





Including Effects of Band Structure and Disorder in Spin Transport Calculations

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Landauer-Büttiker Formulation of Electron Transport



Scattering Theory of Electron Transport

on the atomic scale electrons are wavelike



$$\begin{pmatrix} \mathbf{O} \\ \mathbf{O'} \end{pmatrix} = \begin{pmatrix} \mathbf{r} & \mathbf{t'} \\ \mathbf{t} & \mathbf{r'} \end{pmatrix} \begin{pmatrix} \mathbf{I} \\ \mathbf{I'} \end{pmatrix}$$

Scattering Matrix

Approach: DFT first principles calculations



solve scattering problem at fixed energy $E = E_F$



2 Implementations

1. Tight-Binding Muffin Tin Orbitals (TB-MTO)

- minimal basis (1xs,1xp,1xd orbital per atom)
- suitable for transition metals (magnetism)
- close-packed solids (Atomic Spheres Approx.)

Spin Transport

Xia et al. PRB**63** (2001) PRB**73** (2006)

2. Real-space grid + Pseudopotentials

- full potential
- open structures

Molecular Electronics

Khomyakov et al. PRB**70** (2004)

Spin Transport: Applications

•GMR

- •CPP Interface resistances
- •CIP
- Transport through domain walls
- Magnetization Switching
- Andreev reflection at F/S interfaces
- Enhancement of Gilbert damping
- Spin injection in F/SC (Reflection): DFP
- Spin Valve Transistor
- Tunneling MR
- Spin injection in F/SC (Transmission)
- V. Karpan (Twente) M. Zwierzycki (Twente) P.X. Xu (Beijing) M. Talanana (Twente)
 - K. Xia (Twente/Beijing)
 - A. Brataas (Trondheim)
- G.E.W. Bauer (Delft) K.M. Schep (Philips) J.B.A.N. van Hoof (Philips)

I. Turek (Brno)

Review: A. Brataas, G.E.W. Bauer and P.J. Kelly, Physics Reports 427 (2006)

Spin Transport: Applications

•GMR

•CPP - Interface resistances

·CIP

Transport through domain walls

- Magnetization Switching
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- Spin injection in F/SC (Reflection): DFP
- •Spin Valve Transistor
- •Tunneling MR
- •Spin injection in F/SC (Transmission)

Spin-dependent Transmission

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Cu/Co(111): specular interface - k_{||} conserved



Cu/Co(111): specular case - k_{||} conserved 3rd band 4th band 5th band Energy [eV] -8 -10 L Х **Minority Spin** 3 2

Cu/Co(111): specular case - k₁₁ conserved



Sheet decomposition of transmission

 \rightarrow matrix element effects are important

Giant MagnetoResistance (GMR)

Interface Resistances

$$\frac{1}{R} = G = \frac{e^2}{h} Tr\{t t^+\}$$

Co/Cu

But suppose A=B; then $R \neq 0$?

Correction for $SR_{A/B} = \frac{Sh}{e^2} \left[\frac{1}{tr\{t t^+\}} - \frac{1}{2} \left(\frac{1}{N_A} + \frac{1}{N_B} \right) \right]$

fΩm ²	Orientation	majority	minority
calculation	(111)	0.39	1.46
expt (MSU)	(111)	0.26±0.06	1.84±0.14

Schep et al. PRB56 (1997)

Interface Disorder

Model disorder in lateral supercells as two layers of alloy.

AS potentials calculated self-consistently using layer CPA

Xia et al. PRB**63** (2001) PRB**73** (2006)

Convergence for Cu/Co(111) interface

Interface Disorder

Cu/Co fcc(111)	R↑ fΩm²	R↓ fΩm²	1.8 $\widehat{E_1}^{1.6}$
Clean	0.39	1.46	V-1) (f) (f) (f) (f) (f) (f) (f) (f) (f) (f
2×50-50 alloy	0.41	1.82	R(N)-R(N)-R(N)-R(N)-R(N)-R(N)-R(N)-R(N)-
Expt (MSU)	0.26±0.06	1.84±0.14	0.4 0.2 0
			⁻ 0 5 10 15 Number of interfaces

Differential Interface Resistance

Modelling Interface Disorder

Orientation-dependent interface transparency

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Identify a suitable system to confront theory and experiment

 \rightarrow Study pairs of lattice-matched metals

A/B		G _A	$G_{\scriptscriptstyle B}$	G _{A/B}
Al/Ag a _{fcc} =4.05 Å	(111) (110) (001)	0.69 0.68 0.73	0.45 0.47 0.45	0.41 0.30 0.22
Al/Au	(111)	0.69	0.44	0.41
a _{fcc} =4.05 Å	(001)	0.73	0.46	0.24
Pd/Pt	(111)	0.62	0.71	0.55
<i>a</i> _{fcc} =3.89 Å	(001)	0.58	0.70	0.52
W/Mo	(001)	0.45	0.59	0.42
a _{bcc} =3.16 Å	(110)	0.40	0.54	0.37
Cu/Co	(111)*	0.56	0.47	0.43
Majority	(001)	0.55	0.49	0.46
a _{fcc} =3.61 Å	(110)	0.59	0.50	0.46
Cu/Co	(111)*	0.56	1.05	0.36
Minority	(001)	0.55	1.11	0.32
a _{fcc} =3.61 Å	(110)	0.59	1.04	0.31
Cr/Fe	(111)	0.61	0.82	0.27
Majority	(001)	0.64	0.82	0.11
a _{bcc} =2.87 Å	(110)*	0.59	0.78	0.22
Cr/Fe	(111)	0.61	0.41	0.34
Minority	(001)	0.64	0.46	0.35
a _{bcc} =2.87Å	(110)*	0.59	0.40	0.32

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~13%

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~factor 2!

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Majority	(001)	0.64	0.82	0.11
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Cr/Fe	(111)	0.61	0.41	0.34
Minority	(001)	0.64	0.46	0.35
a _{bcc} =2.87Å	(110)*	0.59	0.40	0.32

~factor 2!

~factor $2\frac{1}{2}$?

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Al/Ag a _{fcc} =4.05 Å	(111) (110) (001)	0.69 0.68 0.73	0.45 0.47 0.45	0.41 (0.36) 0.30 (0.32) 0.22 (0.24)
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a _{fcc} =4.05 Å	(001)	0.73	0.46	0.24 (0.26)
Pd/Pt	(111)	0.62	0.71	0.55 (0.54)
a _{fcc} =3.89 Å	(001)	0.58	0.70	0.52 (0.51)
W/Mo	(001)	0.45	0.59	0.42 (0.42)
a _{bcc} =3.16 Å	(110)	0.40	0.54	0.37 (0.38)
Cu/Co Majority a _{fcc} =3.61 Å	(111)* (001) (110)	0.56 0.55 0.59	0.47 0.49 0.50	0.43 (0.43) 0.46 (0.45) 0.46 (0.46)
Cu/Co Minority a _{fcc} =3.61 Å	(111)* (001) (110)	0.56 0.55 0.59	1.05 1.11 1.04	0.36 (0.31) 0.32 (0.32) 0.31 (0.35)
Cr/Fe	(111)	0.61	0.82	0.27 (0.31)
Majority	(001)	0.64	0.82	0.11 (0.25)
<i>a_{bcc}=2.87 Å</i>	(110)*	0.59	0.78	0.22 (0.27)
Cr/Fe	(111)	0.61	0.41	0.34 (0.34)
Minority	(001)	0.64	0.46	0.35 (0.35)
a _{bcc} =2.87Å	(110)*	0.59	0.40	0.32 (0.32)

A/B		G _A	$G_{\scriptscriptstyle B}$	G _{A/B}	2 <i>5</i> R
Al/Ag a _{fcc} =4.05 Å	(111) (110) (001)	0.69 0.68 0.73	0.45 0.47 0.45	0.41 (0.36) 0.30 (0.32) 0.22 (0.24)	0.64 (0.92) 1.60 (1.39) 2.82 (2.37)
Al/Au	(111)	0.69	0.44	0.41 (0.35)	0.60 (0.99)
a _{fcc} =4.05 Å	(001)	0.73	0.46	0.24 (0.26)	2.37 (2.14)
Pd/Pt	(111)	0.62	0.71	0.55 (0.54)	0.30 (0.33)
a _{fcc} =3.89 Å	(001)	0.58	0.70	0.52 (0.51)	0.37 (0.39)
W/Mo	(001)	0.45	0.59	0.42 (0.42)	0.42 (0.42)
a _{bcc} =3.16 Å	(110)	0.40	0.54	0.37 (0.38)	0.52 (0.47)
Cu/Co	(111)*	0.56	0.47	0.43 (0.43)	0.34 (0.35)
Majority	(001)	0.55	0.49	0.46 (0.45)	0.26 (0.27)
a _{fcc} =3.61 Å	(110)	0.59	0.50	0.46 (0.46)	0.35 (0.35)
Cu/Co	(111)*	0.56	1.05	0.36 (0.31)	1.38 (1.82)
Minority	(001)	0.55	1.11	0.32 (0.32)	1.79 (1.79)
a _{fcc} =3.61 Å	(110)	0.59	1.04	0.31 0.35)	1.89 (1.55)
Cr/Fe	(111)	0.61	0.82	0.27 (0.31)	2.22 (1.84)
Majority	(001)	0.64	0.82	0.11 (0.25)	7.46 (2.55)
a _{bcc} =2.87 Å	(110)*	0.59	0.78	0.22 (0.27)	3.04 (2.18)
Cr/Fe	(111)	0.61	0.41	0.34 (0.34)	0.93 (0.95)
Minority	(001)	0.64	0.46	0.35 (0.35)	0.98 (0.95)
a _{bcc} =2.87Å	(110)*	0.59	0.40	0.32 (0.32)	1.03 (1.06)

Even a small deviation from free-electron model can have large consequences

Effect of Roughness and Disorder on Tunneling Magnetoresistance

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Magnetic Tunnel Junction

First-principles study of MTJ

• vacuum is simplest "insulator"

vacuum is relatively easy to model

no scattering from impurities or defects in insulator

• experiments

Observation of Fe bcc(001) surface states

FIG. 2. Band structure of majority and minority even symmetry states along $\overline{\Gamma} \cdot \overline{X}$ for a 49-layer Fe(001) film. States with high localization in the surface region are marked with circles.

Stroscio et al., PRL 1995

What about disorder, roughness?

Model flexibly in lateral supercells

Fe/vacuum/Fe interface roughness

In case of roughness (with 50% of interface coverage) the majority conductance is higher than minority for the parallel configuration For an ideal junction TMR is about 20000%. Interface roughness reduces the TMR to values comparable to those observed experimentally

Xu et al. PRB73 (2006)

Transport for a fixed vacuum barrier thickness as a function of roughness

Till ~25% of surface coverage the minority conductance decreases as the roughness increases leading to a rapid decline of TMR

Majority conductance increases all the time resulting in an increasing TMR in a range of surface coverage greater than 25%

Xu et al. PRB73 (2006)

Blue lines represent conductances in case of disordered leads

Green lines represent conductances in case of ideal leads

Effect of the alloy leads is not as strong as the effect of roughness especially for higher concentration of Co

Xu et al. PRB73 (2006)

interfacial LDOS^{*} at 2d Γ point for $Fe_{1-x}Co_x$ alloy

Spin injection from Fe into InAs

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¹ University of Twente, Enschede, The Netherlands
² Institute of Physics, Beijing, China
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⁴ Kavli Institute of NanoScience, Delft University of Technology, The Netherlands

Schmidt et al. PRB 62 (2000)

The "Conductance mismatch" argument ignores the possibility of spin-dependent interface resistances - how large are they ?

Origin of conductance mismatch

Fermi surface projections

What about the spin dependence of the interface resistance ?

Ideal Fe/InAs interface conductances

Wunnicke et al. PRB**65** (2002)

Ö Ni

Interface Resistances

Estimate the spin-dependent interface resistances - valid in the diffusive regime - using $SR_{A/B} = \frac{Sh}{e^2} \left[\frac{1}{tr\{t t^+\}} - \frac{1}{2} \left(\frac{1}{N_A} + \frac{1}{N_B} \right) \right]$

and compare these resistances to the resistance of a thickness L $L_{InAs} \rho_{InAs} \sim SR_{Fe/InAs}$ of bulk doped InAs.

Use LT ρ : $\rho_{InAs}(10^{17} \text{ cm}^{-3}) \sim 0.3 \times 10^{-4} \Omega \text{m}$

$f\Omega m^2$	In-	As-
	term	term
R _{maj}	5.5x10 ⁴	2.1×10 ⁴
R _{min}	7.1×10 ⁶	5.2x10 ⁵

 $L_{InAs} = 0.7 \ \mu m - 240 \ \mu m$

... or in terms of interface resistances

8 In (As) interface atoms in a 2x2 lateral supercell. Replace In (As) with Fe:

A small amount of disorder is sufficient to destroy the spin asymmetry of the interface resistance

Zwierzycki et al. PRB**67** (2003)

Spin-dependent transmission

High concentration of impurities where is the proportionality regime?

Spin-dependent transmission

Focus on a single substitutional Fe impurity on In site

Effect of displacing a single Fe_s

The transmission polarization is seen to depend very sensitively on the concentration and configuration of impurities

Alternatively: prevent Fe from contacting the InAs by inserting a barrier between Fe and InAs which preserves the transmission polarization

TΝ

0 Co Ni

$Fe|Au_5|InAs$

Au thickness-dependence Fe|Au_n|InAs

Effect of disorder at Fe|Au interface on the transmission polarization for Fe|Au₅|InAs

with Au

without Au

Interface sharpening? Co/Au (250-300°C): den Broeder et al PRL**60** (1988)

•Electrons can be strongly reflected at a perfect interface (no disorder) between two different metals because of bandstructure mismatch

- •The transmission through an interface with a ferromagnetic material is strongly spin-dependent
- •The spin-dependence of the interface resistance should be enough to make spininjection observable for sufficiently clean Fe/SC interfaces
- •Important to have detailed characterization of interface structure !