

## Near Magnetic/Non-Magnetic Boundaries in CeRhIn<sub>5</sub>

J. D. Thompson  
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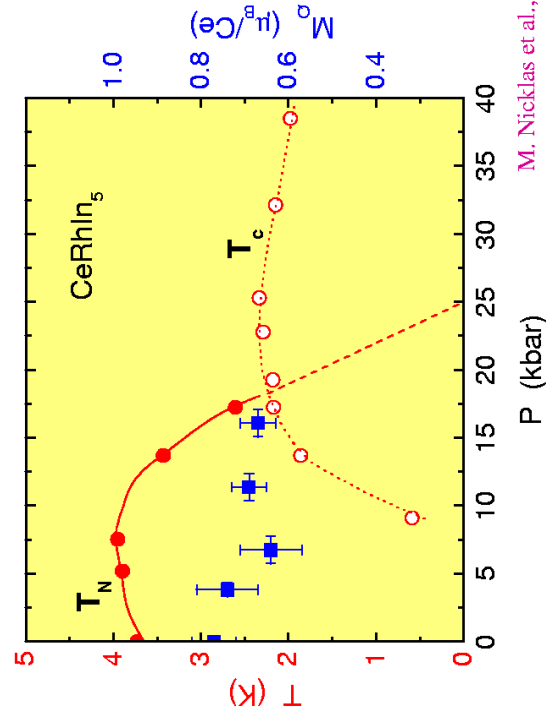
Tuson Park, Eric Bauer, Filip Ronning, Roman Movshovich, John Sarrao  
*Los Alamos National Laboratory*

Huiqiu Yuan and Myron Salamon  
*University of Illinois*

### Outline:

- Introduction--the problem and the materials
- Magnetic/non-magnetic boundaries of CeRhIn<sub>5</sub>
  - accessed by pressure
  - accessed by Sn substitutions
  - implications from comparisons to CeCoIn<sub>5</sub>
- Perspective

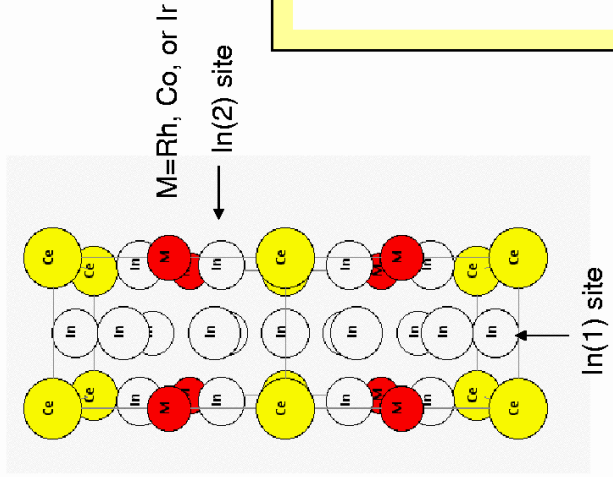
## The problems



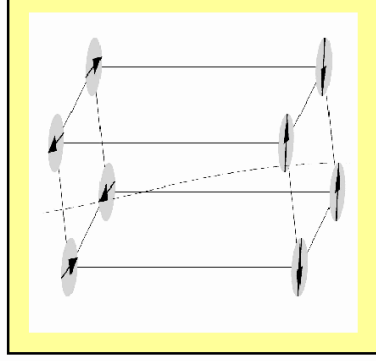
M. Nicklas et al., PRB **70**, 020505 (2004);  
A. Lobet et al., PRB **69**, 024403 (2004)

- ◆ What happens to antiferromagnetism once T<sub>c</sub> exceeds T<sub>N</sub>?
- ◆ Does the 'hidden' AFM order terminate at a quantum-critical point at P<sub>c</sub> ≈ 25 kbar?
- ◆ If so, what is the nature of that criticality?
- ◆ Is CeRhIn<sub>5</sub> relevant to understanding the origin of quantum criticality in isostructural CeCoIn<sub>5</sub>?

### CeRhIn<sub>5</sub> and CeCoIn<sub>5</sub>



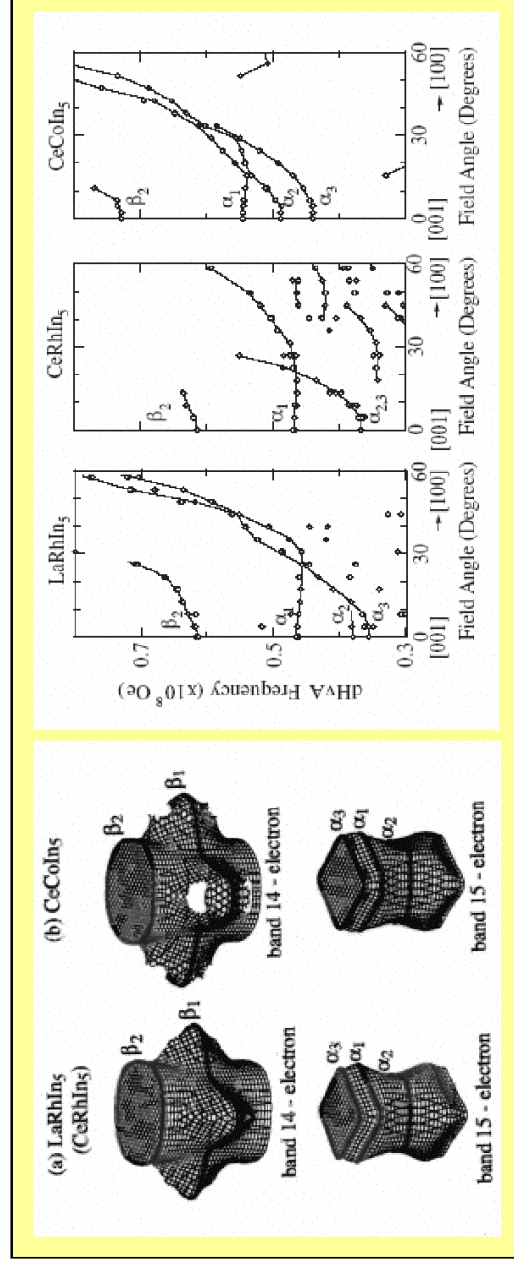
- ◆ HoCoGa<sub>5</sub> structure type: tetragonal with layers of CeIn<sub>3</sub> and MIn<sub>2</sub> stacked sequentially along c-axis
- ◆ heavy-fermion systems, with Sommerfeld coefficients  $\gamma \approx 450\text{--}1000 \text{ mJ/molK}^2 \Rightarrow$  quasiparticle effective mass  $m^* \approx (50\text{--}100)m_e$
- ◆ CeRhIn<sub>5</sub>-- antiferromagnetic with  $T_N=3.8 \text{ K}$



- ordered moment  $0.79 \mu_B$  (expect  $0.84 \mu_B$  for CEF doublet-local moment)
- incommensurate structure with  $Q = (\frac{1}{2}, \frac{1}{2}, 0.297)$

- ◆ CeCoIn<sub>5</sub>-- slightly smaller unit-cell volume than CeRhIn<sub>5</sub> (roughly equivalent to 16-kbar chemical pressure); unconventional superconductor with  $T_c=2.3\text{K}$  and signatures of quantum-critical behavior

### Fermi surfaces of CeRhIn<sub>5</sub> and CeCoIn<sub>5</sub>

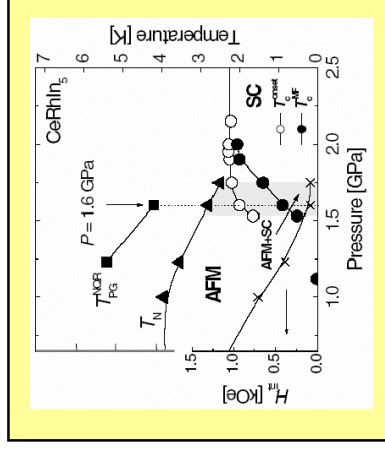
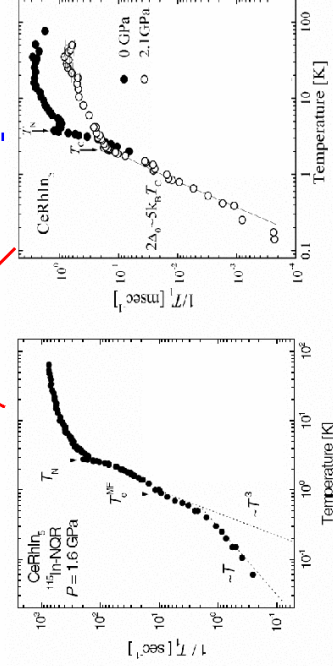
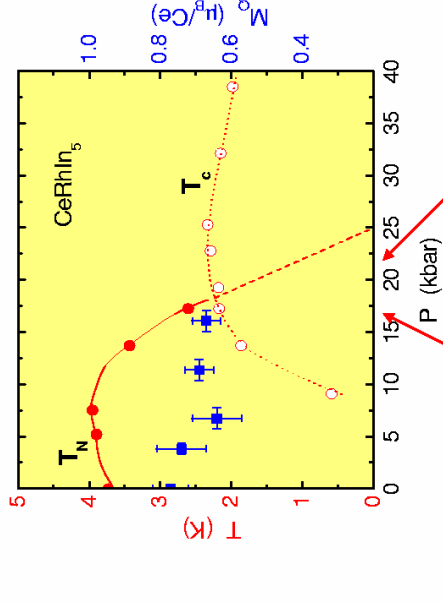


H. Shishido et al., *J. Phys. Soc. Jpn.* **71**, 162 (2002).

- ◆ quasi-2D Fermi surfaces (dominantly cylindrical), expected from layered crystal structure
- ◆ good agreement between experiment and band-structure calculations
- ◆ dHvA frequency: caliber of Fermi surface extremal cross-sections
- ◆ similar dHvA frequencies of LaRhIn<sub>5</sub> and CeRhIn<sub>5</sub>  $\Rightarrow$  Ce's single 4f electron does not contribute to the Fermi surface, i.e., 4f electron is localized
- ◆ uniformly higher dHvA frequencies of CeCoIn<sub>5</sub>  $\Rightarrow$  larger Fermi surface that accommodates  $\sim 90\%$  of a band-like and  $\sim 10\%$  of 'localized' 4f electron (Nakatsuji et al)

### 'Disappearance' of magnetism in CeRhIn<sub>5</sub>: NMR

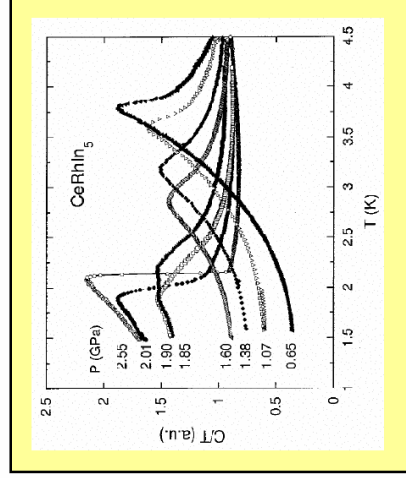
- ◆ coexistence of AFM and unconventional SC at 16 kbar from  $1/T_1$  measurements on In(1)
- ◆ at 21 kbar, no evidence for AFM above 200 mK, but extrapolated  $T_N(P)$  gives  $T_N \approx 1$ K at this pressure
- ◆ NQR  $\Rightarrow$  internal field  $\rightarrow 0$  near 16-17 kbar; inconsistent with neutron experiments (A. Lobet et al., PRB 69, 024403 (2004)); P-dependent hyperfine coupling?



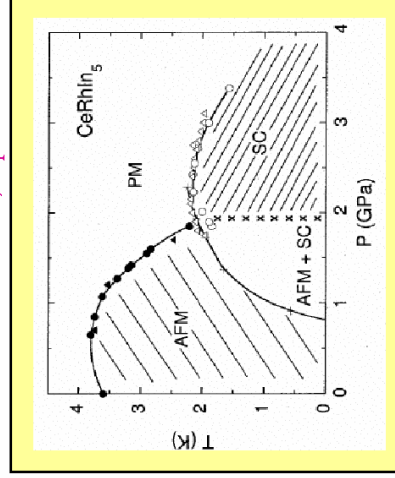
S. Kawasaki et al., PRL 91, 137001 (2003); T. Mito et al., PRB 63, 22507 (2001)

### 'Disappearance' of magnetism in CeRhIn<sub>5</sub>: specific heat

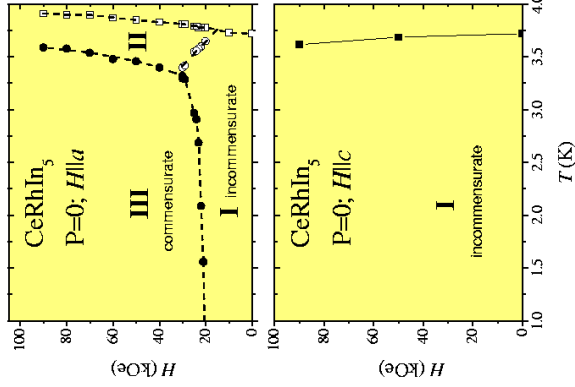
- ◆ *ac* specific heat-qualitatively consistent with earlier adiabatic measurements to 21 kbar (R. A. Fisher et al., PRB 65, 224509 (2002))
- ◆ T-P phase diagram from *ac*  $C_p$ : 1<sup>st</sup> order boundary between AFM+SC ( $T_N > T_c$ ) and SC ( $T_c > T_N$ ) regimes
- ◆ observed relationship between AFM and SC similar to other systems, eg., CePd<sub>2</sub>Si<sub>2</sub>, CeIn<sub>3</sub>, etc.
- ◆ Flouquet: 'to our knowledge there is no heavy-fermion compound where an antiferromagnetic phase appears after entrance into a superconducting state' (J. Flouquet, cond-mat/0501602; to be published in Progress in Low Temp. Phys.)
- ◆ What happens when SC is suppressed by a magnetic field??



G. Knebel et al., unpublished

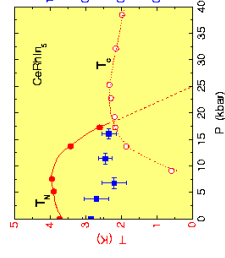


### Magnetism in CeRhIn<sub>5</sub>: low pressure specific heat and resistivity in a magnetic field

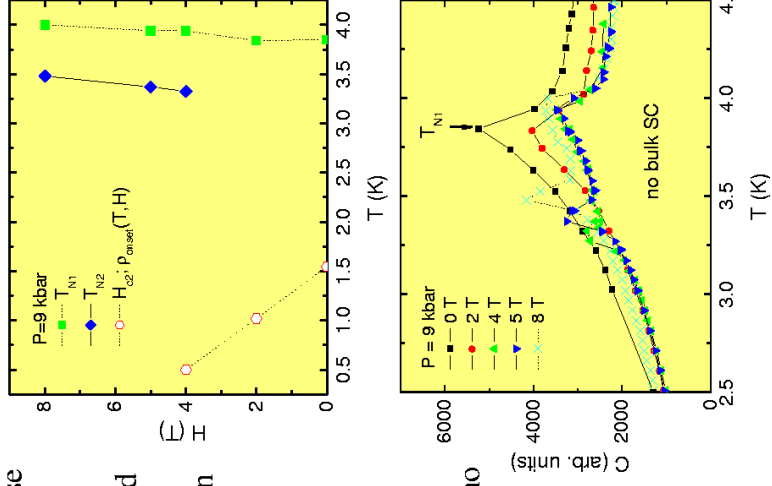


- ◆ magnetic H-T phase diagrams essentially identical at P=0 and P= 9 kbar (determined by isomagnetic temperature sweeps in *ac* specific heat for H//a-b plane); consistent with neutron diffraction
- ◆ resistive onset of incomplete SC transition at 9 kbar--no bulk SC above 0.5 K

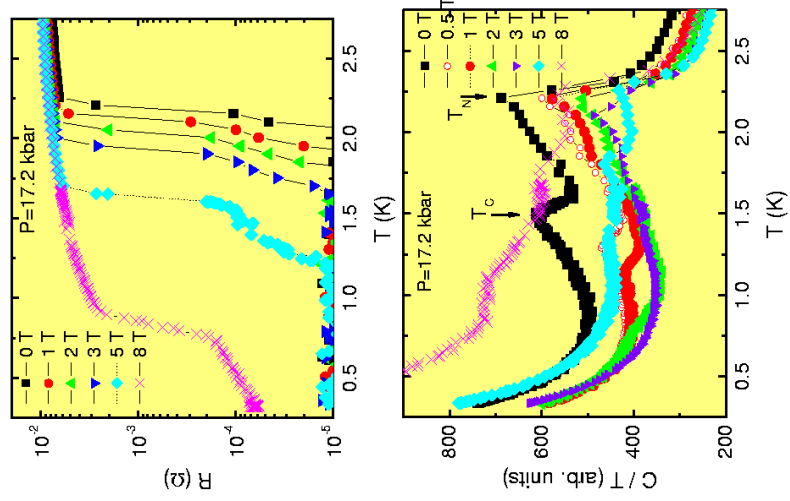
A. Cornelius et al., PRB 64, 144411 (2002); A. Llobet et al., unpublished



T. Park et al., unpublished



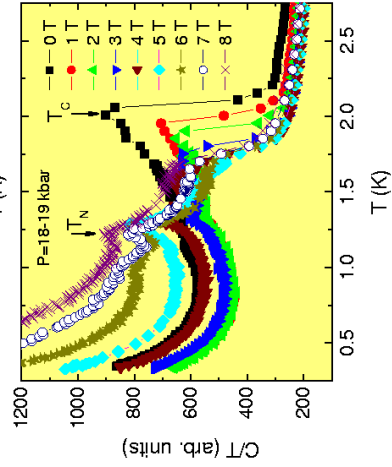
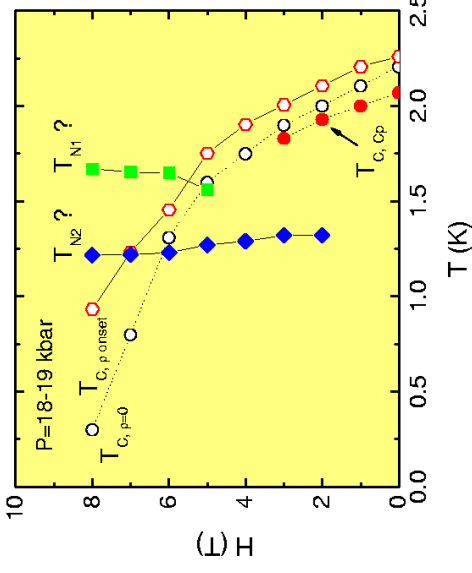
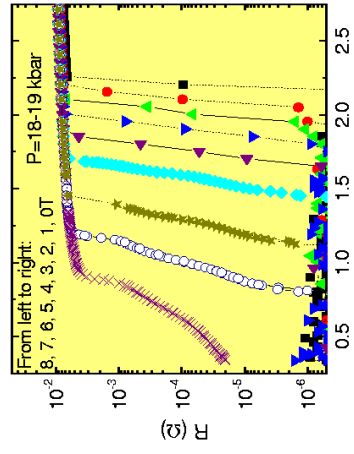
### Magnetism on the border of superconductivity in CeRhIn<sub>5</sub>



- ◆ at H=0, T<sub>N1</sub> and T<sub>c,p onset</sub> nearly coincident and at T<sub>N1</sub> >> T<sub>c,CP</sub>
- ◆ T<sub>N1</sub> and T<sub>N2</sub> evolve with H as at lower P, but T<sub>N2</sub> < T<sub>c,p onset</sub>
- ◆ resistive transition sharp at low field but develops pronounced structure with increasing H; appears ρ≠0 at 8T
- ◆ evidence for phase separation or ??

T. Park et al., unpublished

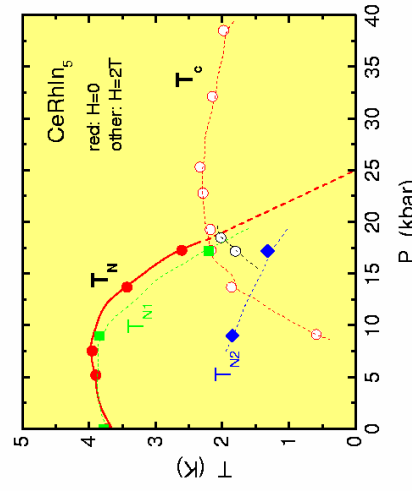
### Emergence of magnetism in CeRhIn<sub>5</sub> at T < T<sub>c</sub>



- ◆ T<sub>c,p onset</sub>, T<sub>c,p=0</sub> and T<sub>c,Cp</sub> nearly coincident ⇒ homogeneity, but resistive transition develops structure with increasing H, as at 17.2 kbar
- ◆ magnetism 'hidden' at H=0 and revealed in a field
- ◆ T<sub>N2</sub>? clearly coexists with bulk superconductivity, and no significant change in T<sub>c</sub> or T<sub>N2</sub>? when they cross
- ◆ for H ≥ 10-11T, only magnetism as T → 0

T. Park et al., unpublished

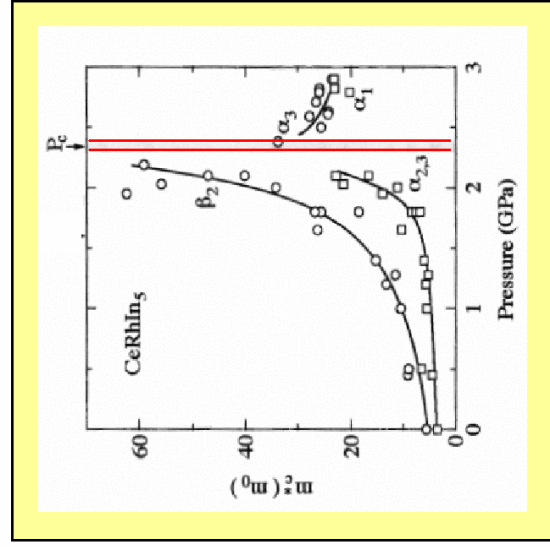
### T-P phase diagram at H=0 and 2T and evidence for criticality



T. Park et al., unpublished

- ◆ clearly more work to be done; nevertheless, initial experiments establish that (1) magnetism does not 'disappear' once T<sub>c</sub> > T<sub>N</sub> and (2) there is a plausible mechanism for an antiferromagnetic quantum-critical point near 25 kbar.

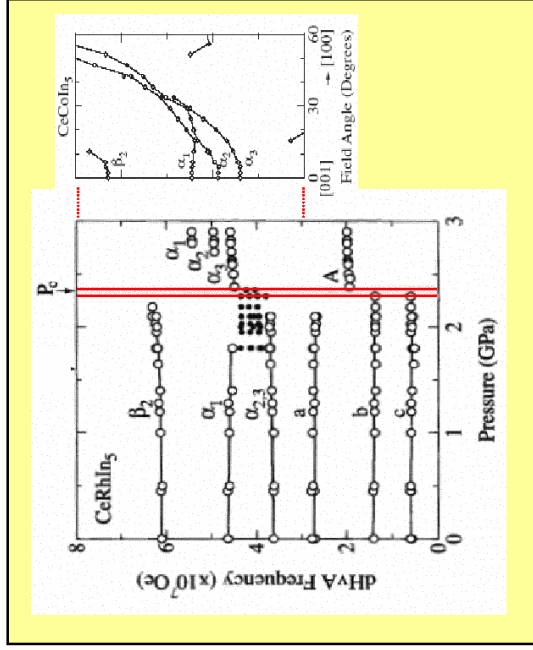
Y. Onuki et al., unpublished



- ◆ Earlier dHvA measurements to 21 kbar (H. Shishido et al., PRB 66, 214510 (2002)) suggested approach to a QCP but a QCP of what?
- ◆ new measures of m\* to 30 kbar, combined now with evidence for magnetism below T<sub>c</sub> ⇒ rather convincing evidence for an antiferromagnetic quantum-phase transition near 24 kbar

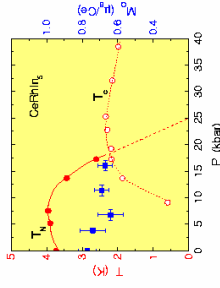


## Fermi-surface volume change at $P_c$



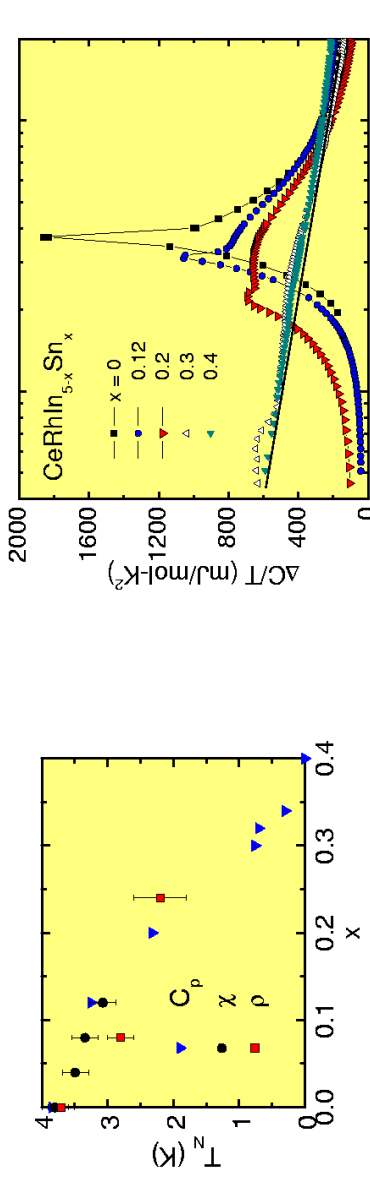
Y. Onuki et al., unpublished

- ◆ main dHvA frequencies (Fermi surface volume) essentially unchanged for  $P < 23.5$  kbar  $\Rightarrow$  f-electron remains localized
- ◆ new, unexplained, branches in a limited P interval,  $18 < P < 23.5$  kbar
- ◆ above 24 kbar, qualitative change in dHvA spectrum, particularly emergence of new  $\alpha_i$  and A branches



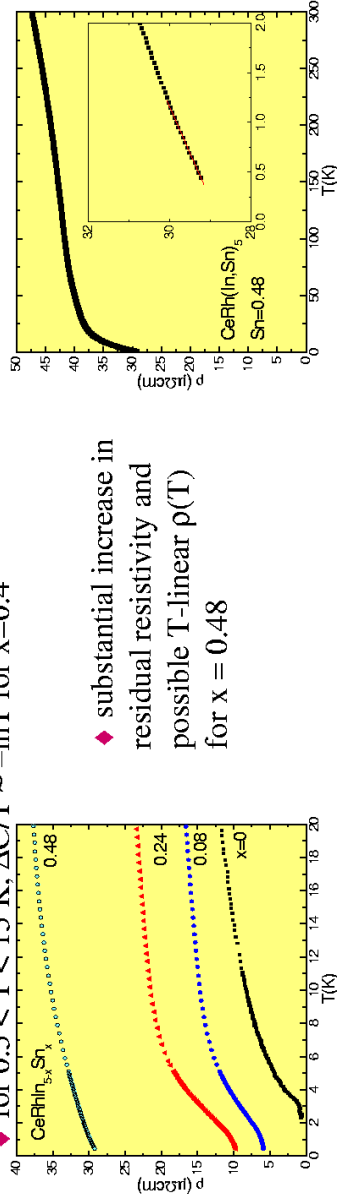
- ◆ frequencies of  $\alpha_i$  branches above 24 kbar essentially identical to those of CeCoIn<sub>5</sub> at  $P=0 \Rightarrow$  f-localized to f-delocalized transition in a very narrow P interval at  $P_c$
- ◆ abrupt change in Fermi surface volume and smoothly varying  $m^*$  above and below  $P_c$
- ◆ not expected for a conventional SDW QCP; appropriate theoretical description?? Coleman? Pepin? Si? Norman? Others?
- ◆ related to quantum-critical behaviors in CeRhIn<sub>5-x</sub>Sn<sub>x</sub> and CeCoIn<sub>5</sub>?

## Accessing the magnetic/non-magnetic boundary with Sn



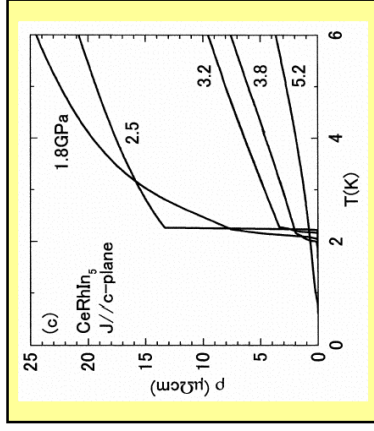
E. D. Bauer, F. Ronning et al., unpublished

- ◆  $T_N \rightarrow 0$  at  $x_c \approx 0.35$  in CeRhIn<sub>5-x</sub>Sn<sub>x</sub>, i.e., about 7% of all In's replaced by Sn but probably a greater fraction of In(1)'s (as found in CeCoIn<sub>5-x</sub>Sn<sub>x</sub>)
- ◆ for  $0.5 < T < 15$  K,  $\Delta C/T \sim -\ln T$  for  $x=0.4$

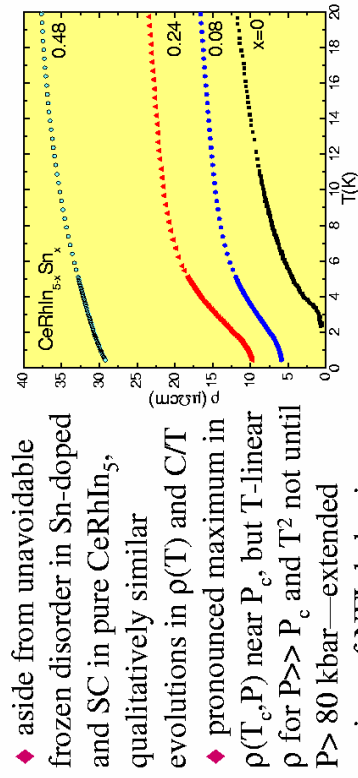


- ◆ substantial increase in residual resistivity and possible T-linear  $\rho(T)$  for  $x = 0.48$

### Pressure versus Sn-doping CeRhIn<sub>5</sub>

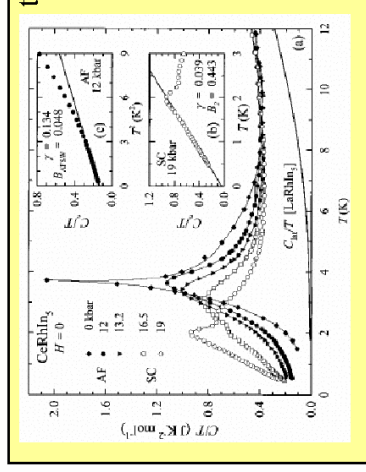


T. Muramatsu et al., *JPSJ* **70**, 3362 (2001).

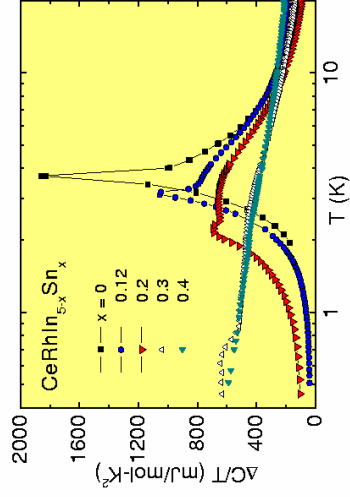


- ◆ aside from unavoidable frozen disorder in Sn-doped and SC in pure CeRhIn<sub>5</sub>, qualitatively similar evolutions in  $\rho(T)$  and  $C/T$
- ◆ pronounced maximum in  $\rho(T_c, P)$  near  $P_c$ , but T-linear  $\rho$  for  $P \gg P_c$  and  $T^2$  not until  $P > 80$  kbar—extended regime of NFL behavior characteristic of

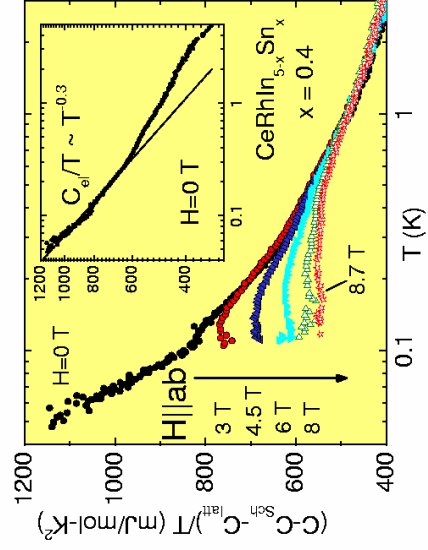
localized/delocalized QP transition?



R. A. Fisher et al., *PRB* **65**, 224509 (2002)

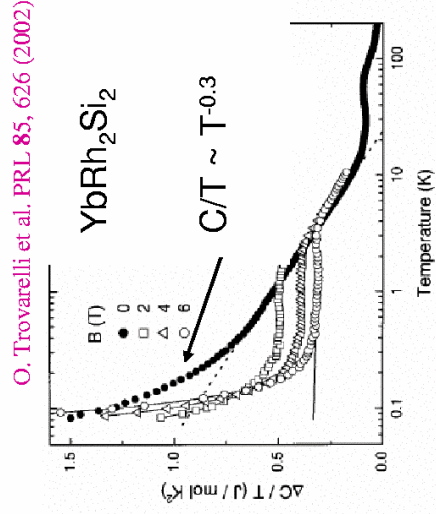


### Localized/delocalized QPT in CeRh<sub>5-x</sub>Sn<sub>x</sub> and YbRh<sub>2</sub>Si<sub>2</sub>?



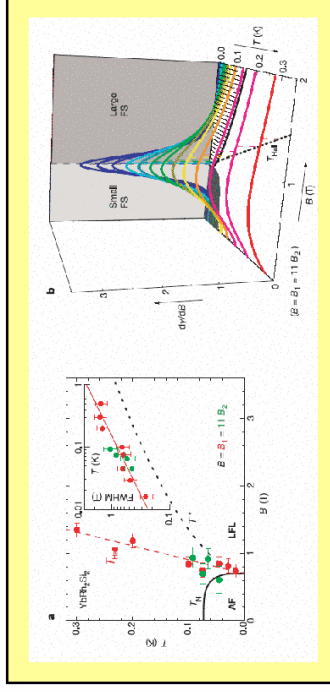
E. D. Bauer, F. Ronning et al., unpublished

- ◆ possible localized/delocalized H-induced QPT in YbRh<sub>2</sub>Si<sub>2</sub> implied by Hall effect
- ◆ unusual  $T^{-0.3}$  divergence in  $C/T$  below  $-\ln T$  regime in both YbRh<sub>2</sub>Si<sub>2</sub> and CeRh<sub>5-x</sub>Sn<sub>x</sub>
- ◆ similar physics?



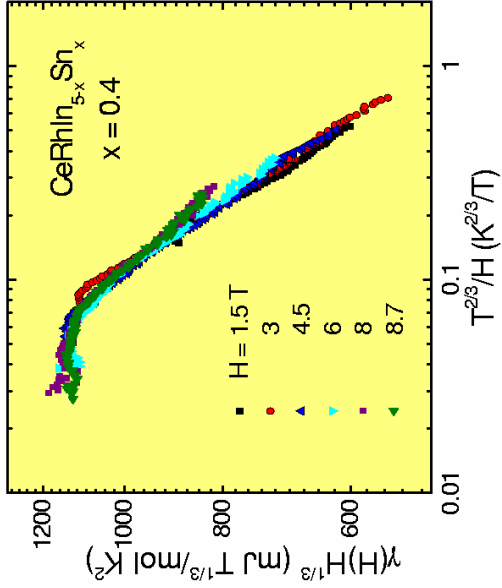
O. Trovarelli et al. *PRL* **85**, 626 (2002)

S. Paschen et al., *Nature* **432**, 881 (2004)

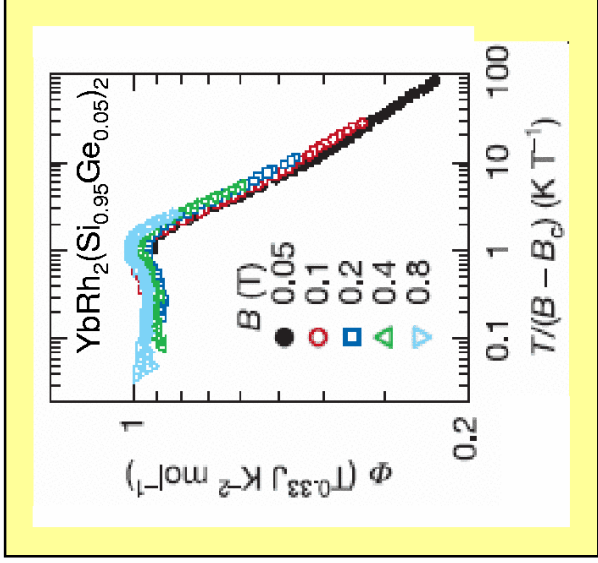


### Similar scaling forms in $CeRh_{5-x}Sn_x$ and $YbRh_2Si_2$

E. D. Bauer et al., unpublished



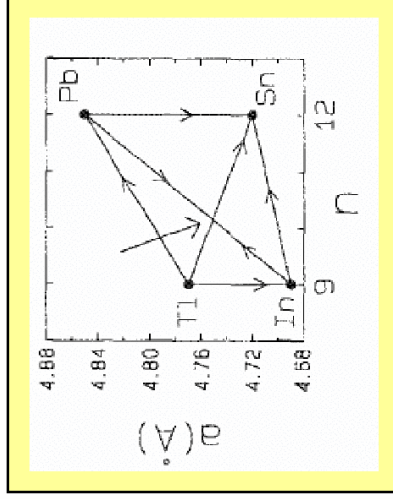
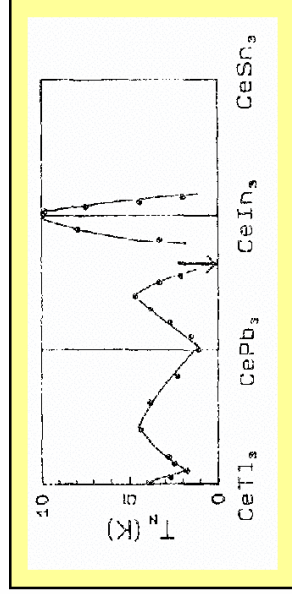
J. Custers et al., Nature 424, 524 (2003)



- ◆ near  $x_c$ , scaling form of  $\gamma(T, H)$  similar to that found in  $YbRh_2(Si_{0.95}Ge_{0.05})_2$  where  $\Phi = \gamma H^{1/3}$  and  $B_c = 0$  in Sn-doped  $CeRhIn_5$
- ◆ difference : characteristic scale governing cross-over from NFL to Fermi-liquid behavior in  $Yb122$ ,  $T_0 \propto (B-B_c)$  but in  $Ce115$ ,  $T_0 \propto B^{3/2}$

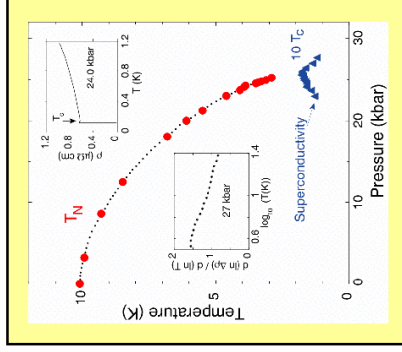
### What is Sn doing?: $CeIn_3$

S. Rahman et al., JAP 67, 5209 (1990)



- ◆ structural building block of  $CeMIn_5$  with commensurate AFM order ( $\mu_0 = 0.5 \mu_B$ )
- ◆  $P_c \approx 25$  kbar, essentially identical to  $P_c$  of  $CeRhIn_5$
- ◆  $T_N$  from 10 K to 0 at  $x_c \approx 0.65$  in  $CeIn_{3-x}Sn_x$  (J. Custers et al, Acta Phys. Polonica 34, 379 (2003)) vs. ( $T_N = 3.8$  K and  $x_c \approx 0.35$  for  $CeRhIn_{5-x}Sn_x$ )
- ◆ Sn substitution not a volume effect: vol.  $\uparrow$ ,  $T_N \downarrow$
- ◆ stronger hybridization + increase in conduction electron count tends to force  $Ce^{3+}$  to  $Ce^{4+}$ , i.e., localized 4f to delocalized 4f; same tendency with P

N.D. Mathur et al., Nature 394, 39 (1998)

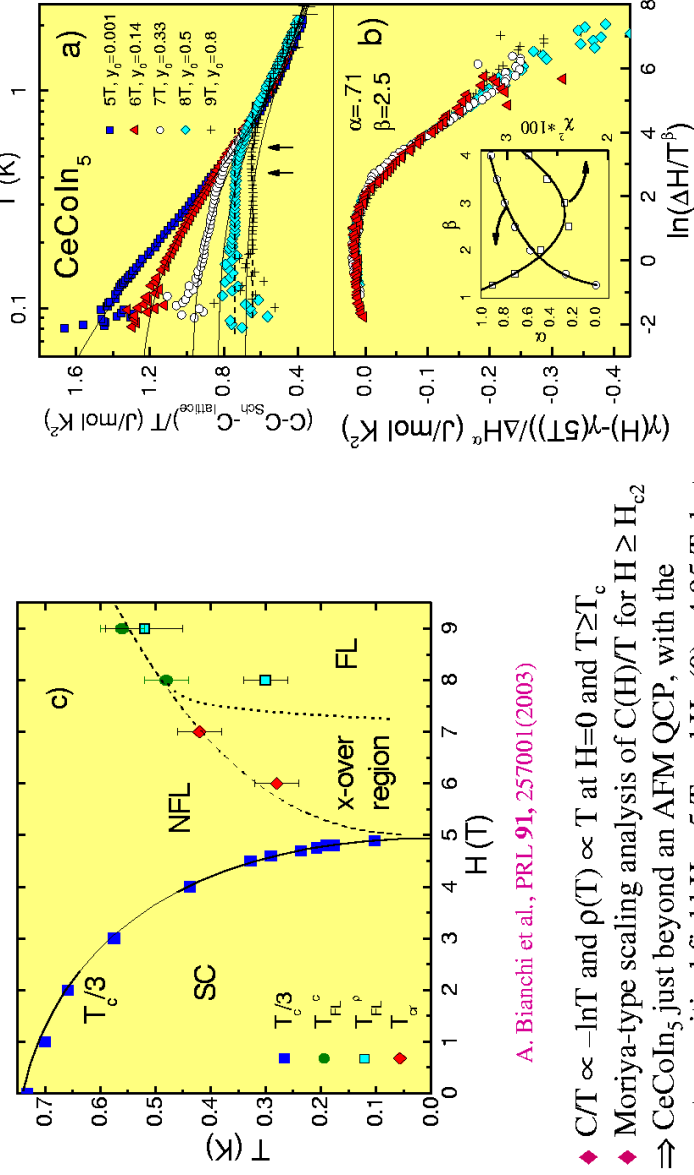




## Quick summary

- ◆ Magnetism emerges below  $T_c$  in  $\text{CeRhIn}_5$ , providing a plausible rationale for the origin of a QCP near  $P_c = 24\text{-}25$  kbar.
- ◆ QCP is not conventional (SDW-like) but is associated with a small-to-large Fermi-surface volume change (localized/delocalized 4f).
- ◆ Evidence for NFL behavior in  $\rho(T)$  extending well above  $P_c$
- ◆ QCP also accessed by Sn doping, with similarities between  $C/T$  of  $\text{CeRhIn}_{5-x}\text{Ce}_x\text{Sn}_{x\text{c}}$  and  $\text{YbRh}_2\text{Si}_2$ , which has a small-to-large Fermi-surface type QCP
- ◆ Are these critical behaviors in pressurized and Sn-doped  $\text{CeRhIn}_5$  relevant to  $\text{CeCoIn}_5$  and vice versa?

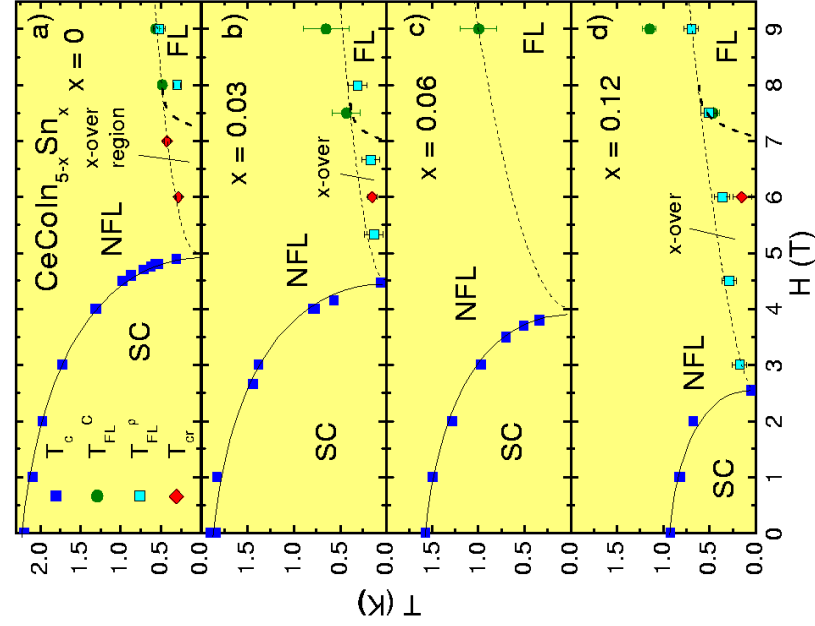
## Criticality in $\text{CeCoIn}_5$



A. Bianchi et al., PRL **91**, 257001 (2003)

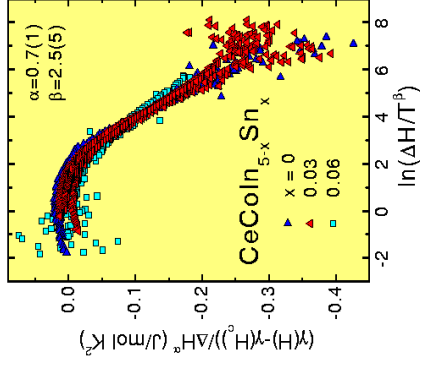
- ◆  $C/T \propto -\ln T$  and  $\rho(T) \propto T$  at  $H=0$  and  $T \geq T_c$
- ◆ Moriya-type scaling analysis of  $C(H)/T$  for  $H \geq H_{c2}$   
 $\Rightarrow \text{CeCoIn}_5$  just beyond an AFM QCP, with the quantum-critical field  $H_c = 5$  T and  $H_{c2}(0) = 4.95$  T, but no evidence for AFM order at  $H=0$  or  $H > 0$
- ◆ quantum criticality associated with hidden/avoided antiferromagnetism or superconductivity?

### 'Avoided AFM' or superconducting criticality in CeCoIn<sub>5</sub>?



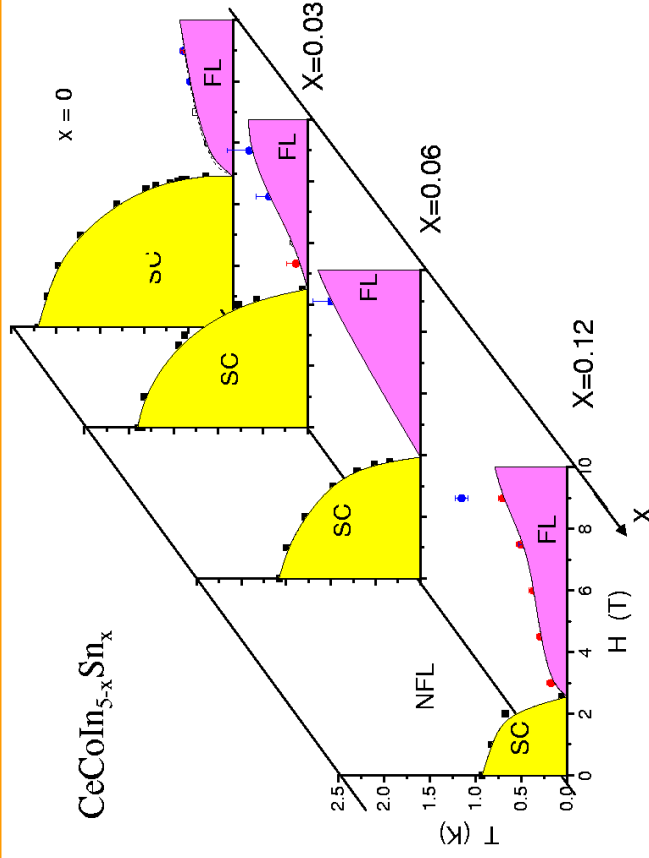
E. D. Bauer et al., PRL 94, 047001 (2005)

- ◆ for CeCoIn<sub>5-x</sub>In<sub>x</sub>,  $dT_c/dx = -0.6\text{K/at.}\% \text{Sn}$ , with  $x_c \approx 0.18$  (Sn dominantly on In(1) site)
- ◆ maximum divergence ( $\sim -\ln T$ ) of  $C/T$  very near  $H_{c2}$  and recovery of Fermi-liquid behavior for  $H \gg H_{c2}$ , as in CeCoIn<sub>5</sub>



- ◆ collapse of Moriya-type scaling onto a common curve for  $x=0, 0.03$  and  $0.06 \Rightarrow$  critical behavior tracks  $H_{c2}(x)$  but is this all?

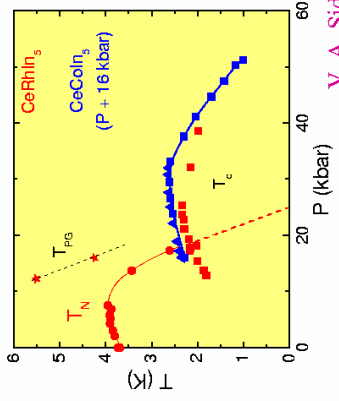
### 'Cone' of superconductivity embedded in NFL space



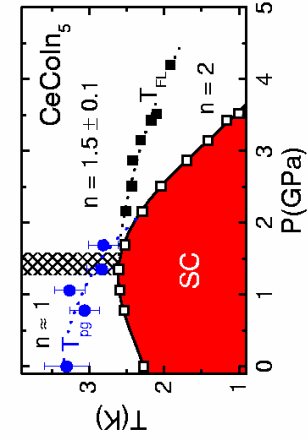
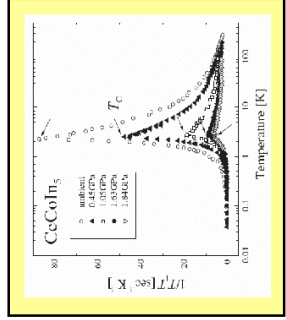
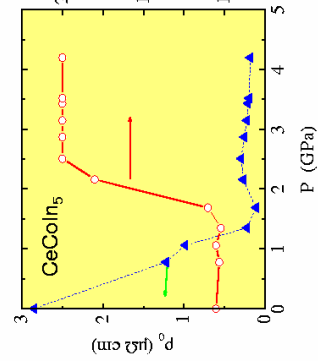
- ◆ huge T-H-x space filled with critical fluctuations in which is embedded a cone of superconductivity bounded by  $T_c$ ,  $H_{c2}$  and  $x_c(H=0)=0.18$
- ◆ not superconducting quantum criticality but what??

### Relationship of CeRhIn<sub>5</sub> and CeCoIn<sub>5</sub>

- ◆ smaller cell volume of CeCoIn<sub>5</sub> ⇒ +16 kbar chemical pressure relative to CeRhIn<sub>5</sub>
- ◆ similar T-P diagram for CeRhIn<sub>5</sub> and T-(P+16 kbar) diagram for CeCoIn<sub>5</sub>
- ◆ 16 kbar chemical pressure- a simple estimate; dHvA on CeRhIn<sub>5</sub> and CeCoIn<sub>5</sub> more consistent with CeCoIn<sub>5</sub> near the localized/delocalized border of CeRhIn<sub>5</sub> (P<sub>c</sub> ~24 kbar)

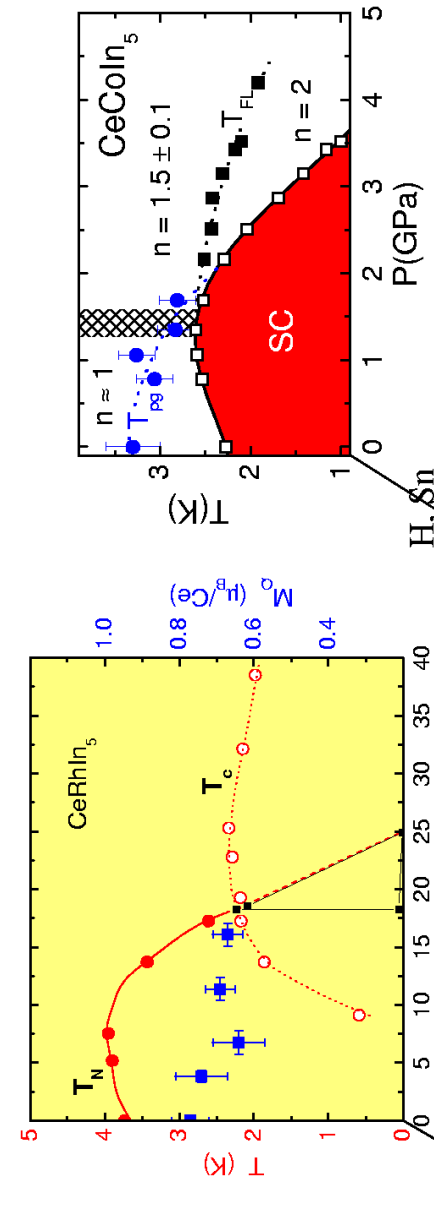


V. A. Sidorov et al., PRL **89**, 157004 (2002)



- ◆ persistence of NFL behaviors in CeCoIn<sub>5</sub> beyond its putative QCP near P=0, as with pressurized CeRhIn<sub>5</sub> and Sn-doped CeCoIn<sub>5</sub>, without a detectable change in Fermi-surface volume to 30 kbar (H. Shishido et al., JPCM **15**, L499 (2003)); recovery of Fermi-liquid-like 1/T ρ (M. Yashima et al. JPSI **73**, 2073 (2004)) and T<sup>2</sup> ρ(T) at P ≥ 20 kbar

### Summary relationships of CeRhIn<sub>5</sub> and CeCoIn<sub>5</sub>



- ◆ P=0: like CeRhIn<sub>5</sub> at P ≥ P<sub>c</sub>; large Fermi surface with partially unscreened moments
- ◆ Moriya-like scaling (itinerant magnetism) with H for CeCoIn<sub>5</sub> and for Sn doped
- ◆ residual resistivity 'collapse' for P= 15-20 kbar; marks appearance of fully coherent Kondo lattice?
- ◆ P=0, Sn doping: H-T scaling similar to YbRh<sub>2</sub>Si<sub>2</sub>
- ◆ triangle of hidden magnetism revealed in magnetic field (like CeCu<sub>2</sub>Si<sub>2</sub>?)

## Speculative perspective

- ◆ by some mechanism, local moment magnetism hidden below  $T_c$  in  $\text{CeRhIn}_5$  for  $P < 24$  kbar and revealed with applied magnetic field
- ◆ for  $P > P_c$  24 kbar,  $\text{CeRhIn}_5 \approx \text{CeCoIn}_5$ , which has extended ranges of NFL behavior as a function of tuning parameters  $P$  or  $x$  and partially unscreened local moment
- ◆ localized/delocalized transition incomplete at  $P_c$  (not fully coherent Kondo lattice); large Fermi surface contains fractionally unscreened 4f moment above  $P_c$ , as it does in  $\text{CeCoIn}_5$  above  $T_c$  at  $P=0$ ,  $x=0$  *la Nakatsuji*, Pines and Fisk two-fluid picture (S. Nakatsuji et al., PRL **92**, 016401 (2004))?
- ◆ mechanism stabilizing the NFL regime: like local moments, superconductivity also 'protects' fractionally unscreened local moments, which are ubiquitous in heavy-fermion systems (N. J. Curro et al. PRB **70**, 235117 (2004)), and that produce NFL-like excitations in the heavy-fermion state??
- ◆ parametric extent of NFL regime a function of how effective hybridization ( $P$  or  $x$ ) is in eventually producing fully coherent Kondo lattice state with maximally large Fermi surface?
- ◆ generic behavior, e.g. also  $\text{YbRh}_2\text{Si}_2$  and  $\text{YbCuIn}_4$ , or specific to  $\text{Ce115}$ 's?