

# Star Formation at Small Scales

## Formation of Circumstellar Disks and Outflows

(or what happens in sub and sub-sub grid models)

Department of Astrophysical Sciences, Princeton University

Department of Physics, University of Tokyo

JSPS Research Fellow

**Kengo TOMIDA**

K. Tomisaka, T. Matsumoto, Y. Hori, S. Okuzumi,

M. N. Machida, K. Saigo

References: Tomida et al., 2013, ApJ, 763, 6

Tomida, Okuzumi & Machida in prep.

# Topics

- Introduction
  - Protostellar Collapse
  - Angular Momentum Problem
  - Magnetic Braking Catastrophe
- RMHD simulations of Protostellar Collapse
  - Ideal RMHD
  - Resistive RMHD
  - Ambipolar Diffusion (very preliminary!)
- Observations
  - Young Circumstellar Disks
  - First Core Candidates
- Summary

# Introduction

# Multi-Scale, Multi-Physics nature of Star Formation

Galactic Scale

Cloud Scale

Core Scale

Star/Disk Scale

Global Flow like  
Merger, Spiral Arms,  
Supernovae, etc.

Turbulence, Chemistry,  
Magnetic Fields,  
Irradiation, Pressure, etc.

Mass, Accretion,  
Magnetic Fields,  
Turbulence, Rotation,  
etc...

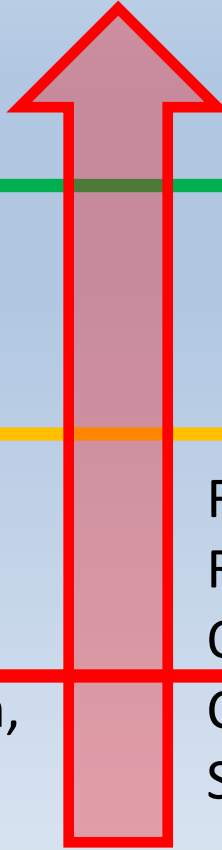
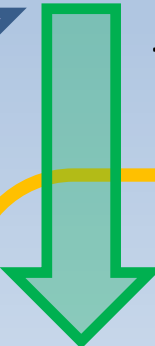
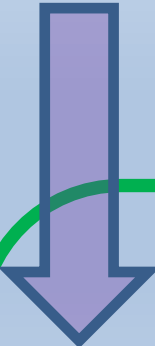
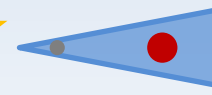
Feedback:  
Radiation,  
Outflow / Jet,  
Chemistry,  
Supernovae, etc.

Circumstellar  
-disk

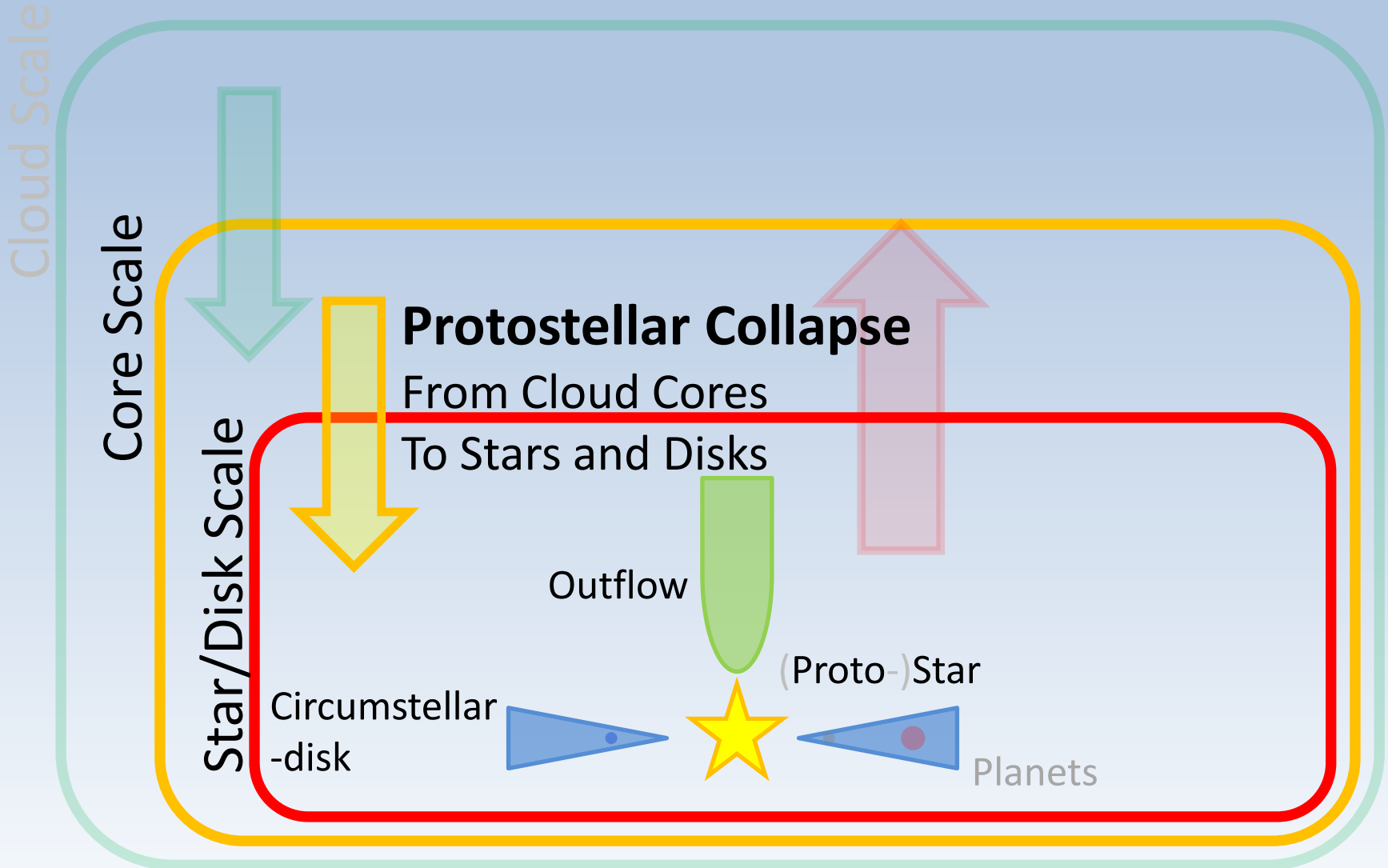
Outflow

(Proto-)Star

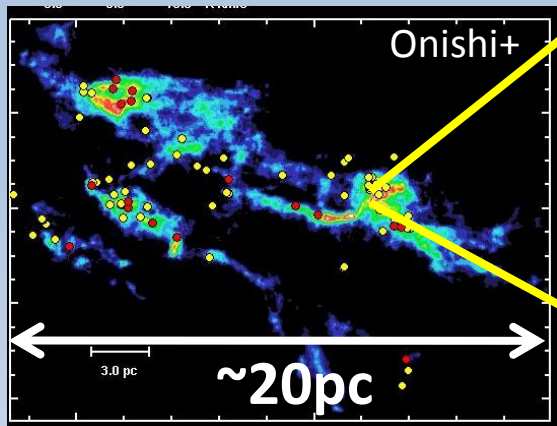
Planets



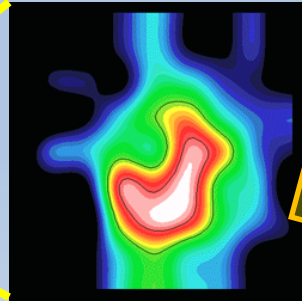
# What this talk covers



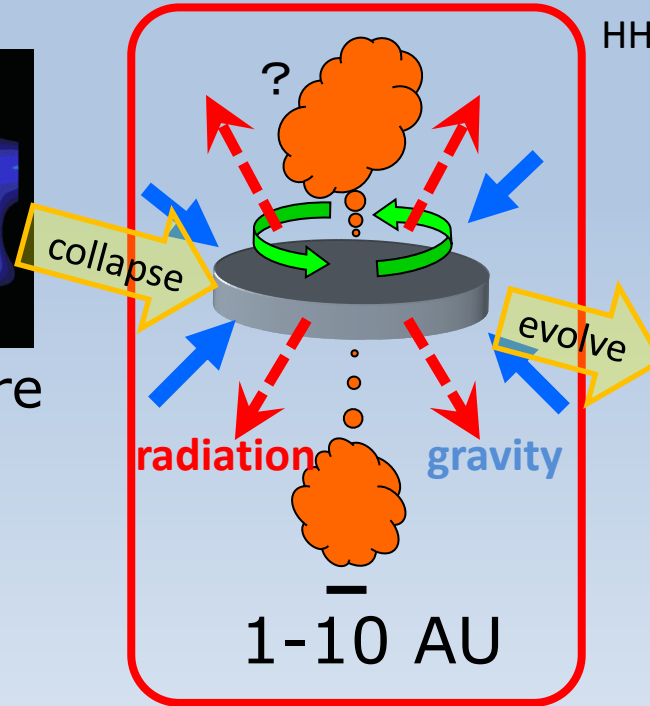
# Protostellar Collapse



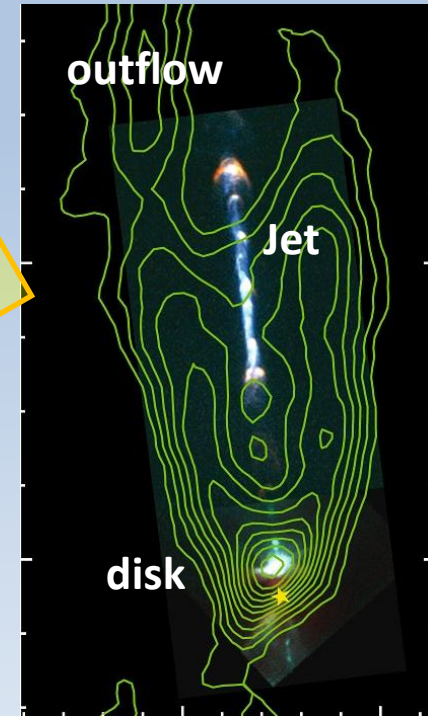
Taurus Molecular Cloud (Nagoya, 4m)



Cloud Core  
~0.1 pc  
 $n \gtrsim 10^4/\text{cc}$



Protostar, Disk, Outflow  
HH111 (Mckee & Ostriker 07)

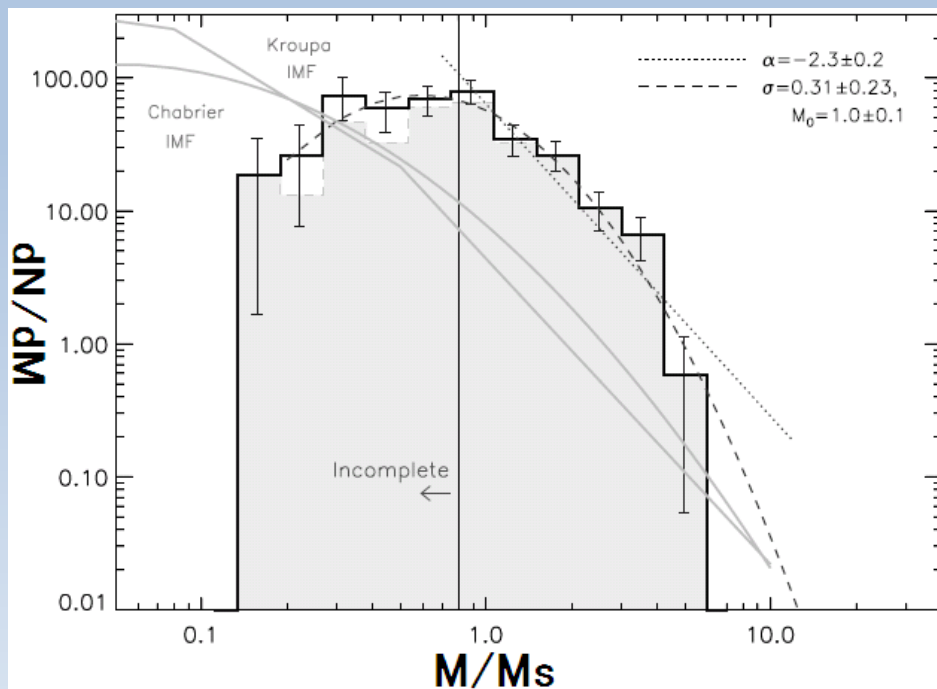


- Many physical processes are involved here: self-gravity, magnetic fields, radiation transfer, turbulence, chemistry, non-ideal MHD effects, etc...
- Huge dynamic range:  $0.1 \text{ pc} / 1 \text{ Rs} \sim 4.5 \times 10^6$   
⇒ Sophisticated numerical simulations are required

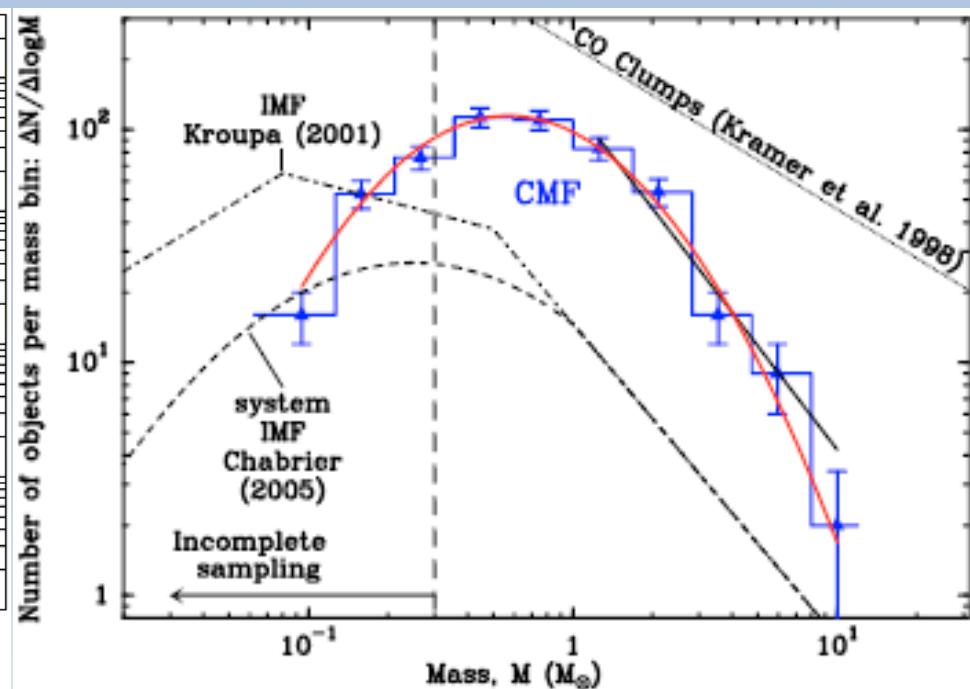
# Why do we care such a small scale?

- Ultimate goal: the origin of the initial mass function
  - Relation between CMF and IMF (?)
    - Star Formation Efficiency (at core scale)
    - Binary / Multiple Formation

# Core and Stellar Mass Functions



(Enoch et al. 2008, Bolocam 1.1mm)



(Andre et al. 2010, Herschel)

Mass Function of Dense Cores looks like the IMF -- with some shift.

- Is there such a simple relation? Is **IMF** imprinted in **CMF**? If so ...
- What is the origin of the CMF?
- What is the origin of the shift, or **efficiency**? How about **binaries**?

To understand this relation, we have to study protostellar collapse.

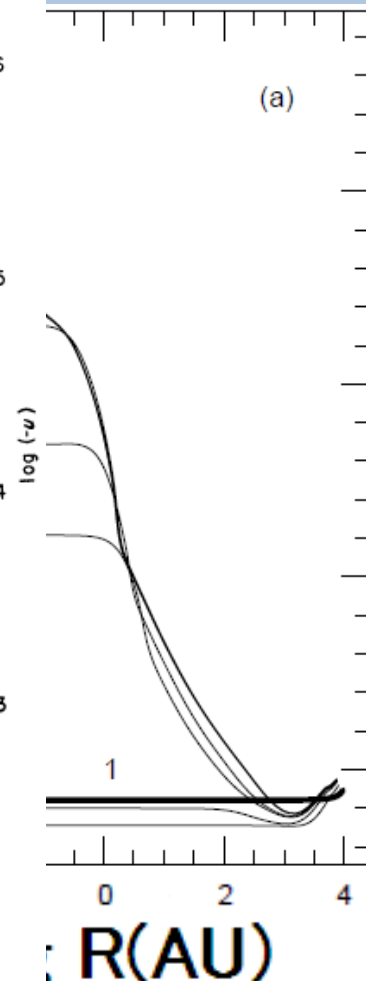
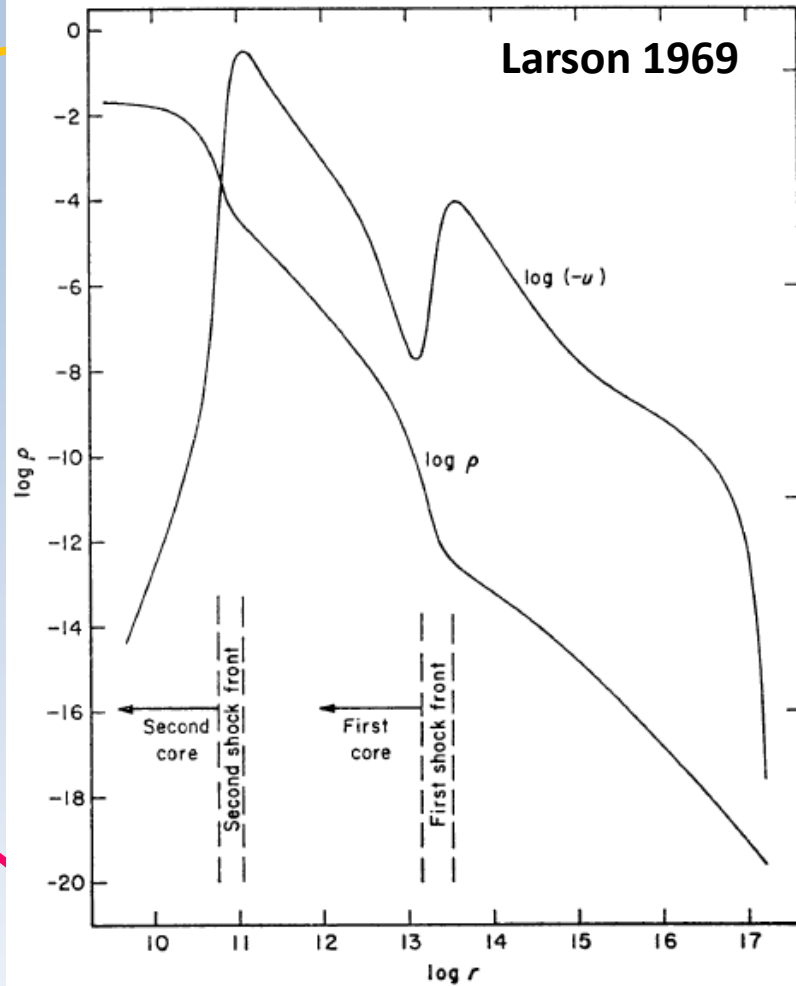
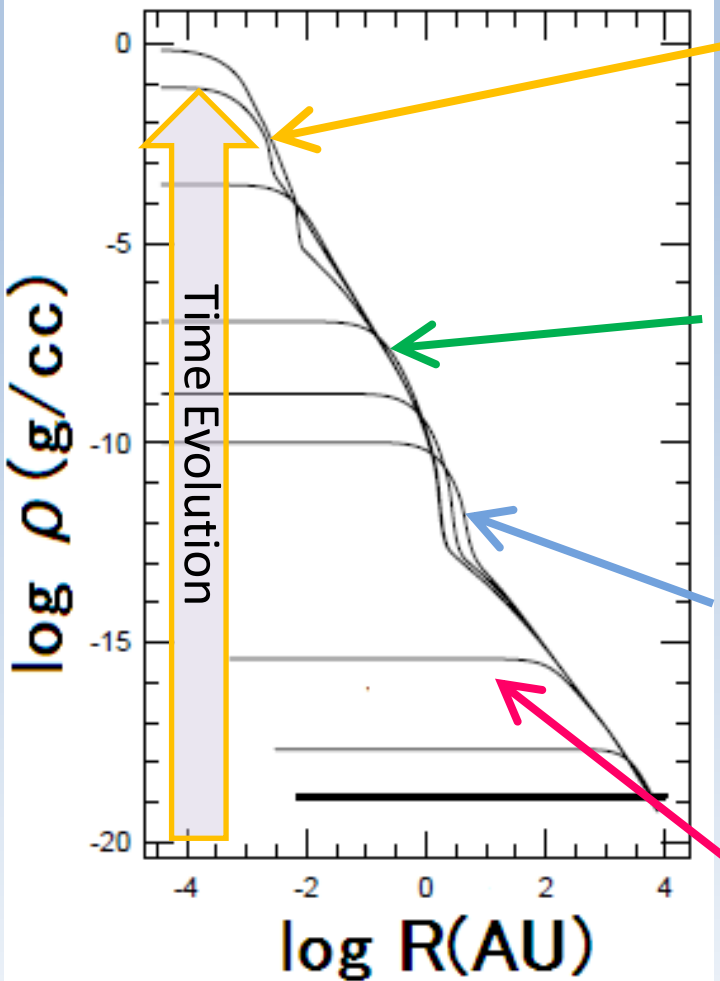


# Why do we care such a small scale?

- Ultimate goal: the origin of the initial mass function
  - Relation between CMF and IMF (?)
    - Star Formation Efficiency (at core scale)
    - Binary / Multiple Formation
- Goal of this talk: the origin of circumstellar disks
  - Angular momentum redistribution
  - Binary / Multiple / Planet Formation
  - Outflow driving
  - Feedback: anisotropic radiation, outflows
    - “Flash light effect” (Yorke & Bodenheimer 1999)
    - Disks can be optically thick without dust (Vaidya+ 2009)
- Significant progress in observations with ALMA
- I have a bad allergy to small particles, like pollen & sink particles 9

# Protostellar Collapse: 1D RHD

Masunaga & Inutsuka 2000



Radiation transfer and chemical reactions control the evolution. This scenario is well established based on 1D RHD simulations.

# “Problems” in Protostellar Collapse

- **Angular Momentum Problem**

Cloud Cores  $j_{cl} \approx 5 \times 10^{21} \left( \frac{R}{0.1 \text{ pc}} \right)^2 \left( \frac{\Omega}{4 \text{ km s}^{-1} \text{ pc}^{-1}} \right) \text{ cm}^2 \text{ s}^{-1} \gg j_* \approx 6 \times 10^{16} \left( \frac{R_*}{2R} \right)^2 \left( \frac{P}{10 \text{ day}} \right)^{-1} \text{ cm}^2 \text{ s}^{-1}$  Stars

→ Efficient angular momentum transport during protostellar collapse  
⇒ Gravitational torque, magnetic braking, outflows

- **Magnetic Flux Problem**

Similarly, magnetic flux in cloud cores  $\gg$  stellar magnetic flux

→ Magnetic fields must dissipate during the collapse  
⇒ Ohmic dissipation, ambipolar diffusion, (Hall effect), turbulence

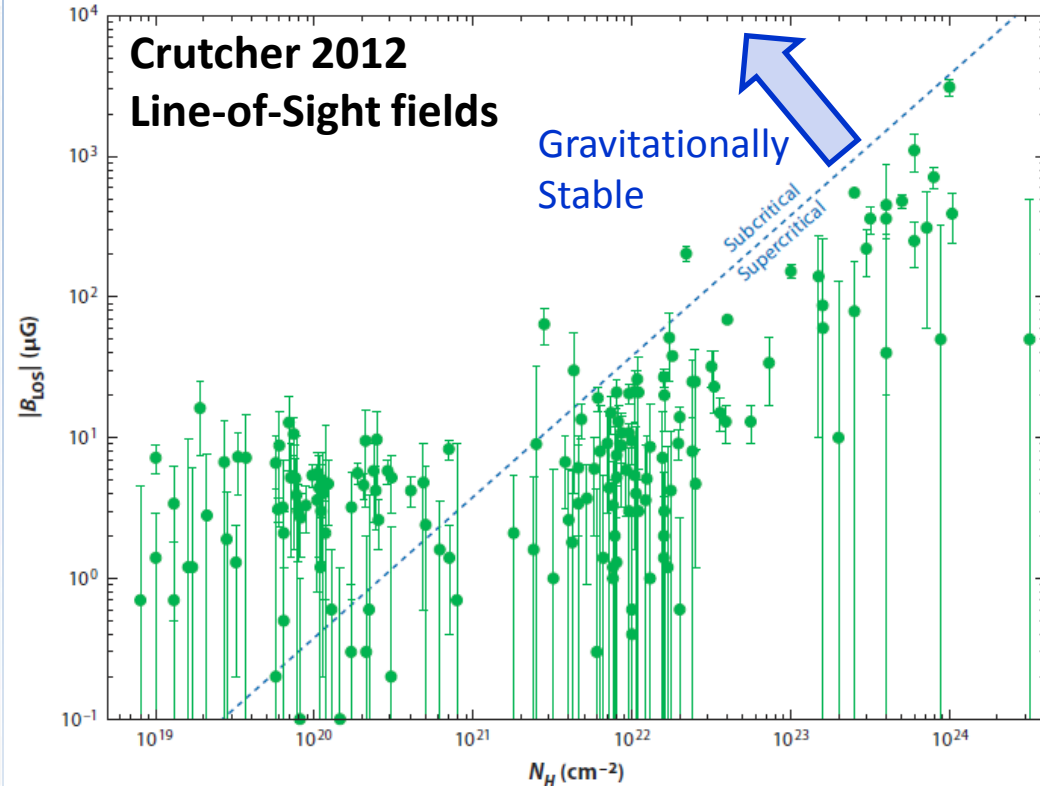
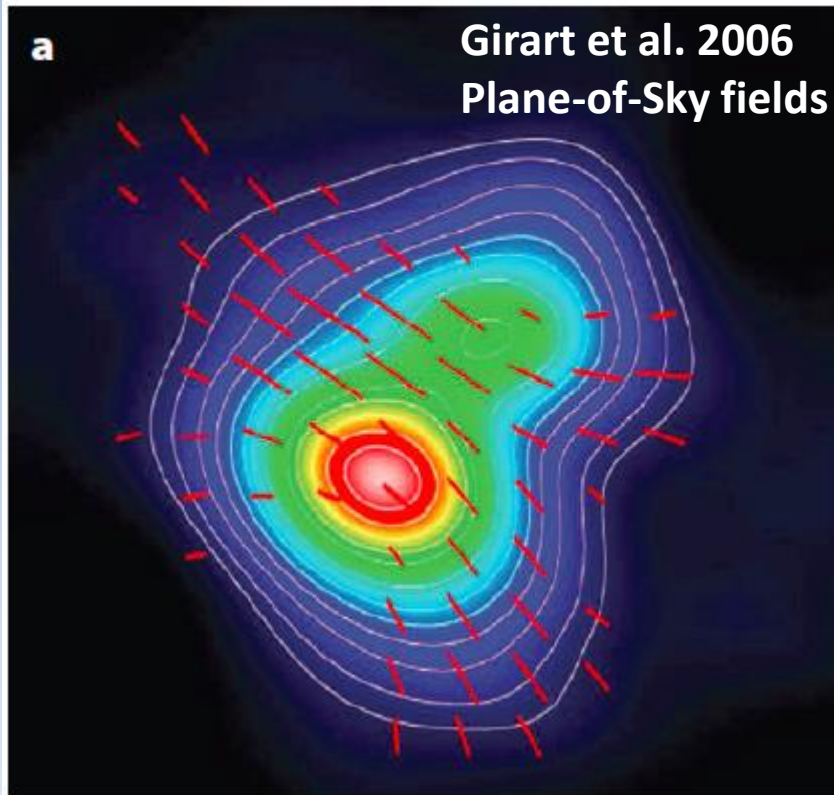
- **“Magnetic Braking Catastrophe”** (Mellon & Li 2008,09, Li+ 2011, etc.)

Magnetic braking is too efficient; no circumstellar disk is formed

⇒ Long-term accretion, non-ideal MHD effects, turbulence

⇒ Realistic **3D simulations with many physical processes**

# Magnetic Fields



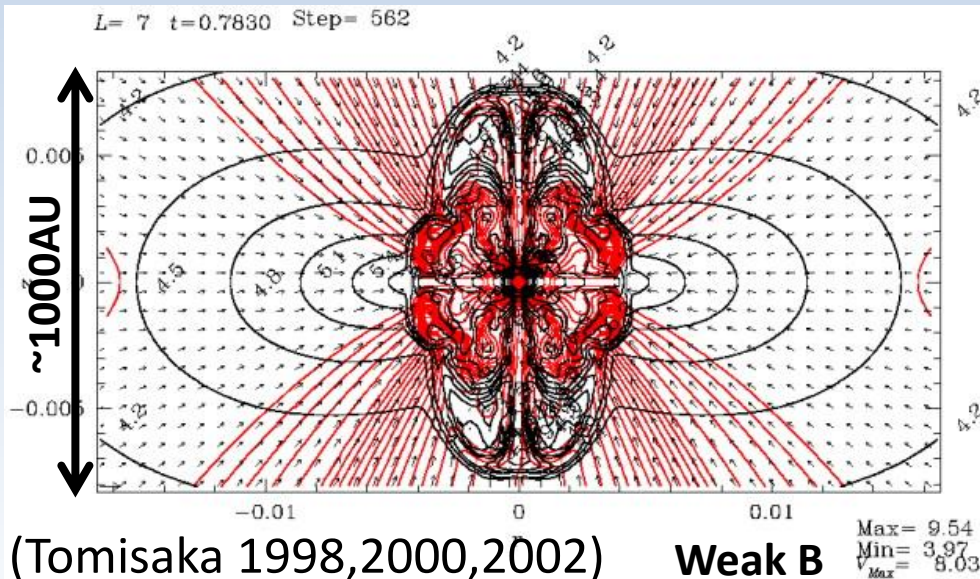
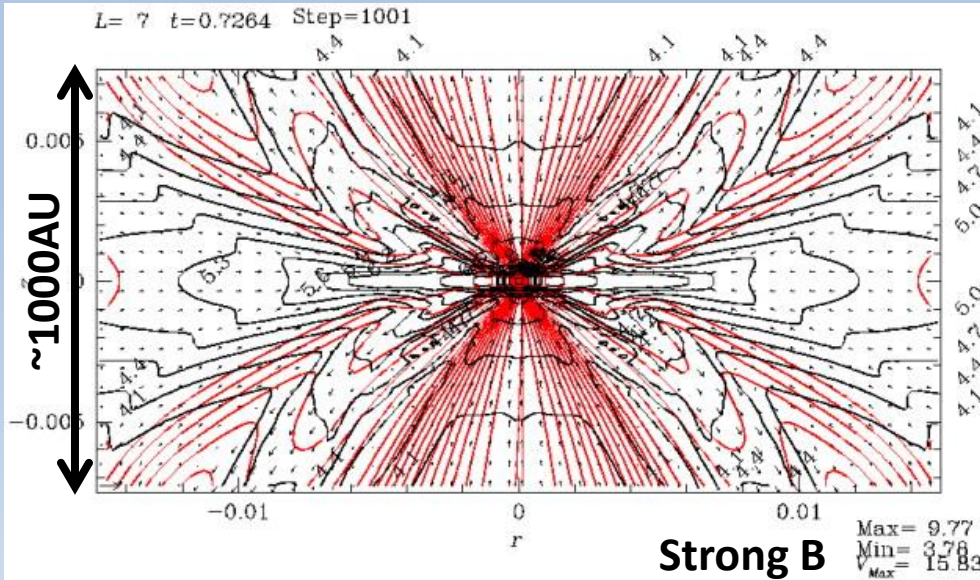
Observations suggest that cloud cores are considerably (supercritical to marginally subcritical) magnetized ( $\mu \sim 2-10$ ). Therefore magnetic fields must have significant effects, actually even in the supercritical regime.

**NOTE:** these observations are difficult and can have large uncertainties.

# Magnetic Braking and Outflows

As a result of interaction between magnetic fields and rotation, bipolar outflows are launched from the collapsing cloud. Those outflows and **magnetic braking** transport angular momentum very efficiently.

Two modes of outflows:  
Strong fields result in Magneto-centrifugal mode (Blandford & Payne 1982), while weak fields drive magnetic-pressure mode.  
(see also, Mouschovias, & Paleologou 1979, 80, Kudoh et al. 1998, etc.)

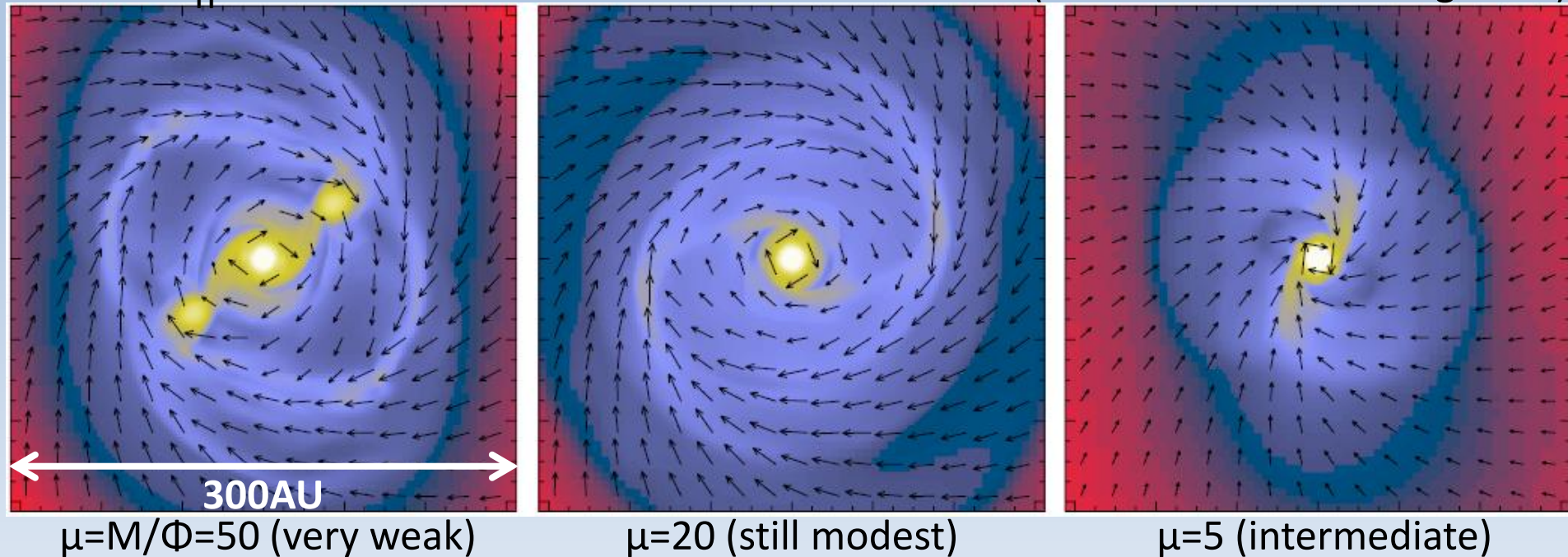




# Magnetic Braking Catastrophe and/or Fragmentation Crisis

$t \sim 1.2 t_{\text{ff}}$

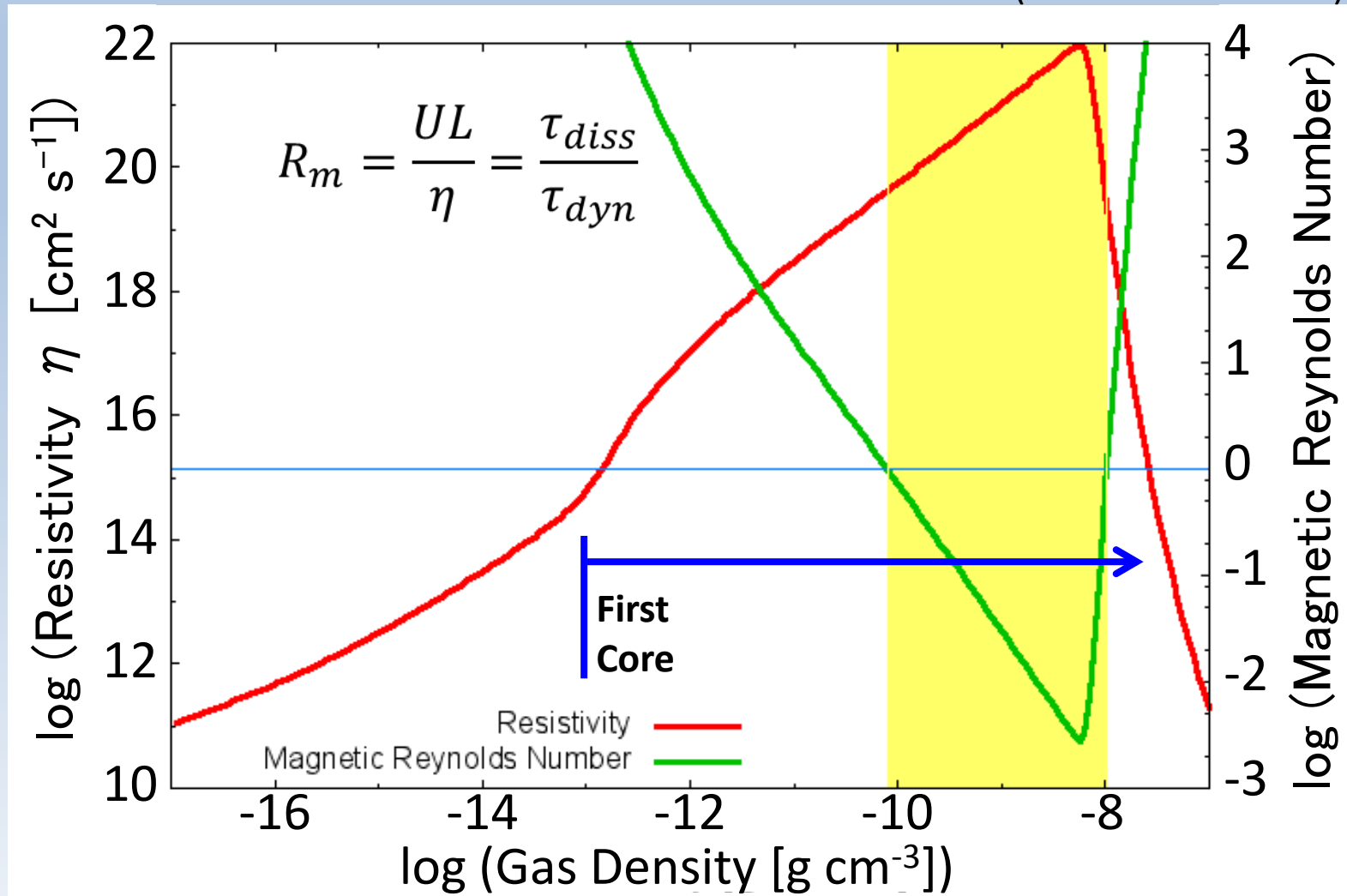
(Hennebelle & Fromang 2008)



Magnetic fields actually transport angular momentum **“too efficiently”**. Circumstellar disks are not formed, fragmentation is strongly suppressed. This is a serious problem: Binary rate is known to be high (M: >30% G : >50%, A: ~80%), and we know lots of circumstellar disks and planets exist. (see also, Mestel & Spitzer **1956**, Mellon & Li 08, 09, Li et al. 11, Hennebelle & Ciardi 09, etc.)

# Non-Ideal MHD effects

(Tomida et al. 2013)



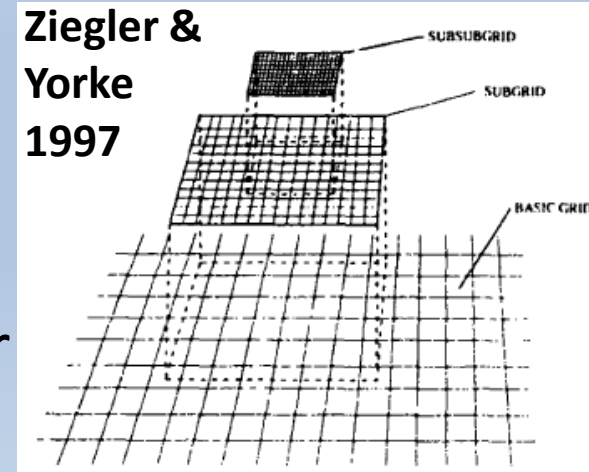
Ohmic resistivity with  $\xi=10^{-17} \text{ s}^{-1}$  (neglecting Cosmic Ray shielding)  
Significant flux loss occurs in the first core. (cf. Kunz & Mouschovias 09, 10)

# **RMHD Simulations of Protostellar Collapse**



# ngr<sup>3</sup>mhd code

- Huge dynamic range: 3D nested-grids
  - MHD → HLLD (Miyoshi & Kusano 2005)  
(+ Carbuncle care → shock detection + HLLD-)
  - ✓ Fast, robust and as accurate as Roe's solver
  - ✓ Independent from the details of EOS
  - $\text{div } \mathbf{B}=0$  constraint → Hyperbolic cleaning (Dedner+ 2002)
  - Self-gravity → Multigrid (Matsumoto & Hanawa 2003)
  - Radiation → Gray Flux Limited Diffusion (Levermore & Pomraning 1981)  
+ Implicit (BiCGStab + ILU decomposition (0) preconditioner)
  - EOS including chemical reactions ( $\text{H}_2$ ,  $\text{H}$ ,  $\text{H}^+$ ,  $\text{He}$ ,  $\text{He}^+$ ,  $\text{He}^{2+}$  and  $\text{e}^-$ )
  - Ohmic dissipation → Super Time Stepping (Alexiades+ 1996)
  - (preliminary!) Ambipolar Diffusion with STS
  - OD & AD tables are derived using a chemical network with dusts
- ⇒ **The latest version of Larson's protostellar collapse simulation.**



# Basic Equations (w/o div **B** cleaning)

$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \mathbf{v}) = 0,$$

Mass Conservation

$$\frac{\partial \rho \mathbf{v}}{\partial t} + \nabla \cdot \left[ \rho \mathbf{v} \otimes \mathbf{v} + \left( p + \frac{1}{2} |\mathbf{B}|^2 \right) \mathbb{I} - \mathbf{B} \otimes \mathbf{B} \right] = -\rho \nabla \Phi + \frac{\sigma_R}{c} \mathbf{F}_r,$$

Eq. of motion

$$\frac{\partial \mathbf{B}}{\partial t} - \nabla \times (\mathbf{v} \times \mathbf{B} - \eta \nabla \times \mathbf{B}) = 0,$$

Induction eq.

$$\nabla \cdot \mathbf{B} = 0,$$

div B=0

$$\frac{\partial e}{\partial t} + \nabla \cdot \left[ \left( e + p + \frac{1}{2} |\mathbf{B}|^2 \right) \mathbf{v} - \mathbf{B} (\mathbf{v} \cdot \mathbf{B}) - \eta \mathbf{B} \times (\nabla \times \mathbf{B}) \right] =$$

Gas Energy Eq.

$$-\rho \mathbf{v} \cdot \nabla \Phi - c \sigma_P (aT^4 - E_r) + \frac{\sigma_R}{c} \mathbf{F}_r \cdot \mathbf{u},$$

$$\nabla^2 \Phi = 4\pi G \rho,$$

Poisson's Eq.

$$\frac{\partial E_r}{\partial t} + \nabla \cdot [\mathbf{u} E_r] + \nabla \cdot \mathbf{F}_r + \mathbb{P}_r : \nabla \mathbf{u} = c \sigma_P (a_r T_g^4 - E_r),$$

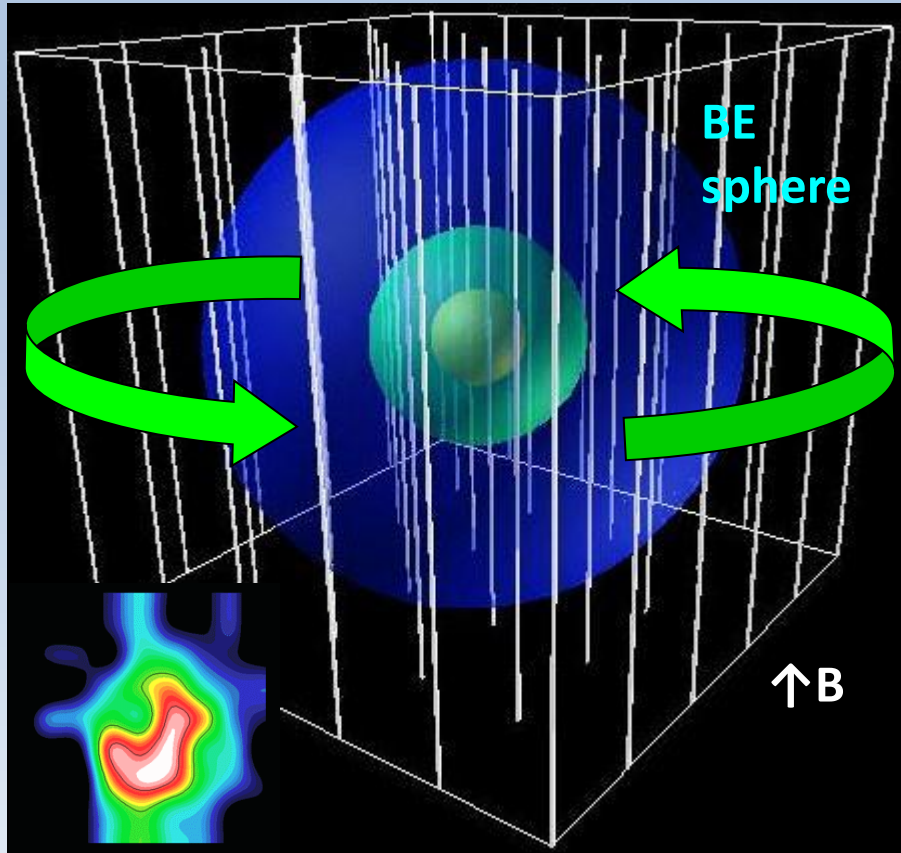
Radiation Transfer

$$\mathbf{F}_r = \frac{c \lambda}{\sigma_R} \nabla E_r, \quad \lambda(R) = \frac{2 + R}{6 + 2R + R^2}, \quad R = \frac{|\nabla E_r|}{\sigma_R E_r},$$

+ Eq. of state

$$\mathbb{P}_r = \mathbb{D} E_r, \quad \mathbb{D} = \frac{1 - \chi}{2} \mathbb{I} + \frac{3\chi - 1}{2} \mathbf{n} \otimes \mathbf{n}, \quad \chi = \lambda + \lambda^2 R^2, \quad \mathbf{n} = \frac{\nabla E_r}{|\nabla E_r|}.$$

# Simulation Setup



Two rotating models:

- Ideal MHD model
- Resistive MHD model

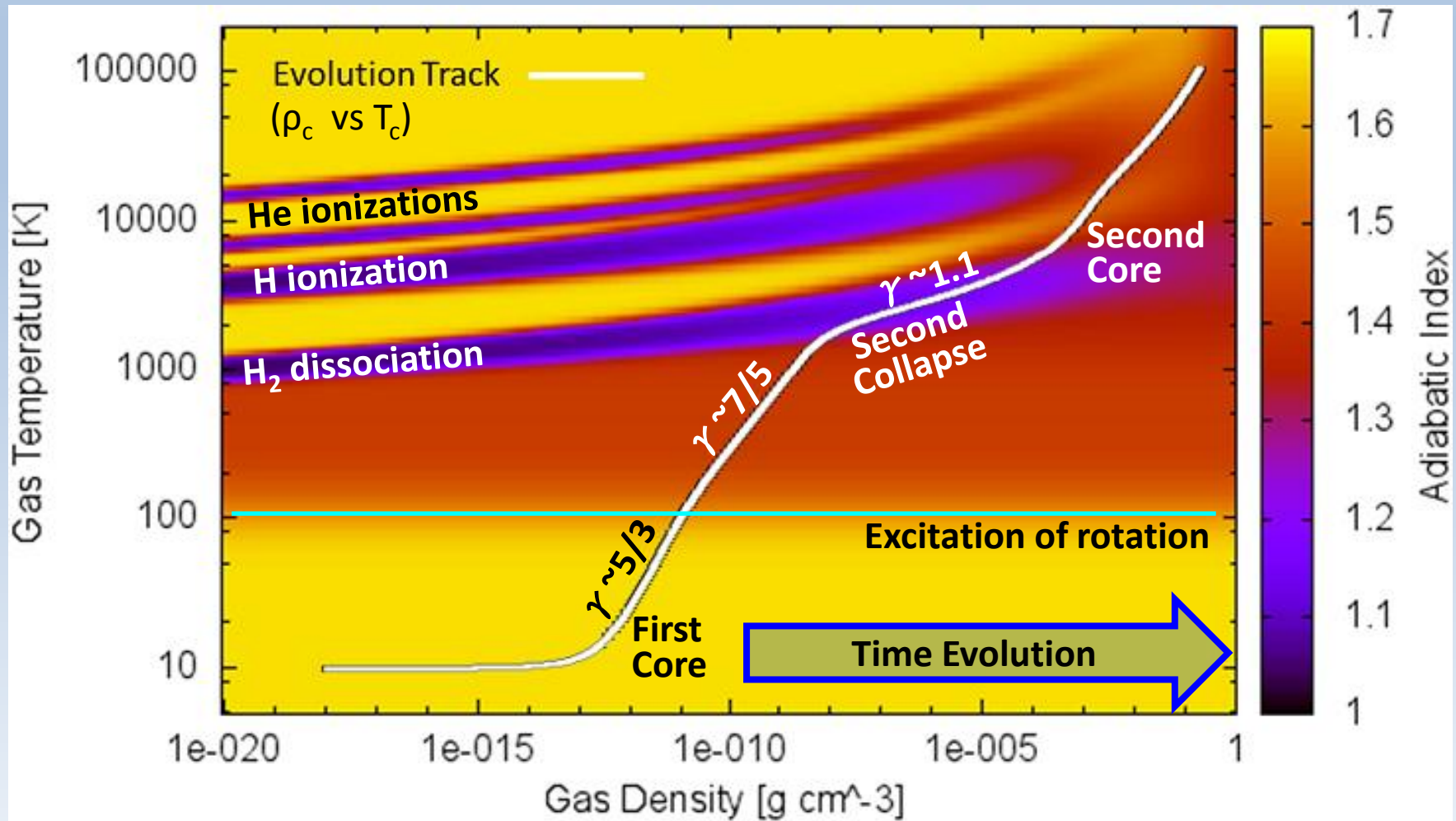
$64^3 \times 23$  levels, 16 cells /  $\lambda_{\text{Jeans}}$   
 $\min(\Delta x) \sim 6.6 \times 10^{-5} \text{AU} \sim 0.014 R_s$

End of simulations:  $T_c \sim 10^5 \text{K}$ ,  
 $\sim 1 \text{yr}$  after 2nd core formation

**Huge dynamic range  $> 10^8$  !**

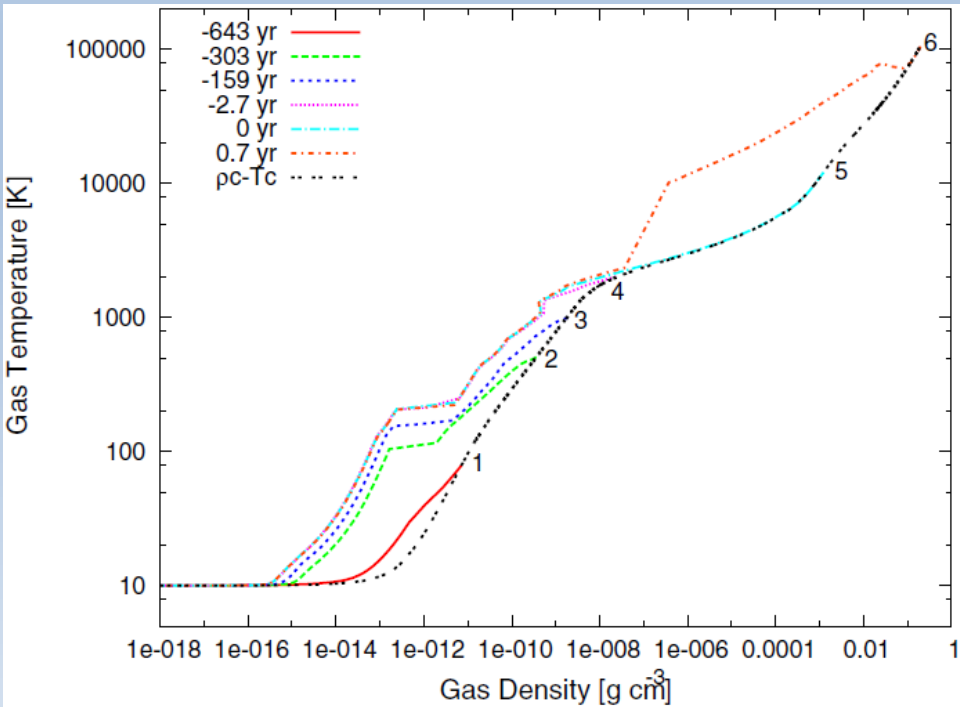
- 1 Ms unstabilized BE sphere ( $\rho_c = 1.2 \times 10^{-18} \text{g/cc}$ ,  $T = 10 \text{K}$ ,  $R = 8800 \text{AU}$ )
- $B_z = 20 \mu\text{G}$  ( $\mu \sim 3.8$ ),  $\Omega = 0.046/t_{\text{ff}} \sim 2.4 \times 10^{-14} \text{s}^{-1}$ , aligned rotator
- 10%  $m=2$  density perturbation
- Opacity: Semenov+ 2003 (dust), Ferguson+ 2005, Seaton+ 1994 (OP)

# Thermal Evolution

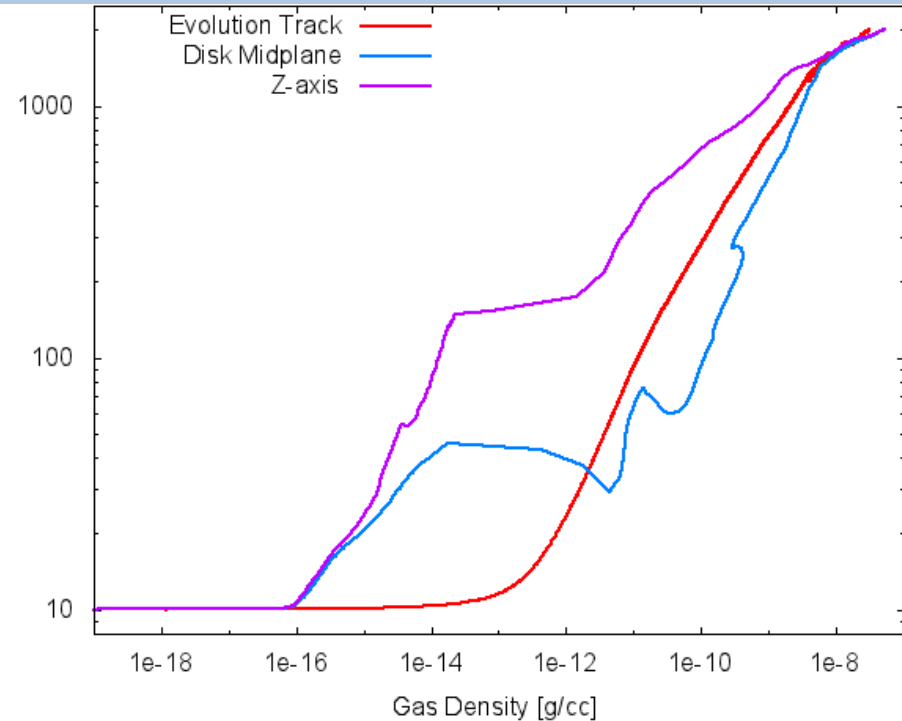


The central gas element evolves following EOS in  $\rho > 10^{-12}$  g /cc. The evolution is consistent with MI2000, except for details of EOS.

# Importance of Radiation (M)HD



**Spherical Model**

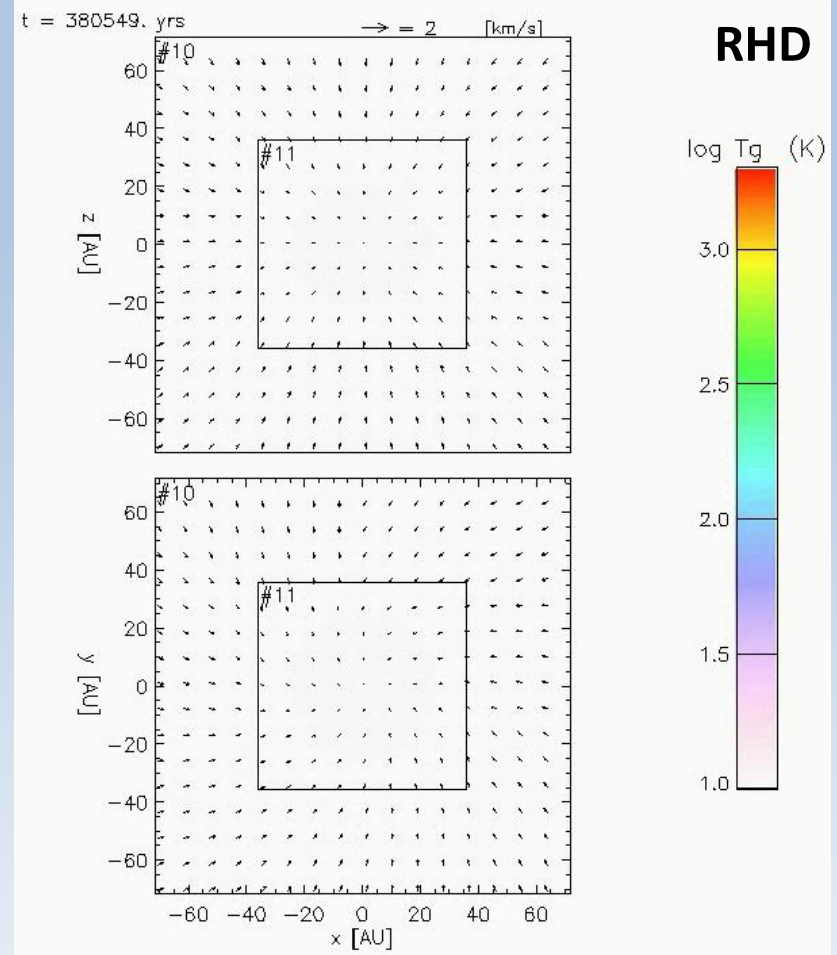
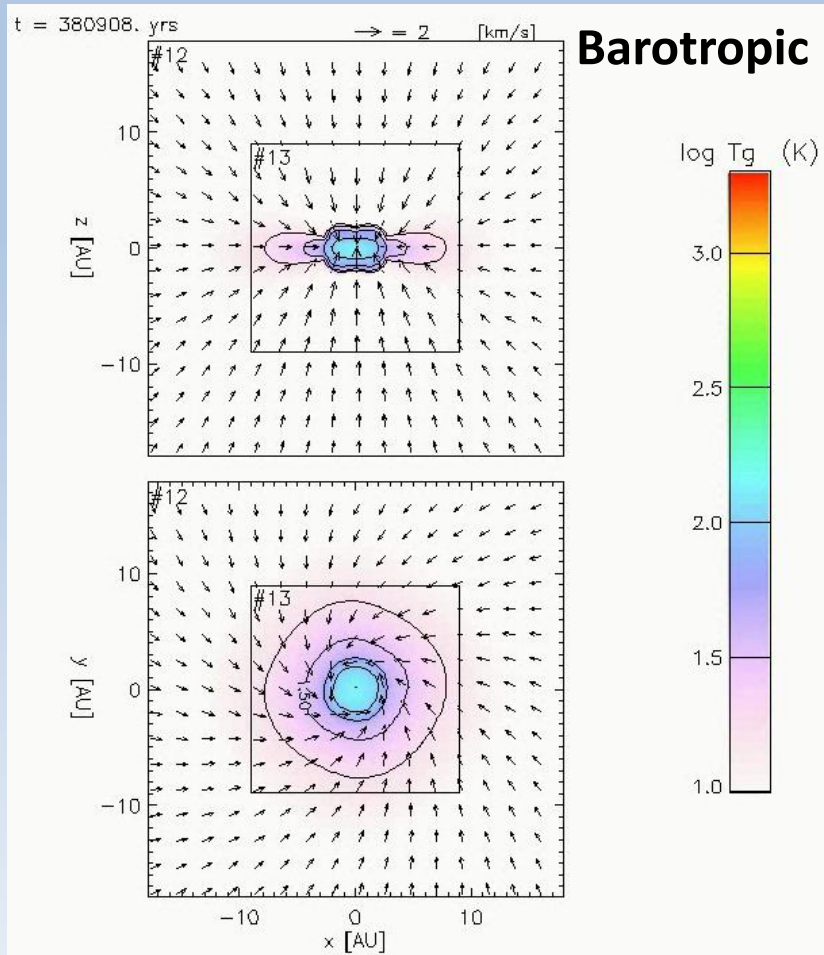


**Non-magnetized Rotating Model**

- Barotropic approximation can under/overestimate the temperature.
- Non/weakly rotating cases: the temperature tend to be underestimated because shock and radiation heating are neglected.
  - More complicated in rotationally-supported disks
- $\sim x5$  difference in  $T \Rightarrow x10$  difference in Jeans Mass, and stability



# RHD Sims with Gray FLD Approx.



Thicker disks, spiral arms, larger first core mean that RHD is more stable. This also has a significant impact on prediction for observations.

(see, Offner et al. 09, Commerçon et al. 10, 11, Tomida et al. 10a,b, Bate 10, 11, etc.)

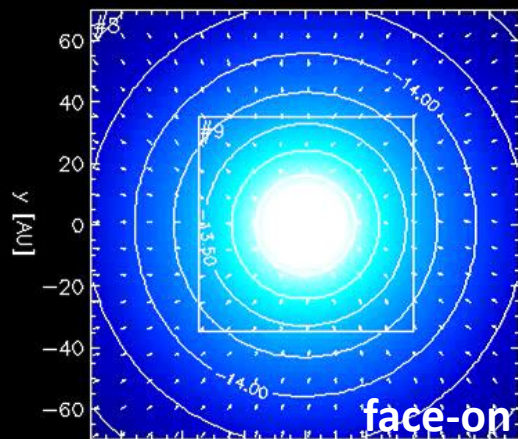
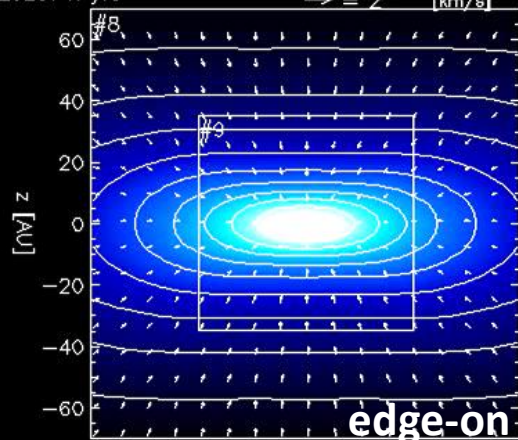
# Outflows

## Density cross section

t = 202574. yrs

→ = 2 [km/s]

log rho (g/cc)

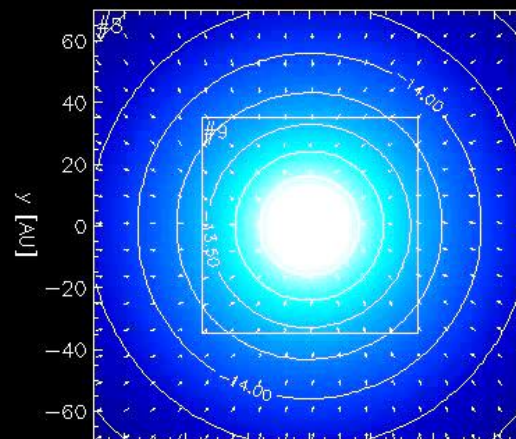
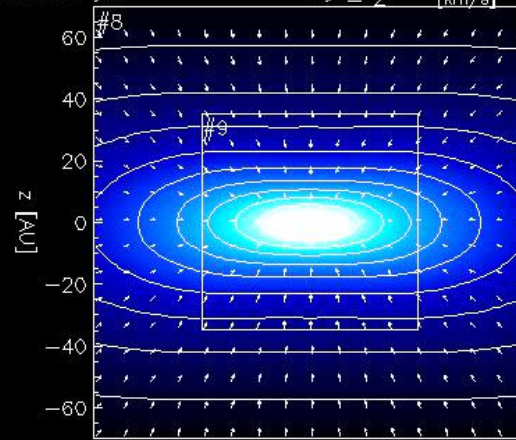


Ideal MHD

t = 202582. yrs

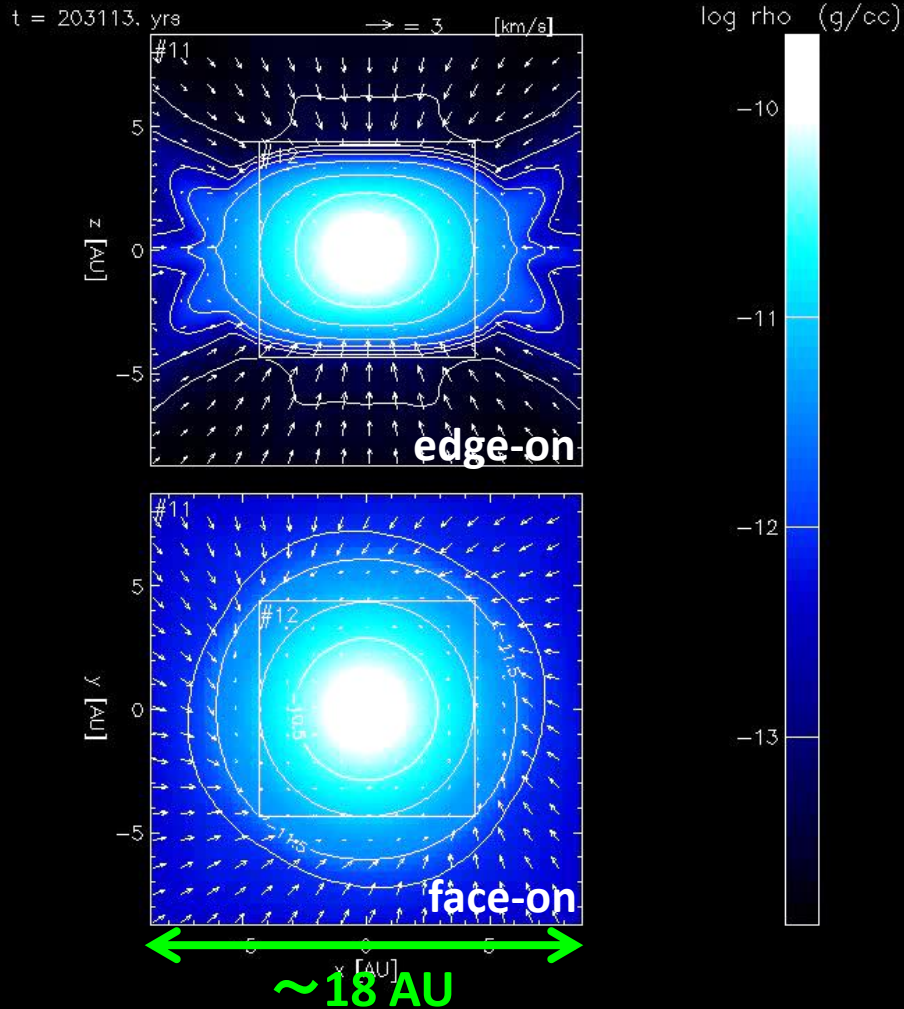
→ = 2 [km/s]

log rho (g/cc)

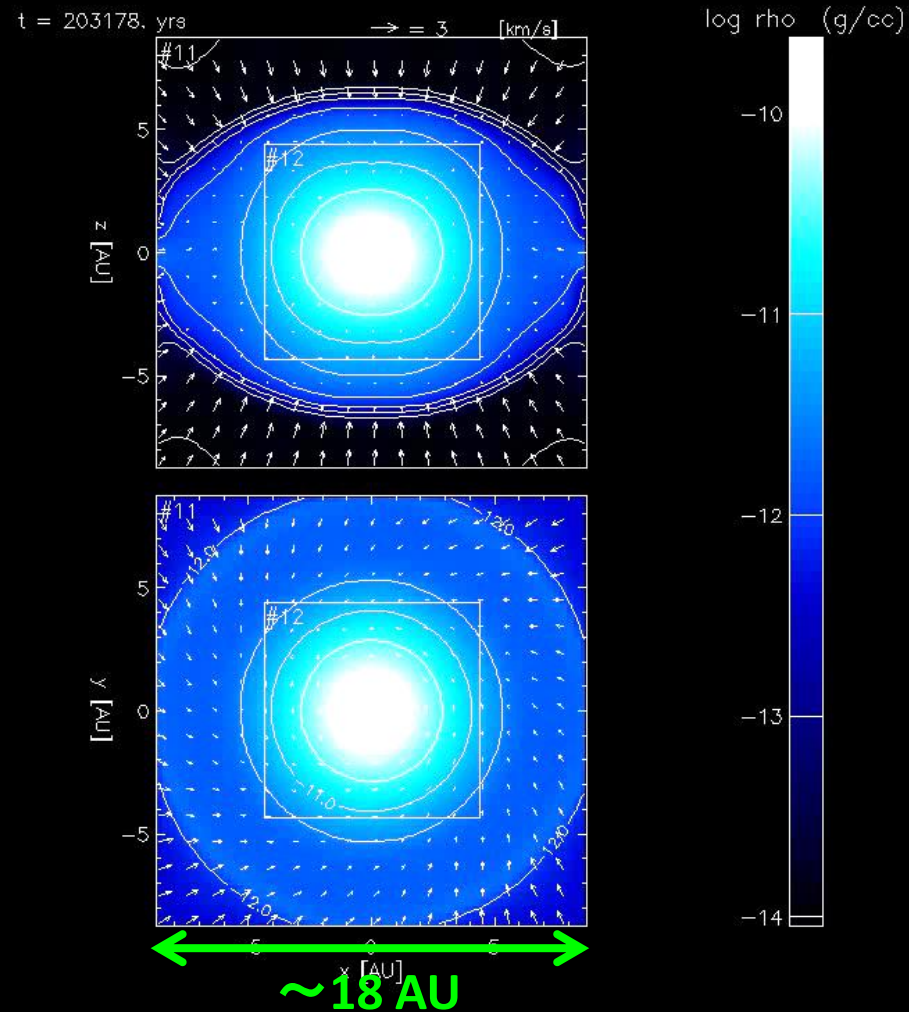


Resistive MHD

# First Cores



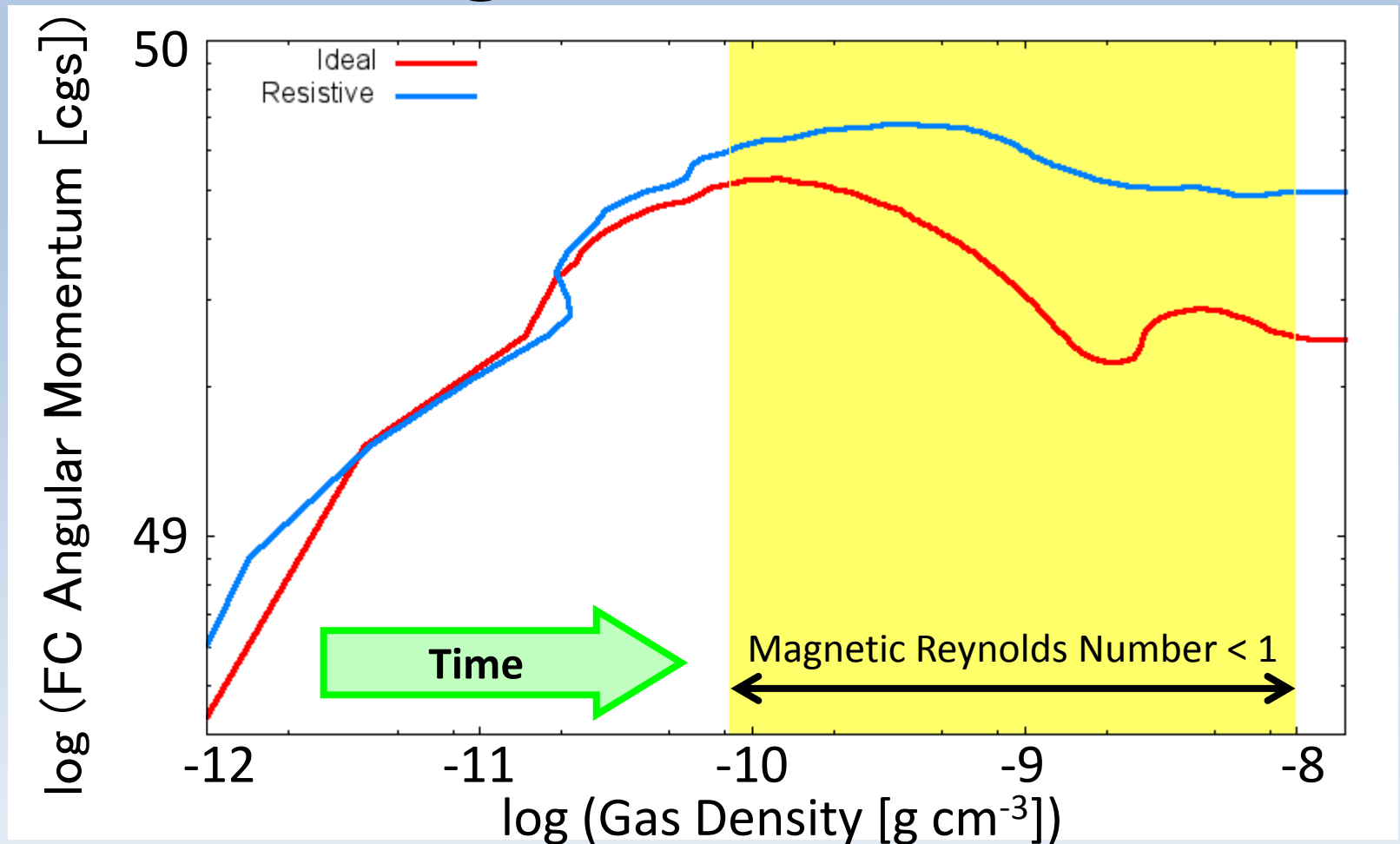
Ideal MHD



Resistive MHD



# First Core Angular Momentum

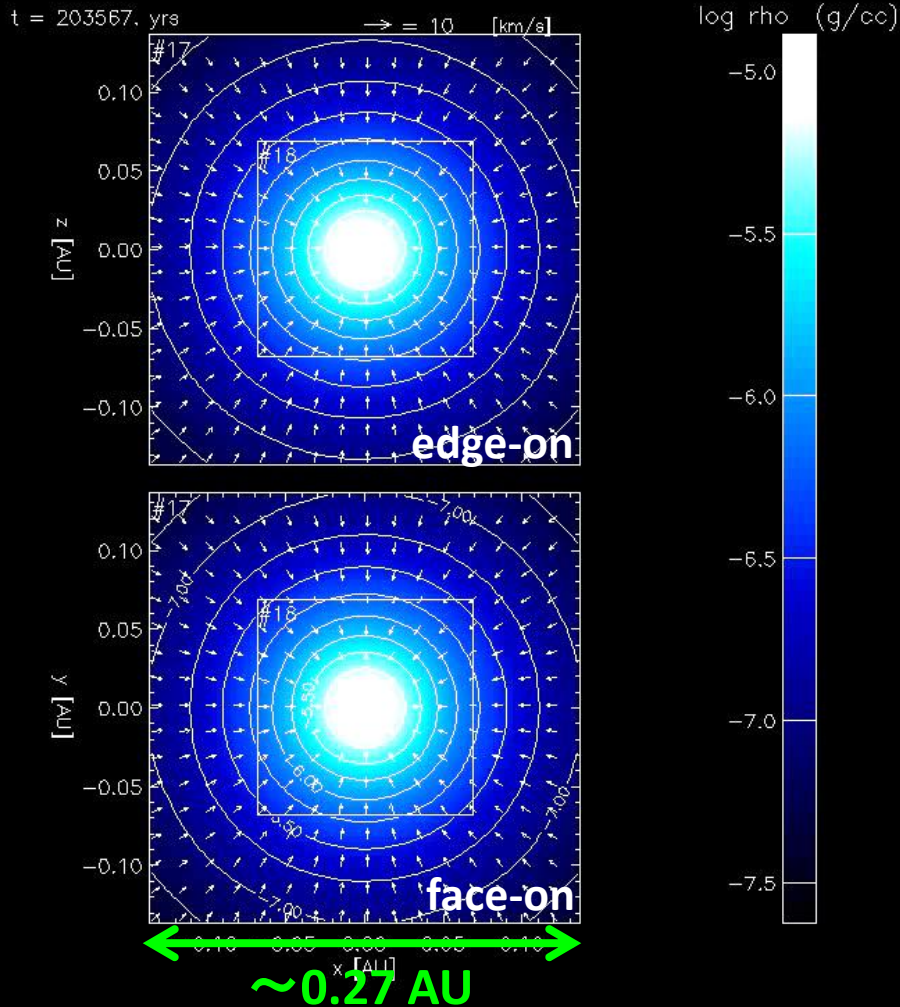


Angular momentum transport is suppressed when resistivity works.

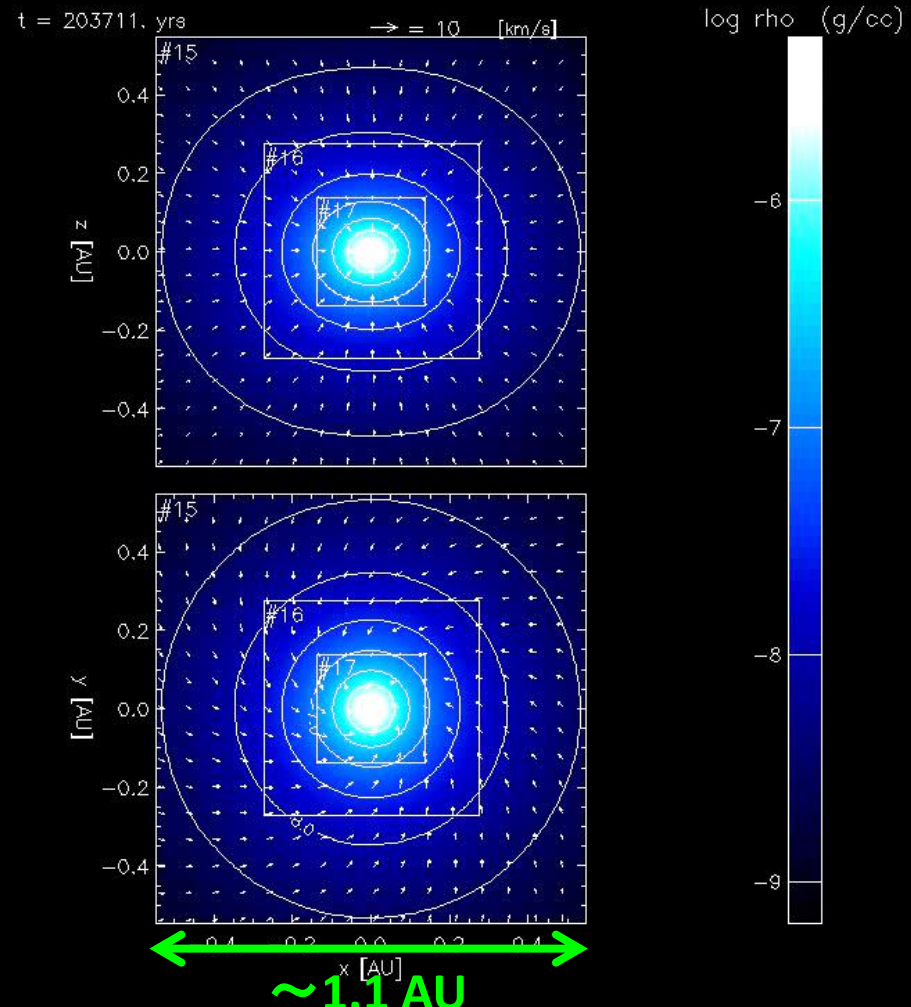
Twice larger angular momentum in FC (more significant in PC)

Longer lifetime due to rotational support: Ideal 800yrs  $\rightarrow$  Resistive 950yrs<sub>5</sub>

# Protostellar Cores, Disk and Jet



Ideal MHD



Resistive MHD

# Protostellar Cores

Radii, Masses, Angular momenta  $\Rightarrow$

PCs acquire  $\sim 0.02 M_{\odot}$  in  $\sim 1$  yr

Ideal MHD model = virtually spherical

$\leftarrow$  very low angular momentum

Circumstellar disk is not formed

**“Magnetic Braking Catastrophe”**

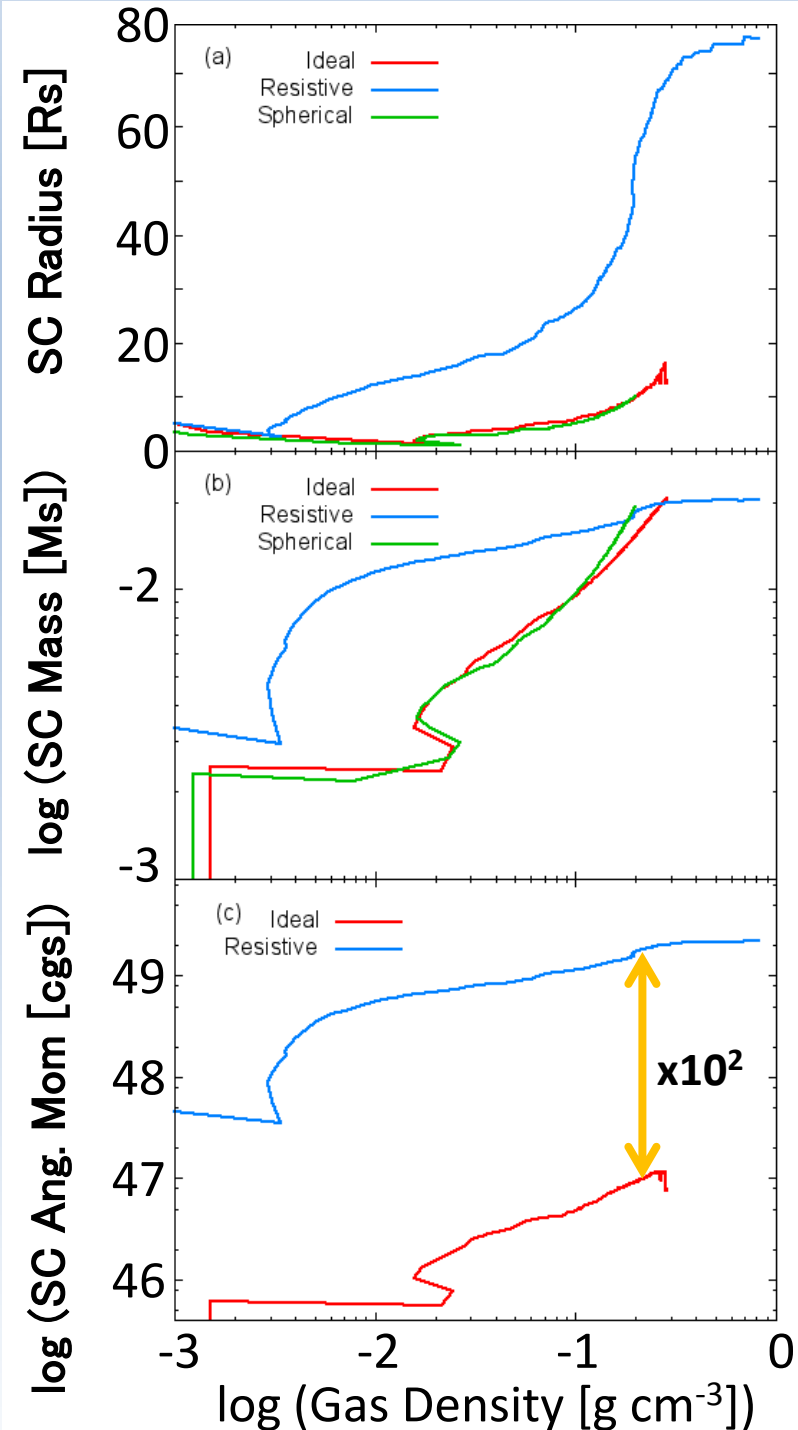
Resistive MHD: large ang. momentum

$\rightarrow$  rotationally supported disk is formed

$R_{\text{disk}} \sim 0.3$  AU at the end of simulation

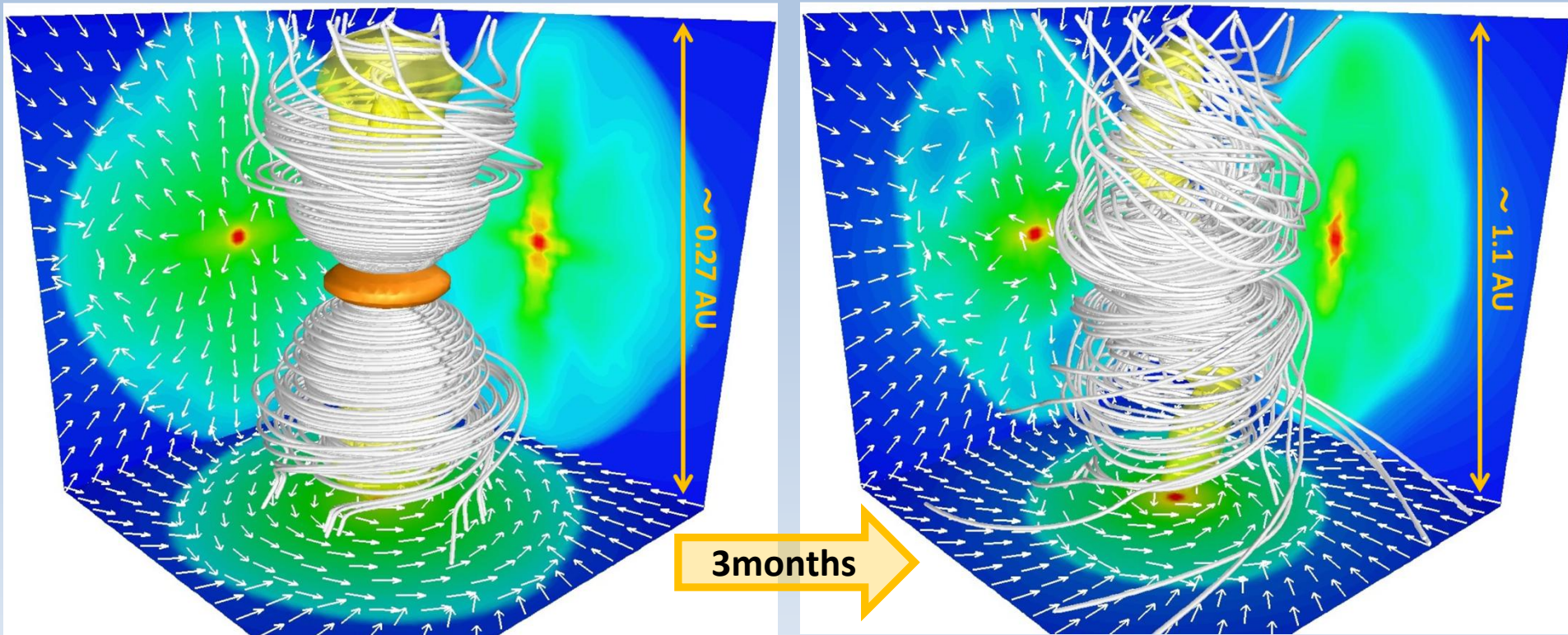
It will continuously grow via accretion

$\Rightarrow$  **NO Magnetic Braking Catastrophe**



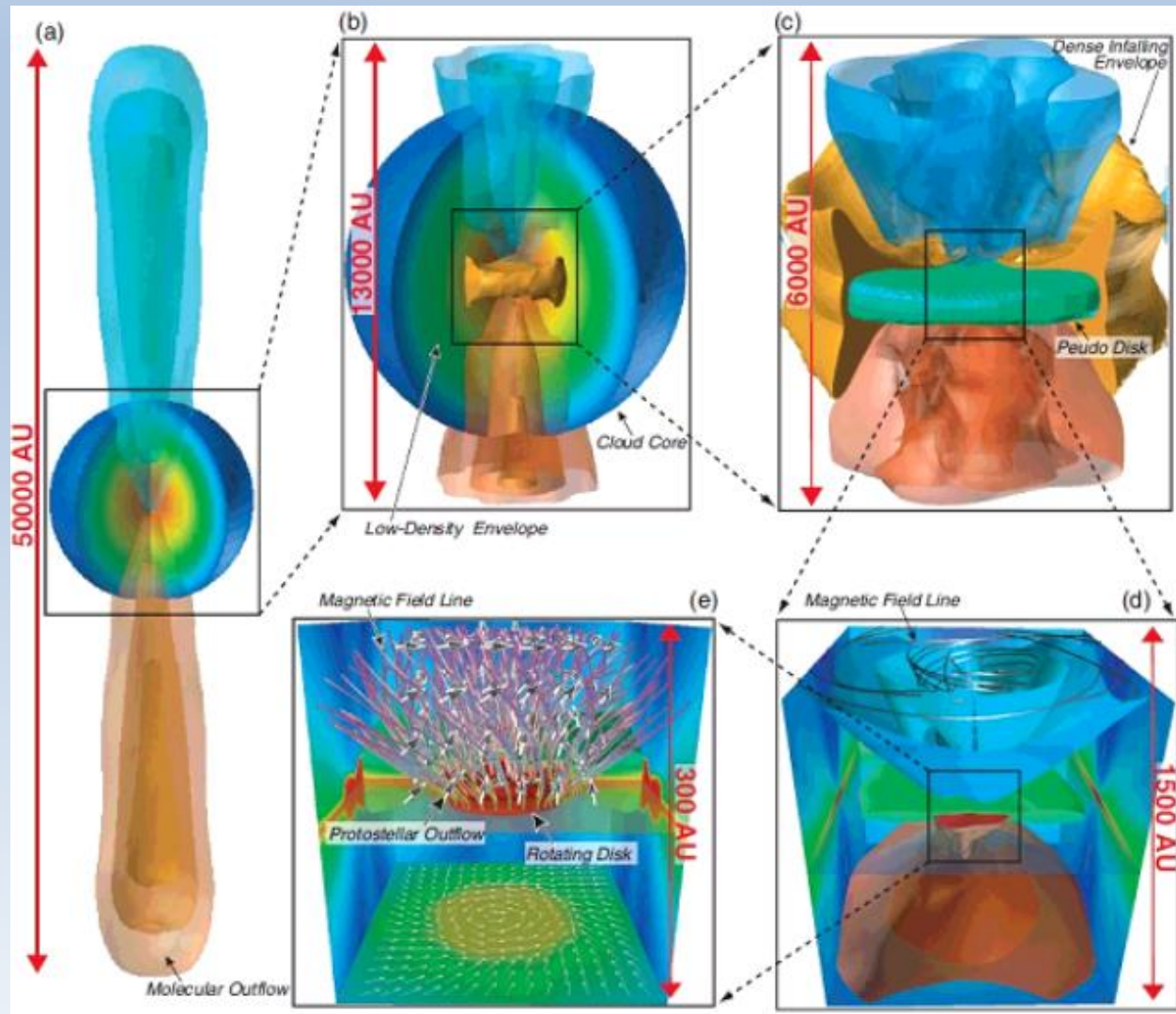


# Fast outflow from protostellar core



Toroidal fields are rapidly amplified by rotation in resistive case.  
→ Fast outflow ( $\gtrsim 15\text{km/s}$ ) is driven by magnetic pressure  
Consistent w/ previous MHD sims (Machida et al. 08 etc.)  
The magnetic tower is disturbed by the kink instability.

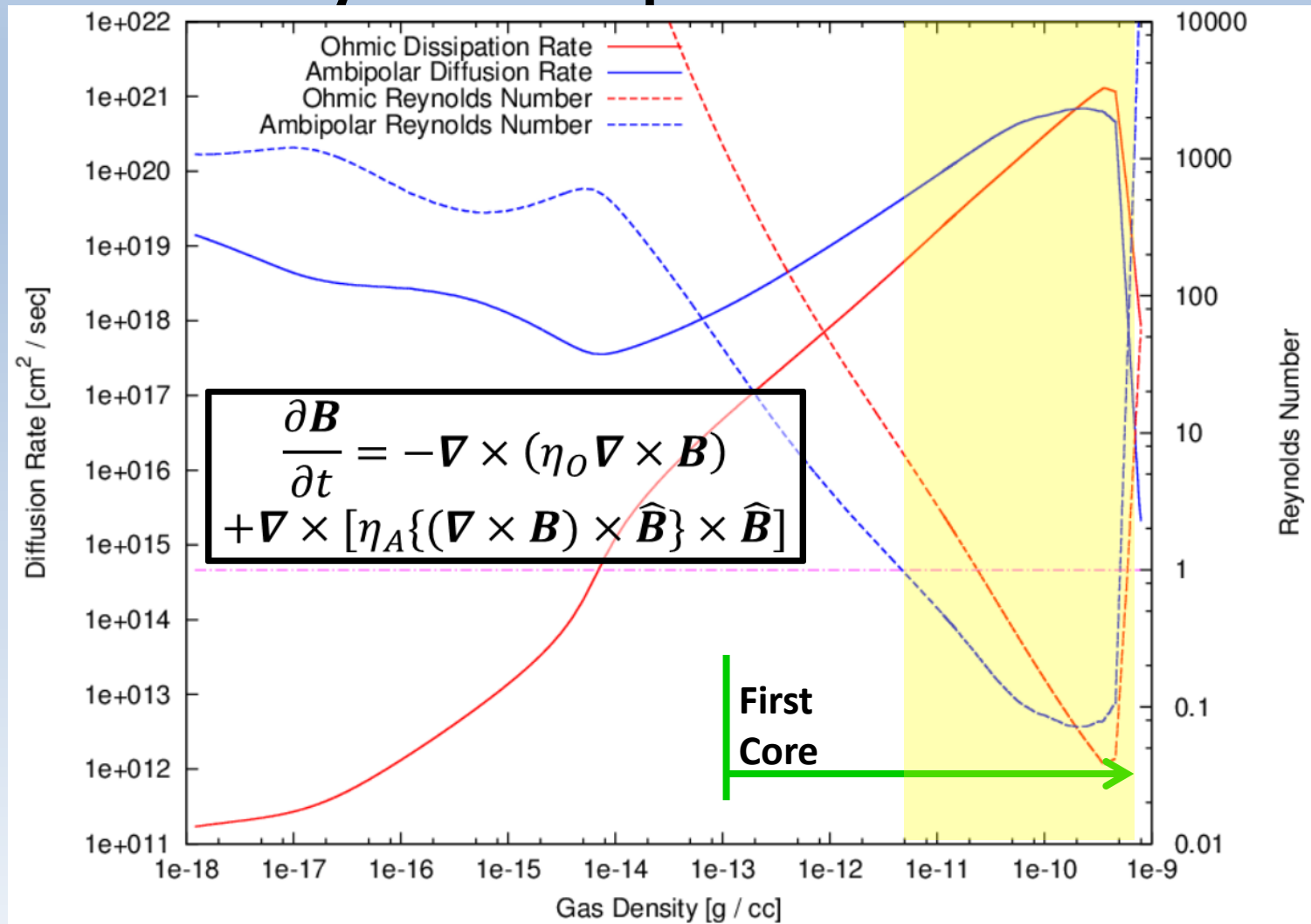
# Fate of the disk and outflows



Machida & Hosokawa 13  
(they are not allergic.)

Long-term (till class-I phase) MHD simulation using a sink particle. Outflows and disks grow continuously,  $R_{\text{disk}} \sim 100 \text{ AU}$

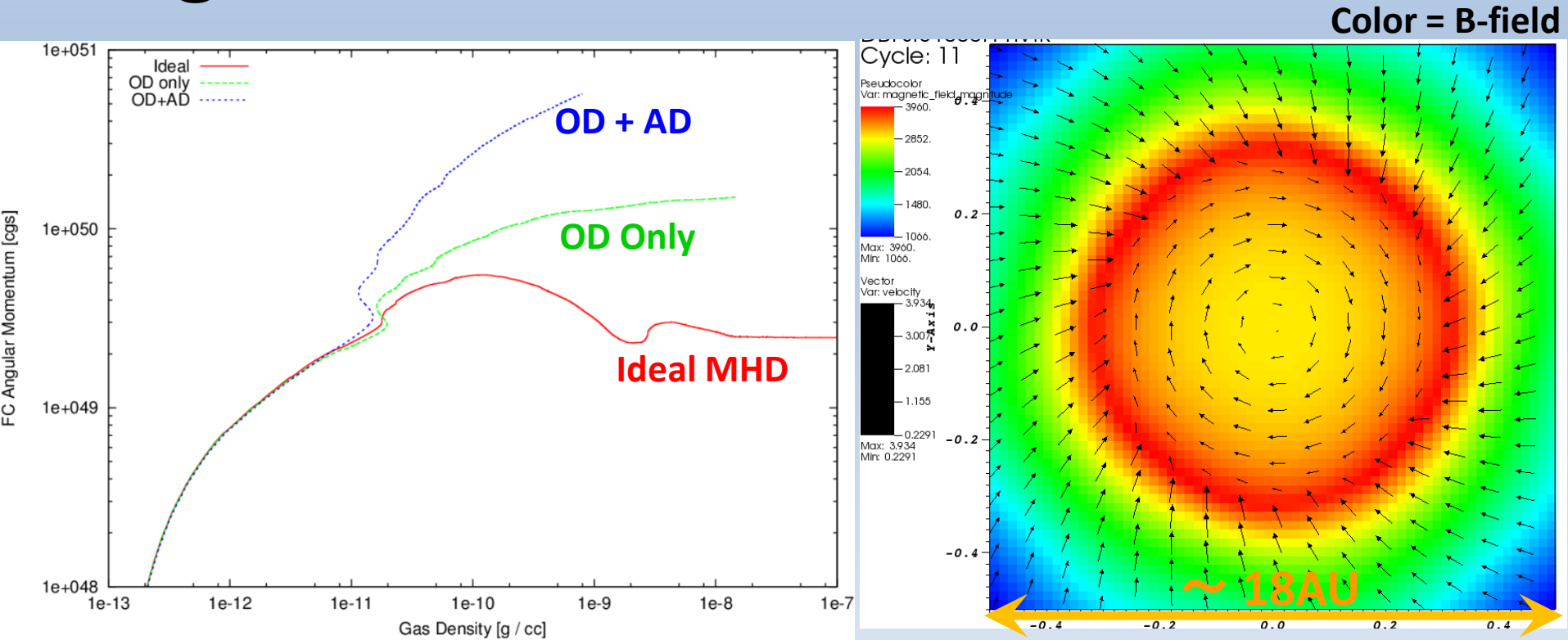
# Preliminary: Ambipolar Diffusion



Ambipolar diffusion rate is very high and works in a relatively low density region  $\Rightarrow$  more magnetic flux loss will occur.



# Angular Momentum in FC

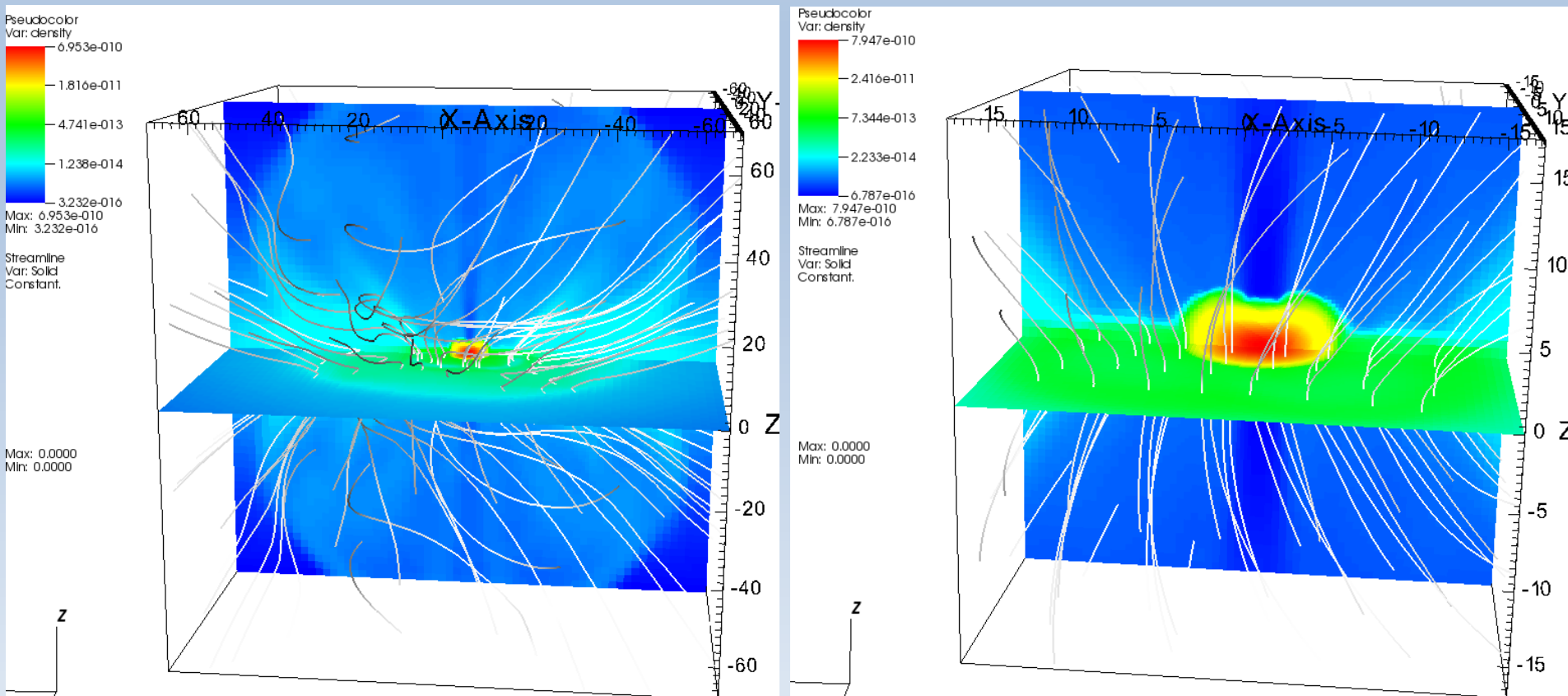


(in the middle of the first core phase,  $T_c \sim 800\text{K}$ )

Large angular momentum remains in the FC  $\Rightarrow$  earlier disk formation.

The rotating disk is resistive: magnetic flux is removed from the dense central region and piles up outside the disk.

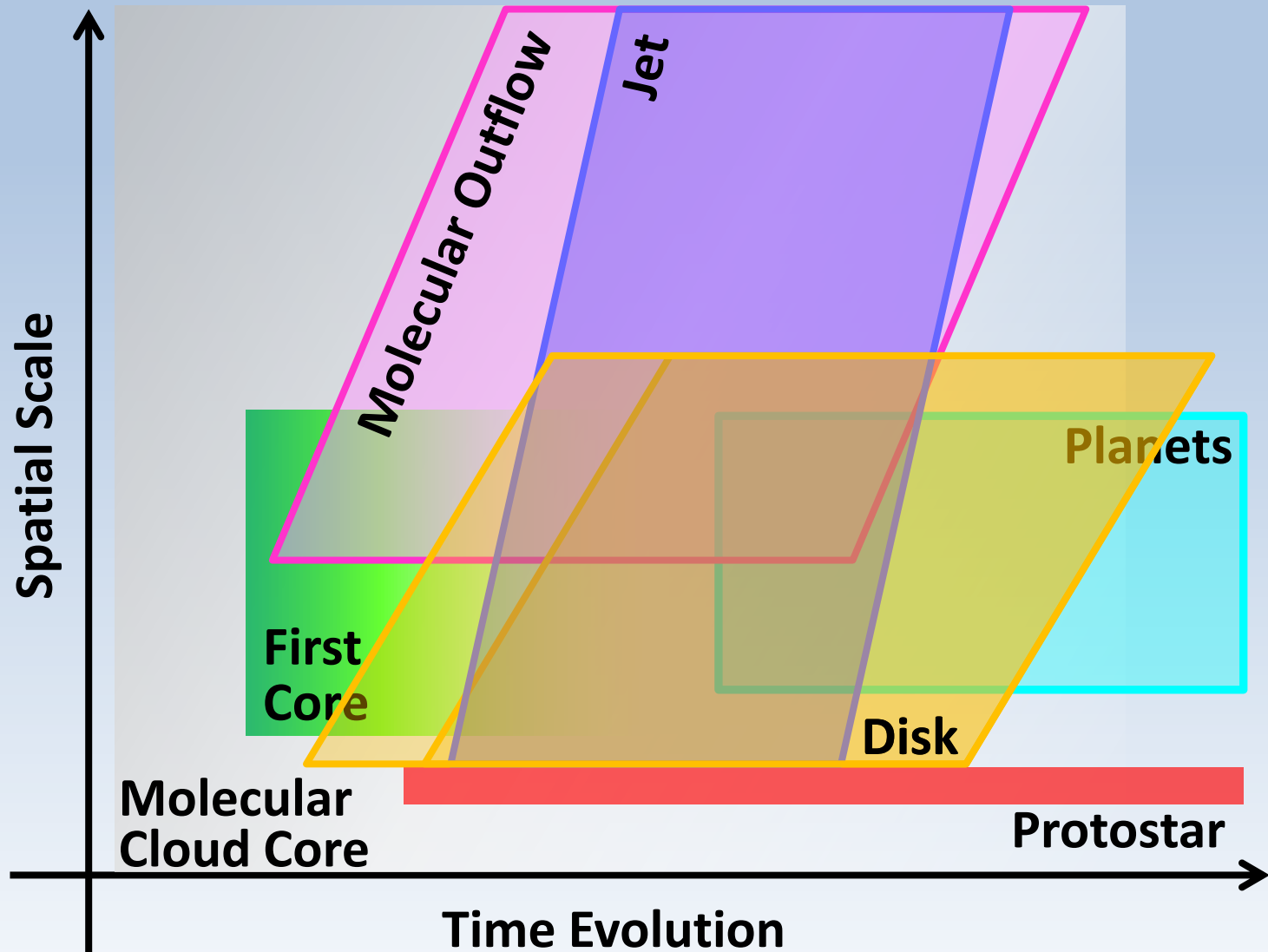
# Outflows and First Core with AD



The bipolar outflows are very similar to the previous cases. First core becomes disk-like because of rotational support. However, the disk radius is still small, about 5 AU.



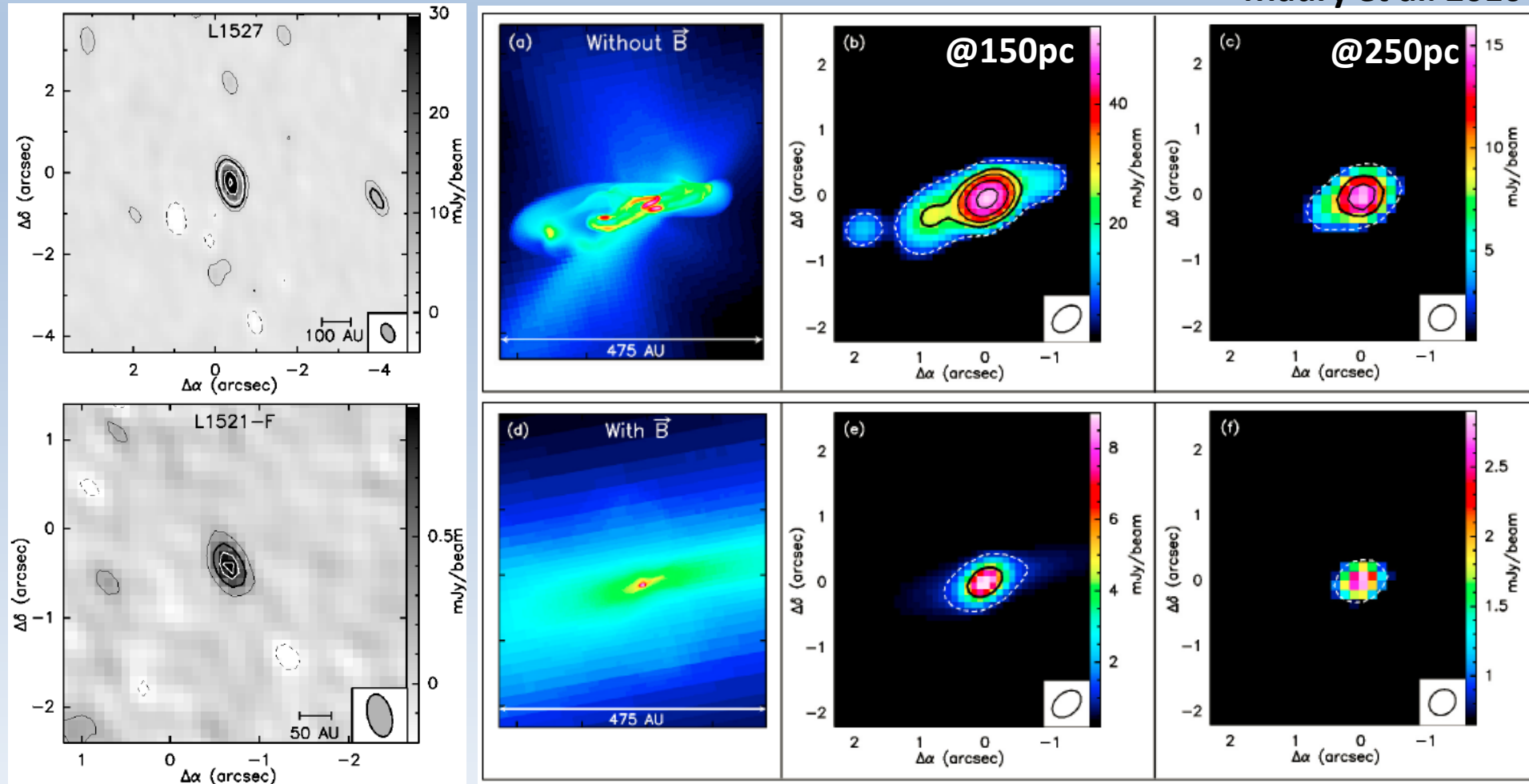
# To Summarize: A Schematic Picture



# Implications from / for Observations

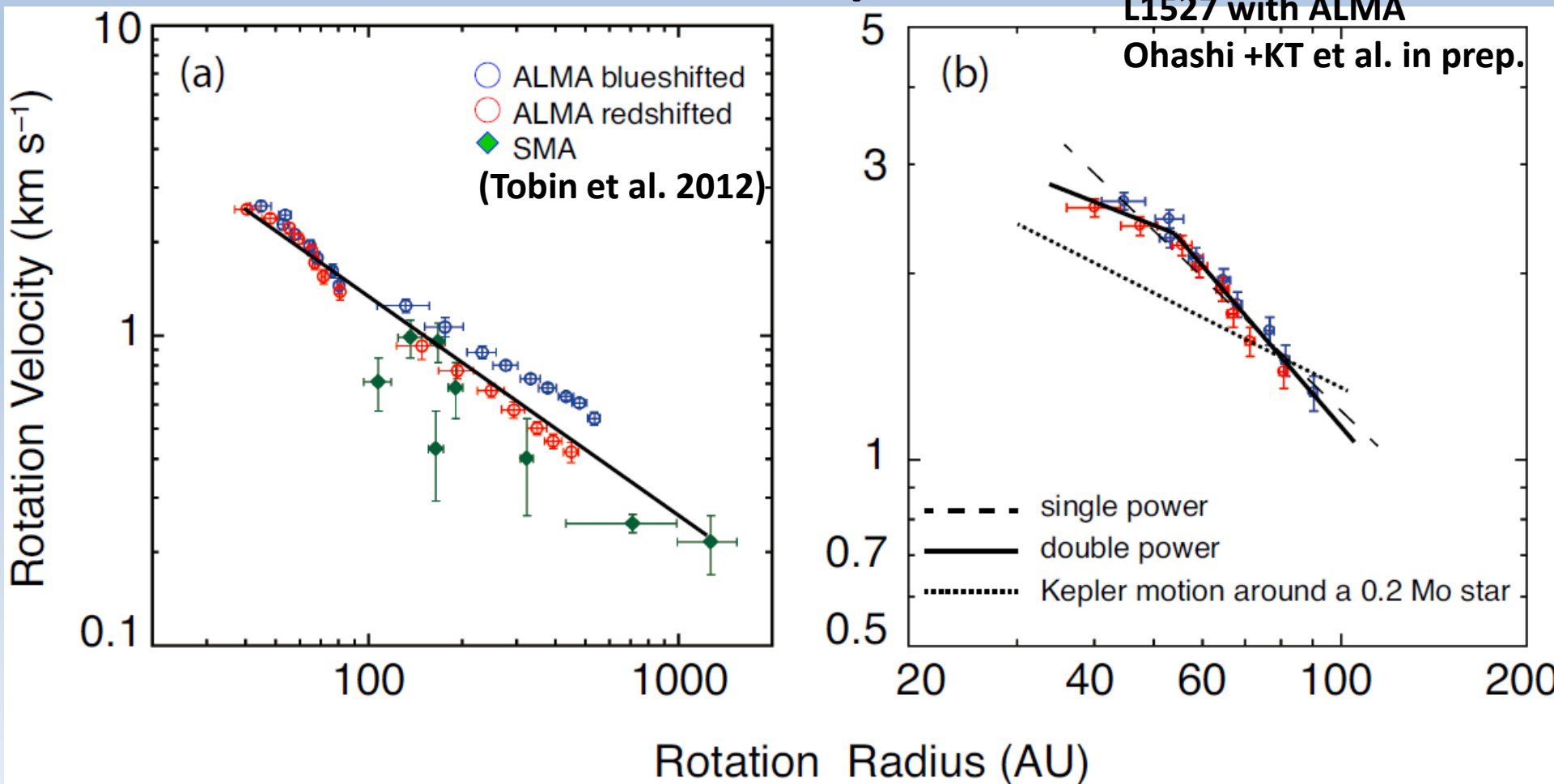
# Observations of Young Disks

Maury et al. 2010



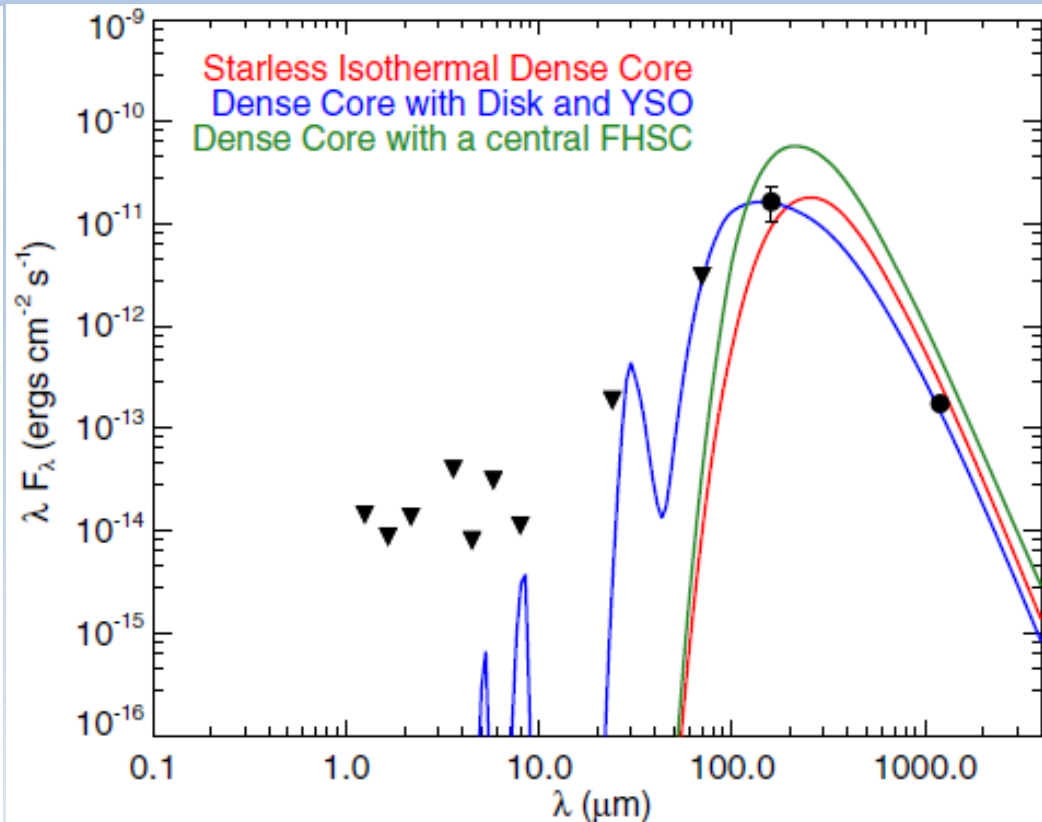
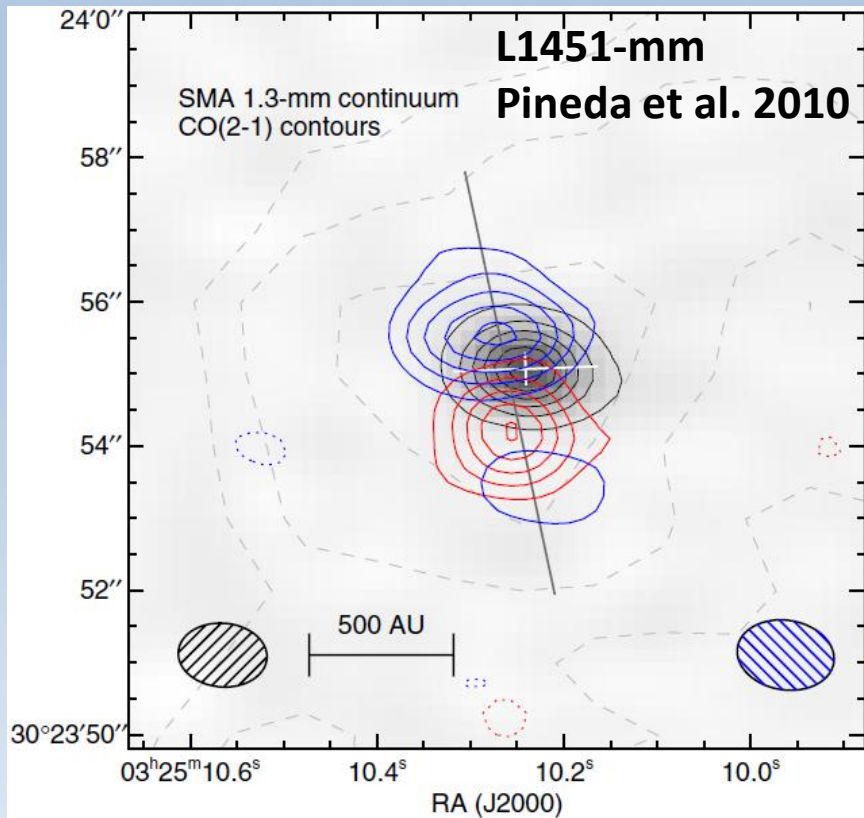
1.3mm Dust continuum observations of Class-0 sources with PdBI.  
The observed disks are small and more consistent with the MHD models.

# A well-studied example: L1527 IRS



Tobin+ 2012 (SMA & CARMA):  $R \sim 120$  AU disk around 0.2 Ms protostar  
Ohashi+ in prep. (ALMA Cycle-0):  $R < 60$  AU disk around 0.3 Ms protostar  
 $\Rightarrow$  Disks can be formed early, but should be small in the early phase

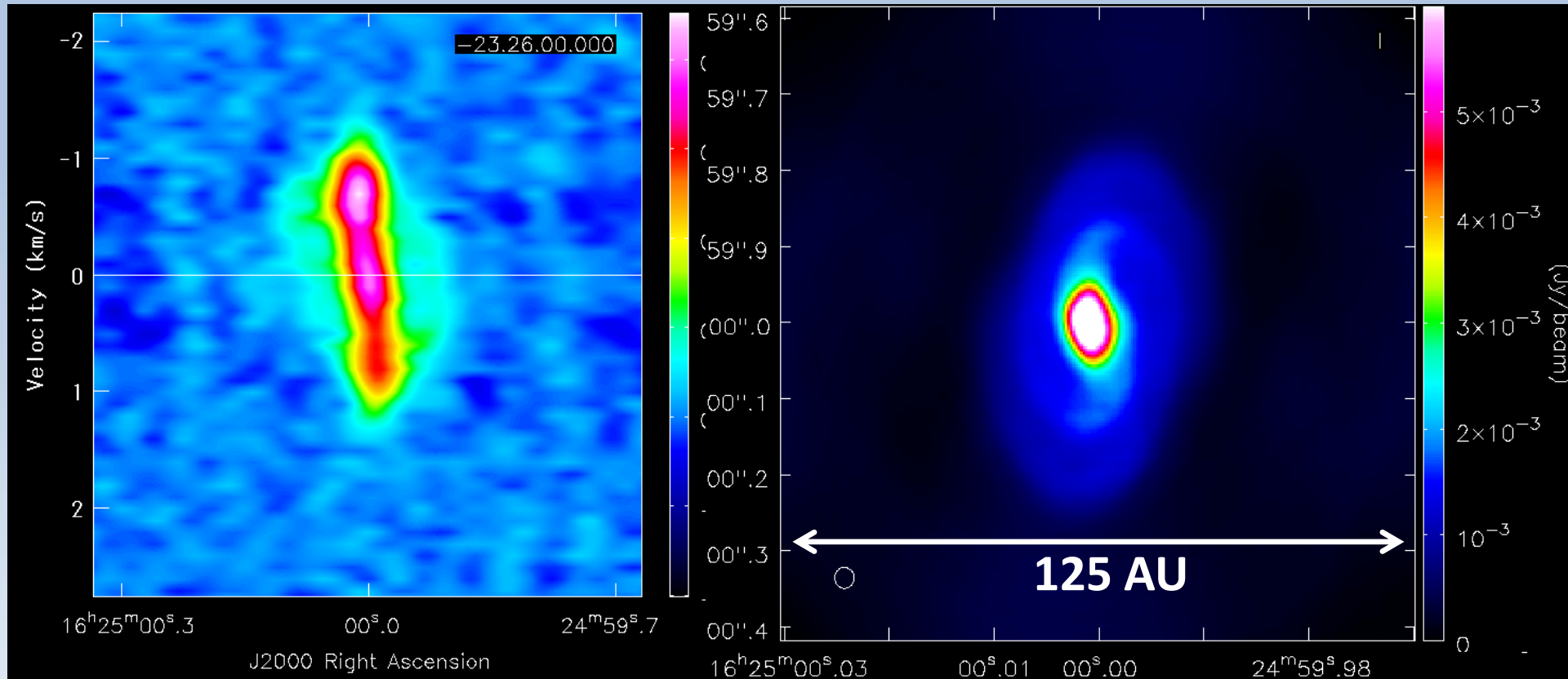
# Even Younger: First Core Candidates



Recent first core candidates: L1451-mm, Barnard 1-bN, Per-Bolo 58 etc.

- Faint compact molecular cores without stellar NIR emission
- Associated with compact, slow outflows without fast jet
- However: it must be rare:  $\sim 1$  FC in 100-1000 molecular cloud cores
- Predicted in Larson 1969 but not confirmed observationally yet

# Synthetic Observations



Left: C<sup>34</sup>S(5-4), Cycle-0, extended, 0.5arcsec, 4h, P-V diagram

Right: 345GHz continuum, Full ALMA, 0.02arcsec, 4h (Tomida, PhD Thesis)

Motivated by ALMA, theoretical predictions based on the results of R(M)HD simulations are actively performed. (especially for first cores.)

# Summary

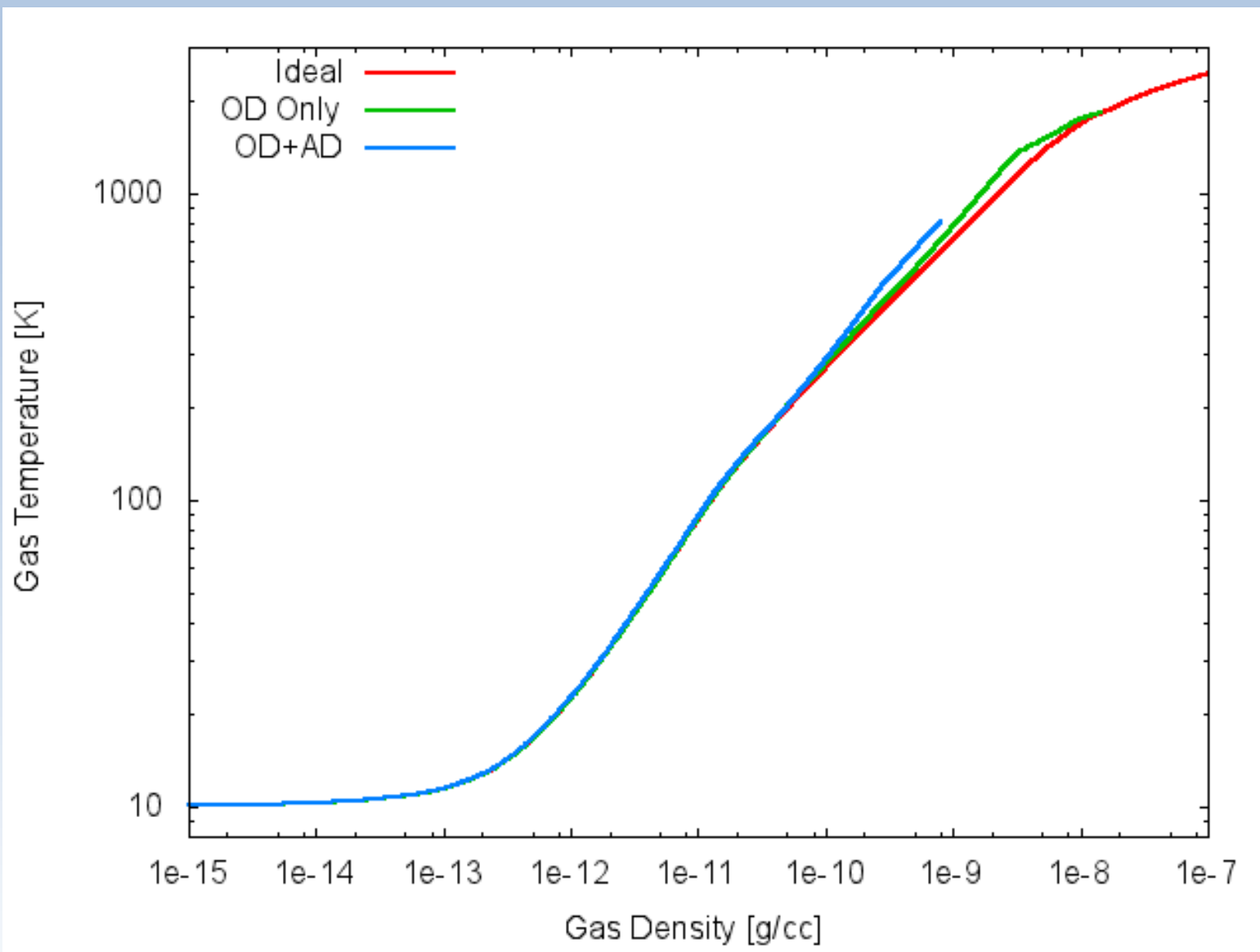
RMHD simulations of protostellar collapse with non-ideal MHD

- Radiation transfer and realistic thermodynamics are important
- Magnetic braking is so efficient in the ideal MHD case that no rotationally-supported disks can be formed in the early phase
- Ohmic dissipation enables early formation of disks
- As natural byproducts, two different outflows are launched: slow, loosely collimated outflows from the first core scale and fast, well collimated jets from the protostellar core scale
- (preliminary!) With ambipolar diffusion, disk formation can be possible even before the second collapse (= birth of a star)
- Disks can be formed early, but should be small, will grow later
- Magnetic Braking Catastrophe is not so catastrophic as it sounds, rather a quantitative question: how, when, and how massive?
- ALMA observations of young disks will be crucial

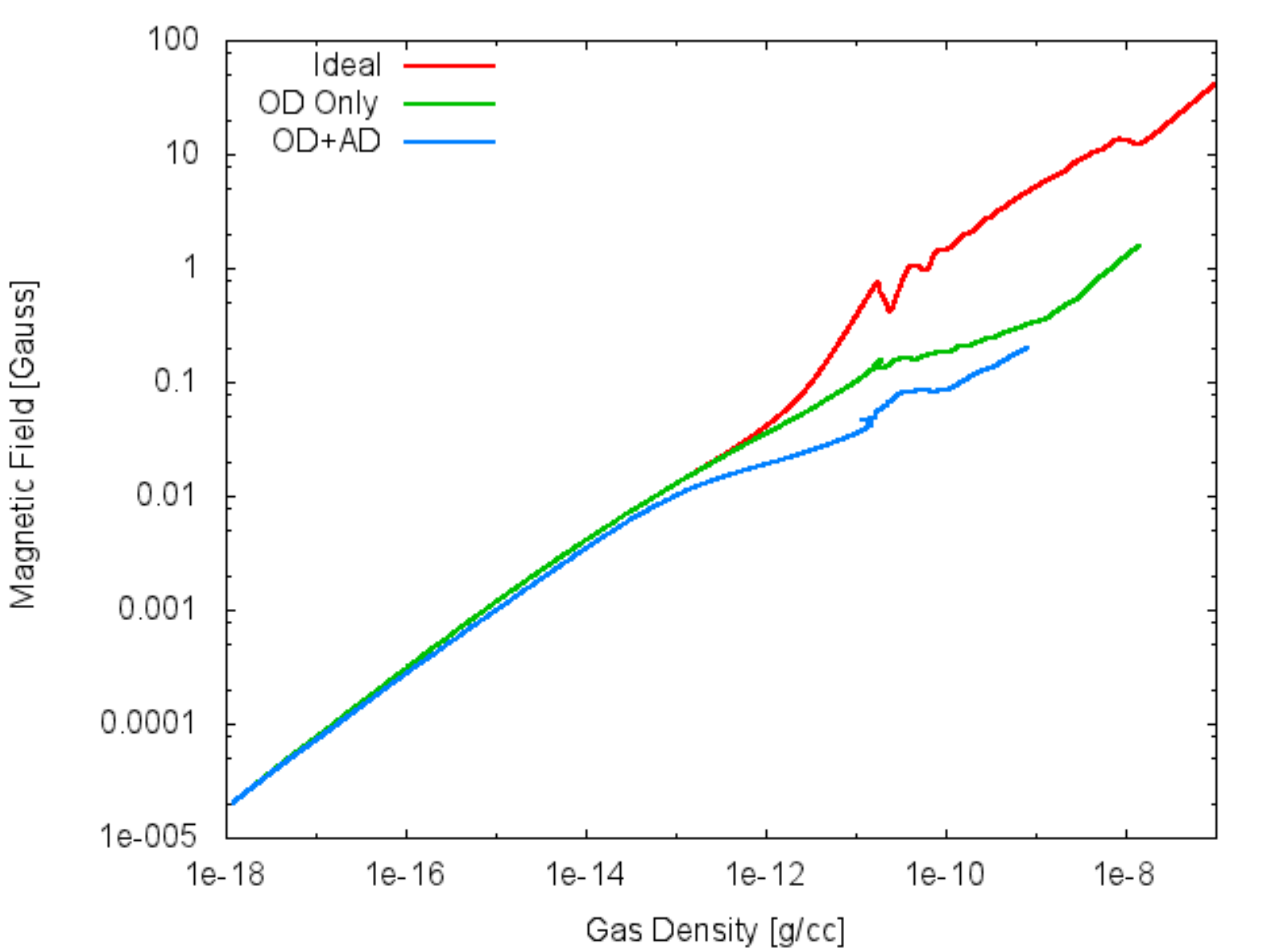
**Thank you!**



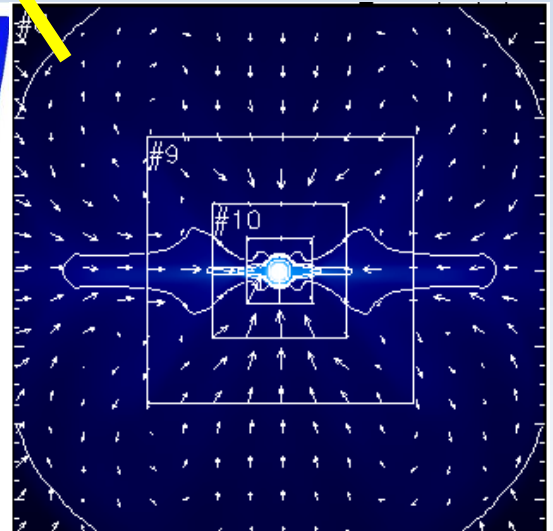
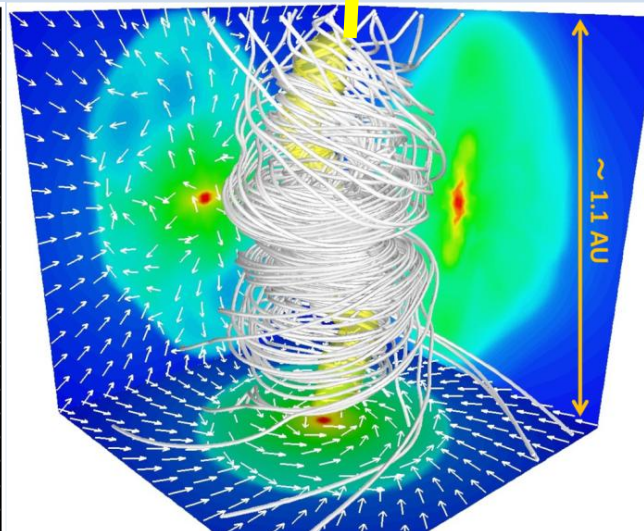
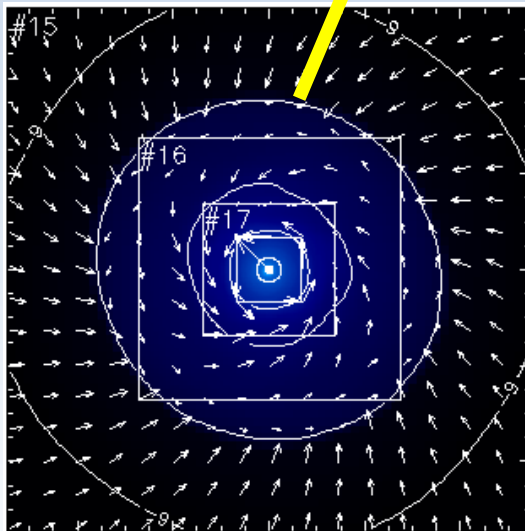
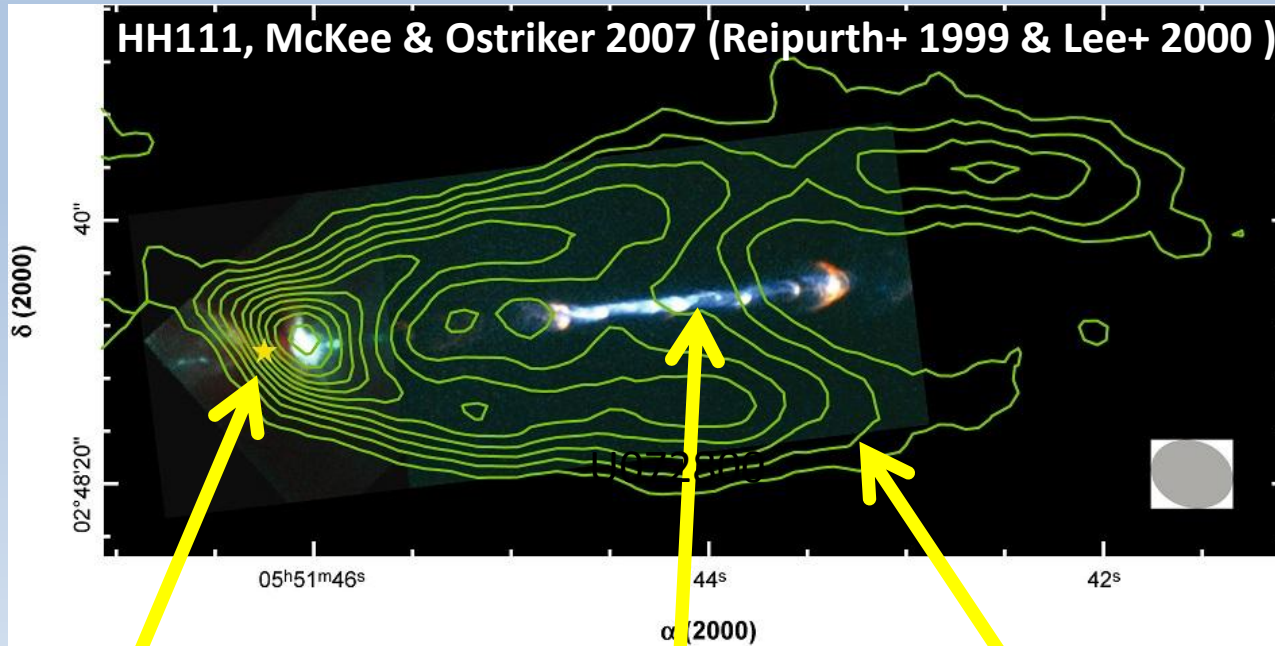
# Thermal Evolution



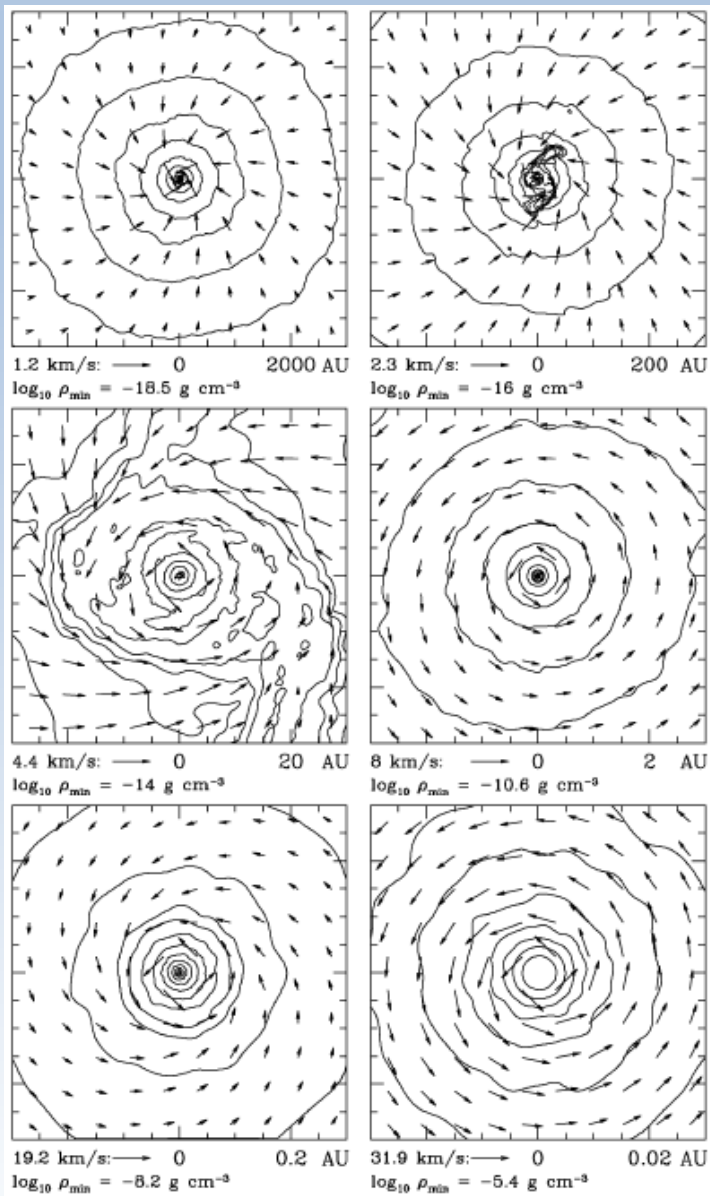
# Magnetic Field



# With some “imagination” ...



# Gravitational Torque



Bate (1998) first performed 3D SPH simulations of protostellar collapse and showed that the rotationally-supported disk becomes unstable and spiral arms are formed.

These non-axis-symmetric structure can transport ang. mom. efficiently and finally a protostar is formed.

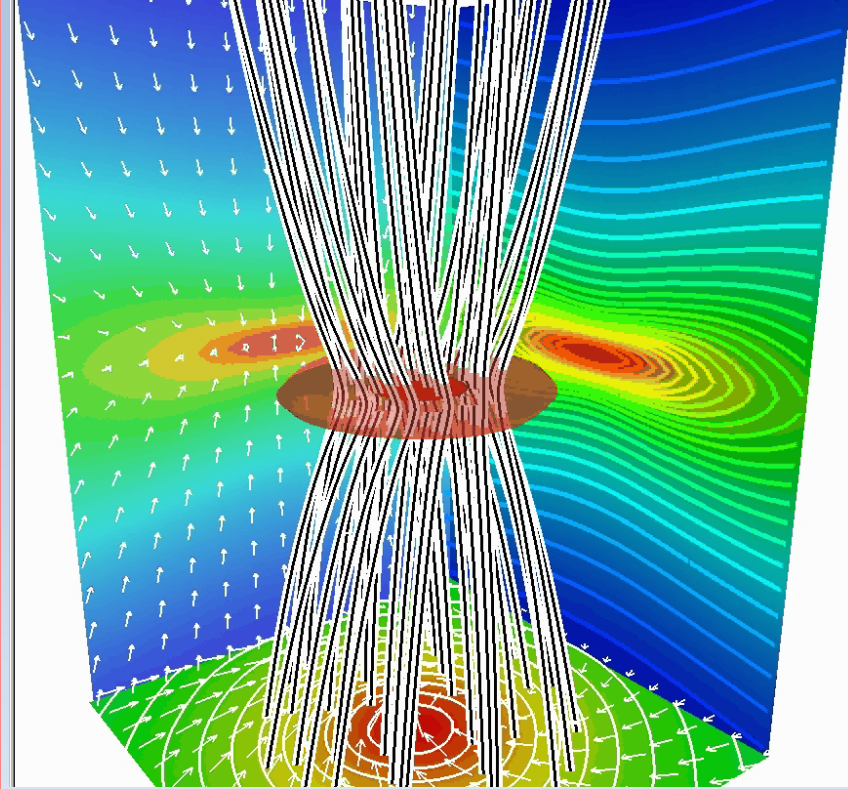
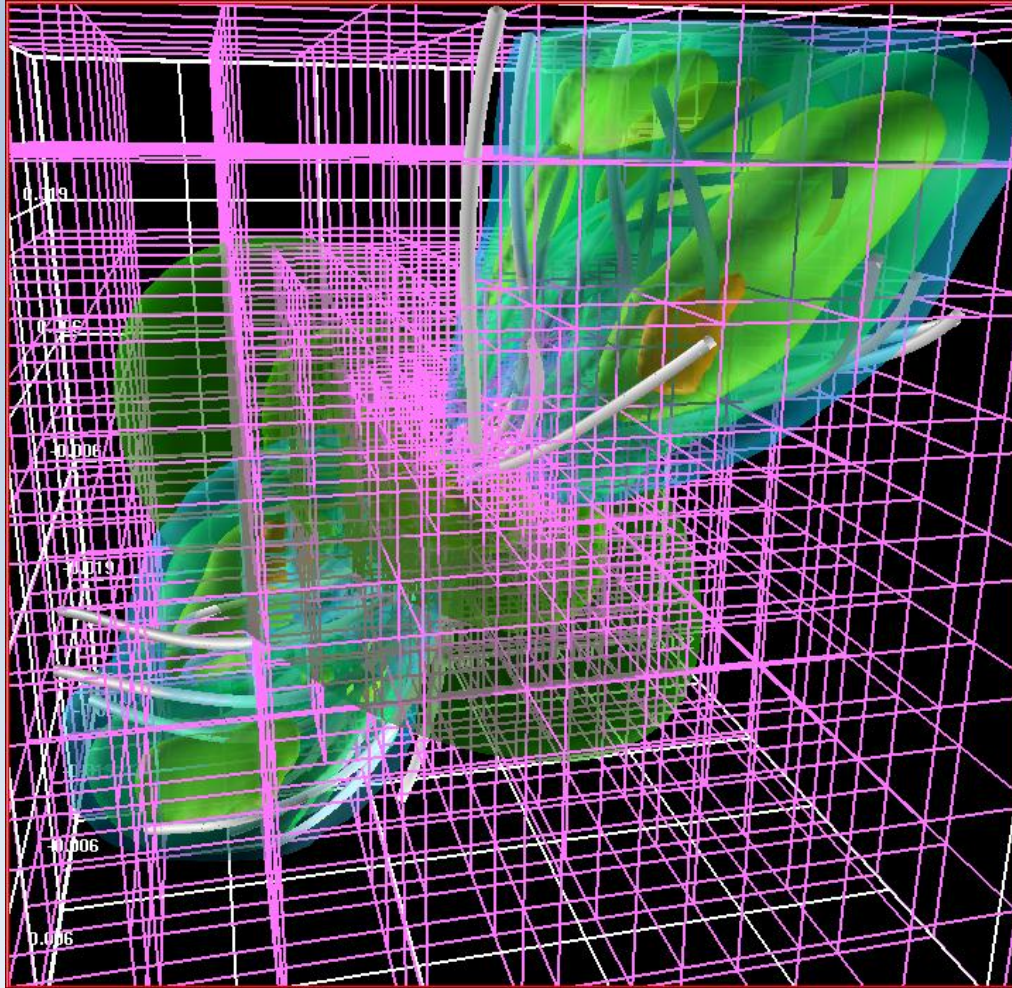
(see also Matsumoto & Hanawa 03, Saigo et al. 08, Commercon et al. 08, etc.)

Note: Thermodynamics (radiation transfer) is modeled using a fitting formula based on 1D RHD simulations (so-called barotropic approximation)



# 3D MHD Protostellar Collapse

(Machida et al. 2008)



3D simulations show that magnetic fields transport ang. mom. efficiently.

(Matsumoto 2007, SFUMATO AMR MHD code)

(see also, Matsumoto & Tomisaka 04, Banerjee & Pudritz 06, Hennebelle & Fromang 08, Hennebelle & Teyssier 08, Duffin & Pudritz 09, Hennebelle & Ciardi 09, etc., etc...)