

# Comments on Supersolid

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## Outline

- I. ODLRO  $\equiv$  coherent state: a phase  $\theta(\mathbf{r})$  exists
- II schematic coherent state wave function
- III Thermodynamics of supersolid (with WFB and DH)
- IV Dynamics of supersolid: a vortex liquid? (DH)

## Why not a supersolid?

Debye Temp is 25 degrees, putative vacancy energy is 15--how can vacancies not be present in quantum fluctuating ground state?

Argument goes back to Chester: absent magical action at a distance, G S must contain finite densities of all local configurations.

Phase space trumps configuration energy. Or,  $T=0$  in 3D-> finite  $T$  in 4D.

## ODLRO or Phase?

Coherent State: defined mean value of phase  $\phi(r)$  of Boson field; that is, the boson field has a mean value.

$\phi$  is meaningless unless number fluctuates:  
 $\langle N | \psi | N \rangle = 0$  (and vice versa) :  $N$  and  $\phi$  are conjugate.

Only rational, *local* description of condensed state is coherent state, since ODLRO implies  $N$  fluctuates in any local region. Think of coherent state as “wave-packet” in the  $N$  variable.

Proposed schematic wave function for supersolid:

$$\Psi = \prod_{sites i} (b_i^* + g e^{i\phi_i}) |vac\rangle, \text{ where}$$

$$b_i^* = \int dr f(r - r_i) \psi^*(r)$$

$g$  is  $\ll 1$  and is just a real number;  $g^2$  = the incommensurability.  $f$  is a normalized wave function centered on site  $i$ , thought of as a localized Hartree-Fock solution to an effective Hamiltonian as discussed in my book.

## Further about wave fn

Hartree-Fock clearly doesn't work with strong He interactions. Could improve either with pseudopotential a la Huang et al; or similar idea of multiplying by Jastrow function.

Superfluid stiffness comes from hopping energy:

$$H_{sf} = \sum_{i,j} g^2 t_{ij} \cos(\varphi_i - \varphi_j)$$

## Thermodynamics of incommensurate solid

Wave function of this type has vacancies (or interstitials) completely delocalized--I e condensed. Energy will depend on relative density of sites quite steeply but not singularly ---we assume no cusp.

There are of course phonons, but I don't think any second Goldstone boson. Non-quadratic terms in the displacements will give the usual Gruneisen dependences of coefficients on the total energy of the phonons, that is on  $T^4$ . In equations:

continued--  
 $\varepsilon \equiv (N_c - N) / N_c = \varepsilon_0 + \delta$

$$F = E_0 + E_2 \delta^2 / 2 - (D_0 + D_1 \delta + \dots) T^4 + \dots$$

minimize, and

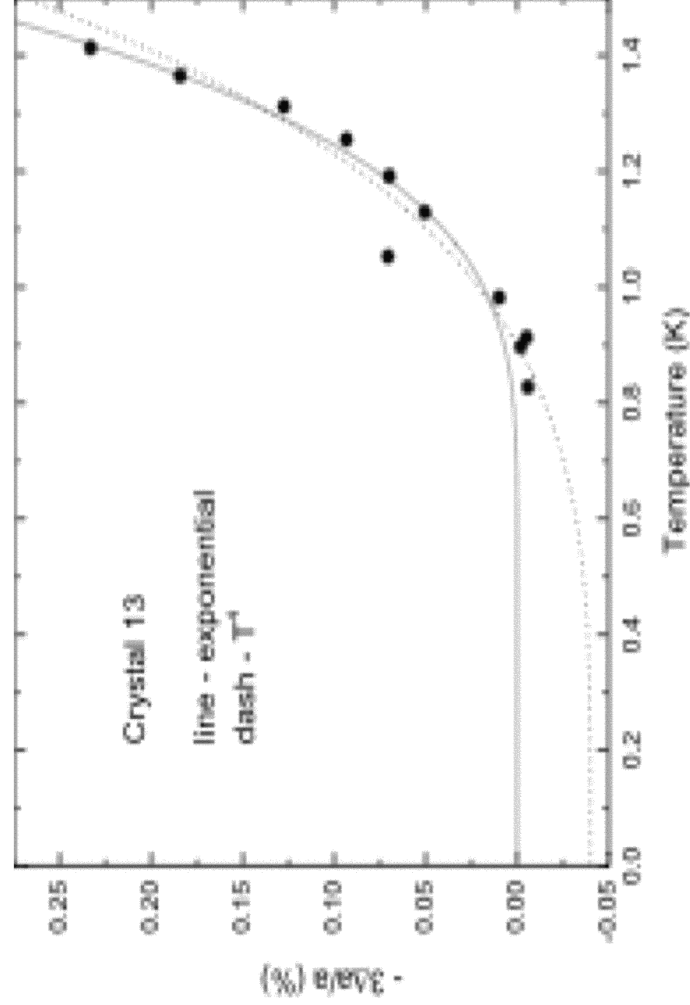
$$\delta \approx D_1 T^4 / E_2$$

Note NO Schottky Term!!!

$$C_V = AT^3 + BT^7$$

<sup>1</sup> W. R. Gardner, J. K. Hoffer and N. E. Phillips, Phys. Rev. A 7, 1029 (1973).

$$F = E_0 - D_0 T^4 - D_1^2 T^8 / 2E_2 + \dots$$



## Vortex Fluid or Supersolid?

Observed: not conventional phase transition but dissipation peak, nonlinear response. Dissipation?  $T$  must be  $>T_c$ .

Vortex fluid:  $\nabla \cdot \mathbf{J}=0$ , so  $\nabla^2 \phi=0$ . State characterized by positions of vortices. [like Kosterlitz-Thouless,  $>T_c$ , in 2D]

To rotate must introduce vortices. Vortex energy, current NOT reduced by thermal background of vortices :  $E \propto \ln[1/\Omega]$  (Note log dependence of  $\delta l$ , experimentally)

We (D Huse) propose phenomena caused by sluggishness of vortex motion.  $T$ -dependent (and He-3 dependent?) rate of vortex response. see illustration

Note similarity to Ong's Nernst phenomena in pseudogap vortex liquid!!

$\Omega=0$  is DC: explains non-leaking data!!

## Huse Proposal

