

# The Star Formation Law in a Multifractal ISM

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# The Star Formation Law

$$\dot{\Sigma}_{\text{SF}} \propto \Sigma_{\text{gas}}^{n_{\text{gas}}} \quad n_{\text{gas}} \simeq 1.5$$

Observationally established for:

- global SF and gas density
- local SF and gas density averaged over scales from kpc to  $\approx 500\text{pc}$

# Traditional Interpretation


$$\left. \begin{array}{l} \dot{\rho}_{\text{SF}} \propto \frac{\rho_g}{\tau_{\text{SF}}} \\ \tau_{\text{SF}} \propto \rho_g^{-0.5} \end{array} \right\} \dot{\rho}_{\text{SF}} \propto \rho_g^{1.5} \implies \dot{\Sigma}_{\text{SF}} \propto \Sigma_g^{1.5}$$

Free-fall but not only

$h \approx \text{const.}$

# Complications

- Conceptual
  - Star formation a local phenomenon only takes place at very dense cores at  $\sim 0.1$  pc scales
  - Mean density dependence of timescale assumed not necessarily meaningful

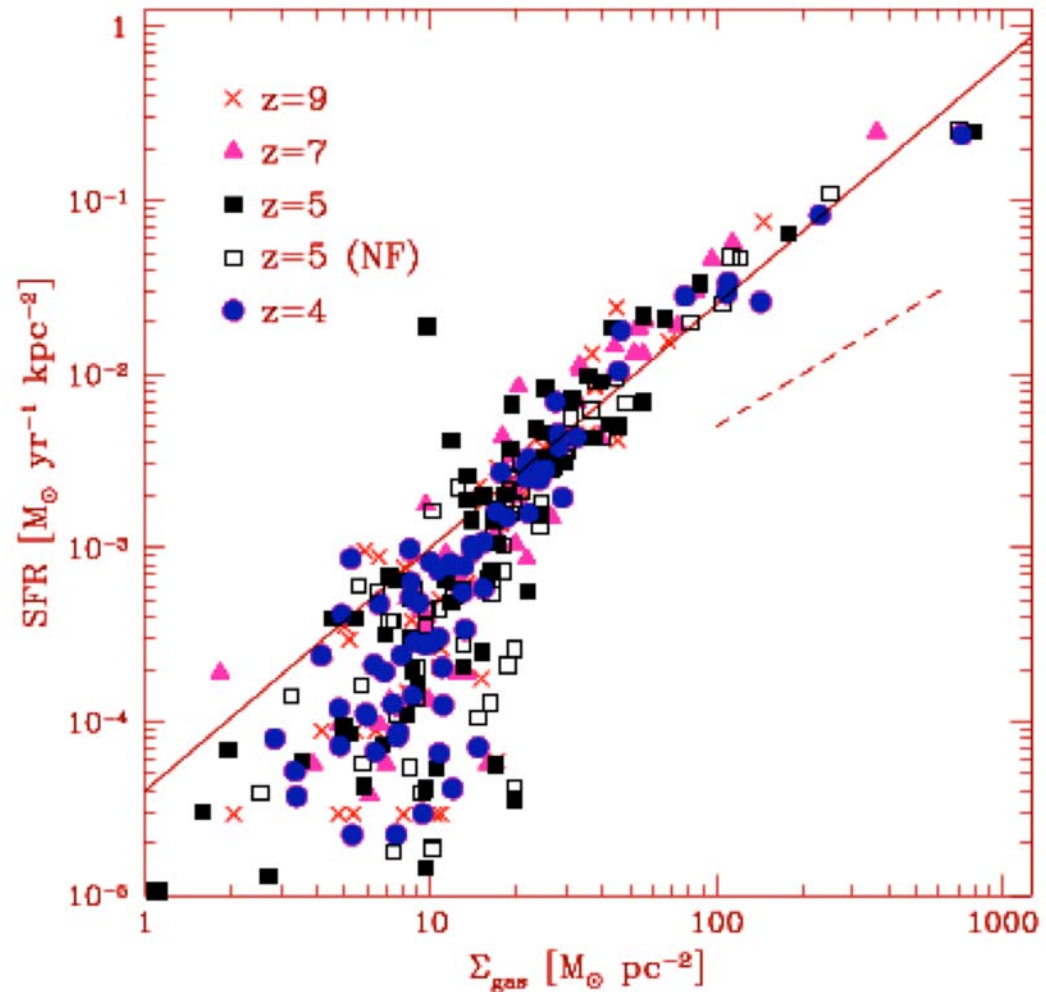
$$\dot{\rho}_{SF} \propto \frac{\rho_g}{\tau_{SF}}$$
$$\tau_{SF} \propto \rho_g^{0.5}$$


# Complications

- In simulations

Large-scale SF law reproduced in ART sims assuming *constant* SF timescale

Kravtsov (2003)



# Complications

- Observational

- In dwarf galaxies

$$\dot{\Sigma}_{SF} \propto \Sigma_g^{n_{\text{gas}}} \quad n_{\text{gas}} > 1.5$$

e.g. : NGC 6822 de Blok & Walter (2006)

M33 Heyer et al. (2004)

IC10 Leroy et al. (2006)

- SF correlates linearly with dense gas

$$\dot{\Sigma}_{SF} \propto \Sigma_{\text{den.gas}}^{n_{\text{den}}} \quad n_{\text{den}} \simeq 1$$

Gao & Solomon (2004)

Wu et al. (2005)

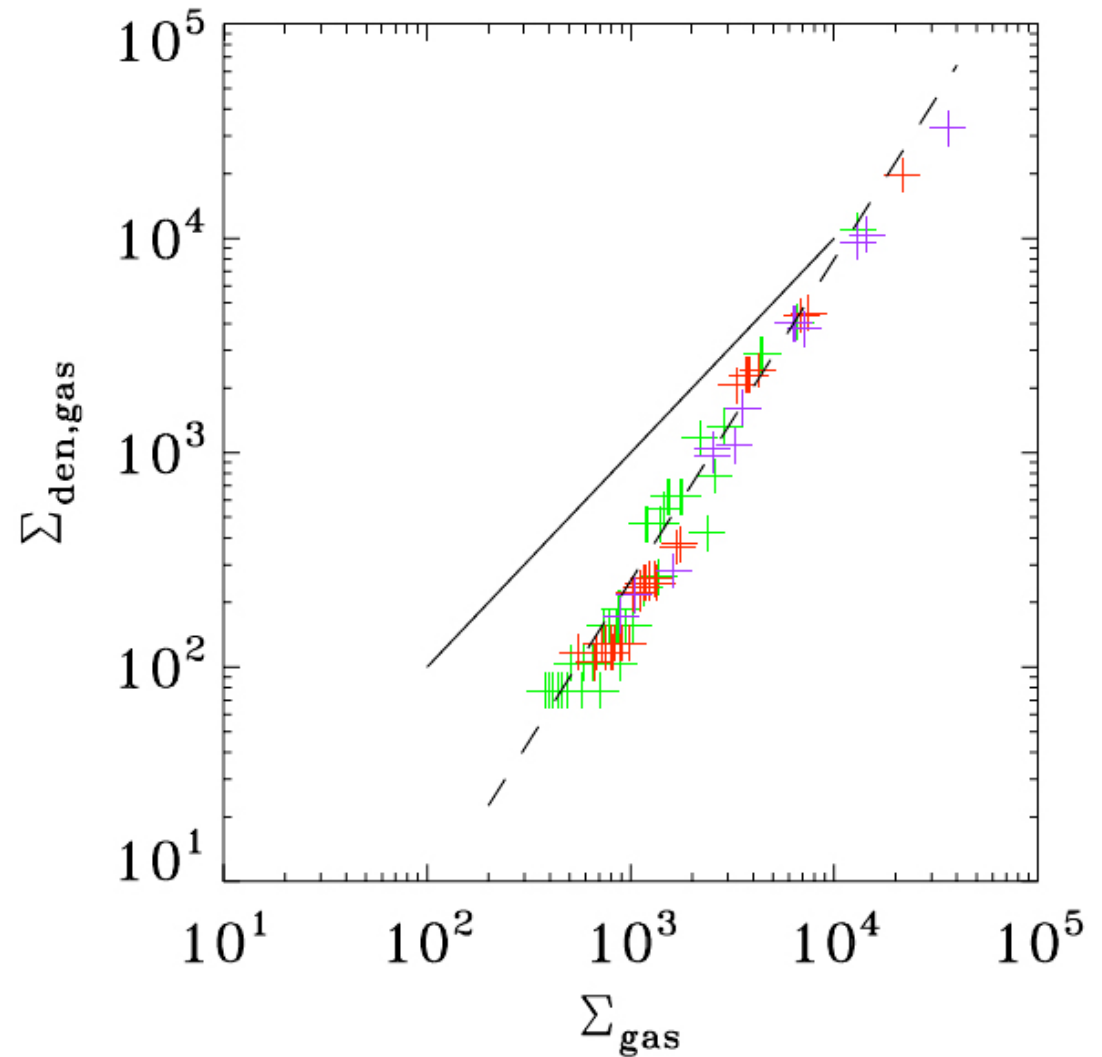
# From Small to Large

$$\left. \begin{aligned} \dot{\Sigma}_{SF} &\propto \Sigma_g^{n_{\text{gas}}} \\ \dot{\Sigma}_{SF} &\propto \Sigma_{\text{den.gas}}^{n_{\text{den}}} \end{aligned} \right\} \Sigma_{\text{den.gas}} \propto \Sigma_{\text{gas}}^n$$
$$n = \frac{n_{\text{gas}}}{n_{\text{den}}} \simeq n_{\text{gas}} \simeq 1.5$$

Non-linear correlation of total gas density and dense gas is implied

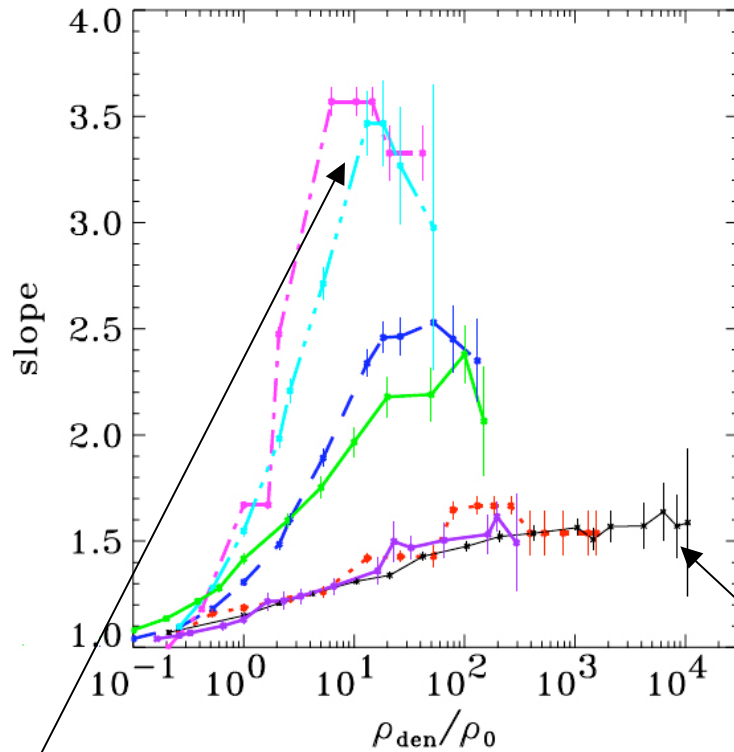
# Multifractal ISM?

Multifractal density field generated using random- $\beta$  model of fully developed turbulence

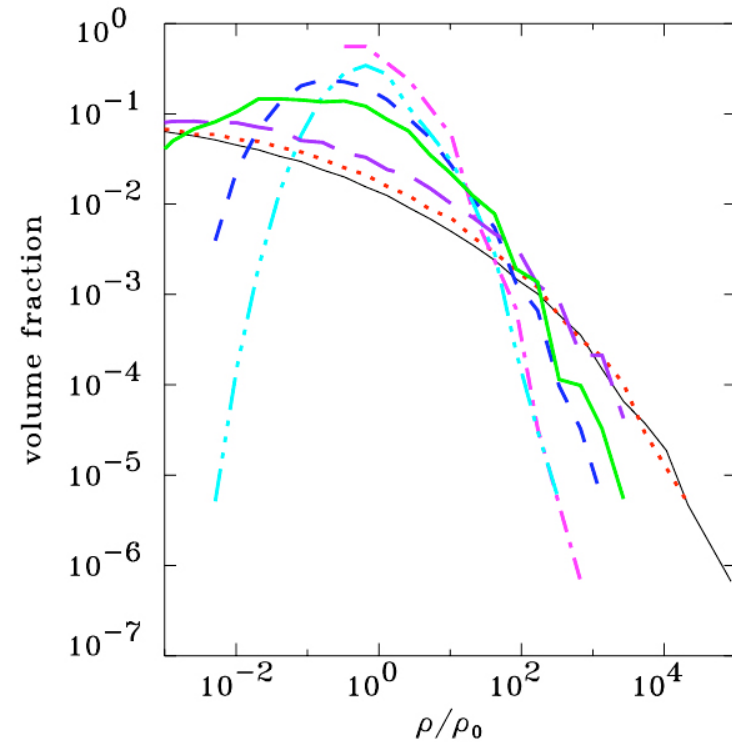




# How robust is this scaling?



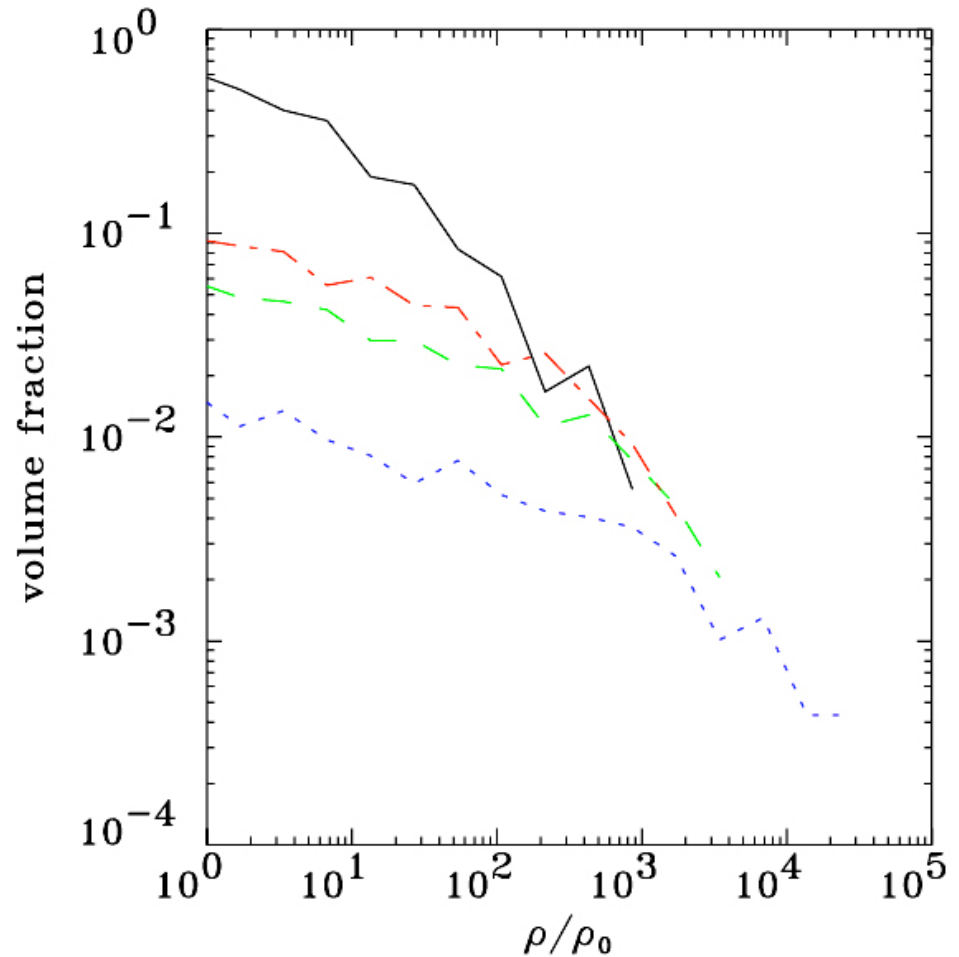
Slope saturates to higher values  
for narrower pdfs  
appropriate for dwarfs  
Tassis et al. (2008)  
Wada & Norman (2007)



Slope saturates close to 1.5  
for wide pdfs  
Not sensitive to  $\rho_{\text{den}}$  def.

# Implications for the pdf

- PDF not universal in the galaxy  
Higher average surface density  $\Rightarrow$  Wider pdf



# Conclusions

Multifractal Topology of ISM  
(observationally & theoretically motivated)

+

SF timescale roughly constant at high densities  
(observationally & theoretically motivated)

Can naturally explain the SF law with its  
complications

