Towards Self-consistent Modeling of Star Formation and the Initial Mass Function

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with

- Paolo Padoan (ICREA/ Barcelona)
- Troels Haugbølle, Michael Küffmeier, Troels Frostholm
 Mogensen, Aris Vasileiades (Copenhagen)

Spatial scales:

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Use larger scales as boundary conditions for smaller scales

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Parameter spaces:

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Parameter spaces:

• Avoid getting lost in multi-dimensional parameter spaces

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- If we have a theory:
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- If we have no theory:
 - Being able to investigate in 4-D (space + time) is a perfect foundation to build one on

Star Formation

- Zoom simulations
- Conclusions / consequences for the IMF

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Initial Mass Function

- Basic questions
- Demo simulations
- High resolution experiments

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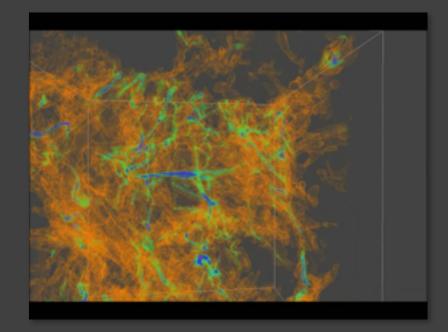
Initial Mass Function

- Basic questions
- Demo simulations
- High resolution experiments

Discussion & Conclusions

What's next / what's missing

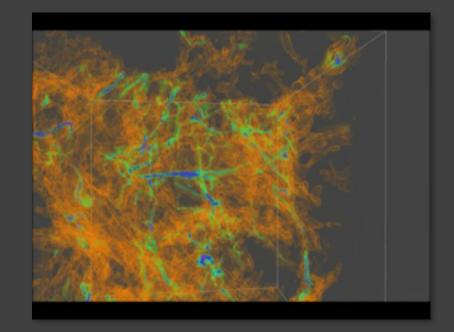
- First of a kind; ab initio simulations of formation of circumstellar disks
 - Using AMR (RAMSES)
- Outer scale 40 pc, inner scale 0.01 AU
 - Ratio 1 : $2^{29} \approx 1 : 1$ billion
 - Animations zoom over 7 orders of magnitude
- So far: Proof of concept
 - 4 solar-mass stars
 - Plan: Get a statistically significant sample of solar mass stars



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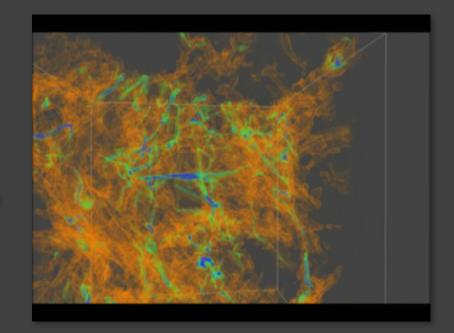
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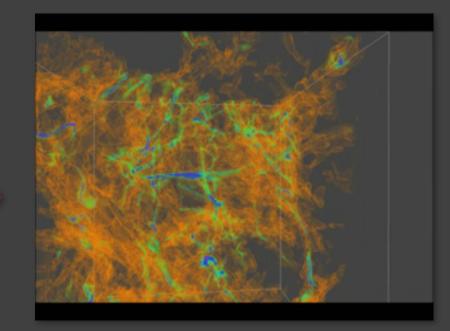
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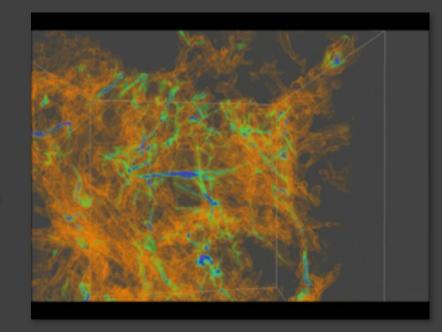
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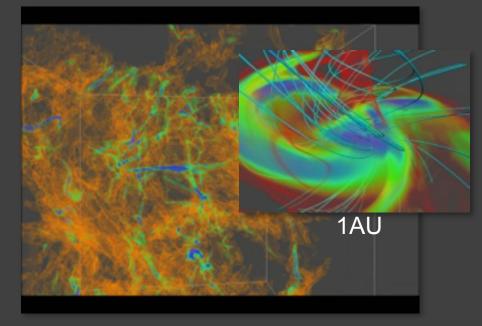


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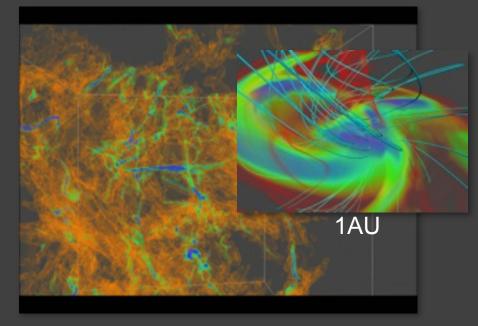
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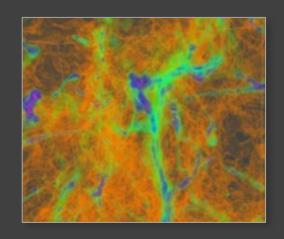
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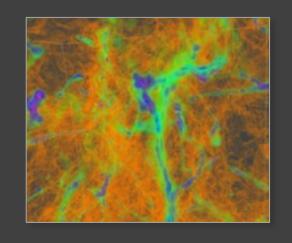


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What if one did the whole box at uniform resolution?

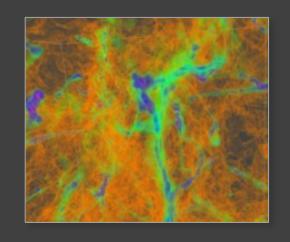


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- At current speed a full 3-D $(2^{30})^4$ simulation would take $^{\sim}10^5$ ages of the Universe ...
 - 1 PetaFlop for 10^{15} yr = 2^{50} times the largest supercomputer grants

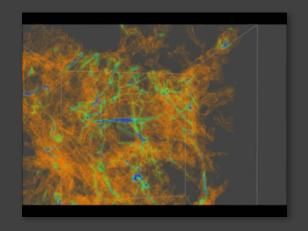
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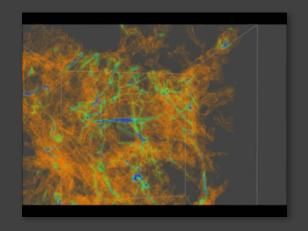
BUT: if Moore's law continues, such an increase with 50 powers of two will take less than 80 years (!)

- "Anchor dynamics" in well-observed spatial range
 - Giant Molecular Clouds (GMCs) and their fragments
 - "Larson relations" (Larson 1979, 1981; Solomon et al 1987, ...)



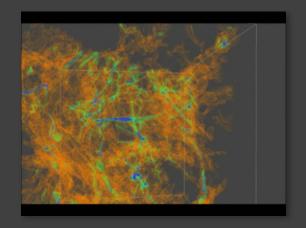
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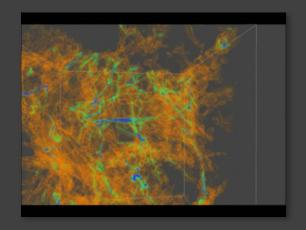
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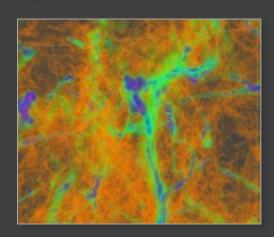
However, even simulating only the PP-disk part would require a scale range from at least ~300 AU to ~0.01 AU – the full range is "only about twice as expensive" (AMR!)

Giant Molecular Cloud scales

■ Size: 40pc

■ Refinement: $2^{16} \Rightarrow \text{cell size } 120 \text{ AU}$

■ Time duration: ≈ 10 Myr

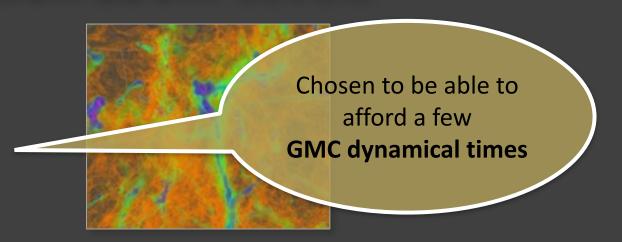


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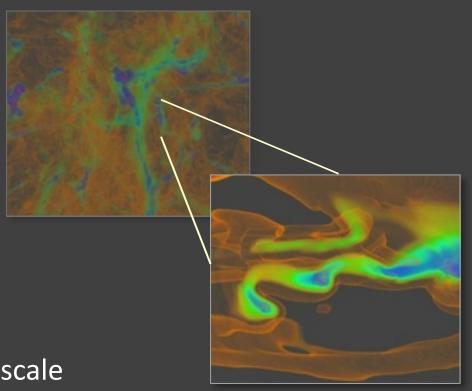


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- Dynamic scale: ~ 0.5 pc
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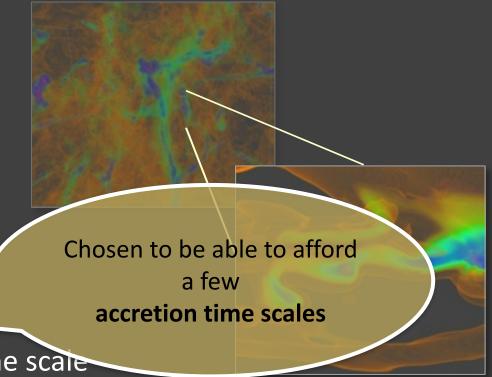


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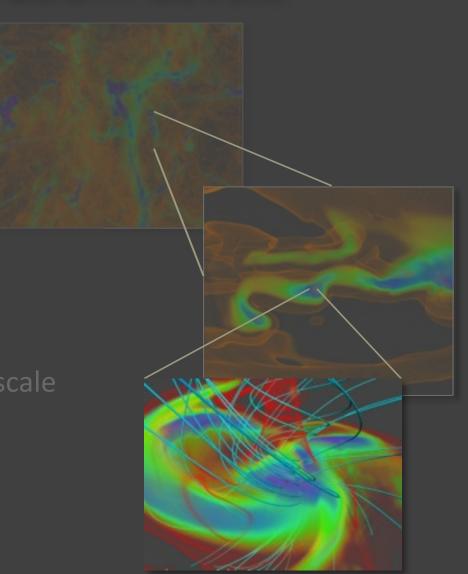
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- Dynamic scale: ~ 5 AU
- Refinement: $2^{30} =$ cell size 0.008 AU (!)
- Time duration: ≈ 100-1000 yr



Three Simulation Zoom Levels

Giant Molecular Cloud scales

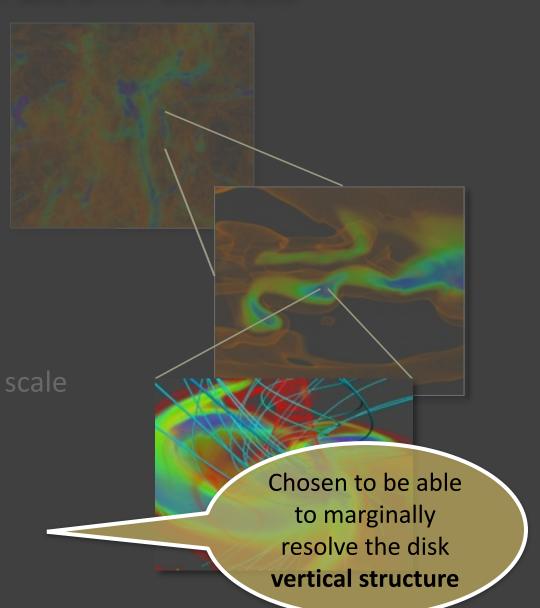
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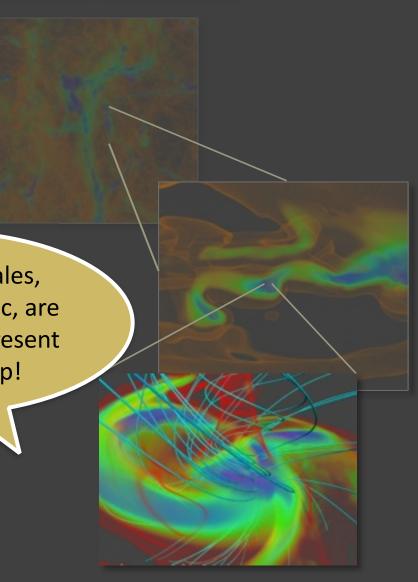
Note that *all* scales, up to the full 40 pc, are simultaneously present also in this step!

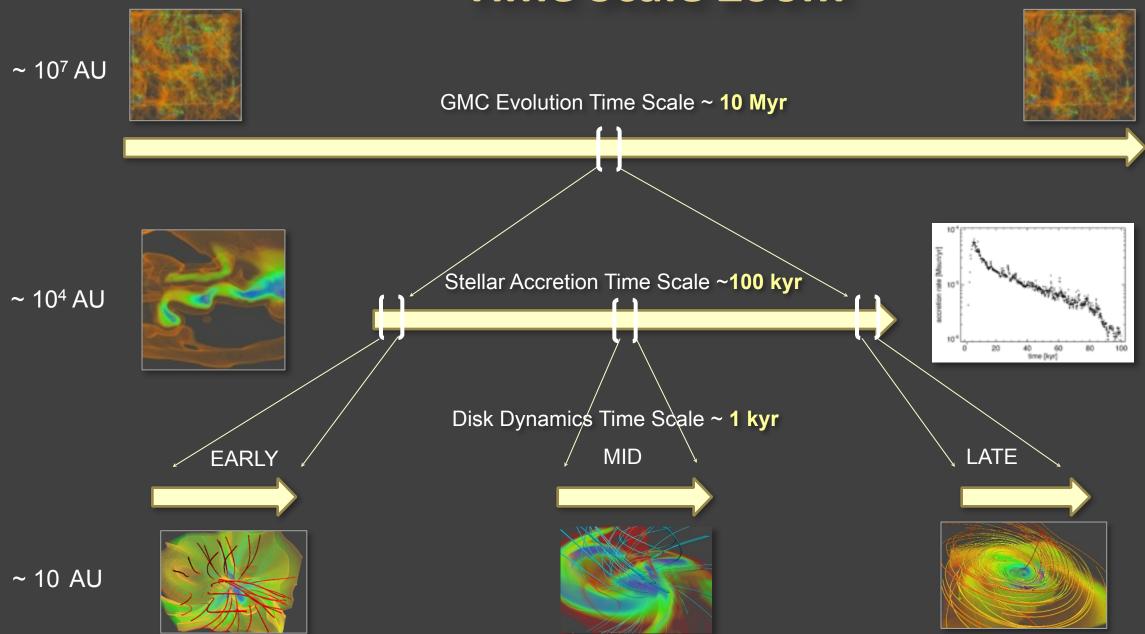
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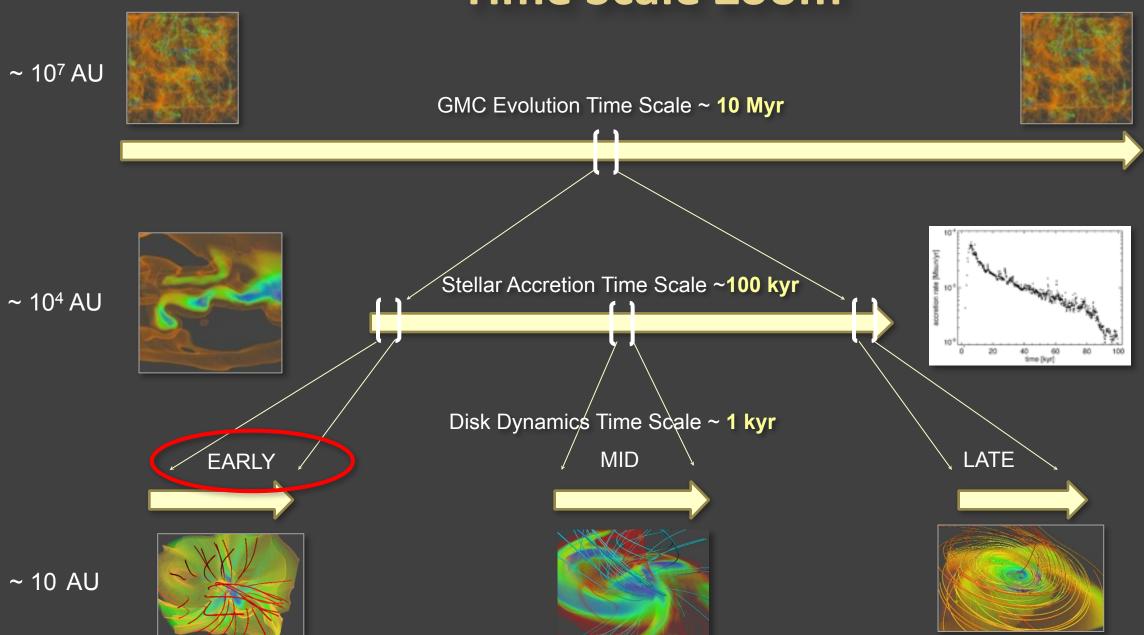
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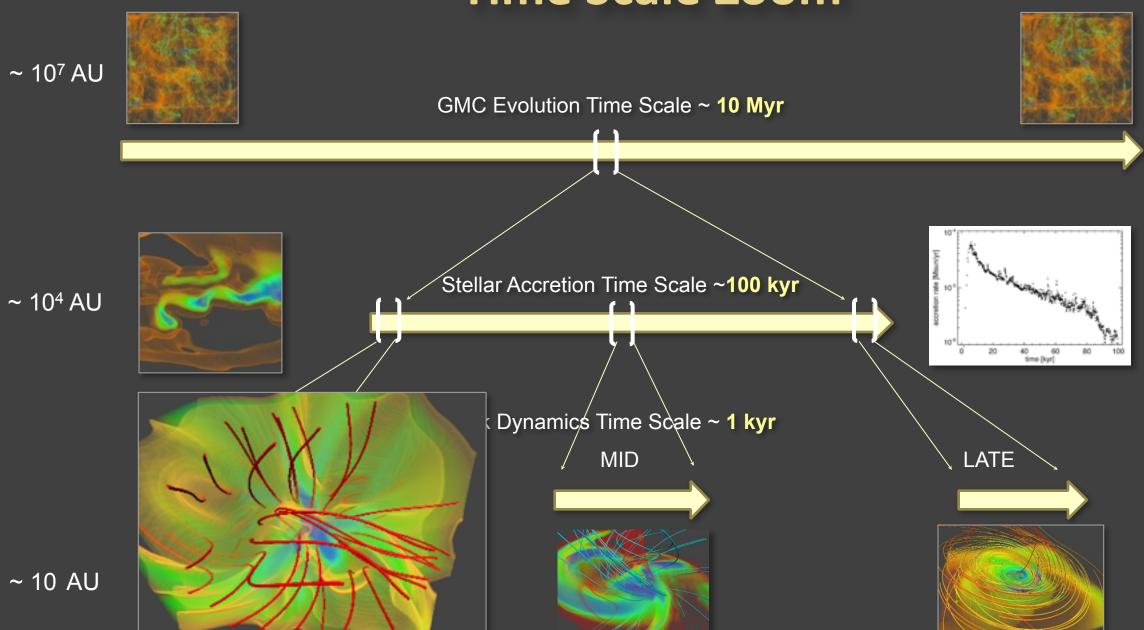
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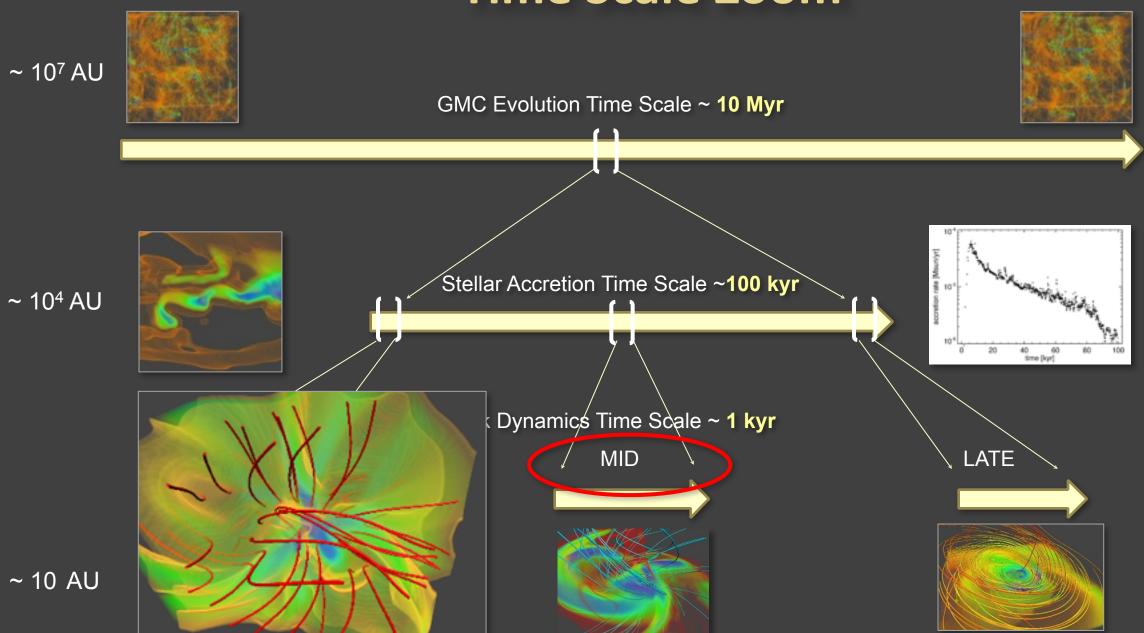
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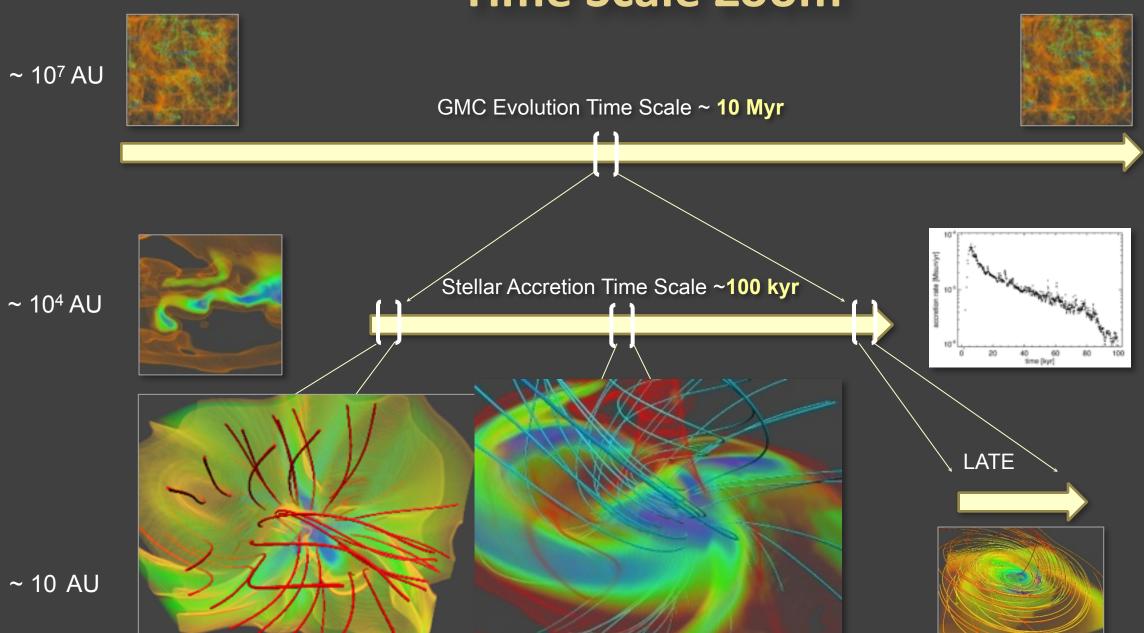


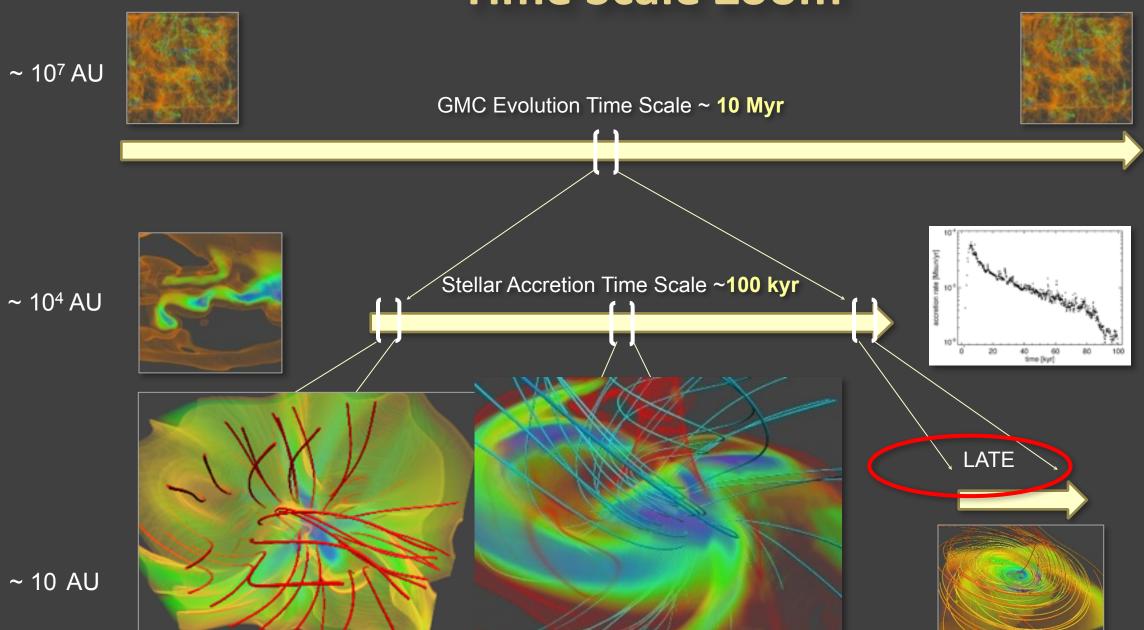


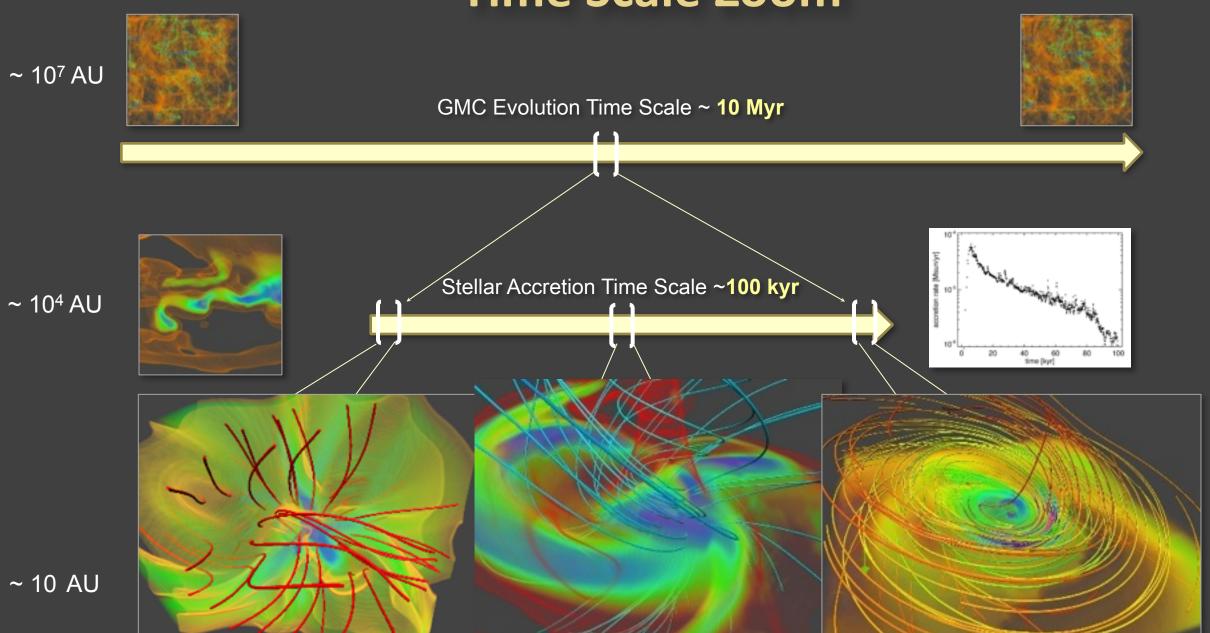




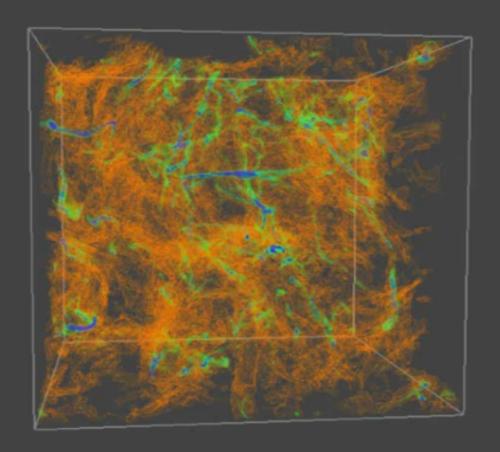




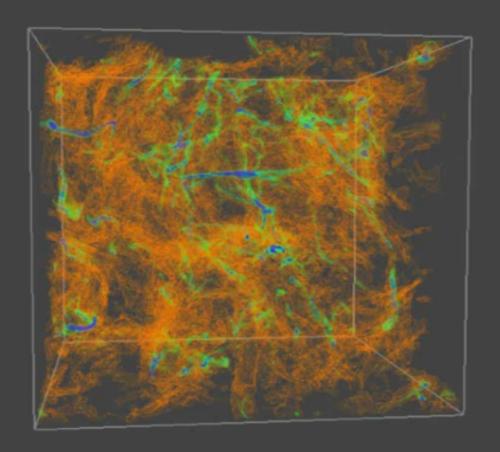




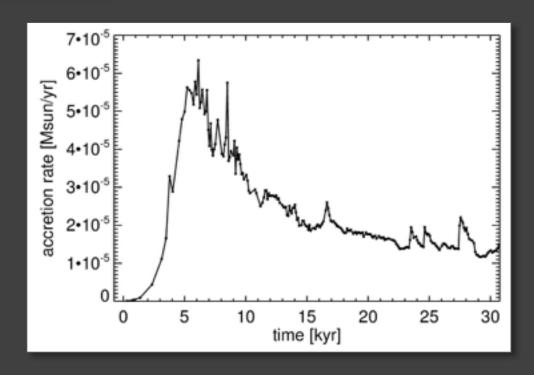
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Accretion Rates



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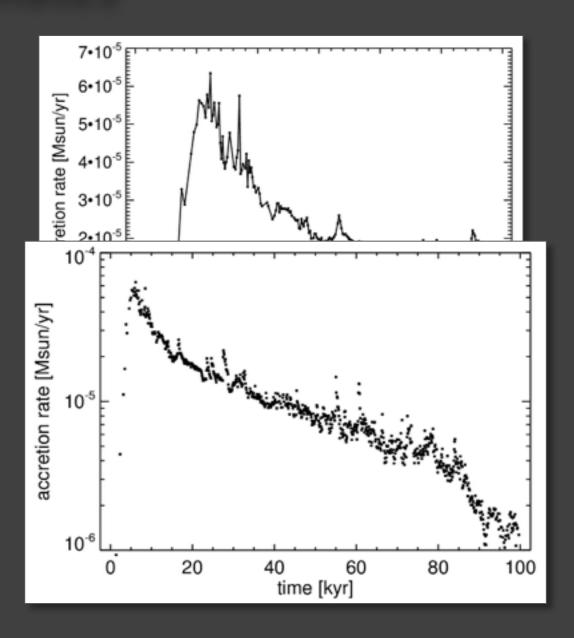


time [kyr]

Accretion Rates

Instantaneous accretion rate to the central sink particle:

- Peaks after about 5 kyr, fluctuates due to magnetic field topology changes
- Decreases exponentially with time thereafter

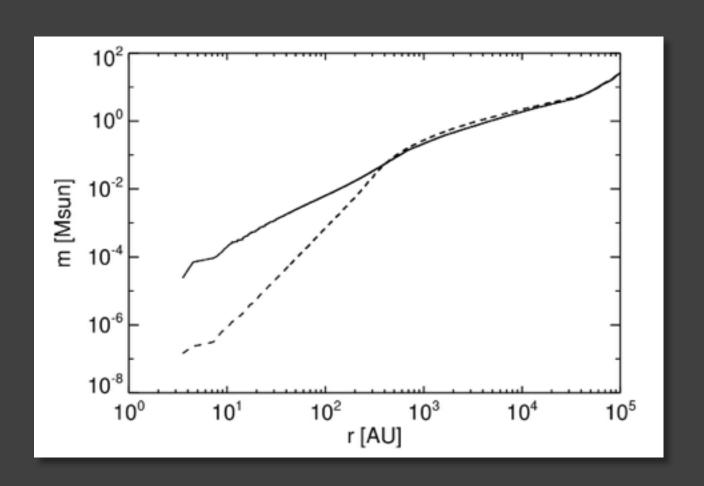


Mass Distribution with Radius

Integrated mass as a function of distance from the central sink particle (star)

Initially (dashed) very steep

- Quickly develops power law dependence m ~ r^{3/2}, characteristic of "free fall"
 - Consequence of magnetic braking!

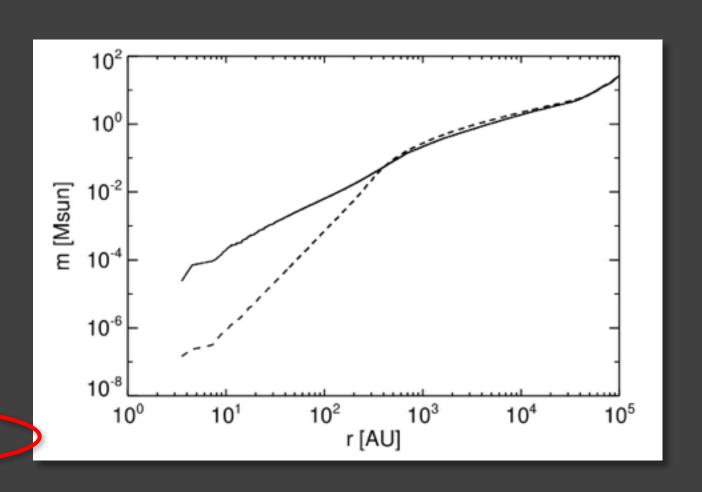


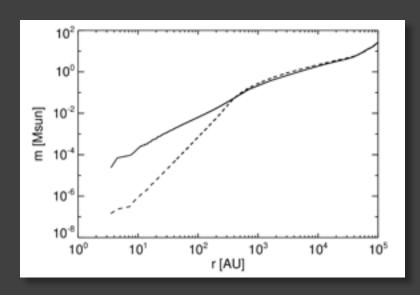
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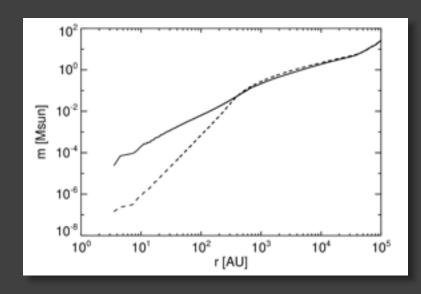
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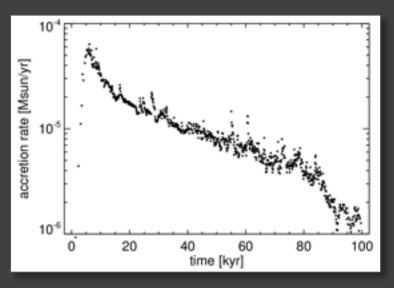
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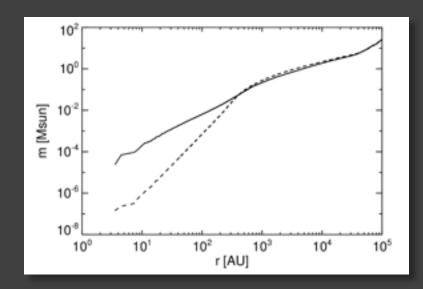
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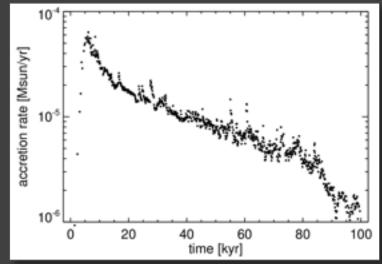


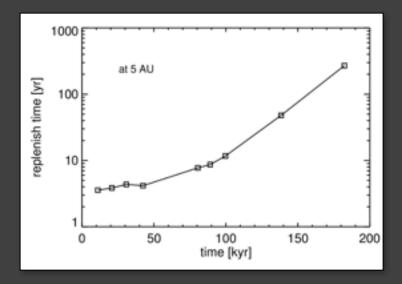


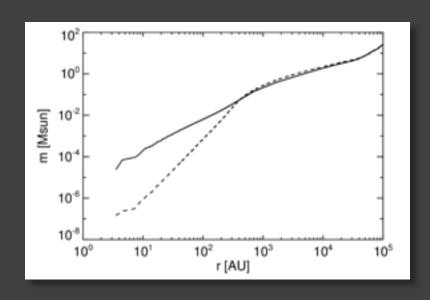


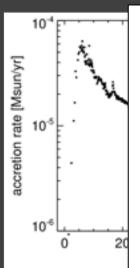


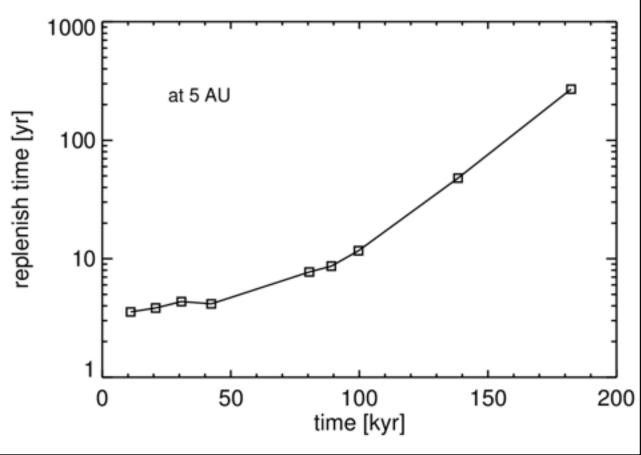


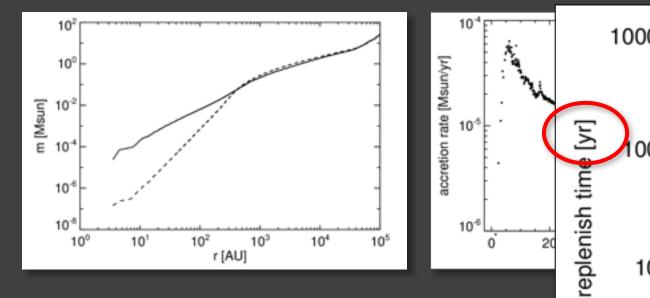


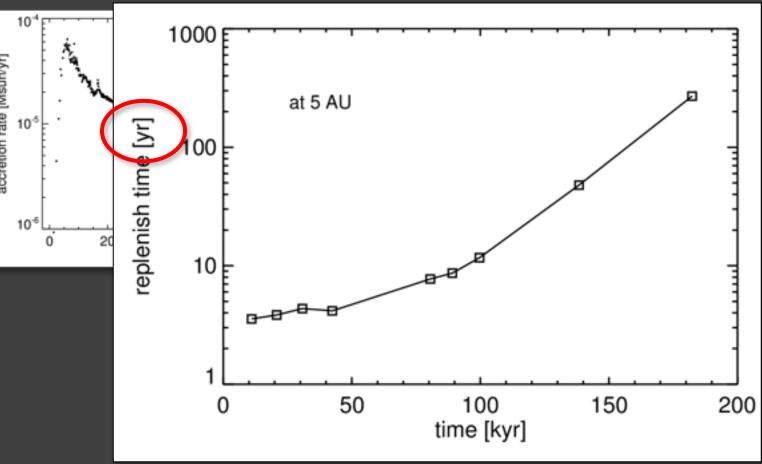


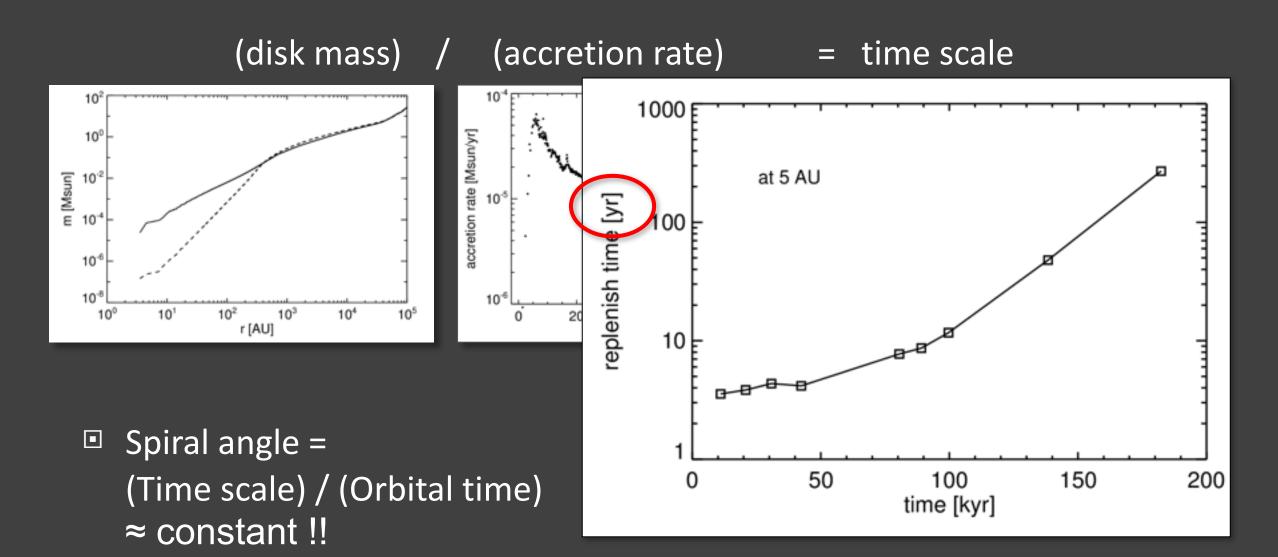










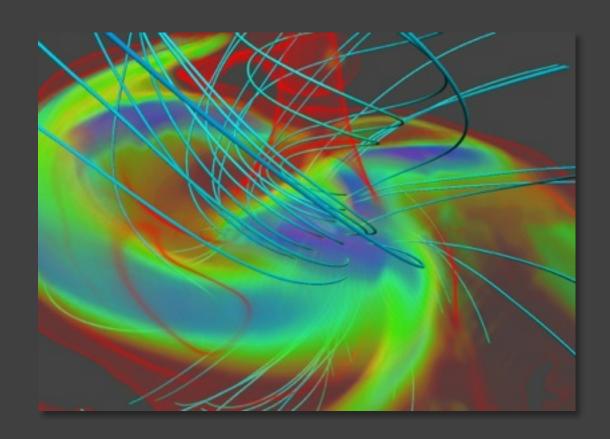


The simulations produce, spontaneously, inner *jets* and larger scale *disk wind outflows*

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 - disk wind with speeds ~ 10 km/s
 - Driven by inclined magnetic fields

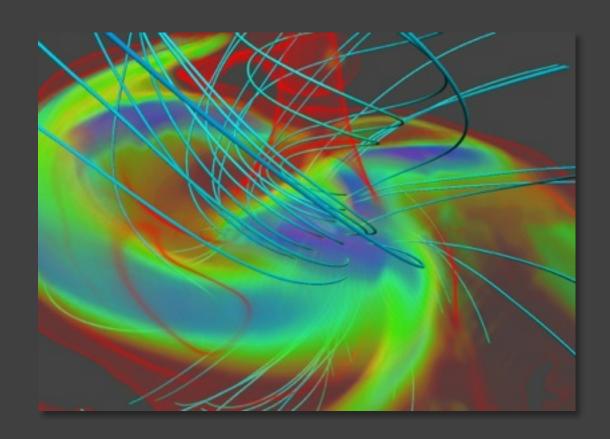
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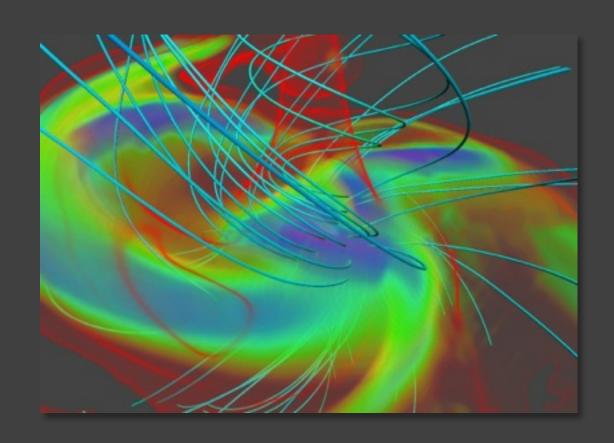
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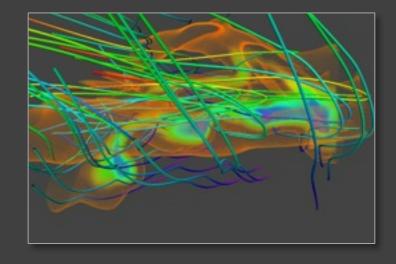
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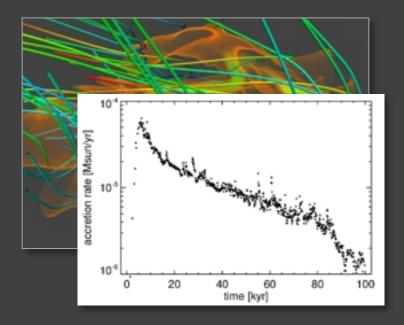
Inner parts:

- Highly collimated jet
 with outflow speeds ~ 100 km/s
- Resolving the near-star environment is **not** necessary for jet formation!

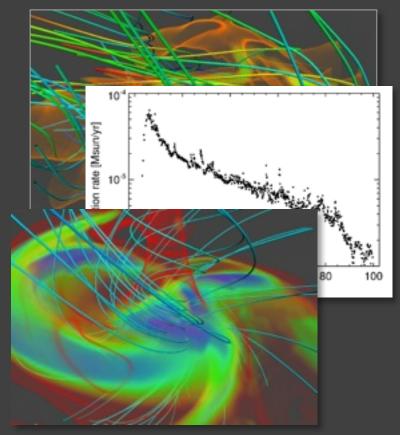




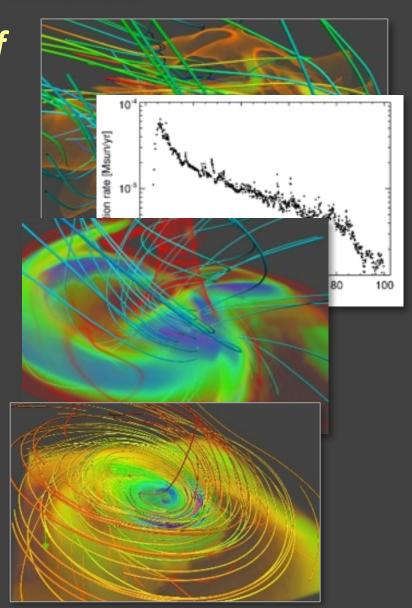
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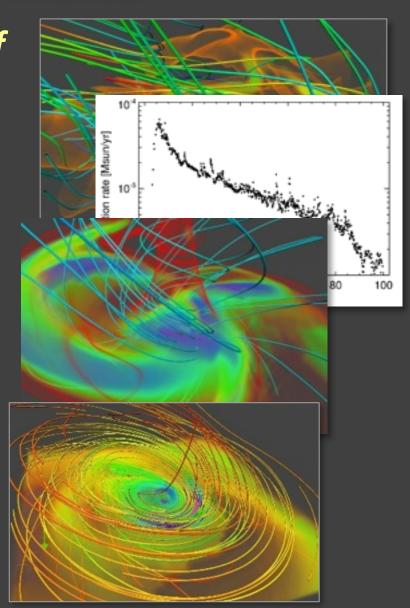
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 - Disk winds and jets carry away ~50% of the mass, or more

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 - SAD (the Standard Accretion Disk scenario) is out-dated!
- Demonstrates that star and planet formation depends crucially on
 - A *pseudo-random 'parameter'* among star forming envelopes!
 - Surviving angular momentum may be a random remnant
- Illustrates the central importance of bi-polar outflows
 - Disk winds and jets carry away ~50% of the mass, or more
 - Much MORE of the angular momentum *and energy*

Conclusions for IMF context

- Resolving the accretion region is affordable
 - Avoids having to define parameters for Bondi-Hoyle type formulae
- Gas pressure gradients should not be ignored
 - Gas is *not* moving ballistically far from it!
- Sink particle recipes should respect the radial density profile
 - Avoid triggering spurious sink particles in accretion flows
 - Calibrate dimensionless accretion rate from highly resolved examples

Main IMF questions

Which mechanisms control the shape of the IMF?

- What determines the power law slope?
- What determines the peak position?
 - Why does it appear to be so independent of the environment?

Which mechanisms are important, and which are not?

What is needed to get the IMF right?

Some answers (Padoan & Nordlund 2002, ...)

The power law slope:

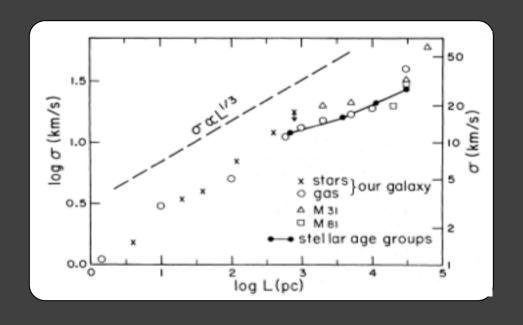
The size distribution of fragments created by super-Alfvénic MHD turbulence

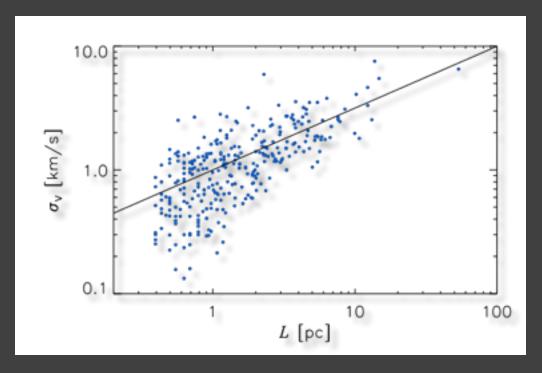
The turn-over and peak:

Rate of failure-to-collapse becomes significant

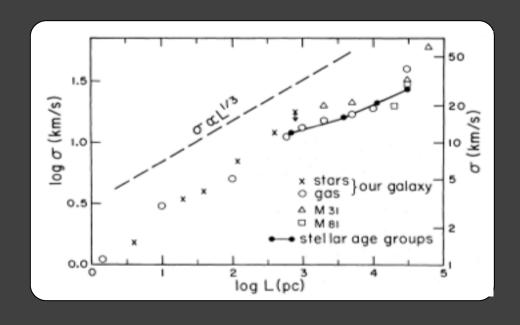
Peak position:

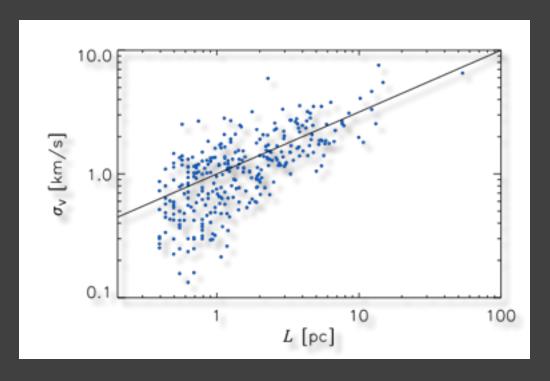
- Larson's law scalings
- Fortuitous cancellation (follows from Larson's relations)
 - Density dependence vs. Mach number (external ram pressure)



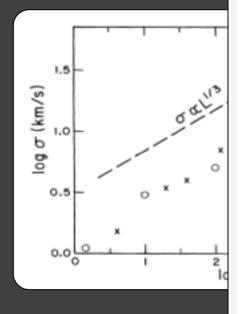


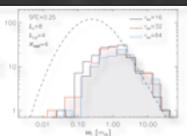
Starting out with the empirical velocity dispersion (Larson's law)



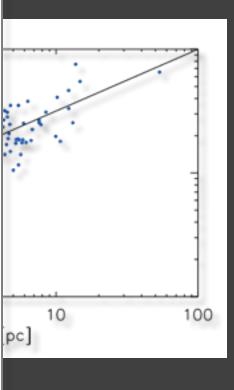


Starting out wi

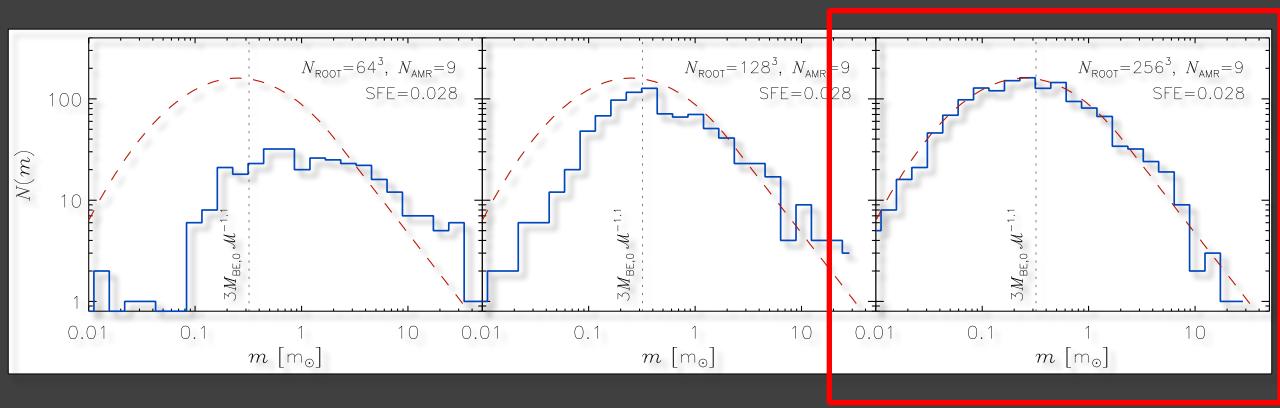




rson's law)



Starting out with the empirical velocity dispersion (Larson's law)



Starting out with the empirical velocity dispersion (Larson's law)

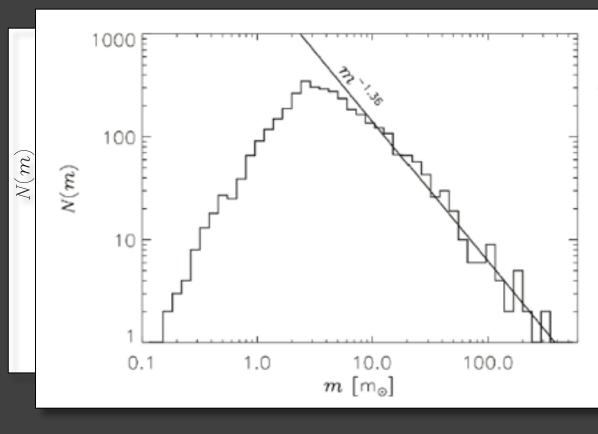
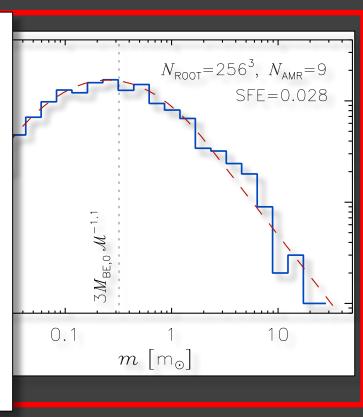
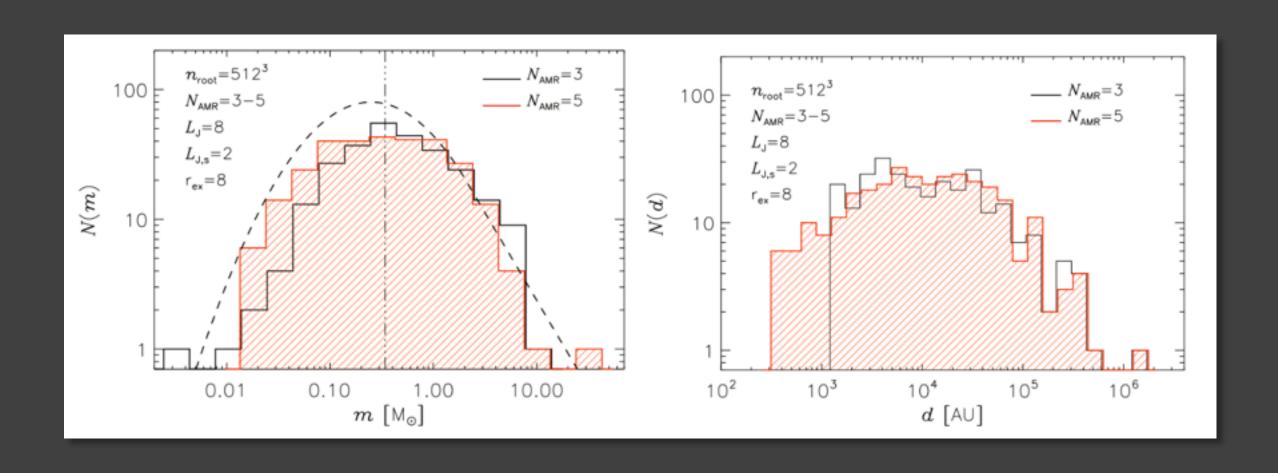


Figure 4: The mass distribution of approximately 4,000 stars from the Fountain1 simulation. Massive stars follow an almost perfect power law, with slope nearly identical to the observed Salpeter value. The power law covers the full range of masses of stars that end their lives as SNae. (Padoan, Haugbølle and Nordlund, in preparation).



Dependence on max AMR level



Demonstration experiment – 2 days @ 400 cores

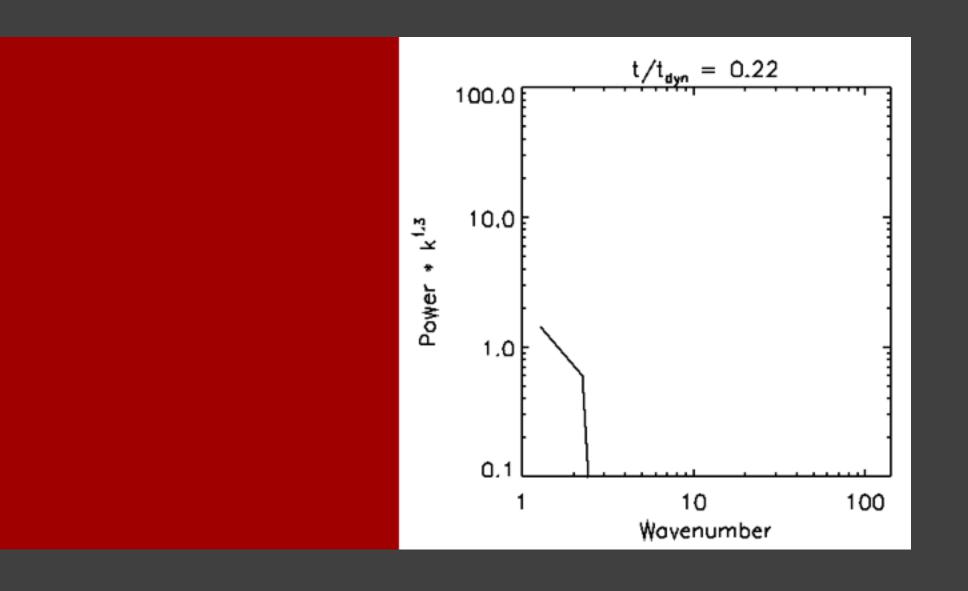
Physical

- Isothermal (T = 10 K, c = 0.18 km/s)
- Box size = 3.33 pc ≈ 0.7 million AU
- Mach number = 12 (consistent with Larson)
- Mean density = $1000 \text{ H}_2/\text{cm}^3$ (slightly overdense relative to Larson)

Computational

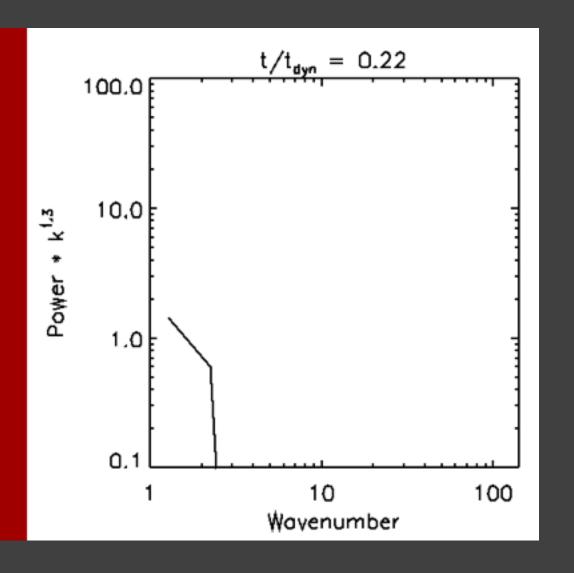
- RAMSES AMR + locally developed sink particle creation & accretion
- levels = 7-14 (root grid 128³, min cell size 1/2¹⁴ = 40 AU)
- HLLD solver, locally developed 3-D slope limiter

Initial initial condition—not useful!

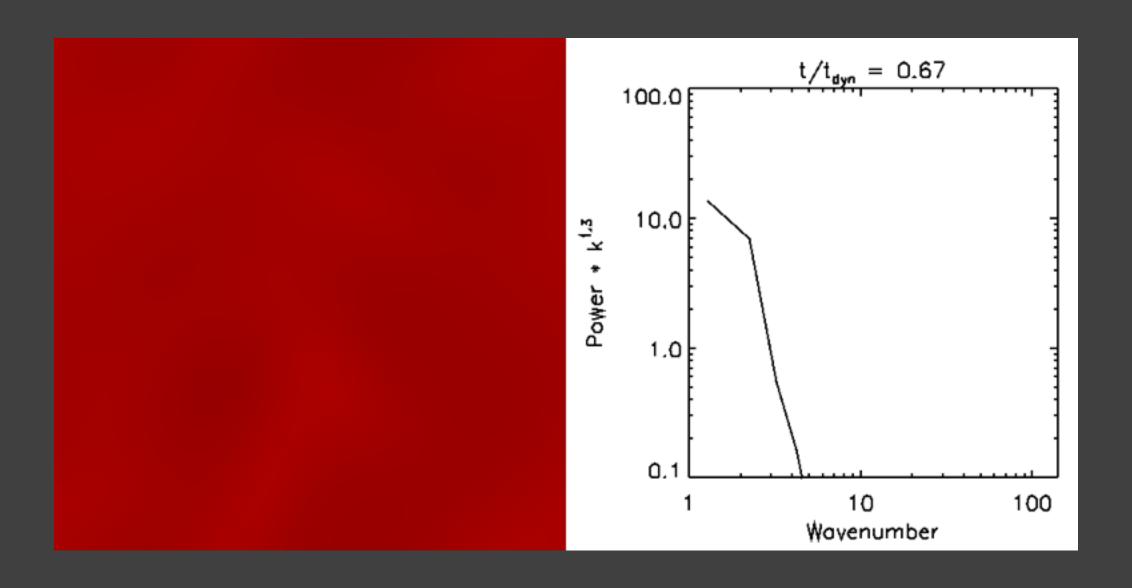


Initial initial condition—not useful!

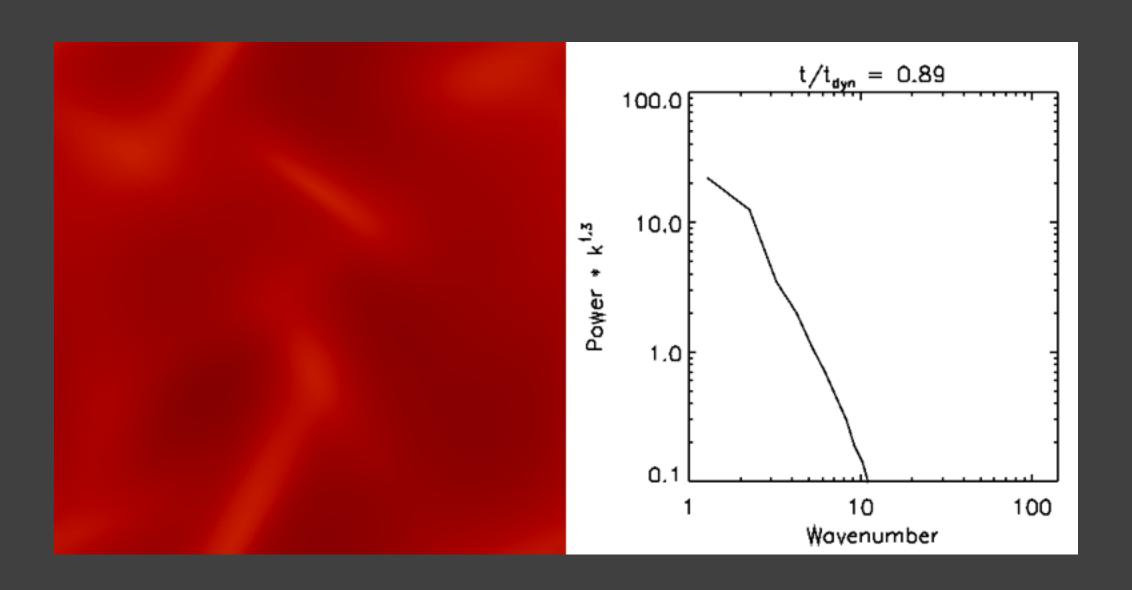
Drive supersonic, super-Alfvenic turbulence (initially no gravity) for about 3 dynamical times



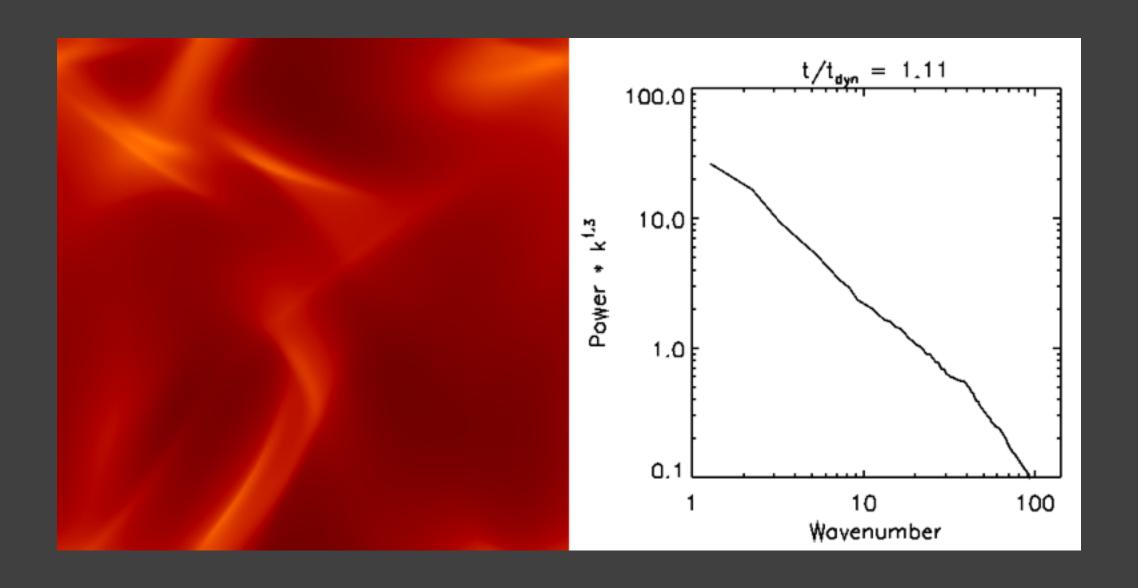
Fraction of dynamic time: weak density fluctuations ...



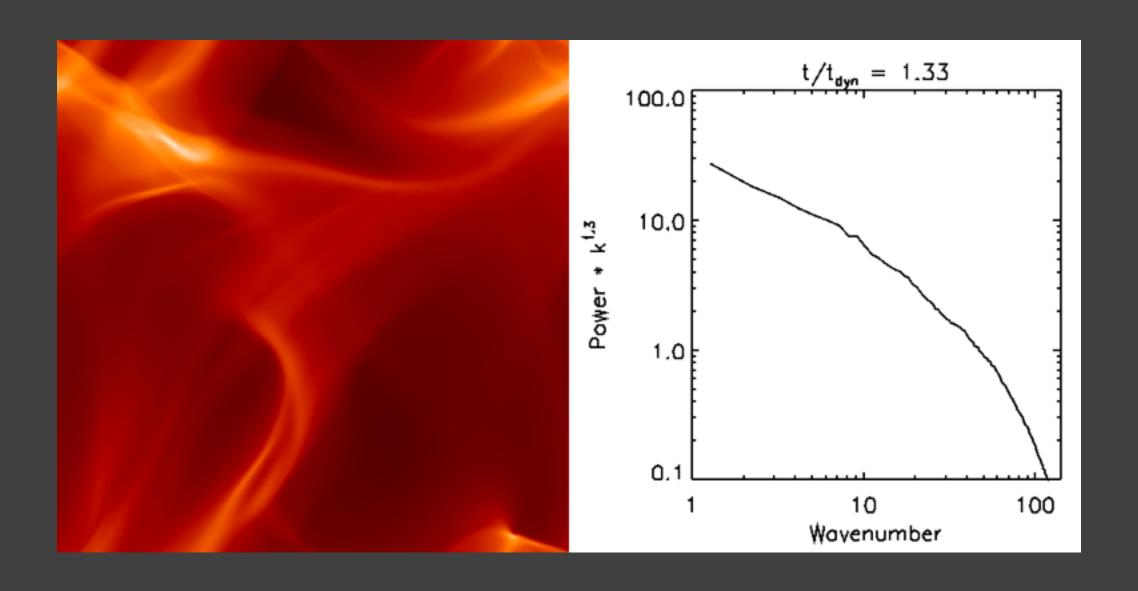
... sharpening ...



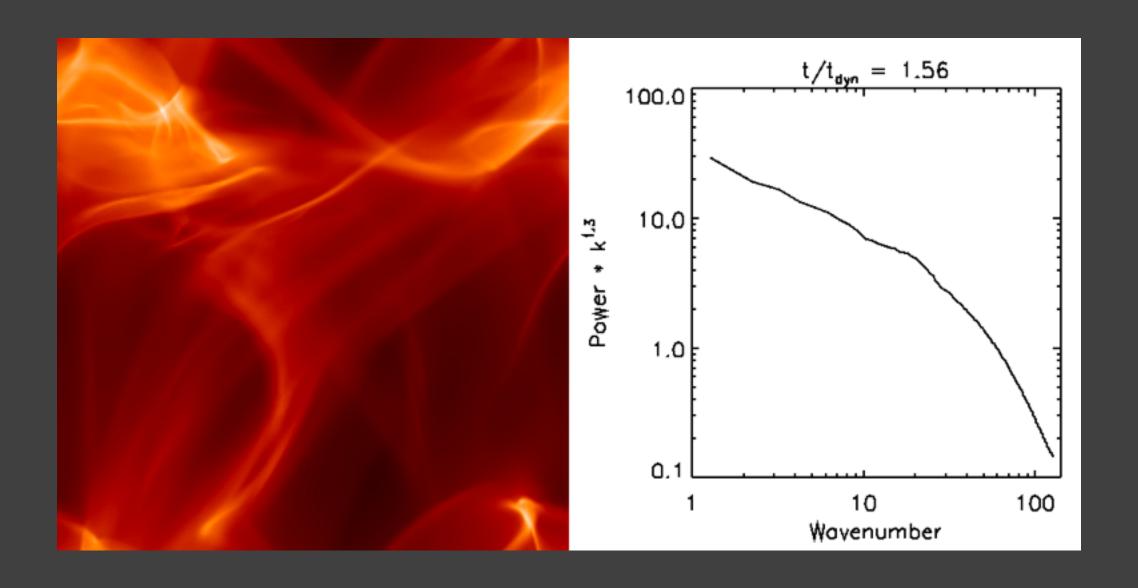
... into shocks at one dynamic time ...



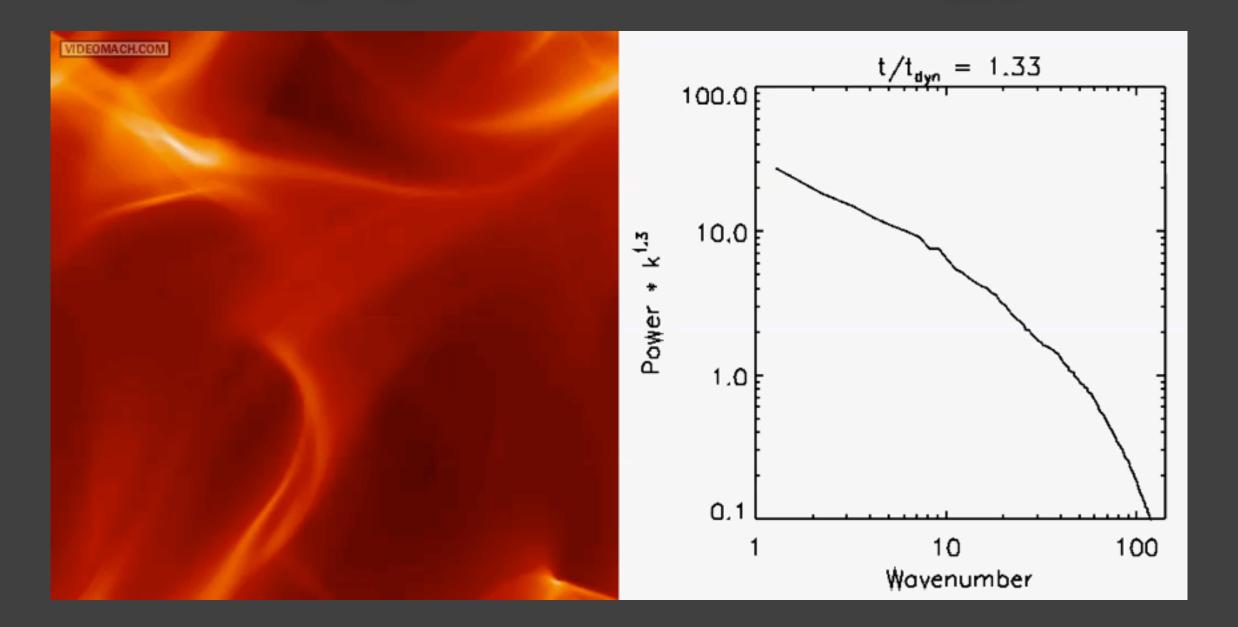
... shock interaction ...



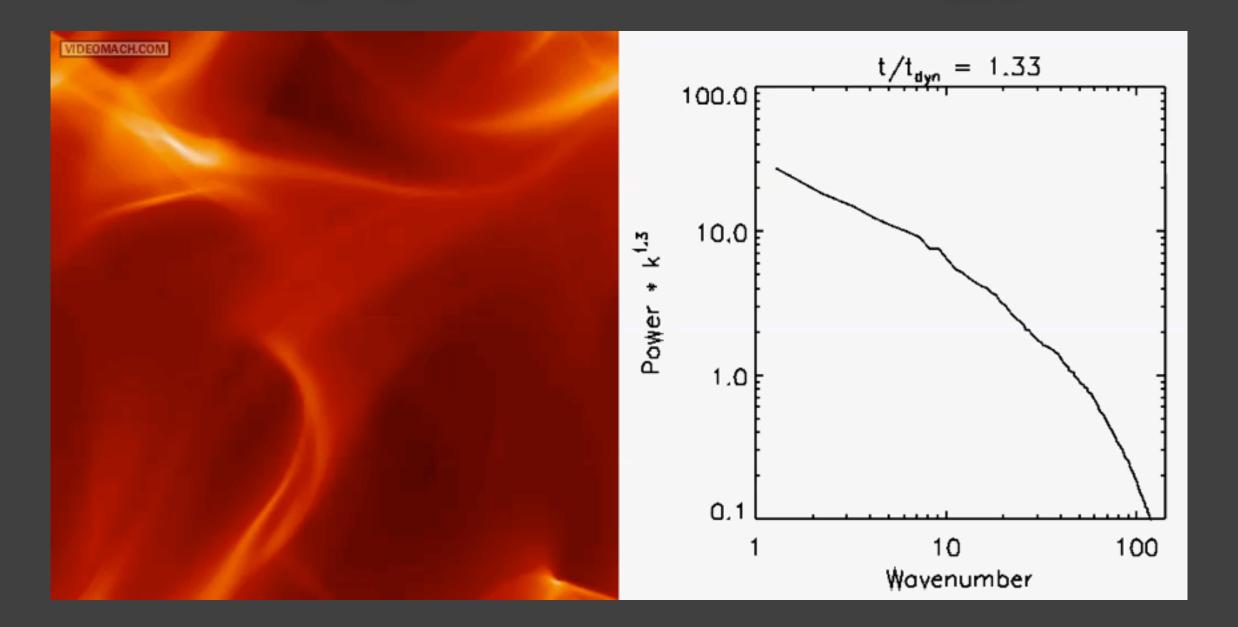
... over to animation ...



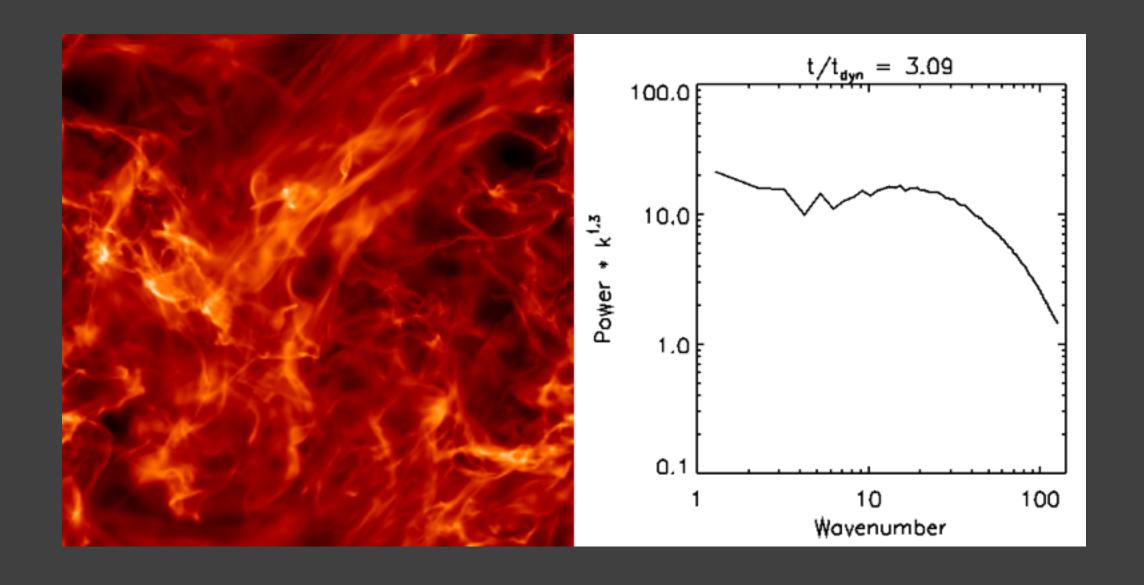
Increasing fragmentation – cf kinetic energy power



Increasing fragmentation – cf kinetic energy power



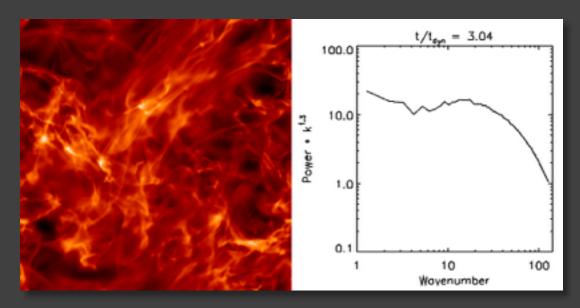
Final Initial Condition for IMF experiment



Turning on gravity

Self-gravity is gradually ramped up to the value consistent with the size and mass (Larson's relations)

This corresponds closely to the gradual compression of this MC as it is assembled in a larger (GMC) context

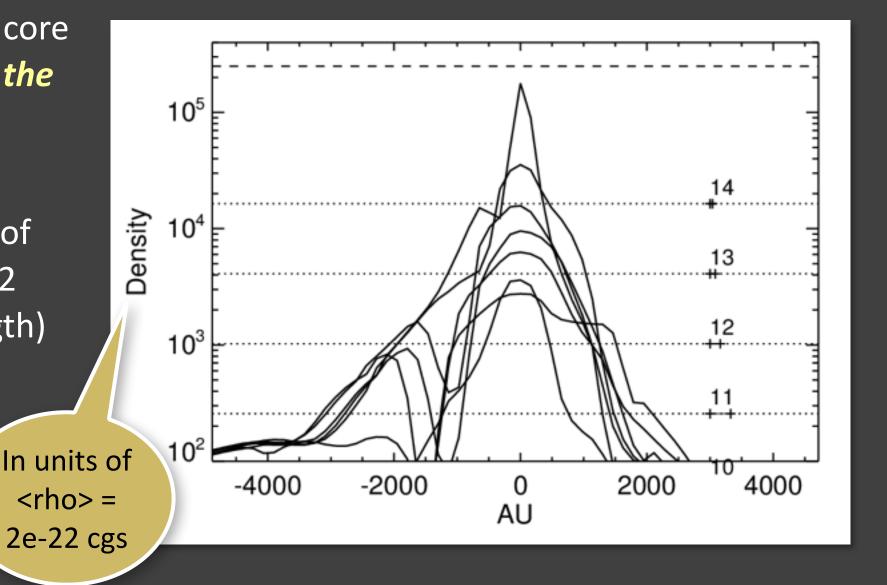


The first star \rightarrow a single star IMF!

Mass in the collapsing core ≈ 0.2 solar masses: *on the IMF peak*!

 Dotted lines: levels of mass refinement (12 cells per Jeans' length)

Dashed line: sink translated line: sink t



Conclusions from numerical experiments

Needed for realistic IMF

- MHD-turbulence = magnetic fields and turbulence
- Supersonic and super-Alfvenic conditions
 - Sound speed \approx 0.2 km/s (T \approx 10 K)
- Respecting Larson's relations
 - Driving of some sort (SNe, artificial, ...)

Not needed:

- Non-isothermal EOS
- Radiative transfer
- Local feedback

Towards self-consistent experiments

- We have SN-feedback
 - Tables of life-times, stars explode at the time (and place!) appropriate
- Radiative transfer
 - Just finished implementing ray-tracing in Ramses AMR
- Chemistry
 - KROME code has just been integrated

Overall conclusions

What controls the IMF?

- Power law slope: Statistics of super-Alfvenic MHD turbulence
- Peak position: Larson's relations = ISM scaling laws

This begs the question: What controls Larson's relations?

- Self-regulated feedback!
- Cannot be dominated by local feedback

Thanks for your attention!