

# Driven quantum Hall models in photonic systems

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**ELECTRONICS**  
& **APPLIED PHYSICS**

Physics  
Frontier  
Center



Joint  
Quantum  
Institute

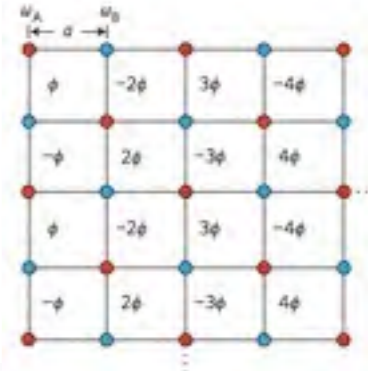
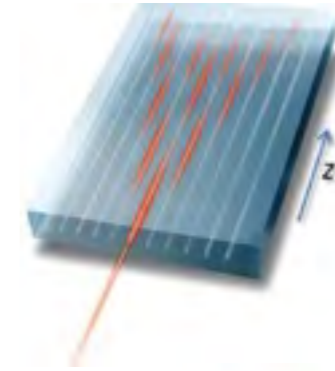
KITP, Synthetic Quantum Matter,  
Sept 2016

# Outline of this talk

- **Review of recent experiments on ring-resonators**  
S. Mittal, S. Ganeshan, J. Fan, A. Vaezi, *Nature Photonics* 10, 180 (2016)
- **Quantum transport of two-photons  
(non-classical input)**  
S. Mittal, V. Orre, and M.H., *Optics Express* 24, 15632 (2016)
- **Topological photonic crystals  
(towards strong photon-photon interaction)**  
S. Barik, H. Miyake, W. DeGottardi, E. Waks and M.H. [arXiv:1605.08822](https://arxiv.org/abs/1605.08822) (2016)
- **Effect of disorder on FQH of photons**

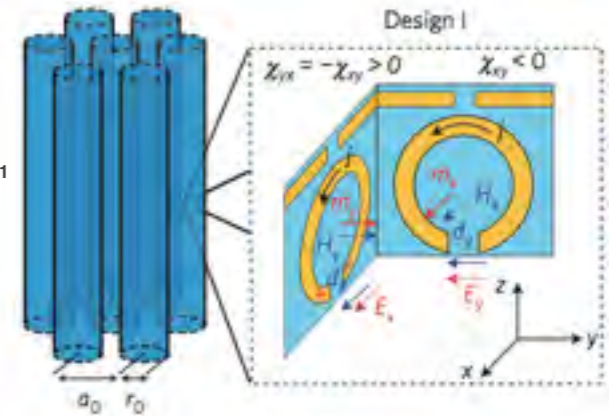
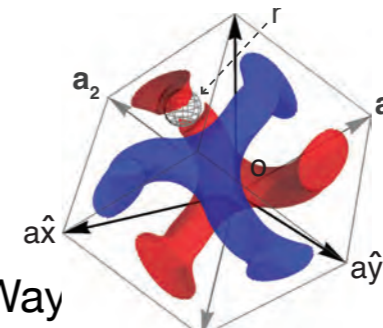
# Recent publications exploring topological properties of light

- Topological States and Adiabatic Pumping in Quasicrystals  
YE Kraus, Y Lahini, Z Ringel, M Verbin, O Zilberberg - *Physical Review Letters*, 2012



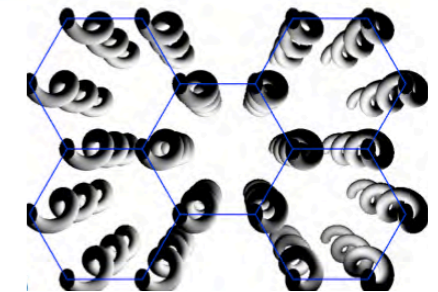
- Weyl points and line nodes in gapless gyroid photonic crystals  
L. Lu, L. Fu, J. Joannopoulos and M. Soljacic *Nature Photonics* 7, 294–299 (2013)

- Realizing effective magnetic field for photons by controlling the phase of dynamic modulation  
K Fang, Z Yu, S Fan - *Nature Photonics* (2012)



- Strain-induced pseudomagnetic field and Landau levels in photonic structures  
M Rechtsman, et al. - *Nature Photonics* (2012)

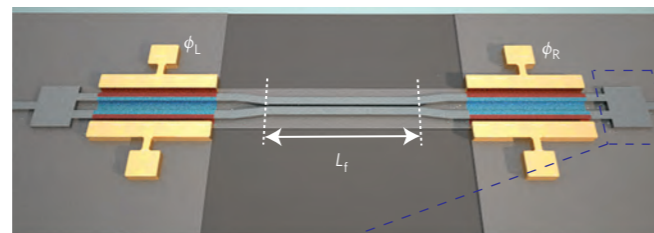
- Photonic Analogue of Two-dimensional Topological Insulators and Helical One-Way Transport in Bi-Anisotropic Metamaterial  
A. Khanikaev, S. Mousavi, W. Tse, M. Kargarian, A. MacDonald, G. Shvets, *Nature Material* (2012)



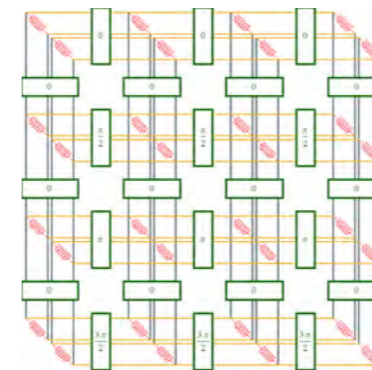
- Photonic Floquet Topological Insulators  
MC Rechtsman, et al. - *Nature* (2013)

- Optical Resonator Analog of a Two-Dimensional Topological Insulator, G. Jiang, Y. Chong *Physical Review Letters* (2013)

- Photonic topological insulator with broken time-reversal symmetry C. Hea, X. Suna, X. Liua,b, M. Lua, Y. Chenc, L. Fengd and Y. Chen *PNAS* (2016)



Lipson Nat. Photon. (2014)



Schuster  
Simon  
PRX (2014)

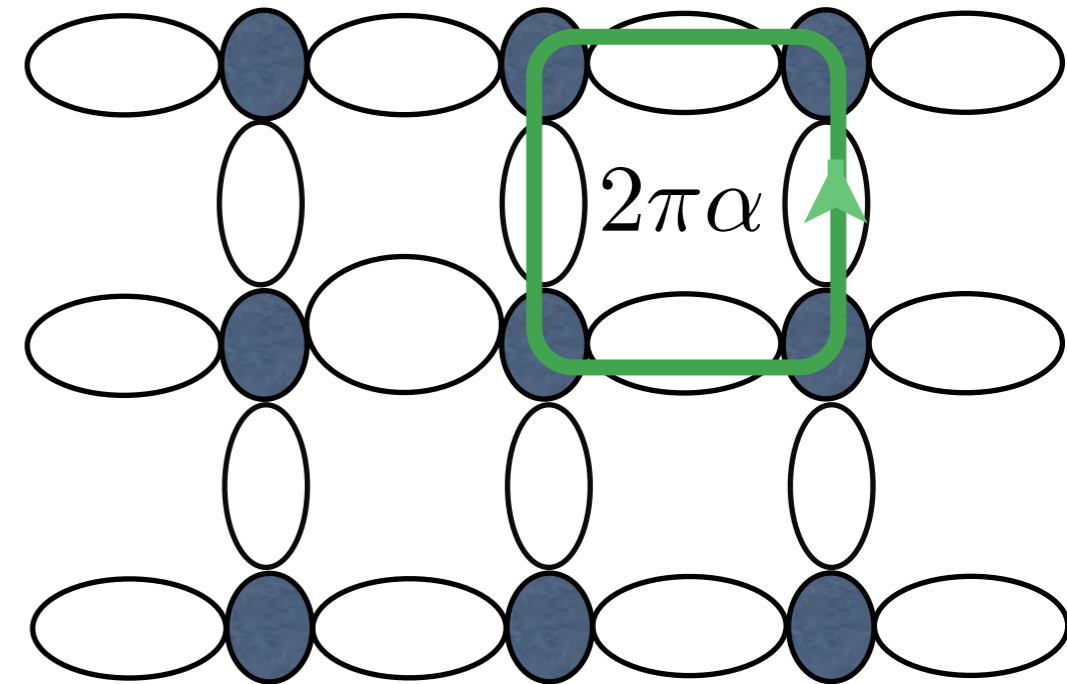
# Synthetic Magnetic Field

Magneto-optical effects are weak ✗  
 we need to synthesize magnetic field ✓

In analogy to electrons on a magnetic lattice:

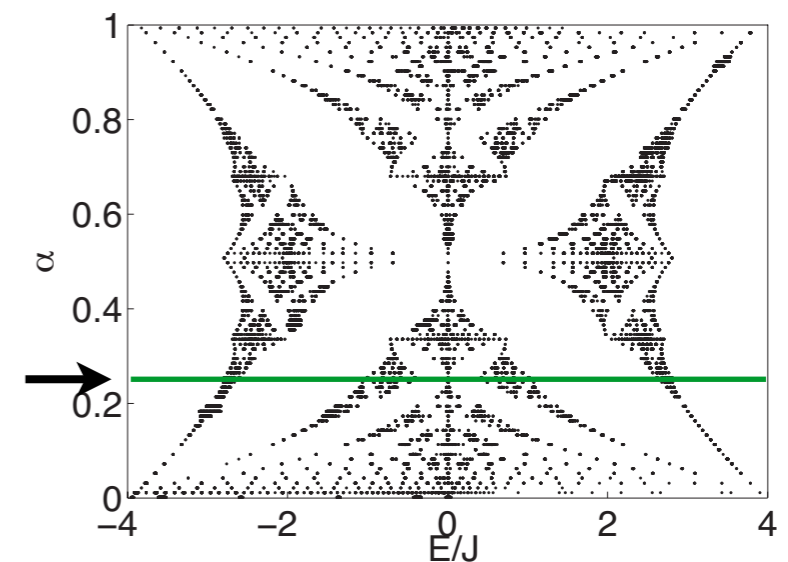
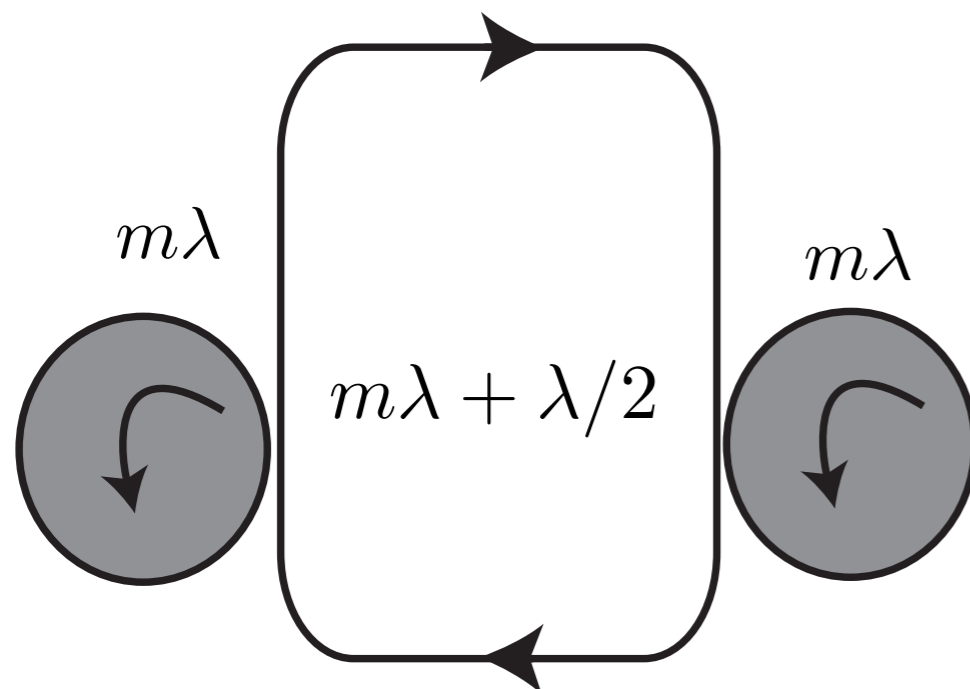
$$H_0 = -J \sum_{x,y} \hat{a}_{x+1,y}^\dagger \hat{a}_{x,y} e^{-i2\pi\alpha y} + \hat{a}_{x,y}^\dagger \hat{a}_{x+1,y} e^{i2\pi\alpha y} \\ + \hat{a}_{x,y+1}^\dagger \hat{a}_{x,y} + \hat{a}_{x,y}^\dagger \hat{a}_{x,y+1}$$

- Tight-binding form
- Magnetic phase



$$H_{eff} = -\kappa \hat{a}_{x+1}^\dagger \hat{a}_x e^{-2\pi i \alpha} - \kappa \hat{a}_x^\dagger \hat{a}_{x+1} e^{2\pi i \alpha}$$

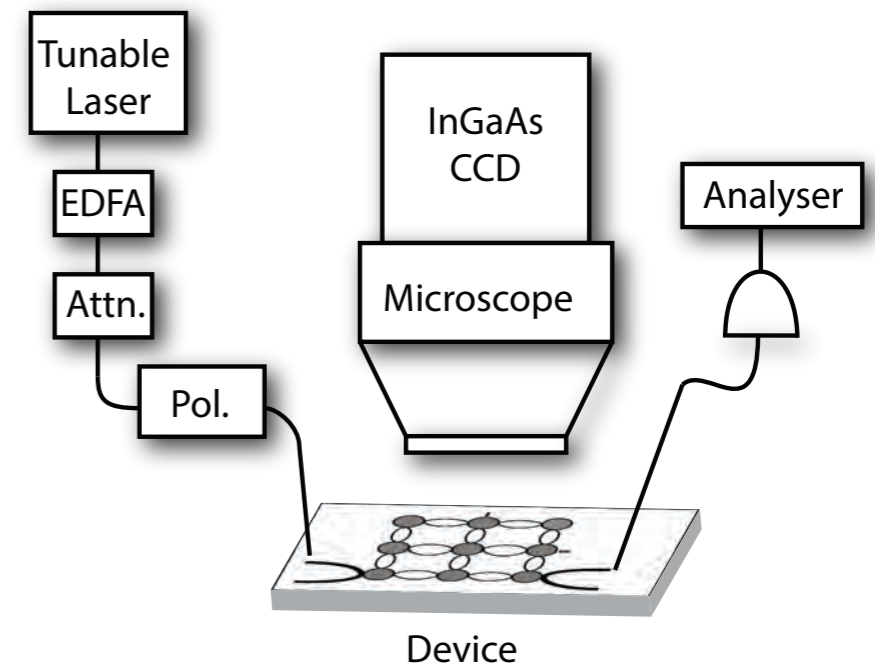
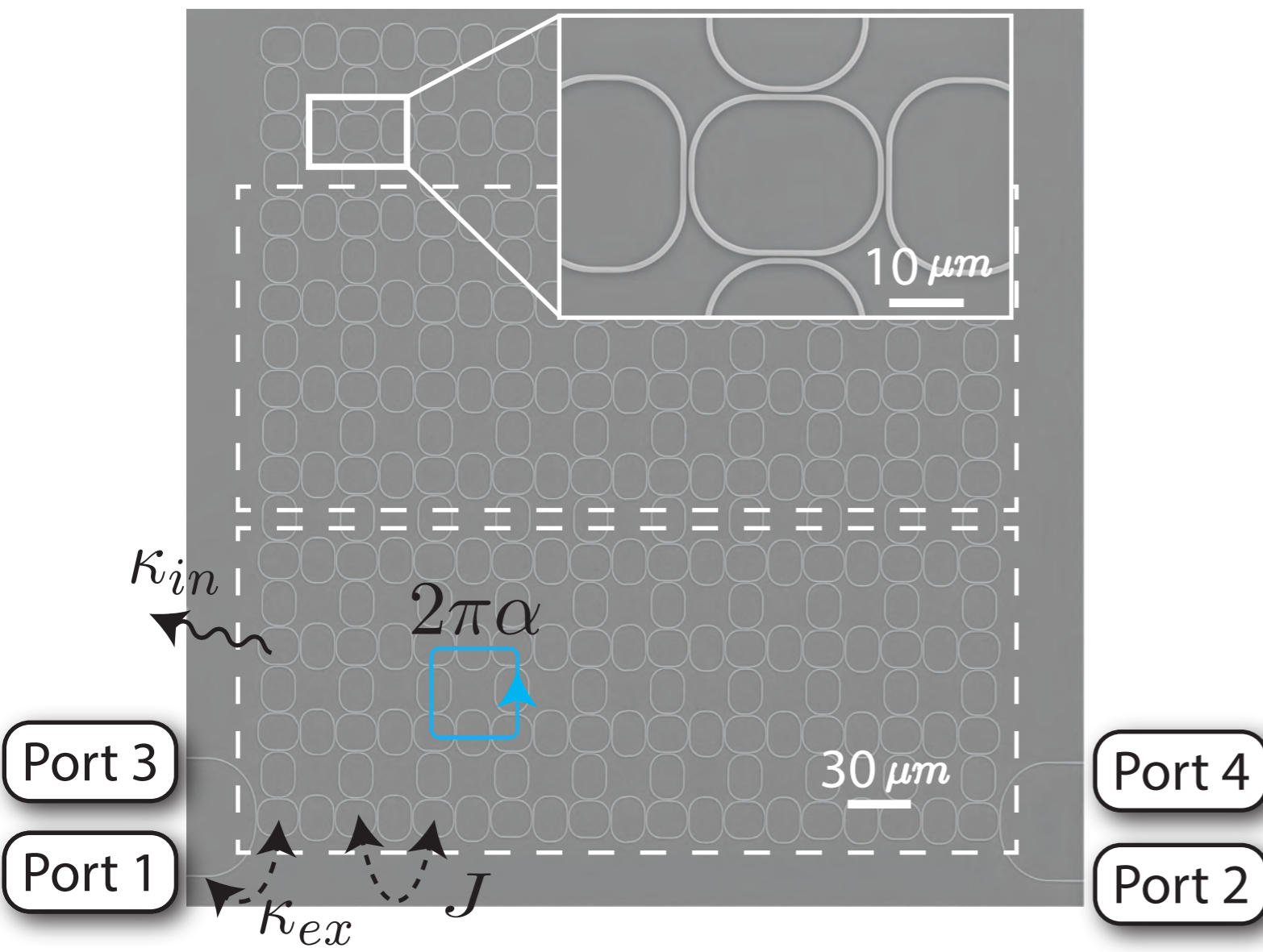
## Two resonator case:



MH, Demler, Lukin, Taylor Nat. Phys. 7, 907 (2011)  
 see also Microwave : Haldane, Raghu PRL (2008),  
 Soljagic's group Nature (2009) Carusotto's group PRA (2011)

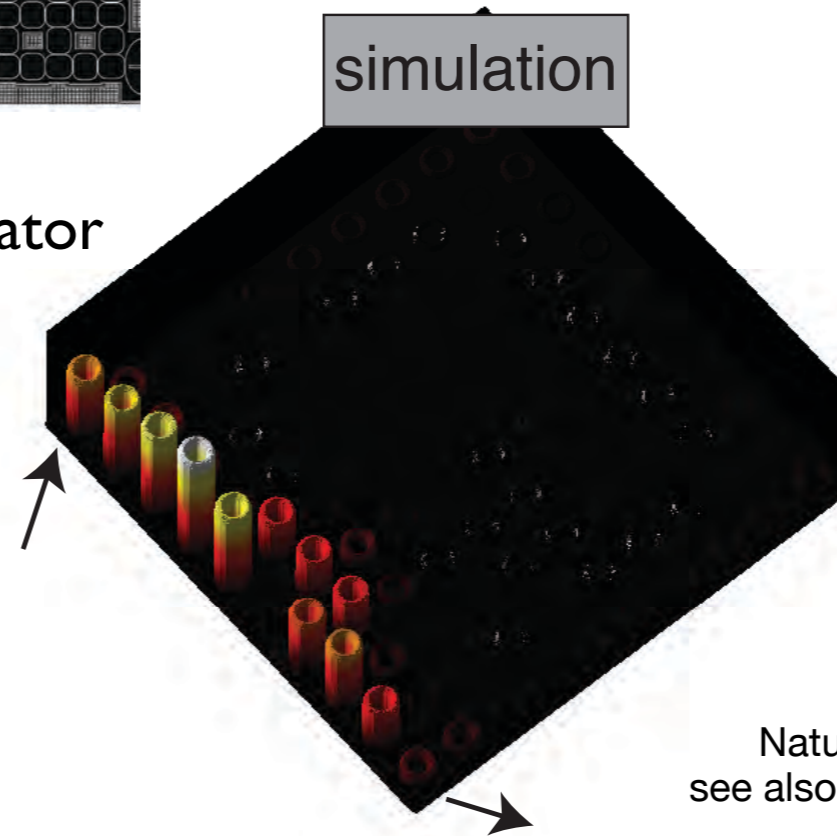
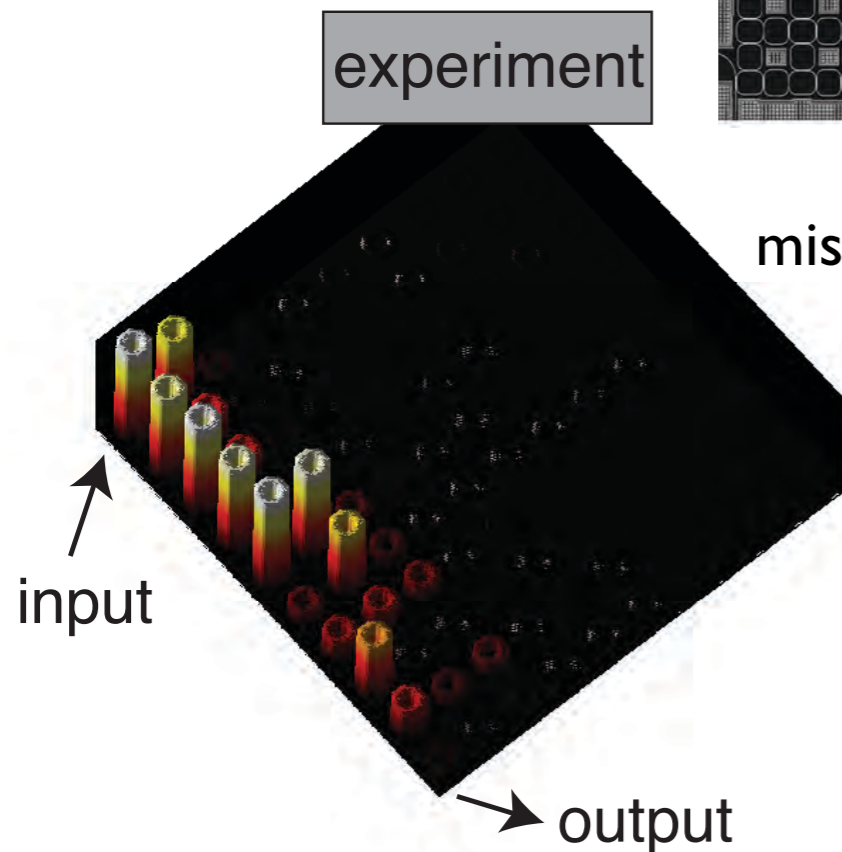
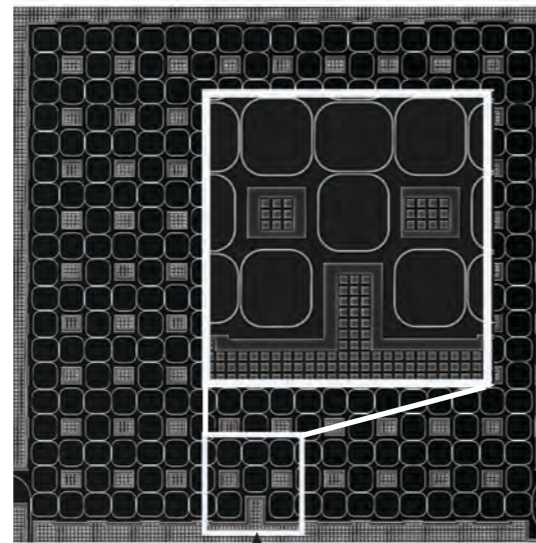
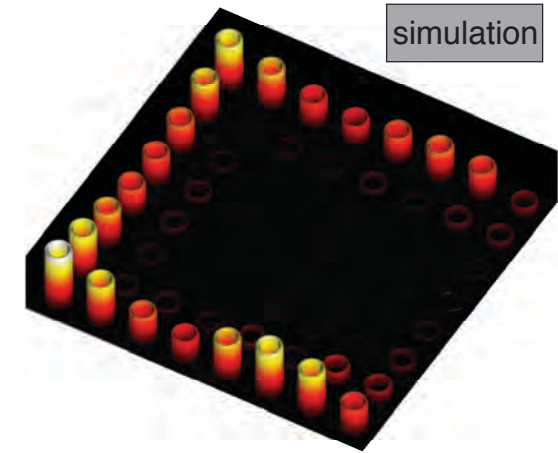
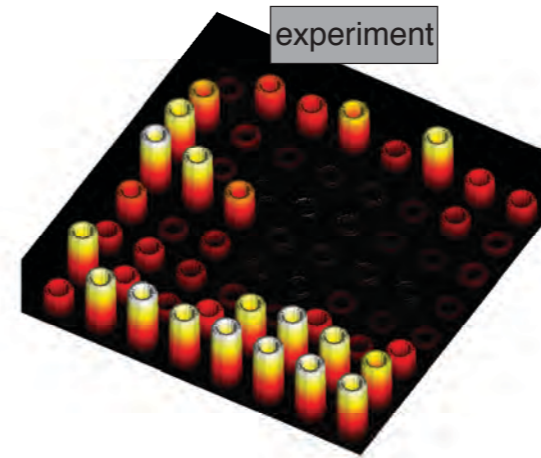
# Experimental realization of the gauge field

Silicon-on-Insulator technology

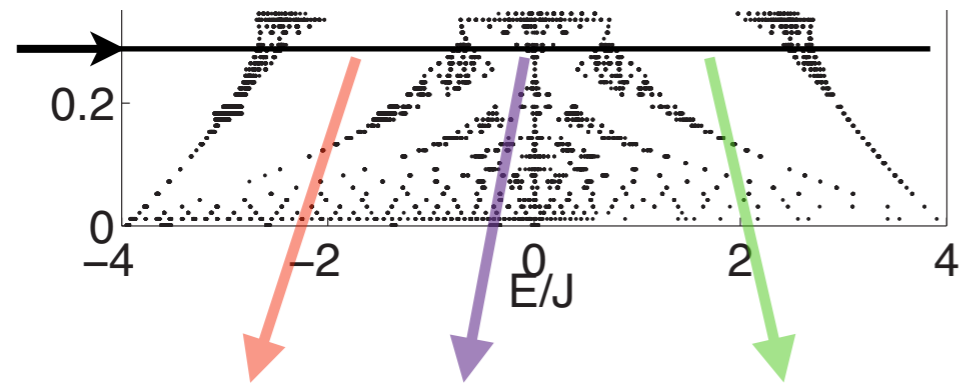


# Robustness disorder

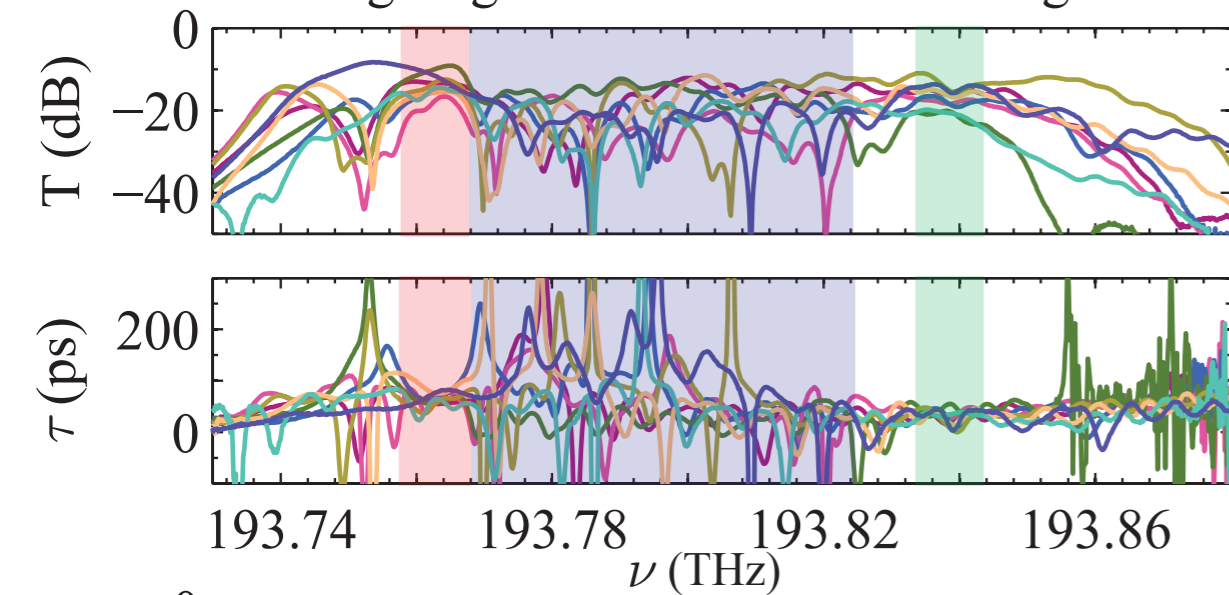
- ✓ Topological edge state when the system is excited in the bulk band gap
- ✓ Robustness against intrinsic and extrinsic disorders



# Transport statistics

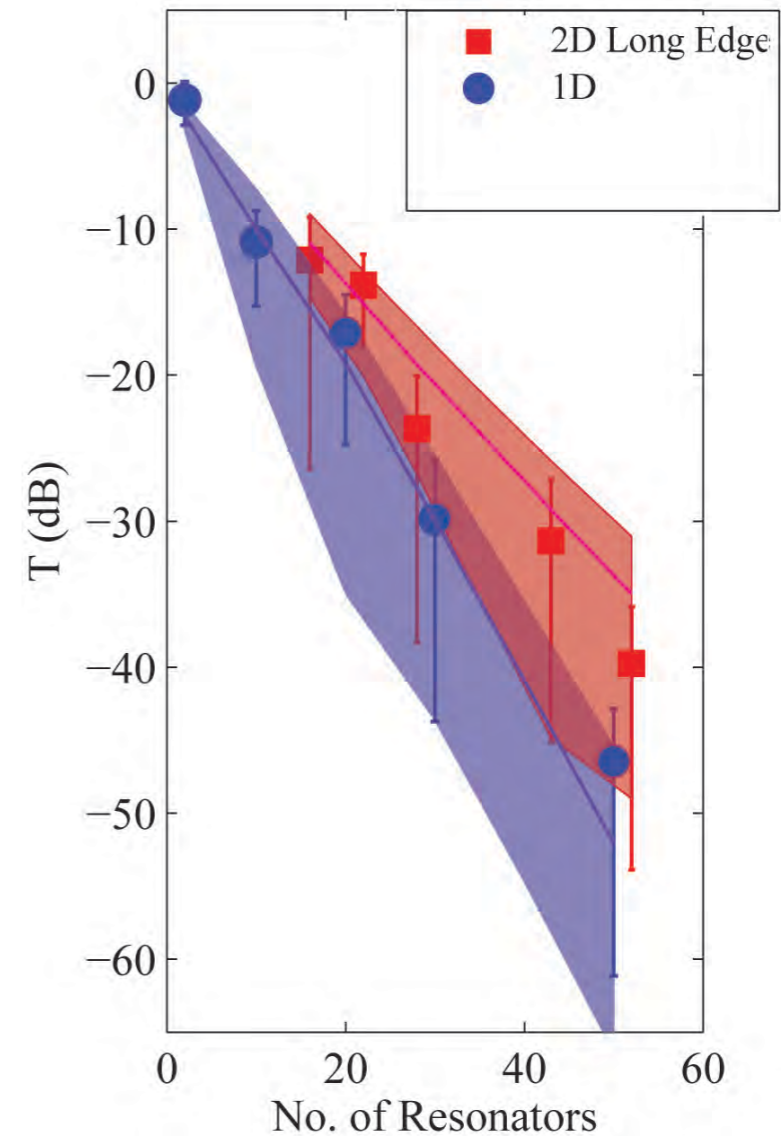


Long Edge      Bulk      Short Edge



15x15 arrays

Different colors: different samples



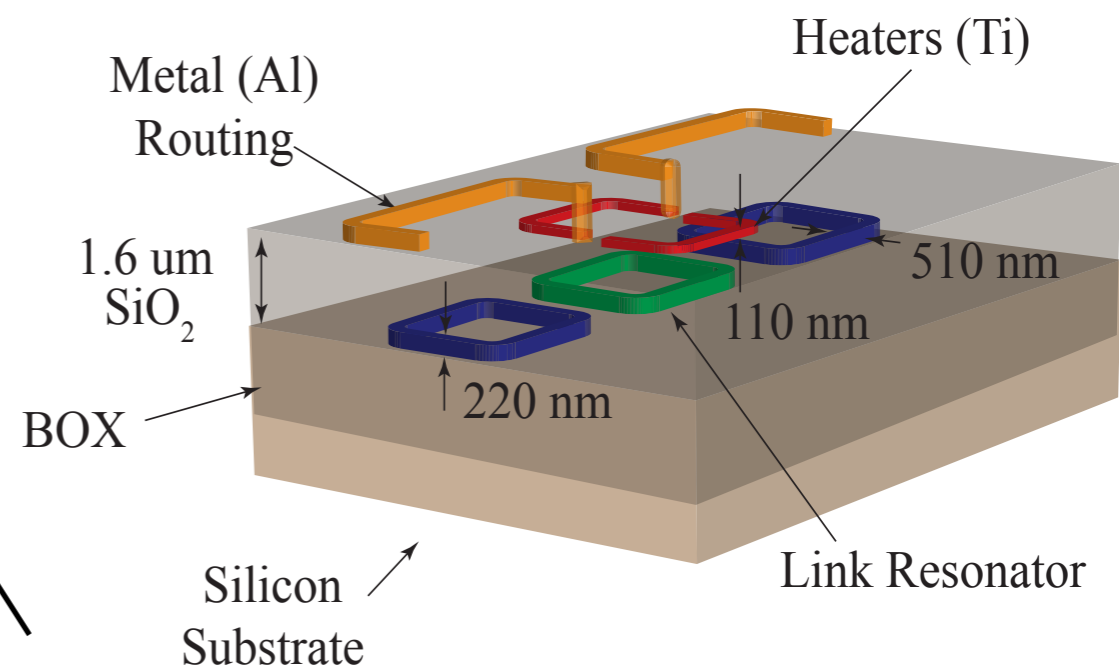
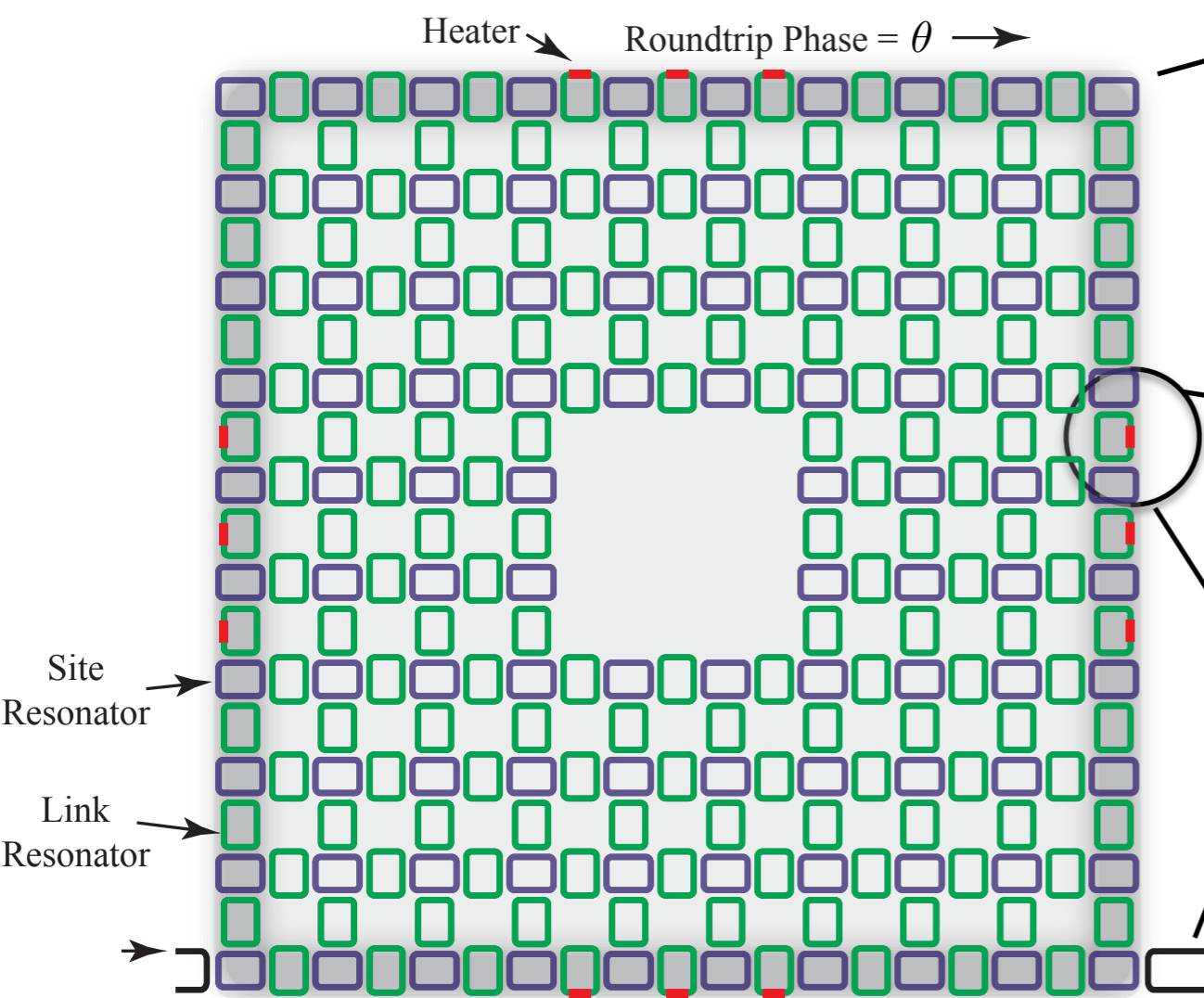
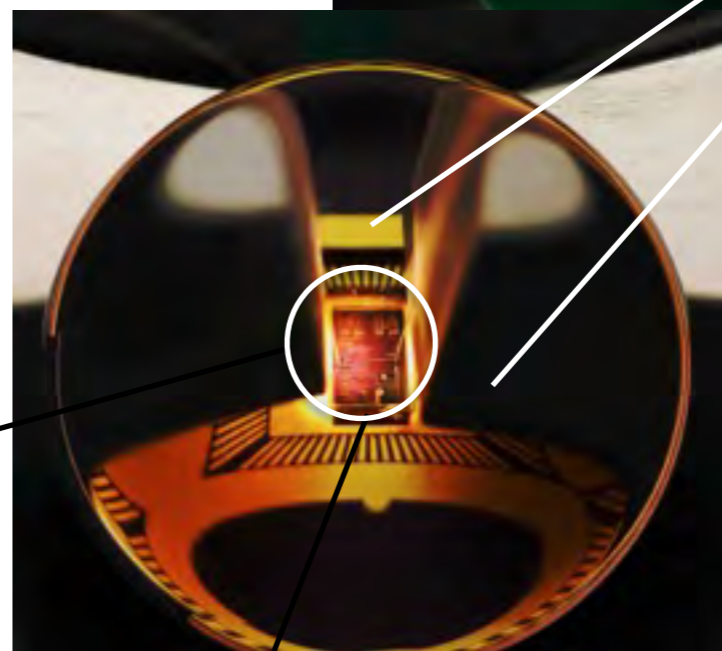
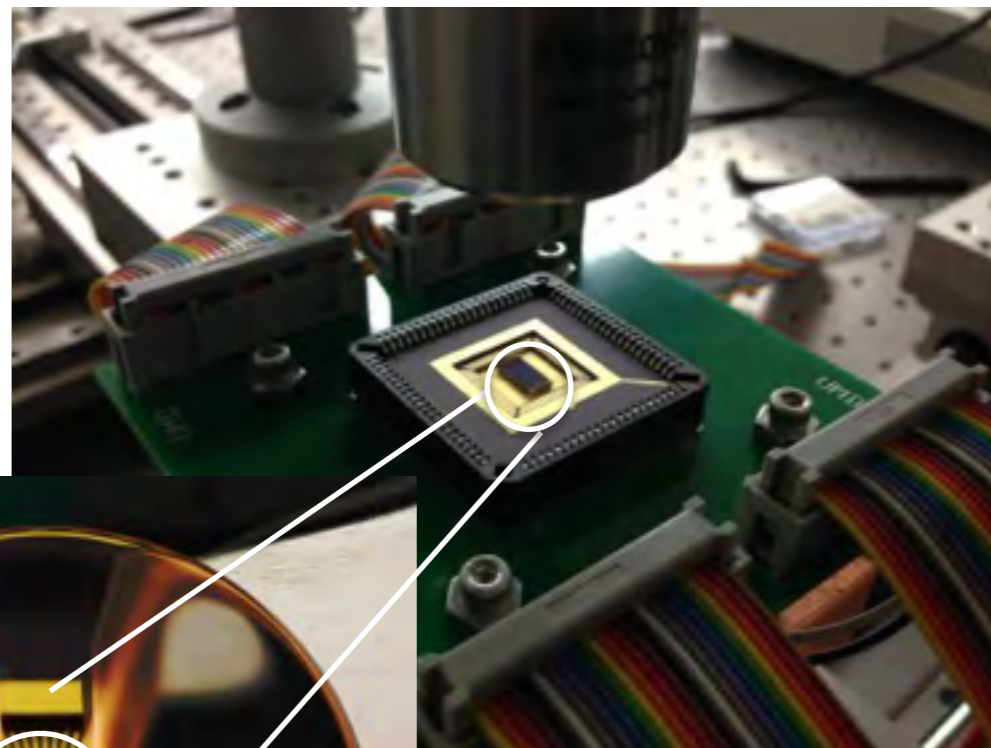
S. Mittal et al.  
Phys. Rev. Lett. 113, 087403 (2014)

# Measuring integer topological invariants

Bulk-edge correspondence

Laughlin-Halperin's argument  
applied to photonic system ✓

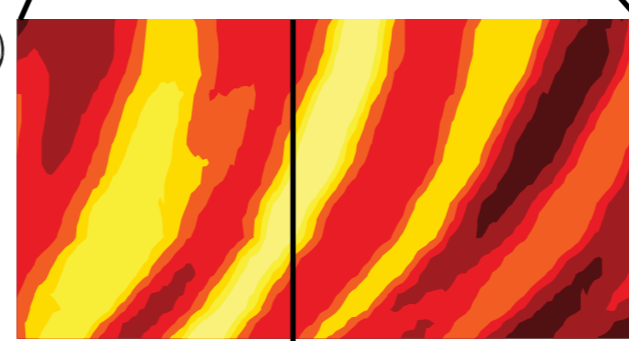
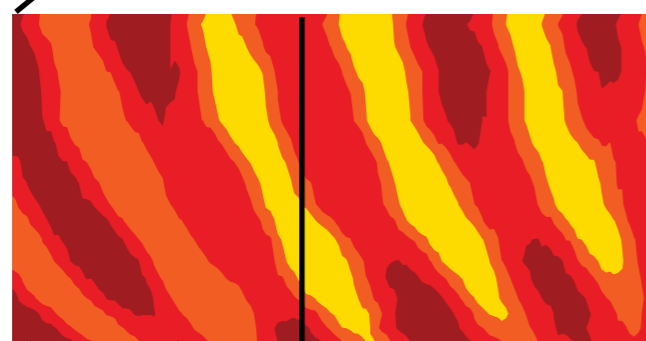
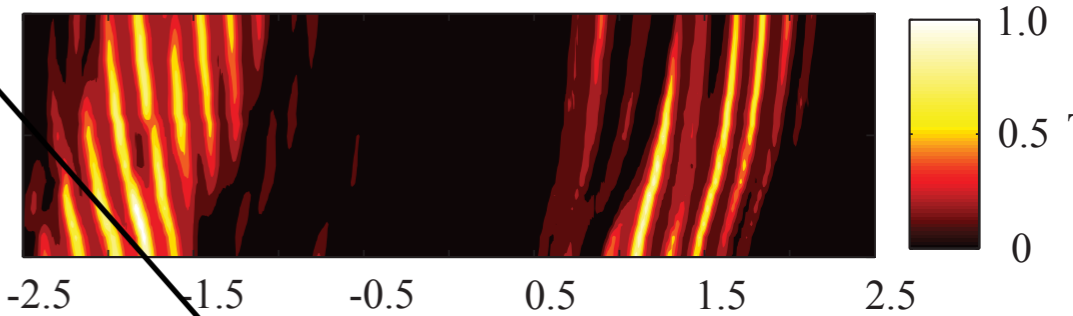
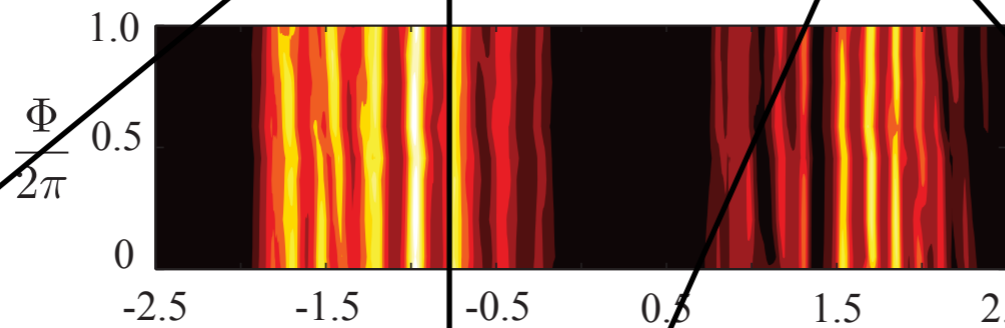
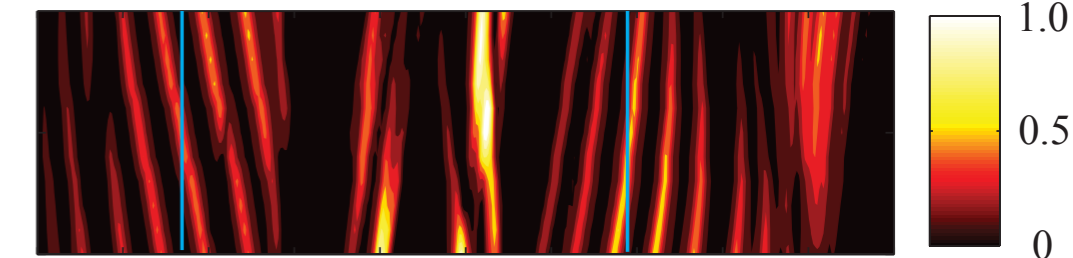
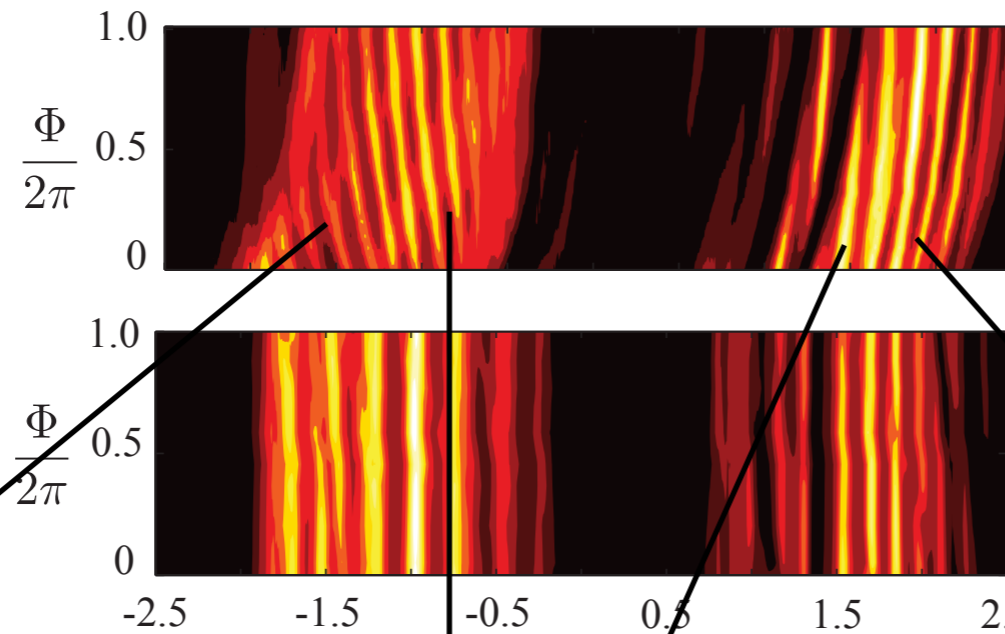
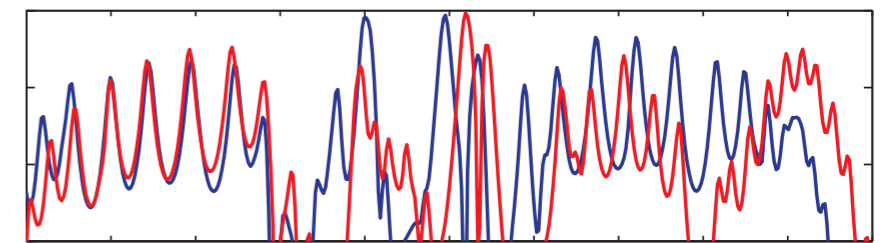
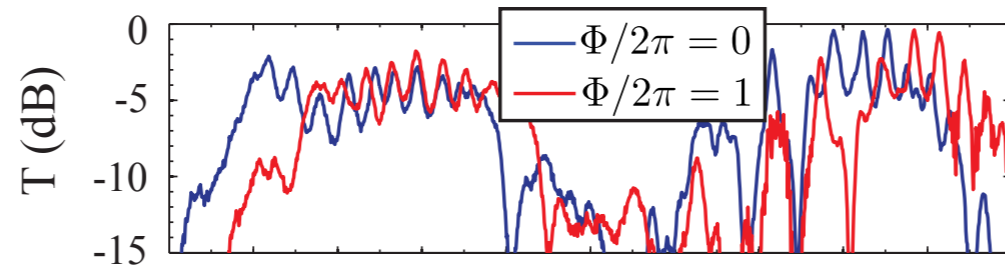
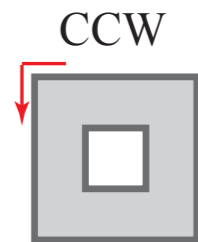
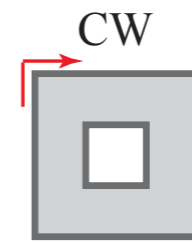
MH, PRL 112, 210405 (2014)





# Measured

# Simulated



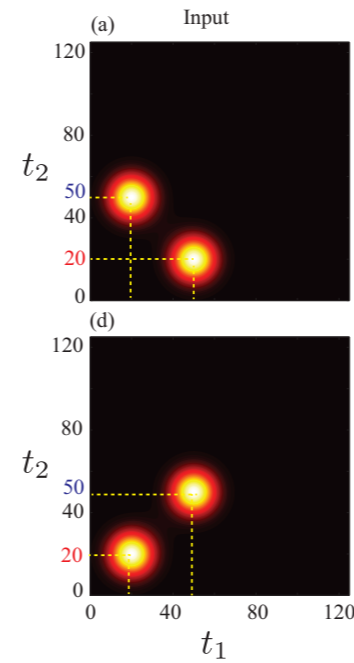
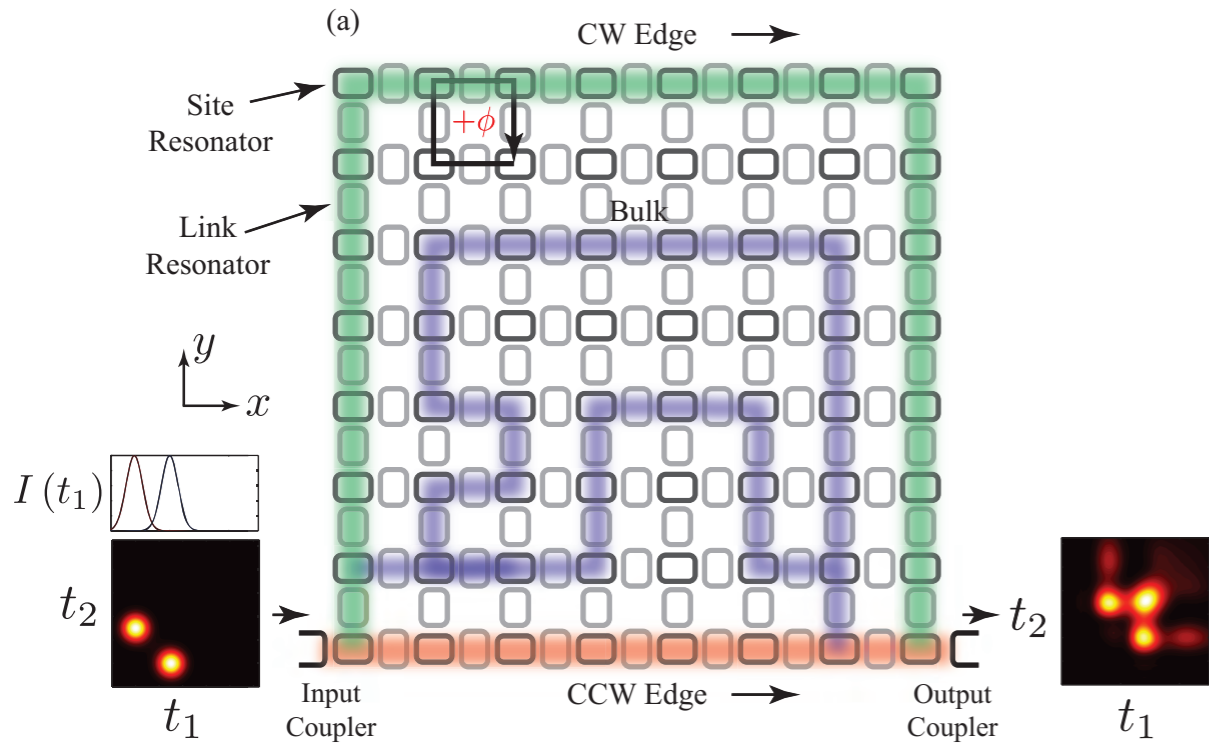
$k = +1.0(1)$

$k = -1.0(2)$

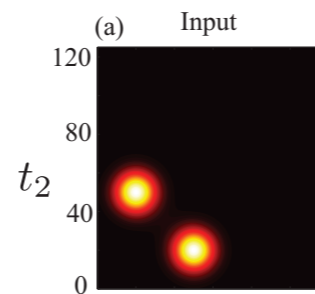
# Outline of this talk

- Review of recent experiments on ring-resonators
- **Quantum transport of two-photons  
(non-classical input)**  
S. Mittal, V. Vikram Orre, and M. H., OPTICS EXPRESS 24, 15632 (2016)
- Topological photonic crystals  
(strong photon-photon interaction)  
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- Effect of disorder on FQH of photons

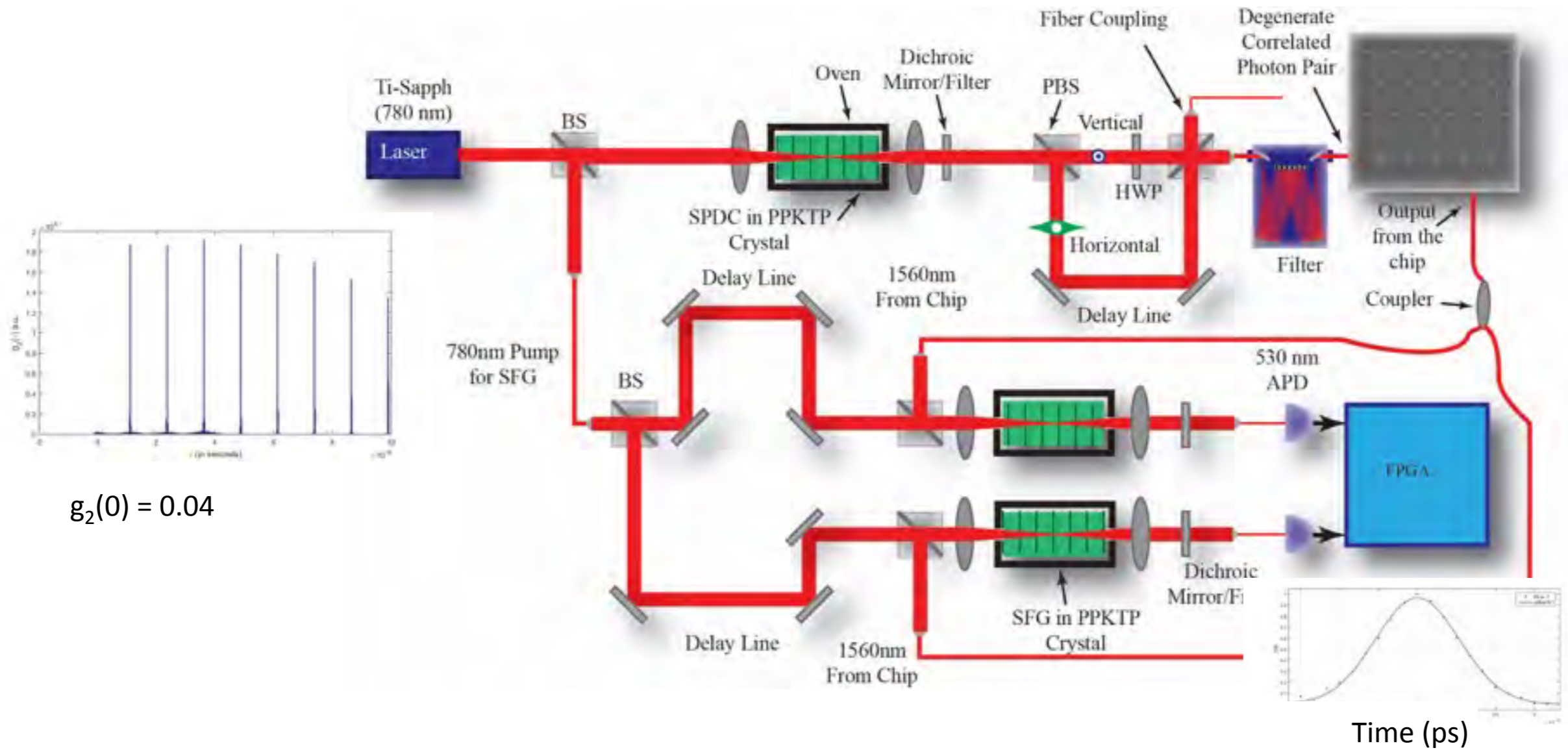
# Quantum transport in topological photonics systems



$$|2\rangle = \int dx_1 dx_2 \psi(x_1, x_2; t) \hat{a}^\dagger(x_1) \hat{a}^\dagger(x_2) |0\rangle$$



# Experiment using SPDC



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# Fractional Quantum Hall state of light

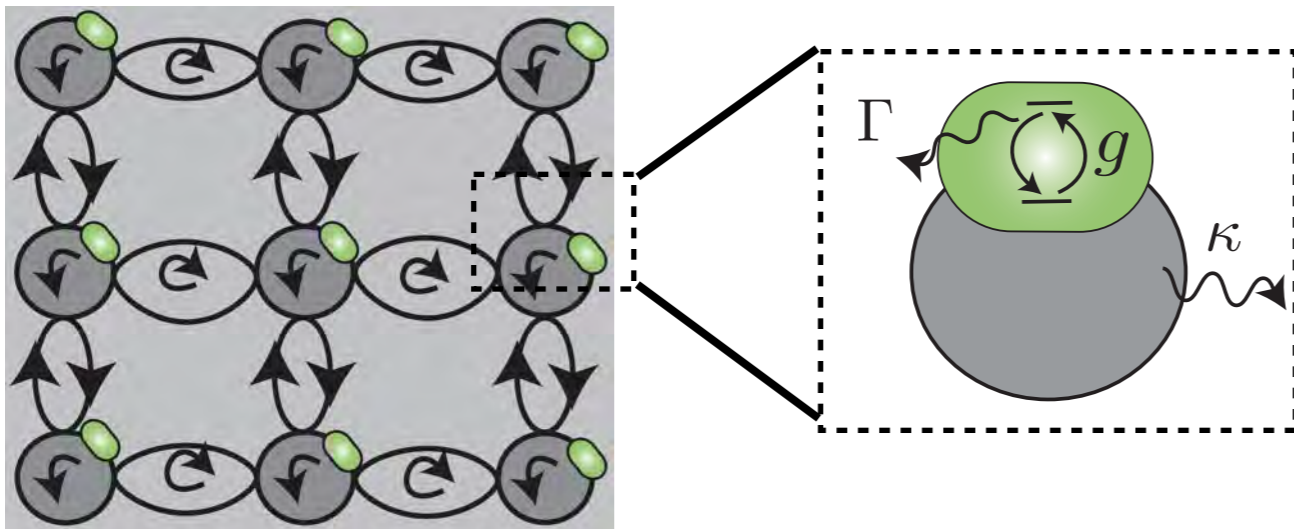
Gauge field

+

interaction



Fractional Quantum Hall states

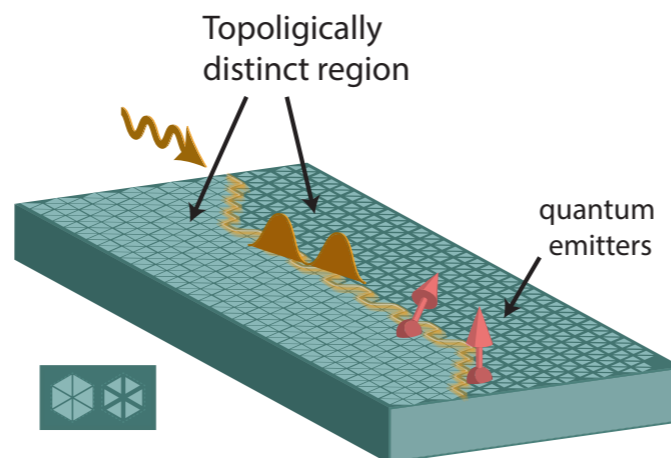
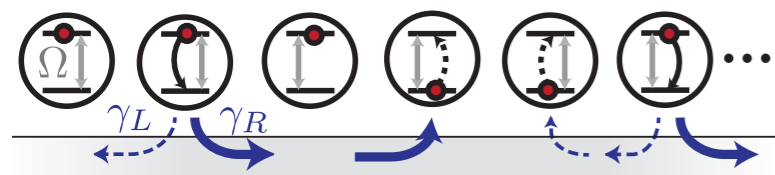


$$H = -J \sum_{x,y} \hat{a}_{x+1,y}^\dagger \hat{a}_{x,y} e^{i2\pi\alpha y} + \hat{a}_{x,y+1}^\dagger \hat{a}_{x,y} + h.c. + U \hat{n}_{x,y} (\hat{n}_{x,y} - 1)$$

$U \gg J$  : photon blockade regime

Angelakis PRL (2008), Carusotto PRL (2012) MH et al. NJP (2013)

## Chiral coupling



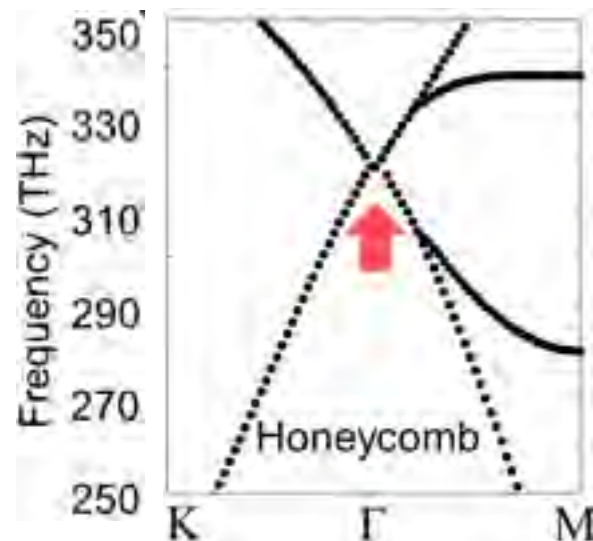
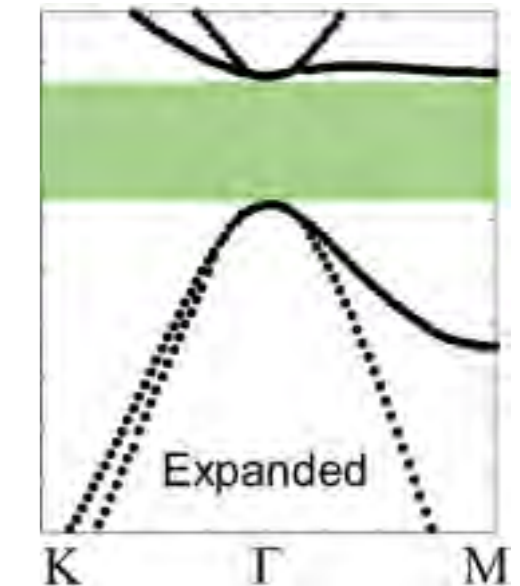
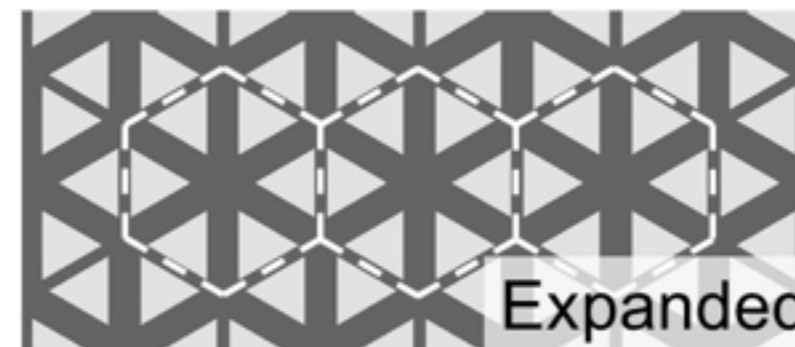
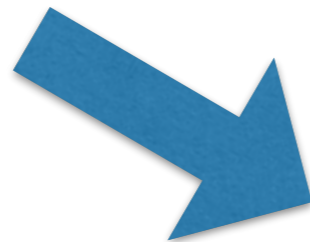
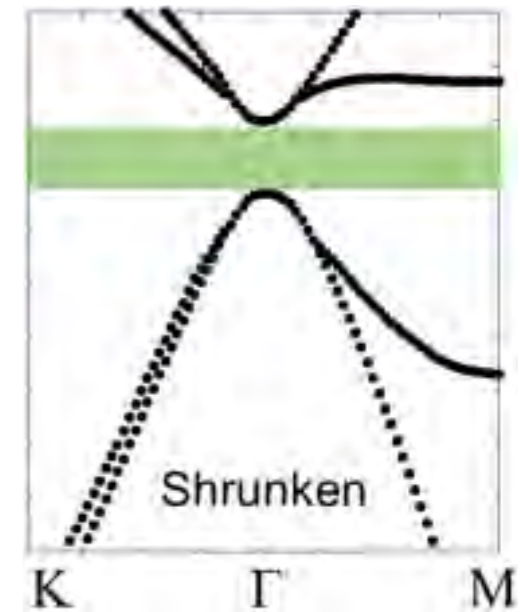
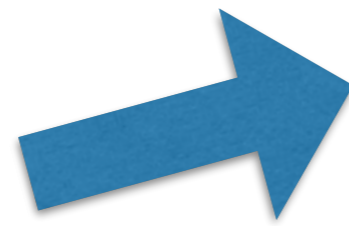
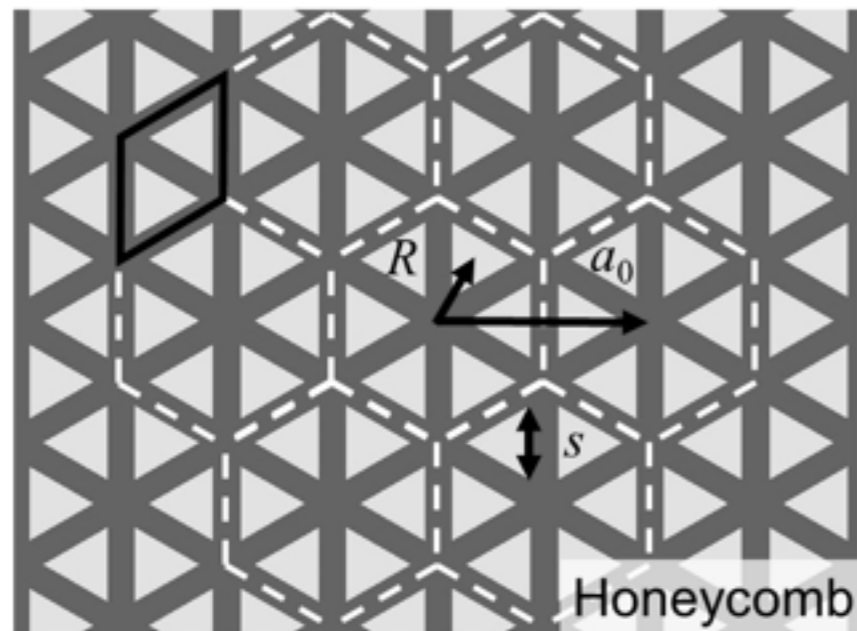
cf. P. Lodahl (Photonic crystal waveguides) and A. Rauschenbeutel (nanofiber)  
 H. Pichler, T. Ramos, A. Daley, P. Zoller PRA (2015)  
 earlier work on non-driven: Yudson, Pletyukhov, Gritsev

# Topological photonic crystals

- Synthesize spin-orbit in photonic crystals
- Find a compatible structure with solid-state emitters in **optical domain**

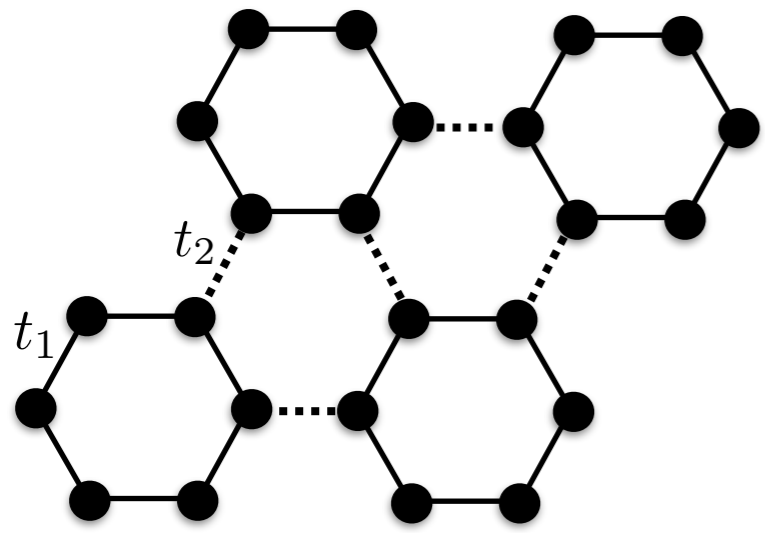
Challenges:

- ★ **Full bandgap** in the bulk
- ★ E&M should be **confined in prep. direction** to the slab

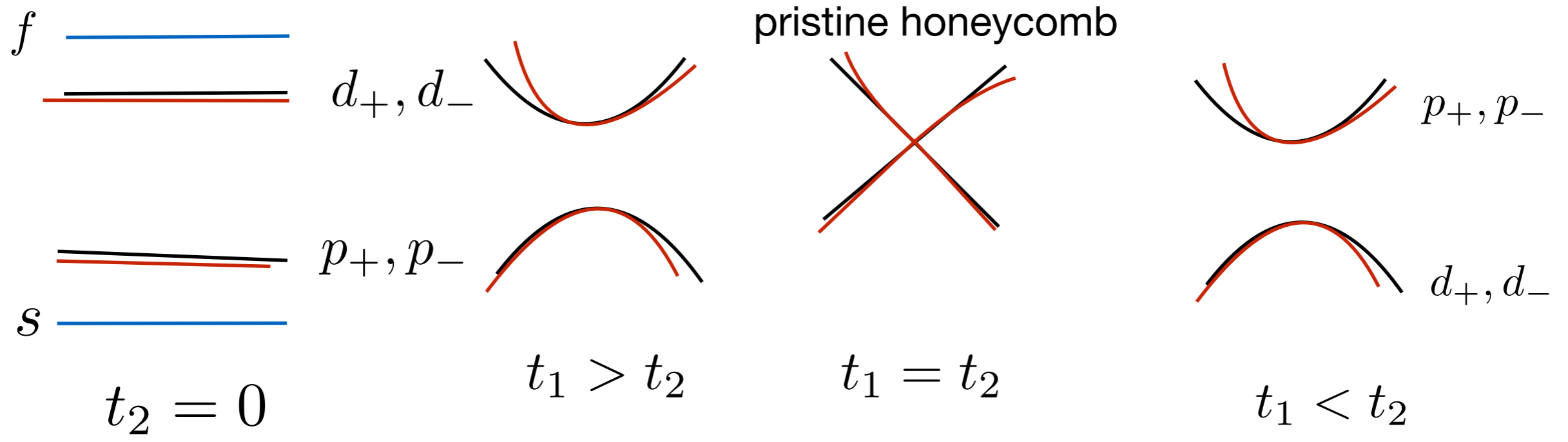
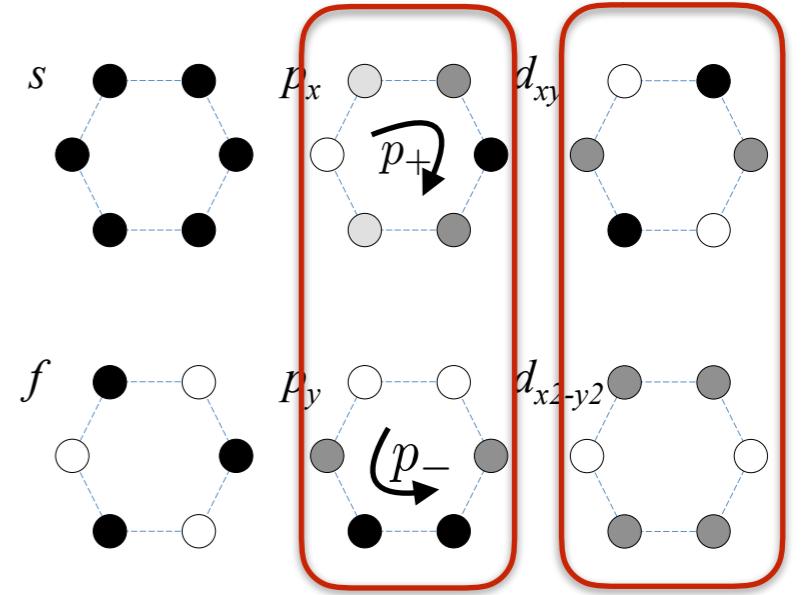


previous works: Rechtsman/Segev Nat. Photon (2012)  
Shvets/Khanikaev PRL (2014), Wu/Hu PRL (2015)

# Tight-binding approximation



$$t_1 \neq 0, t_2 = 0$$



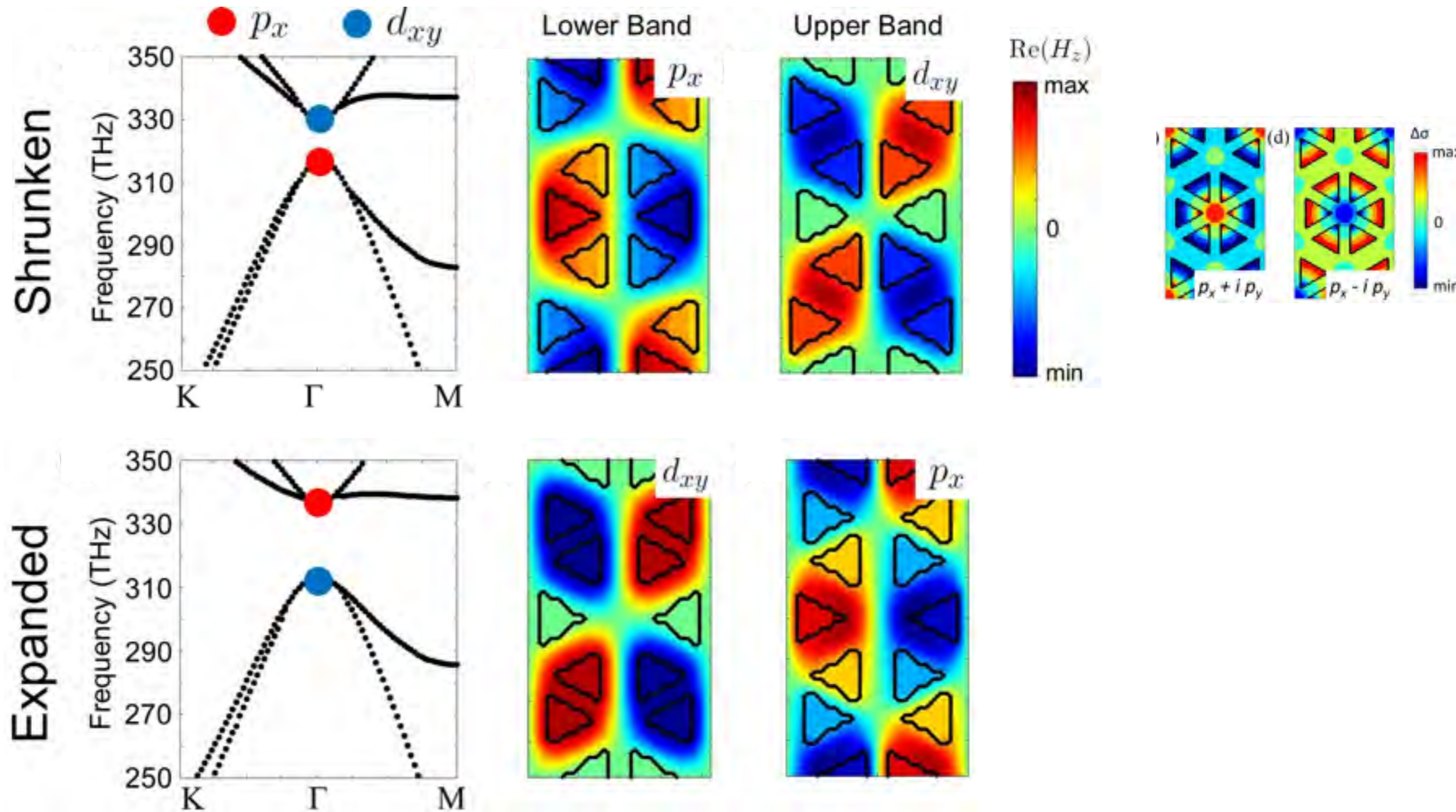
✓ Obtain band inversion, requirement for non-trivial topology

$$\mathcal{H}_+ = \frac{\sqrt{3}}{2} t_2 a (-k_x \sigma_x + k_y \sigma_y) + [t_2 - t_1 + \mathcal{O}(k_x^2 + k_y^2)] \sigma_z \quad (|p_+\rangle, |d_+\rangle)$$

$$\mathcal{H}_- = \frac{\sqrt{3}}{2} t_2 a (k_x \sigma_x + k_y \sigma_y) + [t_2 - t_1 + \mathcal{O}(k_x^2 + k_y^2)] \sigma_z \quad (|p_-\rangle, |d_-\rangle)$$



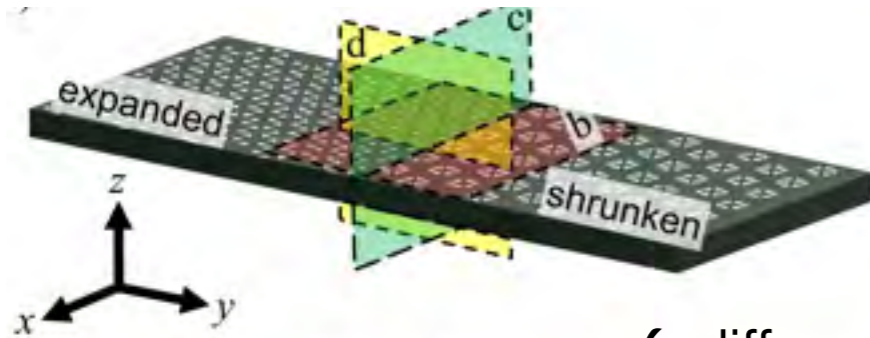
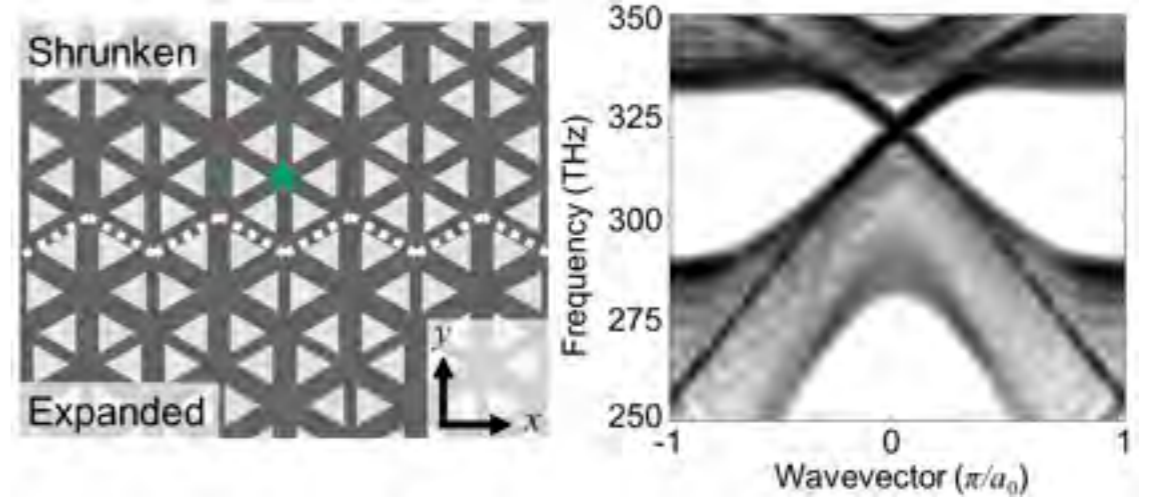
# Band inversion: numerical simulation



- ✓ Bulk/edge correspondence: We expect topological edge states to appear at the interface between expanded/shrunken system

# helical/chiral topological edge states

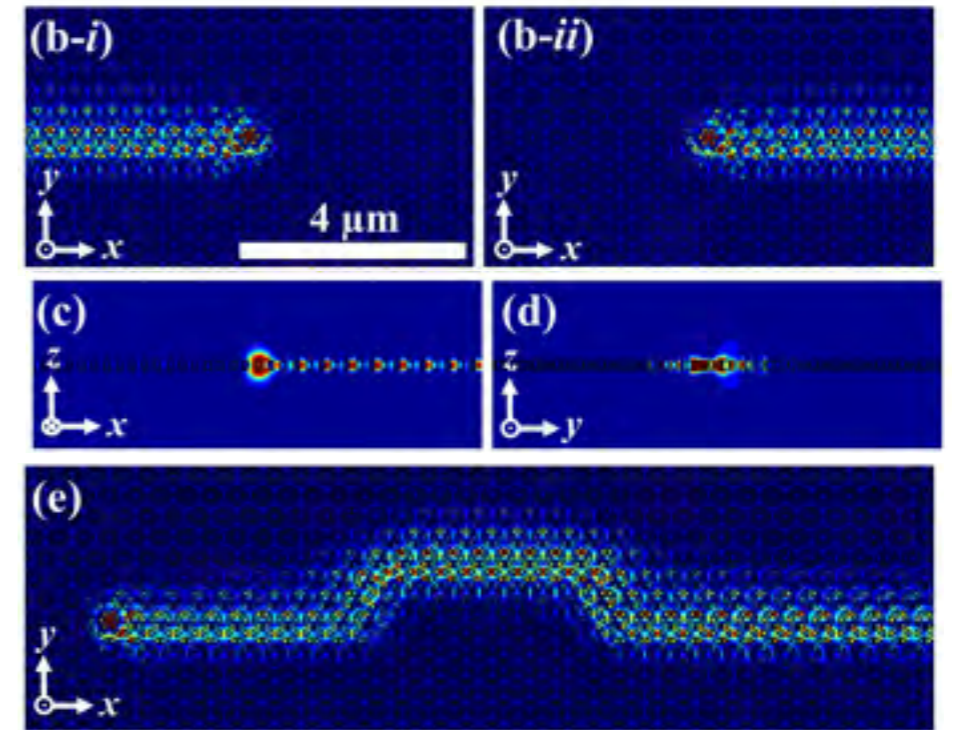
- ✓ Interface between two distinct band structure
- ✓ Topological edge state appear in the bulk gap
- ✓ 2D version/topological version of Lodahl/Rauschenbeutel



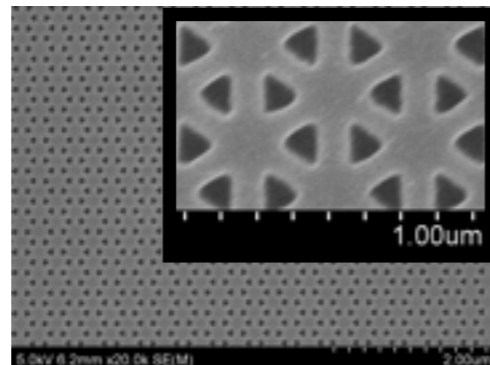
- ✓ different polarization propagate in different directions

- ✓ confinement in prep. direction

- ✓ robustness against deformation of edge



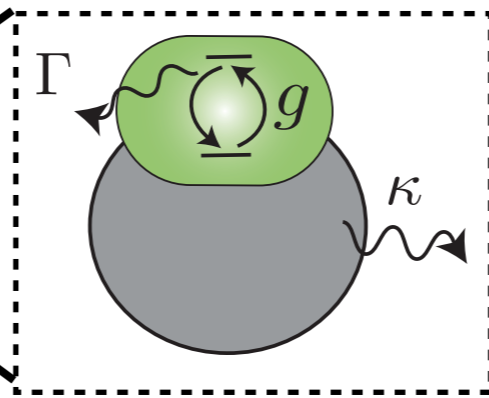
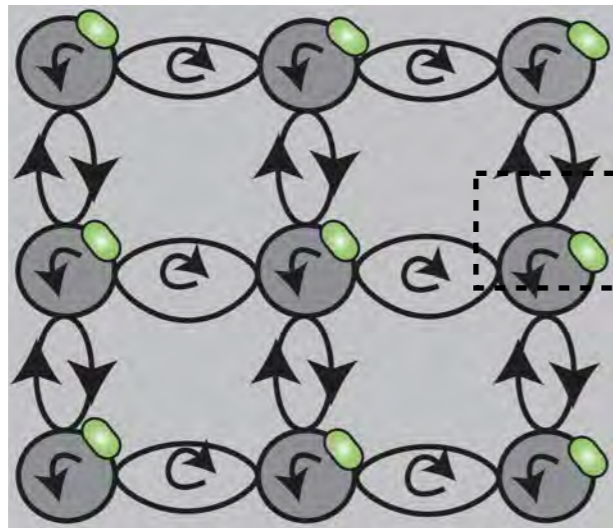
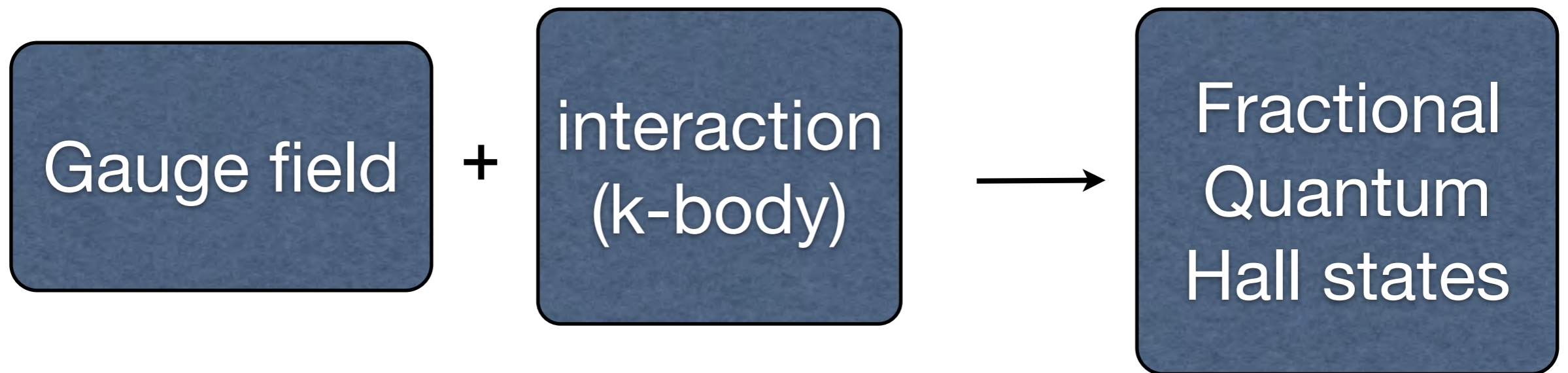
fabrication so far....



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$$H = -J \sum_{x,y} \hat{a}_{x+1,y}^\dagger \hat{a}_{x,y} e^{i2\pi\alpha y} + \hat{a}_{x,y+1}^\dagger \hat{a}_{x,y} + h.c. \\ + U \hat{n}_{x,y} (\hat{n}_{x,y} - 1)$$

$U \gg J$  : photon blockade regime

## Challenges:

- Weak interaction in the optical domain
- Photon loss
- lack of chemical potential
- lack of thermalization

- MH, J. Taylor, M. Lukin NJP (2013)
- E. Kapit, MH and S. Simon PRX (2014)
- MH, Adhikari, Taylor PRB (2015)
- M. Schiro, M. Bordyuh, B. Oztop, and H. Tureci PRL (2012)
- F. Grusdt et al. PRL (2014)
- ....

## Advantages:

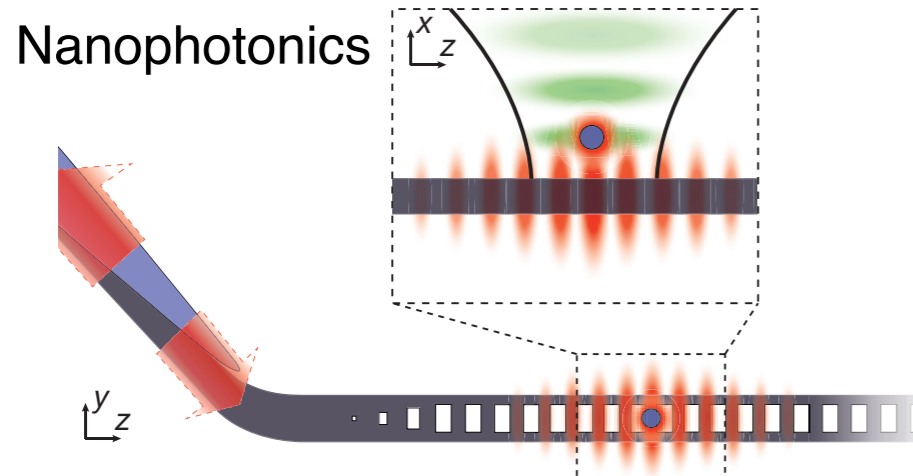
- Synthetic gauge field
- k-body interaction
- length scale
- correlation function measurement

- E. Kapit, S. Simon PRB (2013)
- MH, P. Adhikari, and J. Taylor PRB (2014)  
(three-body interaction and Pfaffian states)
- R. Umucalılar, I. Carusotto PLA (2013)
- .....

# Interaction between photons

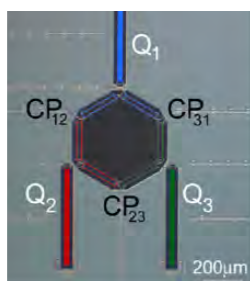
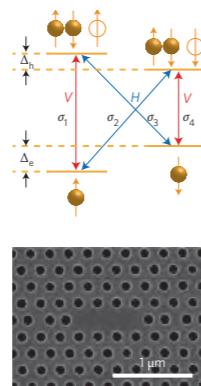
Some challenges:

- Strong photon-photon interaction
- Scalable implementation of various Hamiltonians



Tiecke, Thompson et al. Nature (2014)  
Harvard, Caltech

solid states emitters:  
Quantum dots, color centers in diamond

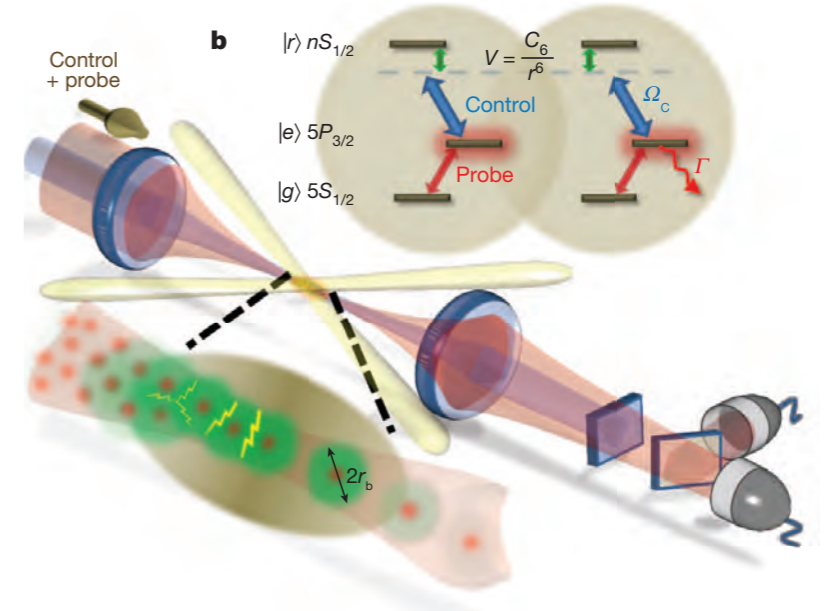


Three sites and synthetic gauge field

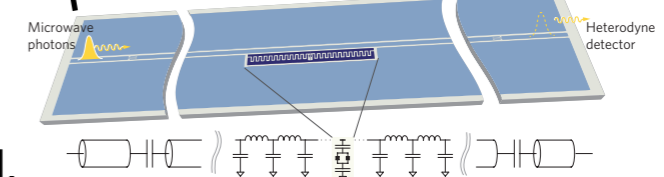
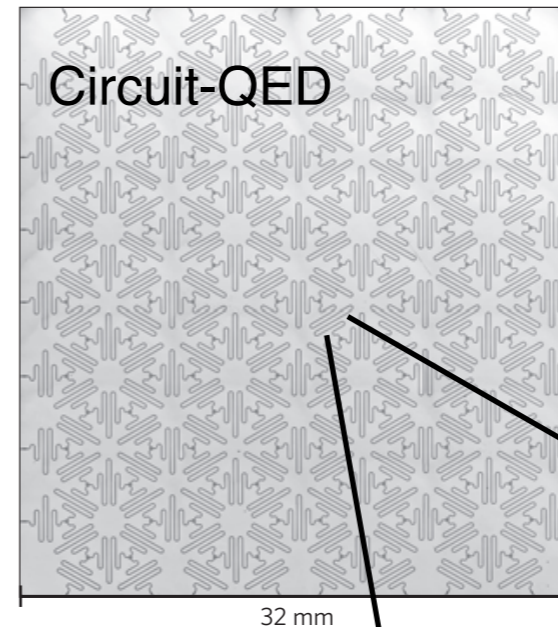
arXiv:1606.00077

Houck, Tureci, Koch (2012)  
Yale, Google, Princeton, JQI,  
Chicago, ....

## Rydberg polaritons



Peyronel et al. Nature (2012)  
Harvard-MIT, Stuttgart, Chicago, ....



# Fractional Quantum Hall state of light

$$H = -J \sum_{x,y} \hat{a}_{x+1,y}^\dagger \hat{a}_{x,y} e^{i2\pi\alpha y} + \hat{a}_{x,y+1}^\dagger \hat{a}_{x,y} + h.c. \\ + U \hat{n}_{x,y} (\hat{n}_{x,y} - 1)$$

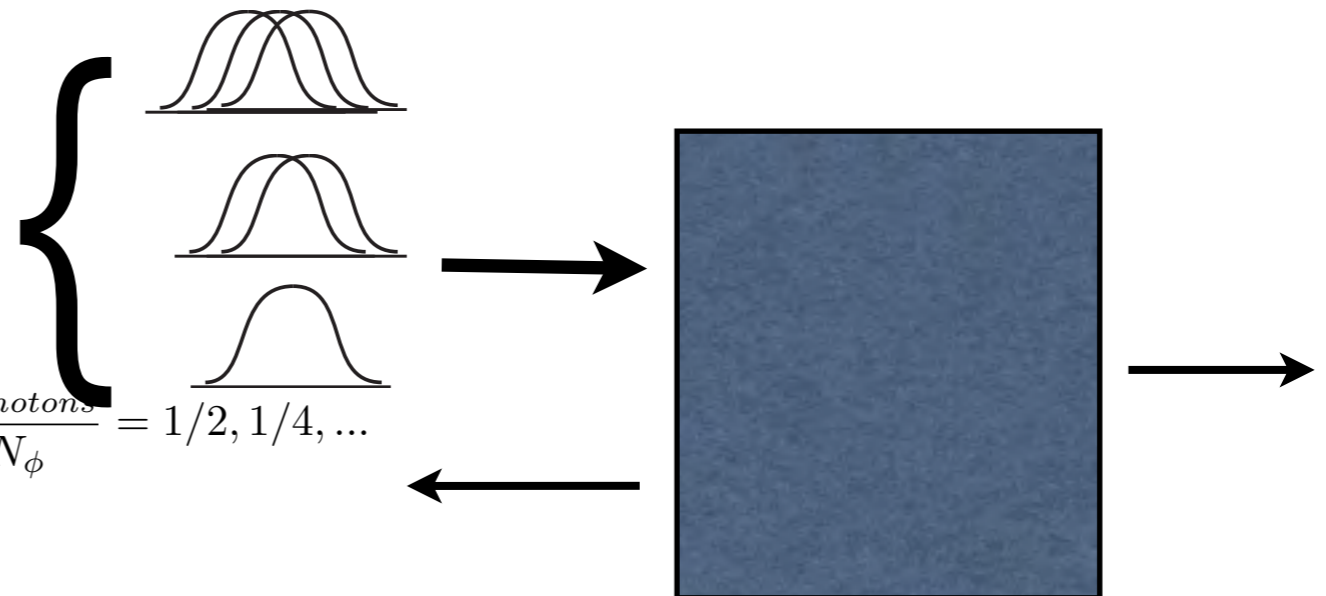
$U \gg J$  : photon blockade regime

Starting with a **fixed number of photons**,  
we can prepare a Laughlin state at  $\nu = \frac{N_{ph}}{N_{mag}} = \frac{1}{2}$

$$\Psi_m(z_1, z_2, \dots, z_N) \propto \prod_{j < k} (z_j - z_k)^m \prod_{j=1}^{N_e} e^{-|z_j|^2/4}$$

Driven by a coherent state:

$$|\beta\rangle = e^{-\frac{|\beta|^2}{2}} \sum_{n=0}^{\infty} \frac{\beta^n}{\sqrt{n!}} |n\rangle$$



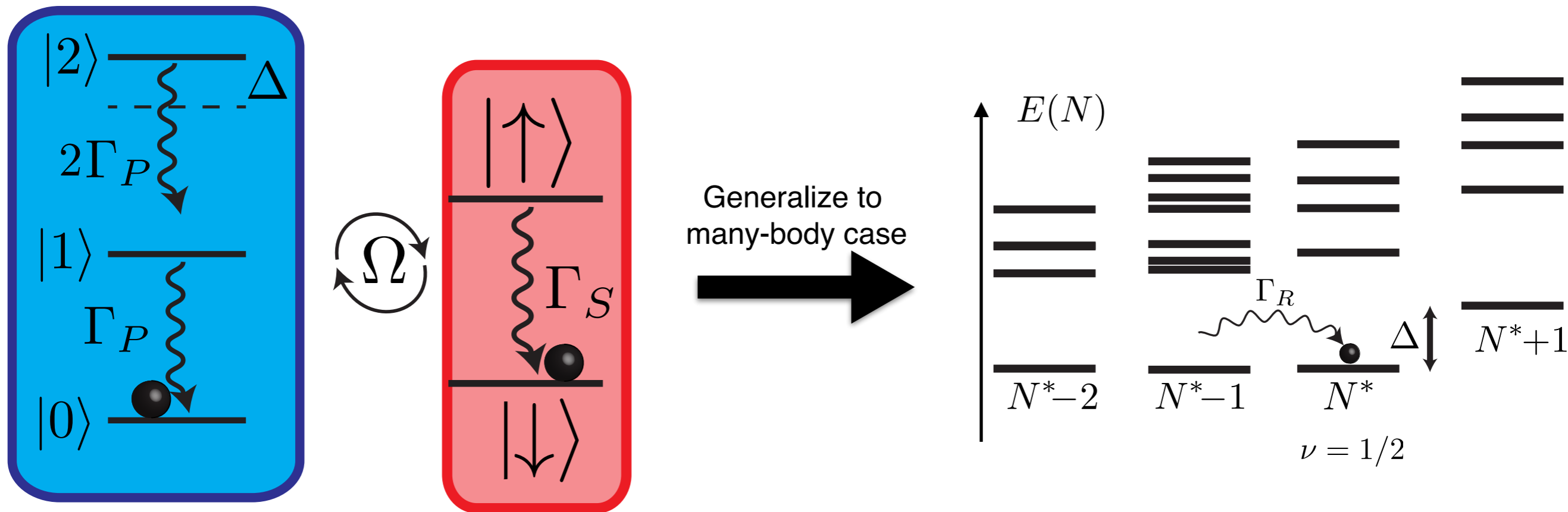
If the number of photons is such that  $\nu = \frac{N_{photons}}{N_\phi} = 1/2, 1/4, \dots$   
then photons reorganize themselves  
and form a “Laughlin state”

✓ Good for a few-photon states, can **not** be generalized to many-body

# Use incompressibility (blockade) to prepare many-body states of photons

$$E(N) - E(N - 1) \neq E(N + 1) - E(N)$$

How to prepare a cavity in the single photon state:



$$\Omega \cos(2\omega_0 t) \left[ a_P^\dagger \sigma_S^+ + a_P \sigma_S^- \right]$$

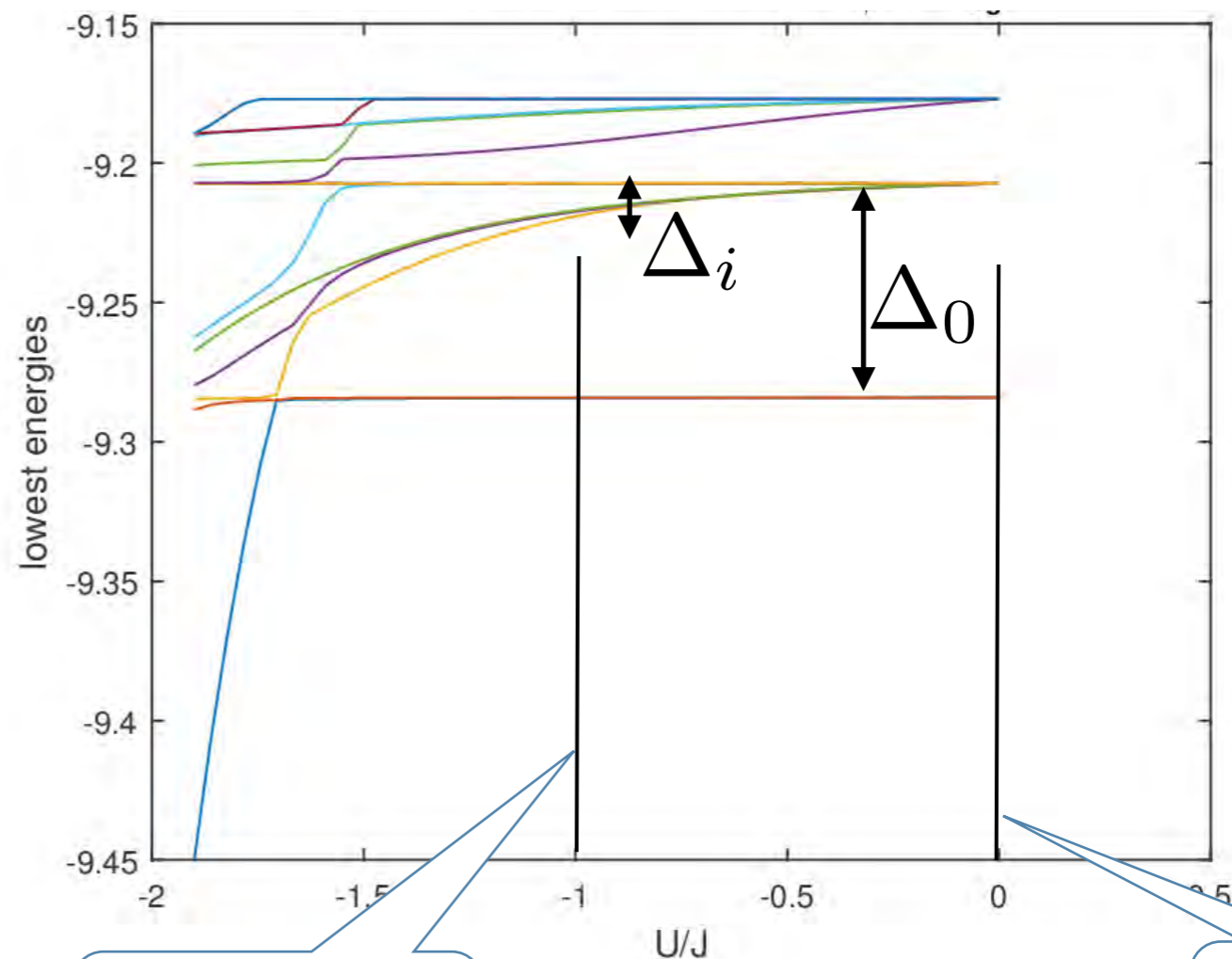
$$\Delta \gg \Gamma_S \sim \Omega \gg \Gamma_P$$



# Stability of fractional quantum Hall states in the presence of disorder

**X** Interaction is synthetic, the hard-core condition may be violated, e.g. some sites are non-interacting B. Anderson arXiv:1605.03177

Can we expect the tunneling to save the quantum Hall states?

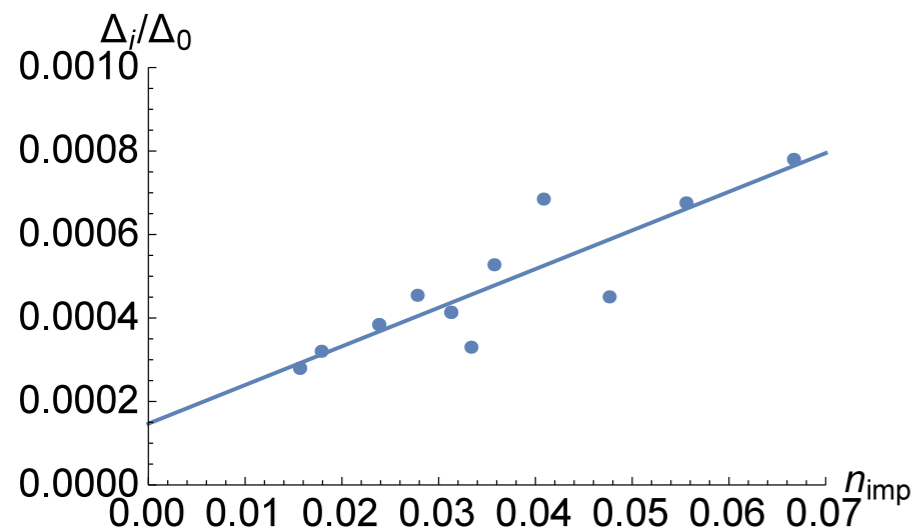


$U = 0$  at one site.

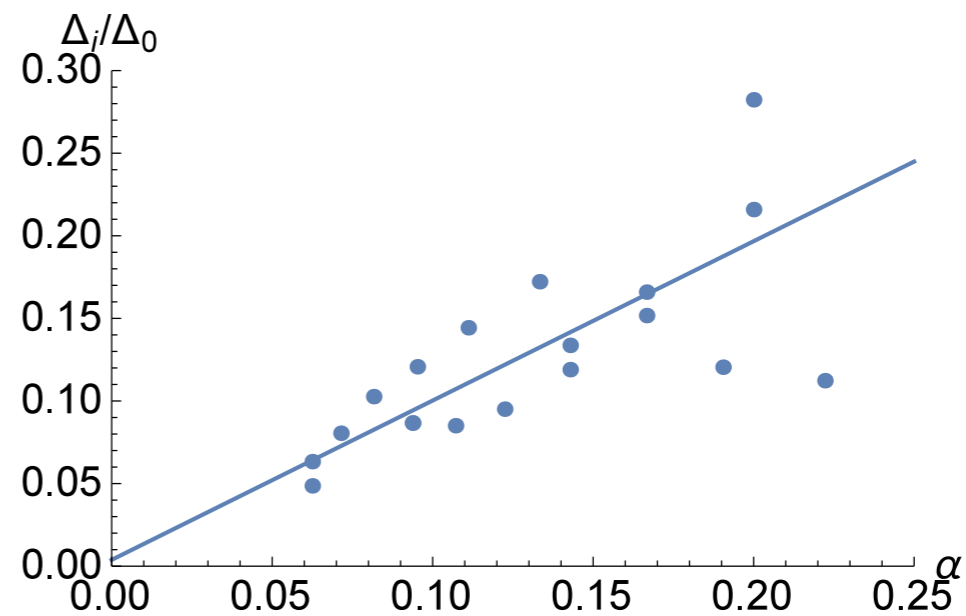
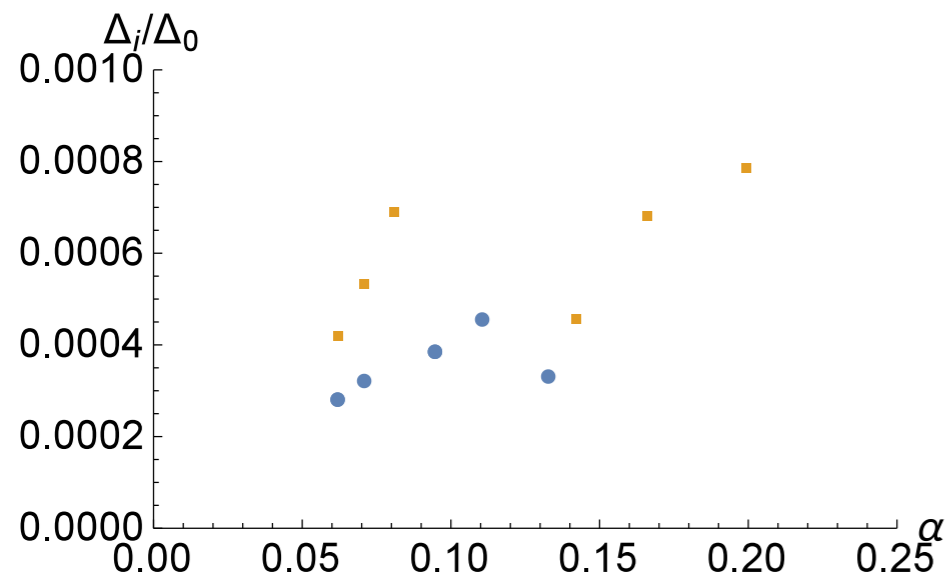
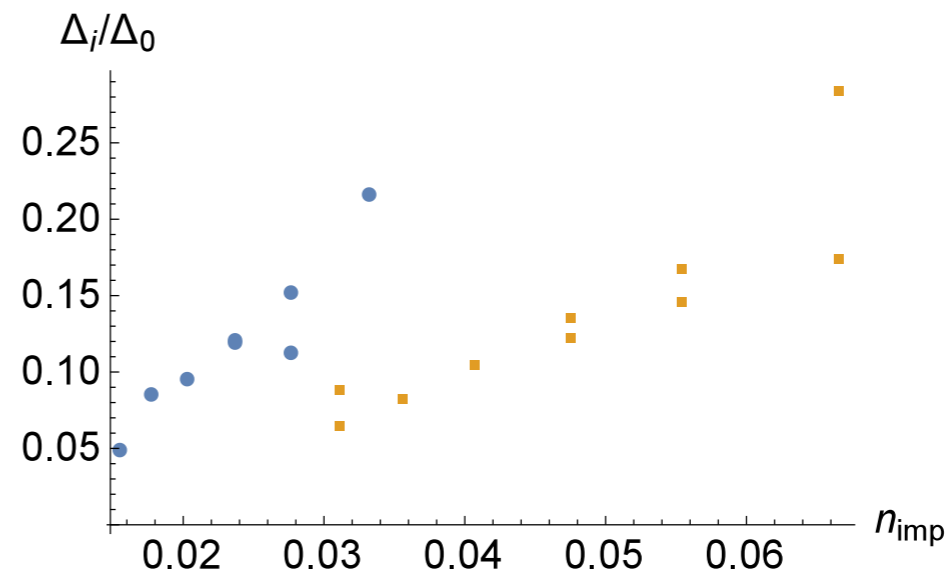
Uniform system.

- Laughlin state remains an eigenstate, regardless of the impurity
- quasi-particles becomes energetically favorable and dive down

Weak impurity  $U_{imp} = -0.01U$



Strong impurity  $U_{imp} = -U$

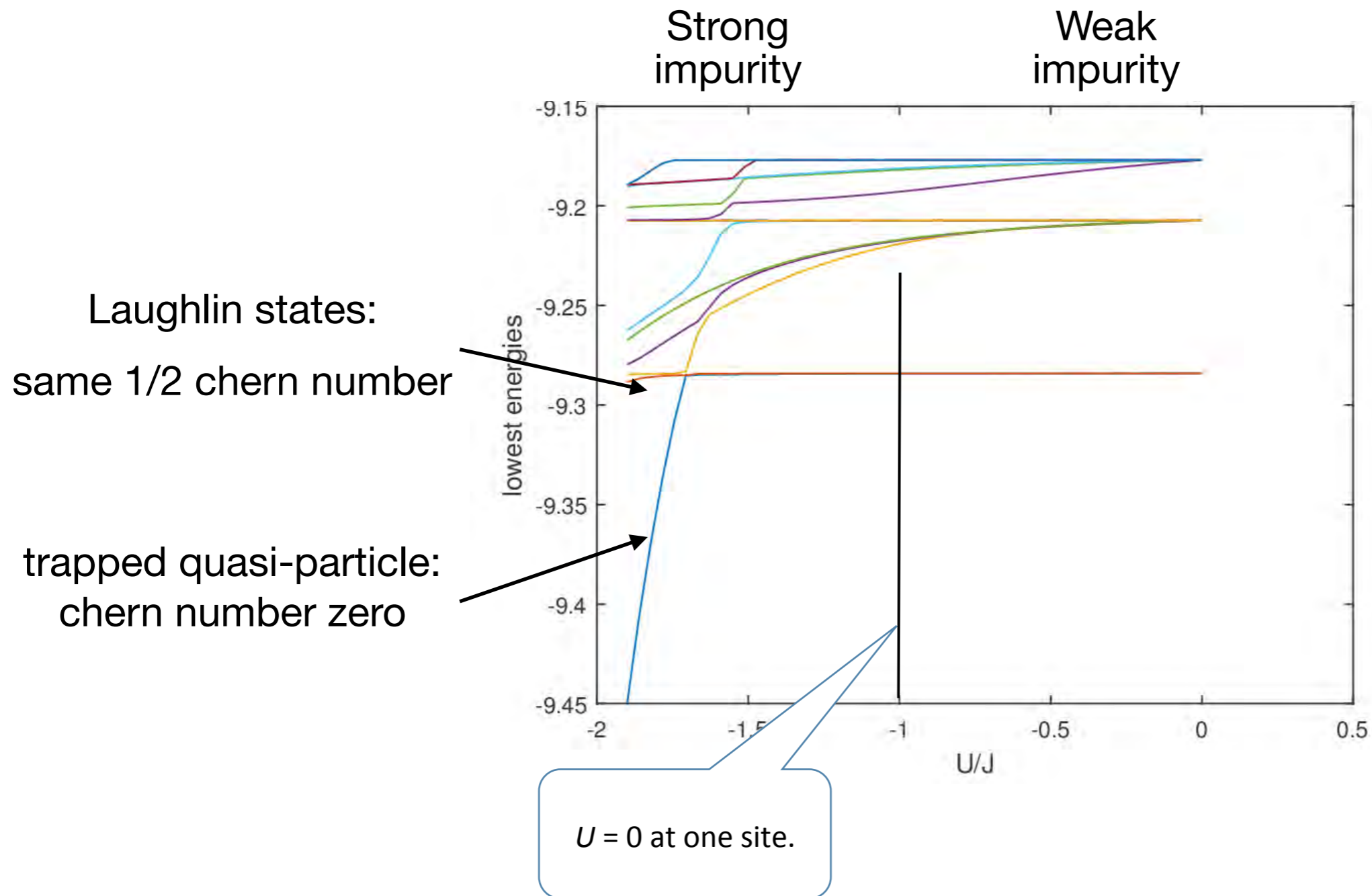


quasi-particles sample over the system:

gap is modified by the density of impurities

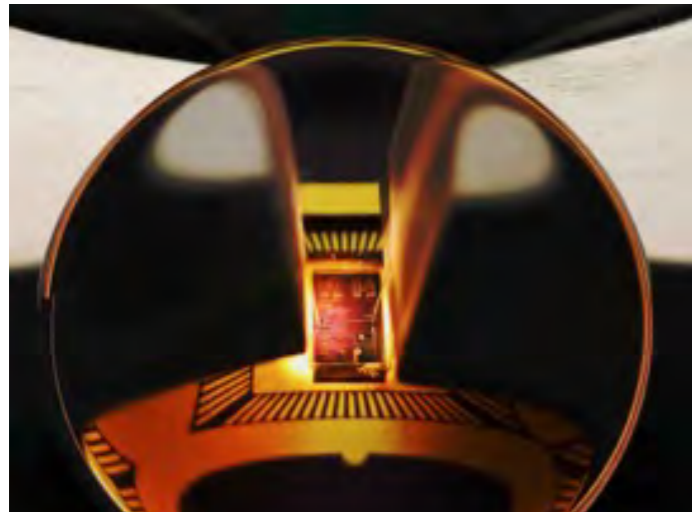
quasi-particles are trapped in one site:

gap is modified by the overlap between q-particle wavefunction and the impurity



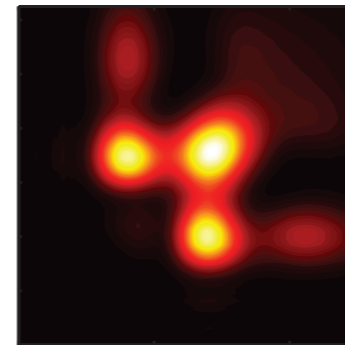
Wavefunction/ground state is modified, transport properties remain intact ✓

# Measuring topological invariants



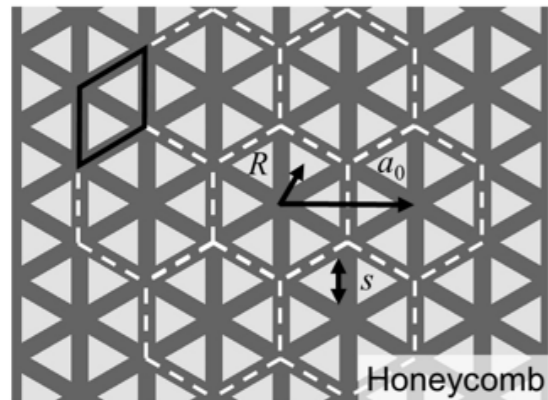
S. Mittal, S. Ganeshan, J. Fan, A. Vaezi, *Nature Photonics* 10, 180 (2016)

# Propagation of non-classical light



S. Mittal, Vikram Orre, and M. H., *Optics Express* 24, 15632 (2016)

# Topological photonic crystals



# E. Kapit, *Nature* and S. Simon *PRX* 2014



S. Barik, H. Miyake, W. DeGottardi, E. Waks, M.H. [arXiv:1605.08822](https://arxiv.org/abs/1605.08822)

