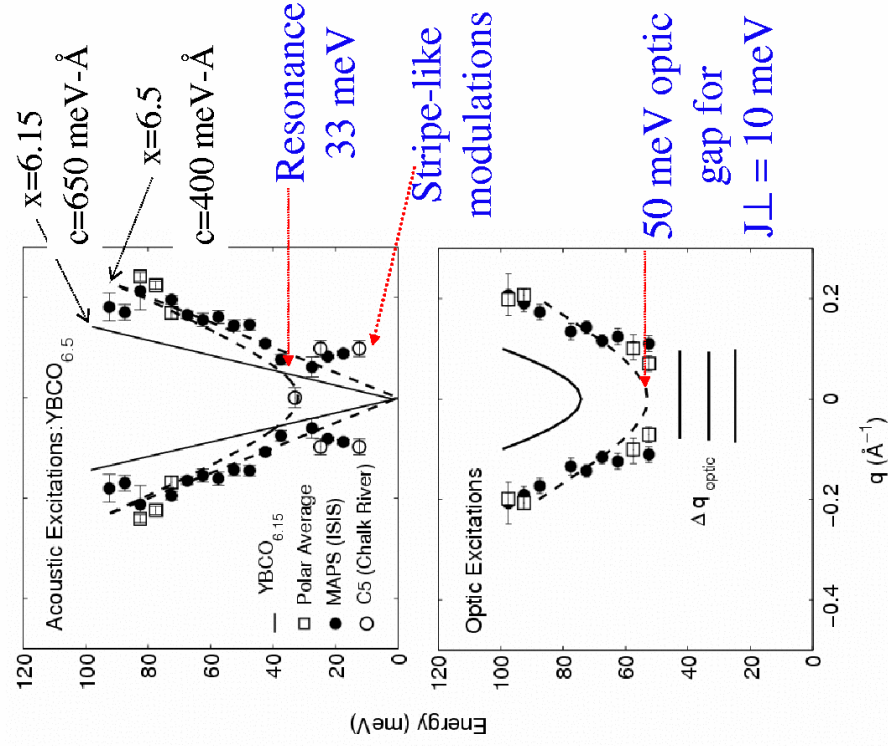


Doping p (holes per planar CuO<sub>2</sub>)

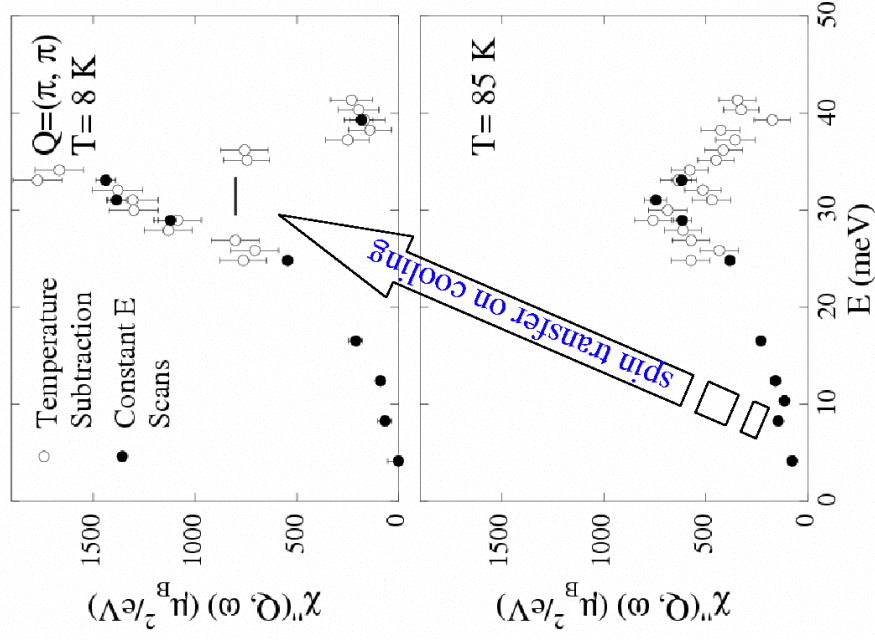
**DISPERSION  $x=6.5$**

Wave vector increases with energy  
 $\omega=cq$  centred on  $Q_{AF}$   
 No 'silent' q-band like  $x=6.85$  – Pailhes  
 weak Landau damping

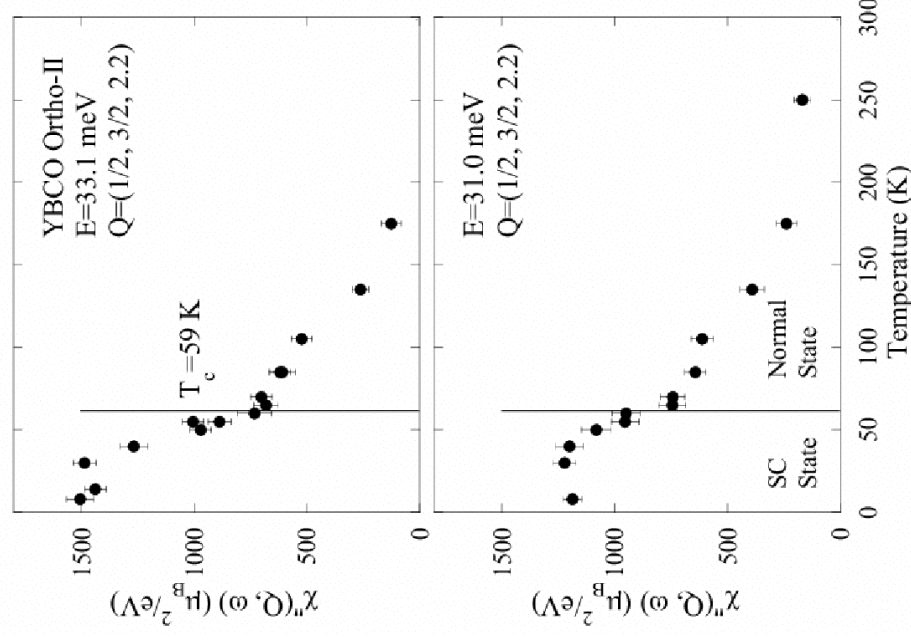
The velocity of  $c=400 \text{ meV-Å}$  is reduced to 60% of the insulator.  
 $J_{||} = 70 \text{ meV}$   
 $J_{\perp} = 10 \text{ meV}$



- Resonance YBCO<sub>6.5</sub>
- T<sub>c</sub>=59K
- Has spin triplet symmetry (polarized neutrons)
- a particle-particle process seen via SC pairing?
- a particle-hole exciton below energies with Landau damping?
- spin response pushed up by SC gap energy?
- incoherence ?



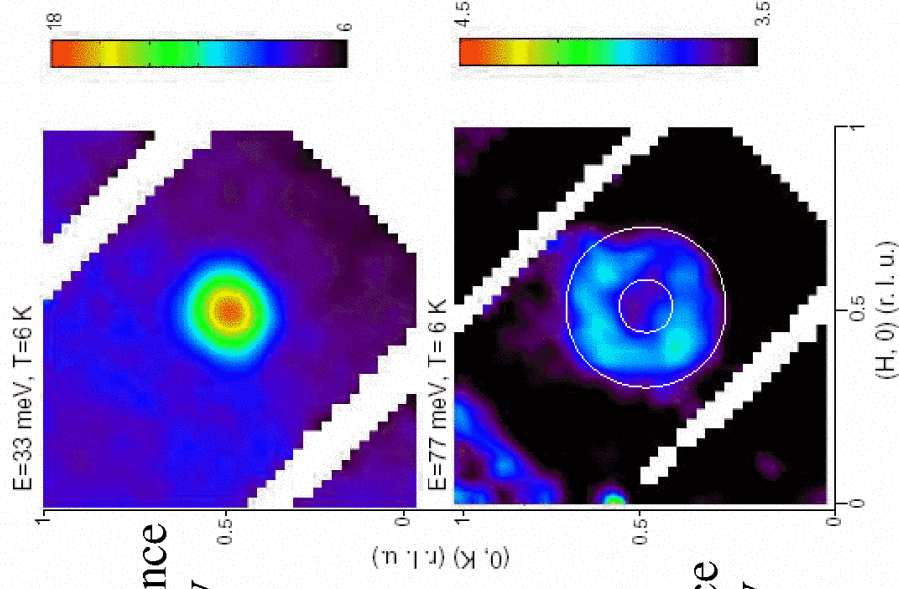
- Resonance: peak susceptibility
- The resonance is ~40% preformed in the normal phase
- Local pairs occur dynamically.
- Pairs achieve coherence in the superconducting phase.



High energies :

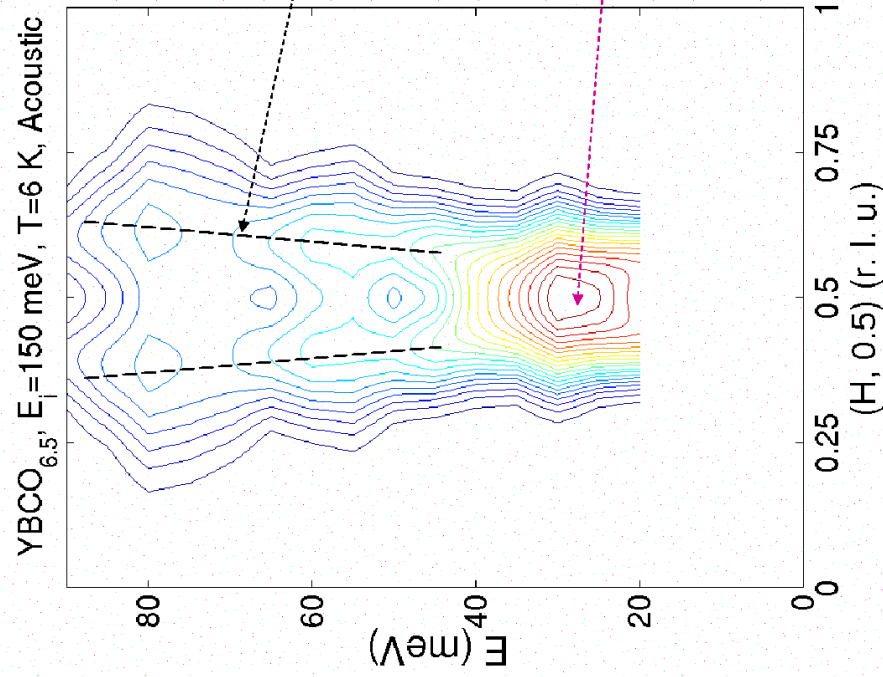
MAPS of  
smoke rings:  
intersection  
with cone of  
spin excitations

isotropic  
for  
 $33 < E < 110$  meV



On resonance  
33 meV

Above  
resonance  
77 meV

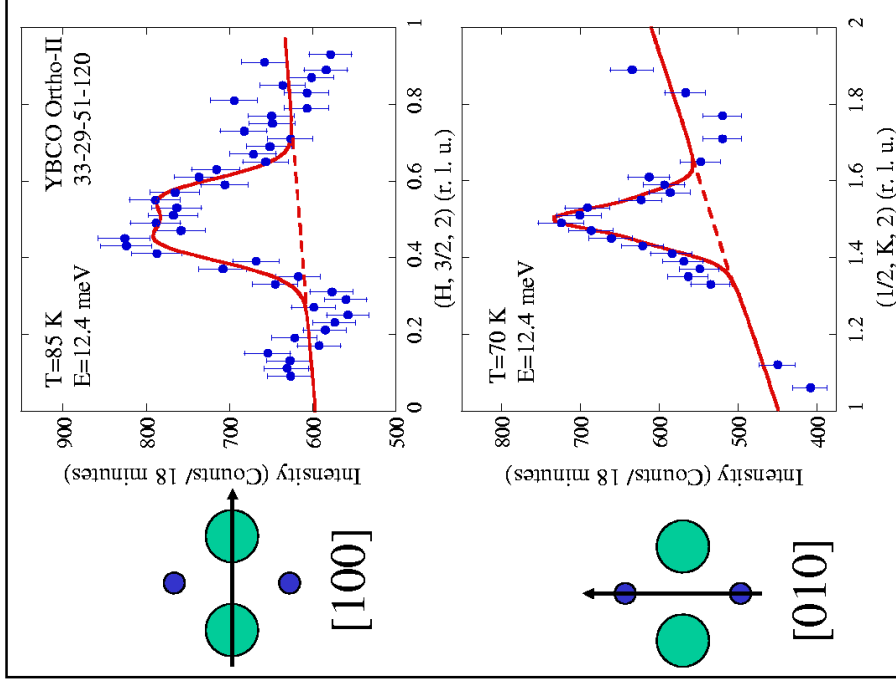
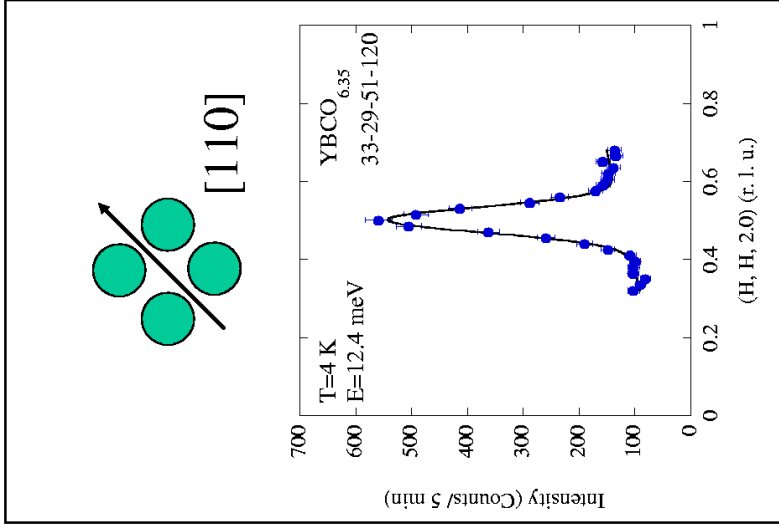


High-energy  
spin map in  
 $\text{YBCO}_{6.5}$

Ridge of  
paramagnon  
velocity  
– from  $(\pi, \pi)$

Resonance:  
Q-width same as  
for stripes below  
resonance

**Incommensurate Structure:**



**Incommensurate fluctuations: STM charge modulation is twice the spin**

matches nesting wave vector

For  $\text{YBCO}_{6.5}$  ( $T_c=59$  K), we plot from BSCCO Hoffmann, Science (2002)

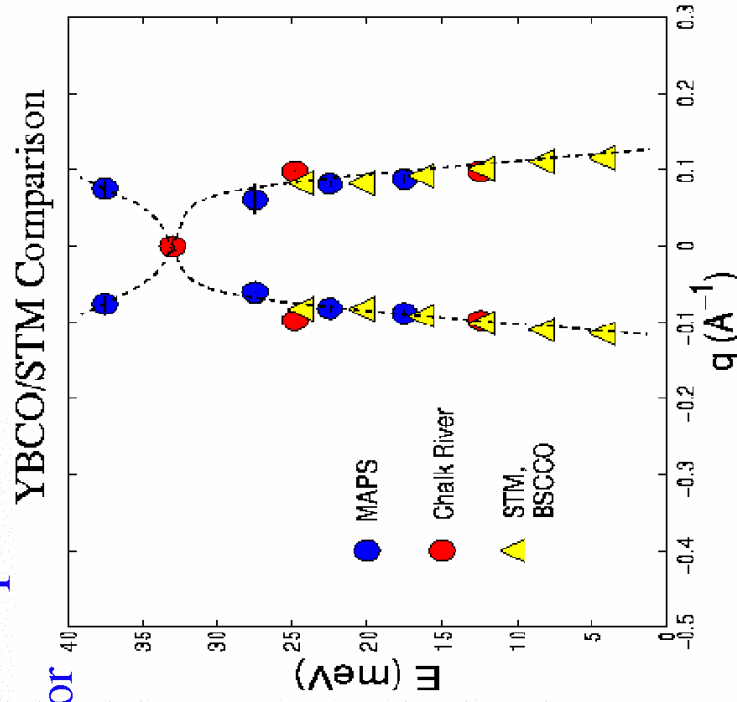
$$Q_{\text{spin}} = Q_{59/2} = 0.08 \text{ rlu}$$

At 12 meV we observe

$$Q_{\text{spin}} = 0.06 \text{ rlu} = 0.10 \text{ \AA}^{-1}$$

Q of BSCCO scaled by doping E scaled by resonance energy

See Christensen *et al* 0403439 for optimally doped LSCO



Neutron data from Stock *et al* 0408071

Spin squared couples to charge density  
via Landau or via antiphase domains

Ensures that  $Q_{\text{spin}} = \frac{1}{2} Q_{\text{charge}}$

$$(\pi + \delta_{\text{spin}}, \frac{1}{2})^2 \implies 2 \delta_{\text{spin}} = \delta_{\text{charge}}$$

If  $Q_{\text{charge}}$  follows spin then it is not a caliper of a  
Fermi surface dimension?

t-J model – linear in spin – quadratic in charge:

$$H = t \sum_{i,j}(t) (b_i^\dagger + b_j^\dagger) h_i^\dagger h_j + \frac{1}{4} J \sum_{i,j}(t) (b_i^\dagger b_i + b_j^\dagger b_j + b_i^\dagger b_j + b_i^\dagger b_j^\dagger)$$

Spin-charge coupling fails along (110)

q-STM expands with

energy

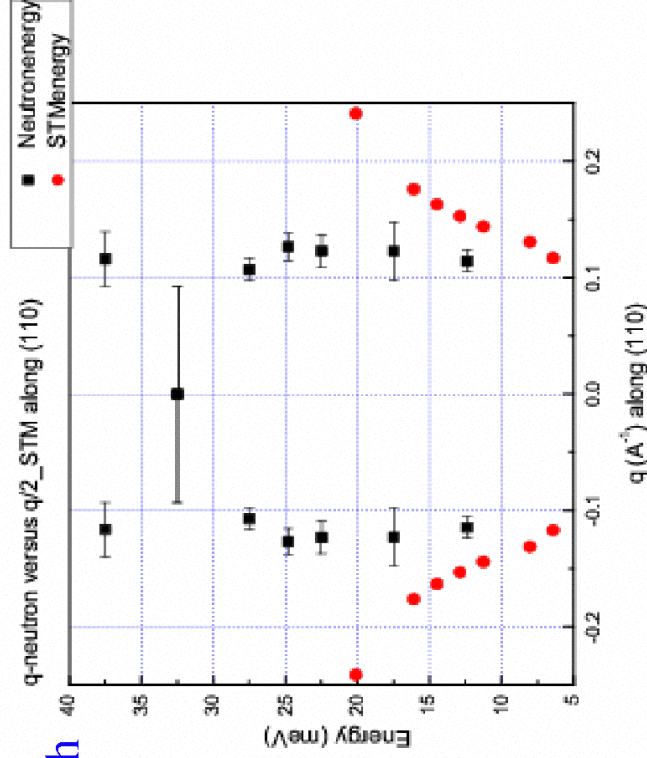
q-neutron remains

constant

Hence relation to

STM is not

generally valid

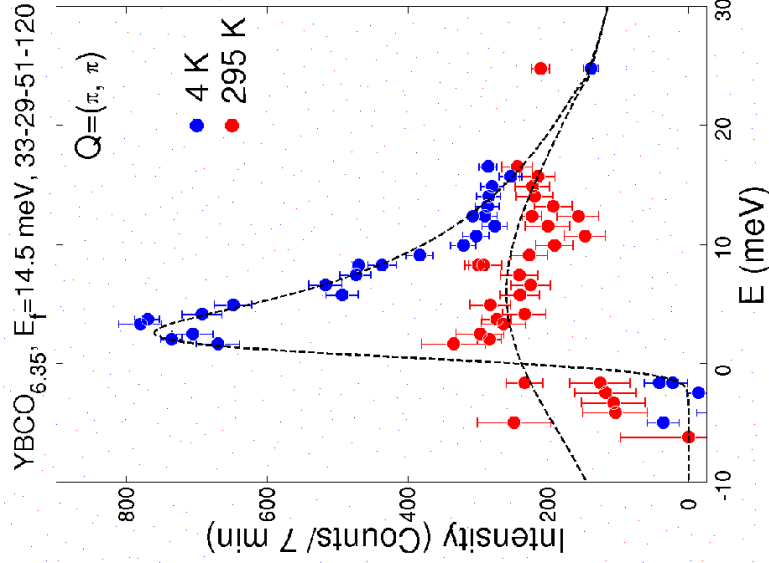


We find that checkerboards with a commensurate ( $\pi, \pi$ ) background are not low-energy states of t-J model and can only be stabilized with large external potentials.

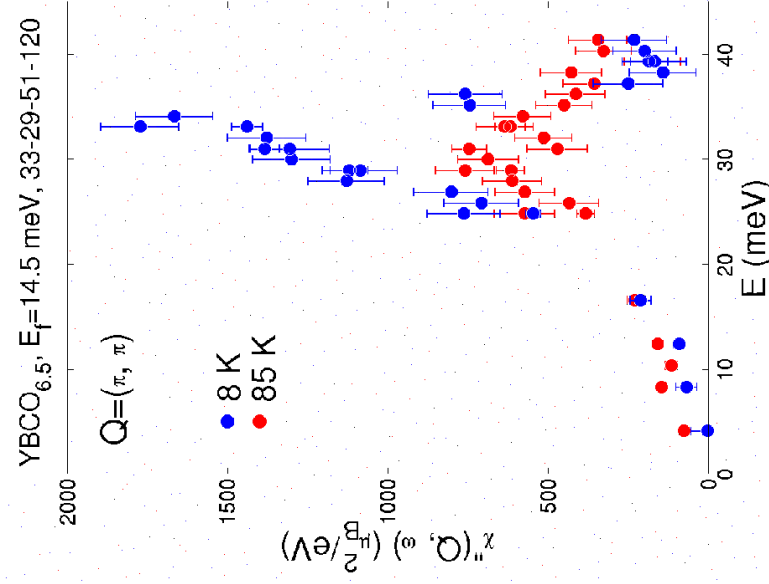
White, Scalapino PRB **70**, 220506(R) (2004)

Contrasting Low-energy Spectrum:  $x=6.35$  and  $6.5$

$T_c=18$  K     $3$  meV

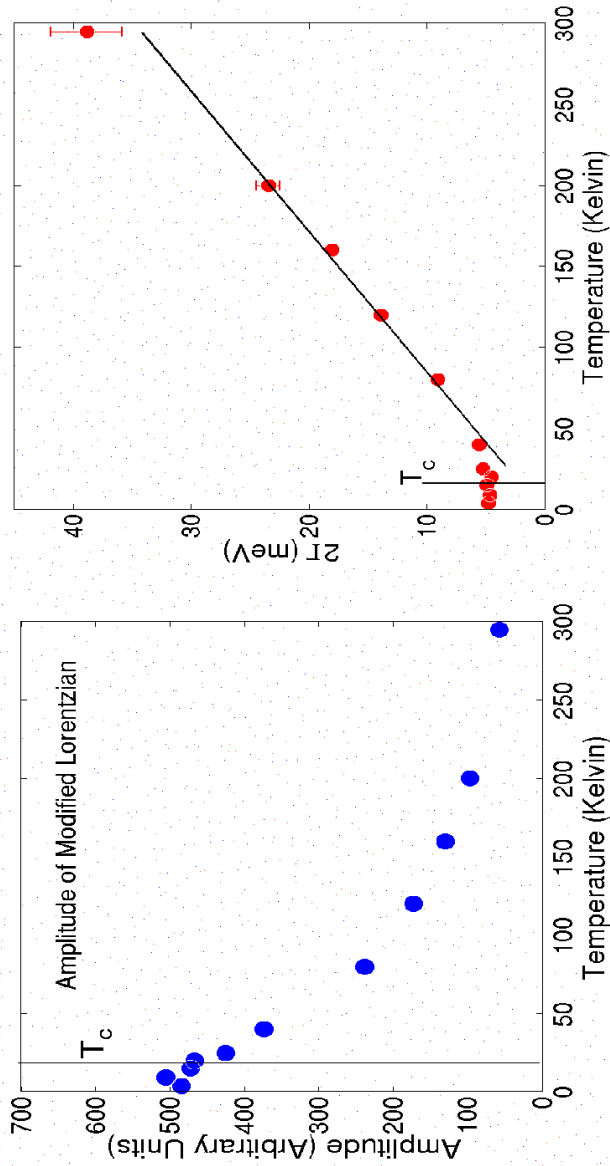


$T_c=59$  K     $33$  meV



**YBCO<sub>6.35</sub>: Modified Lorentzian**

Resonance is overdamped with a relaxation rate  $\sim 2.5$  meV  $\sim 0.6$  ps<sup>-1</sup>



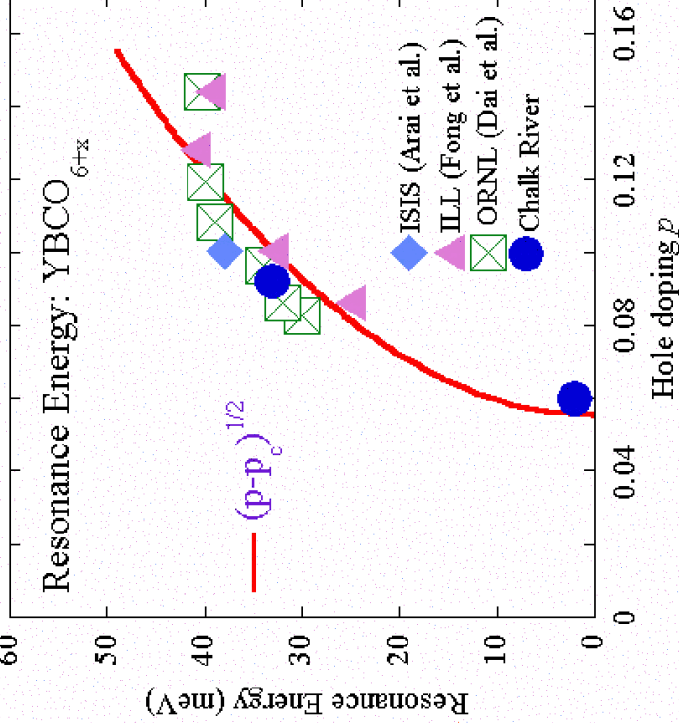
**The resonance as soft mode**

The resonance is critical: it is the *soft-mode* at the superconducting - phase boundary - but not the pairing boson

It tracks

$$T_c \sim (p-p_c)^{1/2}$$

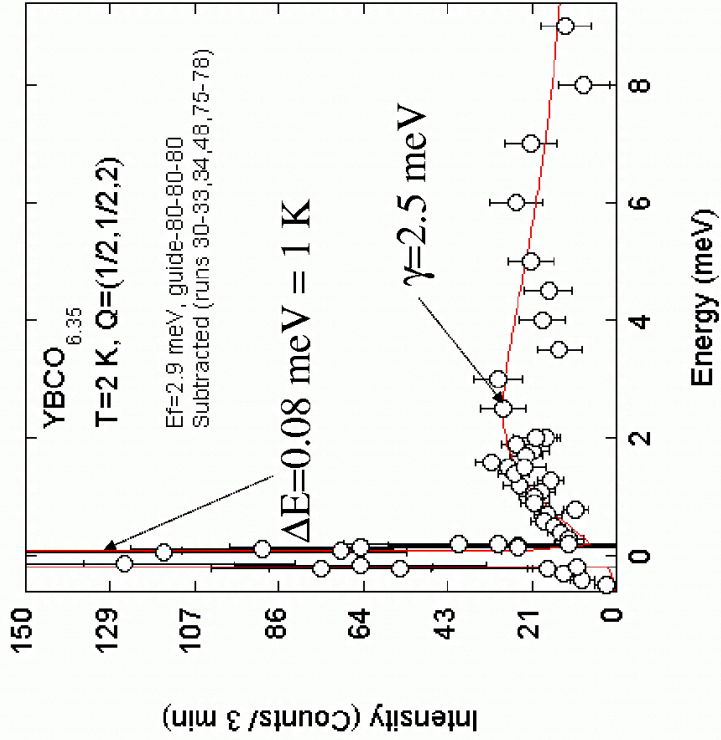
not the doping,  $p \sim \delta$ , nor ladder width



It drives the transition from superconductor to antiferromagnet.



A new lower energy scale: below damped resonance lies a Central mode: 30 times lower in energy & 150 times stronger.



Two energy scales:

- Central Peak
- 0.08 meV
- Damped resonance
- 2.5 meV
- Are they coupled?

YBCO<sub>6.35</sub>: conserved total moment— sample is single-phase.

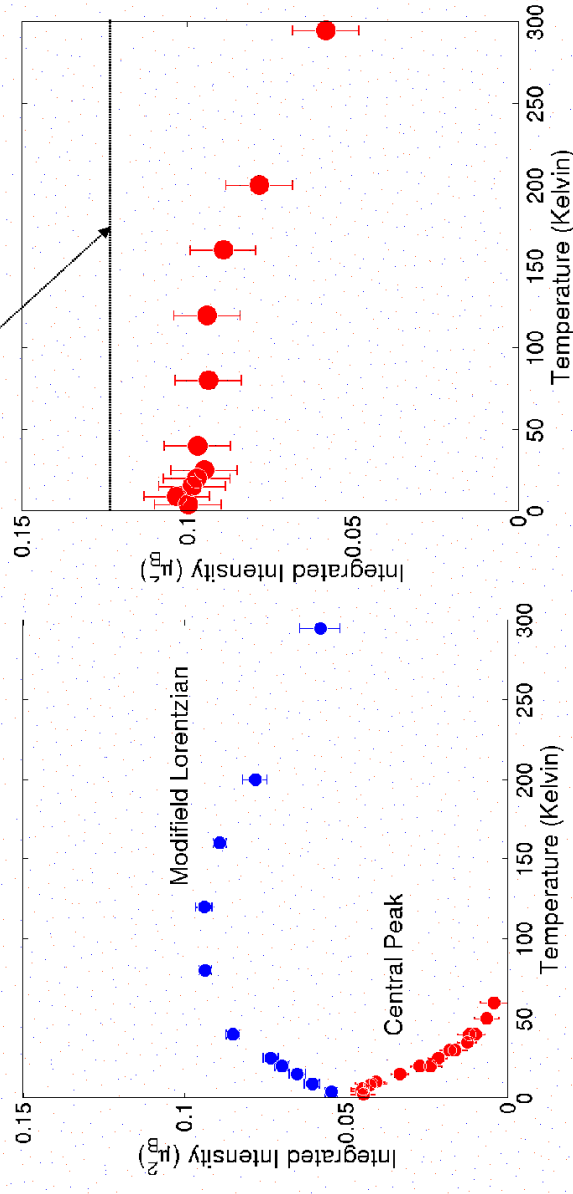
$$S(S+1) = Z_x \frac{1}{\pi} \int d\omega \int d^3q [n(\omega) + 1] \chi''(q, \omega)$$

$$Z_x \sim 0.5$$

Full moment to 32 meV detected

Soft mode drives central mode

6% expected for E<32 meV



Triplet spin  
fluctuations

$$\chi^{xx} = \chi$$

all x, all  $\omega$

$\therefore$  holes cant

spins

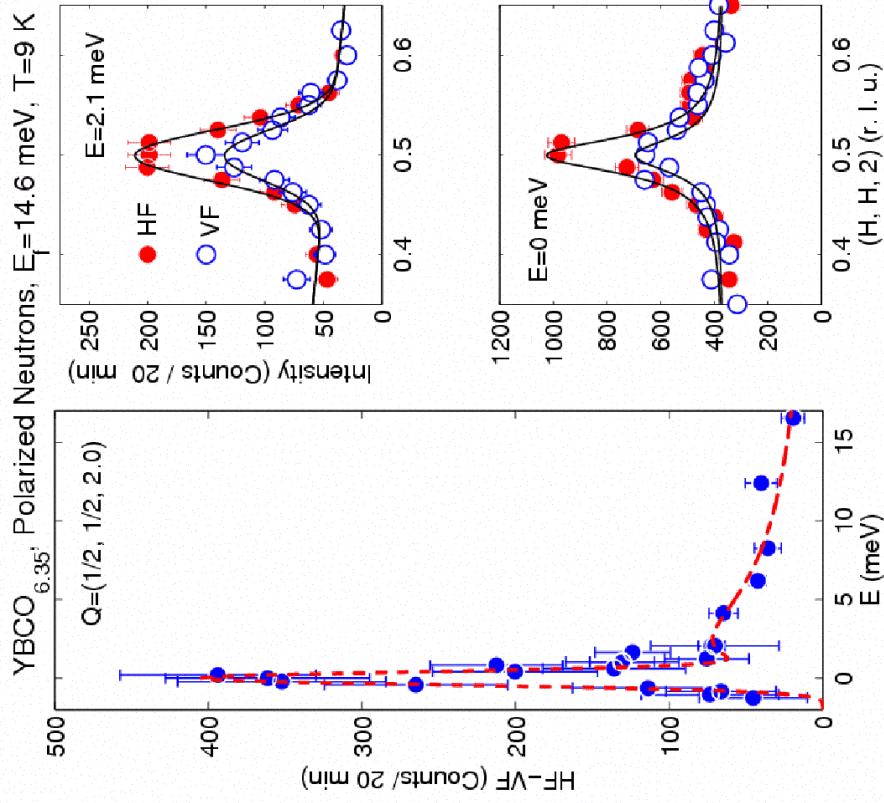
Schraiman Siggia

-Short-range in

space

8 cells

-Slow in time



Spins behave as 3D coupled bilayers

Correlation length

$$\xi_c = 8 \pm 2 \text{ \AA} \sim 1 \text{ cell}$$

AF between planes

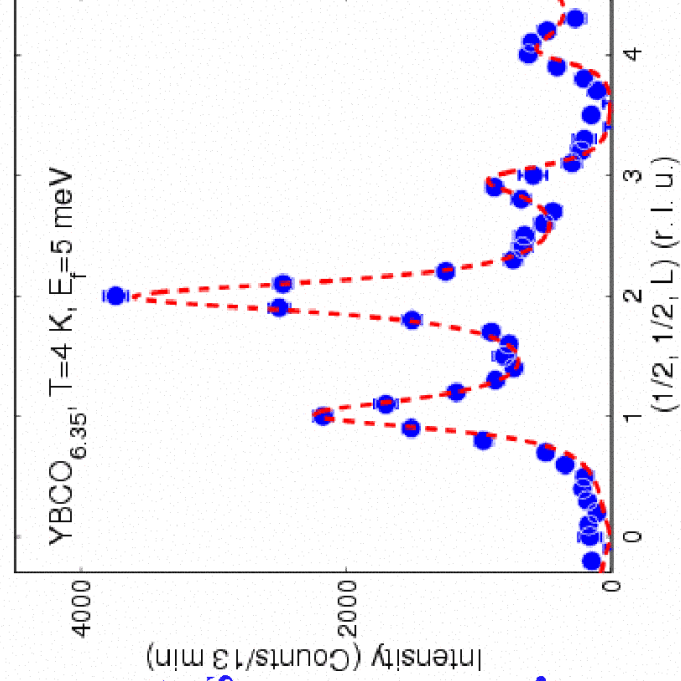
In-plane

$$\xi_{xy} = 8 \text{ cells}$$

$\therefore$  Not Bragg LRO.

- glass phase

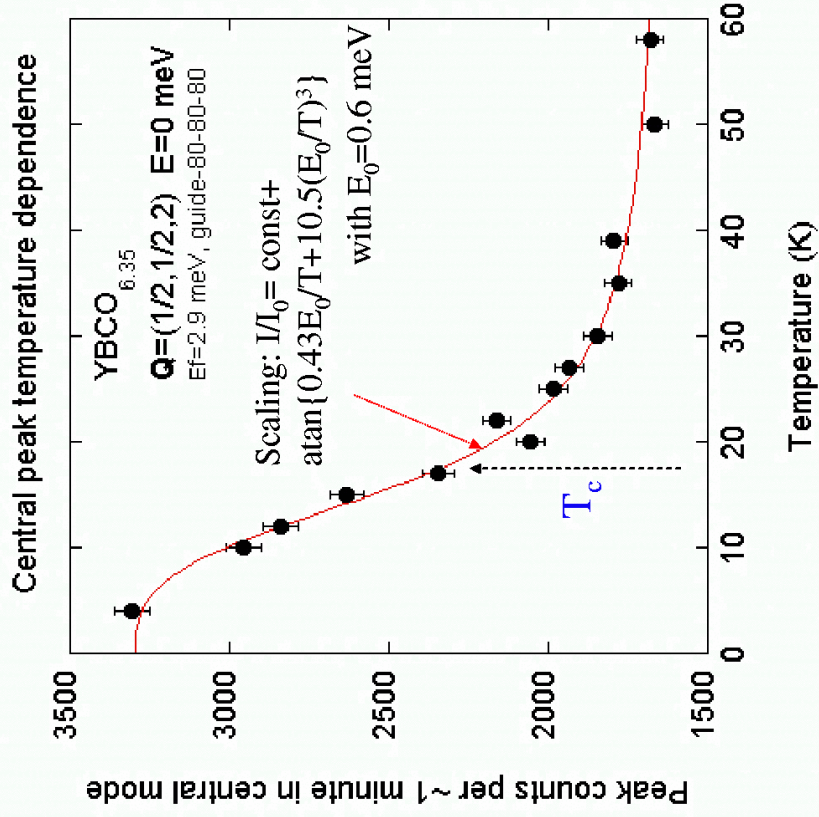
coexists with SC



Central peak  
grows as  $T \rightarrow 0$   
but  $T_c(p, 0, T)$  is  
subcritical

Spin amplitude  
ignores  $T_c$

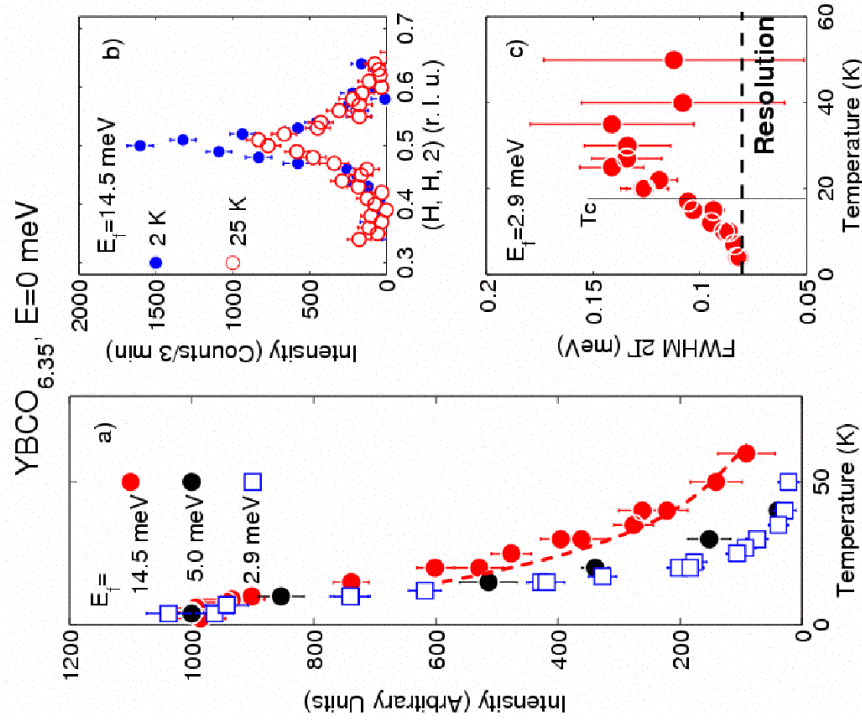
Finite DOS at  
 $\omega=0$  since  $\xi$   
finite  
 $C_v(T), \rho(T),$   
 $K(T)?$



Central peak  
 $T, q$  &  $\gamma(T)$

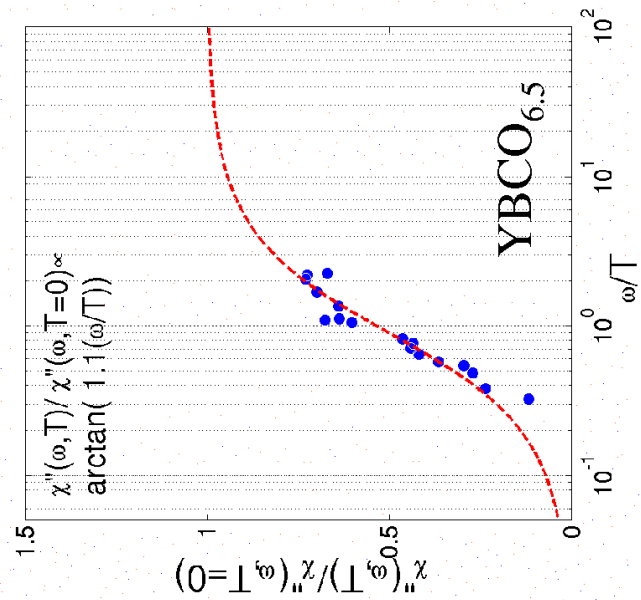
- strong spin  
weak SC response

- only  $\gamma = \tau^{-1}$   
senses  $T_c$

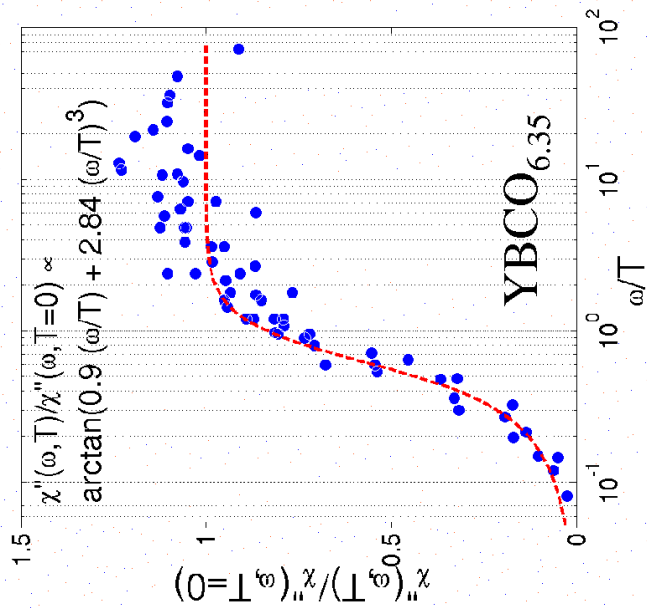


$\omega/T$  Scaling:  $I(\omega, T)/I(\omega, T=0) \sim \arctan(\omega/a_1 T) + (\omega/a_2 T)^3 + \dots$

$T > T_c = 59$  K  $\omega < 20$  meV  
farther from QCP?



T above and below  $T_c = 18$  K  $\omega < 30$  meV



Spin response of  
soft mode driving a defect mode  
à la antiferroelectric SrTiO3  
Halperin Varma '76

$$\chi^{-1} = \omega_0^2 - \omega^2 - i\omega[\Gamma + \delta^2/(\gamma - i\omega)]$$

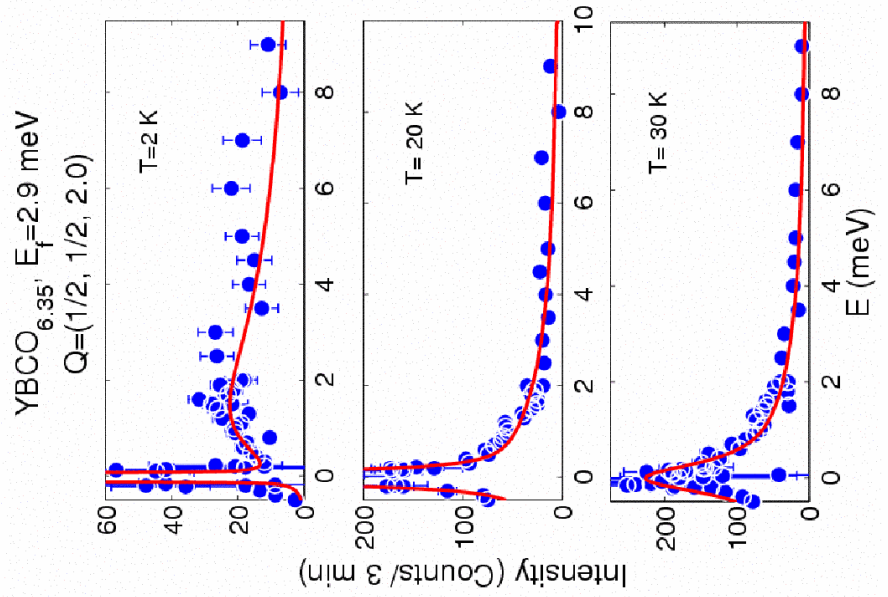
$$\gamma \ll \omega_0, \Gamma$$

$$2 \text{ K } \omega_0 = 0.65 \text{ meV}$$

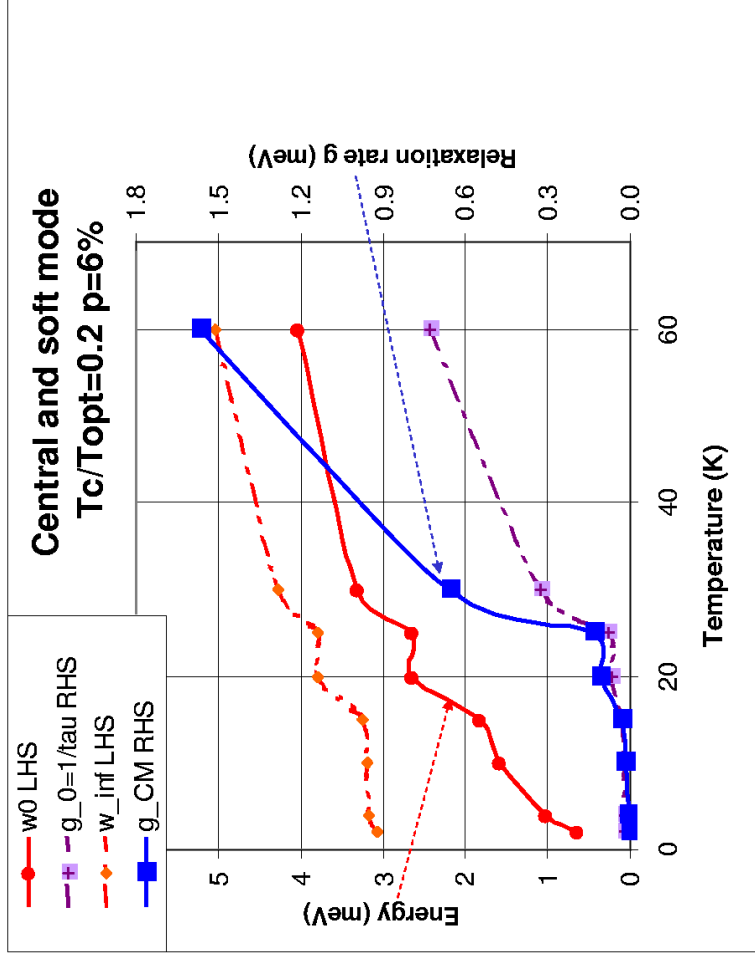
$$\gamma = 0.07 \text{ meV (0.8 K)}$$

$$\Gamma = 6.5 \text{ meV}$$

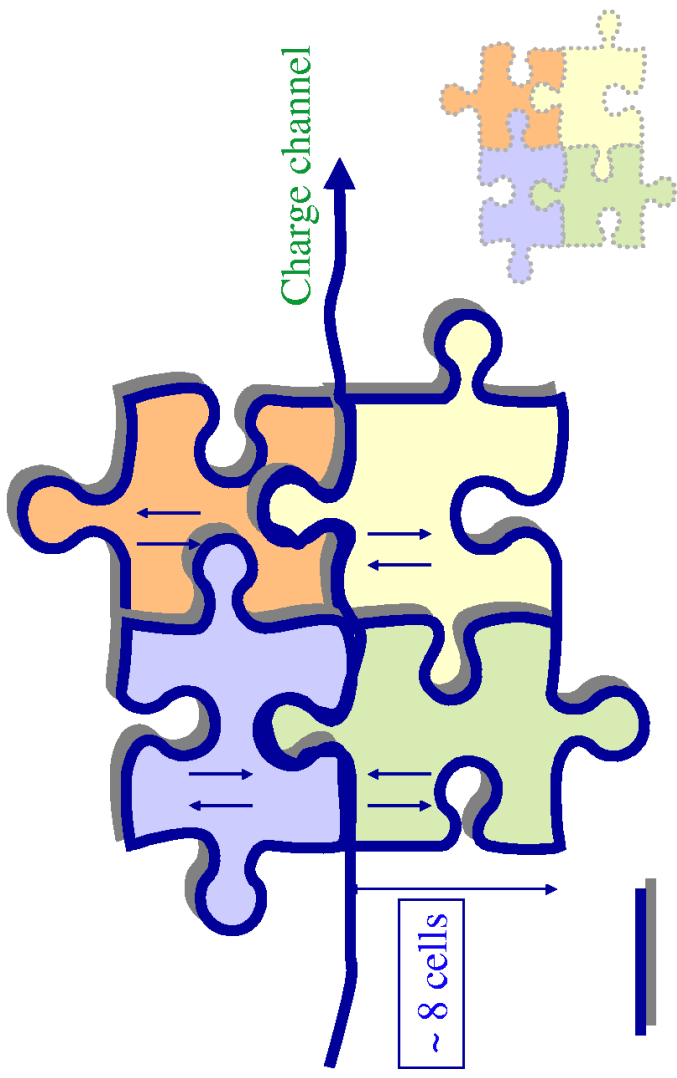
$$\text{Coupling } \delta = 3.0 \text{ meV}$$



# Slow hopping of driven “defect” What is the slow object?



# Guessed texture of spins and carriers



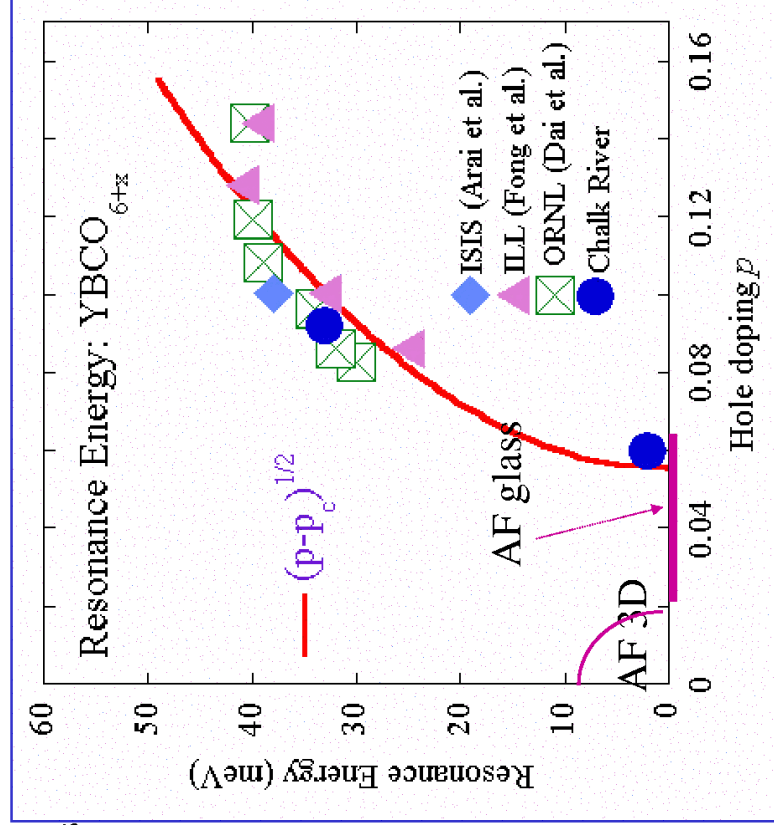
Superconducting fermion channels wrapping the spin clusters  
 Glassy spins confined in antiphase islands

Large islands of AF correlated spins (8x8) entirely turn over only very slowly. As doping decreases the hopping rate slows – hence CM for p=6% not for 9%

Spins in adjacent islands are coupled through a frustrated (ferro) charge region (antiphase domains at large p)  
 Soft spin resonance has same symmetry as the central mode to which it transfers its weight - CM means non-zero spin DOS.  
 Holes break the spin rotation invariance- QCP to glass?  
 SC boundary is far from the critical AF point but SC coexists with a nearly critical glass phase. But farther from dome QPT!

## YBCO phase diagram

**Low p:** AF spin correlations suppress charge density up to a large pseudogap.  
**Medium p:** AF correlations suppressed by SC below SC spin gap  $\chi(\omega) \sim \omega$   $q_{inc}$ ; transfer up to  $E_{res}$ . SW above.  
**Large p:** SF too weak to see below  $E_{res}$



No D-density-wave peak at  $E=0$  in YBCO nor a spin gap

Dynamic stripes at low energy signify spin-charge domains

Resonance is a fingerprint of SC d-wave DOS and shows that local pairs exist dynamically in the normal phase

At high energy the isotropic spin wave cone is recovered - it is well defined in  $q$  but overdamped in  $E$

The approach to the antiferromagnetic insulator is driven by a soft-mode collapse of the resonance

No SC-AF coexistence: near the SC transition the spins are confined; AF LR-ordered state does not coincide with the SC boundary

Stripes and spin confinement show that spin-charge spatial separation takes place at medium and small doping

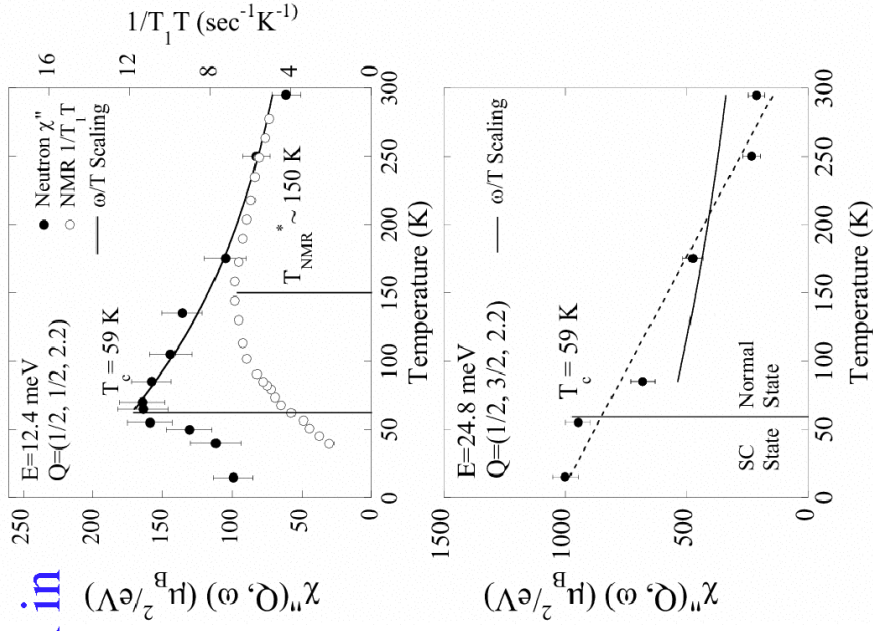
Separation contrasts with periodic spin-fermion theories

End of KITP talk.

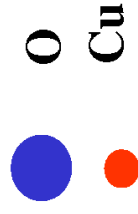
The following are background and related slides.

## Spin response and NMR in YBCO<sub>6.5</sub>

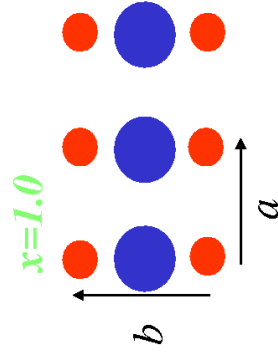
- grows on cooling
- shows no pseudogap decrease below T\* NMR
- is suppressed below T<sub>c</sub> by the superconducting order but only for E < 16 meV
- SC gap is ~3.5T<sub>c</sub> ~20 meV
- pseudogap is ~ 100 meV (Norman)



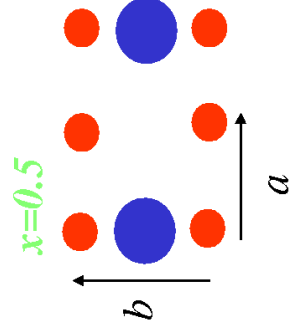
## Chain Oxygen Staging and Superstructures (YBCO<sub>6+x</sub>):



*Ortho-I Phase:*



*Ortho-II Phase:*



*Ortho-III Phase:*

*x=0.67 F-F-E*

*x=0.33 F-E-E*

N. H. Andersen *et al.*

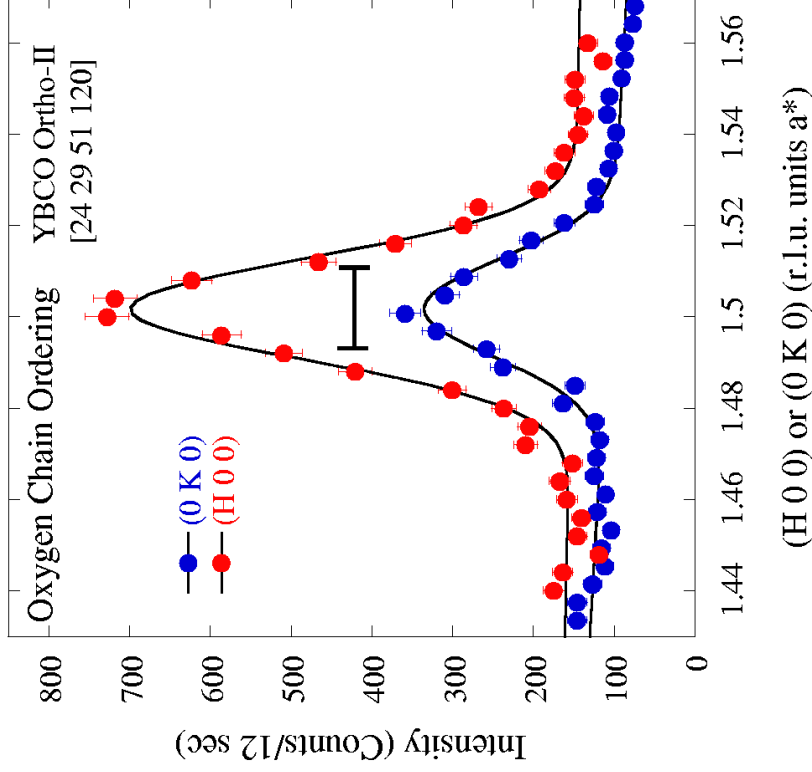
Physica C 317-318,

259 (1999).



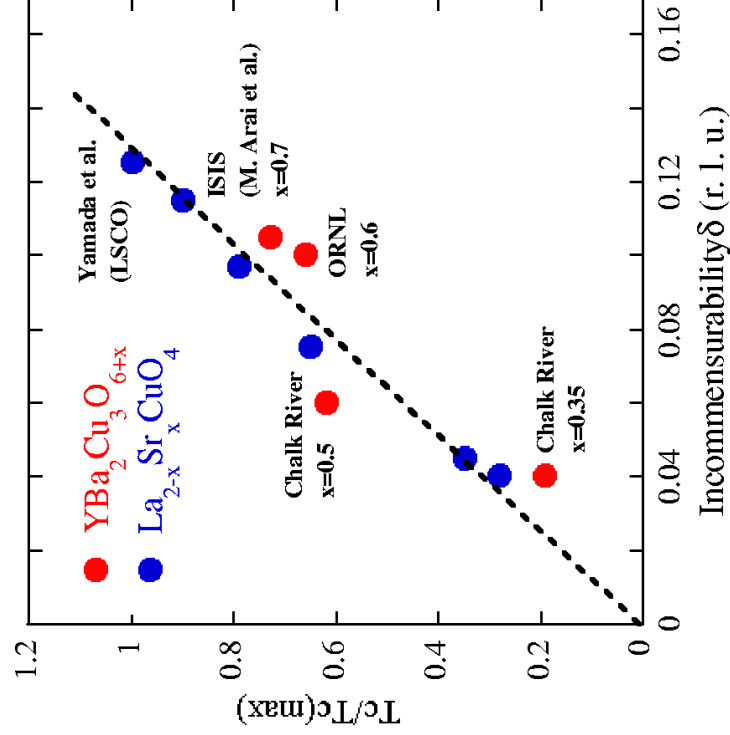
# Oxygen order

- Ortho-II ordered (every second chains filled)
- Oxygen ordered (correlation length of 100 Angstroms)
- Detwinned (70% single domain)

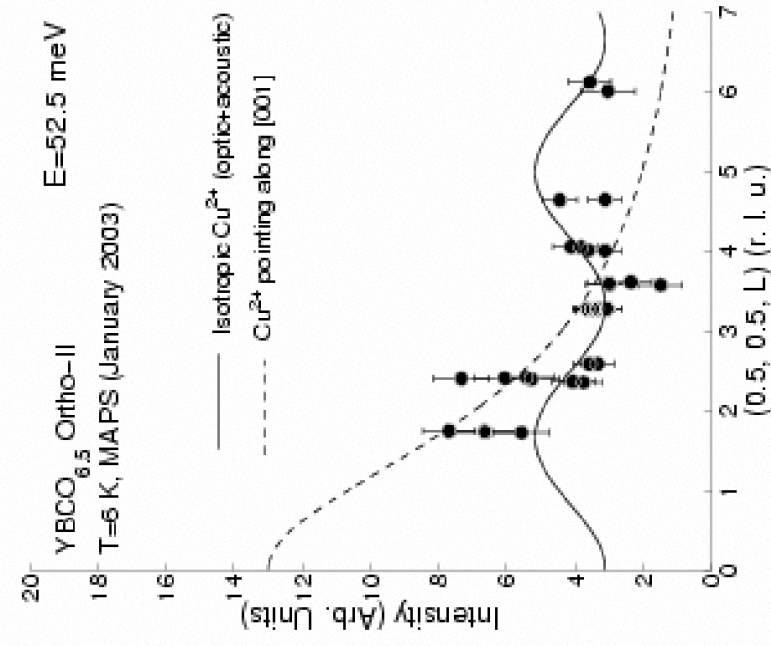
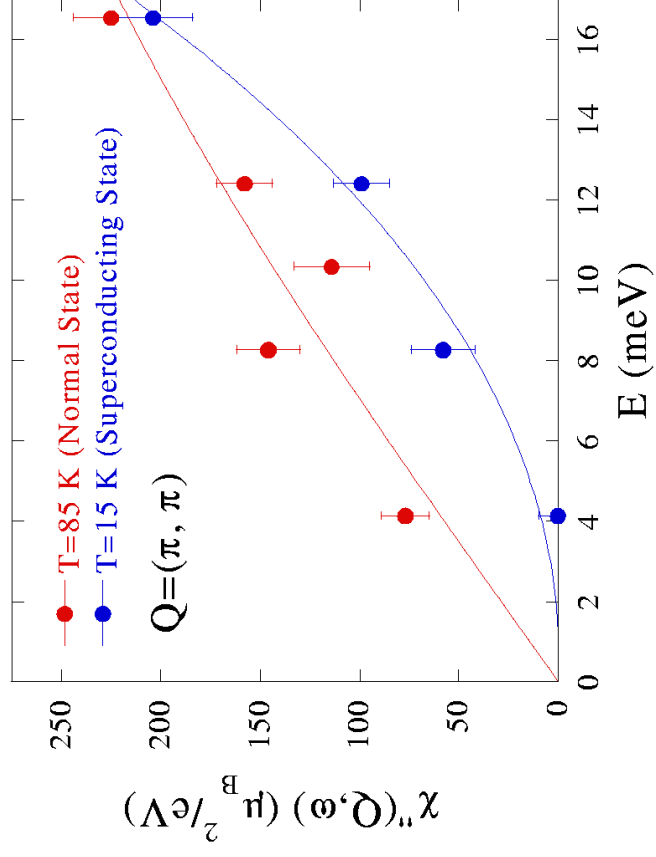


# Yamada Plot: $T_c \sim$ Incommensurability

- $T_c \sim \delta$  (Yamada et al.)
- A universal relation for YBCO and possibly all cuprates?
- Not for  $\delta < \delta_c$   $p < p_c$



YBCO<sub>6.5</sub> Low-energy Excitations  
(Gapless but Suppression at low temperatures)



Orbital currents?  
The form factor falls slowly like a local spin, not the fast  $Q^{-4}$  falloff for plaquette currents

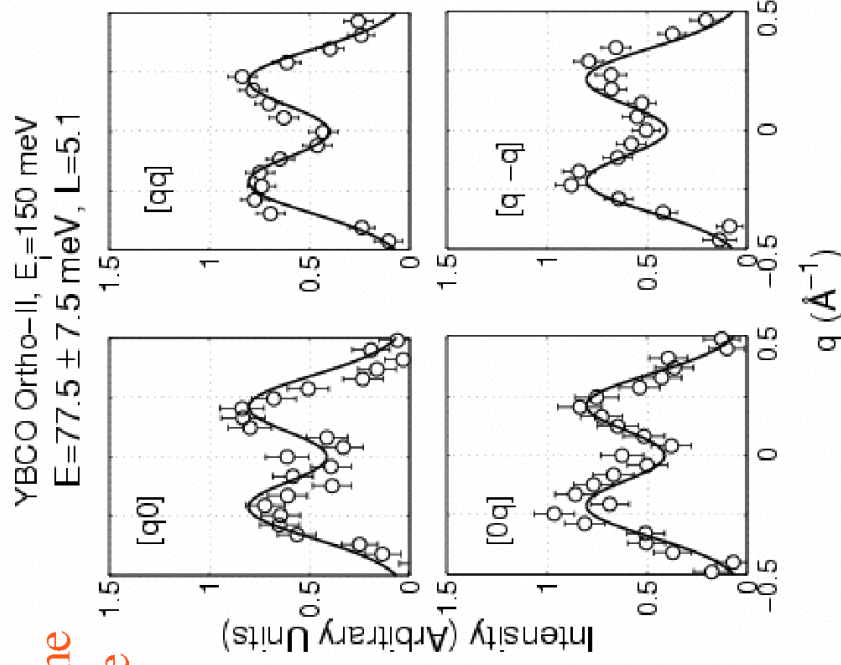
The wave vector and intensity are the same in all directions in plane

- A symmetric cone of spin excitations  
-  $q$  opens with energy.

- Not a square pattern as for  $x=6.6$  (Hayden)

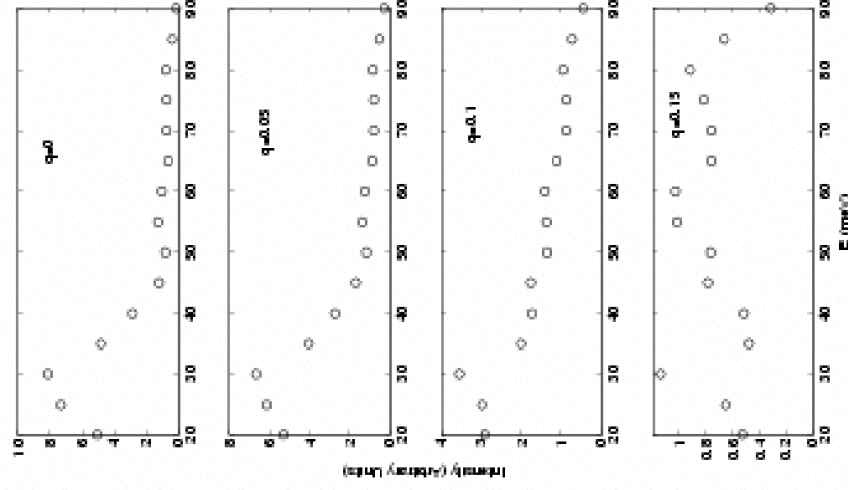
-  $q$  fixed with energy

- Dispersion centred on  $(\pi, \pi)$  as in Tranquada on LBCO 2004

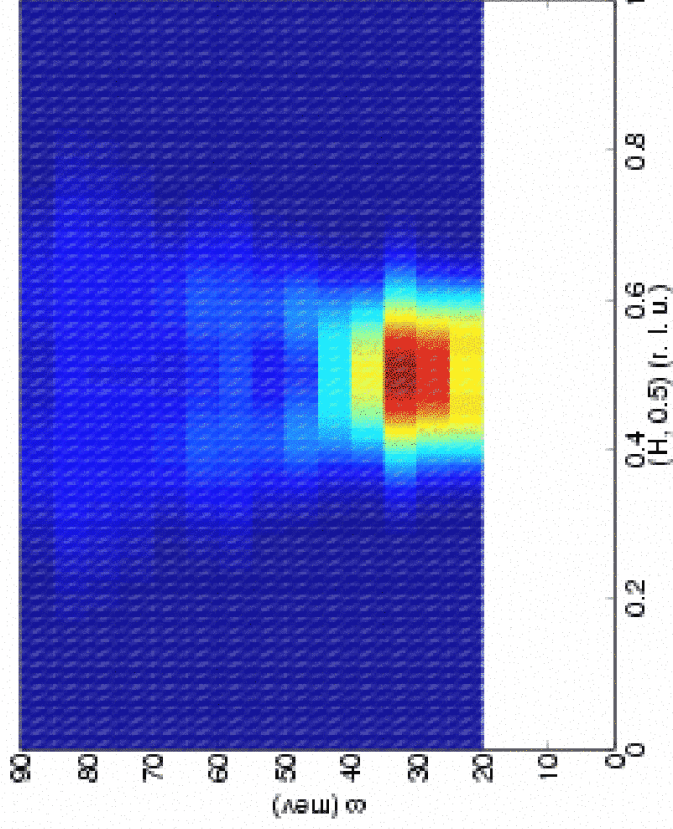


## YBCO6.35

Overdamped spin fluctuations at all momenta



Spin  
fluctuations  
in  $\text{YBCO}_{6.35}$   
emanating  
from the  
resonance  
at 33 meV



Muons:  
coexistence of  
AF and SC?  
  
Muons  
Sanna 0403608  
- Coexistence  
of magnetism and  
superconductivity

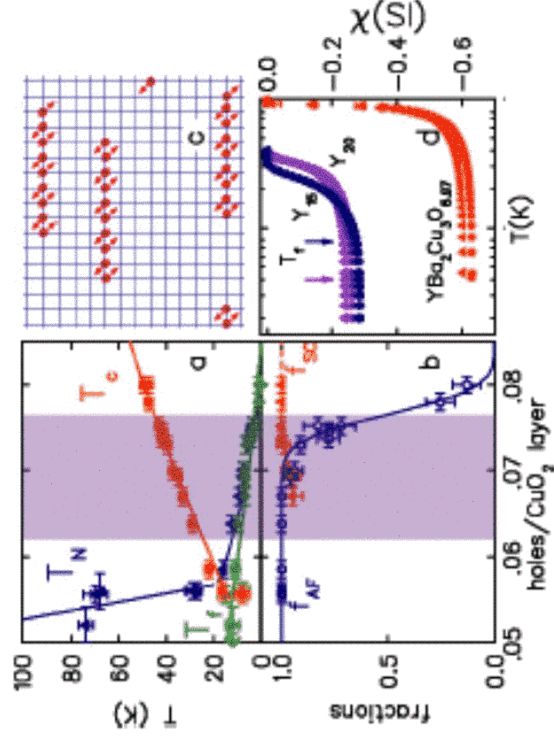


FIG. 3: Samples  $Y_{8-24}$ . a) magnetic transition temperatures ( $\blacktriangle$  from  $w_L$ ,  $\blacklozenge$  from  $T_1^{-1}$ ) and SC critical temperature  $T_c$ , vs. hole concentration  $h$ ; three samples show a distinct  $T_N > T_c$ . b) Muon volume fractions vs.  $h$ : AF ( $\circ$ , at  $T = 0$  K) and SC ( $\blacktriangle$ , for  $T_f \leq T_c$ ). c) Sketch of a stripe superconductor. d) SQUID susceptibility in  $\text{YBa}_2\text{Cu}_3\text{O}_{6.97}$ ,  $Y_{15}$  ( $h=0.70$ ) and  $Y_{20}$  ( $h=0.75$ ):  $H = 1$  Oe, FC ( $\blacktriangle$ ) and ZFC ( $\bullet$ ).

-Neutrons say no:  
no LRO