

# Flipped $SU(5)$ from $Z_{12-I}$ orbifold with Wilson line

(String MSSM through flipped  $SU(5)$  from  $Z_{12}$  orbifold)

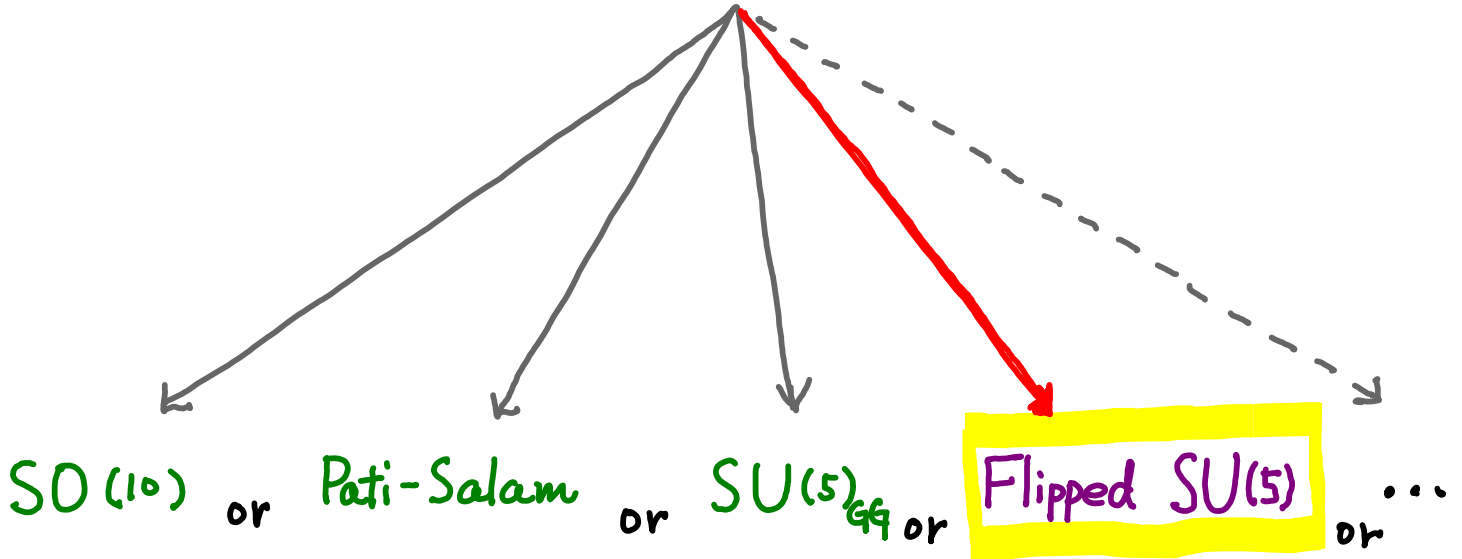
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Based on [hep-th/0608085](#)  
[hep-th/0608086](#)

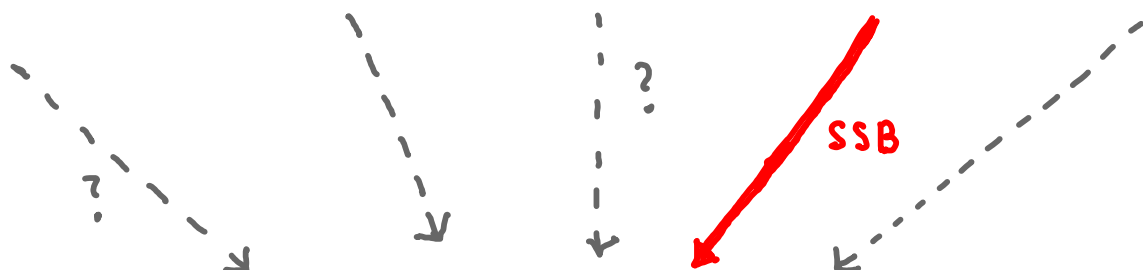
in collaboration with

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# STRING



- |   |   |   |  |
|---|---|---|--|
| <ul style="list-style-type: none"> <li>• <math>\sin^2 \theta_w = \frac{3}{8} !</math></li> <li>• D-W mech. ?</li> <li>• how <math>m_d \neq m_e</math> ?</li> <li>• Adj. Higgs ?</li> <li>• ...</li> </ul> | <ul style="list-style-type: none"> <li>• <math>\sin^2 \theta_w = \frac{3}{8} !</math></li> <li>• No D/T splitting prob.</li> <li>• how <math>m_d \neq m_e</math> ?</li> </ul> | <ul style="list-style-type: none"> <li>• <math>\sin^2 \theta_w = \frac{3}{8} !</math></li> <li>• D/T splitting ?</li> <li>• how <math>m_d \neq m_e</math> ?</li> <li>• Adj. Higgs ?</li> <li>• ...</li> </ul> | <ul style="list-style-type: none"> <li>• <math>\sin^2 \theta_w = \frac{3}{8} ?</math></li> <li>• Simply D/T split</li> <li>• just <math>m_u = m_D</math></li> <li>• Adj. Higgs not necessary</li> <li>• ...</li> </ul> |
|---|---|---|--|



# MSSM

# Summary of our Results

1.  $G = \underline{SU(5) \otimes U(1)_x \otimes U(1)^3 \otimes \text{Hidden gp.}}$

with 3 families of matter + vec.-like Higgs  
MSSM  $\{10_H, \bar{10}_H, 5_w, \bar{5}_w\}$

( $U(1)_x$  charge assignments  
coincident with Flipped  $SU(5)$ )

2. Yukawa Coupling Analysis shows

a. vec.-like (exotic) states Massive

b. Flipped  $SU(5) \xrightarrow{\langle 10_H \rangle, \langle \bar{10}_H \rangle}$  MSSM

c. D/T splitting

d. Fermion masses

e.  $\exists$  R-parity

if  $\langle 1_0 \rangle \neq 0$

Current algebra  
in string theory  
determines  $U(1)$  charge  
normalization.

3.  $\sin^2 \theta_w = \frac{3}{8}$  at the full unif. scale

# Physical Massless States in Orbifold Compactification of the Heterotic String

## 1. Massless Conditions

- L-mover:  $\frac{1}{2} |P + kV|^2 + \sum_j N_j^L \tilde{\phi}_j - \tilde{c} = 0$   
if  $kW = 0$ ,  $(P + kV) \cdot W = \text{integer}$
- R-mover:  $\frac{1}{2} |S + k\phi|^2 + \sum_j N_j^R \tilde{\chi}_j - c = 0$

## 2. Multiplicity

$$P_k = \frac{1}{N} \sum_{l=0}^{N-1} \tilde{\chi}(\theta^k \theta^l) e^{2\pi i l \mathbb{H}_0}$$

↑ degeneracy factor

$$\left( \mathbb{H}_0 = \sum_j (N_j^L - N_j^R) \hat{\phi}_j + \frac{k}{2} (V^2 - \phi_s^2) + (P + kV) \cdot V + (\tilde{S} + k\phi_s) \cdot \phi_s \right)$$

In the presence of Wilson line,

$$e^{2\pi i \mathbb{H}_0} \longrightarrow \frac{1}{N_W} \sum_{f=0}^{N_W-1} e^{2\pi i l \mathbb{H}_f}$$

$$\left( \mathbb{H}_f = \mathbb{H}_0 [V \rightarrow V_f] \right)$$

# The Model

$\mathbb{Z}_{12-1}$  orbifold compactification

$\vec{\phi}_s = \left( \frac{5}{12}, \frac{4}{12}, \frac{1}{12} \right) : \sim SO(8) \times SU(3)$  lattice

$\sim \mathbb{Z}_3 : \left\{ \begin{array}{l} \text{Wilson Line of order 3} \\ \text{can be set} \\ \text{on this sub-lattice.} \end{array} \right.$

$V = \left( \frac{3}{12} \frac{3}{12} \frac{3}{12} \frac{3}{12} \frac{3}{12} ; \frac{5}{12} \frac{6}{12} 0 \right) \left( \frac{2}{12} \frac{2}{12} 0 ; 0^5 \right)$   
 $a_3 = \left( \begin{array}{ccc} & & 0^5 \\ & & \\ & & \end{array} ; 0 \frac{4}{12} \frac{4}{12} \right) \left( 0 \ 0 \ \frac{4}{12} ; 0^5 \right)$   
 $= a_4 \quad (a_1 = a_2 = a_5 = a_6 = 0)$

$Q_x = \left( \underbrace{-2 \ -2 \ -2 \ -2 \ -2}_{SU(5) \otimes U(1)_x} ; \underbrace{0^3}_{(\otimes [U(1)]^3)} \right) \left( \underbrace{0^2}_{SU(2)'} \ 0 ; \underbrace{0^5}_{SO(10)'} \right)$   
 $(\otimes [U(1)']^1)$

$SU(2)'$   
↑

\* Simple roots satisfying  $P \cdot V = P \cdot a_3 = 0$   $(1 \ -1 ; 0^6)'$   
 $(\underline{1 \ -1 \ 0 \ 0 \ 0} ; 0^3) : SU(5), SO(10)'$   
 $\left\{ \begin{array}{l} (0 \ 0 ; \frac{14}{3} \ 0^3)' \\ ( " ; 0^3 \ 11)' \end{array} \right.$

# Field Spectrum (Result)

$$U: \quad 2 \times \{ \bar{5}_{-3}, 10_1, 1_5 \} + 1 \times 5_{-2} + \text{neutral singlet} + \text{CTP}$$

$\nearrow$  matter  $\nearrow$  EW Higgs

$$T_6: \quad 4 \times 10_1 + 3 \times \bar{10}_{-1} + 2 \times \{ \bar{5}_{-3}, 5_3 \} + 2 \times \{ 1_5, 1_{-5} \} + \text{neutral singlets} + \text{CTP}$$

$$\begin{cases} 10_1 = \begin{pmatrix} d^c & Q \\ & \nu^c \end{pmatrix} \\ \bar{5}_{-3} = \begin{pmatrix} u^c \\ L \end{pmatrix} \\ 1_5 = e^c \end{cases}$$

$$T_2: \quad 1 \times \{ \bar{5}_{-3}, 1_5 \} + \text{neutral singlets}$$

$\nearrow$  matter  
 (CTP: from  $T_{10}$ )

$$T_4: \quad 3 \times \bar{5}_2 + 2 \times 5_{-2} + \text{neutral singlets}$$

(CTP: from  $T_8$ )

$$T_1: \quad 2 \times \{ \bar{5}_{-1/2}, 5_{1/2} \} + 7 \times \{ 1_{5/2}, 1_{-5/2} \}$$

$$T_7: \quad 2 \times \{ \bar{5}_{-1/2}, 5_{1/2} \} + 7 \times \{ 1_{5/2}, 1_{-5/2} \}$$

(CTP: from  $T_{11}$ )  
 (CTP: from  $T_5$ )  
 } vec. -like

$$T_3: \quad \text{No Massless States satisfying } (P+3V)a_3=0$$

# Yukawa Couplings

$\rightarrow \langle \theta_A \theta_B \theta_C \dots \rangle$   
A vertex op. should satisfy

## 1. Gauge Invariance

## 2. H-mom. Conservation (discrete R-charge conservation) (bosonic)

$$\sum_z R_1(z) = -1 \pmod{12}, \quad \sum_z R_2(z) = 1 \pmod{3}, \quad \sum_z R_3(z) = 1 \pmod{12}$$

$\uparrow$  A, B, C, ...

$$\text{where } R_i = (\tilde{r} + k\phi_s)_i - (N_i^L - N_i^R)$$

$\uparrow$   $\uparrow$   
 $i=1,2,3$

(bosonic) shifted SO(8) weight  
satisfying the Mass shell condition

## 3. Space Group Selection Rules

$$\left\{ \begin{array}{l} \sum_z k(z) = 0 \pmod{12} \\ \sum_z [k m_f](z) = 0 \pmod{3} \end{array} \right.$$

# Allowed Yukawa Couplings

With the assumption  $\langle 1_0 \rangle_s \sim \Lambda$

a.  $W \supset f_1 [1_0 s] \cdot 5_{\frac{1}{2}} \bar{5}_{\frac{1}{2}} + f_2 [1_0 s] \cdot 1_{5/2} 1_{-5/2}$   
 $+ f_3 [1_0 s] \cdot 10, \bar{10}_1 + f_4 [1_0 s] \cdot 5_3 \bar{5}_3 + f_5 [1_0 s] \cdot 1_5 1_{-5}$   
 $+ f_6 [1_0 s] 5_{-2} \bar{5}_2 + \dots$

All  $\{5_{\frac{1}{2}} \bar{5}_{\frac{1}{2}}\}, \{1_{5/2}, 1_{-5/2}\}$  in  $T_1, T_7$ ,  
 $3 \times \{10_1, \bar{10}_1\}, 2 \times \{5_3, \bar{5}_3, 1_5, 1_{-5}\}$  in  $T_6$ ,  
 $2 \times \{5_{-2}, \bar{5}_2\}$  in  $T_4$  can be heavy.

Thus,

U:  $2 \times \{16\} + 5_{-2}$  <sup>↗ Higgs</sup>,  $T_6: 10_1$ ,  $T_2: \bar{5}_3 + 1_5$   
 (3 families of MSSM matter)  $T_4: \bar{5}_2$  <sub>↘ Higgs</sub>

⇒ Flipped SU(5) field spectrum



**b.**

$$W \supset f_7 [1_0^D s] [ 10', \overline{10}'_1 + 10'', \overline{10}''_1 + \dots - f_8 [1_0 s] ]$$

$$\Rightarrow \langle 10, \overline{10}_1 \rangle = M_G$$

**c.**

$$W \supset \langle 10_1 \rangle 10_1 5_h + f_9 [1_0 s] \langle \overline{10}_1 \rangle \overline{10}_1 \overline{5}_h$$

$$( \langle \nu^c \rangle d^c D )$$

$$( \langle \overline{\nu}^c \rangle \overline{d}^c \overline{D} )$$

pair up to be heavy

$\left( \begin{array}{l} \text{!} \{Q, \overline{Q}\} \text{ in } 10, \overline{10}_1 \text{ are eaten} \\ \text{by the massive gauge sector.} \end{array} \right)$

$$\Rightarrow \underline{D/T \text{ splitting}}$$

d.

Cubic couplings

$10, \bar{5}_{-3}, \bar{5}_2 (T_6 T_2^0 T_4^0)$ : t quark  
& Dirac  $\tau$  neutrino

$10, 10, 5_{-2} \begin{pmatrix} T_6 T_6 U_2 \\ U_1 U_2 U_3 \end{pmatrix}$ : b-type quarks

But only if  $\langle 1_0 \rangle_s \neq 0$  all the components

in  $(10_i)(\bar{5}_{-3}_j)\bar{5}_2$ ,  $(10_i)(10_i)5_{-2}$ ,  $(15_i)(\bar{5}_{-3}_j)5_2$   
 $\langle \bar{10}_i \bar{10}_i \rangle (10_i)(10_i)_j$  can be non-zero.

e.

R-parity (matter parity) relevant at low energy still can be defined.