
Modeling jet and outflow feedback
in star cluster formation:
Impact on the SFR and IMF

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Australian Government
Australian Research Council

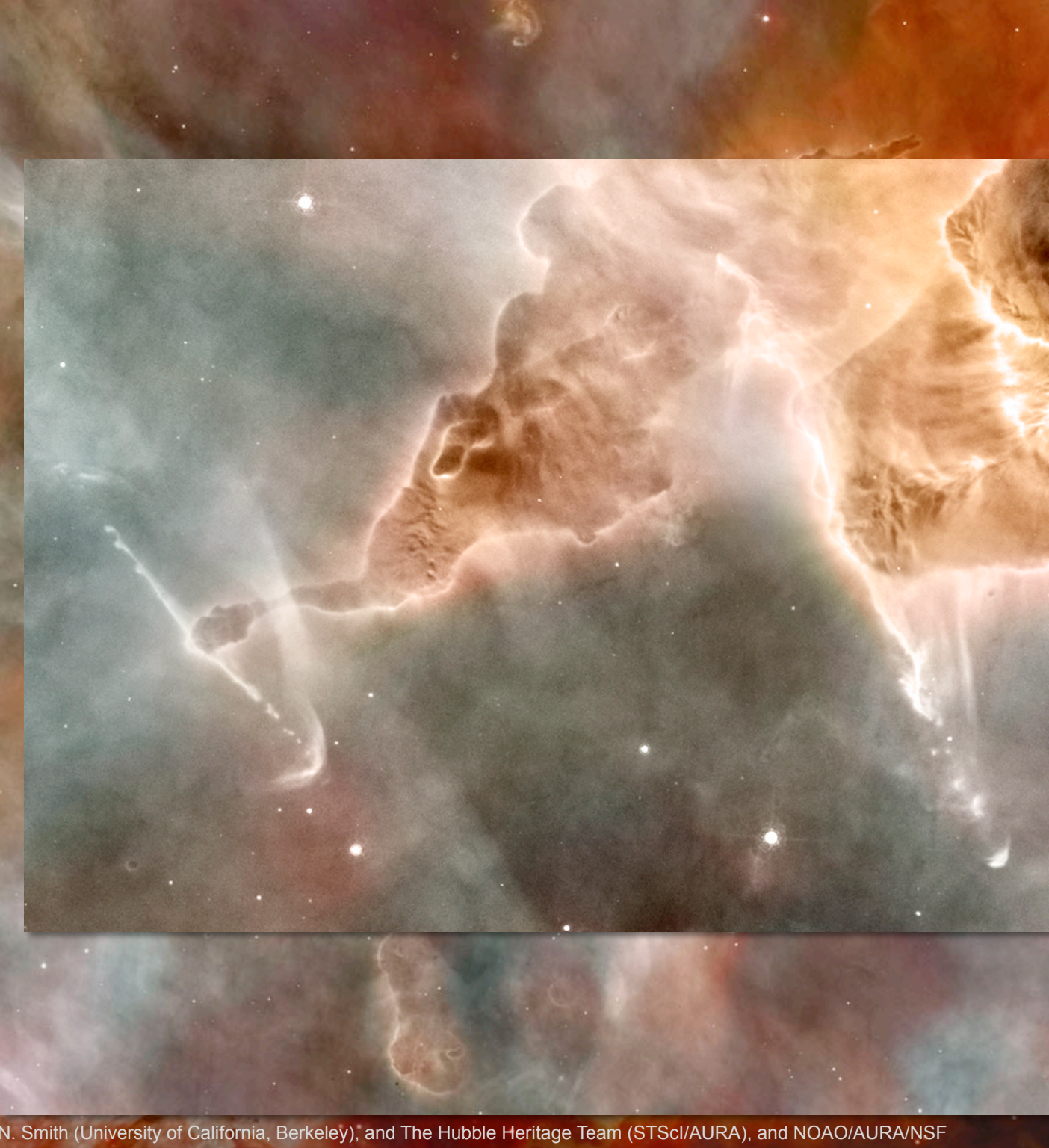
Modeling jet and outflow feedback

Turbulence \rightarrow Density PDF

Density PDF \rightarrow Star Formation Rate



Federrath – KITP – 29.04.2014

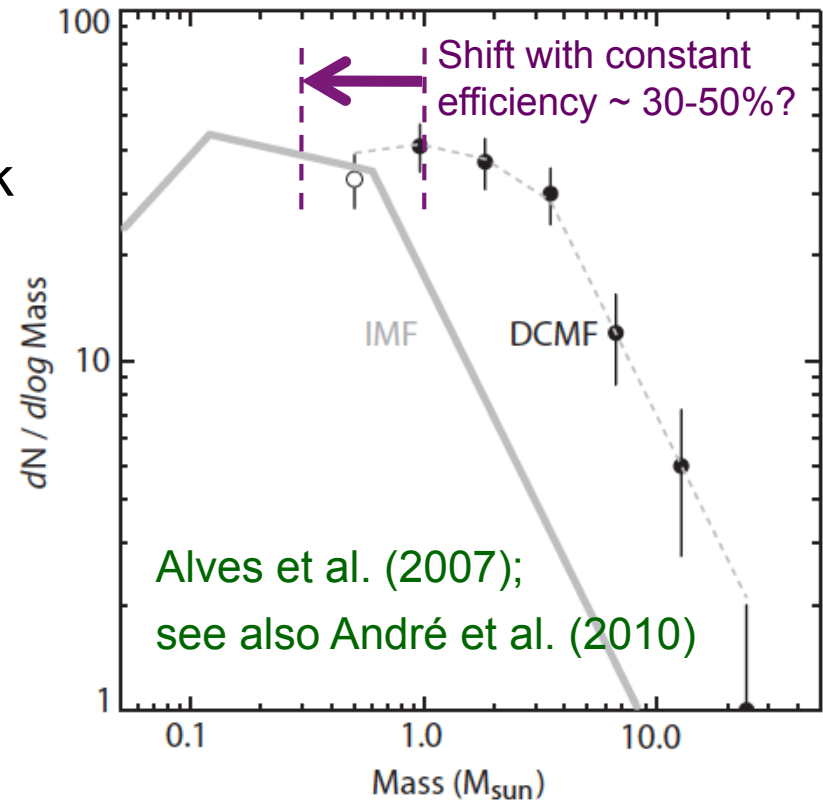


Carina Nebula, NASA, ESA, N. Smith (University of California, Berkeley), and The Hubble Heritage Team (STScI/AURA), and NOAO/AURA/NSF

Star Formation – Outflows/Jets

Outflows/Jets

- ◆ Energy comparable to other feedback
(Mac Low & Klessen 2004; Nakamura & Li 2014;
Krumholz et al. 2014)
- ◆ Driven by magnetic field

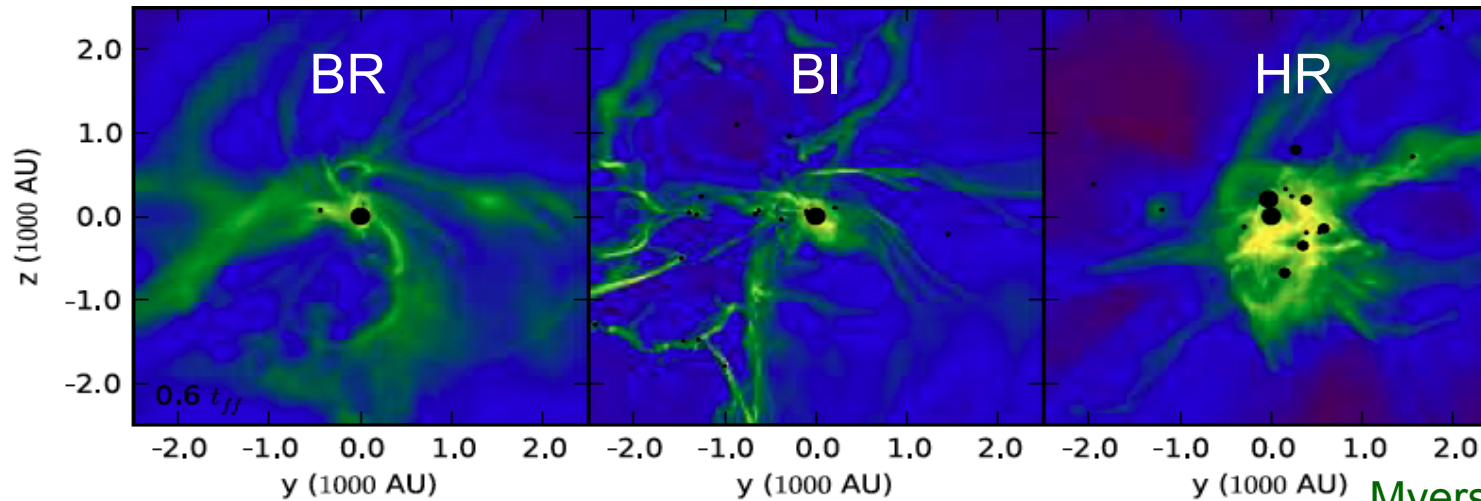


Impact on SFR and IMF:
core-to-star efficiency $\epsilon \sim 0.3-0.5$

(see also Matzner & McKee 2002)

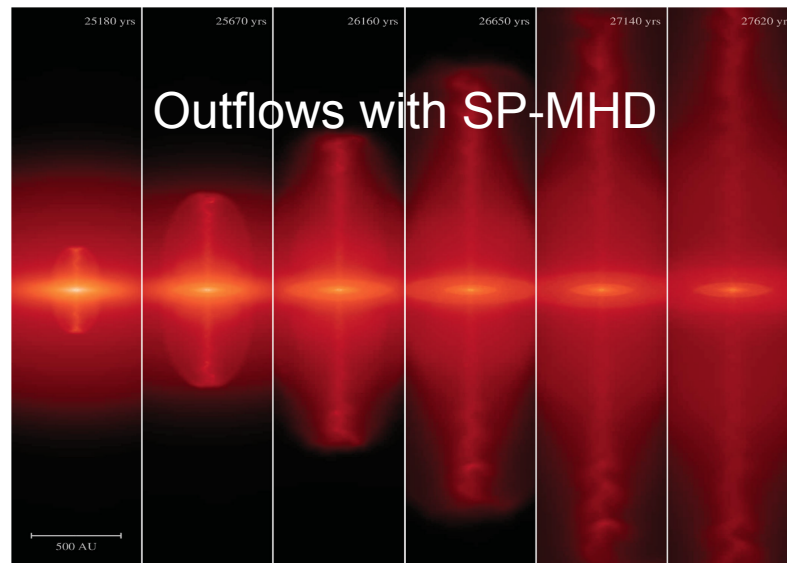
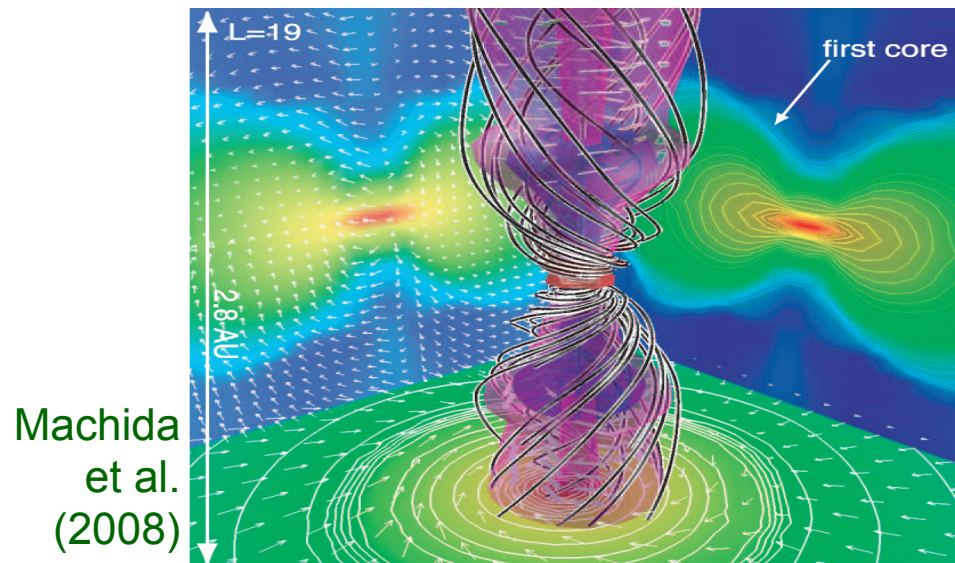
Star Formation – Magnetic Fields

Reduce fragmentation (Hennebelle & Teyssier 08, Bürzle+11, Federrath & Klessen 12)



Myers et al. (2013)

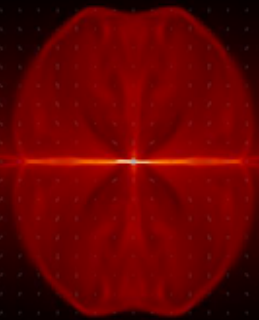
Drive jets / outflows (Banerjee & Pudritz 2006, Seifried et al. 2012, Moraghan et al. 2013)



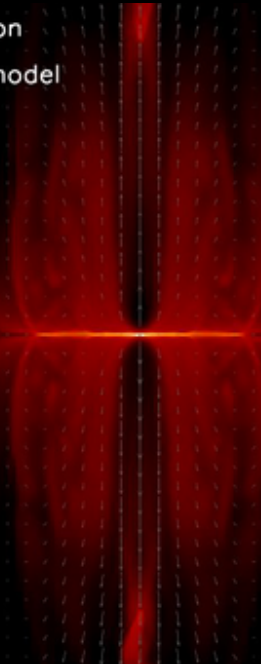
Price et al. (2012)

Modeling jets/outflows

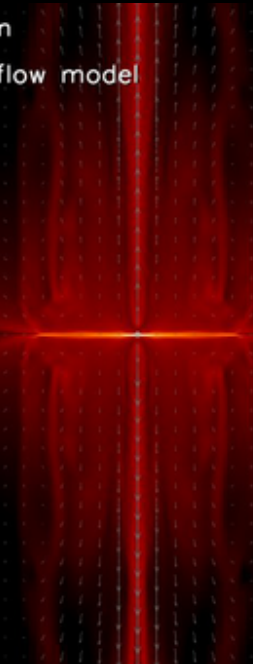
Low resolution
No subgrid model



High resolution
No subgrid model

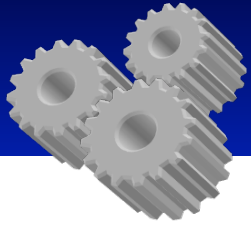


Low resolution
With SGS outflow model



Federrath et al. (2014)

Movies available: http://www.ita.uni-heidelberg.de/~chfeder/pubs/outflow_model/outflow_models.shtml



Sink particles

- Quantify fragmentation and accretion
- Prevent code from stalling

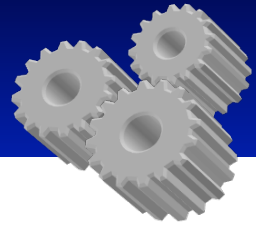
$$t_{\text{ff}} = \left(\frac{3\pi}{32G\rho} \right)^{1/2}$$

- Resolve Jeans length

$$\lambda_{\text{J}} = \left(\frac{\pi c_s^2}{G\rho} \right)^{1/2} \rightarrow \rho_{\text{res}} \quad (\text{resolution criterion})$$

Truelove et al. (1997)

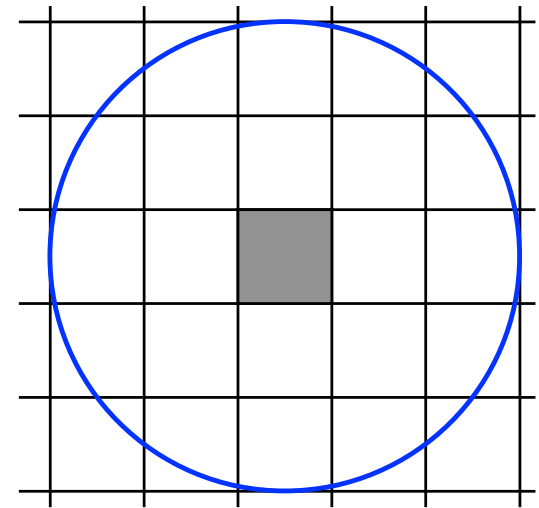
(see also Bate & Burkert 1997)



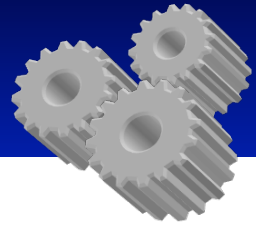
Sink particle implementation in FLASH

Collapse checks to avoid spurious sink creation

1. Cell exceeds density threshold, $\rho > \rho_{\text{res}}$



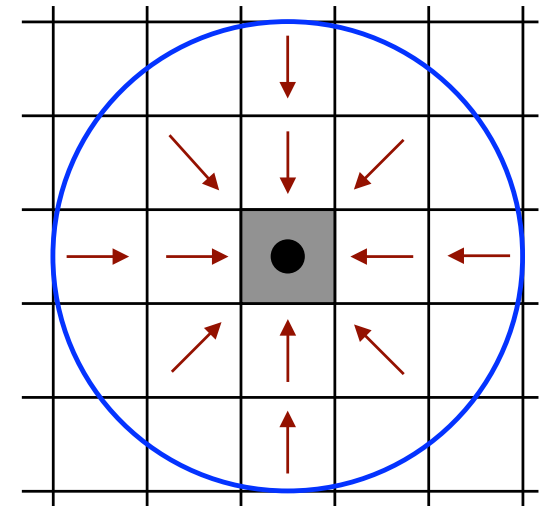
Federrath, Banerjee, Clark, Klessen (2010, ApJ 713, 269)



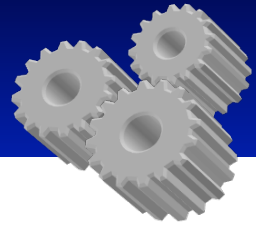
Sink particle implementation in FLASH

Collapse checks to avoid spurious sink creation

1. Cell exceeds density threshold, $\rho > \rho_{\text{res}}$
2. Highest level of AMR
3. Converging towards the center
4. Central minimum in gravitational potential
5. Jeans unstable, $|E_{\text{grav}}| > 2E_{\text{th}}$
6. Bound, $E_{\text{grav}} + E_{\text{th}} + E_{\text{kin}} + E_{\text{mag}} < 0$
7. Not within the accretion radius of an existing sink particle

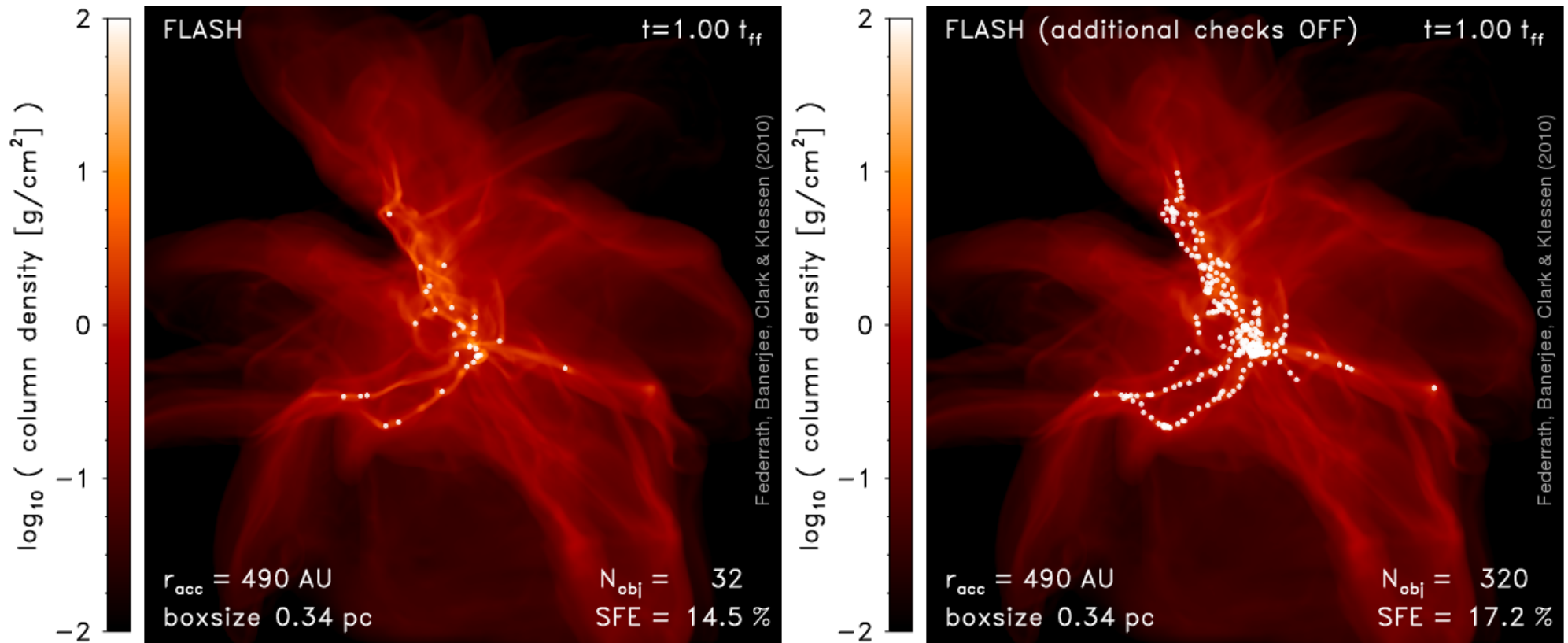


Federrath, Banerjee, Clark, Klessen (2010, ApJ 713, 269)



Sink particle implementation in FLASH

Movies available: <http://www.ita.uni-heidelberg.de/~chfeder/pubs/sinks/sinks.shtml>

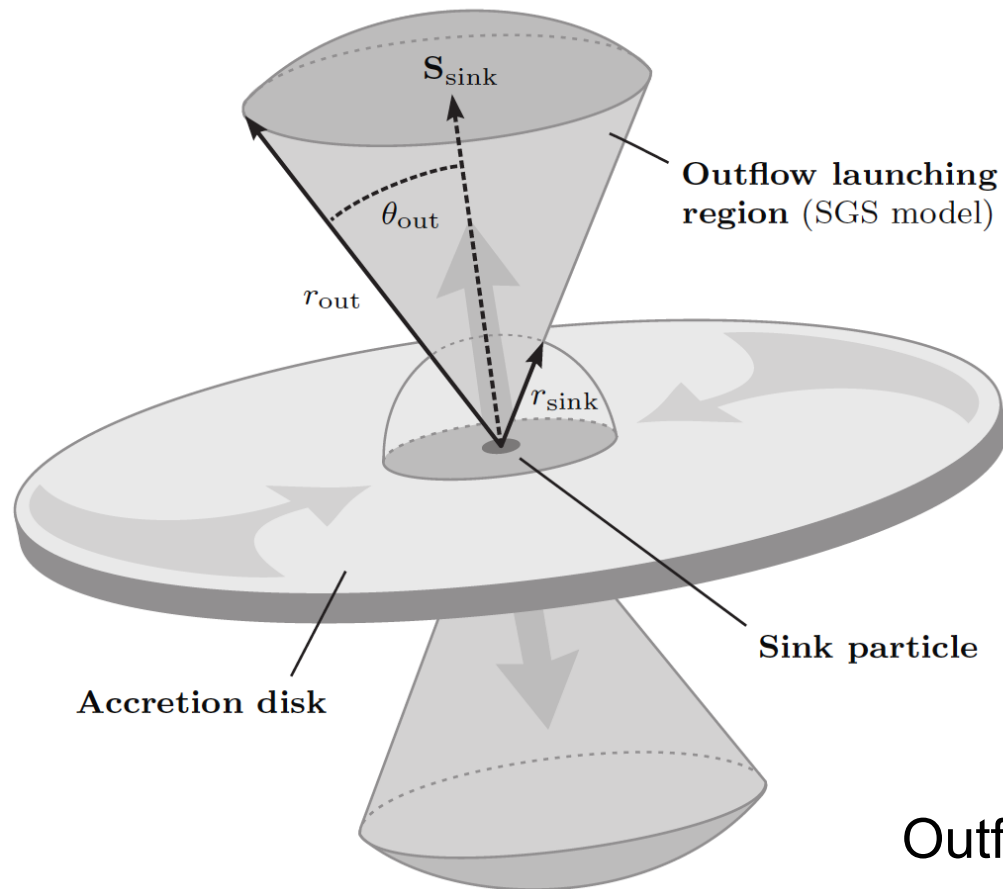


all checks ON

$\rho > \rho_{res}$ **only**

Federrath, Banerjee, Clark, Klessen (2010, ApJ 713, 269)

A subgrid model for jets/outflows



List of SGS outflow parameters.

SGS Parameter	Symbol	Default	Reference
Outflow Opening Angle	θ_{out}	30°	[1]
Mass Transfer Fraction	f_m	0.3	[2]
Jet Speed Normalization ^a	$ \mathbf{V}_{\text{out}} $	100 km s^{-1}	[3]
Angular Momentum Fraction	f_a	0.9	[4]
Outflow Radius	r_{out}	$16 \Delta x$	Section 4

Notes. ^a The outflow velocities are dynamically computed according to the Kepler speed at the footpoint of the jet, $|\mathbf{V}_{\text{out}}| = 100 \text{ km s}^{-1} (M_{\text{sink}}/0.5 M_\odot)^{1/2}$ (see Equation 13). References: [1] Blandford & Payne (1982); Appenzeller & Mundt (1989); Camenzind (1990); [2] Hartmann & Calvet (1995); Calvet (1998); Tomisaka (1998); Bacciotti et al. (2002); Tomisaka (2002); Lee et al. (2006); Cabrit et al. (2007); Lee et al. (2007); Hennebelle & Fromang (2008); Duffin & Pudritz (2009); Bacciotti et al. (2011); Price et al. (2012); Seifried et al. (2012); [3] Herbig (1962); Snell et al. (1980); Blandford & Payne (1982); Draine (1983); Uchida & Shibata (1985); Shibata & Uchida (1985, 1986); Pudritz & Norman (1986); Wardle & Königl (1993); Bacciotti et al. (2000); Königl & Pudritz (2000); Bacciotti et al. (2002); Banerjee & Pudritz (2006); Machida et al. (2008); [4] Pelletier & Pudritz (1992); Bacciotti et al. (2002); Banerjee & Pudritz (2006); Hennebelle & Fromang (2008).

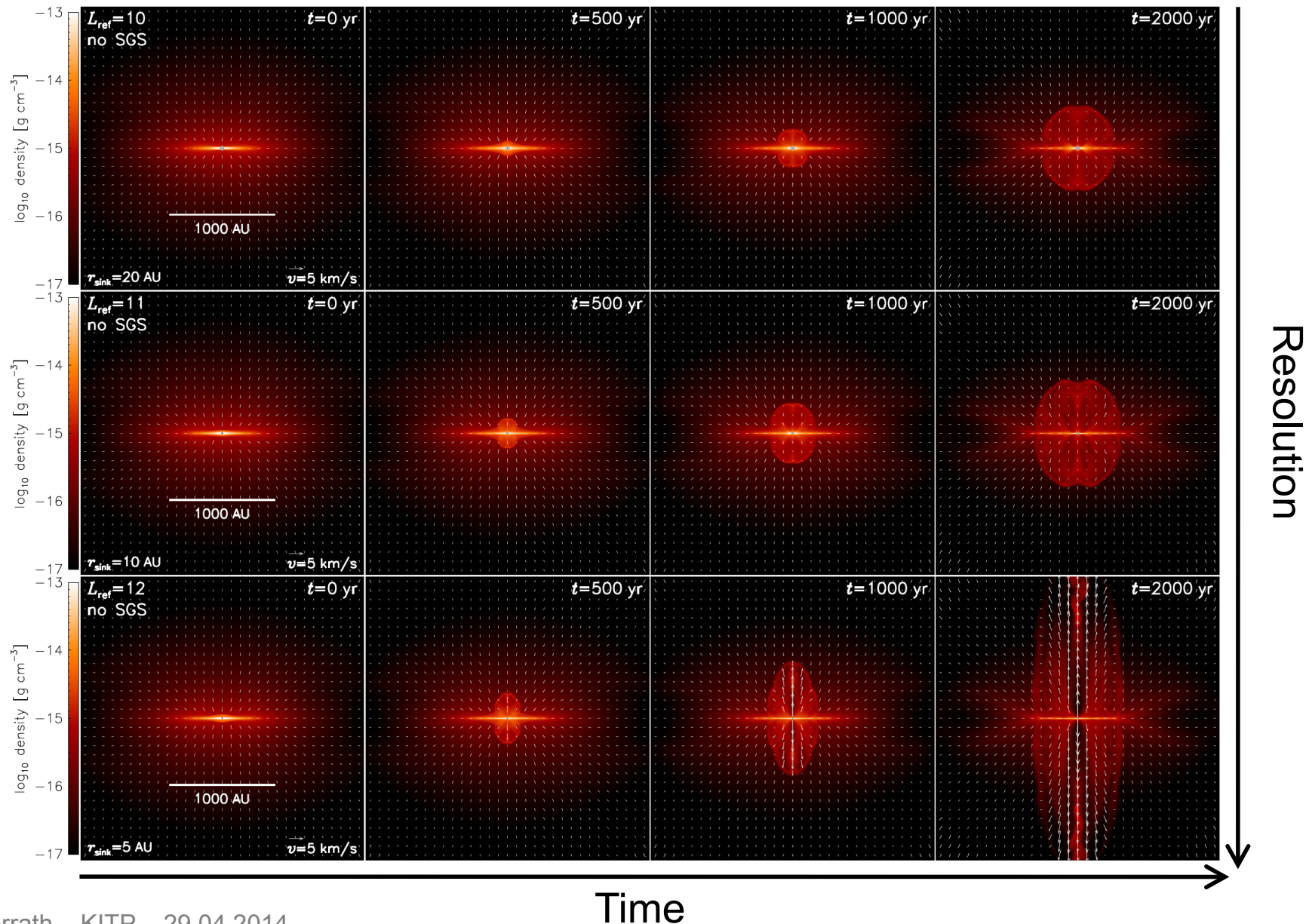
$$\text{Outflow mass: } M_{\text{out}} = f_m \dot{M}_{\text{acc}} \Delta t$$

$$\text{Outflow velocity: } |\mathbf{V}_{\text{out}}| = \left(\frac{GM_{\text{sink}}}{10 R_\odot} \right)^{1/2} = 100 \text{ km s}^{-1} \left(\frac{M_{\text{sink}}}{0.5 M_\odot} \right)^{1/2}$$

$$\text{Outflow angular momentum: } \mathbf{L}_{\text{out}} = f_a (\mathbf{S}'_{\text{sink}} - \mathbf{S}_{\text{sink}}) \cdot \mathbf{S}'_{\text{sink}} / |\mathbf{S}'_{\text{sink}}|$$

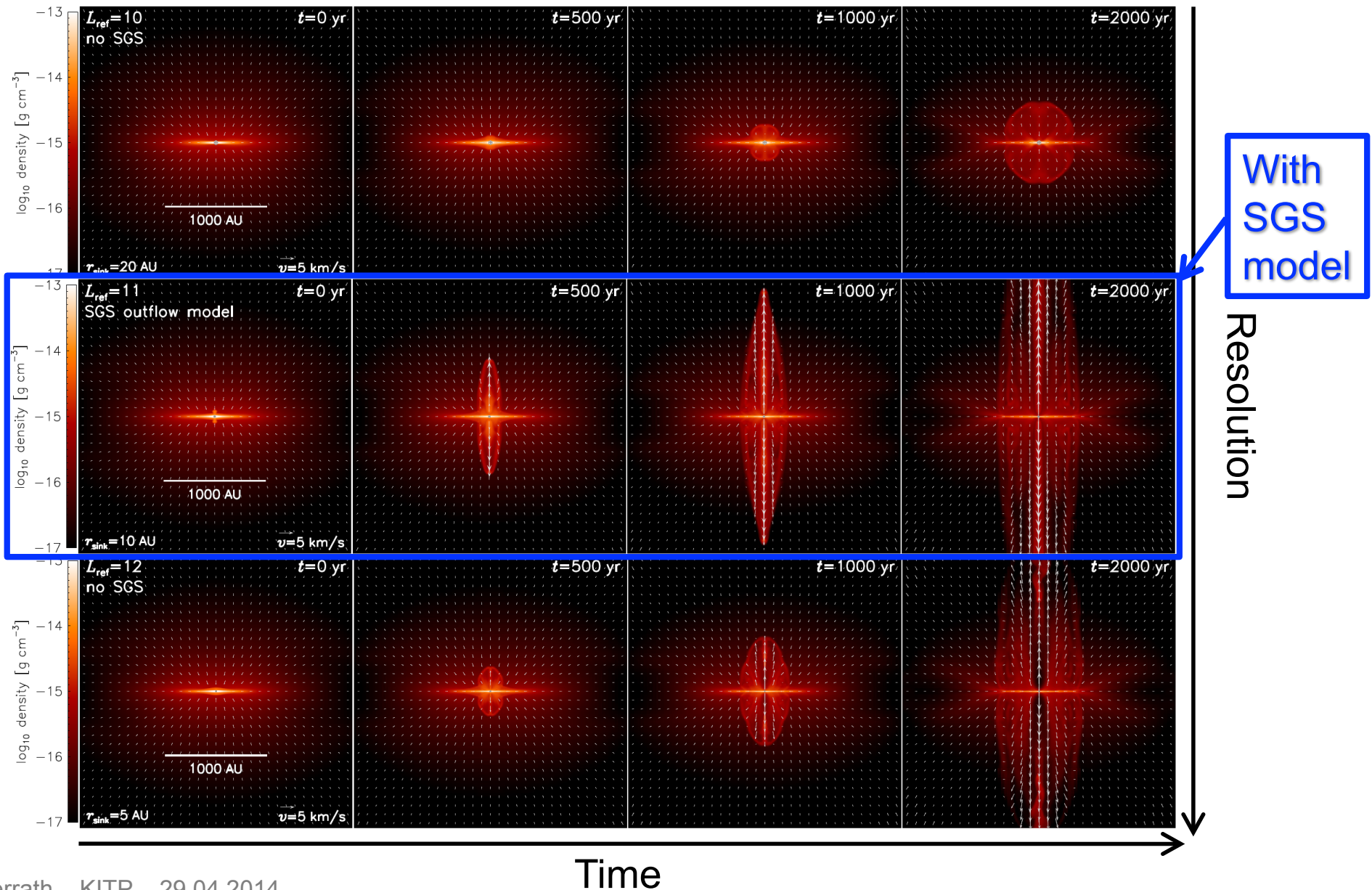
A subgrid model for jets/outflows

Resolution study *without* SGS model:



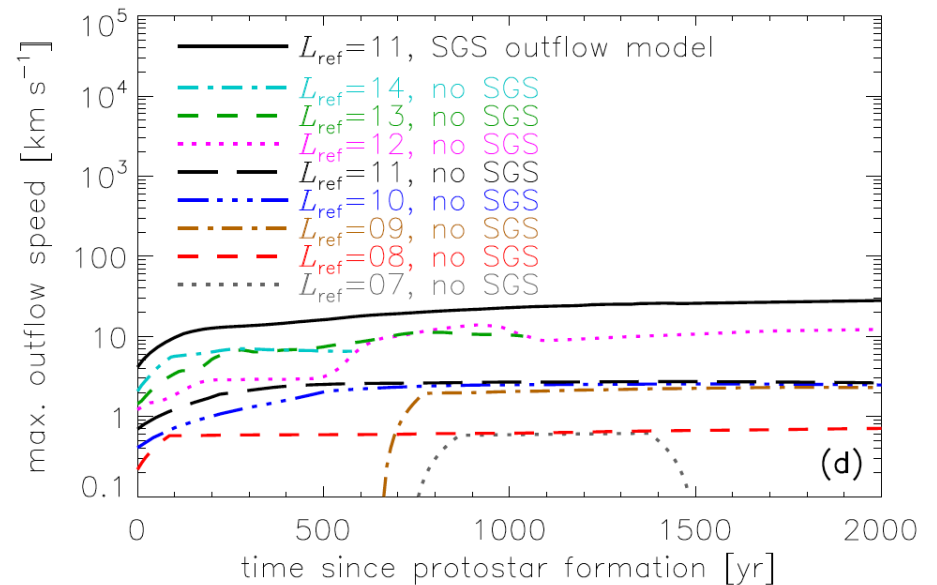
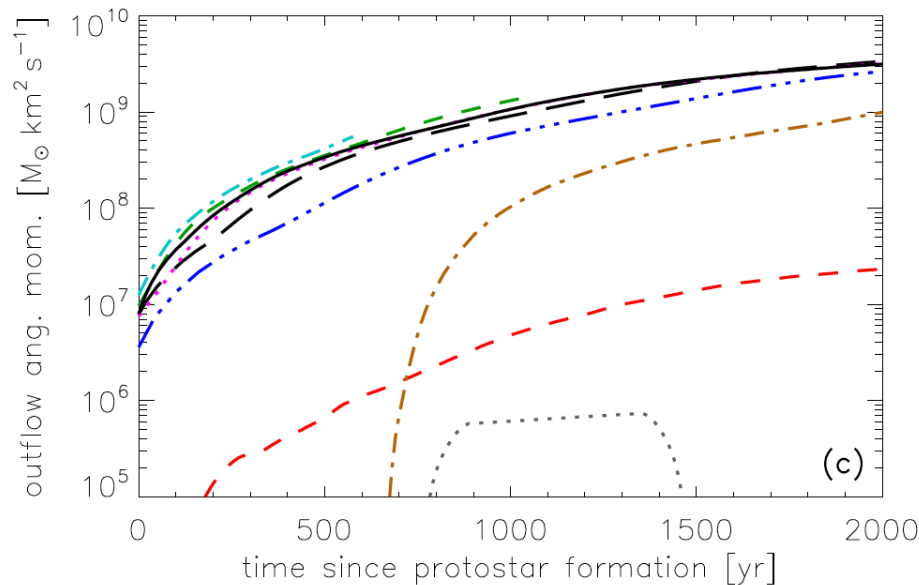
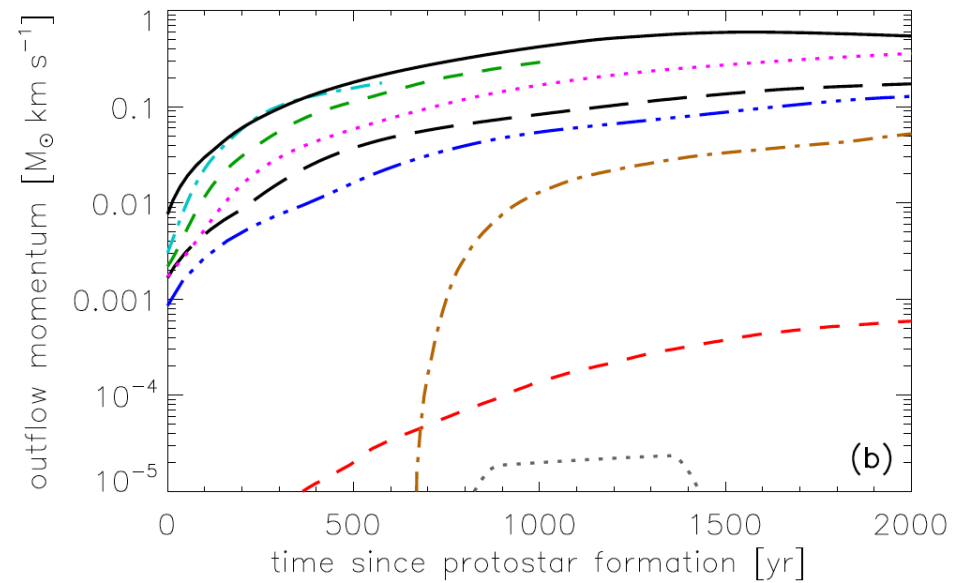
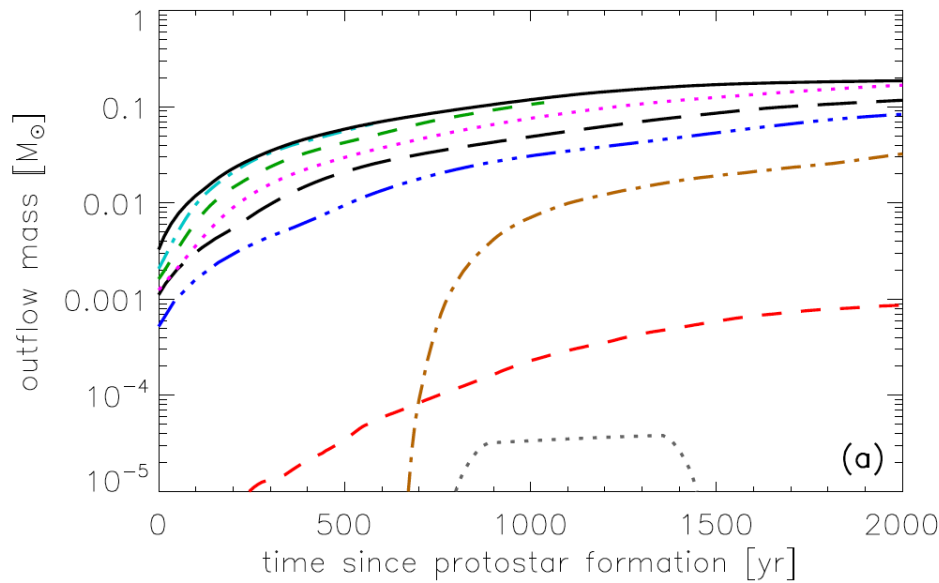
A subgrid model for jets/outflows

Resolution study without SGS model:



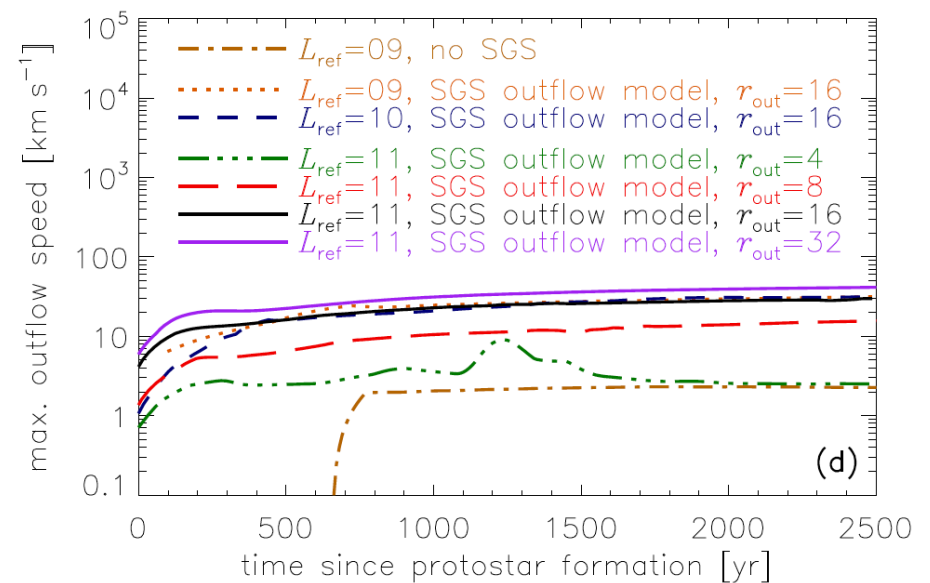
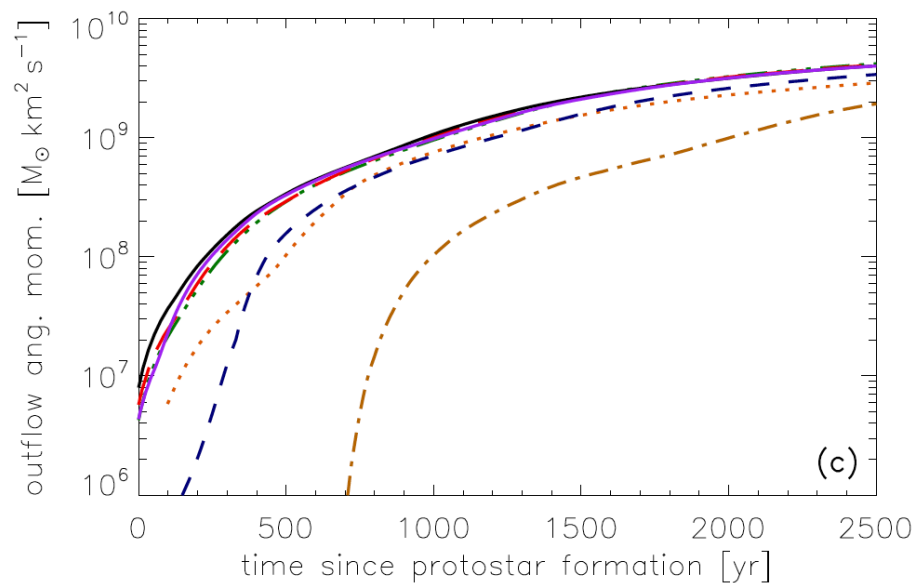
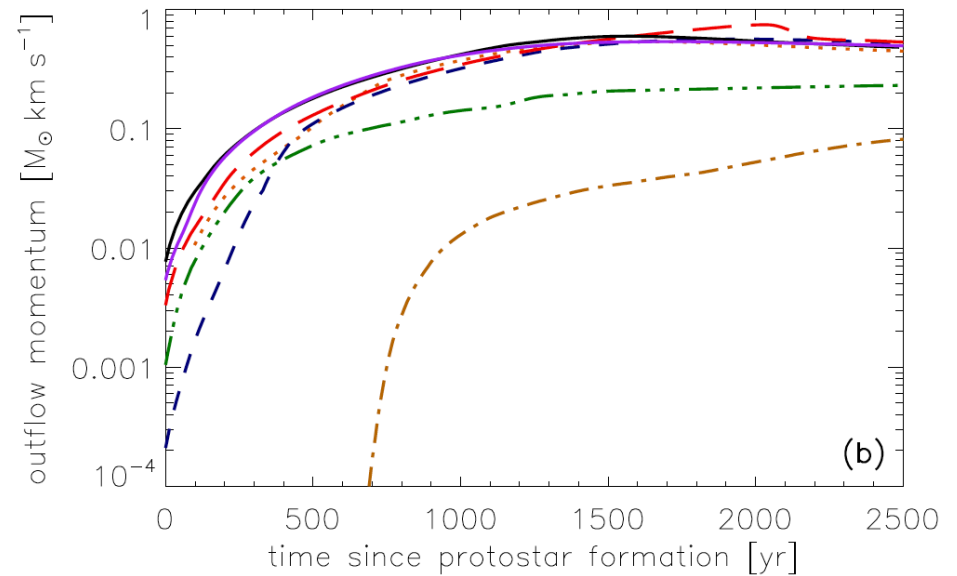
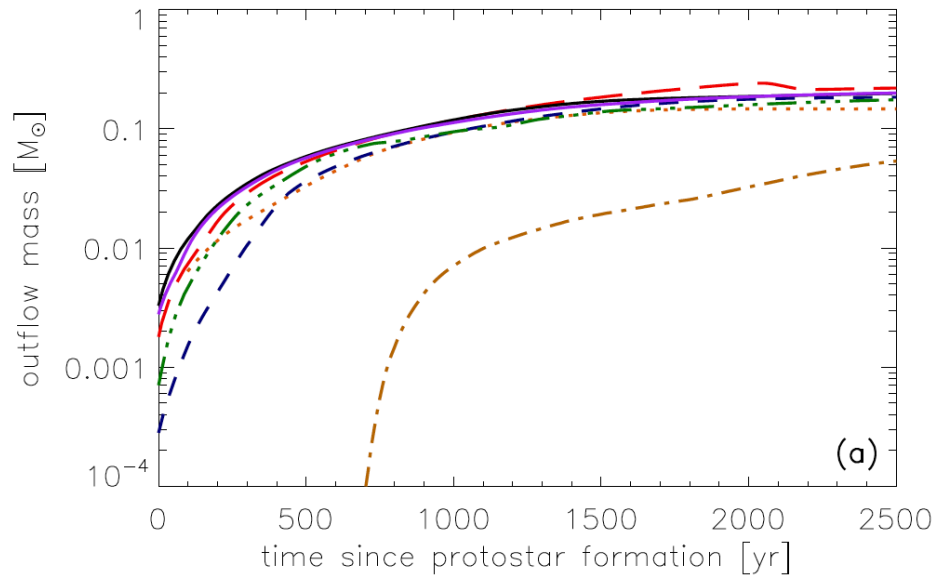
A subgrid model for jets/outflows

SGS model must reproduce small-scale physics:



A subgrid model for jets/outflows

SGS model must converge:



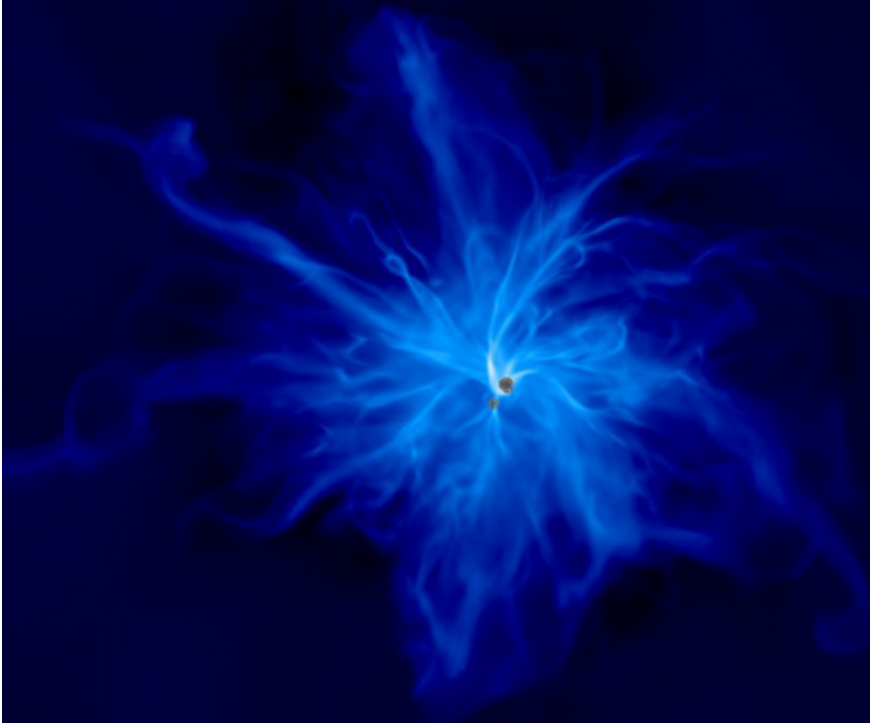
The role of outflow/jet feedback for star cluster formation

Movies available: http://www.ita.uni-heidelberg.de/~chfeder/pubs/outflow_model/outflow_models.shtml

No outflows

With outflows

$t/t_{\text{ff}} = 1.50$



$N_{\text{sink}} = 23$

SFE = 87.6%

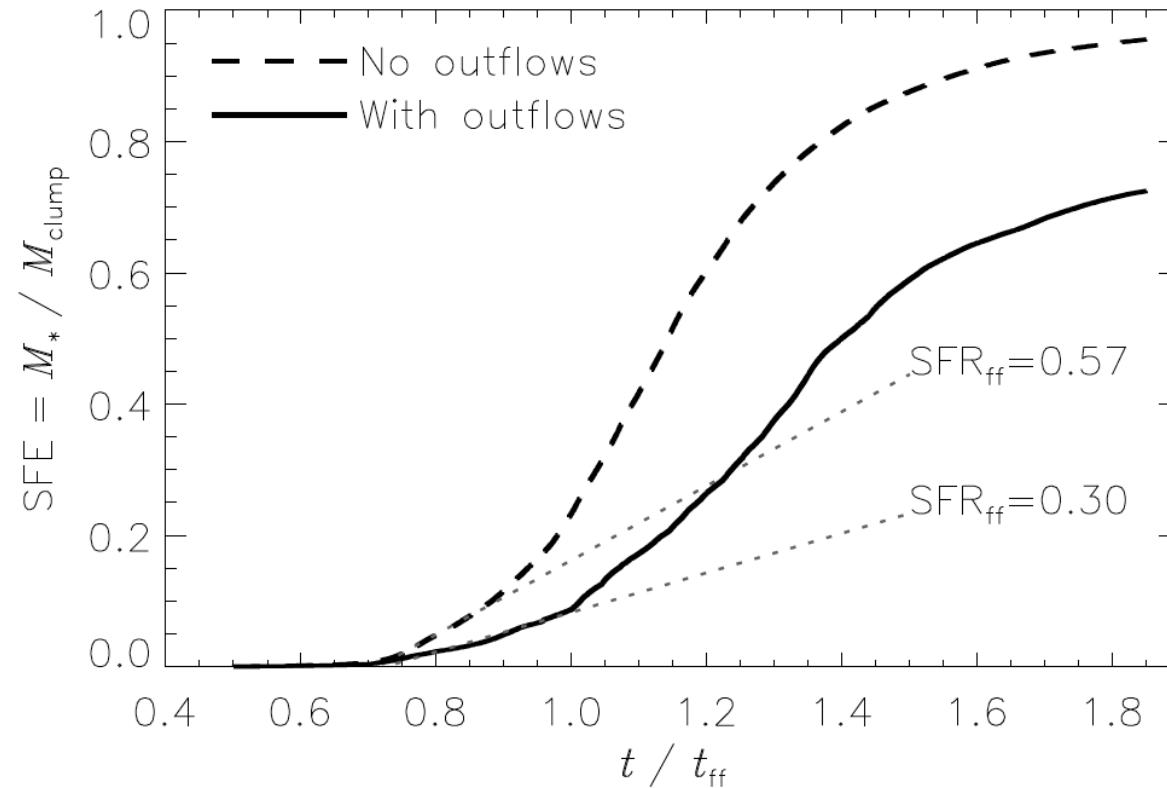
$N_{\text{sink}} = 49$

SFE = 59.0%

SGS off

SGS on

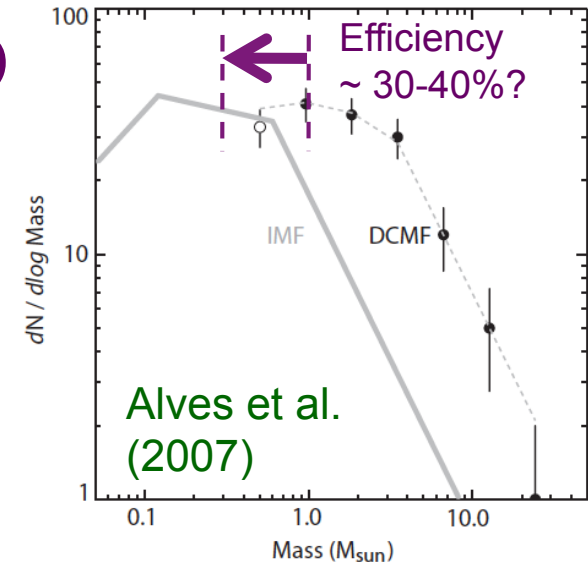
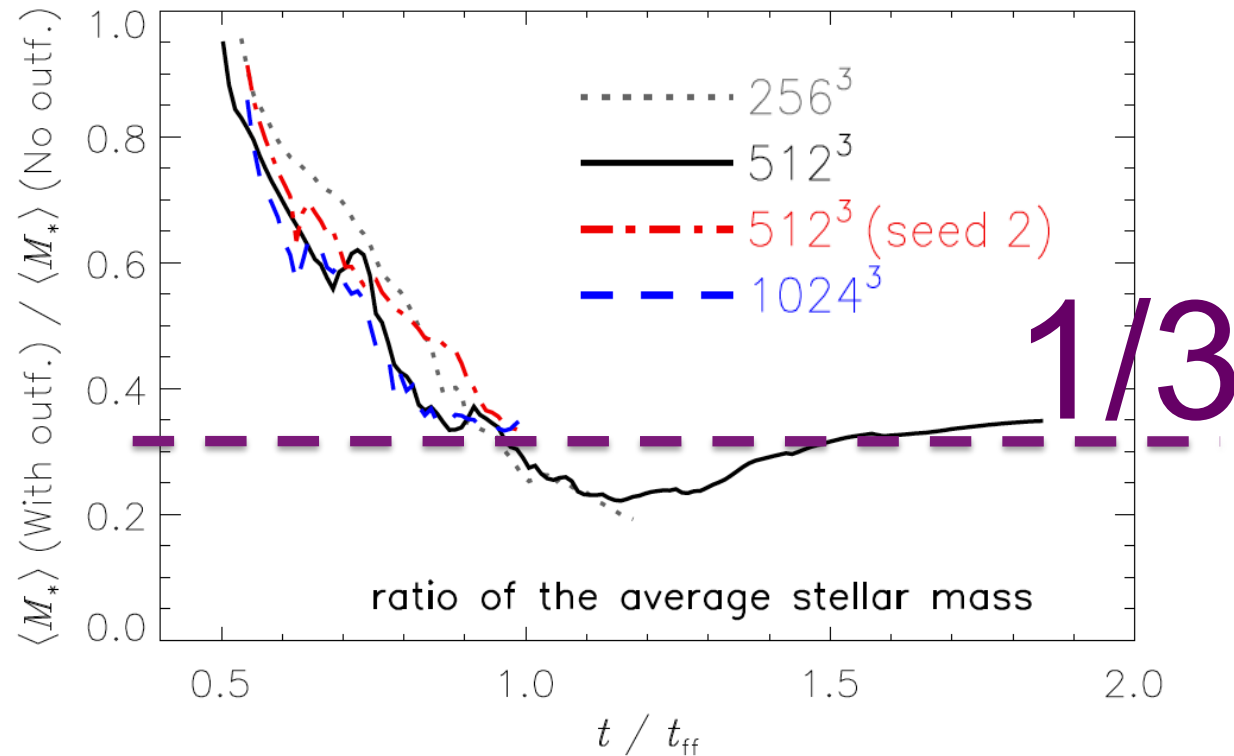
The role of outflow/jet feedback for star cluster formation



RESULTS:

- Outflow/Jet feedback reduces the SFR by factor ~ 2
- Outflow/Jet feedback reduces average star mass by factor ~ 3

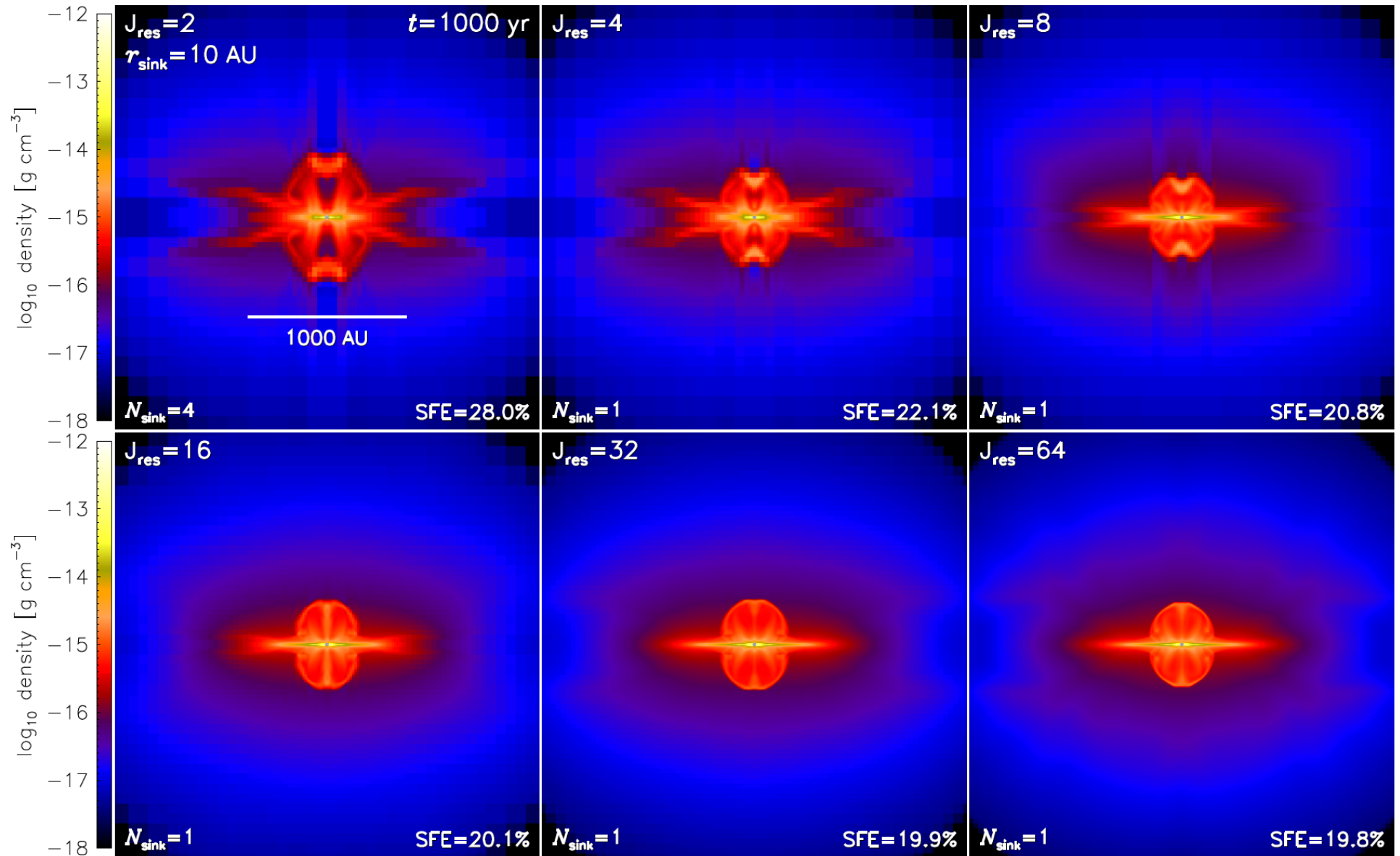
The role of outflow/jet feedback for star cluster formation



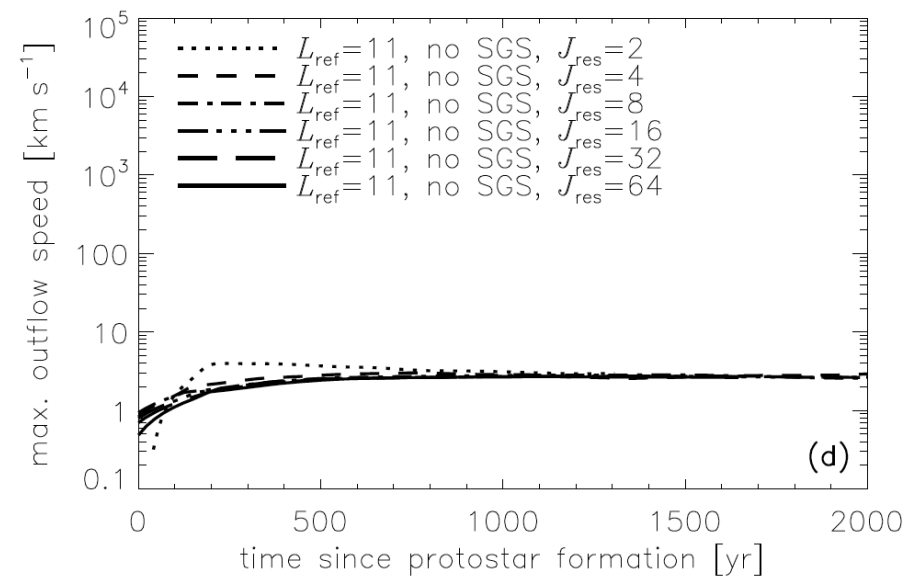
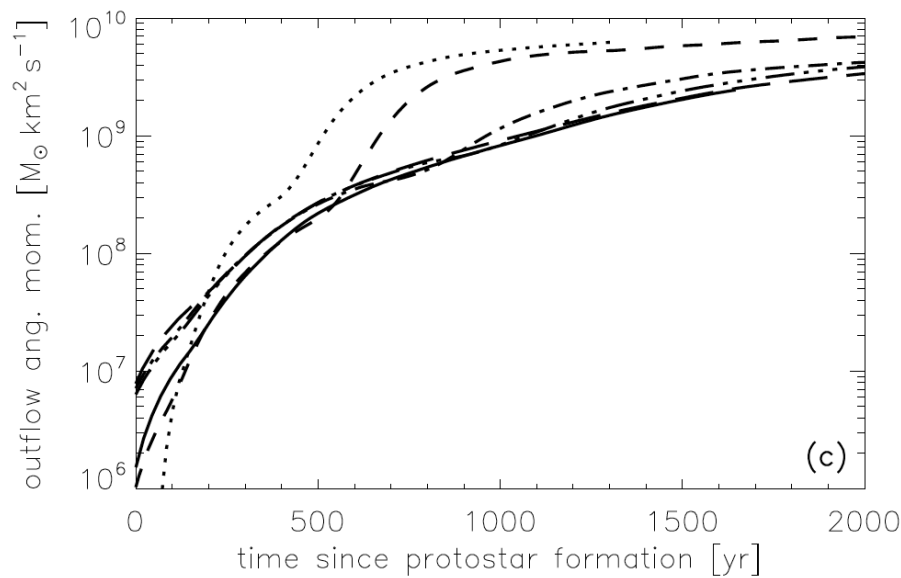
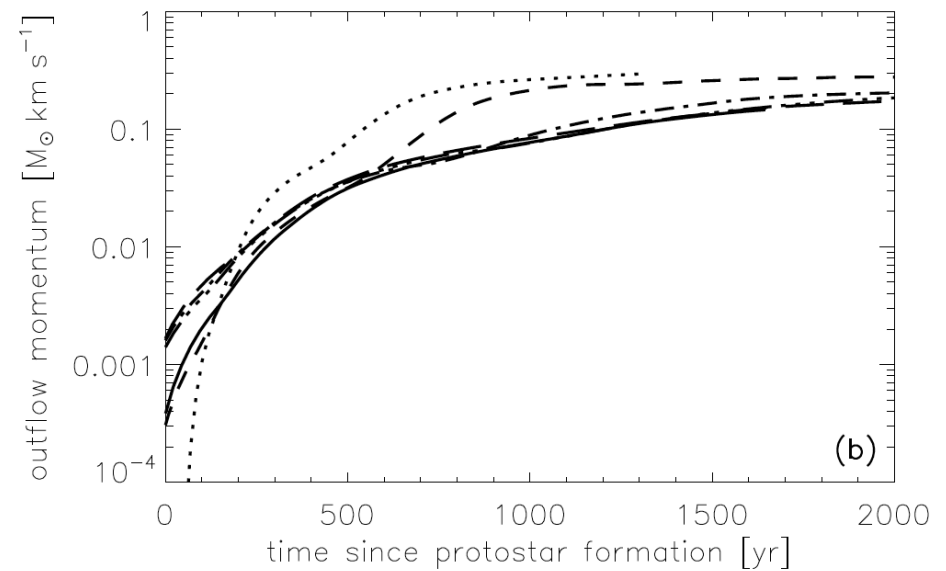
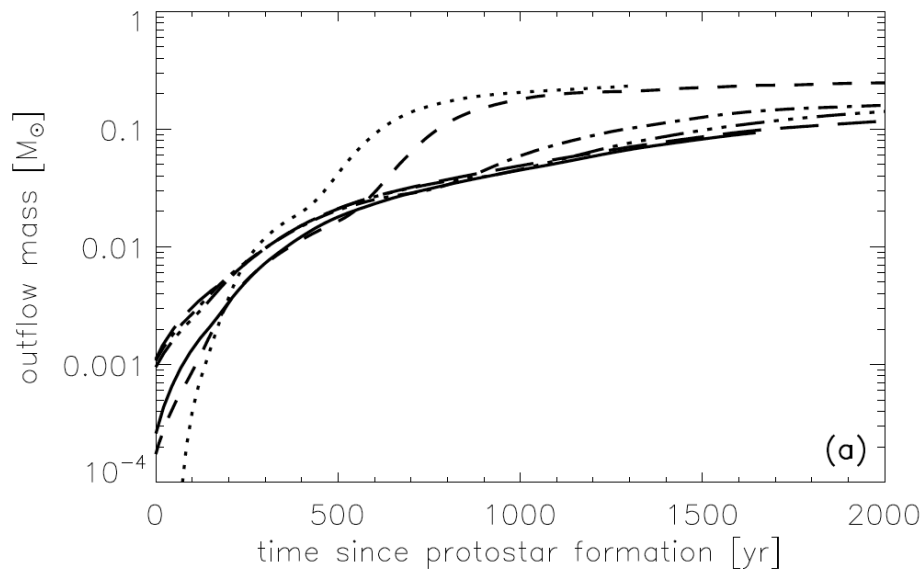
RESULTS:

- Outflow/Jet feedback reduces the SFR by factor ~ 2
- Outflow/Jet feedback reduces average star mass by factor ~ 3

Jeans resolution study



“The answer is 42” – roughly...



→ At least 30 grid cells per Jeans length required (see also Federrath et al. 2011, ApJ)

Modeling jet and outflow feedback

Turbulence → Density PDF

Density PDF → Star Formation Rate



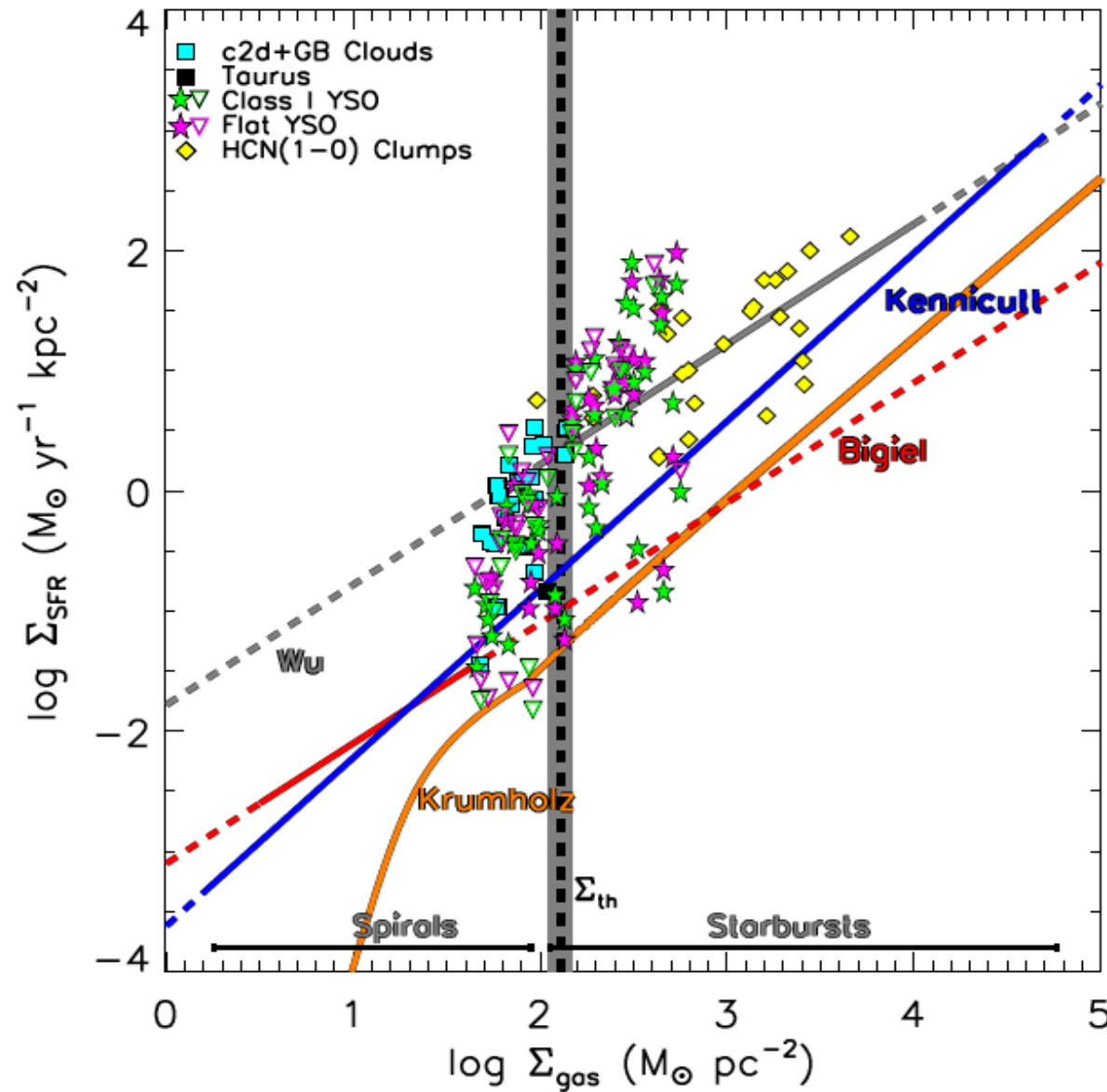
S. Guisard ESO

Pipe Nebula

Rho Ophiuchi Cloud

$$\mathbf{SFR}_{\text{Oph}} = 15 \times \mathbf{SFR}_{\text{Pipe}}$$

Universal star formation “law”?



- Relation?
- Offset?
- Scatter?



Observational scatter
and physical variations:

Turbulence

Milky Way clouds (Heiderman et al. 2010; Lada et al. 2010, Gutermuth et al. 2011)

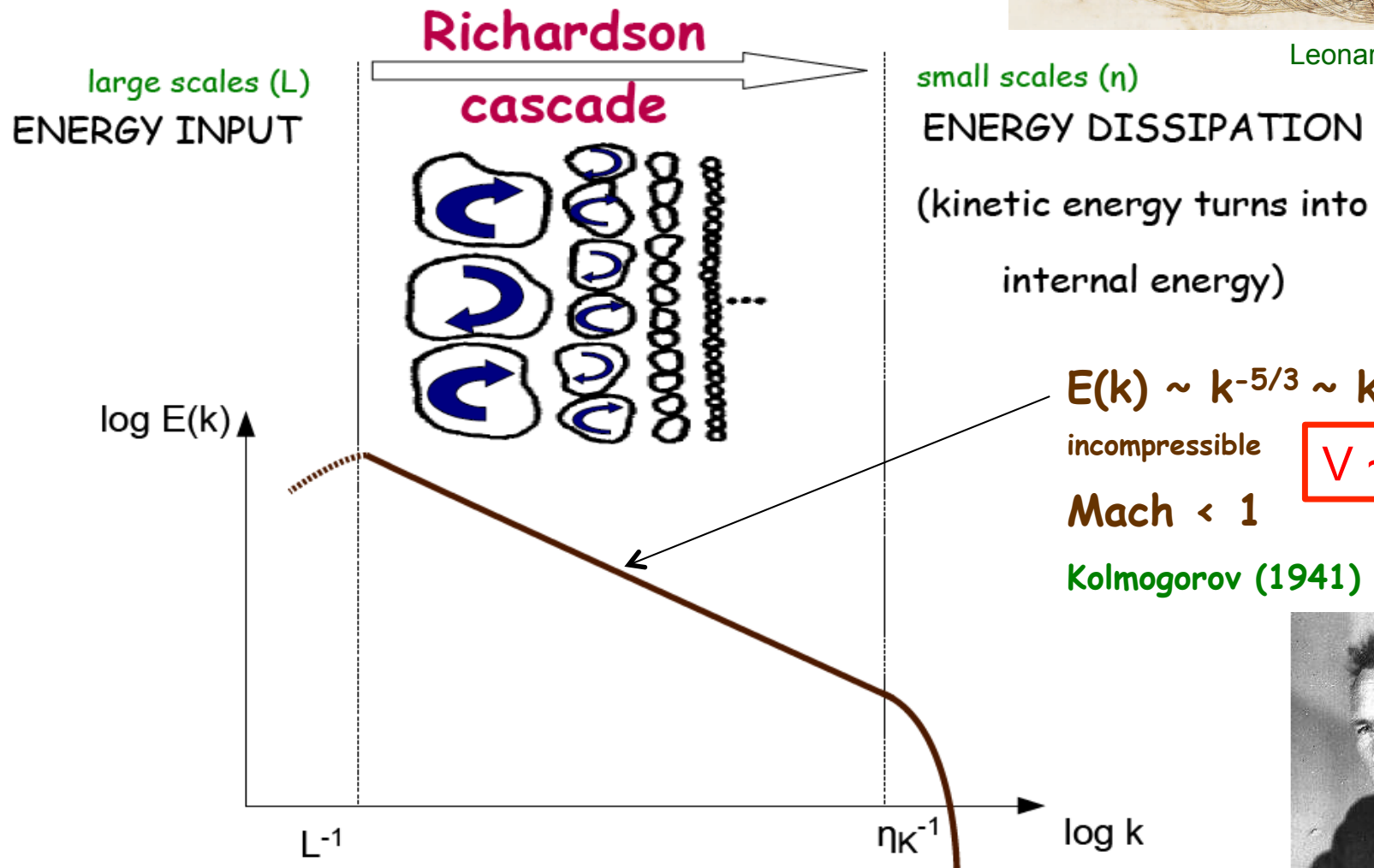
Turbulence

- Reynolds numbers > 1000
- Kinetic energy cascade



Leonardo da Vinci's illustration of the swirling flow of turbulence. (The Royal Collection © 2004. Her Majesty Queen Elizabeth II)

Leonardo da Vinci

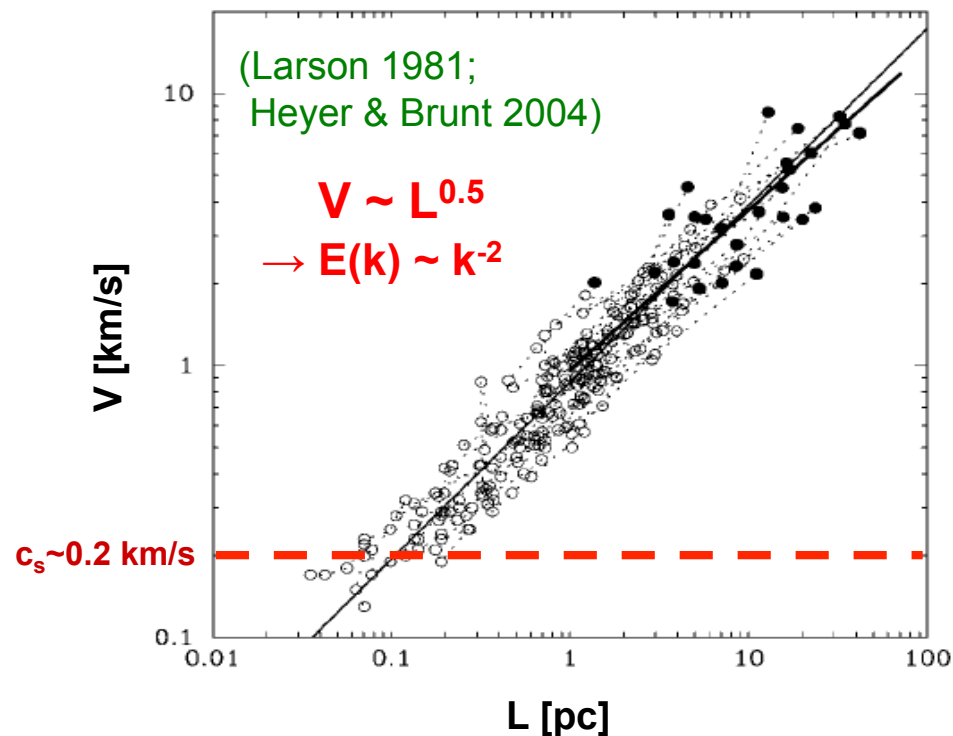


Interstellar Turbulence – scaling

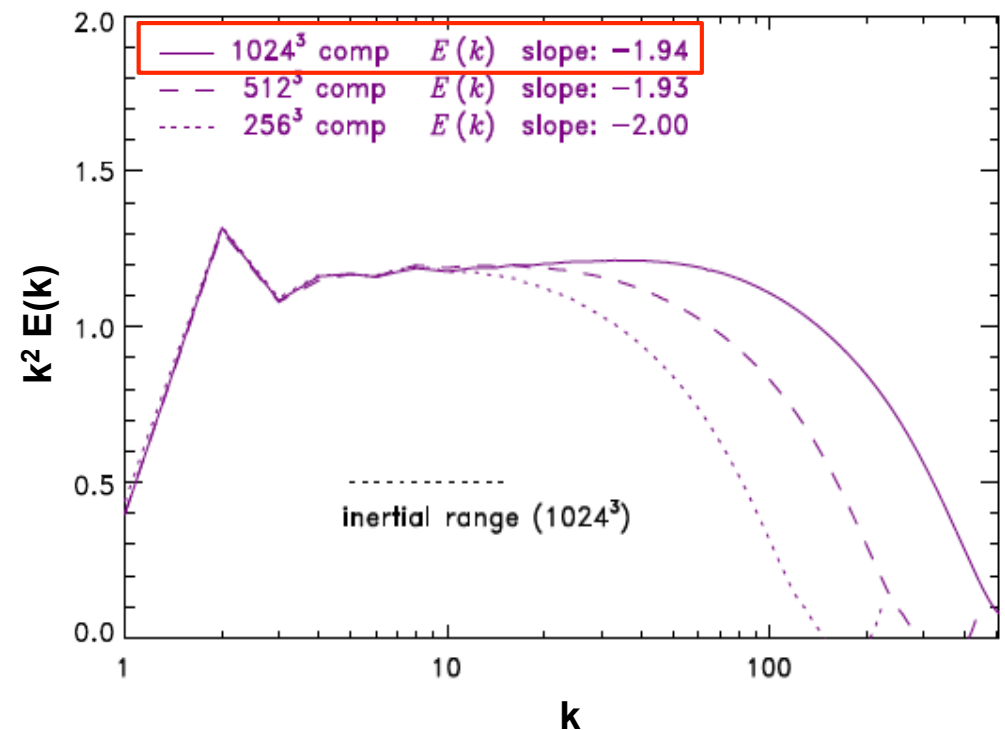
BUT: Larson (1981) relation: $E(k) \sim k^{-1.8-2.0}$

(see also Heyer & Brunt 2004; Roman-Duval et al. 2011)

Observation



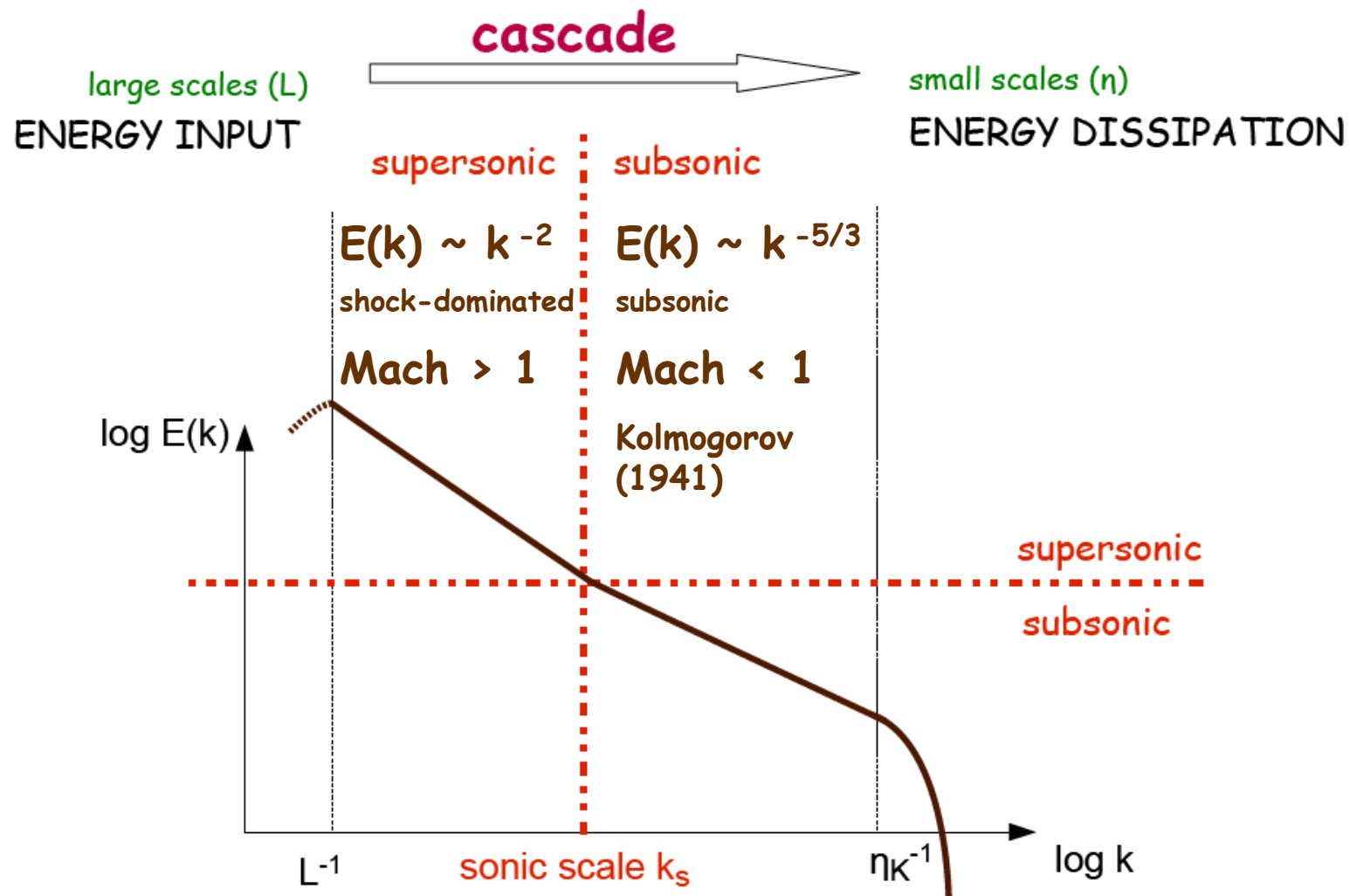
Simulation



Supersonic, compressible turbulence has steeper $E(k) \sim k^{-1.9}$ than Kolmogorov ($E \sim k^{-5/3}$)

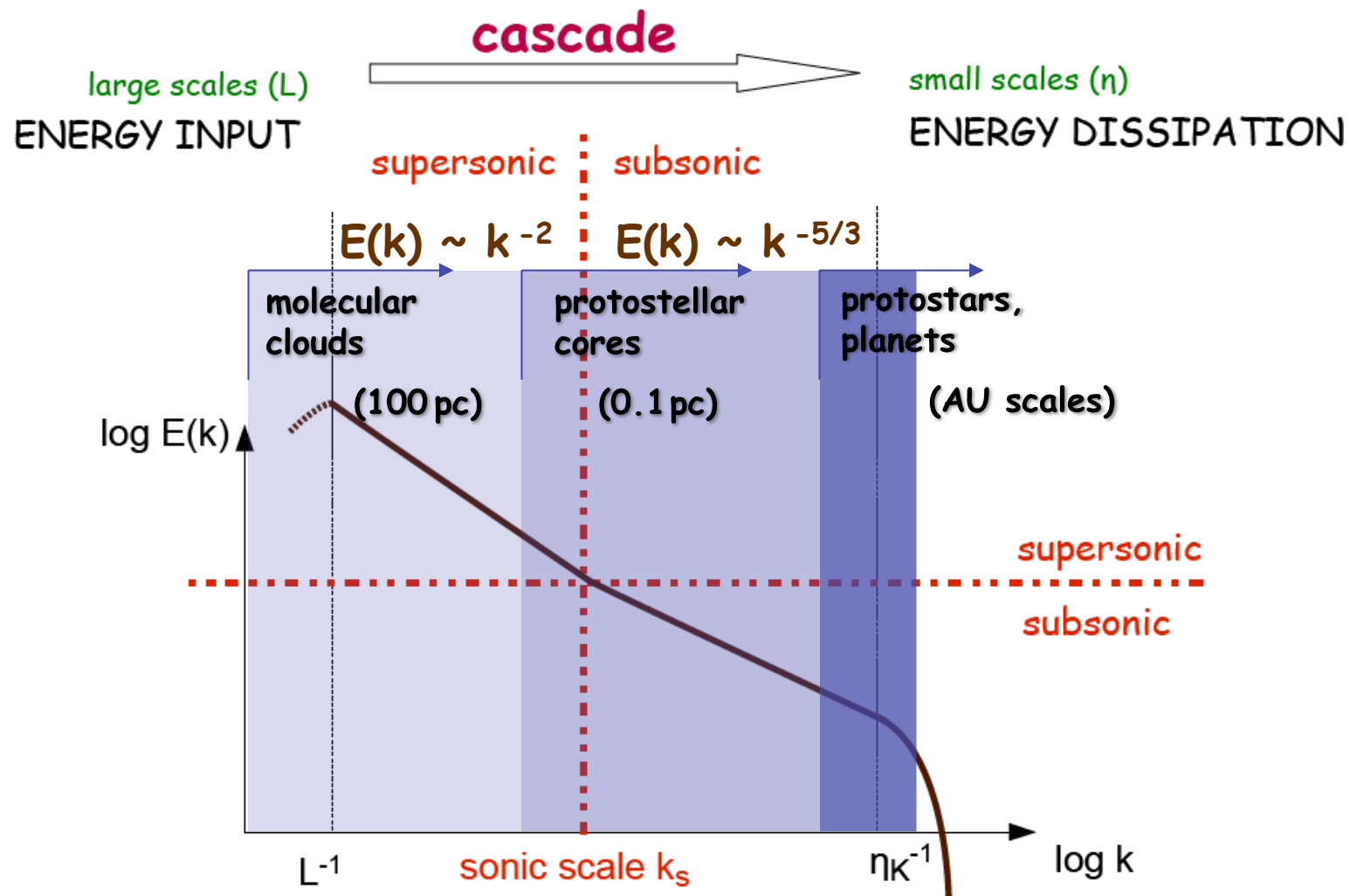
Interstellar Turbulence

- Reynolds numbers > 1000
- Kinetic energy cascade



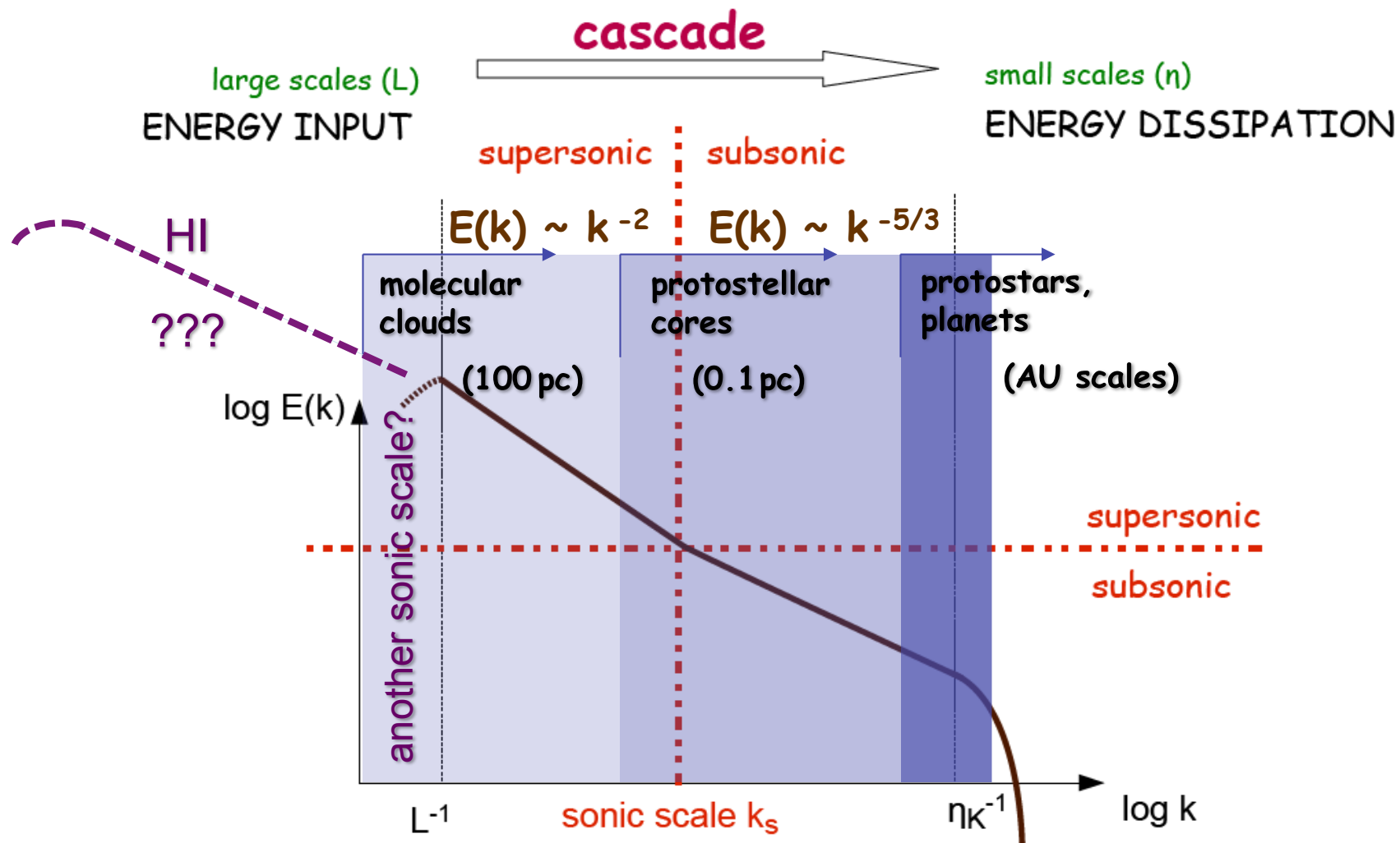
Interstellar Turbulence

- Reynolds numbers > 1000
- Kinetic energy cascade



Interstellar Turbulence

- Reynolds numbers > 1000
- Kinetic energy cascade





Turbulence driven by

- Ionization fronts, bubbles?
- Protostellar jets/winds?
- Supernova explosions?
- MRI / shear?
- Gravitational infall?
- Galactic spiral shock?

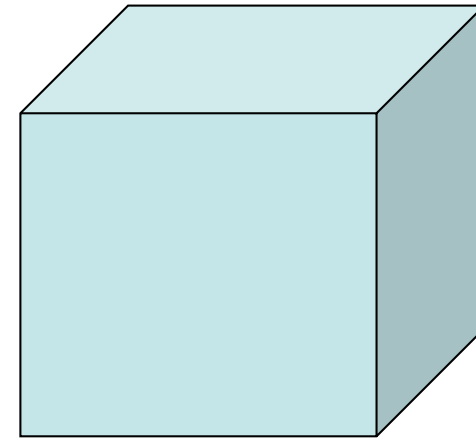
Mac Low & Klessen (2004)

Significant compressive forcing component

Turbulence driving – solenoidal versus compressive

“Turbulence in a box”

- 3D, periodic boundaries
- Driven to supersonic speeds (Mach 2 - 50)
- Large-scale **Forcing Term f**

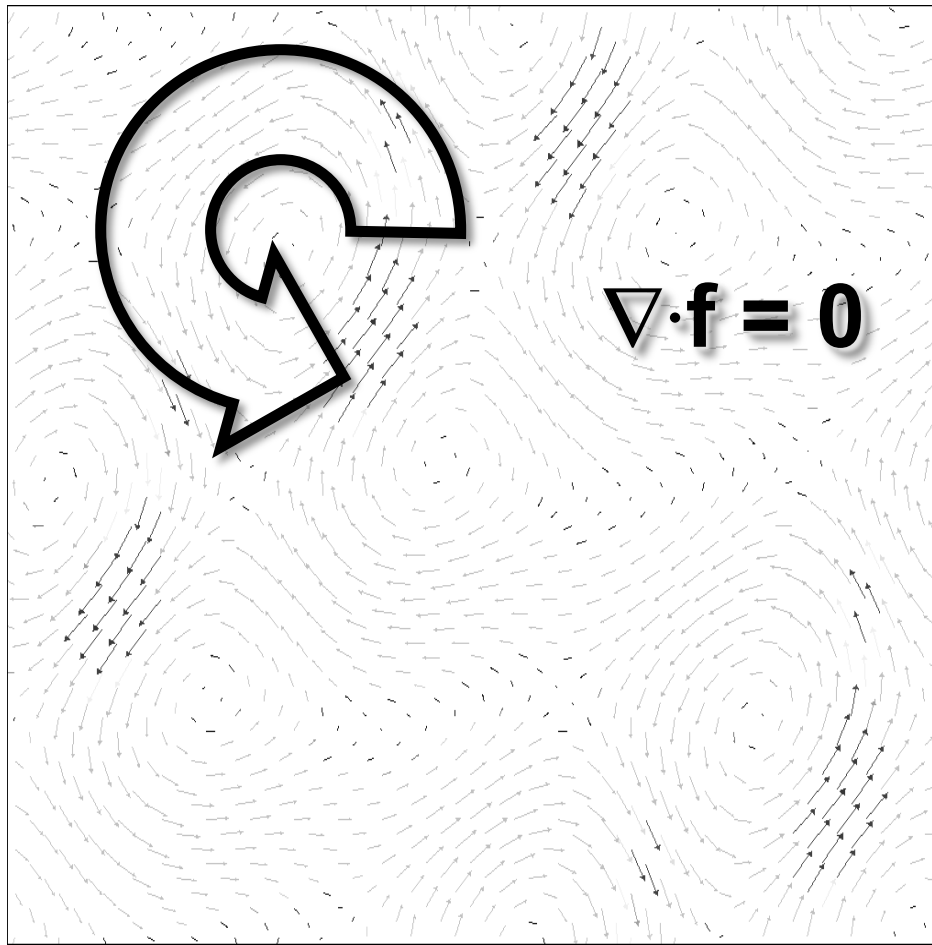


e.g., Vazquez 1994, Padoan+1997, Passot+1998, Stone+1998, Mac Low 1999, Klessen+2000, Ostriker+2001, Heitsch+2001, Cho+2002, Boldyrev+2002, Li+2003, Haugen+2004, Padoan+2004, Jappsen+2005, Ballesteros+2006, Mee+Brandenburg 2006, Kritsuk+2007, Kowal+2007, Dib+2008, Offner+2008, Schmidt+2009, Burkhart +2009, Cho+2009, Lemaster+2009, Glover+2010, Price+2011, DelSordo+2011, Collins +2012, Walch+2012, Scannapieco+2012, Pan+2012, Micic+2012, Robertson+2012, Price+2012, Bauer+2012 +++

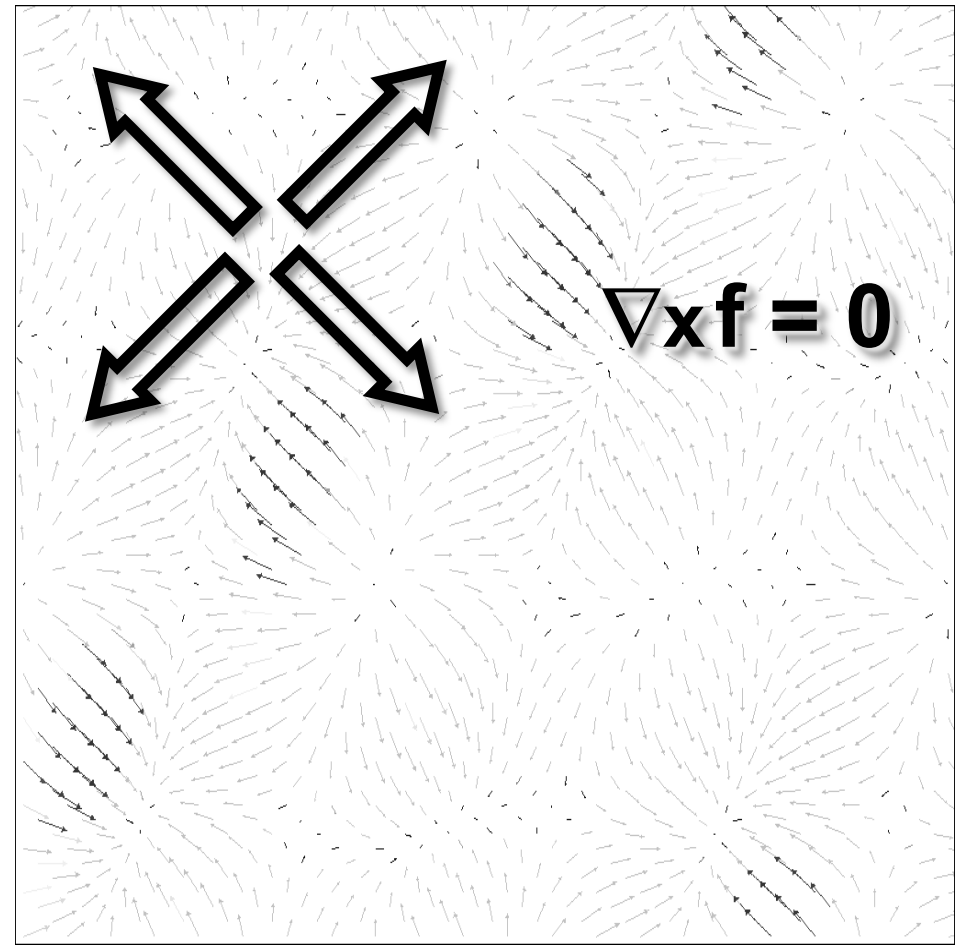
Turbulence driving – solenoidal versus compressive

Ornstein-Uhlenbeck process (stochastic process with autocorrelation time)
→ forcing varies smoothly in space and time,
following a well-defined random process

Solenoidal forcing



Compressive forcing



Turbulence driving – solenoidal versus compressive

Column Density

Movies available: <http://www.ita.uni-heidelberg.de/~chfeder/pubs/supersonic/supersonic.shtml>

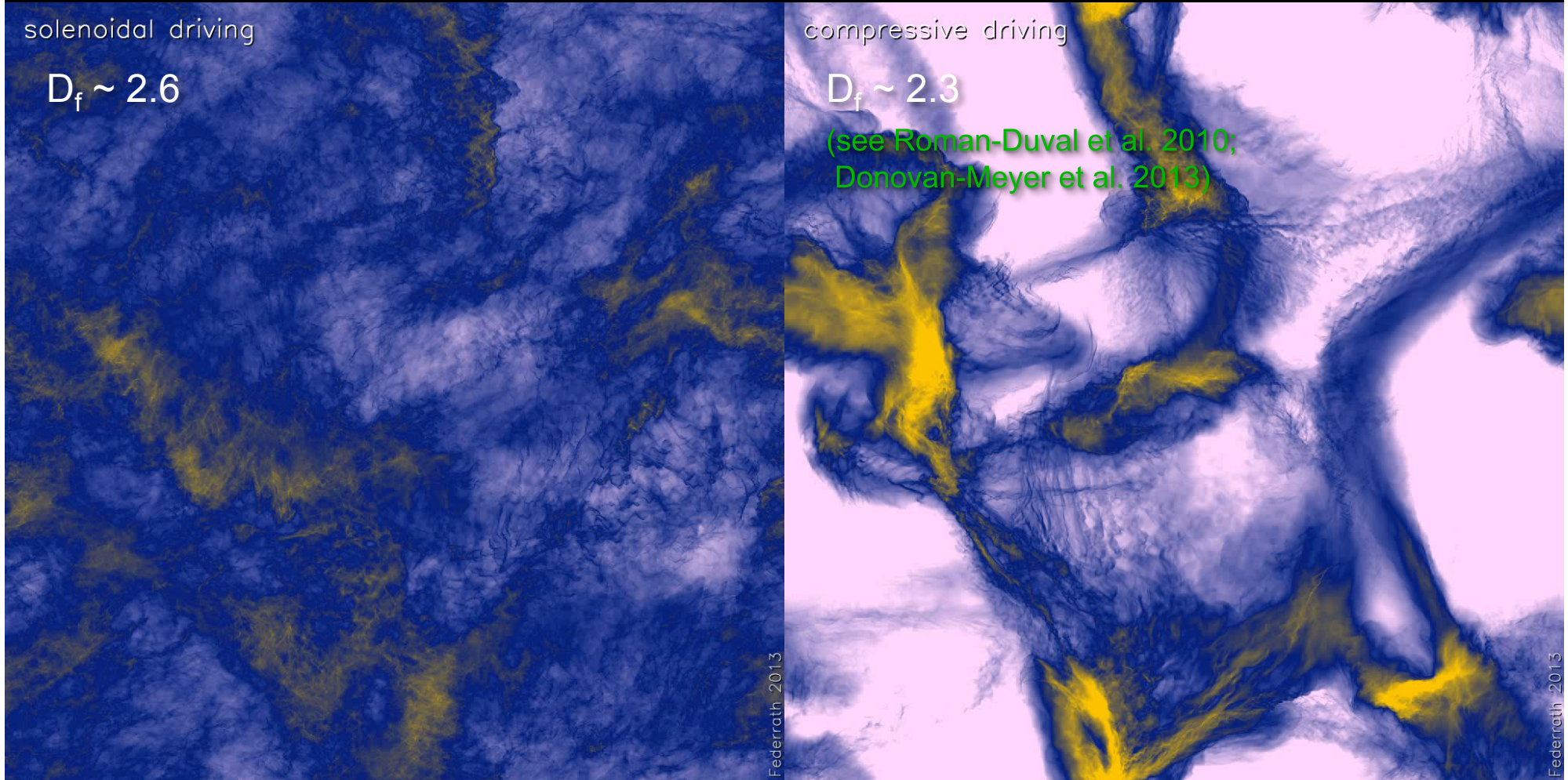
solenoidal driving

$$D_f \sim 2.6$$

compressive driving

$$D_f \sim 2.3$$

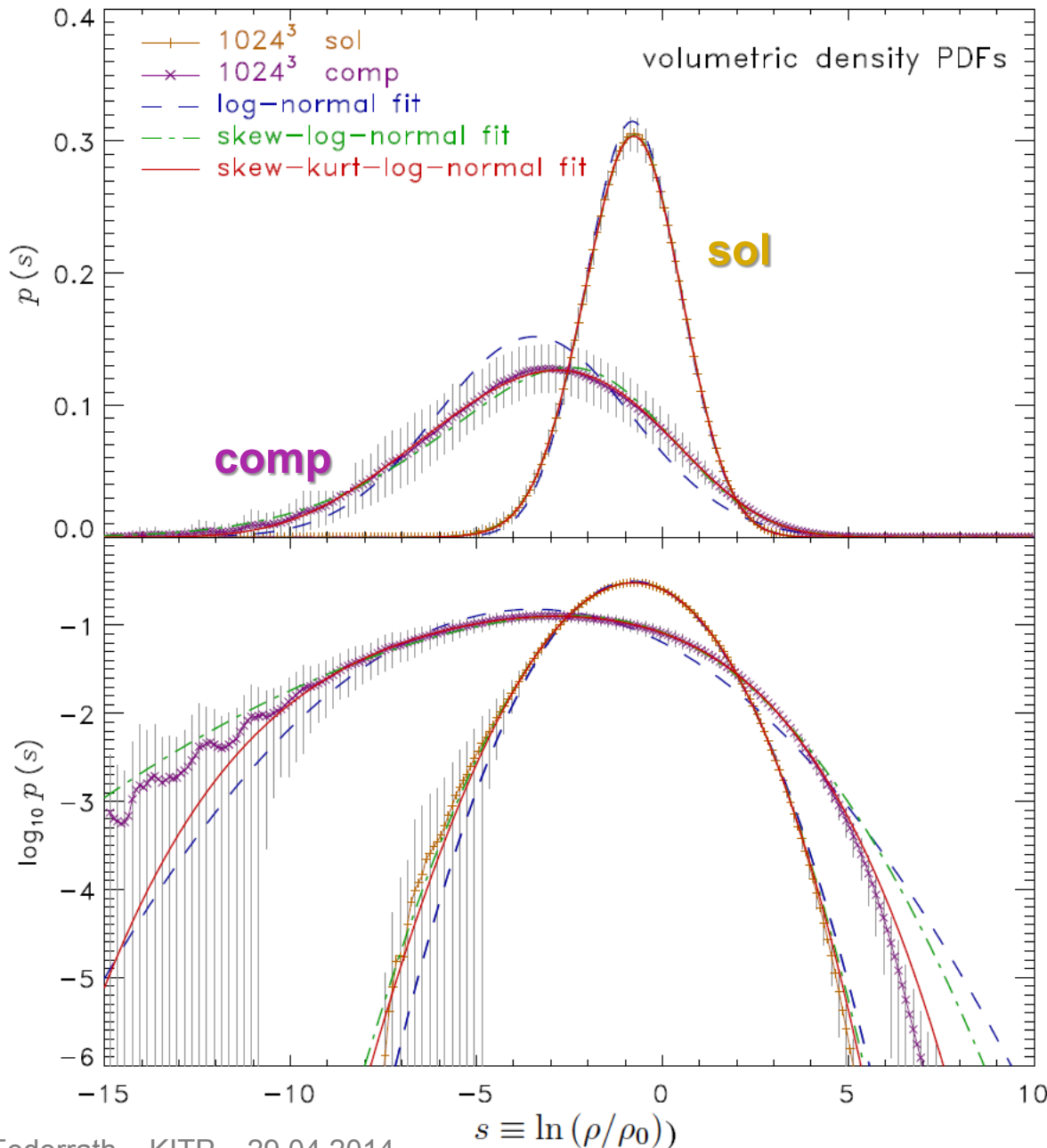
(see Roman-Duval et al. 2010;
Donovan-Meyer et al. 2013)



Compressive forcing produces stronger density enhancements

(Federrath 2013, MNRAS 436, 1245: Supersonic turbulence @ 4096³ grid cells)

The density PDF



gas density PDF

PDFs are close to log-normals:

$$p_s ds = \frac{1}{\sqrt{2\pi\sigma_s^2}} \exp\left[-\frac{(s - \langle s \rangle)^2}{2\sigma_s^2}\right] ds$$

$$s \equiv \ln(\rho/\rho_0)$$

Vazquez-Semadeni (1994); Padoan et al. (1997);
Ostriker et al. (2001); Hopkins (2013)

$$\sigma_s^2 = \ln(1 + b^2 \mathcal{M}^2)$$

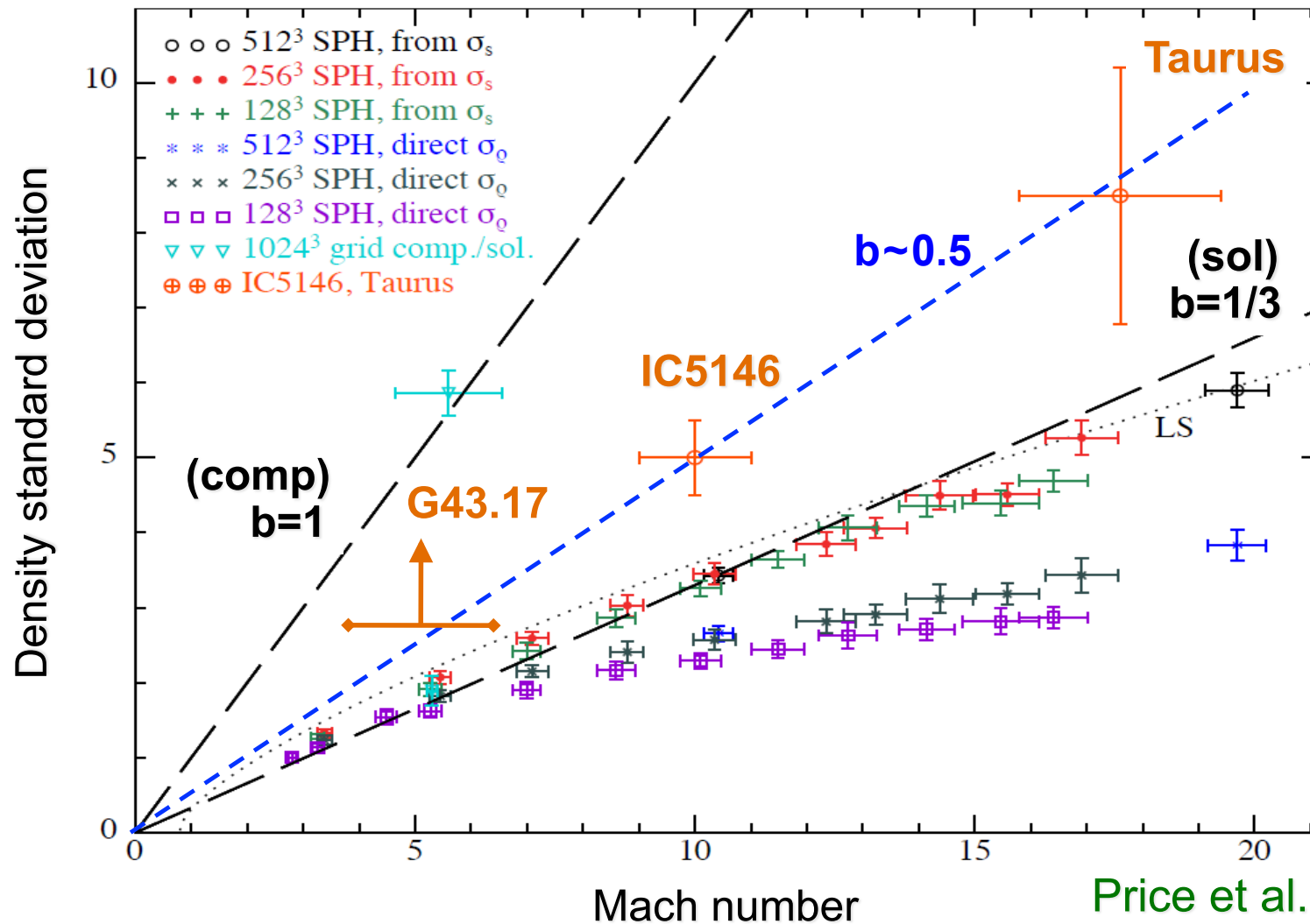


$$b = 1/3 \text{ (sol)}$$

$$b = 1 \text{ (comp)}$$

Federrath et al. (2008, 2010);
Konstandin et al. (2012)

The density PDF



2D \rightarrow 3D
conversion
 $\sigma_{N/N_0} \rightarrow \sigma_{\rho/\rho_0}$
(Brunt et al. 2010a,b)

Price et al. (2011)

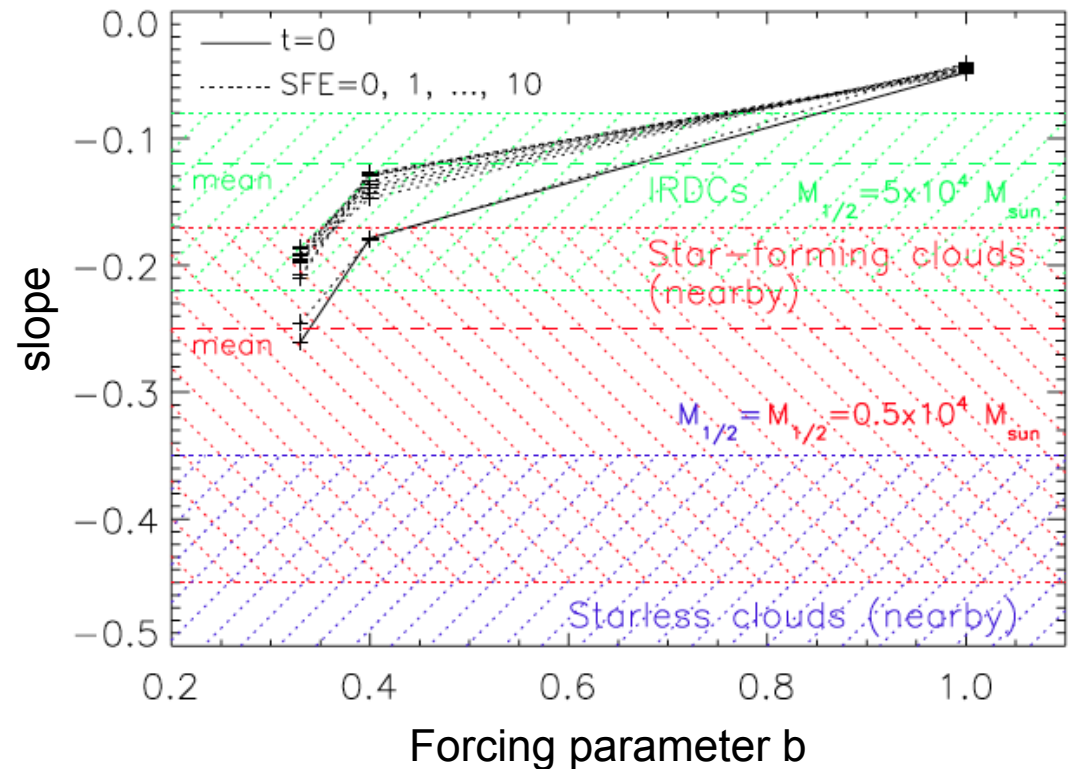
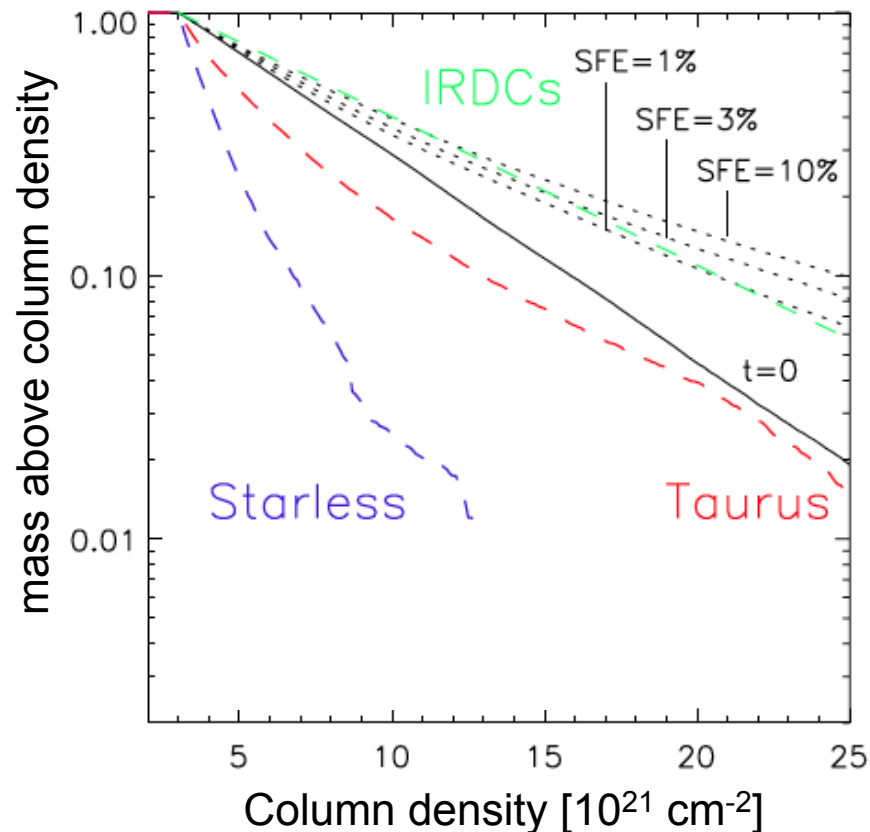
Padoan et al. (1997), Brunt (2010),
Burkhart & Lazarian (2012),
Ginsburg et al. (2013)

$$\sigma_s^2 = \ln(1 + b^2 \mathcal{M}^2) \xrightarrow{p(s)} \sigma_{\rho/\rho_0} = b \mathcal{M}$$

Compressive forcing and/or gravity required to explain observations

PDF → The dense gas mass fraction

Kainulainen et al. (2013); See also
Kainulainen et al. (2014, *Science* Vol. 344 no. 6180 pp. 183-185)



Sequence: **Starless** → **Star-forming (nearby)** → **IRDCs** → more massive clouds?
 $(5 \times 10^3 M_{\odot})$ $(5 \times 10^4 M_{\odot})$

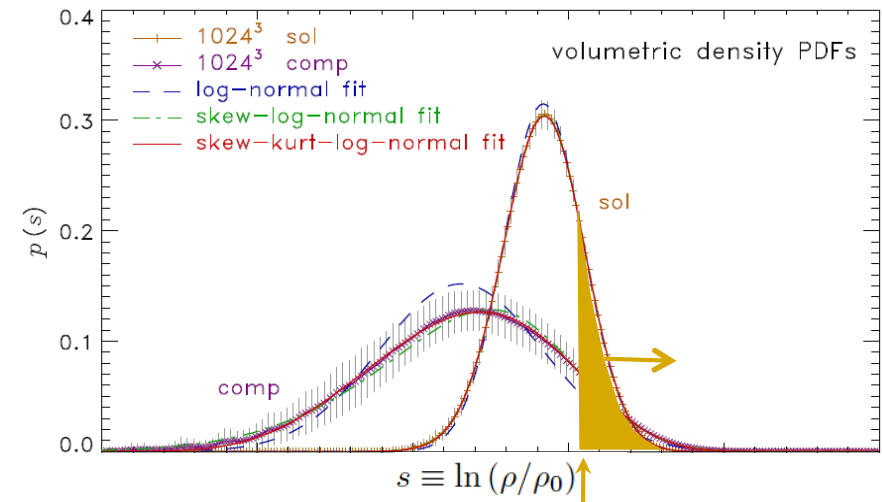
Modeling jet and outflow feedback

Turbulence \rightarrow Density PDF

Density PDF \rightarrow Star Formation Rate

Density PDF \rightarrow Star Formation Rate

Density PDF is key for star formation theories



- **Initial Mass Function** (Padoan & Nordlund 02, Hennebelle & Chabrier 08,09, Elmegreen 11, Veltchev+11, Hopkins 12)
- **Star Formation Efficiency** (Elmegreen 08, Federrath & Klessen 13)
- **Kennicutt-Schmidt relation** (Elmegreen 02, Krumholz & McKee 05, Tassis 07, Ostriker+10)
- **Star Formation Rate** (Krumholz & McKee 05, Padoan & Nordlund 11, Renaud+12)

All based on integrals over the turbulent density PDF

$$\text{SFR}_{\text{ff}} = \frac{\epsilon_{\text{core}}}{\phi_t} \int_{x_{\text{crit}}}^{\infty} xp(x) dx$$

Krumholz & McKee (2005), Padoan & Nordlund (2011); Hennebelle & Chabrier (2011,2013)

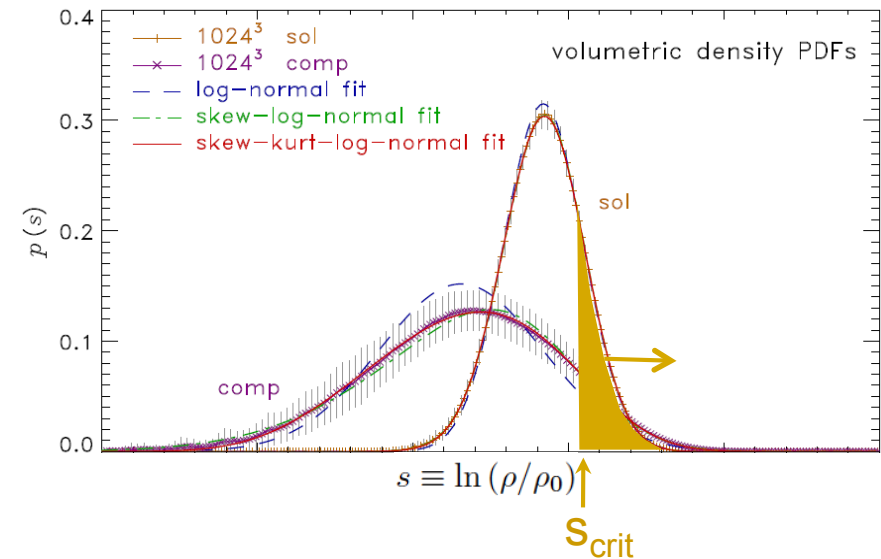
Density PDF \rightarrow Star Formation Rate

Statistical Theory for the Star Formation Rate:

SFR \sim Mass/time

freefall time mass fraction

$$\text{SFR}_{\text{ff}} = \epsilon \int_{s_{\text{crit}}}^{\infty} \overbrace{\frac{t_{\text{ff}}(\rho_0)}{t_{\text{ff}}(\rho)}}^{\text{freefall time}} \overbrace{\frac{\rho}{\rho_0}}^{\text{mass fraction}} p(s) ds$$



Hennebelle & Chabrier (2011) : “multi-freefall model”

Density PDF \rightarrow Star Formation Rate

Statistical Theory for the Star Formation Rate:

SFR \sim Mass/time **freefall time** **mass fraction**

$$\begin{aligned} \text{SFR}_{\text{ff}} &= \epsilon \int_{s_{\text{crit}}}^{\infty} \overbrace{\frac{t_{\text{ff}}(\rho_0)}{t_{\text{ff}}(\rho)}}^{\text{freefall time}} \overbrace{\frac{\rho}{\rho_0}}^{\text{mass fraction}} p(s) \, ds = \epsilon \int_{s_{\text{crit}}}^{\infty} \exp\left(\frac{3}{2}s\right) p(s) \, ds \\ &= \frac{\epsilon}{2} \exp\left(\frac{3}{8}\sigma_s^2\right) \left[1 + \text{erf}\left(\frac{\sigma_s^2 - s_{\text{crit}}}{\sqrt{2}\sigma_s^2}\right) \right] \end{aligned}$$

$$p(s) = \frac{1}{\sqrt{2\pi\sigma_s^2}} \exp\left(-\frac{(s - s_0)^2}{2\sigma_s^2}\right)$$

$$s = \ln(\rho/\rho_0) \quad t_{\text{ff}}(\rho) = \left(\frac{3\pi}{32G\rho}\right)^{1/2}$$

Hennebelle & Chabrier (2011): “multi-freefall model”

Density PDF \rightarrow Star Formation Rate

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Hennebelle & Chabrier (2011) : “multi-freefall model”

From sonic and Jeans scales:

$$s_{\text{crit}} \propto \ln(\alpha_{\text{vir}} \mathcal{M}^2)$$

(Krumholz & McKee 2005, Padoan & Nordlund 2011)

$$\text{SFR}_{\text{ff}} = \text{SFR}_{\text{ff}}(\alpha_{\text{vir}}, b, \mathcal{M})$$

$$\sigma_s^2 = \ln(1 + b^2 \mathcal{M}^2)$$

(e.g., Federrath et al. 2008)

$2E_{\text{kin}}/E_{\text{grav}}$

forcing

Mach number

Density PDF \rightarrow Star Formation Rate

$$\text{SFR}_{\text{ff}} = \text{SFR}_{\text{ff}}(\alpha_{\text{vir}}, b, \mathcal{M})$$

$$2E_{\text{kin}}/E_{\text{grav}}$$

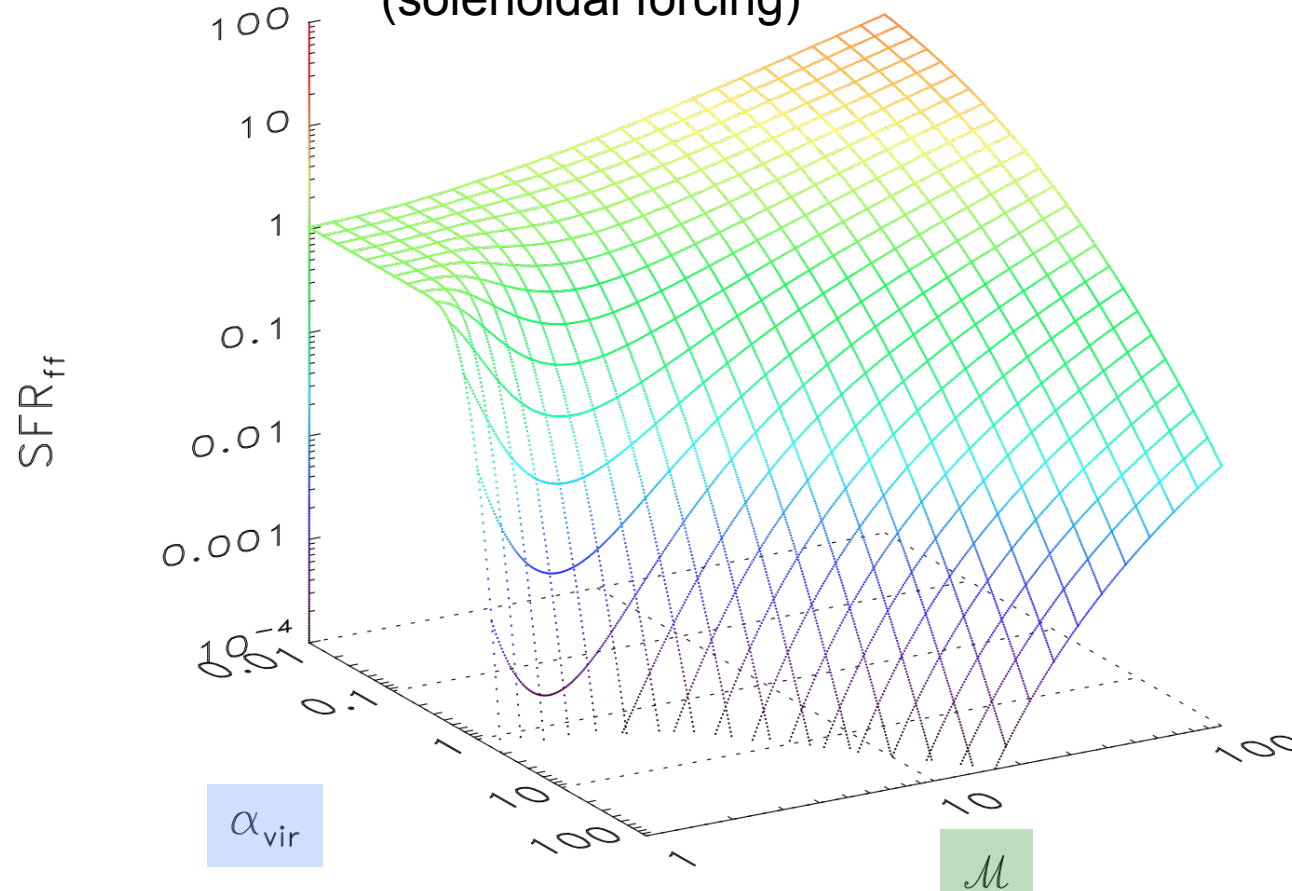
forcing

Mach number

forcing parameter ($b=0.33$)

multi-freefall

(solenoidal forcing)



If $\alpha_{\text{vir}} \uparrow$ then $\text{SFR} \downarrow$

If $\mathcal{M} \uparrow$ then $\text{SFR} \uparrow$

Density PDF \rightarrow Star Formation Rate

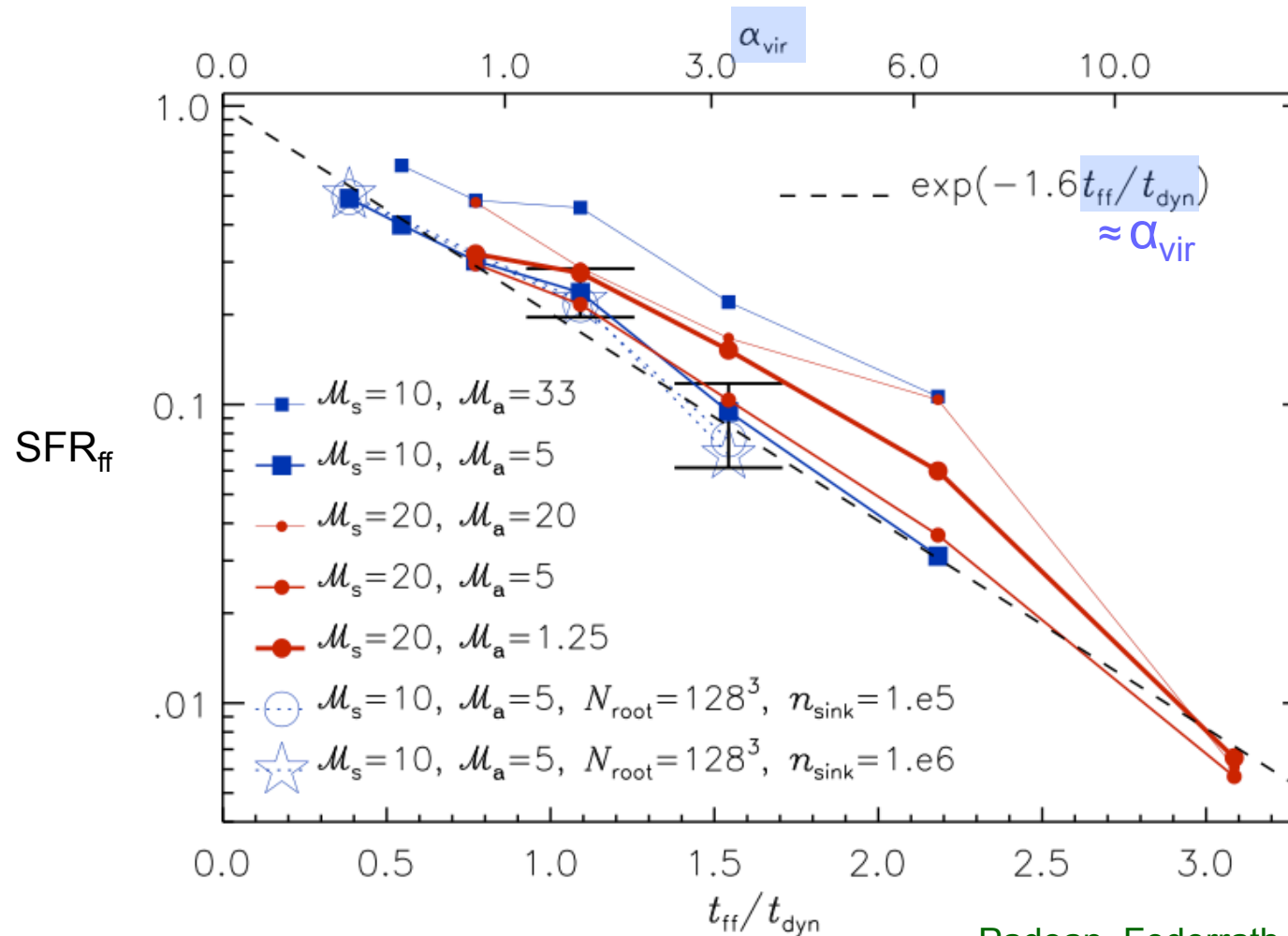
$$\text{SFR}_{\text{ff}} = \text{SFR}_{\text{ff}}(\alpha_{\text{vir}}, b, \mathcal{M})$$

$$2E_{\text{kin}}/E_{\text{grav}}$$

forcing

Mach number

Numerical simulations varying α_{vir}



Density PDF \rightarrow Star Formation Rate

$$\text{SFR}_{\text{ff}} = \text{SFR}_{\text{ff}}(\alpha_{\text{vir}}, b, \mathcal{M})$$

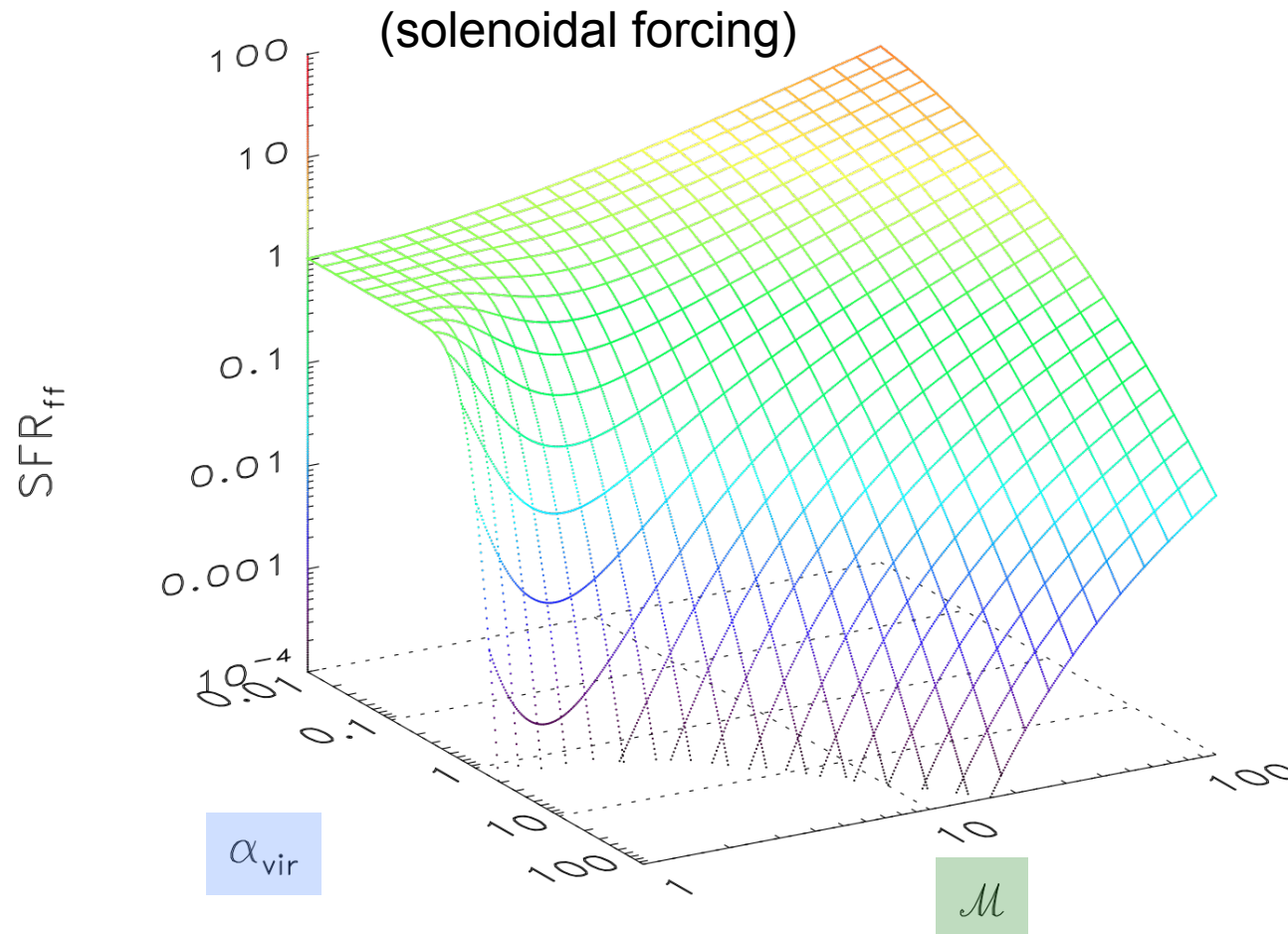
$$2E_{\text{kin}}/E_{\text{grav}}$$

forcing

Mach number

forcing parameter ($b=0.33$)

multi-freefall



Density PDF \rightarrow Star Formation Rate

$$\text{SFR}_{\text{ff}} = \text{SFR}_{\text{ff}}(\alpha_{\text{vir}}, b, \mathcal{M})$$

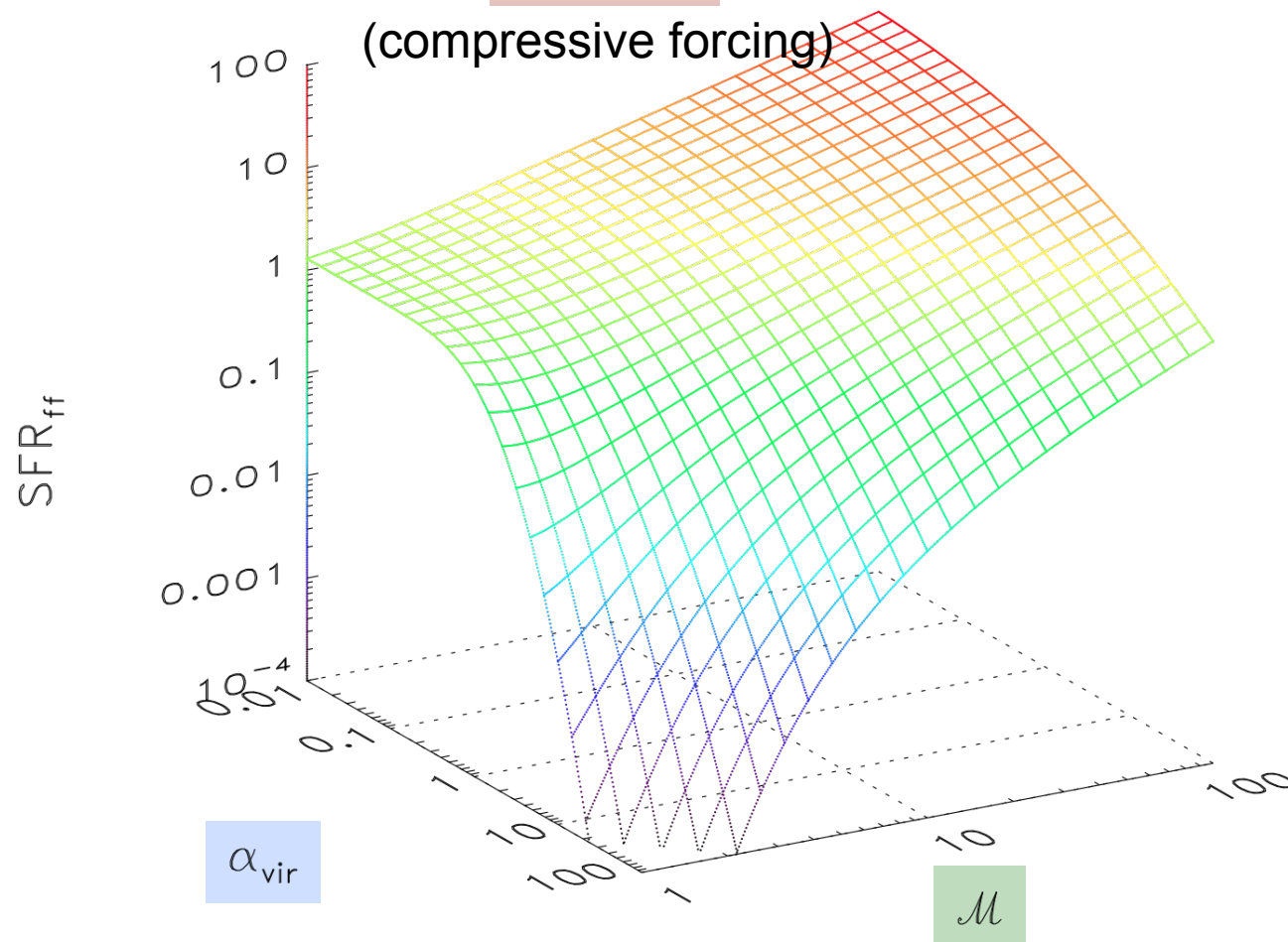
$$2E_{\text{kin}}/E_{\text{grav}}$$

forcing

Mach number

forcing parameter ($b=1.00$)

multi-freefall



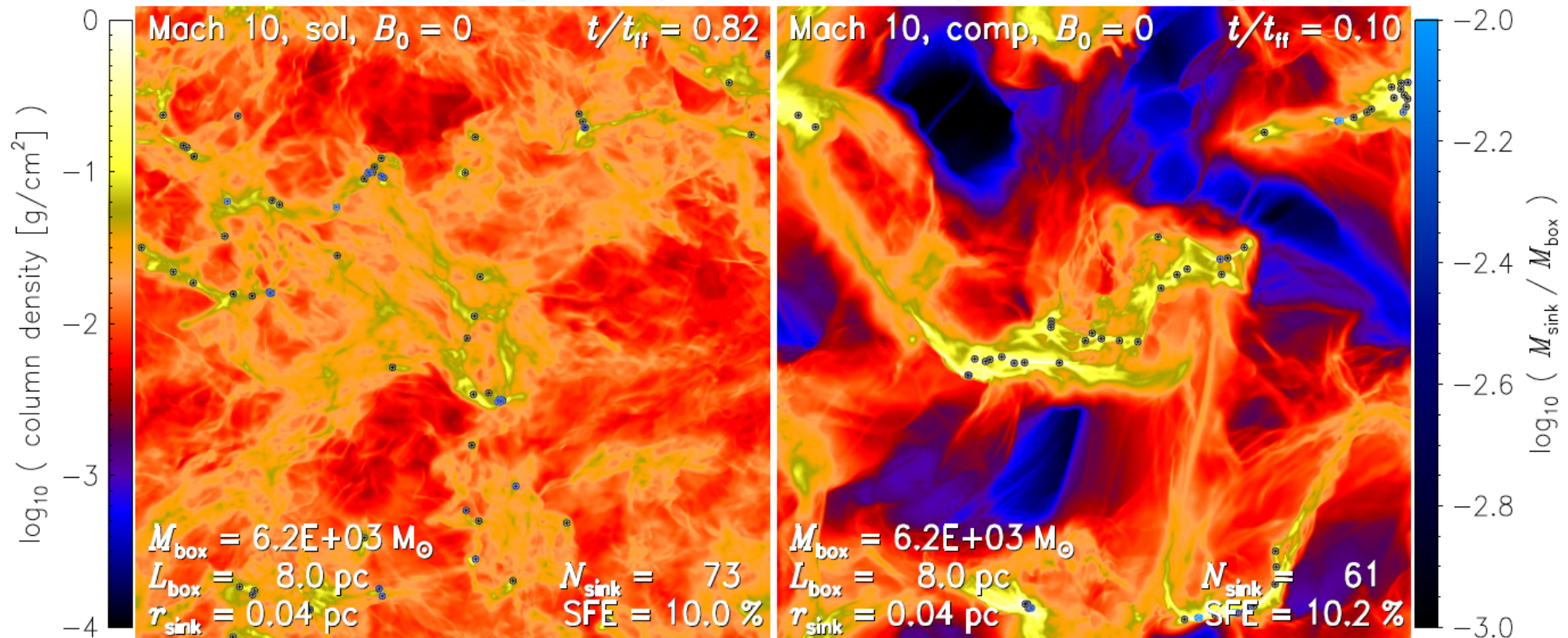
Density PDF \rightarrow Star Formation Rate

Numerical Test for Mach 10 and $\alpha_{\text{vir}} \sim 1$

Movies available: <http://www.ita.uni-heidelberg.de/~chfeder/pubs/sfr/sfr.shtml>

Solenoidal Forcing ($b=1/3$)

Compressive Forcing ($b=1$)



SFR_{ff} (simulation) = **0.14** **x20**
SFR_{ff} (theory) = **0.15** **x15**

SFR_{ff} (simulation) = **2.8**
SFR_{ff} (theory) = **2.3**

Theory and Simulation agree well.

The Star Formation Rate – Magnetic fields

Statistical Theory for the Star Formation Rate:

SFR ~ Mass/time

freefall time fraction

$$\begin{aligned} \text{SFR}_{\text{ff}} &= \epsilon \int_{s_{\text{crit}}}^{\infty} \frac{t_{\text{ff}}(\rho_0)}{t_{\text{ff}}(\rho)} \frac{\rho}{\rho_0} p(s) ds = \epsilon \int_{s_{\text{crit}}}^{\infty} \exp\left(\frac{3}{2}s\right) p(s) ds \\ &= \frac{\epsilon}{2} \exp\left(\frac{3}{8}\sigma_s^2\right) \left[1 + \text{erf}\left(\frac{\sigma_s^2 - s_{\text{crit}}}{\sqrt{2}\sigma_s^2}\right) \right] \end{aligned}$$

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$$s = \ln(\rho/\rho_0) \quad t_{\text{ff}}(\rho) = \left(\frac{3\pi}{32G\rho}\right)^{1/2}$$

MAGNETIC FIELD:

$$P_{\text{th}} \rightarrow P_{\text{th}} + P_{\text{mag}} \quad \mathcal{M} \rightarrow \mathcal{M} (1 + \beta^{-1})^{-1/2}$$

$$s_{\text{crit}} \propto \ln\left(\alpha_{\text{vir}} \mathcal{M}^2 \frac{\beta}{\beta + 1}\right)$$

$$\sigma_s^2 = \ln\left(1 + b^2 \mathcal{M}^2 \frac{\beta}{\beta + 1}\right)$$

$$\text{SFR}_{\text{ff}} = \text{SFR}_{\text{ff}}(\alpha_{\text{vir}}, b, \mathcal{M}, \beta)$$

(Padoan & Nordlund 2011; Molina et al. 2012)

$2 E_{\text{kin}}/E_{\text{grav}}$ forcing Mach number plasma $\beta = P_{\text{th}}/P_{\text{mag}}$

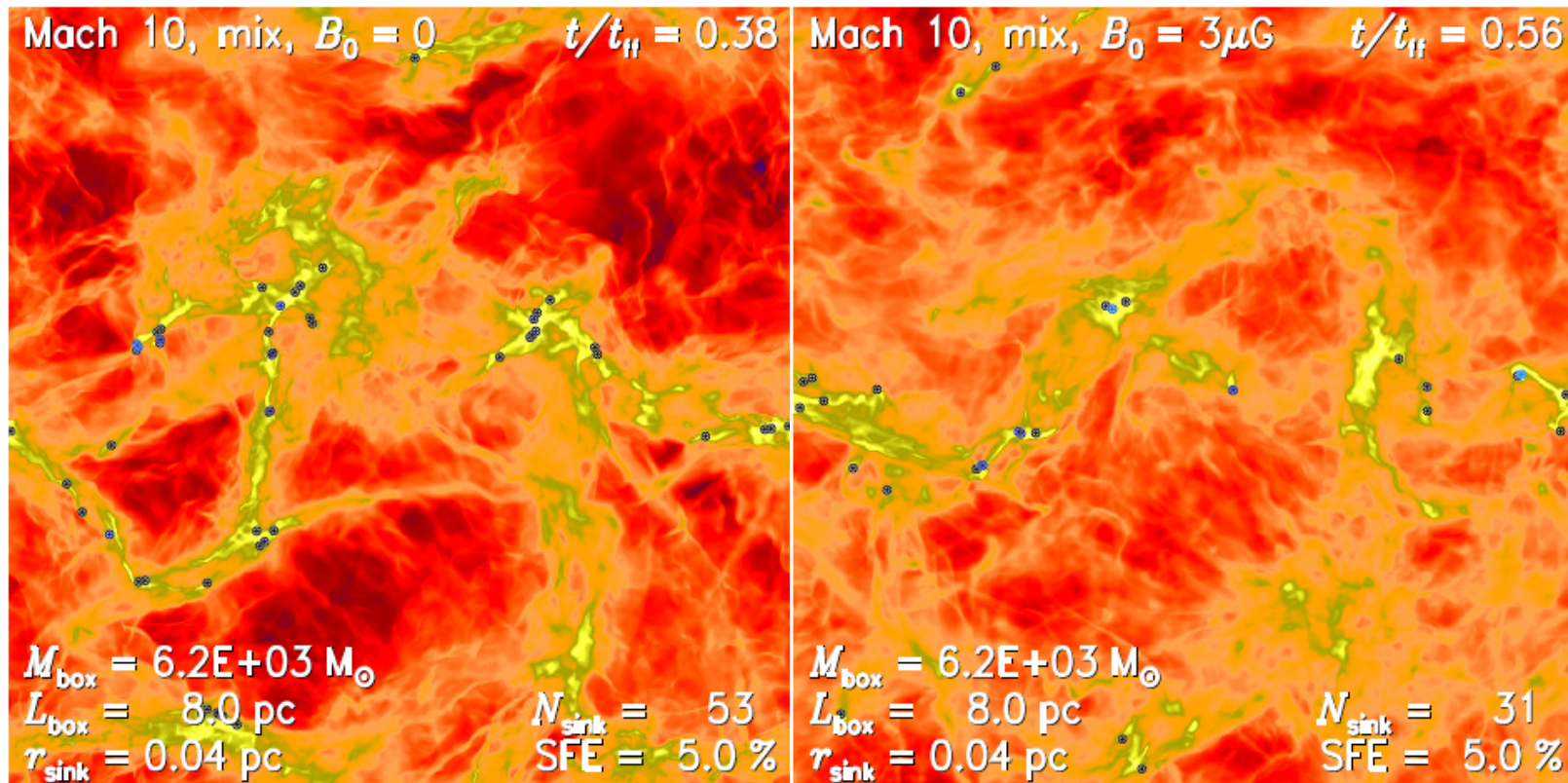
The Star Formation Rate – Magnetic fields

Numerical Test for Mach 10 with mixed forcing

Movies available: <http://www.ita.uni-heidelberg.de/~chfeder/pubs/sfr/sfr.shtml>

$B=0$ ($M_A = \infty$, $\beta = \infty$)

$B=3\mu\text{G}$ ($M_A = 2.7$, $\beta = 0.2$)



SFR_{ff} (simulation) = **0.46**

x**0.63**

SFR_{ff} (simulation) = **0.29**

SFR_{ff} (theory) = **0.45**

x**0.40**

SFR_{ff} (theory) = **0.18**

Magnetic field reduces SFR and fragmentation (by factor ~2).

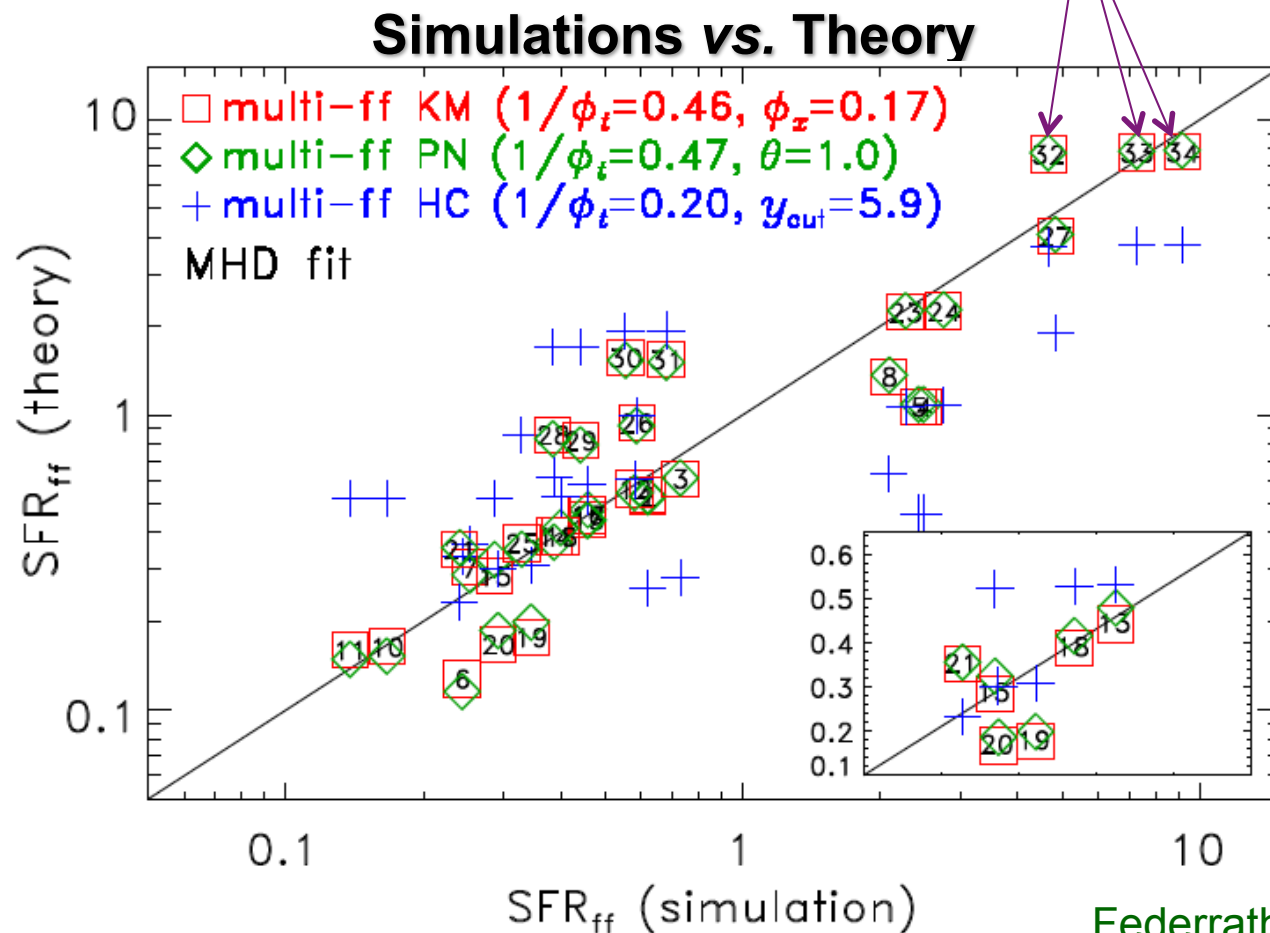
Padoan & Nordlund (2011); Padoan et al. (2012); Federrath & Klessen (2012)

The Star Formation Rate of MHD turbulence

Compare simulations with

- cloud masses of $300 - 4 \times 10^6 M_{\odot}$
- solenoidal, mixed, and compressive forcing
- sonic Mach numbers 3 – 50
- Alfvén Mach numbers 1 – infinity

Convergence with numerical resolution

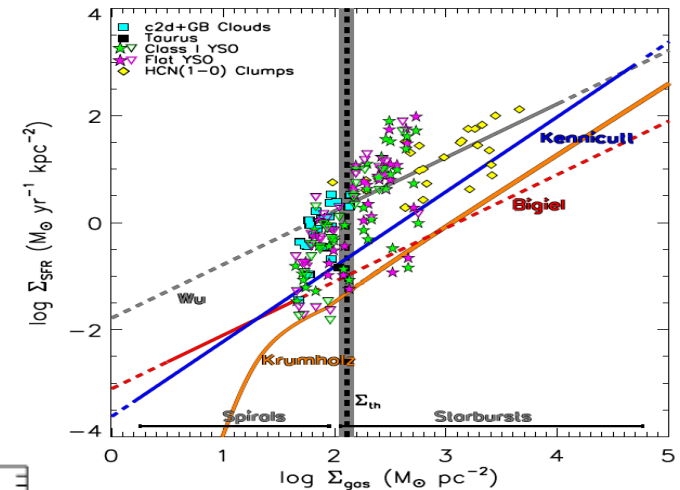
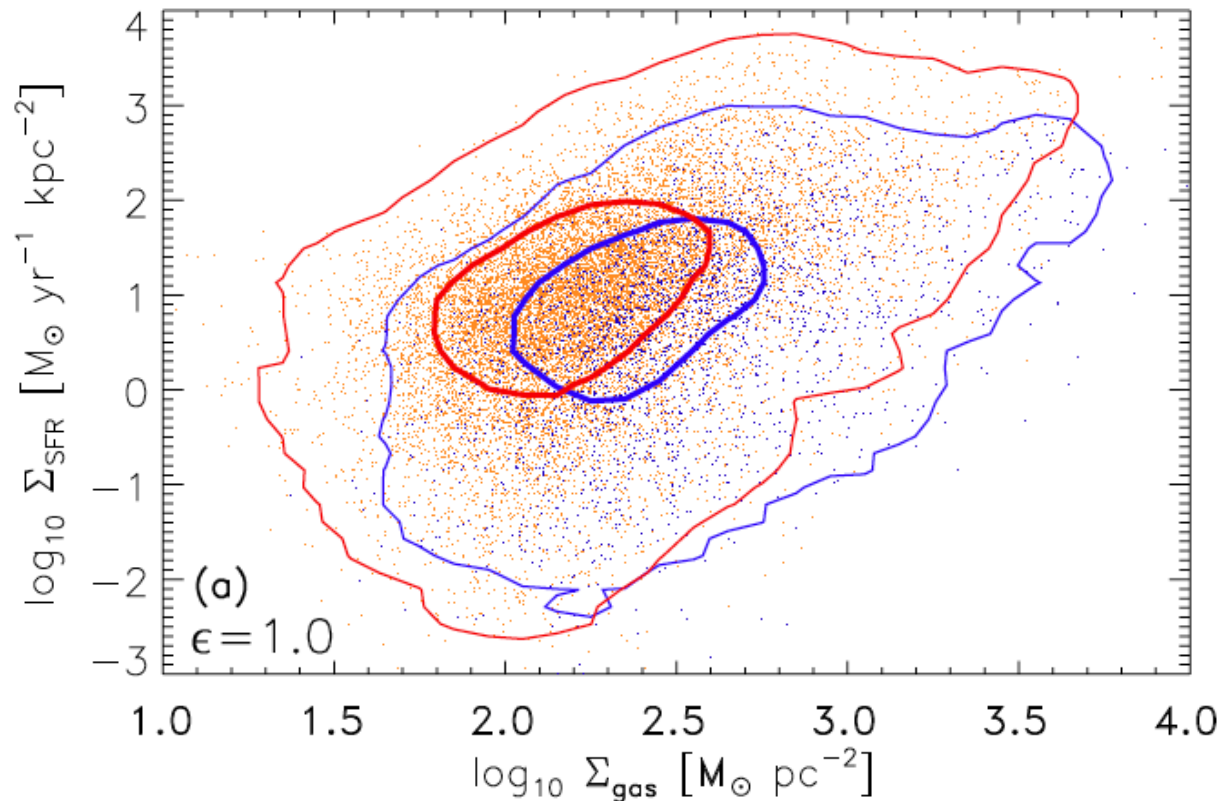


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Simulations vs. Observations



(Heiderman et al. 2010)

SFEs $\sim 1\text{-}10\%$ (Evans+2009; Burkert & Hartmann 2013; Federrath & Klessen 2013)

— GRAVTURB SFE=10%
— GRAVTURB SFE= 1%

Taurus ■
Class I YSO ☆▽
Flat YSO ☆▽
HCN(1-0) Clumps ◇
C2D+GB Clouds □

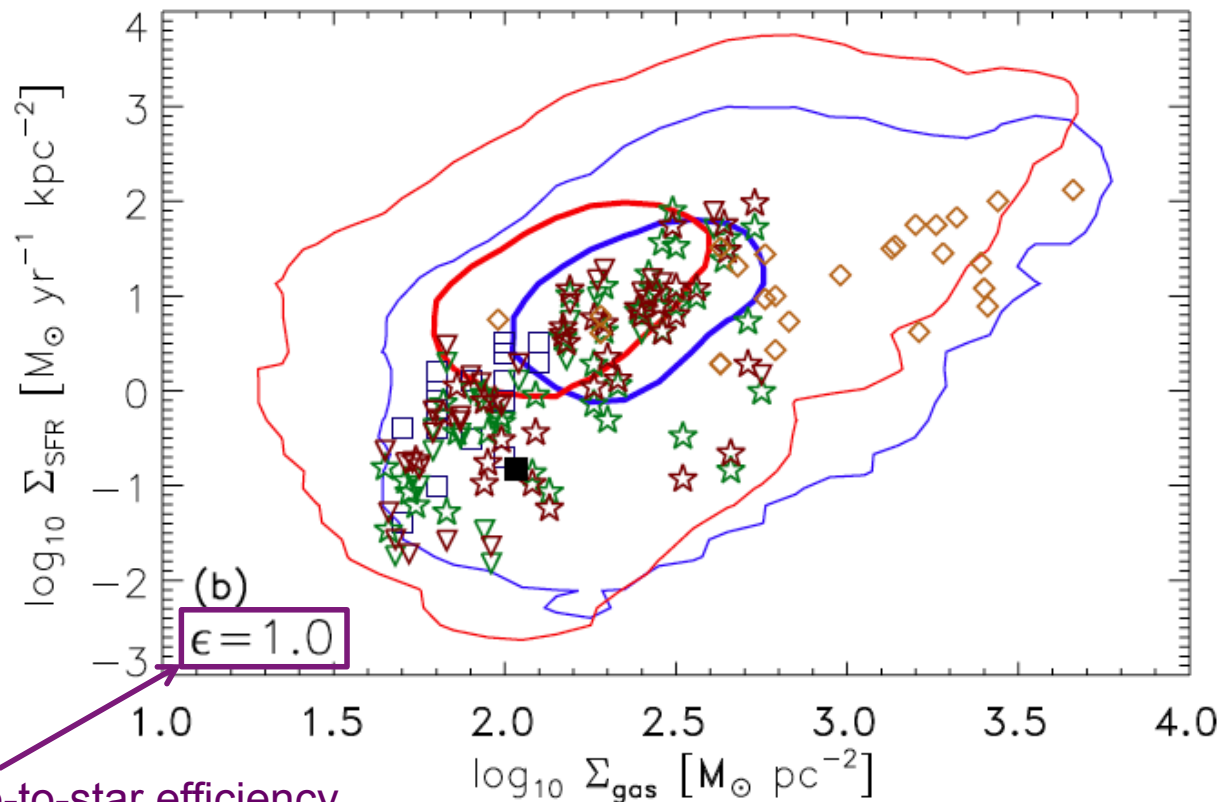
Federrath & Klessen (2012)

The Star Formation Rate of MHD turbulence

Compare simulations with

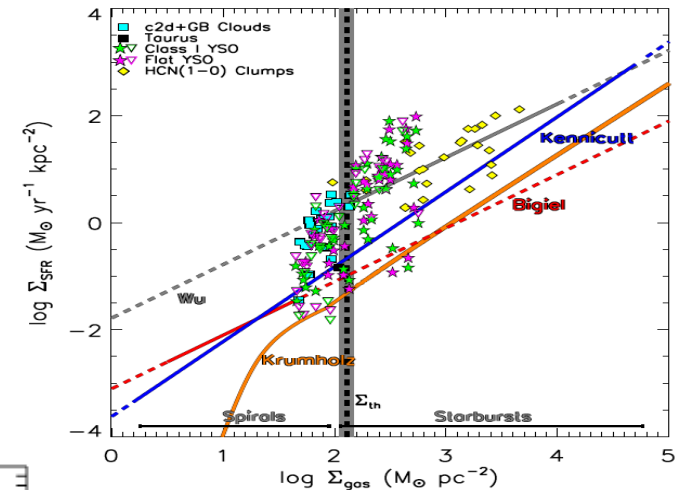
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Simulations vs. Observations



core-to-star efficiency

Federrath – KITP – 29.04.2014



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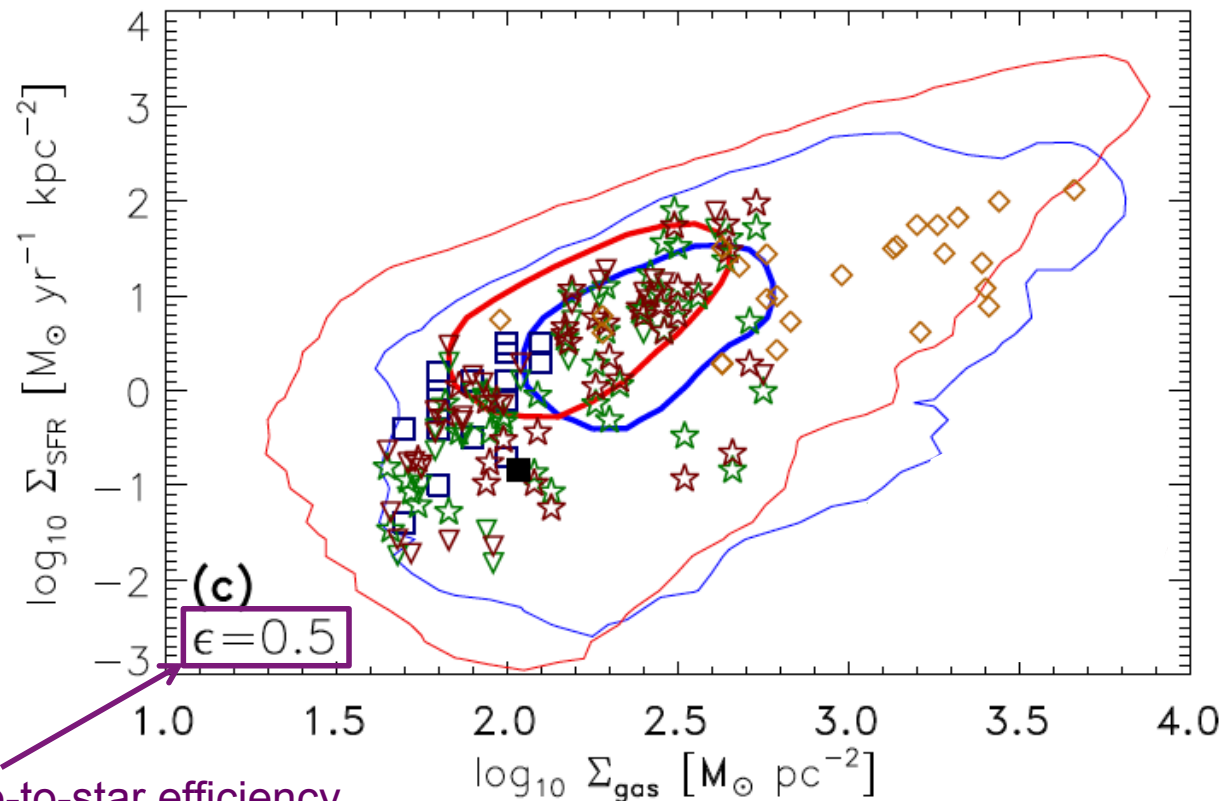
Federrath & Klessen (2012)

The Star Formation Rate of MHD turbulence

Compare simulations with

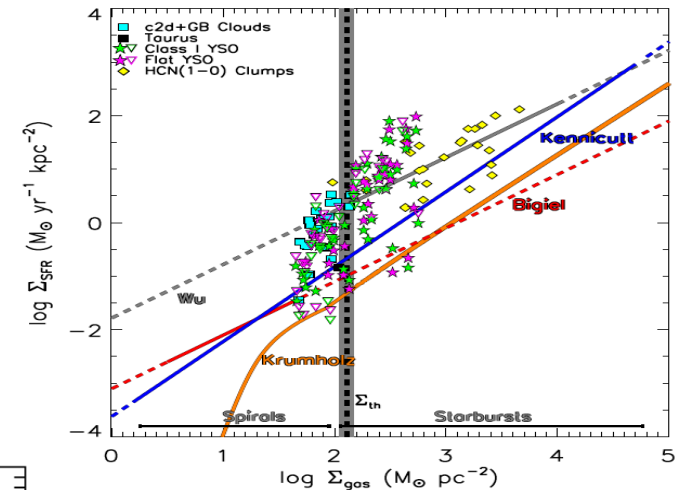
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Federrath & Klessen (2012)

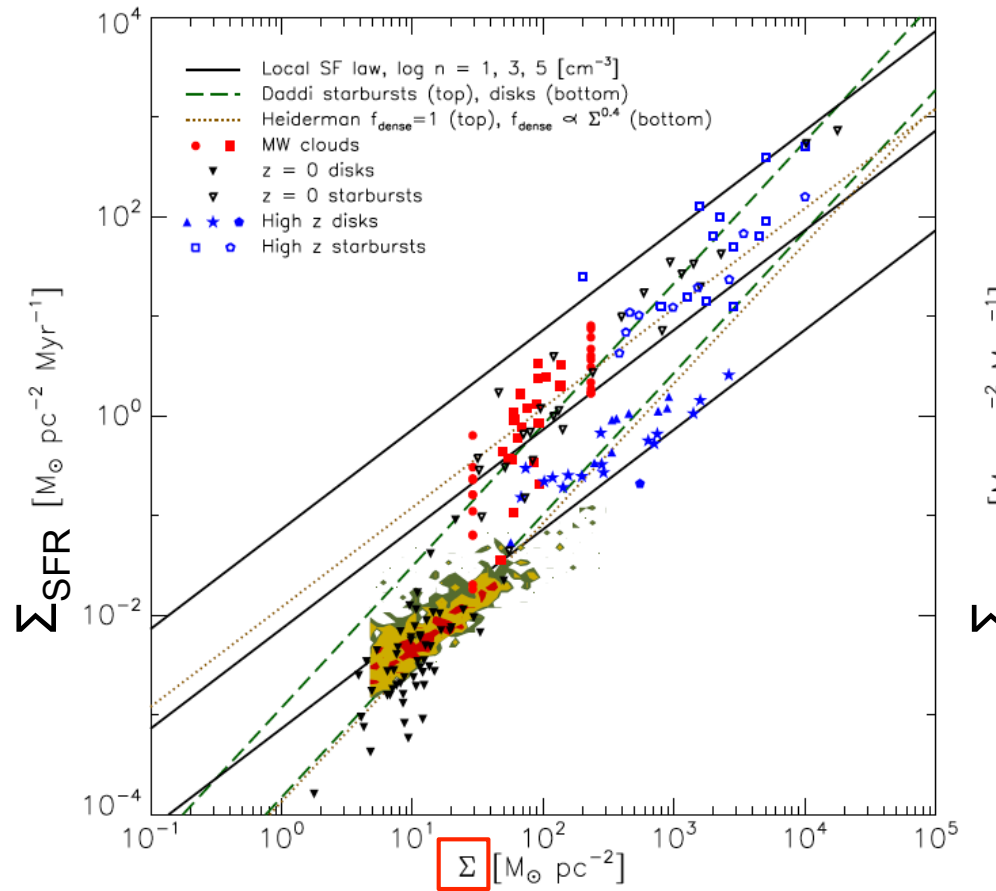
Application to Extra-Galactic Star Formation



Physical Variations in the Universal Star Formation Law

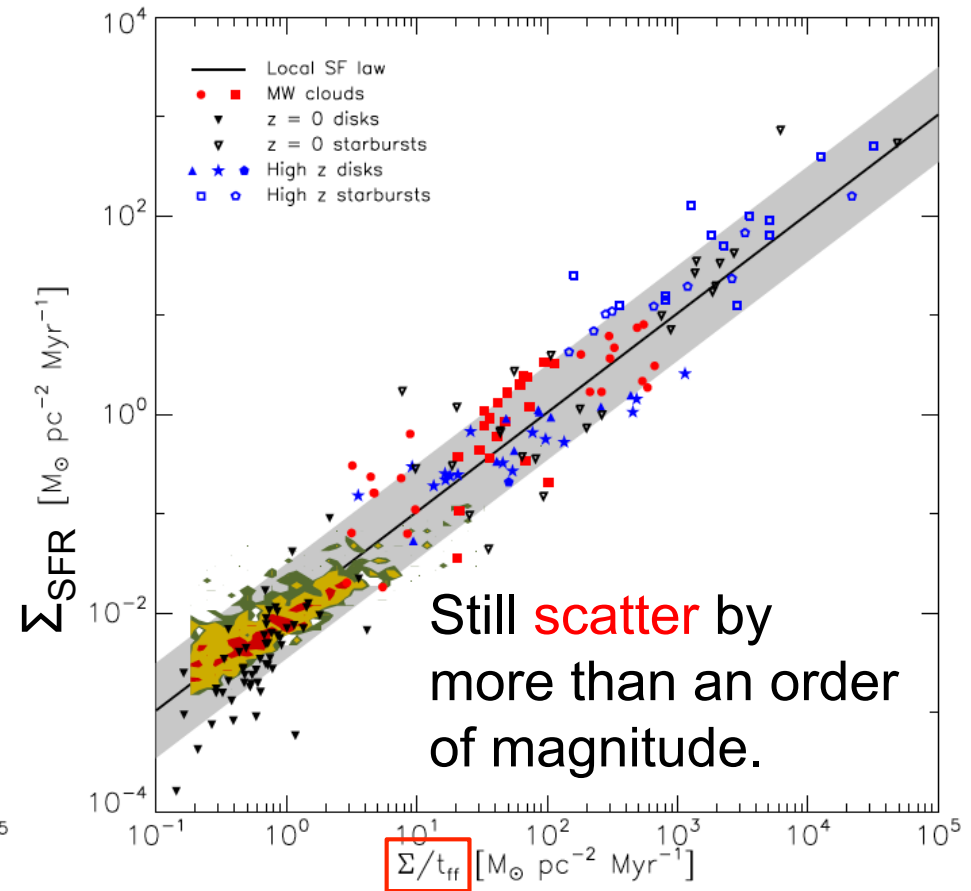
Krumholz, Dekel, McKee (2012)

A more universal star formation “law”?



just Σ_{gas}

(classical Kennicutt-Schmidt relation)

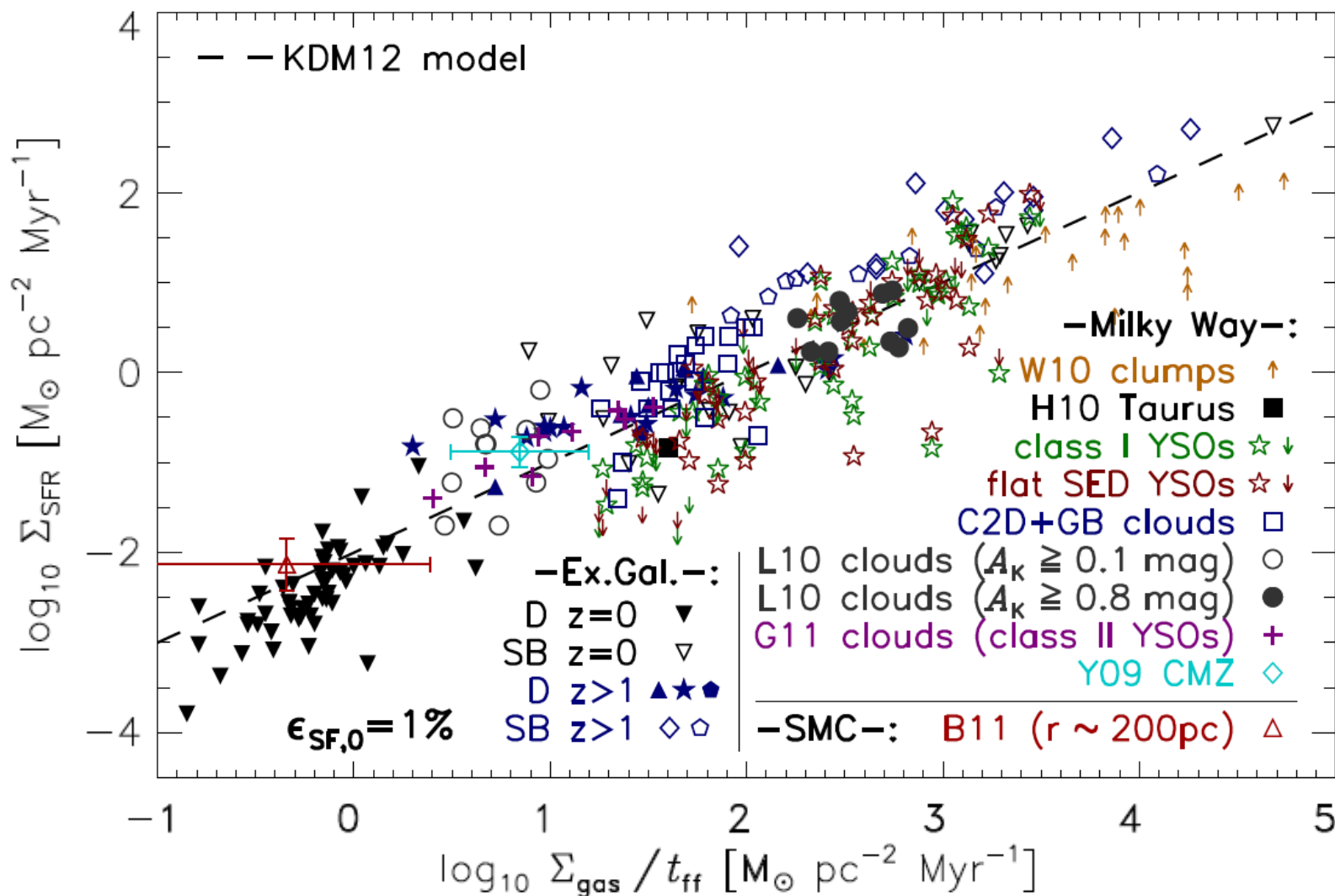


Still **scatter** by more than an order of magnitude.

divide Σ_{gas}

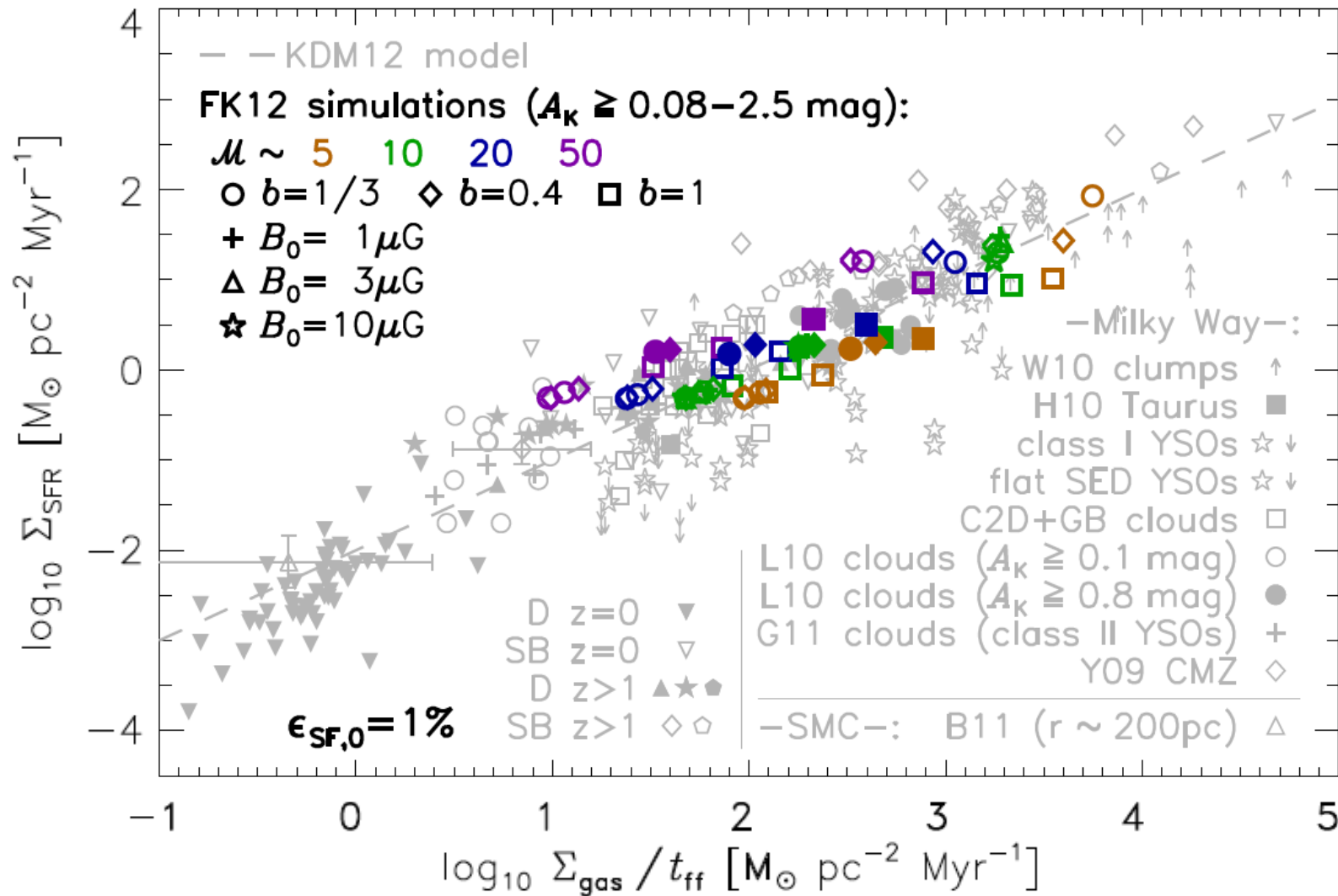
by local freefall time t_{ff}

Physical Variations in the Universal Star Formation Law



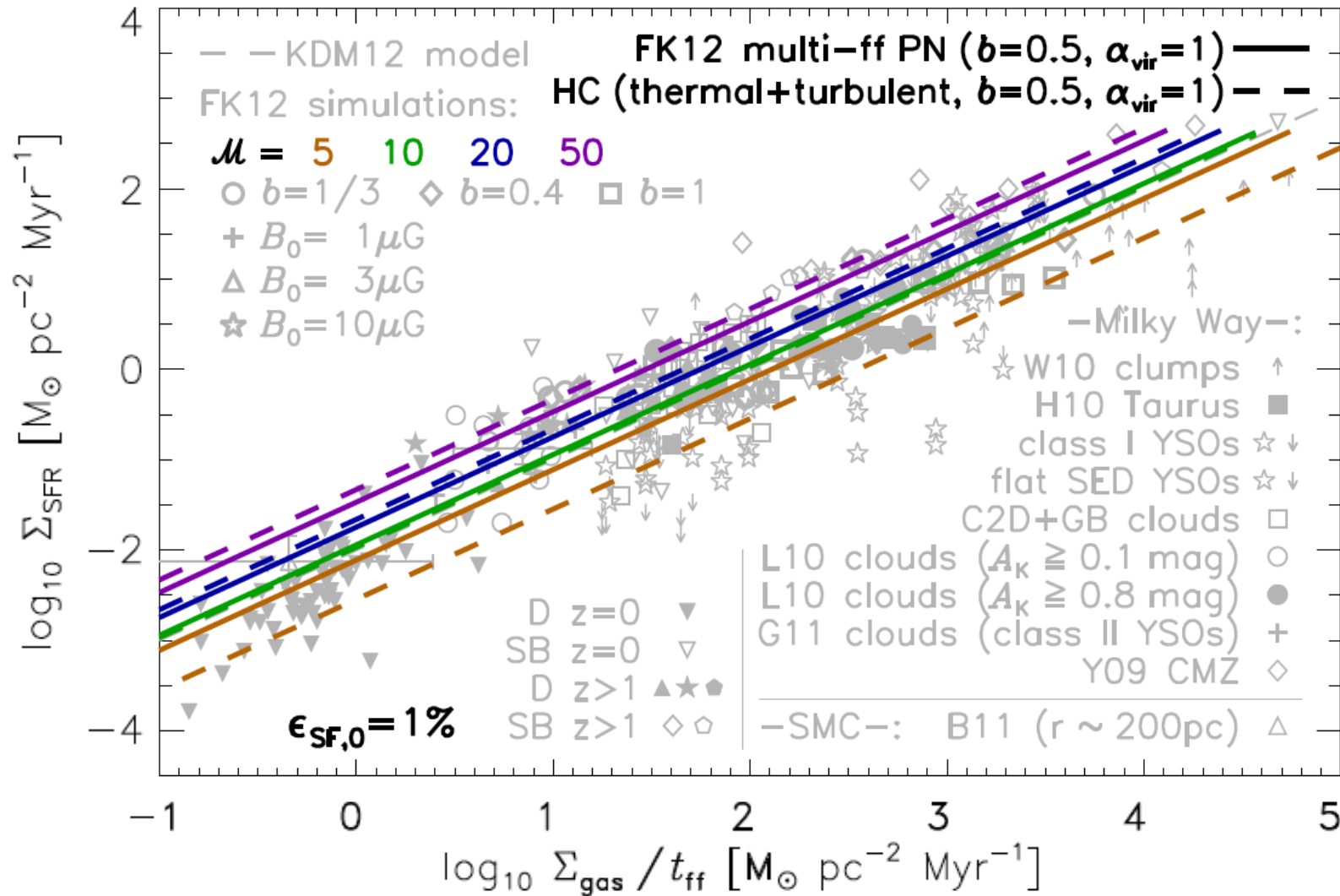
Scatter caused by variations in the turbulence (Mach number, driving)

Physical Variations in the Universal Star Formation Law



Scatter caused by variations in the turbulence (Mach number, driving)

Physical Variations in the Universal Star Formation Law



Scatter caused by variations in the turbulence (Mach number, driving)

- **Subgrid model for jet/outflow feedback** in star cluster formation:
 - Implemented for AMR, tested, and demonstrated **convergence**
 - Star formation rate reduced by $\sim 2x$
 - Average star mass reduced by $\sim 3x \rightarrow$ **IMF**
- **Supersonic, magnetized turbulence** is key for **star formation**
 - SFR from density PDF depends on **virial parameter**, **forcing parameter**, **Mach number**, **plasma beta**
 - Very good agreement between theory, simulations and observations
- Scatter in **star formation relations** \rightarrow potentially caused by variations in the **turbulence**