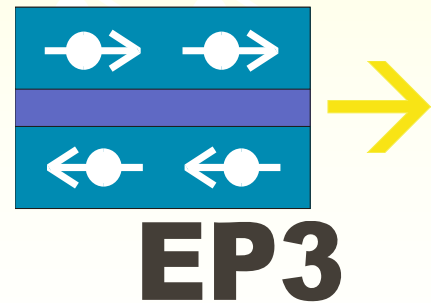
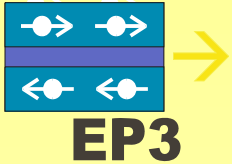


# Spintronic Nanostructures

*Laurens W. Molenkamp*  
*Physikalisches Institut (EP3)*  
*Würzburg University*





## Overview

II-VI Dilute Magnetic Semiconductors

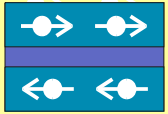
- Spin RTDs using II-VI DMSs

III-V Dilute Magnetic Semiconductors

- Tunnel AMR in GaMnAs

II-VI Narrow Gaps

- intrinsic SHE and AHE



**EP3**

## Wide gap II-VI and FM III-V DMS



- Spin RTD: voltage adjustable spin-switch; zero field spin filter
- SADs show finite spin splitting at zero B
- TAMR results from double step switching + anisotropic dos
- Why extra anisotropy along [001]?
- gives bistable hysteresis for single FM layer; is huge for two FM layers
- Details of MI transition. Do we see the Efros-Shklovskii gap?

### **Collaborators:**

**Charles Gould, Georg Schmidt, Karl Brunner,  
Peter Bach, Idriss Chado, Romain Giraud, Peter Grabs, Jian Liu, Katrin  
Pappert, Christian Rüster, Daniel Supp, Gisela Schott, Anatoly and Taras  
Slobodskyy, Tatjana Borzenko, Volkmar Hock**

**Michael Flatté, Pawel Hawrylak, Tomas Jungwirth, David Sanchez, Jairo  
Sinova**

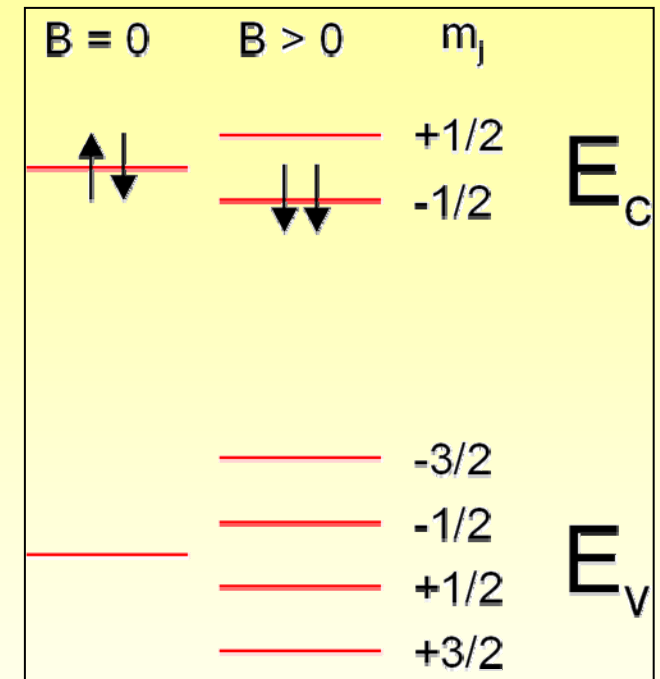


# II-VI Dilute magnetic semiconductors (DMS)



## *The 100% spin-aligner*

- II-VI Semiconductors with magnetic components (e. g. ZnMnSe), which are non-magnetic or antiferromagnetically aligned at zero B-field.
- For  $B \neq 0$ : **Finite magnetization, 'giant' Zeeman splitting** of up to 100 meV of which 10 - 20 meV in the conduction band
- Low Fermi energy at high doping due to impurity bands: half-metallic behavior at high B-field.



$\Rightarrow \beta = 100\%$  for  $kT \ll \Delta E_C$

$$g^* = g_0 - \frac{(\Delta E)_{\max}}{\mu_B B} B_{5/2} \left[ \frac{5 g_{Mn} \mu_B B}{2 k_B T (T + T_0)} \right]$$

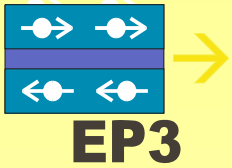
$g_{Mn}$ : g factor for Mn

$B_{5/2}$ : Brillouin function for  $S=5/2$

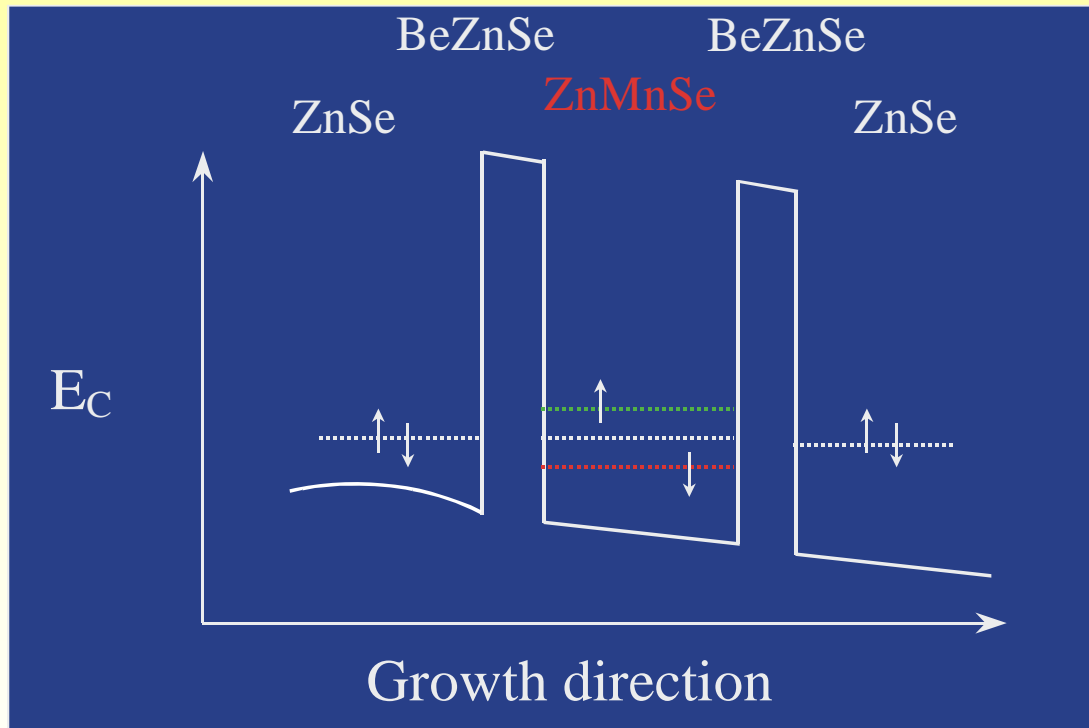
$(\Delta E)_{\max}$ : saturation spin splitting energy

$T_0$ : scaling temperature

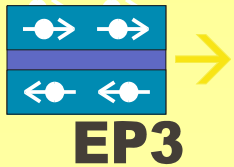
(accounts for spin spin interaction)



# (Zn,Be,Mn)Se-based Spin-switch RTD



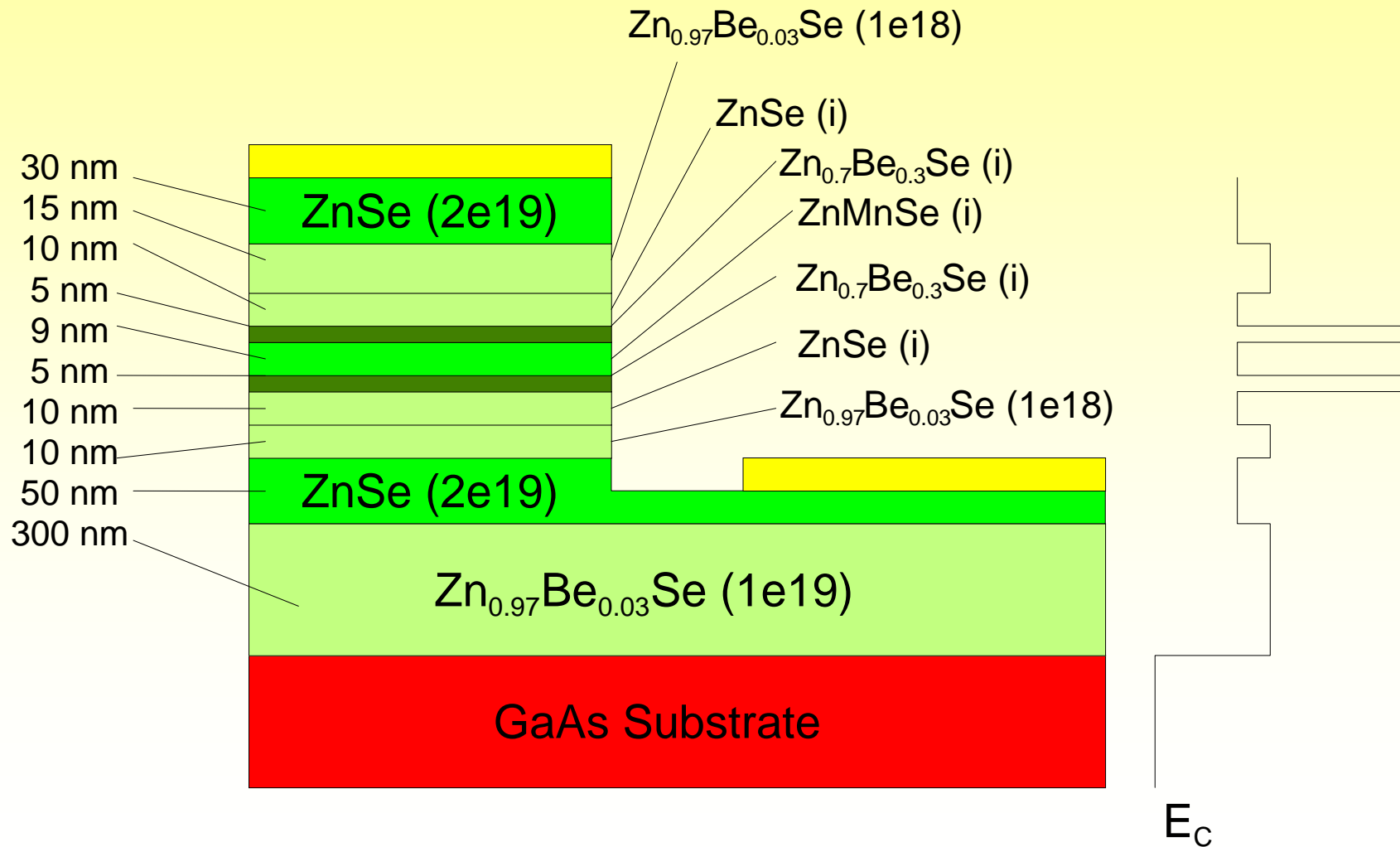
Voltage-adjustable spin selective injector and detector?

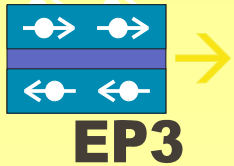


# Spin-switch RTD in the (Zn,Be,Mn)Se-System



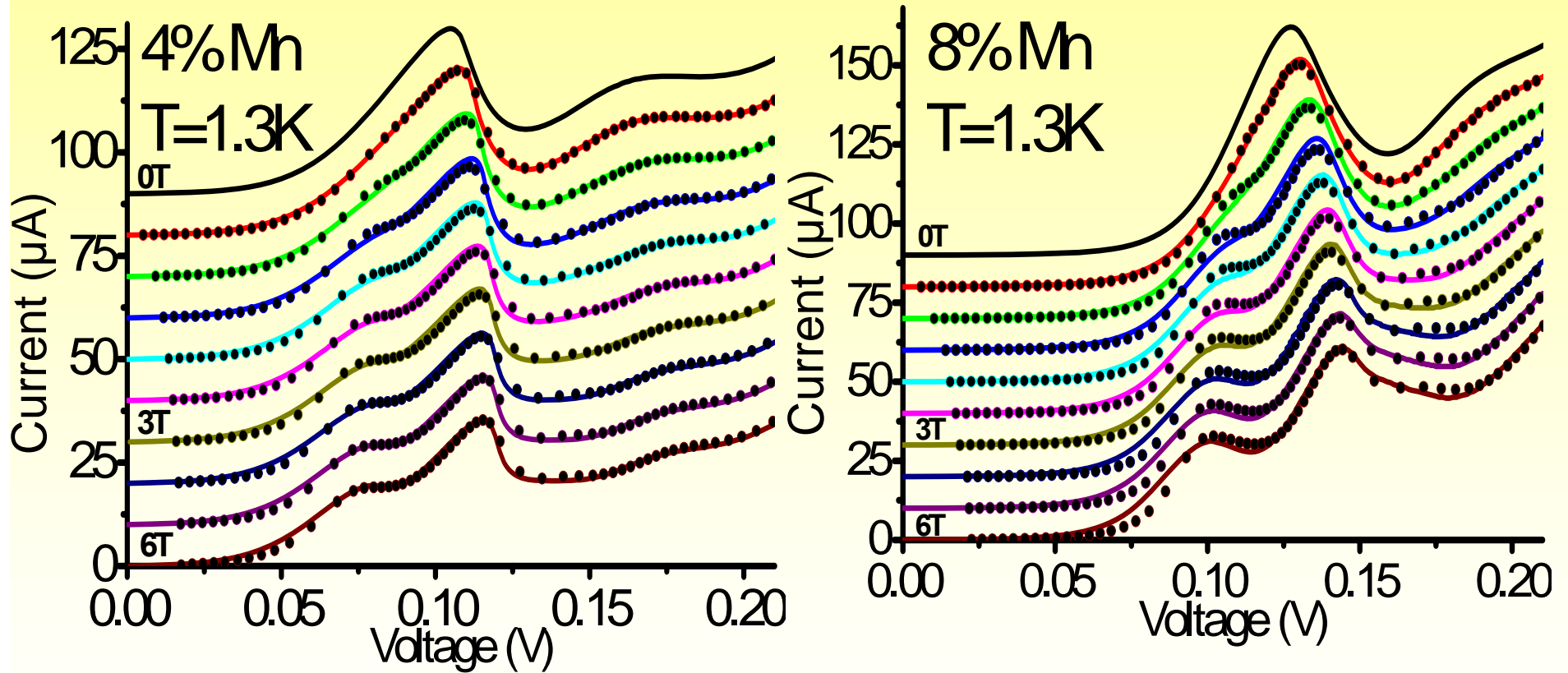
all doping n-type



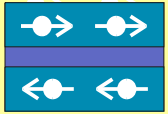


# Spin-switch RTD in the (Zn,Be,Mn)Se-System

A. Slobodskyy et al., PRL 90, 246601 (2003)

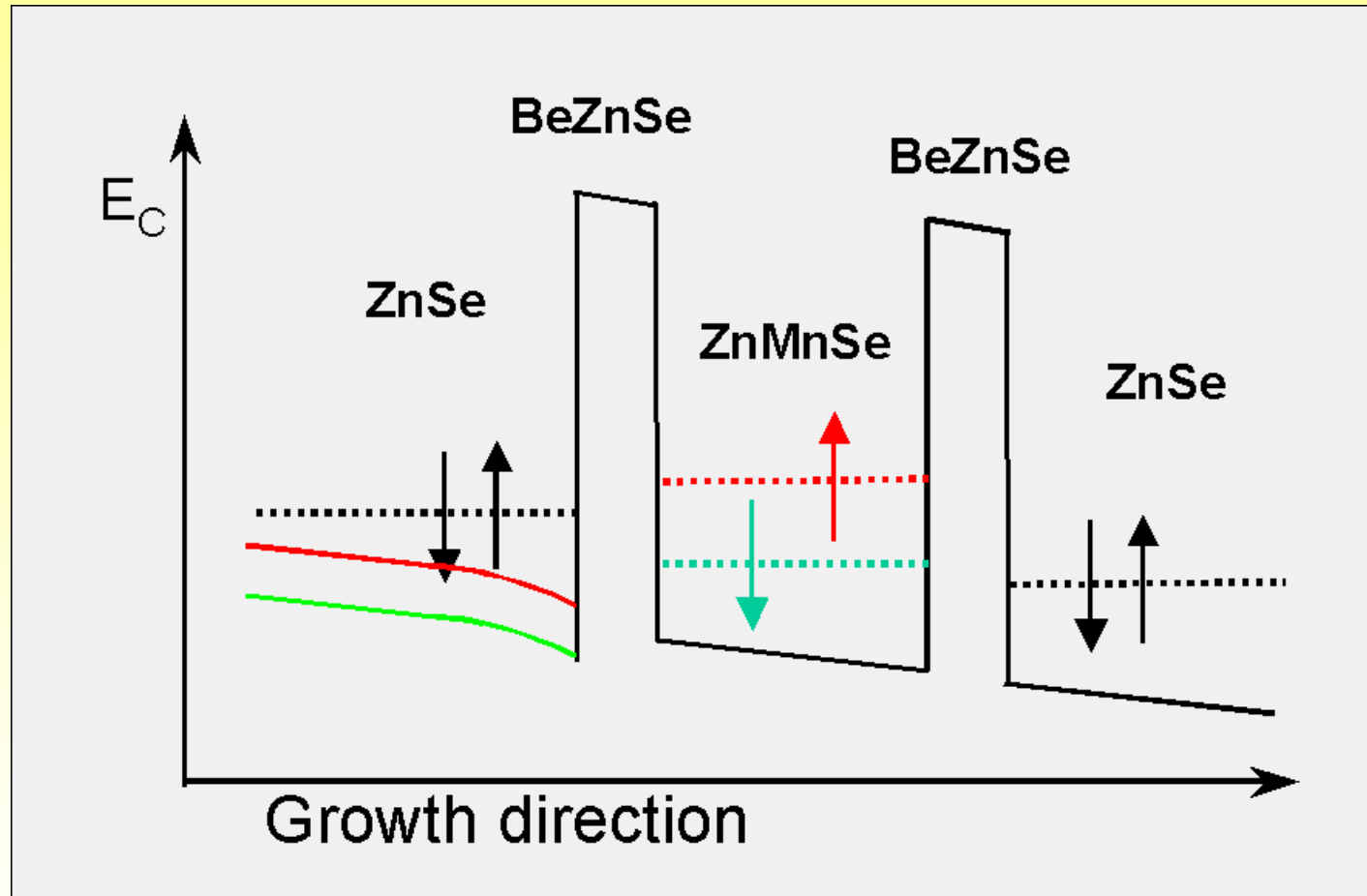


The dots are fits assuming each spin-channel has the same resonance behavior as the B=0 T signal. The fits yield the exact resonance splitting.



EP3

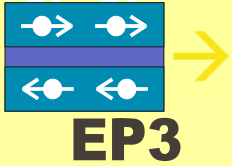
## High field band structure



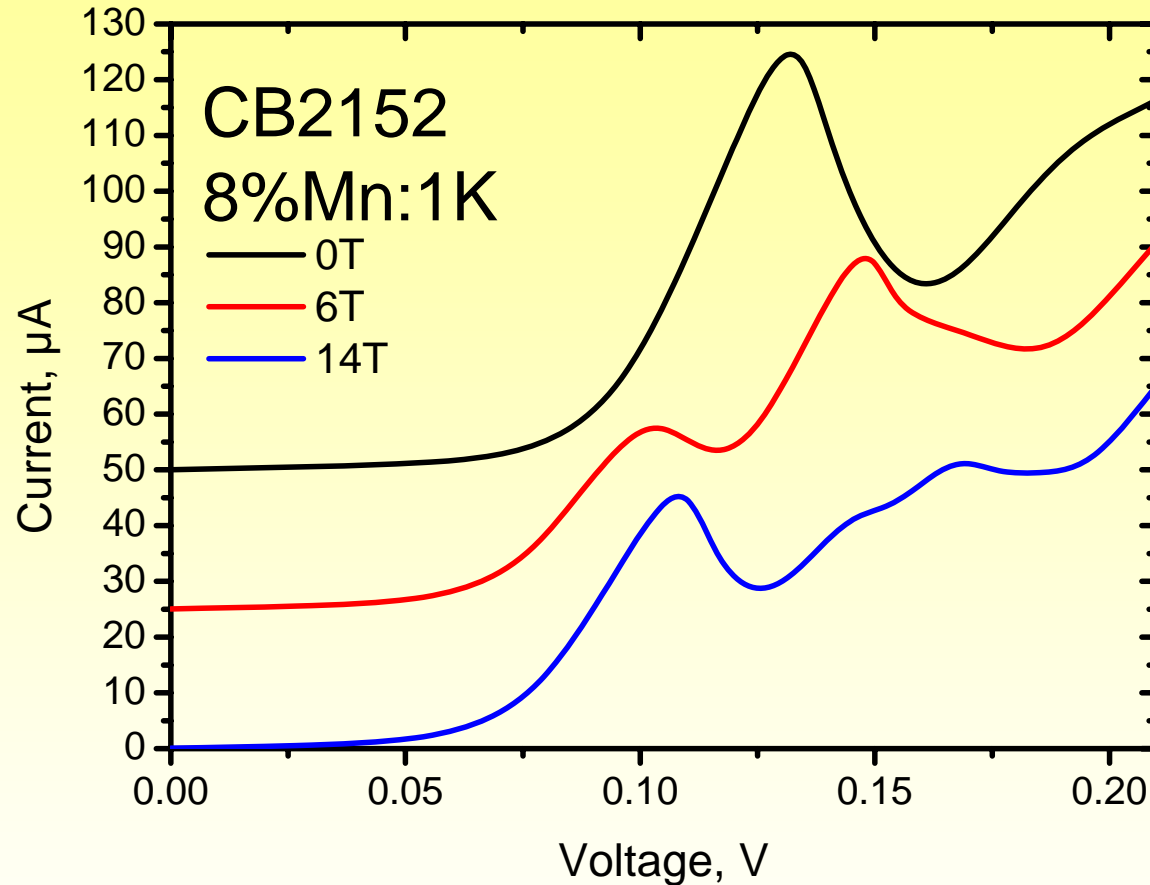
### *High fields*

- Quantized levels show constant splitting
- Conduction band in emitter shows increasing splitting

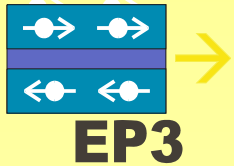




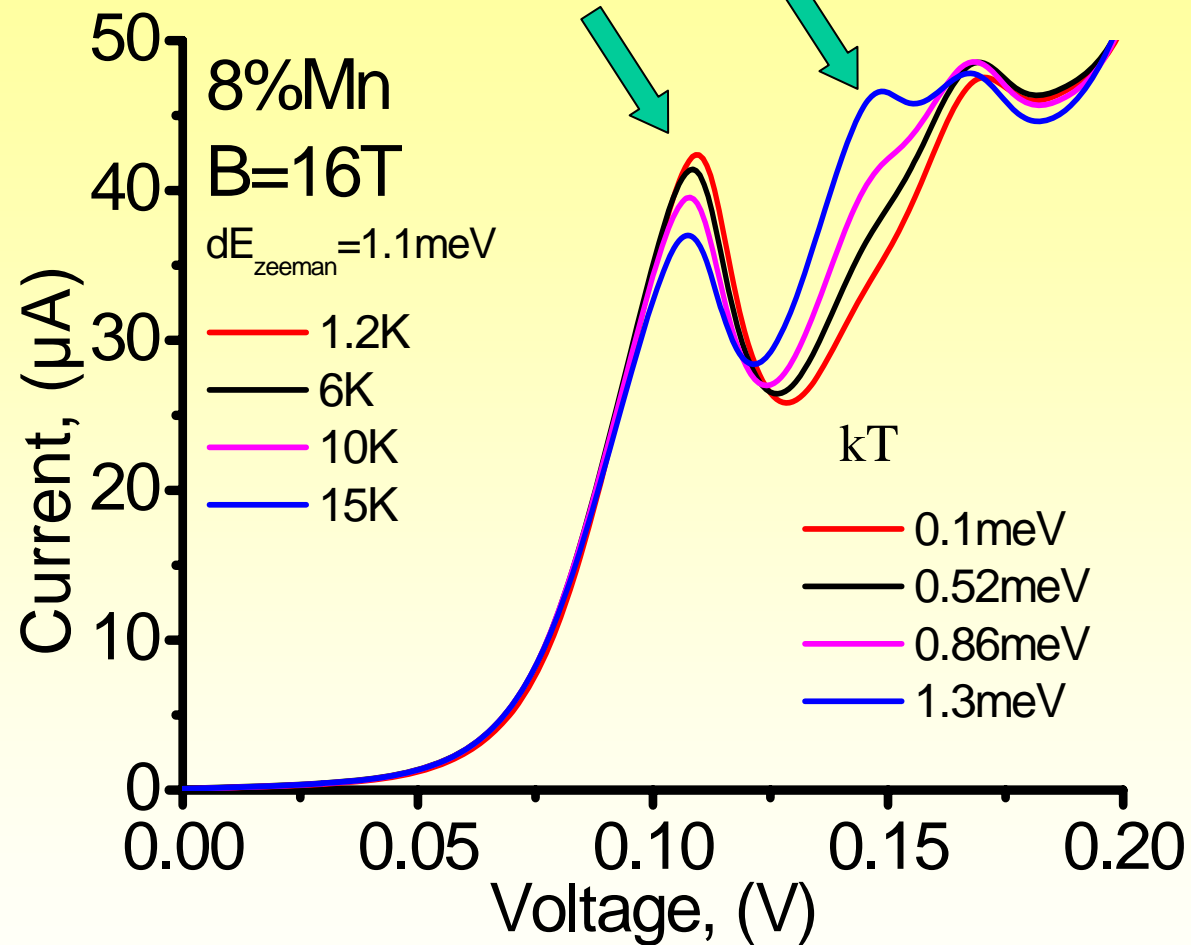
## Experiments at higher B-field



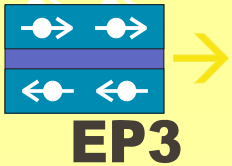
- Up to 6 T only giant Zeeman splitting is visible
- For higher fields the upper (minority) resonance is decreased due to spin polarisation in the ZnSe leads.



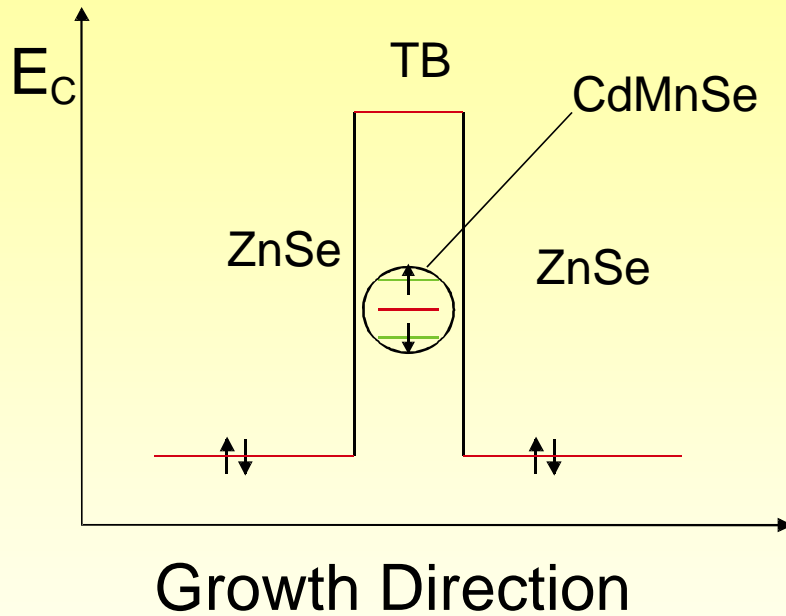
## Experiments at higher B-field



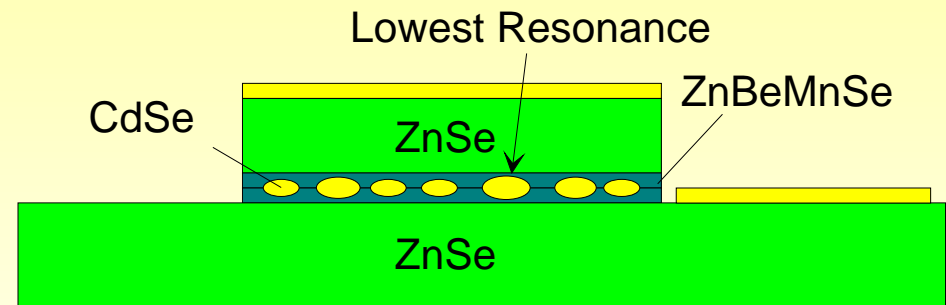
I/V curves at different temperatures with constant Zeeman splitting in emitter  
Modeling in collaboration with David Sanchez (University of the Balears)  
Need numbers for the spin relaxation time!



# RTDs with self-assembled dots

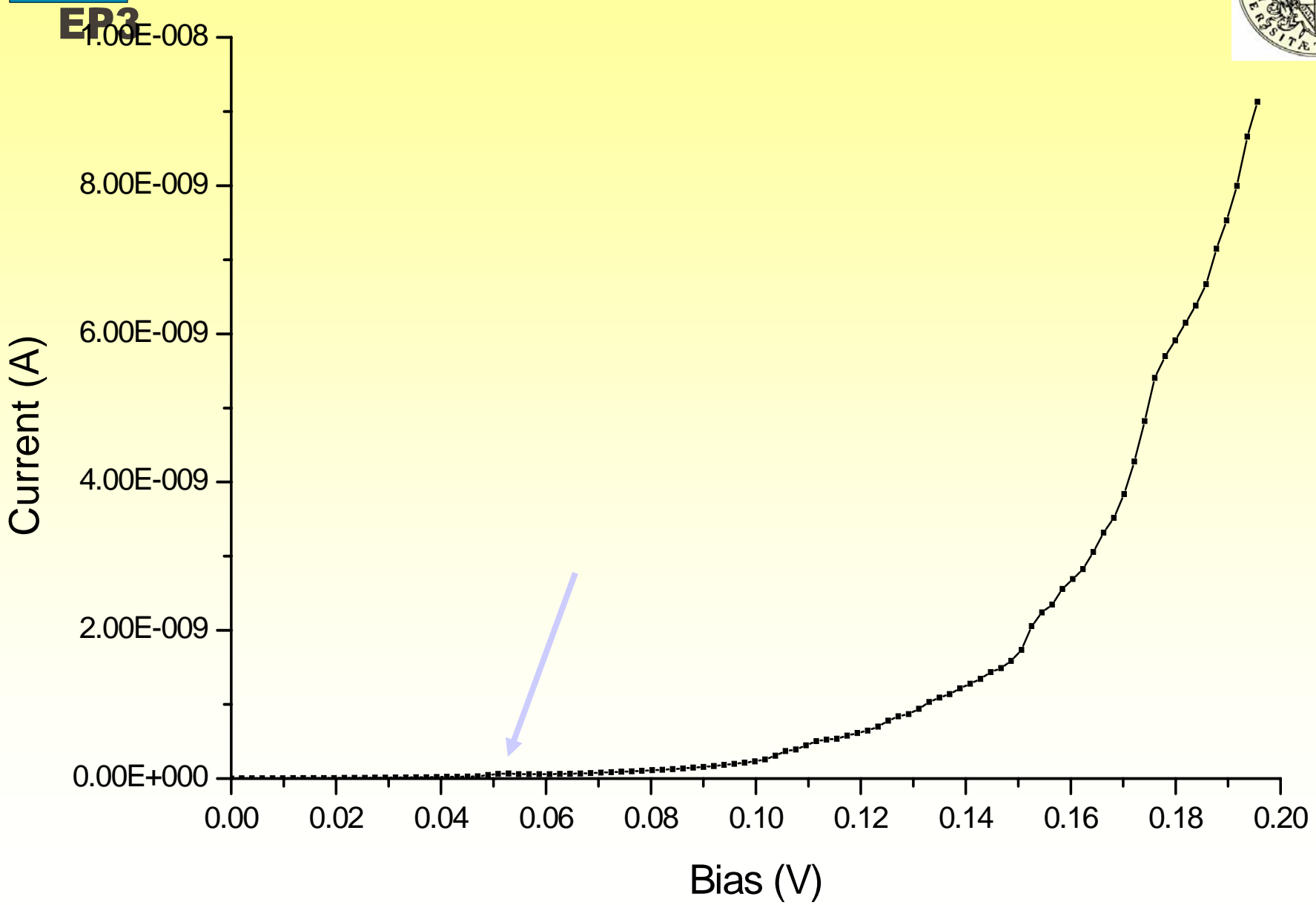
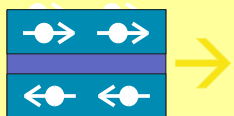


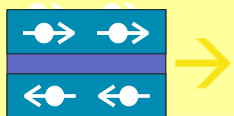
principle



in practice: Mn in barrier

Fabricate sub-micron RTD, largest dot dominates at small bias.

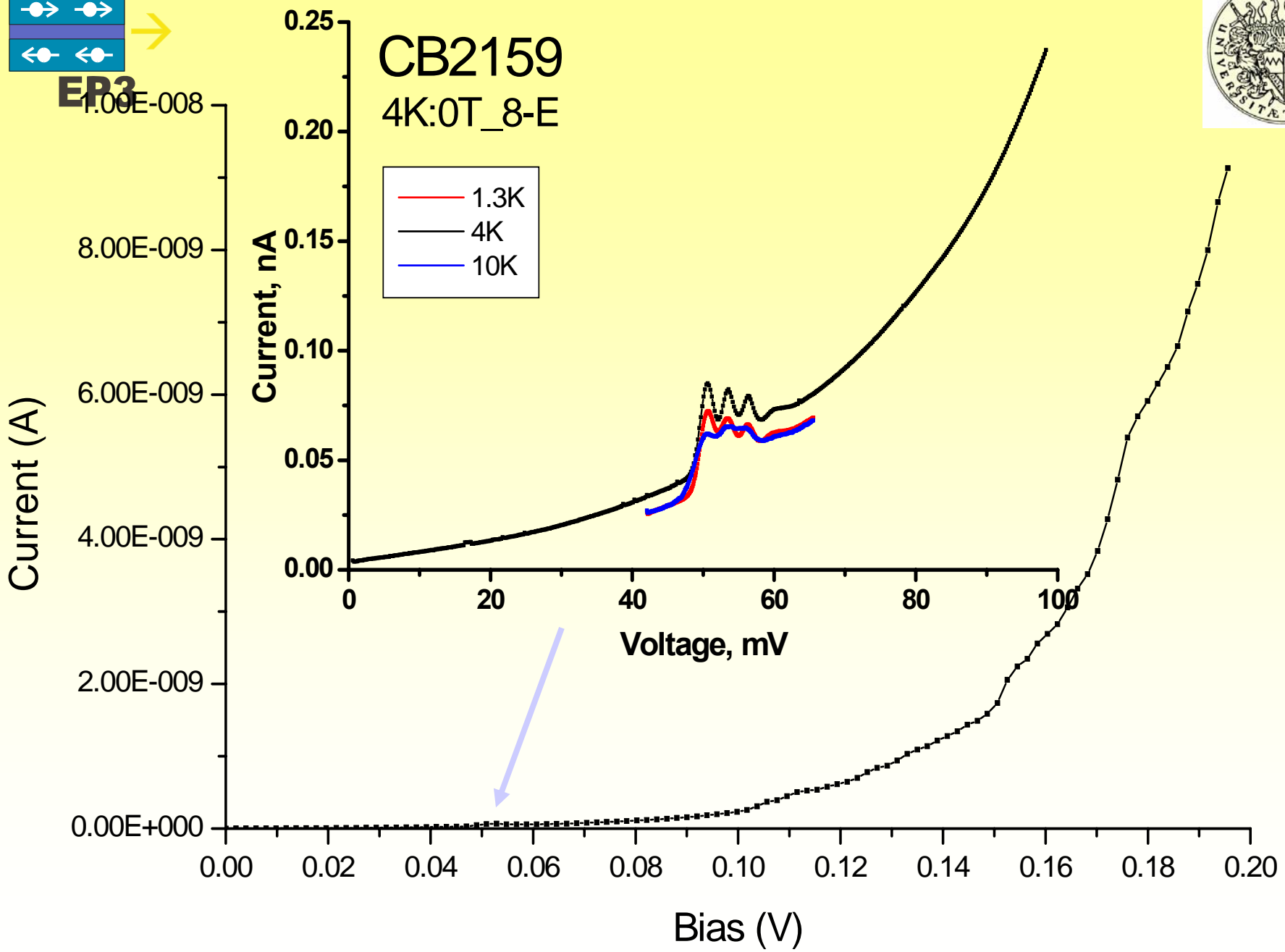


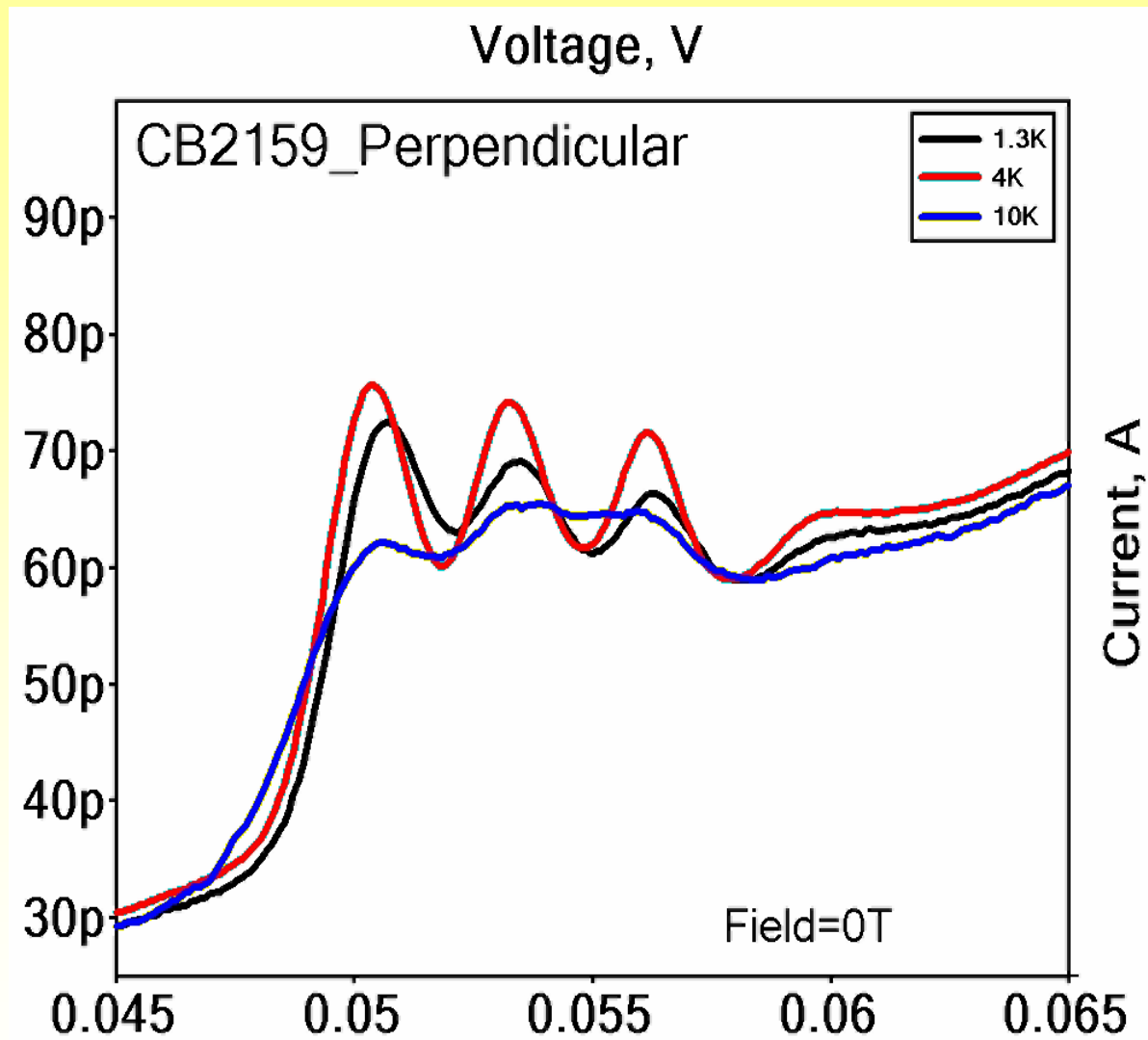
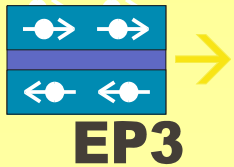


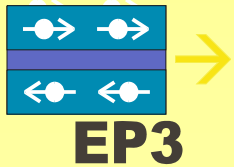
EP3



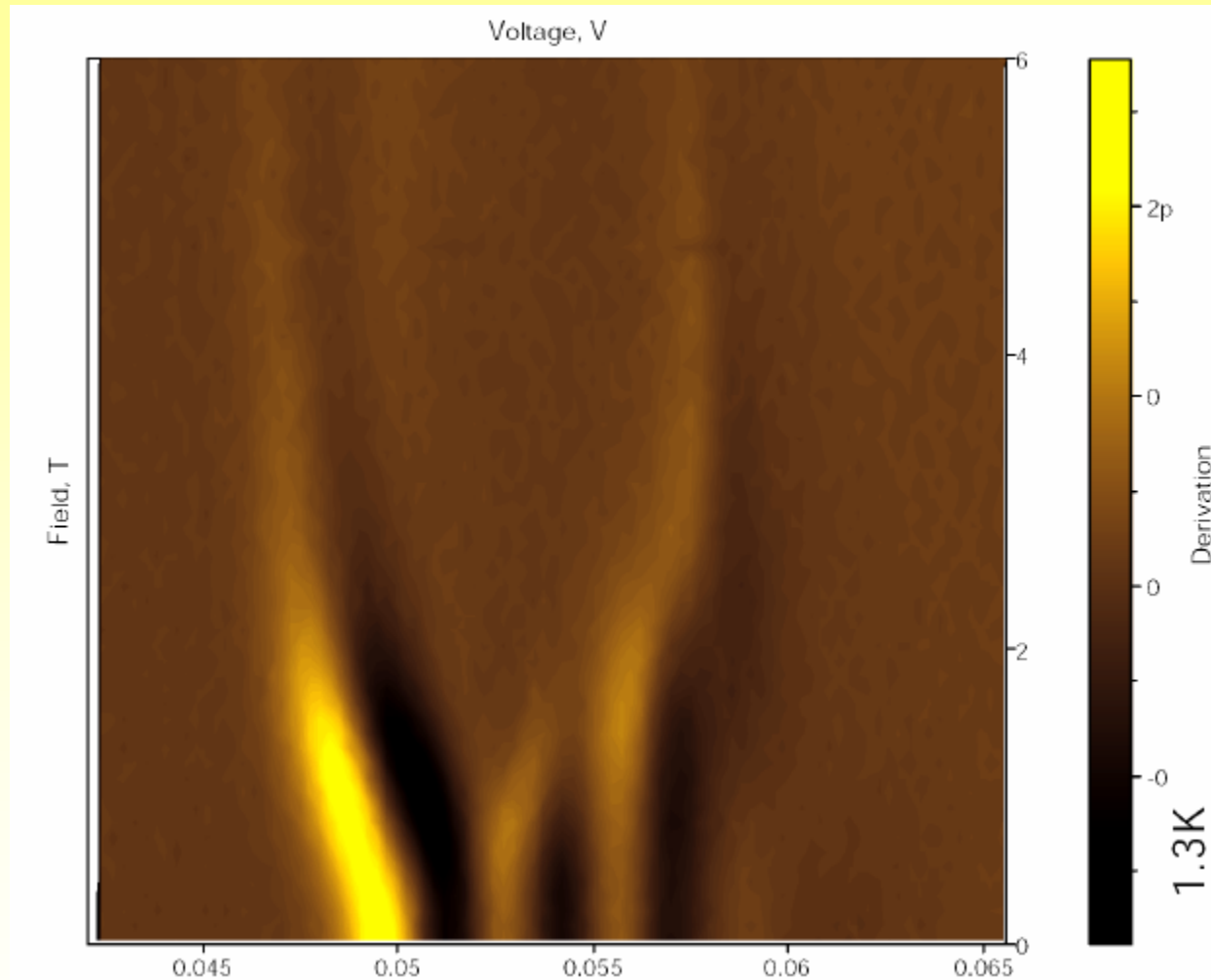
CB2159  
4K:0T\_8-E



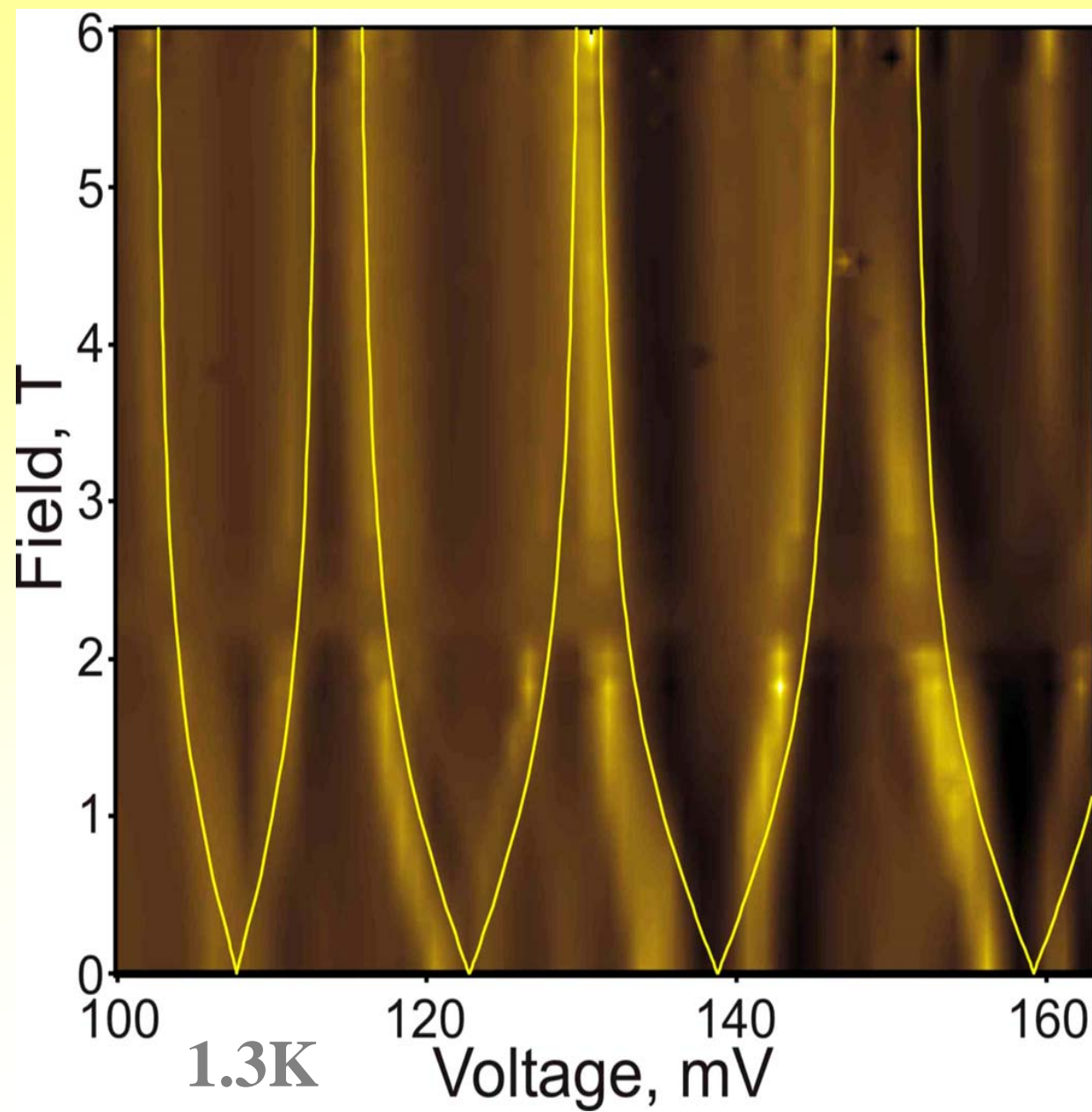
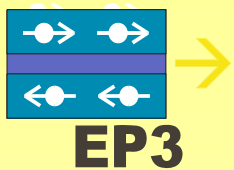




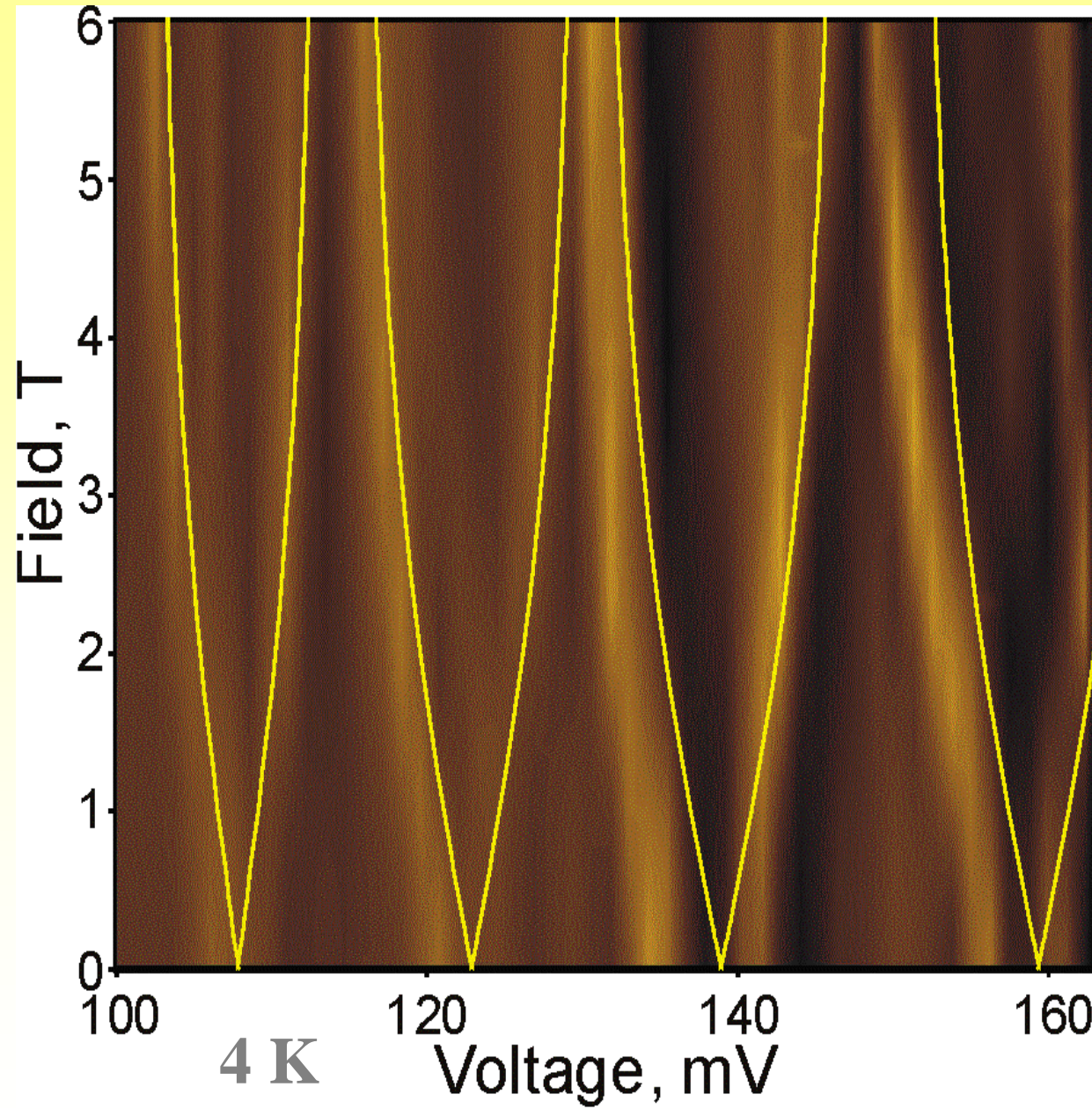
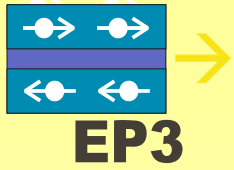
## RTDs with self-assembled dots



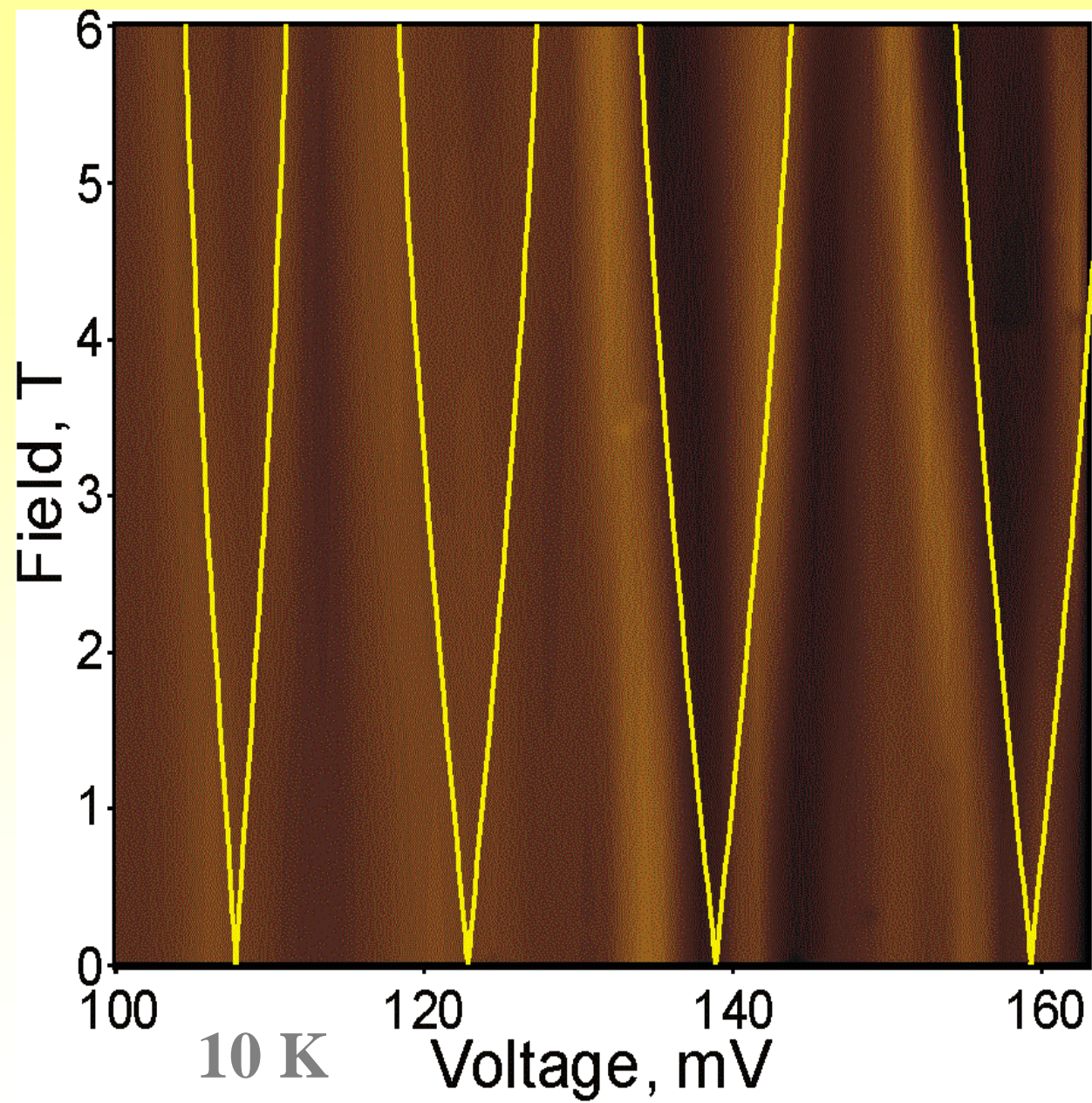
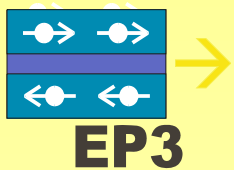
- Clear evidence that barrier Mn mixes with dot wave functions.
- Anti-crossing plus Zeeman pair imply single dot
- Single spin levels at zero field

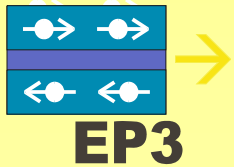










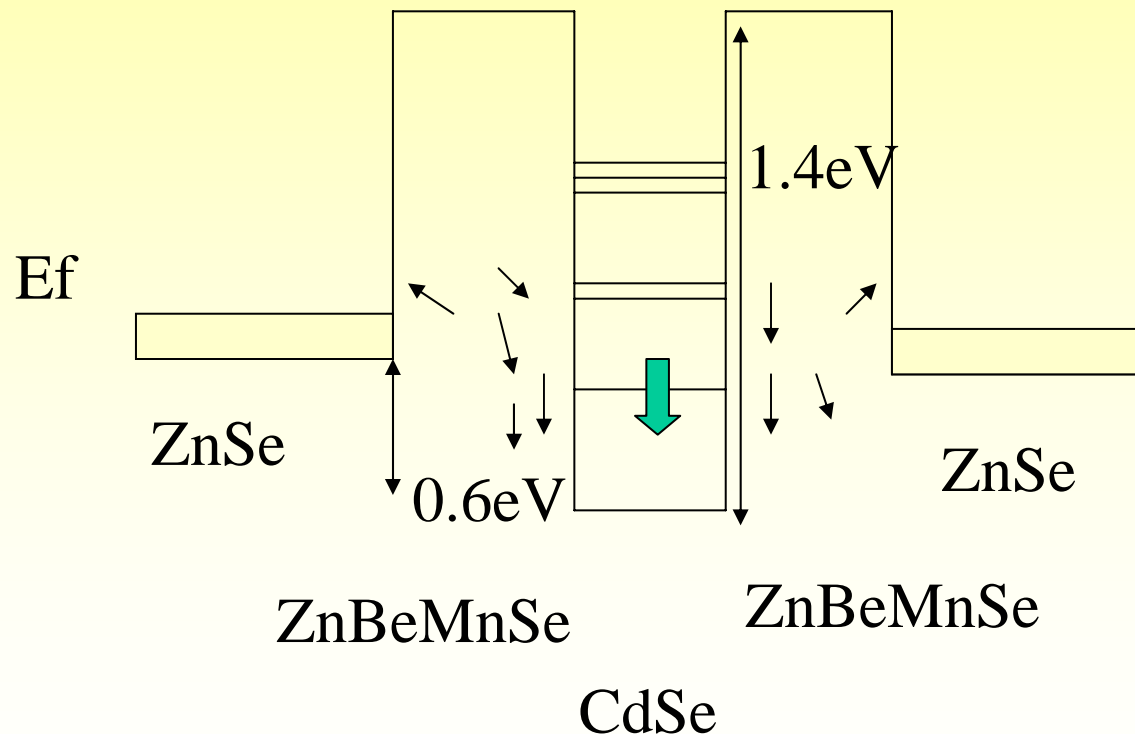


## Tunneling structure



electrons in the dot lead to ferromagnetic arrangement of Mn ions

→ effective spin splitting of the tunneling structure

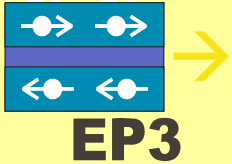


Quantum dot as single magnetic polaron

P. Hawrylak, NRC

Previous theories by  
A. Efros, et al., PRL  
L. Brey, et al., PRL

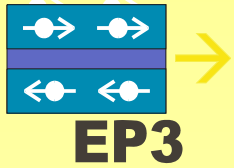
Need to extend Efros/Rashba theory to more spins.



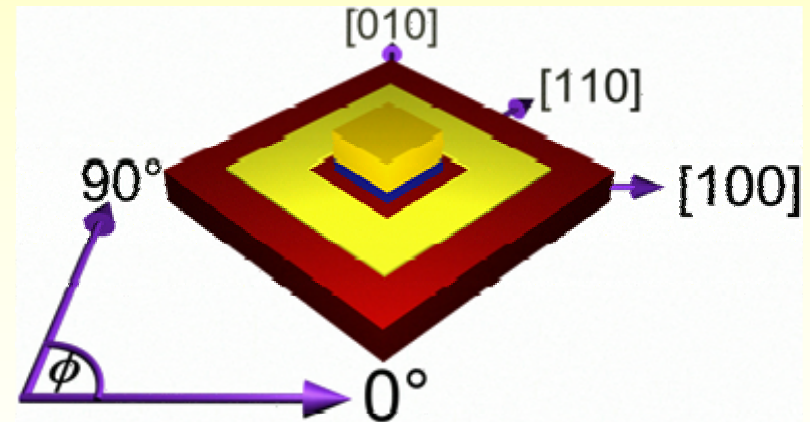
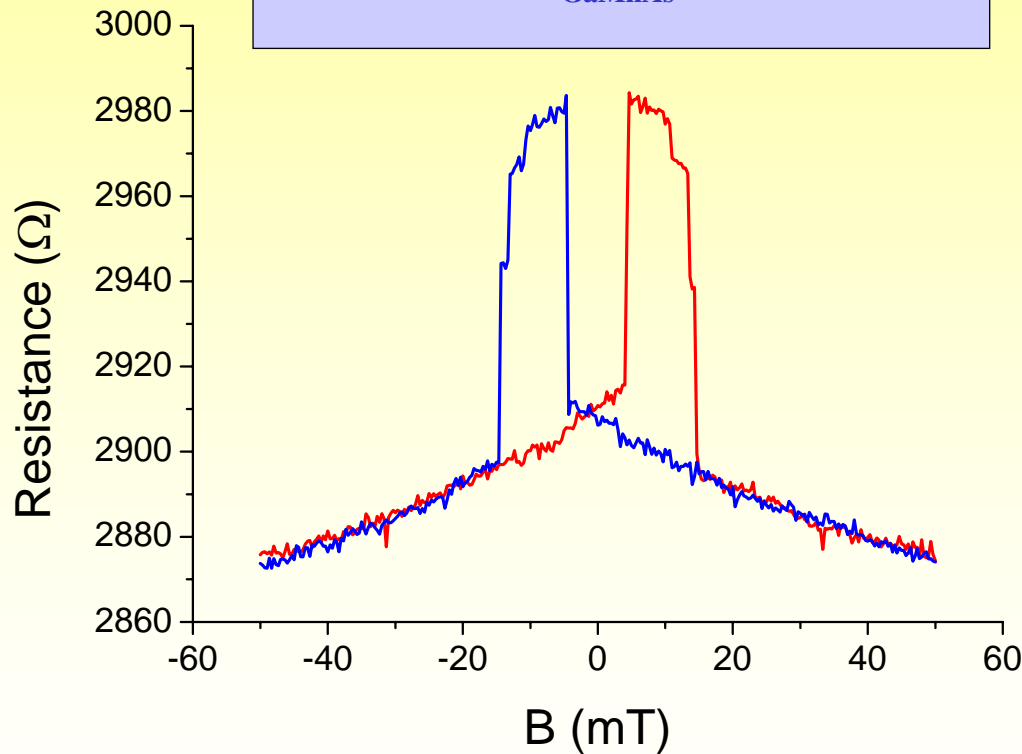
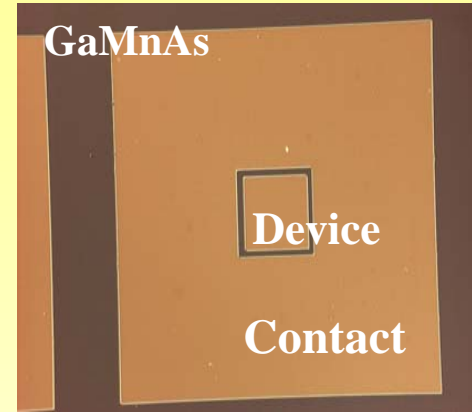
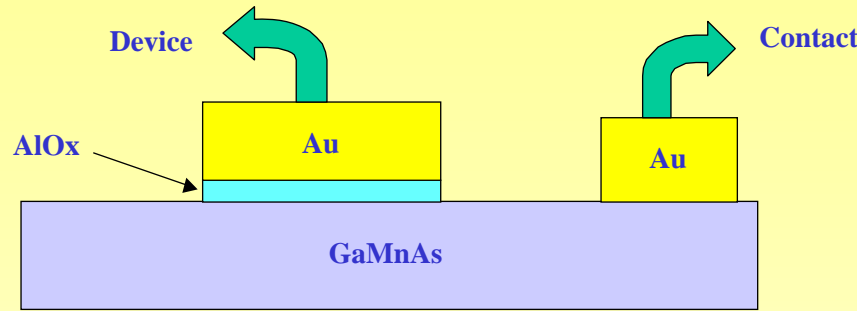
## III-V DMS: (Ga,Mn)As



- GaAs with typically 1 to 8% Mn
- Grown at  $\sim 220^\circ$  to prevent MnAs formation.
- Exhibits carrier mediated ferromagnetism.
- Mn substitutes on Ga sites 😊 (acceptor) or goes in interstitially ☹️ (donor)
- Tc around 70K as grown, 150 K with annealing is routine.  
Current WR: Nottingham 173K; Tanaka 250K in 2D layers.
- Always p-type .
- Basically metallic transport  $T_{4k} \sim T_{room}$
- Complex anisotropy both in transport and magnetism.
- Very large domains (mm's)

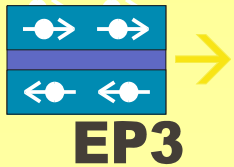


# TAMR in (Ga,Mn)As/AlOx/metal

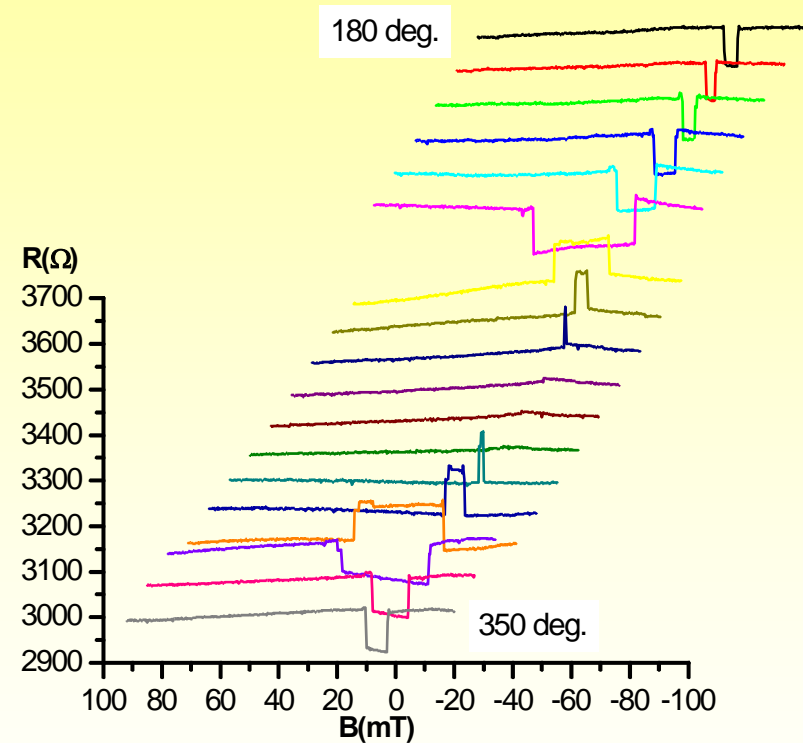
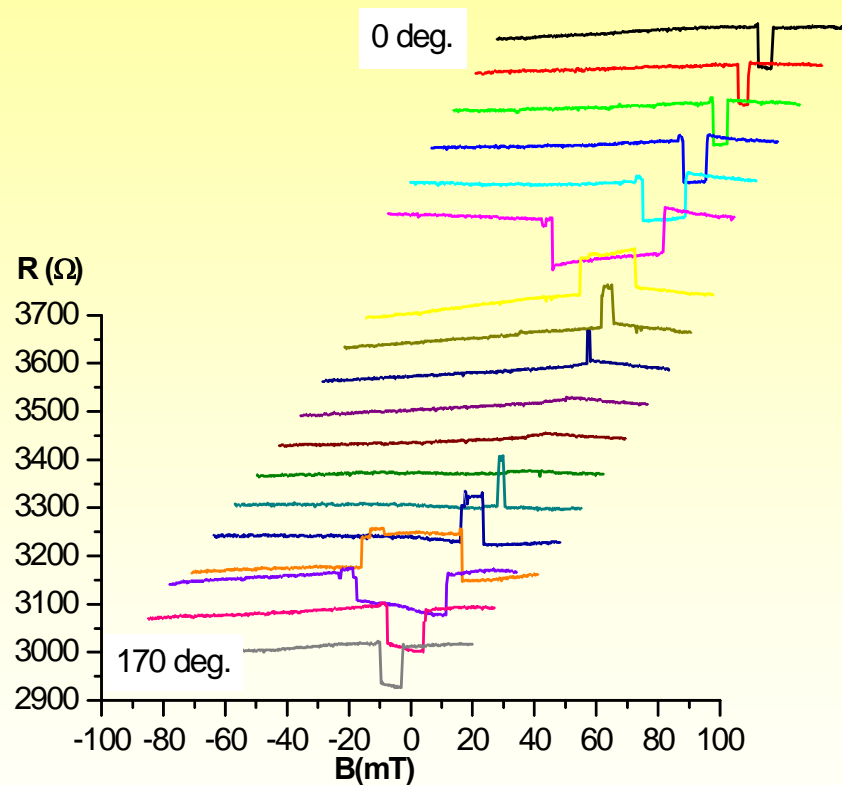


A tunnel barrier between a non-magnetic metal (Au) and ferromagnetic (Ga,Mn)As can exhibit a huge magnetoresistance that can show the signature of a spin valve.

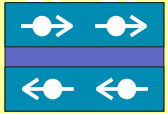




# Spin-Valve like TMR in (Ga,Mn)As/AlO<sub>x</sub>/Non-magnet devices



Dependence of the magnetoresistance effect on the in-plane field angle (angle with respect to [100]).



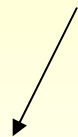
EP3

## (Ga,Mn)As has biaxial magnetic anisotropy



Total energy of a single domain:

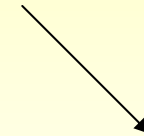
$$E_m = K_u \sin^2(\theta) + K_c \sin^2(2\theta) - MH \cos(\theta - \varphi)$$



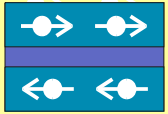
**Co-linear** uniaxial  
anisotropy



Biaxial  
anisotropy



Zeeman  
energy



EP3

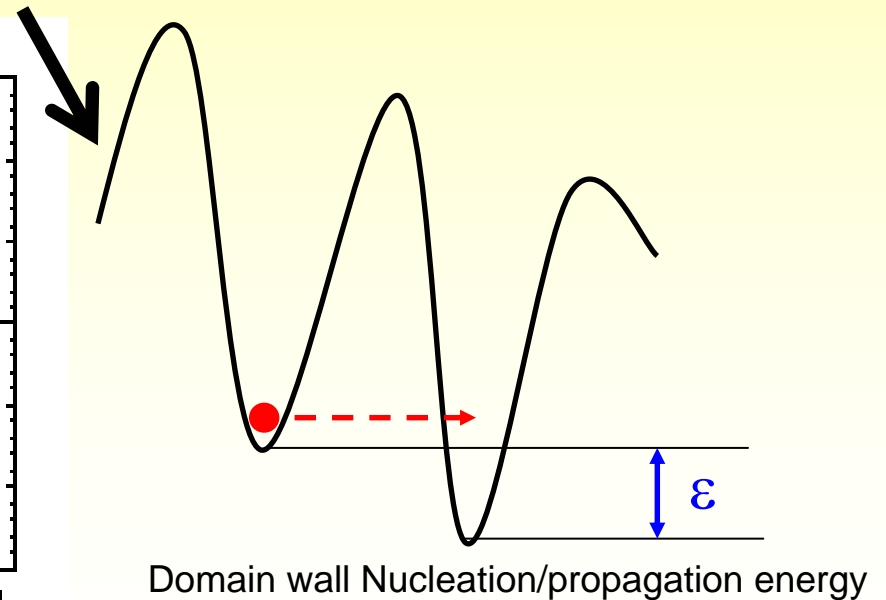
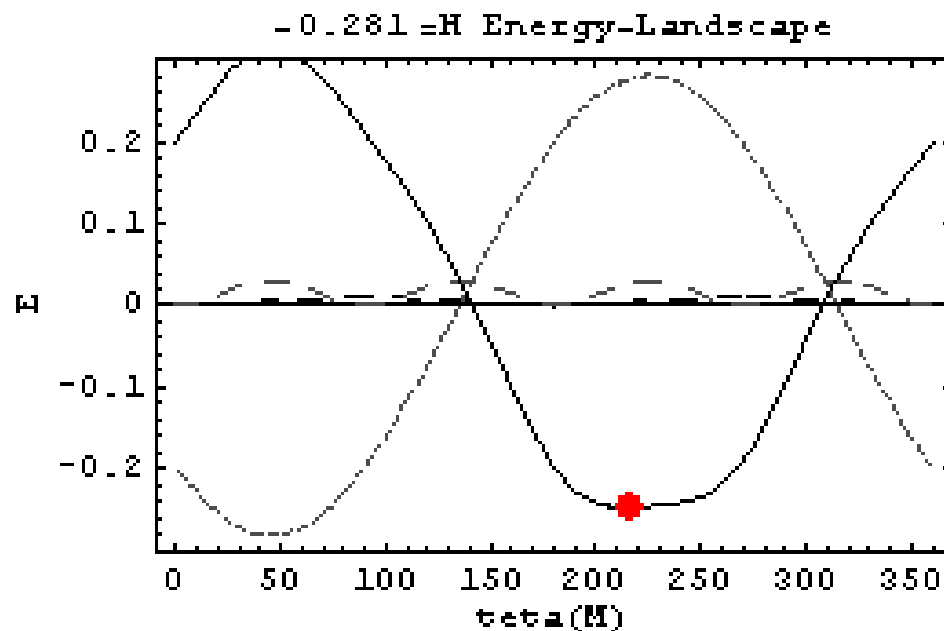
## Double step switching



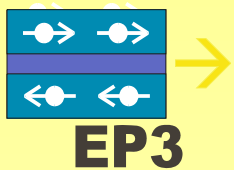
$$E_m = K_u \sin^2(\theta) + K_c \sin^2(2\theta) - MH \cos(\theta - \varphi)$$

-Coherent rotation a la Stoner-Wohlfarth.

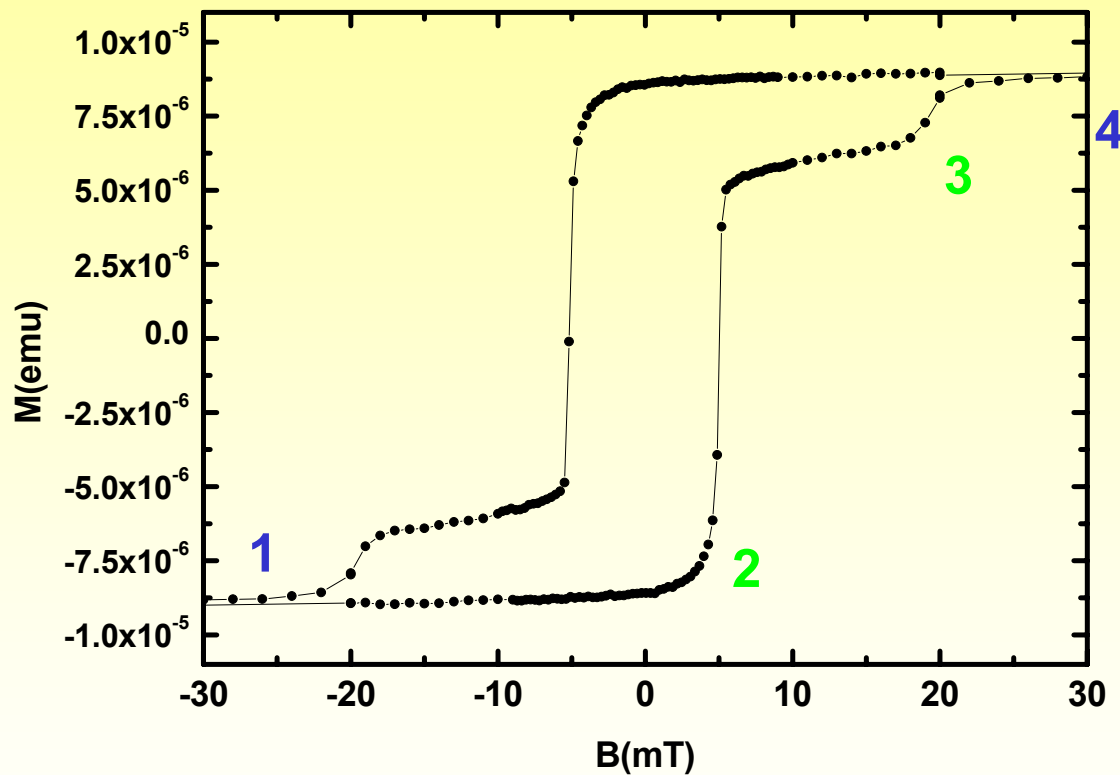
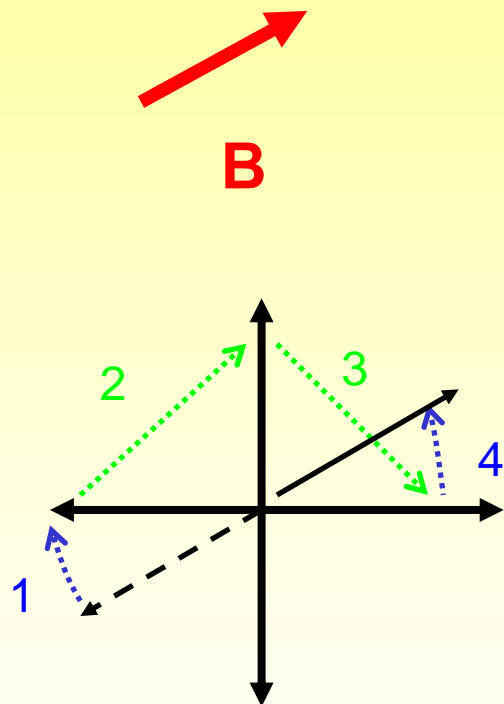
-Domain wall nucleation and propagation.



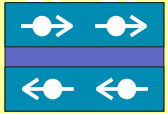




# SQUID Signature

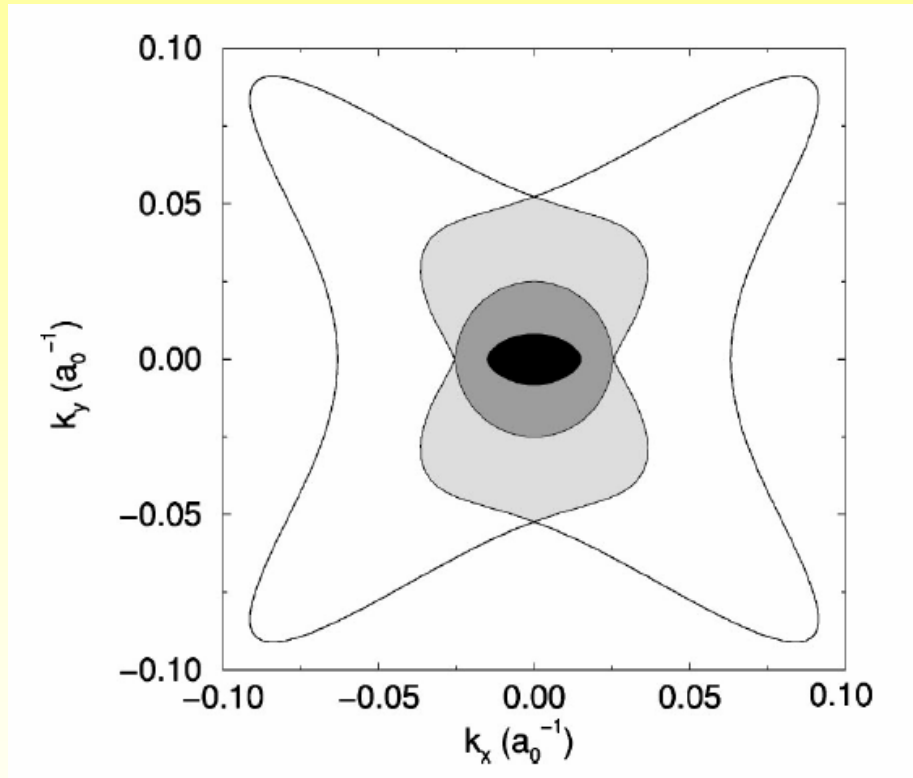


Double-step switching

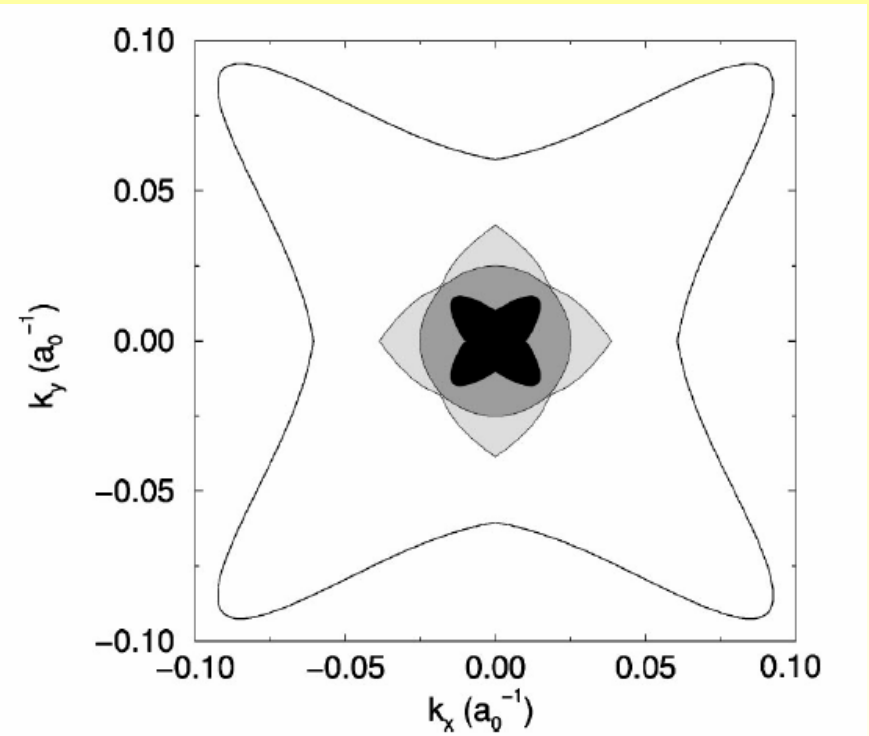


EP3

Total dos of valence band strongly anisotropic.

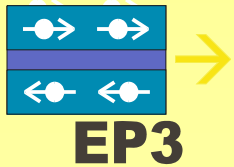


B // [100]

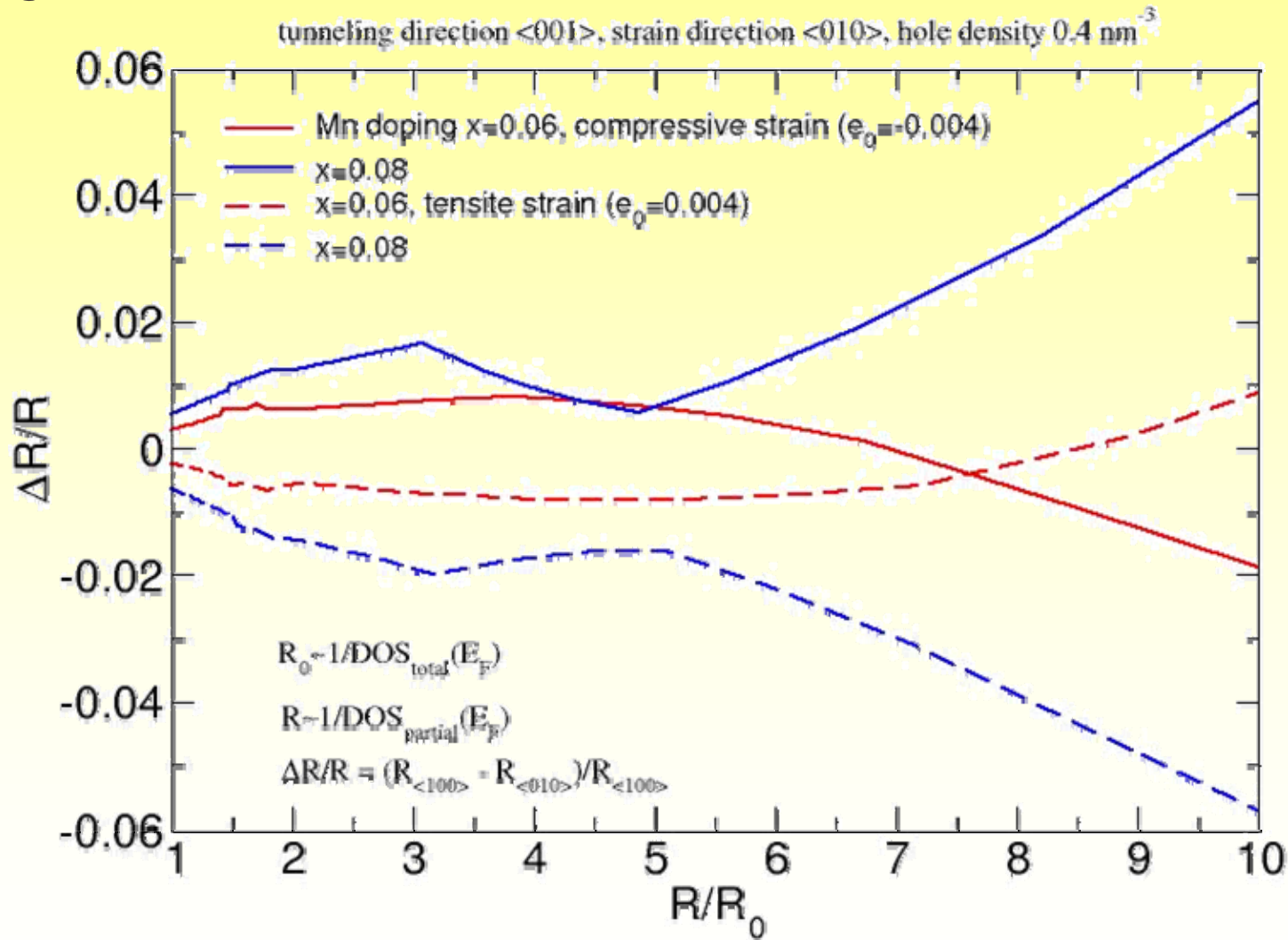


B // [110]

Abolfath et al., Phys. Rev. B 63, 054418 (2000).

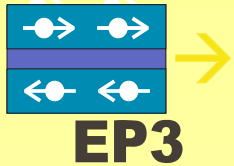


# Theory: TAMR in (Ga,Mn)As/AlOx/metal devices

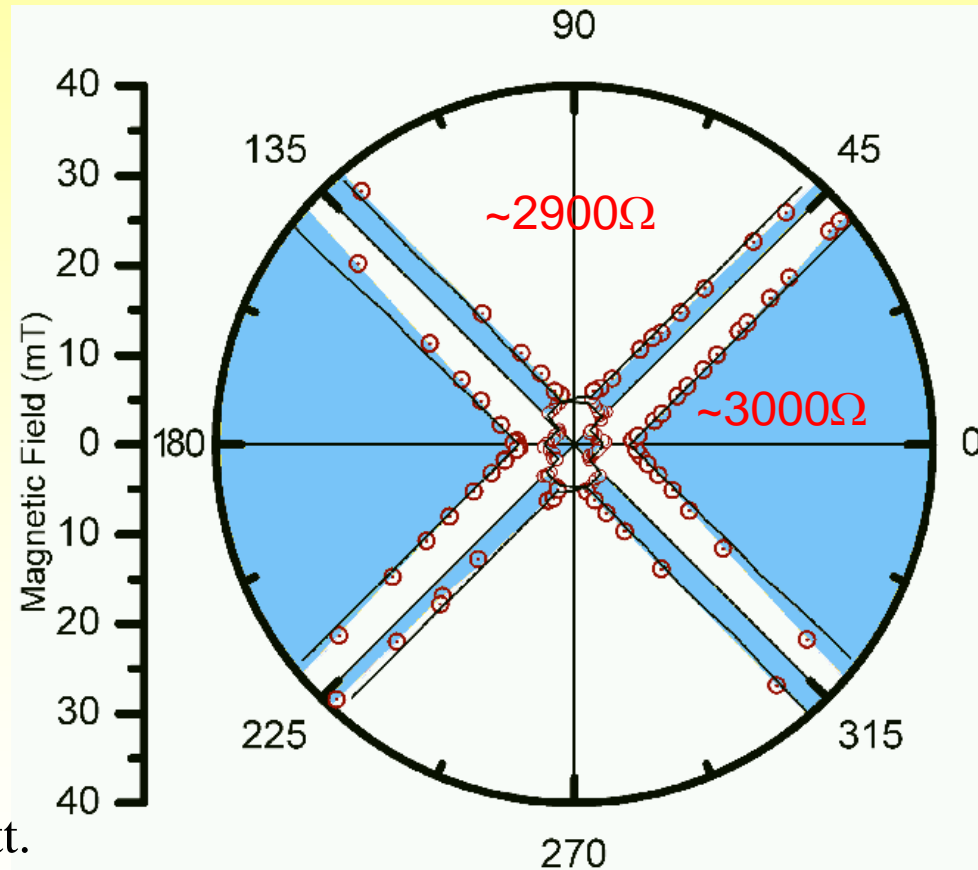
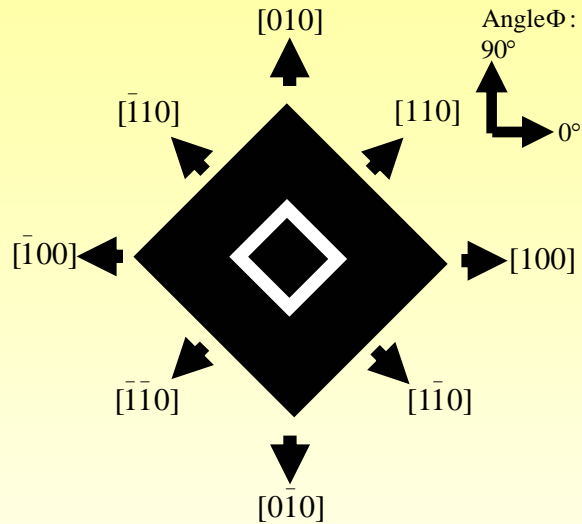


Increasing in-plane momentum conservation  $\longrightarrow$

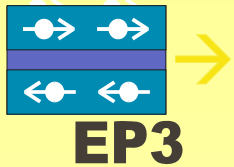
T. Jungwirth



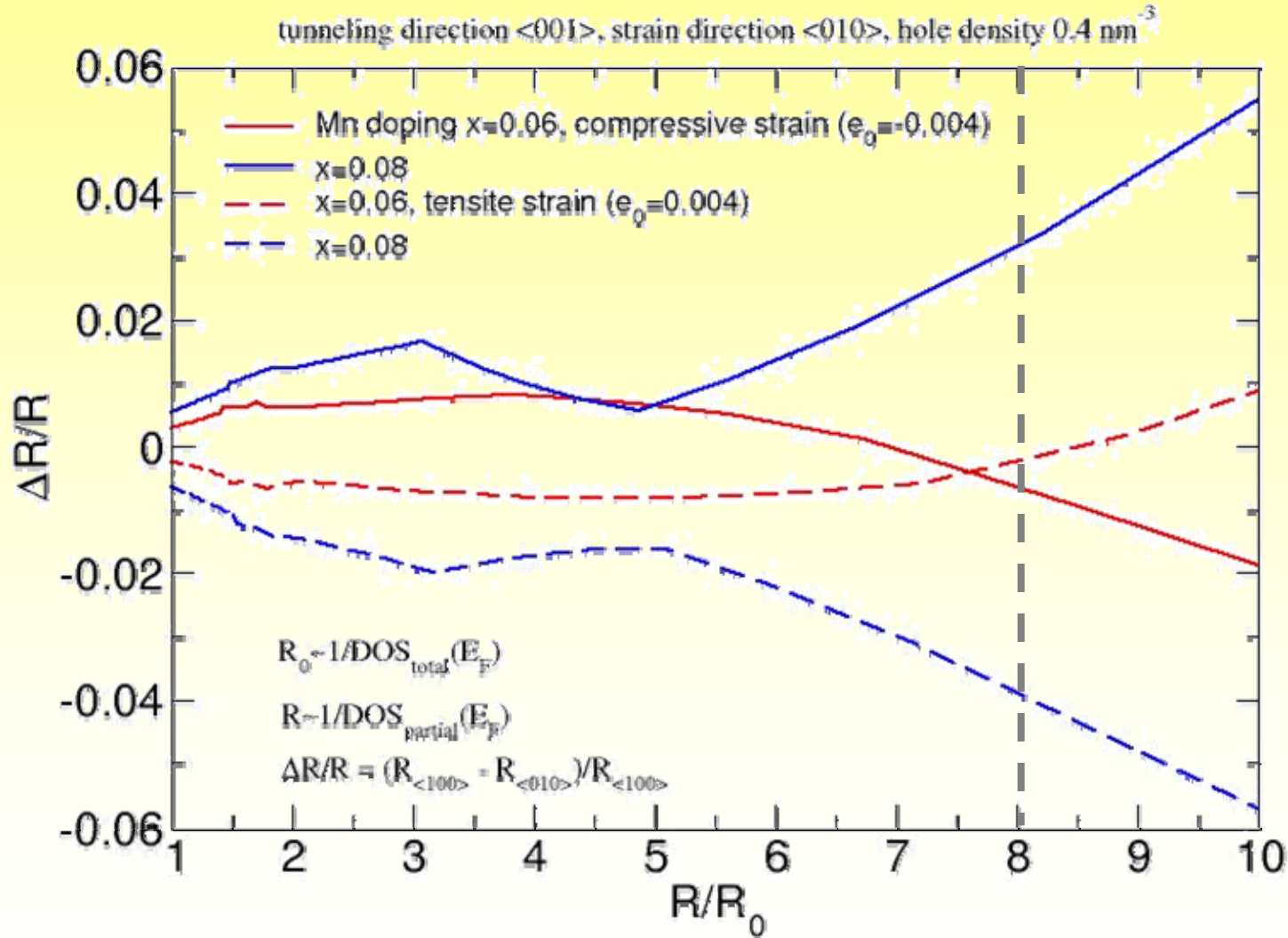
# Comparing Theory and Experiment



C. Gould et al., Phys. Rev. Lett.  
**93**, 117203 (2004).

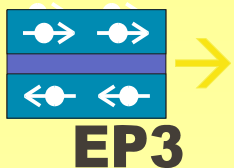


# Theory: TAMR in (Ga,Mn)As/AlOx/metal devices

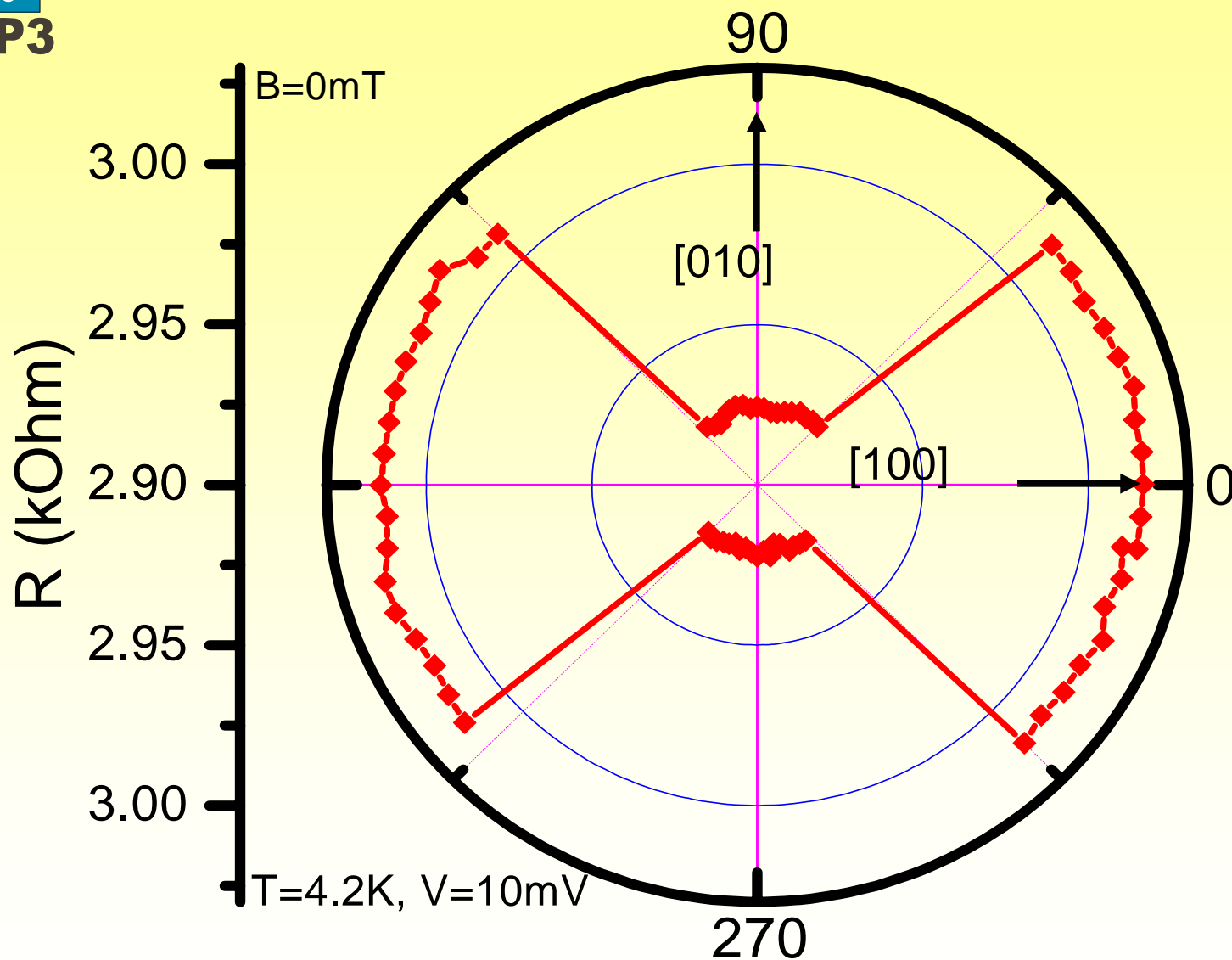


Increasing in-plane momentum conservation  $\longrightarrow$

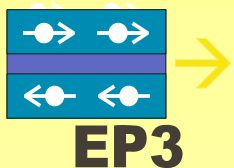
T. Jungwirth



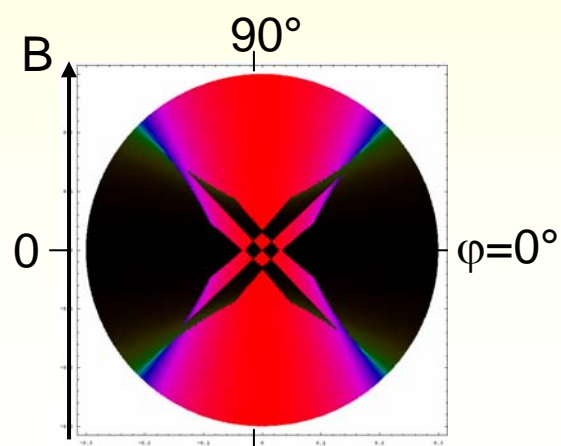
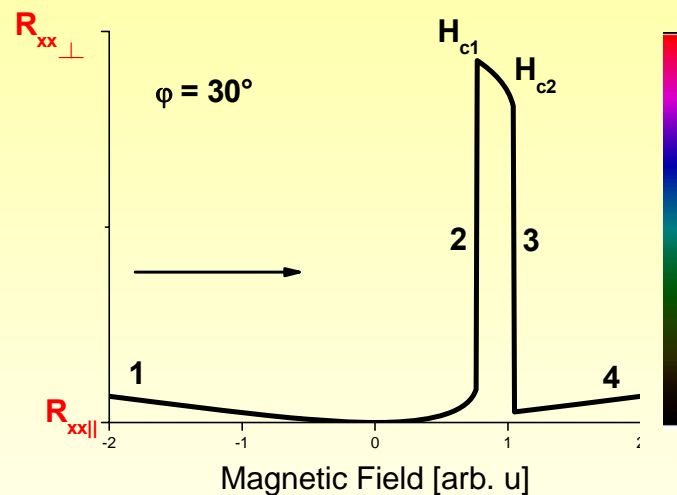
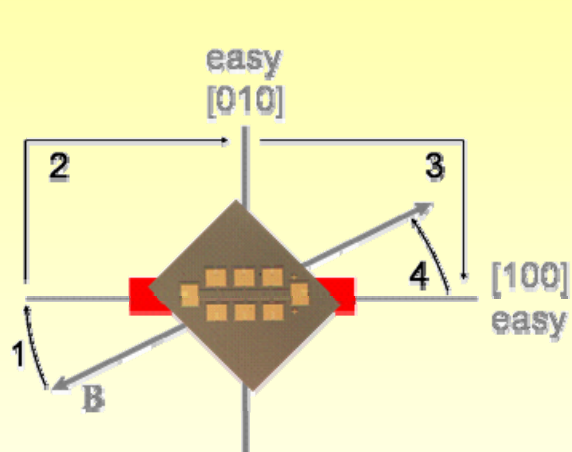
# A READ-WRITE MEMORY DEVICE!



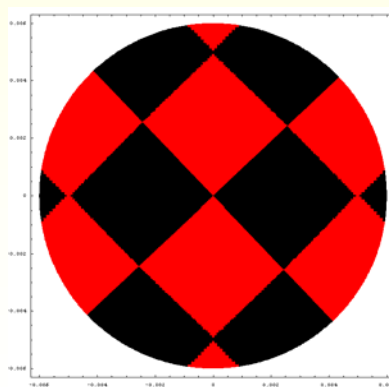
Resistance at  $B=0\text{mT}$



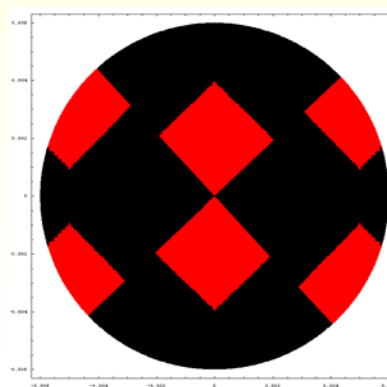
## Transport Characterization of (Ga,Mn)As Magnetic Anisotropy



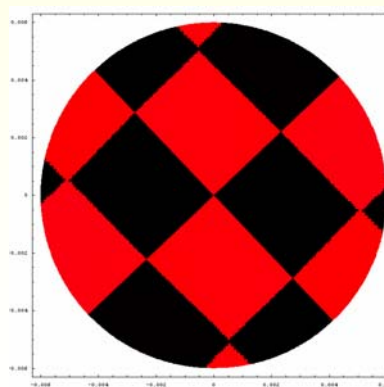
Typical at 4 K



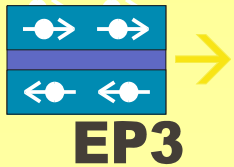
Biaxial anisotropy



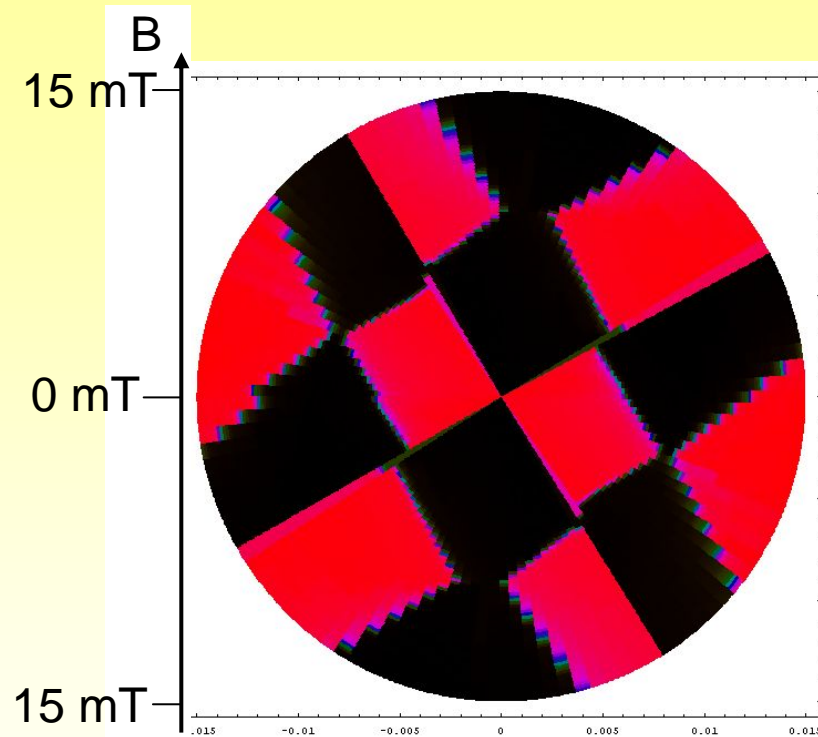
+ small uniaxial ||0° + uniaxial ||45°







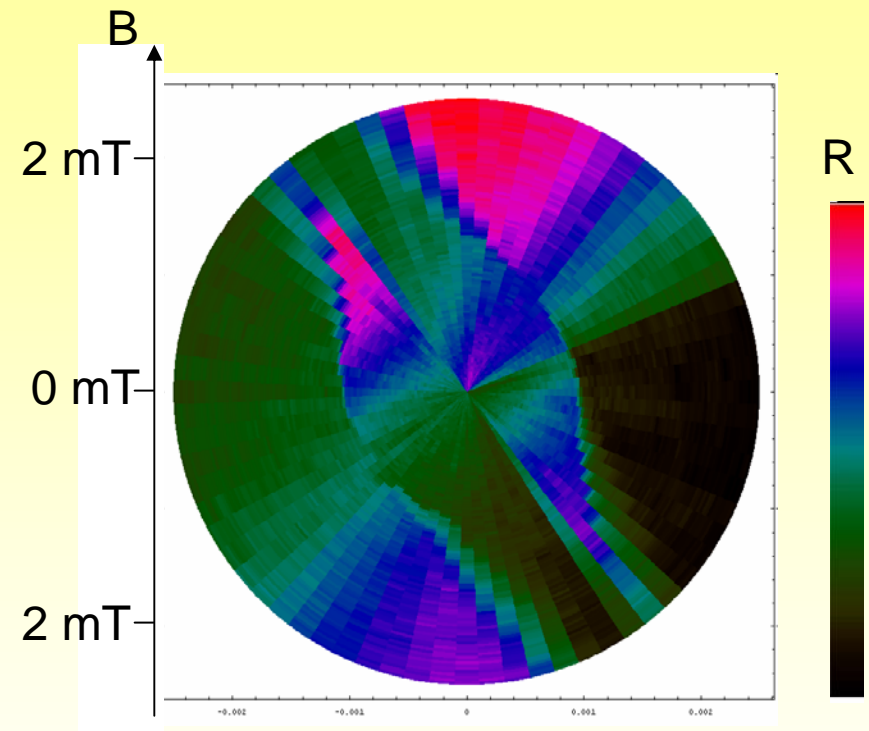
# Results



4.2K

Open corners evidence [001] is indeed easier.

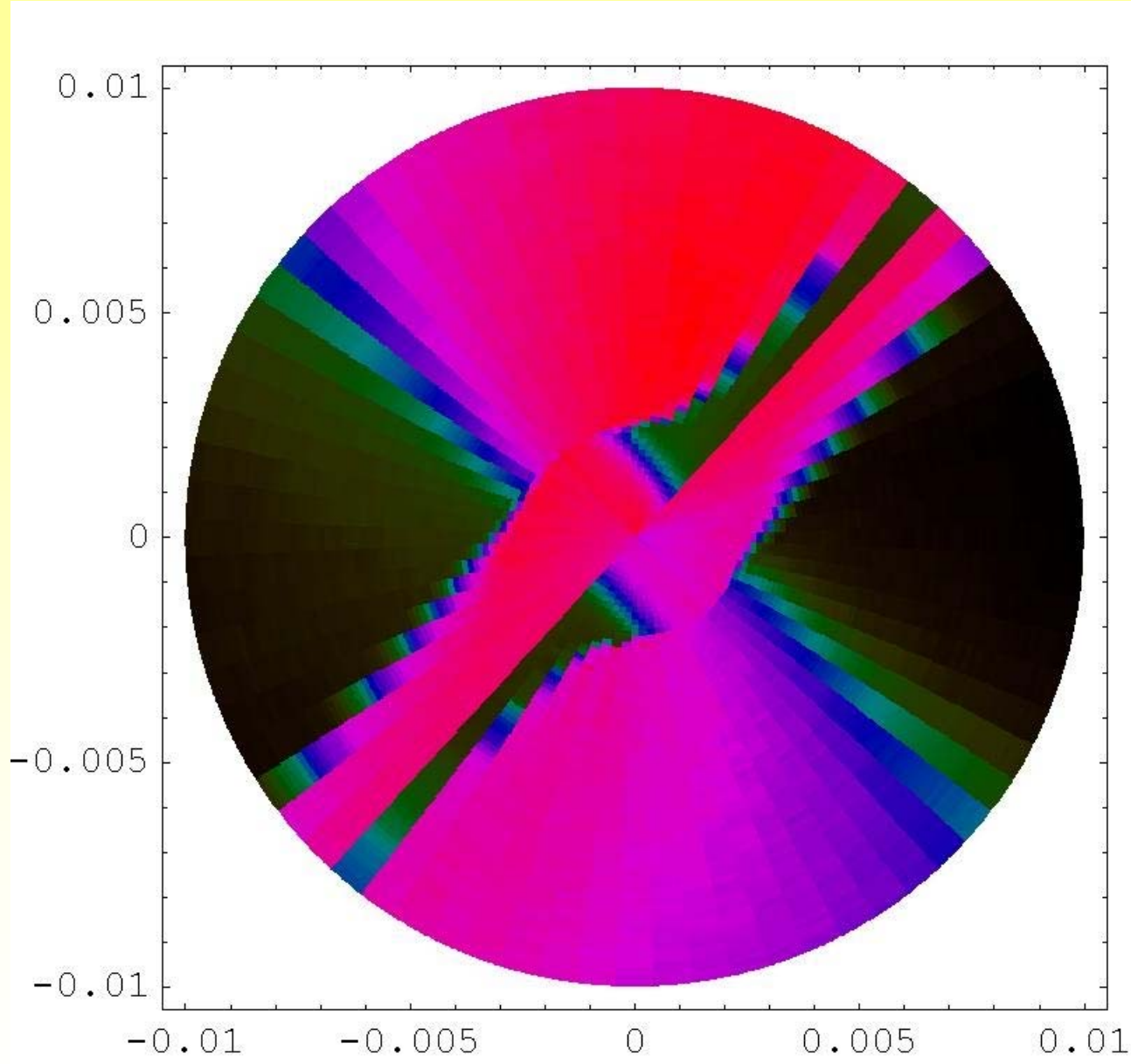
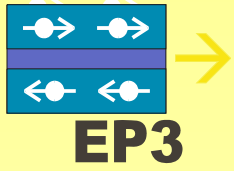
This is present on samples from various sources. Why is it there???



40K

The uniaxial 45° axis takes over

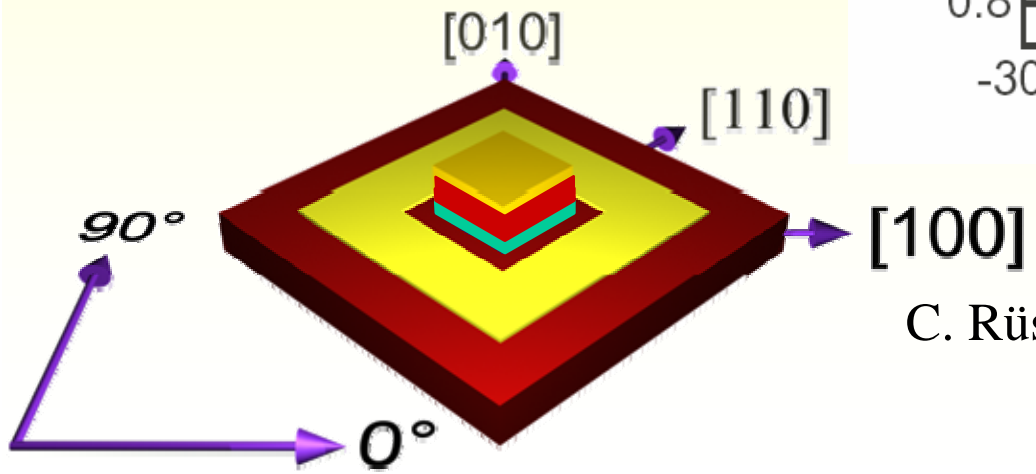
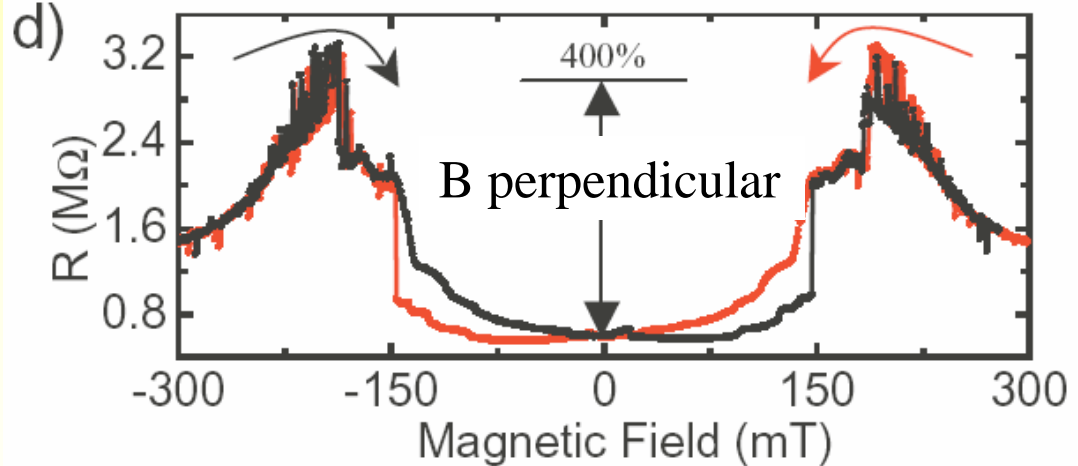
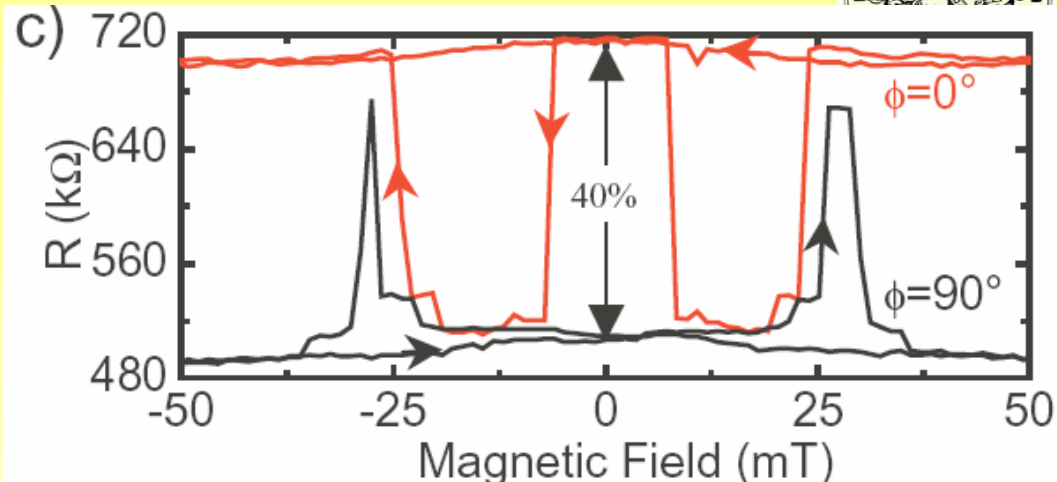
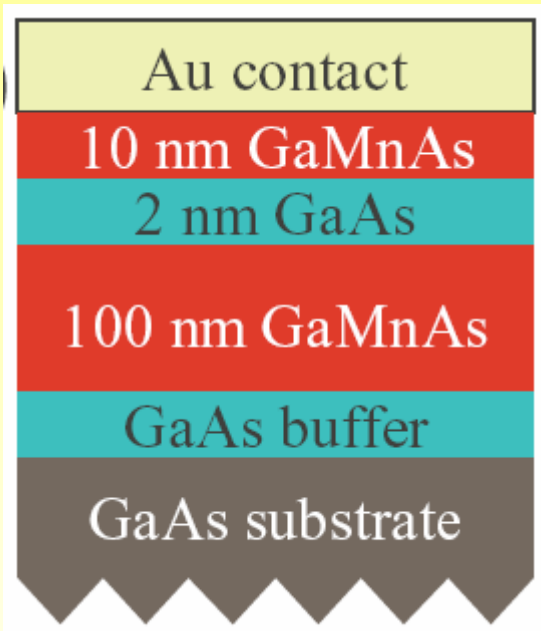
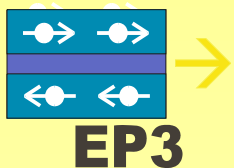




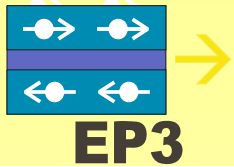
40K



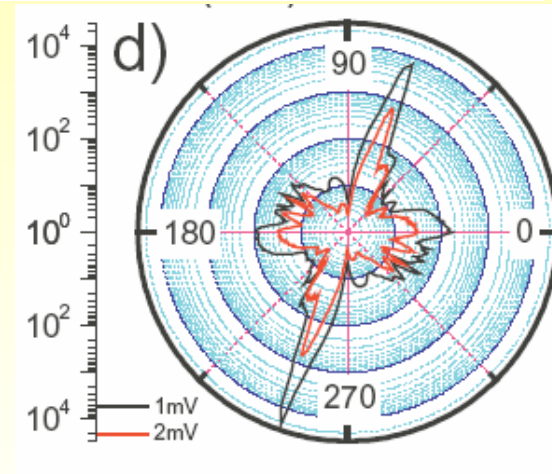
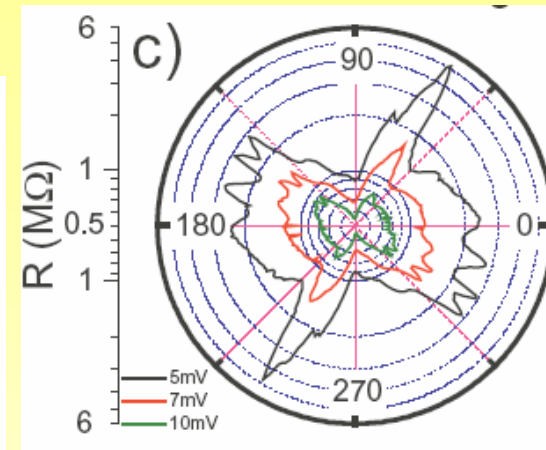
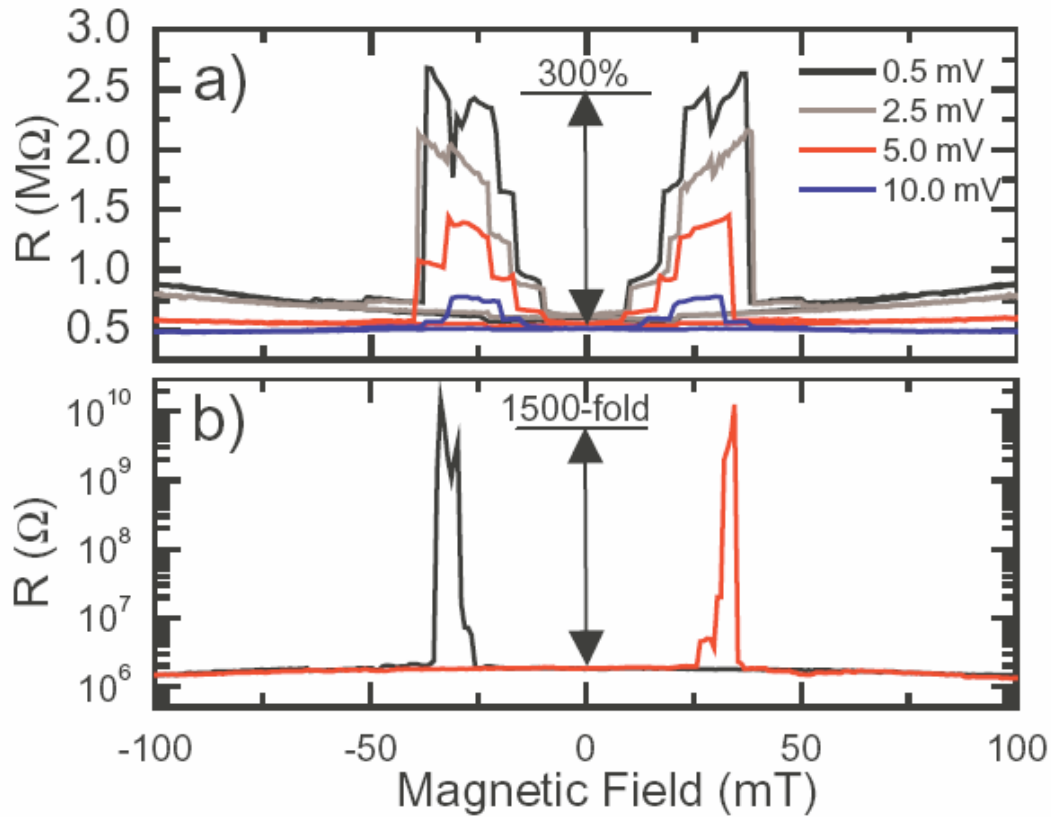
# Amplifying TAMR



C. Rüster et al., PRL 94, 027203 (2005)



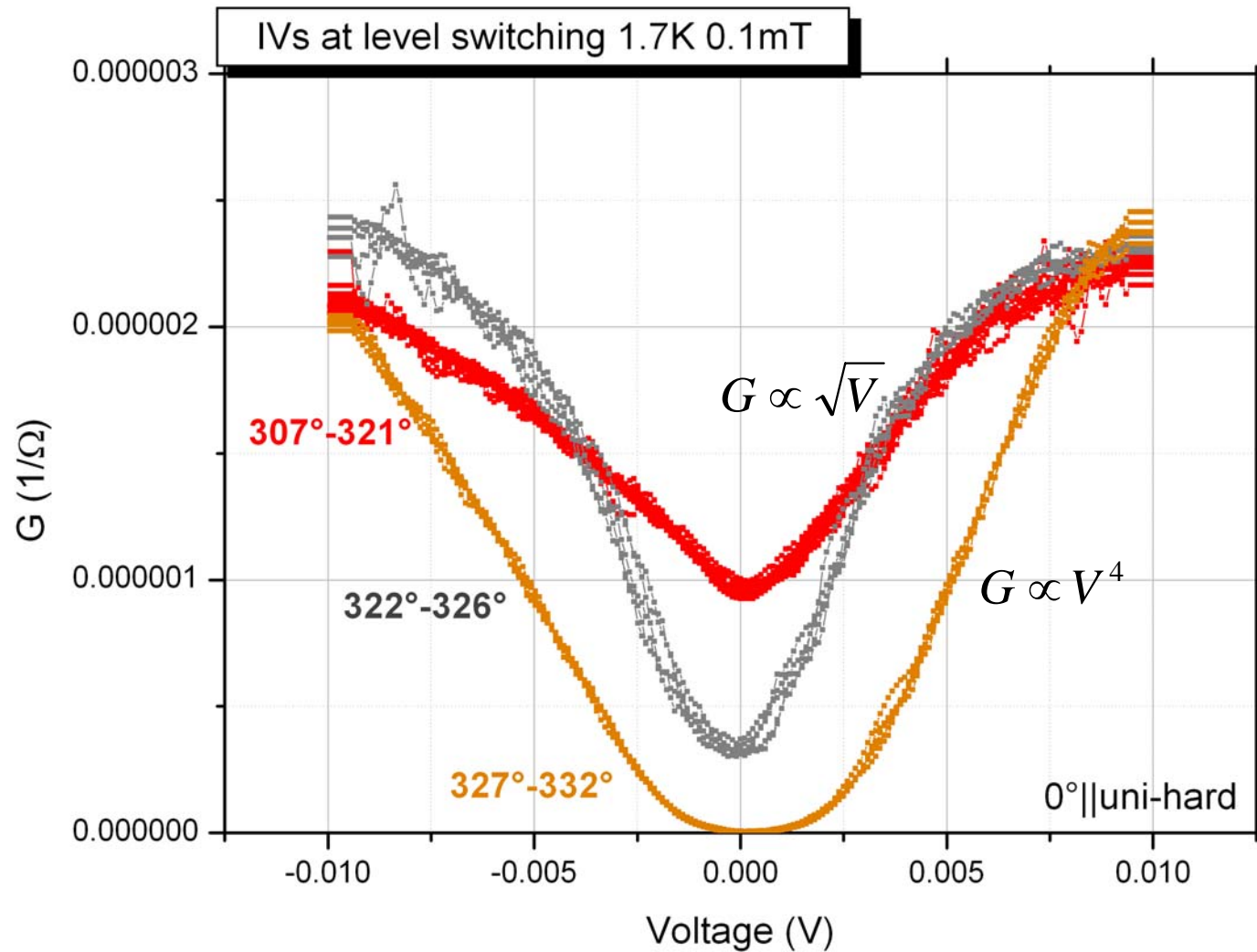
# Massive amplification of TAMR



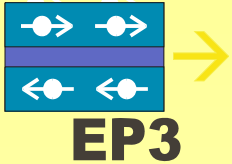
Effect blows up for low T, low bias: Efros-Shklovski gap.



# Massive amplification of TAMR



G-V curves indicative of metal (insulator) for low R (high R) state.



## How does the structure of the Mn-hole wavefunction vary with B-field direction? Iterative numerical solution of the Luttinger equation



Reformulation of the Luttinger equation in k-space to an iteration relation.

$$B_n(\mathbf{k}) = \frac{1}{E_b - H_{FL}^{nn}(\mathbf{k})} \left[ \sum_{n' \neq n} H_{FL}^{nn'} B_{n'}(\mathbf{k}) + \int \mathcal{U}(\mathbf{k} - \mathbf{k}') B_n(\mathbf{k}') d^3 \mathbf{k}' \right]$$

$H_{FL}^{nn'}(\mathbf{k})$  6 band Luttinger-Hamiltonian with SO-, PD-coupling and Strain

$\mathcal{U}(\mathbf{k} - \mathbf{k}')$  Yukawa potential in k-space

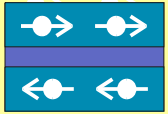
$B_{n'}(\mathbf{k})$  Bound hole wavefunction in k-space

$E_b$  Binding energy

Binding energy and the wavefunction will be determined at representative points.

Only the ground state.

Manuel J. Schmidt, Würzburg



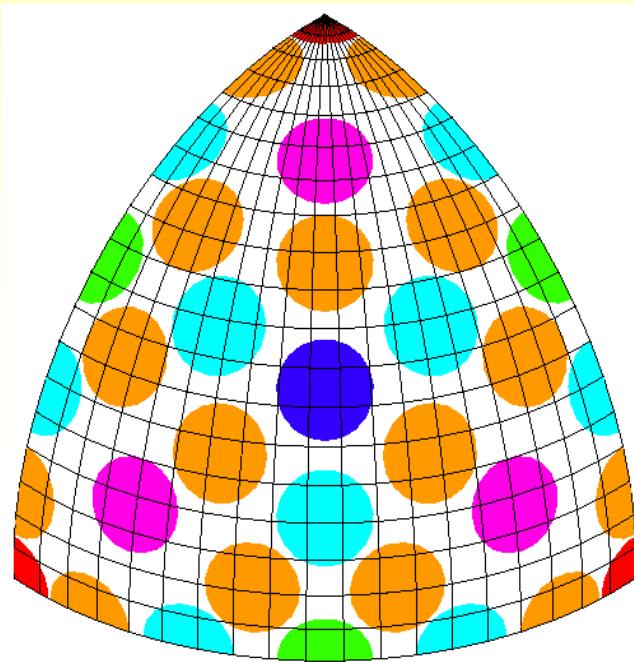
EP3

## Iterative numerical solution of the Luttinger equation

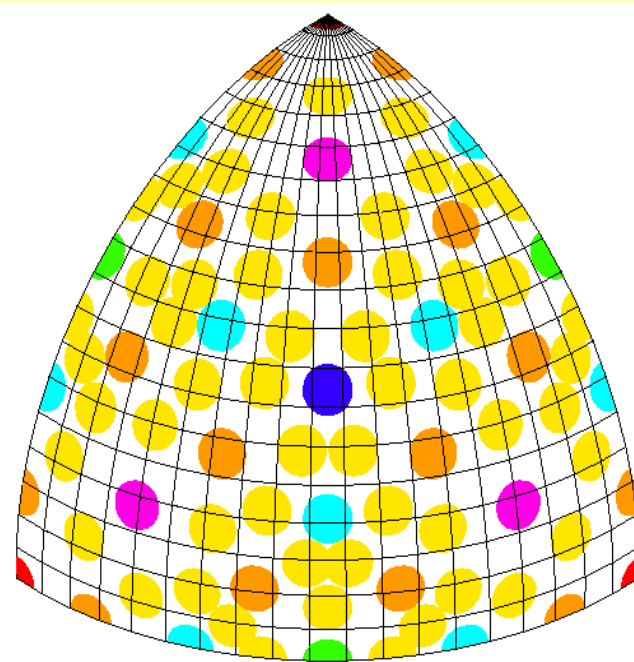


The points in k-space are chosen on particular sets of rays through the origin. The directions must obey the following requirements:

- Point group invariance
- Uniform direction-distribution (as far as possible)
- Some directions are available in all stars([001],[111],[011],...)

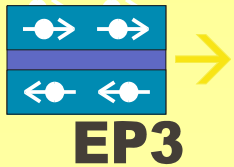


194star



602star

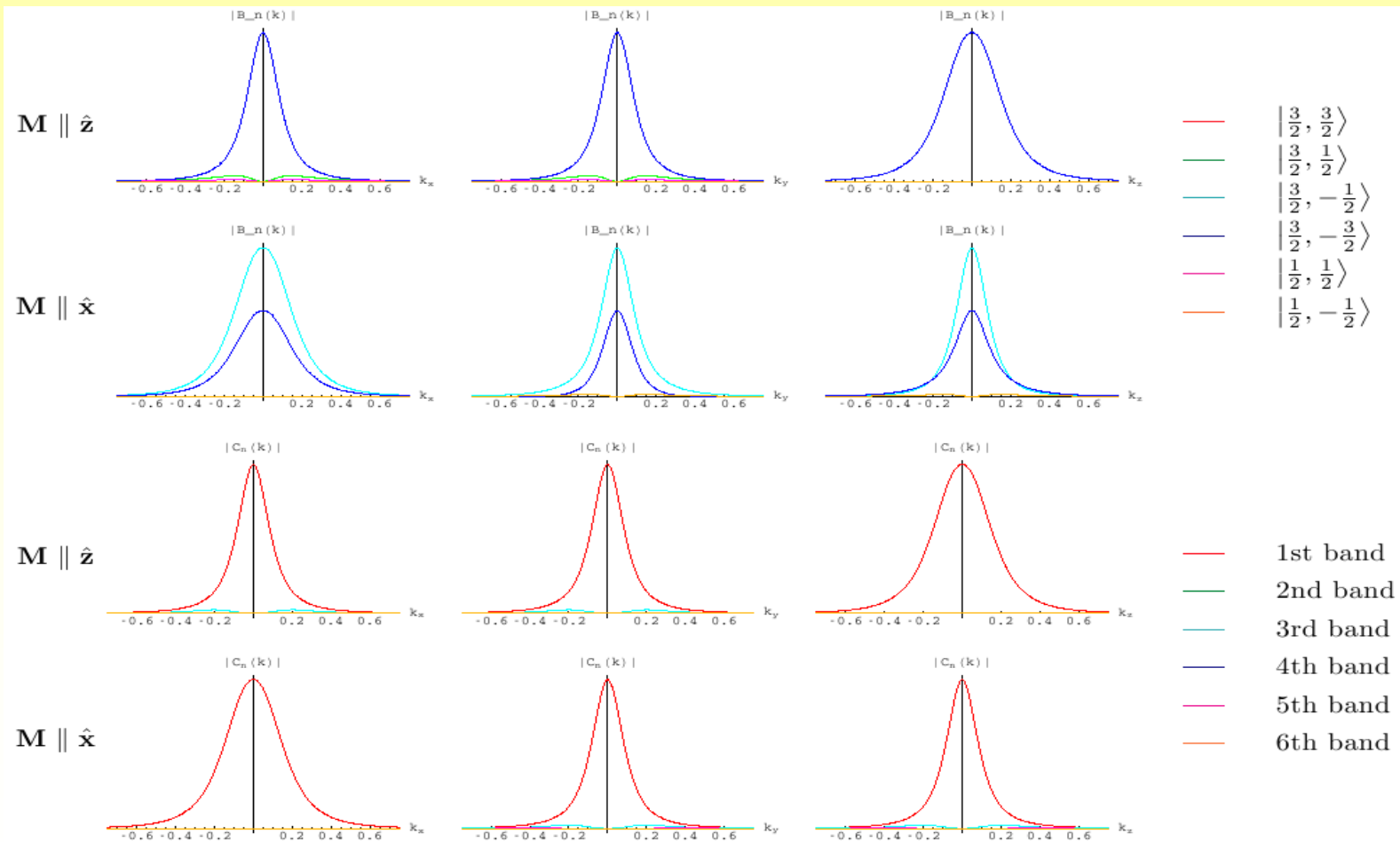


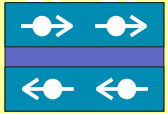


# Iterative numerical solution of the Luttinger equation



Wavefunction resides mainly in the top band, as seen from a transform to the eigenbasis of the full Luttinger Hamiltonian.





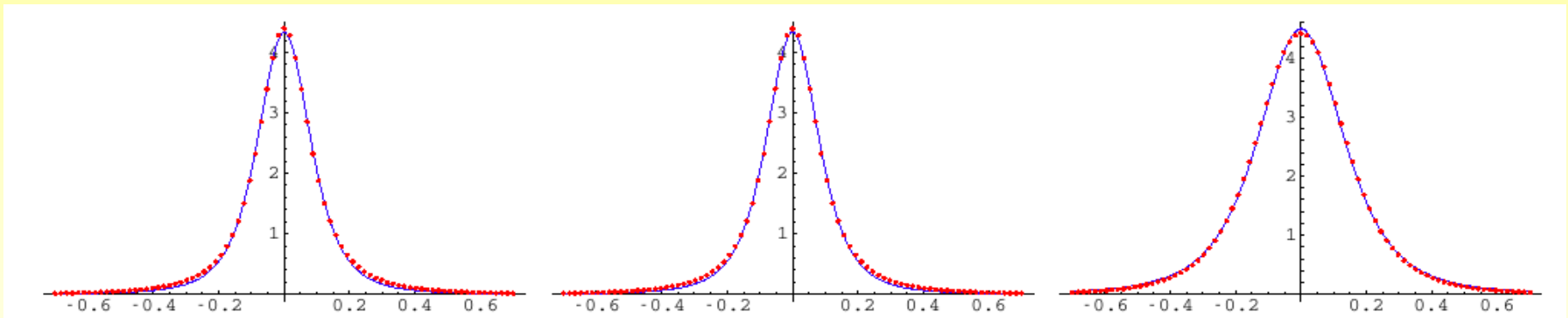
EP3



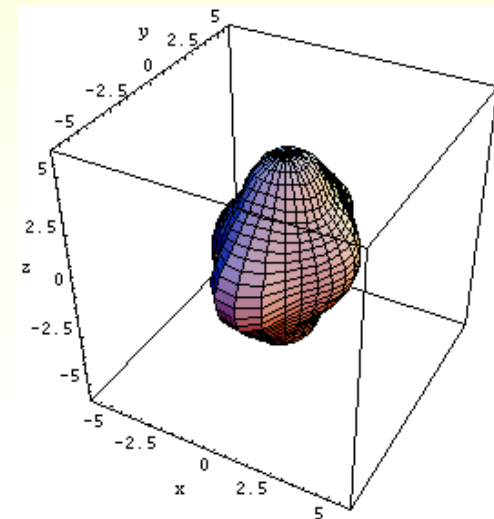
## Iterative numerical solution of the Luttinger equation



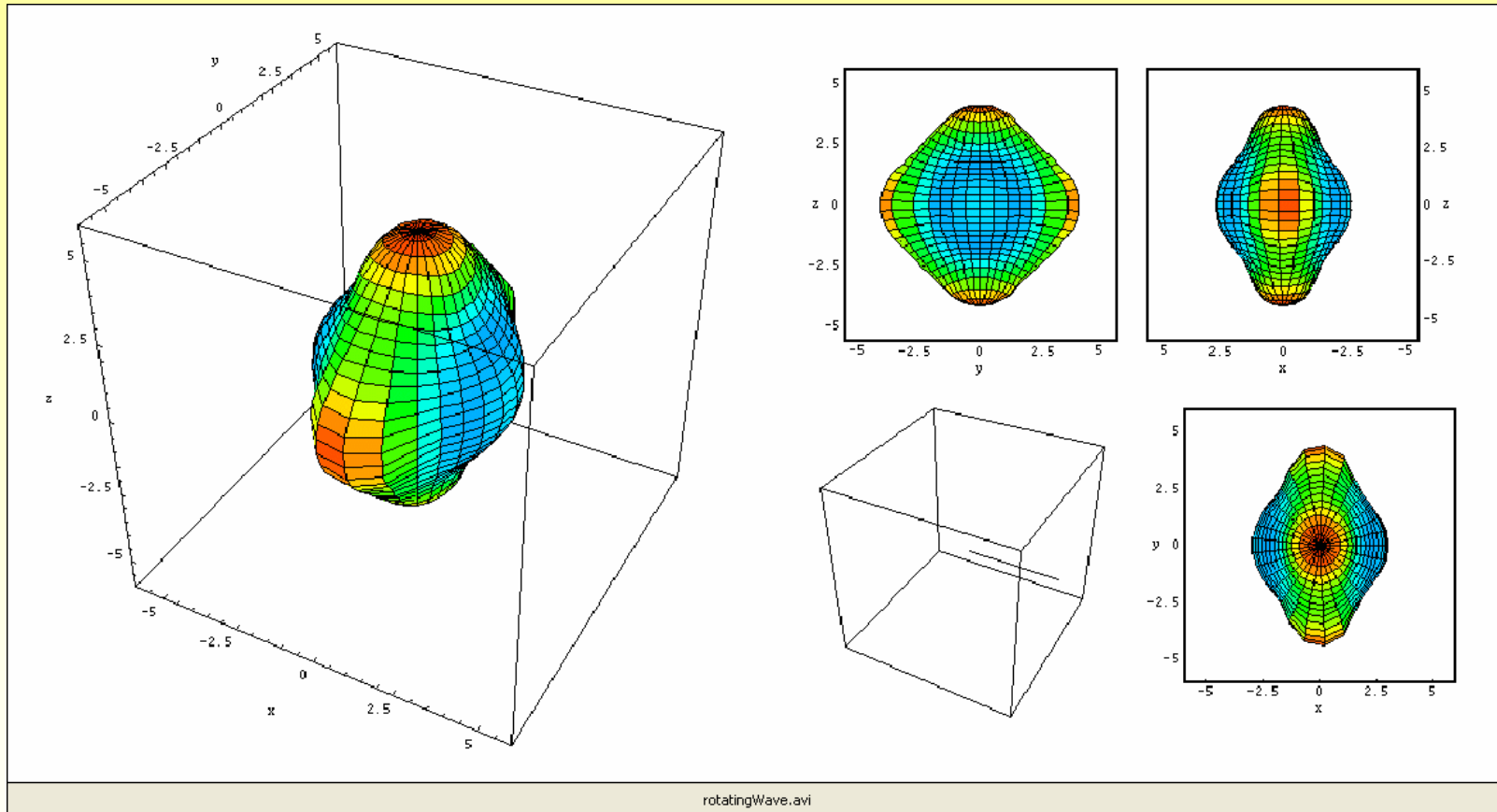
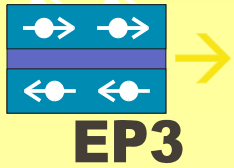
Hydrogen wavefunctions in k-space can be fitted to the numerical solution for each direction in order to obtain the Bohr radius.



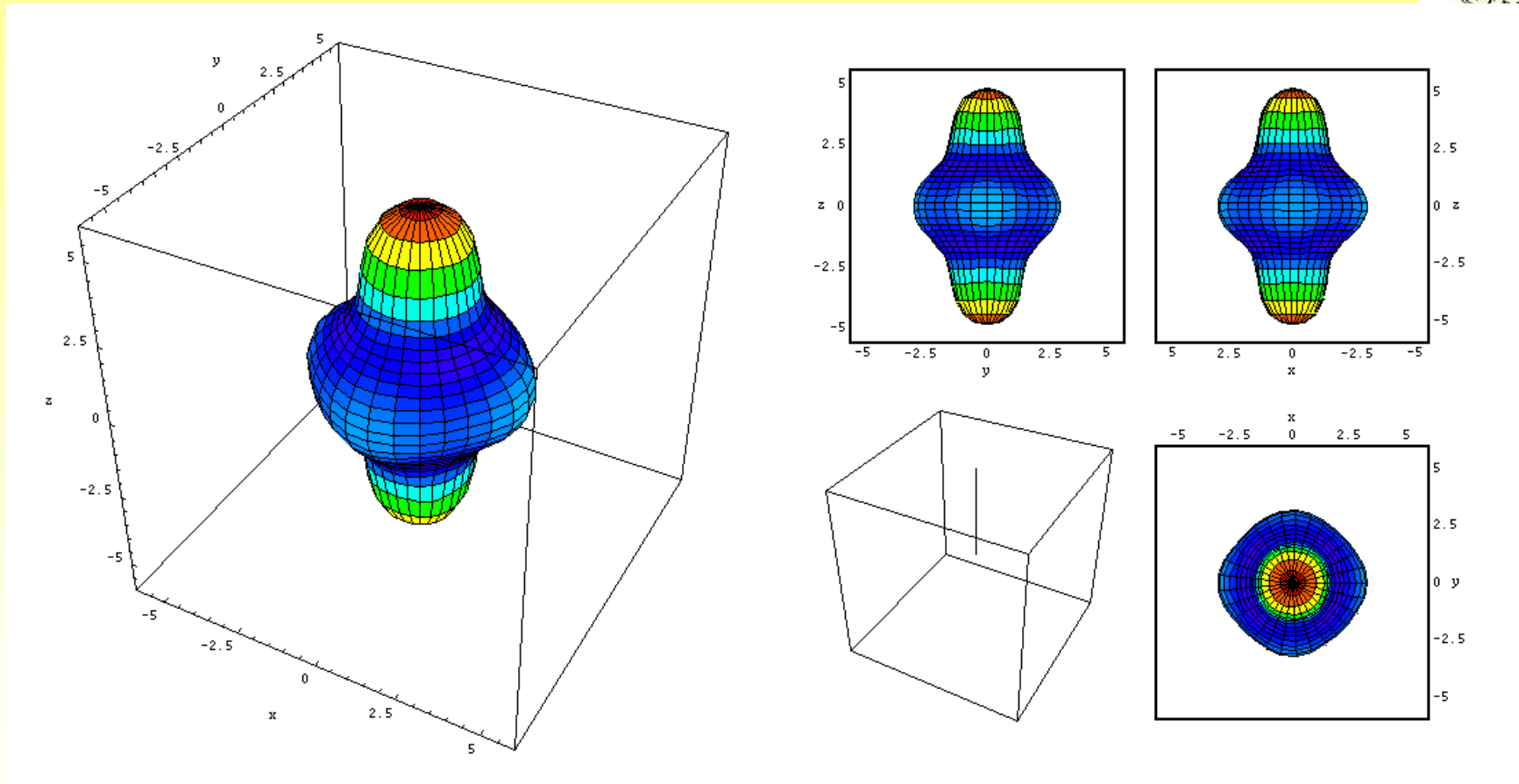
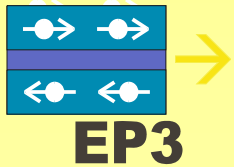
The Bohr radii for an arbitrary direction is interpolated. One can see a strong dependence on magnetization direction.



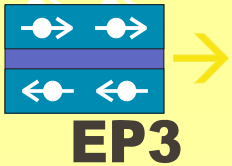




Wave function w/o strain breaking the symmetry



Including the strain (and exchange) parameters used in fitting the TAMR results.  
The change in Bohr radius drives the MI transition.



# Evidence for insulator phase: fluctuations in hopping transport

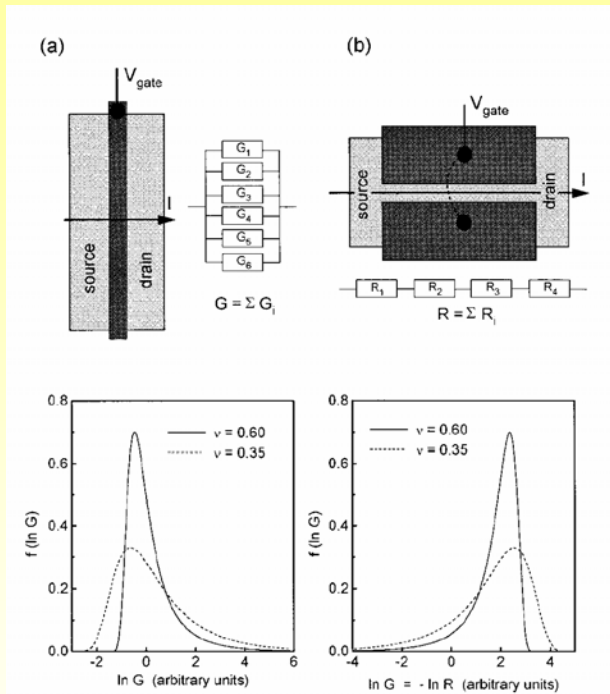


FIG. 1. Device schematics and theoretical DF's for two values of the parameter  $\nu$ . (a) The 2D device behaves like a sum of parallel conductors and its DF has a tail out to high  $\ln G$ . (b) The 1D device behaves like a sum of series resistances with a tail on the DF towards low  $\ln G$ .

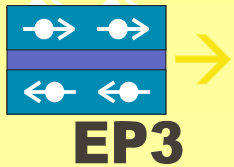
$$Q \equiv \ln\left(\frac{R}{R_0}\right) = \frac{\nu^{1/2} T_0}{T} \approx \left\{ 2 \frac{T_0}{T} \ln \left[ \frac{L}{\xi} \left( \frac{T_0}{T} \right)^{1/2} \ln^{1/2} \left( \frac{L}{\xi} \right) \right] \right\}^{1/2}. \quad (5)$$

The probability distribution function (DF) for the quantity  $Q$  is best written in terms of  $\nu$  and a new parameter  $\Delta$ . For  $\nu < 1$  it is given by the following integral:

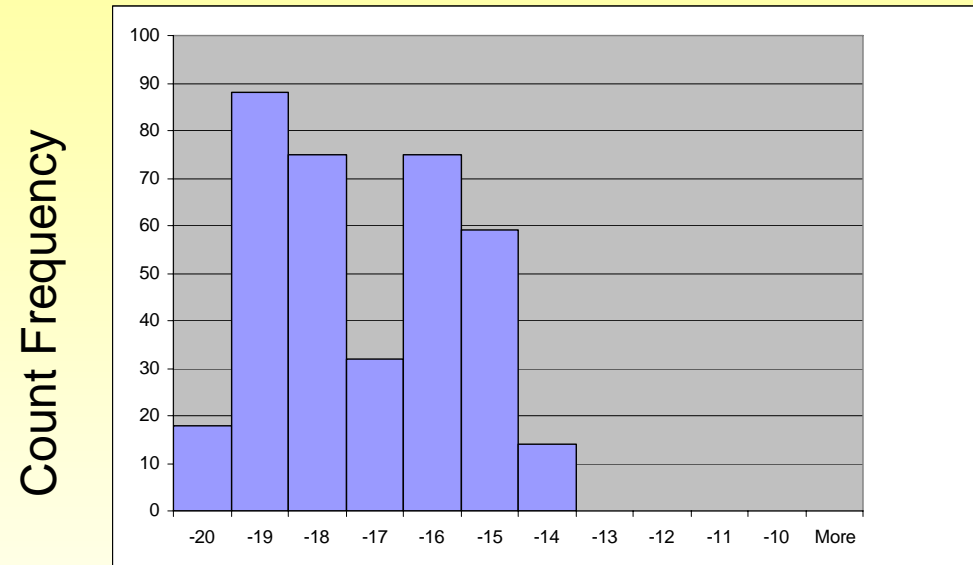
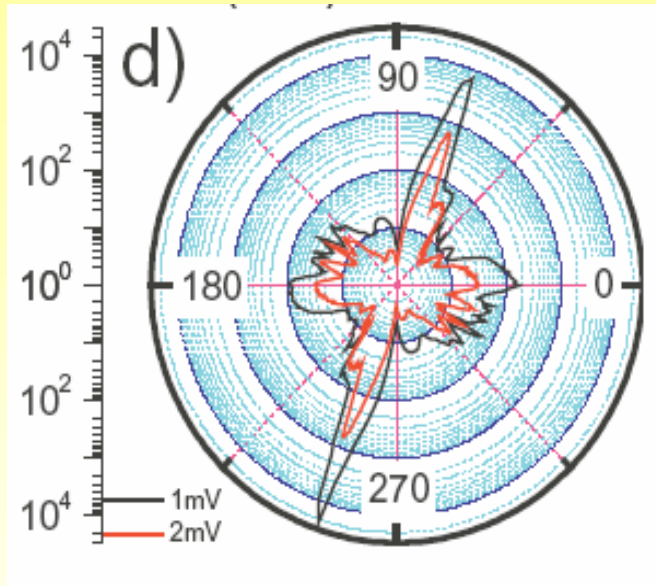
$$f(\Delta) = \frac{e^\Delta}{\pi} \int_0^\infty dx \exp\left(-x^{\nu/2} \cos \frac{\pi\nu^{1/2}}{2}\right) \times \cos\left(xe^\Delta - x^{\nu/2} \sin \frac{\pi\nu^{1/2}}{2}\right), \quad (6)$$

$$\Delta \equiv Q - \frac{\nu^{1/2} T_0}{T}. \quad (7)$$

- <sup>9</sup>M. E. Raikh and I. M. Ruzin, in *Mesoscopic Phenomena in Solids*, edited by B. I. Altshuler, P. A. Lee, and R. A. Webb (Elsevier Science, Amsterdam, 1991).
- <sup>10</sup>M. E. Raikh and I. M. Ruzin, *Zh. Éksp. Teor. Fiz.* **92**, 2257 (1987) [*Sov. Phys. JETP* **65**, 1273 (1987)].

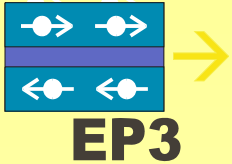


# Analysis of amplitude of experimental fluctuations



Is this at all a healthy way of analyzing our data?

How can we do better?



## Narrow Gap II-VIs: HgMnTe



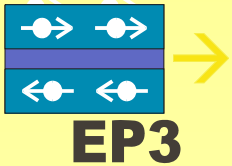
- Introduction: HgTe Quantum Wells
- Interplay Rashba/Zeeeman Splitting
- Odd and Even Hall plateaus
- Nanostructured Hall bars
- Gated H-bars
- Aharonov Casher effect

### ***Collaborators:***

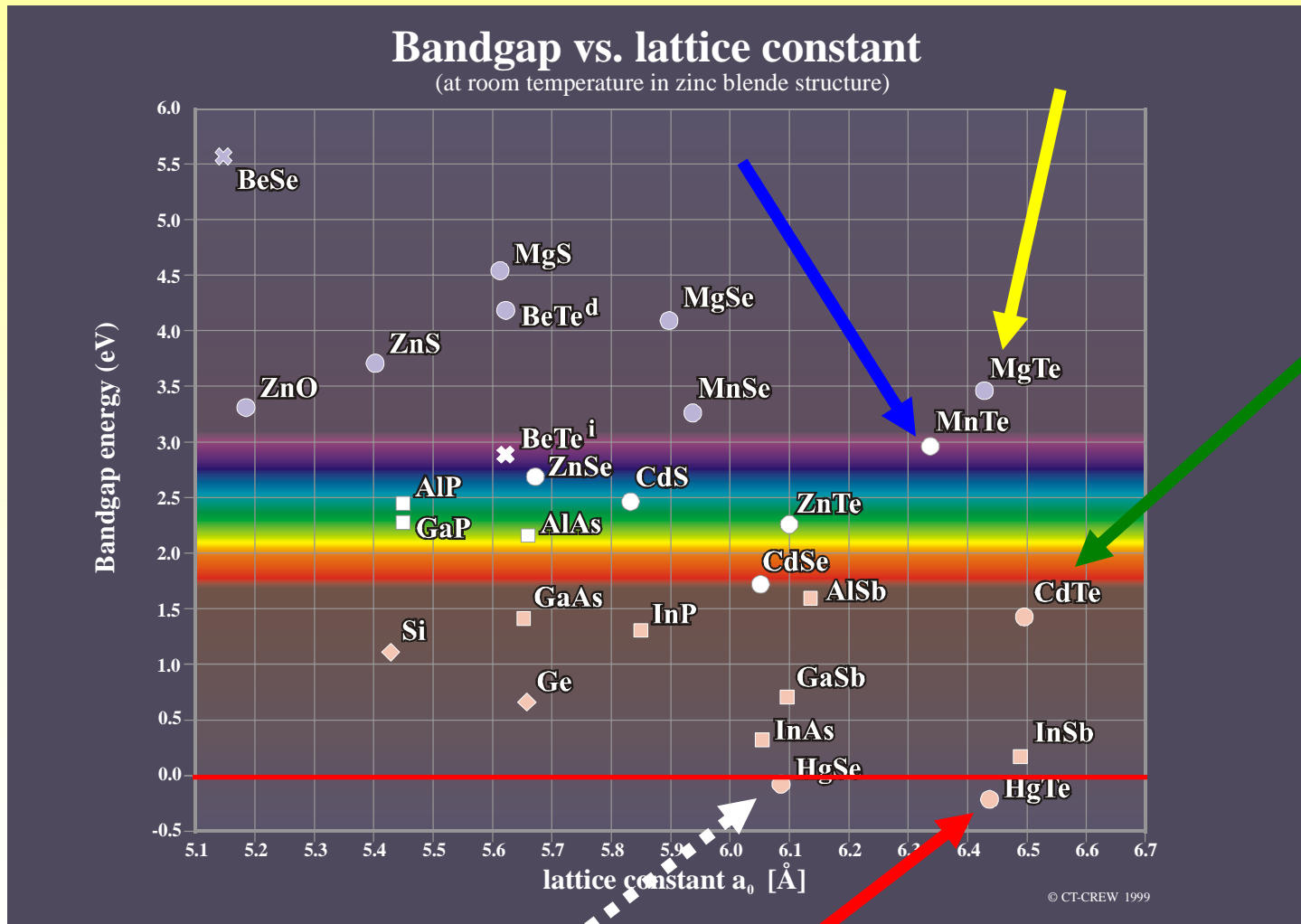
***Hartmut Buhmann, Charlie Becker, Volker Daumer,  
Yongshen Gui, Markus König, Jian Liu, Alina Novik, Matthias  
Schäfer***

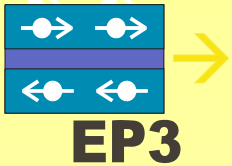
***Gerrit Bauer, Junichiro Inoue***

***Tomas Jungwirth, Jairo Sinova, Ewelina Hankiewicz***

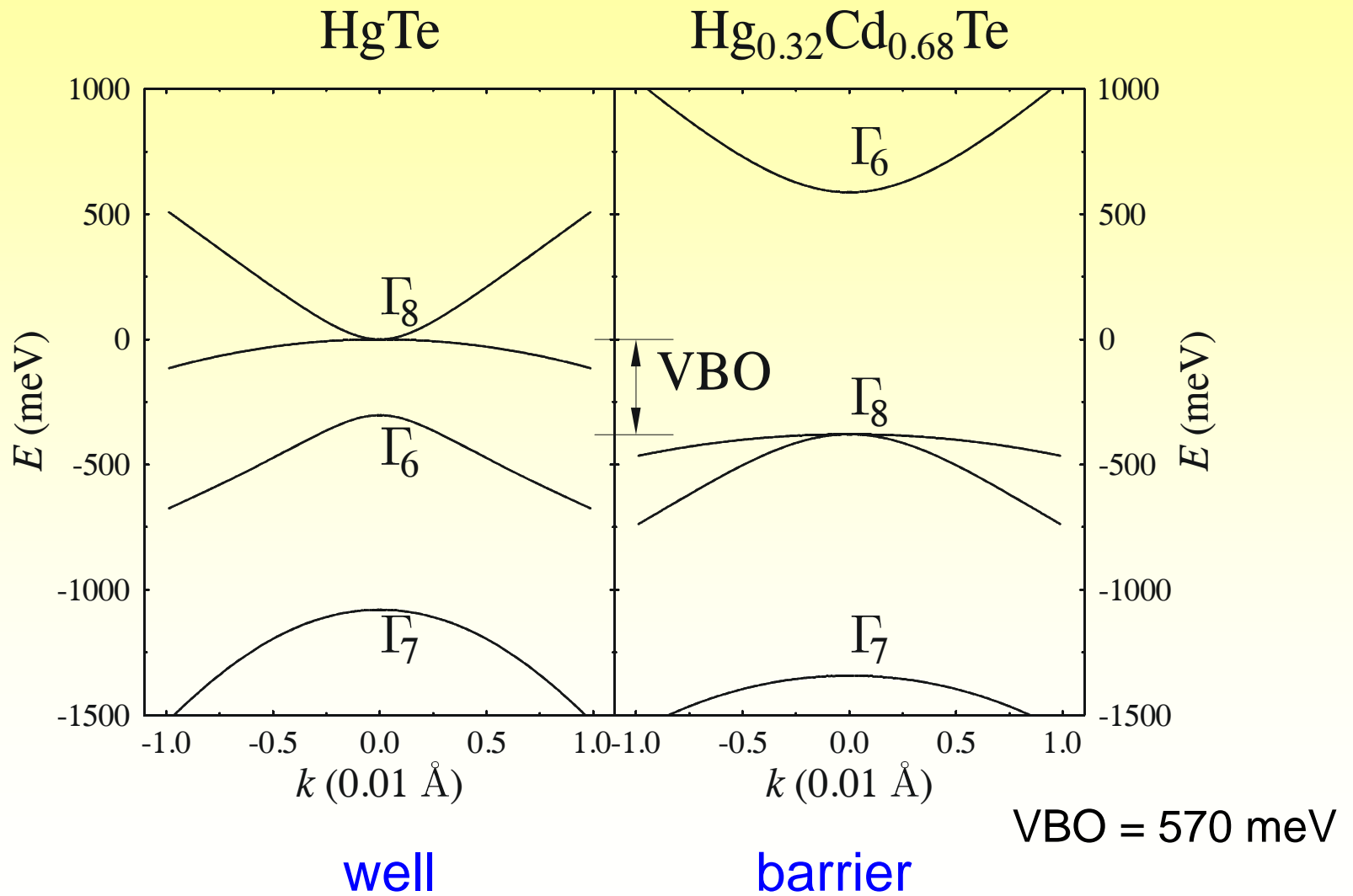


# HgTe Fabrication: MBE

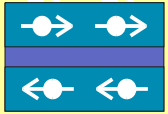




# HgTe Quantum-Well





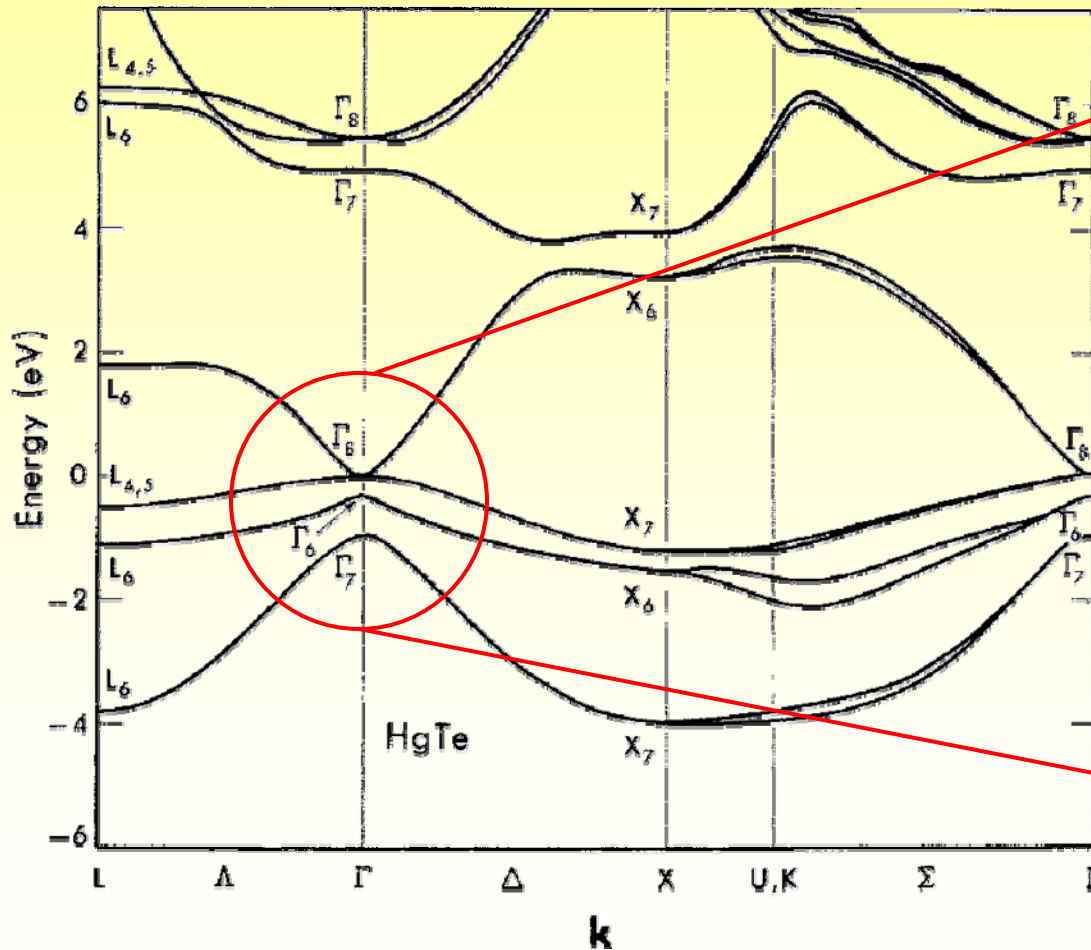


EP3

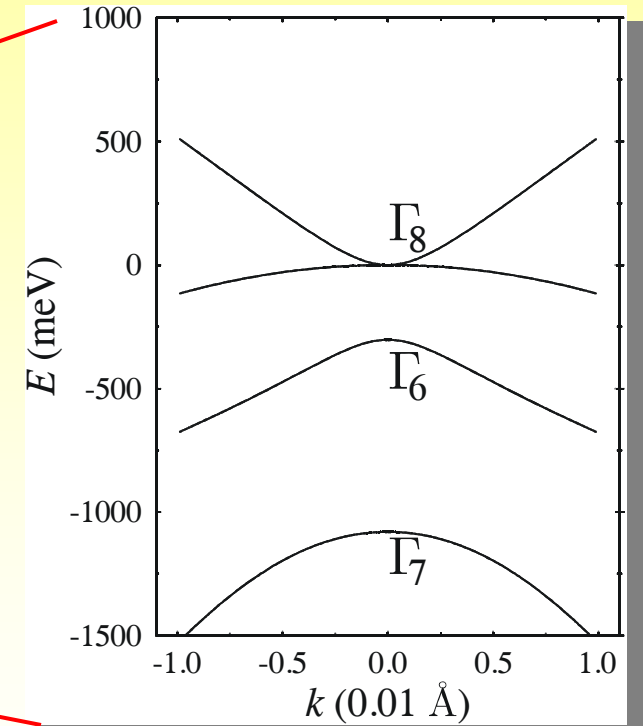
# HgTe: Semimetal or Semiconductor



bandstructure



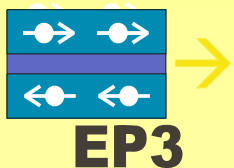
zero gap:



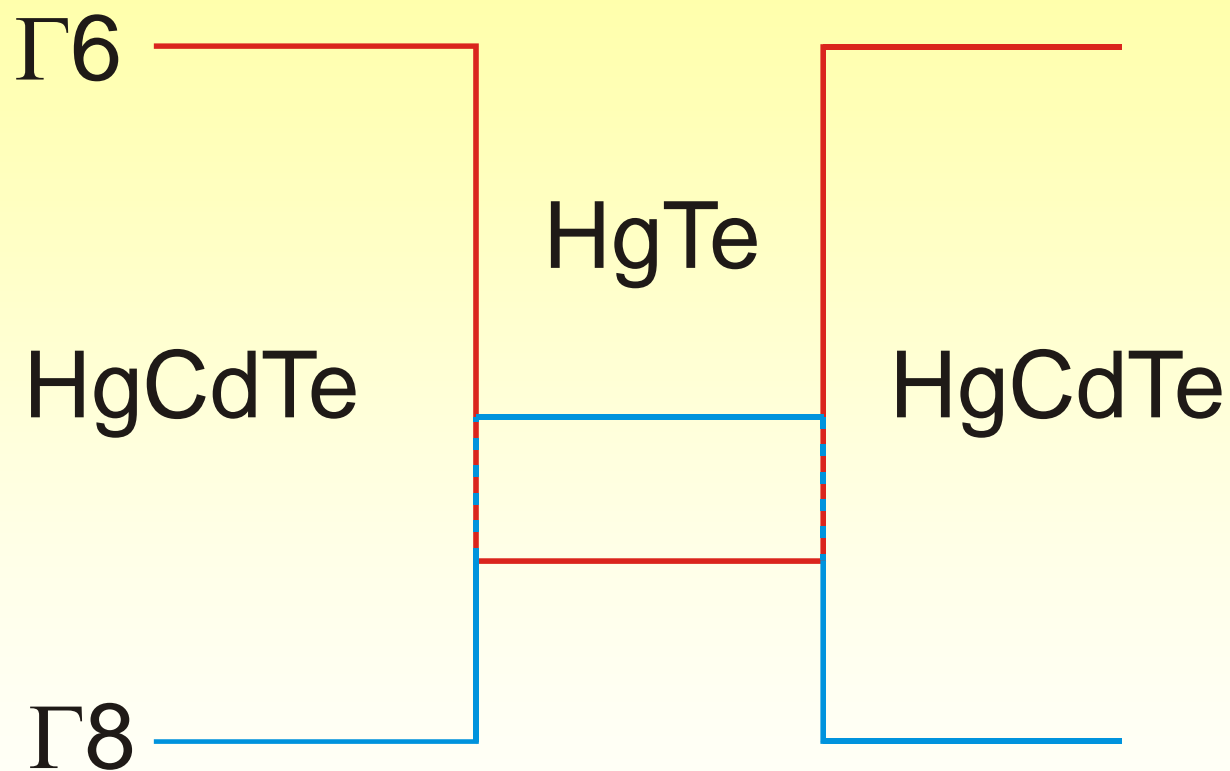
fundamental gap

D.J. Chadi et al. PRB, 3058 (1972)

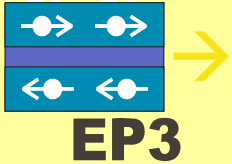
$$E^{\Gamma_6} - E^{\Gamma_8} \approx -300 \text{ meV}$$



# Inverted Bandstructure



type-III QW



# Band Structure of HgTe QWs

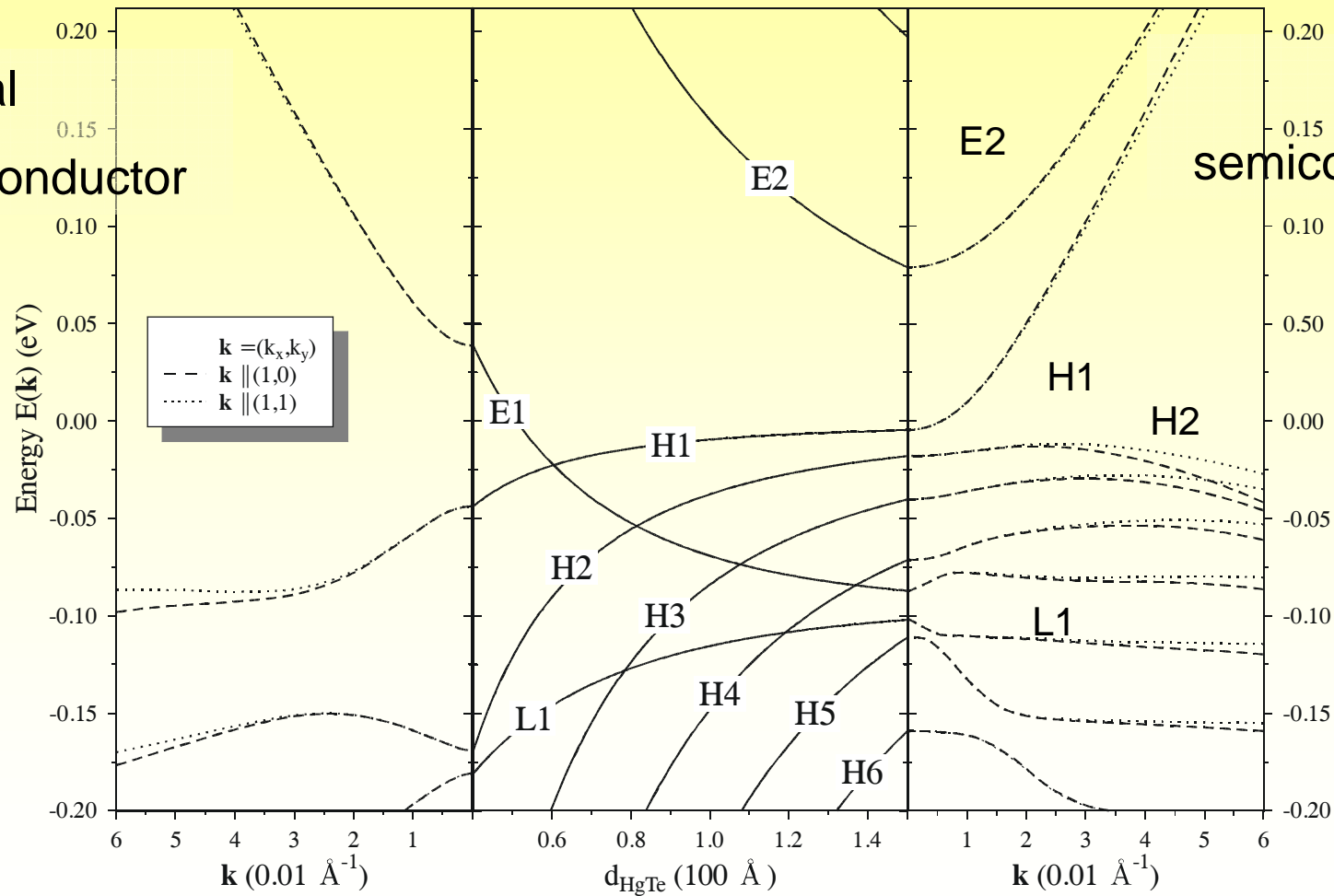


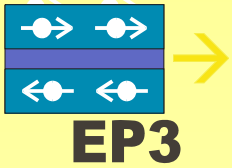
4 nm QW

15 nm QW

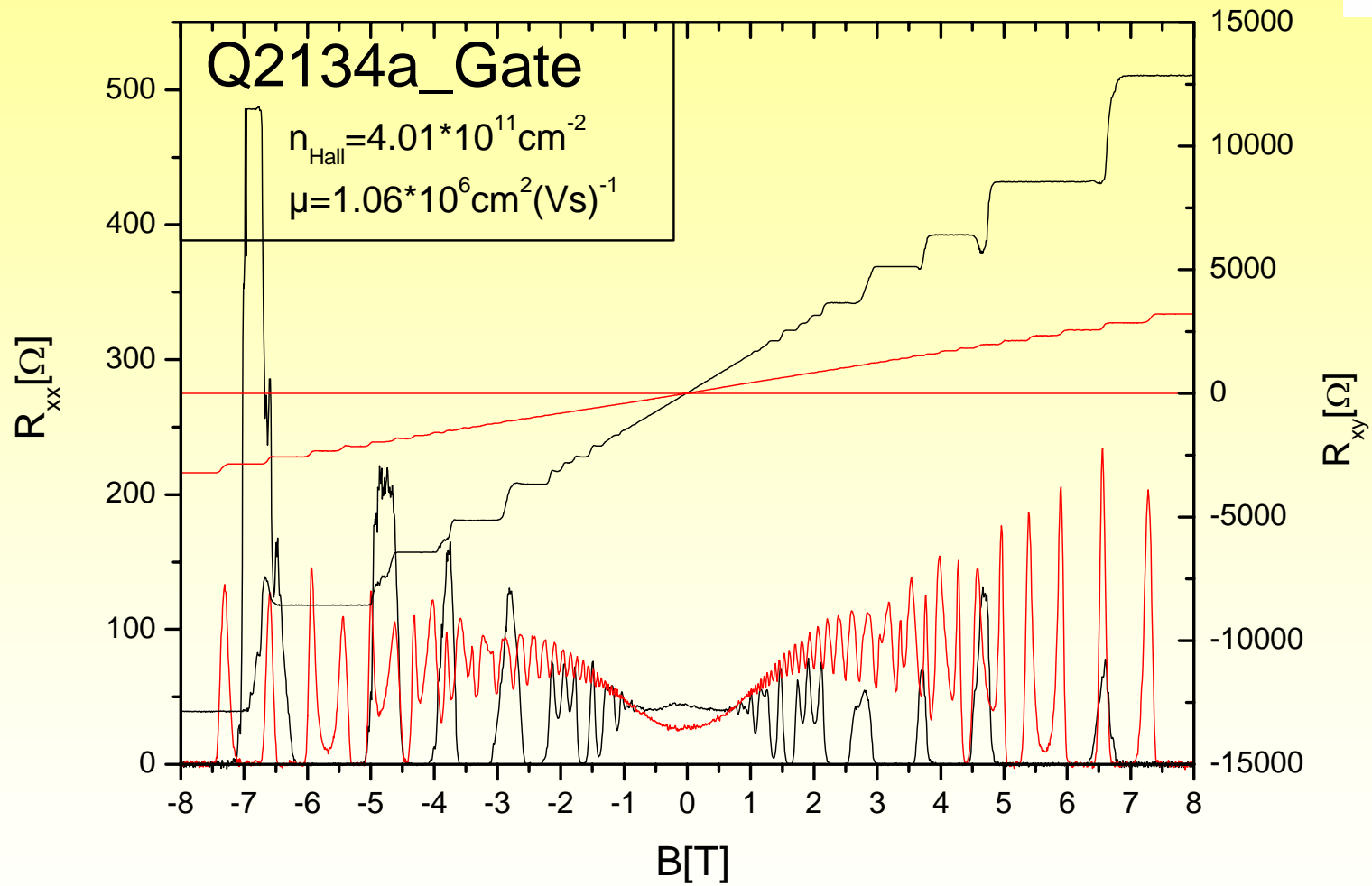
normal  
semiconductor

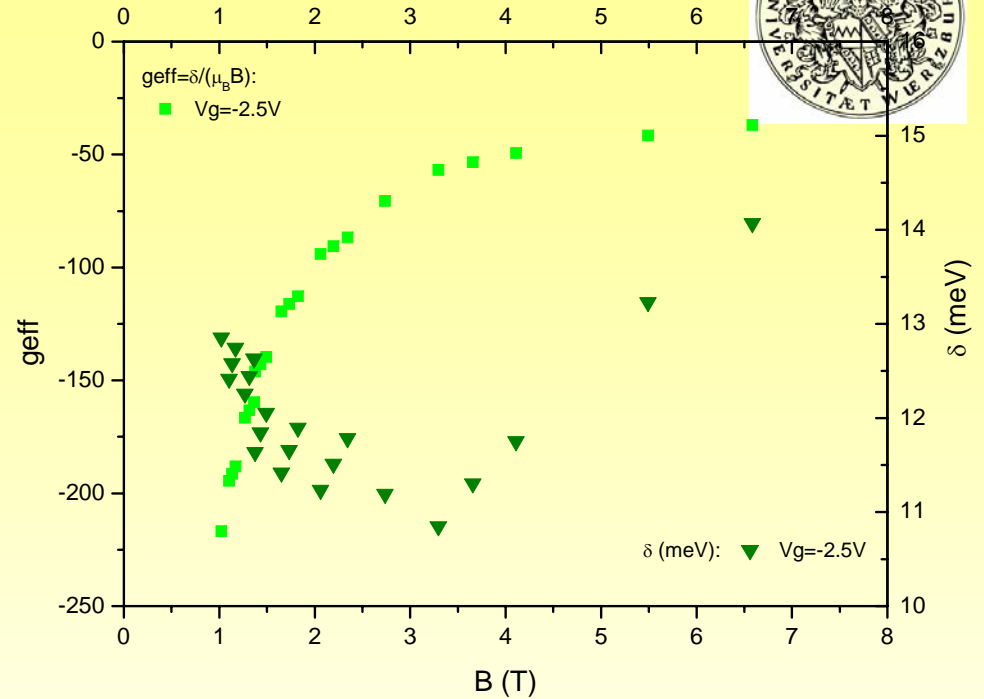
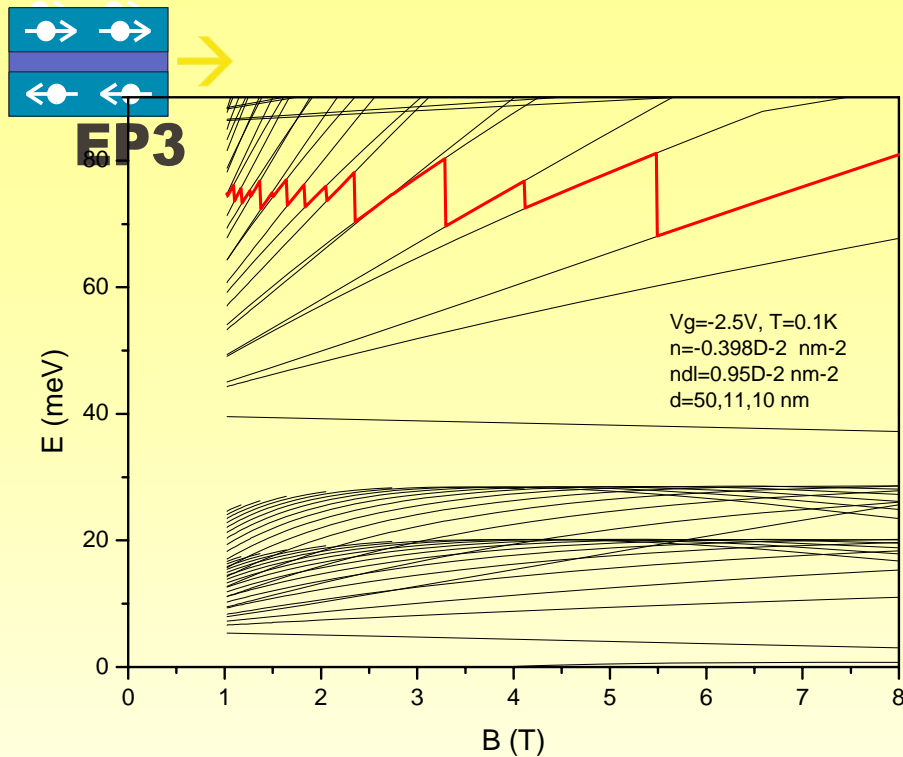
inverted  
semiconductor





## High Electron Mobility

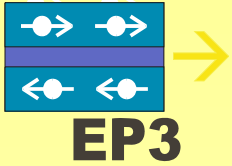




Large spin polarisation, large Rashba - and NO (intrinsic) AHE  
 Inoue et al. – intrinsic AHE does not survive vertex for linear-in-k S.O.  
 But: Rashba in HgTe is not simply linear in k.  
 And: AHE seems also absent in HgMnTe....

A. Novik et al., PRB 72, 035321 (2005).

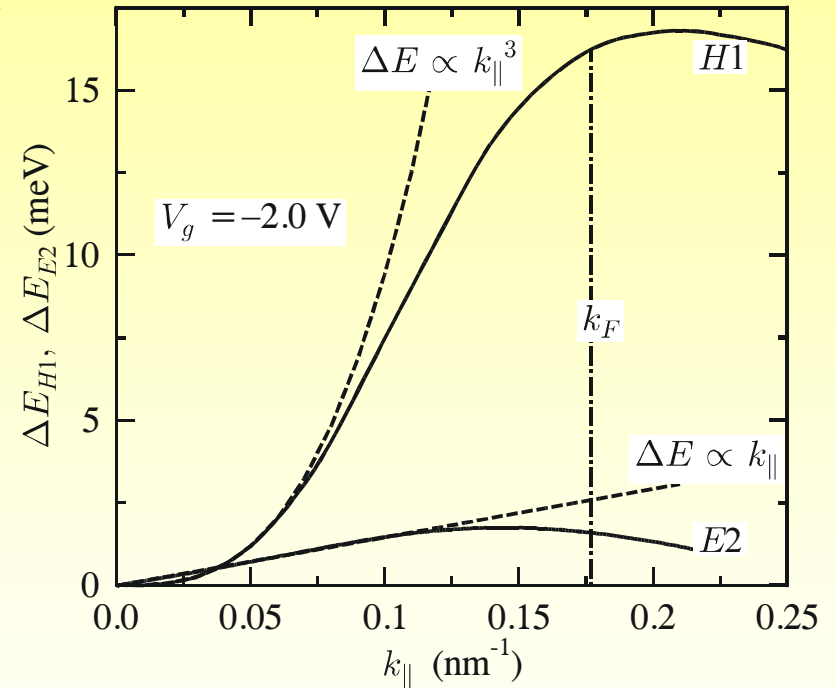
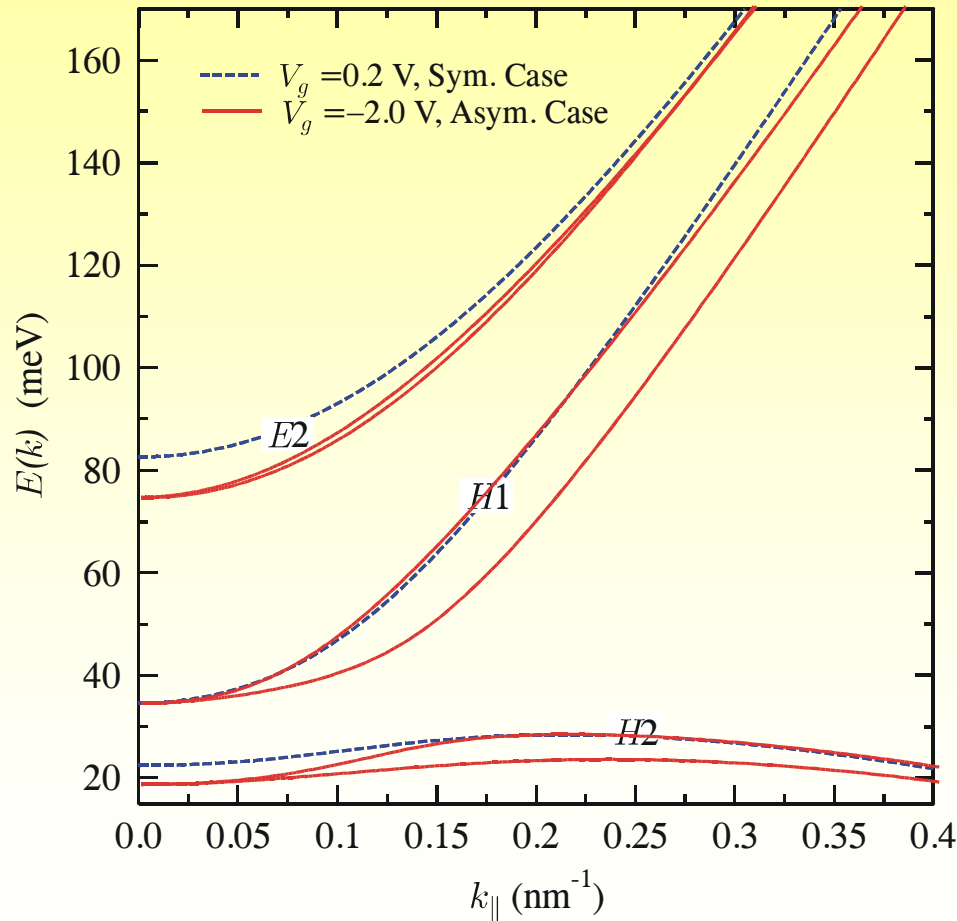
Y.S. Gui et al., PRB 70, 115328 (2004).



# Rashba Effect in HgTe



## 8 x 8 $k \cdot p$ band structure model

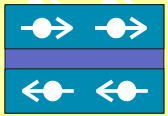


Rashba splitting energy

$$\Delta_{R,\text{max}} = 30 \text{ meV}$$

A. Novik et al., PRB 72, 035321 (2005).

Y.S. Gui et al., PRB 70, 115328 (2004).

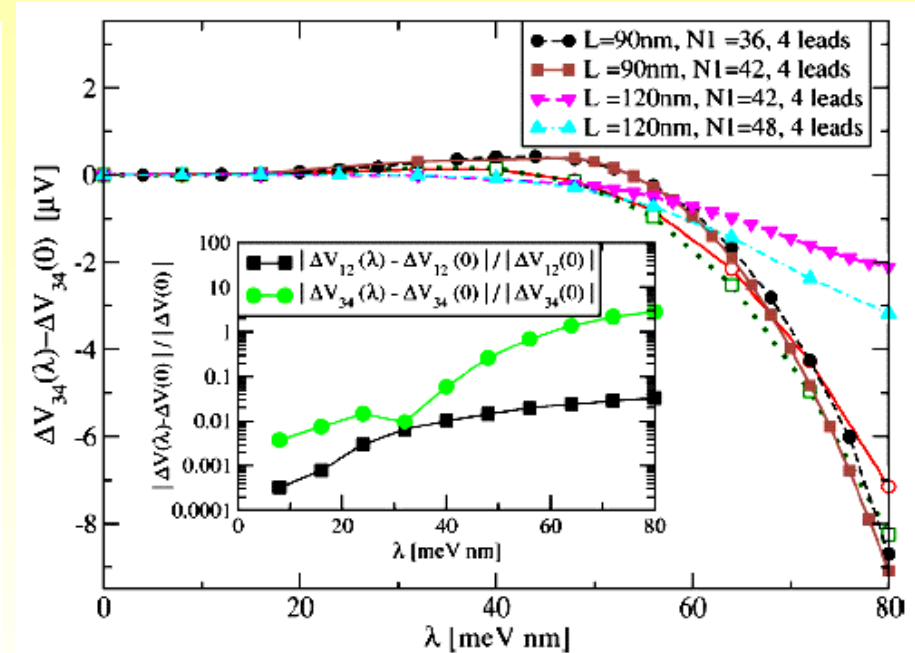
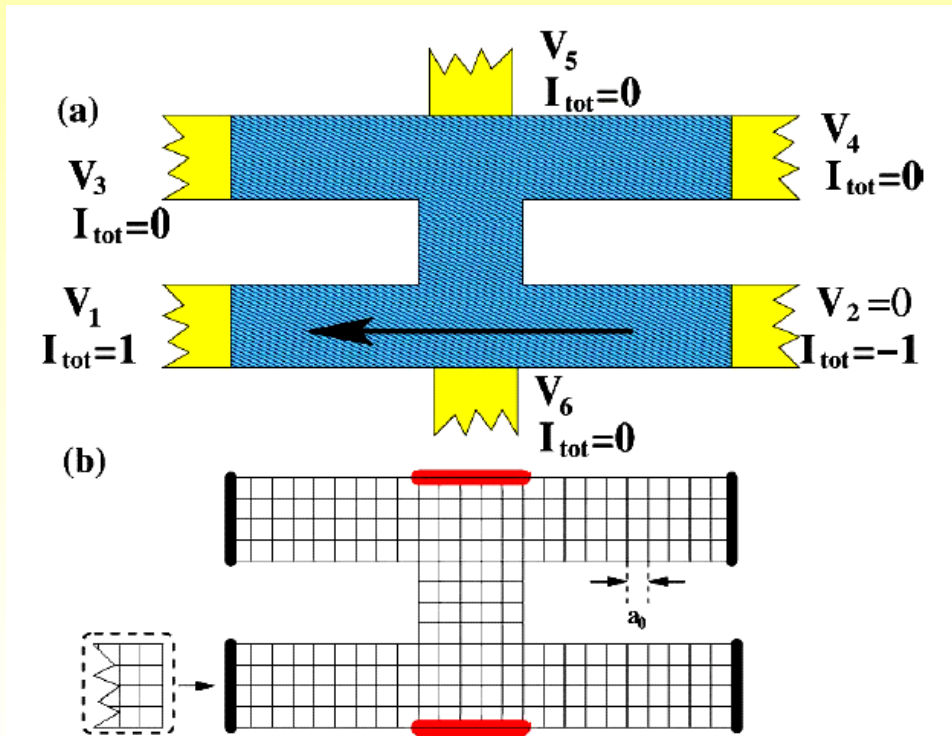


EP3

# H-bar for detection of Spin-Hall-Effect

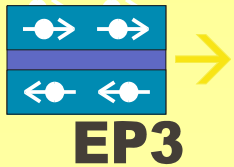


(electrical detection through inverse SHE)



E.M. Hankiewicz et al., PRB 70, R241301 (2004)



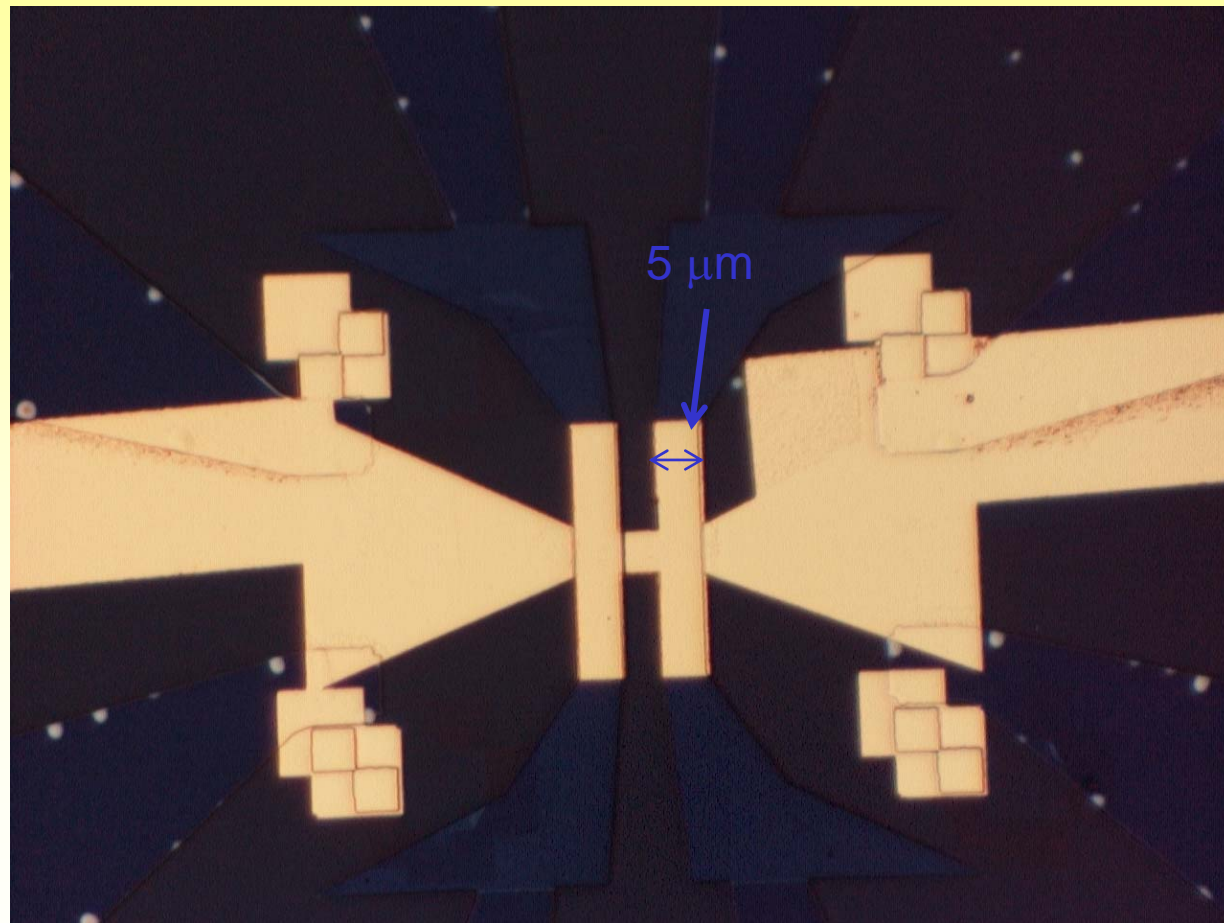


# Actual gated H-bar sample



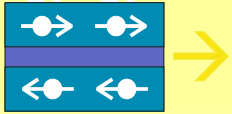
HgTe-QW

$$\Delta_R = 5-15 \text{ meV}$$



Gate-Contact

ohmic Contacts



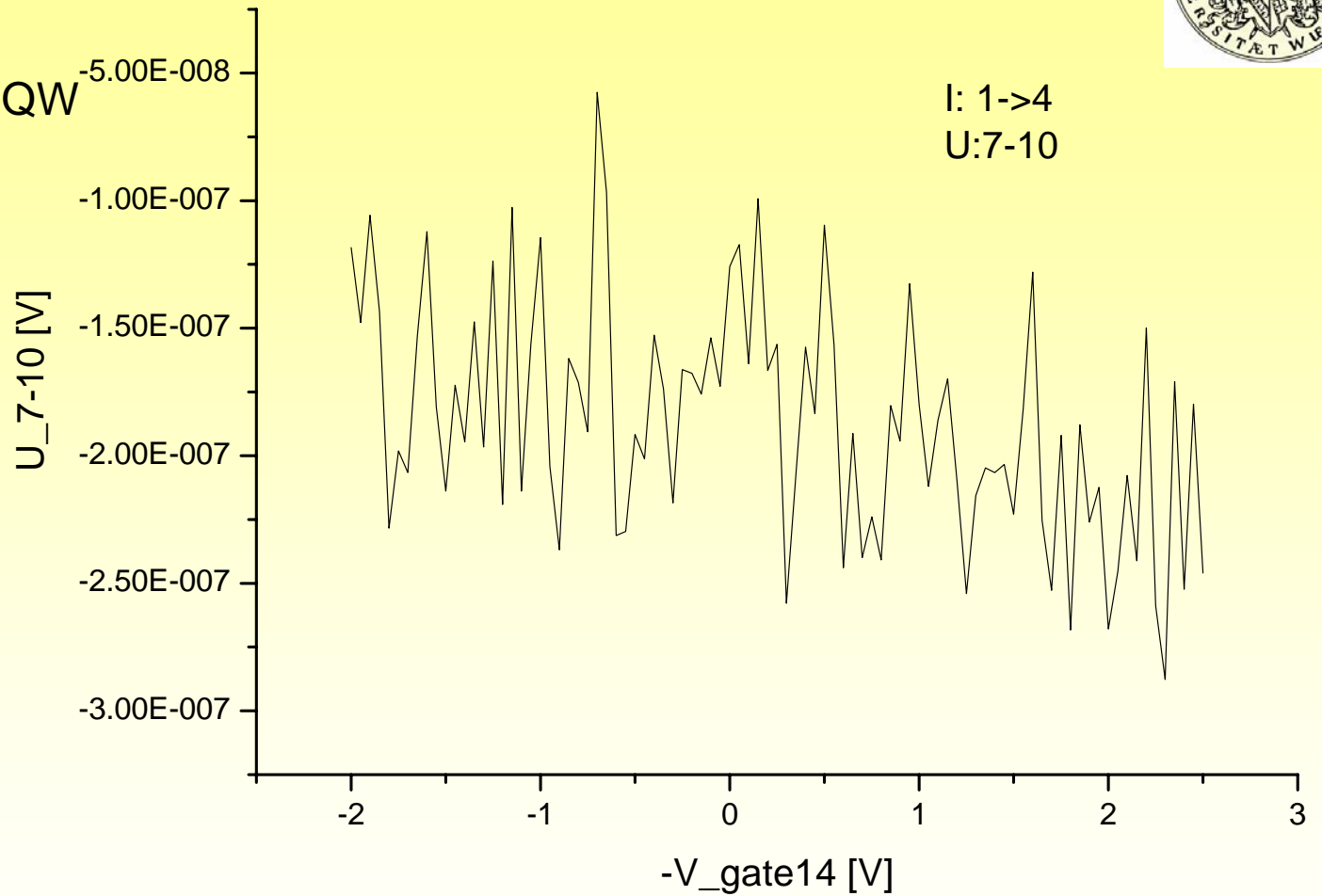
**EP3**

Symmetric HgTe-QW

$\Delta_R = 0-5$  meV

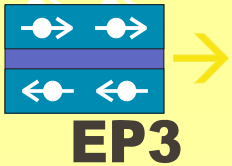
Signal less than  $10^{-4}$

## Results...

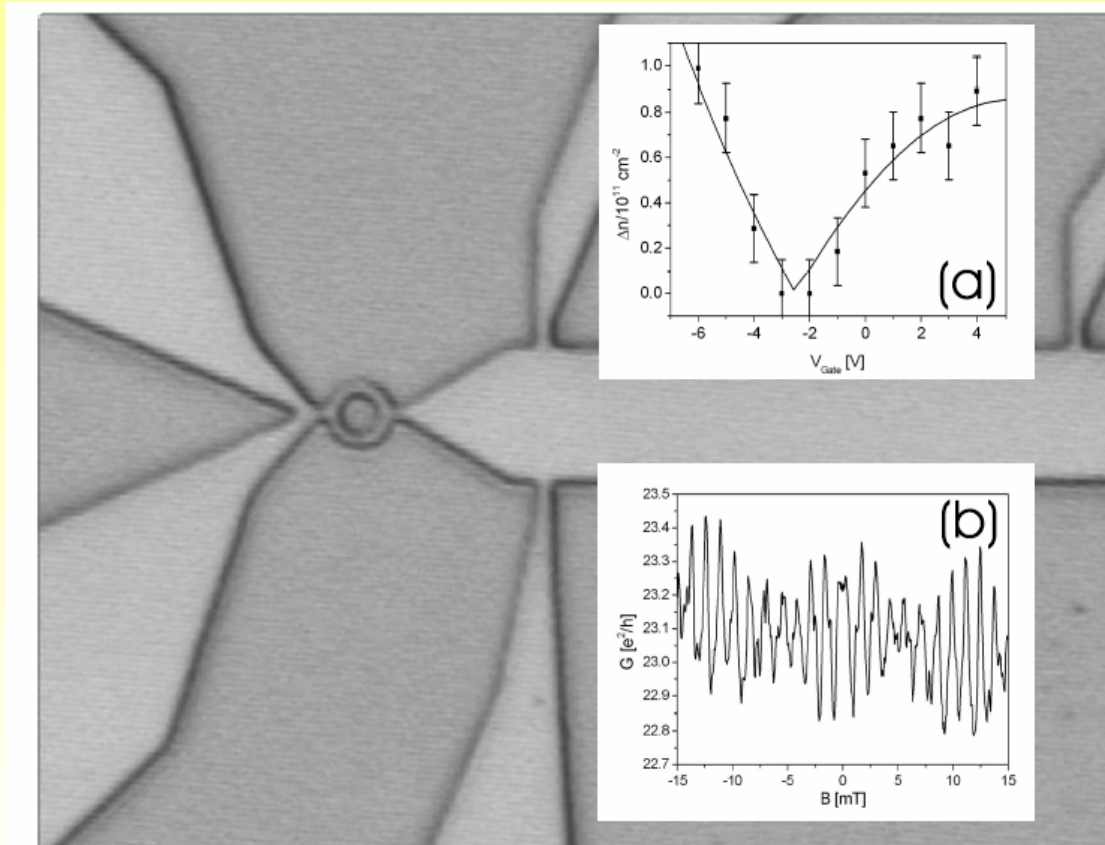


Remember:

Rashba splitting is not simply linear in  $\mathbf{k}$



## HgTe Ring-Structures



Three phase factors:

Aharonov-Bohm

Berry

Aharonov-Casher

$$\Delta \varphi_{\psi_s^+ - \psi_s^-} = -2\pi \frac{\Phi}{\Phi_0} - b\pi(1 - \cos\theta)$$

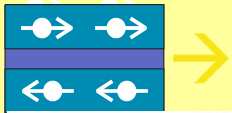
$$\Delta \varphi_{\psi_s^+ - \psi_{\bar{s}}^-} = -2\pi \frac{\Phi}{\Phi_0} - b2\pi r \frac{m^* \alpha}{\hbar^2} \sin\theta$$

$s = \uparrow$  and  $\downarrow$ ,

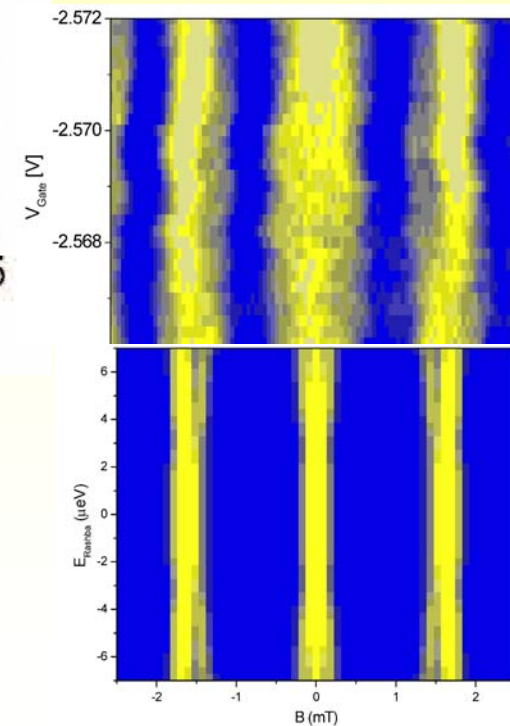
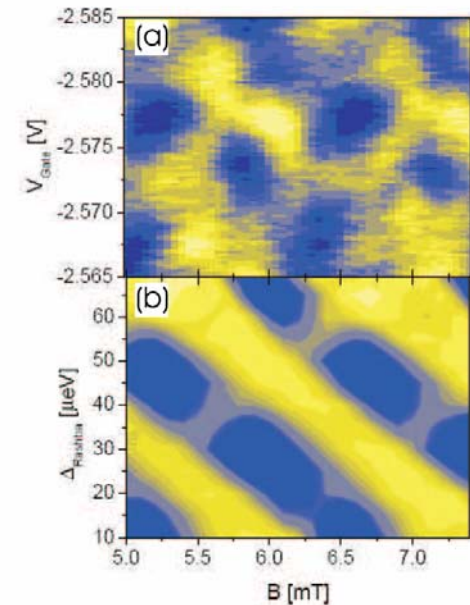
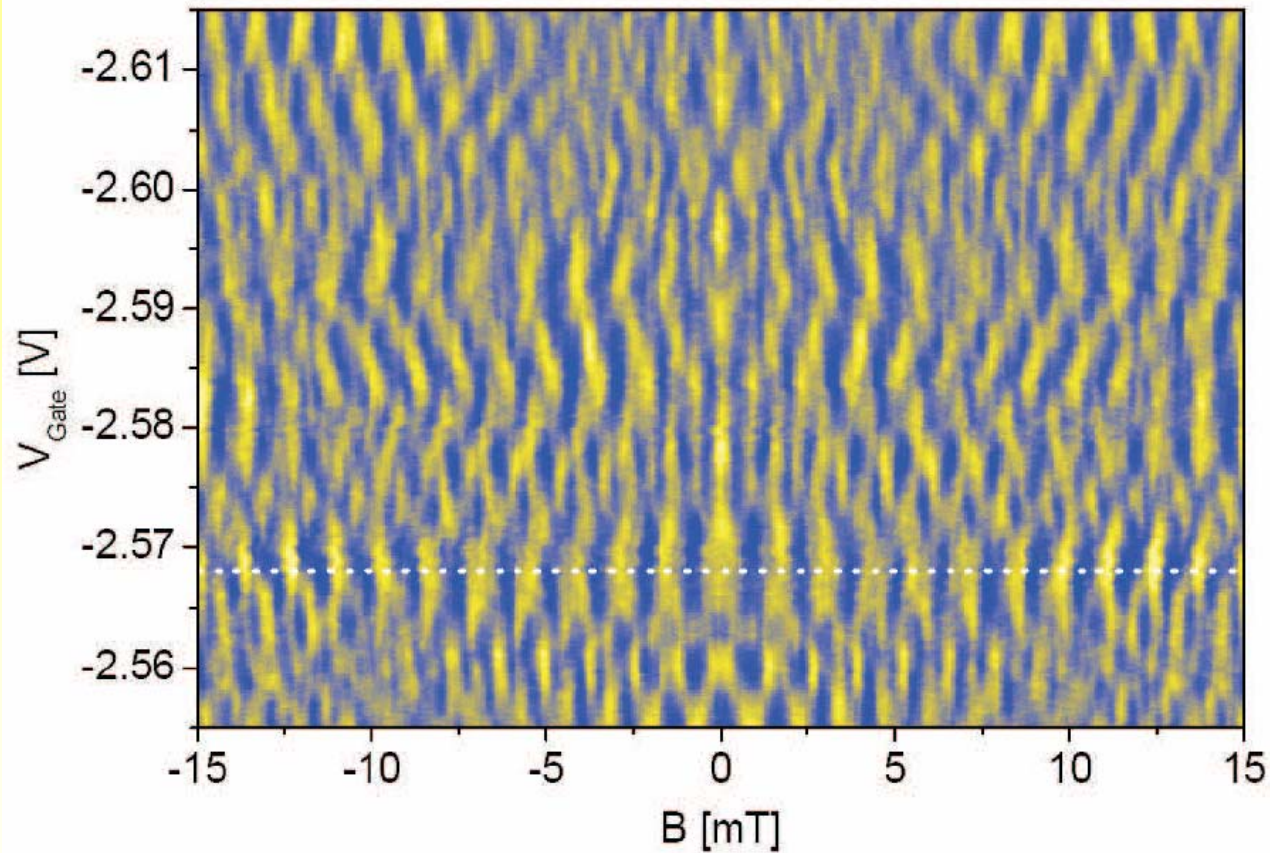
parallel and anti-parallel to  $B_{\text{tot}}$

$b = \pm 1$  for  $\uparrow, \downarrow$

$\theta \ll B_{\text{ext}}, B_{\text{tot}}$ ;  $B_{\text{tot}} = B_{\text{ext}} + B_{\text{eff}}$

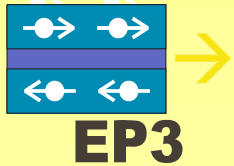


## HgTe Ring-Structures



Modeling E. Hankiewicz, J. Sinova,  
 Concentric Tight Binding Model (a la Nikolic)+ B-field  
 M. König et al., Phys. Rev.Lett. **96**, 76804 (2006).





## Main questions



- SAD RTDs show finite spin splitting at zero B. Why?
- TAMR in GaMnAs: Why extra anisotropy along [001]?
- Details of MI transition in GaMnAs. Do we see the Efros-Shklovskii gap?
- Why don't we see intrinsic SHE or AHE
- Discuss possible experiments on (quantum,insulator) SHE and AHE