

# Mirage Mediation

*also known as*  
*MixedModulus-AnomalyMediation*

**Hans Peter Nilles**

Physikalisches Institut, Universität Bonn, Germany

Based on work with K. Choi, A. Falkowski, M. Olechowski, S. Pokorski,

hep-th/0411066, hep-th/0503216

J. Martin, O. Loaiza, M. Ratz, hep-th/0509158

O. Lebedev, M. Ratz, hep-ph/0511320, hep-th0603047

# Outline

- Basic questions: moduli stabilization and Susy breakdown: Fluxes and Gaugino Condensation
- A large and a little hierarchy
- Mirage Mediation
- Distinct pattern of soft terms
- Soft Susy breaking (flavour and CP)
- Dark matter candidates
- Avoiding cosmological (moduli) problems
- Some remarks on fine tuning
- Conclusions and outlook

# Two Basic Questions

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Relevant moduli are

- Dilaton ( $S$ )
- Kähler ( $T_i$ ) and complex structure moduli ( $Z_\alpha$ )
- Other moduli are needed.
- They might come from Chern-Simons terms, additional matter fields.....

(Lebedev, HPN, Ratz, 2006)

# Fluxes and gaugino condensation

Is there a general pattern of the soft mass terms?

We always have (from **flux** and **gaugino condensate**)

$$W = \text{something} - \exp(-X)$$

where “**something**” is small and  $X$  is moderately large.

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where “**something**” is small and  $X$  is moderately large.

In fact in this simple scheme

$$X \sim \log(M_{\text{Planck}}/m_{3/2})$$

providing a “**little**” **hierarchy**.

(Choi, Falkowski, HPN, Olechowski, 2005)

# Mixed Modulus Anomaly Mediation

The contribution from “Modulus Mediation” is therefore suppressed by the factor

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Thus the contribution due to “Anomaly Mediation” (suppressed by a loop factor) becomes competitive, leading to a Mixed Modulus-Anomaly-Mediation scheme.

For reasons that will be explained later we call this scheme

**MIRAGE MEDIATION**

(Loaiza, Martin, HPN, Ratz, 2005)

# The little hierarchy

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- moduli and gravitino are heavy
- relieves the Susy flavour and CP problems
- distinct pattern of soft breaking terms.

(Endo, Yamaguchi, Yoshioka, 2005; Choi, Jeong, Okumura, 2005)

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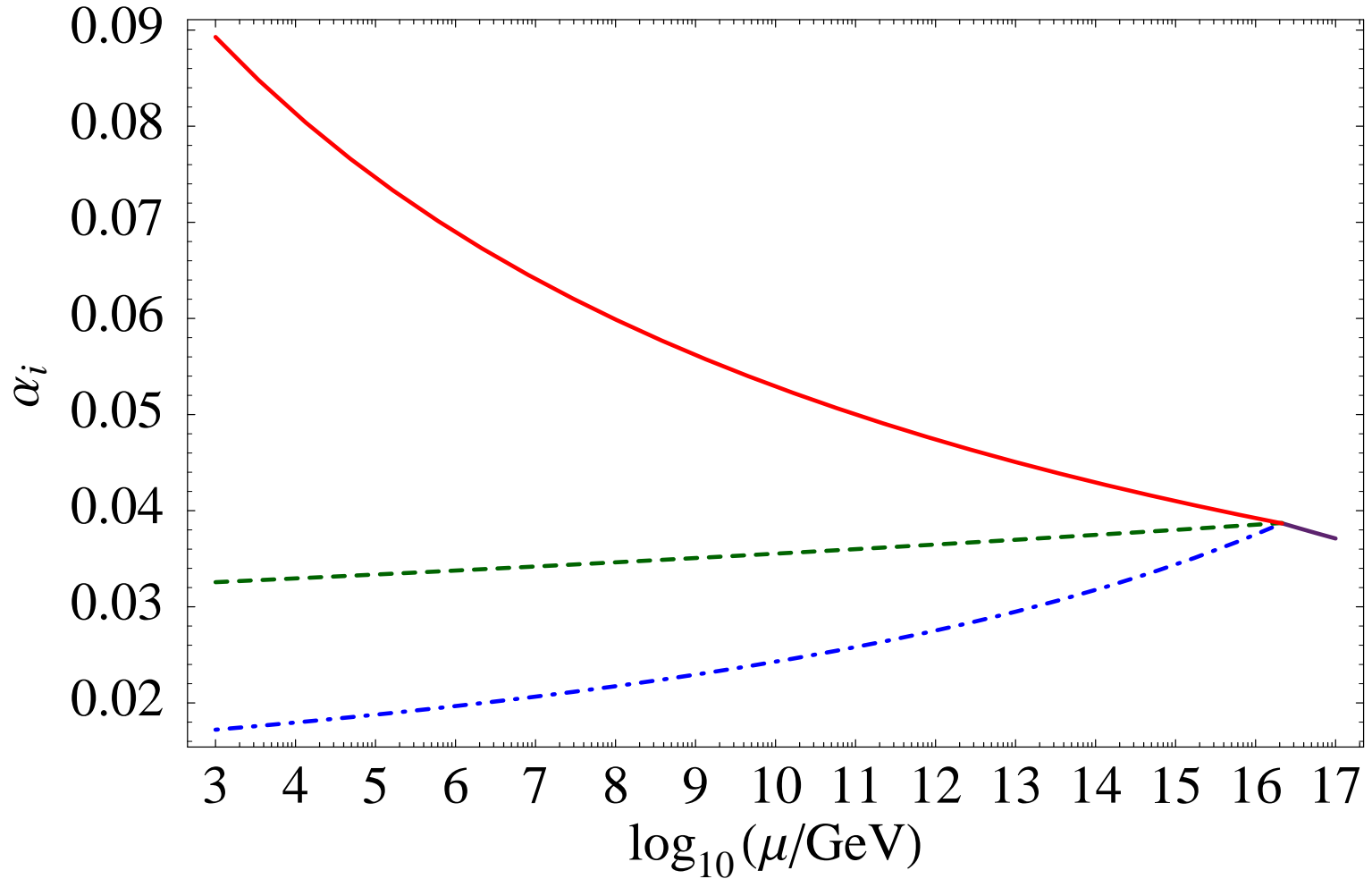
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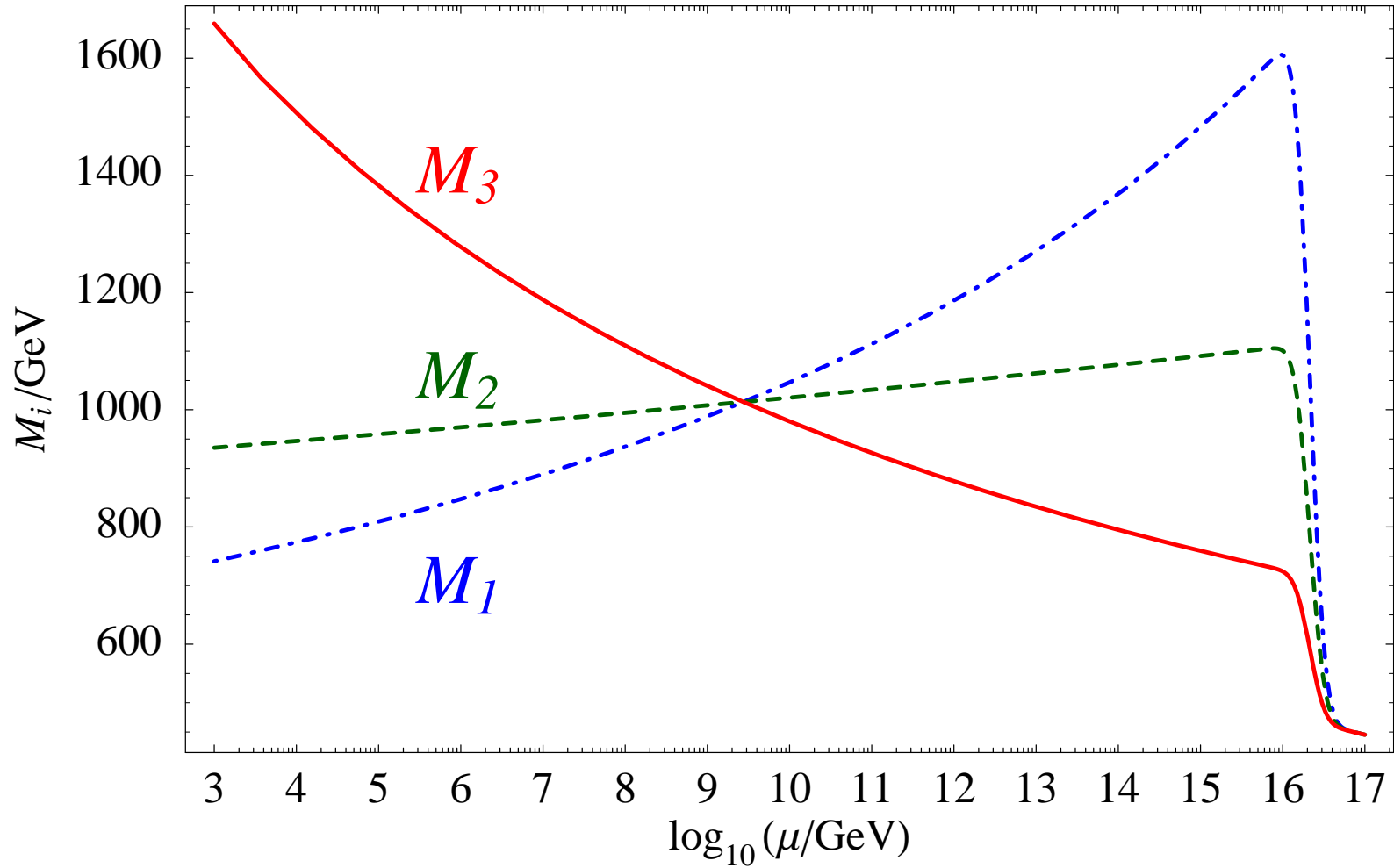
- $M_{\text{anomaly}}$  is proportional to the  $\beta$  function,  
i.e. **negative** for the gluino, **positive** for the bino
- thus  $M_{\text{anomaly}}$  is non-universal below the GUT scale

# Evolution of couplings





# The Mirage Scale



(Lebedev, HPN, Ratz, 2005)

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The gaugino masses coincide

- above the GUT scale
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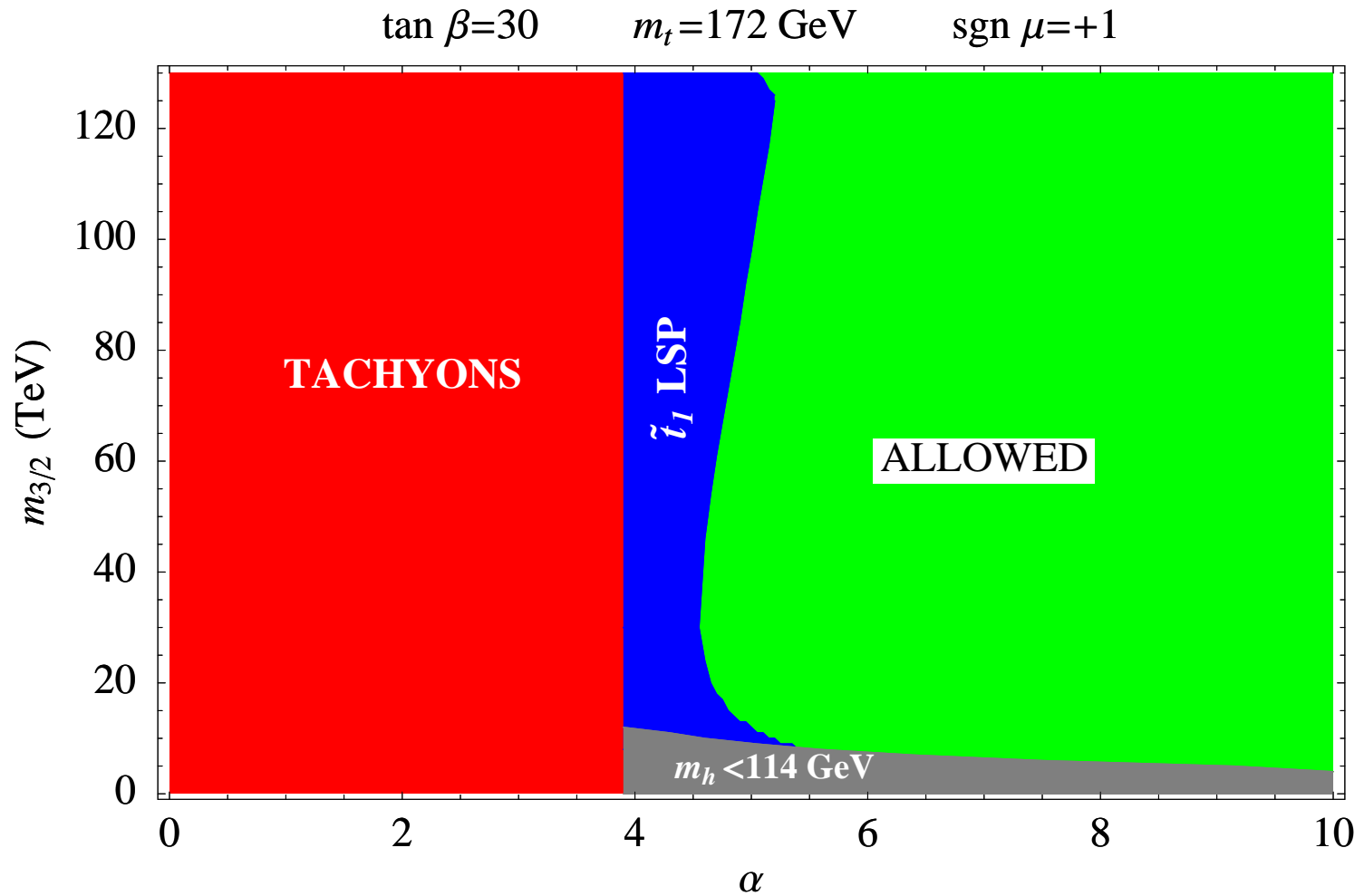
$$\mu_{\text{mirage}} = M_{\text{GUT}} \exp(-8\pi^2/\alpha)$$

where  $\alpha$  denotes the “ratio” of the contribution of **modulus** vs. **anomaly mediation**. We write the gaugino masses as

$$M_a = M_s(\alpha + b_a g_a^2) = \frac{m_{3/2}}{16\pi^2}(\alpha + b_a g_a^2)$$

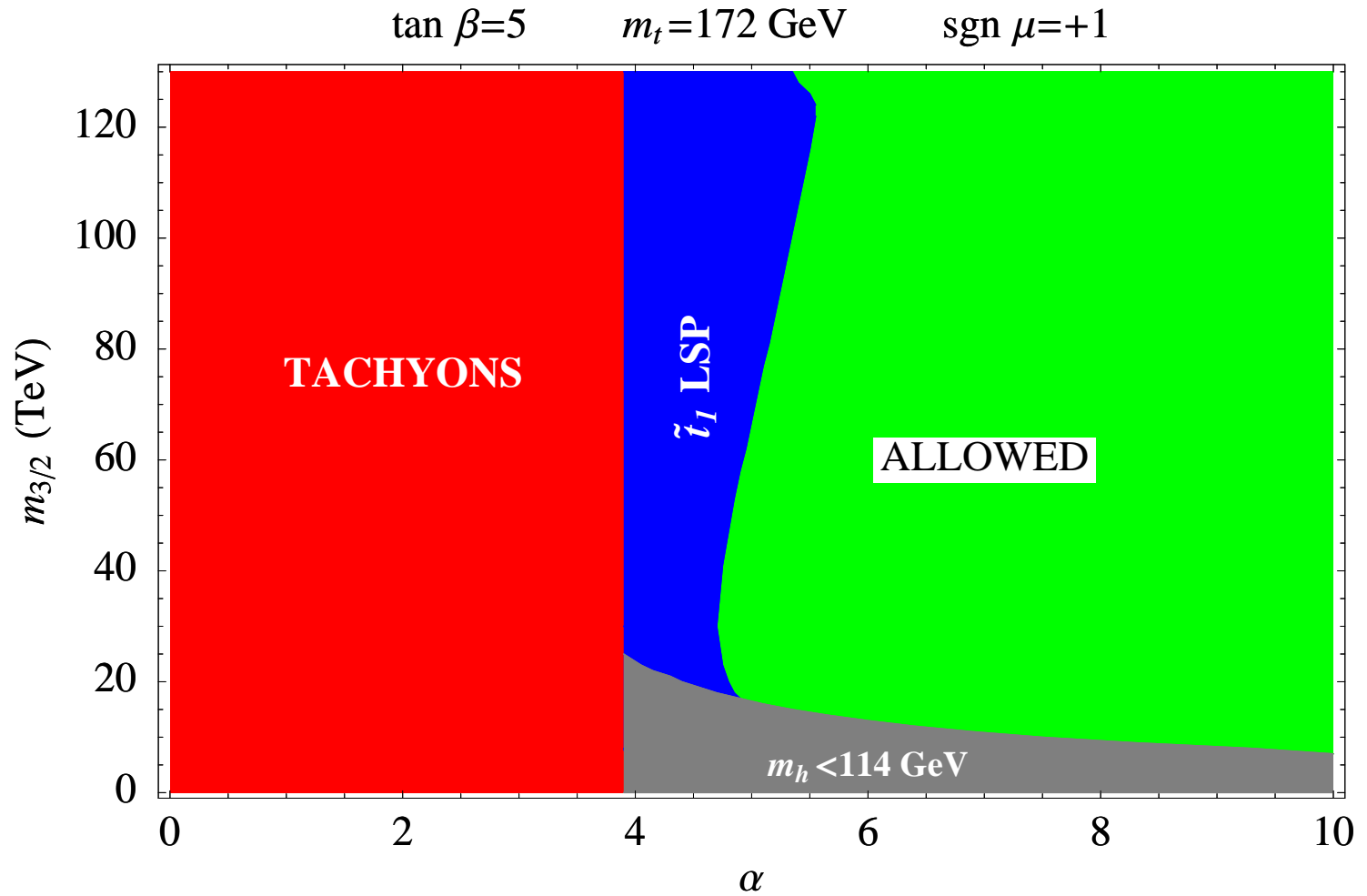
and  $\alpha \rightarrow 0$  corresponds to pure anomaly mediation.

# Constraints on the mixing parameter



(Löwen, HPN, Ratz, 2006)

# Constraints on $\alpha$



(Löwen, HPN, Ratz, 2006)

# Constraints from cosmology

The scheme leads to

- neutralino Dark Matter

(Falkowski, Lebedev, Mambrini, 2005; Baer, Park, Tata, Wang, 2006)

Cosmological moduli problem revived through

- modulus decay into gravitini

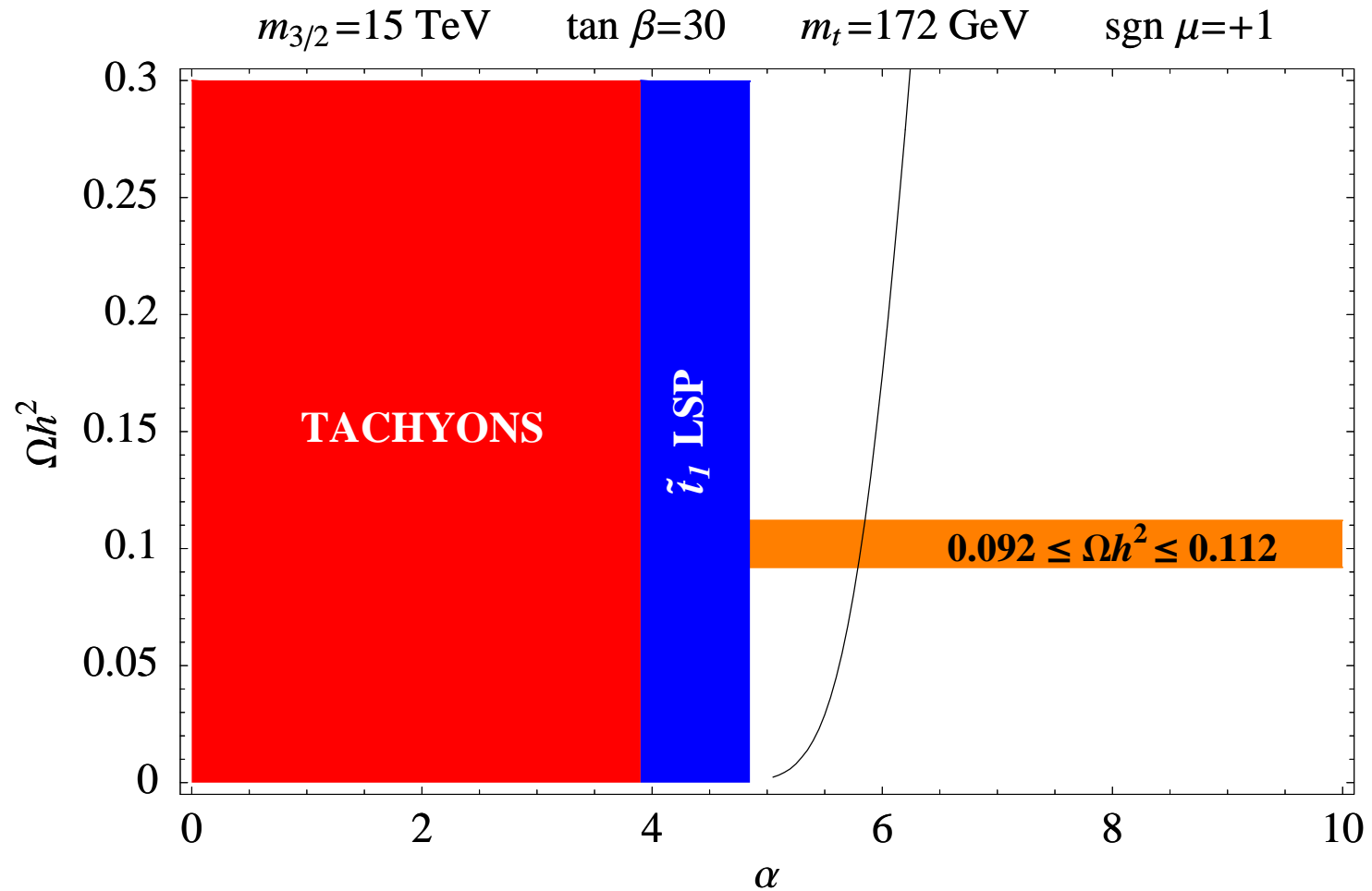
(Endo, Hamaguchi, Takahashi, 2006; Nakamura, Yamaguchi, 2006)

Seems to require the presence of

- additional light moduli

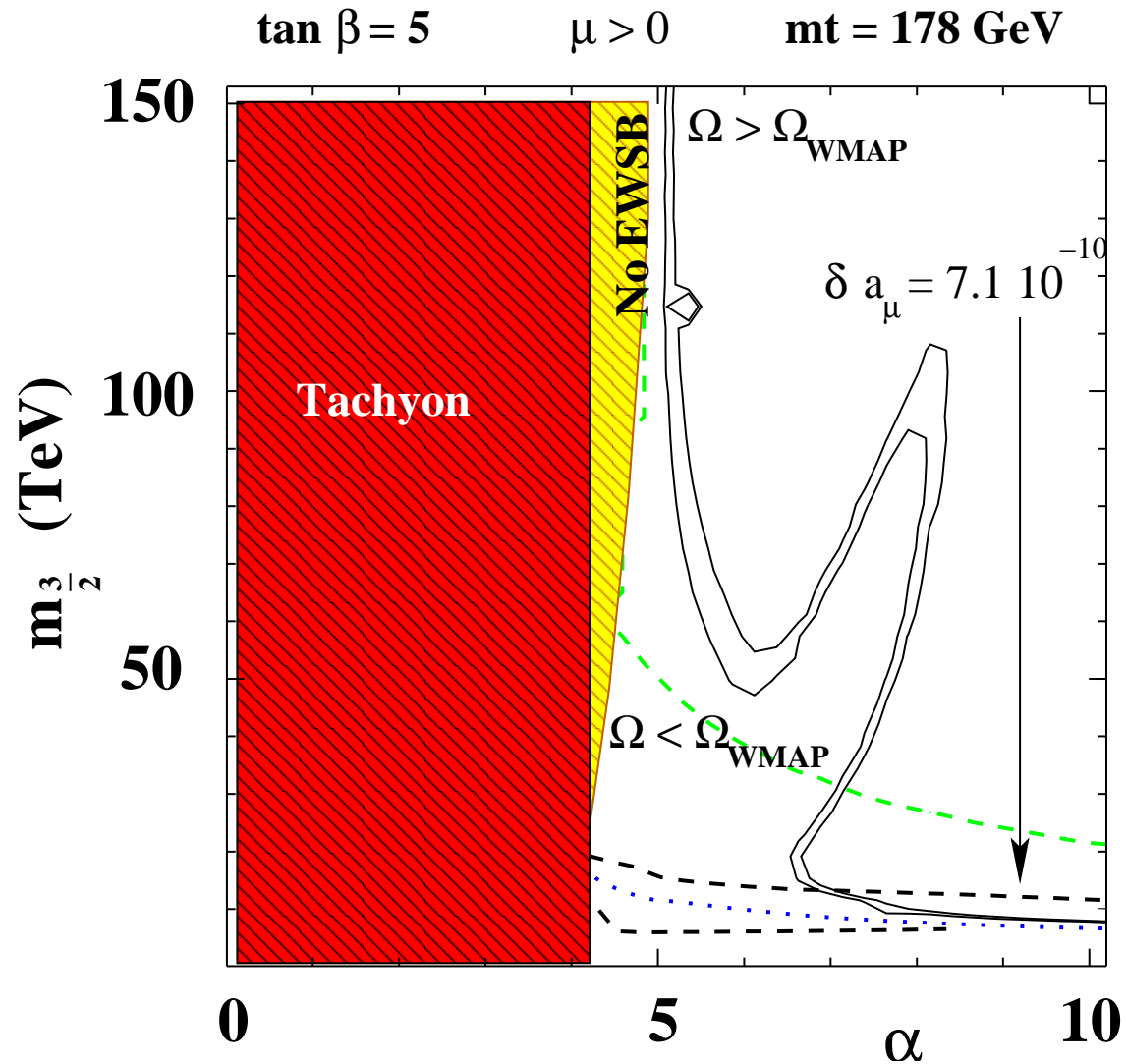
(Lebedev, HPN, Ratz, 2006; Dine, Kitano, Morisse, Shirman, 2006)

# Dark Matter



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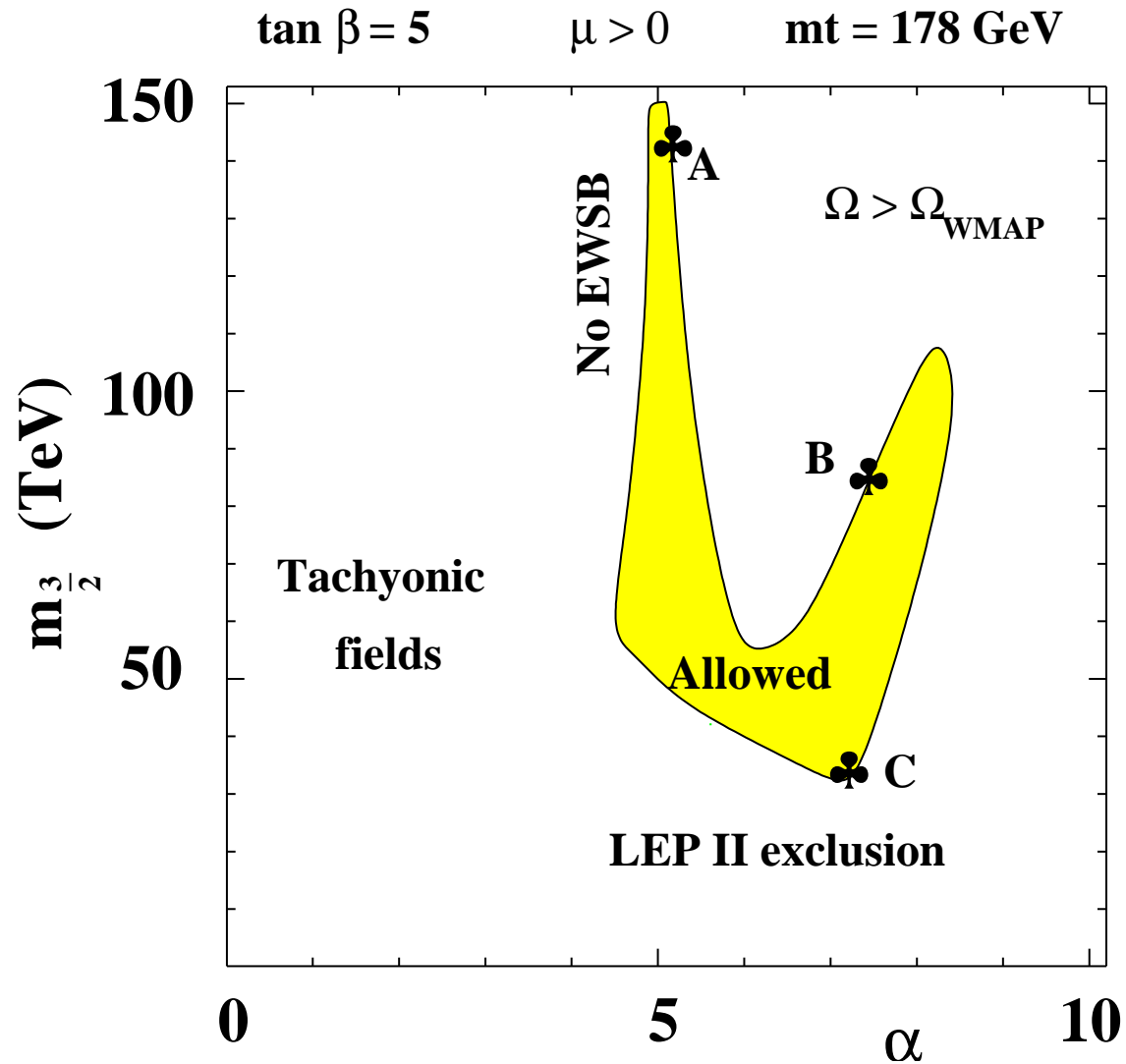
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# Dark Matter

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# The “MSSM hierarchy problem”

The scheme predicts a rather high mass scale

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- rather high mass for the LSP-Neutralino

Thus we might worry about a **fine-tuning** to obtain

- the mass of the weak scale around 100 GeV from

$$\frac{m_Z^2}{2} = -\mu^2 + \frac{m_{H_d}^2 - m_{H_u}^2 \tan^2 \beta}{\tan^2 \beta - 1},$$

and there are large corrections to  $m_{H_u}^2$  .....

(Choi, Jeong, Kobayashi, Okumura, 2005)

# The “MSSM hierarchy problem” solved?

The influence of the various soft terms is given by

$$m_Z^2 \simeq -1.8 \mu^2 + 5.9 M_3^2 - 0.4 M_2^2 - 1.2 m_{H_u}^2 + 0.9 m_{q_L^{(3)}}^2 + \\ + 0.7 m_{u_R^{(3)}}^2 - 0.6 A_t M_3 + 0.4 M_2 M_3 + \dots ,$$

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Mirage mediation improves the situation

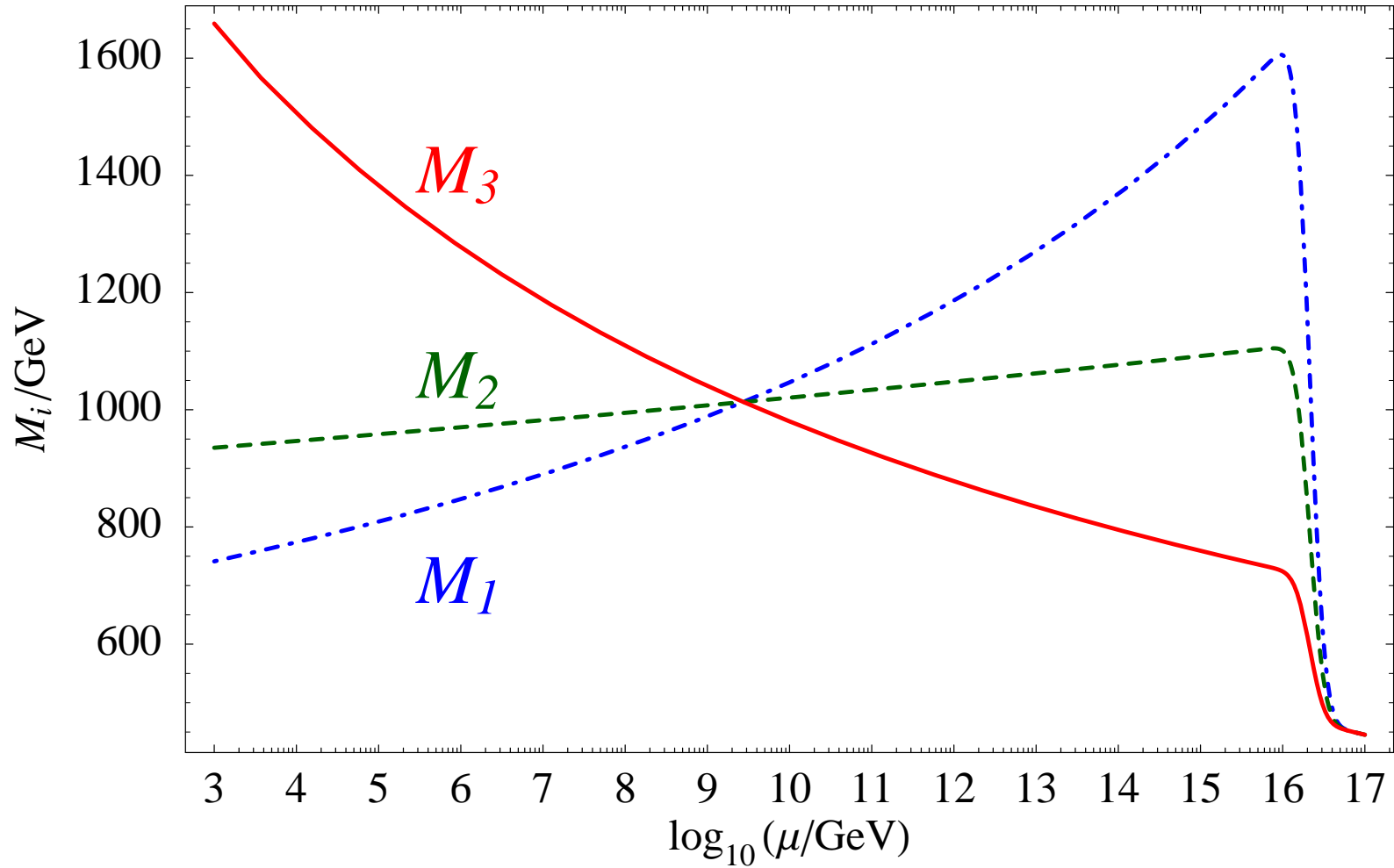
- especially for **small  $\alpha$**
- because of a **reduced gluino mass**

(Choi, Jeong, Kobayashi, Okumura, 2005)

- explicit model building required

(Lebedev, HPN, Ratz, 2005; Pierce, Thaler, 2006)

# The Mirage Scale



(Lebedev, HPN, Ratz, 2005)

# Explicit schemes

The different schemes depend on the mechanism of uplifting:

- **uplifting with anti D3 branes**

(Kachru, Kallosh, Linde, Trivedi, 2003)

- $\alpha \sim 5$  in the original KKLT scenario leading to
- a **mirage scale** of approximately  $10^{11}$  GeV

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- **de Sitter vacua from matter superpotentials**

(Lebedev, HPN, Ratz, 2006)

- allows a continuous variation of  $\alpha$
- leads to new contributions for sfermion masses



# Conclusion

Mirage Mediation naturally appears in string theory models with background fluxes and gaugino condensation. It

- relieves cosmological problems of moduli and gravitino
- partially solves the Susy-flavour and CP problem
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It avoids

- the problems of conventional schemes like anomaly and modulus mediation
- gives a consistent picture with **very few parameters**

# Conclusion

The **source of Mirage Mediation** is the appearance of a small parameter

$$X^{-1} \sim \log(m_{3/2}/M_{\text{Planck}})$$

that leads to a (heavy) superpartner spectrum exhibiting

- a little hierarchy  $m_X \sim \langle X \rangle m_{3/2} \sim \langle X \rangle^2 m_{\text{soft}}$
- a rather heavy gravitino mass
- and an **unusual relation** between the gaugino masses.

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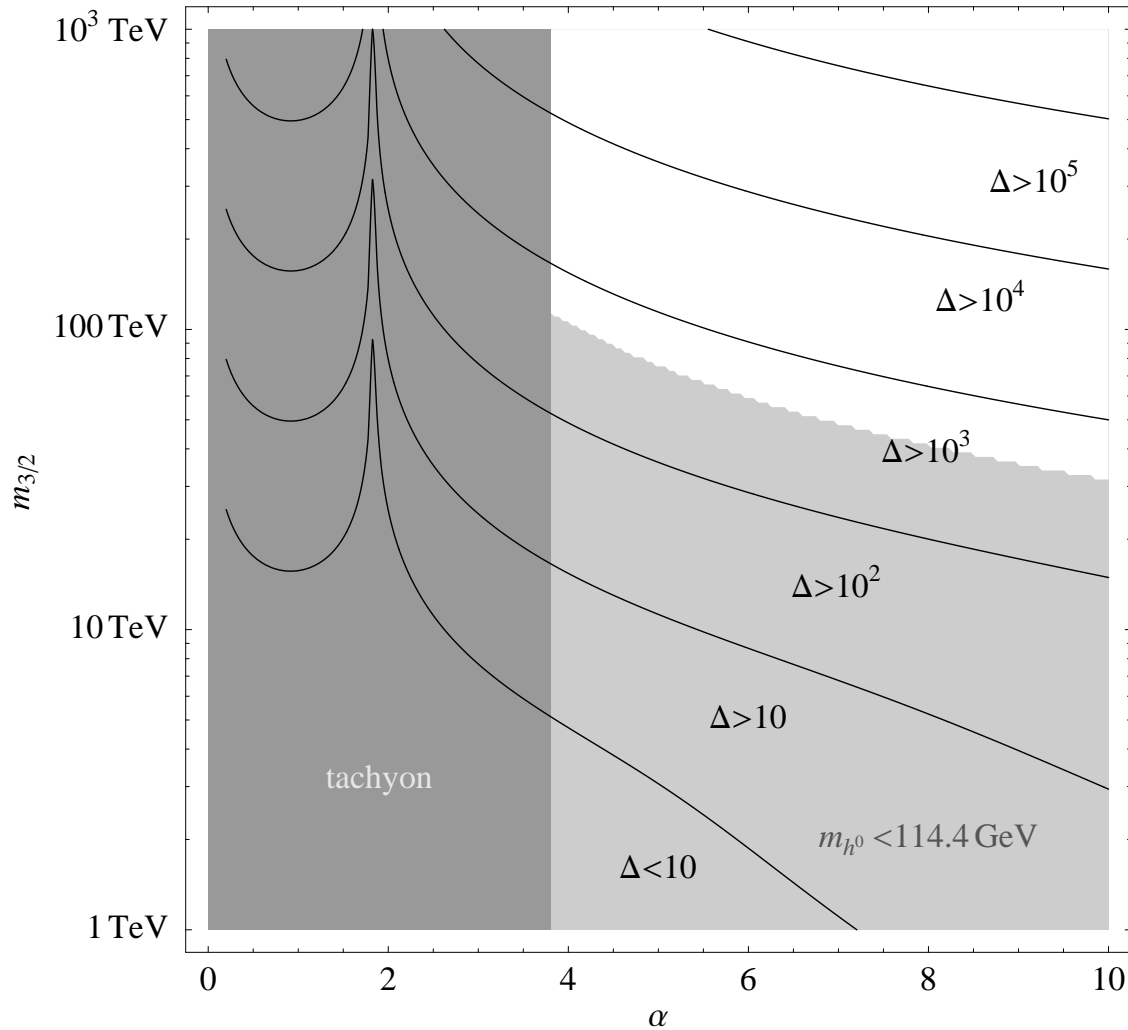
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**Mirage Mediation provides a distinct pattern of soft terms that could be tested at the LHC!**

# Sensitivity of the weak scale



(Lebedev, HPN, Ratz, 2005)