

# Stable Burning on Accreting White Dwarfs

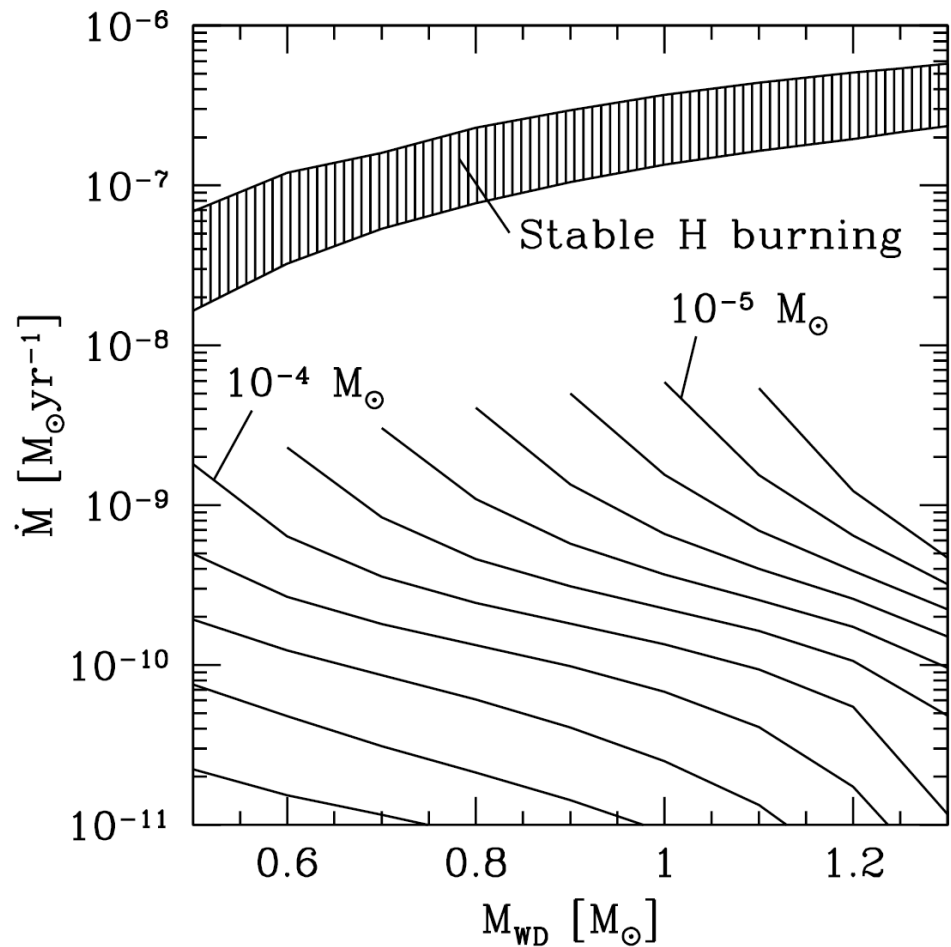
*(Shen & Bildsten '07, accepted for publication in ApJ)*



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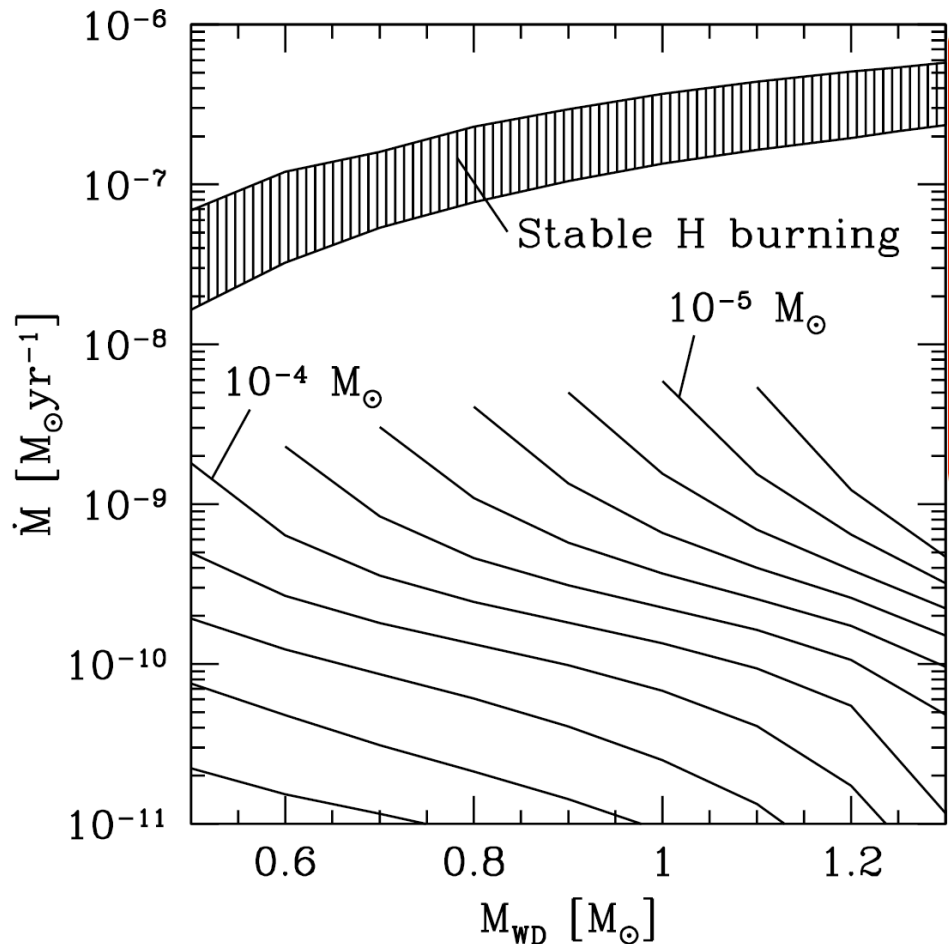
# Motivation



- There have already been previous studies of accreting WD stability (Fujimoto '82; Paczynski '83; Nomoto et al. '06)
- Stable accretion rate regime is factor of  $\sim 3$  wide: why?

(Nomoto et al. '06; Townsley & Bildsten '05)

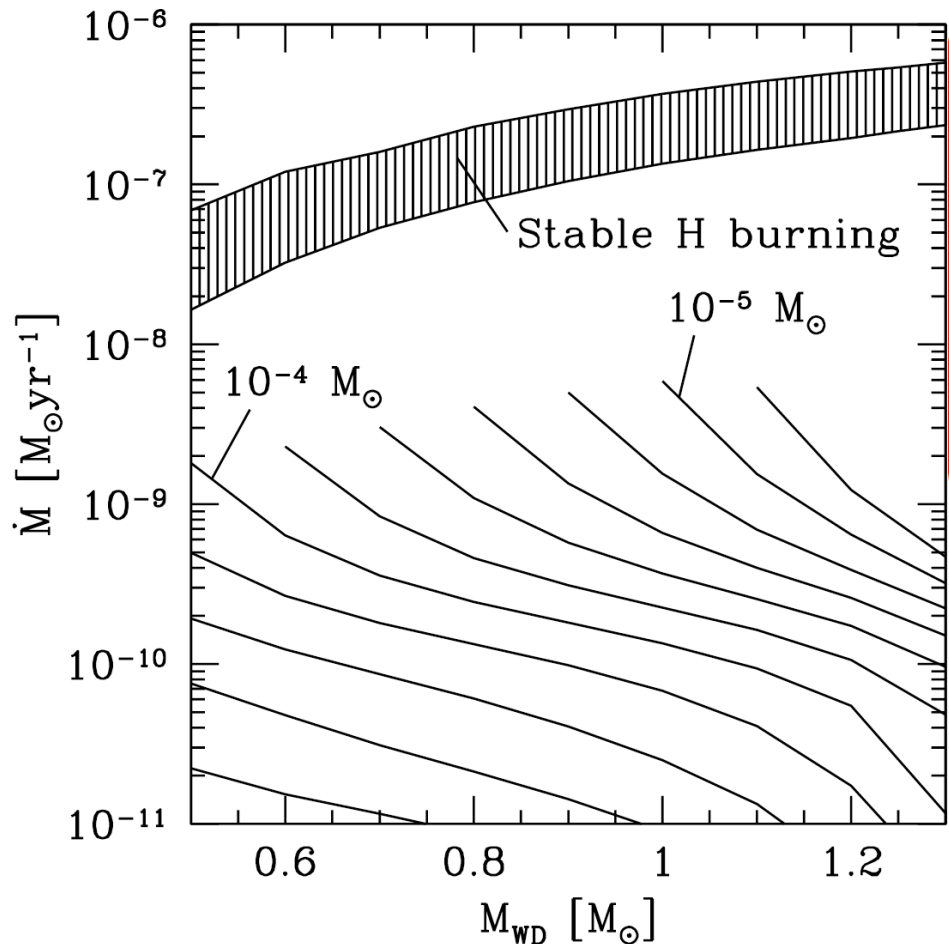
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- Hot WD? Full nuclear network?
- **Supersoft X-ray sources (van den Heuvel et al. '92)**
- Type Ia supernovae:
  - Likely progenitor system is white dwarf (WD) accreting from companion star until it reaches  $1.4 M_{\odot}$
  - Need to burn accreted material stably; otherwise material may be ejected due to thermonuclear runaway in the envelope (classical novae)
- Shell burning (H, He, etc.) occurs in post-main sequence stars

# Generic stability analysis

- Assume steady-state (matter accreted and burned at the same rate)
- Solve for steady-state conditions given parameters:

$$X, Z, M, \dot{M}, L_b$$

- Perturb entropy equation:

$$\begin{aligned} T \frac{ds}{dt} &= c_P \left( \frac{dT}{dt} - \nabla_{\text{ad}} \frac{T}{P} \frac{dP}{dt} \right) \\ &= \epsilon - \frac{\partial L}{\partial M} \end{aligned}$$

- Stable if perturbation decays with time

# Steady-state solutions

- In steady-state, time-derivatives are zero ( $dT/dt = dP/dt = 0$ ), and burning equals cooling with burning determined by the accretion rate:

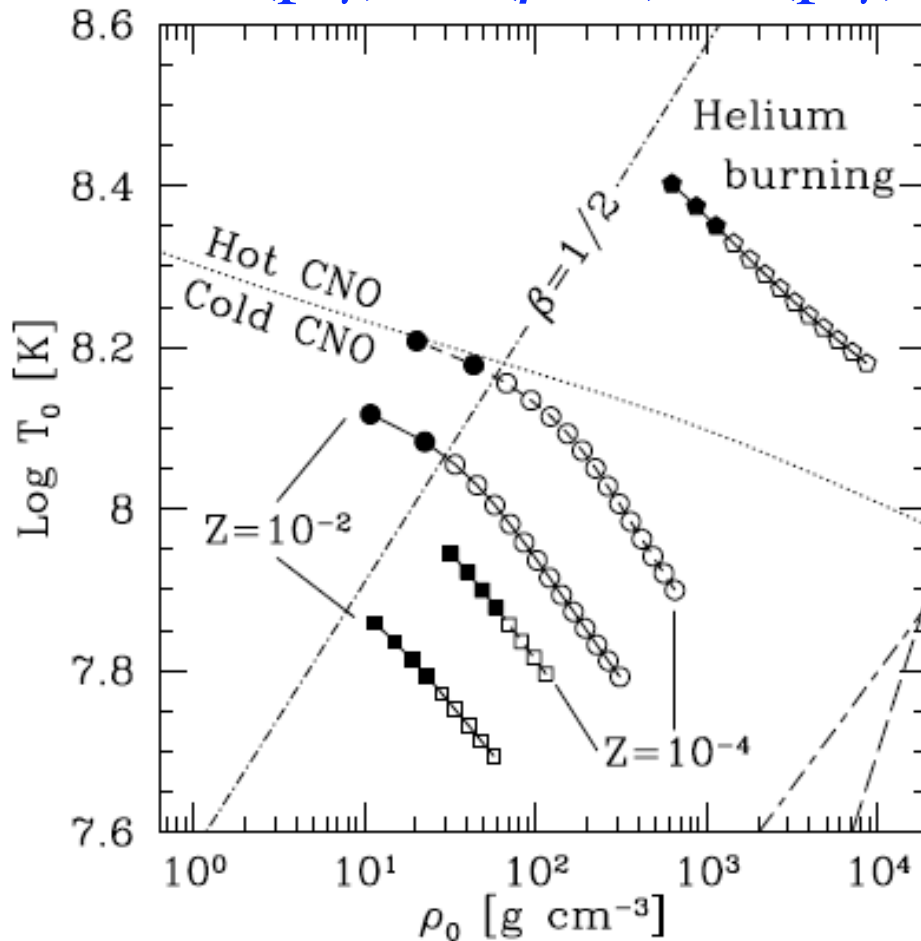
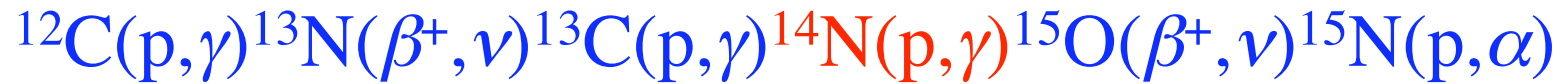
$$\epsilon = \frac{L - L_b}{4\pi R^2} \frac{g}{P} \qquad L - L_b = \dot{M} X E$$

- $X$  is the hydrogen mass fraction;  $E$  is the energy per mass from  $H \rightarrow He$
- With a form for the energy generation rate, luminosity (rad. diff.), equation of state (non-degenerate, include radiation pressure), and opacity (Thomson), we can solve for the steady-state burning conditions
- Heat transport by radiative diffusion:

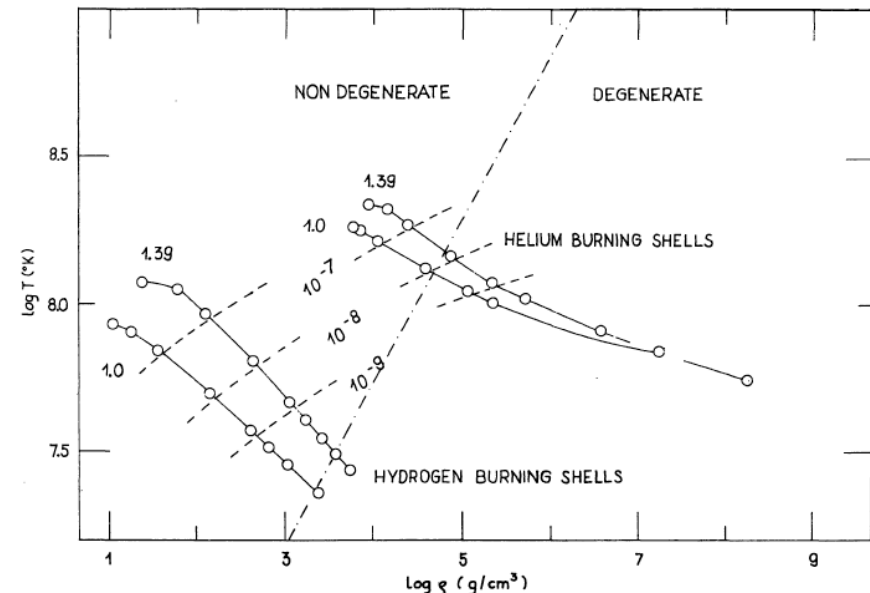
$$L = \frac{4\pi G M c}{\kappa_T} \frac{a T^4}{3P} \qquad 1 - \beta = \frac{\dot{M}}{\dot{M}_{\text{Edd}}} + \frac{L_b}{L_{\text{Edd}}}$$

- Ratio of gas pressure to total pressure is  $\beta = P_{\text{gas}} / P$ . Increase importance of radiation pressure by increasing accretion rate and core luminosity: **Eddington standard model**.

# Steady-state solutions (cold CNO)



- Squares:  $0.5 M_{\odot}$ ; circles:  $1.35 M_{\odot}$
- Solutions are non-degenerate and Thomson opacity, so assumptions are self-consistent
- Cold CNO very  $T$ -sensitive ( $\propto T^{10}$ ), so not much range in  $T$
- Massive (ultra)-low metallicity WDs bump up into hot CNO limit; motivates later work



# Relating $\delta\rho$ and $\delta P$ to $\delta T$

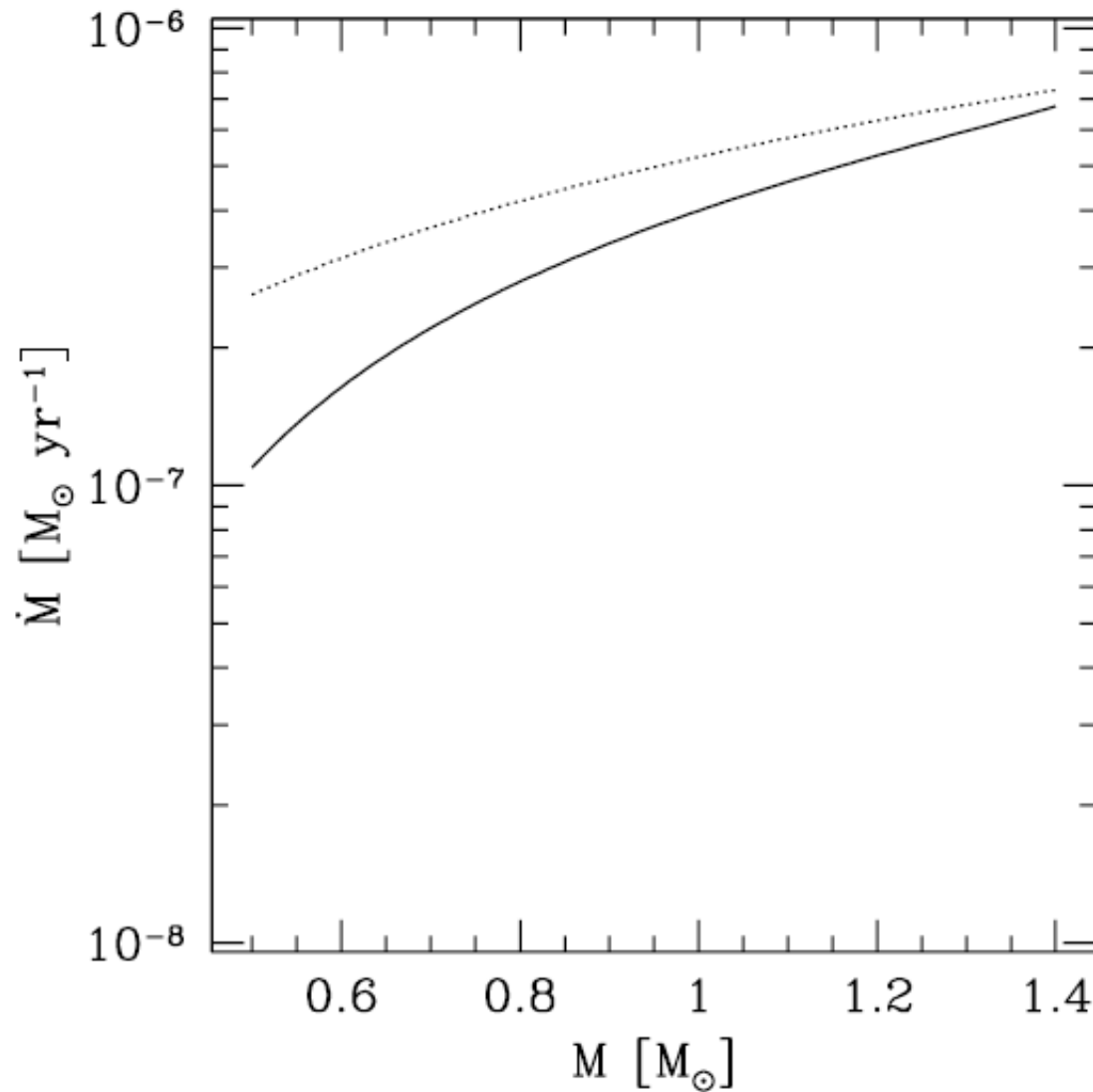
- To calculate perturbation timescale, need to relate density and pressure perturbations to change in temperature
- Could do homologous expansion (e.g., Yoon et al. '04), but instead we integrate hydrostatic equilibrium (HSE) to obtain  $M_{\text{env}}$  and keep it fixed during perturbation
- Solving HSE yields upper bound on scale height:

$$4h < R_{\text{base}} \quad h = \frac{P}{\rho g} = \frac{k_{\text{B}}T}{\beta\mu m_{\text{p}}g}$$

- In other words,  $\beta$  can't go to zero; there is a **sub-Eddington upper limit to the accretion rate**, above which no steady-state HSE solutions exist. Essentially the standard RG  $L$ - $M_{\text{core}}$  relationship (Paczynski '70), modulo additional He-burning.



# HSE constraint



- Dotted line: nuclear Eddington limit
- Solid line: HSE constraint

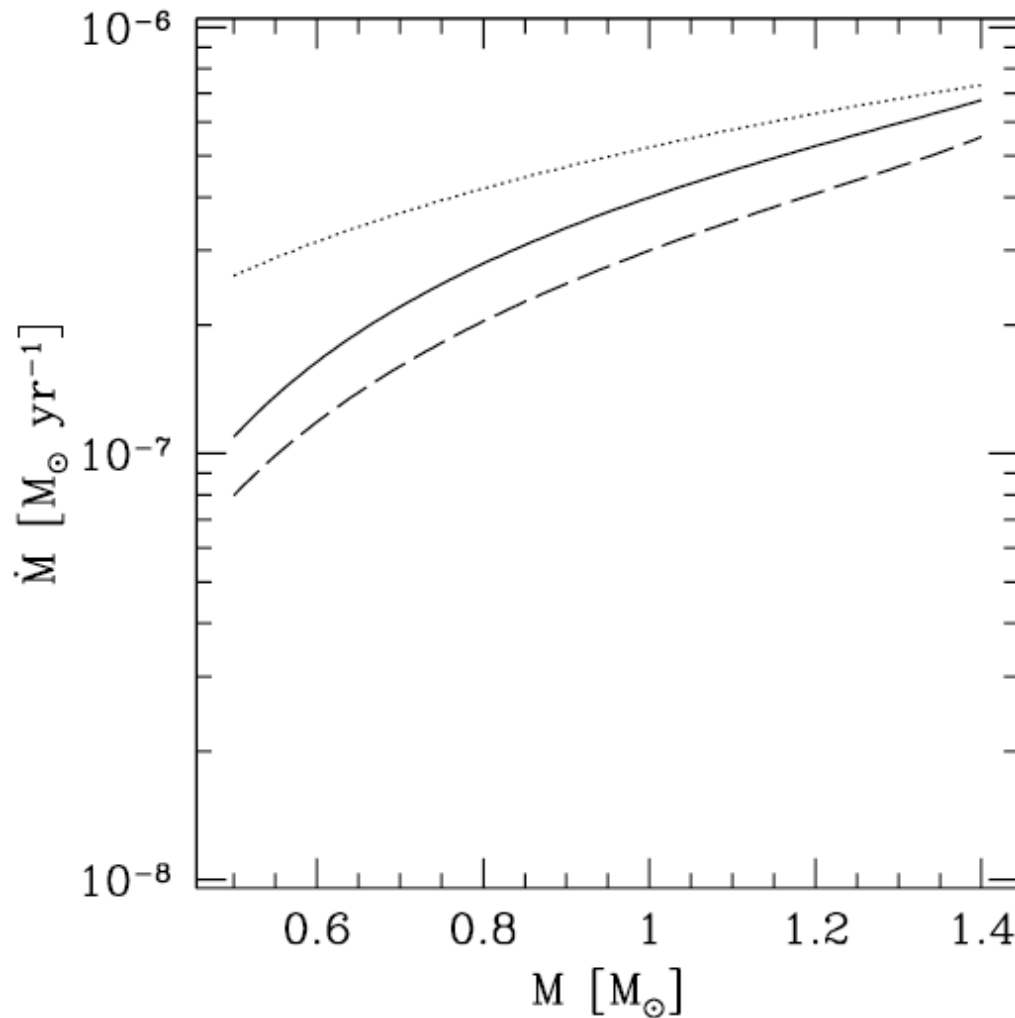
## 2 channels for stability: Thick shell case (higher $\dot{M}$ )

- Negative gravothermal specific heat,  $c_*$ :

$$\begin{aligned} T\delta s &= \delta u - \frac{P}{\rho}\delta \ln \rho \\ &= c_*\delta T \end{aligned}$$

- Injection of heat causes an even larger amount of expansion work to be done, so **internal energy and  $T$  drop**
- This is what stars as a whole do; they contract, radiate energy away, and  $T$  increases:  $c_* < 0$  so they're stable (the ultimate thick shell!)
- Independent of burning/cooling mechanism (aside from setting steady-state solution)

## 2 channels for stability: Thick shell case (higher $\dot{M}$ )



- Dotted: nuclear Eddington limit
- Upper solid line: HSE constraint
- Long-dashed line:  $c_*$  switches signs

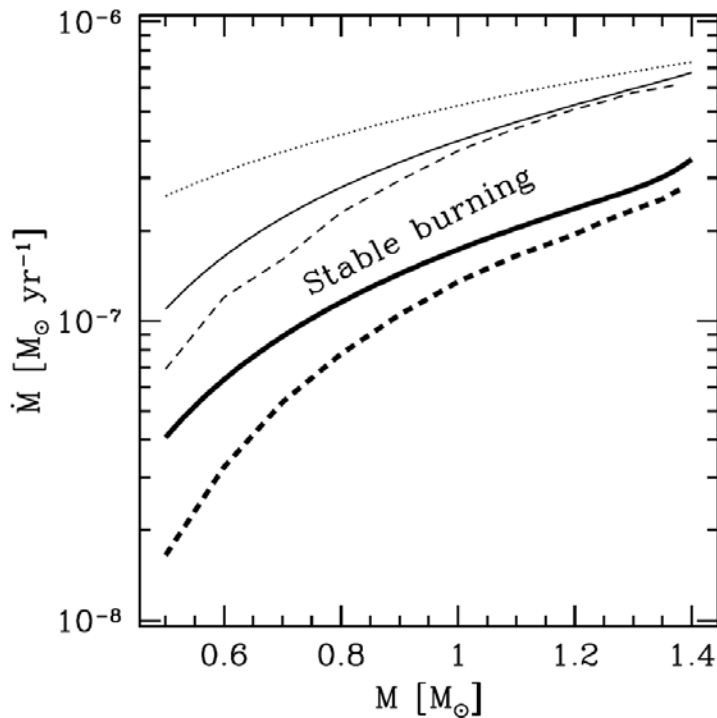
## 2 channels for stability: Thin shell case (lower $\dot{M}$ )

- Competition between heating and cooling
- To zeroth order, stable if  $T$ -dependence of heating is lower than 4 ( $L \propto T^4$ )
- Also need to put in the effect of  $\rho$  and  $P$  perturbations, which help to stabilize, especially if radiation pressure is high:

$$P = \frac{\rho k_B T}{\mu m_p} + \frac{1}{3} a T^4$$

- Consider density change at constant pressure. If radiation pressure dominated, small increase in  $T$  yields large decrease in  $\rho$ ; quenches burning even in extremely thin shell limit
- Inclusion of drop in  $P$  makes this even more dramatic

# Thermally stable Mdot's (cold CNO)

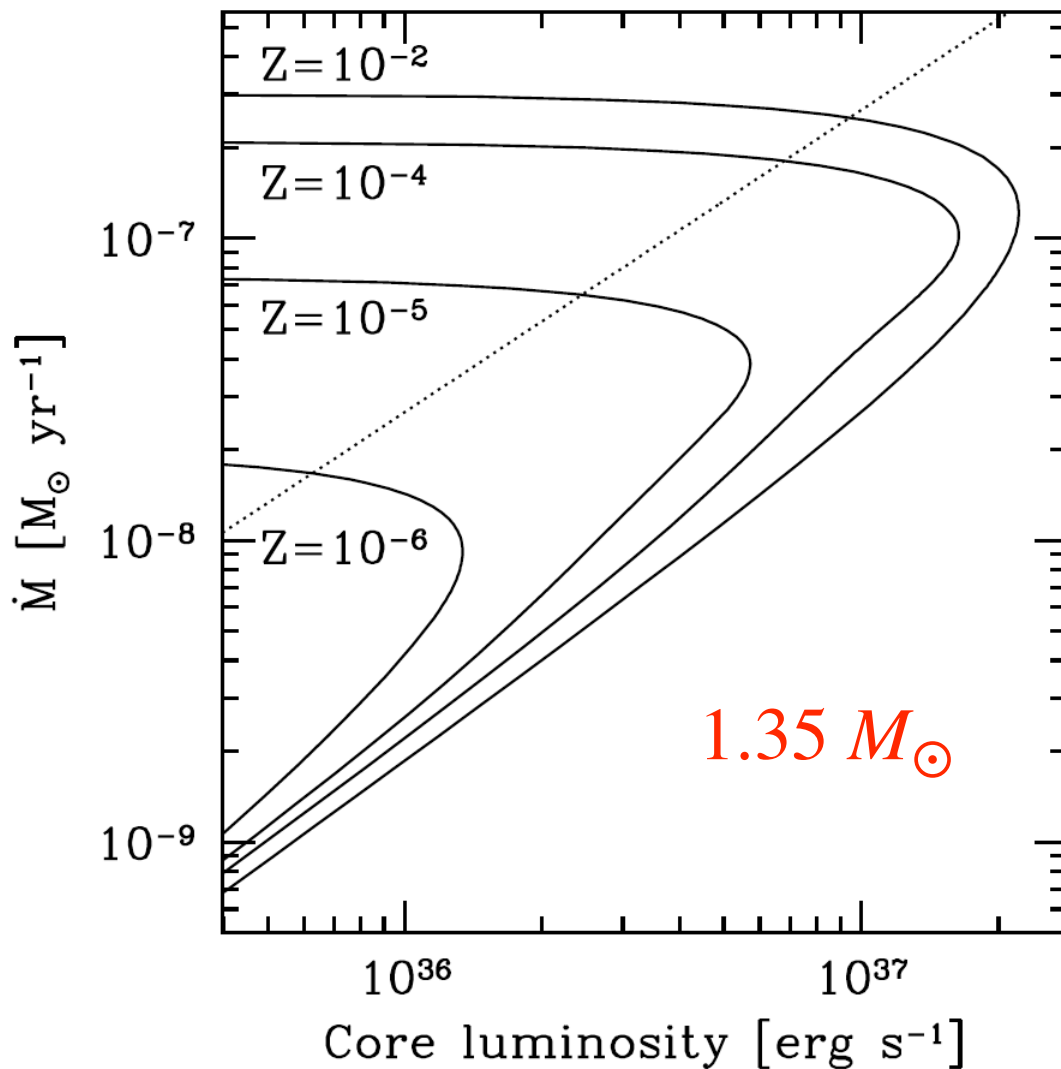


- Dotted: nuclear Eddington limit
- Upper solid line: HSE constraint
- Bottom solid line: thin shell stability
- Dashed lines: numerical work (Nomoto et al. 2006)
- Factor of 3 between min and max Mdot's
- Why a factor of 3? Can calculate ratio of max and min Mdot's, assuming burning  $\propto T^{10}$  and  $T$  constant over accretion range (remember steady-state plot?), to get:

$$\frac{\dot{M}_{\max}}{\dot{M}_{\min}} = 2.9 \left[ 1 + O \left( \beta_{\min} - \frac{3}{4} \right) \right]$$

- Ratio not very dependent on  $T$  exponent: pre-factor  $\sim 3$  for  $T^{9-12}$

# Flux stabilization

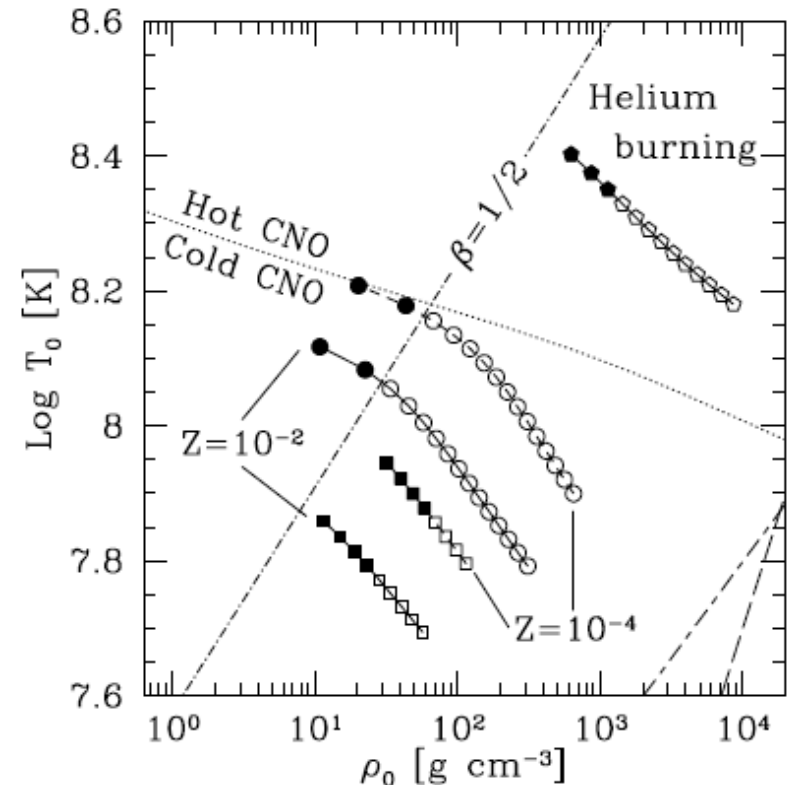


- So far, I've assumed negligible core luminosity
- Take limiting case of ultra-high  $L_{\text{core}}$ ; then conditions in envelope are set purely by this, so it's always stable
- But can't have arbitrarily high  $L_{\text{core}}$  for duration of accretion; max possible is from steady burning of He layer below (*dotted line*), which doesn't open up much parameter space

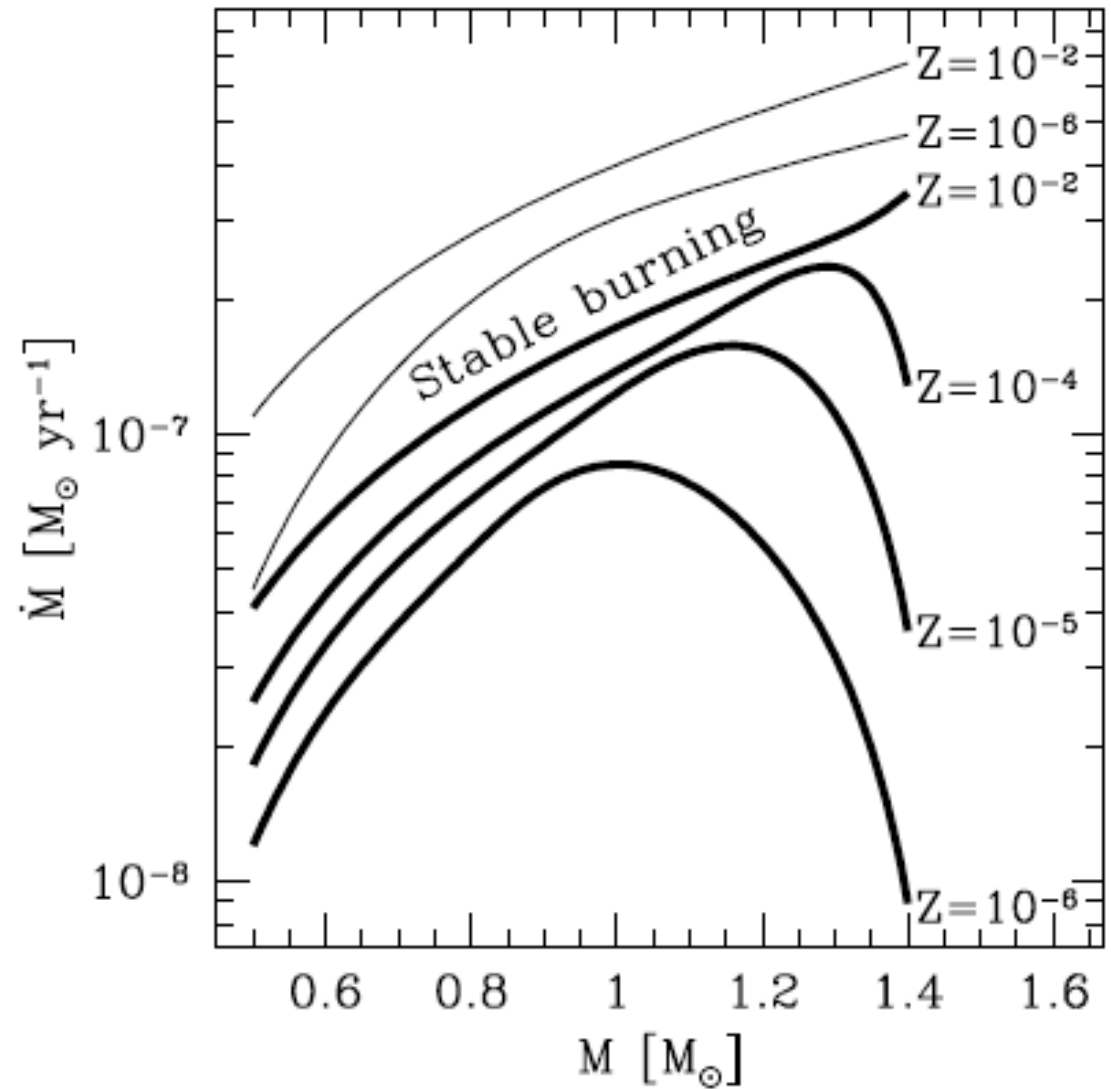
# Hot CNO stabilization



- If the layer is really hot/dense, proton captures occur faster than the  $T$ -independent  $\beta$ -decays. Rate-limiting steps are the two  $\beta$ -decays, and H-burning is stable (like on NSs).
- So what do we have to do to get the  $\beta$ -decays to matter? Increase  $g$  and decrease  $Z_{\text{CNO}}$  (which result in hotter/denser conditions).
- To test stability, same procedure as before: solve for steady-state solutions; calculate  $T$ - and  $\rho$ -dependences of burning in equil. (fun exercise in algebra and pre-calc!); see if perturbation decays or grows.



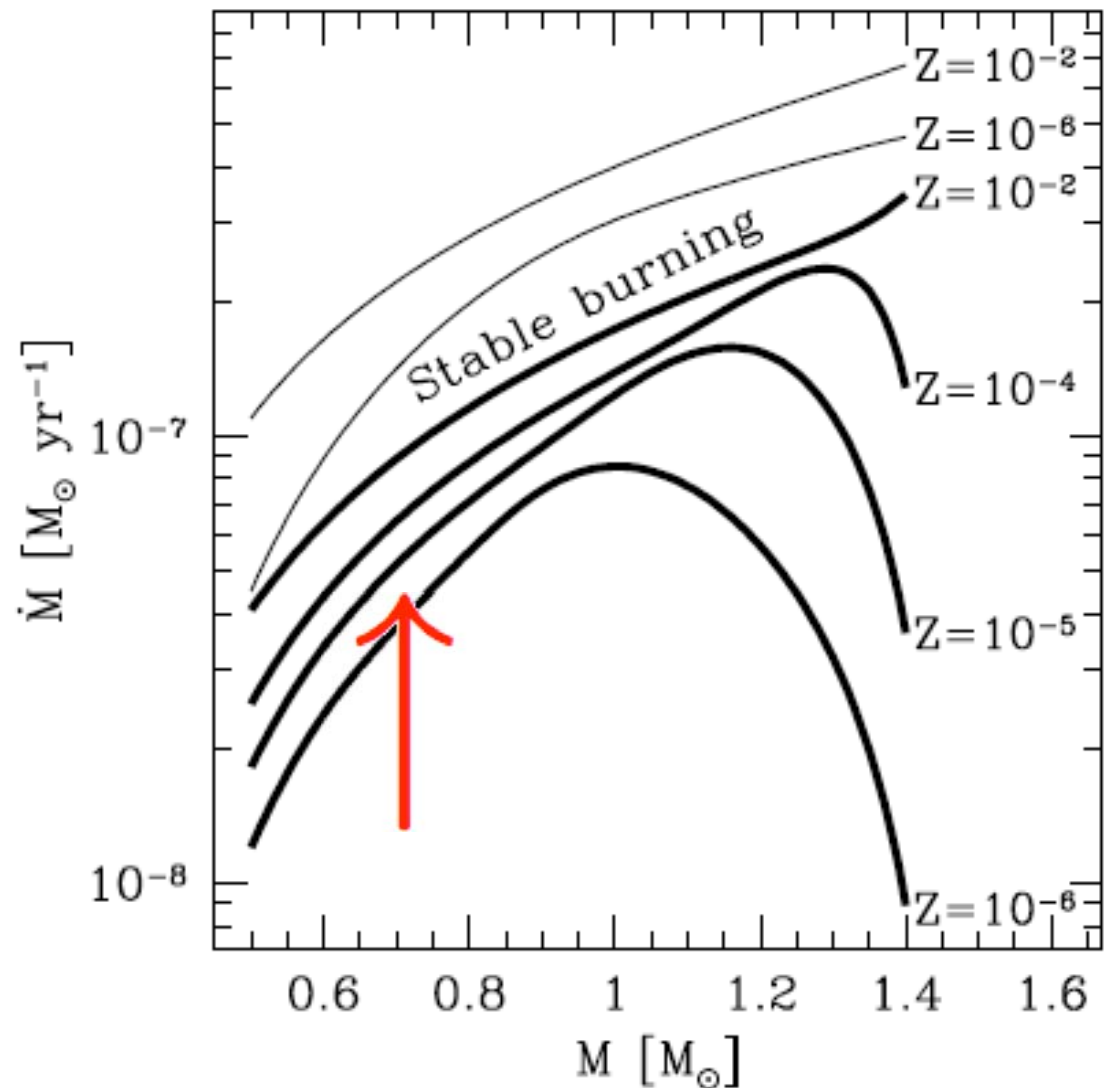
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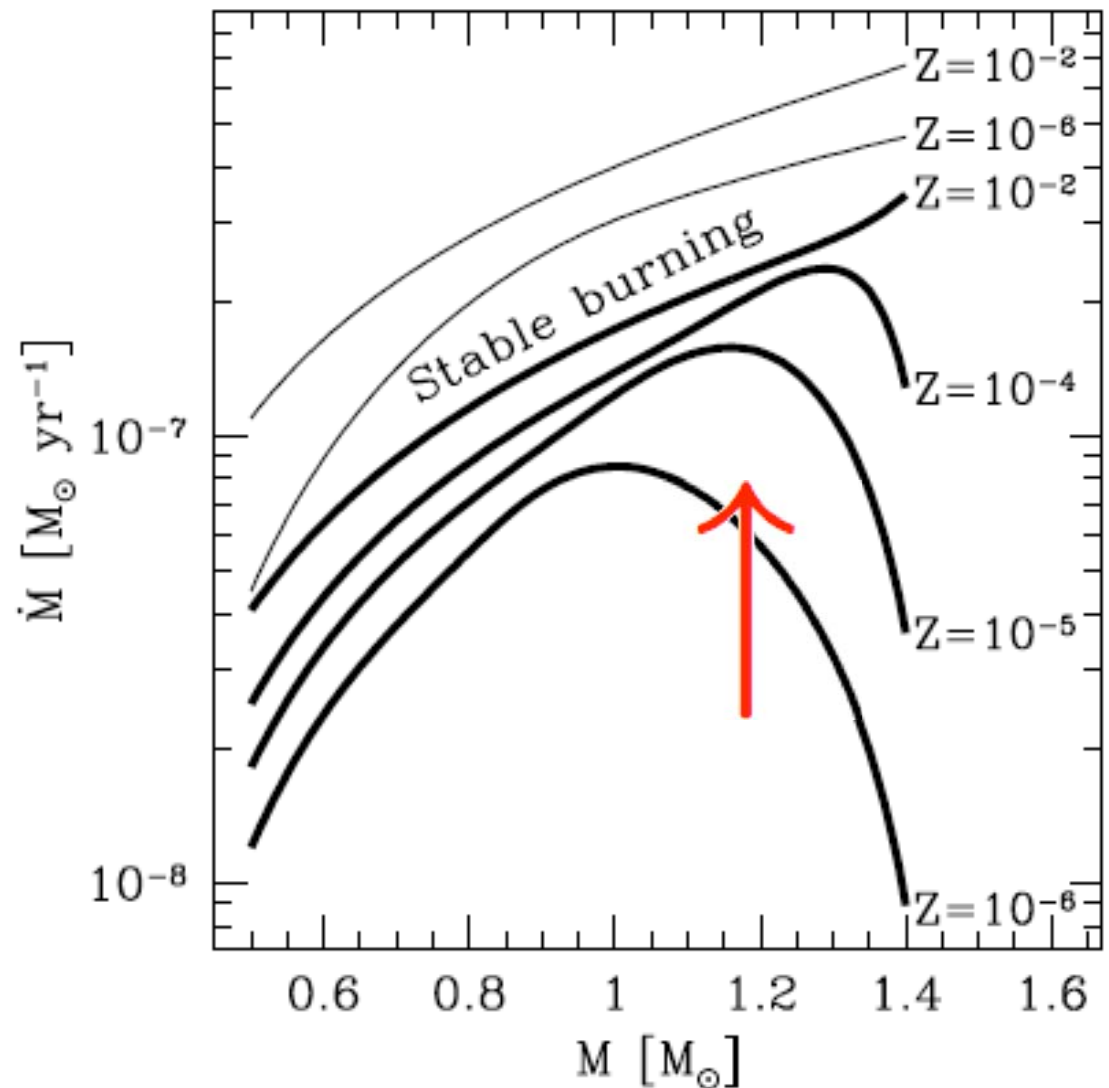
# Thermally stable Mdot's (full CNO)

- Low masses, still burning via cold CNO. Lower stable Mdot's because lower  $Z_{\text{CNO}}$  means higher  $T$  and weaker  $T$ -dependence of cold CNO burning. Ratio of min and max Mdot's still  $\sim 3$ .



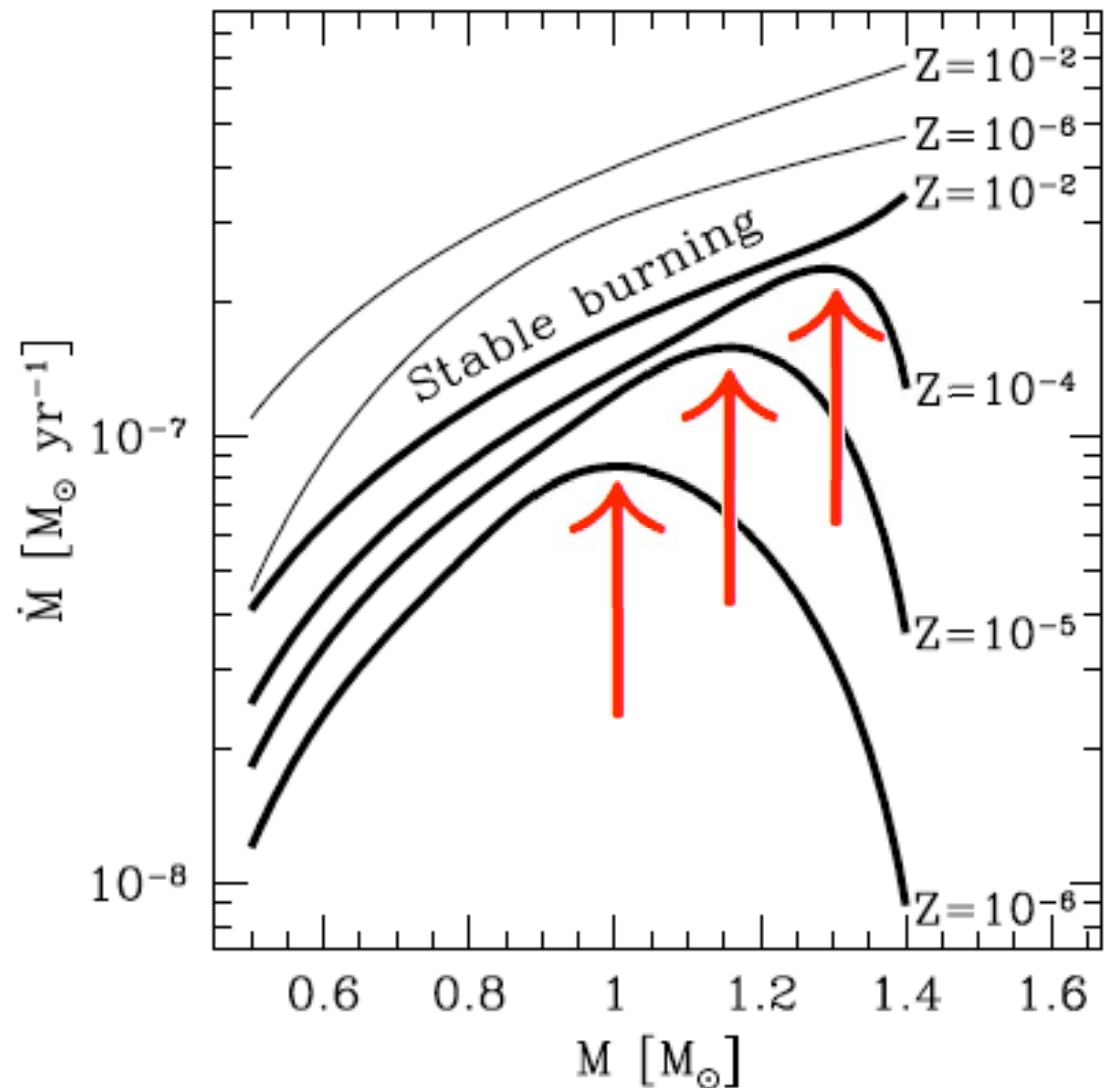
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- For higher masses, hot CNO comes into play!  $\beta$ -decays are thermally stable. BIG effect...for  $10^{-2} Z_{\odot}$
- The lower  $Z$  is, the lower the mass that hot CNO starts to matter



# Conclusions

- Thermally stable accretion rate range on WDs is narrow:
  - Upper bound from HSE constraint
  - Thick shell stability for higher  $\dot{M}$ 's is due to negative gravothermal specific heat
  - Thin shell stability for lower  $\dot{M}$ 's is due to competition between heating and cooling (radiation pressure is important!)
  - Yields factor of  $\sim 3$  in accretion rate range
- Core luminosity can stabilize, but need a LOT of it
- Hot CNO can stabilize, but need VERY low metallicity (or high gravity)
  
- Will post on astro-ph this afternoon
- Many thanks to Lars Bildsten and Tony Piro