

**I(SM)<sup>2</sup>**  
INSTITUTE FOR SOFT MATTER  
SYNTHESIS AND METROLOGY



# Oobleck Exposed! Microscopic Measurements of Shear Thickening Fluids

Daniel Blair, Vikram Rathee, Jeff Urbach

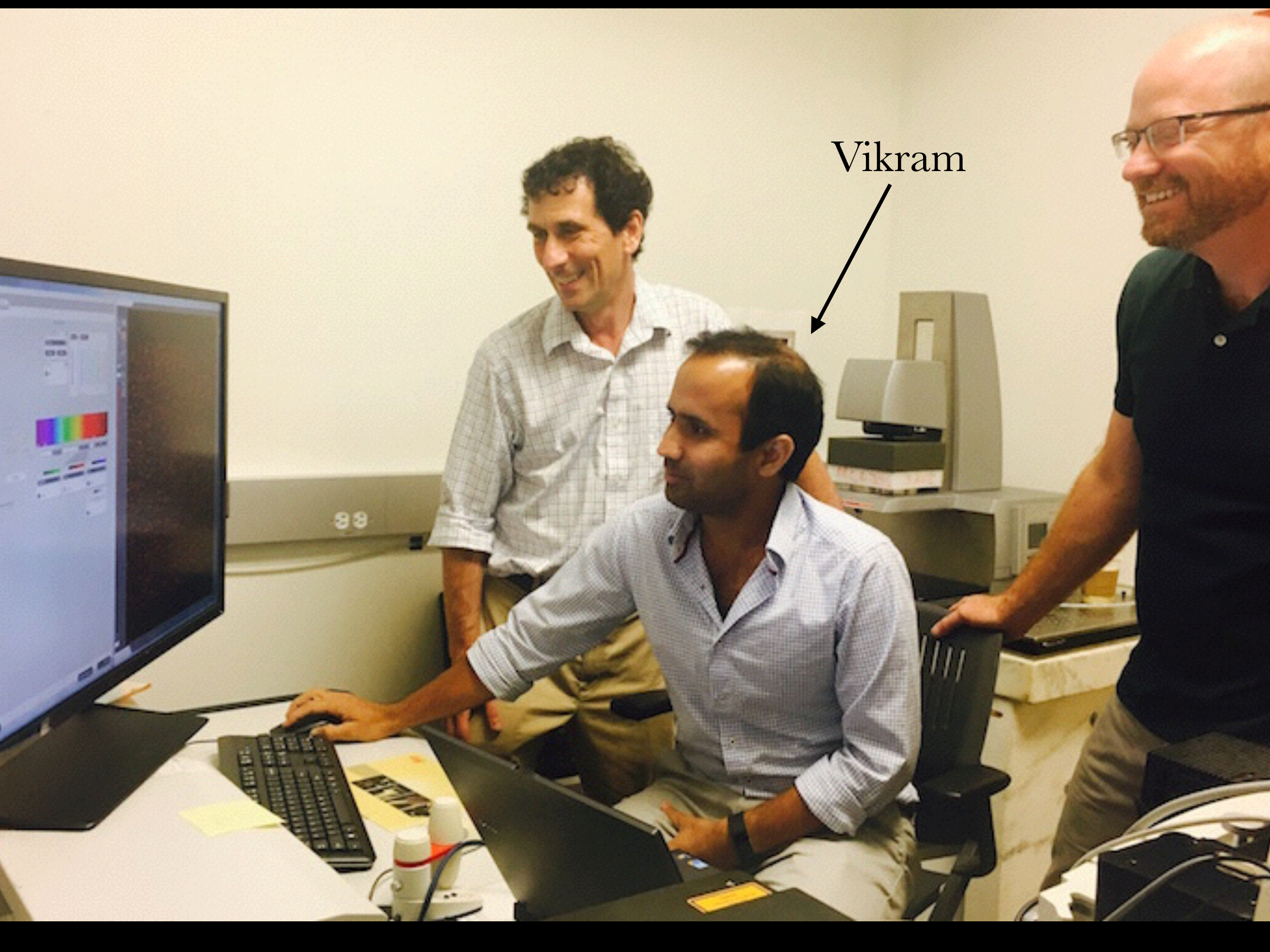
Georgetown University

Department of Physics

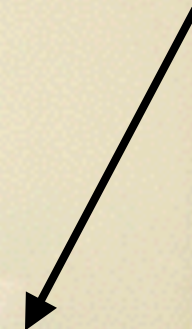
Institute for Soft Matter Synthesis and Metrology

<http://blairlab.georgetown.edu>





Vikram











“If yo don’t know what you’re talking about  
just show a lot of fun animations and tell jokes”  
-Itai Cohen





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just show a lot of fun animations and tell jokes”

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“If you want to convince someone you know what  
you’re talking about, invent/use an acronym.”

-Itai Cohen

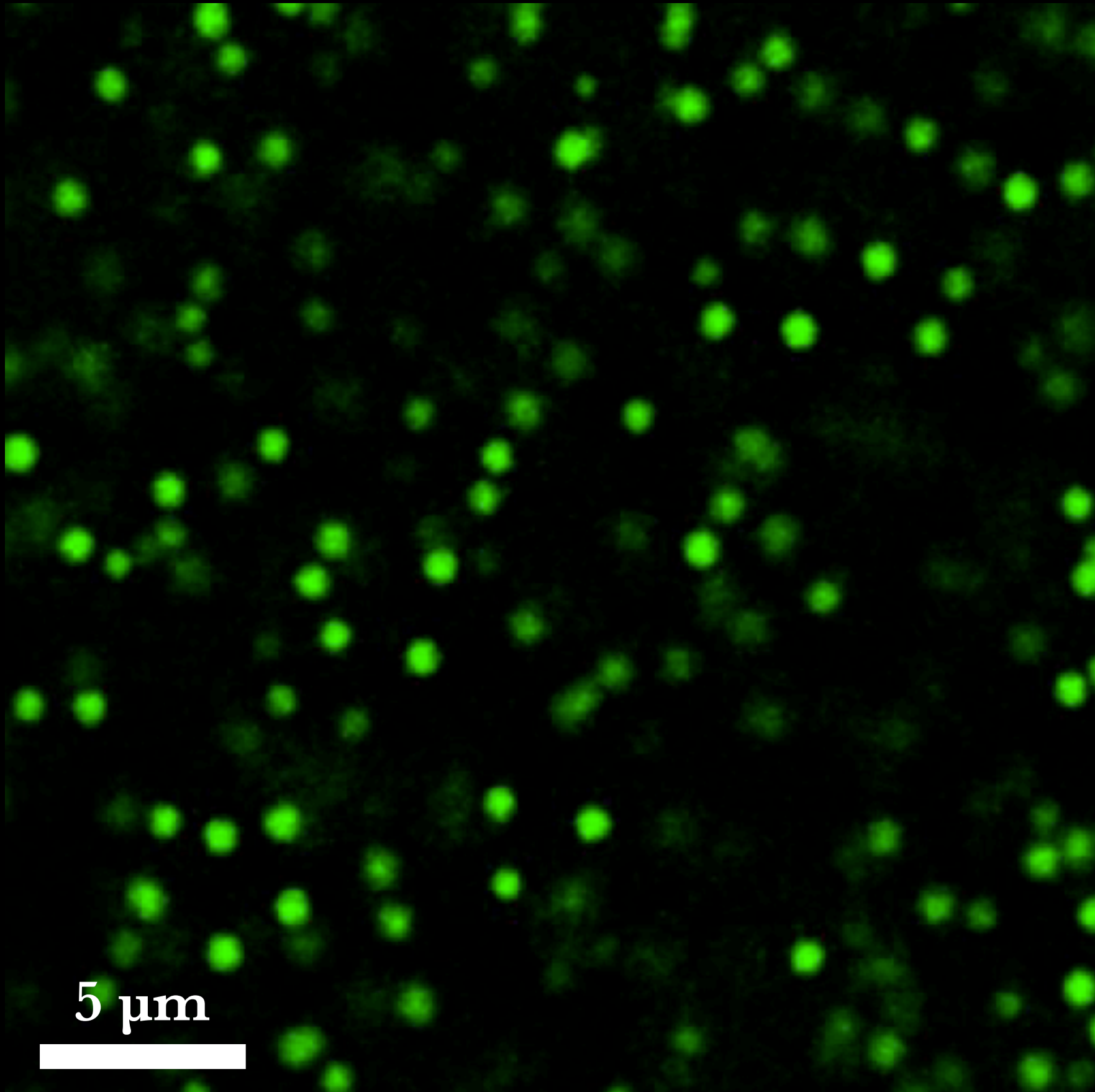


# Brief Outline

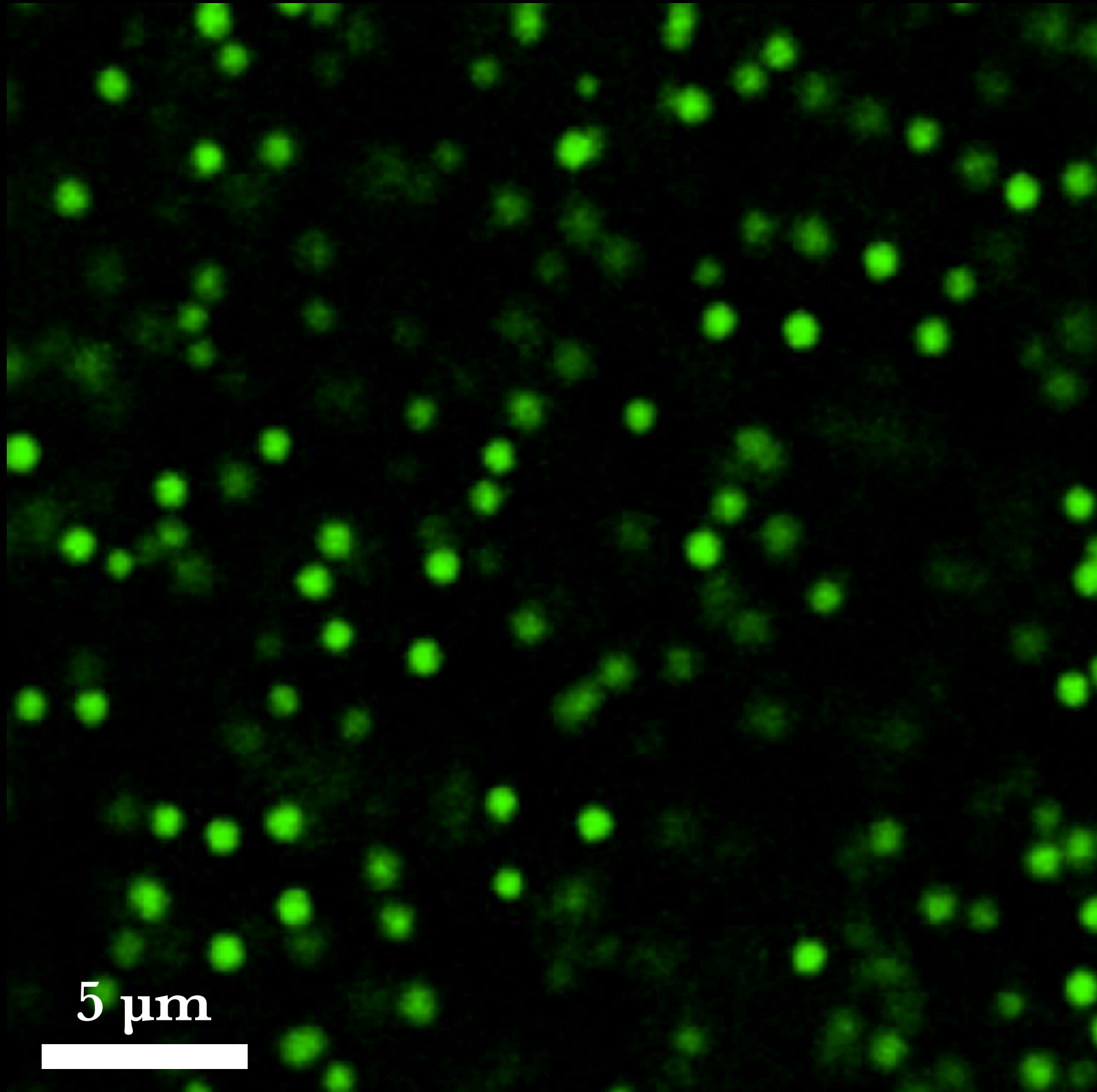
- Shear Thickening in Thermal Systems
- Boundary Stress Microscopy
- Colloid Science
- Shear Thickening Fluids (colloids)
  - Macroscopic Dynamics
  - Microscopic Understanding
- What's coming next...



# Colloidal Suspensions



# Colloidal Suspensions





# Central Dogma of Colloid Science



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# Central Dogma of Colloid Science

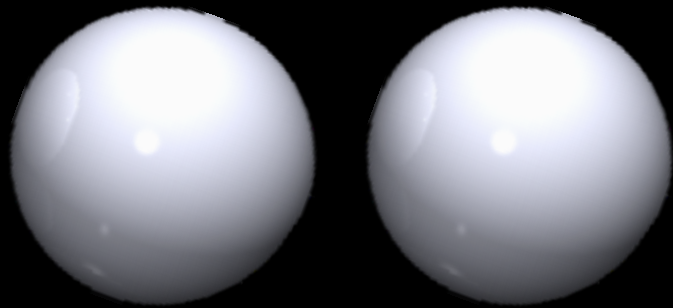
# Central Dogma of Colloid Science

Colloidal Particles “Stick” When in Contact



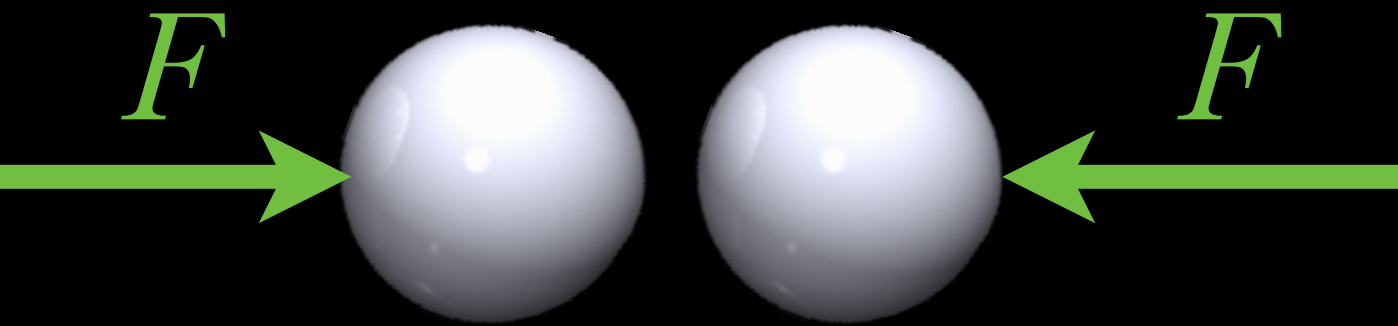
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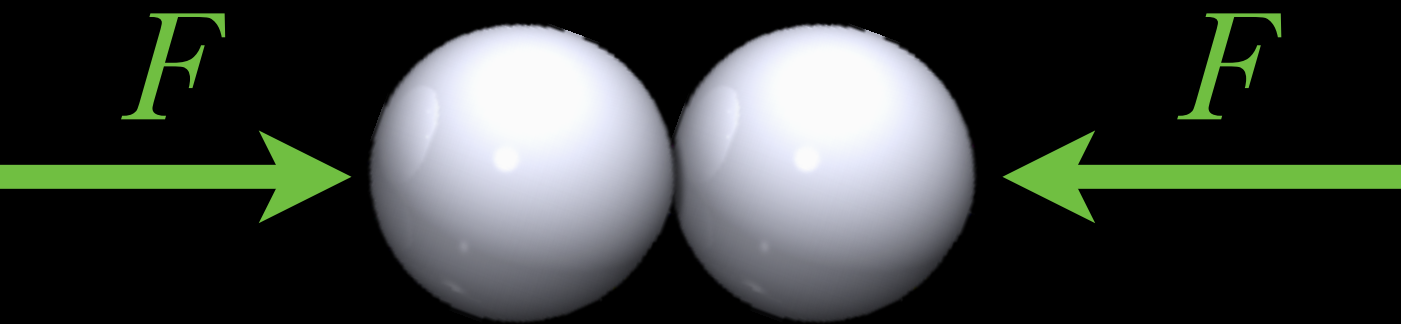
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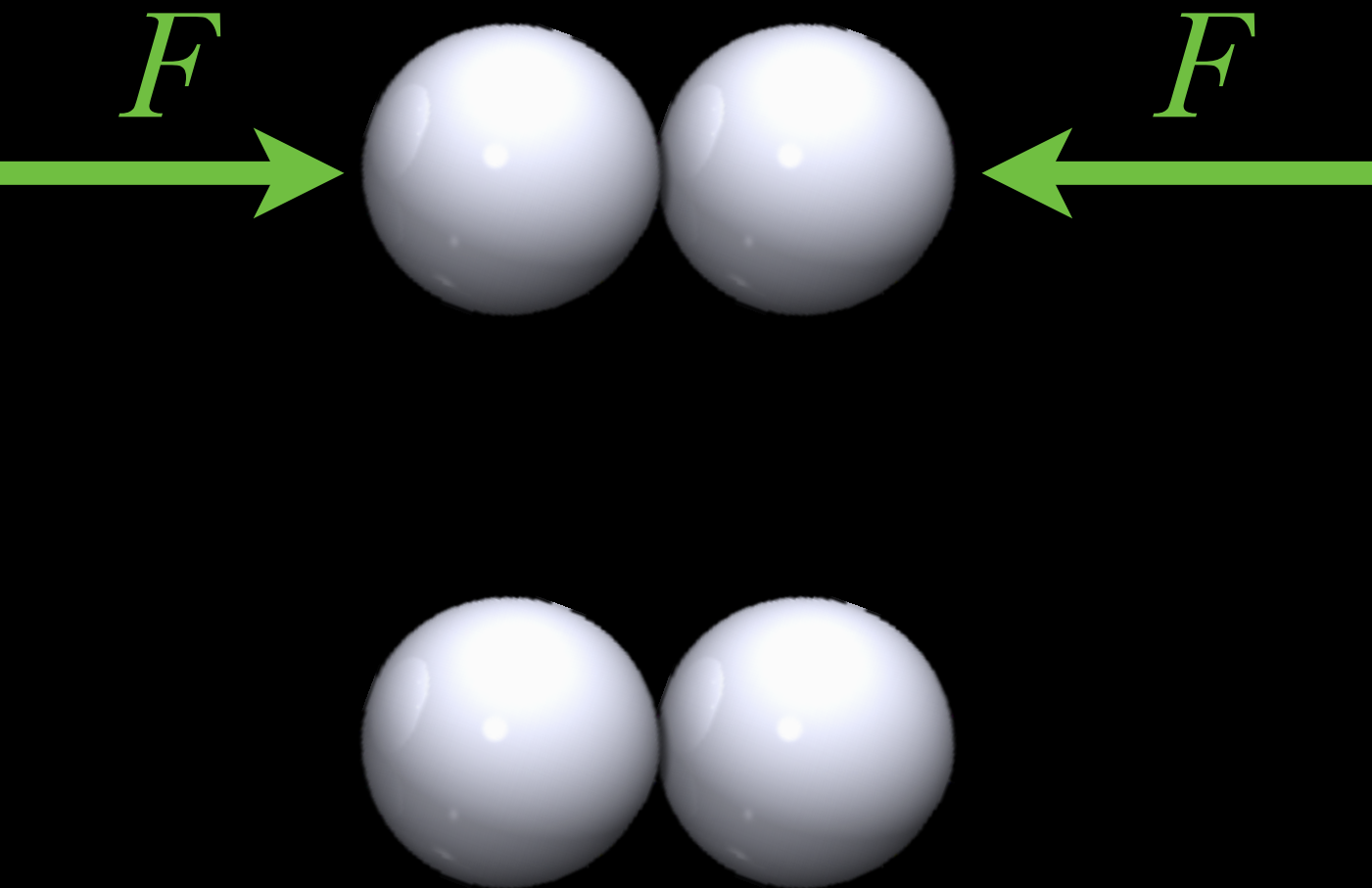
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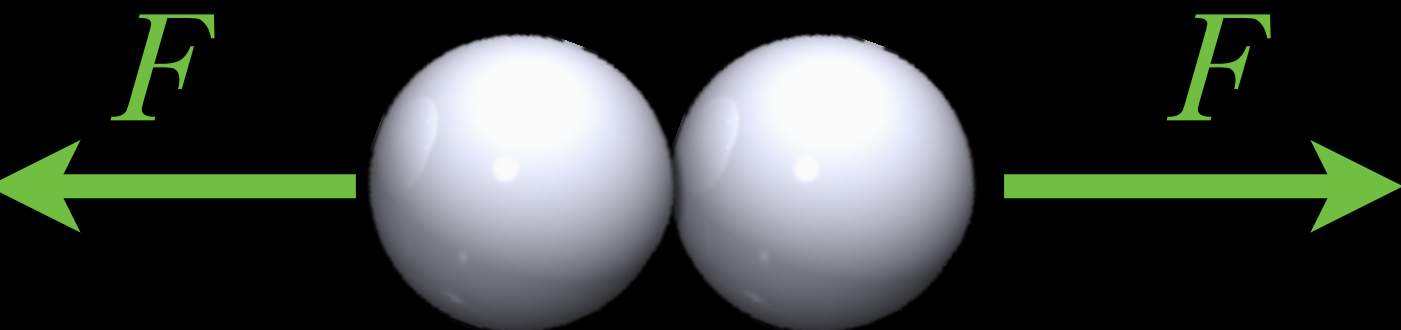
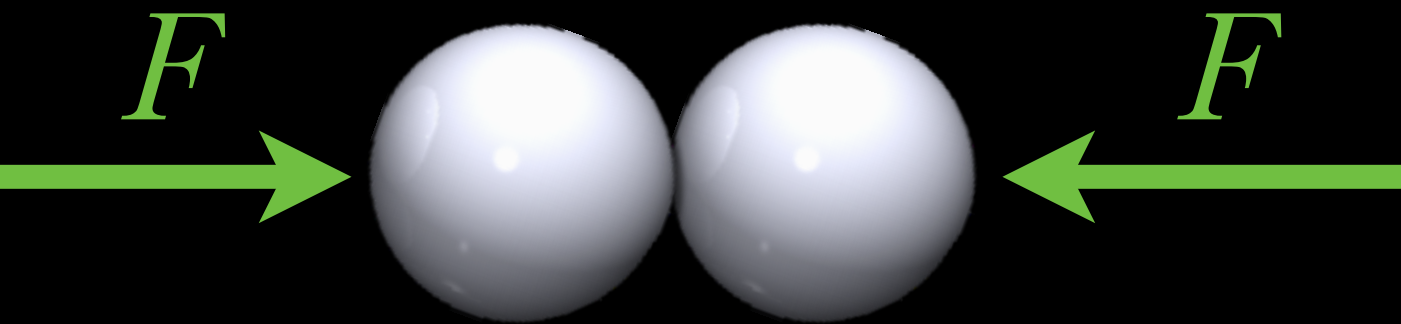
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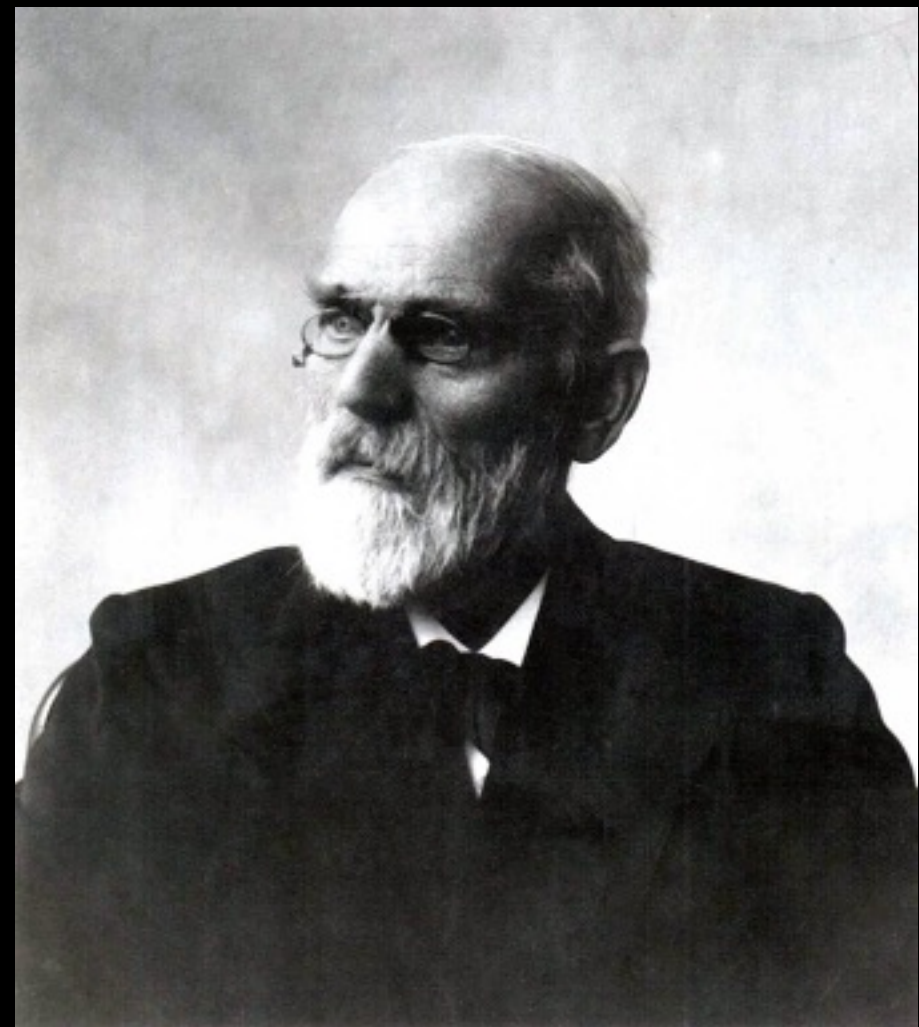
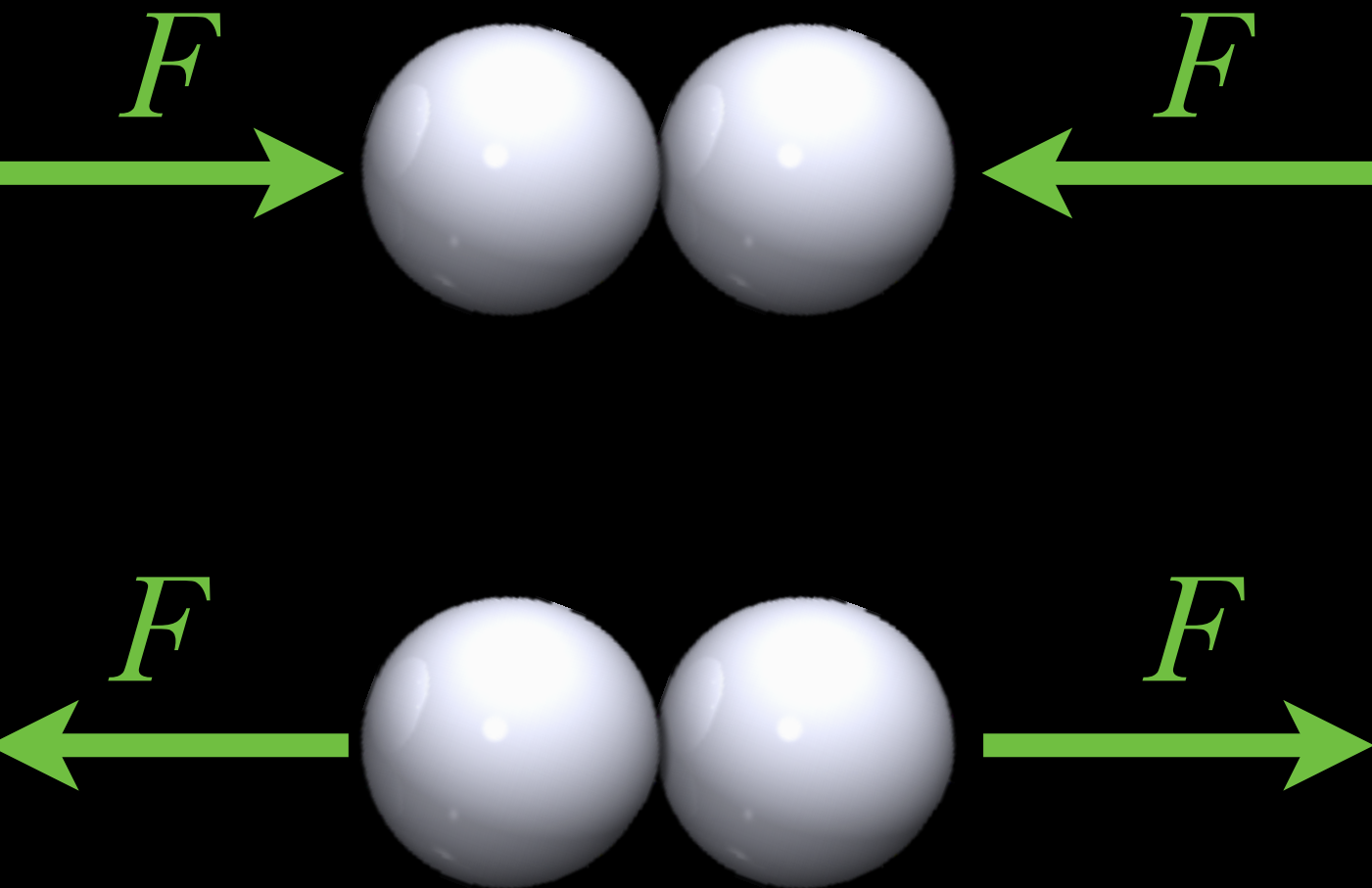
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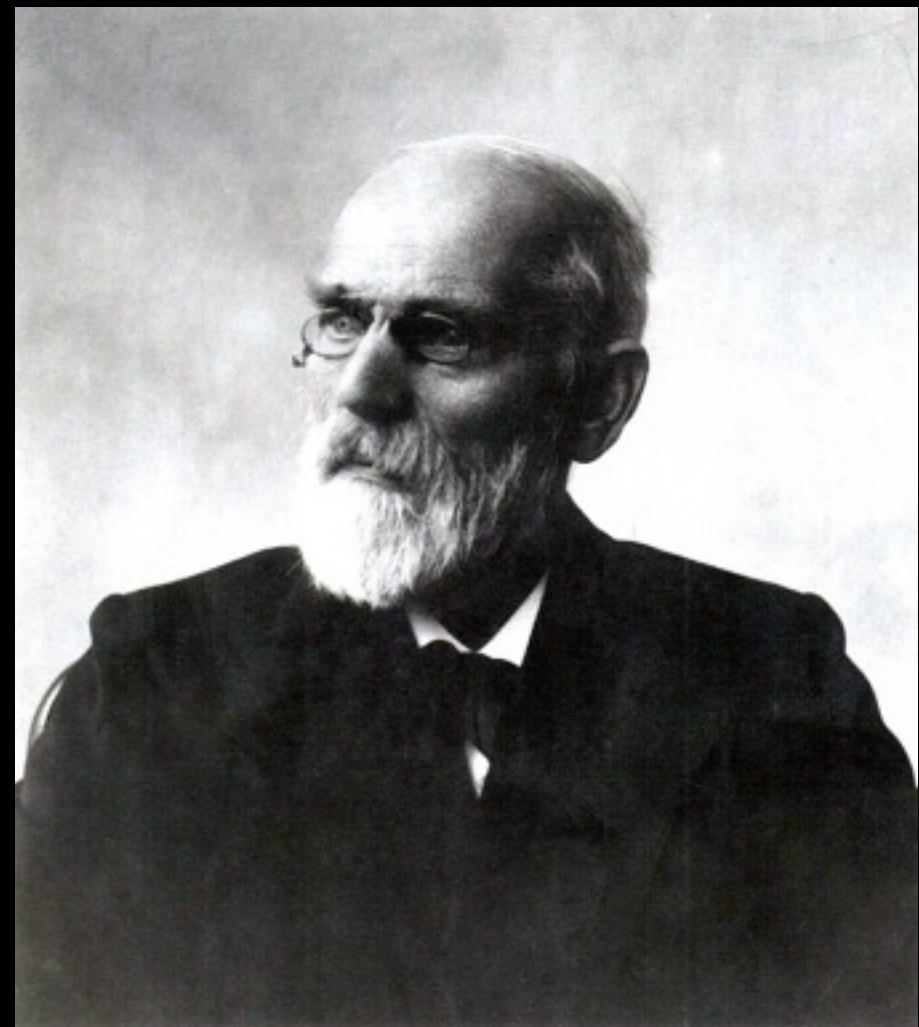
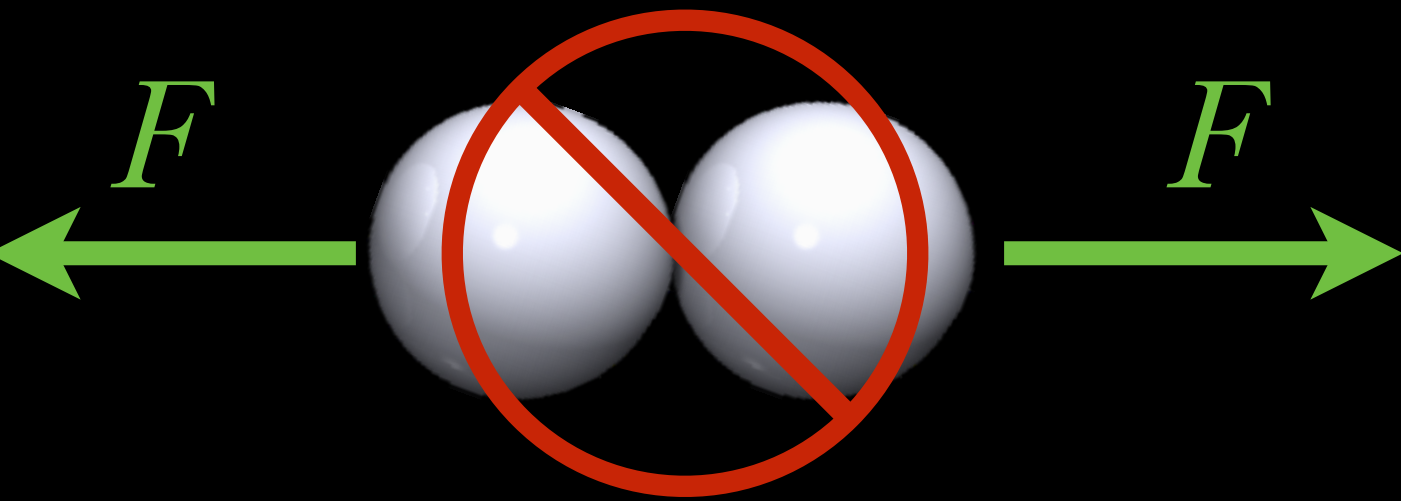
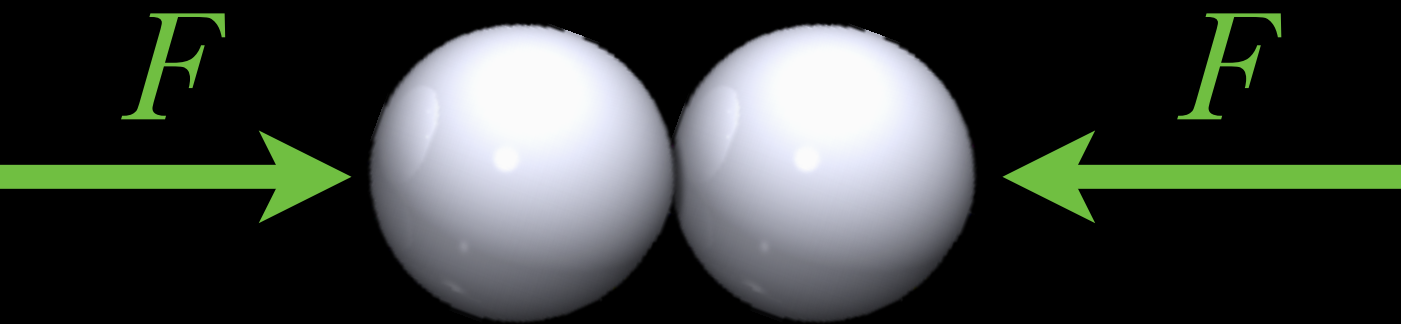
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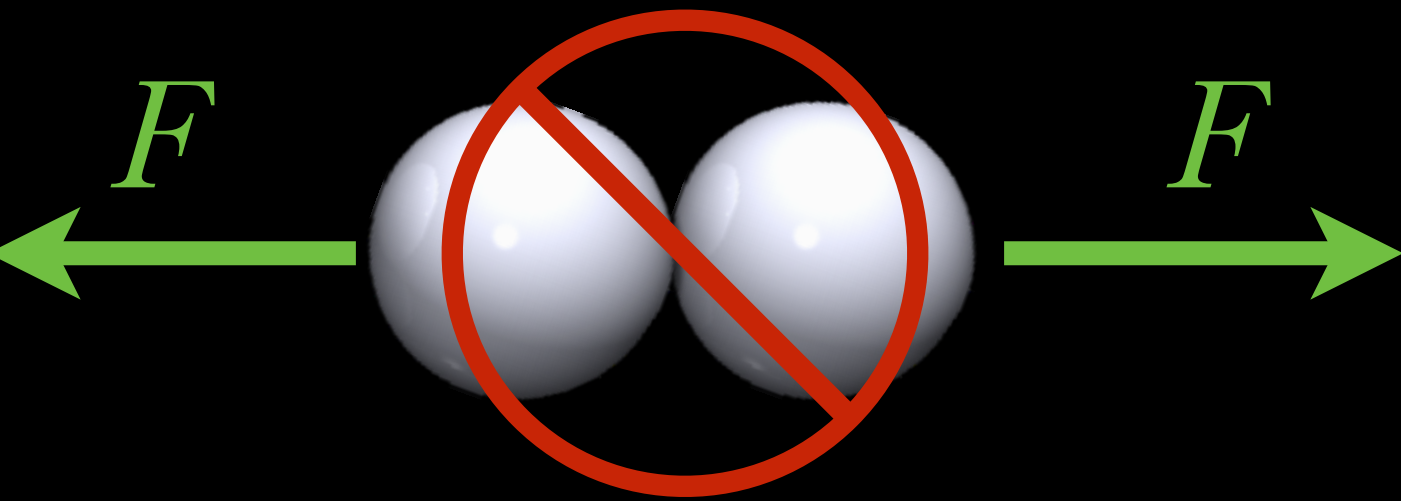
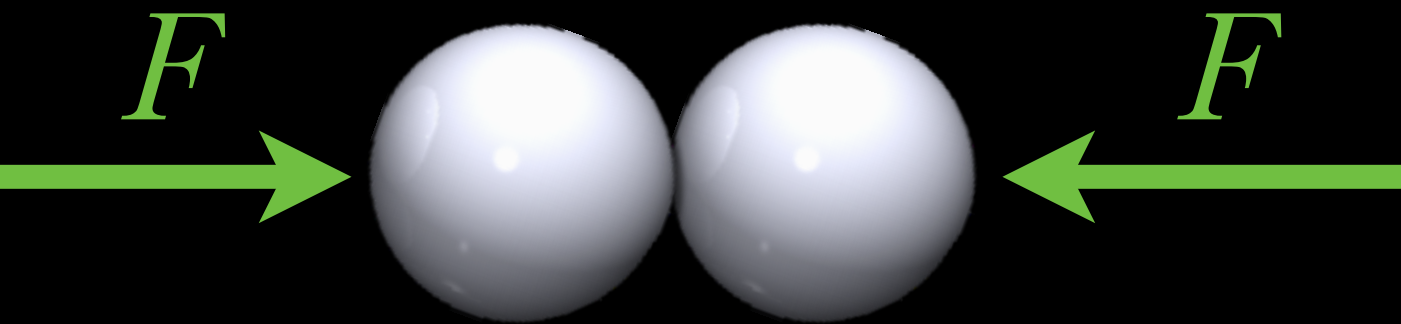
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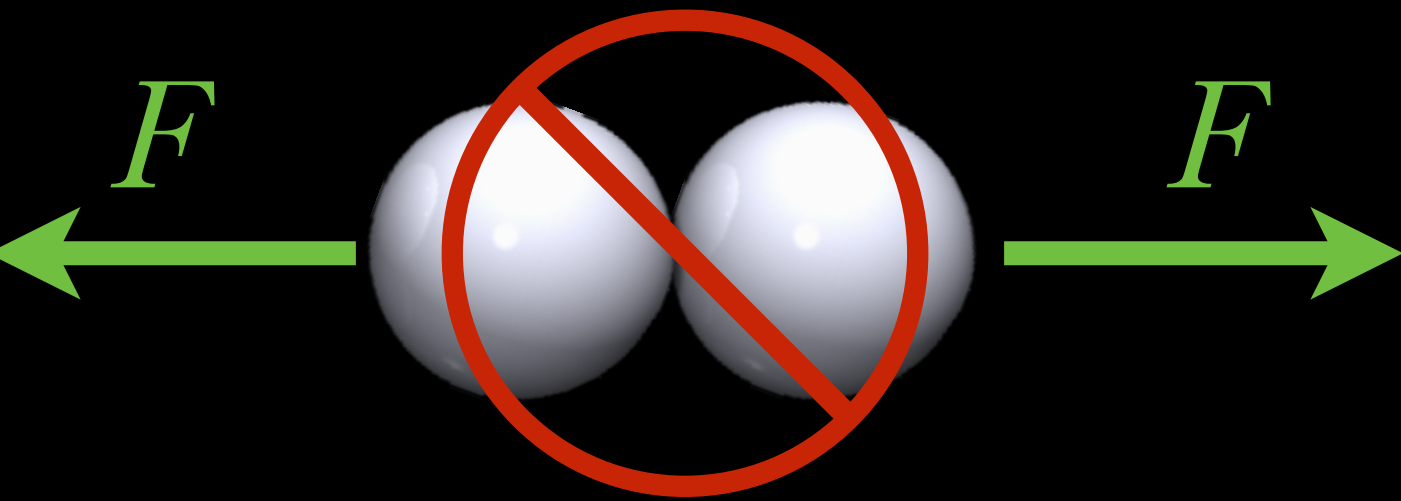
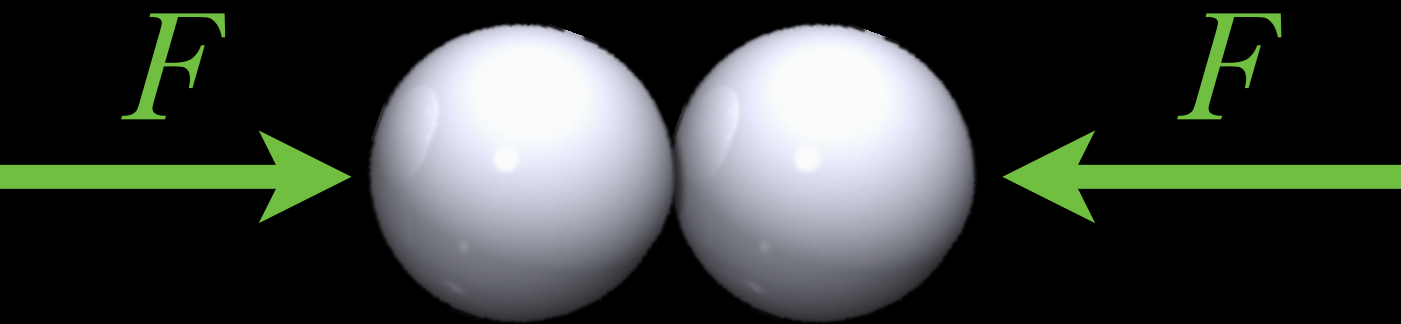
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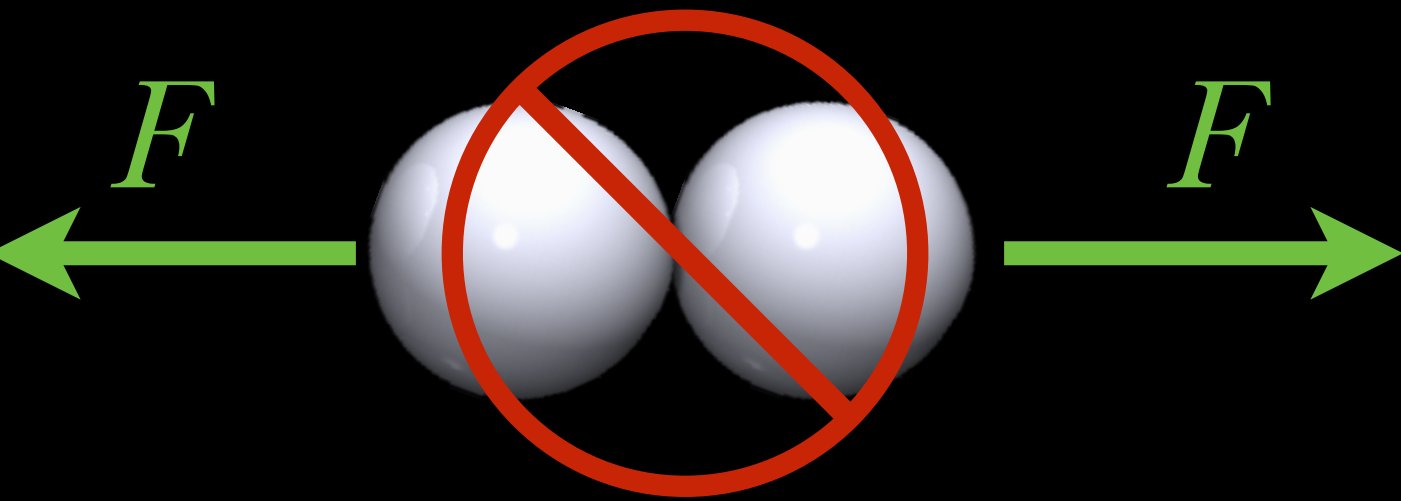
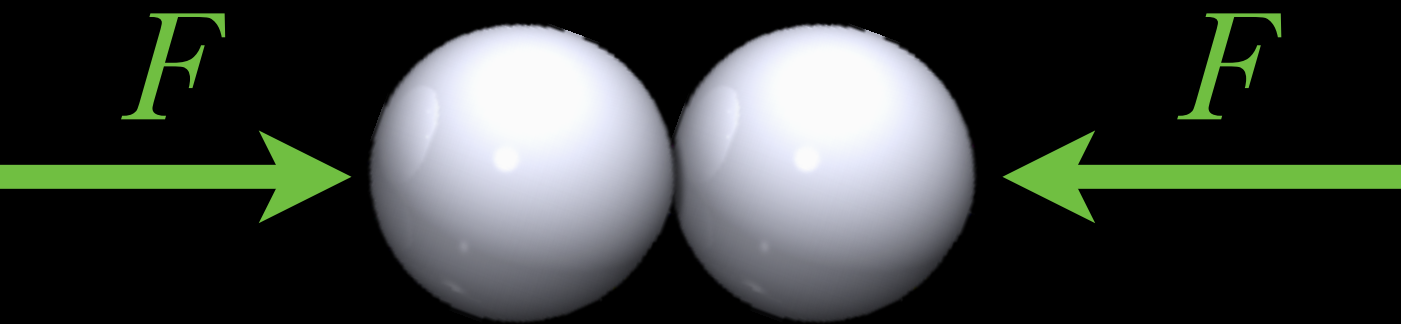
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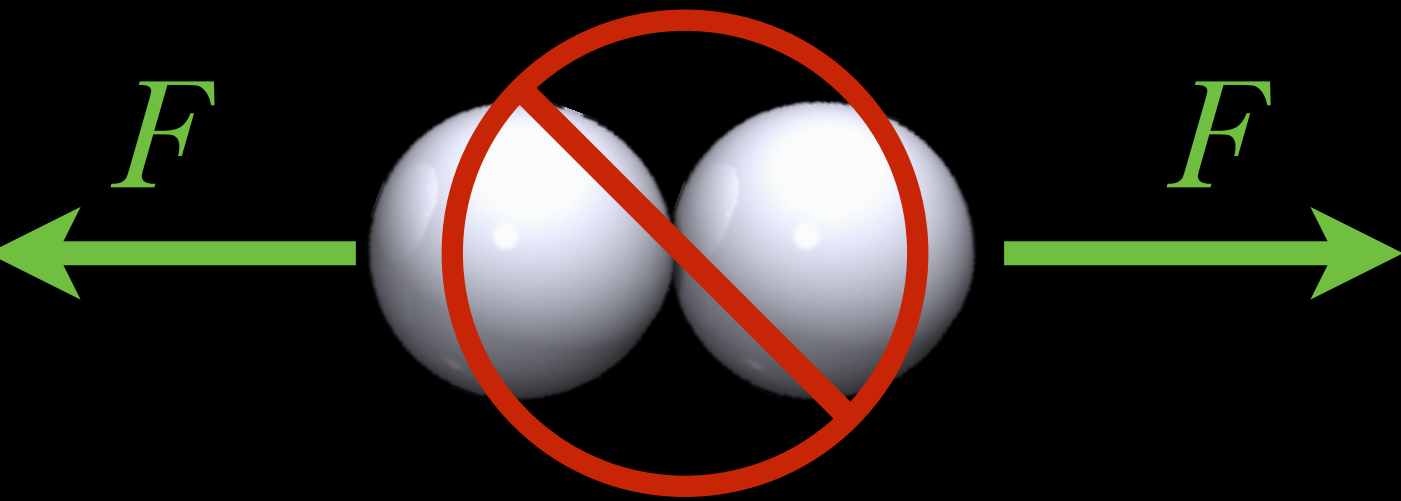
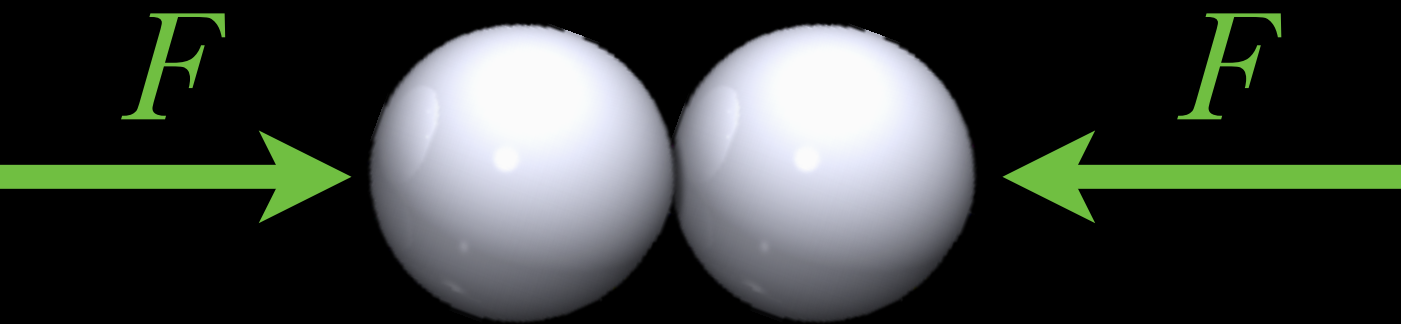
Colloidal Particles “Stick” When in Contact



*Q:* Can there be friction between colloids?

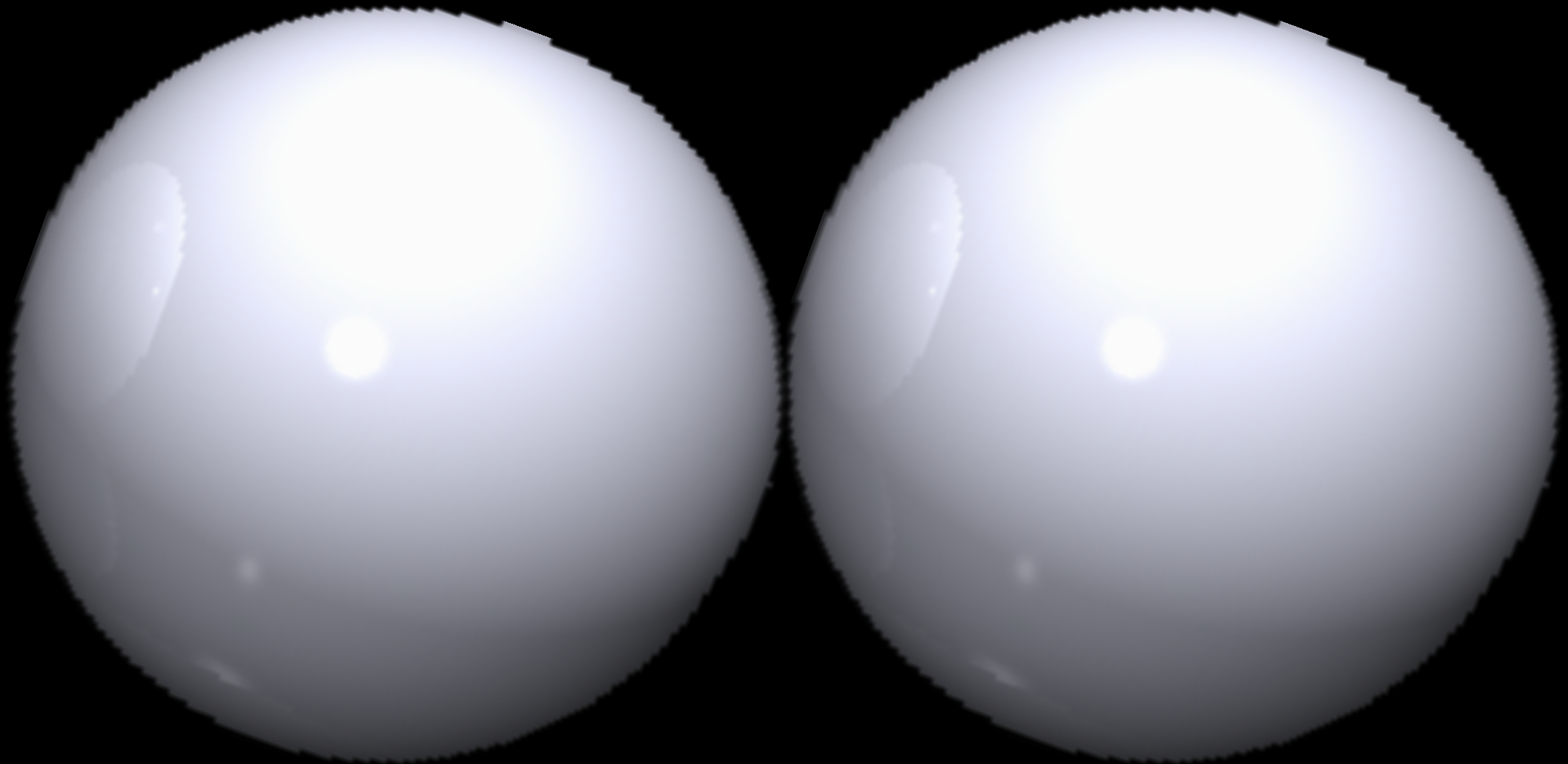
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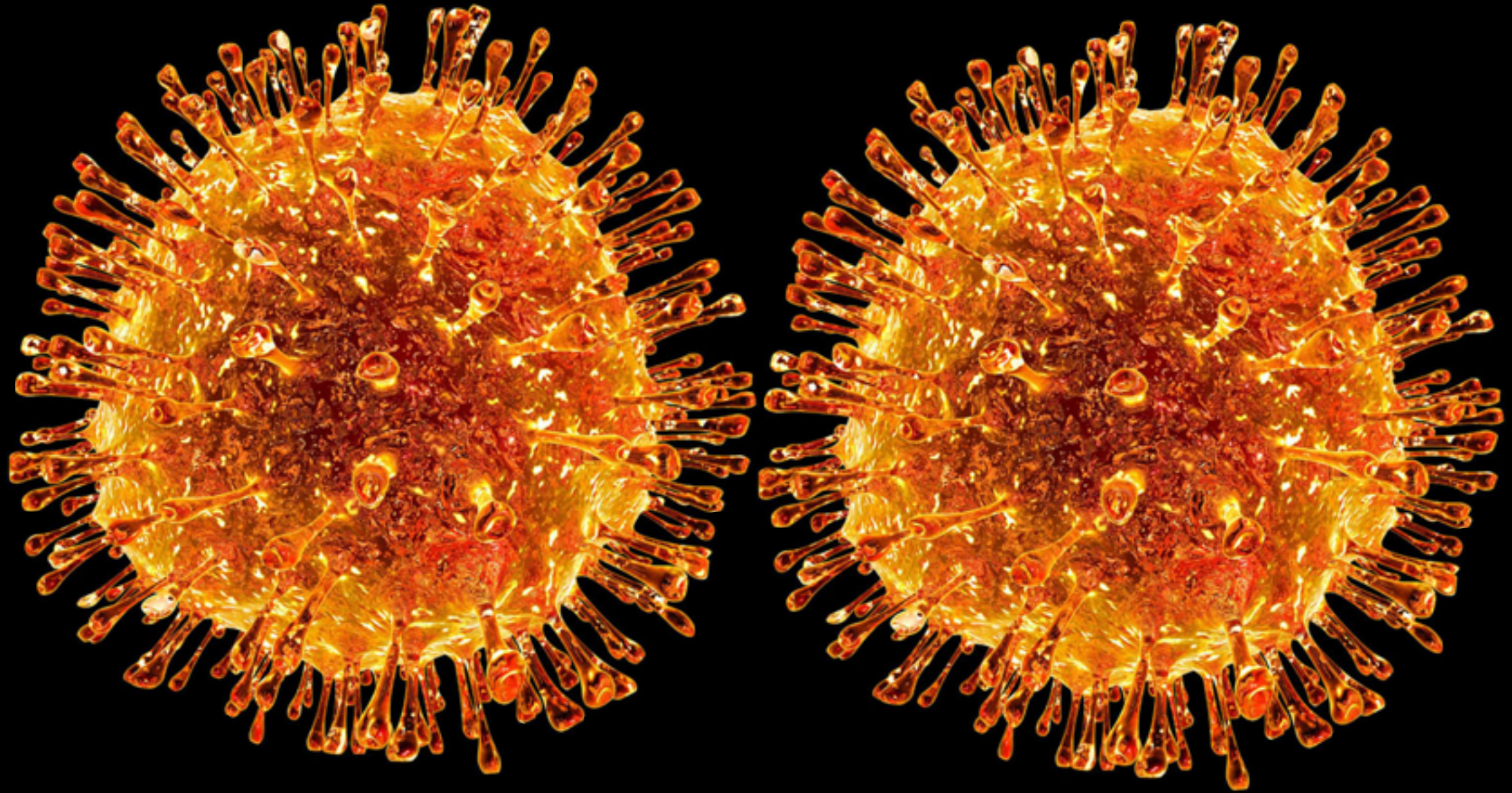
*Q:* Can there be friction between colloids? **Does it Matter?**

*Are hard spheres enough?*

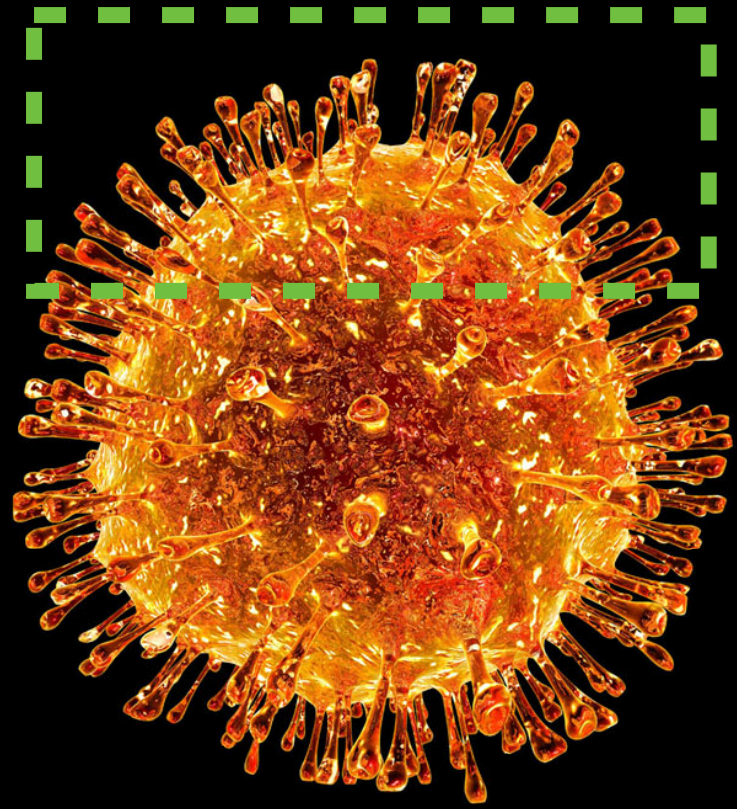


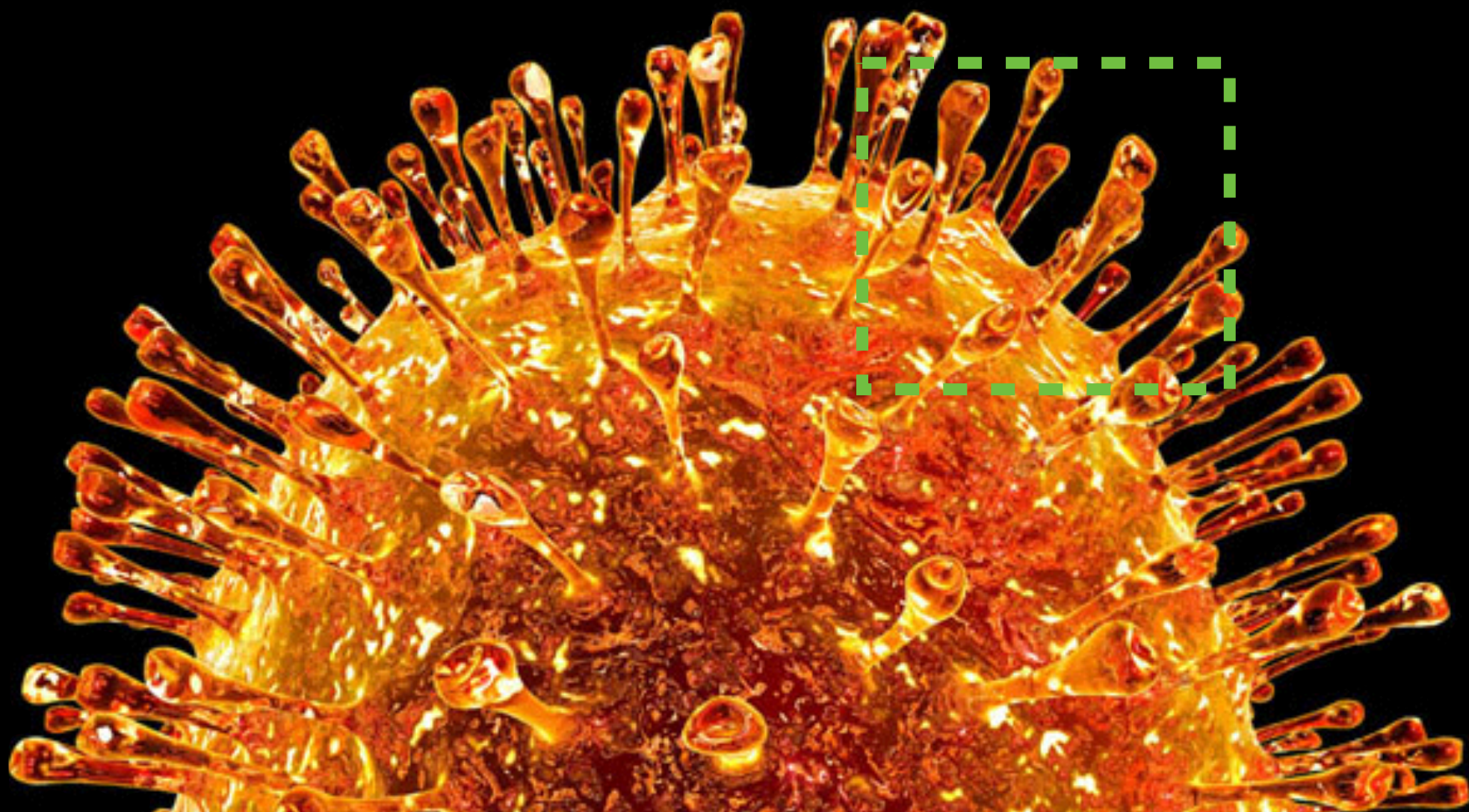


Are hard spheres enough?

















H1N1

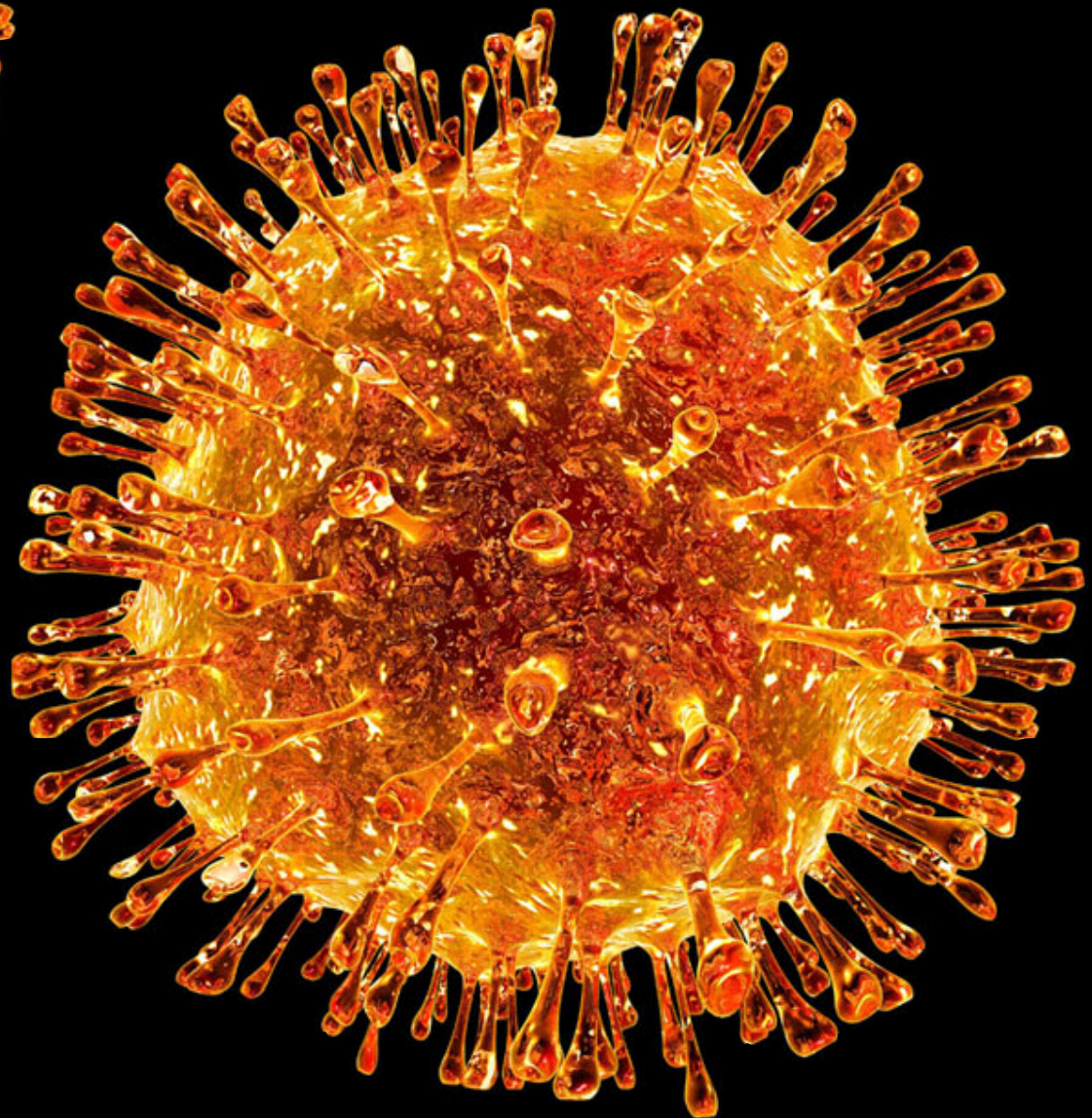
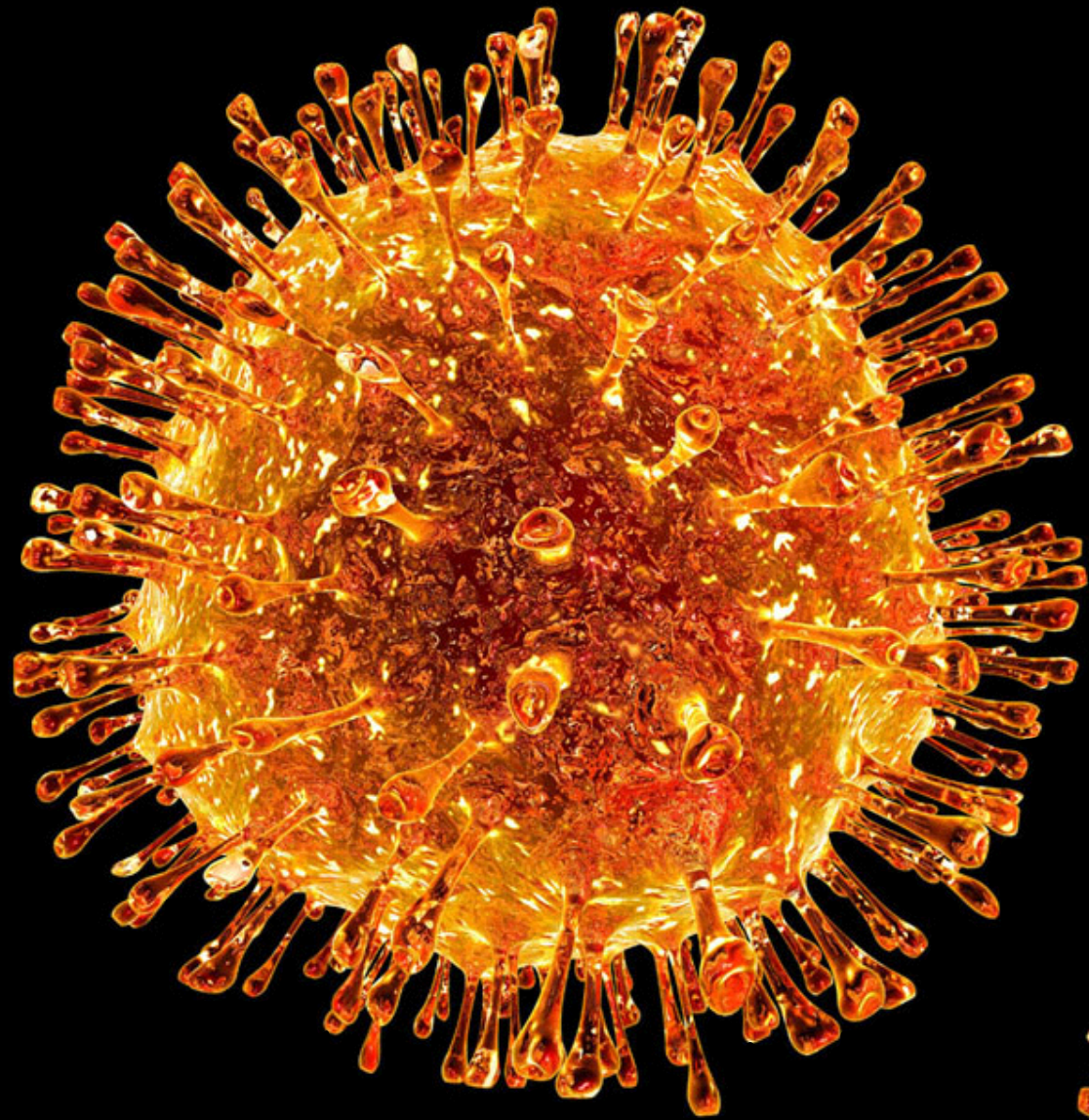




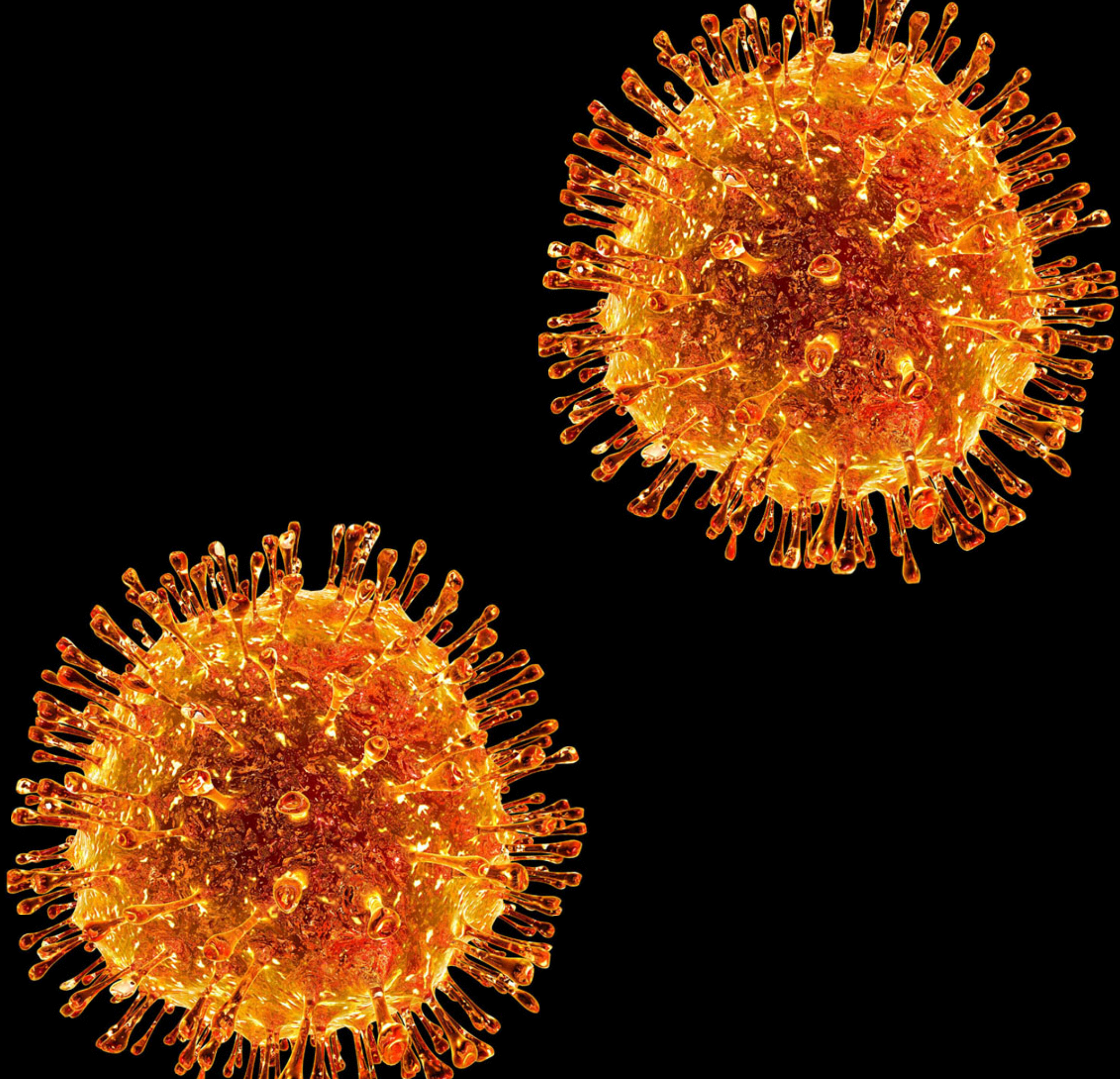
H1N1  
E  
I  
N  
R  
I  
C  
H



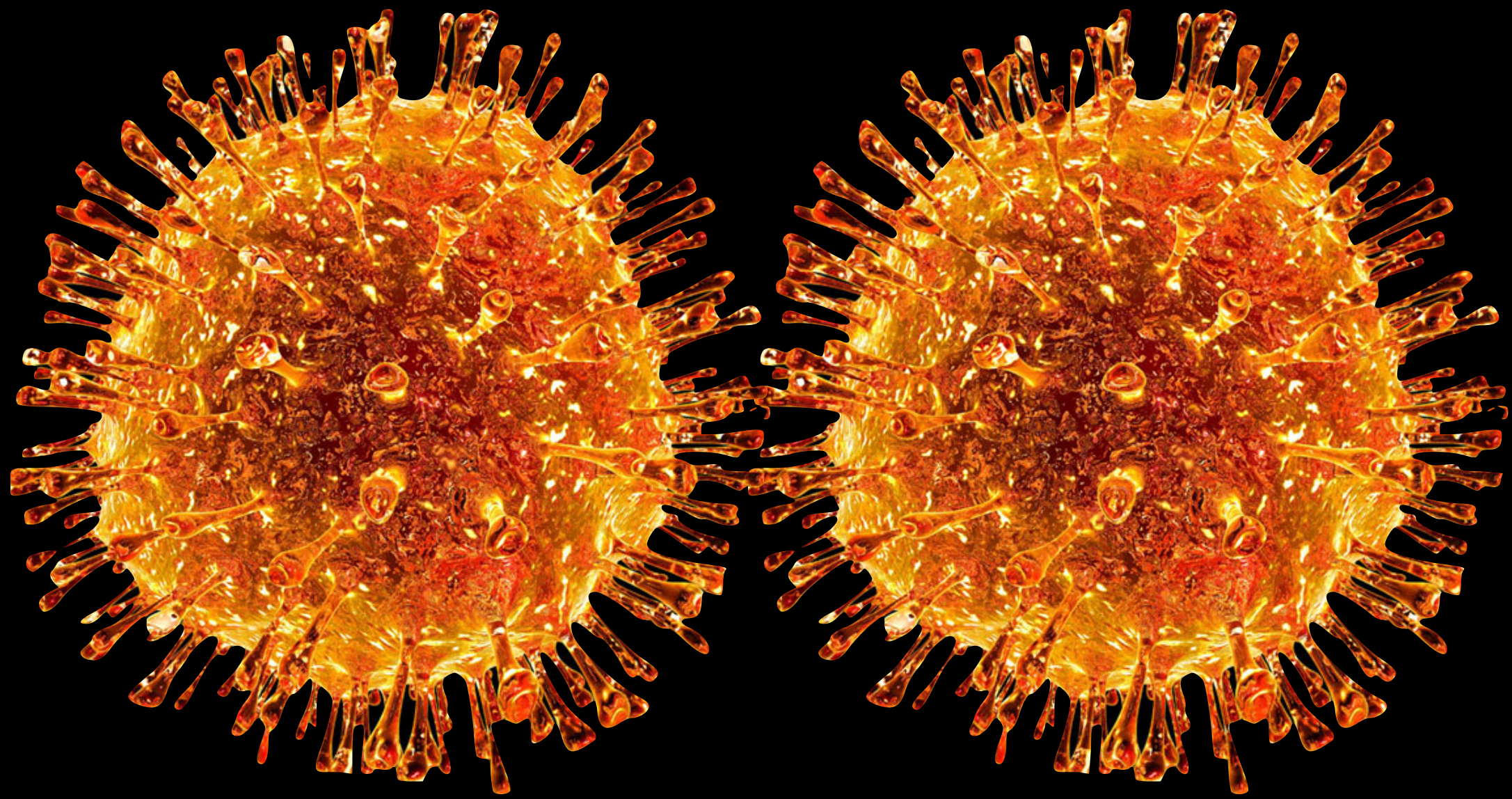




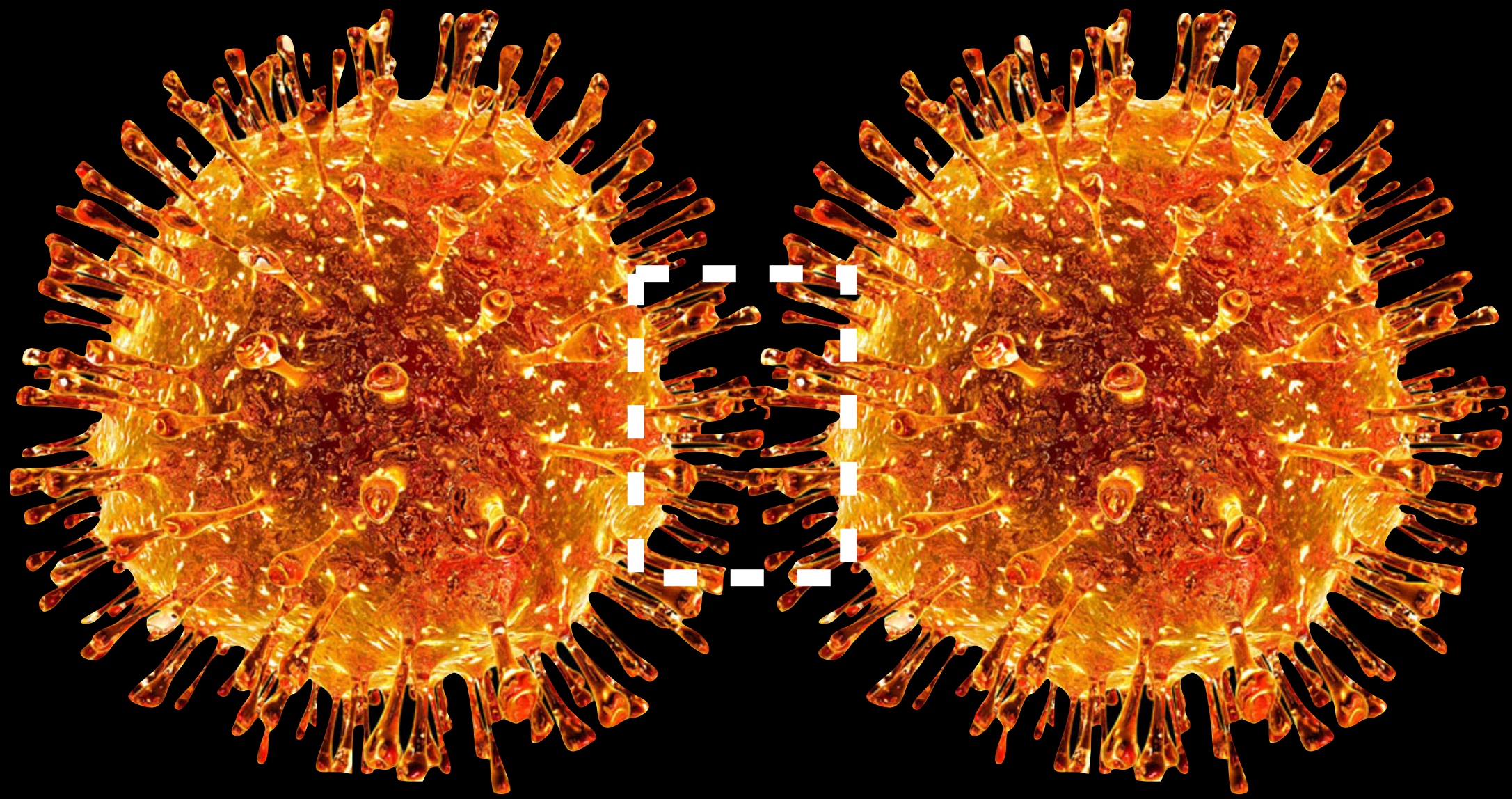




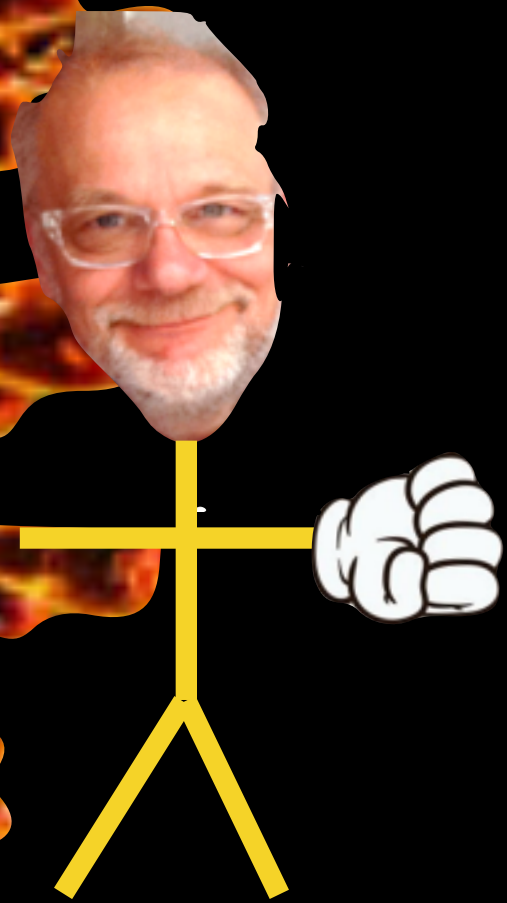
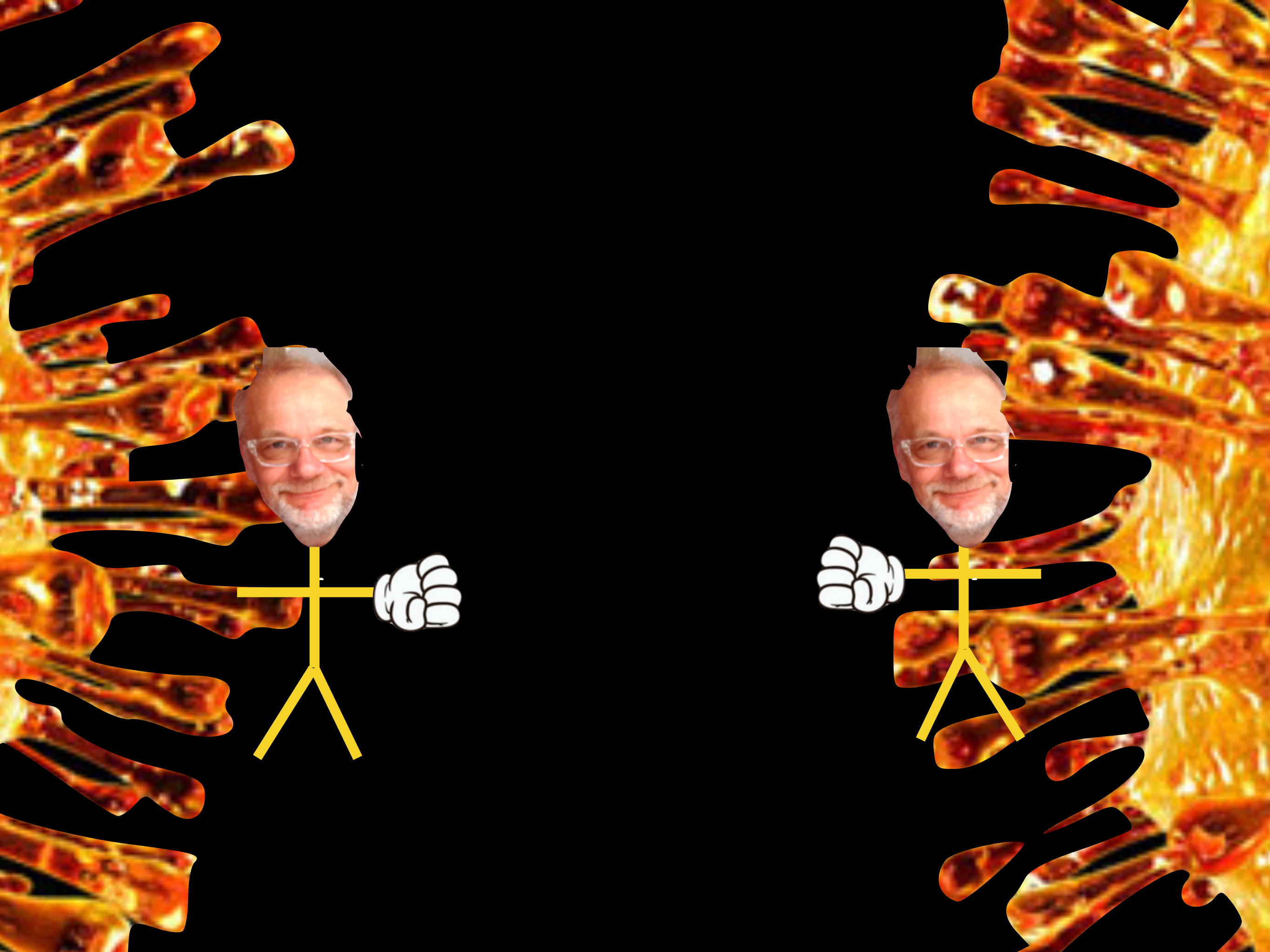




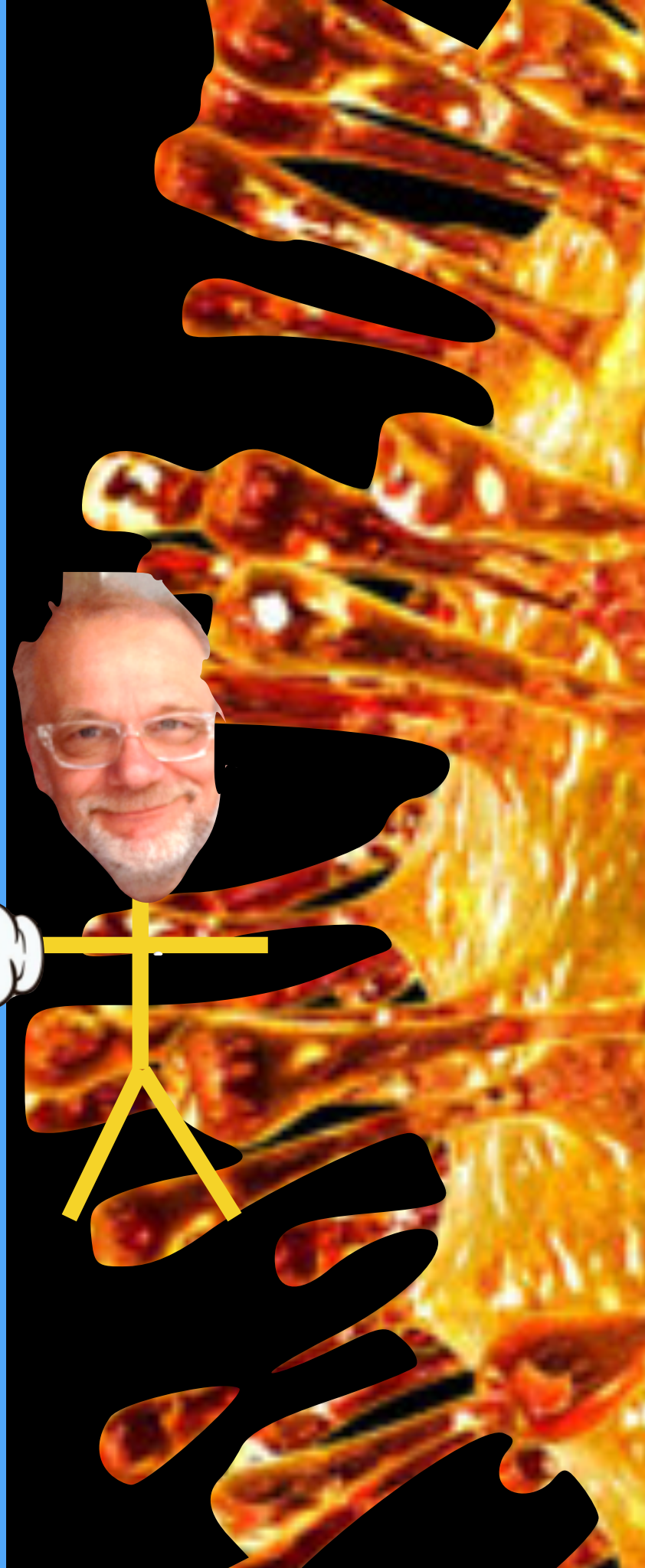
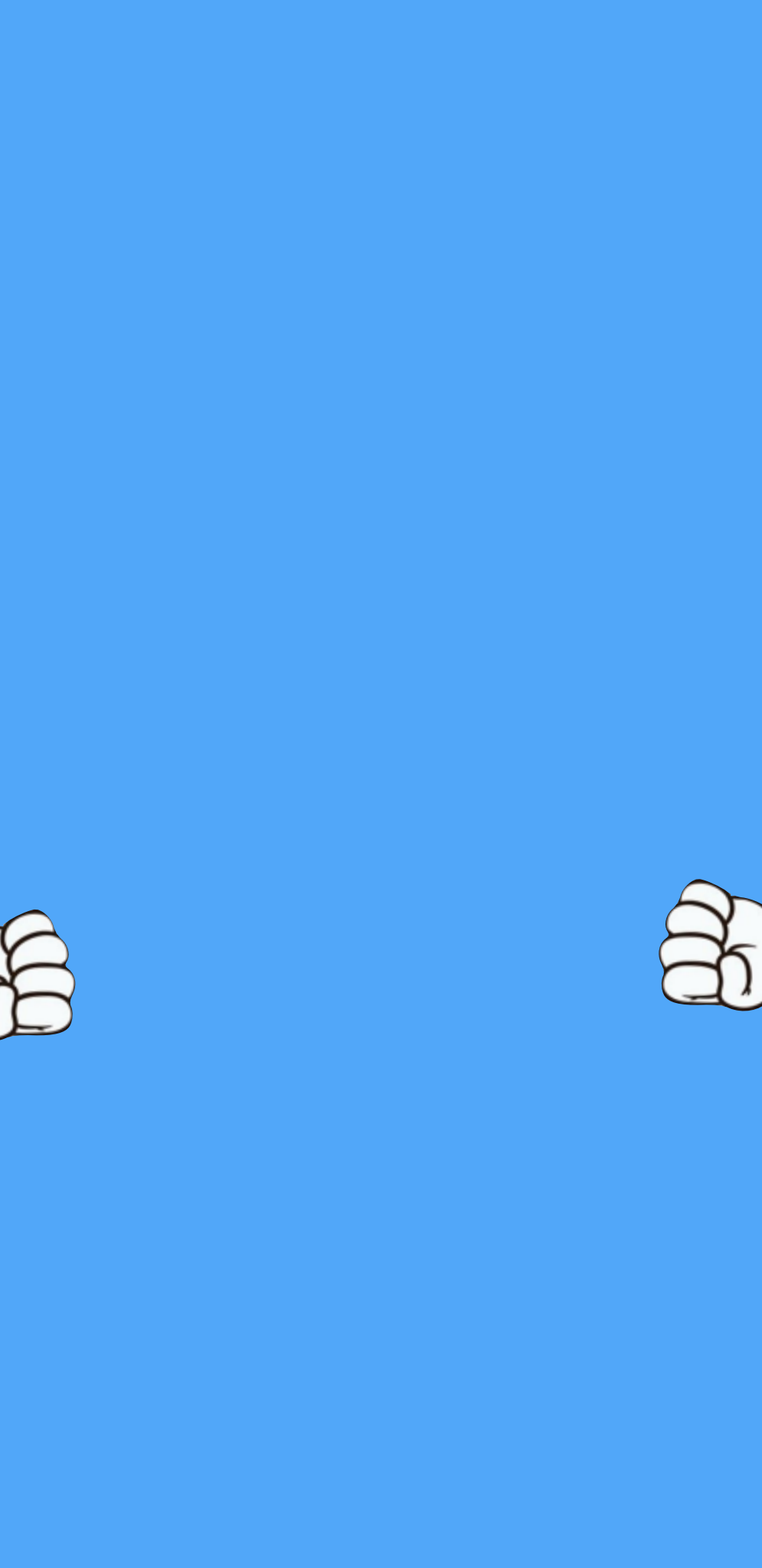




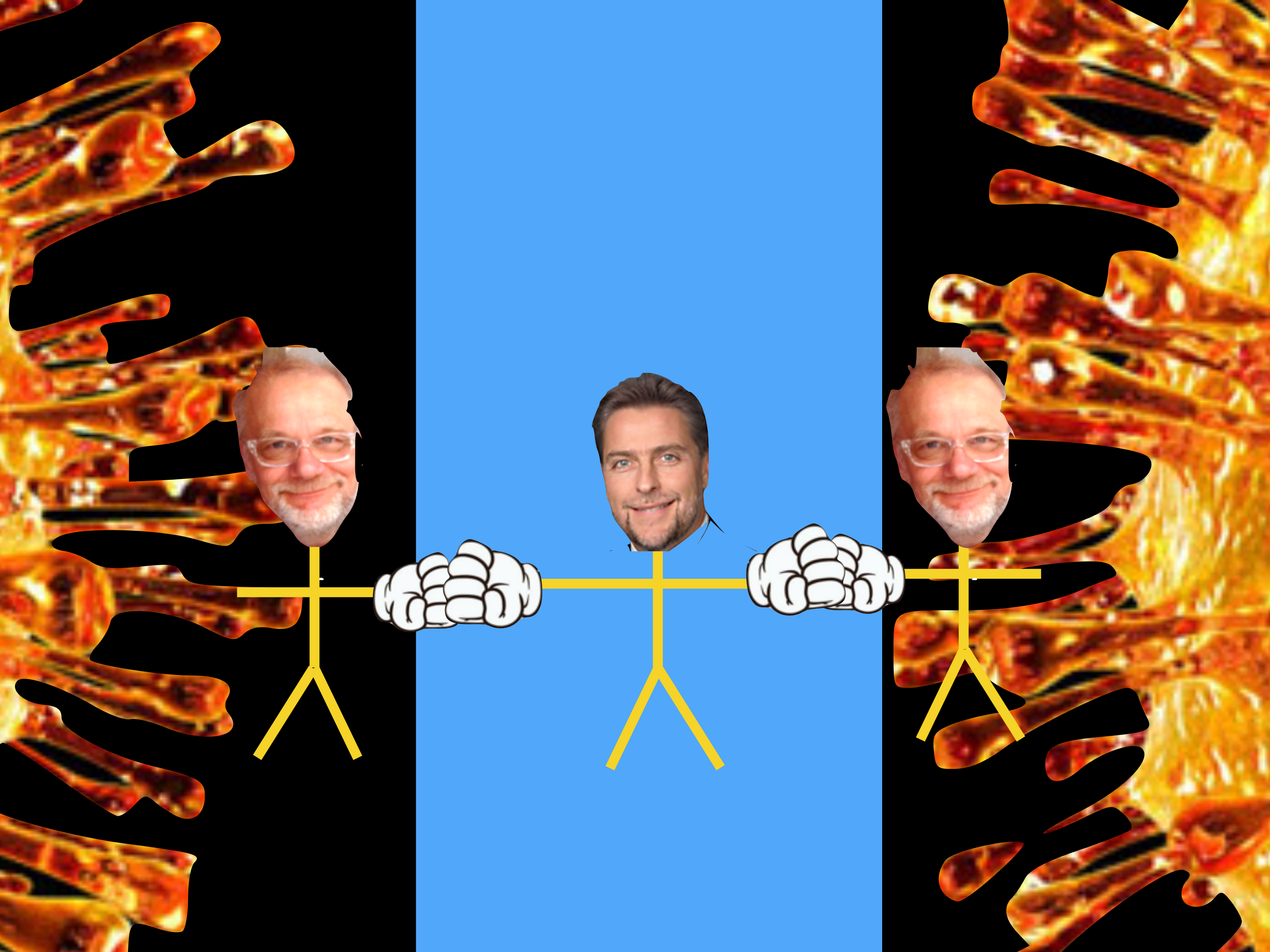




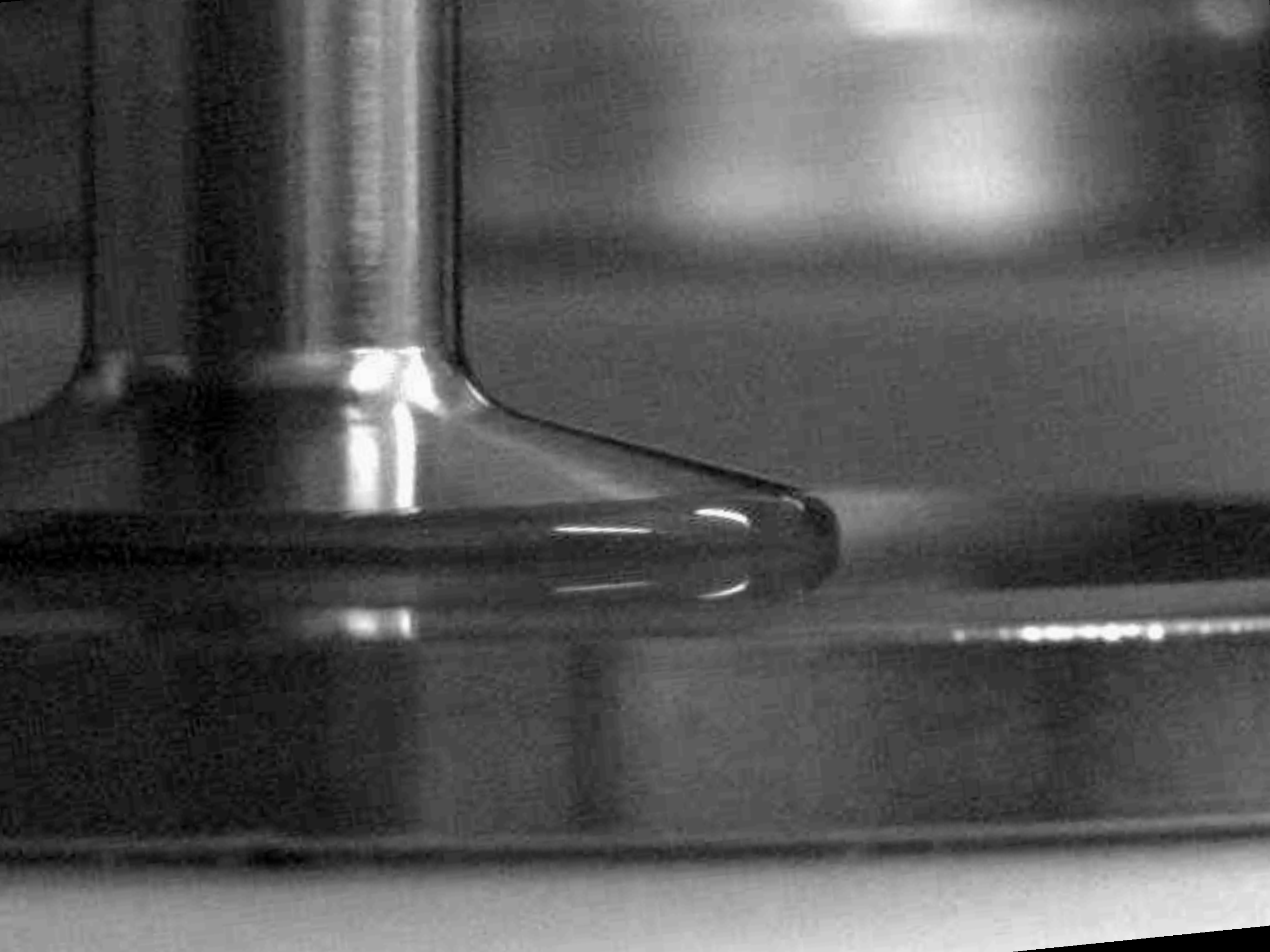


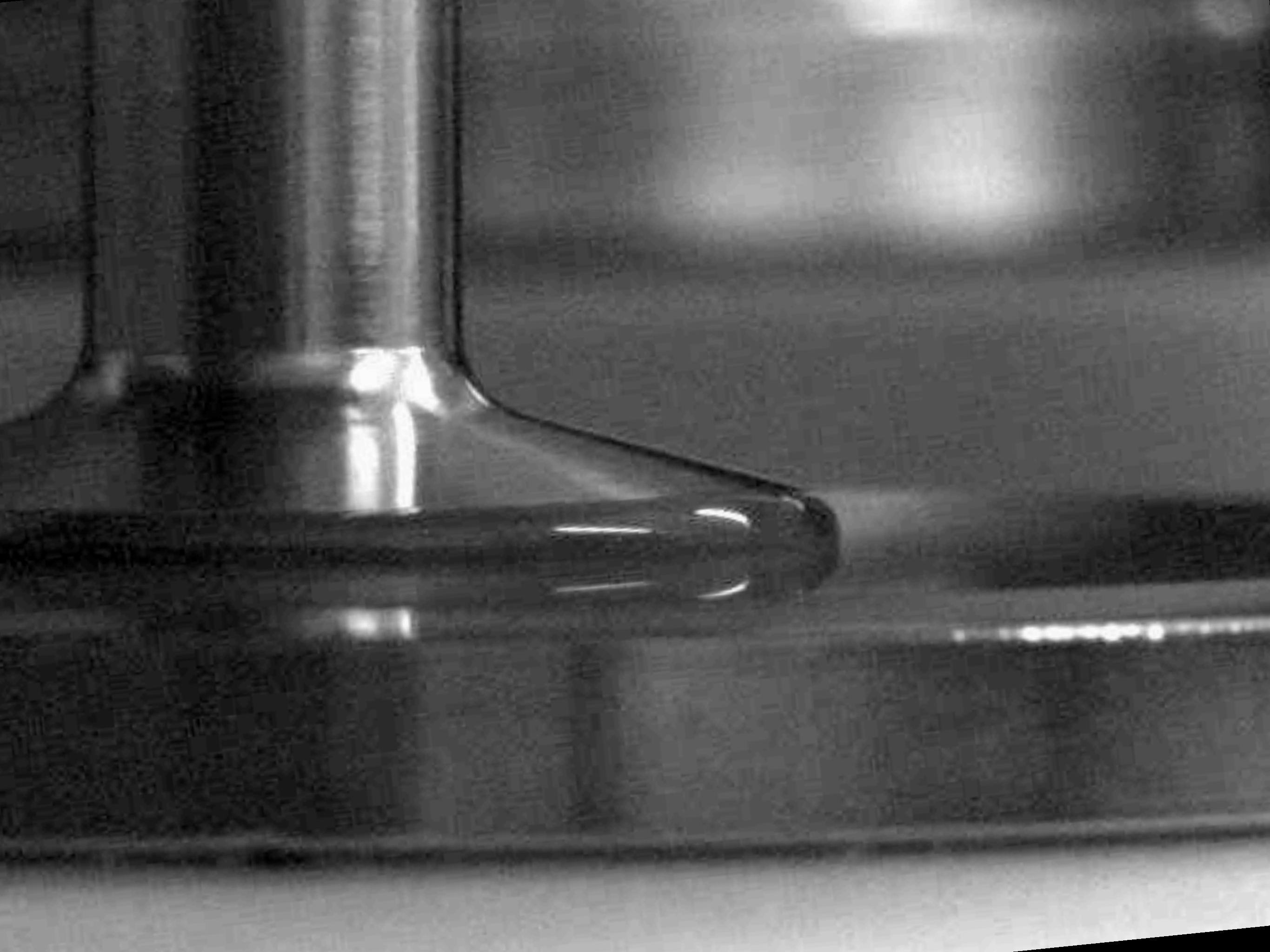










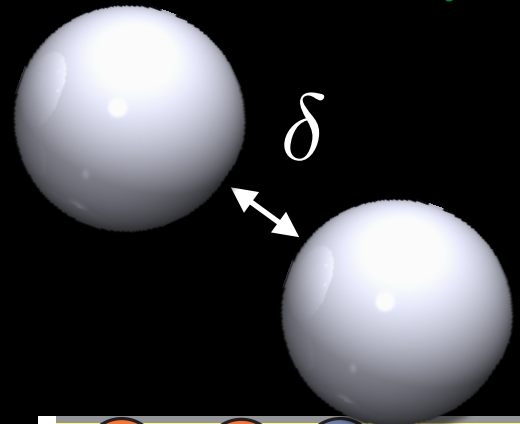


# Shear Thickening Mechanisms

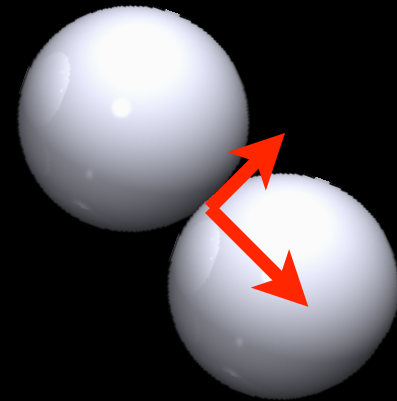
‘Hydroclusters’

VS

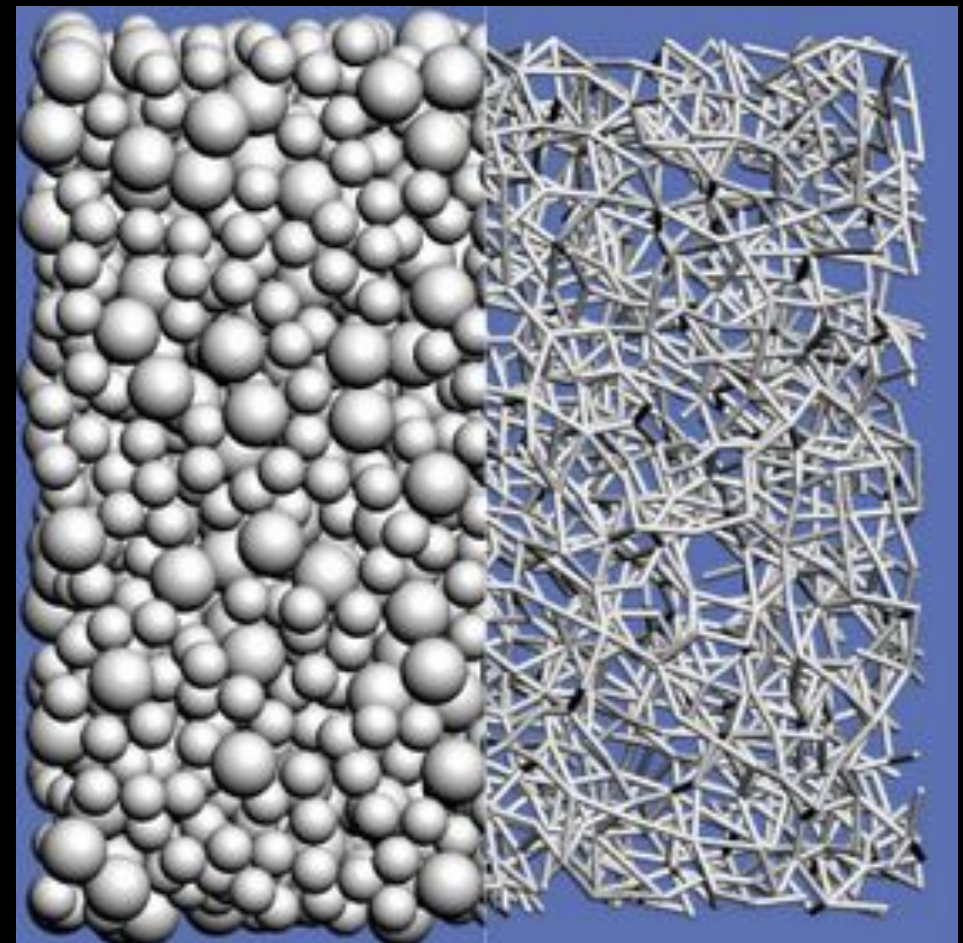
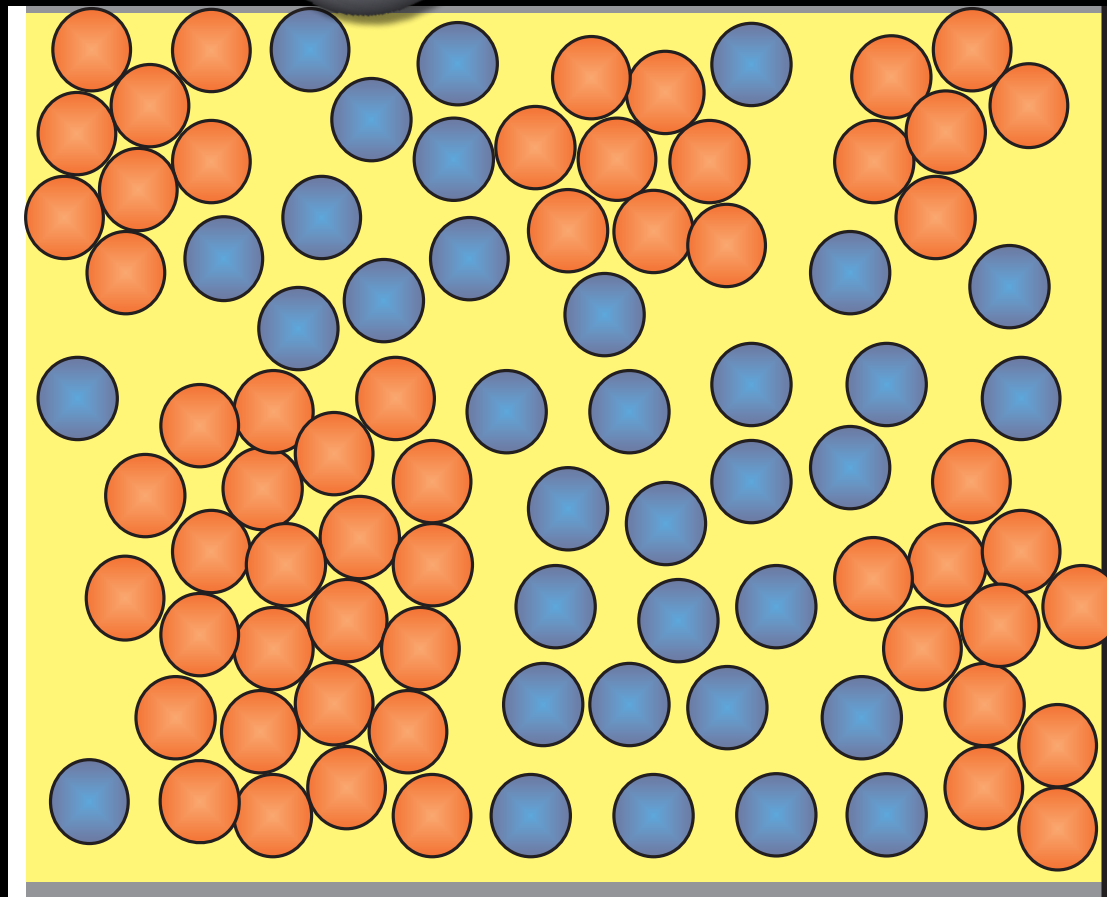
‘Friction’



$$F_{lub} \propto \frac{1}{\delta}$$



$$F_T \leq \mu |F_N|$$

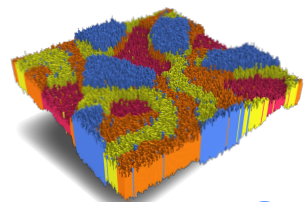


Wagner, Brady Phys. Today 2009

Seto et al PRL 2013

Wyart & Cates, PRL 2014

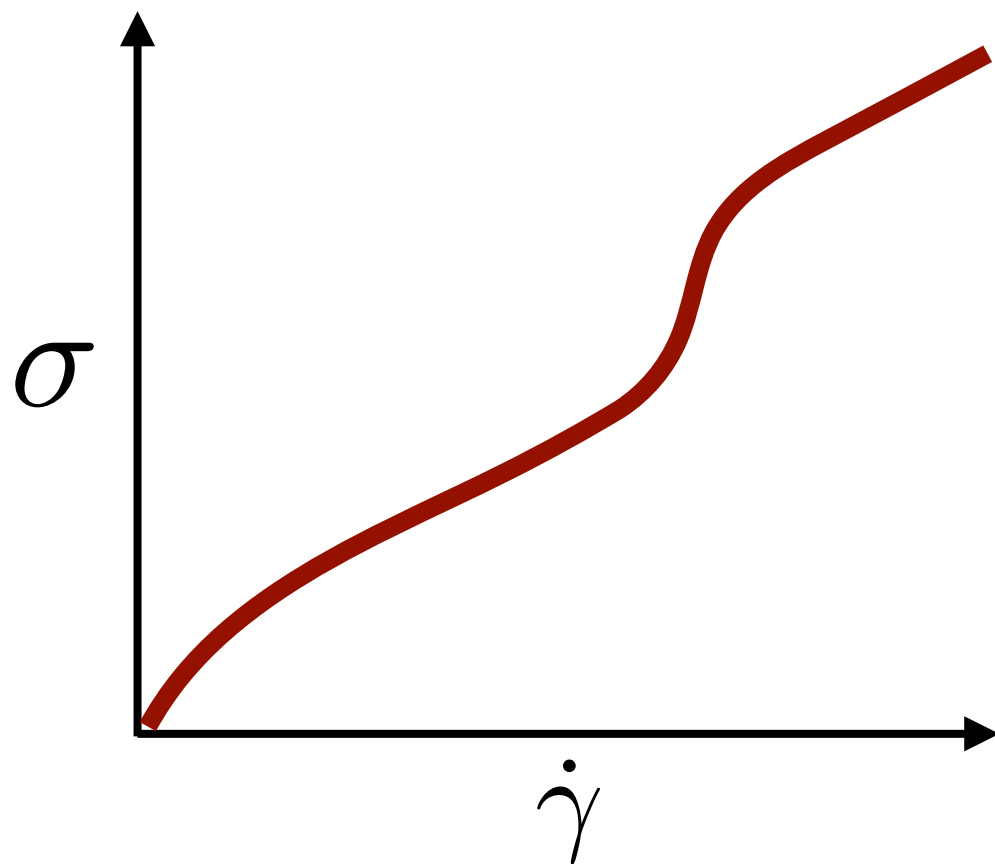




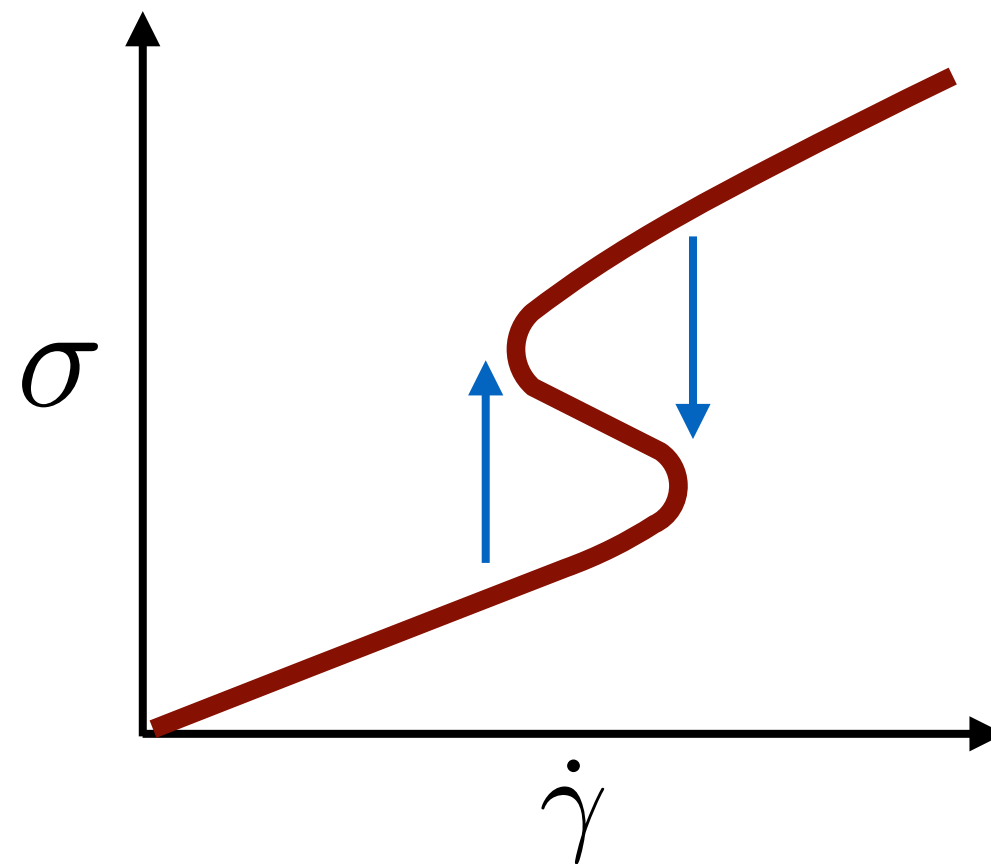
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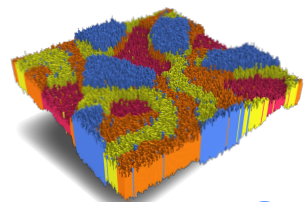
“continuous”



“dis-continuous”



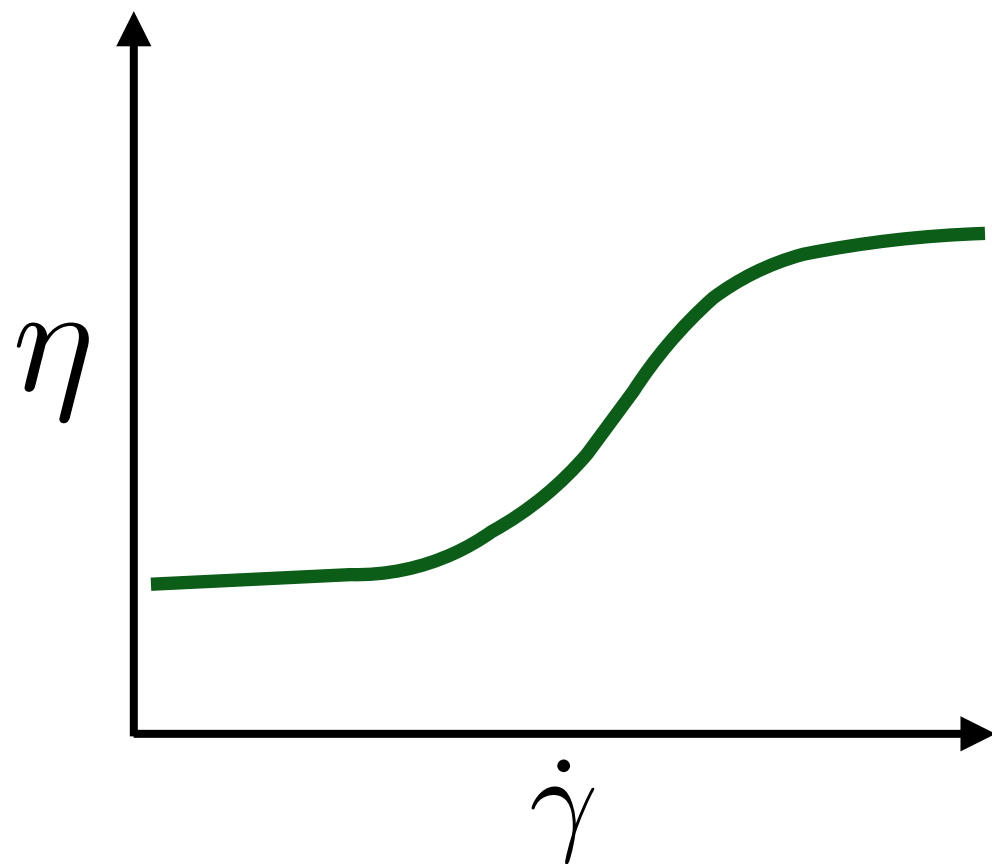




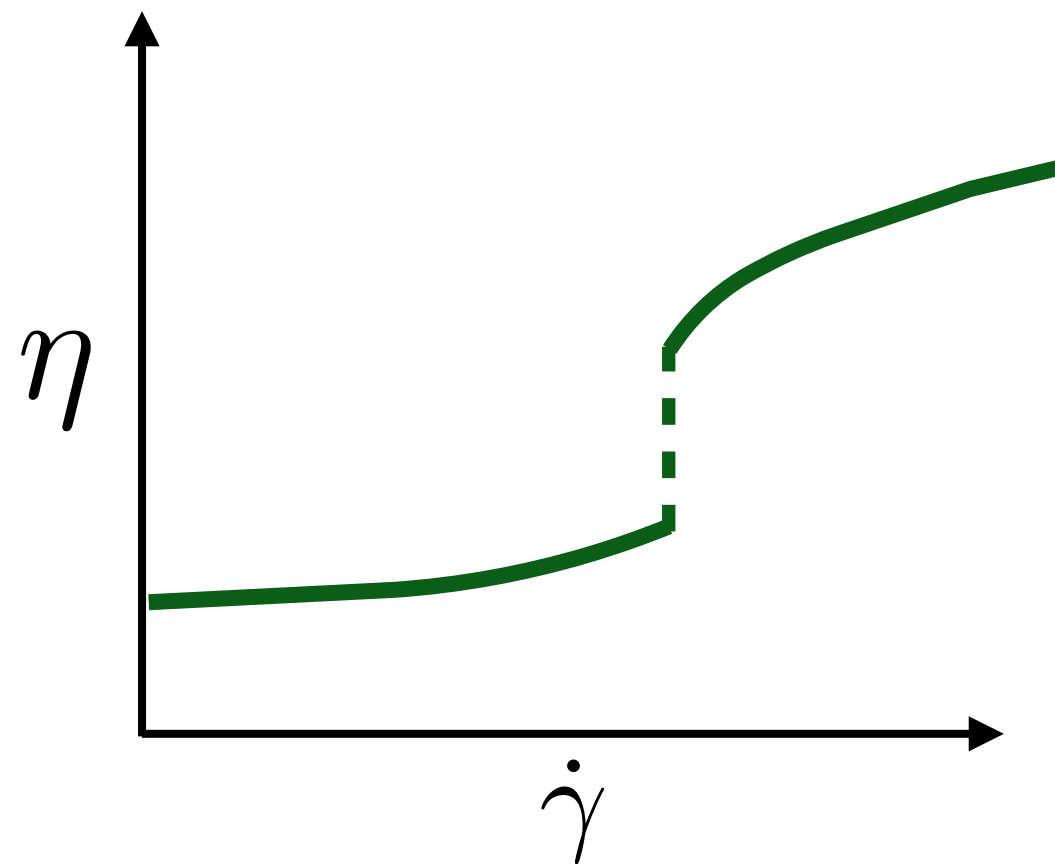
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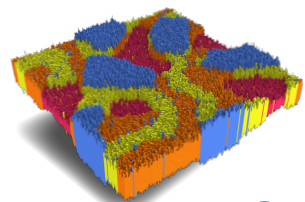


“continuous”



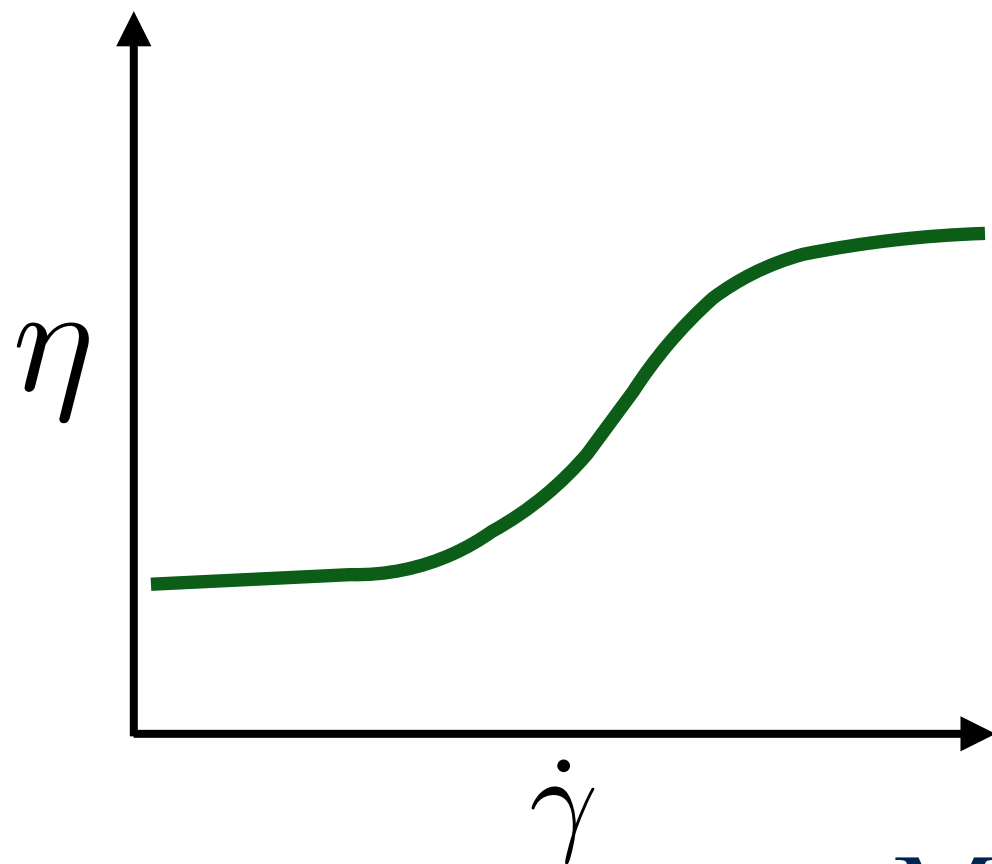
“dis-continuous”



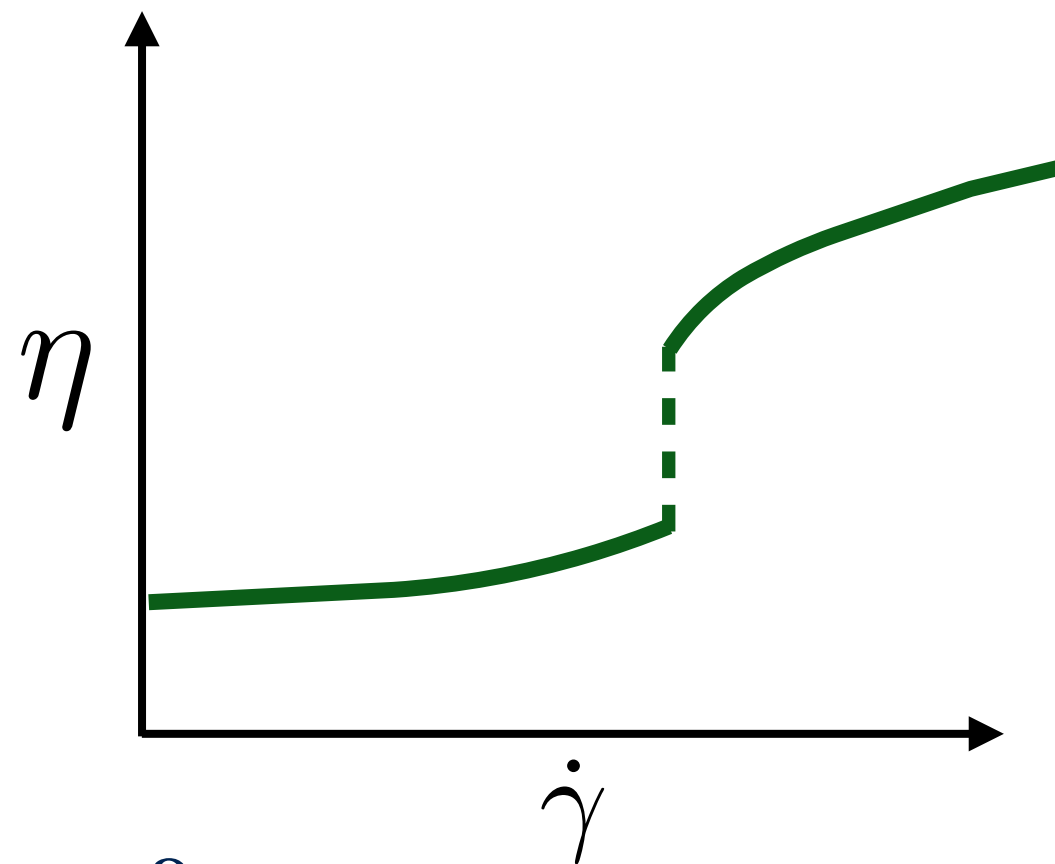


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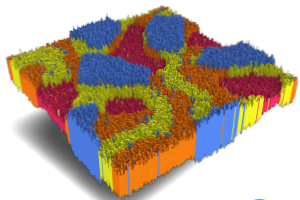
“continuous”



“dis-continuous”



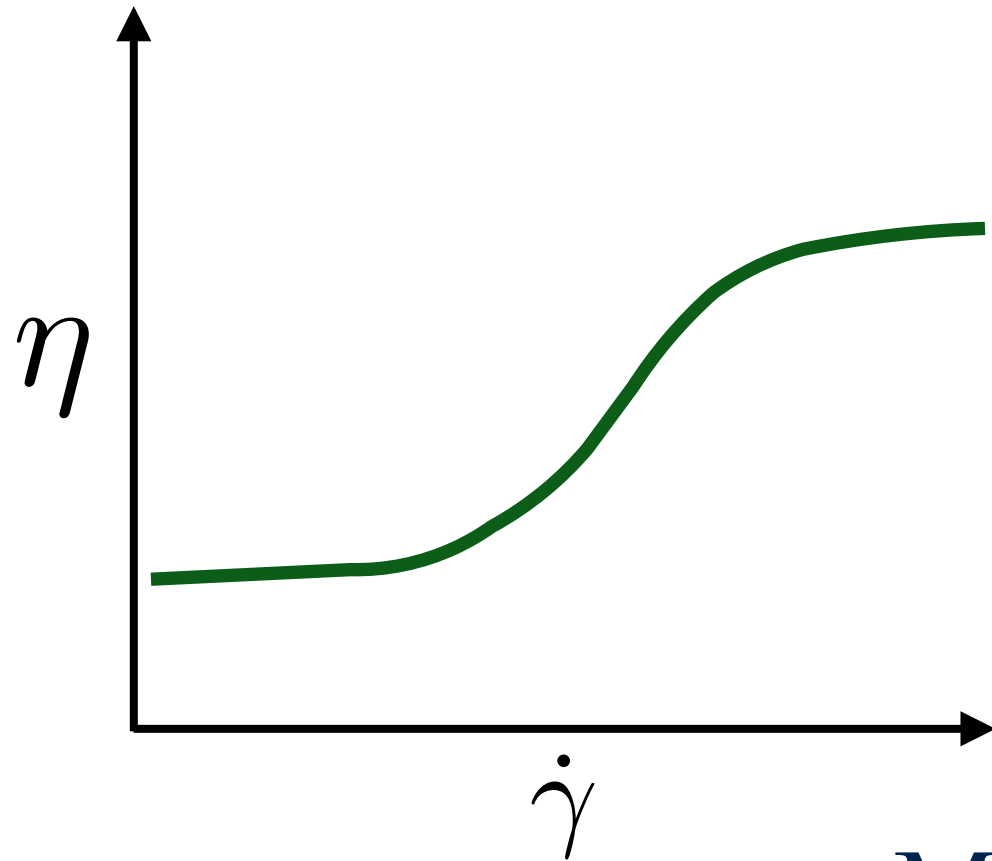
Mechanisms?



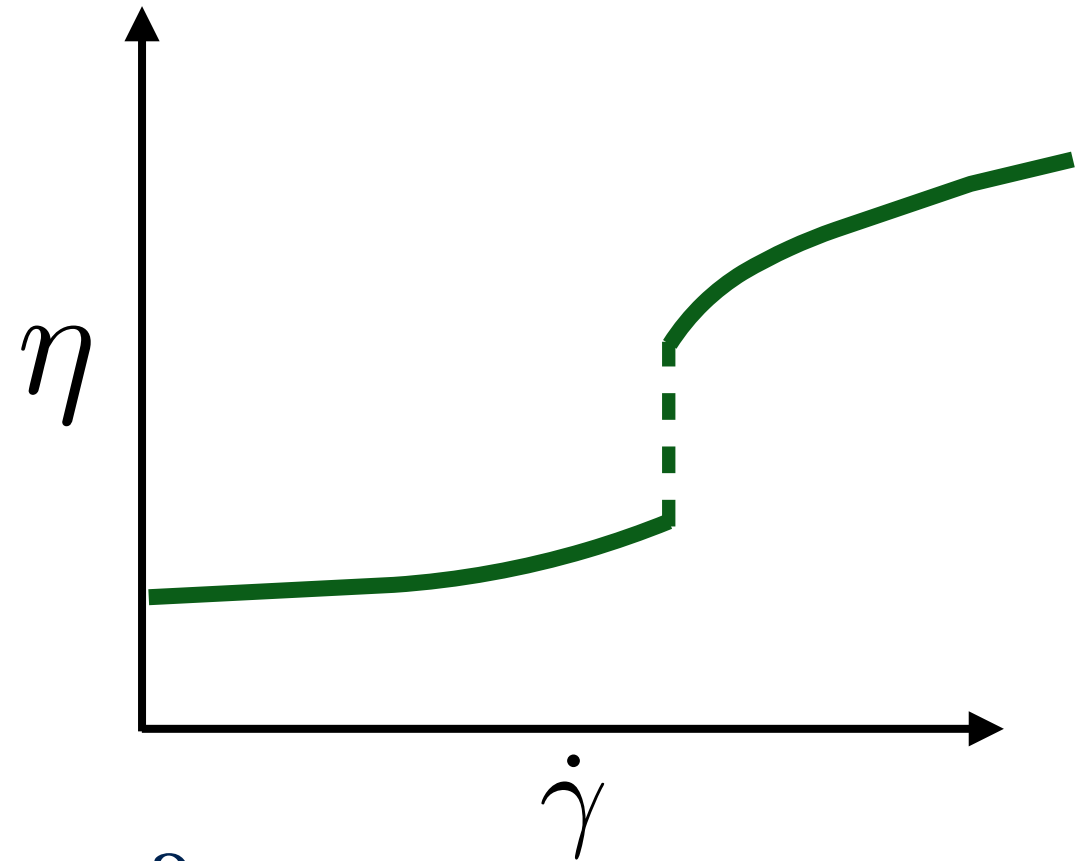
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“continuous”



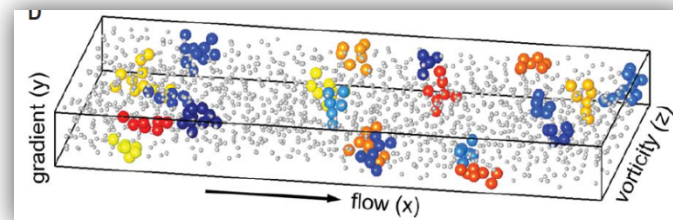
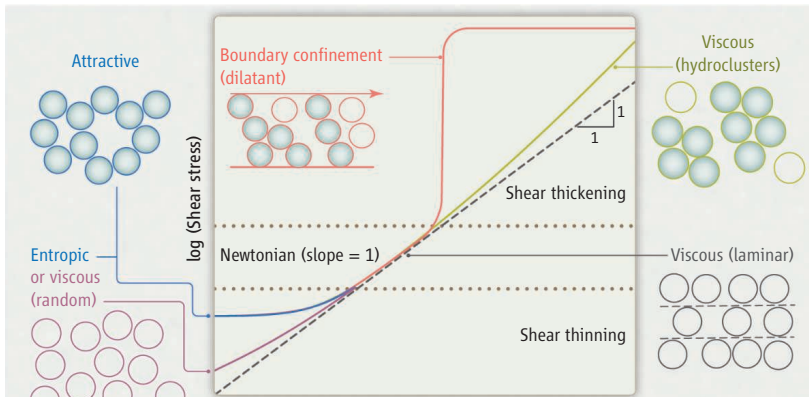
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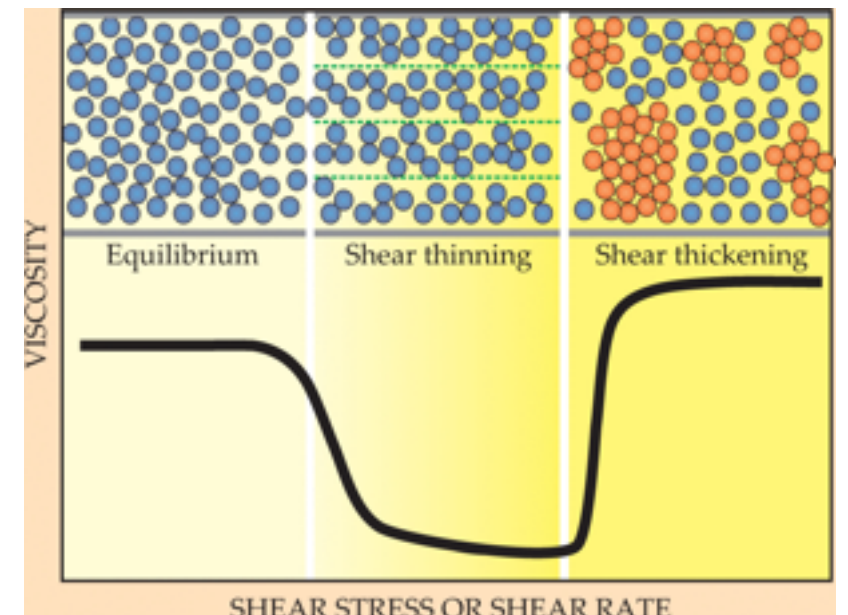
## Mechanisms?

Hydrodynamics (*i.e.* hydroclusters)

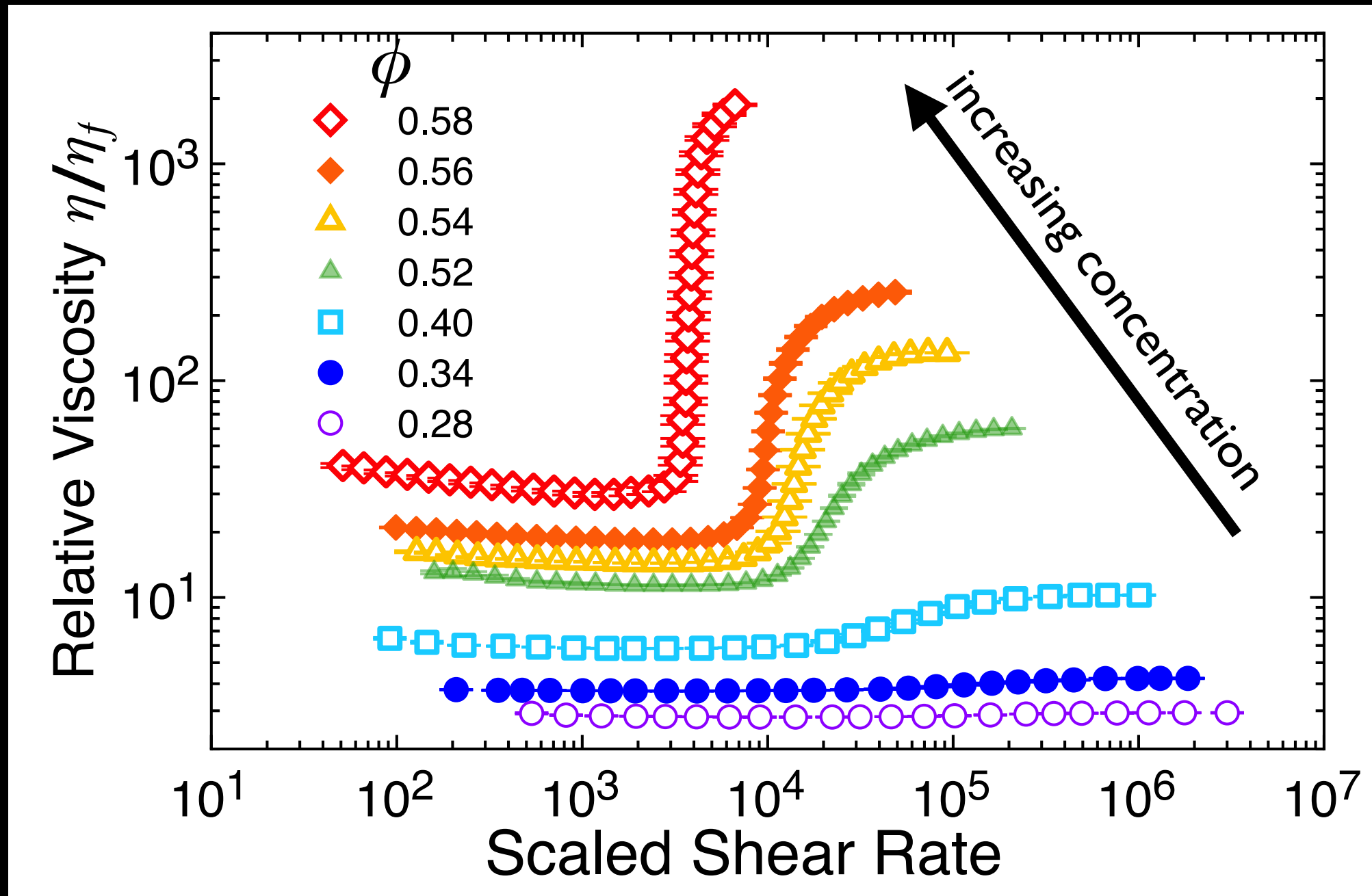
Frictional interactions (*i.e.* dilatancy, granularity)



Real-space configuration of hydroclusters



# Continuous shear thickening



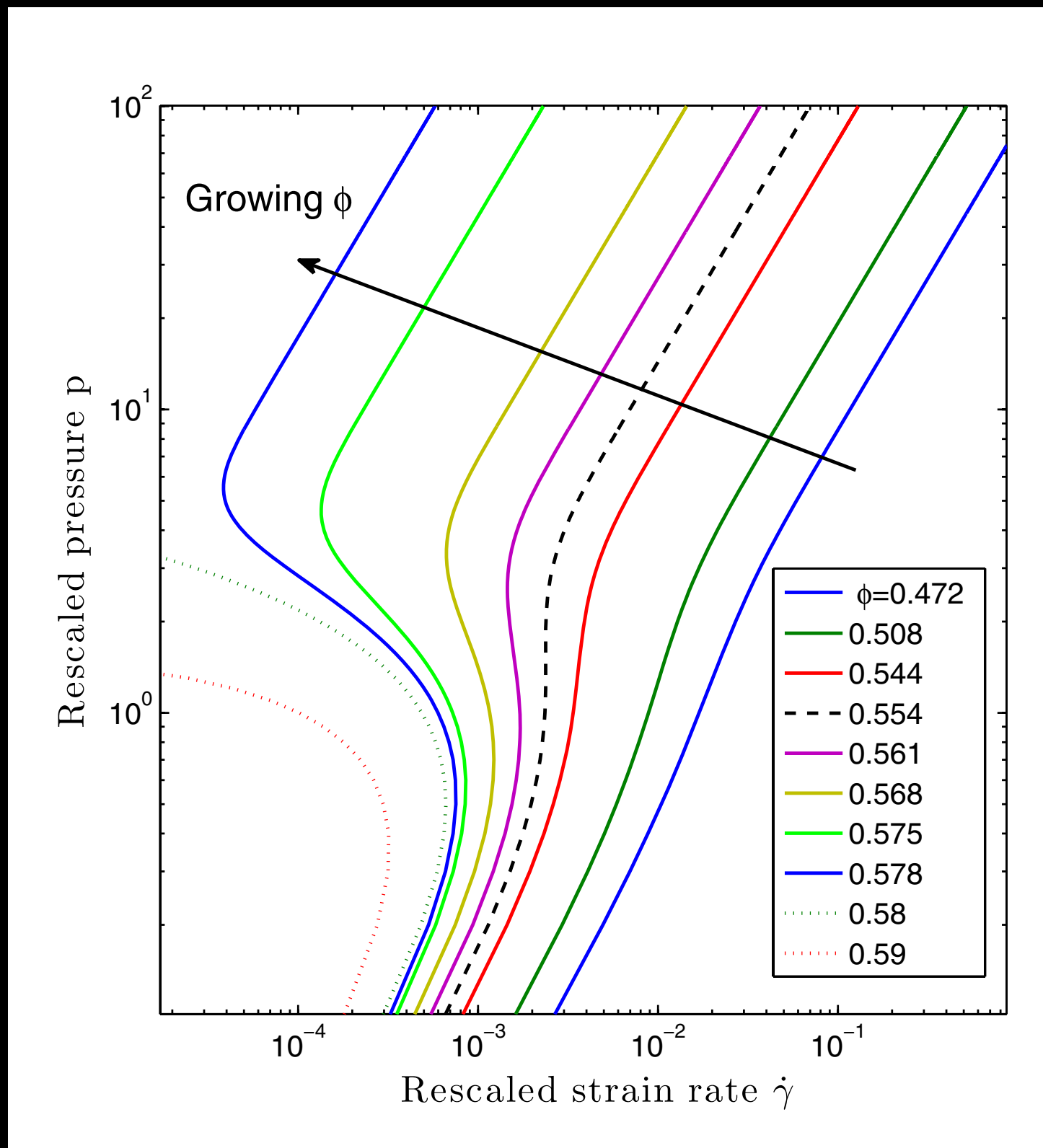
J. Royer, DLB, S.Hudson, PRL 2016

Volume Fraction:  $\phi = \frac{V_{part}}{V_{total}}$

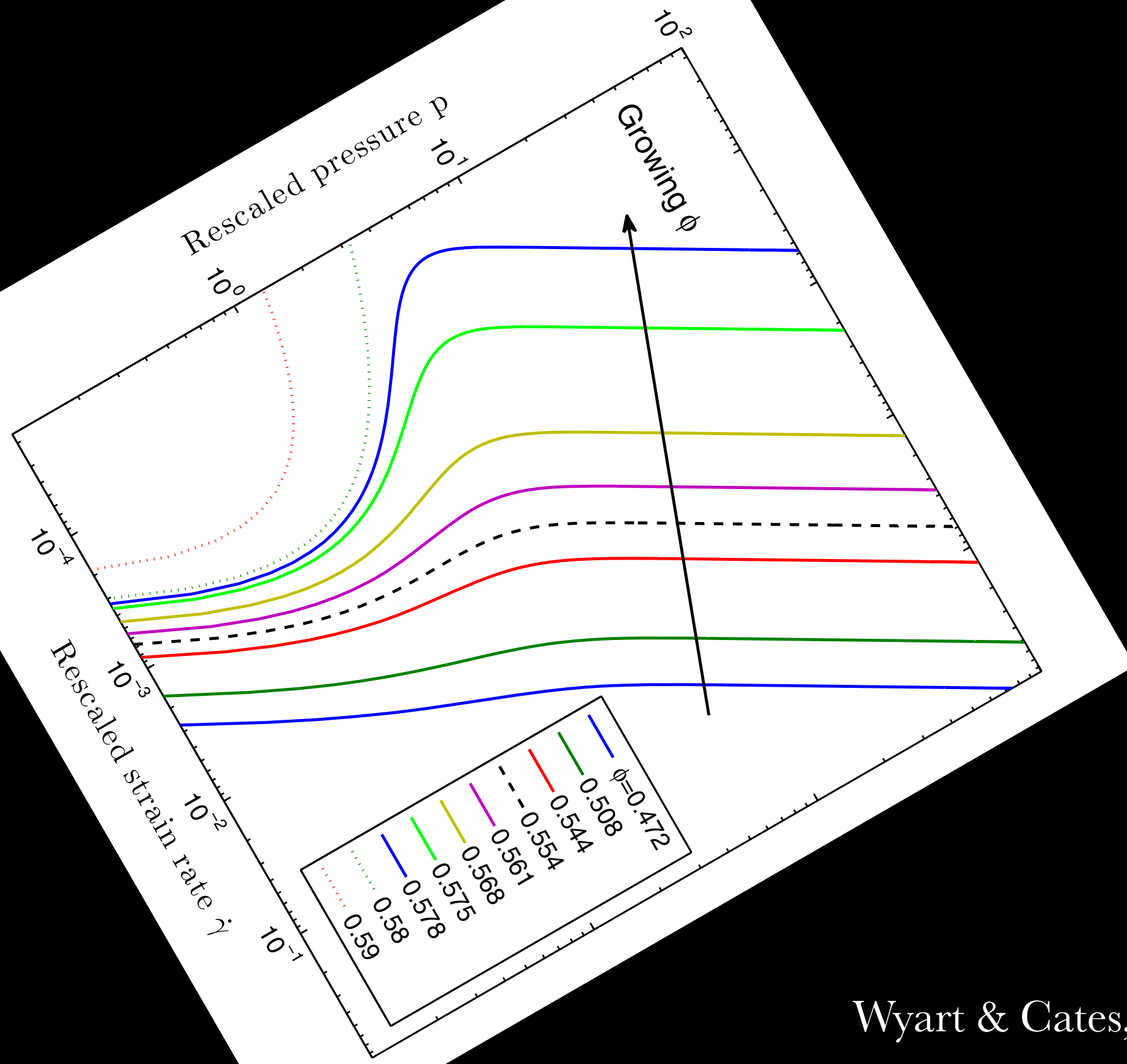
particles: 1.5  $\mu\text{m}$  silica colloids  
solvent: glycerol/water



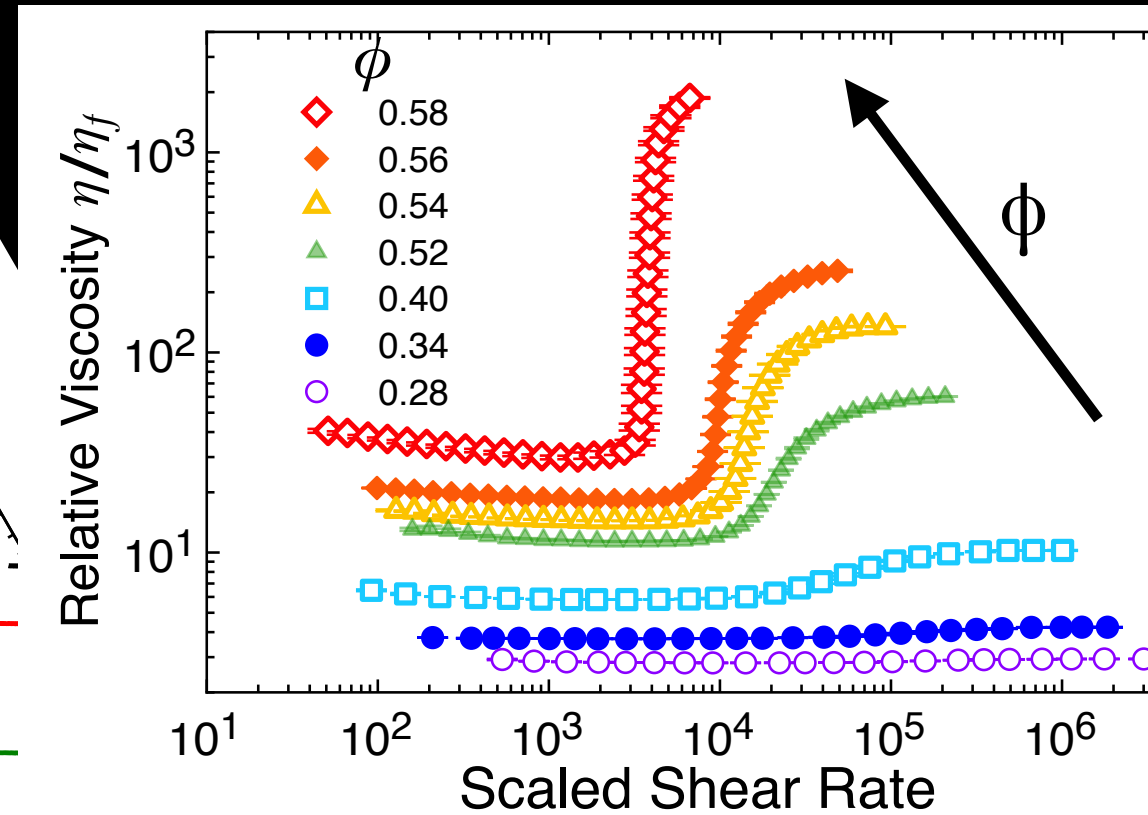
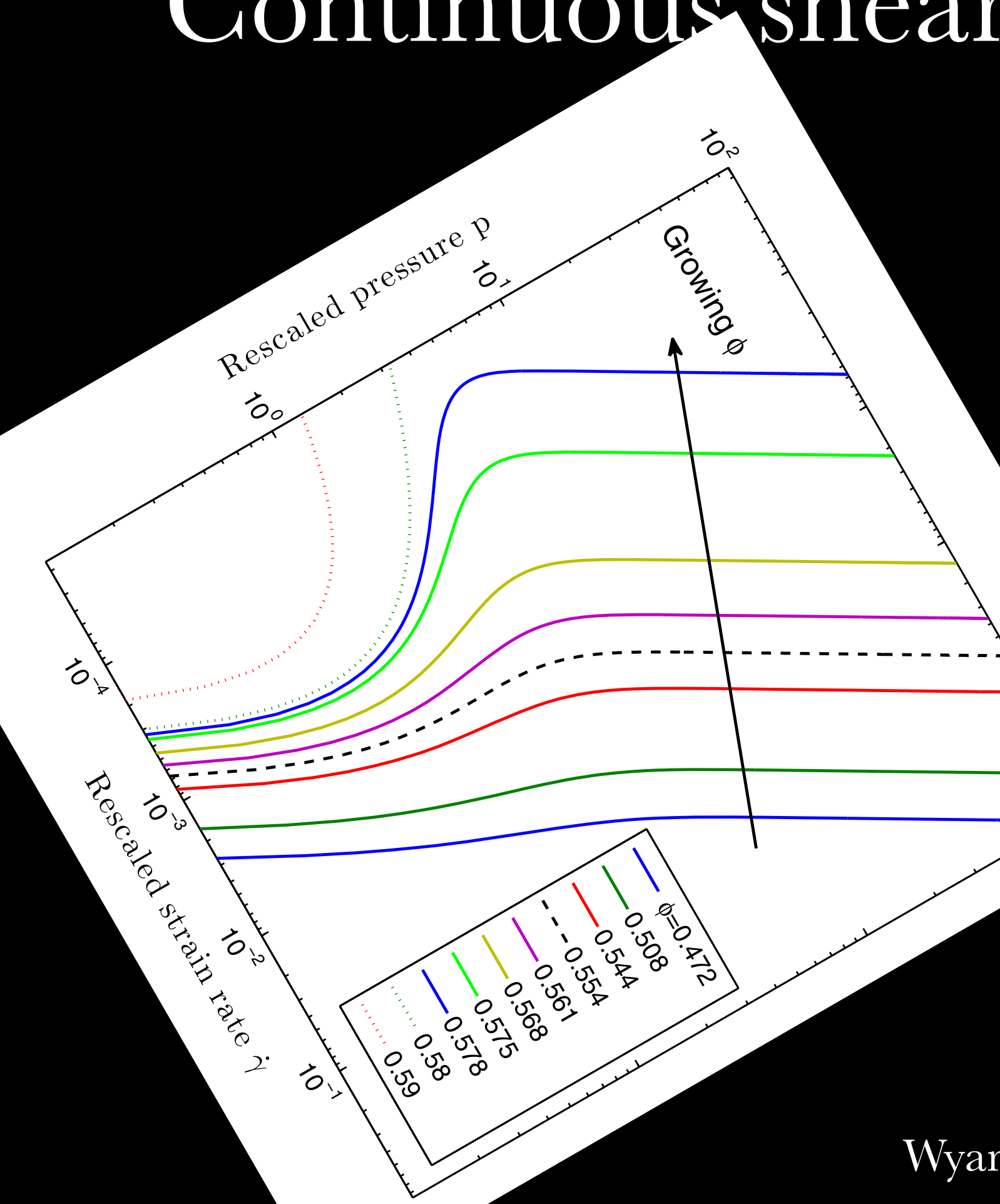
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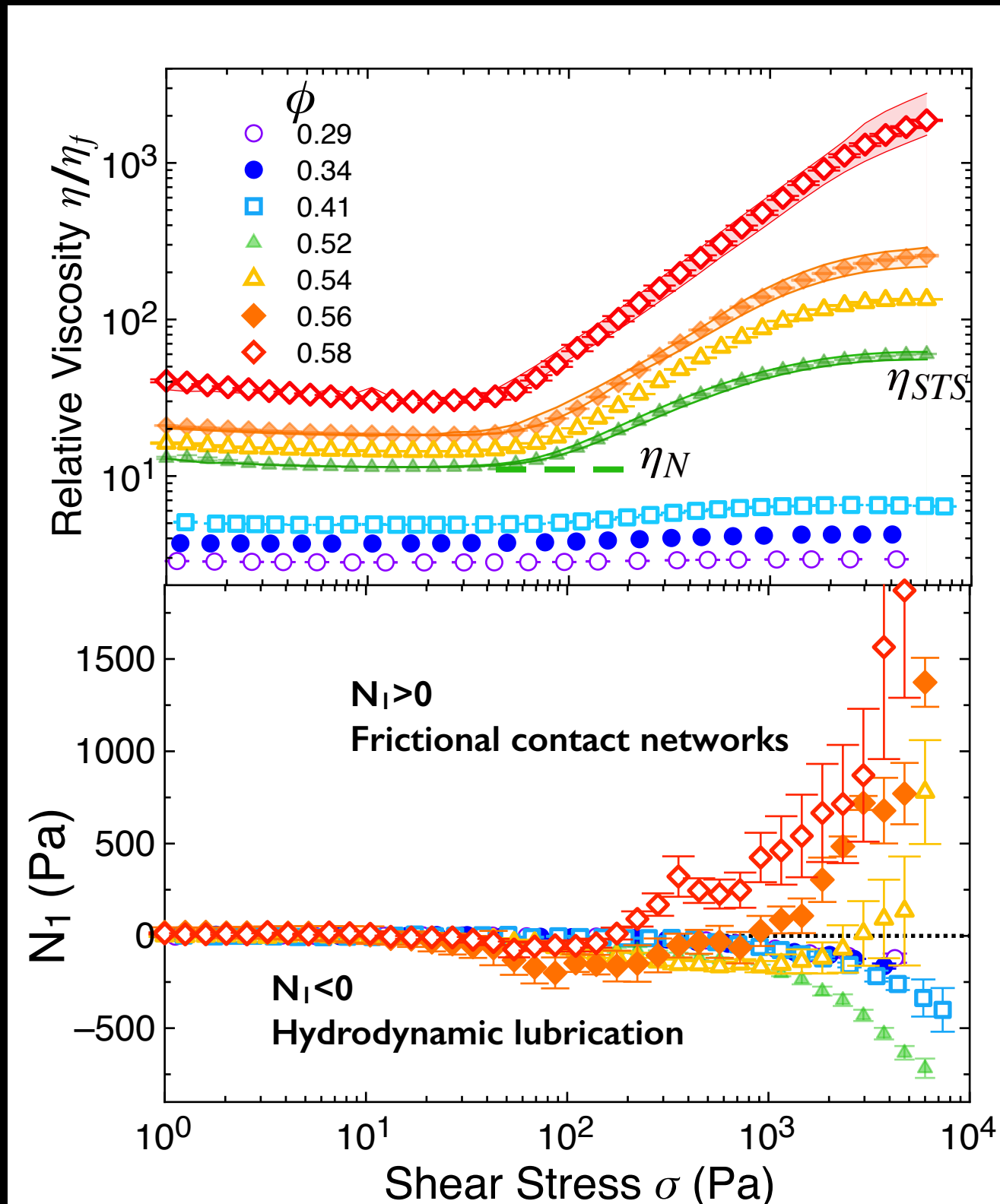


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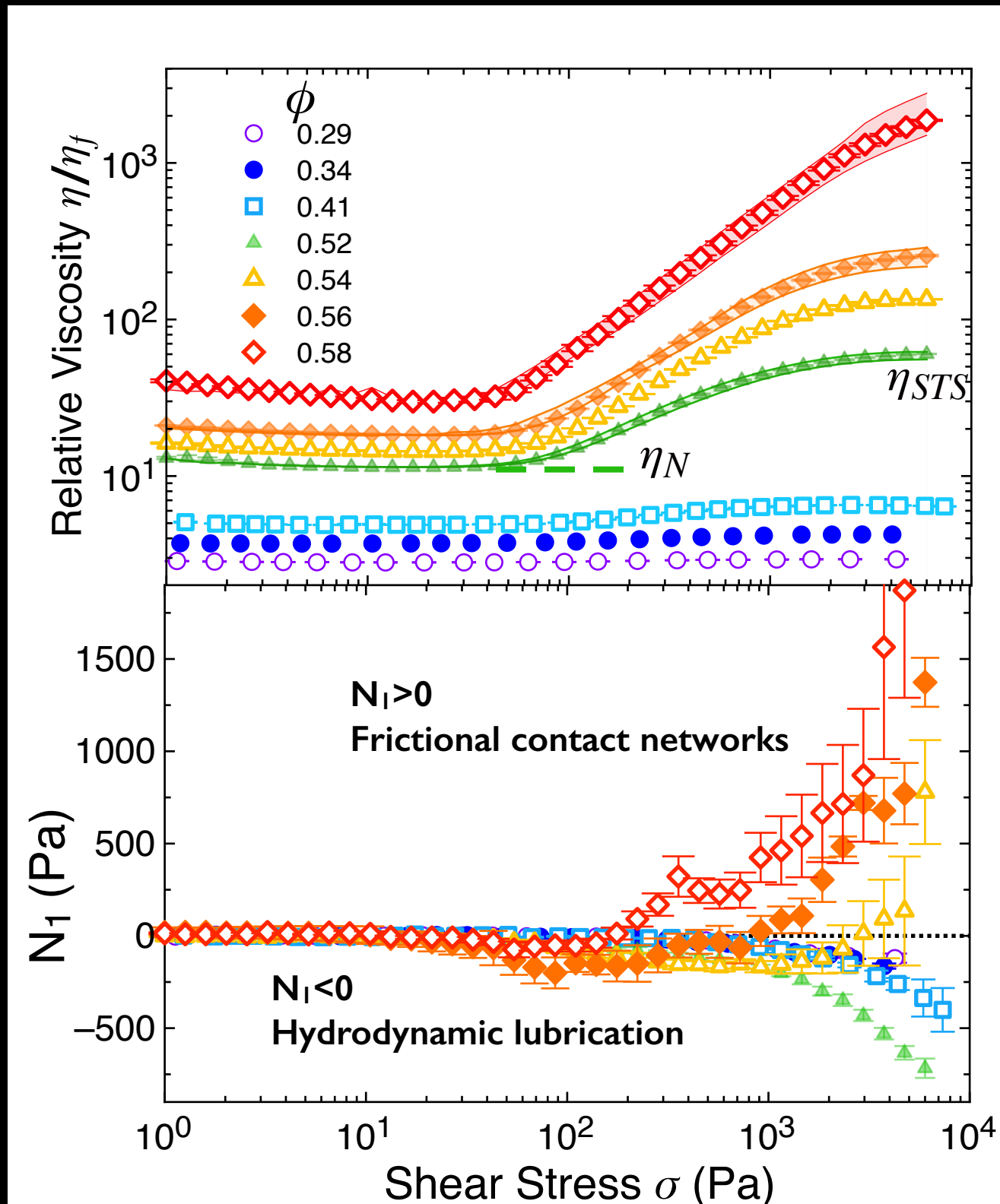


# $\mathcal{N}_1$ Reveals New Transition



Change in  $\mathcal{N}_1$

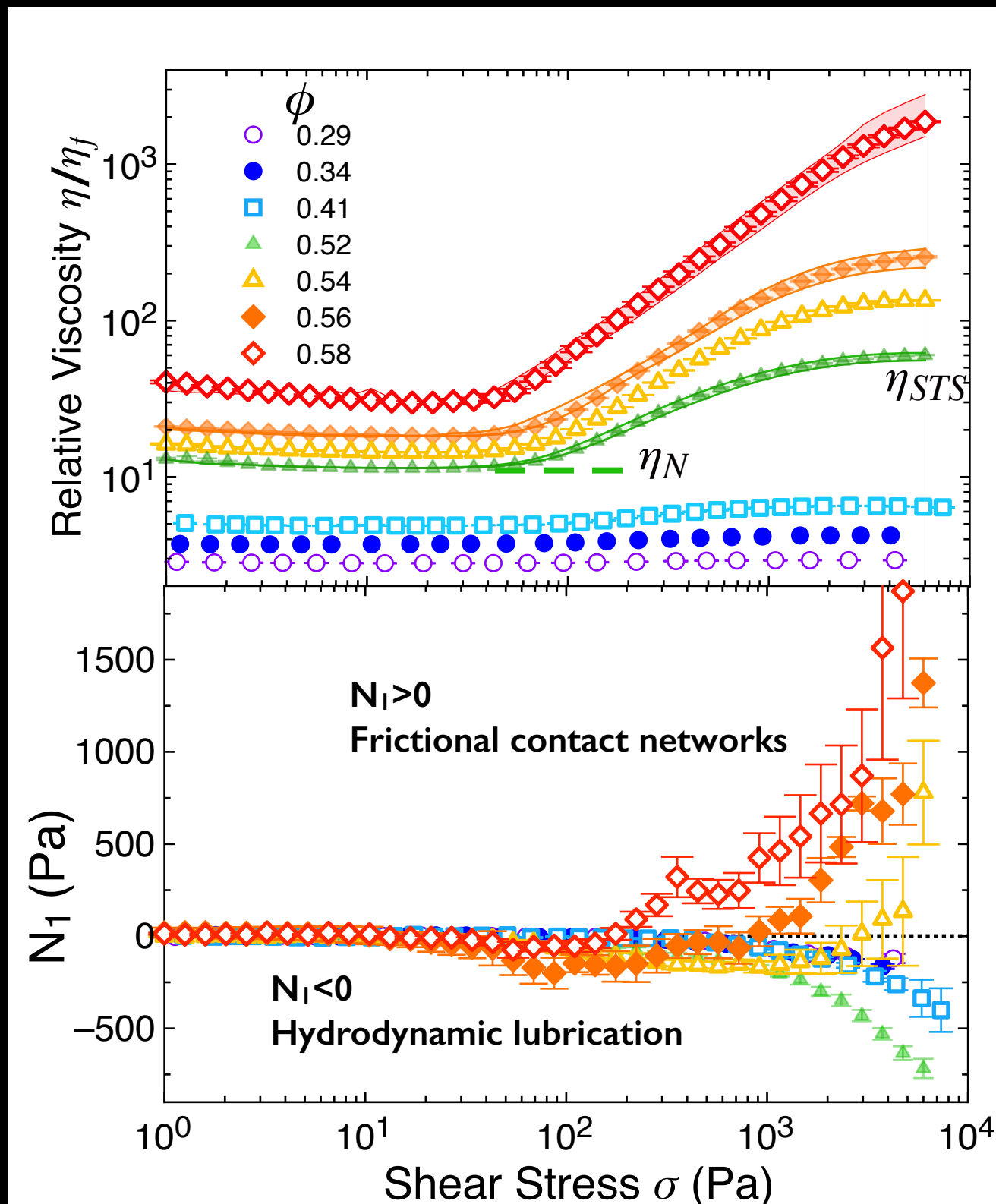
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Change in  $\mathcal{N}_1$

No signature in viscosity

# $\mathcal{N}_1$ Reveals New Transition



Change in  $N_1$

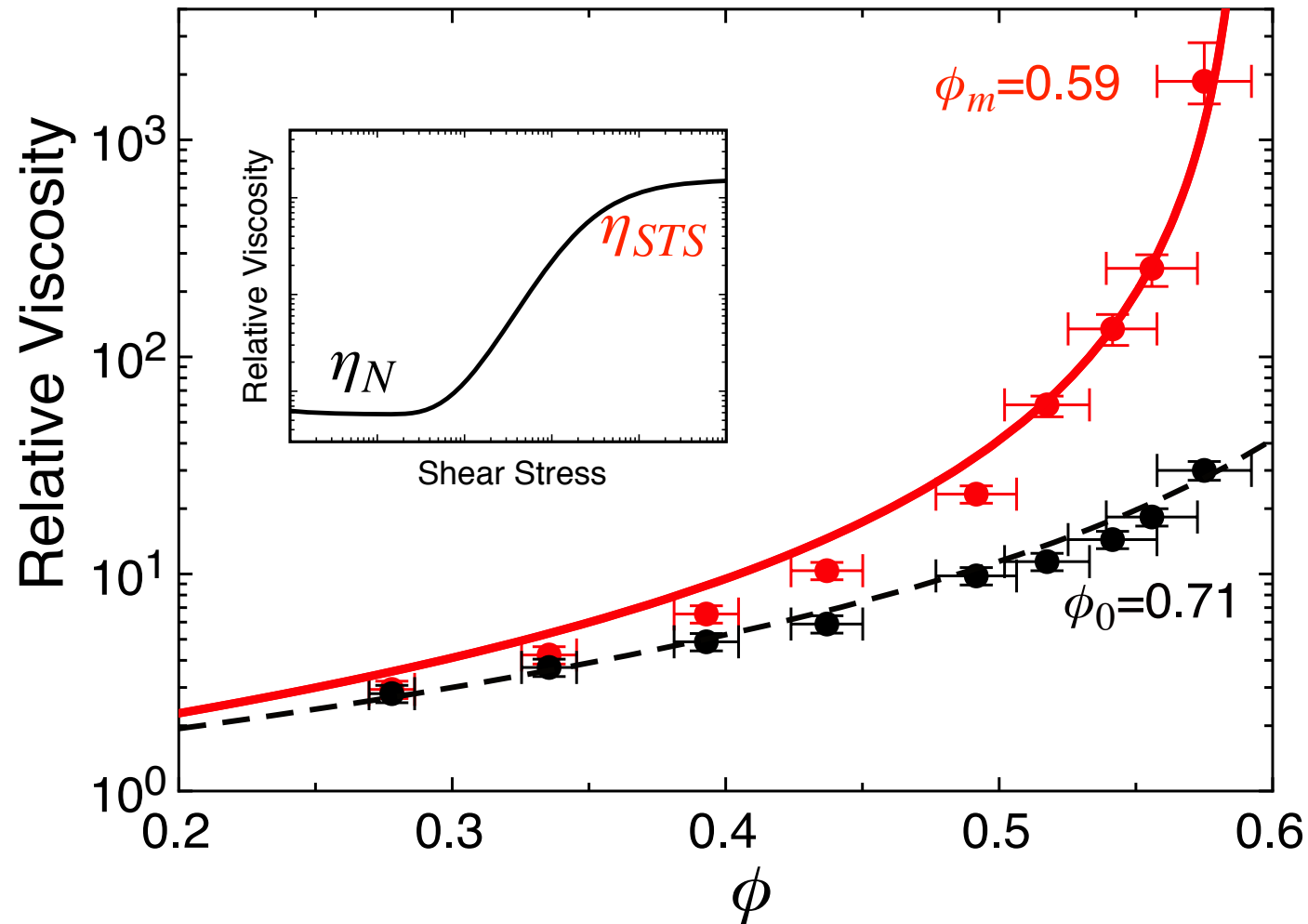
No signature in viscosity



# Friction-based model

Shear thickening: stress activated frictional contacts

- Wyart and Cates PRL, 2014
- Guy, Hermes & Poon, PRL 2015

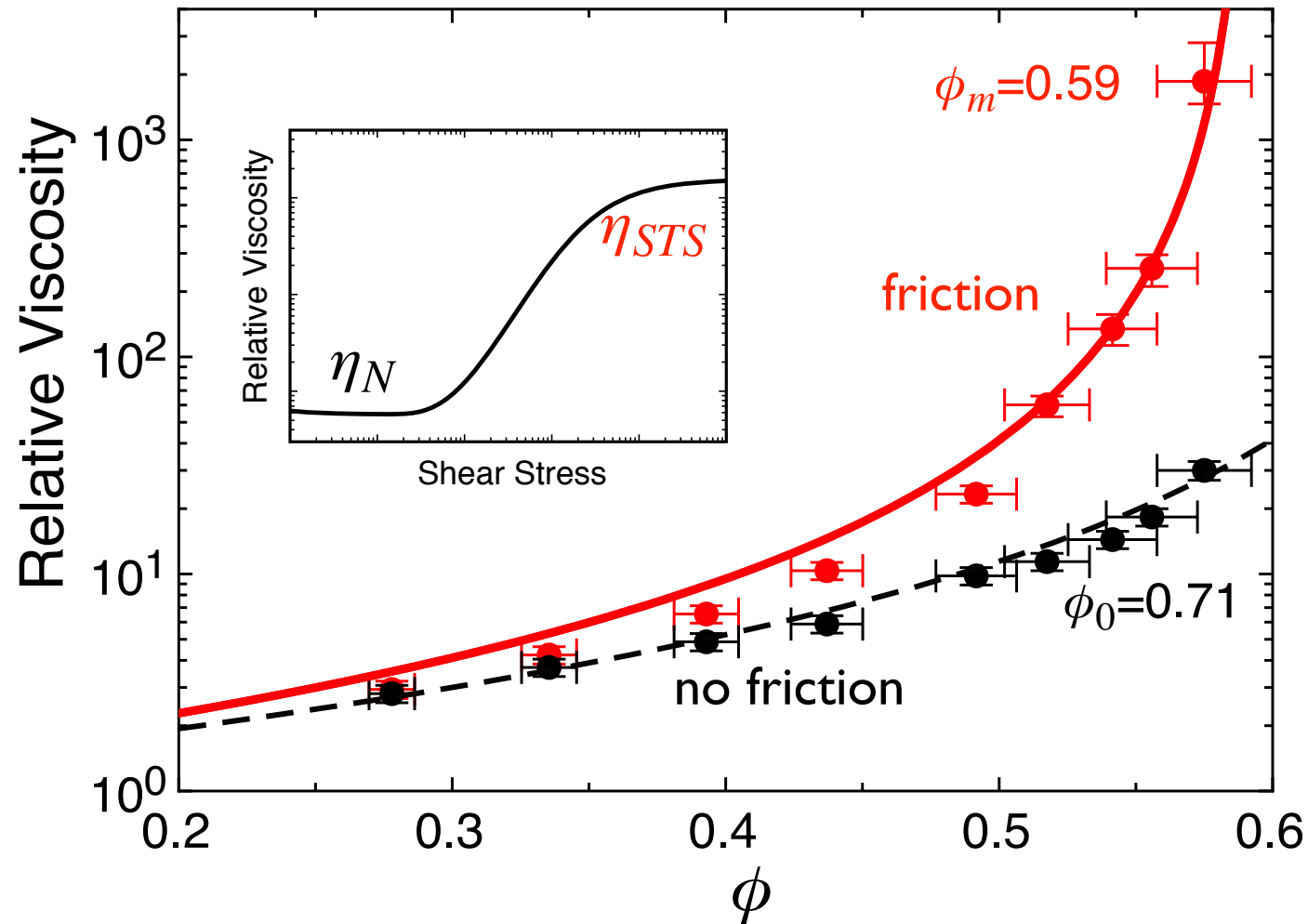


$$\eta_r = \left(1 - \frac{\phi}{\phi_c(\sigma)}\right)^{-2}$$

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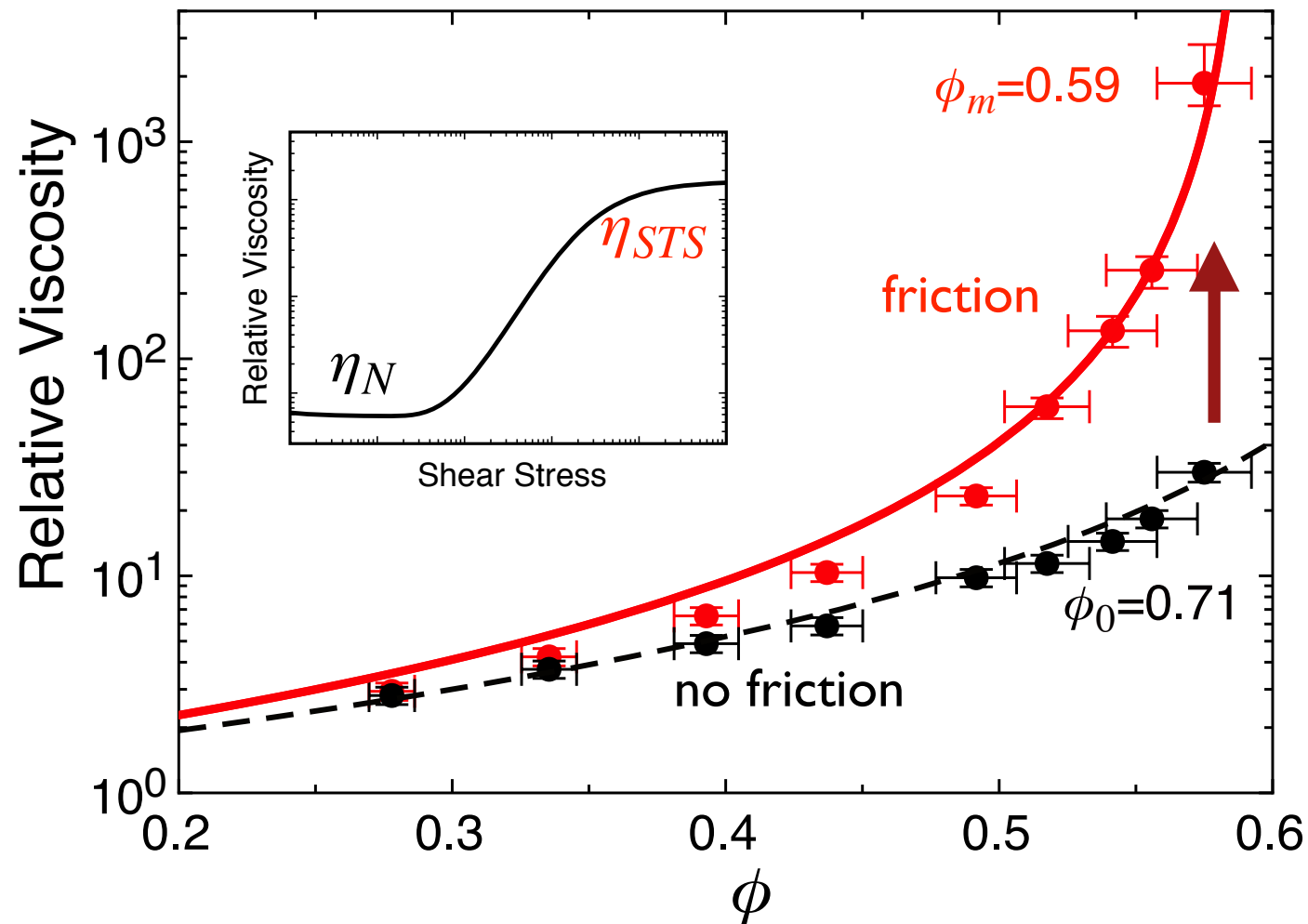


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$$\eta_r = \left(1 - \frac{\phi}{\phi_c(\sigma)}\right)^{-2}$$

$$\phi_c(\sigma) = f\phi_m + (1 - f)\phi_0$$

$f$  = fraction of frictional contacts



# Confocal-Rheology Platform

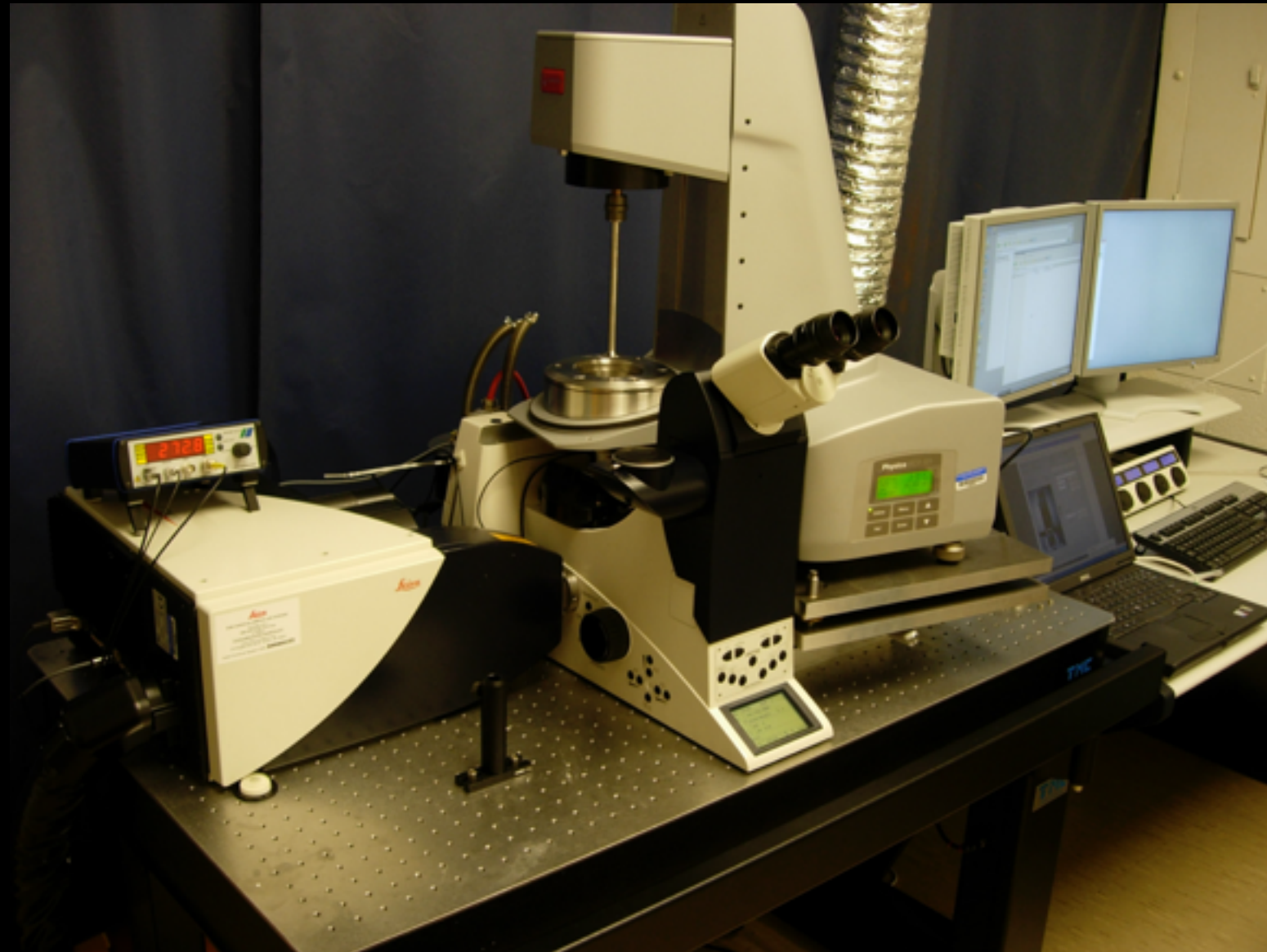


**Anton-Paar MCR-301**

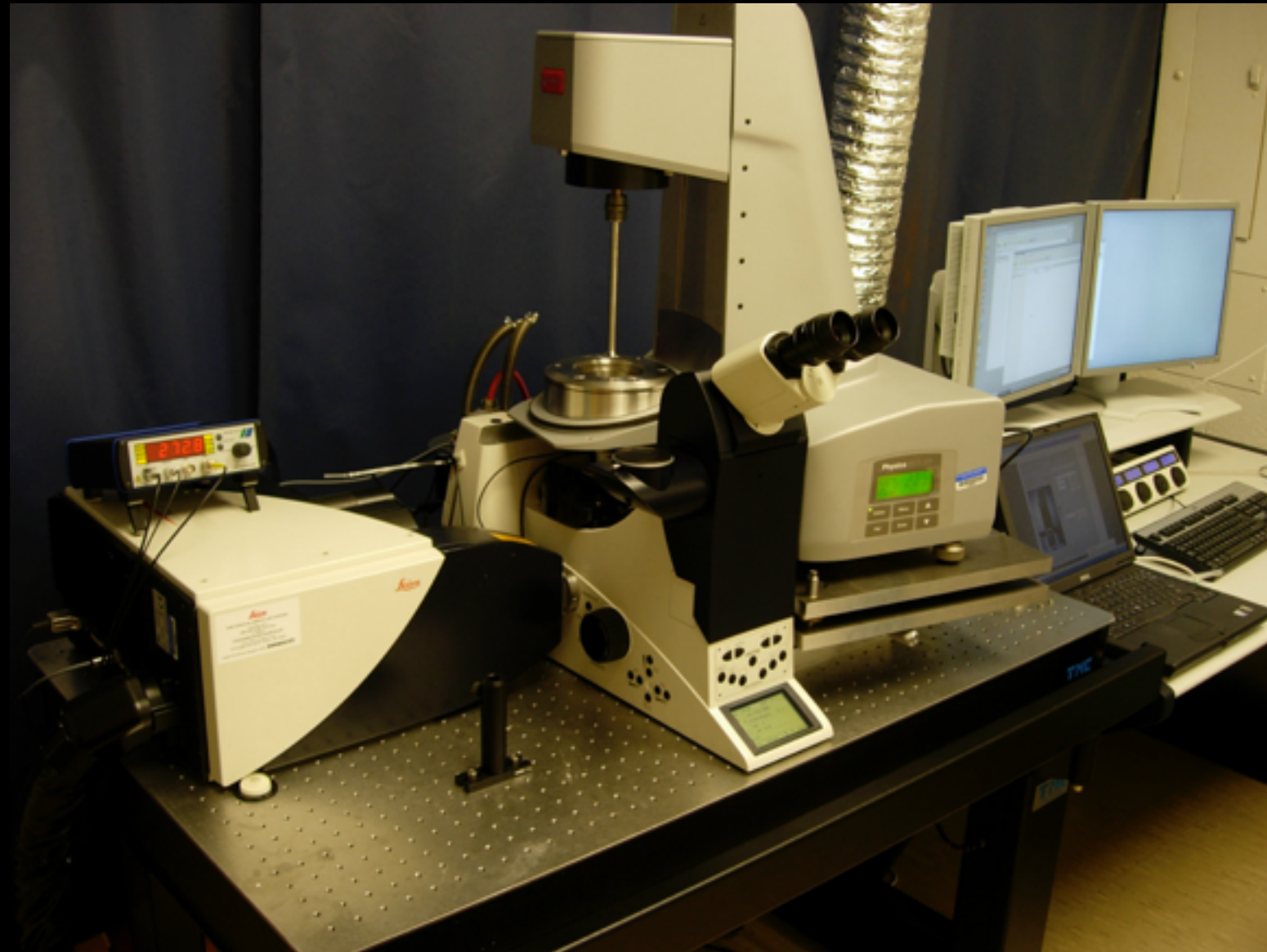


**Leica SP5**

# Confocal-Rheology Platform

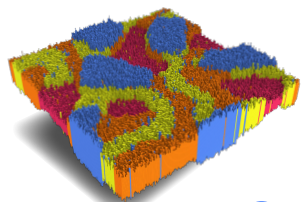


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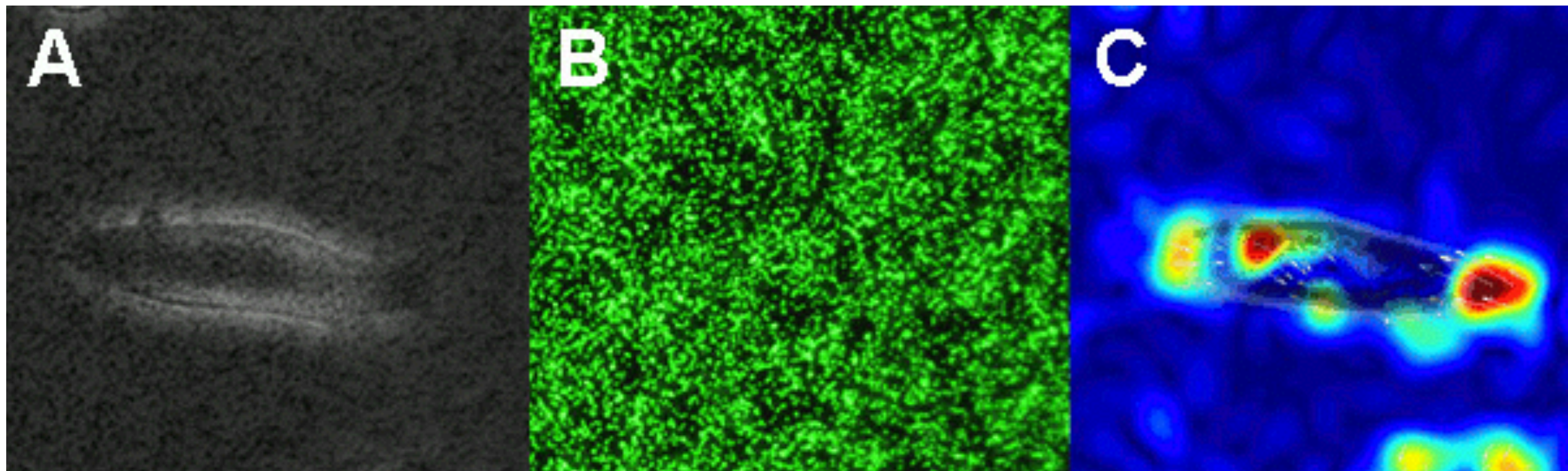
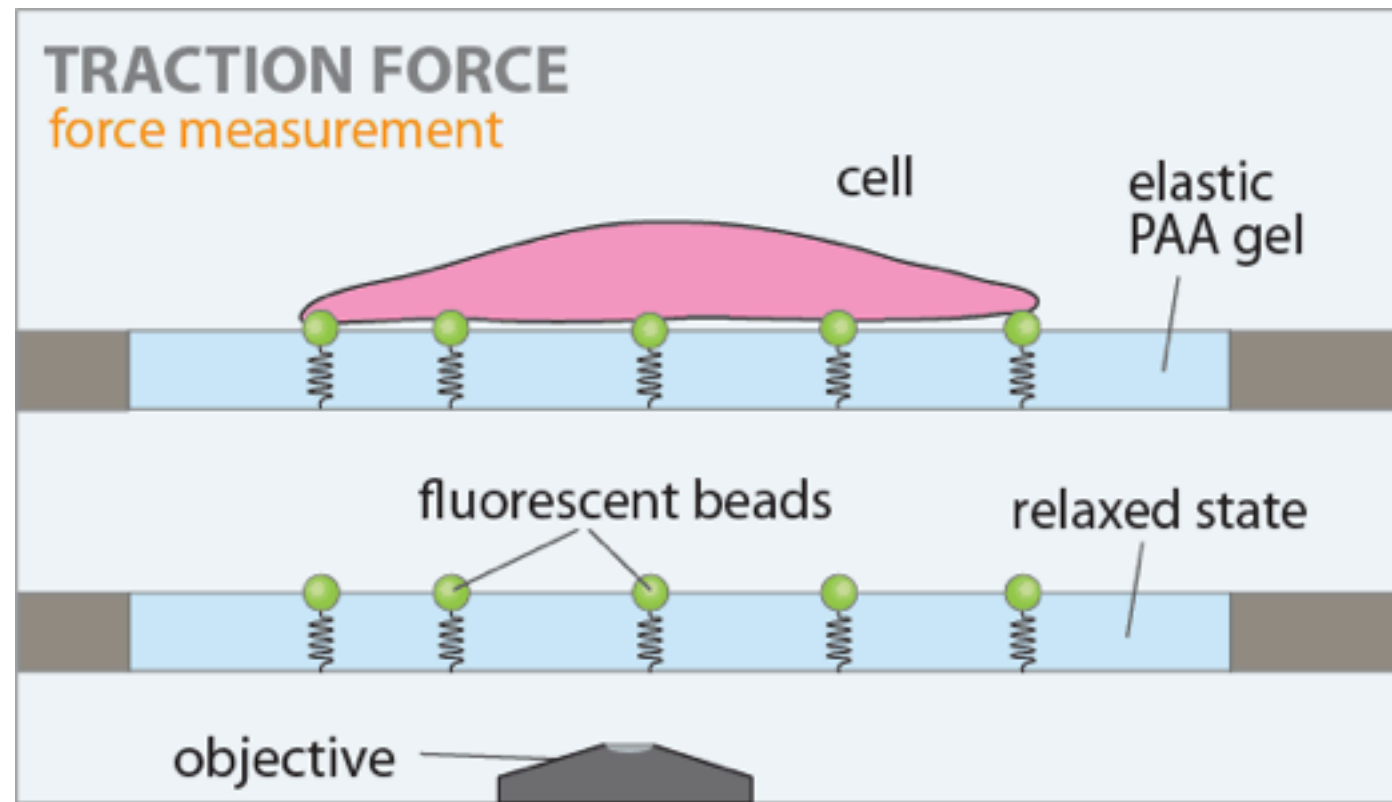


## Confocal-Rheology (con-rheo)

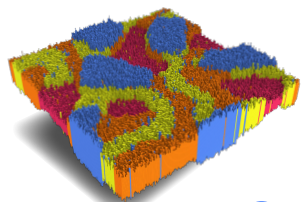




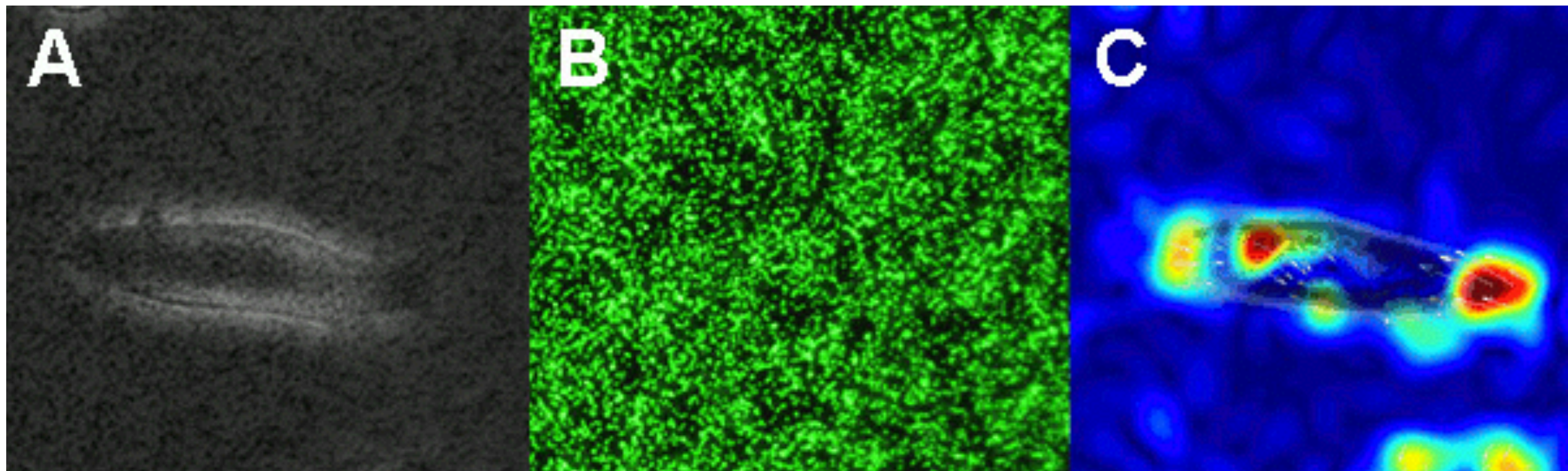
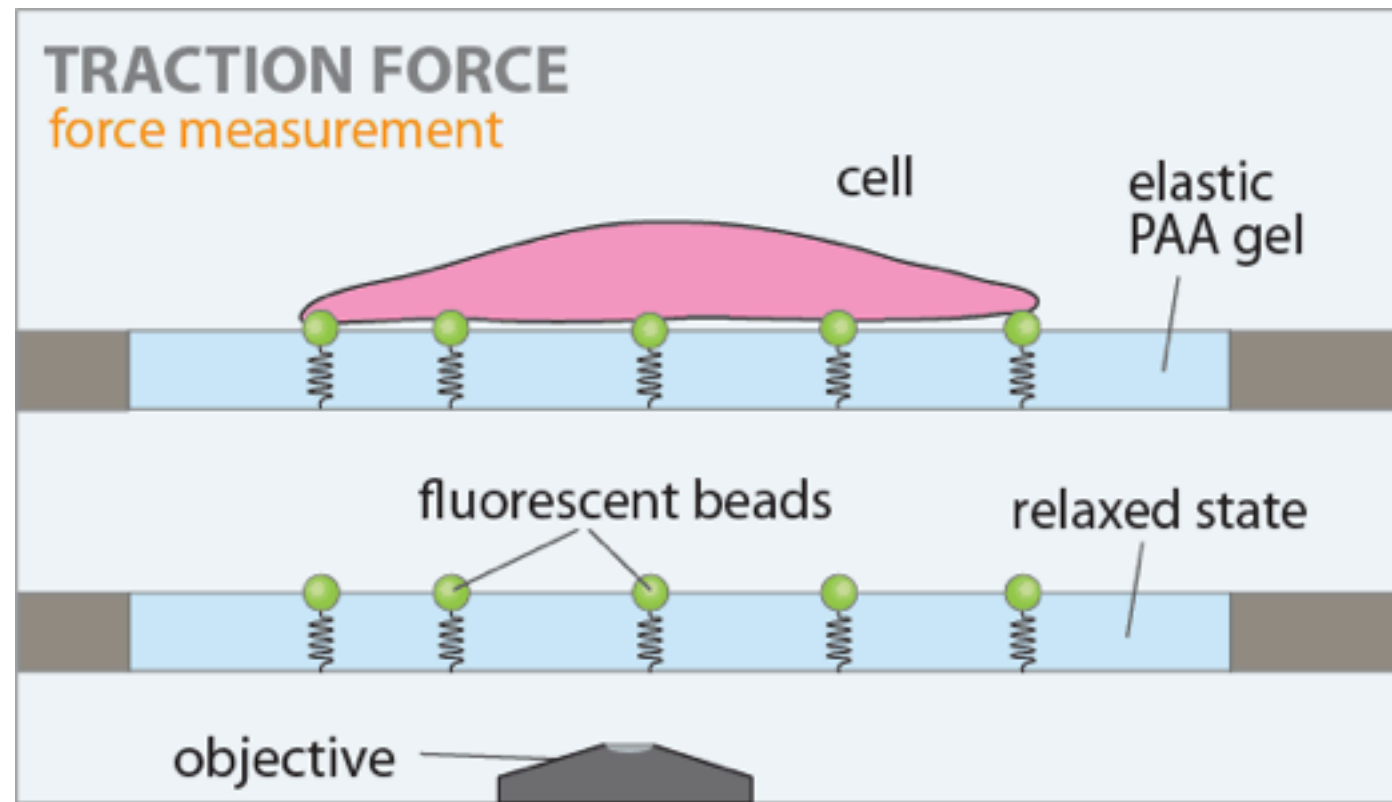
# Traction Forces/Boundary Stresses



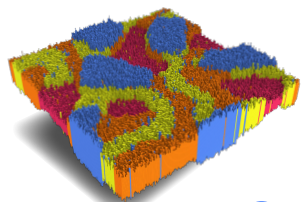




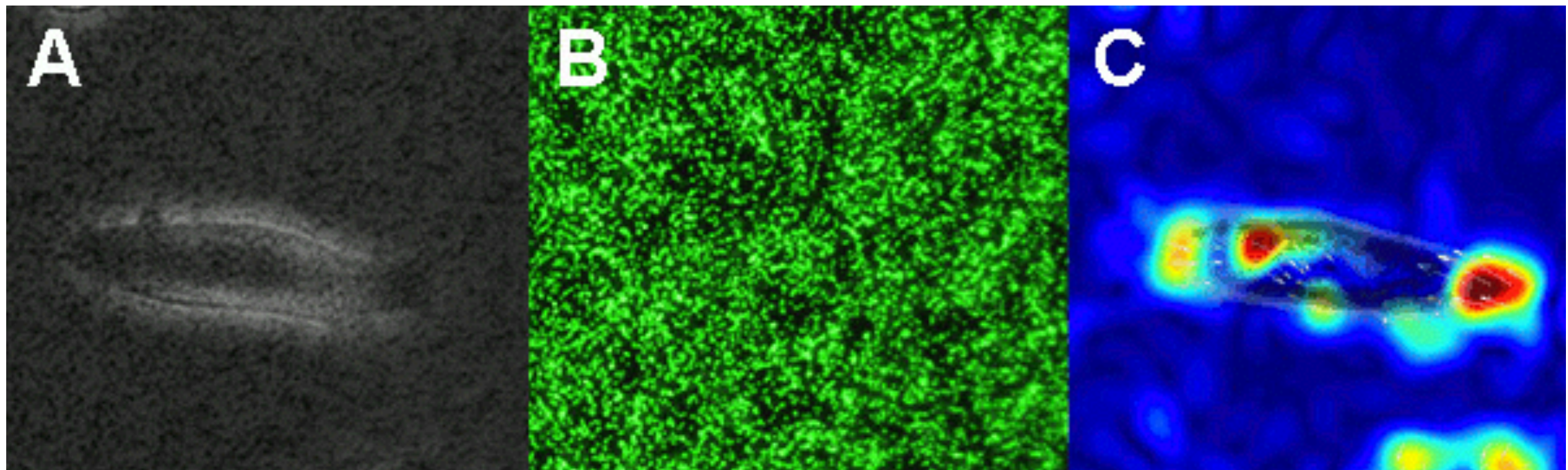
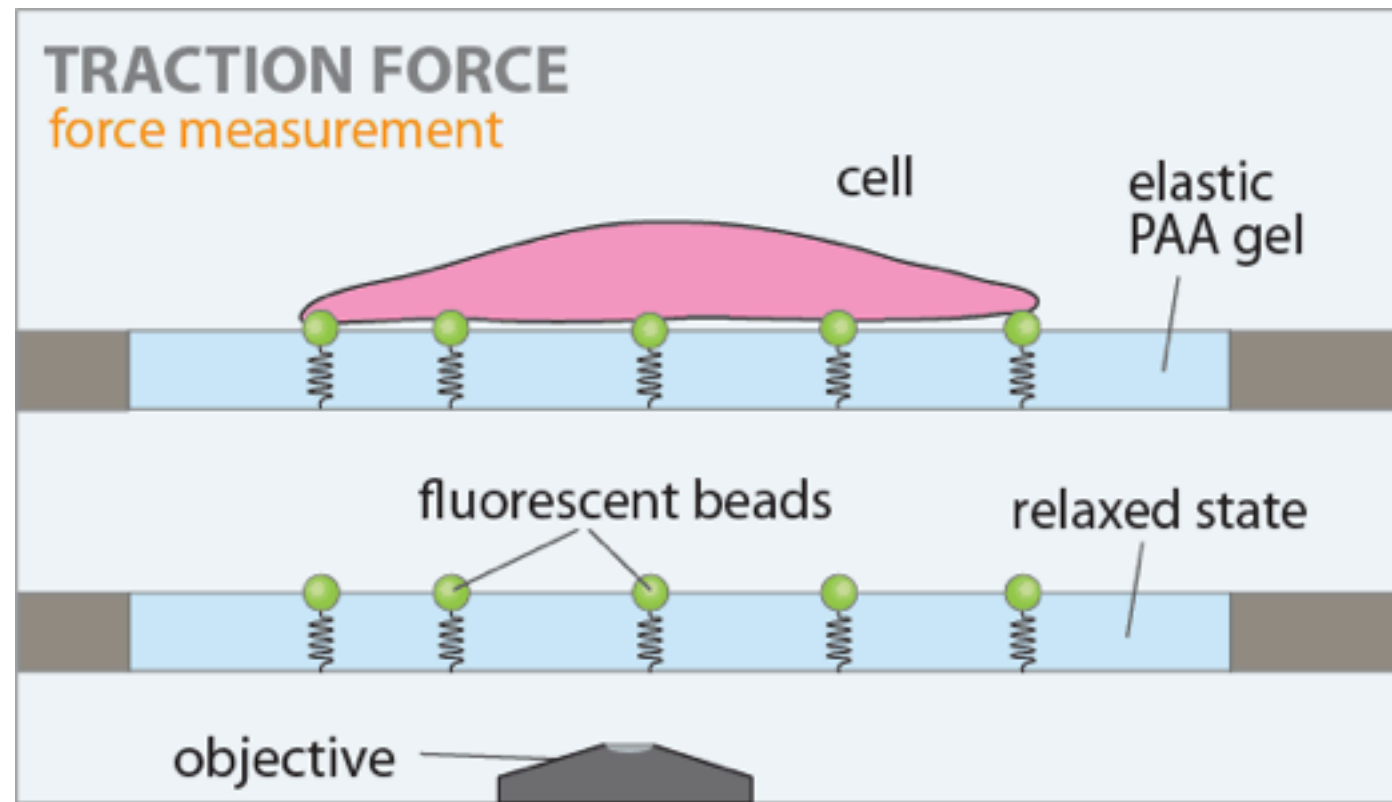
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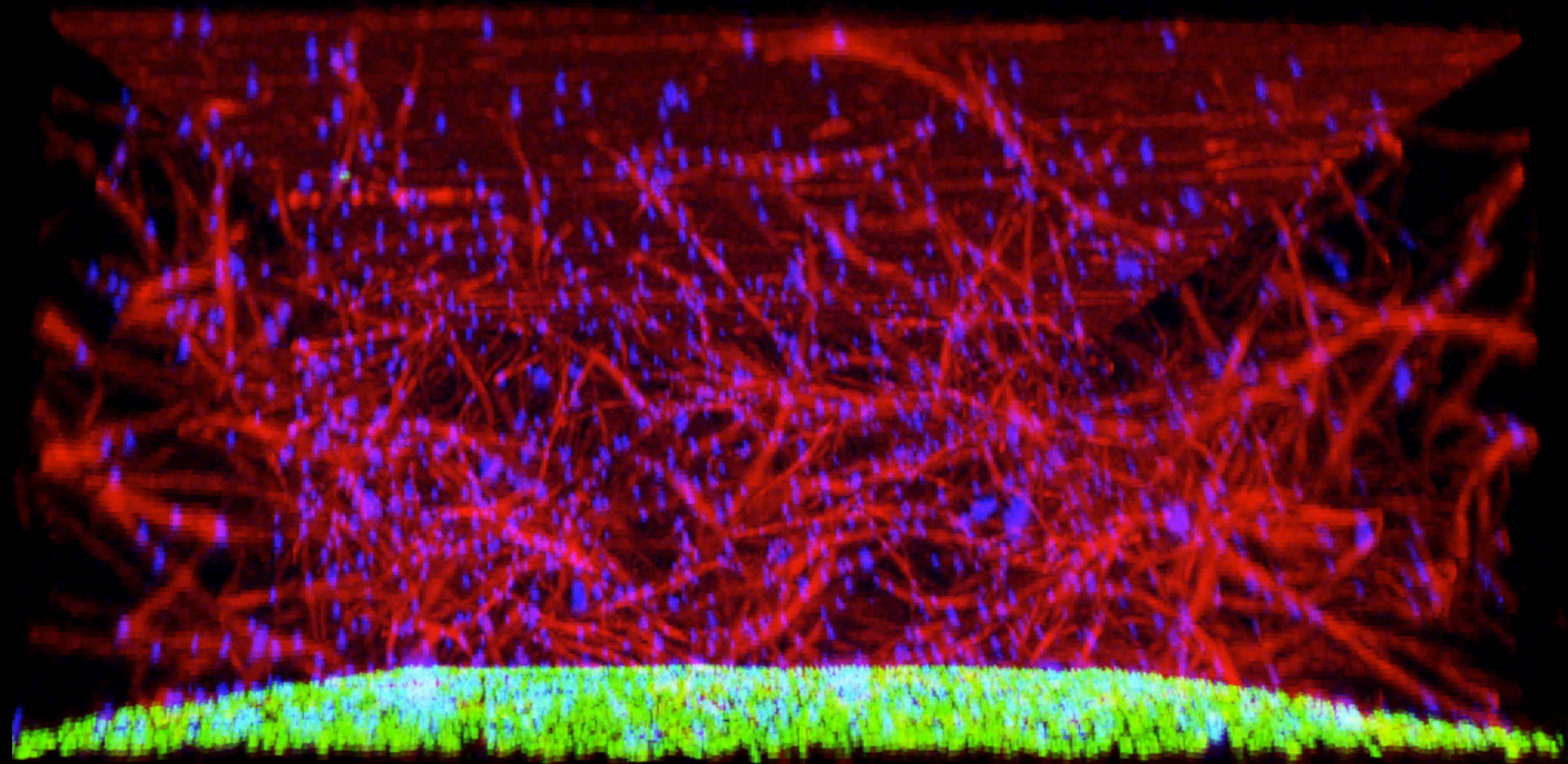




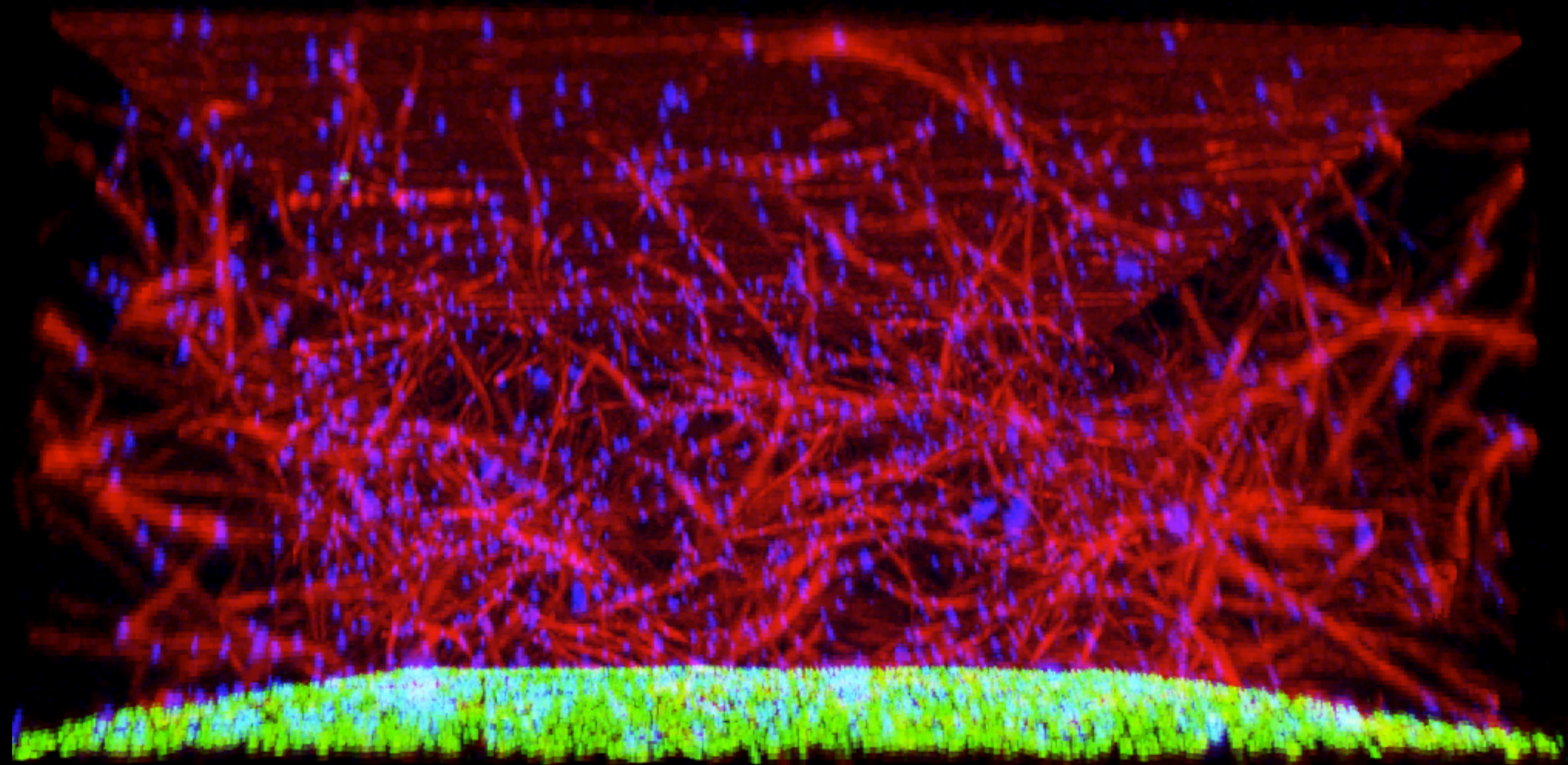
# Traction Forces/Boundary Stresses



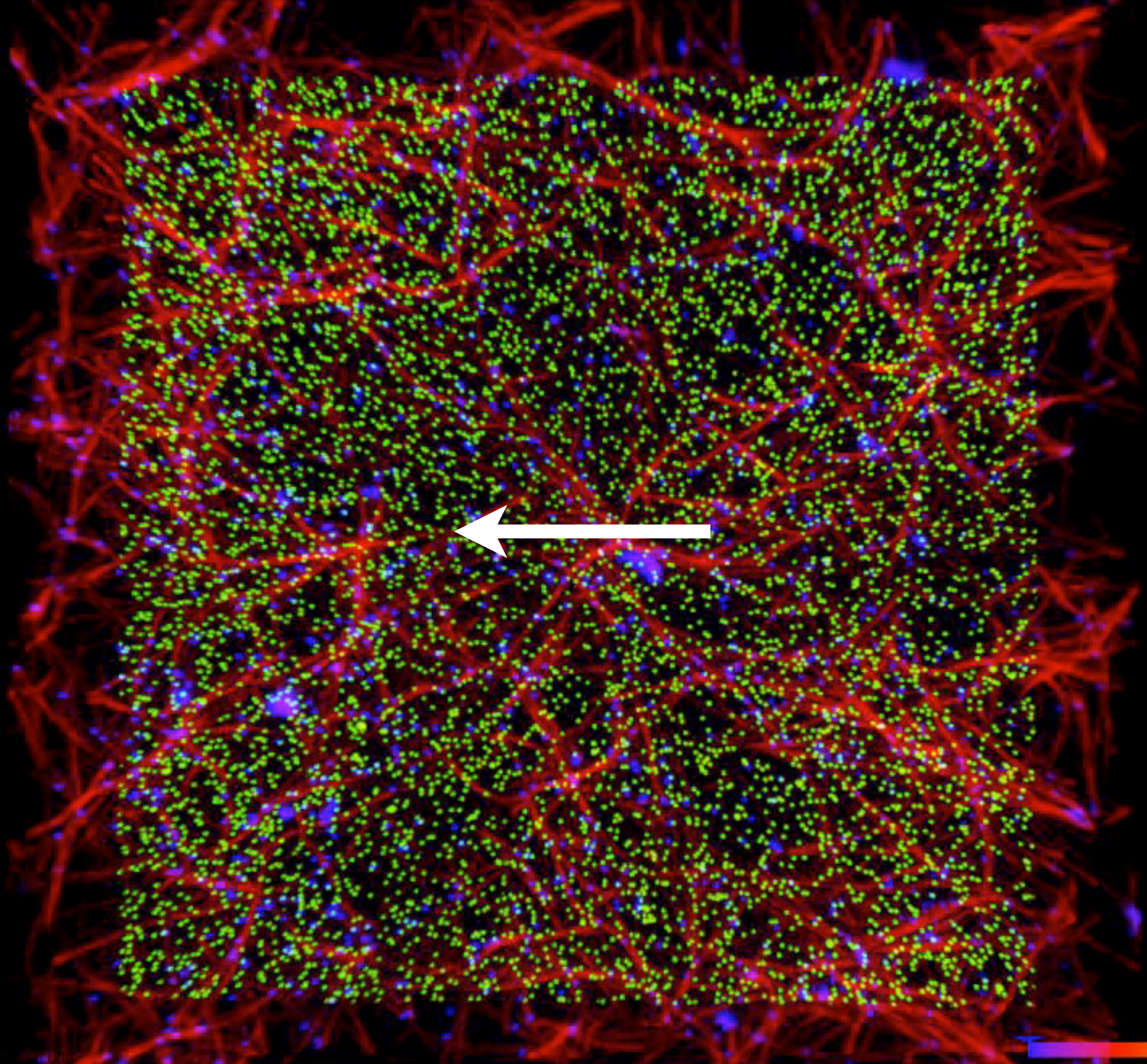




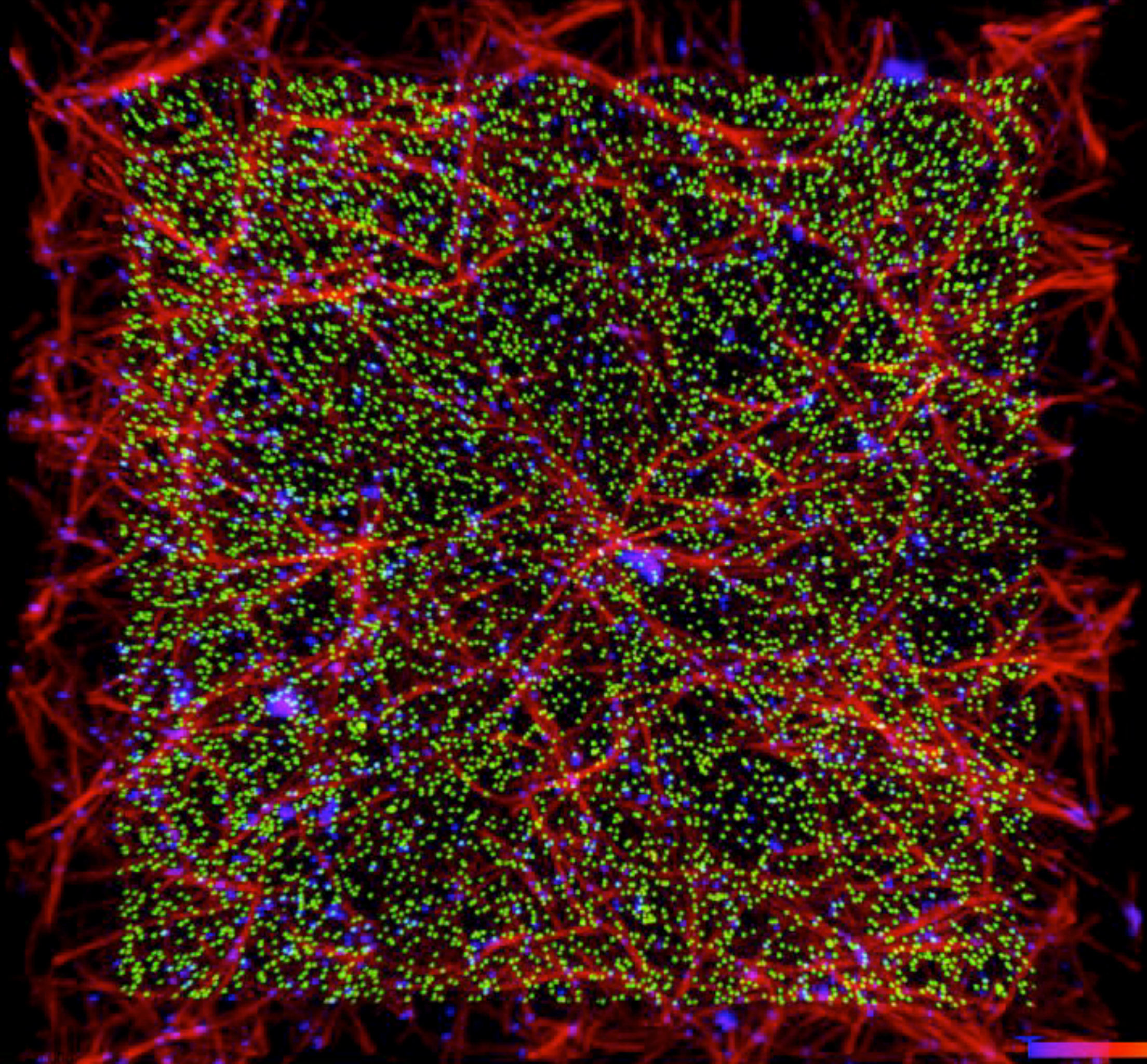






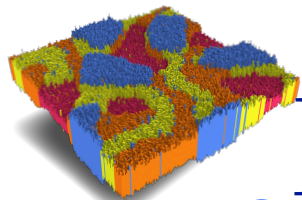






Time

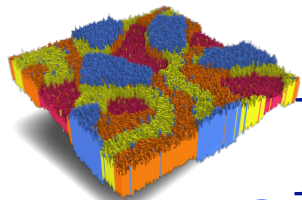




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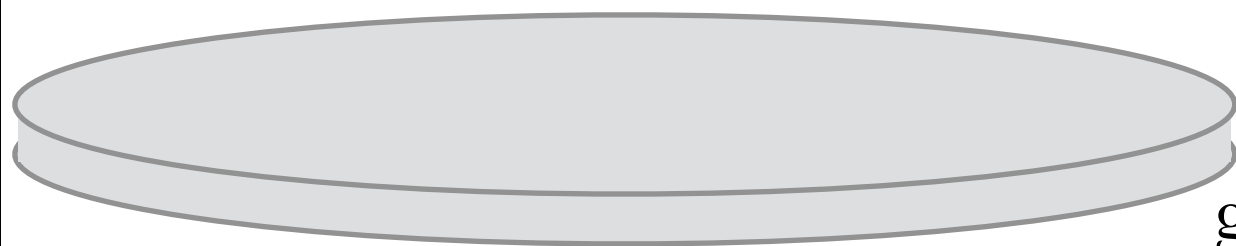
# Boundary Stress Microscopy (BSM) For Shear Thickening





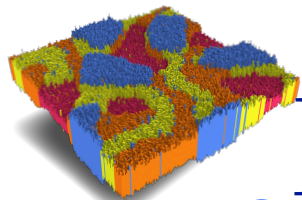
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# Boundary Stress Microscopy (BSM) For Shear Thickening



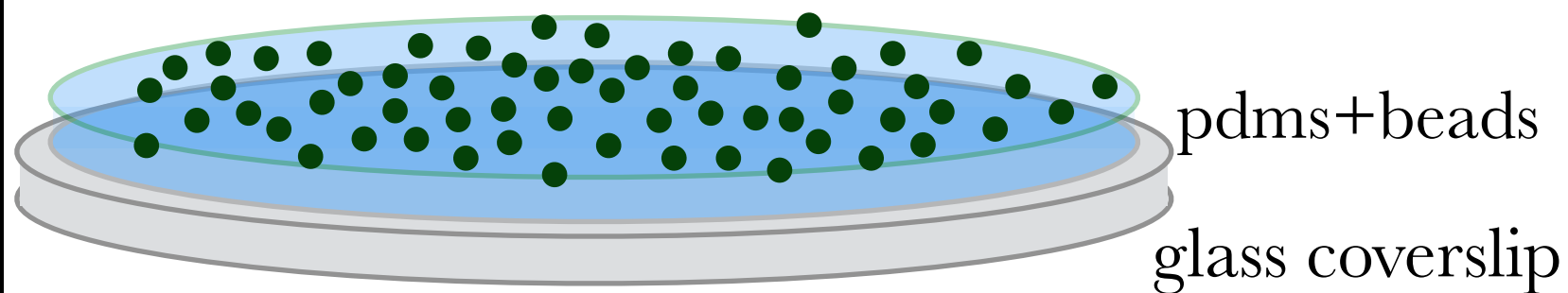
glass coverslip

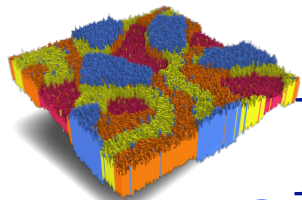




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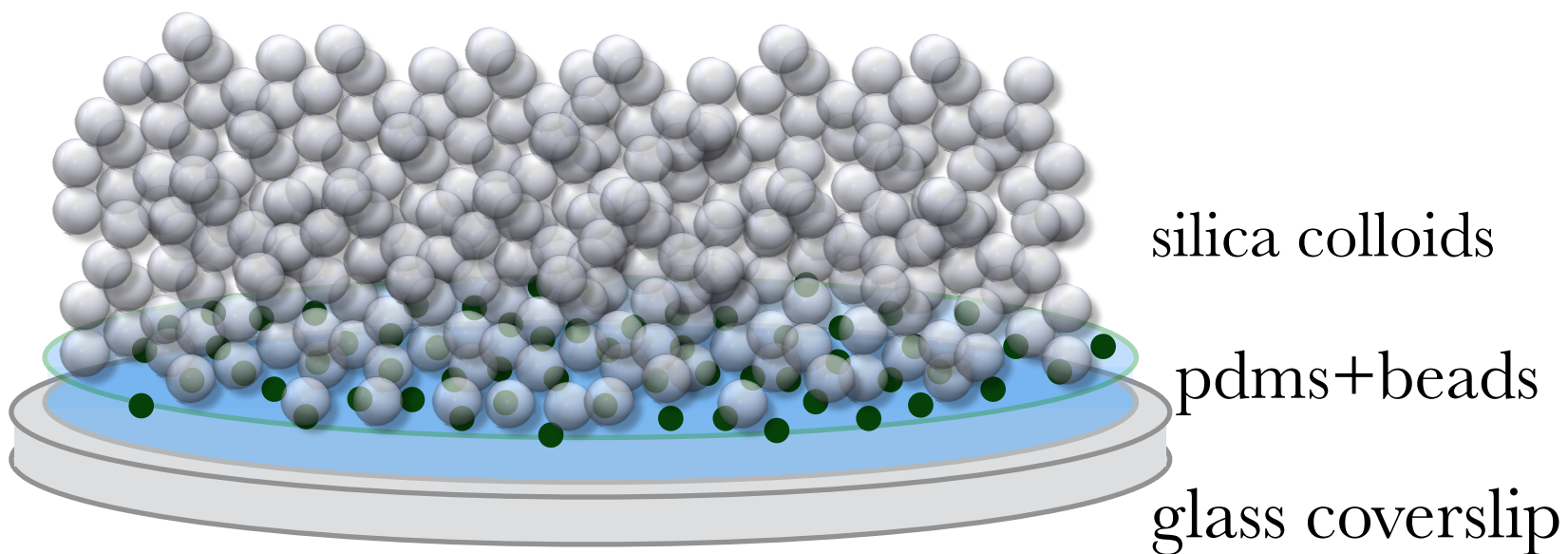
# Boundary Stress Microscopy (BSM) For Shear Thickening





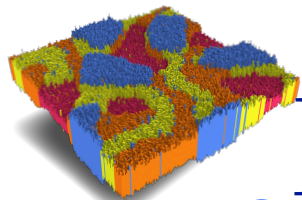
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# Boundary Stress Microscopy (BSM) For Shear Thickening



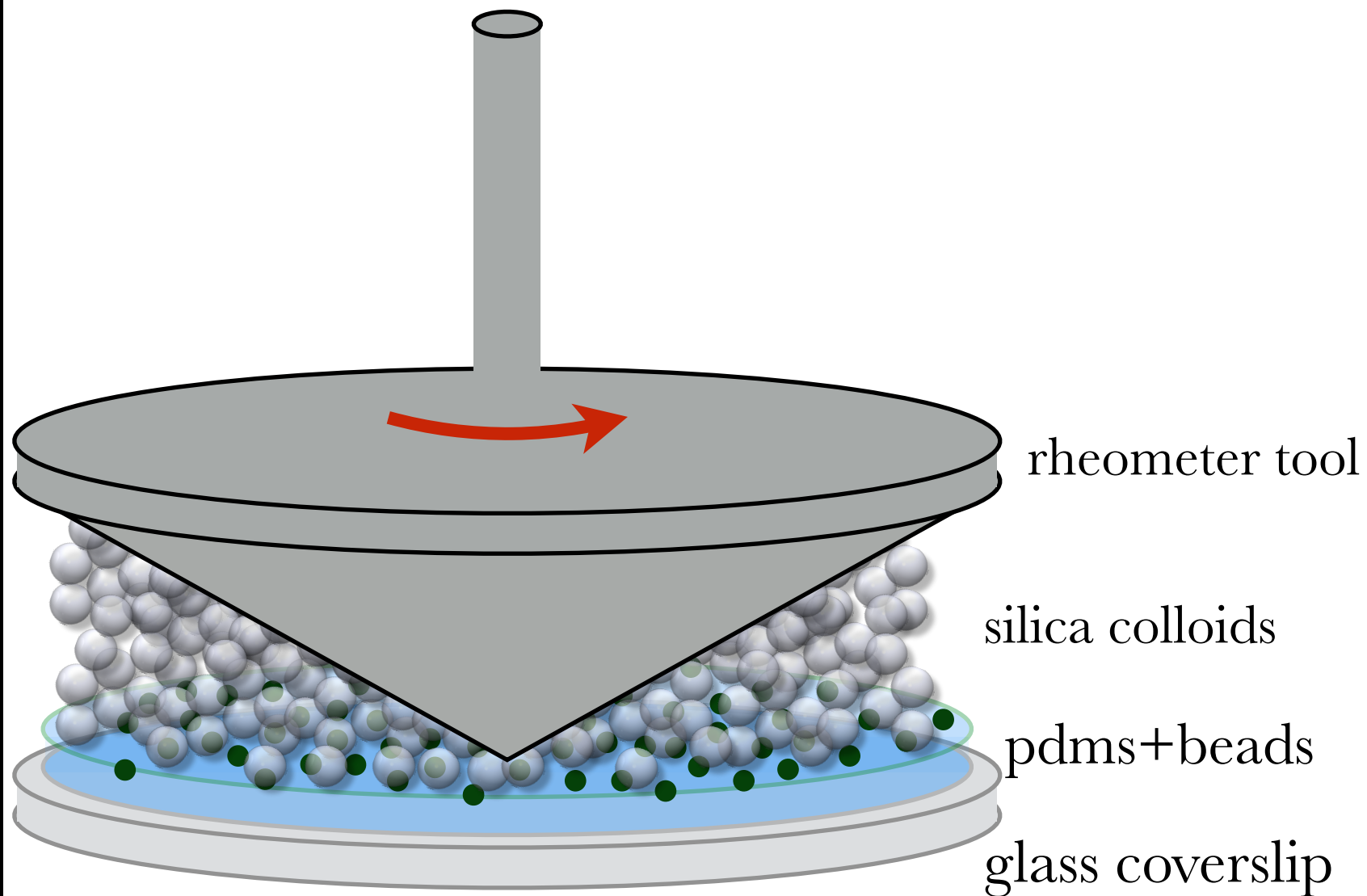
arXiv:1702.02068, *PNAS* (on the way)



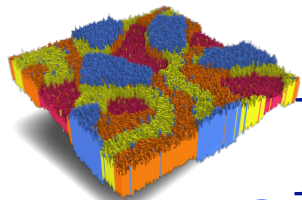


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# Boundary Stress Microscopy (BSM) For Shear Thickening

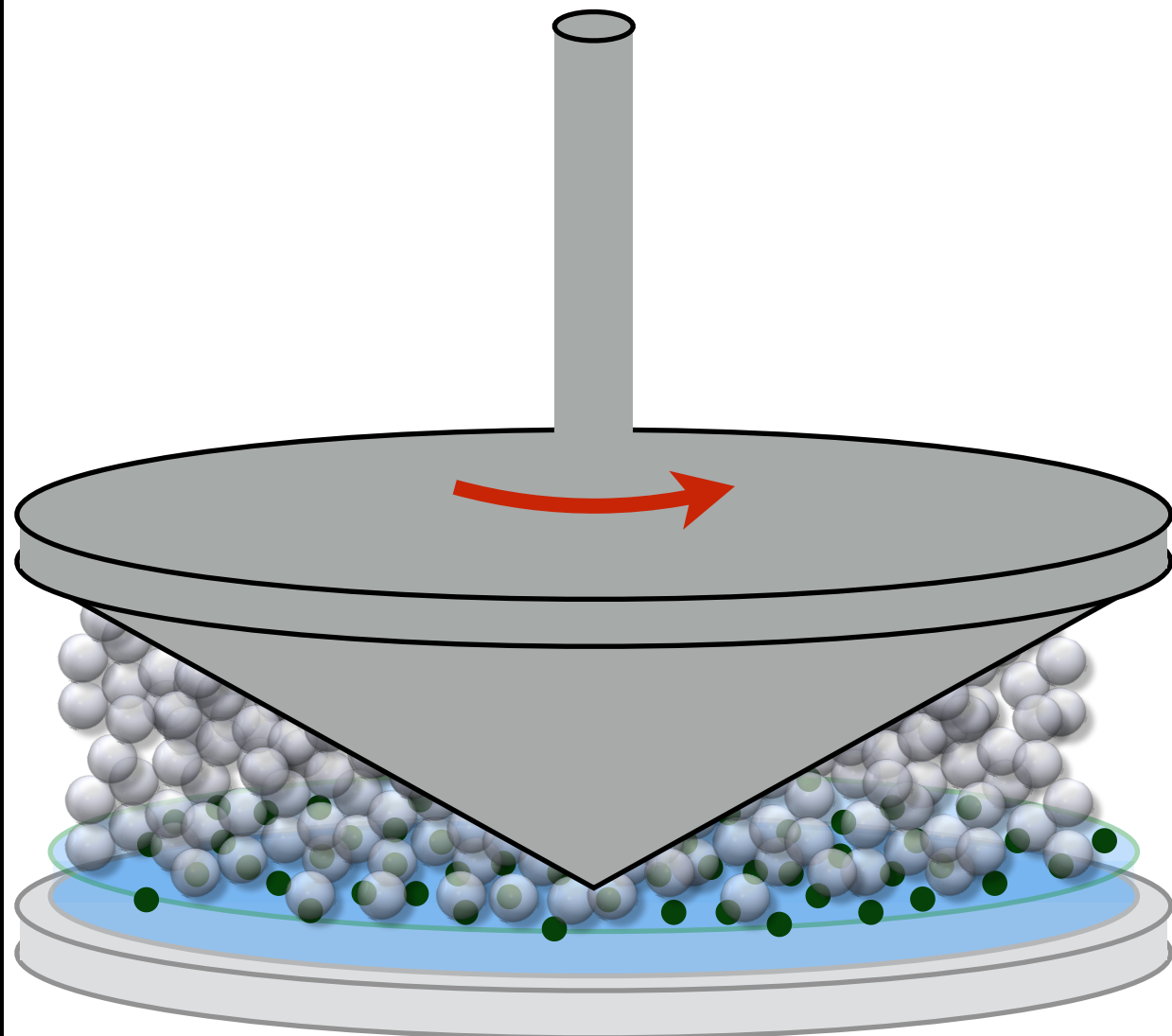


arXiv:1702.02068, *PNAS* (on the way)

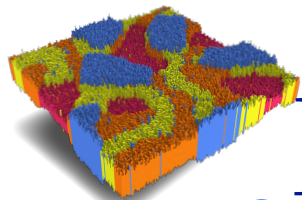


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# Boundary Stress Microscopy (BSM) For Shear Thickening



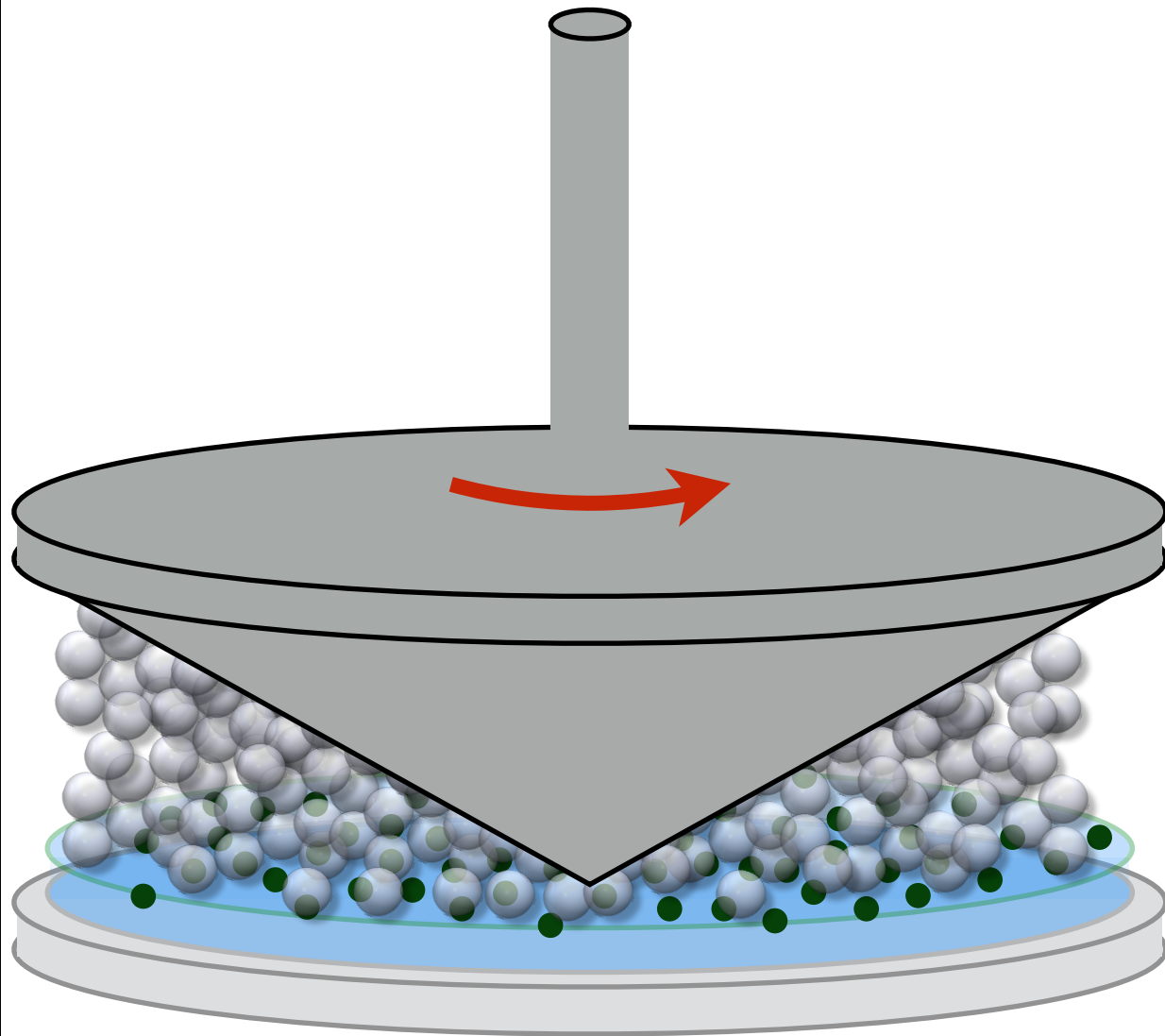
arXiv:1702.02068, *PNAS* (on the way)



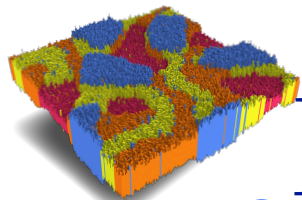
# Boundary Stress Microscopy (BSM) For Shear Thickening

## System Details

- Suspension:  
silica —  $2a = 0.96 \mu\text{m}$   
glycerol/water
- Boundary  
PDMS —  $\gamma = 10 \text{ kPa}$   
markers —  $2a = 1.0 \mu\text{m}$

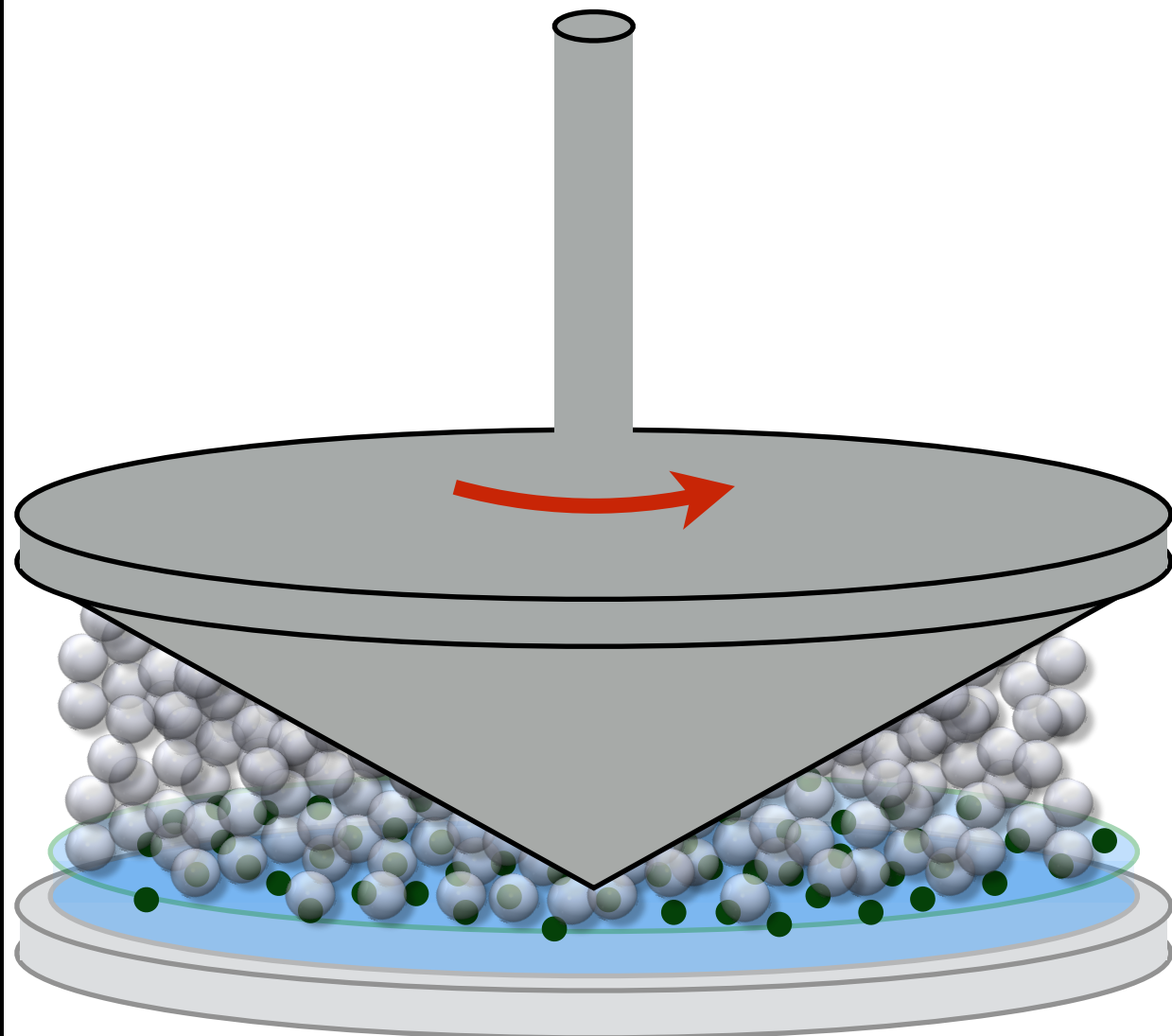






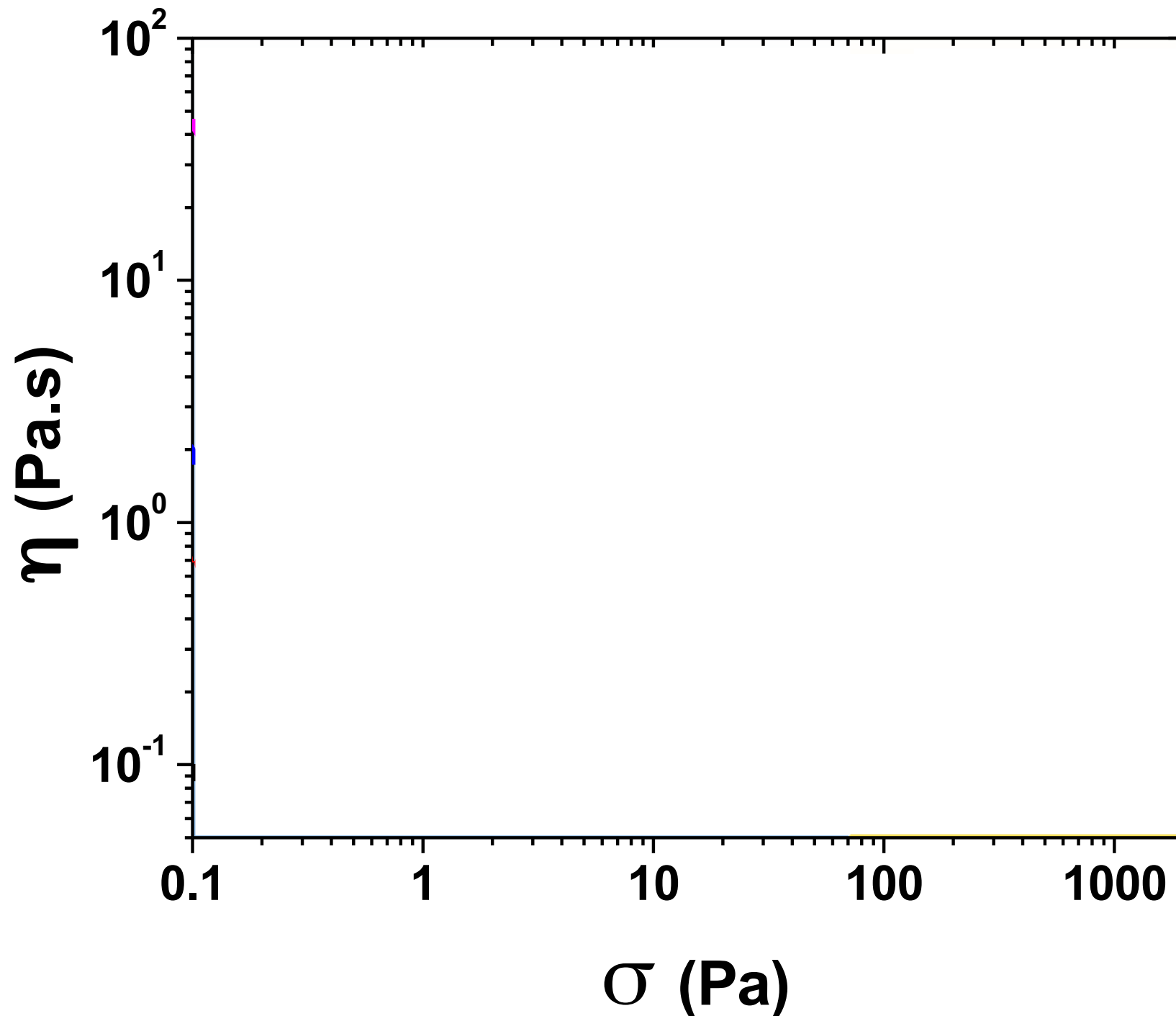
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# Boundary Stress Microscopy (BSM) For Shear Thickening

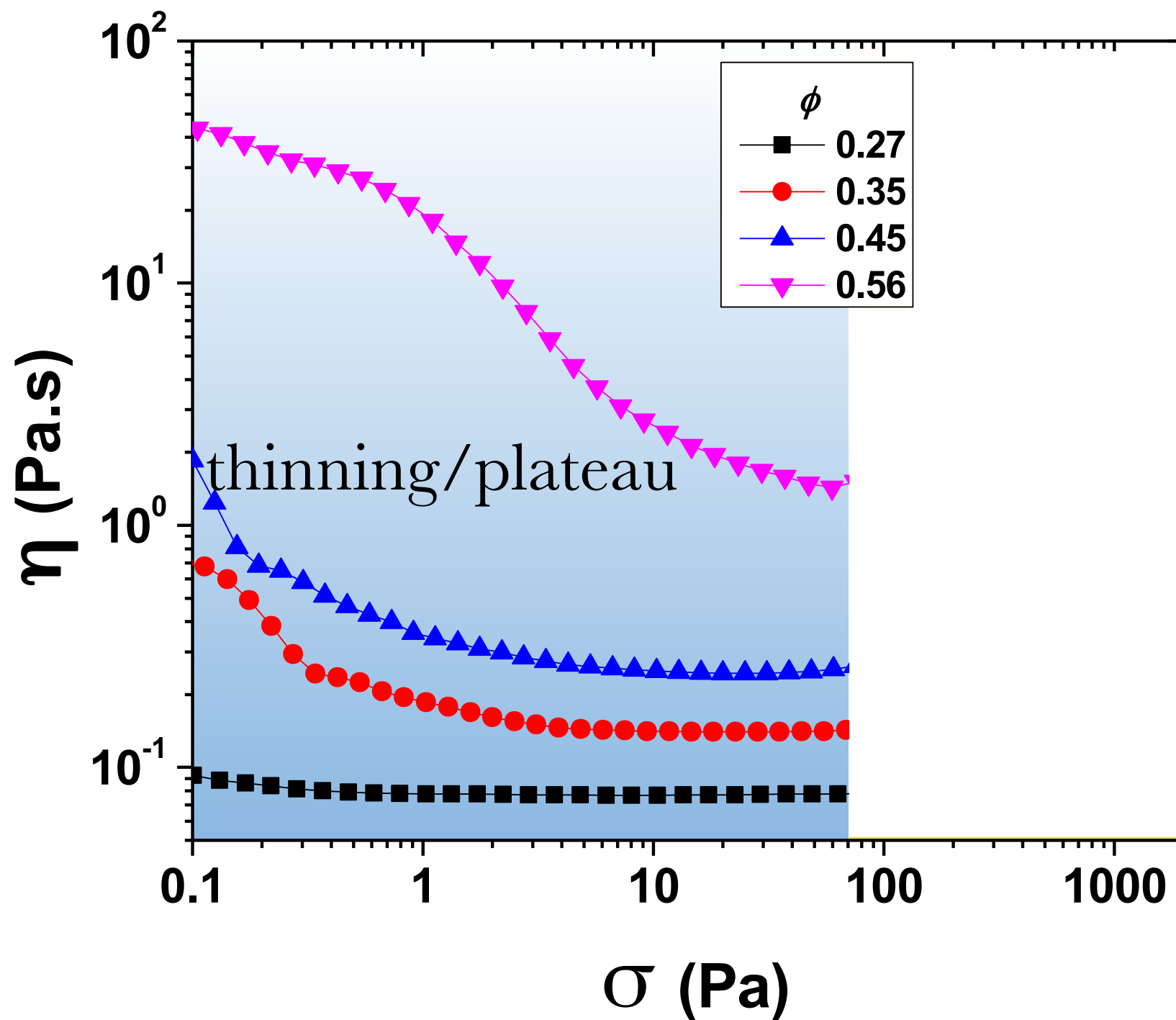


arXiv:1702.02068, *PNAS* (on the way)

# Continuous Shear Thickening Rheology

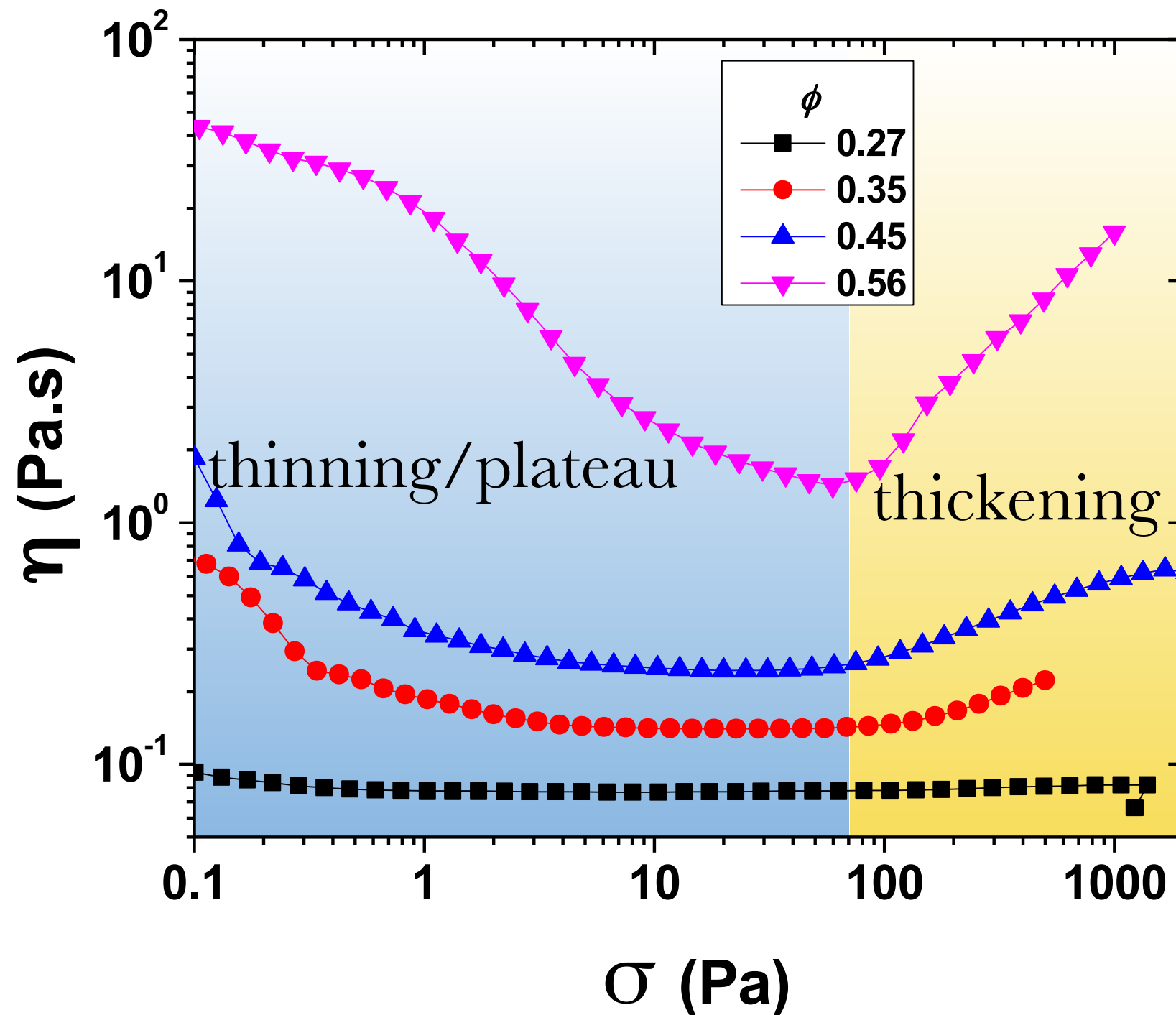


# Continuous Shear Thickening Rheology

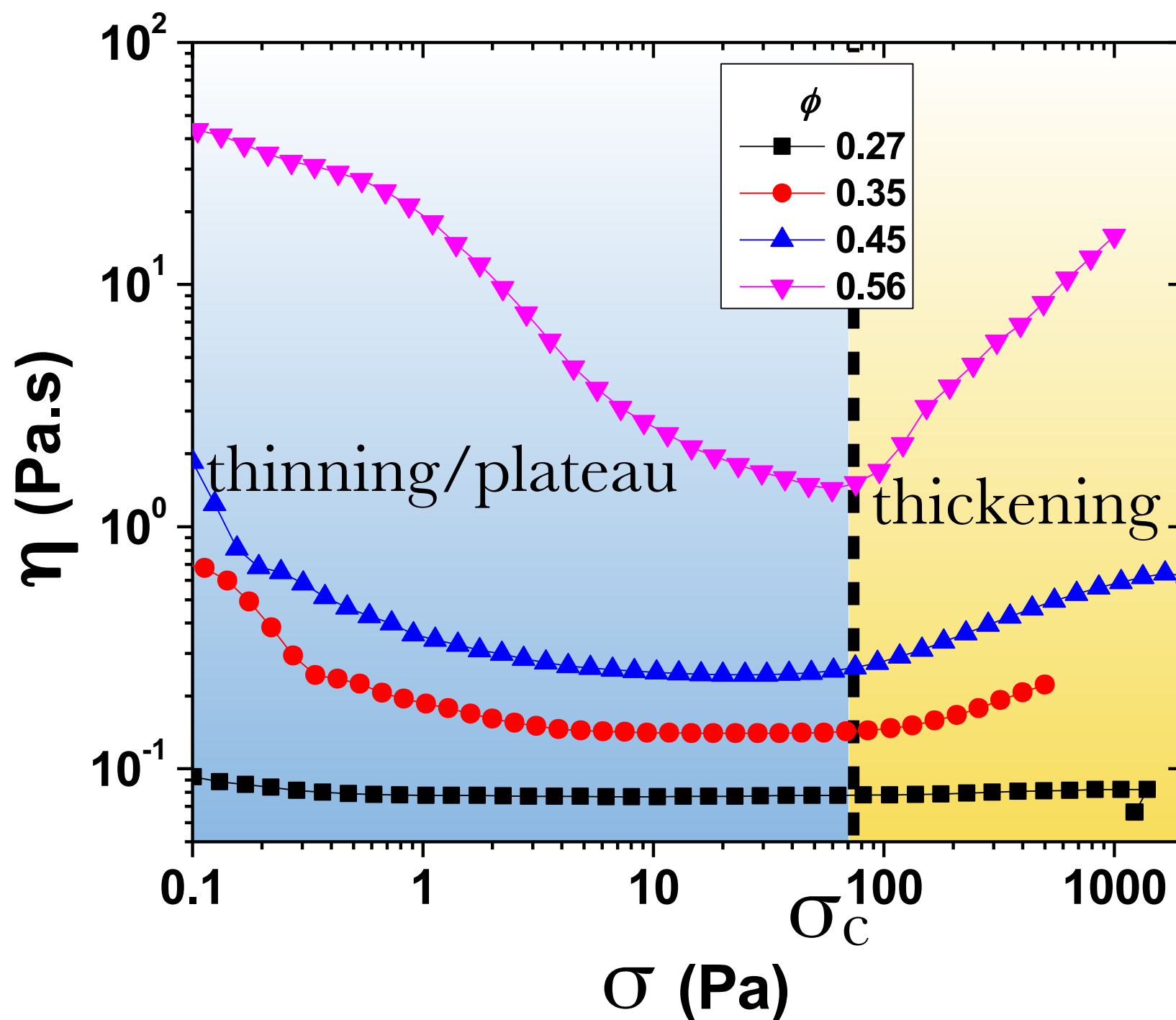




# Continuous Shear Thickening Rheology

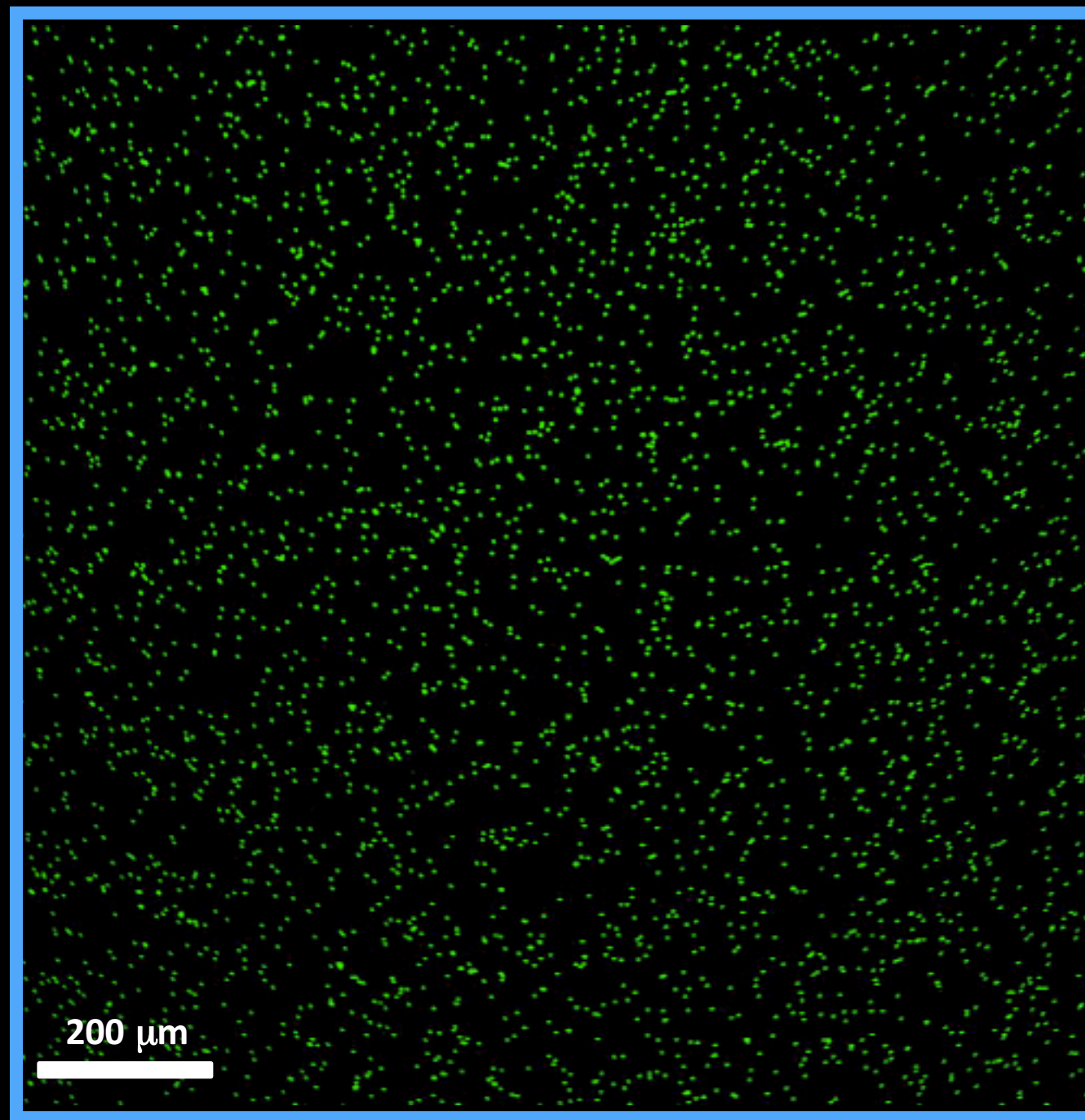


# Continuous Shear Thickening Rheology

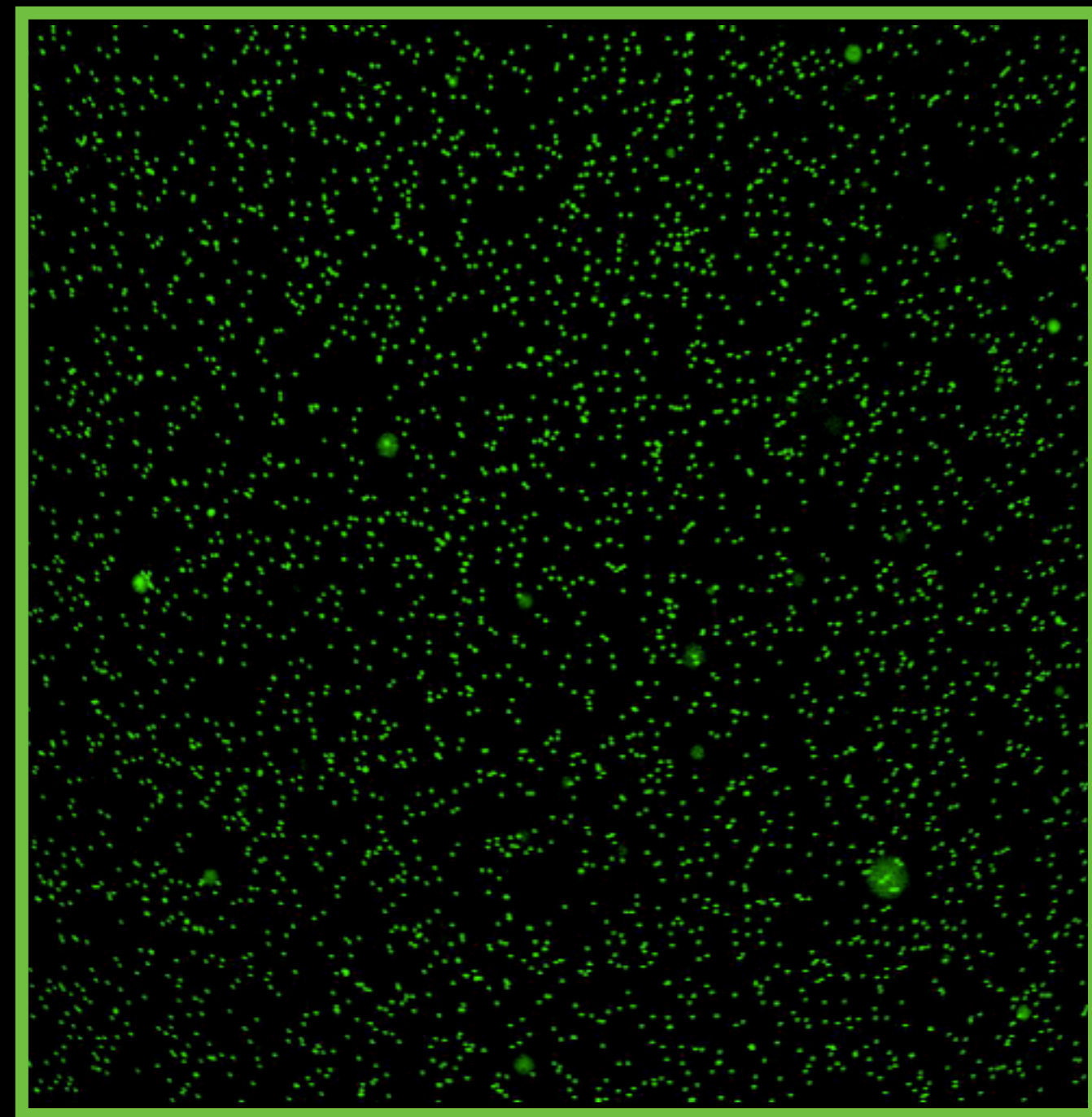


# Boundary Stresses: $\phi = 56\%$

## Displacements



$\sigma = 100 \text{ Pa}$



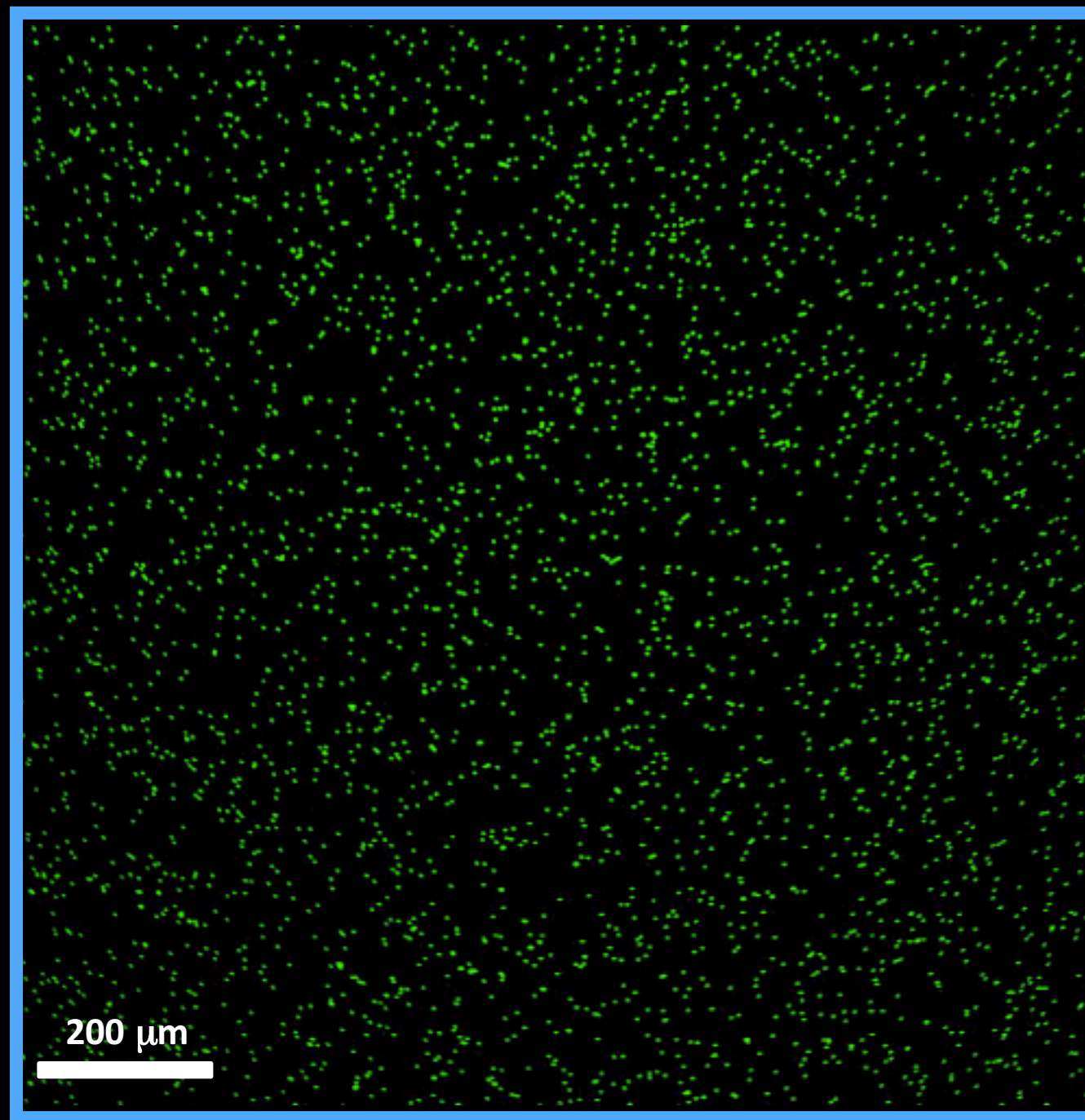
$\sigma = 1000 \text{ Pa}$

velocity  $\leftarrow$   
vorticity  $\uparrow$

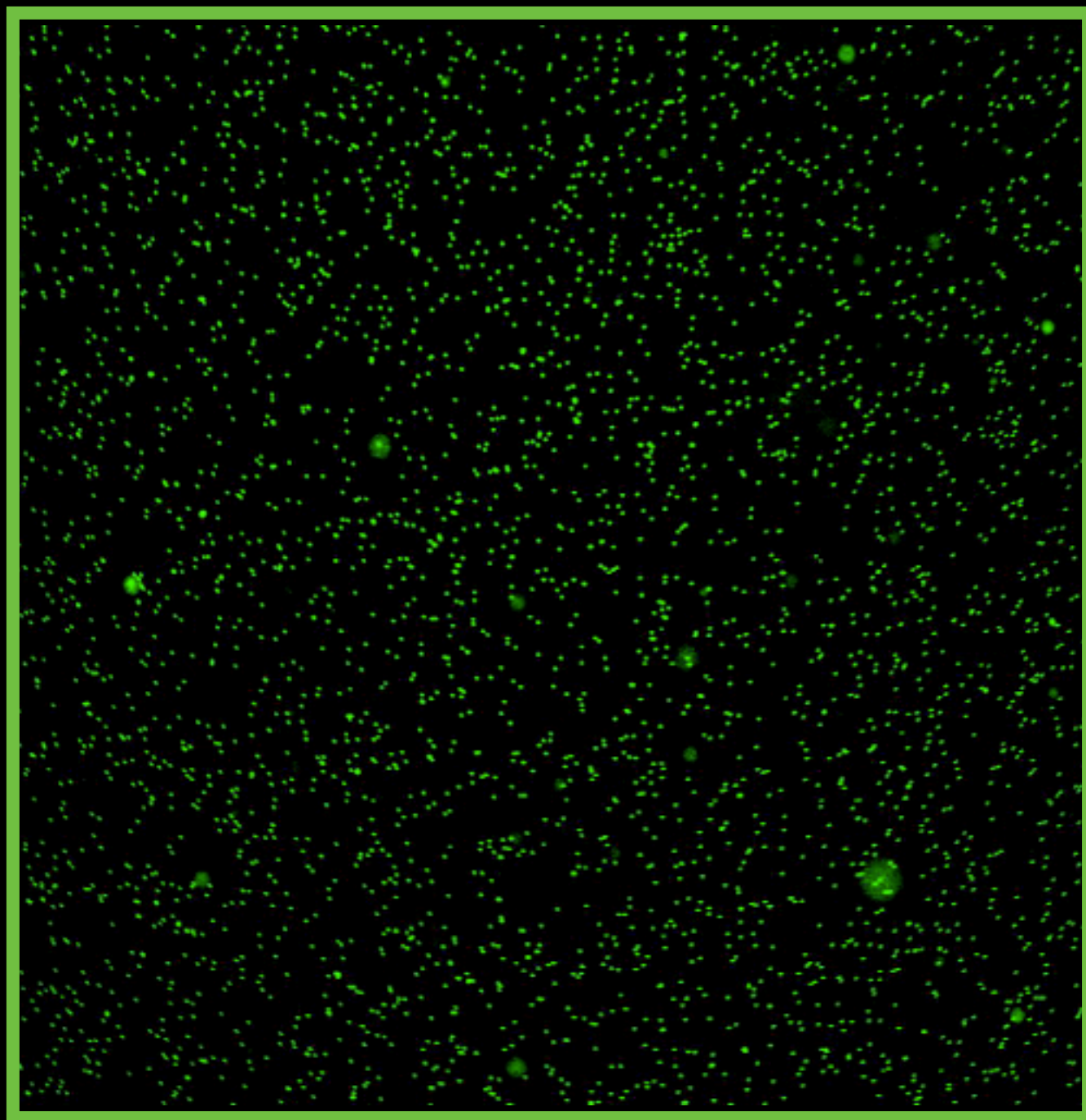


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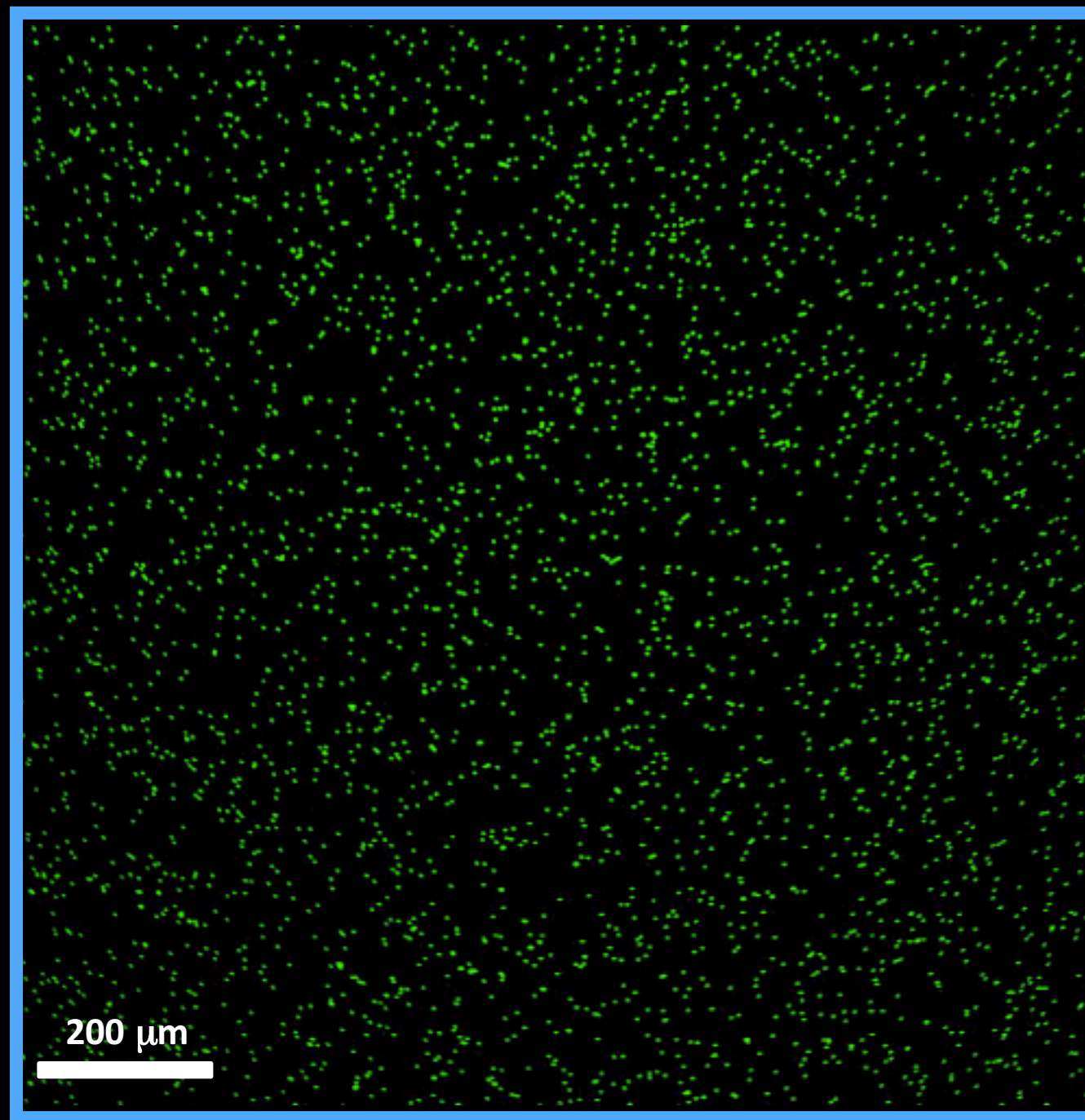
$\sigma = 1000 \text{ Pa}$

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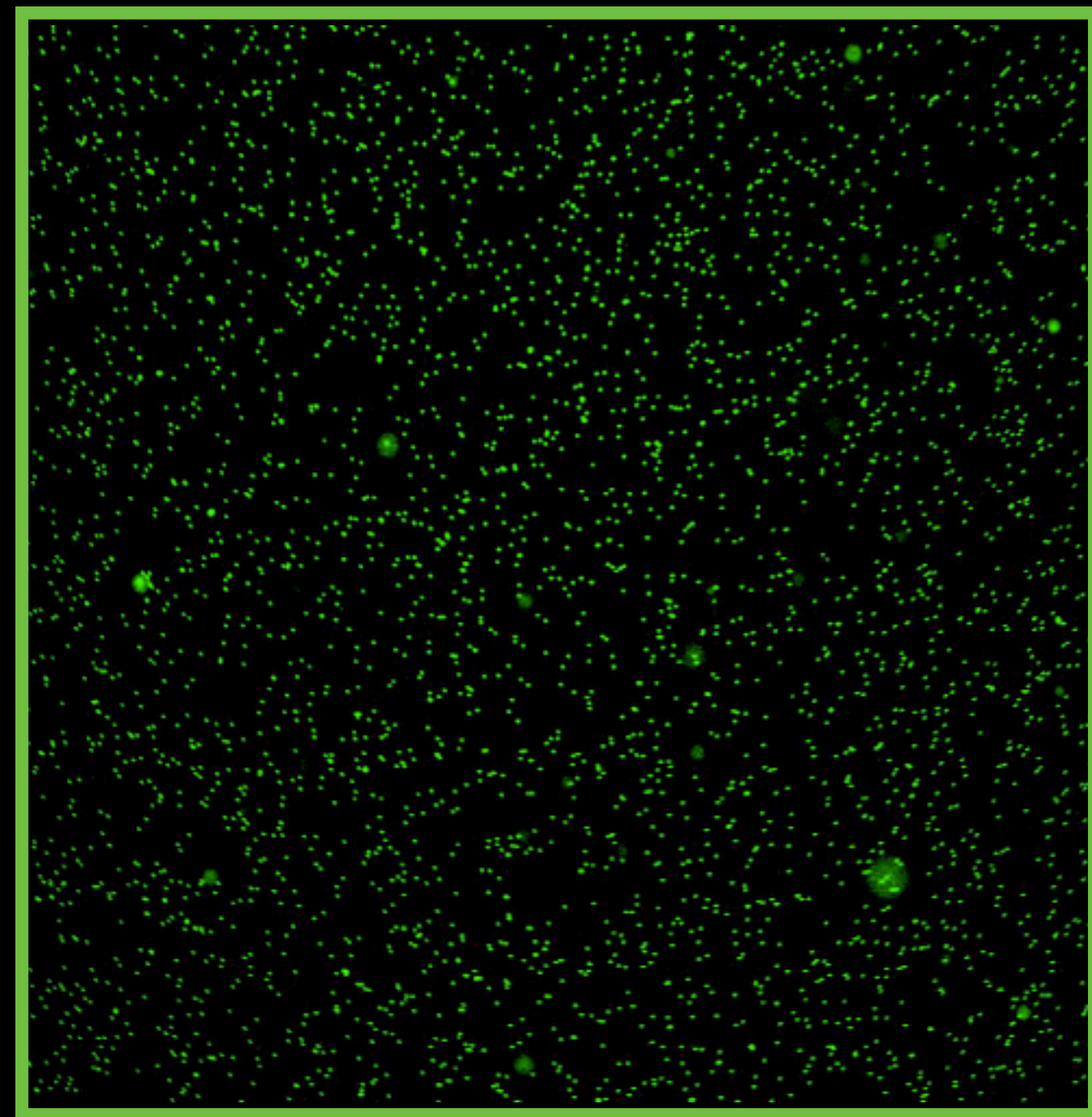


# Boundary Stresses: $\phi = 56\%$

## Displacements



$\sigma = 100 \text{ Pa}$

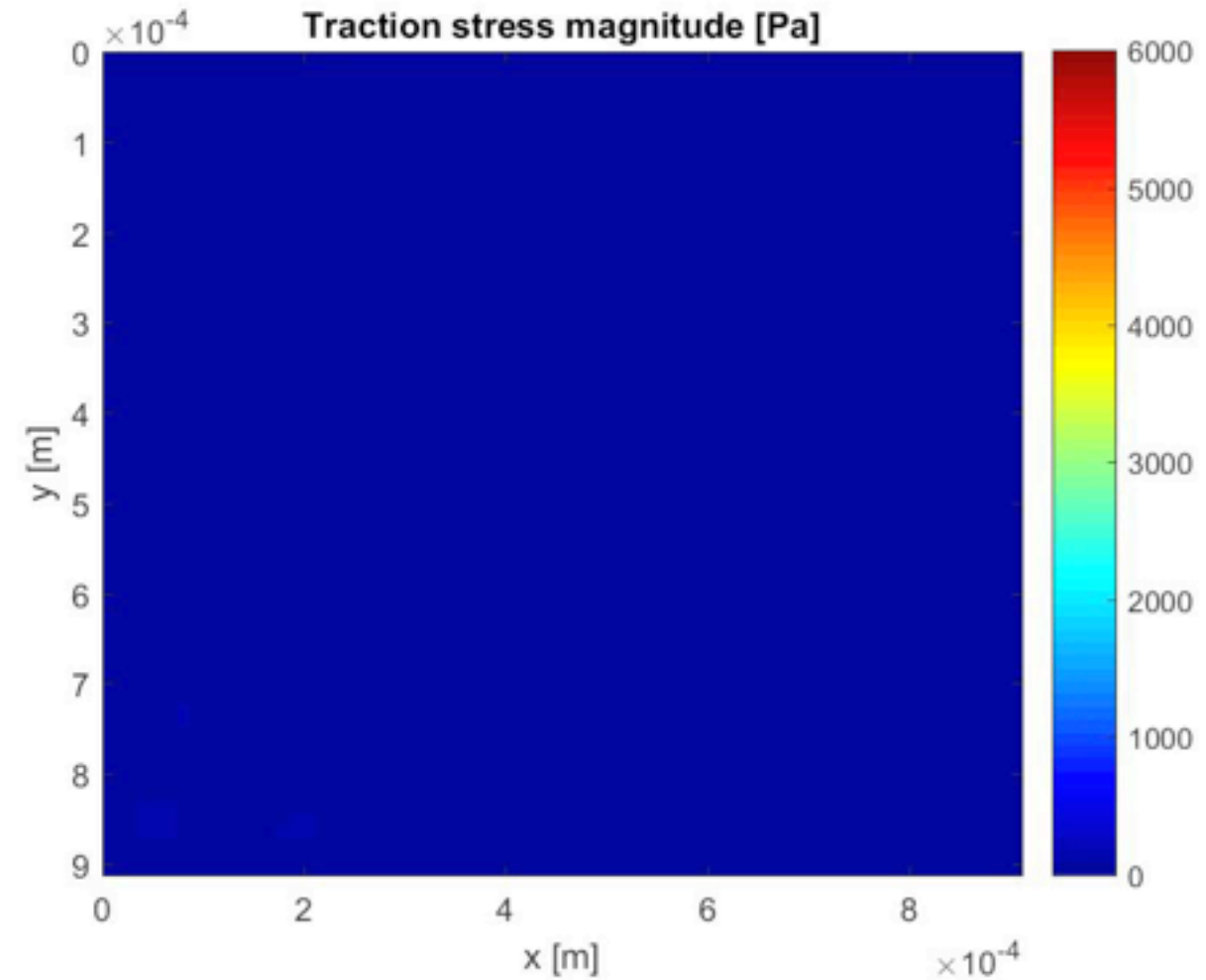
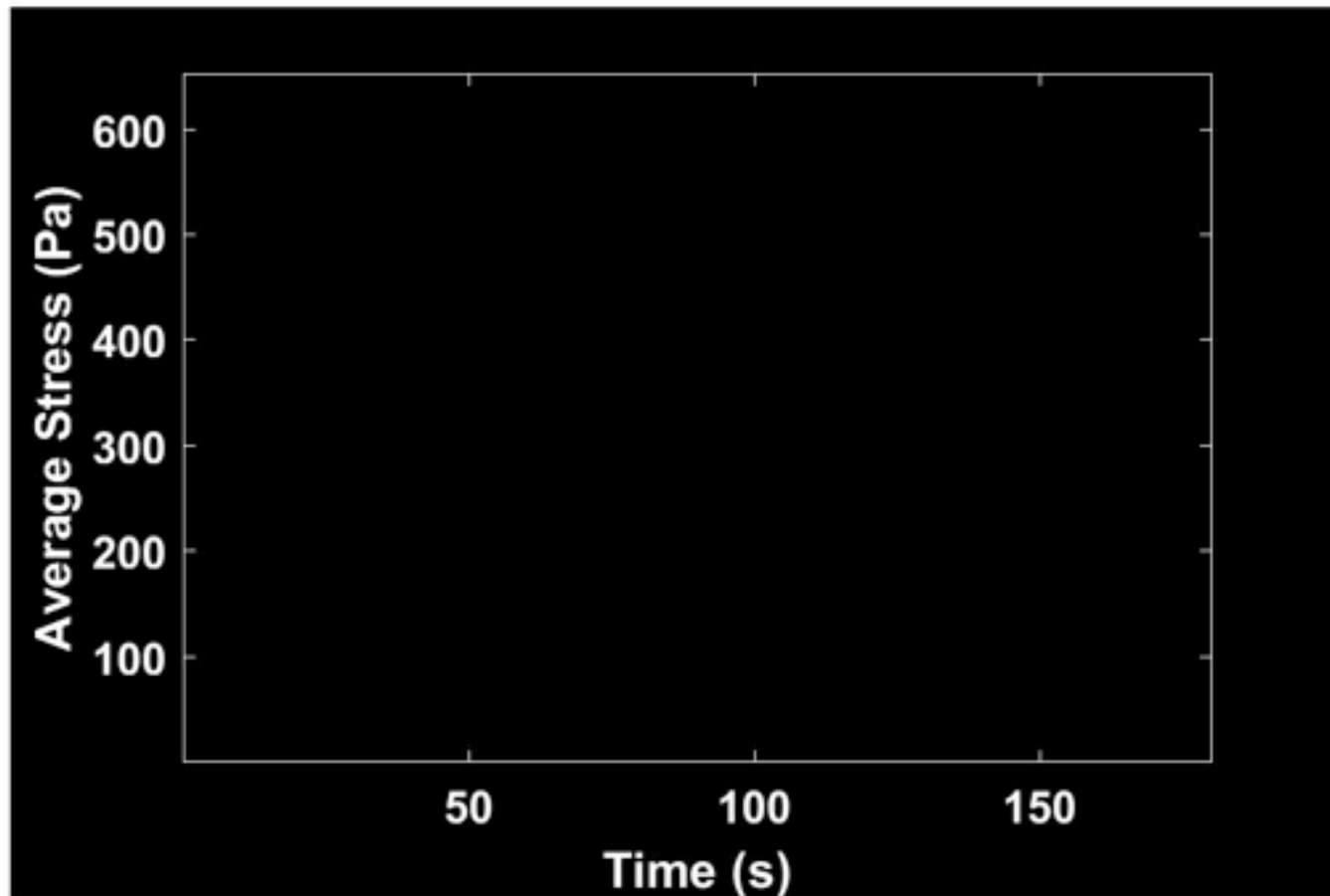


$\sigma = 1000 \text{ Pa}$

velocity  $\leftarrow$   
vorticity  $\uparrow$

# Boundary Stresses: $\phi = 56\%$

## Stress at the Interface

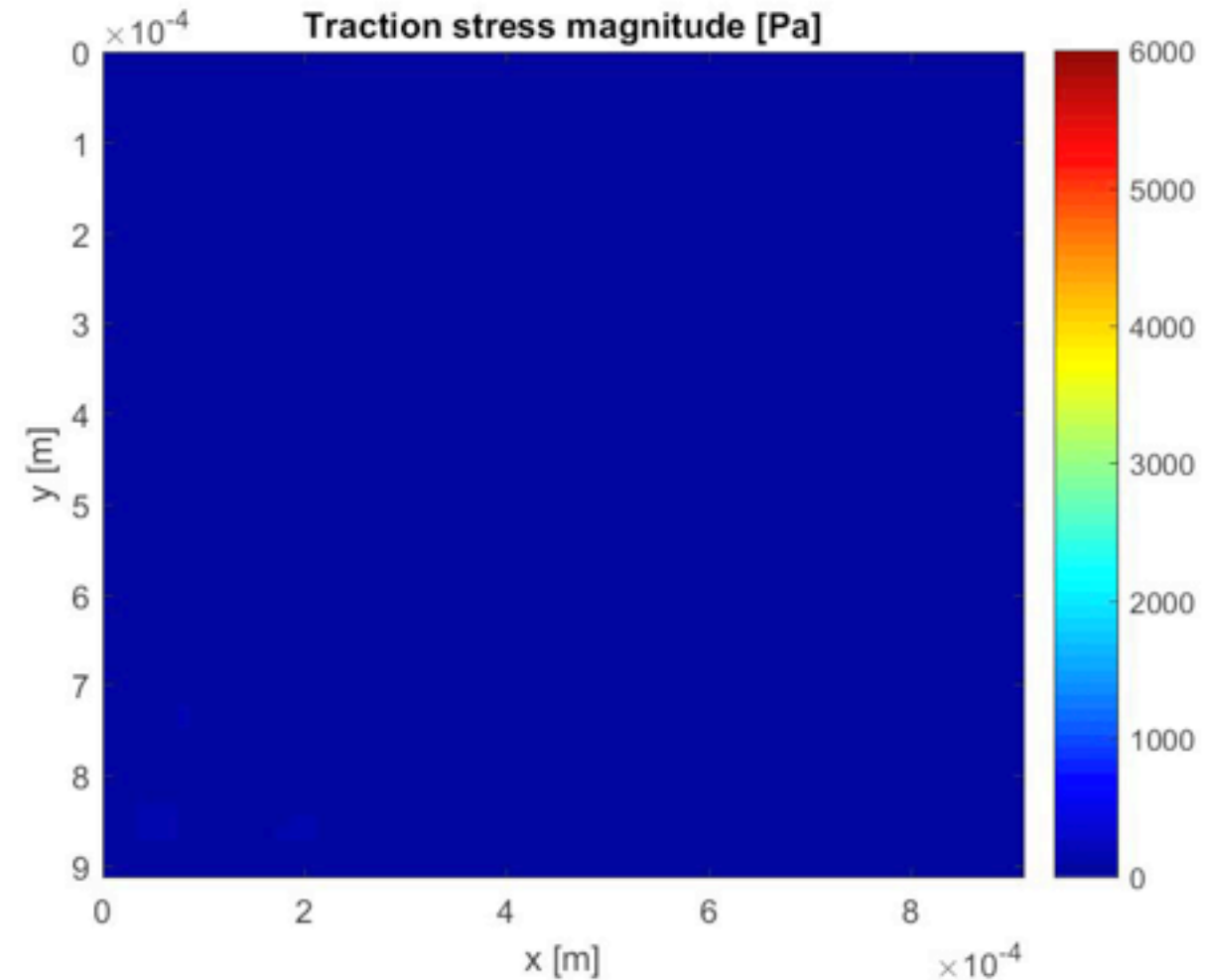
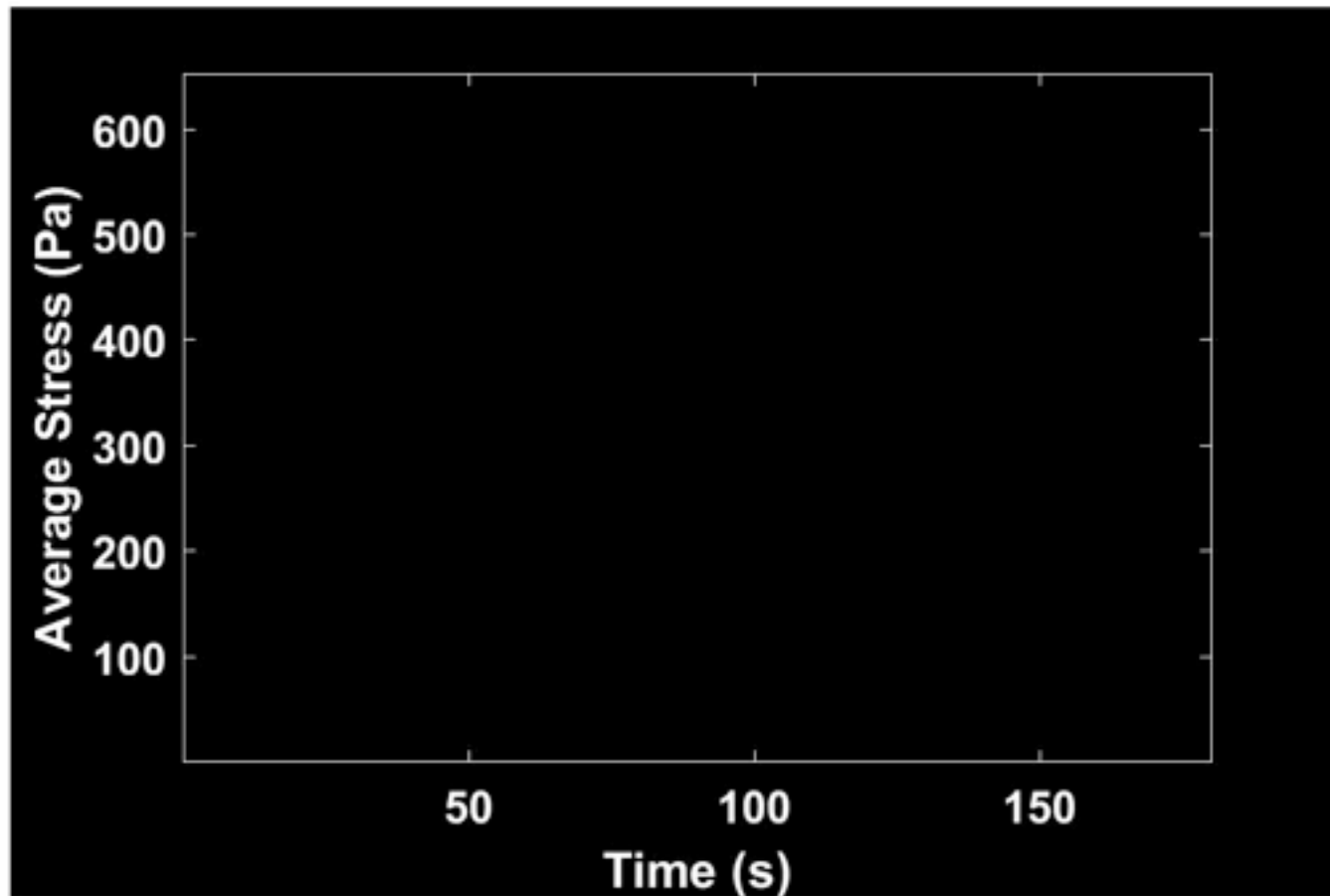


Applied Stress:  $\sigma = 100 \text{ Pa}$



# Boundary Stresses: $\phi = 56\%$

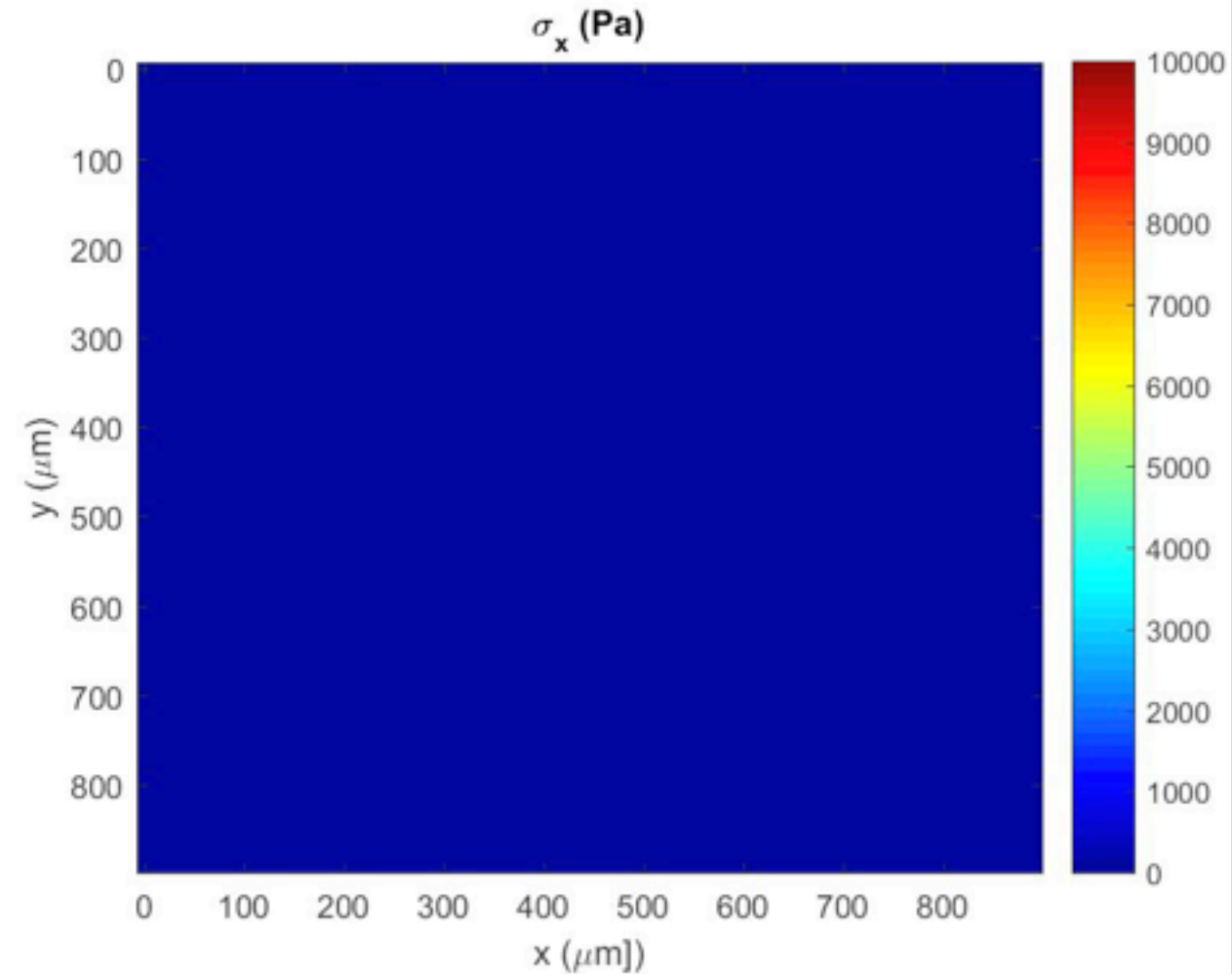
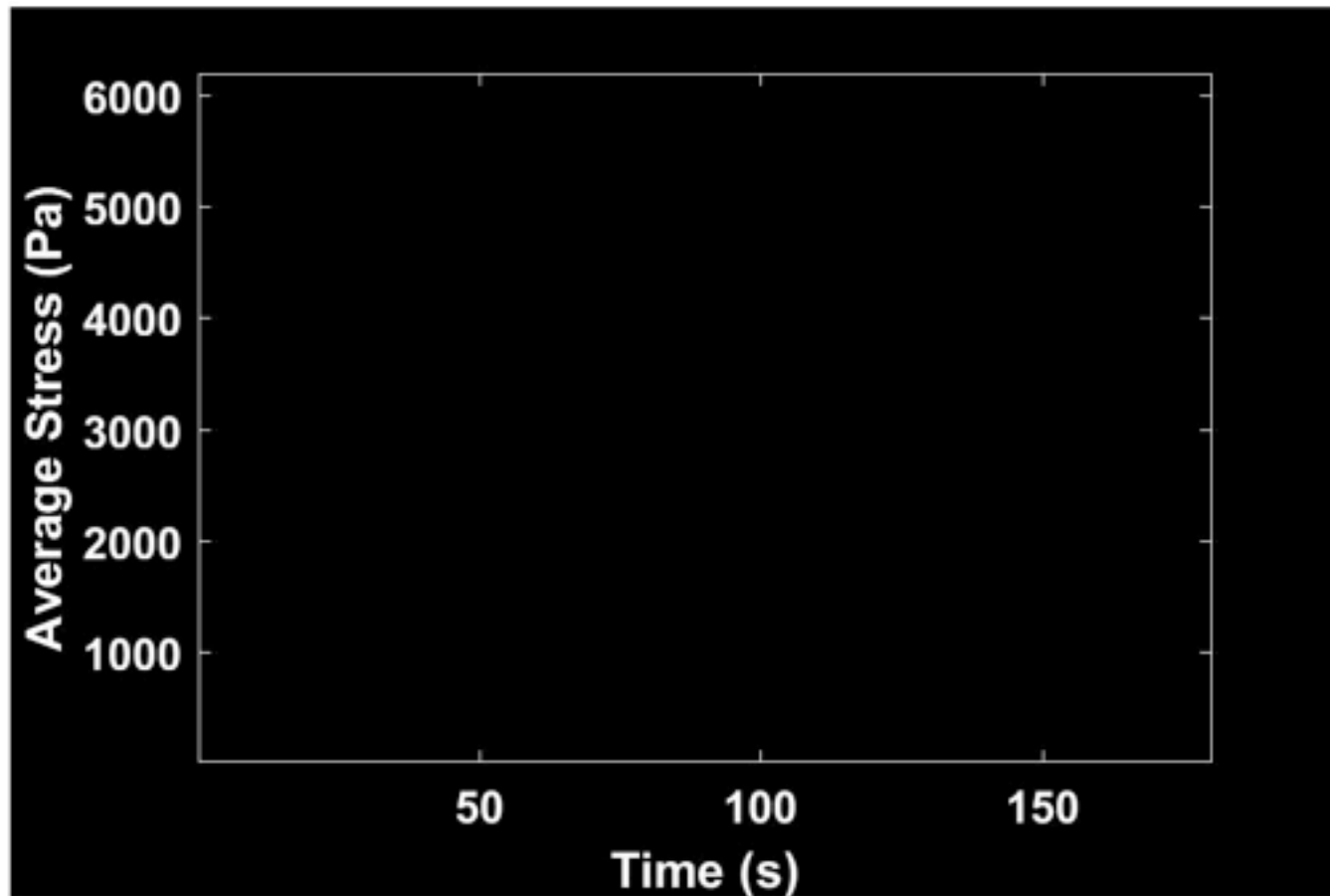
## Stress at the Interface



Applied Stress:  $\sigma = 100 \text{ Pa}$

# Boundary Stresses: $\phi = 56\%$

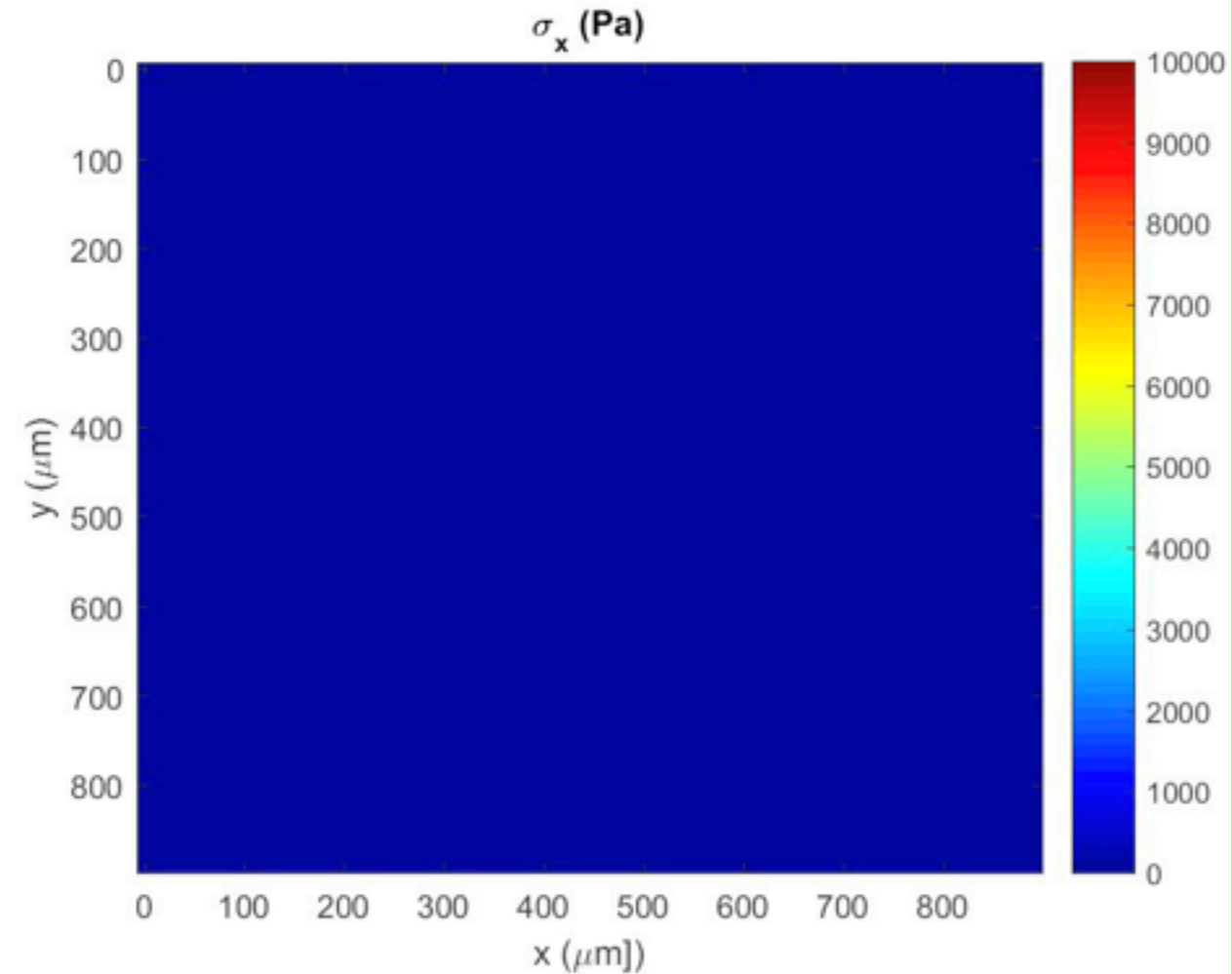
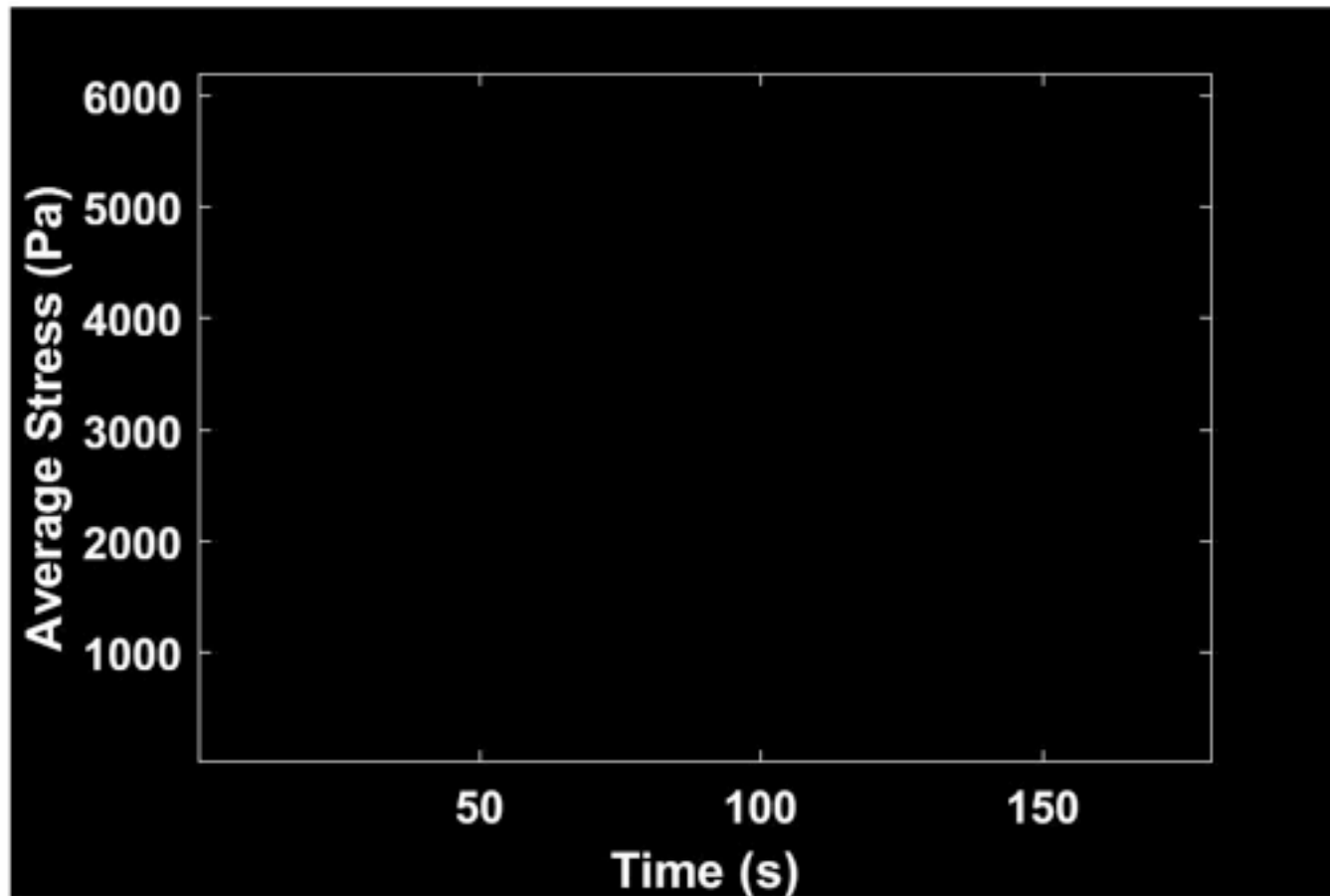
## Stress at the Interface



Applied Stress:  $\sigma = 1000$  Pa

# Boundary Stresses: $\phi = 56\%$

## Stress at the Interface



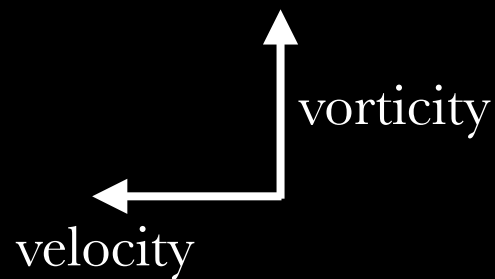
Applied Stress:  $\sigma = 1000$  Pa



# Boundary Stresses: $\phi = 56\%$

## Stress Fields

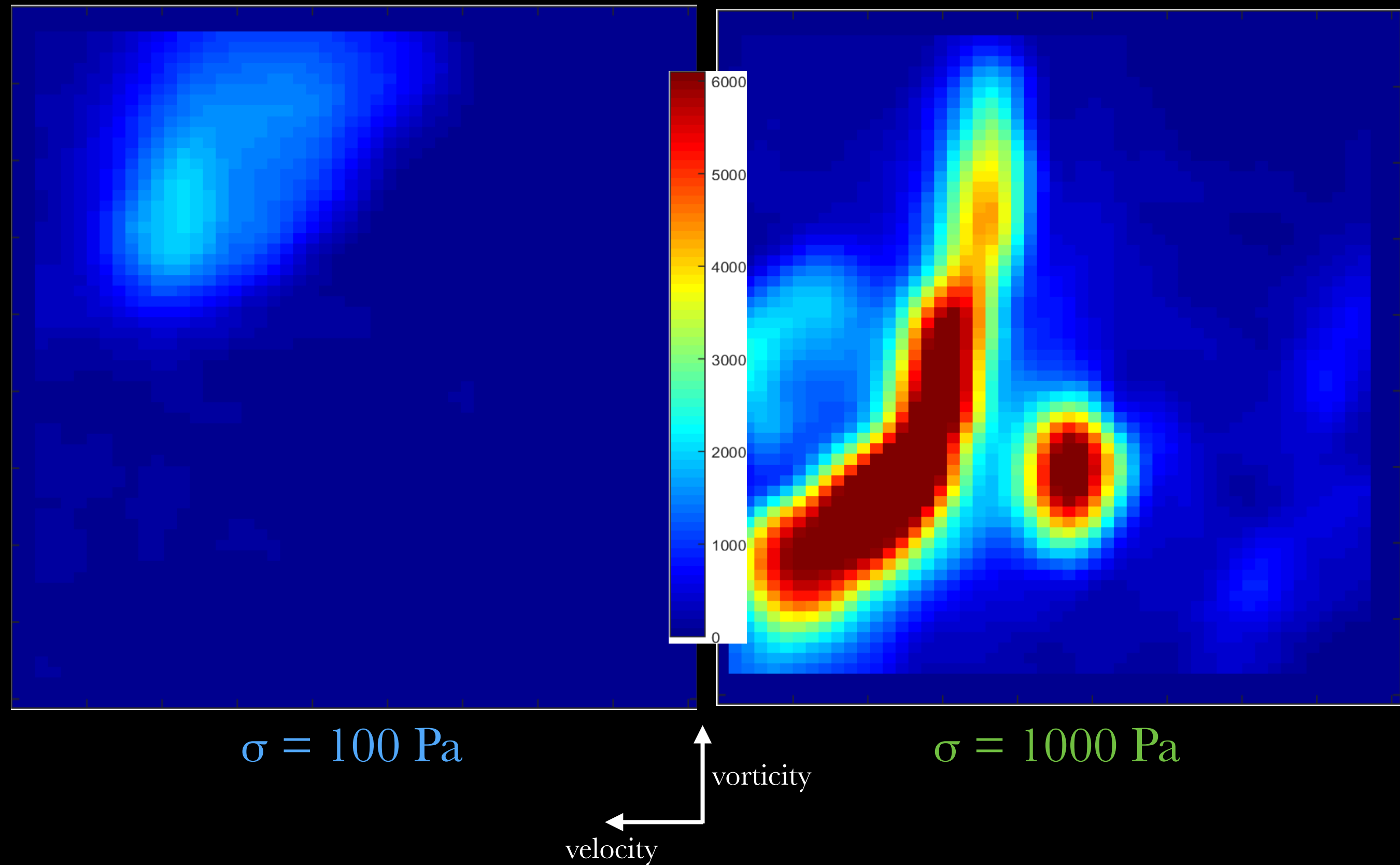
$$\sigma = 100 \text{ Pa}$$

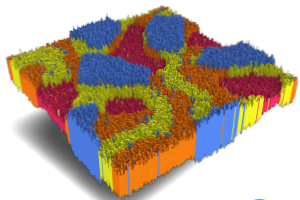


$$\sigma = 1000 \text{ Pa}$$

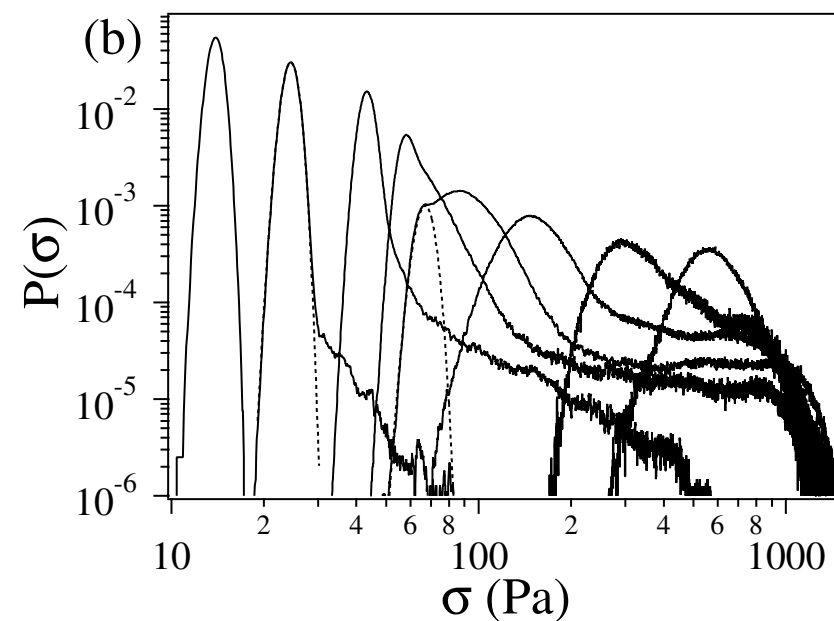
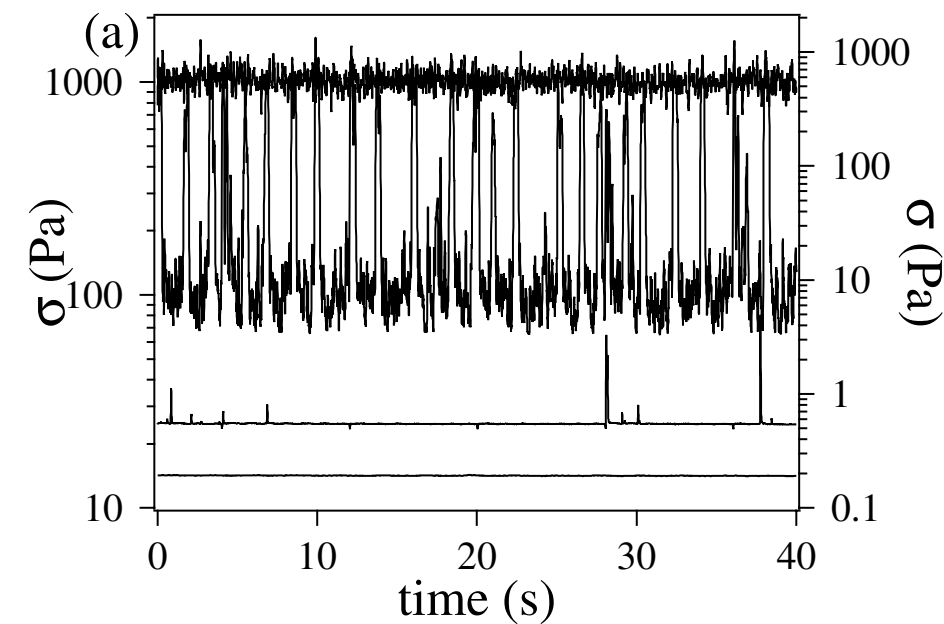
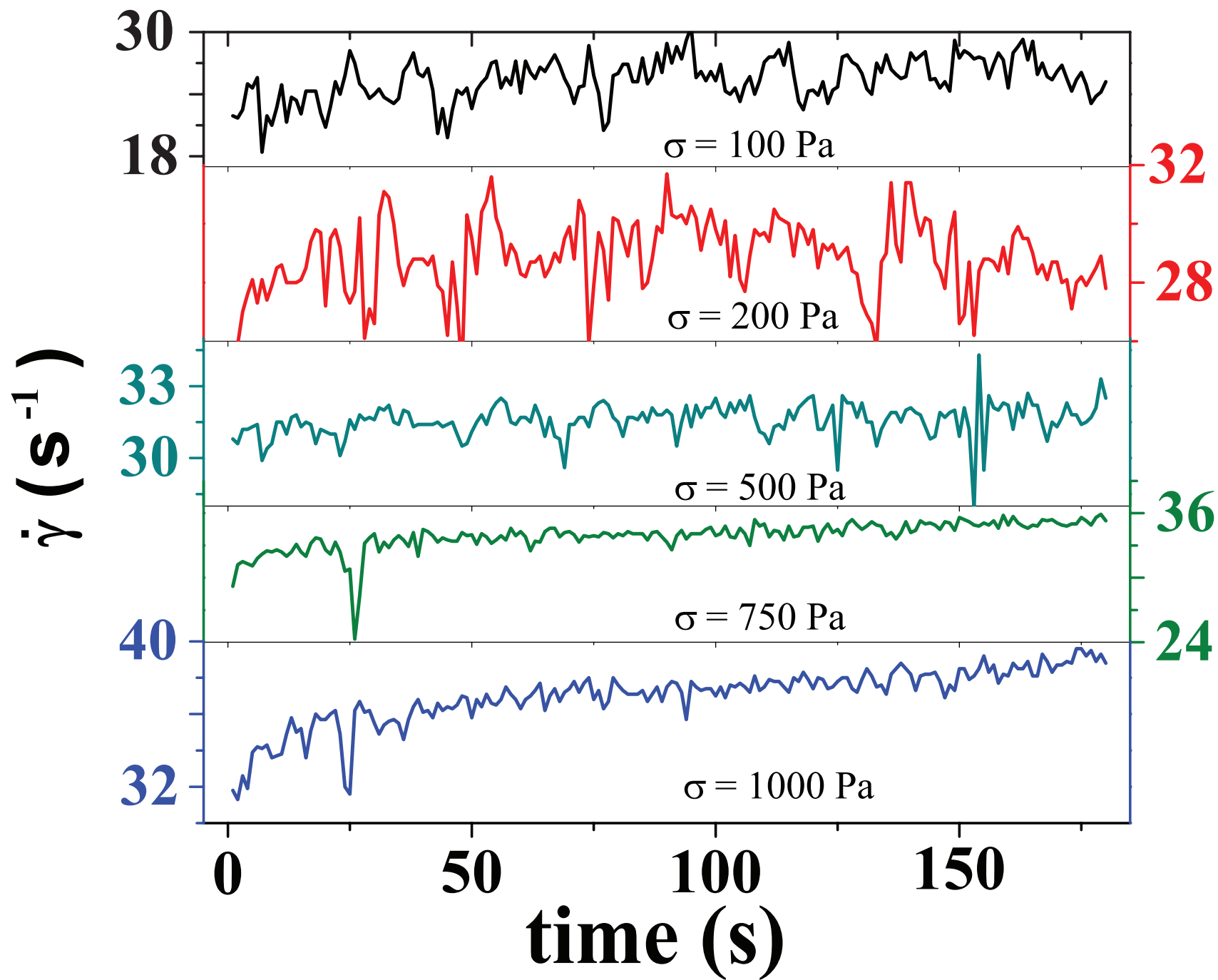
# Boundary Stresses: $\phi = 56\%$

## Stress Fields



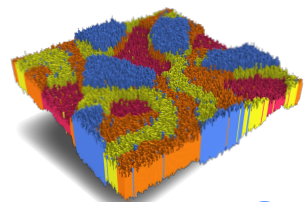


# Time Resolved Rheology



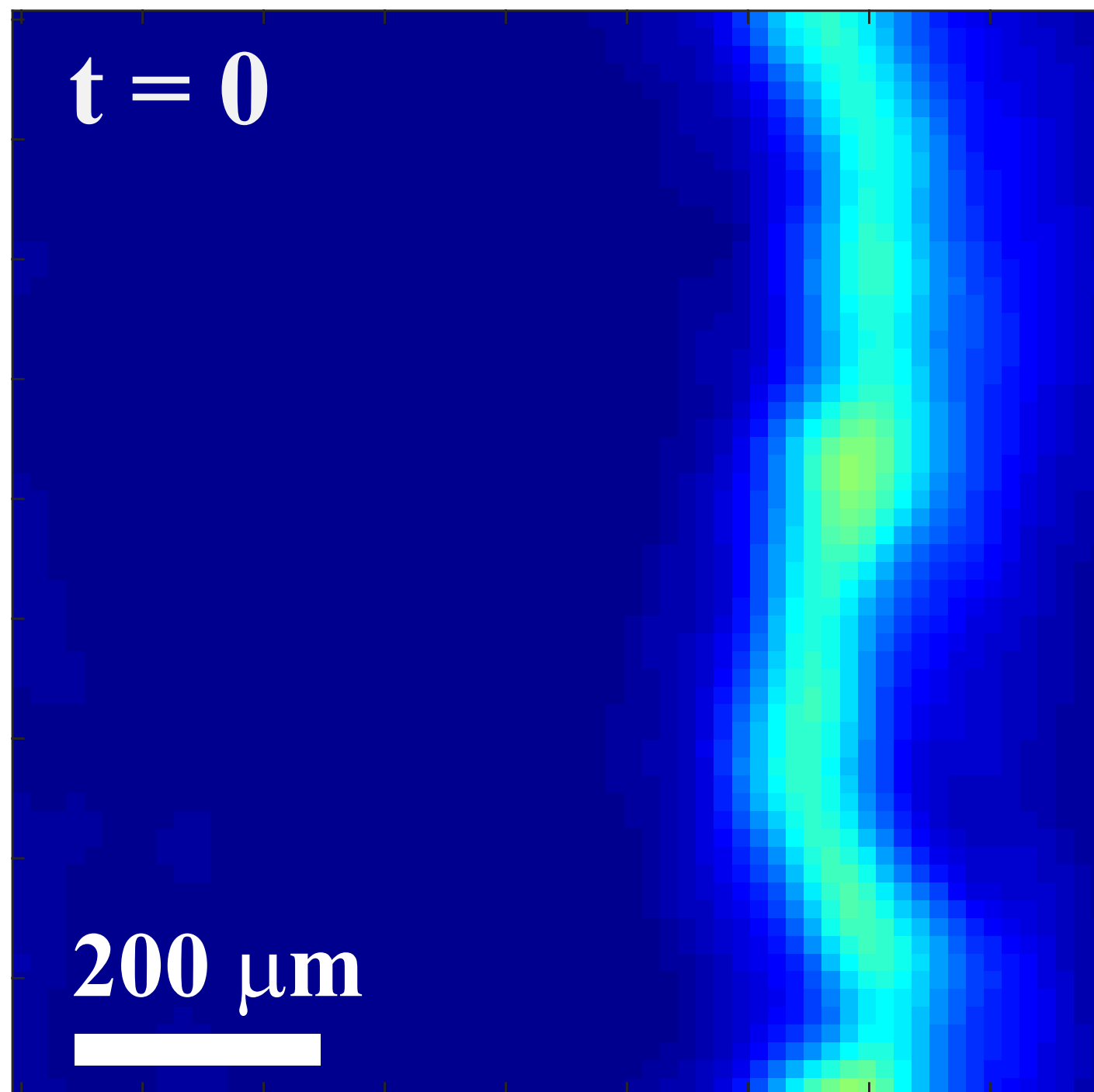
Lootens *et al.*, PRL 2003

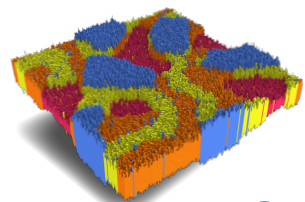




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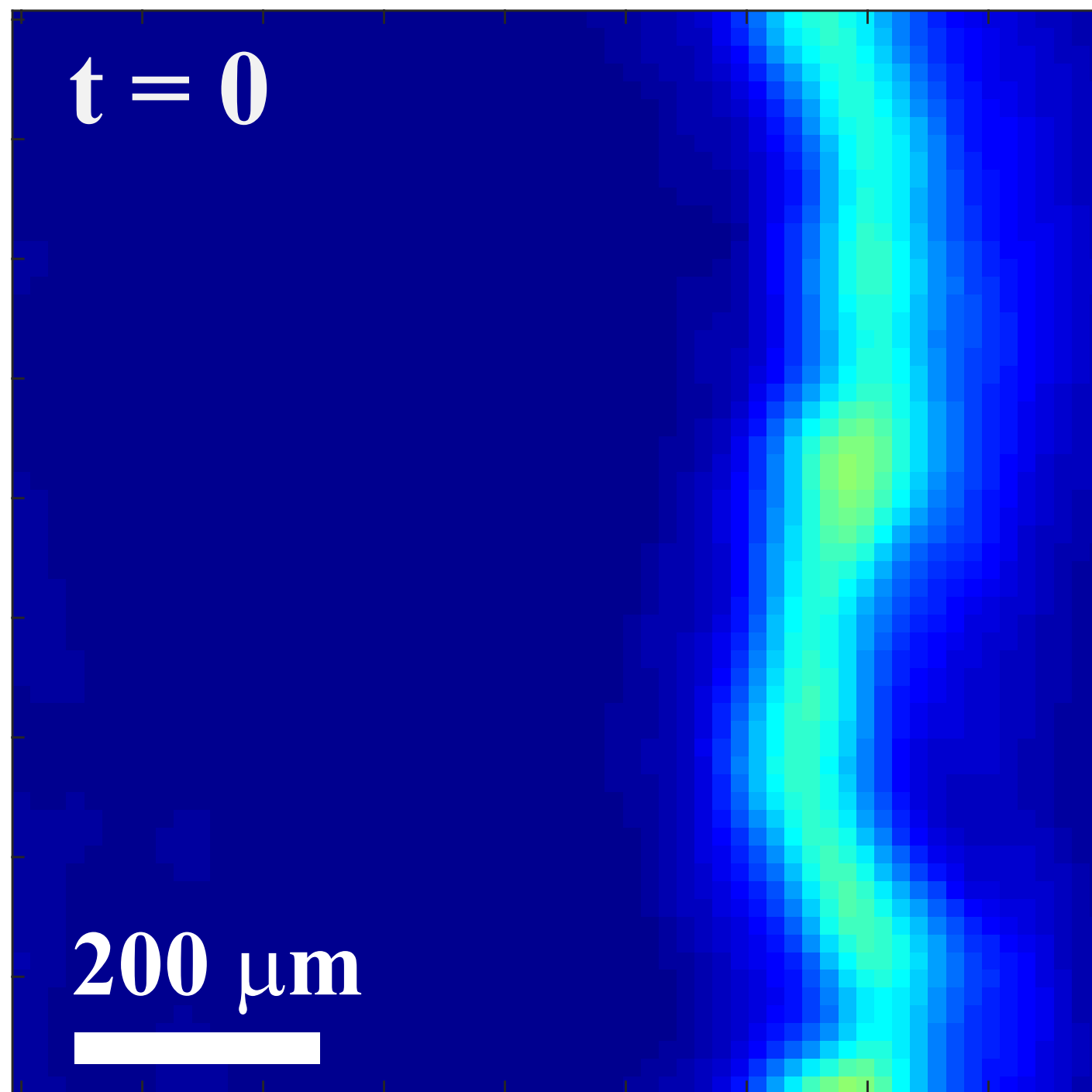
# Tracking the Dynamics





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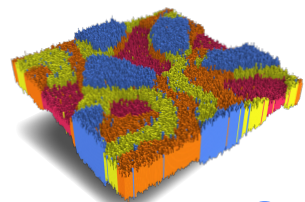
# Tracking the Dynamics



**t = 0**

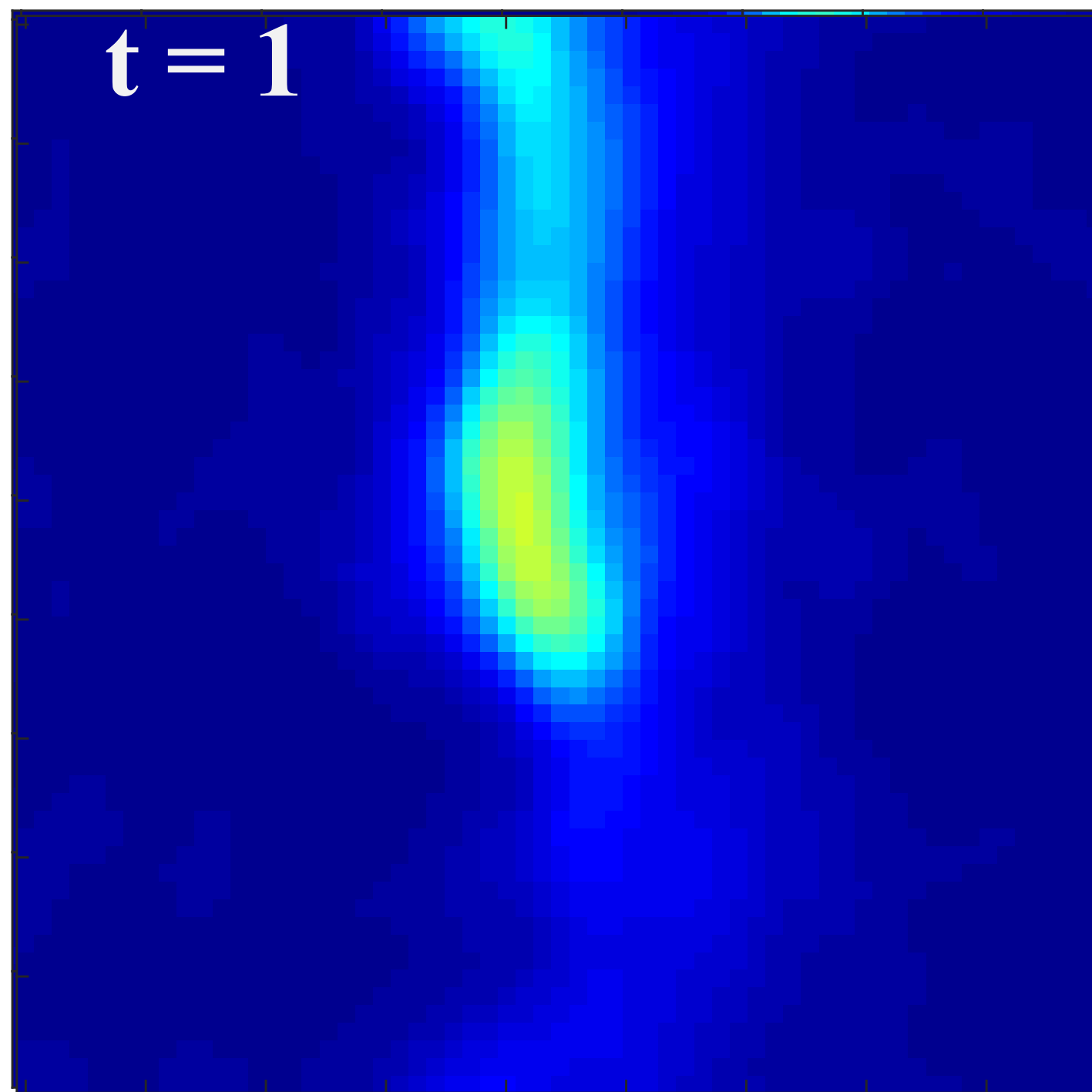
**200  $\mu\text{m}$**

velocity  
vorticity



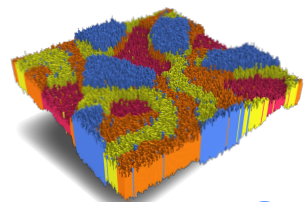
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# Tracking the Dynamics



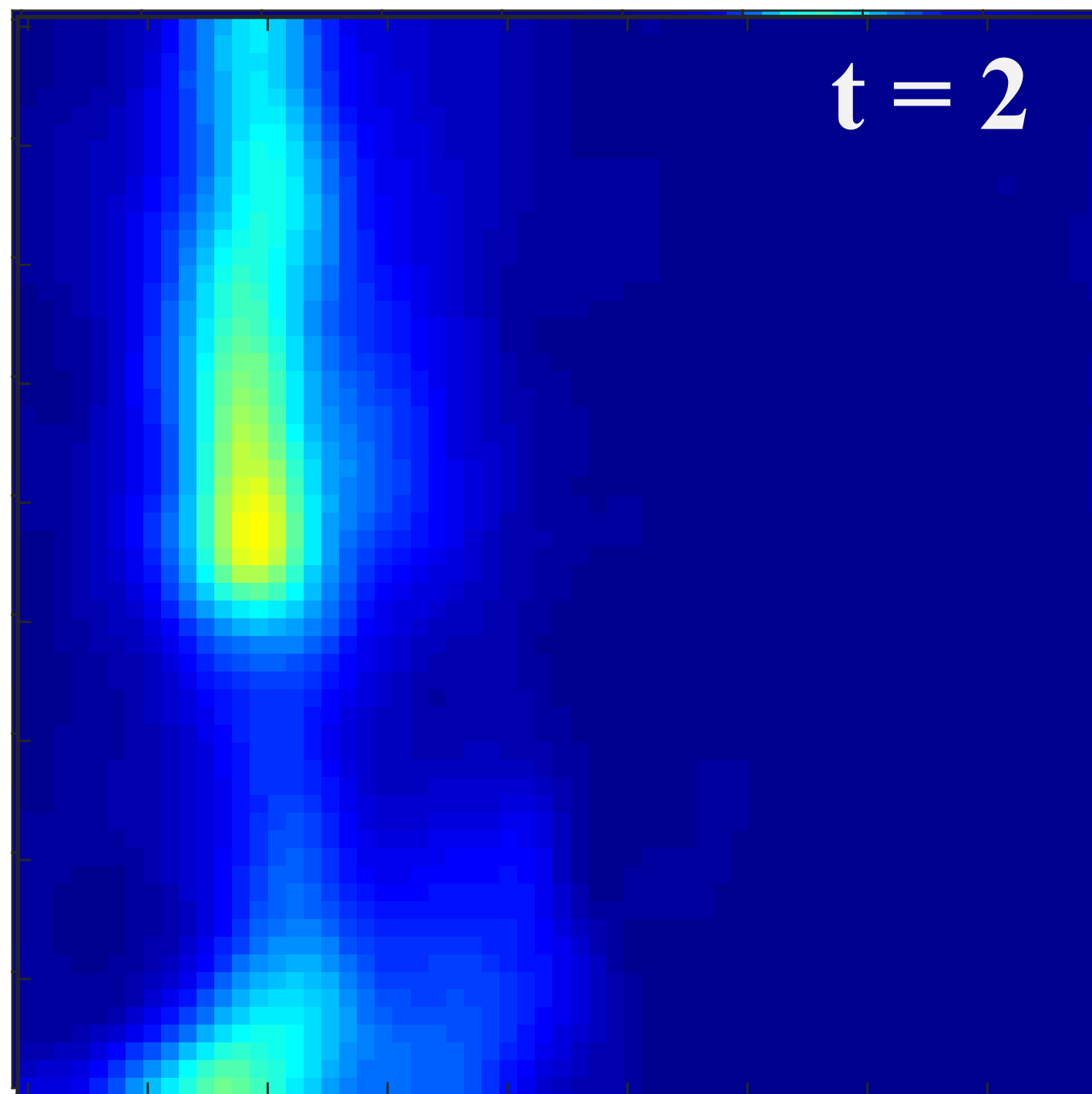
velocity  
vorticity



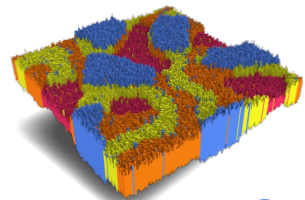


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# Tracking the Dynamics



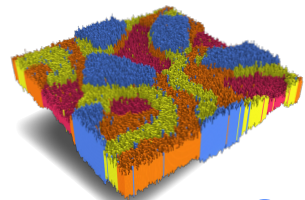
velocity  
vorticity



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# Tracking the Dynamics



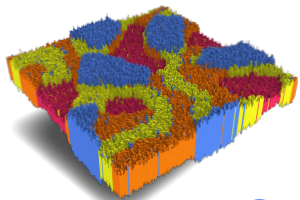


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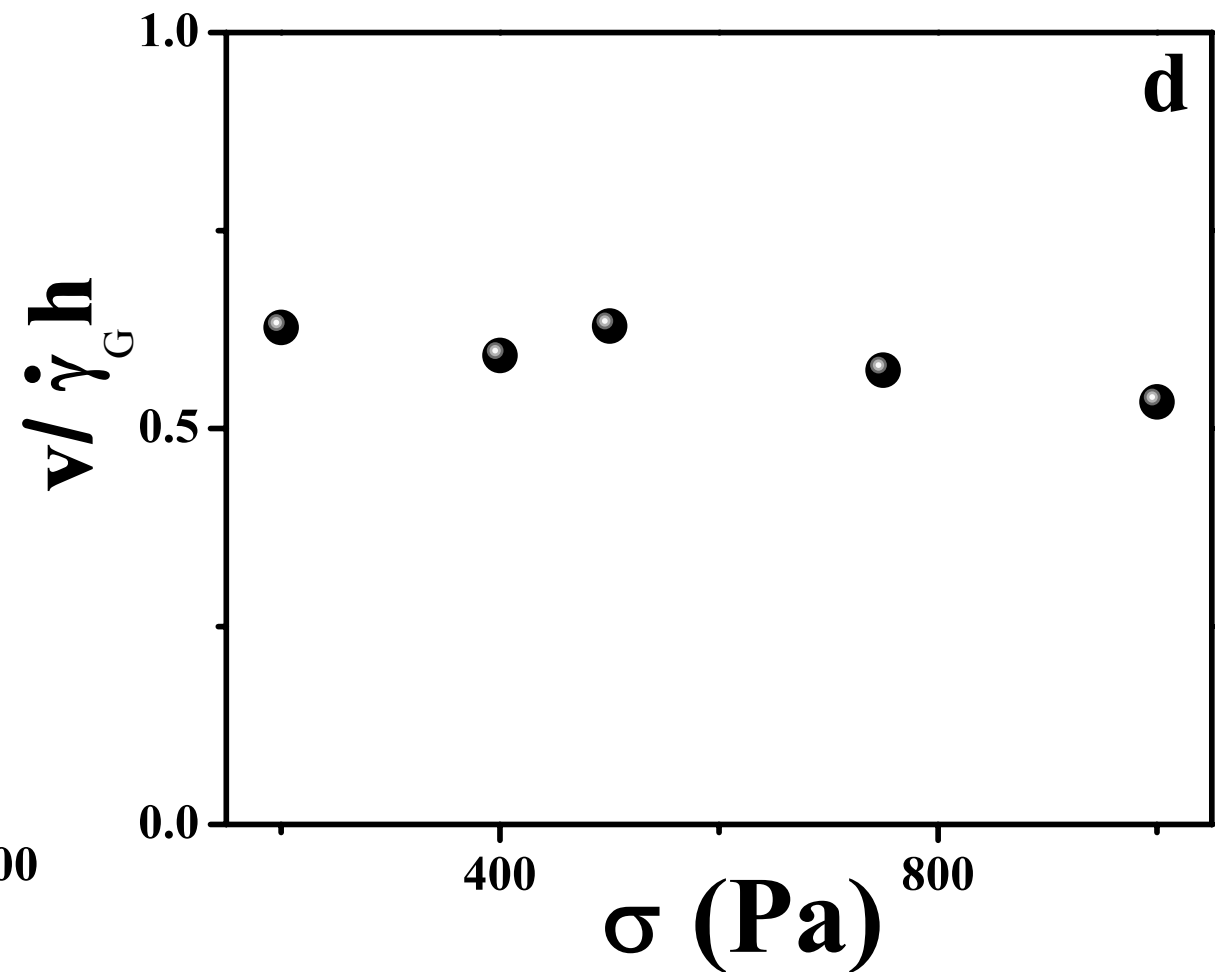
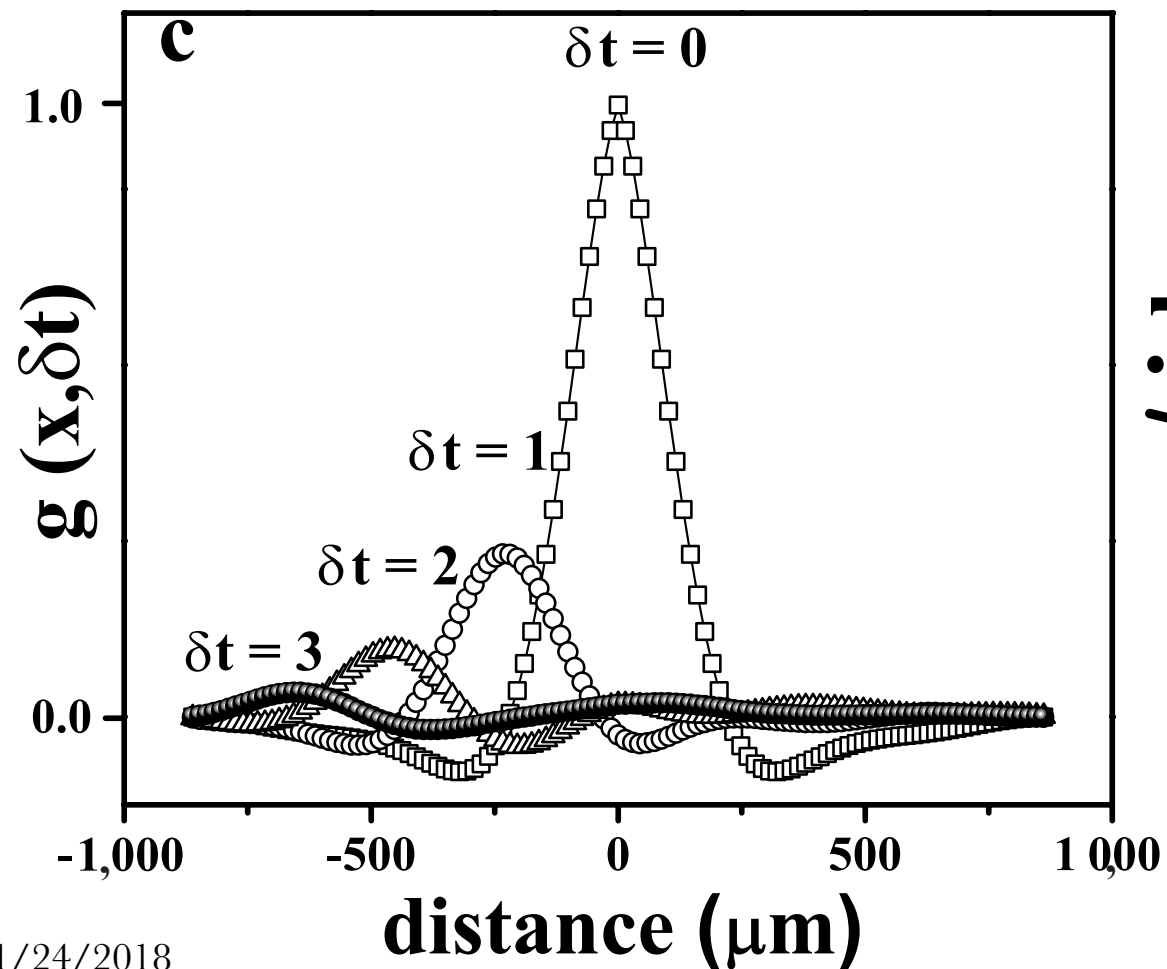
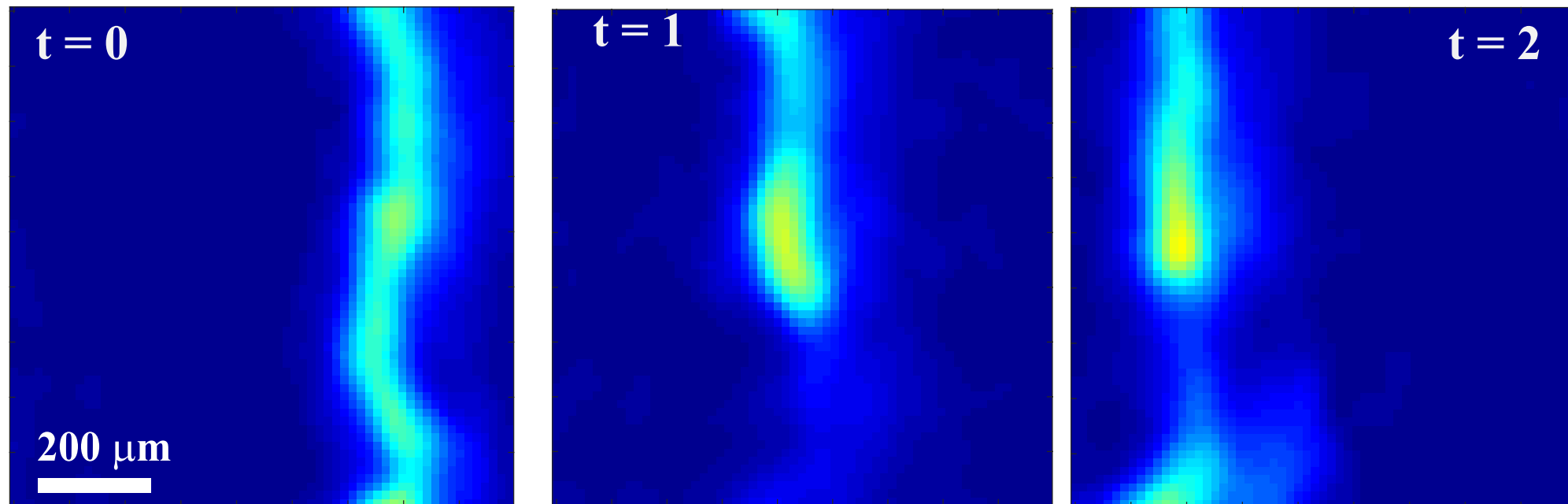
# Tracking the Dynamics





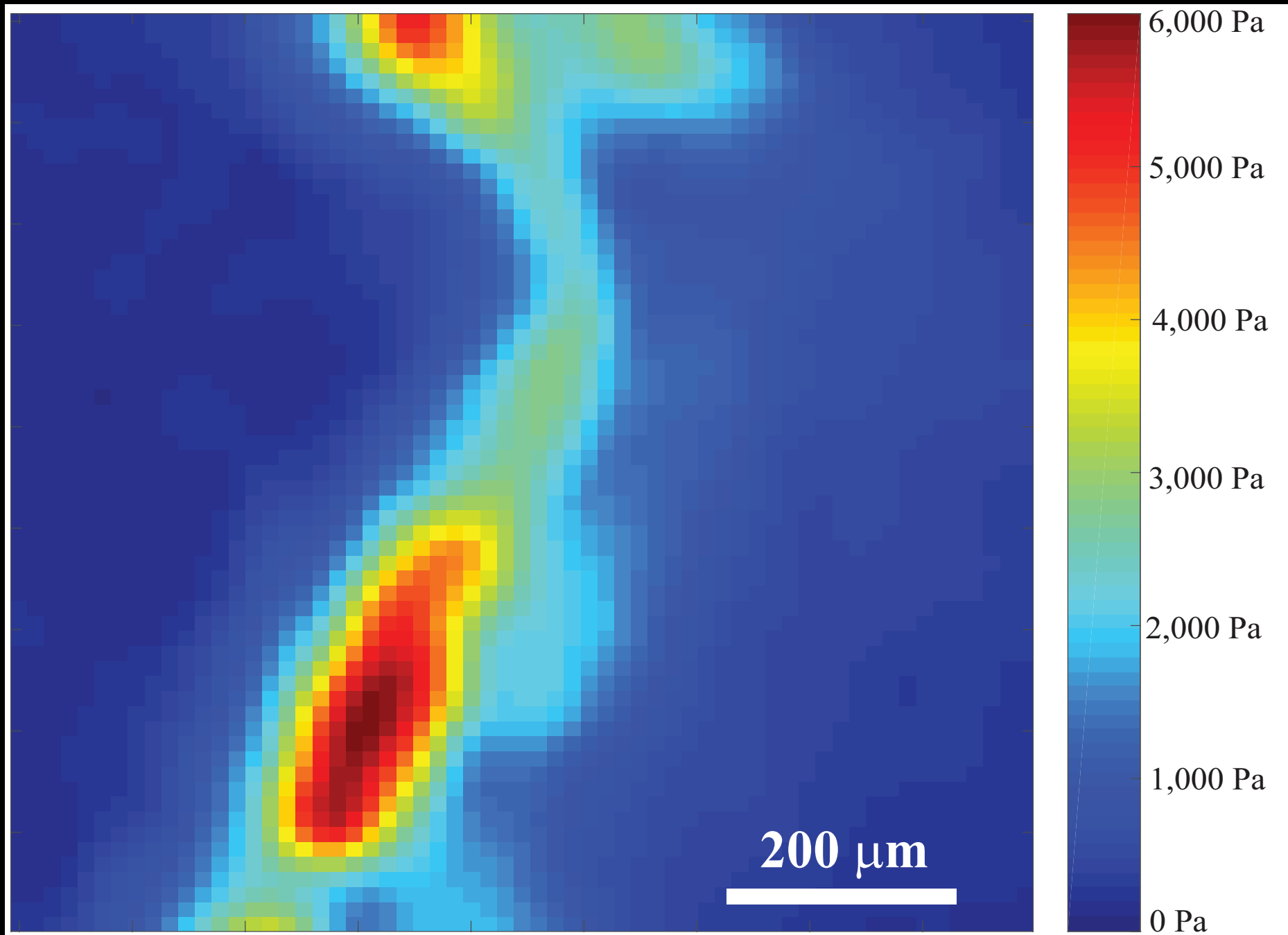


# Tracking the Dynamics



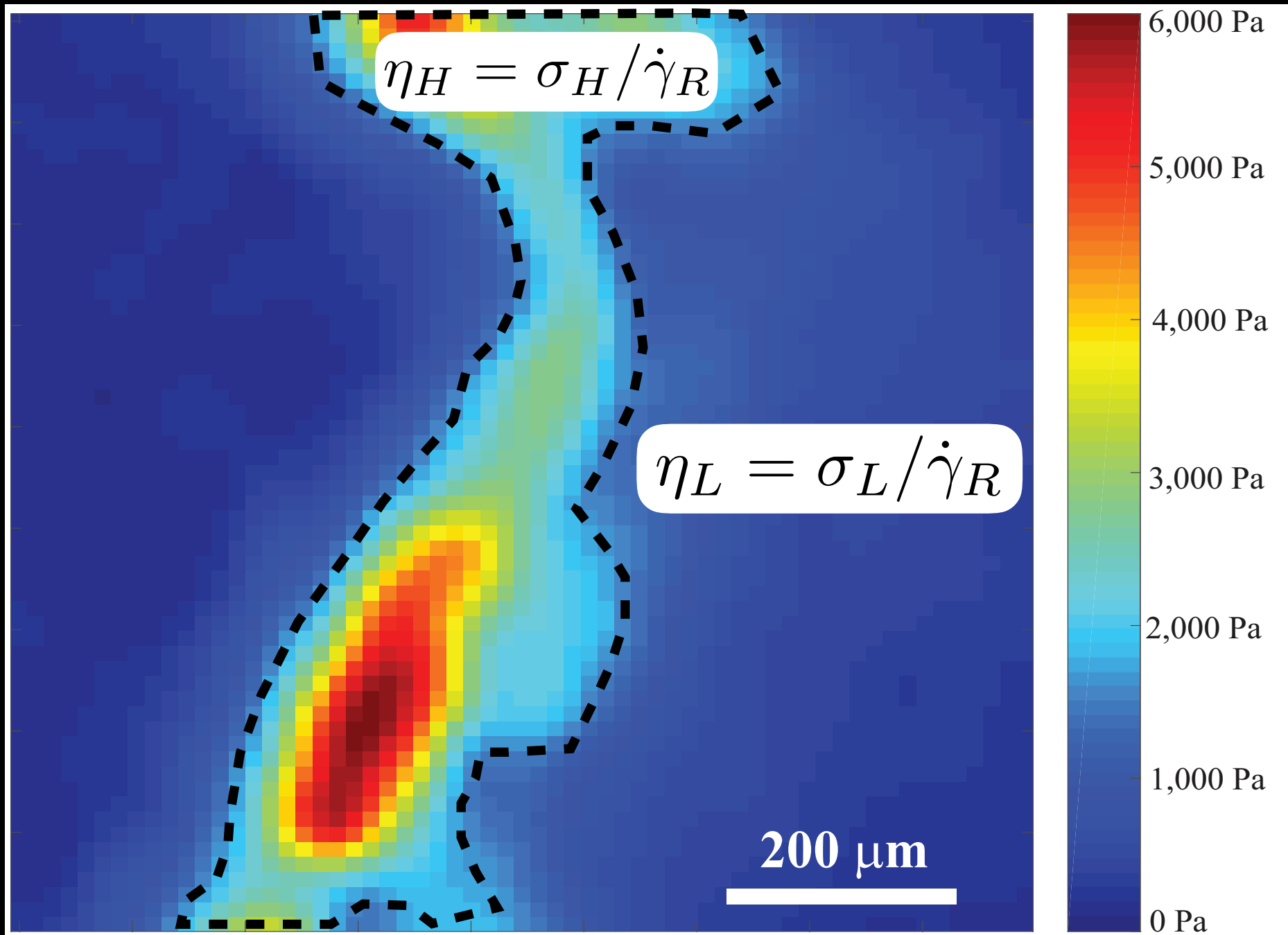
What Are These High Stress Regions?

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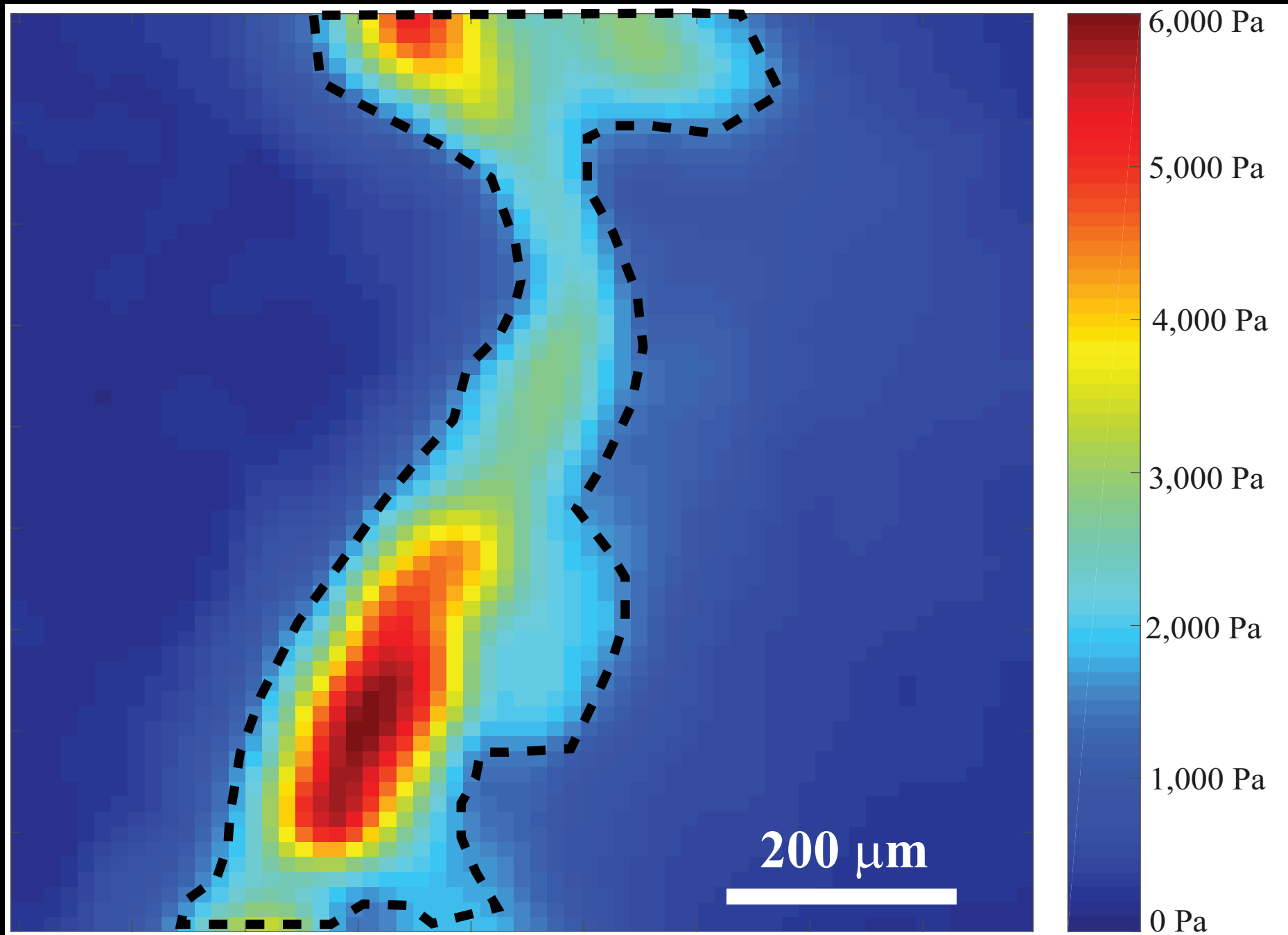




# What Are These High Stress Regions?



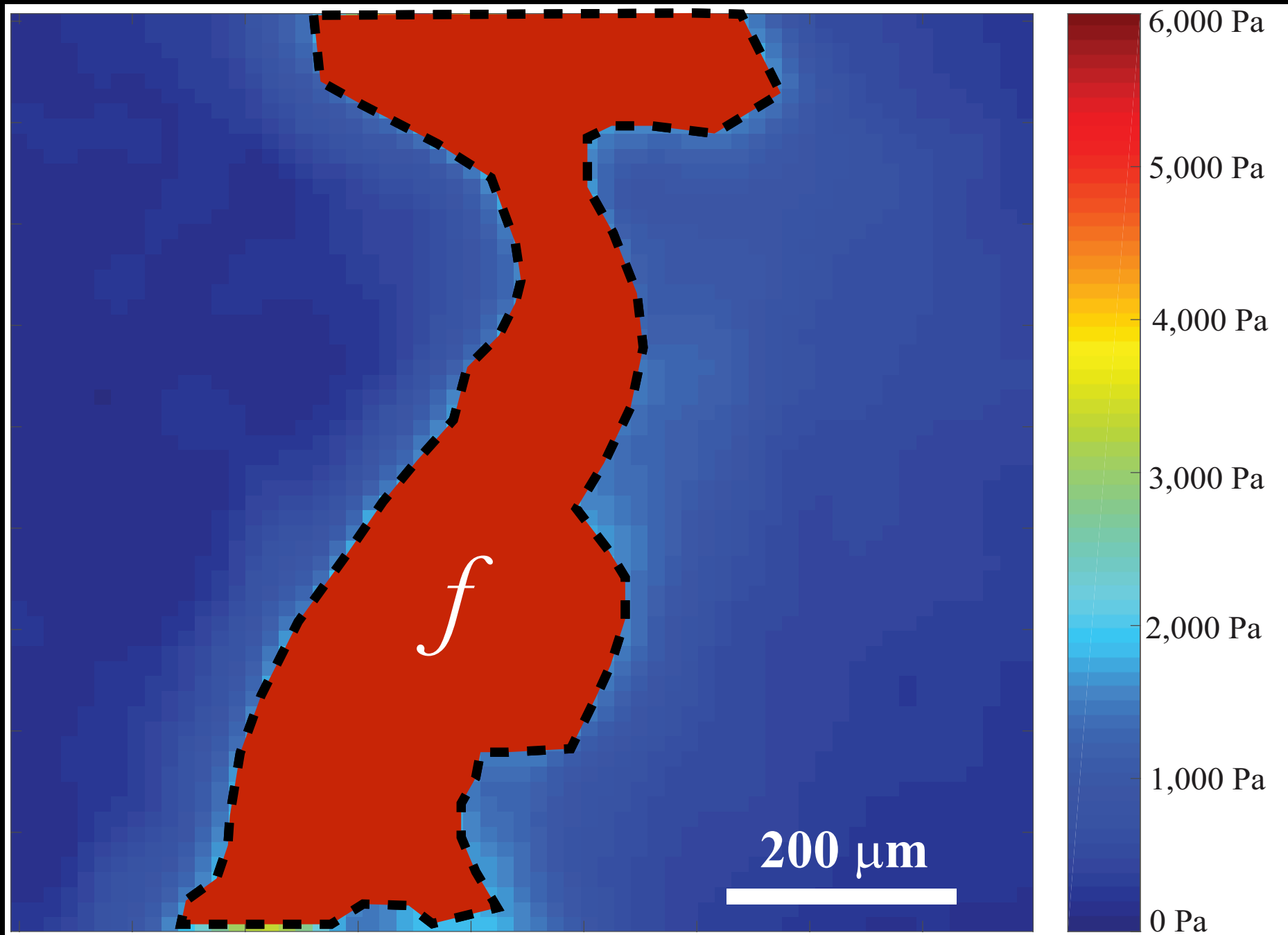
# What Are These High Stress Regions?



$$\eta_H = \sigma_H / \dot{\gamma}_R$$

$$\eta_L = \sigma_L / \dot{\gamma}_R$$

# What Are These High Stress Regions?

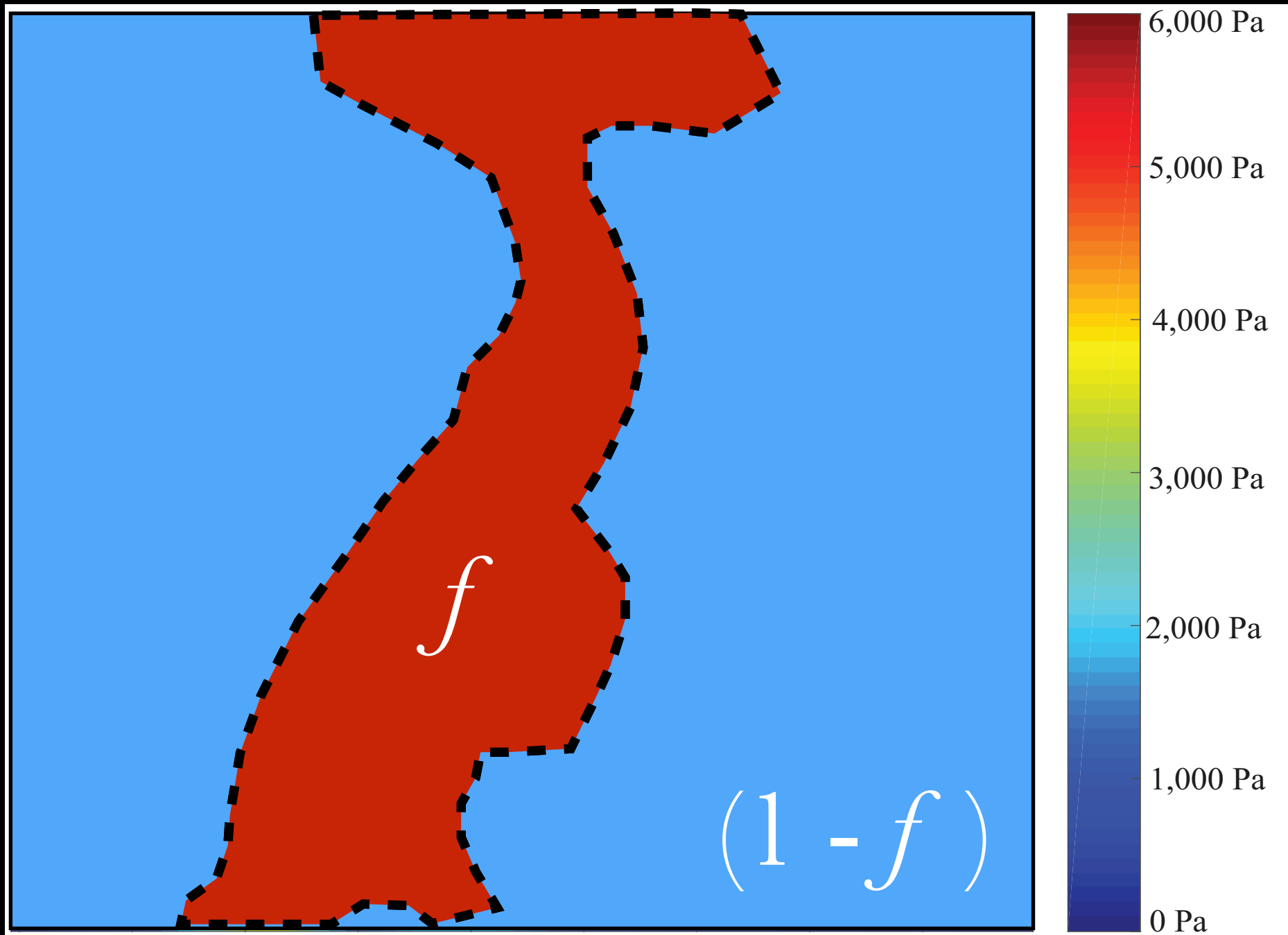


$$\eta_H = \sigma_H / \dot{\gamma}_R$$

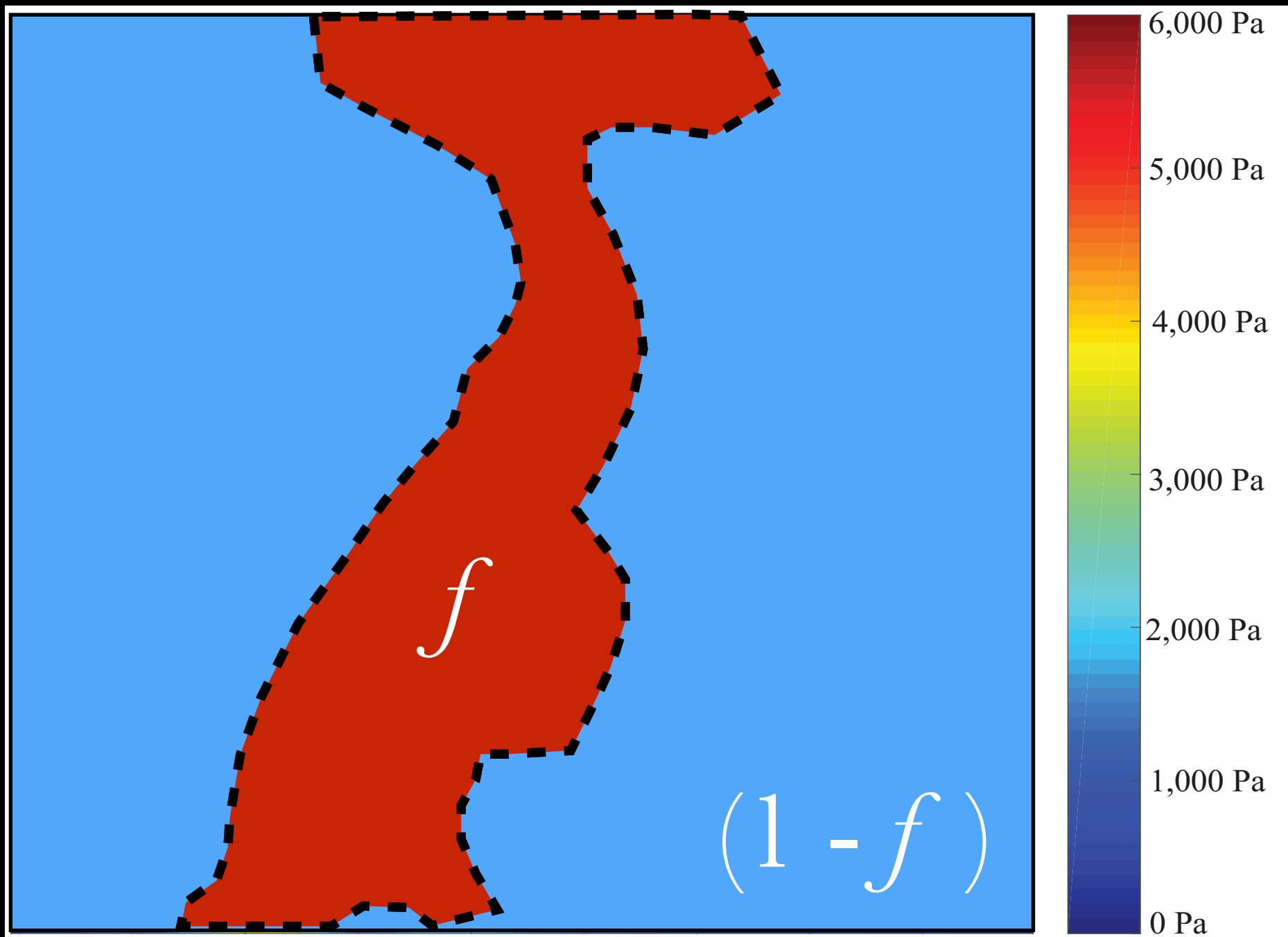
$$\eta_L = \sigma_L / \dot{\gamma}_R$$



# What Are These High Stress Regions?

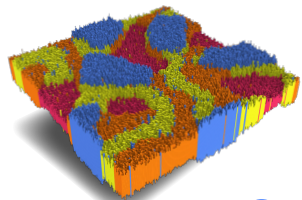


# What Are These High Stress Regions?

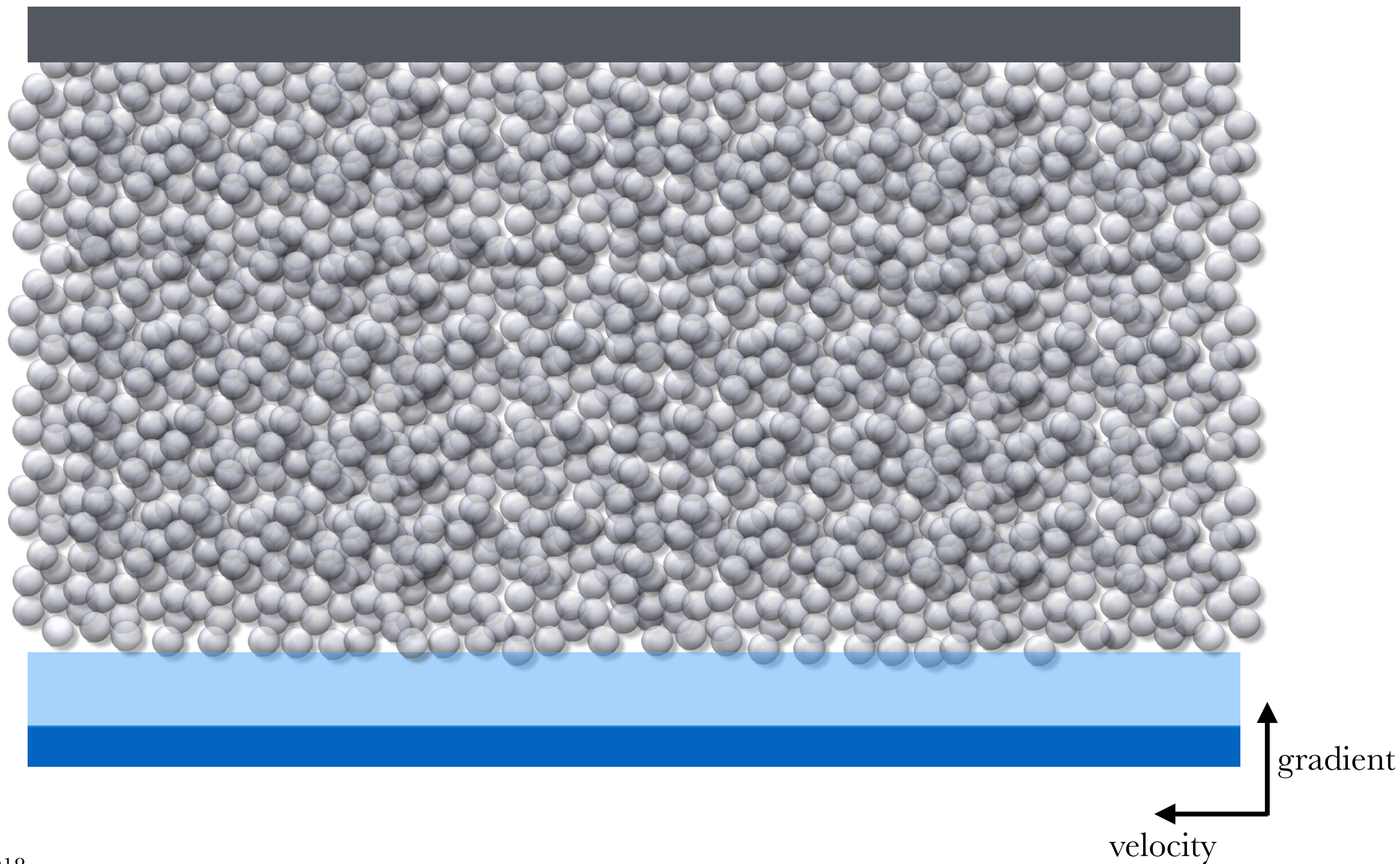


$$\eta_A = (1 - f)\eta_L + f\eta_H$$

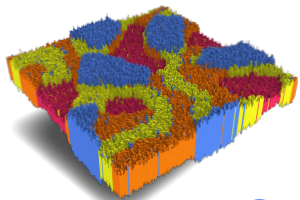
$f$  — area fraction of high stress



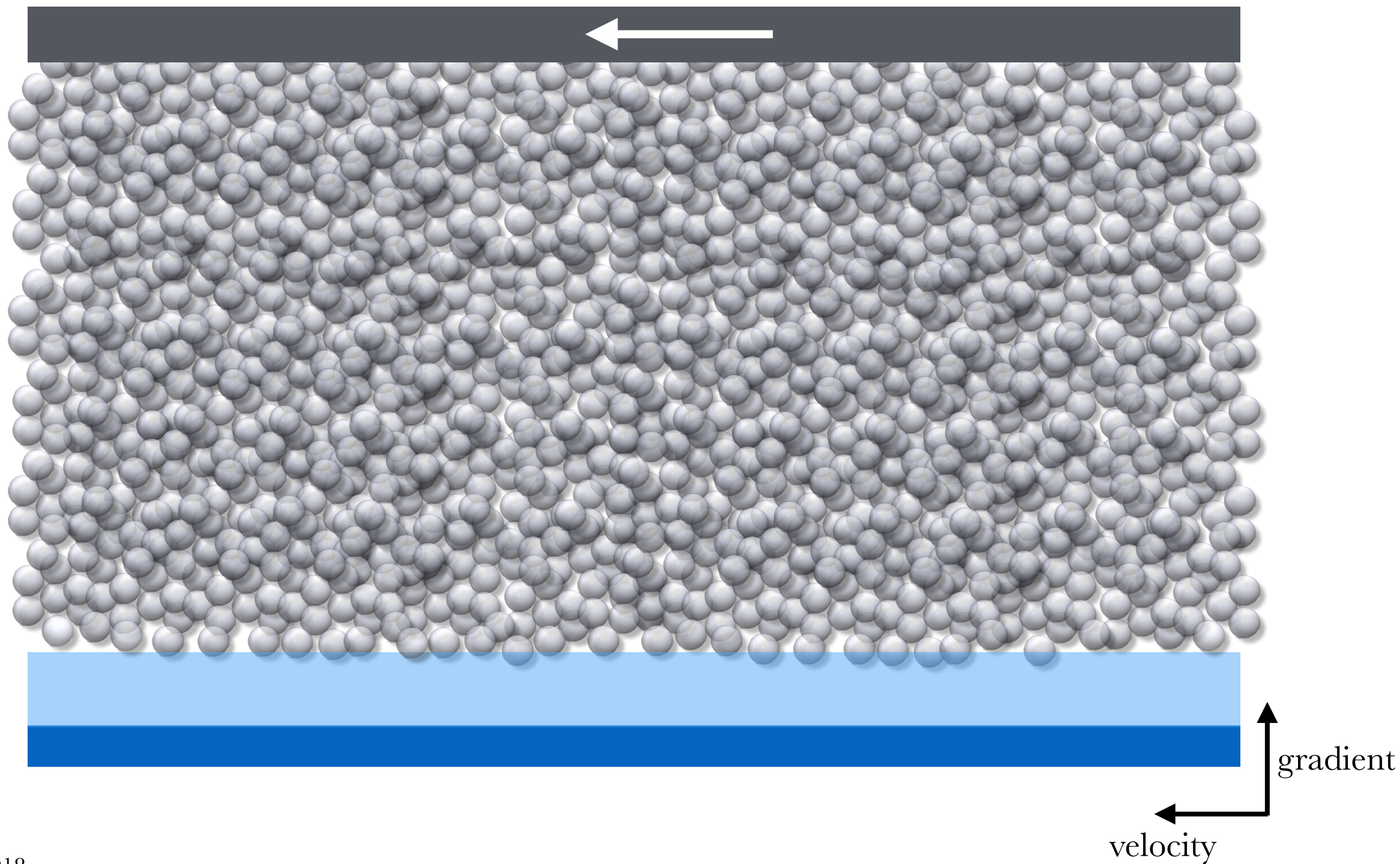
# Our Simple Picture



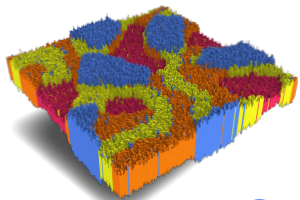




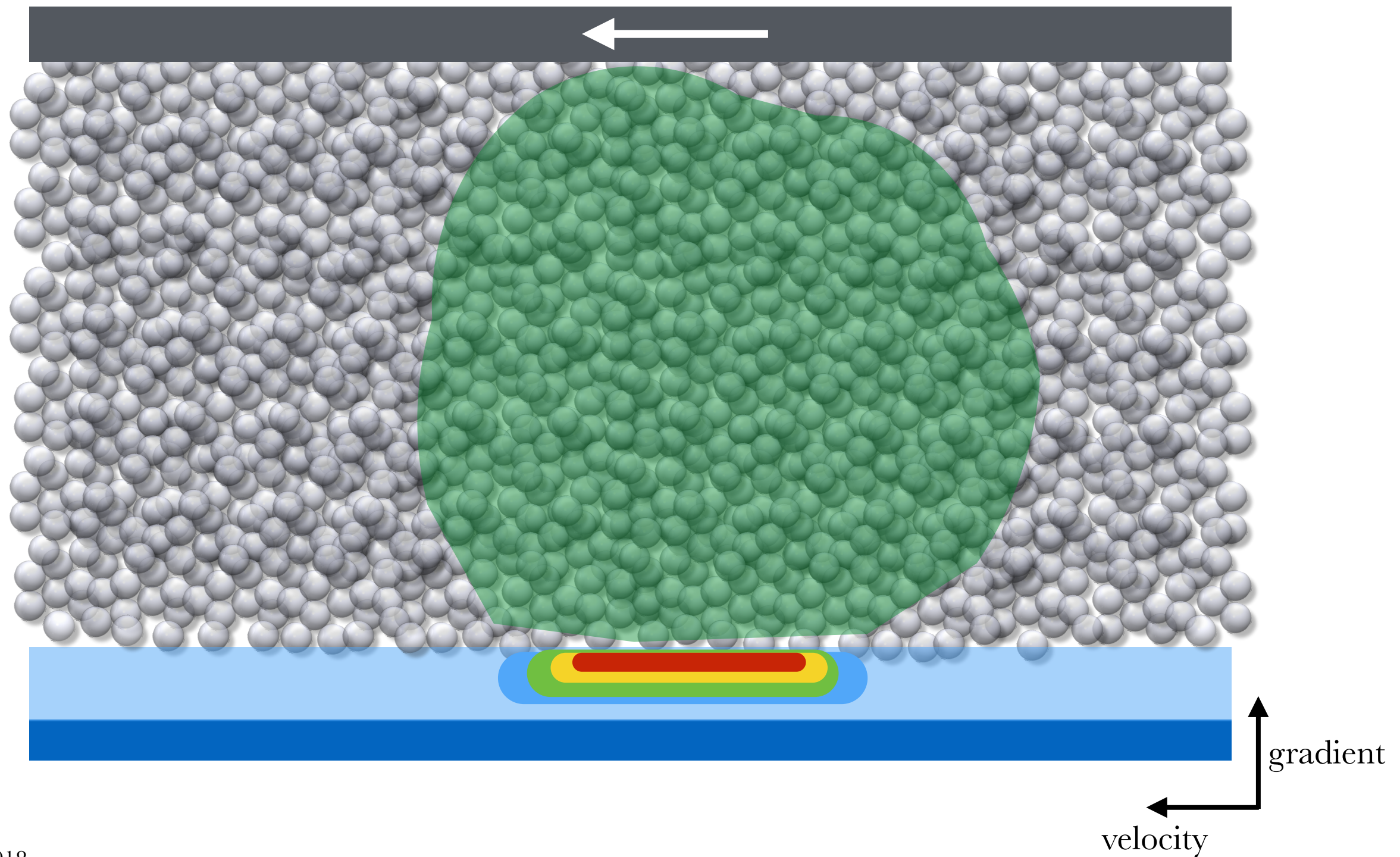
# Our Simple Picture



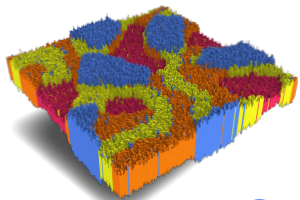




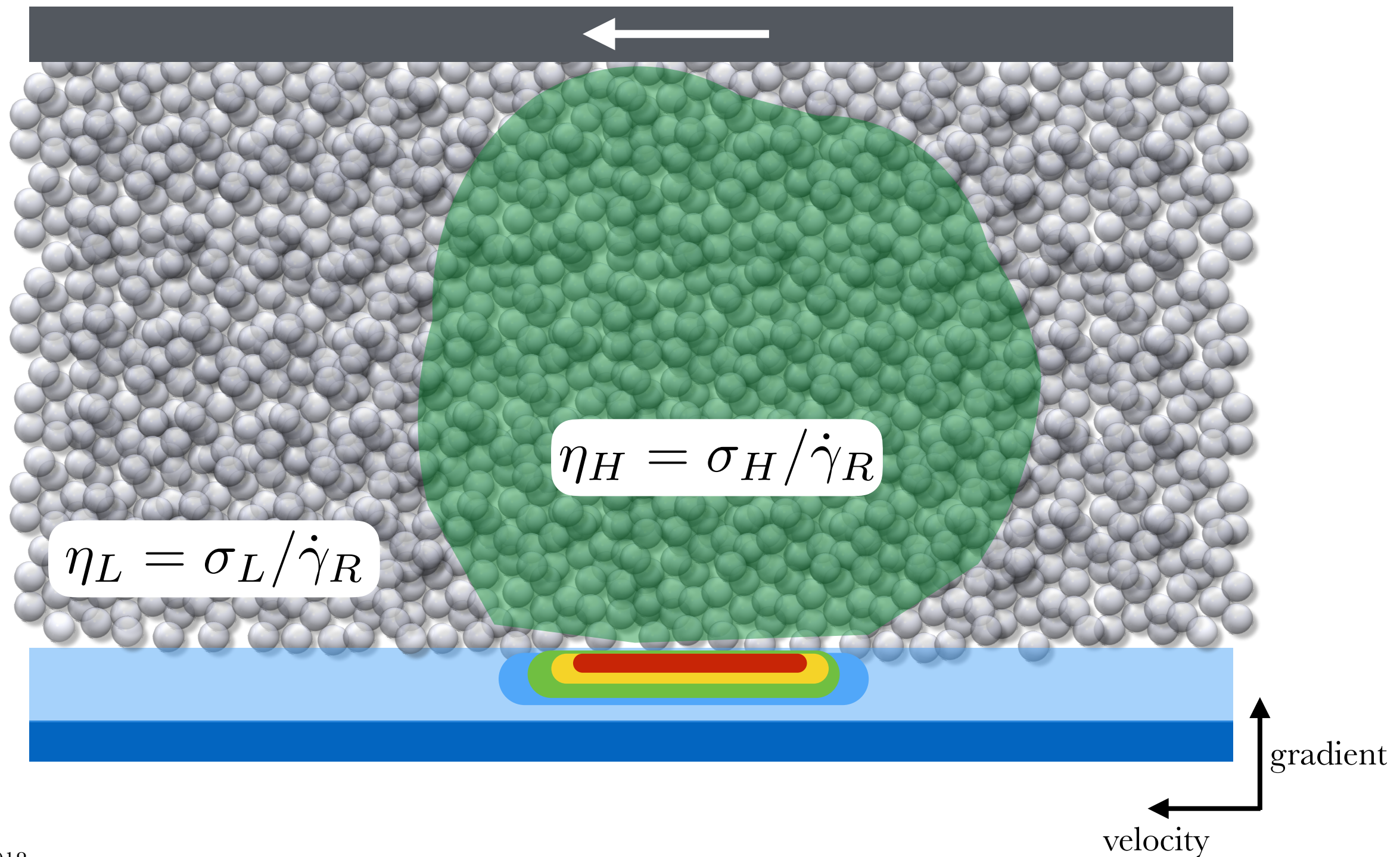
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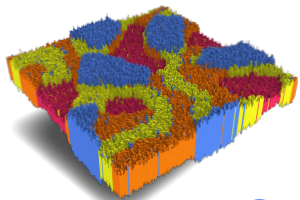




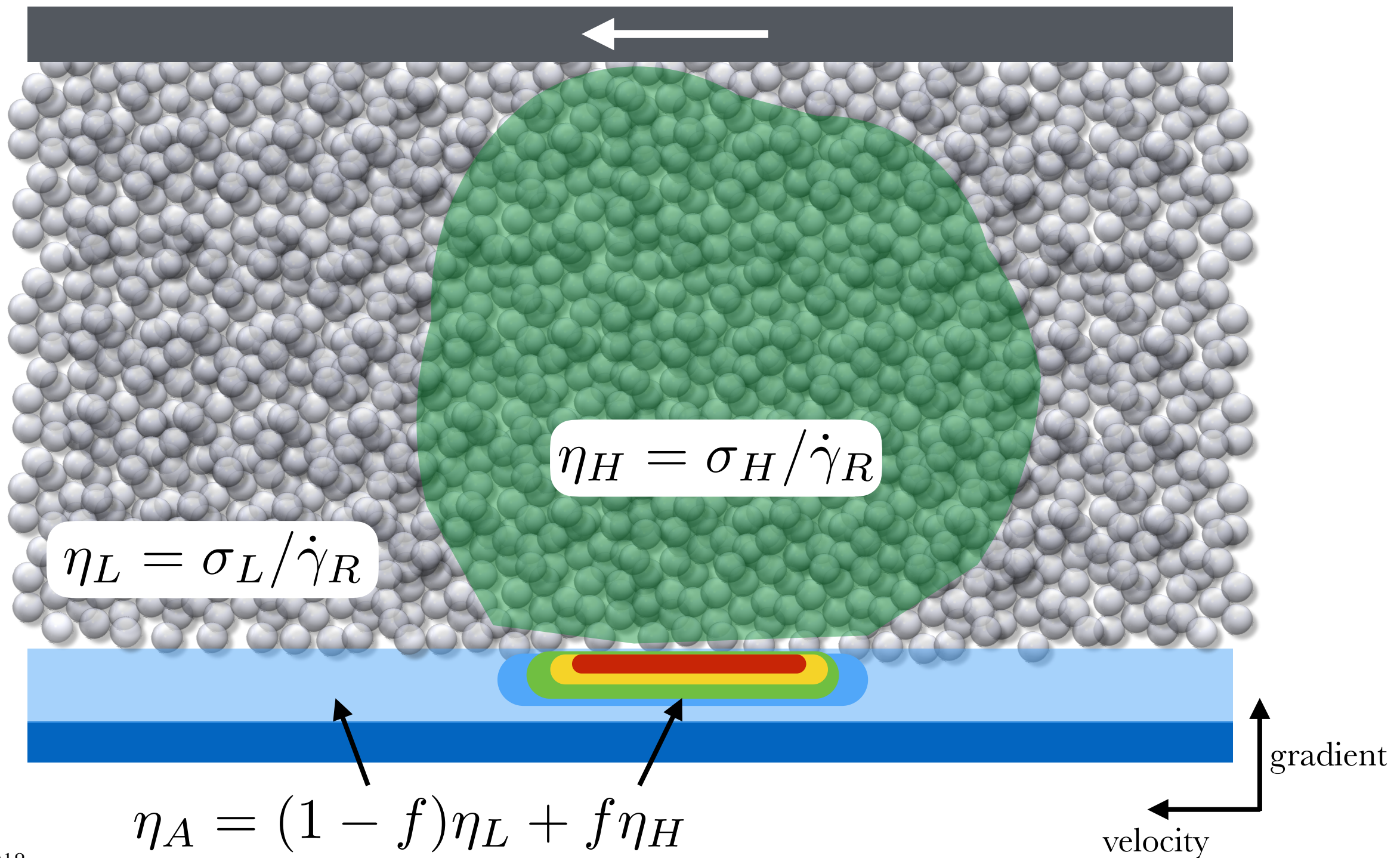
# Our Simple Picture



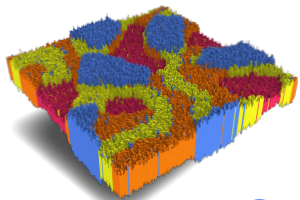




# Our Simple Picture

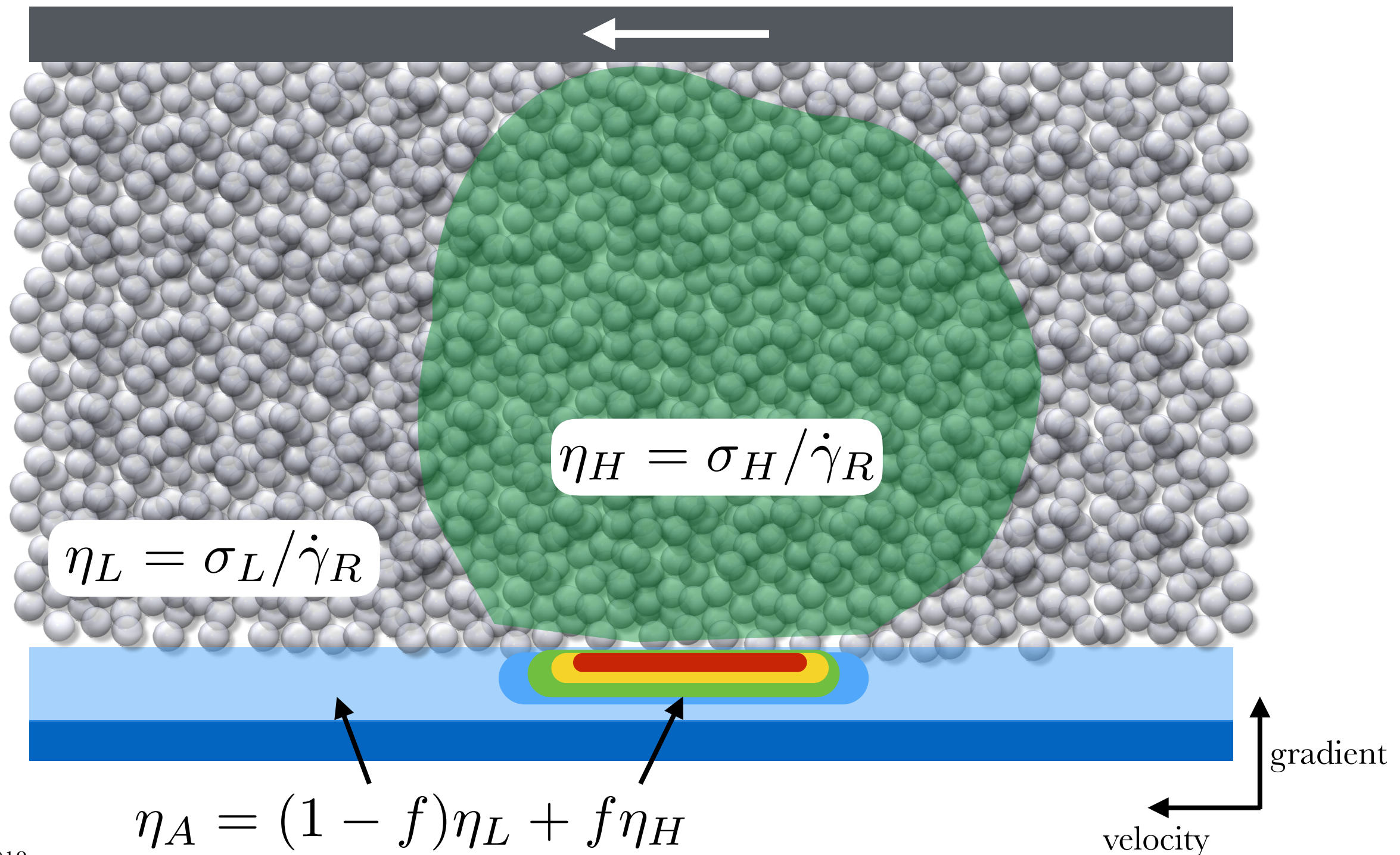


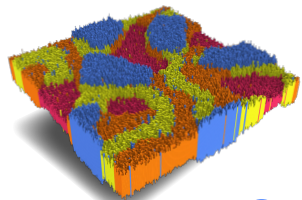




# Our Simple Picture

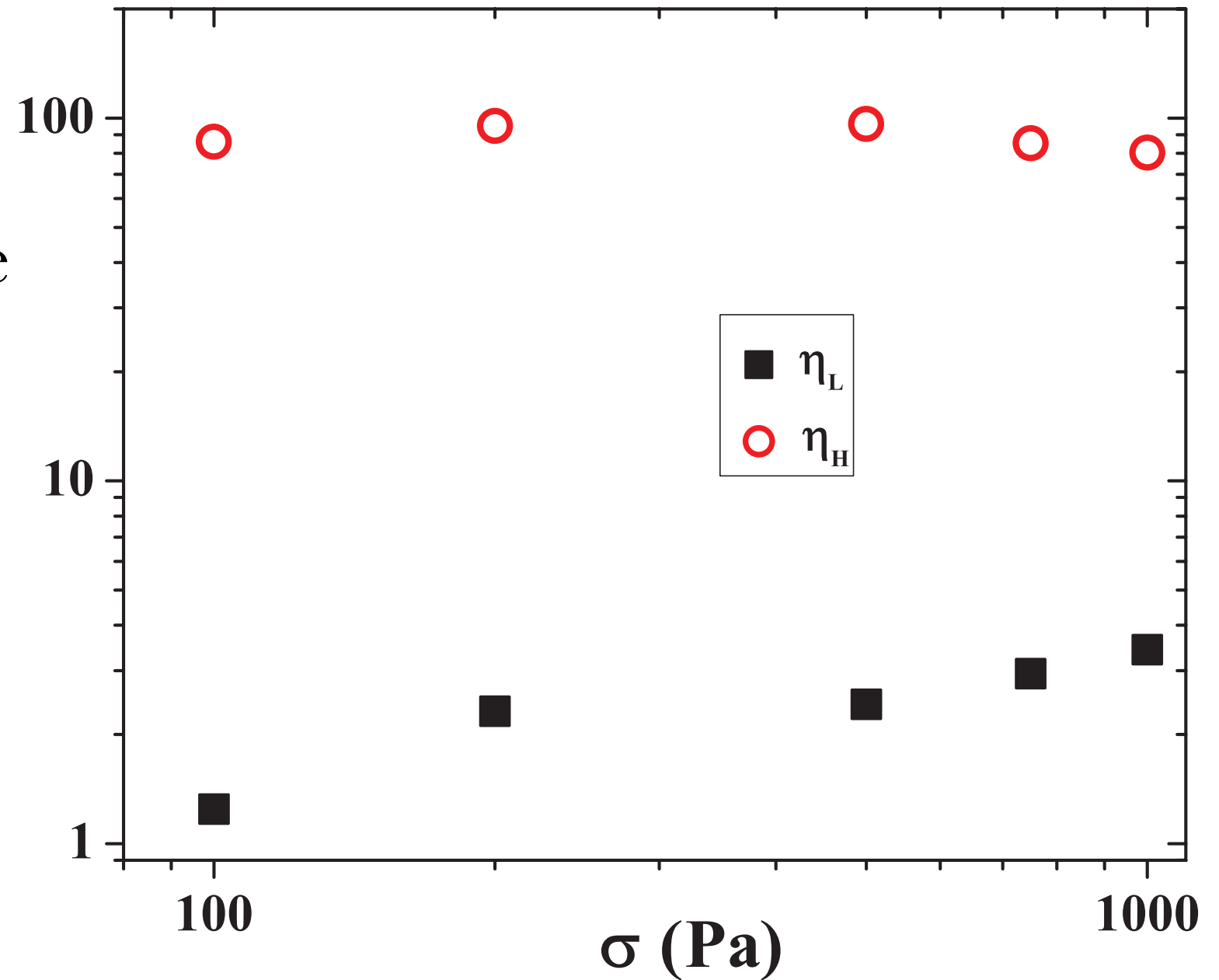
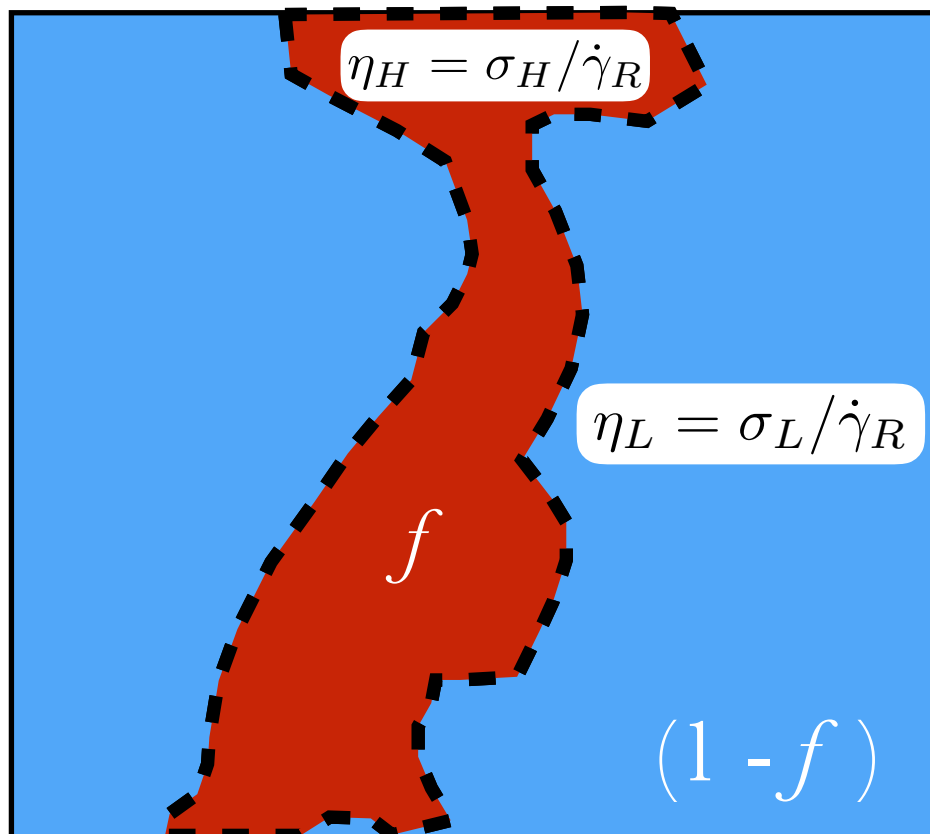
## Two fluid model: Distinct Viscosities



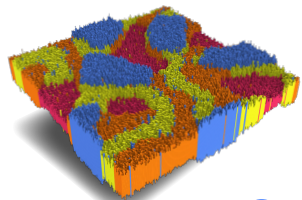


# Locally Shear Thickened

Viscosity for each phase



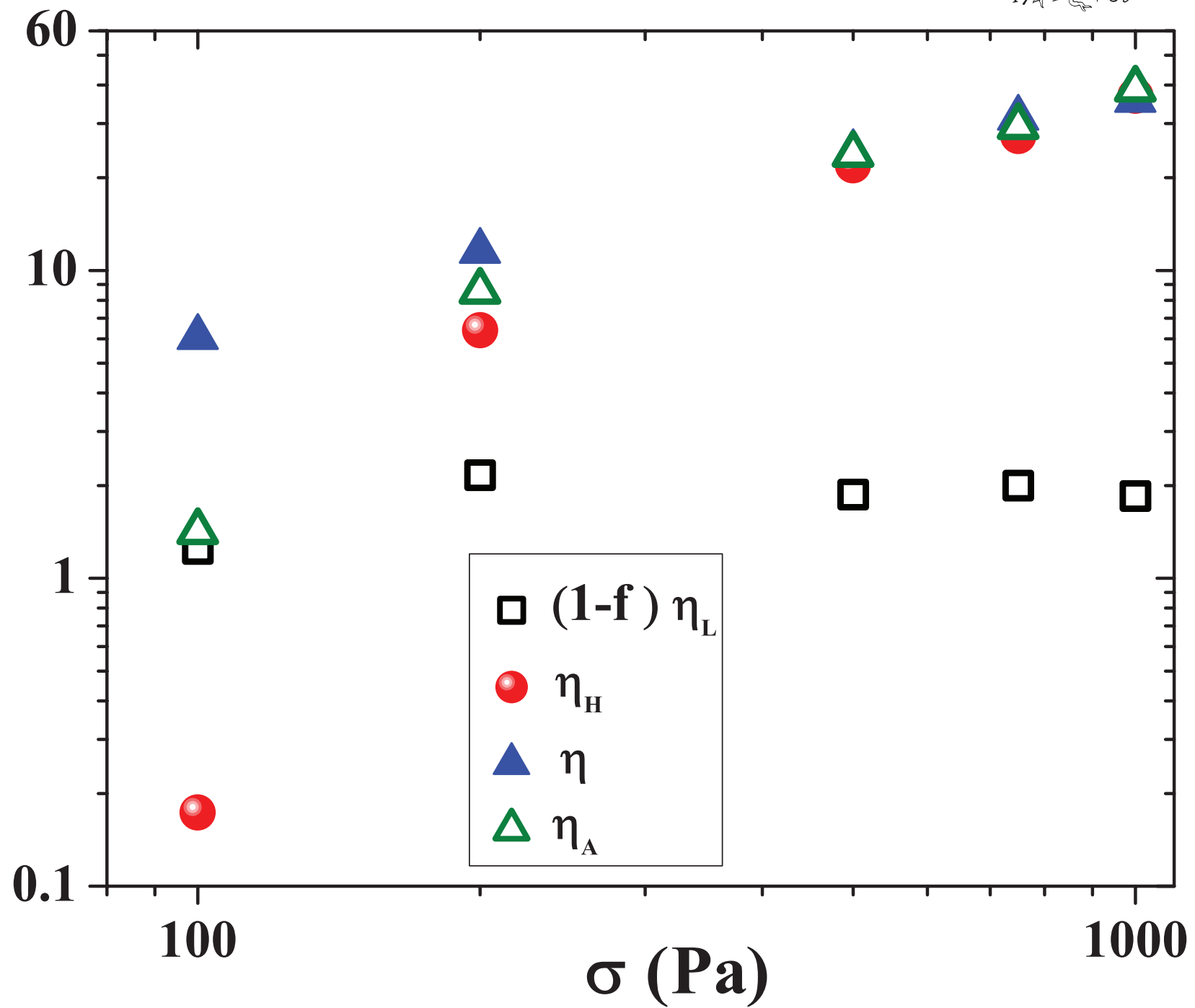
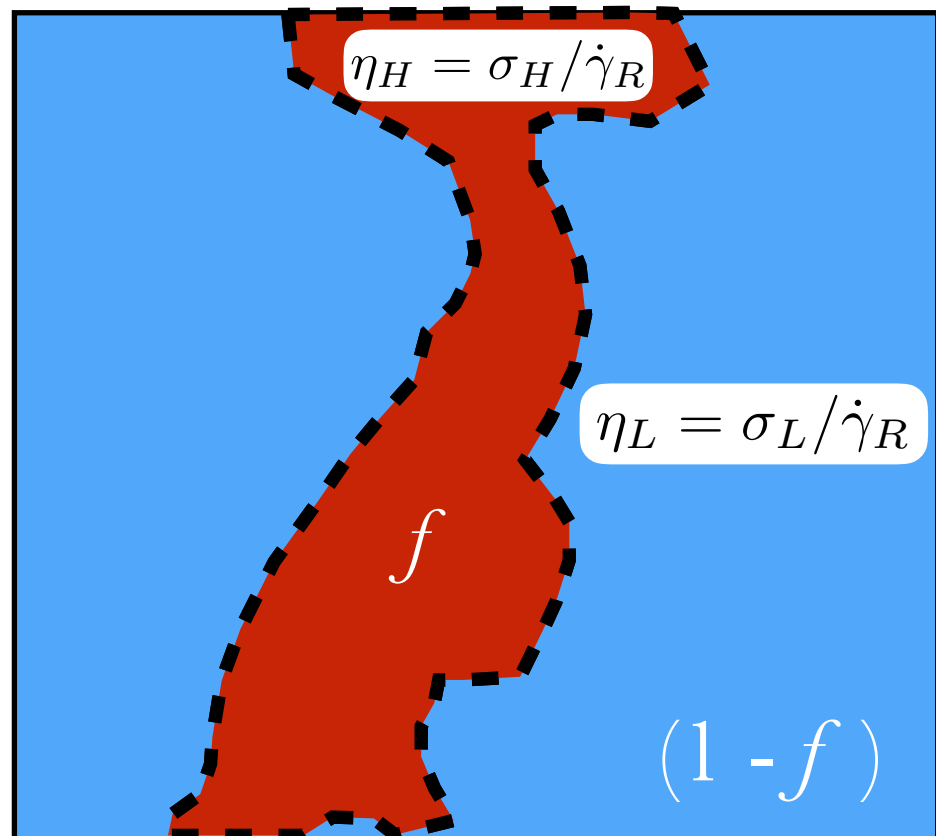


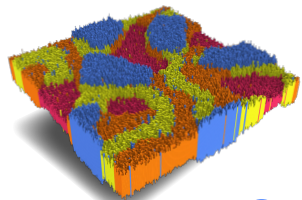


# Viscosity of Distinct Phases



$f$  — area fraction



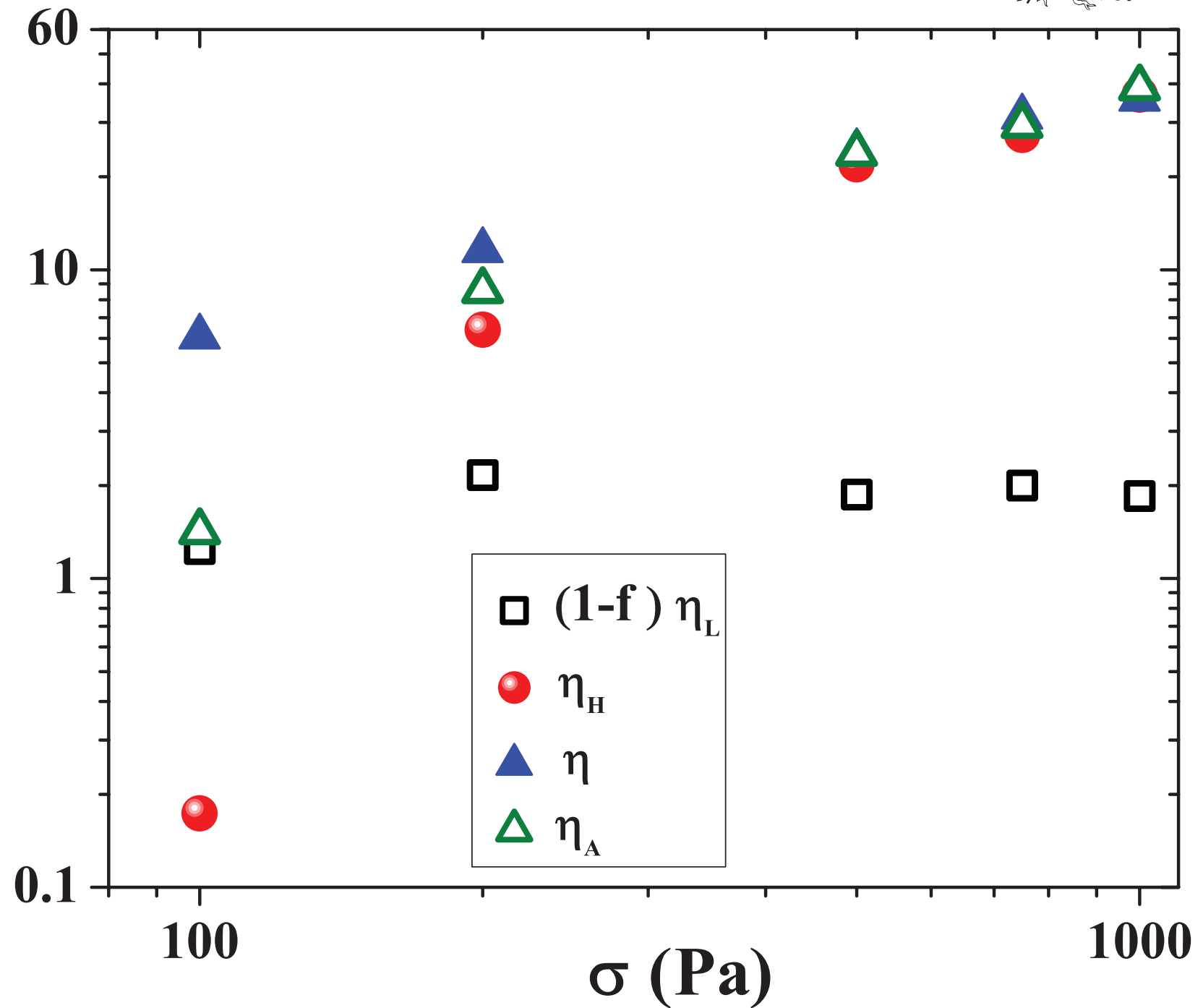
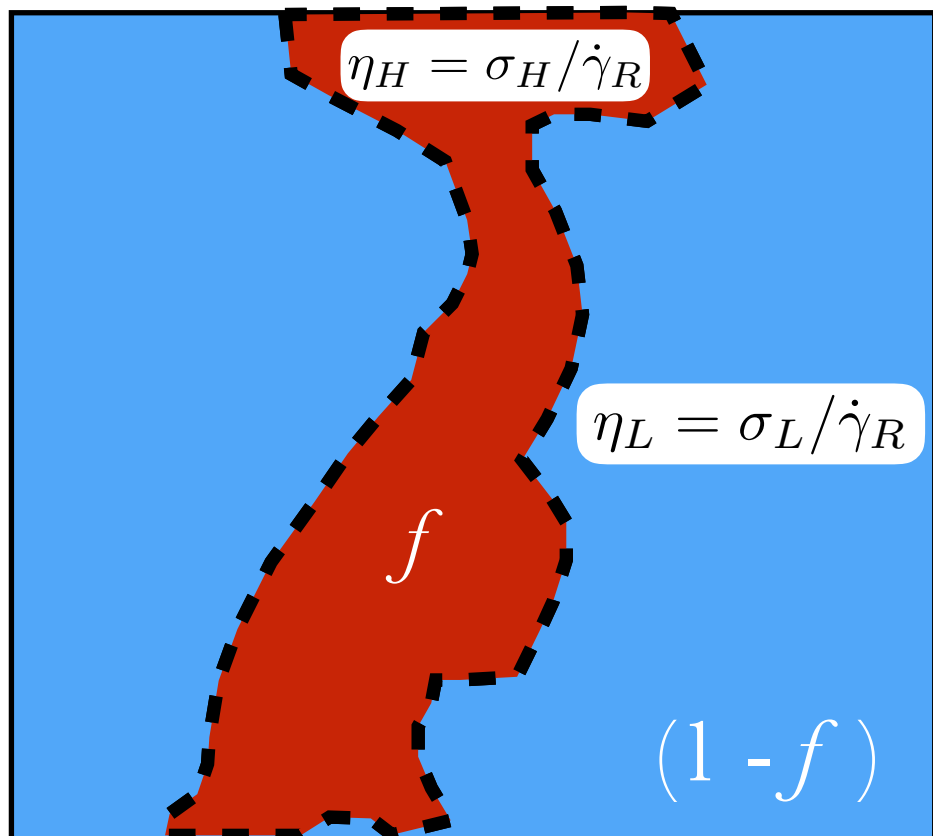


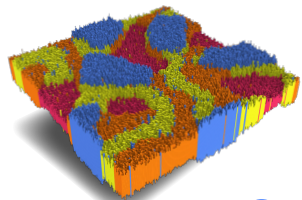
# Viscosity of Distinct Phases



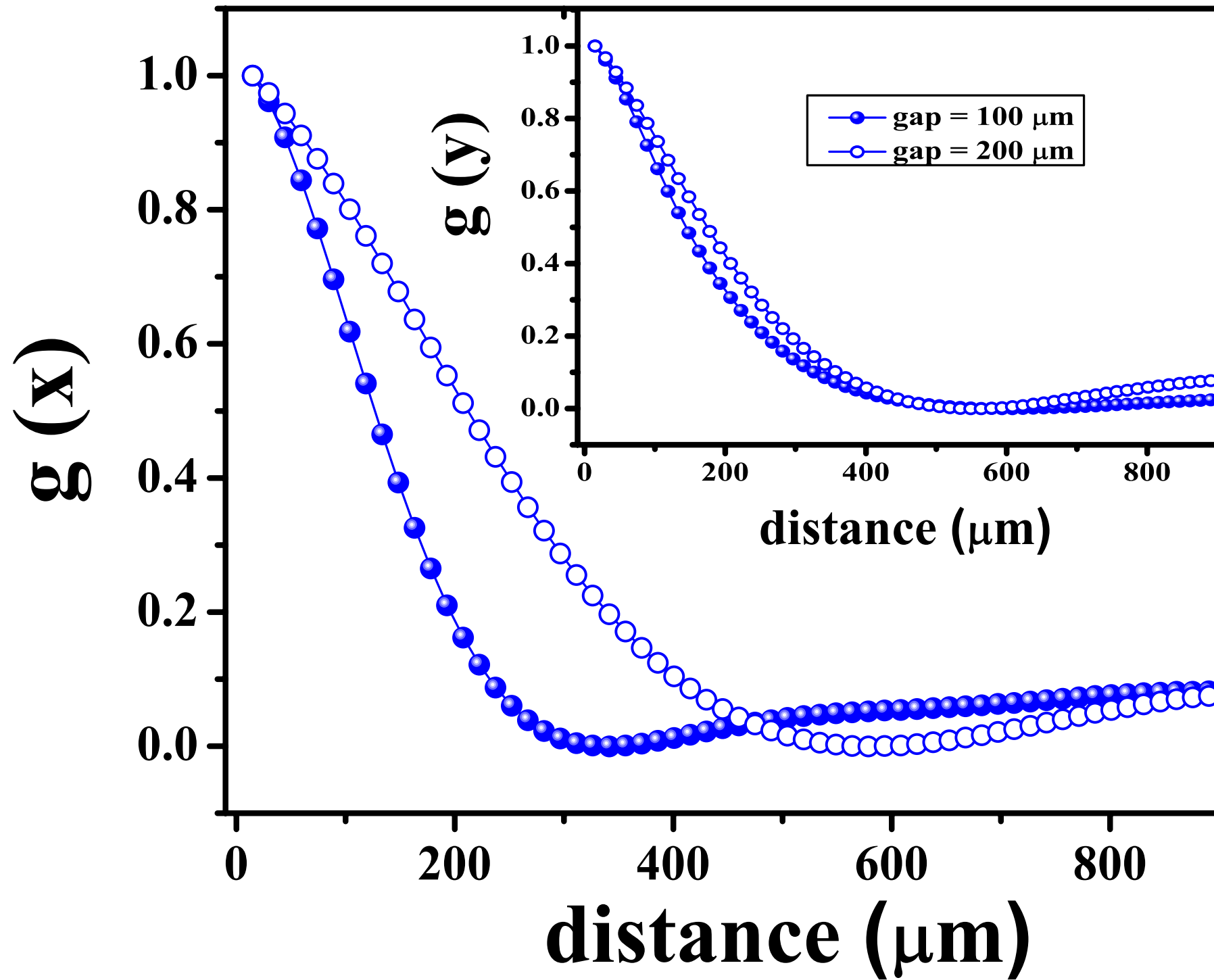
$$\eta_A = (1 - f)\eta_L + f\eta_H$$

$f$  — area fraction



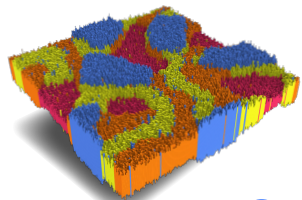


# Gap Determines Scale

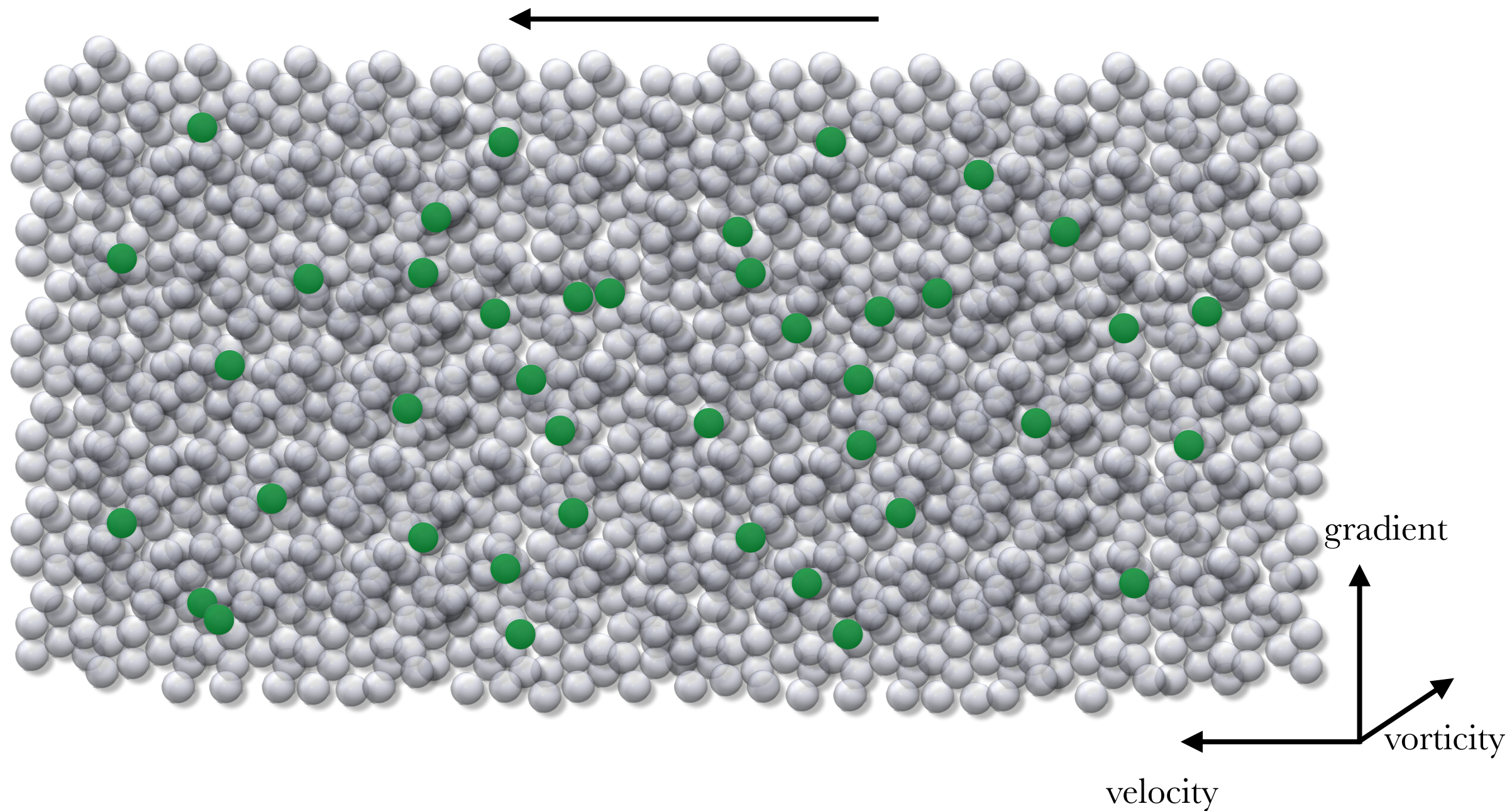


$$g(\delta r) = \frac{\langle \delta\sigma_x(\vec{r}, t) \delta\sigma_x(\vec{r} + \vec{\delta r}, t) \rangle}{\langle \delta\sigma_x(0, t)^2 \rangle}$$

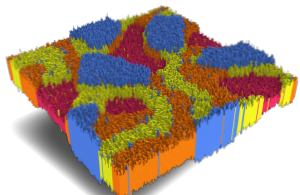




# Shear Jamming/DST

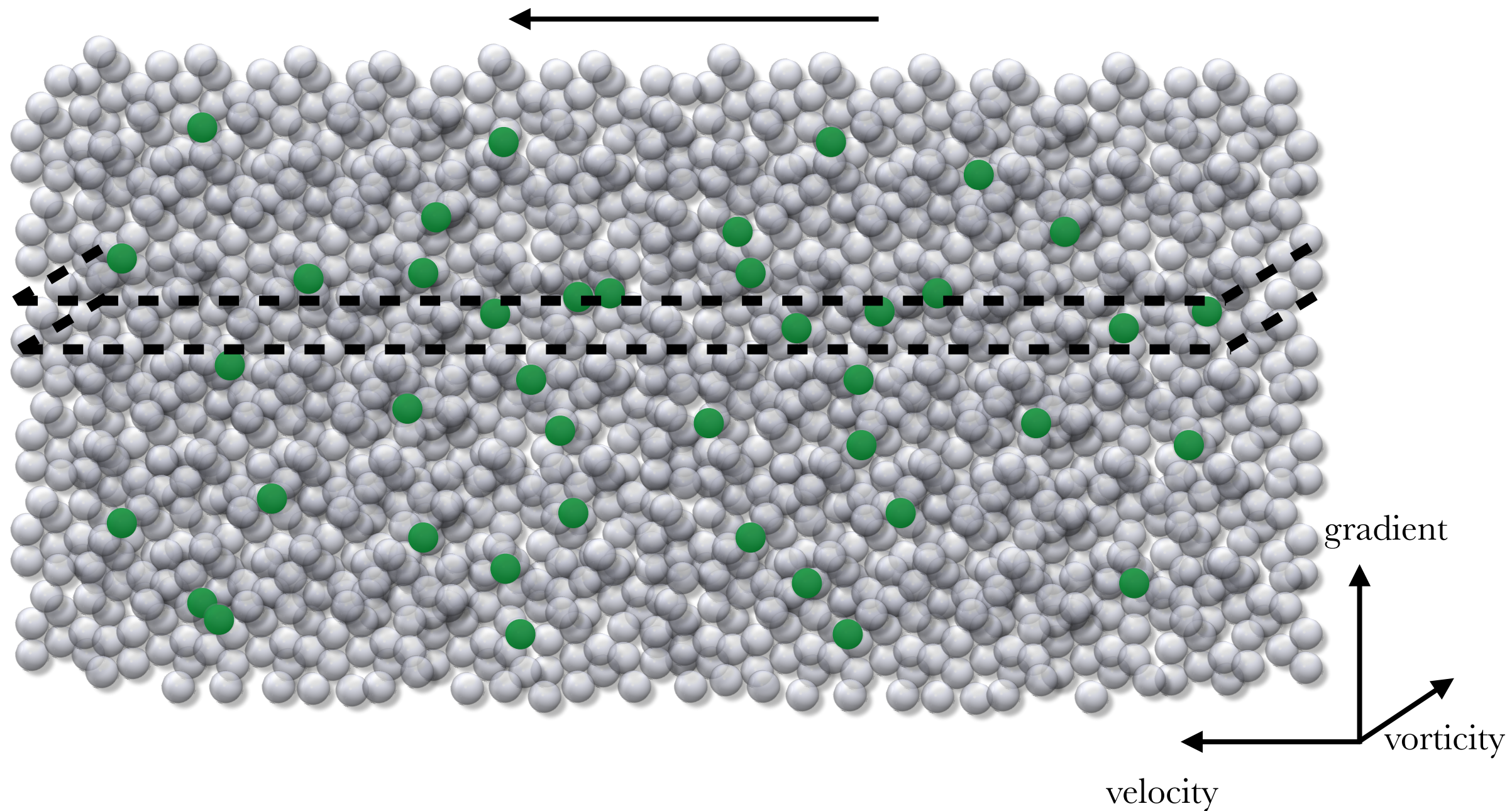






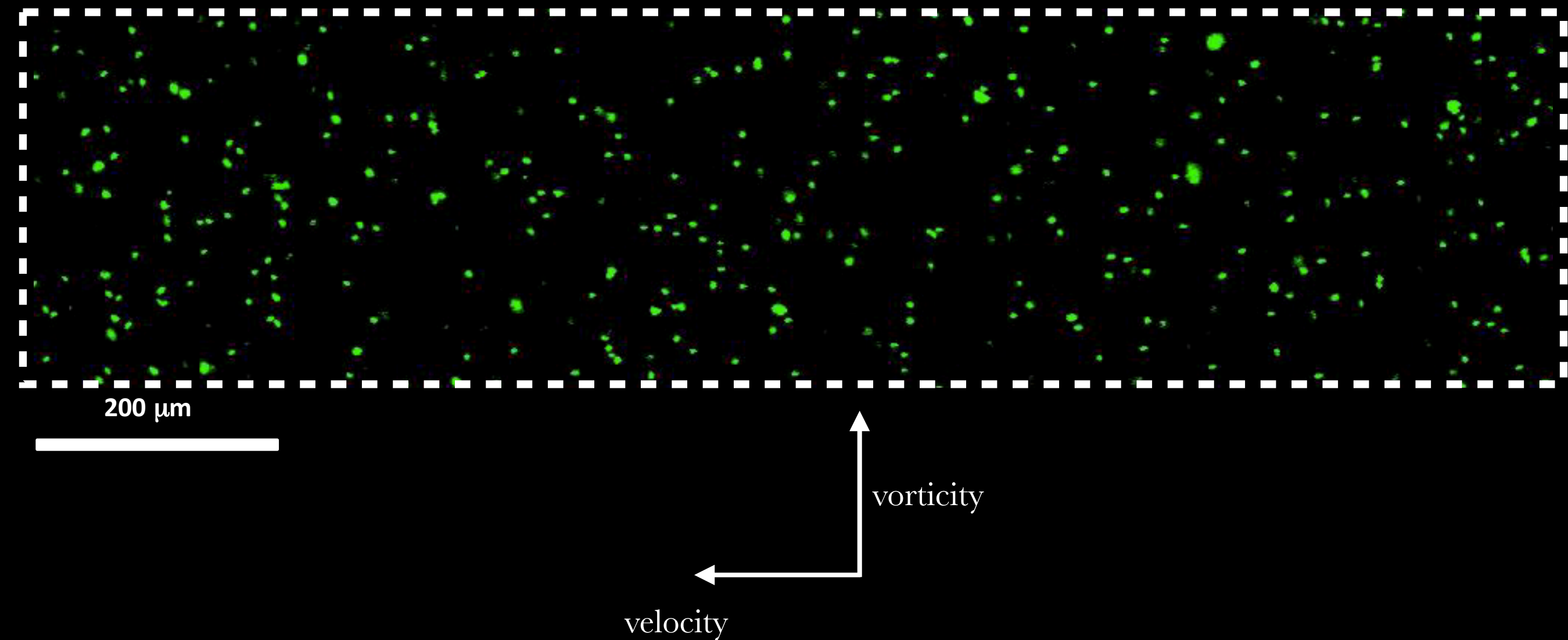
**I(SM)<sup>2</sup>**  
INSTITUTE FOR SOFT MATTER  
SYNTHESIS AND METROLOGY

# Shear Jamming/DST



# Bulk Flow Behavior: Constant Stress

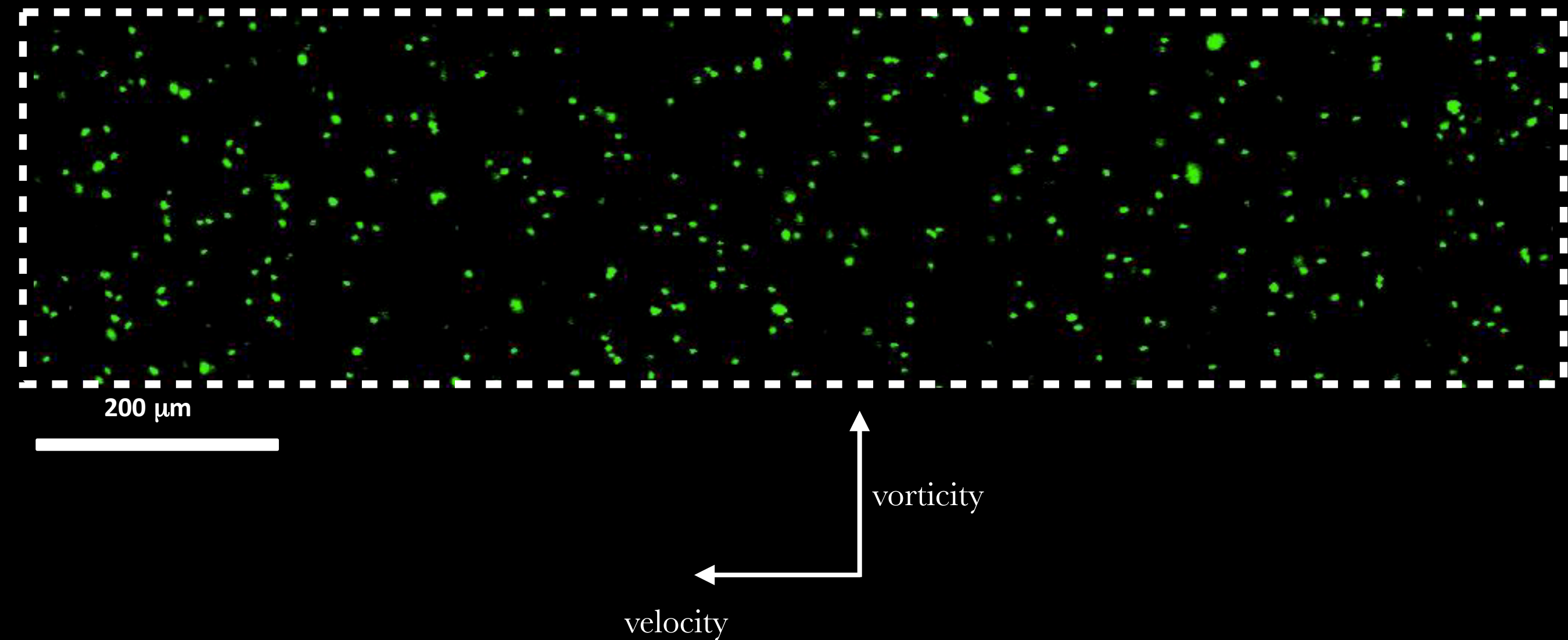
$$\sigma = 2200 \text{ Pa}$$





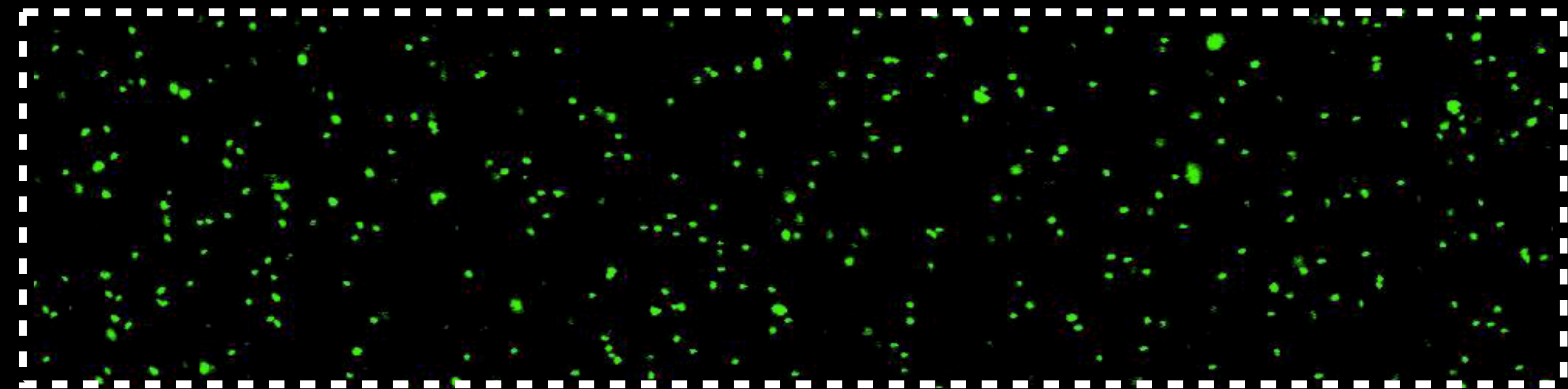
# Bulk Flow Behavior: Constant Stress

$$\sigma = 2200 \text{ Pa}$$

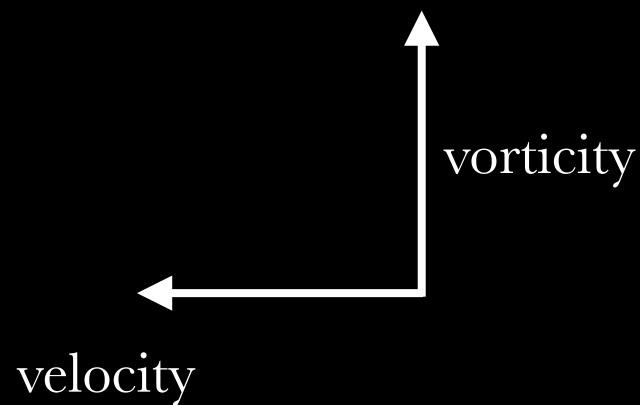


# Bulk Flow Behavior: Constant Stress

$$\sigma = 2200 \text{ Pa}$$



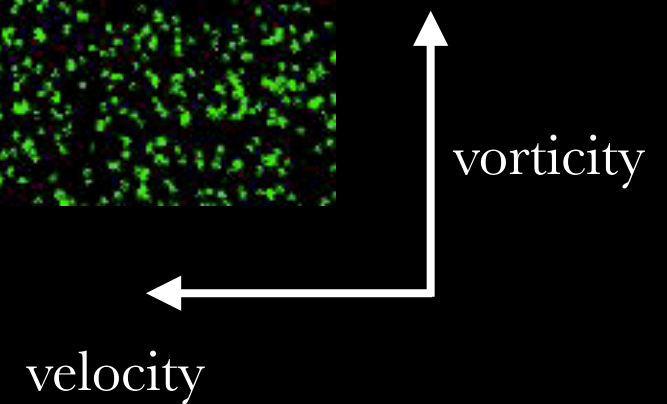
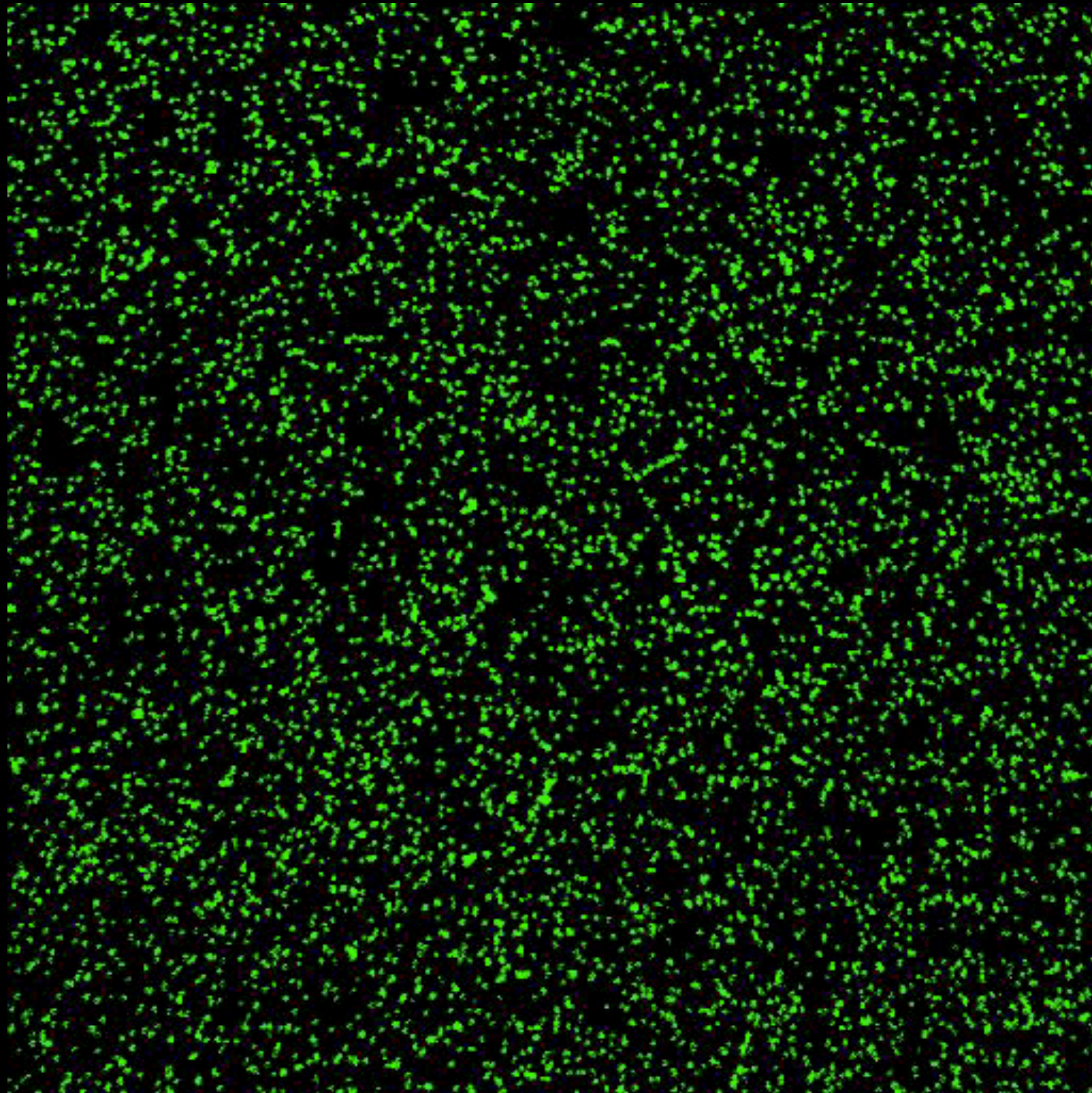
200  $\mu\text{m}$



when flow stops: dilatancy?



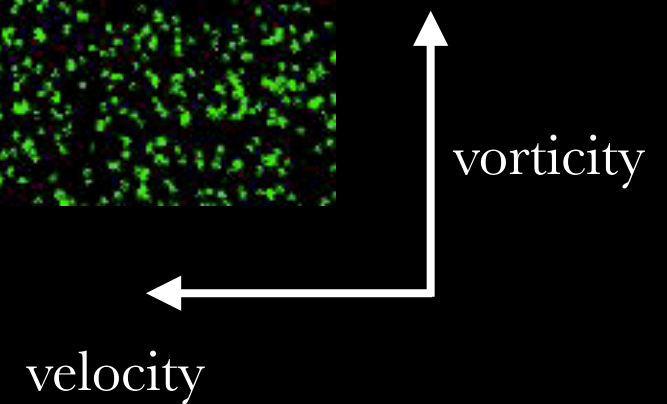
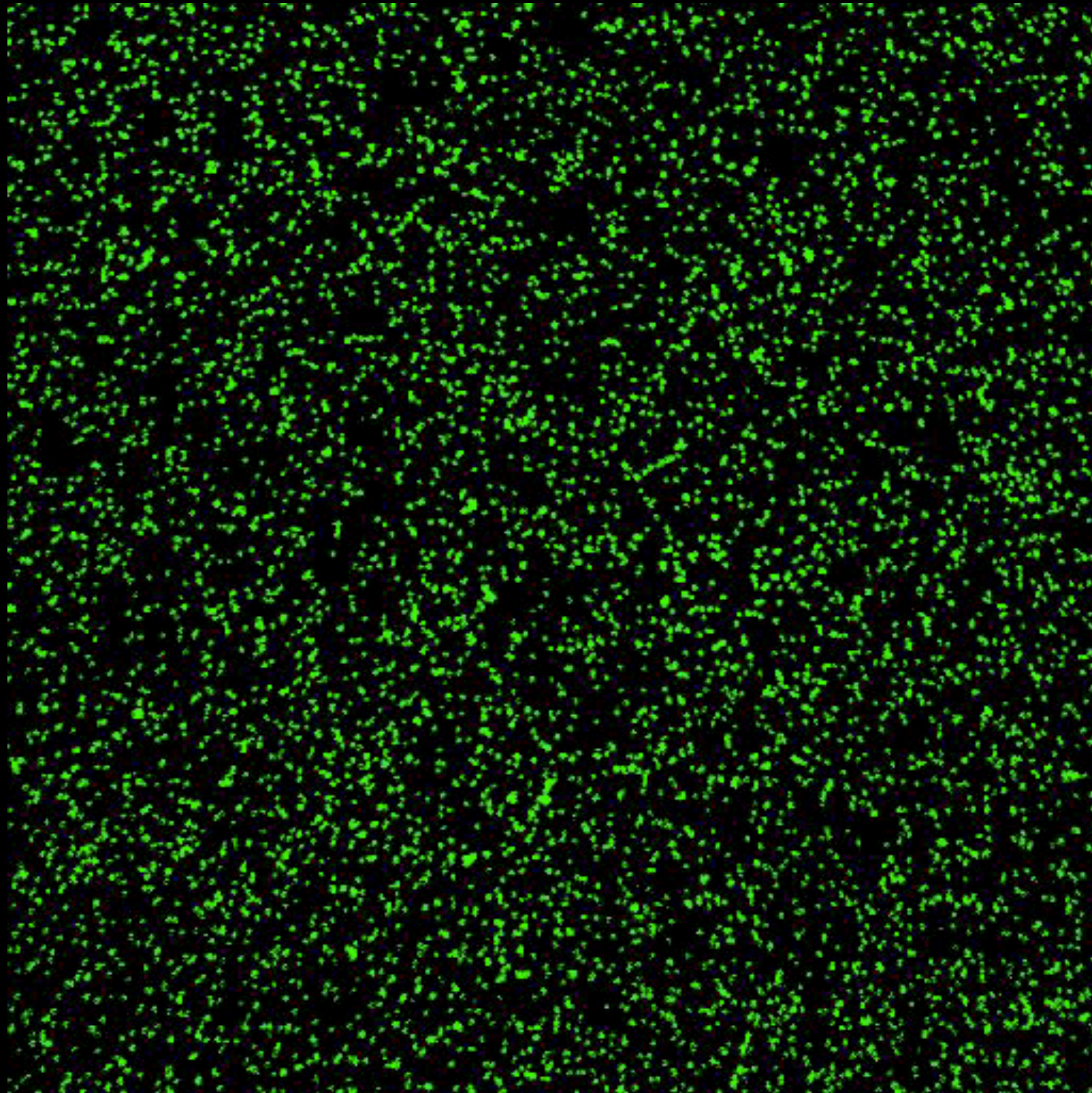
# Boundary Stresses: Dilatancy



$$\sigma = 2200 \text{ Pa}$$

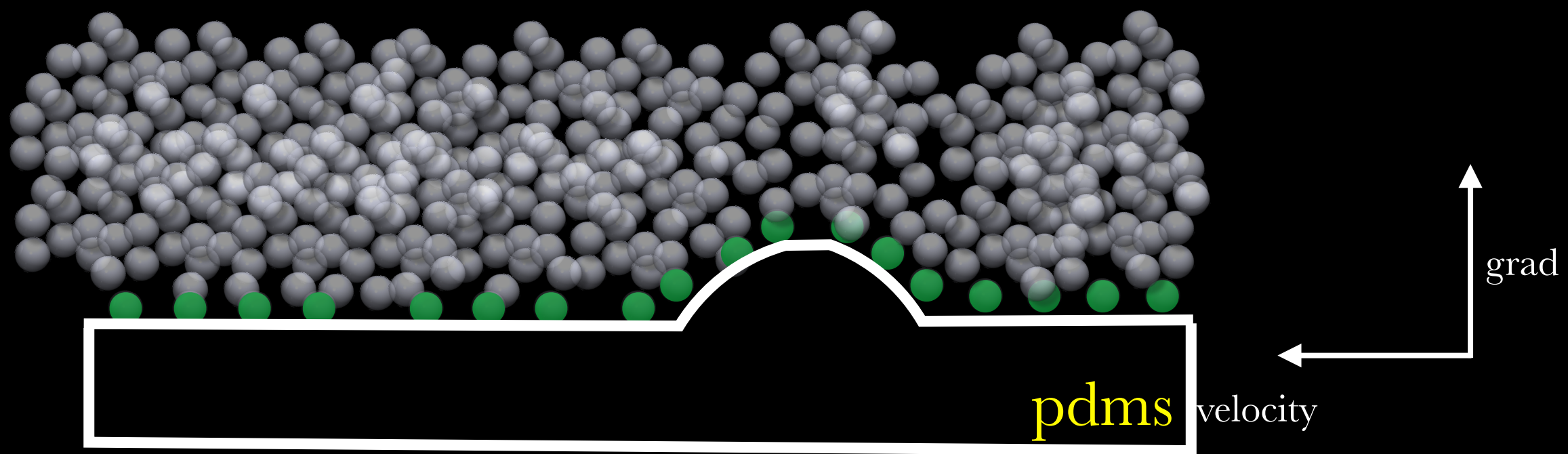
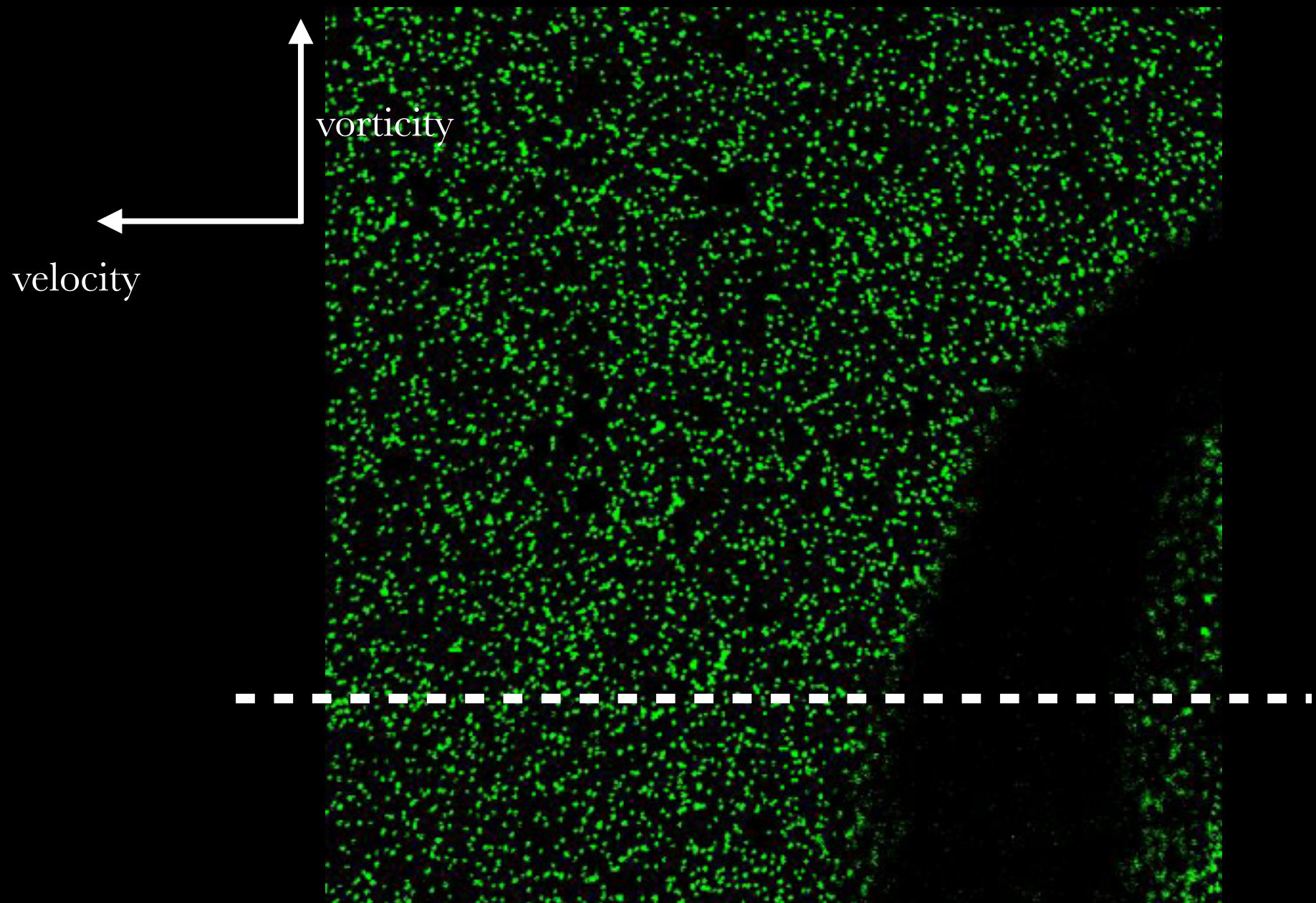


# Boundary Stresses: Dilatancy

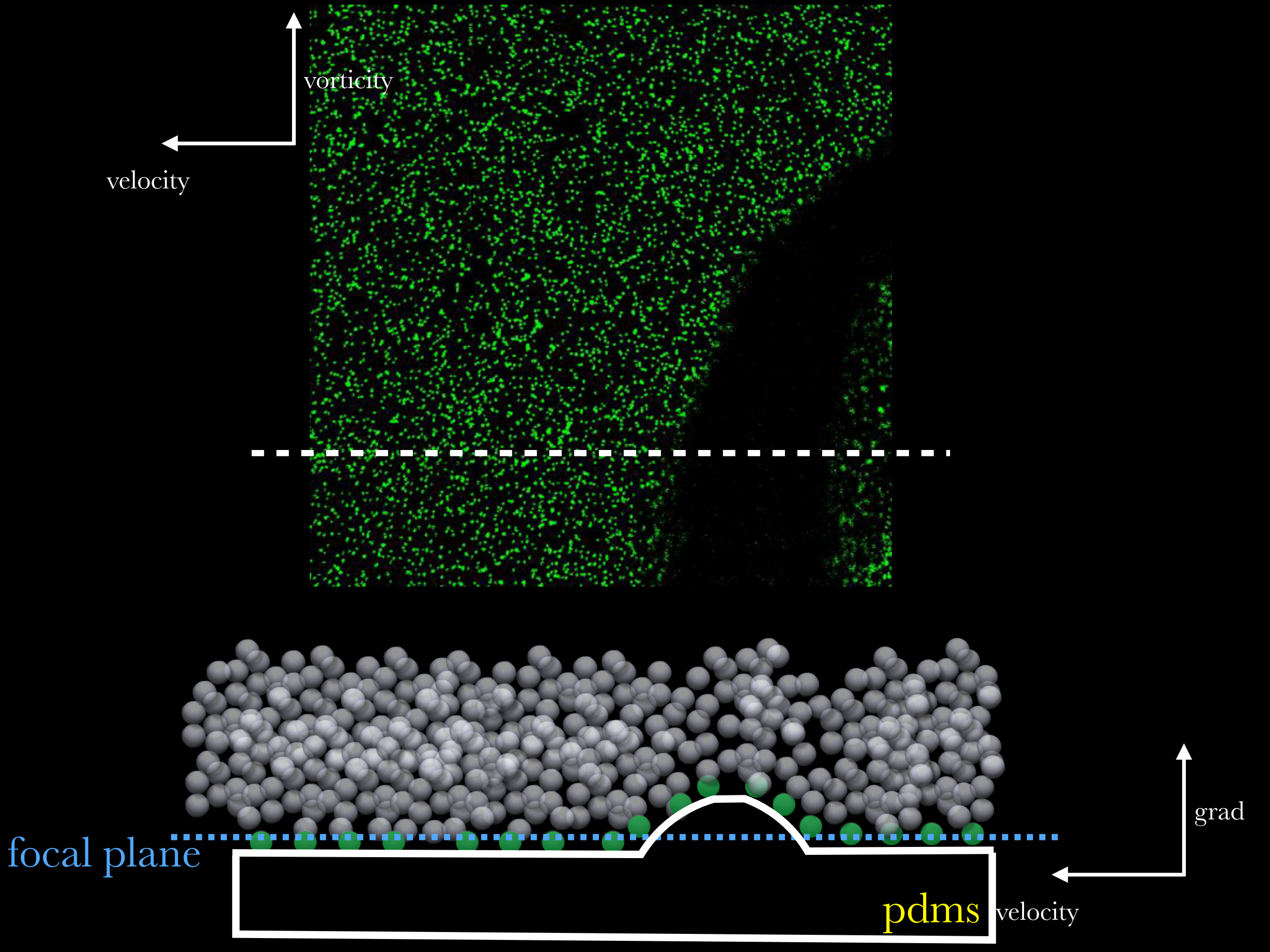


$$\sigma = 2200 \text{ Pa}$$

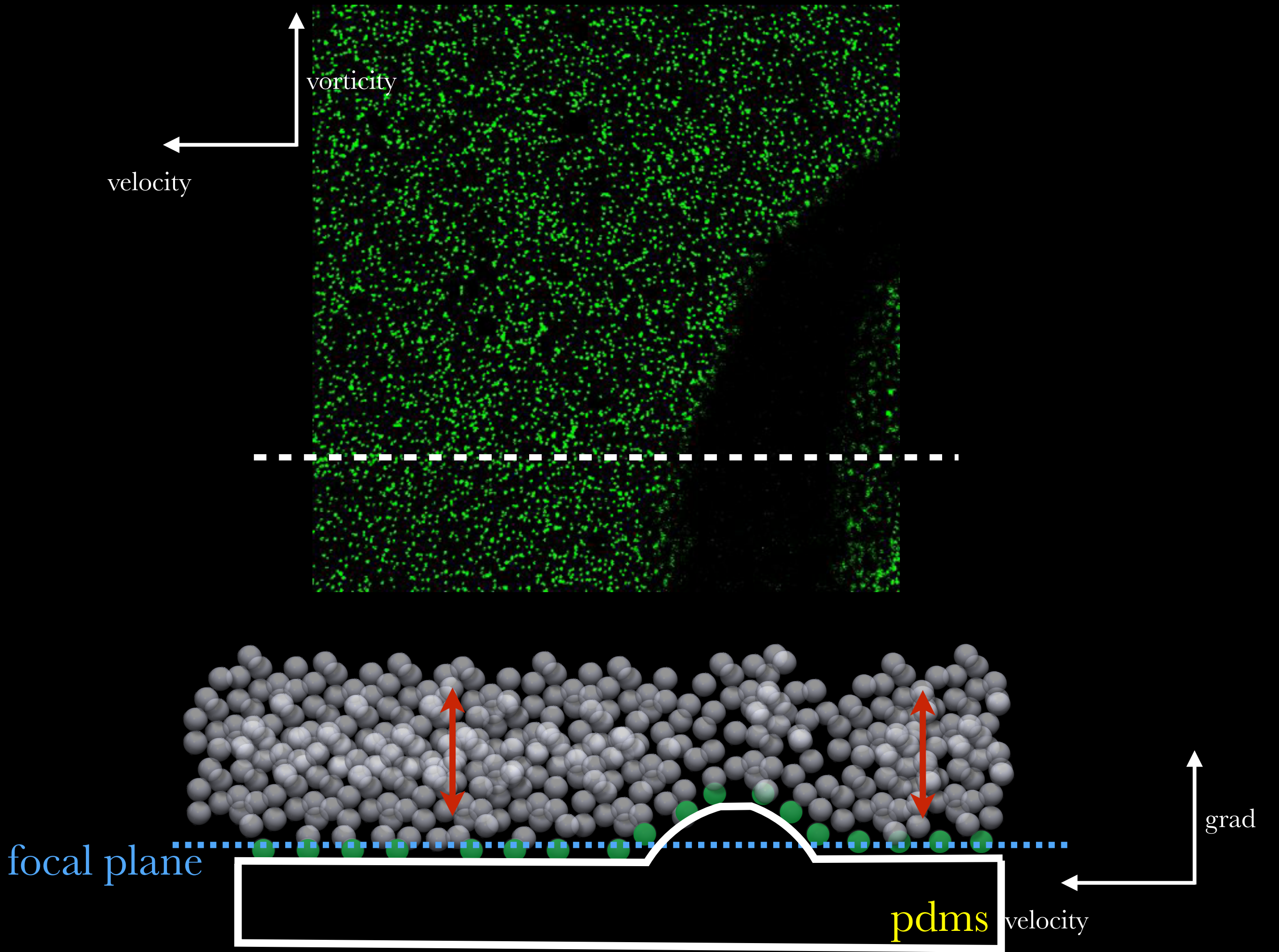




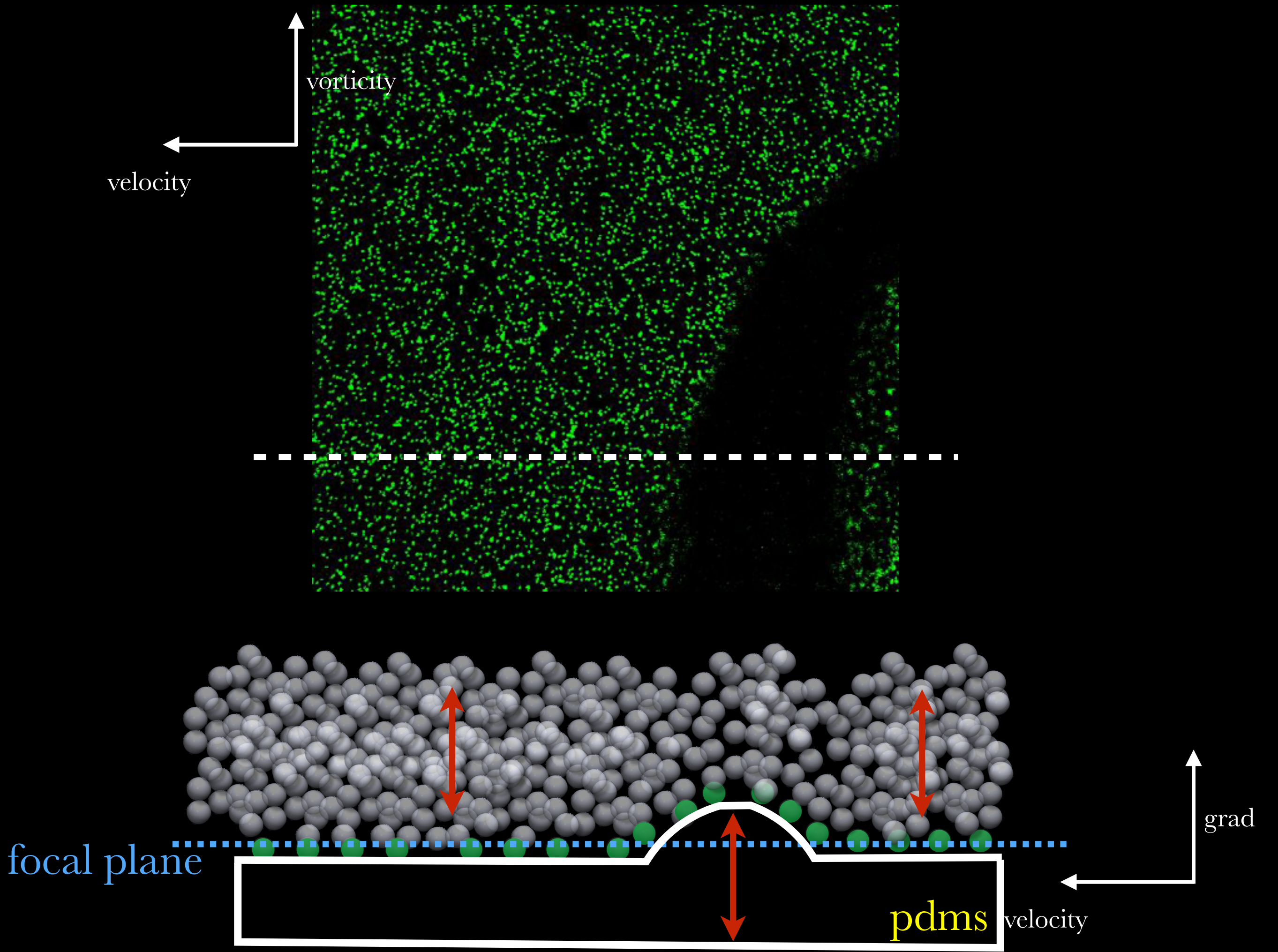






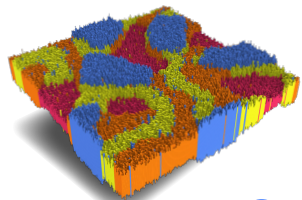




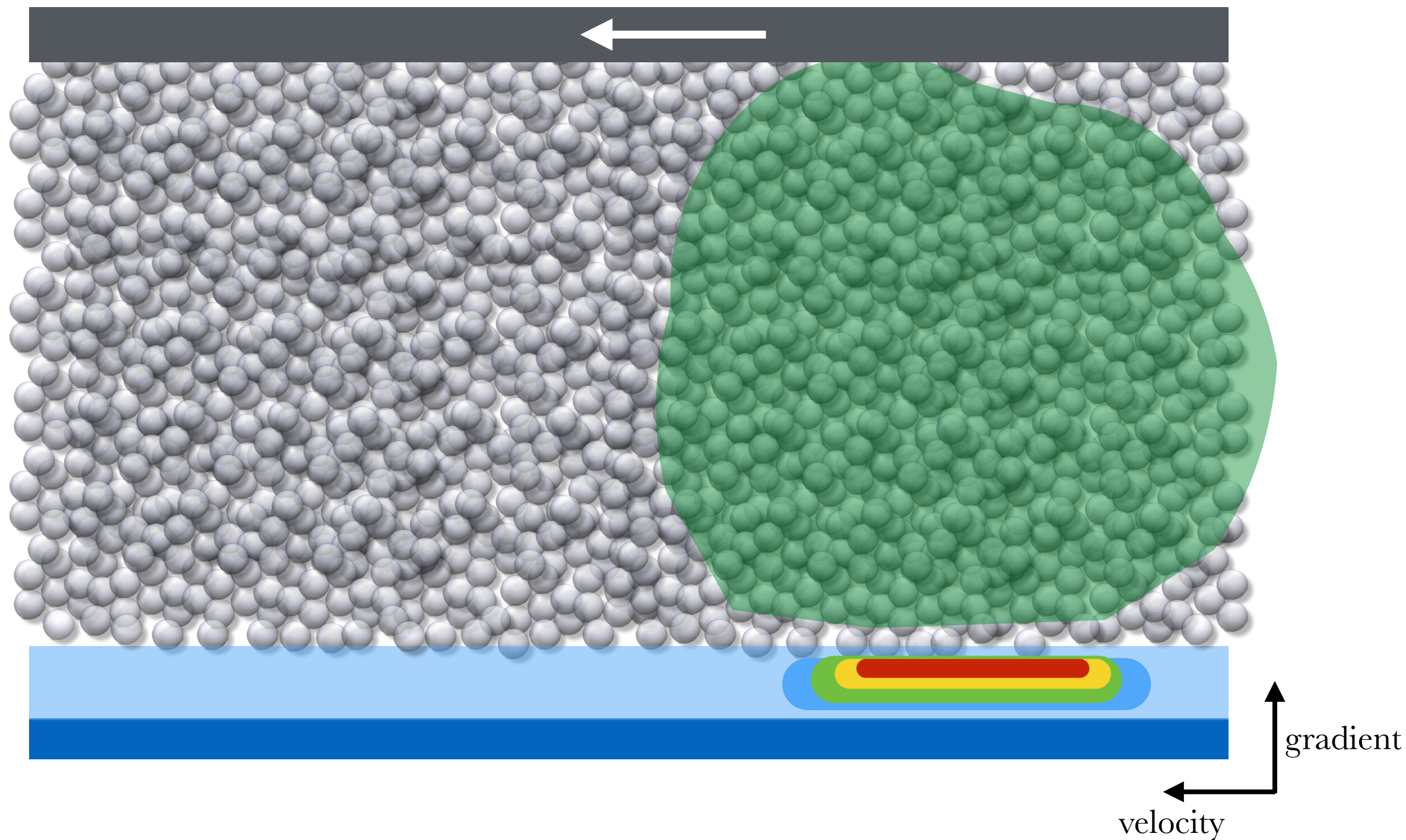


So, What's Next?

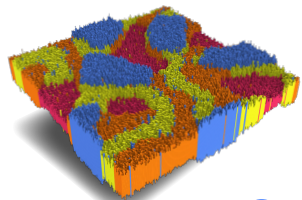




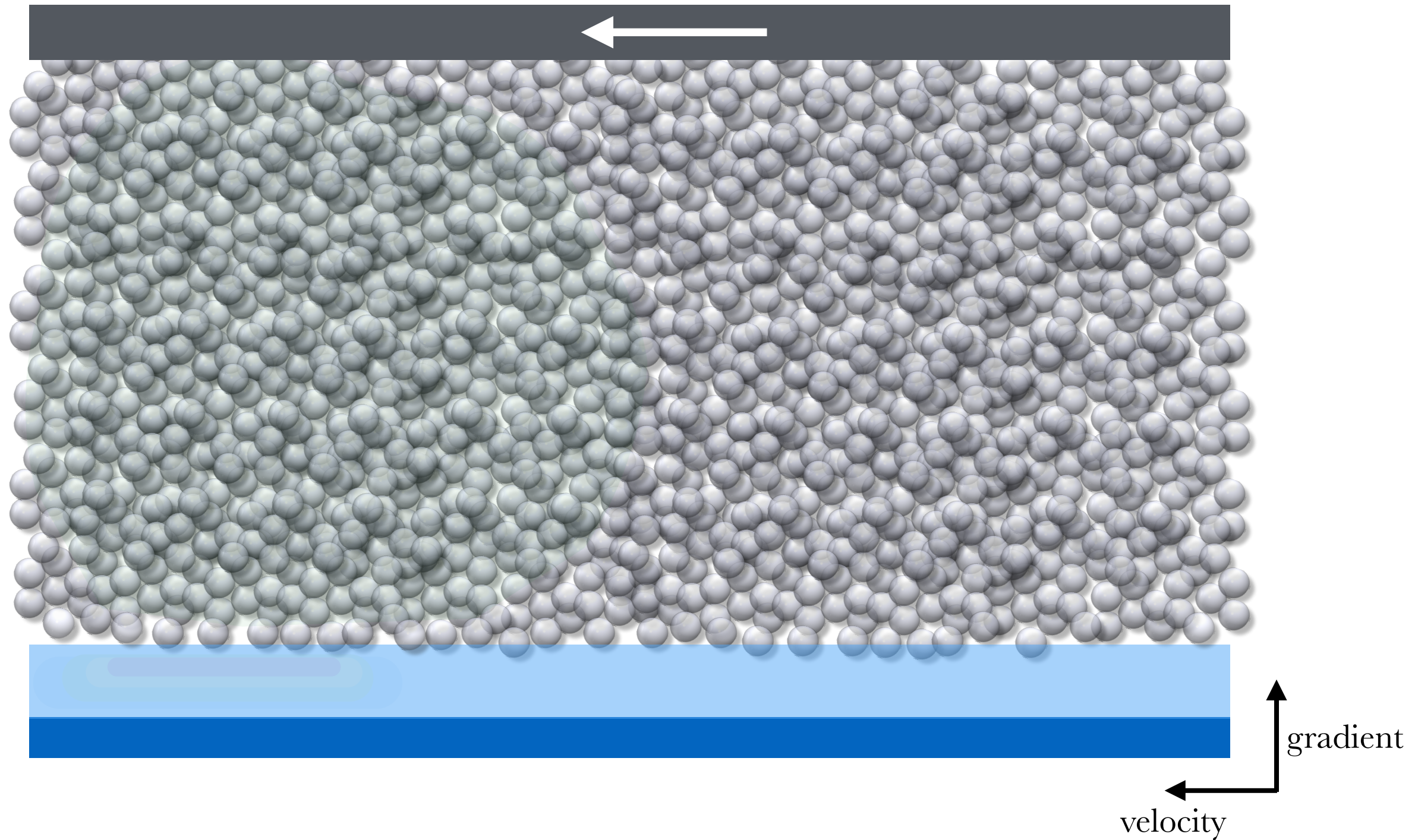
# What Controls the Lifetime?







# What Controls the Lifetime?



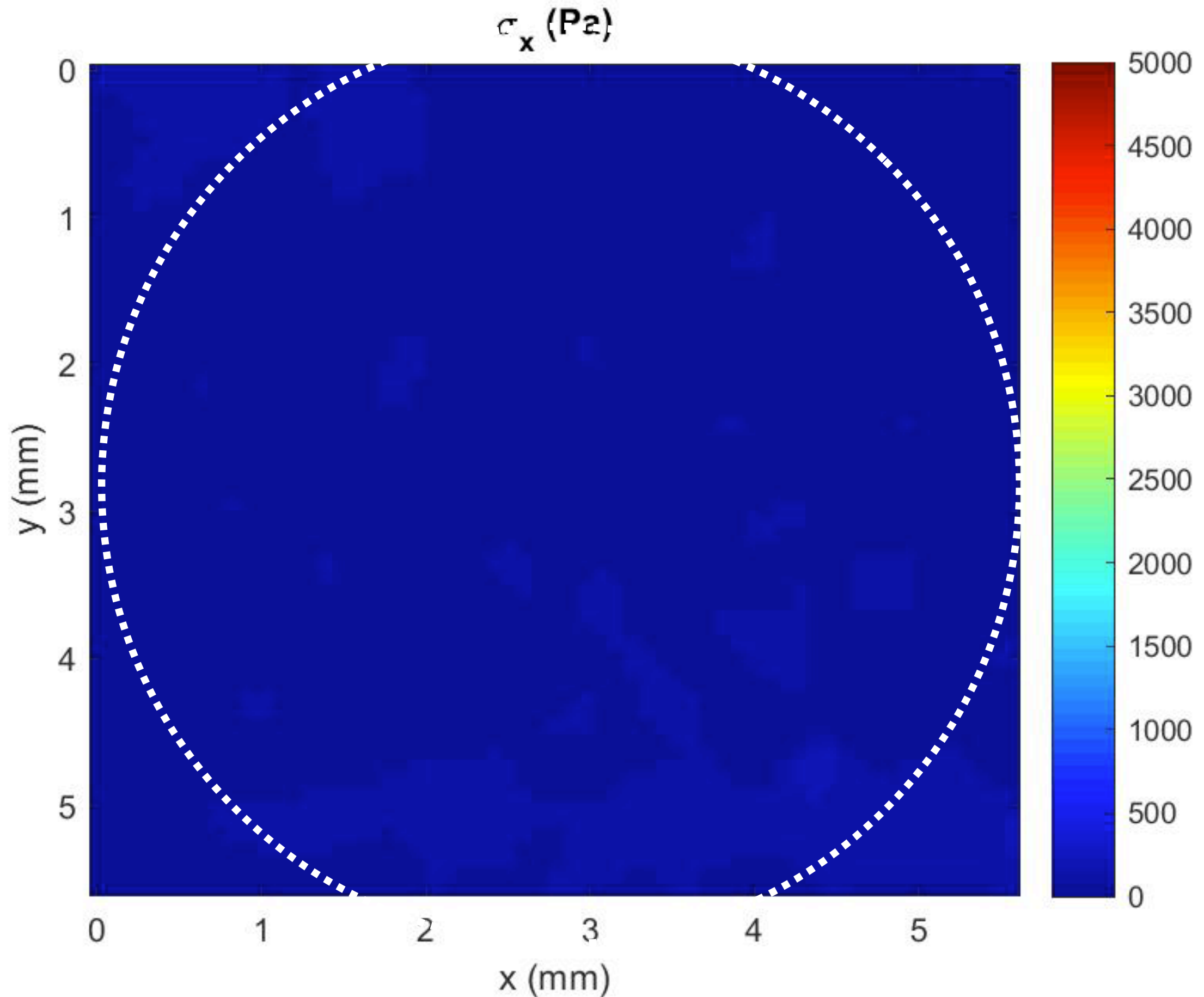






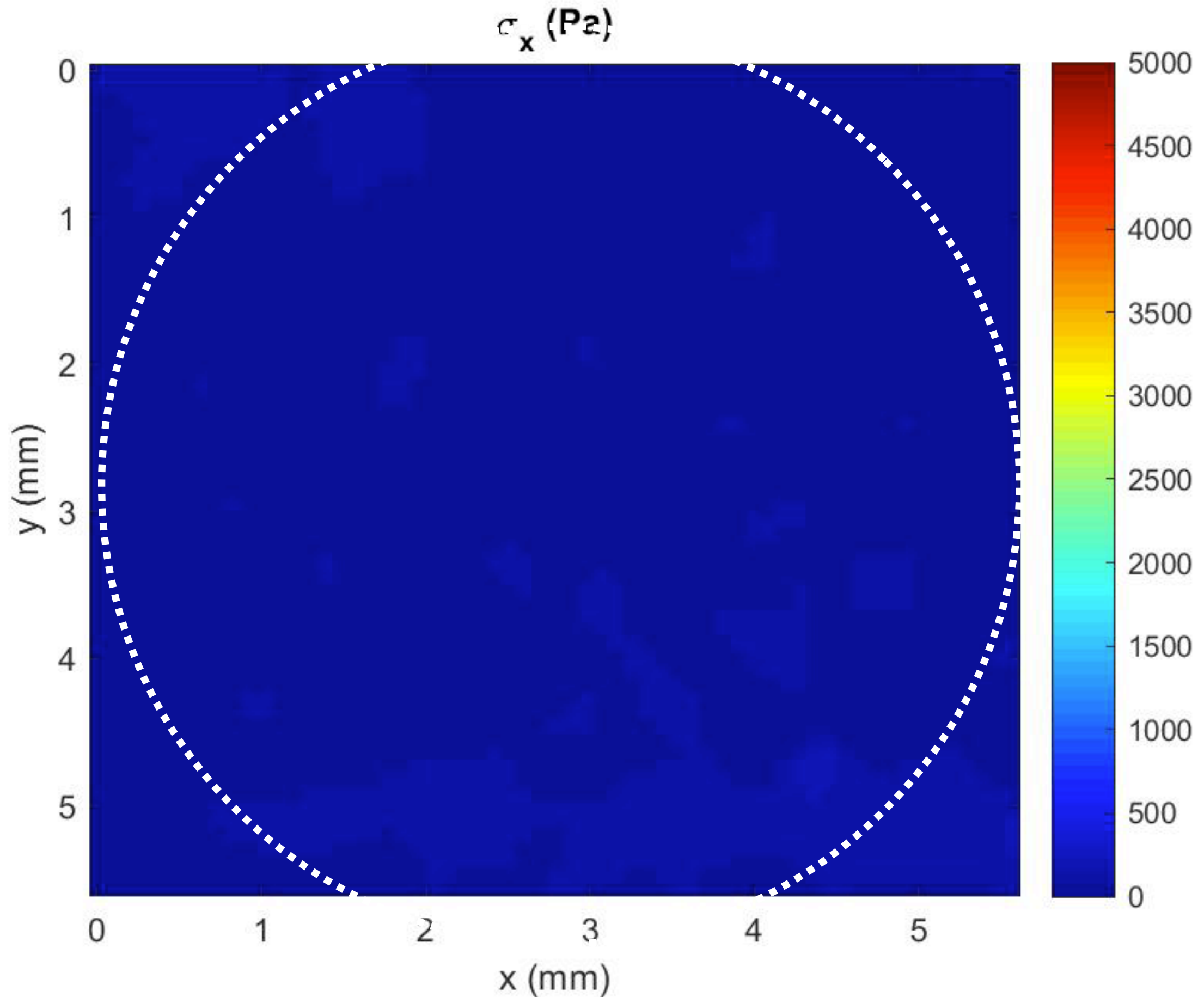


75 Pa  $h=300\mu\text{m}$   $\phi=56\%$   $d = 1.5\mu\text{m}$

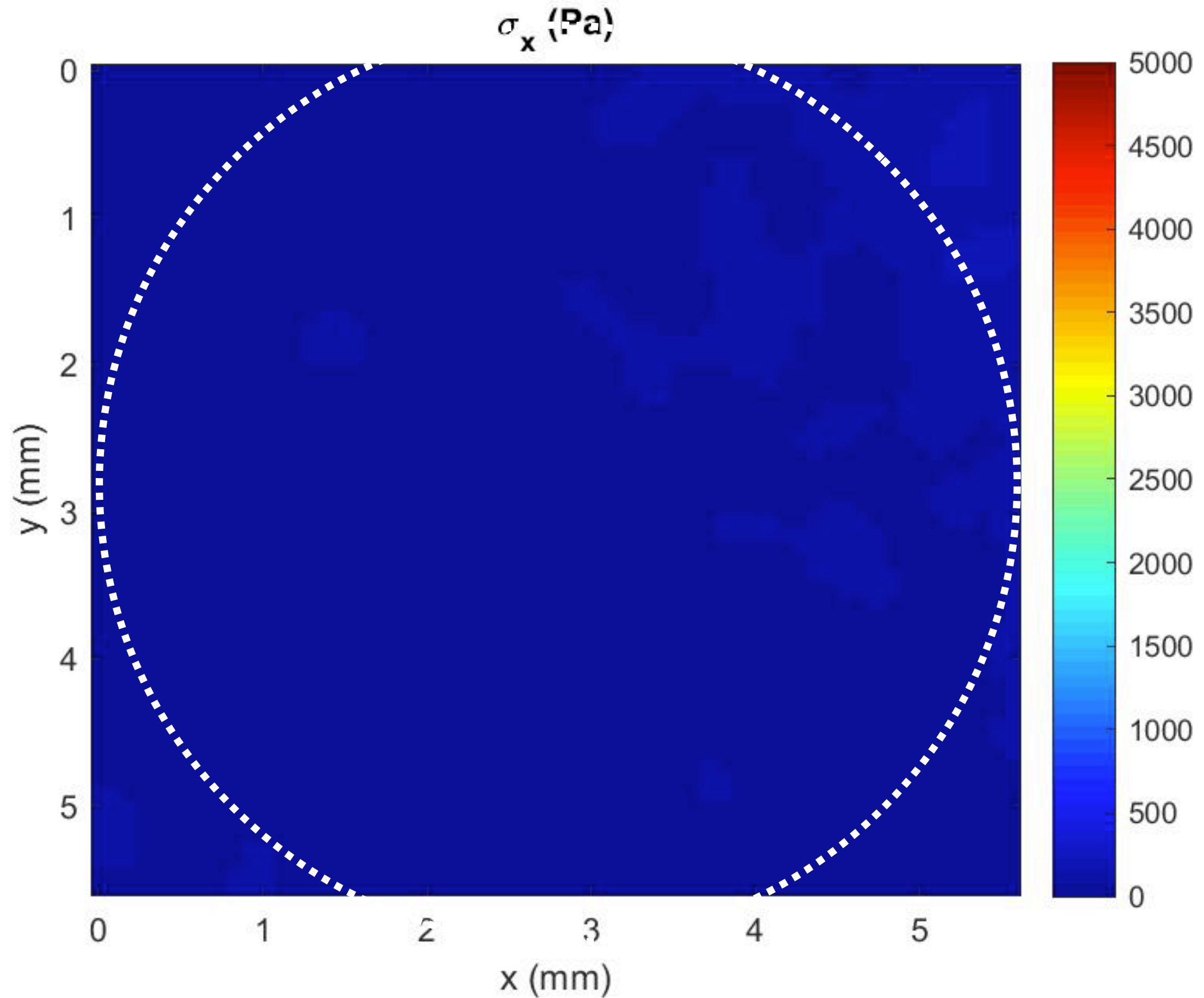




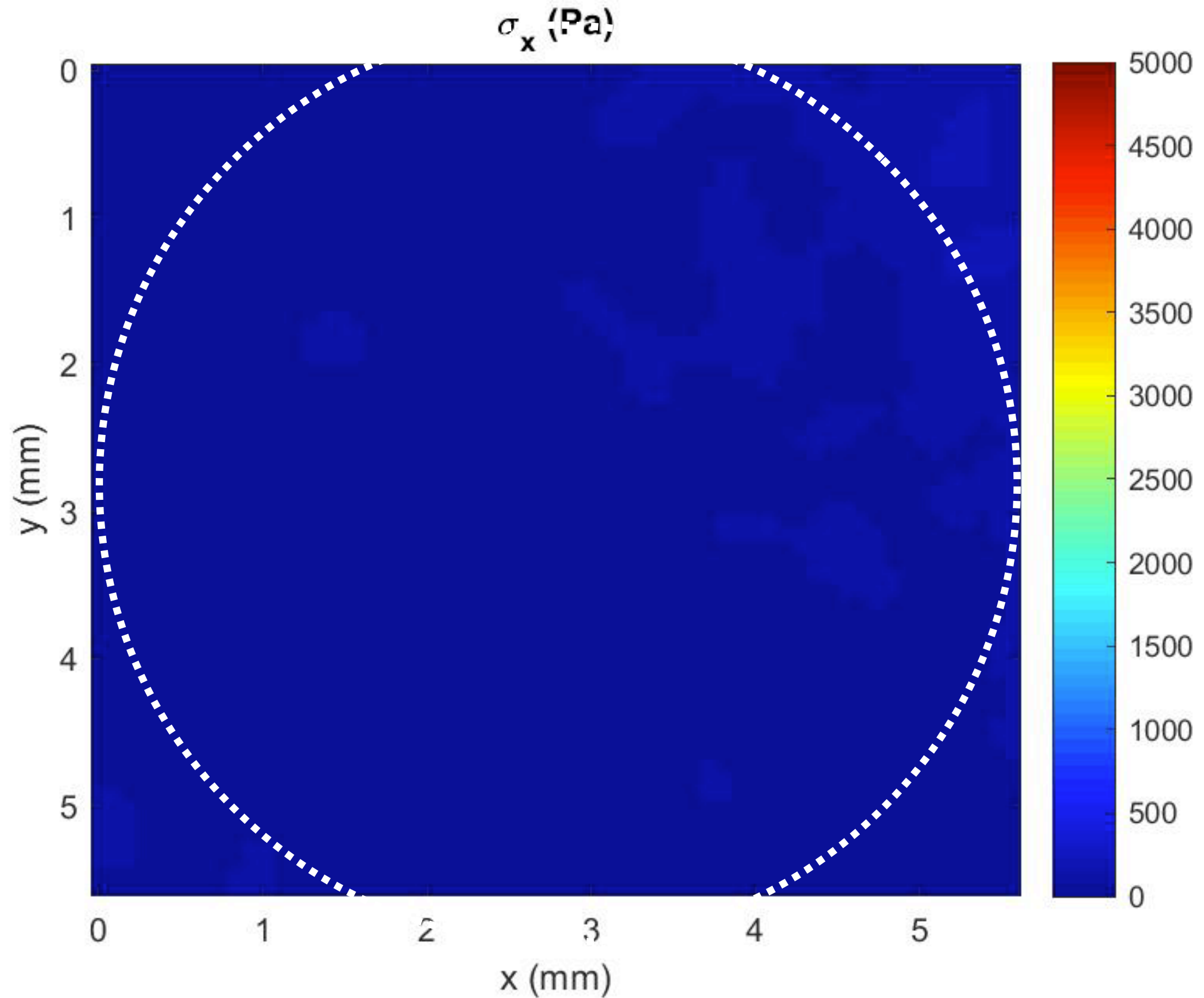
75 Pa  $h=300\mu\text{m}$   $\phi=56\%$   $d = 1.5\mu\text{m}$



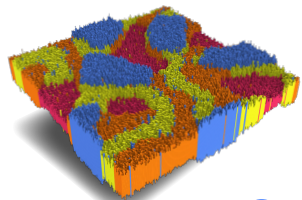
200 Pa  $h=200\mu\text{m}$   $\phi=56\%$   $d = 1.5\mu\text{m}$



200 Pa  $h=200\mu\text{m}$   $\phi=56\%$   $d = 1.5\mu\text{m}$





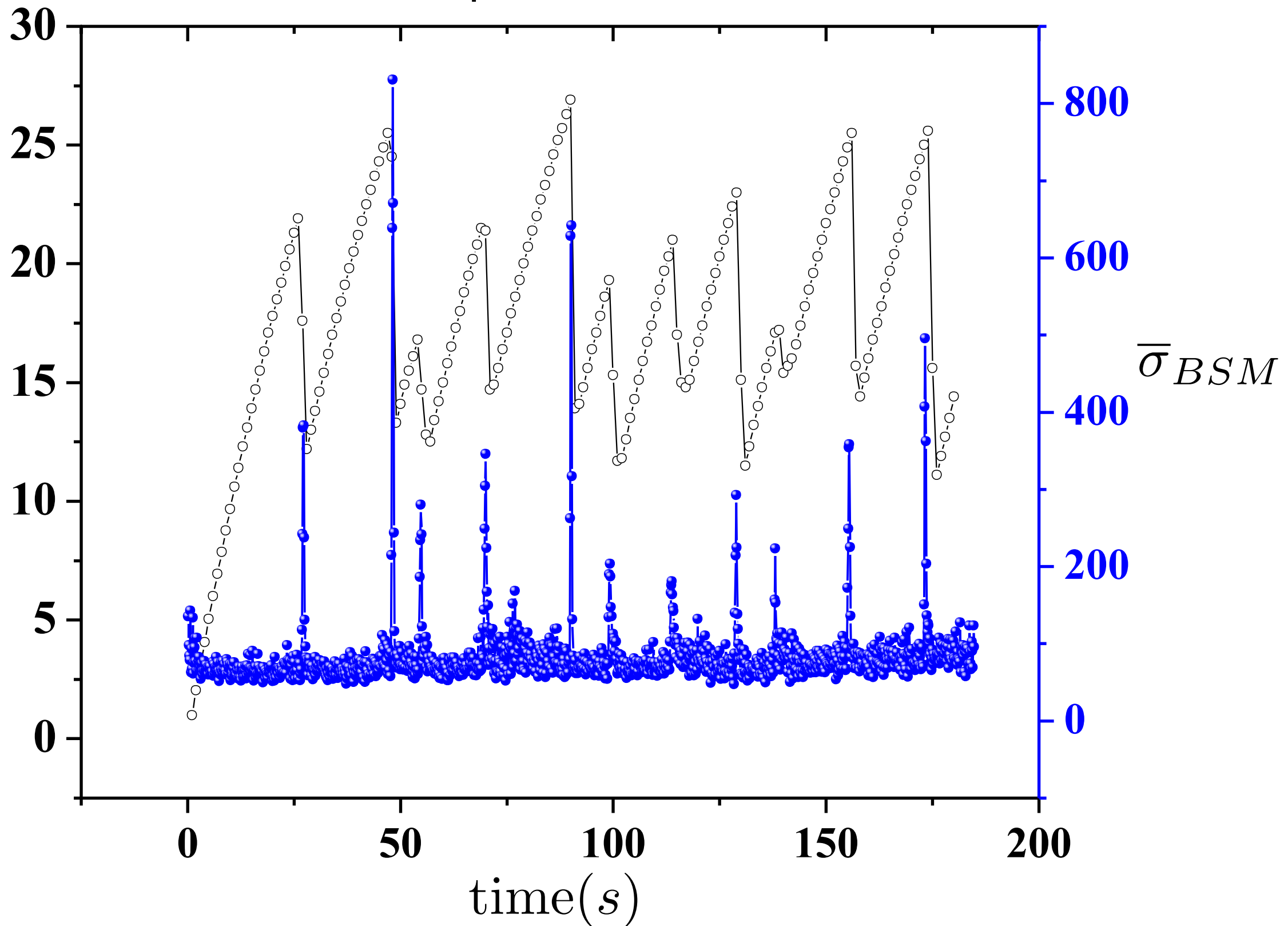


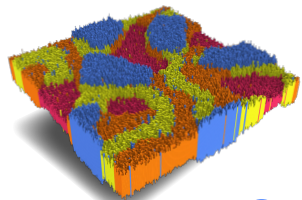
# Local and Global Fluctuations



$\tau = 75 \text{ Pa}, \phi = 0.56, \text{PP 5.2}$

$\gamma$



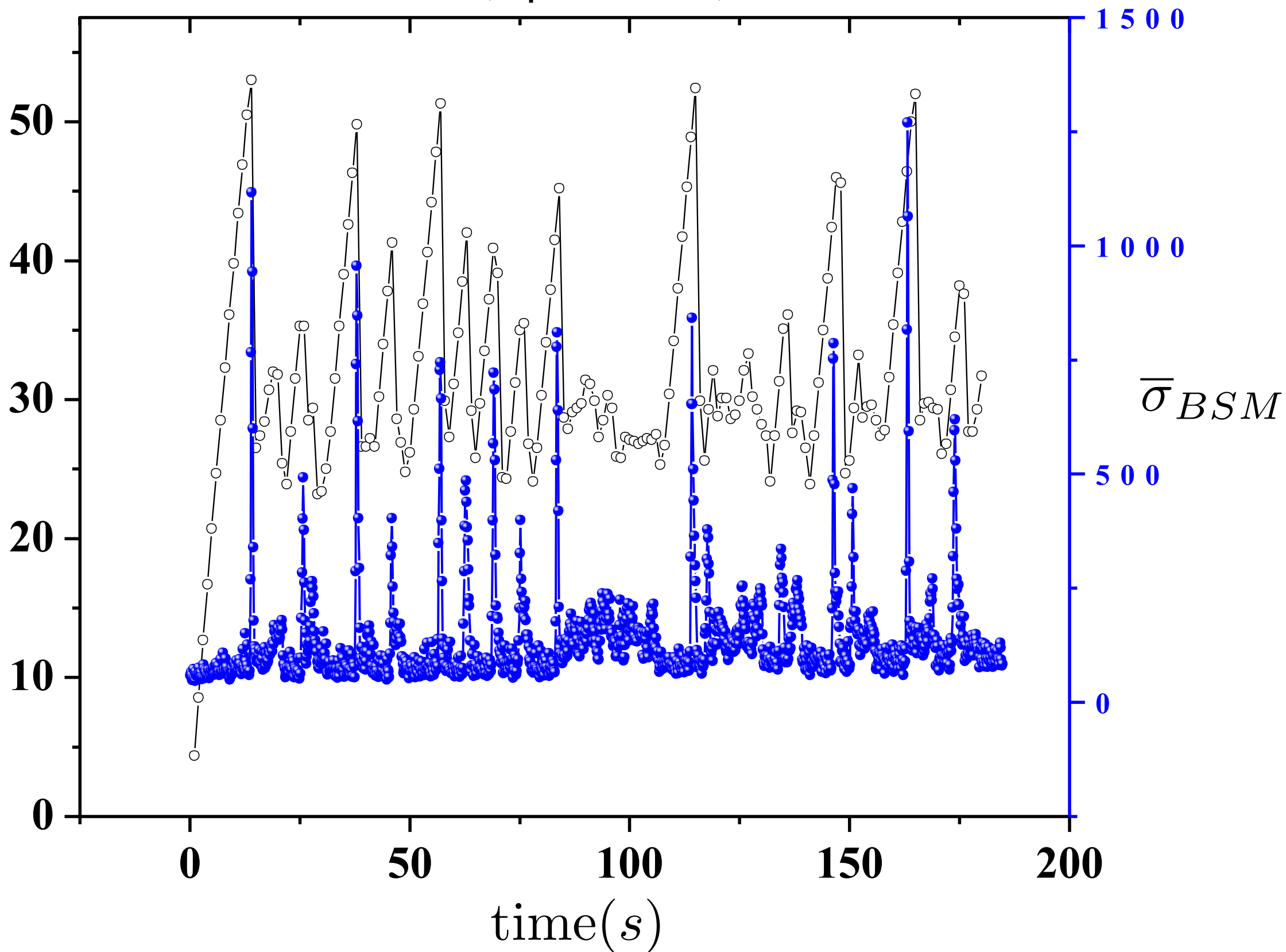


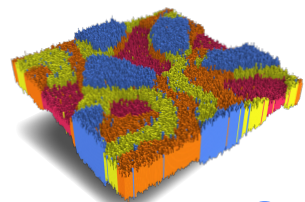
# Local and Global Fluctuations

$\tau = 200 \text{ Pa}$ ,  $\phi = 0.56$ , PP 5.2



$\dot{\gamma}$





# Conclusions



- Shear Thickening — frictional / dilatant
- Phase separation process — low/high viscosity
- Surface Stress Reveals Intermittency
- The Boundary Reveals New Rheology



# The Boundary is Cool

Thank You For Your Attention



- Blair-lab Members
  - **Vikram Rathee** (post-doc)
  - **Rich Arevalo** (grad student)
  - Pasha Tabatabai (now at Yale)
  - Kara Googins (grad student)



John  
Templeton  
Foundation