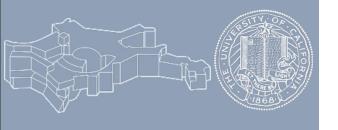


Type Ia Supernova Simulations: The Deflagration Model and Beyond

Friedrich Röpke

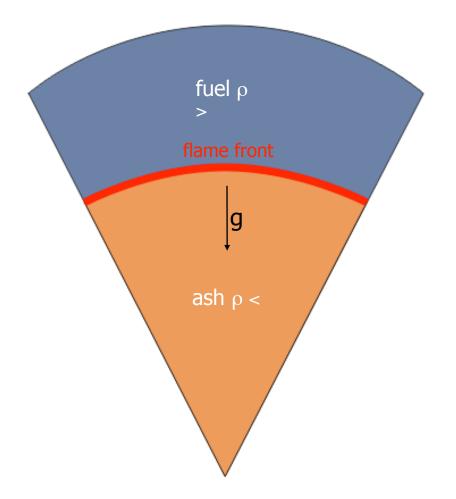
University of California at Santa Cruz and Max-Planck-Institut für Astrophysik, Garching



W. Hillebrandt, S. Woosley, M. Reinecke, M. Gieseler, C. Travaglio, M. Stehle,P. Mazzali, J. Niemeyer, W. Schmidt, S. Blinnikov, E. Sorokina

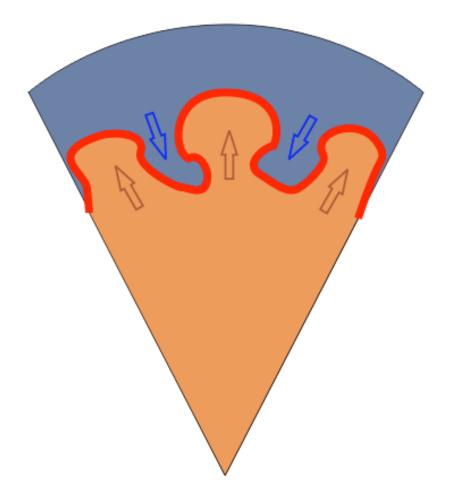
Turbulent combustion in SNe Ia

Turbulent flame propagation in deflagration mode (consistent treatment)



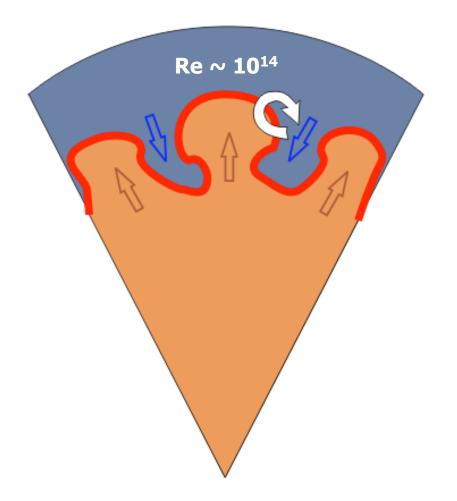
Turbulent combustion in SNe Ia

Turbulent flame propagation in deflagration mode (consistent treatment)



Turbulent combustion in SNe Ia

Turbulent flame propagation in deflagration mode (consistent treatment)



Turbulent deflagration

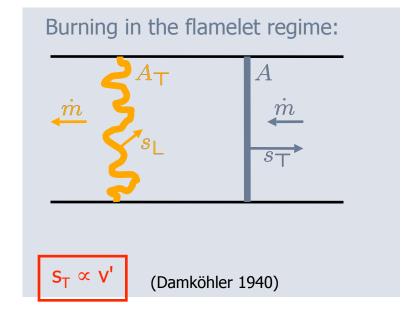


KITP 07, 3/22/2006

Turbulent deflagration

most parts of the SN Ia explosion: turbulence does not penetrate internal flame structure: flamelet regime of turbulent combustion





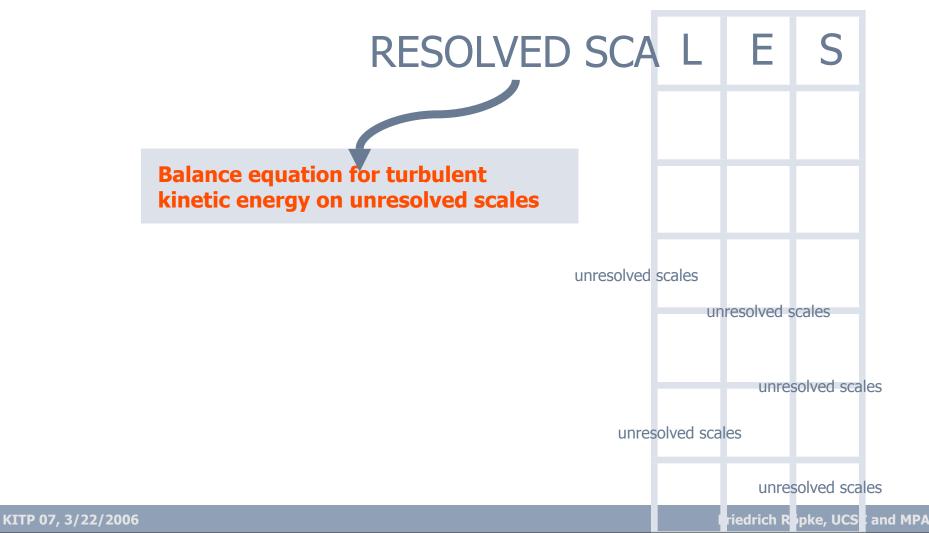
In very late stages: turbulence may affect burning microphysics → onset of distributed burning regime

- Large Eddy Simulation (LES) approach
- Subgrid-scale turbulence model (Niemeyer et al., 1995; Schmidt et al., 2005)

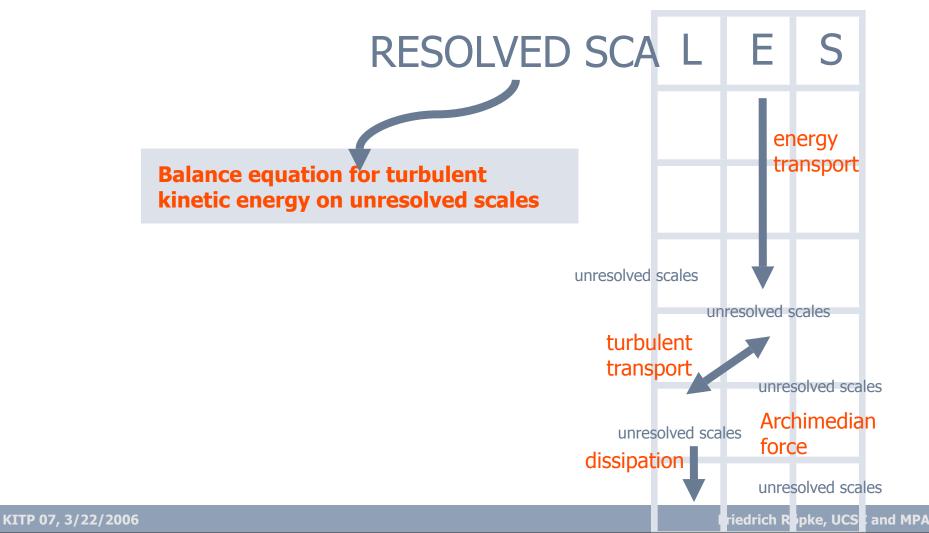


KITP 07, 3/22/2006

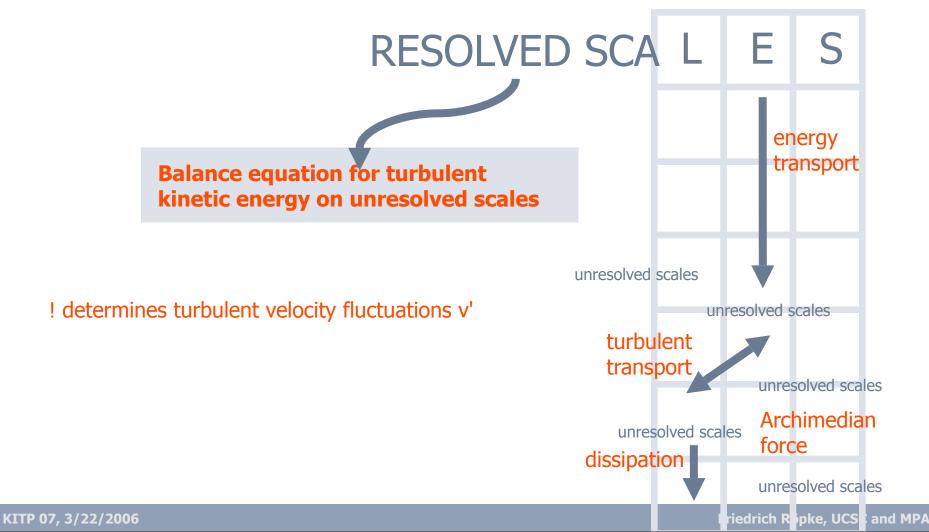
- Large Eddy Simulation (LES) approach
- Subgrid-scale turbulence model (Niemeyer et al., 1995; Schmidt et al., 2005)

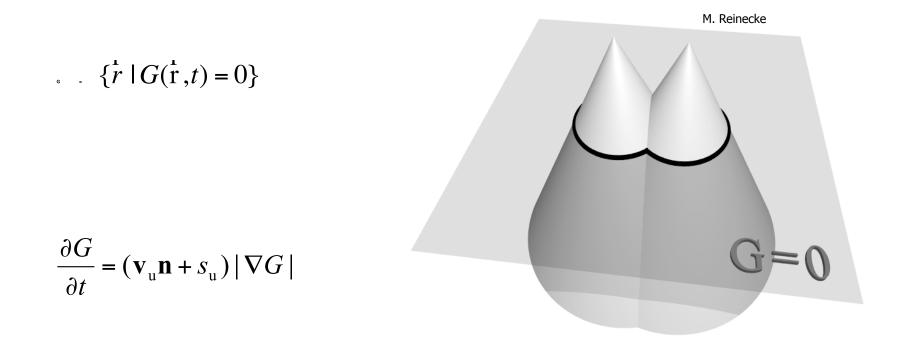


- Large Eddy Simulation (LES) approach
- Subgrid-scale turbulence model (Niemeyer et al., 1995; Schmidt et al., 2005)

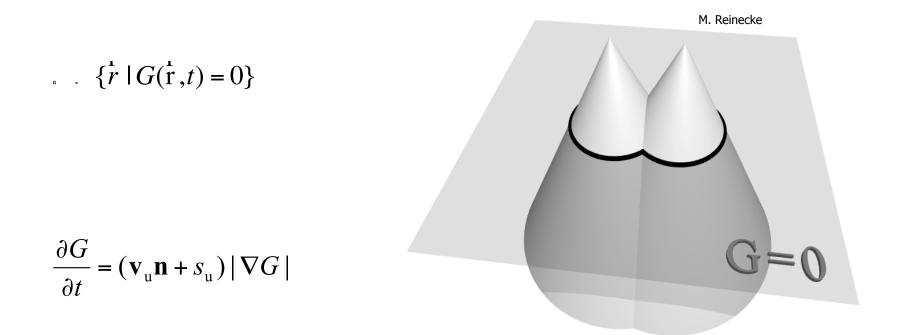


- Large Eddy Simulation (LES) approach
- Subgrid-scale turbulence model (Niemeyer et al., 1995; Schmidt et al., 2005)

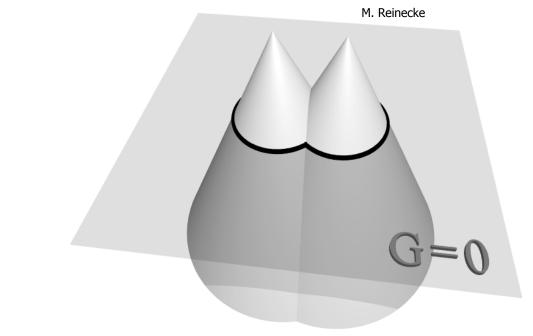




seen from scales of WD: flame is discontinuity between fuel and ashes



- seen from scales of WD: flame is discontinuity between fuel and ashes
- flame propagation via Level Set Method

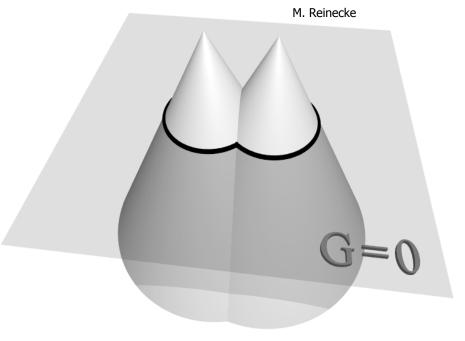


$$\frac{\partial G}{\partial t} = (\mathbf{v}_{\mathrm{u}}\mathbf{n} + s_{\mathrm{u}}) |\nabla G|$$

 $. . \{ r \mid G(r, t) = 0 \}$

- seen from scales of WD: flame is discontinuity between fuel and ashes
- flame propagation via Level Set Method
- associate flame front with

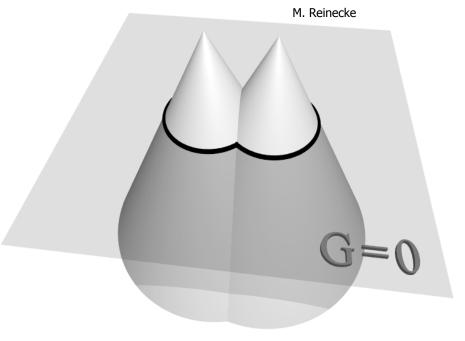
$$\ \ \, . \ \ \, \{ \overset{{}_{\mathbf{r}}}{r} \mid G(\overset{{}_{\mathbf{r}}}{r},t) = 0 \}$$



$$\frac{\partial G}{\partial t} = (\mathbf{v}_{\mathrm{u}}\mathbf{n} + s_{\mathrm{u}}) |\nabla G|$$

- seen from scales of WD: flame is discontinuity between fuel and ashes
- flame propagation via Level Set Method
- associate flame front with

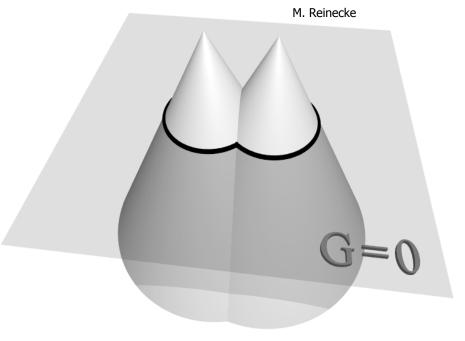
$$\ \ \, . \ \ \, \{ \overset{{}_{\mathbf{r}}}{r} \mid G(\overset{{}_{\mathbf{r}}}{r},t) = 0 \}$$



$$\frac{\partial G}{\partial t} = (\mathbf{v}_{\mathrm{u}}\mathbf{n} + s_{\mathrm{u}}) |\nabla G|$$

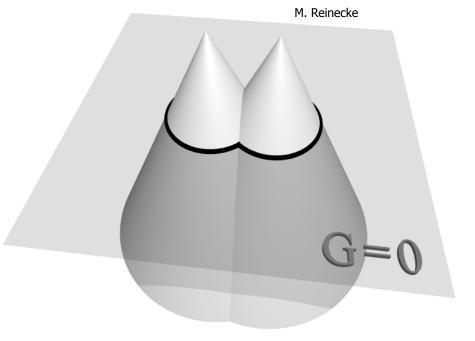
- seen from scales of WD: flame is discontinuity between fuel and ashes
- flame propagation via Level Set Method
- associate flame front with

$$\ \ \, . \ \ \, \{ \overset{{}_{\mathbf{r}}}{r} \mid G(\overset{{}_{\mathbf{r}}}{r},t) = 0 \}$$



$$\frac{\partial G}{\partial t} = (\mathbf{v}_{\mathrm{u}}\mathbf{n} + s_{\mathrm{u}}) |\nabla G|$$

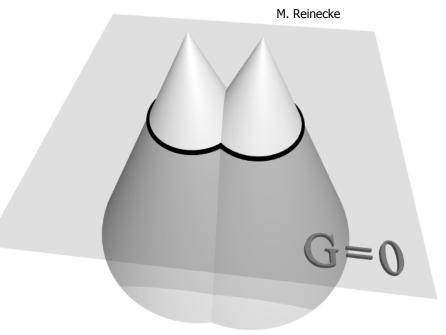
- seen from scales of WD: flame is discontinuity between fuel and ashes
- flame propagation via Level Set Method
- associate flame front with
 - $. . \{r \mid G(r,t) = 0\}$
- distance function G,



$$\frac{\partial G}{\partial t} = (\mathbf{v}_{\mathrm{u}}\mathbf{n} + s_{\mathrm{u}}) |\nabla G|$$

- seen from scales of WD: flame is discontinuity between fuel and ashes
- flame propagation via Level Set Method
- associate flame front with
 - $\ \ \, . \ \ \, \{ \overset{{}_{\mathbf{r}}}{r} \mid G(\overset{{}_{\mathbf{r}}}{r},t) = 0 \}$
- distance function G,
 G<0 in fuel, G>0 in ashes

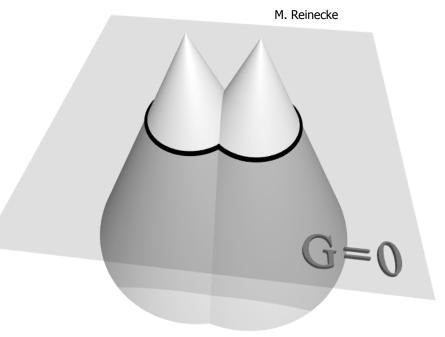
$$\frac{\partial G}{\partial t} = (\mathbf{v}_{\mathrm{u}}\mathbf{n} + s_{\mathrm{u}}) |\nabla G|$$



- seen from scales of WD: flame is discontinuity between fuel and ashes
- flame propagation via Level Set Method
- associate flame front with

 $\ \ \, . \ \ \, \{ \overset{{}_{\mathbf{r}}}{r} \mid G(\overset{{}_{\mathbf{r}}}{r},t) = 0 \}$

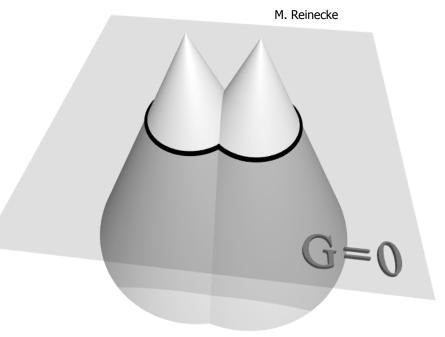
- distance function G,
 G<0 in fuel, G>0 in ashes
- equation of motion:



- seen from scales of WD: flame is discontinuity between fuel and ashes
- flame propagation via Level Set Method
- associate flame front with

 $\ \ \, . \ \ \, \{ \overset{{}_{\mathbf{r}}}{r} \mid G(\overset{{}_{\mathbf{r}}}{r},t) = 0 \}$

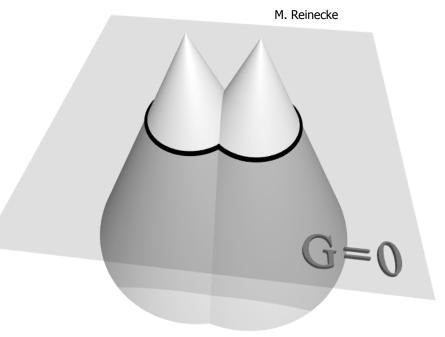
- distance function G,
 G<0 in fuel, G>0 in ashes
- equation of motion:



- seen from scales of WD: flame is discontinuity between fuel and ashes
- flame propagation via Level Set Method
- associate flame front with

 $\ \ \, . \ \ \, \{ \overset{{}_{\mathbf{r}}}{r} \mid G(\overset{{}_{\mathbf{r}}}{r},t) = 0 \}$

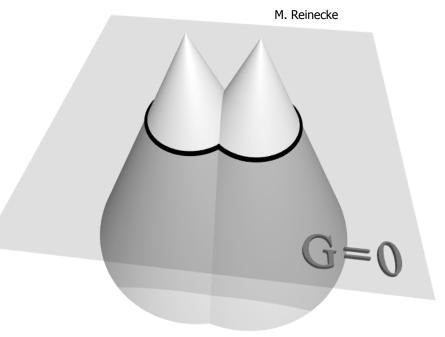
- distance function G,
 G<0 in fuel, G>0 in ashes
- equation of motion:



- seen from scales of WD: flame is discontinuity between fuel and ashes
- flame propagation via Level Set Method
- associate flame front with

 $\ \ \, . \ \ \, \{ \overset{{}_{\mathbf{r}}}{r} \mid G(\overset{{}_{\mathbf{r}}}{r},t) = 0 \}$

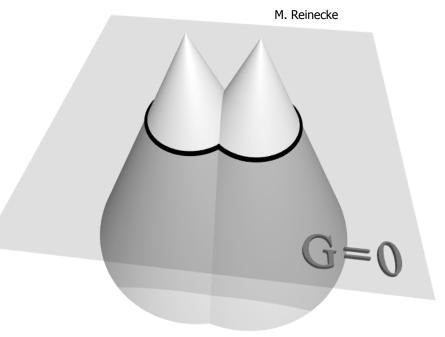
- distance function G,
 G<0 in fuel, G>0 in ashes
- equation of motion:



- seen from scales of WD: flame is discontinuity between fuel and ashes
- flame propagation via Level Set Method
- associate flame front with

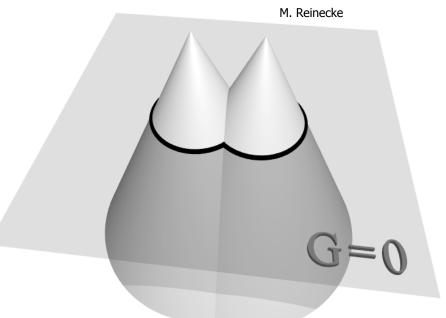
 $\ \ \, . \ \ \, \{ \overset{{}_{\mathbf{r}}}{r} \mid G(\overset{{}_{\mathbf{r}}}{r},t) = 0 \}$

- distance function G,
 G<0 in fuel, G>0 in ashes
- equation of motion:



- seen from scales of WD: flame is discontinuity between fuel and ashes
- flame propagation via Level Set Method
- associate flame front with
- distance function G,
 G<0 in fuel, G>0 in ashes
- equation of motion:

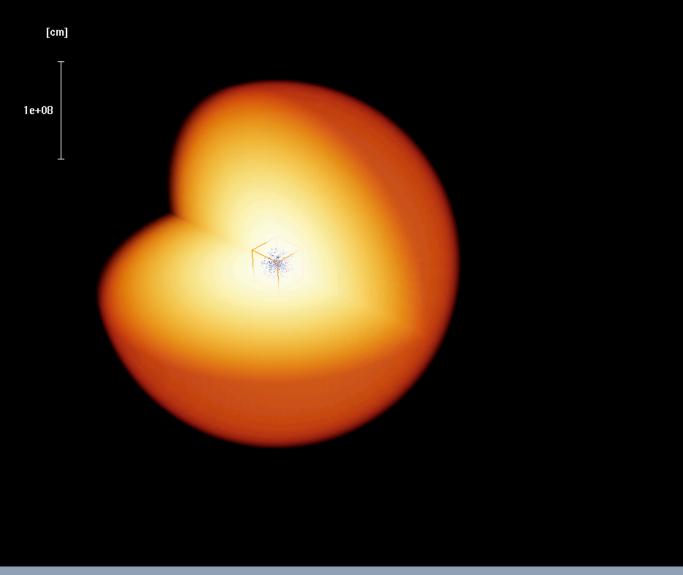
$$\frac{\partial G}{\partial t} = (\mathbf{v}_{\mathrm{u}}\mathbf{n} + s_{\mathrm{u}}) |\nabla G|$$



simplified description of burning: everything behind G=0 isosurface is nuclear ash; depending on fuel density at burning: intermediate mass elements ("Mg") or NSE (mixture of "Ni" and ⁴He)

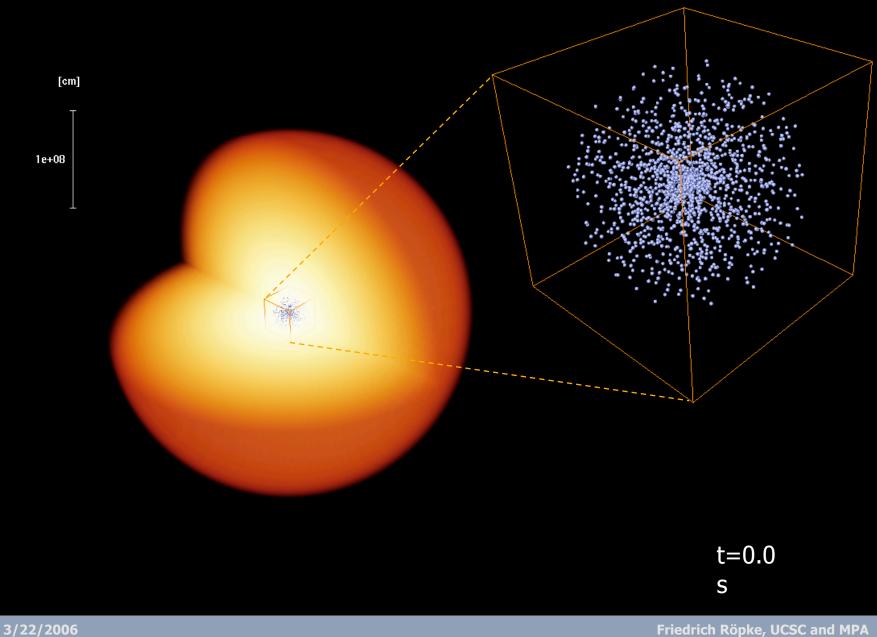
high-resolution model, improved subgrid-scale turbulence model, new burning law, multi-spot ignition:

1024³ computational cells, 500.000 CPU hours on IBM regatta

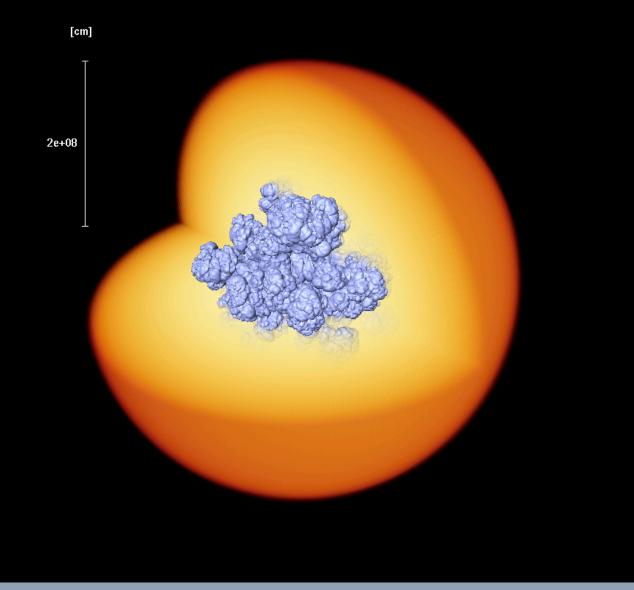


t=0.0

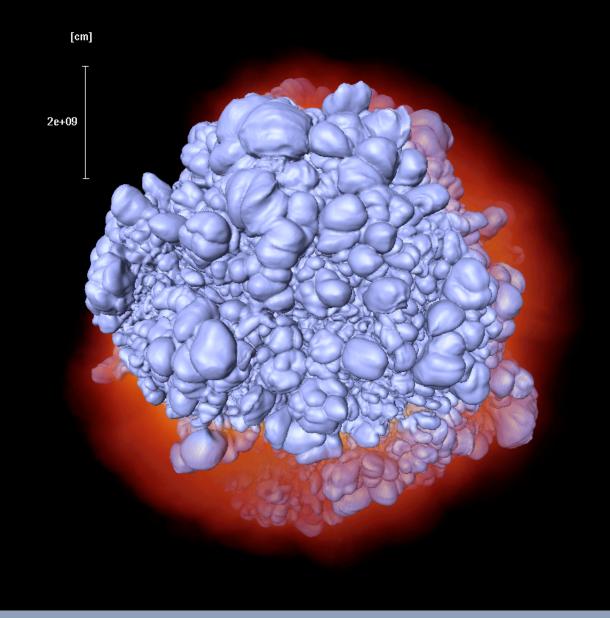
S



KITP 07, 3/22/2006





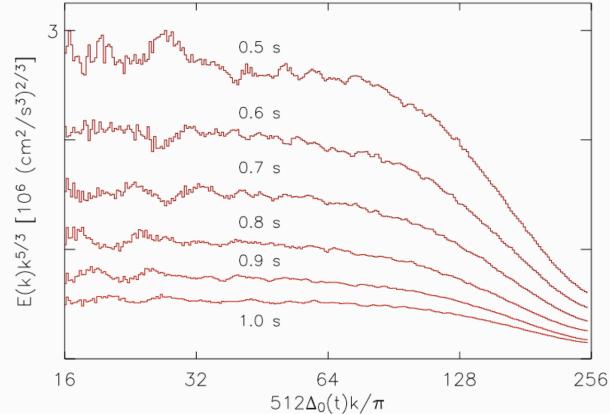






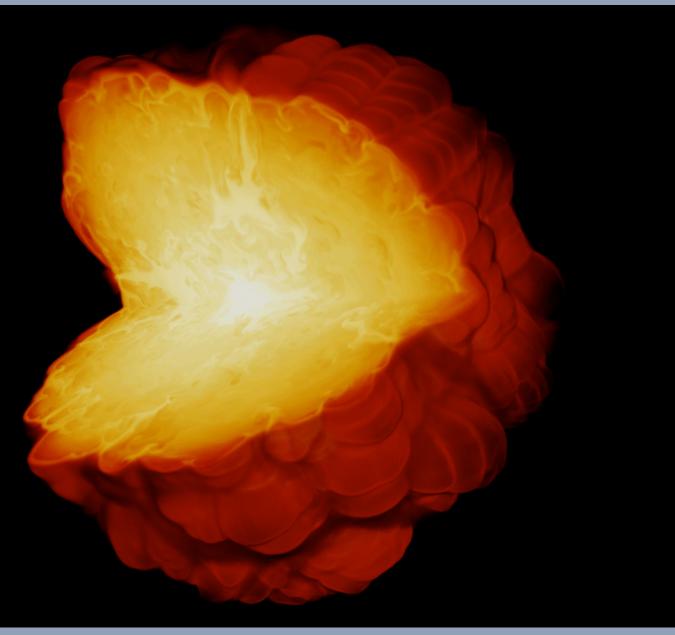
Turbulence on resolved scales

Spectrum normalized to Kolmogorov scaling (Schmidt et al. in prep., Röpke et al., subm.)



Turbulence following Kolmogorov scaling found on resolved scales ! LES ansatz justified

Results

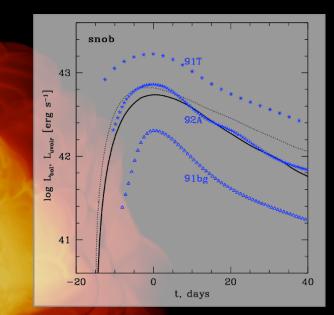


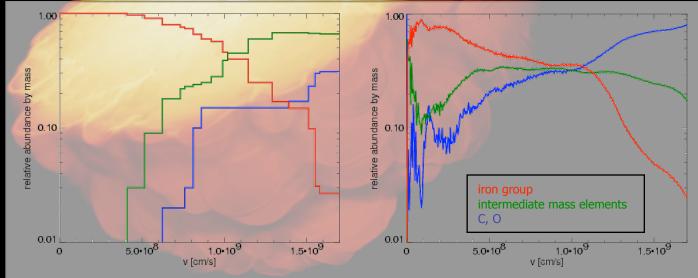
Results

- asymptotic kinetic energy: 0.81 foe
- hydro: 0.61 M- of iron group elements,
 0.43 M- of intermediate mass elements
- postprocessing step (Travaglio et al., 2004) with ~150 000 tracer particles in full-star simulations ! 0.33 M- of ⁵⁶Ni

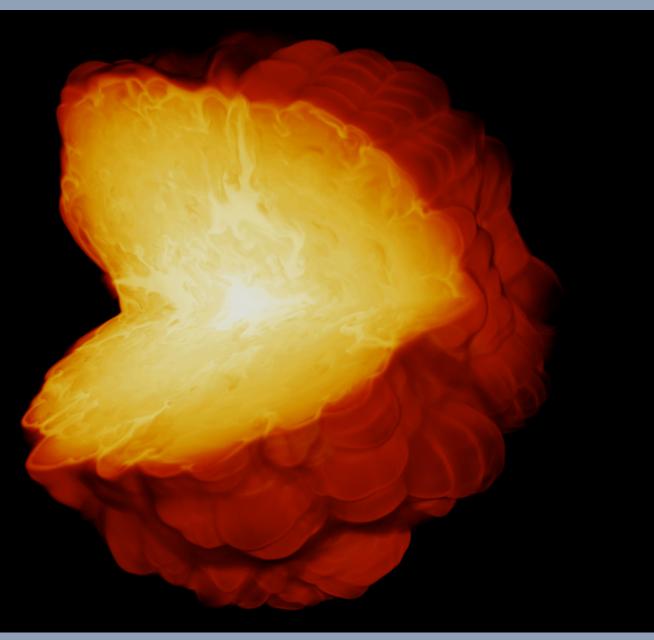
Results

- asymptotic kinetic energy: 0.81 foe
- hydro: 0.61 M- of iron group elements,
 0.43 M- of intermediate mass elements
- postprocessing step (Travaglio et al., 2004) with ~150 000 tracer particles in full-star simulations ! 0.33 M- of ⁵⁶Ni





Deflagration model



Deflagration model

Successes

- yields explosion
- based on fundamental physical principles
- no tunable parameters except for initial conditions (flame ignition configuration)
- reasonable agreement with weaker
 examples of normal SNe Ia

Deflagration model

Successes

- yields explosion
- based on fundamental physical principles
- no tunable parameters except for initial conditions (flame ignition configuration)
- reasonable agreement with weaker
 examples of normal SNe Ia

Shortcomings

- do not reproduce brighter SNe Ia (>0.7 M- of ⁵⁶Ni)
- composition of outer layers in disagreement with those expected for brighter SNe Ia

Deflagration model

Successes

- yields explosion
- based on fundamental physical principles
- no tunable parameters except for initial conditions (flame ignition configuration)
- reasonable agreement with weaker
 examples of normal SNe Ia

Shortcomings

- do not reproduce brighter SNe Ia (>0.7 M- of ⁵⁶Ni)
- composition of outer layers in disagreement with those expected for brighter SNe Ia

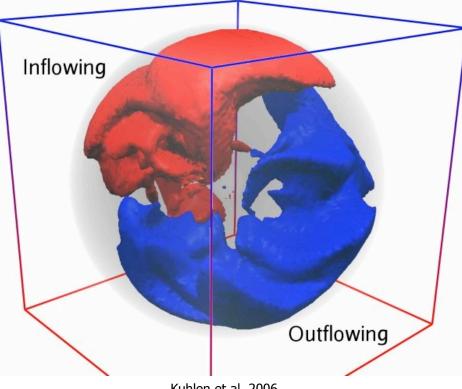
Questions

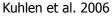
- Do pure deflagrations account for a sub-class of SNe Ia (Phillips et al., 2006)?
- Do they represent the first (and for some objects dominant) building block of an extended model?

Off-center ignition model

Motivation:

 pre-igntion convection may cause dipole flow (Kuhlen et al. 2006)
 ! lop-sided ignition?





conceivable initial flame configurations: sphere (Calder et al., 2004), perturbed sphere, perturbed teardrop-like shape, two-sided configurations (Röpke et al. 2007, ApJ in print: ~20 2D simulations, 6 3D simulations testing the parameter space)

Off-center ignition model: example

Gravitationally Confined Detonations?

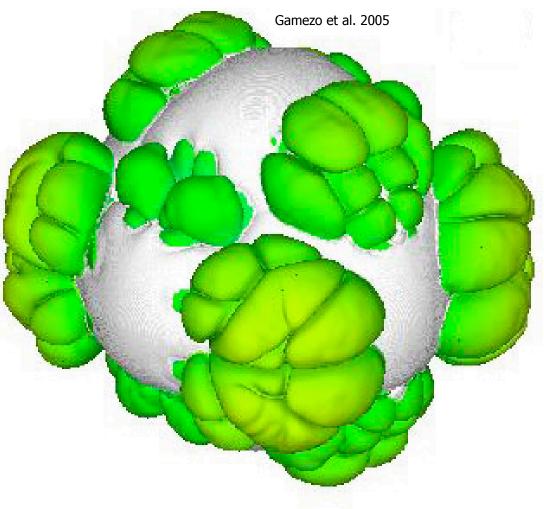
GCD scenario (Plewa et al., 2004): colliding ash compresses fuel material at the surface of the WD and triggers detonation
analysis of conditions in collision region (Röpke et al., 2007 ApJ in print):
deciding parameter: energy release in deflagration phase ! depends on ignition location/shape and flame model (!)
! GCD possible, but conditions for detonation only reached in specially tuned 2D simulations, no detonation found in 3D simulations

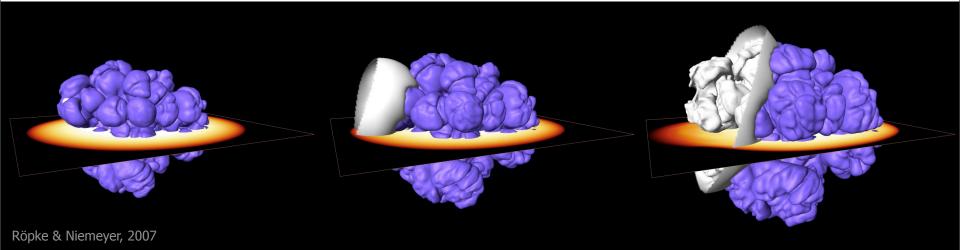
! GCD not a robust mechanism for SNe Ia, if working would produce very bright events

Delayed detonation model

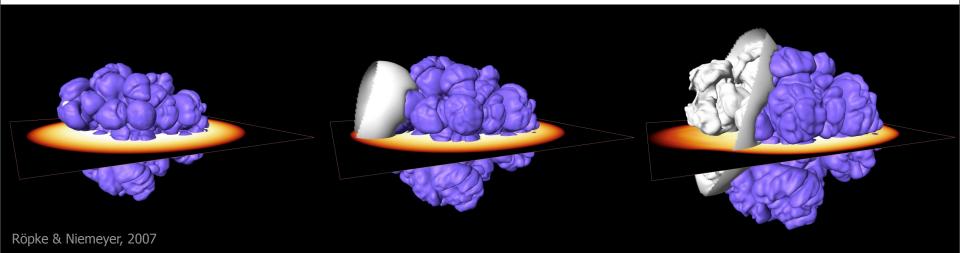
Idea:

- transition (DDT) to detonation after deflagration phase (Khokhlov, 1991)
- supersonic detonation front burns parts of remaining fuel

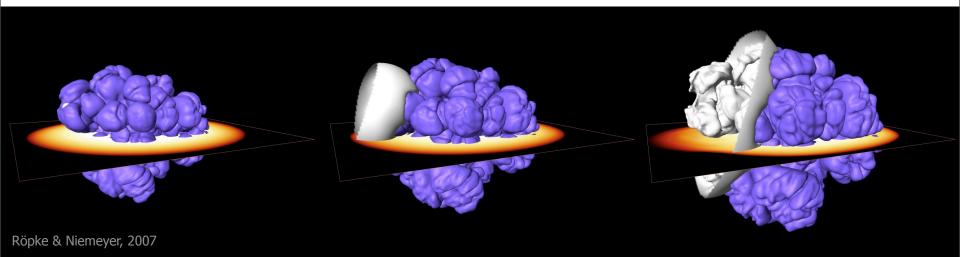




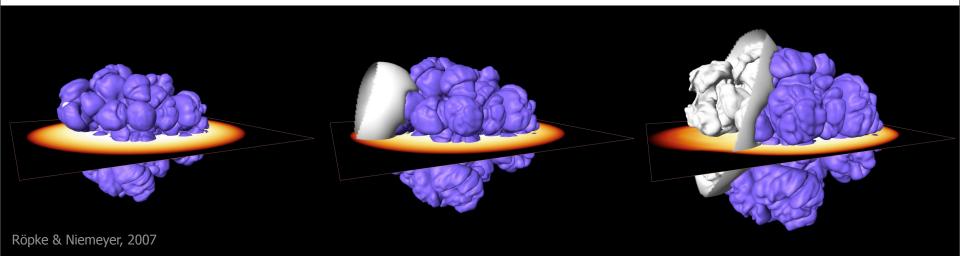
DDT mechanism unknown in astrophysical context (e.g. Niemeyer 1999, Oran & Gamezo, 2006)



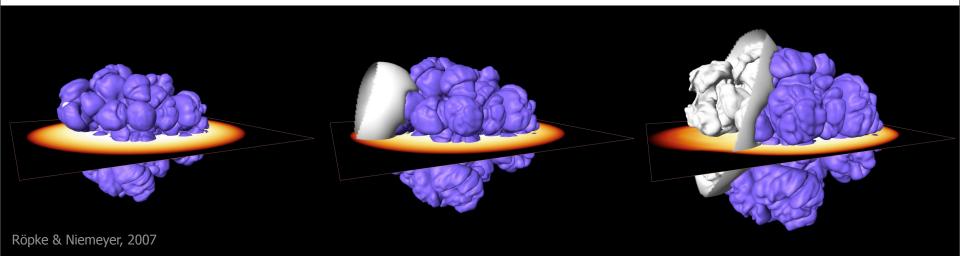
- DDT mechanism unknown in astrophysical context (e.g. Niemeyer 1999, Oran & Gamezo, 2006)
- detonation cannot cross even tiny regions of ash (Maier & Niemeyer 2006) ! pockets of unburnt material may remain, needs to burn around complicated deflagration structure



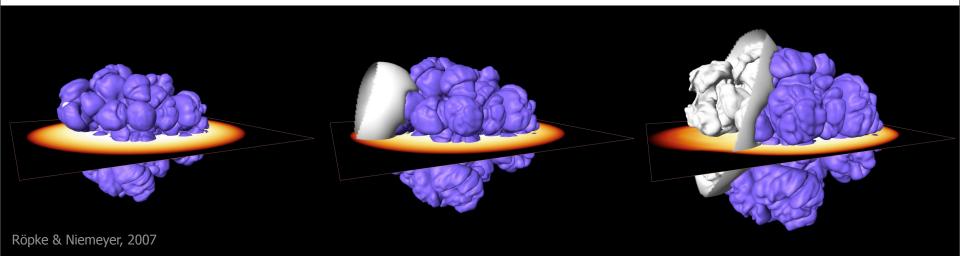
- DDT mechanism unknown in astrophysical context (e.g. Niemeyer 1999, Oran & Gamezo, 2006)
- detonation cannot cross even tiny regions of ash (Maier & Niemeyer 2006) ! pockets of unburnt material may remain, needs to burn around complicated deflagration structure
- competition with expansion: does it reach far side when triggered off-center?



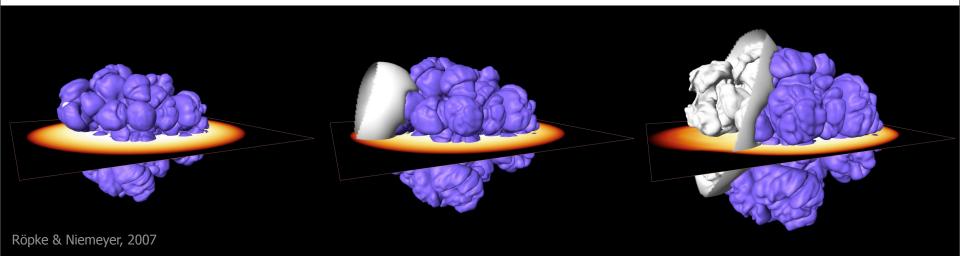
- DDT mechanism unknown in astrophysical context (e.g. Niemeyer 1999, Oran & Gamezo, 2006)
- detonation cannot cross even tiny regions of ash (Maier & Niemeyer 2006) ! pockets of unburnt material may remain, needs to burn around complicated deflagration structure
- competition with expansion: does it reach far side when triggered off-center?



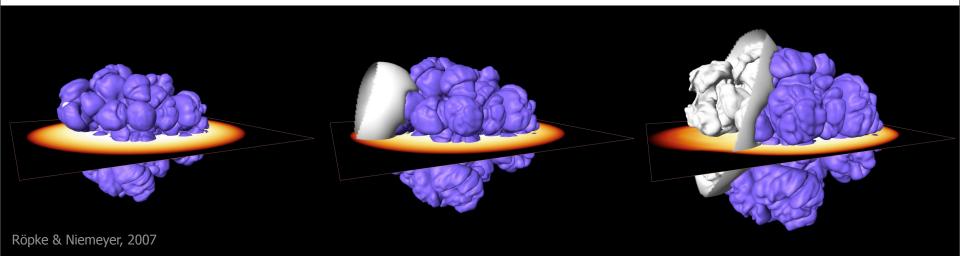
- DDT mechanism unknown in astrophysical context (e.g. Niemeyer 1999, Oran & Gamezo, 2006)
- detonation cannot cross even tiny regions of ash (Maier & Niemeyer 2006) ! pockets of unburnt material may remain, needs to burn around complicated deflagration structure
- competition with expansion: does it reach far side when triggered off-center?



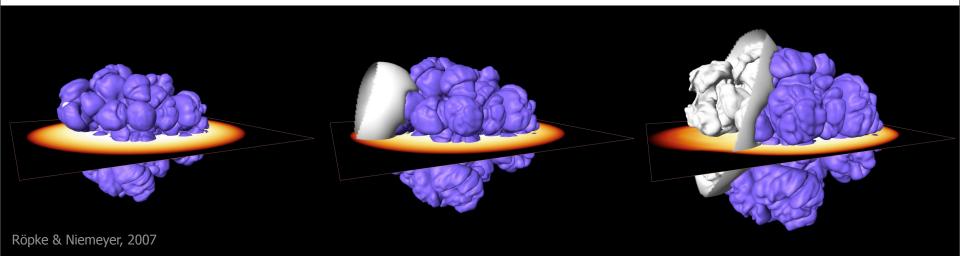
- DDT mechanism unknown in astrophysical context (e.g. Niemeyer 1999, Oran & Gamezo, 2006)
- detonation cannot cross even tiny regions of ash (Maier & Niemeyer 2006) ! pockets of unburnt material may remain, needs to burn around complicated deflagration structure
- competition with expansion: does it reach far side when triggered off-center?



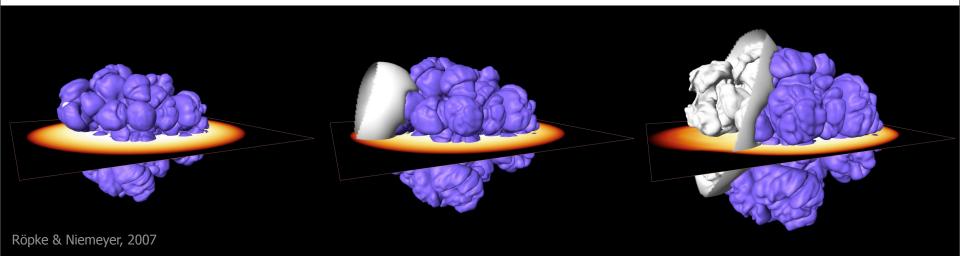
- DDT mechanism unknown in astrophysical context (e.g. Niemeyer 1999, Oran & Gamezo, 2006)
- detonation cannot cross even tiny regions of ash (Maier & Niemeyer 2006) ! pockets of unburnt material may remain, needs to burn around complicated deflagration structure
- competition with expansion: does it reach far side when triggered off-center?



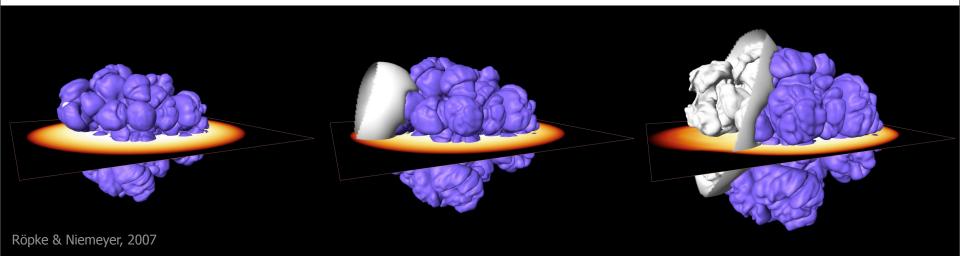
- DDT mechanism unknown in astrophysical context (e.g. Niemeyer 1999, Oran & Gamezo, 2006)
- detonation cannot cross even tiny regions of ash (Maier & Niemeyer 2006) ! pockets of unburnt material may remain, needs to burn around complicated deflagration structure
- competition with expansion: does it reach far side when triggered off-center?



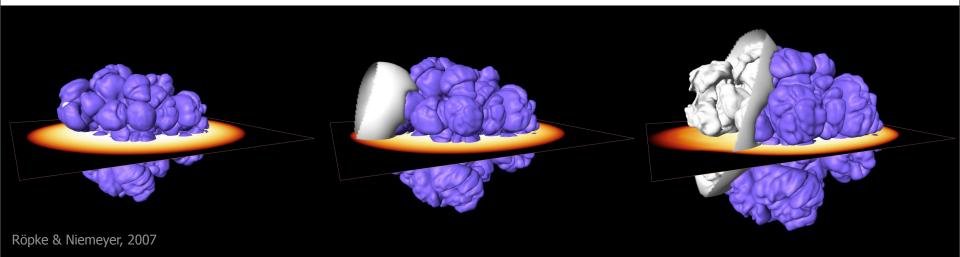
- DDT mechanism unknown in astrophysical context (e.g. Niemeyer 1999, Oran & Gamezo, 2006)
- detonation cannot cross even tiny regions of ash (Maier & Niemeyer 2006) ! pockets of unburnt material may remain, needs to burn around complicated deflagration structure
- competition with expansion: does it reach far side when triggered off-center?



- DDT mechanism unknown in astrophysical context (e.g. Niemeyer 1999, Oran & Gamezo, 2006)
- detonation cannot cross even tiny regions of ash (Maier & Niemeyer 2006) ! pockets of unburnt material may remain, needs to burn around complicated deflagration structure
- competition with expansion: does it reach far side when triggered off-center?

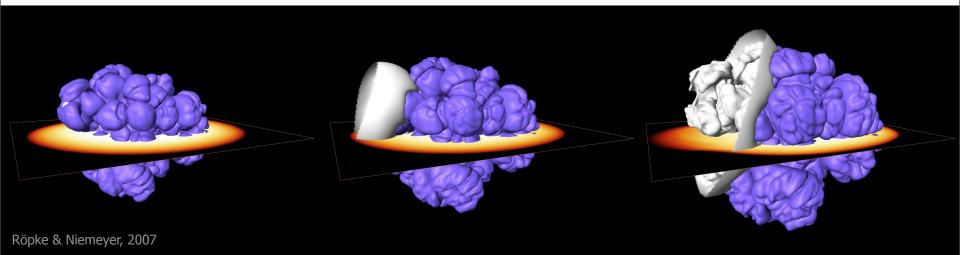


- DDT mechanism unknown in astrophysical context (e.g. Niemeyer 1999, Oran & Gamezo, 2006)
- detonation cannot cross even tiny regions of ash (Maier & Niemeyer 2006) ! pockets of unburnt material may remain, needs to burn around complicated deflagration structure
- competition with expansion: does it reach far side when triggered off-center?



Parametrizations (in 3D simulations):

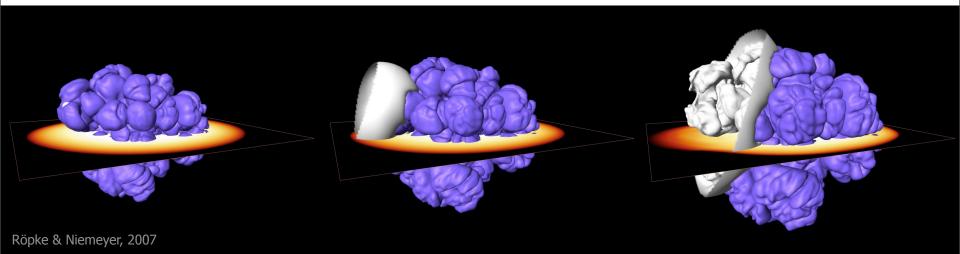
- DDT mechanism unknown in astrophysical context (e.g. Niemeyer 1999, Oran & Gamezo, 2006)
- detonation cannot cross even tiny regions of ash (Maier & Niemeyer 2006) ! pockets of unburnt material may remain, needs to burn around complicated deflagration structure
- competition with expansion: does it reach far side when triggered off-center?



Parametrizations (in 3D simulations):

arbitrarily prescribe position and time for DDT (Gamezo et al. 2005)

- DDT mechanism unknown in astrophysical context (e.g. Niemeyer 1999, Oran & Gamezo, 2006)
- detonation cannot cross even tiny regions of ash (Maier & Niemeyer 2006) ! pockets of unburnt material may remain, needs to burn around complicated deflagration structure
- competition with expansion: does it reach far side when triggered off-center?



Parametrizations (in 3D simulations):

- arbitrarily prescribe position and time for DDT (Gamezo et al. 2005)
- DDT once deflagration flame enters distributed burning regime (Golombeck & Niemeyer 2005)

Delayed detonation model: example

Delayed detonation model

- varying the number of ignition kernels of the deflagration flame shifts emphasis from deflagration to detonation phase
- elegant way to reproduce range of observations of SNe Ia (Röpke & Niemeyer, 2007)

| ignition configuration | 5 | 20 | 800 |
|----------------------------------|------|------|------|
| E _{kin,asympt} [foe] | 1.5 | 1.2 | 1.0 |
| M(NSE) [M-] | 1.14 | 0.83 | 0.64 |
| M(IME) [M-] | 0.22 | 0.44 | 0.55 |

Niemeyer & Woosley (1997) hypothesis: DDT at onset of distributed burning regime

- Niemeyer & Woosley (1997) hypothesis: DDT at onset of distributed burning regime
- only instance of drastic change in flame properties

| LIMITING | THRESHOLD | FOR | TURBULENT | VELOCITY | u'(L) | AT | |
|----------|-----------|-----|------------|----------|-------|----|--|
| GIVEN | | | | | | | |
| | DENSITY | AND | FUEL COMPO | SITION | | | |

| u'(L) (cm s-1) | $(\times 10^7 \text{ g cm}^{-3})$ | $X(^{12}C)$ | X(¹⁶ O) |
|----------------------------|-----------------------------------|-------------|---------------------|
| >0.5 × 10 ⁸ | 2.3 | 0.5 | 0.5 |
| >0.6 × 10 ⁸ | 1.3 | 0.5 | 0.5 |
| >0.8 × 10 ⁸ | 0.8 | 0.5 | 0.5 |
| $> 0.25 \times 10^8 \dots$ | 2.3 | 0.75 | 0.25 |
| >0.3 × 10 ⁸ | 1.3 | 0.75 | 0.25 |
| >0.4 × 10 ⁸ | 0.8 | 0.75 | 0.25 |
| > 0.9 × 10 ⁸ | 2.3 | 0.25 | 0.75 |
| >10 ⁸ | 1.3 | 0.25 | 0.75 |
| >10 ⁸ | 0.8 | 0.25 | 0.75 |

- Niemeyer & Woosley (1997) hypothesis: DDT at onset of distributed burning regime
- only instance of drastic change in flame properties

| u'(L) (cm s ⁻¹) | $(\times 10^7 \text{ g cm}^{-3})$ | <i>X</i> (¹² C) | X(¹⁶ O) | |
|--------------------------------|-----------------------------------|-----------------------------|---------------------|--|
| (0113) | (~10 g th) | A(C) | A(0) | |
| >0.5 × 10 ⁸ | 2.3 | 0.5 | 0.5 | |
| >0.6 × 10 ⁸ | 1.3 | 0.5 | 0.5 | |
| >0.8 × 10 ⁸ | 0.8 | 0.5 | 0.5 | |
| > 0.25 × 10 ⁸ | 2.3 | 0.75 | 0.25 | |
| >0.3 × 10 ⁸ | 1.3 | 0.75 | 0.25 | |
| >0.4 × 10 ⁸ | 0.8 | 0.75 | 0.25 | |
| > 0.9 × 10 ⁸ | 2.3 | 0.25 | 0.75 | |
| >10 ⁸ | 1.3 | 0.25 | 0.75 | |
| >10 ⁸ | 0.8 | 0.25 | 0.75 | |

Limiting Threshold for Turbulent Velocity u'(L) at Given Density and Fuel Composition

- Niemeyer & Woosley (1997) hypothesis: DDT at onset of distributed burning regime
- only instance of drastic change in flame properties

| u'(L) (cm s ⁻¹) | $(\times 10^7 \text{ g cm}^{-3})$ | <i>X</i> (¹² C) | X(¹⁶ O) | |
|--------------------------------|-----------------------------------|-----------------------------|---------------------|--|
| (0113) | (~10 g th) | A(C) | A(0) | |
| >0.5 × 10 ⁸ | 2.3 | 0.5 | 0.5 | |
| >0.6 × 10 ⁸ | 1.3 | 0.5 | 0.5 | |
| >0.8 × 10 ⁸ | 0.8 | 0.5 | 0.5 | |
| > 0.25 × 10 ⁸ | 2.3 | 0.75 | 0.25 | |
| >0.3 × 10 ⁸ | 1.3 | 0.75 | 0.25 | |
| >0.4 × 10 ⁸ | 0.8 | 0.75 | 0.25 | |
| > 0.9 × 10 ⁸ | 2.3 | 0.25 | 0.75 | |
| >10 ⁸ | 1.3 | 0.25 | 0.75 | |
| >10 ⁸ | 0.8 | 0.25 | 0.75 | |

Limiting Threshold for Turbulent Velocity u'(L) at Given Density and Fuel Composition

- Niemeyer & Woosley (1997) hypothesis: DDT at onset of distributed burning regime
- only instance of drastic change in flame properties
- occurs at $\rho_{fuel} \sim 10^7$ g cm⁻³ ! for this transition density best fits obtained in one-dimensional delayed detonation models

| | TY AND FUEL COMPO | DSITION | |
|--------------------------------|-----------------------------------|-------------|---------------------|
| u'(L) (cm s ⁻¹) | $(\times 10^7 \text{ g cm}^{-3})$ | $X(^{12}C)$ | X(¹⁶ O) |
| >0.5 × 10 ⁸ | 2.3 | 0.5 | 0.5 |
| >0.6 × 10 ⁸ | 1.3 | 0.5 | 0.5 |
| >0.8 × 10 ⁸ | 0.8 | 0.5 | 0.5 |
| > 0.25 × 10 ⁸ | 2.3 | 0.75 | 0.25 |
| >0.3 × 10 ⁸ | 1.3 | 0.75 | 0.25 |
| >0.4 × 10 ⁸ | 0.8 | 0.75 | 0.25 |
| > 0.9 × 10 ⁸ | 2.3 | 0.25 | 0.75 |
| >10 ⁸ | 1.3 | 0.25 | 0.75 |
| >10 ⁸ | 0.8 | 0.25 | 0.75 |

TABLE 1 Limiting Threshold for Turbulent Velocity u'(L) at

- Niemeyer & Woosley (1997) hypothesis: DDT at onset of distributed burning regime
- only instance of drastic change in flame properties
- analysis by
 Lisewski et al.(2000): claim

| LIMITING | THRESHOLD | FOR | TURBULENT | VELOCITY | u'(L) | AT | |
|----------|-----------|-----|------------|----------|-------|----|--|
| GIVEN | | | | | | | |
| | DENSITY | AND | FUEL COMPO | SITION | | | |

| | $(\times 10^7 \text{ g cm}^{-3})$ | $X(^{12}C)$ | X(¹⁶ O) |
|--------------------------|-----------------------------------|-------------|---------------------|
| >0.5 × 10 ⁸ | 2.3 | 0.5 | 0.5 |
| >0.6 × 10 ⁸ | 1.3 | 0.5 | 0.5 |
| >0.8 × 10 ⁸ | 0.8 | 0.5 | 0.5 |
| > 0.25 × 10 ⁸ | 2.3 | 0.75 | 0.25 |
| >0.3 × 10 ⁸ | 1.3 | 0.75 | 0.25 |
| >0.4 × 10 ⁸ | 0.8 | 0.75 | 0.25 |
| > 0.9 × 10 ⁸ | 2.3 | 0.25 | 0.75 |
| >10 ⁸ | 1.3 | 0.25 | 0.75 |
| >10 ⁸ | 0.8 | 0.25 | 0.75 |

- Niemeyer & Woosley (1997) hypothesis: DDT at onset of distributed burning regime
- only instance of drastic change in flame properties
- analysis by
 Lisewski et al.(2000): claim

| LIMITING | THRESHOLD | FOR | TURBULENT | VELOCITY | u'(L) | AT | |
|----------|-----------|-----|------------|----------|-------|----|--|
| GIVEN | | | | | | | |
| | DENSITY | AND | FUEL COMPO | SITION | | | |

| | $(\times 10^7 \text{ g cm}^{-3})$ | $X(^{12}C)$ | X(¹⁶ O) |
|--------------------------|-----------------------------------|-------------|---------------------|
| >0.5 × 10 ⁸ | 2.3 | 0.5 | 0.5 |
| >0.6 × 10 ⁸ | 1.3 | 0.5 | 0.5 |
| >0.8 × 10 ⁸ | 0.8 | 0.5 | 0.5 |
| > 0.25 × 10 ⁸ | 2.3 | 0.75 | 0.25 |
| >0.3 × 10 ⁸ | 1.3 | 0.75 | 0.25 |
| >0.4 × 10 ⁸ | 0.8 | 0.75 | 0.25 |
| > 0.9 × 10 ⁸ | 2.3 | 0.25 | 0.75 |
| >10 ⁸ | 1.3 | 0.25 | 0.75 |
| >10 ⁸ | 0.8 | 0.25 | 0.75 |

- Niemeyer & Woosley (1997) hypothesis: DDT at onset of distributed burning regime
- only instance of drastic change in flame properties
- analysis by
 Lisewski et al.(2000): claim

| LIMITING | THRESHOLD | FOR | TURBULENT | VELOCITY | u'(L) | AT | |
|----------|-----------|-----|------------|----------|-------|----|--|
| GIVEN | | | | | | | |
| | DENSITY | AND | FUEL COMPO | SITION | | | |

| | $(\times 10^7 \text{ g cm}^{-3})$ | $X(^{12}C)$ | X(¹⁶ O) |
|--------------------------|-----------------------------------|-------------|---------------------|
| >0.5 × 10 ⁸ | 2.3 | 0.5 | 0.5 |
| >0.6 × 10 ⁸ | 1.3 | 0.5 | 0.5 |
| >0.8 × 10 ⁸ | 0.8 | 0.5 | 0.5 |
| > 0.25 × 10 ⁸ | 2.3 | 0.75 | 0.25 |
| >0.3 × 10 ⁸ | 1.3 | 0.75 | 0.25 |
| >0.4 × 10 ⁸ | 0.8 | 0.75 | 0.25 |
| > 0.9 × 10 ⁸ | 2.3 | 0.25 | 0.75 |
| >10 ⁸ | 1.3 | 0.25 | 0.75 |
| >10 ⁸ | 0.8 | 0.25 | 0.75 |

- Niemeyer & Woosley (1997) hypothesis: DDT at onset of distributed burning regime
- only instance of drastic change in flame properties
- analysis by
 Lisewski et al.(2000): claim

| LIMITING | THRESHOLD | FOR | TURBULENT | VELOCITY | u'(L) | AT | |
|------------------------------|-----------|-----|-----------|----------|-------|----|--|
| GIVEN | | | | | | | |
| DENSITY AND FUEL COMPOSITION | | | | | | | |

| | $(\times 10^7 \text{ g cm}^{-3})$ | $X(^{12}C)$ | X(¹⁶ O) |
|--------------------------|-----------------------------------|-------------|---------------------|
| >0.5 × 10 ⁸ | 2.3 | 0.5 | 0.5 |
| >0.6 × 10 ⁸ | 1.3 | 0.5 | 0.5 |
| >0.8 × 10 ⁸ | 0.8 | 0.5 | 0.5 |
| > 0.25 × 10 ⁸ | 2.3 | 0.75 | 0.25 |
| >0.3 × 10 ⁸ | 1.3 | 0.75 | 0.25 |
| >0.4 × 10 ⁸ | 0.8 | 0.75 | 0.25 |
| > 0.9 × 10 ⁸ | 2.3 | 0.25 | 0.75 |
| >10 ⁸ | 1.3 | 0.25 | 0.75 |
| >10 ⁸ | 0.8 | 0.25 | 0.75 |

- Niemeyer & Woosley (1997) hypothesis: DDT at onset of distributed burning regime
- only instance of drastic change in flame properties
- analysis by
 Lisewski et al.(2000): claim

| LIMITING | THRESHOLD | FOR | TURBULENT | VELOCITY | u'(L) | AT | |
|------------------------------|-----------|-----|-----------|----------|-------|----|--|
| GIVEN | | | | | | | |
| DENSITY AND FUEL COMPOSITION | | | | | | | |

| | $(\times 10^7 \text{ g cm}^{-3})$ | $X(^{12}C)$ | X(¹⁶ O) |
|--------------------------|-----------------------------------|-------------|---------------------|
| >0.5 × 10 ⁸ | 2.3 | 0.5 | 0.5 |
| >0.6 × 10 ⁸ | 1.3 | 0.5 | 0.5 |
| >0.8 × 10 ⁸ | 0.8 | 0.5 | 0.5 |
| > 0.25 × 10 ⁸ | 2.3 | 0.75 | 0.25 |
| >0.3 × 10 ⁸ | 1.3 | 0.75 | 0.25 |
| >0.4 × 10 ⁸ | 0.8 | 0.75 | 0.25 |
| > 0.9 × 10 ⁸ | 2.3 | 0.25 | 0.75 |
| >10 ⁸ | 1.3 | 0.25 | 0.75 |
| >10 ⁸ | 0.8 | 0.25 | 0.75 |

- Niemeyer & Woosley (1997) hypothesis: DDT at onset of distributed burning regime
- only instance of drastic change in flame properties
- analysis by
 Lisewski et al.(2000): claim

| LIMITING | THRESHOLD | FOR | TURBULENT | VELOCITY | u'(L) | AT | |
|------------------------------|-----------|-----|-----------|----------|-------|----|--|
| GIVEN | | | | | | | |
| DENSITY AND FUEL COMPOSITION | | | | | | | |

| | $(\times 10^7 \text{ g cm}^{-3})$ | $X(^{12}C)$ | X(¹⁶ O) |
|--------------------------|-----------------------------------|-------------|---------------------|
| >0.5 × 10 ⁸ | 2.3 | 0.5 | 0.5 |
| >0.6 × 10 ⁸ | 1.3 | 0.5 | 0.5 |
| >0.8 × 10 ⁸ | 0.8 | 0.5 | 0.5 |
| > 0.25 × 10 ⁸ | 2.3 | 0.75 | 0.25 |
| >0.3 × 10 ⁸ | 1.3 | 0.75 | 0.25 |
| >0.4 × 10 ⁸ | 0.8 | 0.75 | 0.25 |
| > 0.9 × 10 ⁸ | 2.3 | 0.25 | 0.75 |
| >10 ⁸ | 1.3 | 0.25 | 0.75 |
| >10 ⁸ | 0.8 | 0.25 | 0.75 |

- Niemeyer & Woosley (1997) hypothesis: DDT at onset of distributed burning regime
- only instance of drastic change in flame properties
- analysis by
 Lisewski et al.(2000): claim

| LIMITING | THRESHOLD | FOR | TURBULENT | VELOCITY | u'(L) | AT | |
|------------------------------|-----------|-----|-----------|----------|-------|----|--|
| GIVEN | | | | | | | |
| DENSITY AND FUEL COMPOSITION | | | | | | | |

| | $(\times 10^7 \text{ g cm}^{-3})$ | $X(^{12}C)$ | X(¹⁶ O) |
|--------------------------|-----------------------------------|-------------|---------------------|
| >0.5 × 10 ⁸ | 2.3 | 0.5 | 0.5 |
| >0.6 × 10 ⁸ | 1.3 | 0.5 | 0.5 |
| >0.8 × 10 ⁸ | 0.8 | 0.5 | 0.5 |
| > 0.25 × 10 ⁸ | 2.3 | 0.75 | 0.25 |
| >0.3 × 10 ⁸ | 1.3 | 0.75 | 0.25 |
| >0.4 × 10 ⁸ | 0.8 | 0.75 | 0.25 |
| > 0.9 × 10 ⁸ | 2.3 | 0.25 | 0.75 |
| >10 ⁸ | 1.3 | 0.25 | 0.75 |
| >10 ⁸ | 0.8 | 0.25 | 0.75 |

 $> 0.25 \times 10^8 \dots$

 $>0.3 \times 10^8$

>0.4 × 10⁸

 $> 0.9 \times 10^8 \dots$

>10⁸

>10⁸

- Niemeyer & Woosley (1997) hypothesis: DDT at onset of distributed burning regime
- only instance of drastic change in flame properties
- analysis by
 Lisewski et al.(2000): claim

| GIVEN DENSITY AND FUEL COMPOSITION | | | | | |
|---------------------------------------|-----------------------------------|-----------------------------|---------------------|--|--|
| u'(L) (cm s ⁻¹) | $(\times 10^7 \text{ g cm}^{-3})$ | <i>X</i> (¹² C) | X(¹⁶ O) | | |
| >0.5 × 10 ⁸ | 2.3 | 0.5 | 0.5 | | |
| >0.6 × 10 ⁸ | 1.3 | 0.5 | 0.5 | | |
| >0.8 × 10 ⁸ | 0.8 | 0.5 | 0.5 | | |

2.3

1.3

0.8

2.3

1.3

0.8

0.75

0.75

0.75

0.25

0.25

0.25

TABLE 1 Limiting Threshold for Turbulent Velocity u'(L) at

needs updated analysis

| KITP 07, 3/ | /22/ | 2006 | |
|-------------|------|------|--|
|-------------|------|------|--|

0.25

0.25

0.25

0.75

0.75

0.75

Deflagration-to-Detonation Transitions?

- Niemeyer & Woosley (1997) hypothesis: DDT at onset of distributed burning regime
- only instance of drastic change in flame properties
- occurs at $\rho_{fuel} \sim 10^7$ g cm⁻³ ! for this transition density best fits obtained in one-dimensional delayed detonation models
- analysis by GIVEN DENSITY AND FUEL COMPOSITION Lisewski et al.(2000): claim u'(L) $(\times 10^7 \text{ g cm}^{-3})$ $(cm s^{-1})$ X(12C) X(16O) >0.5 × 10⁸ 0.5 0.5 2.3 >0.6 × 10⁸ 1.3 0.5 0.5 $>0.8 \times 10^8$ 0.8 0.5 0.5 $> 0.25 \times 10^8 \dots$ 2.3 0.75 0.25 $>0.3 \times 10^8$ 0.75 0.25 1.3 >0.4 × 10⁸ 0.25 0.8 0.75 $> 0.9 \times 10^8 \dots$ 2.3 0.75 0.25 >10⁸ 1.3 0.25 0.75 >10⁸

- needs updated analysis ►
- necessary but not sufficient conditions for DDT ! met in SN Ia models? ►

0.75

LIMITING THRESHOLD FOR TURBULENT VELOCITY u'(L) at

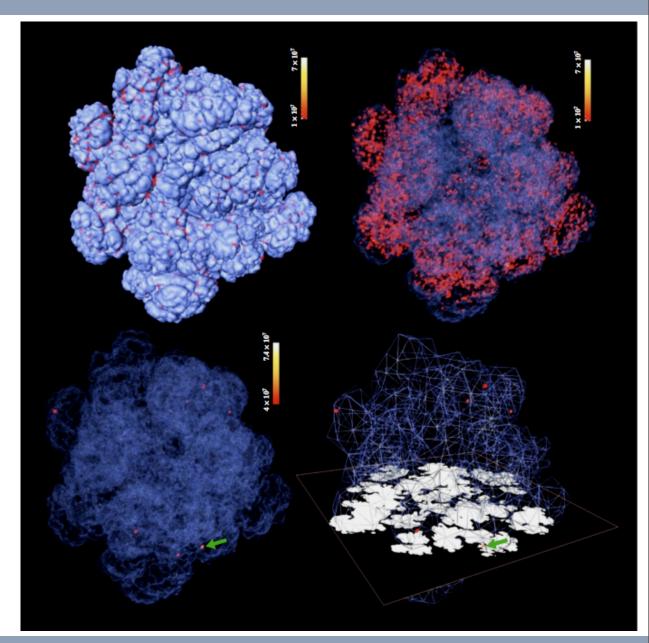
0.8

0.25

TABLE 1

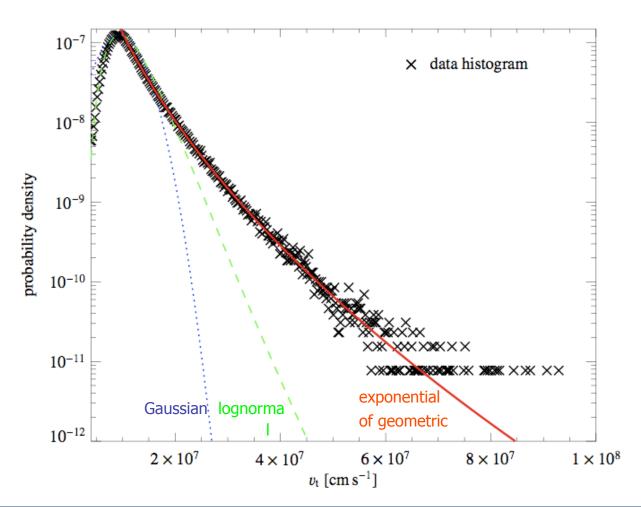
Deflagration-to-Detonation Transitions?

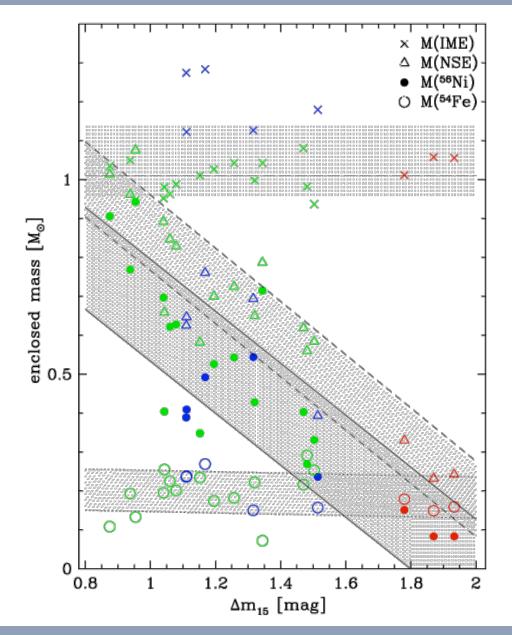
 Analysis of turbulent velocity flucutations
 as predicted by sub-grid scale model at the flame front for densities
 1...3 £ 10⁷ g cm⁻³ (Röpke, in prep.)



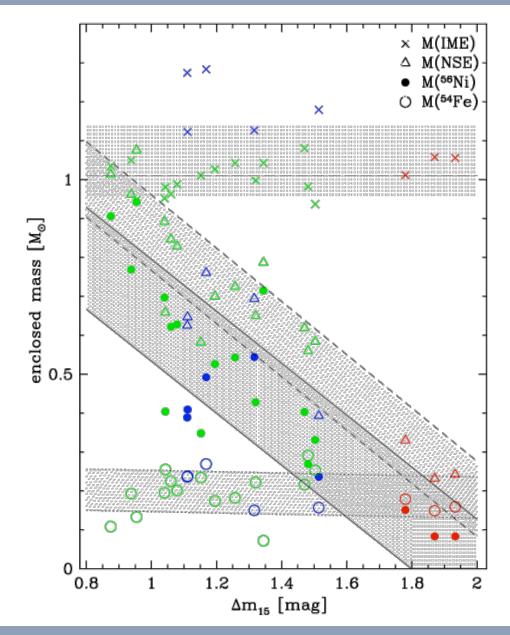
Deflagration-to-Detonation Transitions?

High-amplitude turbulent velocity fluctuarions (~10⁸ cm s⁻¹) occur at the onset of distributed burning regime on sufficiently large area of flame (~10¹² cm²)

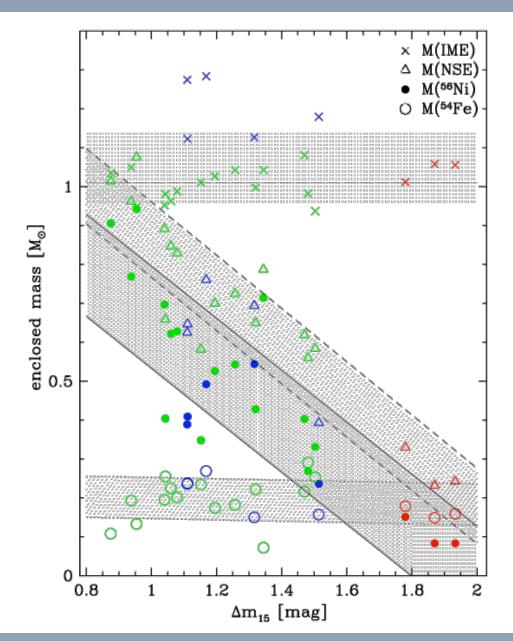


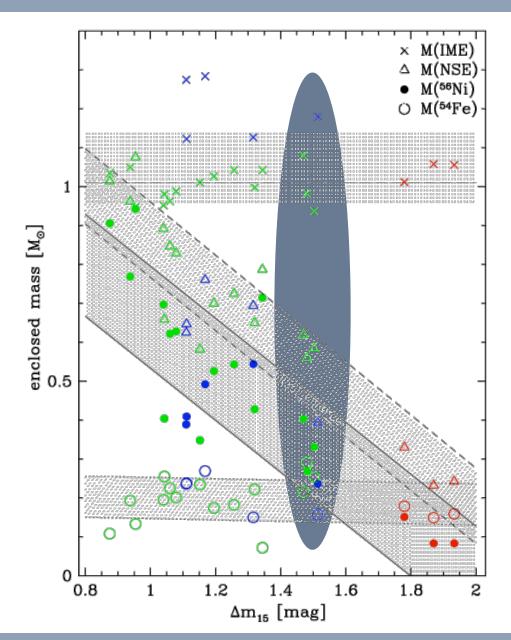


"Zorro diagram"



Friedrich Röpke, UCSC and MPA

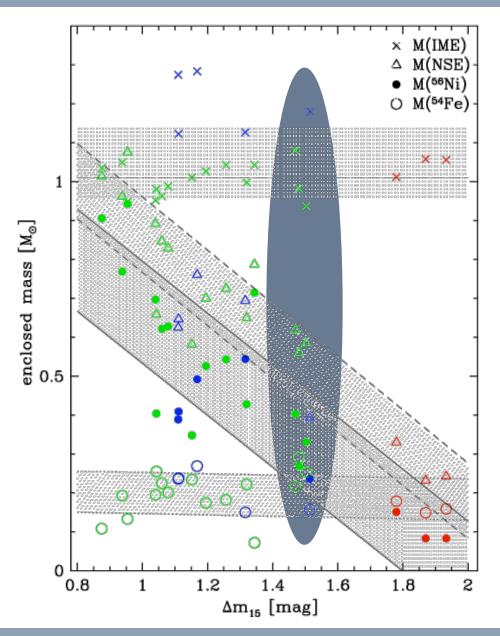




KITP 07, 3/22/2006

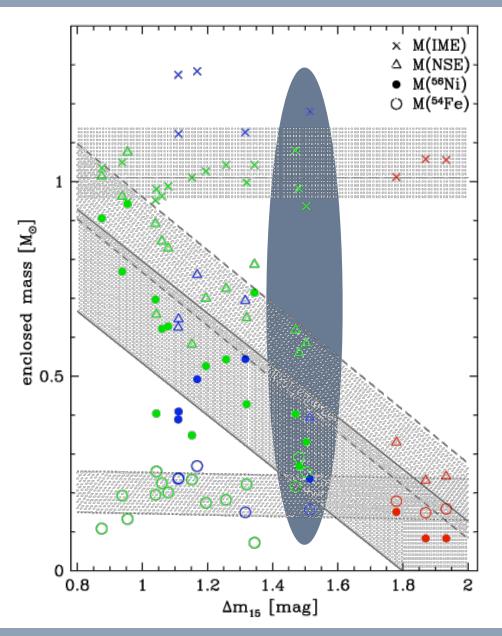
"Zorro diagram" (Mazzali et al., 2007)

weak normal SNe Ia



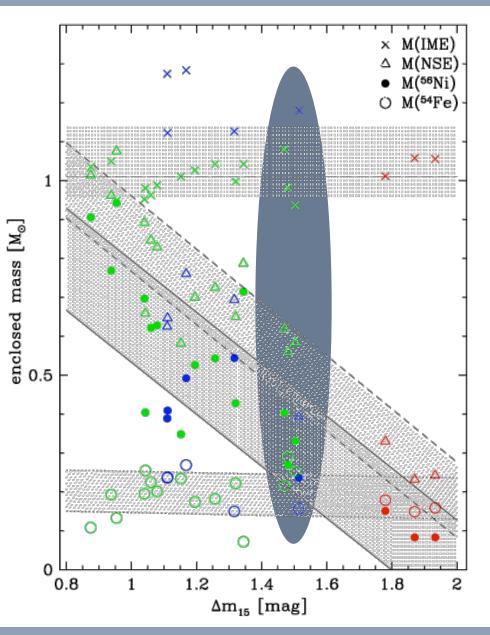
"Zorro diagram" (Mazzali et al., 2007)

 weak normal SNe Ia deflagrations or



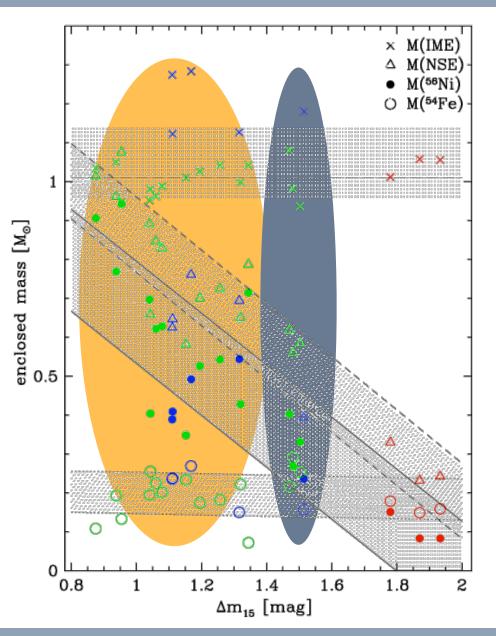
"Zorro diagram" (Mazzali et al., 2007)

 weak normal SNe Ia deflagrations or deflagration phase dominant

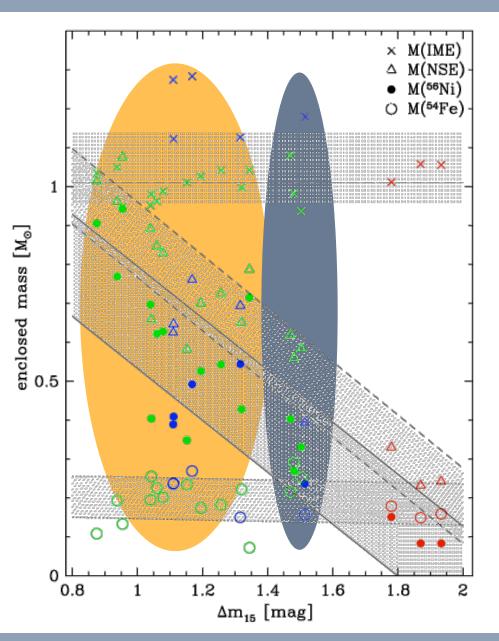


"Zorro diagram" (Mazzali et al., 2007)

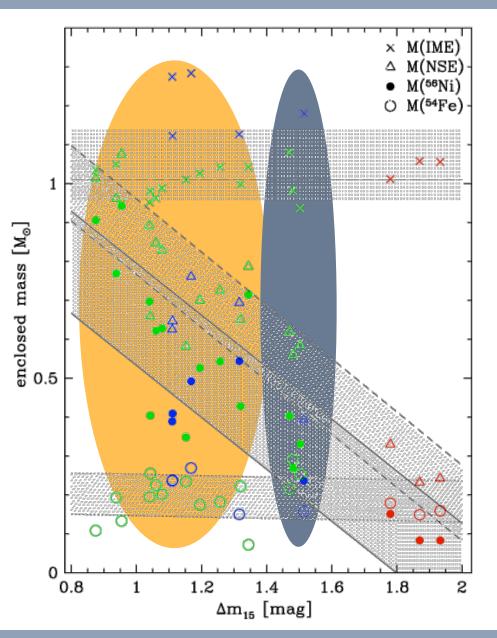
 weak normal SNe Ia deflagrations or deflagration phase dominant



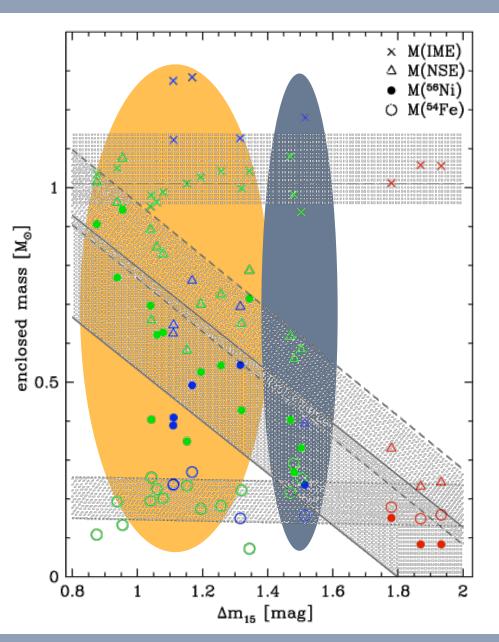
- weak normal SNe Ia deflagrations or deflagration phase dominant
- bright SNe Ia



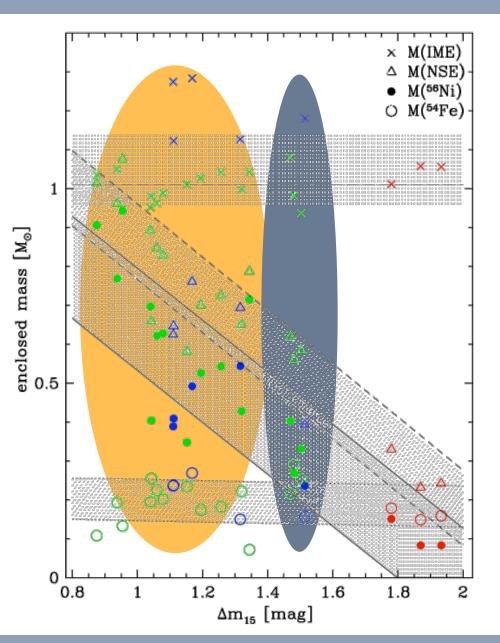
- weak normal SNe Ia deflagrations or deflagration phase dominant
- bright SNe Ia delayed detonations



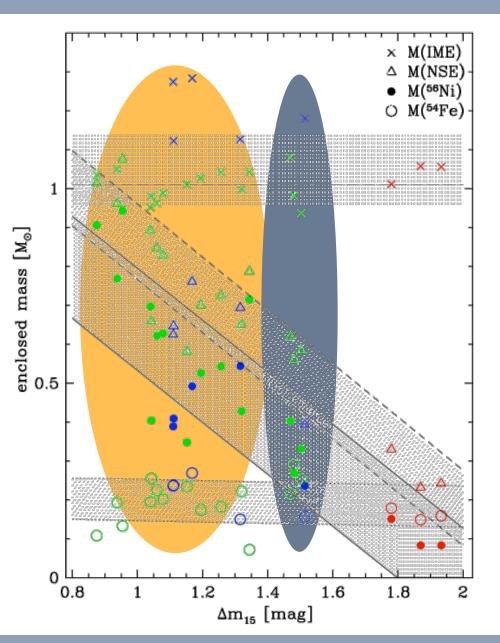
- weak normal SNe Ia deflagrations or deflagration phase dominant
- bright SNe Ia delayed detonations for brightes examples:



- weak normal SNe Ia deflagrations or deflagration phase dominant
- bright SNe Ia delayed detonations for brightes examples: detonation phase dominant



- weak normal SNe Ia deflagrations or deflagration phase dominant
- bright SNe Ia delayed detonations for brightes examples: detonation phase dominant



- weak normal SNe Ia deflagrations or deflagration phase dominant
- bright SNe Ia delayed detonations for brightes examples: detonation phase dominant
- sub-luminous: ???

