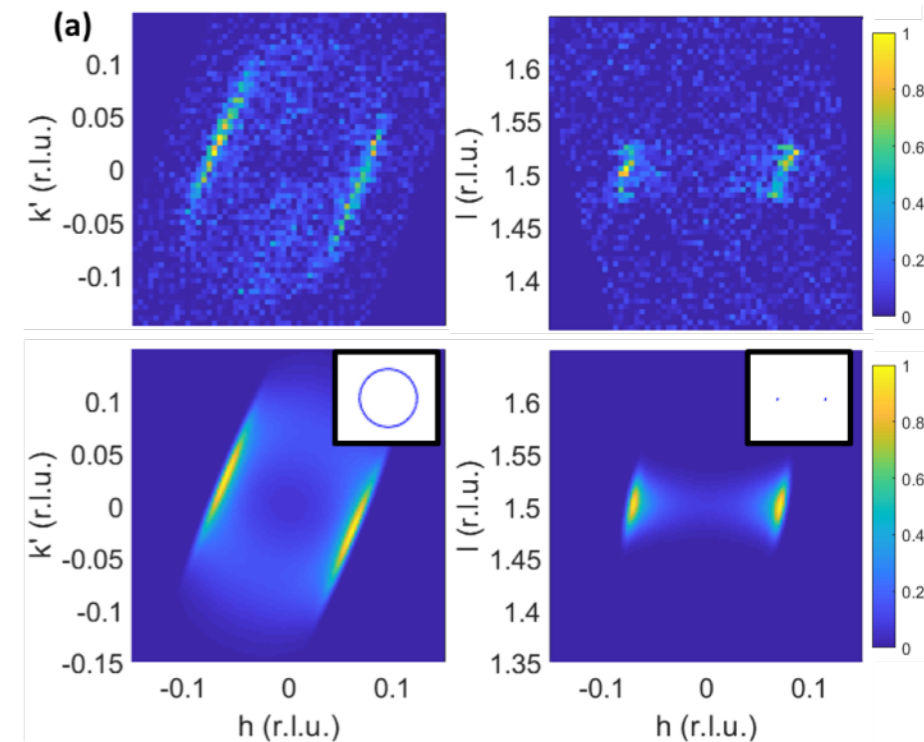
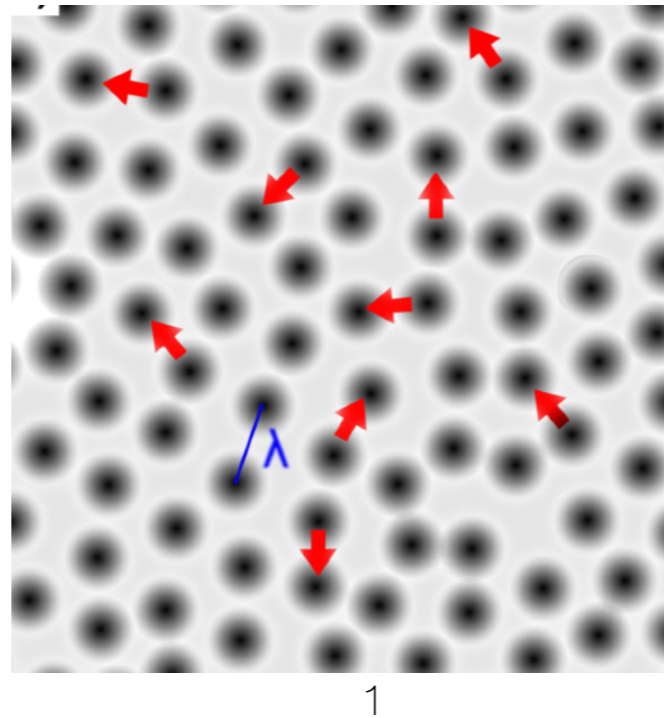
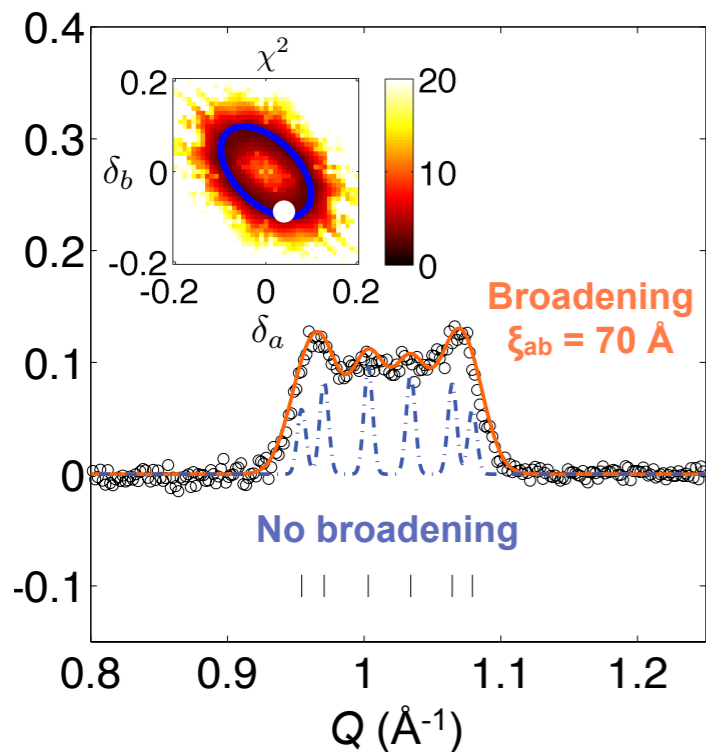


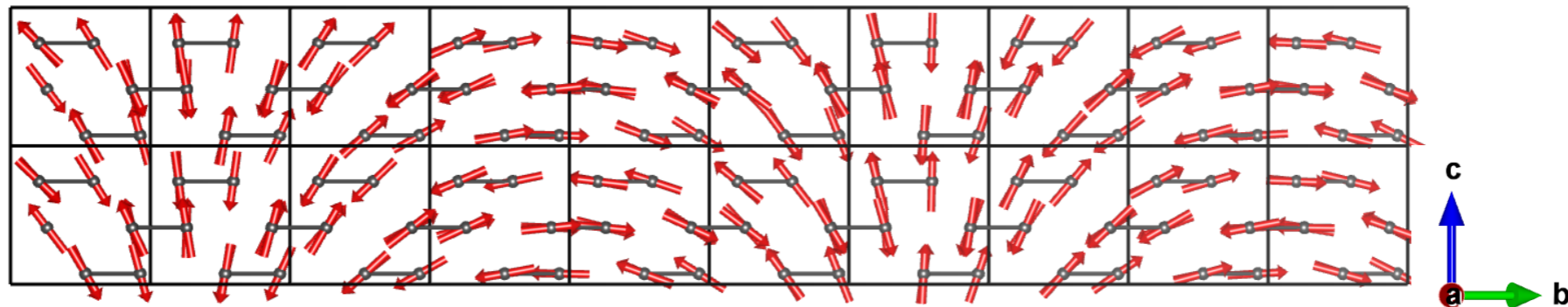
Partial Antiferromagnetic Helical Order in $\text{Fe}_3\text{PO}_4\text{O}_3$

Kate A. Ross
Colorado State University

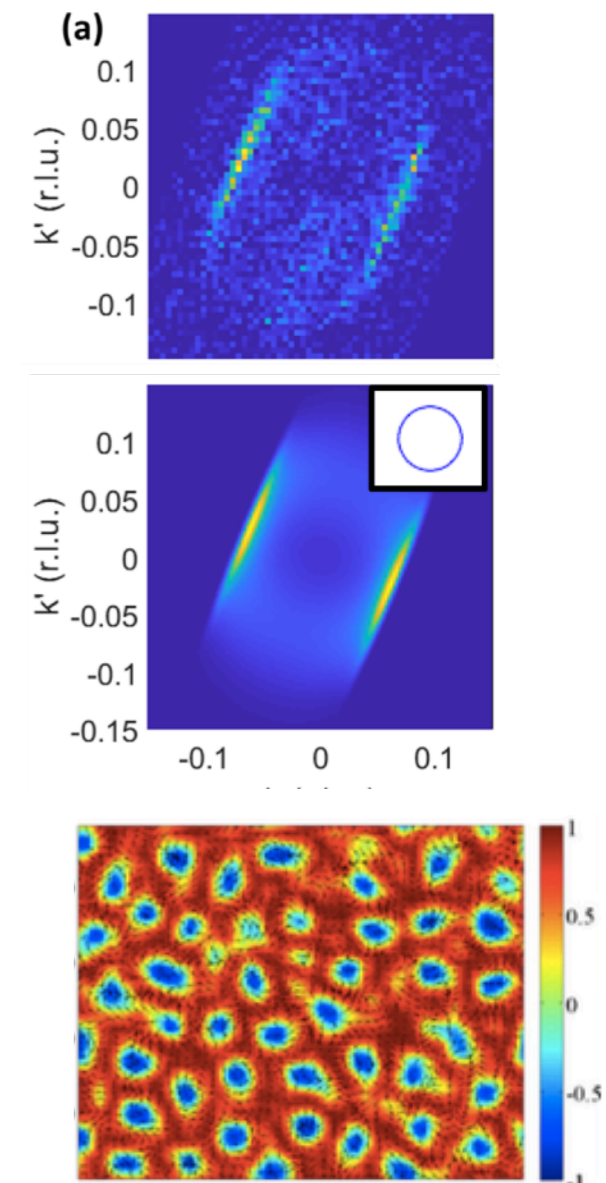
EPIQS-TMS meeting 2019
KITP, Santa Barbara, CA



Outline



- “Partial” helical order
- $\text{Fe}_3\text{PO}_4\text{O}_3$: Antiferromagnetic partial helical order with short correlation length
- Evidence for a disordered, antiferromagnetic Skymion-like state



Helical order

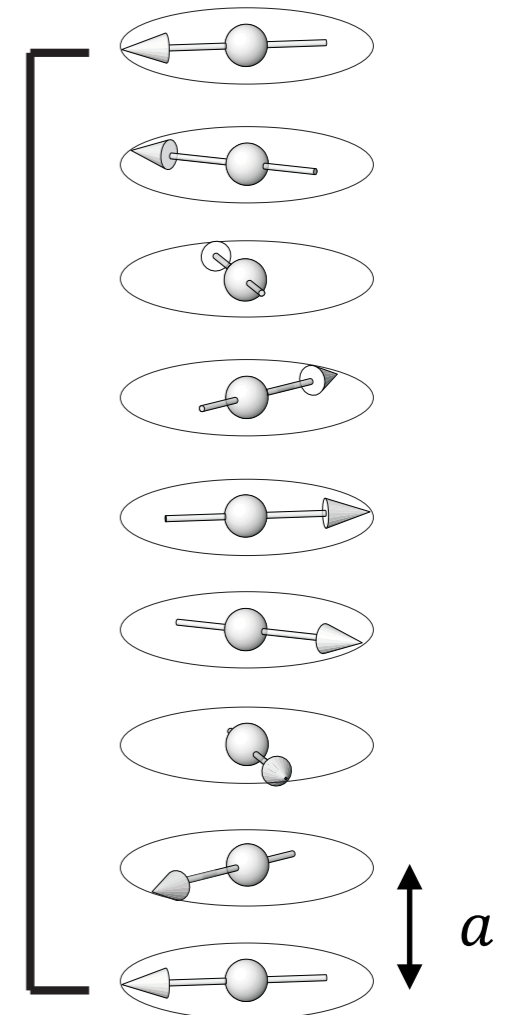
Caused by competing interactions e.g.:

- 1) Ferromagnetism competing with Dzyaloshinskii Moriya ($S_i \times S_j$)
- 2) Heisenberg AFM 1st and 2nd neighbors

$$H = J_1 \sum_{\langle i,j \rangle} S_i \cdot S_j + J_2 \sum_{\langle\langle i,j \rangle\rangle} S_i \cdot S_j$$

$$H = J \sum_{\langle i,j \rangle} S_i \cdot S_j + D \sum_{\langle i,j \rangle} S_i \times S_j$$

pitch length, λ



Diffraction from helical order: “satellite” peaks

real space



a

reciprocal space
(lattice and magnetic)

● $2\pi/a$

● 0

● $-2\pi/a$

real space



a

$\lambda/2$

reciprocal space
(lattice and magnetic)

●● $2\pi/a \pm 2\pi/\lambda$

●● 0 $\pm 2\pi/\lambda$

●● $-2\pi/a \pm 2\pi/\lambda$

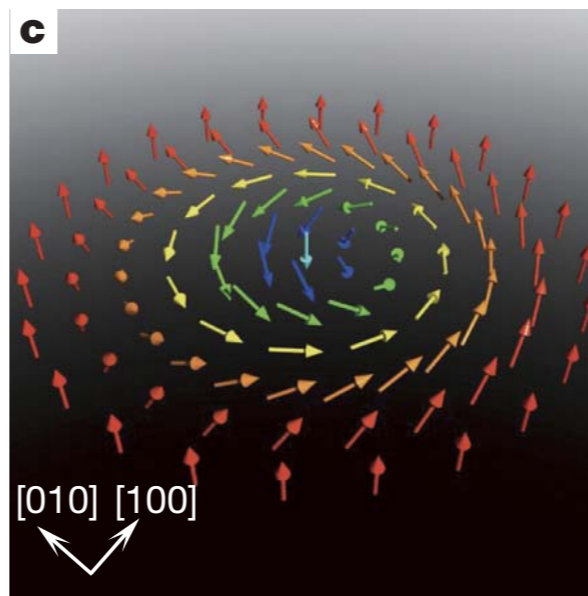
“satellite peaks”
near the parent
magnetic structure
zone centers

Example: B20 Compounds

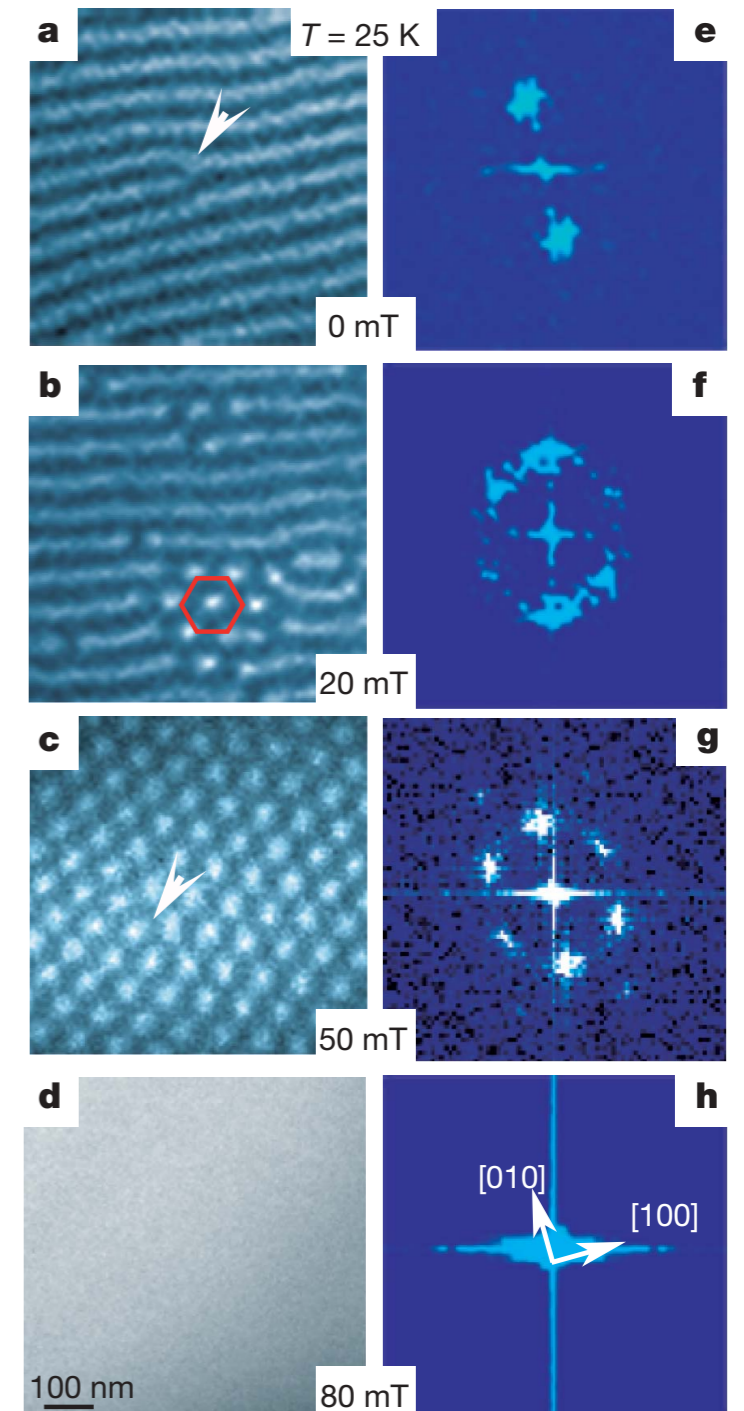
- The B20 compounds with space group $P2_13$, e.g. MnSi , $\text{Fe}_{1-x}\text{Co}_x\text{Si}$ exhibit helical order
- Dominant FM interactions plus DM interaction are responsible (“locally ferromagnetic”)
- **Bonus:** under a small applied field, the helical order transforms into a Skyrmion Lattice!

Lorentz TEM: real space images of helical and Skyrmion lattice order in $\text{Fe}_{0.5}\text{Co}_{0.5}\text{Si}$

Yu, Onose, Kanazawa, Park, Han, Matsui, Nagaosa, Tokura, *Nature*, (2010), 465, 901–904.

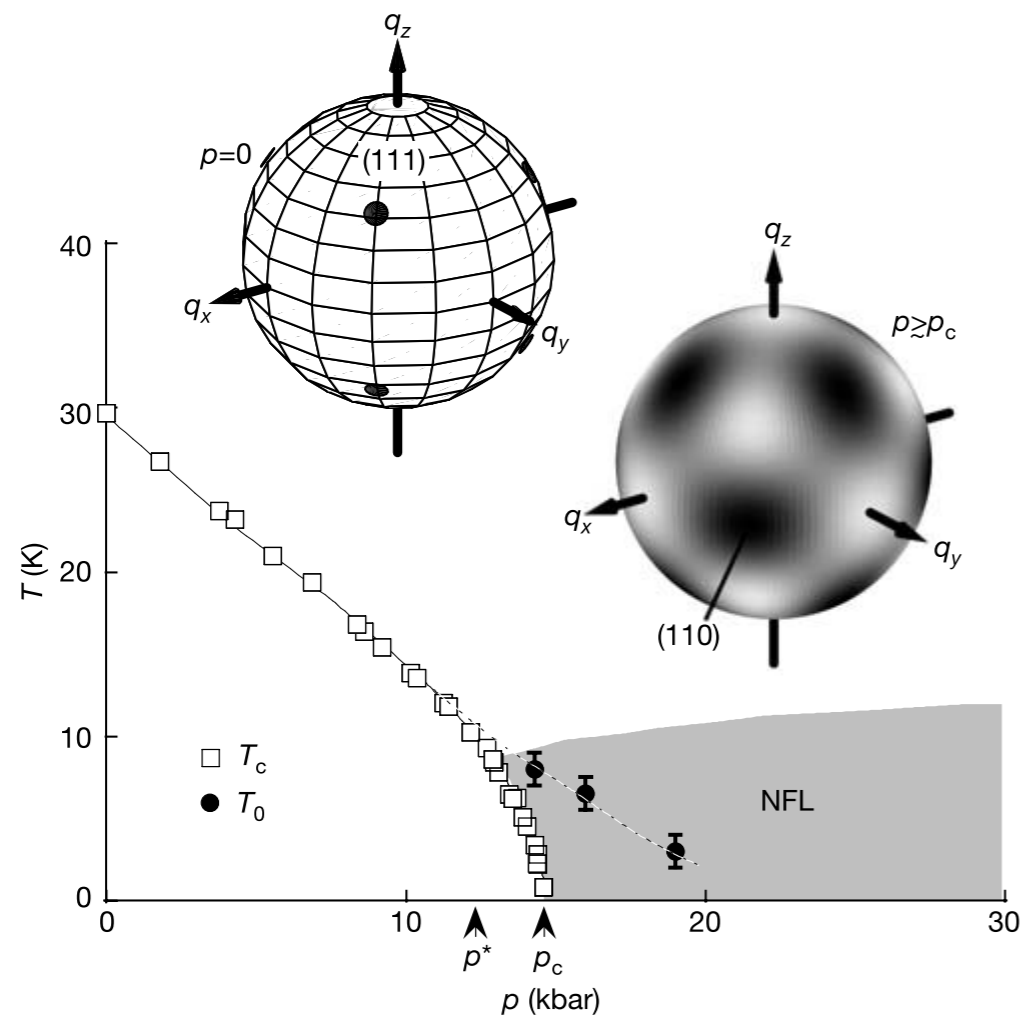


real space “diffraction” (FFT)

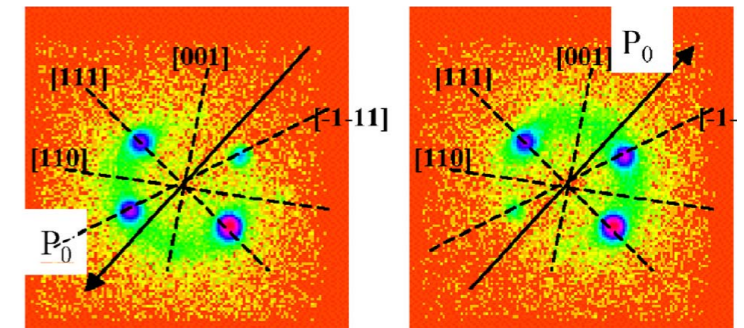


“Partial” Helical order

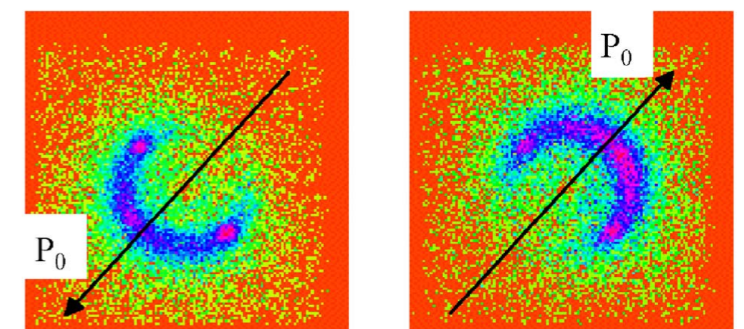
- MnSi: under pressure, and at temperatures $T > T_c$, exhibits a **spherical shell** instead of Bragg spots
- **“Partial order”**: Well-defined pitch length, but not *direction*



below T_c
(helical)



Above T_c
(Partial order)



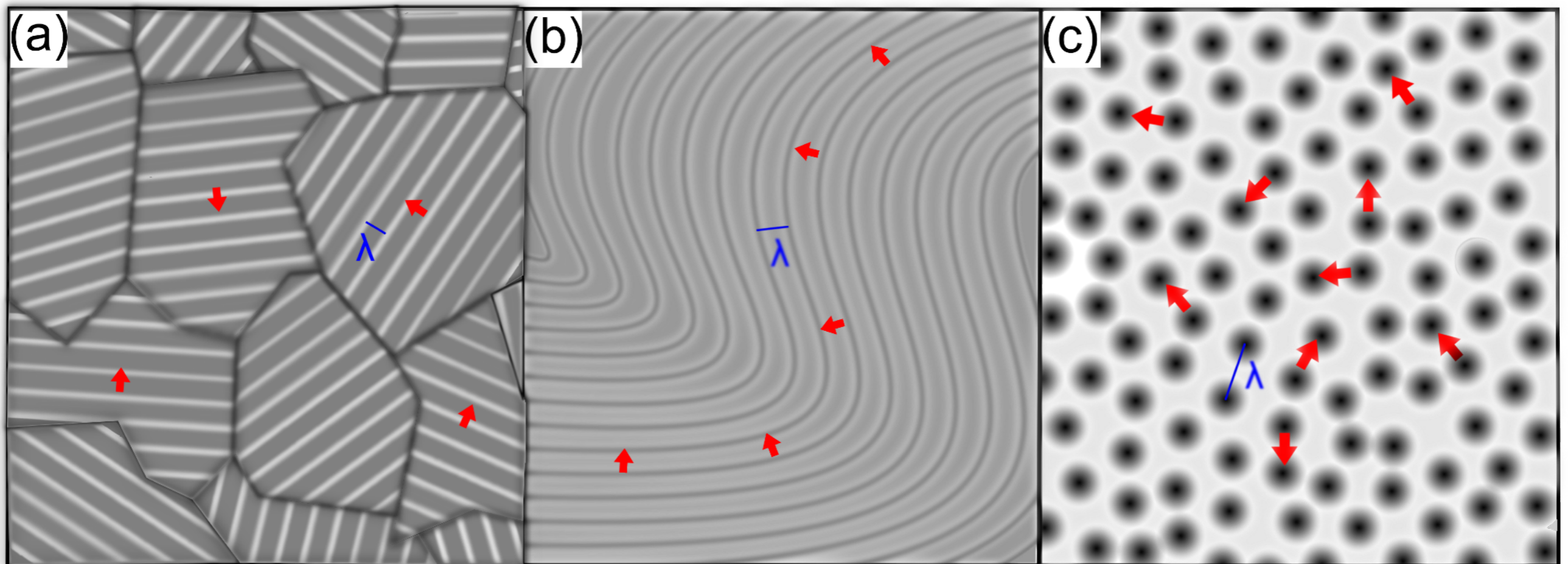
Origin of “Partial” Helical order?

“**Partial order**”: Well-defined pitch length, but not *direction*

Helical Domains

Unpinned Helical Wavevector

Disordered Skyrmion State

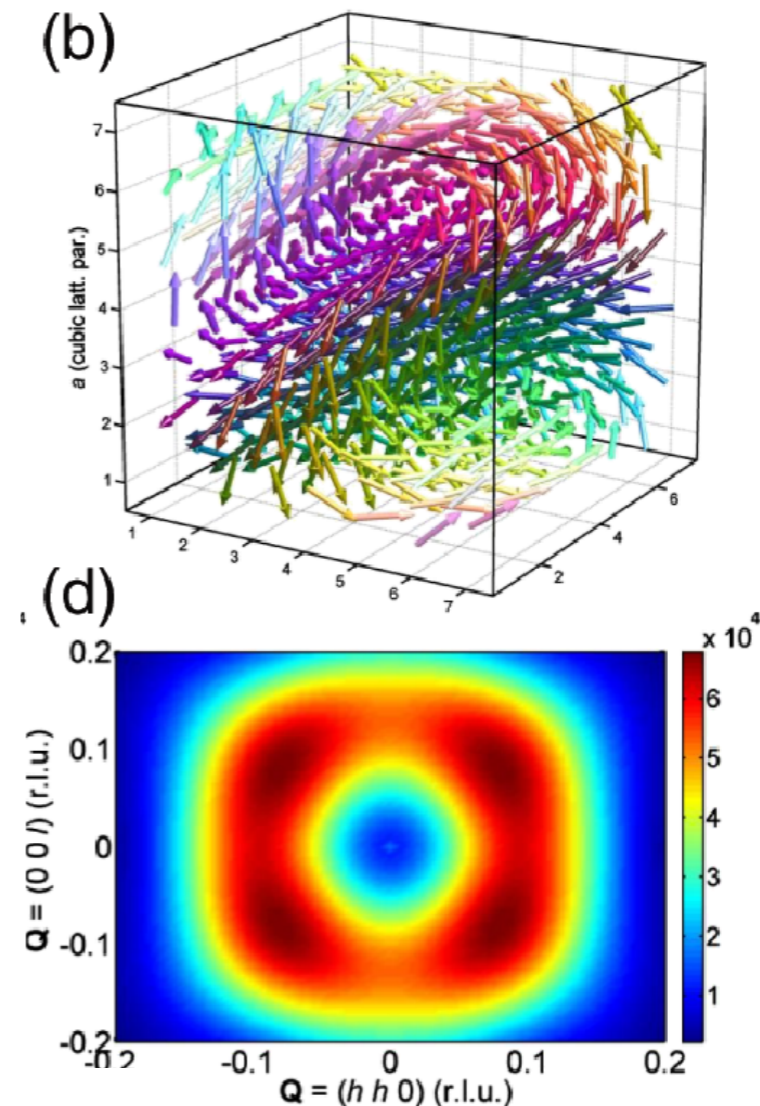
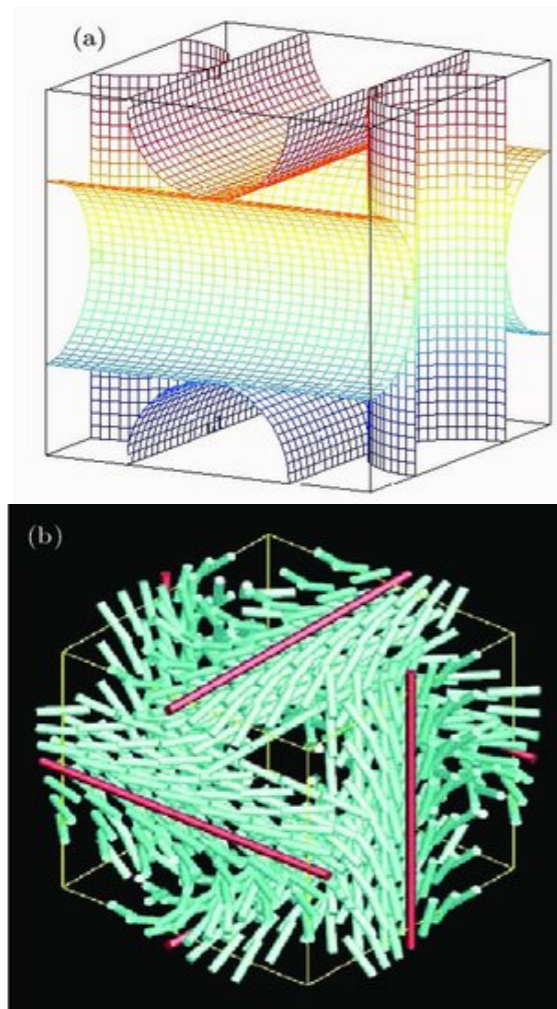


“Blue Phase” description of partial Helical order in MnSi

"Blue Phase" of Liquid Crystals: "Double twist Cylinders"



Same topologies proposed in partial order phase of MnSi. **Very similar to disordered Skyrmions.**



Dou Hu, Ma Hong-Mei, Sun Yu-Bao.
Acta Physica Sinica 64 126101 (2015)

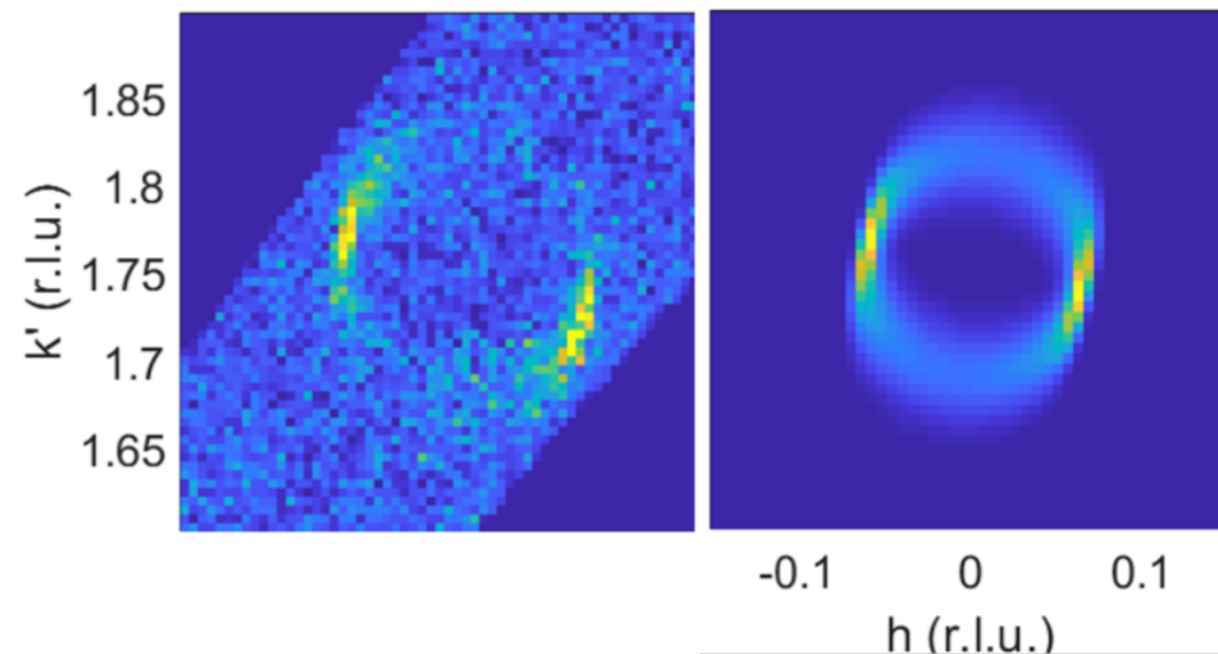
A. Hamann, D. Lamago, Th. Wolf, H. v. Lohneysen, D. Reznik, PRL 107, 037207 (2011)

$\text{Fe}_3\text{PO}_4\text{O}_3$

K. A. Ross, M.M. Bordelon, G. Terho, J. R. Neilson. *Nanosized helical magnetic domains in strongly frustrated $\text{Fe}_3\text{PO}_4\text{O}_3$* . Phys. Rev. B **92**, 134419 [Editor's suggestion] (2015)

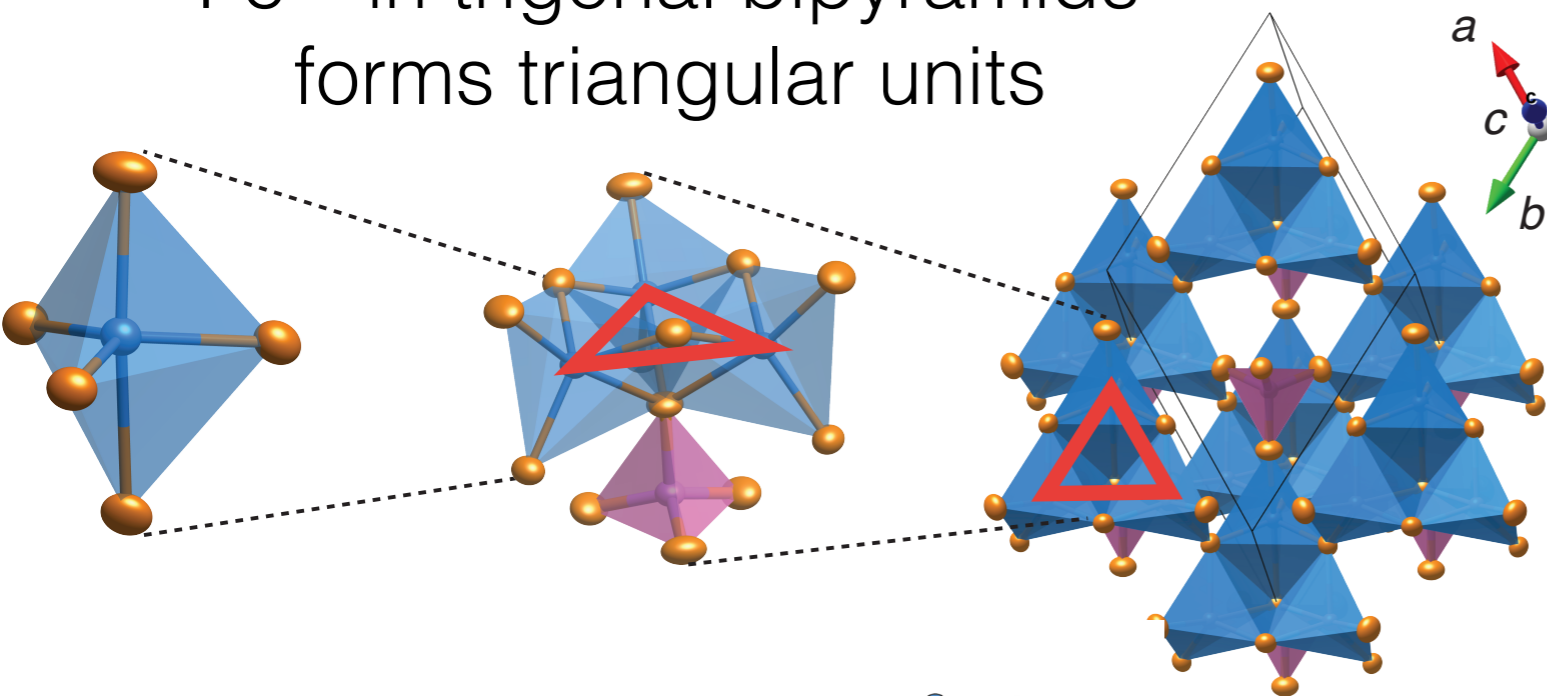
M.J. Tarne, M.M. Bordelon, S. Calder, J.R. Neilson, K.A. Ross. *Tuning the antiferromagnetic helical pitch length and nanoscale domain size in $\text{Fe}_3\text{PO}_4\text{O}_3$ by magnetic dilution*. Phys. Rev. B **96**, 214431 (2017)

C. Sarkis, M.J. Tarne, H. Cao, E. Coldren, M. Gelfand, J.R. Neilson, K.A. Ross. *Partial Antiferromagnetic Helical Order in $\text{Fe}_3\text{PO}_4\text{O}_3$* . arXiv:1910.08818 [cond-mat.str-el] (2019)

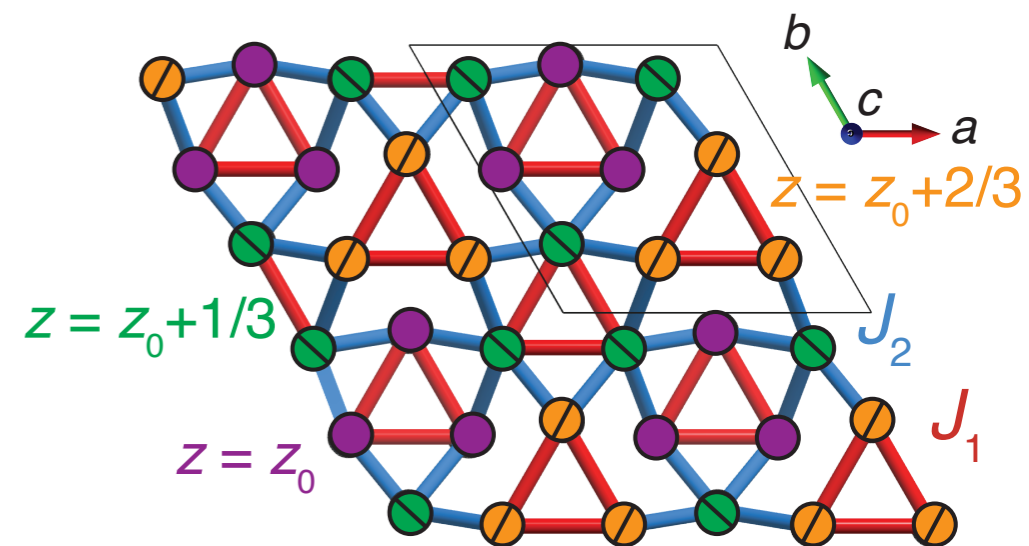


Triangular plaquettes on a rhombohedron

Fe³⁺ in trigonal bipyramids forms triangular units

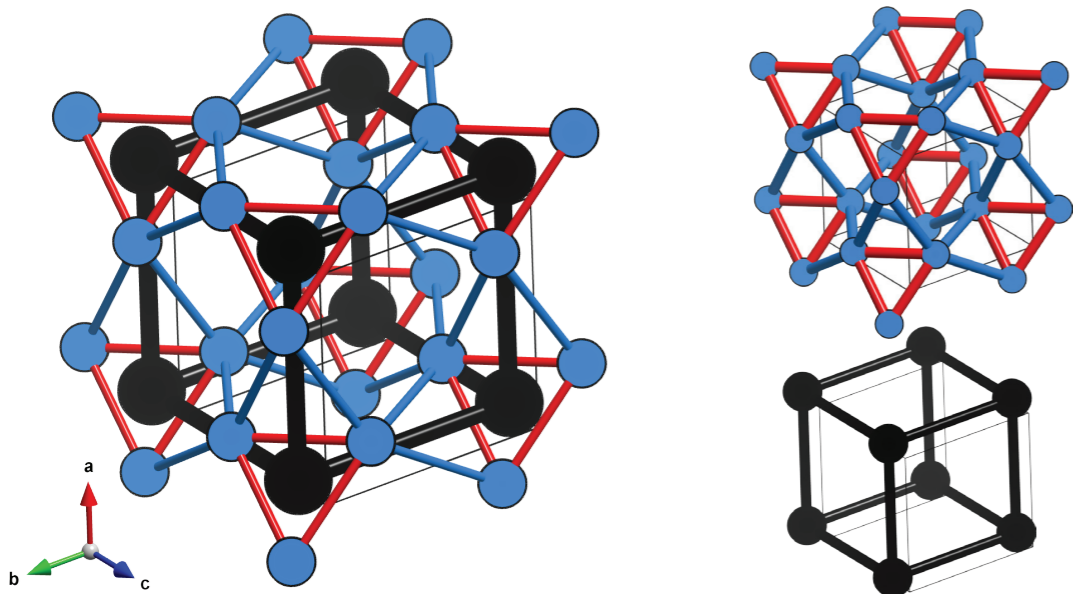


From *c*-axis, looks like “triangular lattice of triangles”



R3m: non-centrosymmetric

Triangles decorate corners of a rhombohedral cell:
fully connected 3D structure



within a triangle: J_1
between triangles: J_2

$$H = \sum_{n.n.} J_1 \vec{S}_i \cdot \vec{S}_j + \sum_{n.n.n.} J_2 \vec{S}_i \cdot \vec{S}_j$$

Frustration and Antiferromagnetic Order in $\text{Fe}_3\text{PO}_4\text{O}_3$

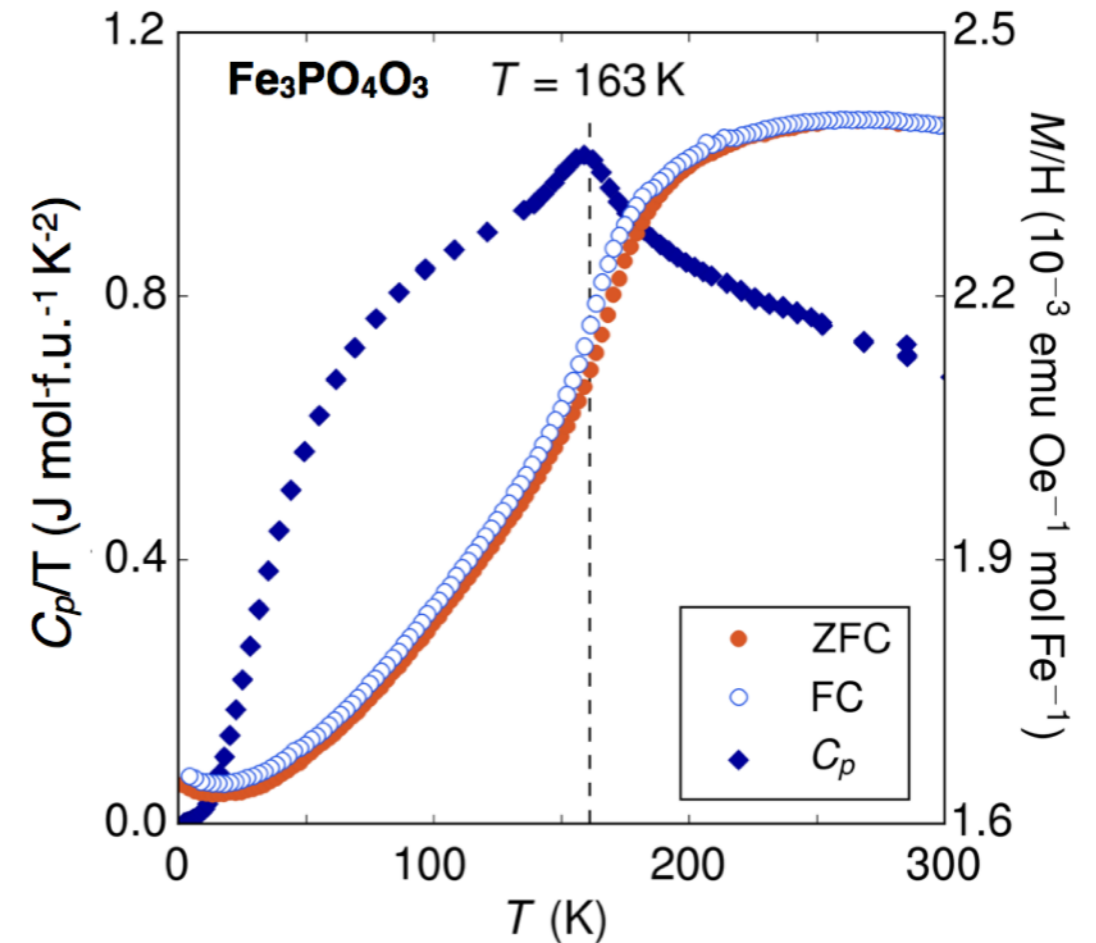
Antiferromagnetic order: peak in the specific heat and drop in the susceptibility; $T_N \sim 163$ K.

Frustration index:

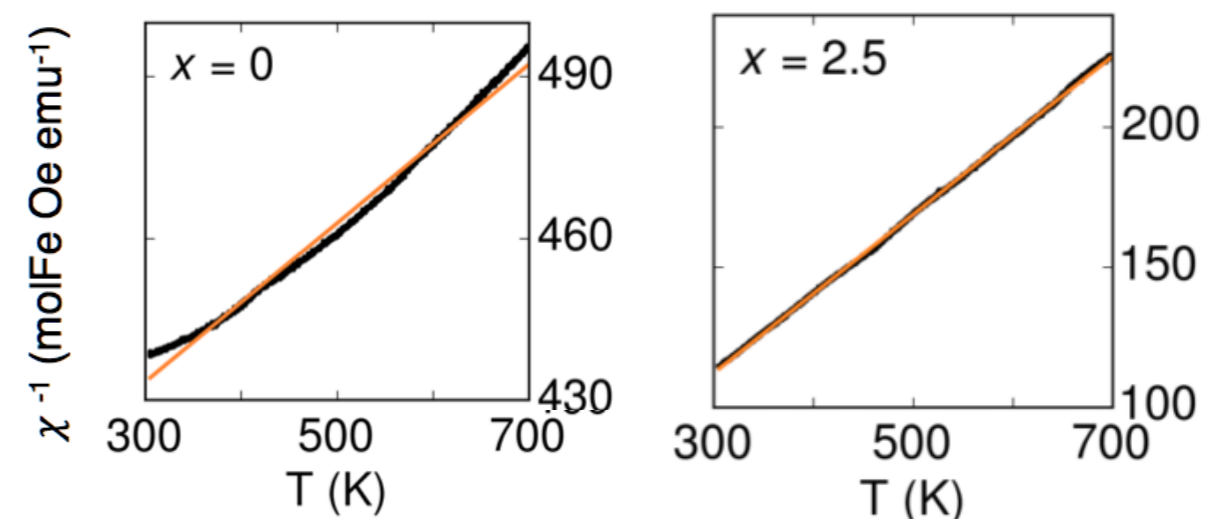
$$f > 900 \text{ K} / 163 \text{ K} = 5.52$$

$$J_1 > 319 \text{ K}$$

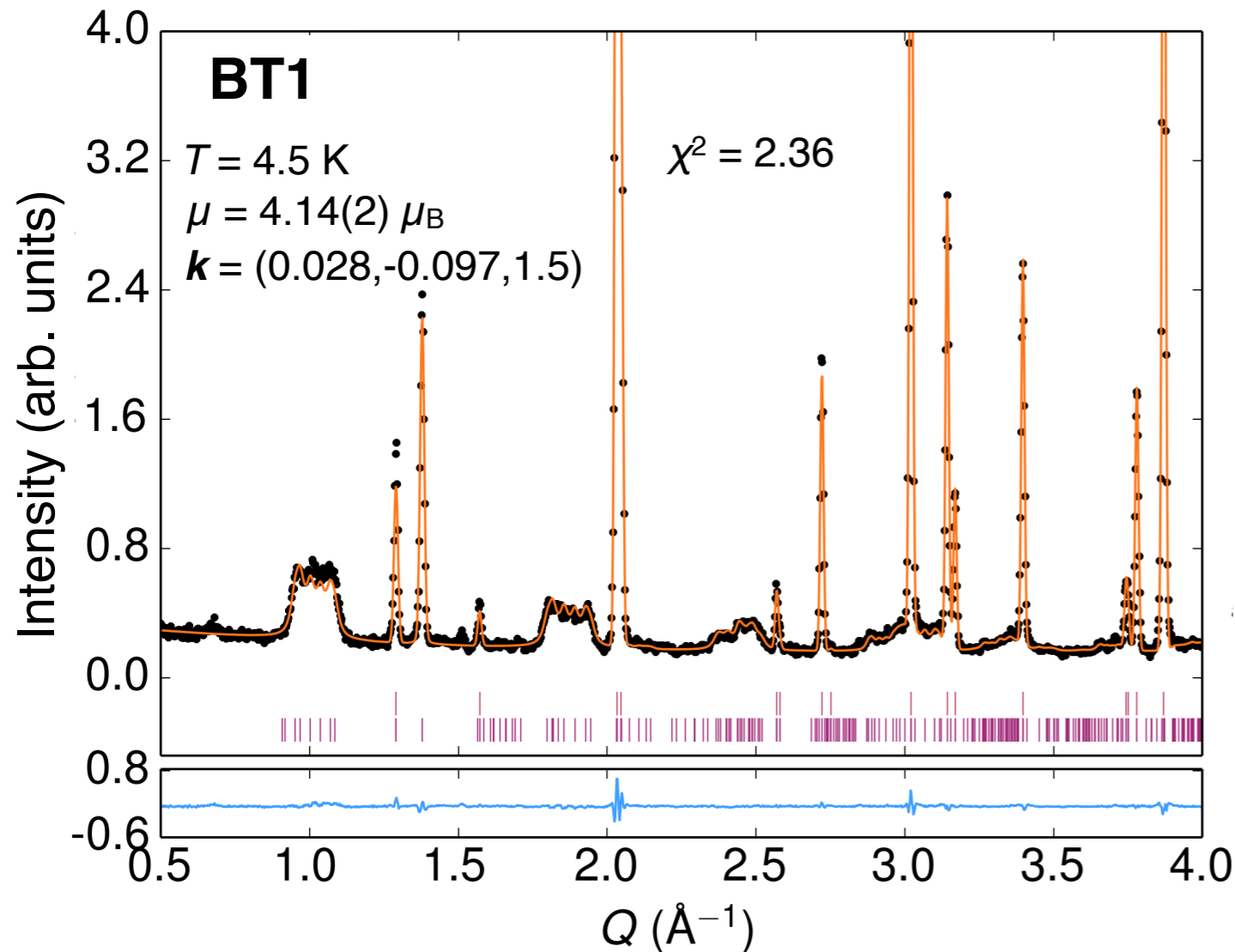
Very strong magnetic interactions and frustration.



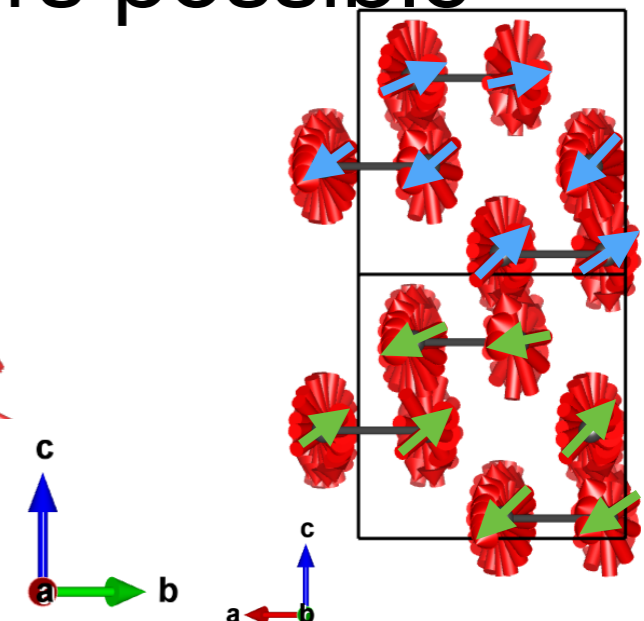
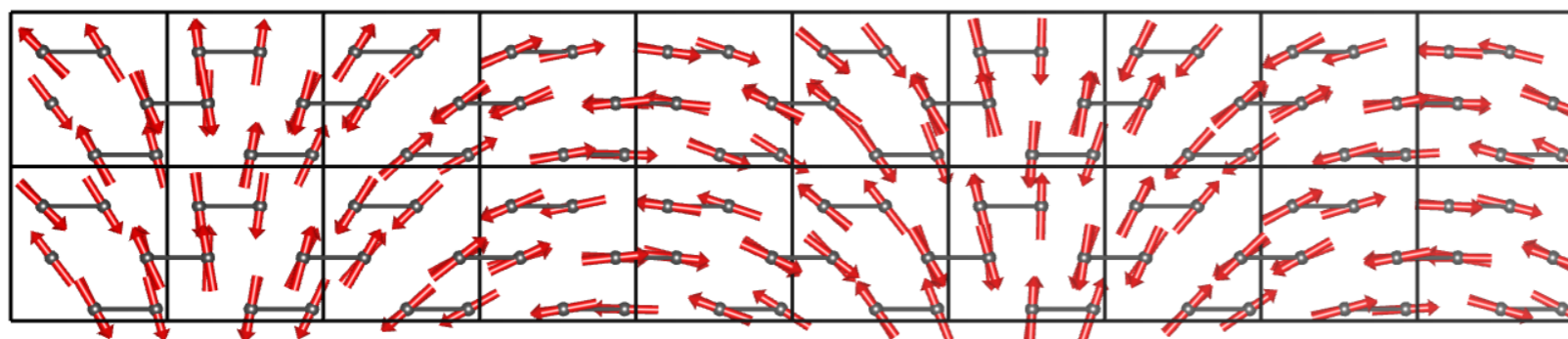
Ross, Bordelon, Terho, Neilson, PRB 92, 134419 (2015)



Antiferromagnetic structure...

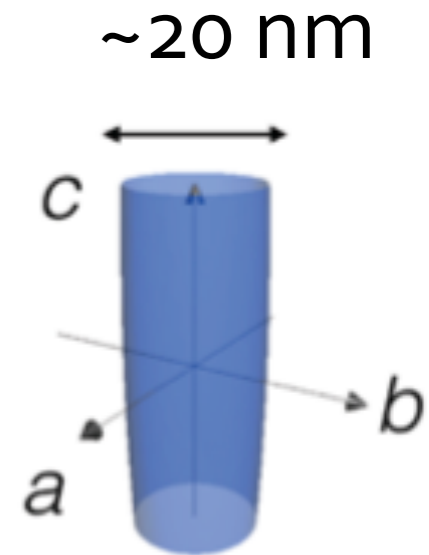
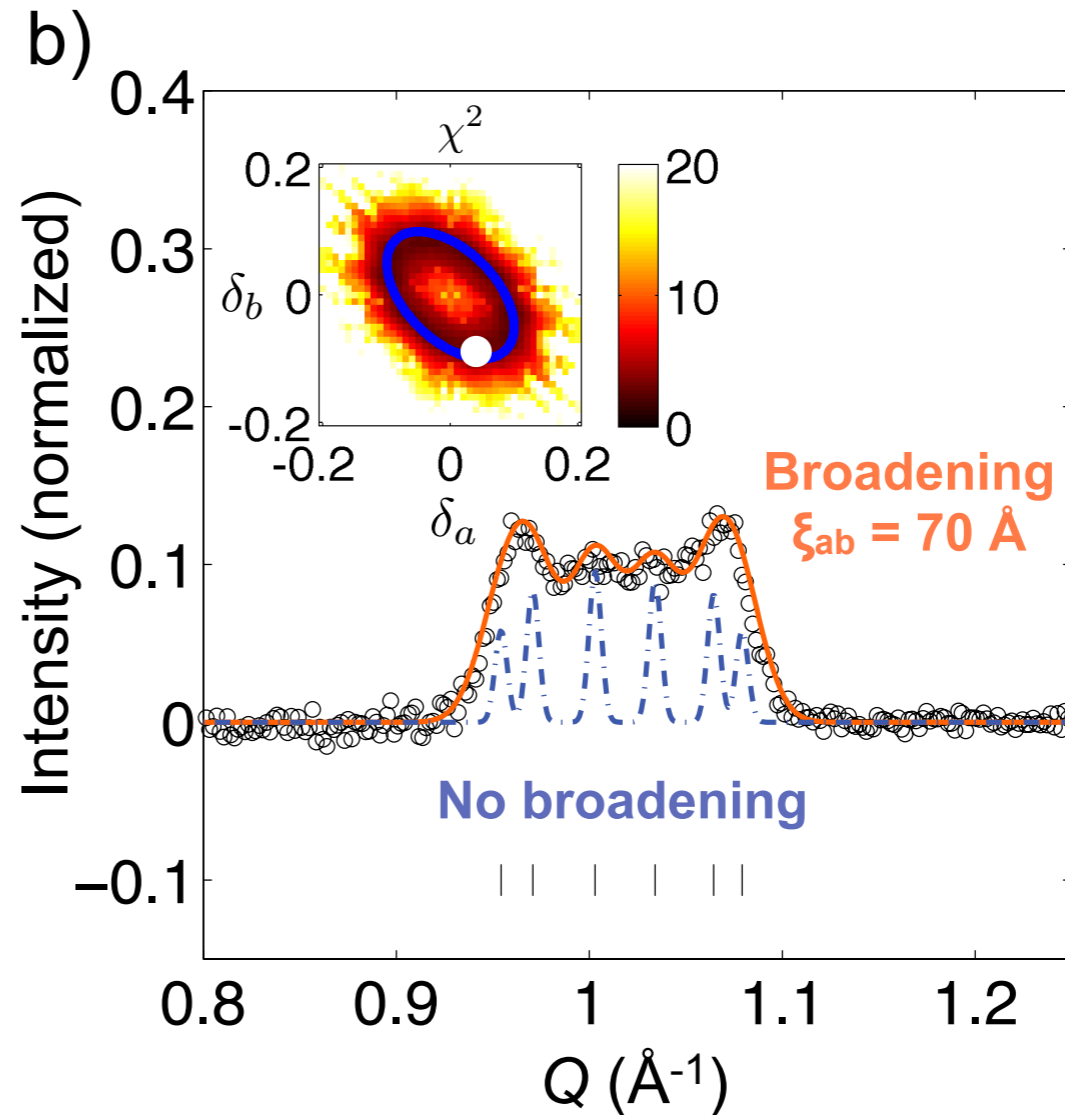
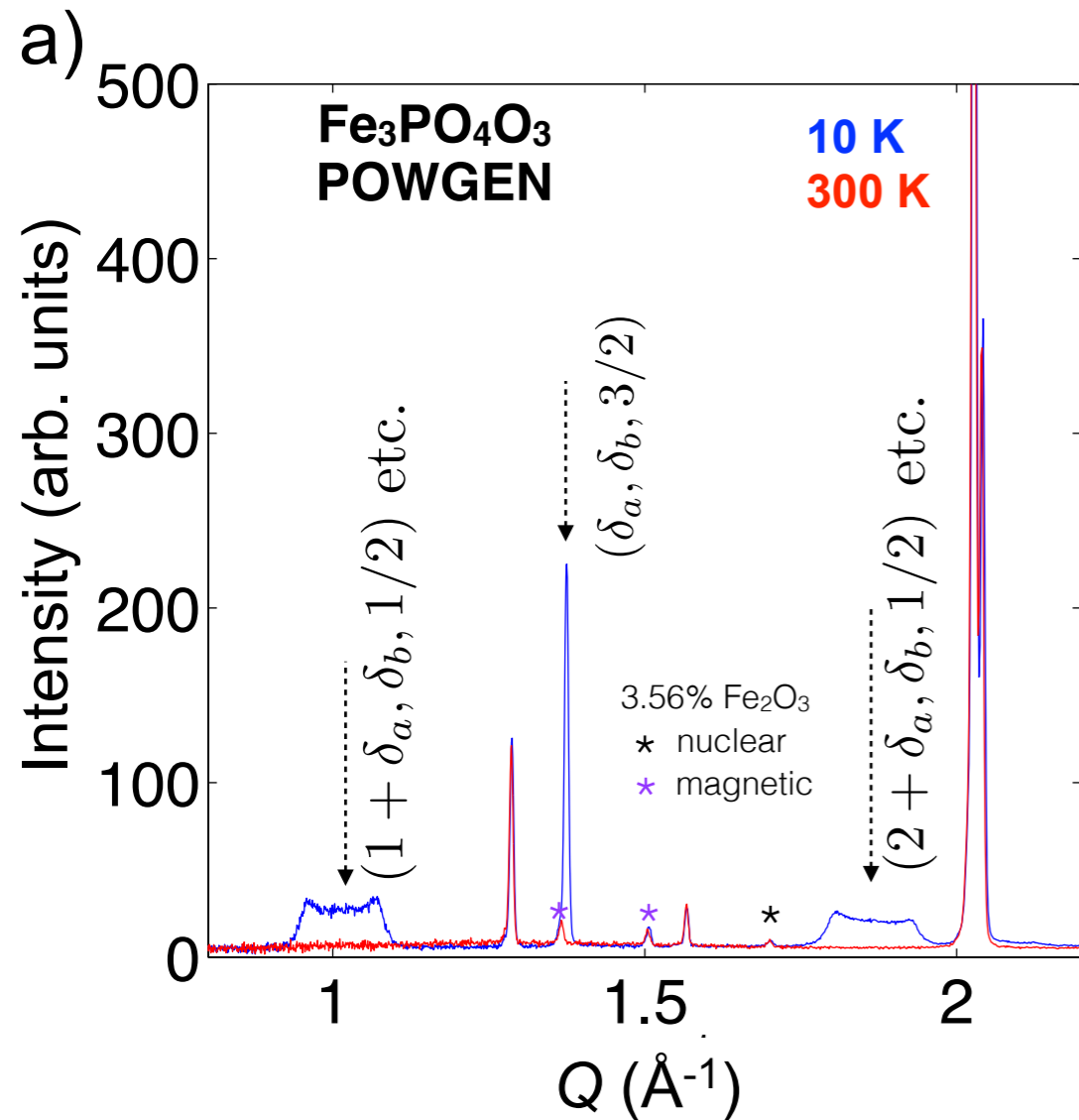


- Helical structure with perfect cancellation of moments along c -axis (“AFM Helical”)
- $\lambda = 86 \text{ \AA}$
- $\mathbf{k}_{\text{ord}} = (\delta_a, \delta_b, 1.5)$
- 6 symmetry-related k vectors possible



Ross, Bordelon, Terho, Neilson, PRB 92, 134419 (2015)

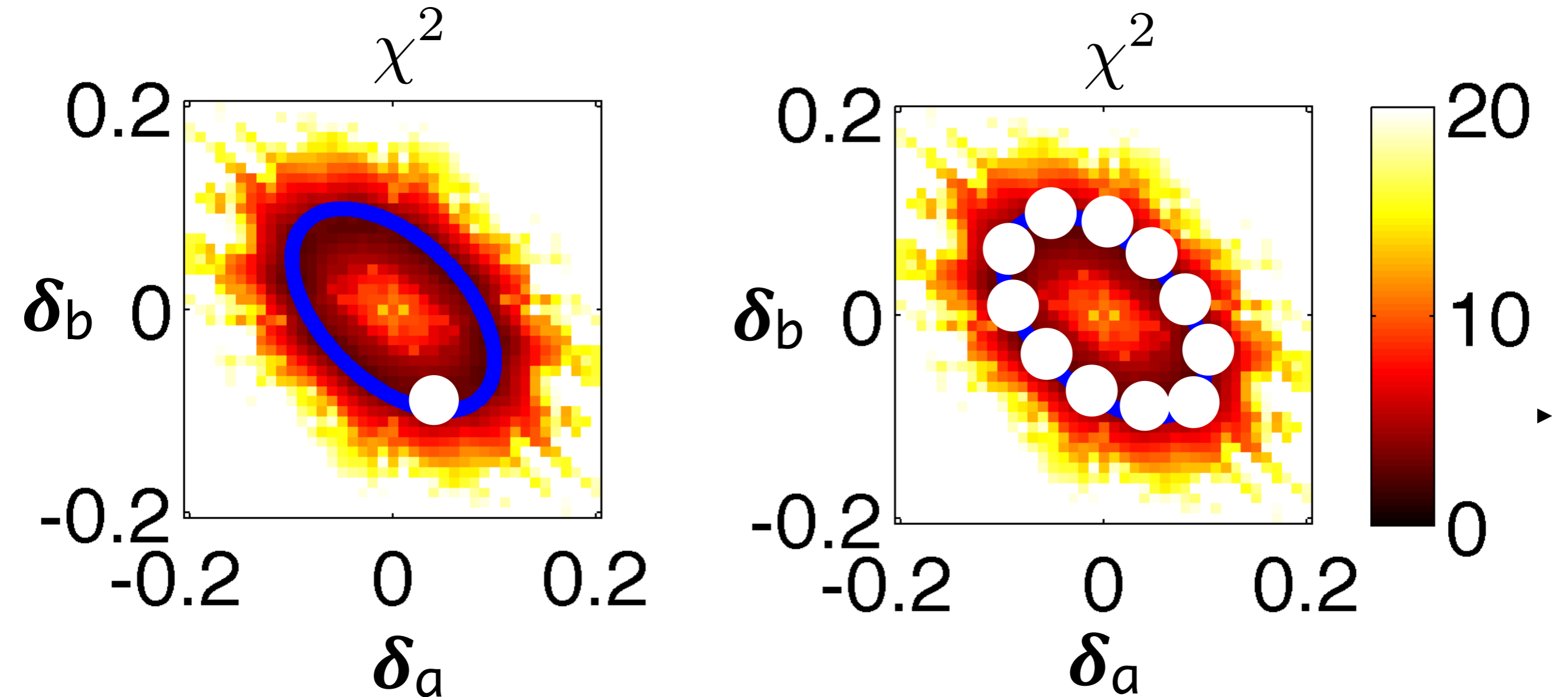
Finite size broadening required in *ab* plane



Need finite size broadening in *ab* plane only:
needle domains

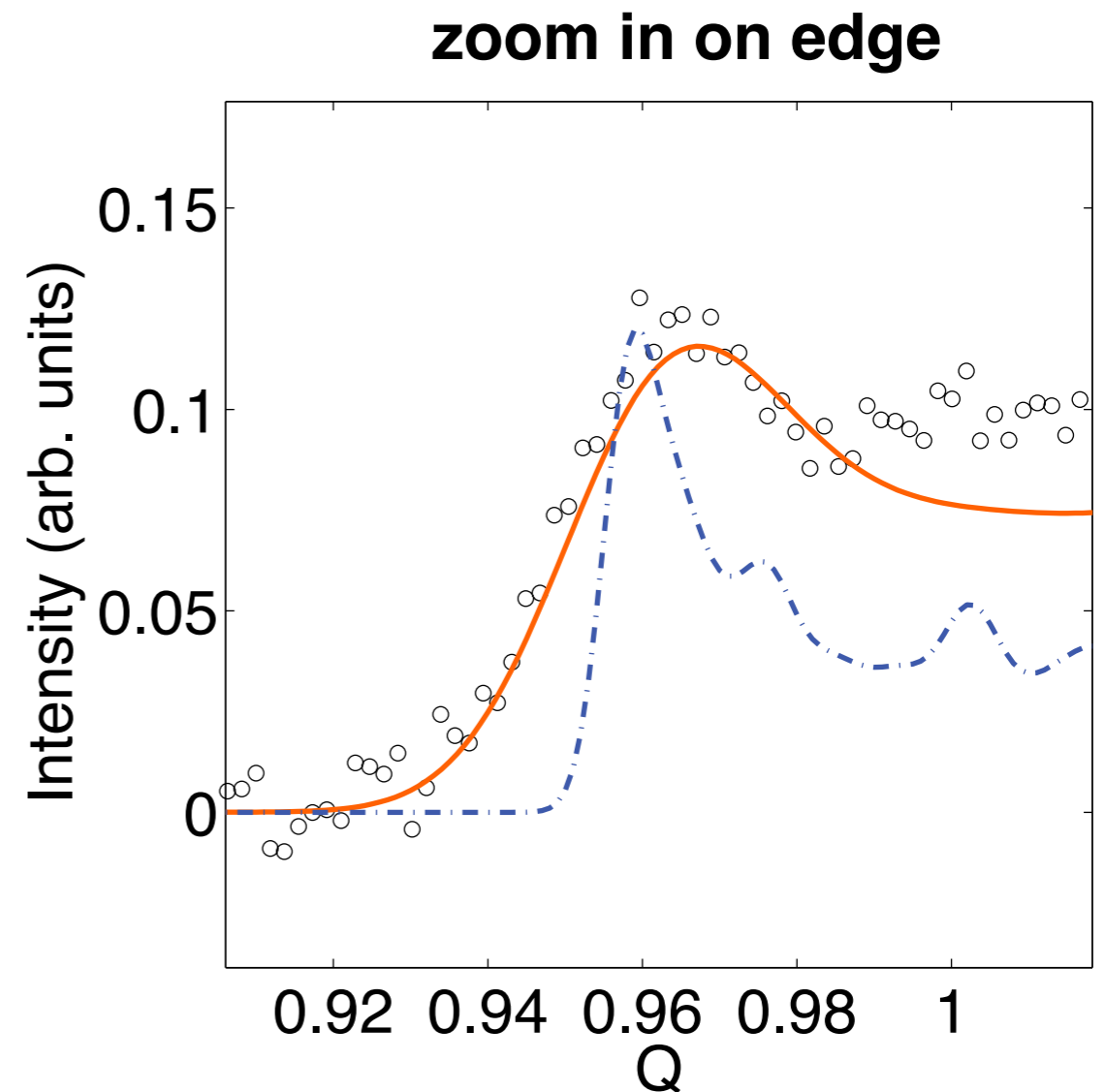
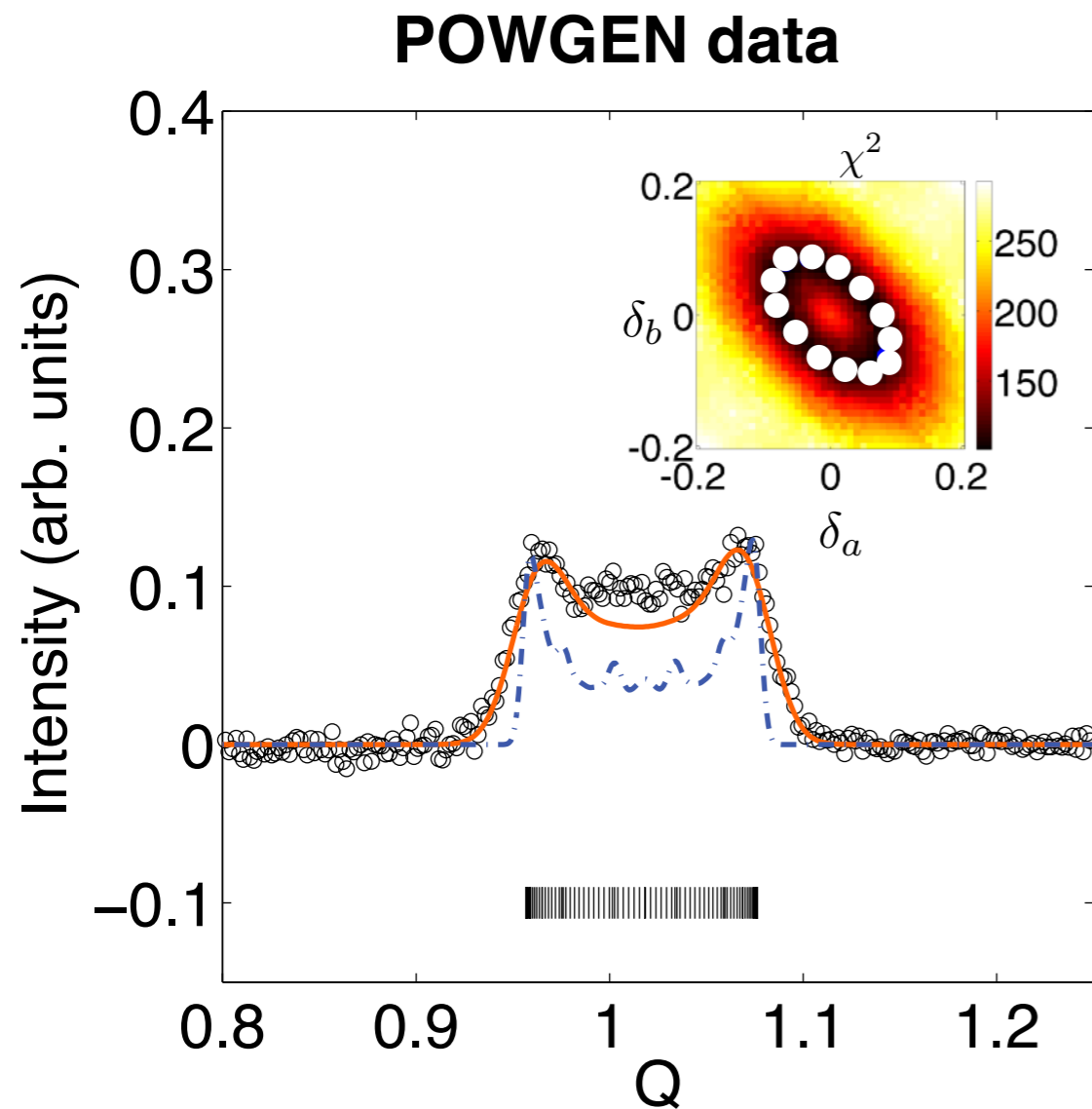
What if it is actually a circular structure factor?

$$k_{\text{ord}} = (\delta_a, \delta_b, 1.5)$$



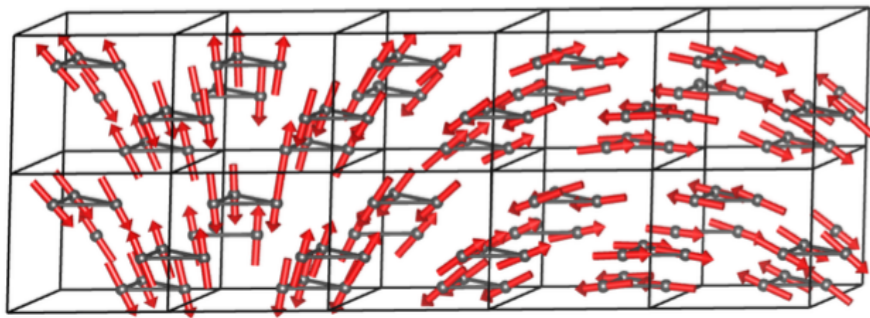
Broadening STILL required in *ab* plane

Assuming an **approximately circular structure factor**, still need broadening in *ab* plane

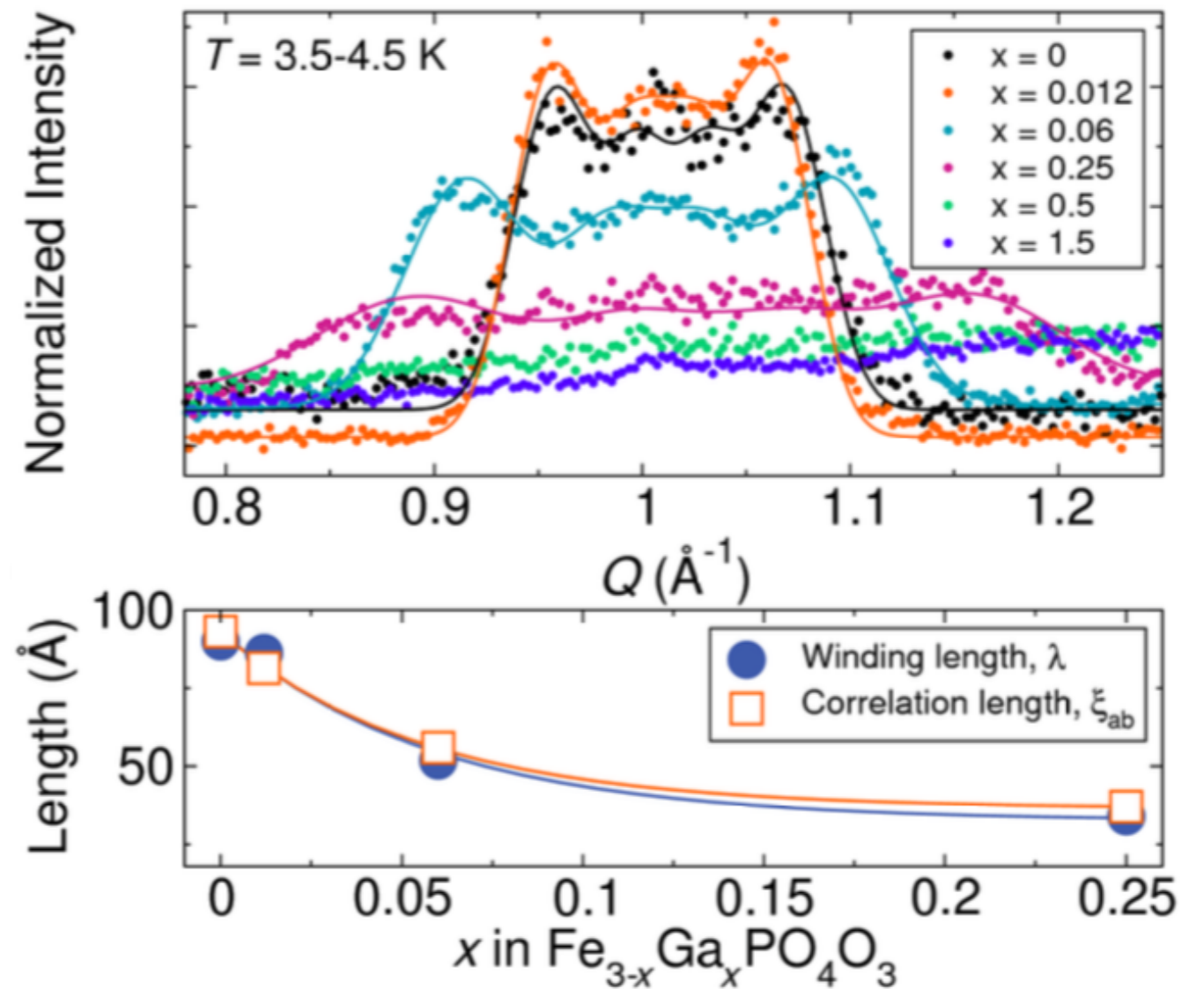


Correlation length and pitch length are connected!

Magnetic Dilution: $\text{Fe}_{3-x}\text{Ga}_x\text{PO}_4\text{O}_3$

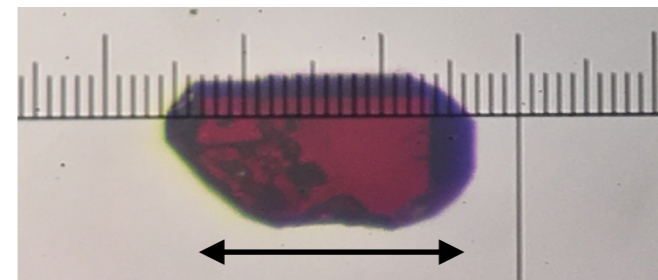


Helical pitch and
“domain radius” are
tracking each other!
What could cause this?

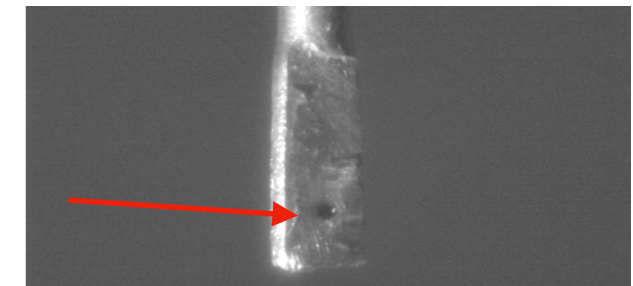


Neutron Diffraction: single crystals

- Crystals grown by chemical vapor transport by Neilson group at CSU
- But they are *tiny*: need huge neutron flux, 2D area detector, and a focusing monochromator



0.33 mm

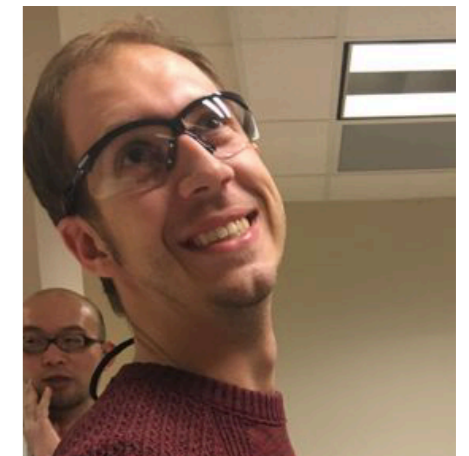


HB-3A at High Flux Isotope Reactor (HFIR)

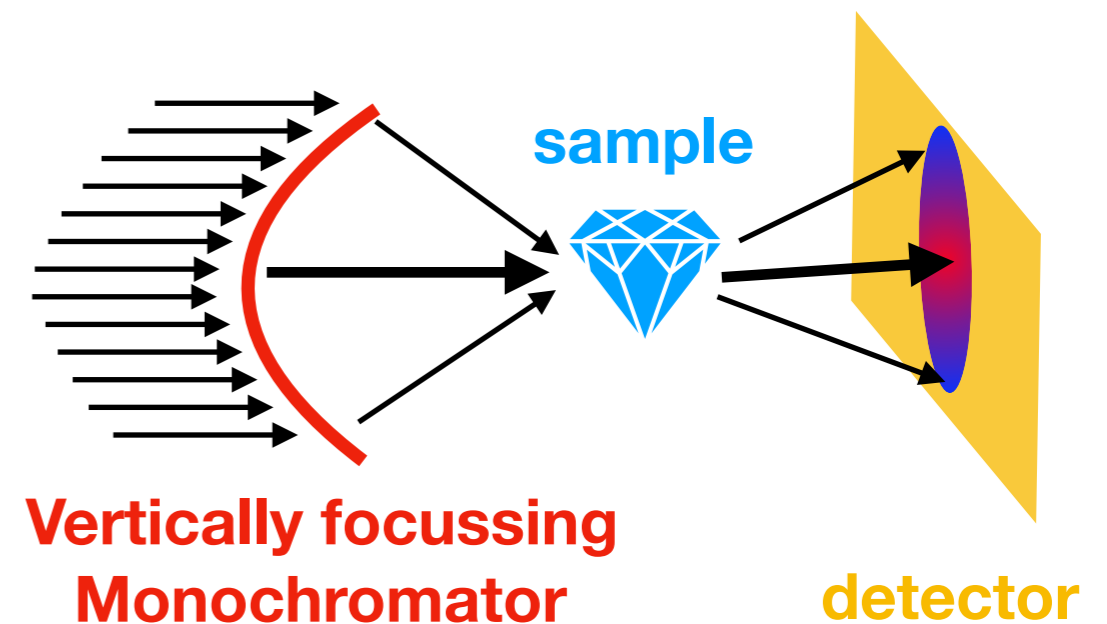
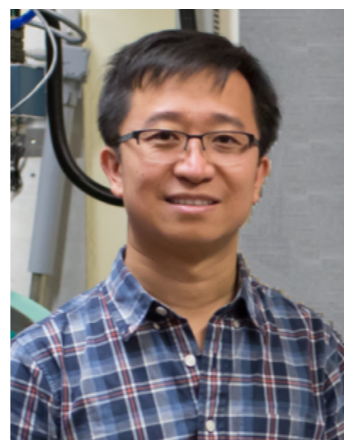
Jamie Neilson



Michael Tarne



Huibo Cao

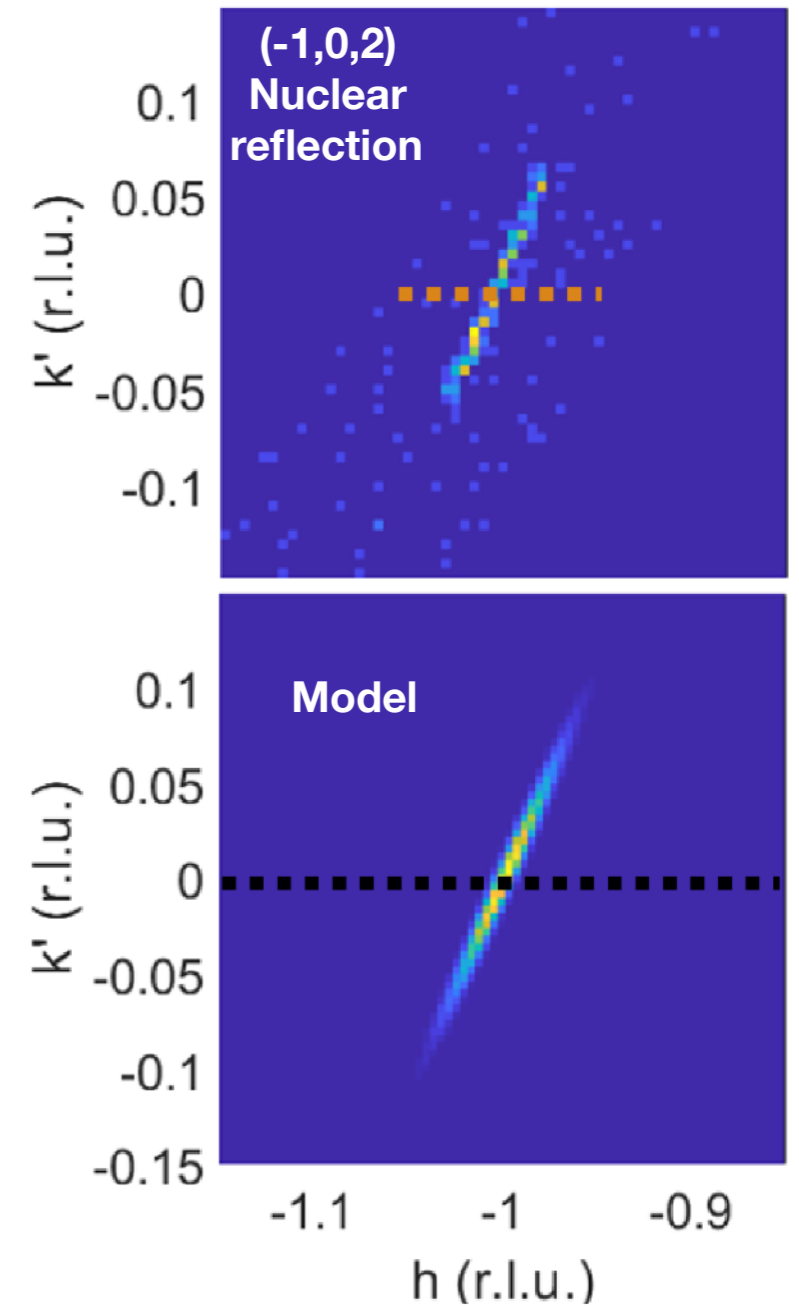
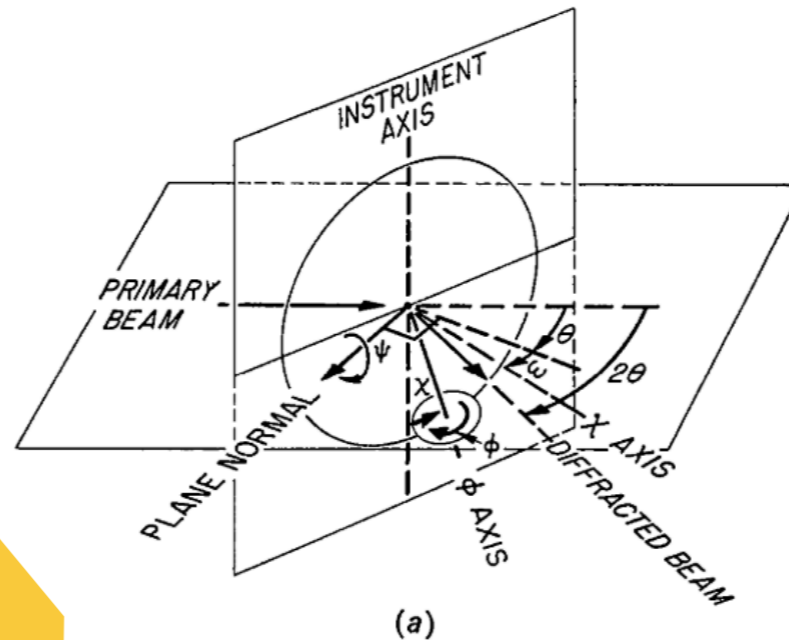
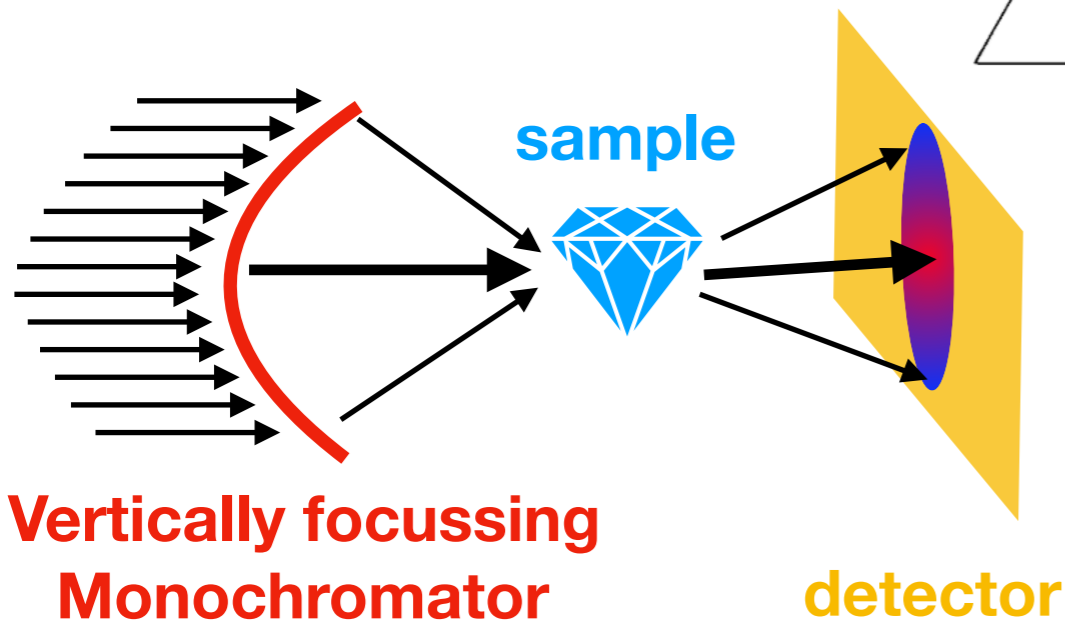


Modeling resolution function: key to success!

- Vertical focusing/divergence creates a very elongated ellipsoid for resolution function
- Resolution function rotates into hkl differently depending on specific measurement conditions



Colin Sarkis



Acta Cryst. (1967). **22**, 457

Angle Calculations for 3- and 4- Circle X-ray and Neutron Diffractometers*

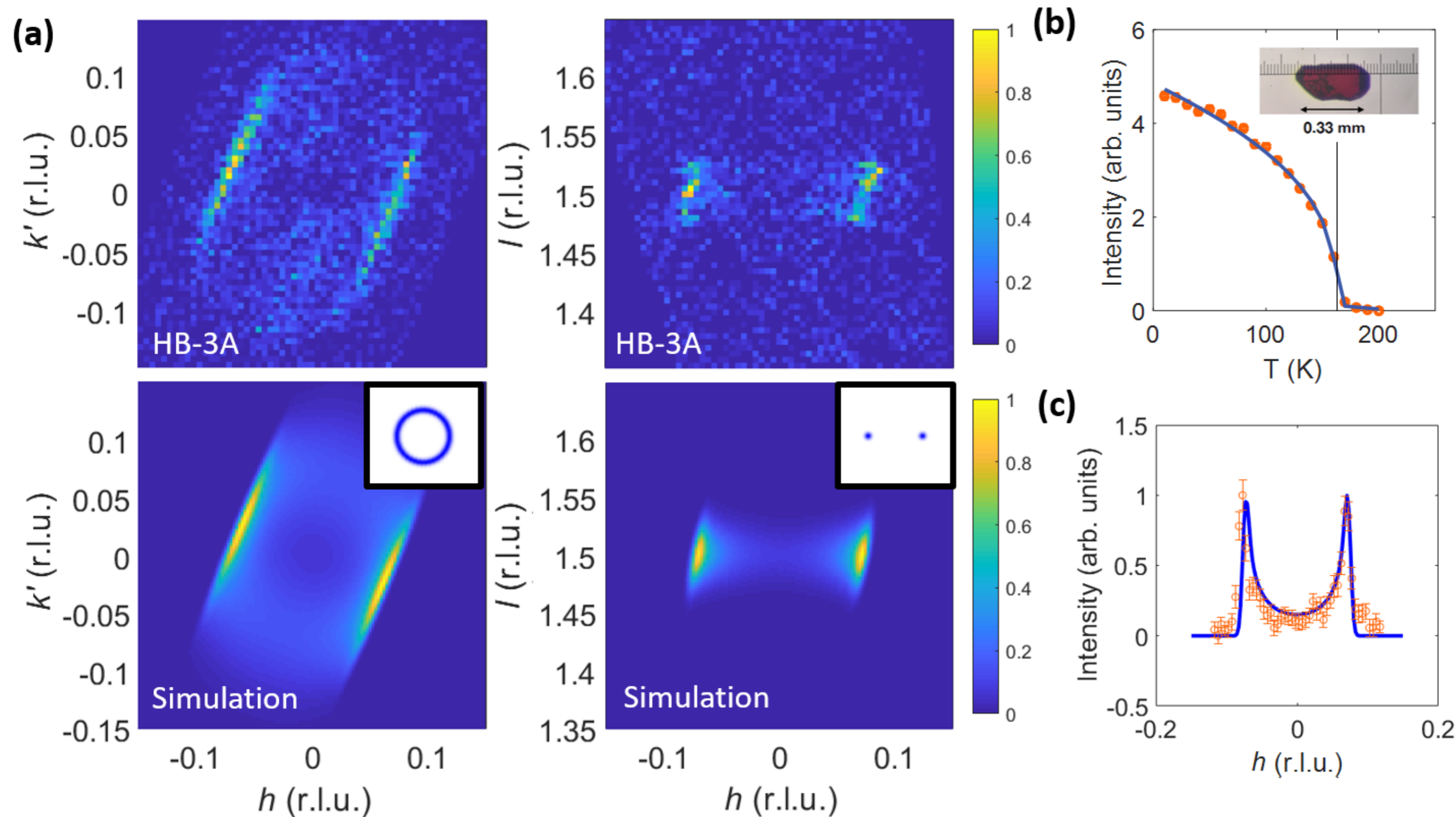
By WILLIAM R. BUSING AND HENRI A. LEVY

Chemistry Division, Oak Ridge National Laboratory, Oak Ridge, Tennessee 37830, U.S.A.

(Received 13 June 1966)

"Incommensurate Rings" in Structure Factor: Helical modulation with no preferred direction

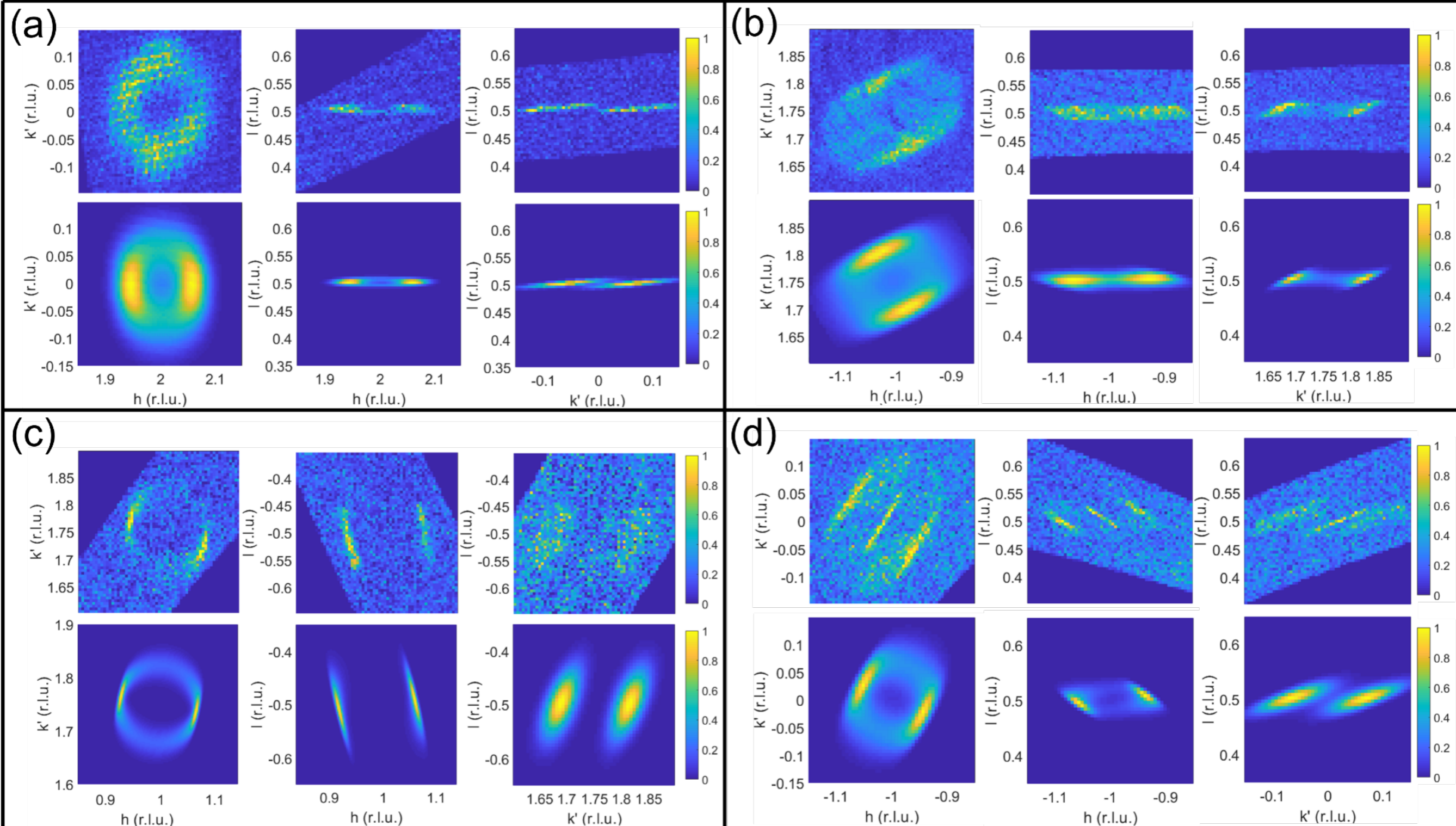
Incommensurate ordering wave vector
ring around (0,0,1.5): $\lambda = 98 \pm 12 \text{ \AA}$



"Incommensurate Rings" in Structure Factor: Helical modulation with no preferred direction

(2,0,0.5)

(-2,2,0.5)



(0,2,-0.5)

(-2,2,0.5)

Quasi-degenerate ring of k -vectors in the frustrated Heisenberg model

Ethan Coldren

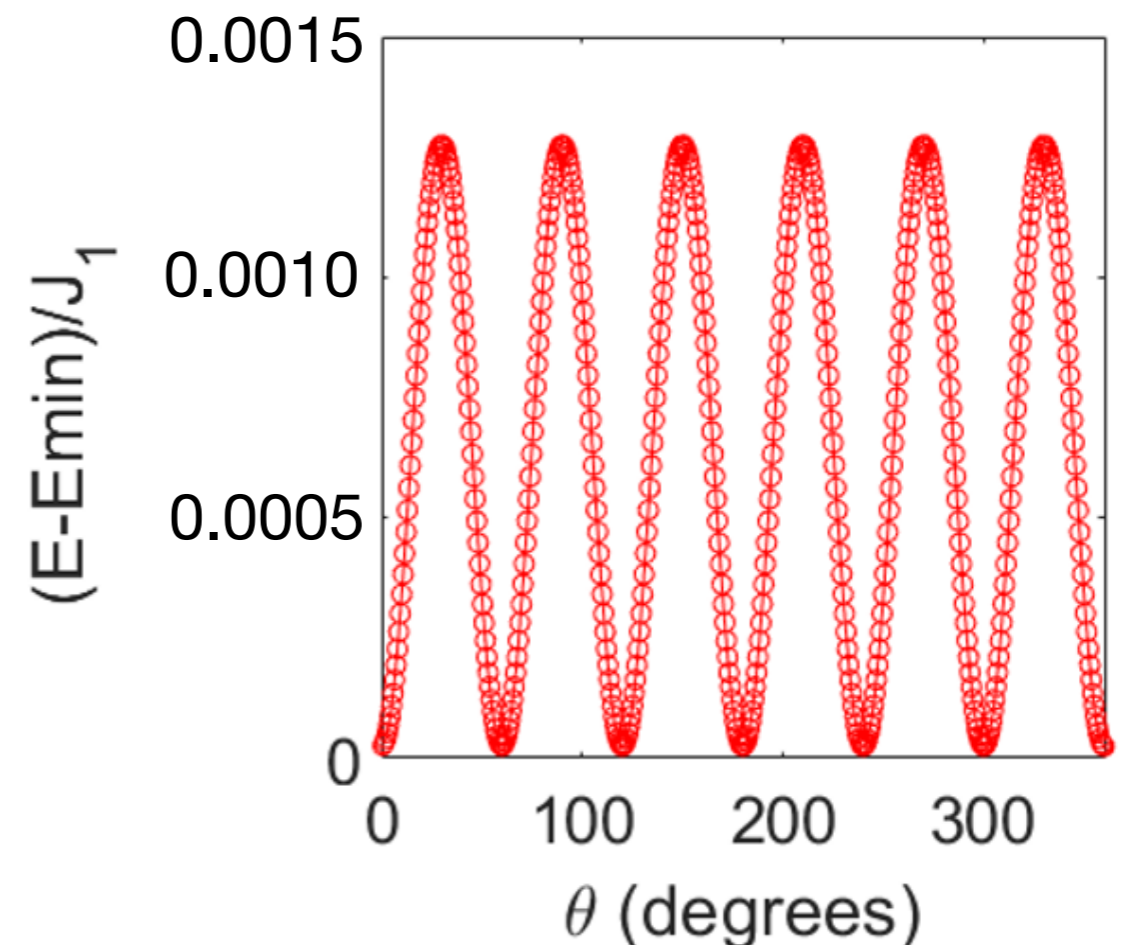
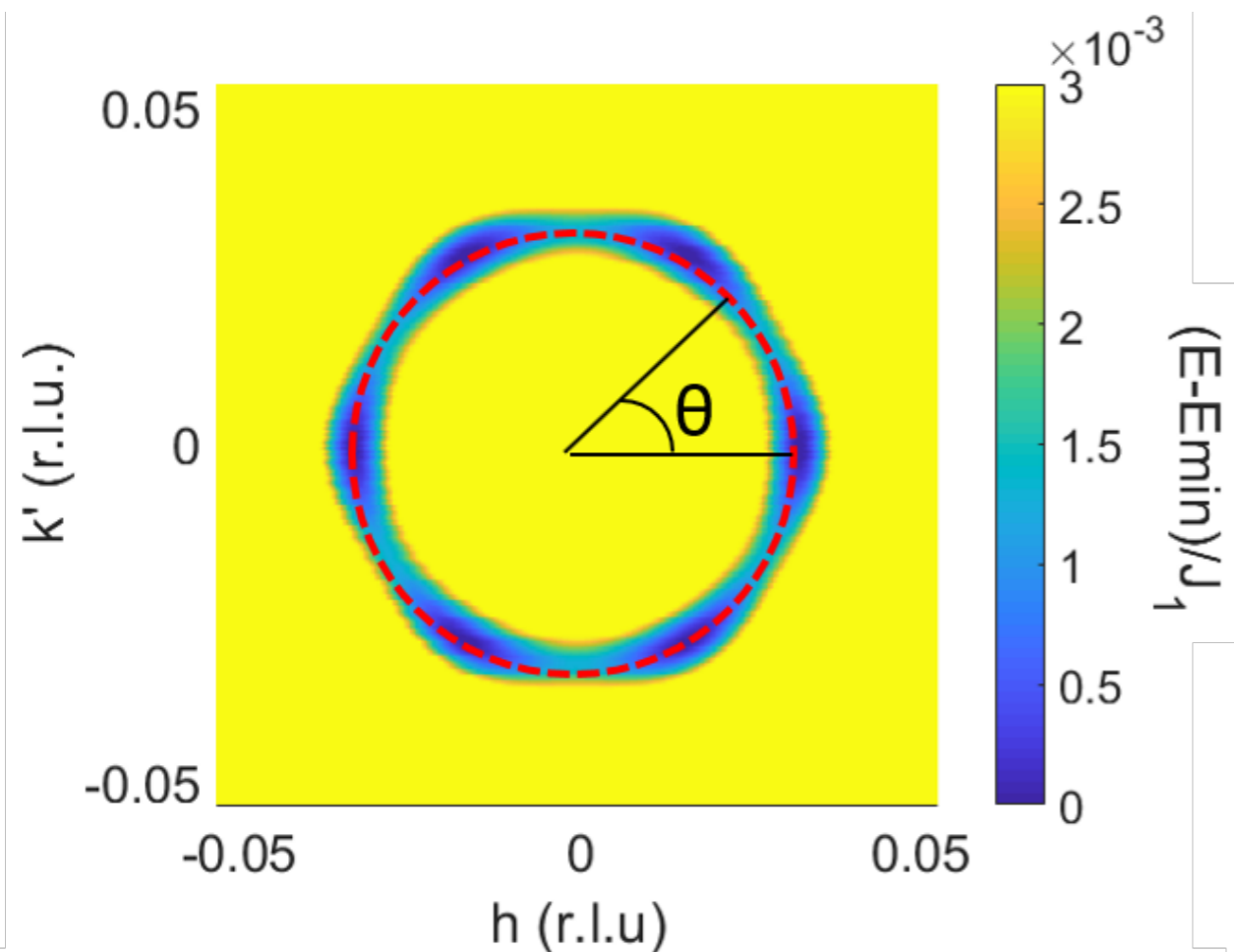


$$H = \sum_{n.n.} J_1 \vec{S}_i \cdot \vec{S}_j + \sum_{n.n.n.} J_2 \vec{S}_i \cdot \vec{S}_j$$

Marty Gelfand

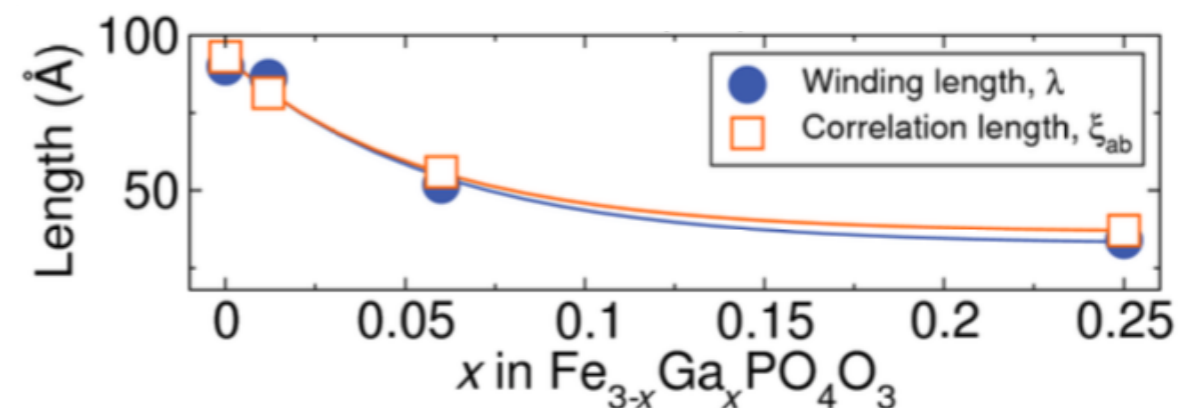
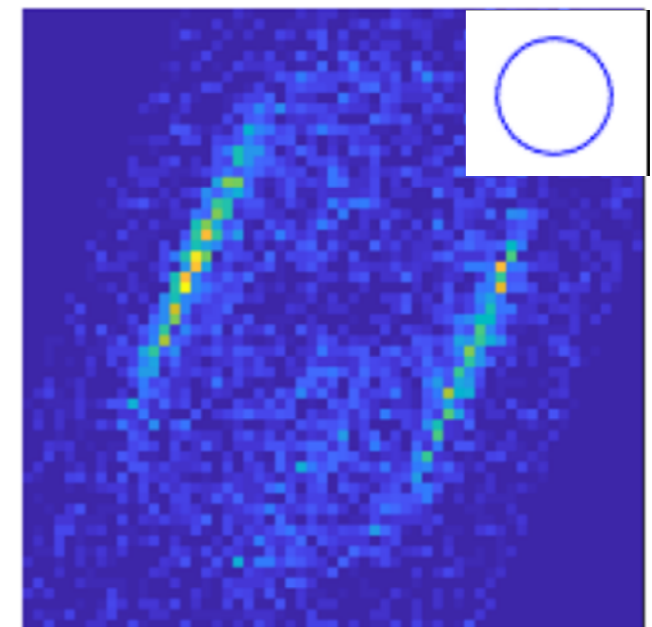
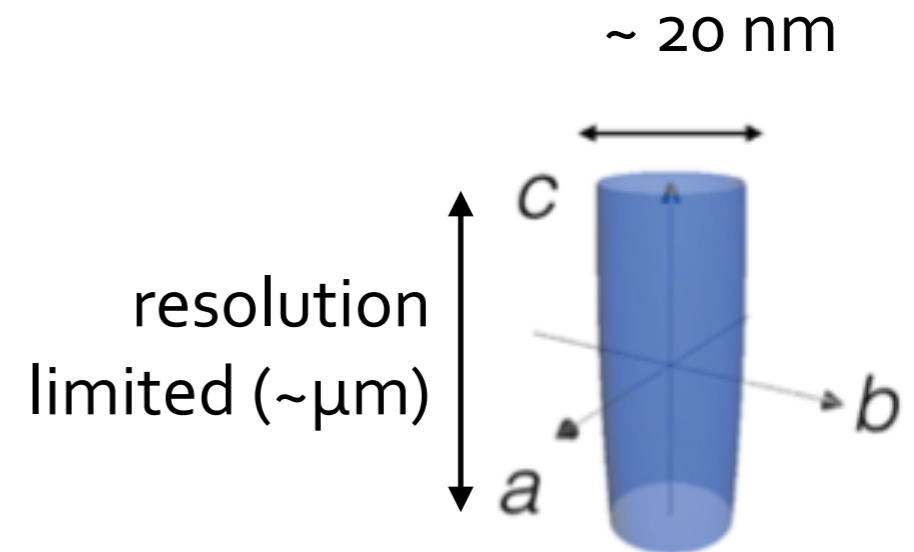


Luttinger-Tisza shows that energetic variation around the ring is ~ 400 mK (aka **TINY!**) for $J_1 \sim 319$ K and $J_2/J_1 \sim 1.9$, appropriate for $\text{Fe}_3\text{PO}_4\text{O}_3$



So what do we have?

- $\text{Fe}_3\text{PO}_4\text{O}_3$ has **needle-like domains of antiferromagnetic helical (partial) order**
- **The helical order does not have a preferred modulation direction:** (quasi-)degenerate ring of ordering wavevectors is observed, and is consistent with $J_1 - J_2$ frustrated Heisenberg model
- **Correlation length in ab plane *tracks* helical pitch length**



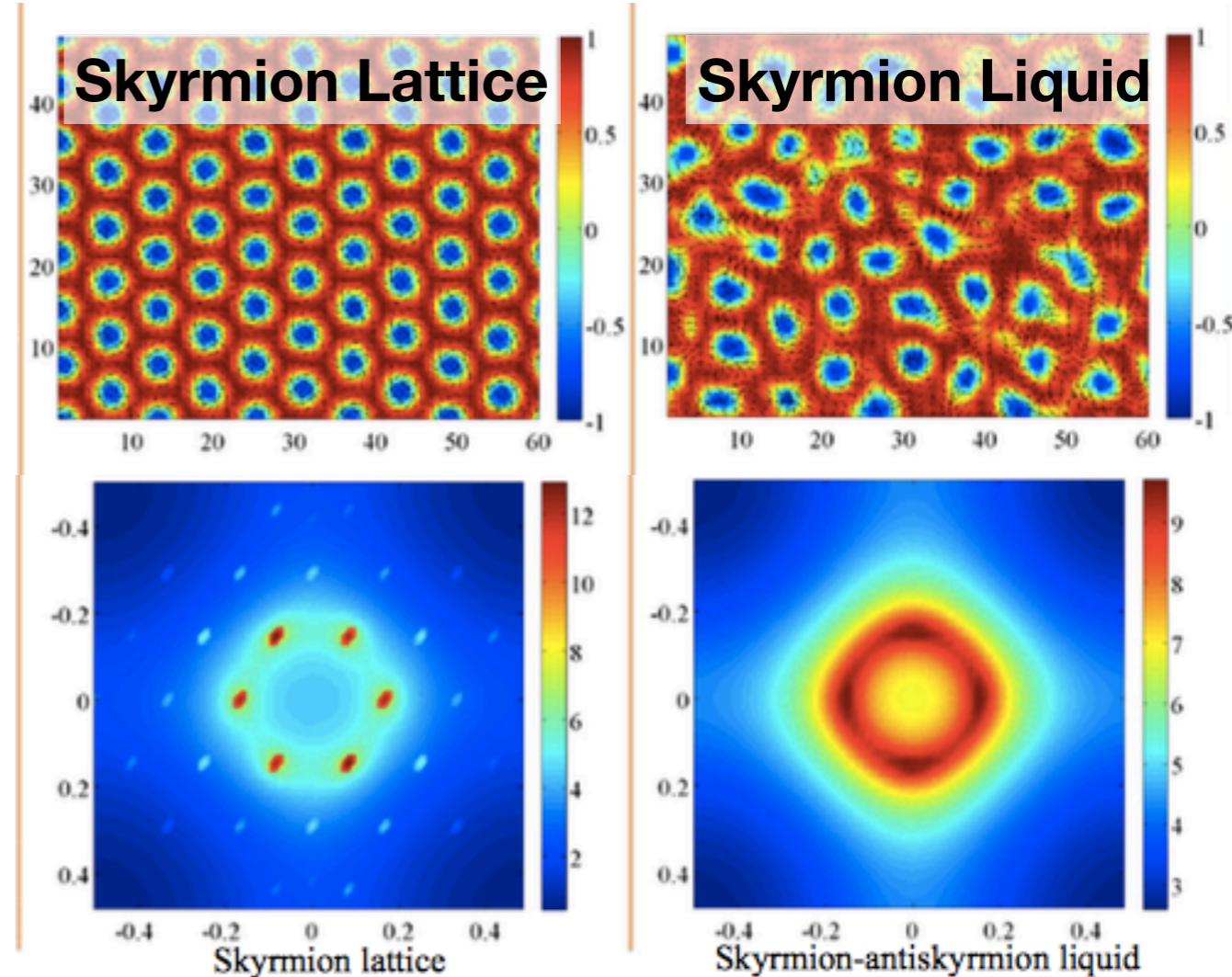
Skyrmion-like liquid / glass in $\text{Fe}_3\text{PO}_4\text{O}_3$?

- "Skyrmion liquids" can be seen above ordering transitions
- **Skyrmion-Skyrmion distance** is the same as in the Skyrmion lattice phase, i.e. **set by helical pitch length**

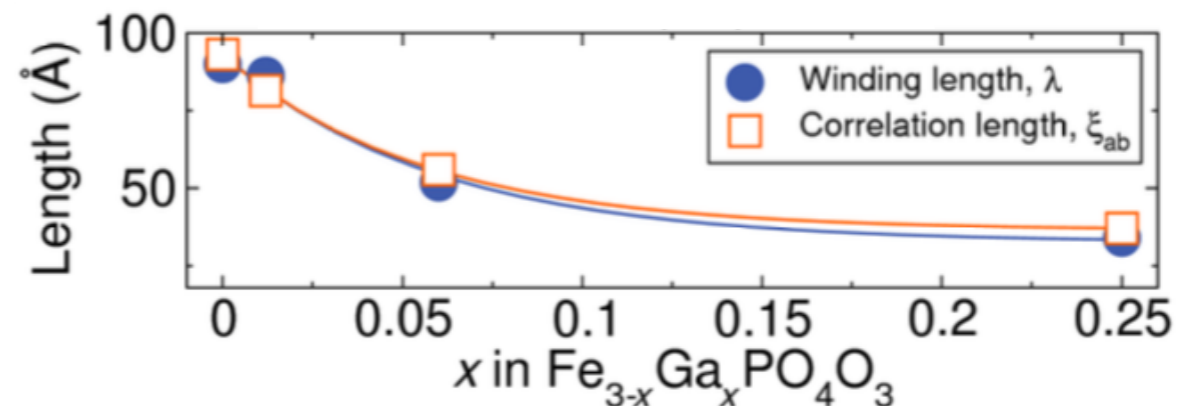
Spin configuration

Spin Structure factor

Monte Carlo: J_1 - J_2 - J_3 Square Lattice, H_{app}

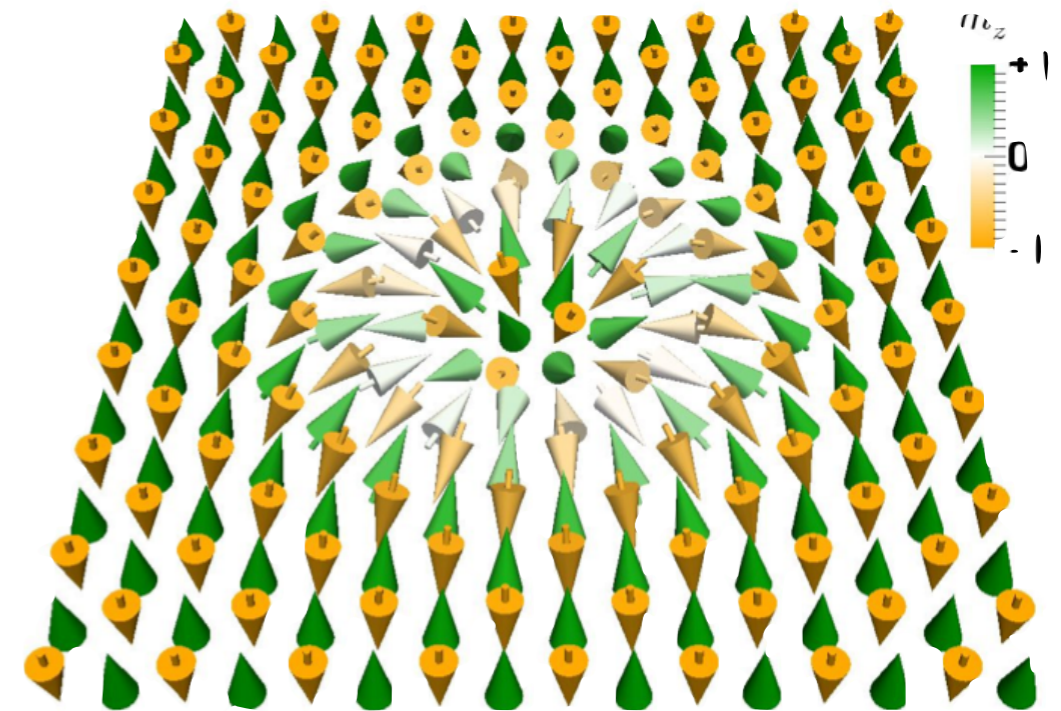


S.Z. Lin, S. Hayami, PRB 93 064430 (2016)

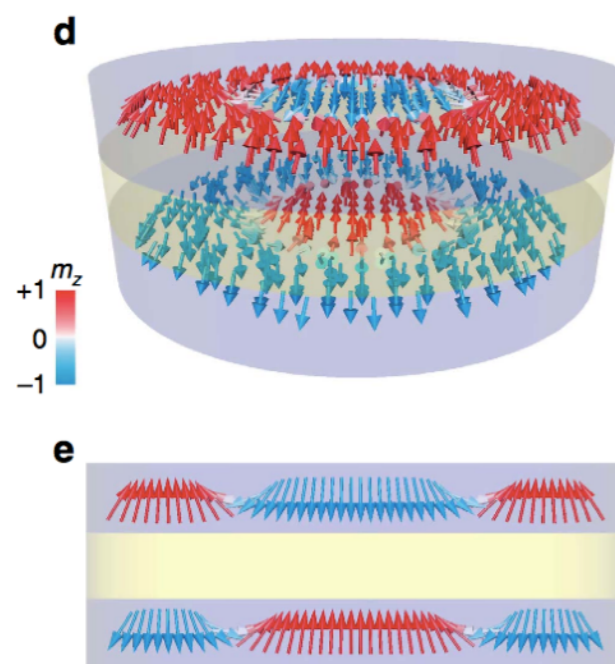


Locally Antiferromagnetic Skymions

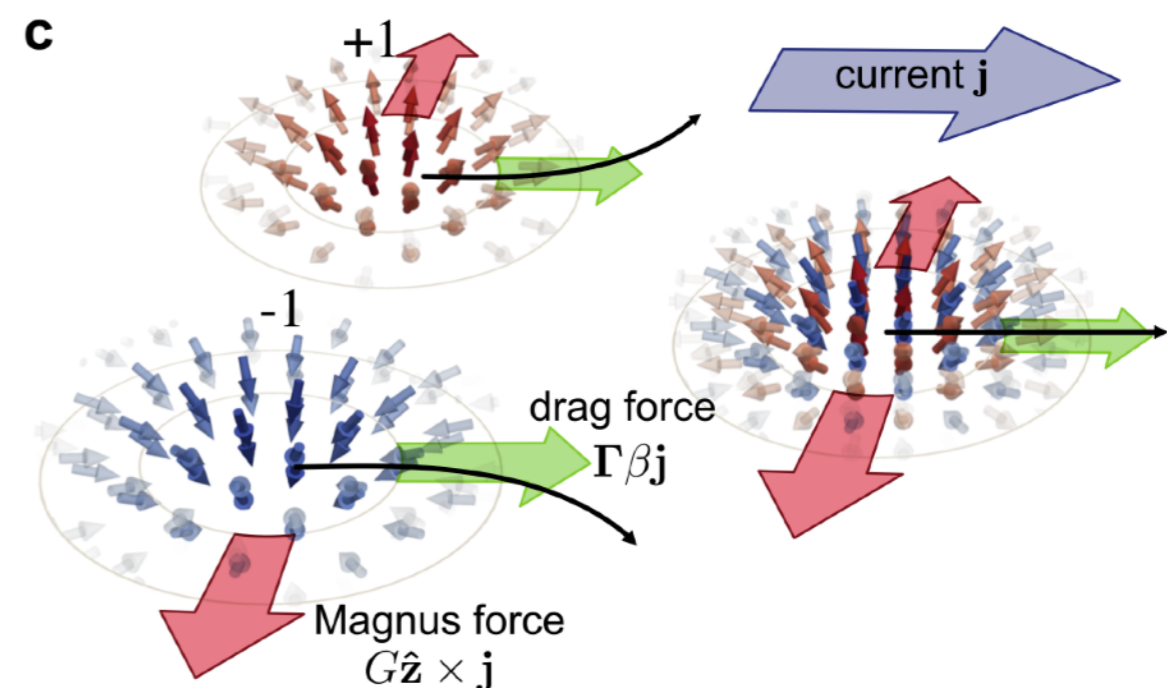
- locally compensated moments in a single layer or as “bilayers”
- Stable against stray fields (Magnus force), smaller — better for information processing
- Recently made in a synthetic antiferromagnet: Legrand et al, Nat. Mater. 2019



Zhang, Zhou, Ezawa, *Sci. Rep.* 6, 24795 (2016)



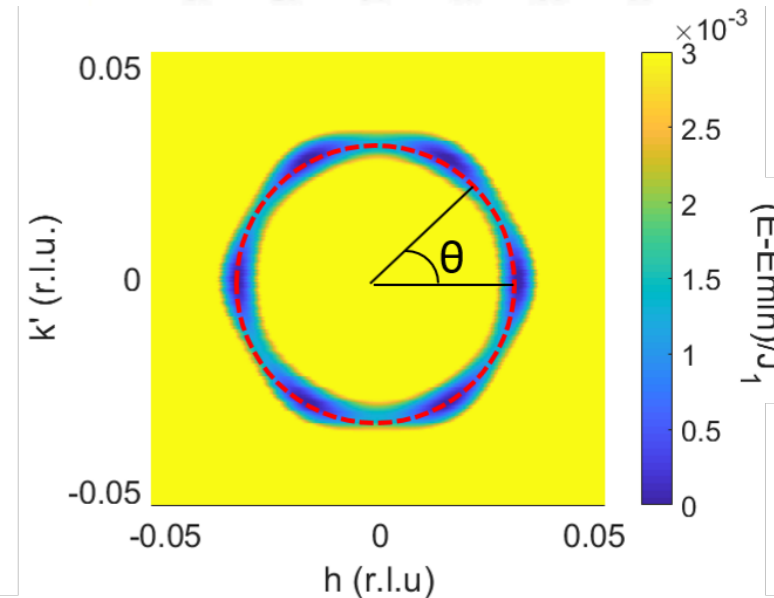
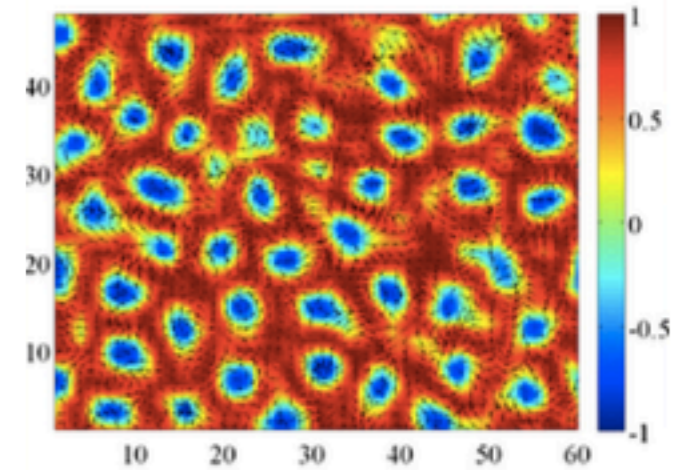
X. Zhang et al, Nat.Comm, 7, 102932016 (2016)



Barker, Tretiakov, PRL 116, 147203 (2016)

Open questions in $\text{Fe}_3\text{PO}_4\text{O}_3$

- If $\text{Fe}_3\text{PO}_4\text{O}_3$ displays a (frozen?) AFM Skymion-like phase (or something like Blue phase), how are the spin textures / defects stabilized?
- What role does the quasi-degeneracy of the frustrated J_1 - J_2 model play in generating these textures? What role does the DM interaction play?
- **How to see the spin structure in real space?**
NOTE: compensated moments, no net field!
- What are the *dynamics* of this weird magnetic phase? Can it be manipulated with e.g. thermal gradients, electric fields?



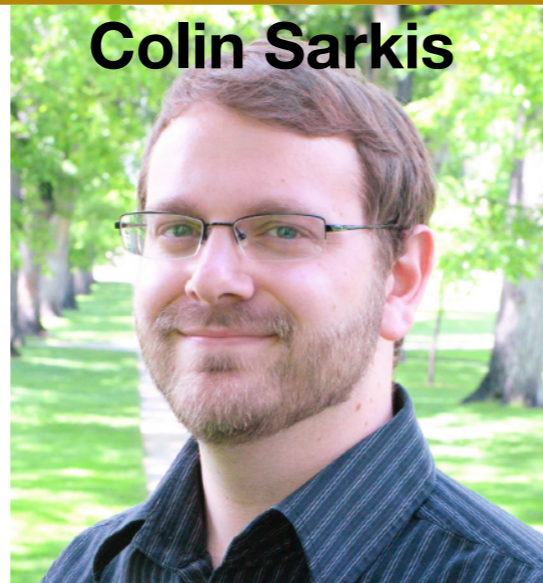
Acknowledgements

K. A. Ross, et al. Phys. Rev. B **92**, 134419 (2015)

M. J. Tarne, et al. Phys. Rev. B **96**, 214431 (2017)

**C. Sarkis, et al. arXiv:1910.08818 [cond-mat.str-el]
(2019)**

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- **Michael Tarne** (CSU)
- **Ethan Coldren** (CSU)
- **Jamie Neilson** (CSU)
- Marty Gelfand (CSU Physics)
- Huibo Cao (ORNL)
- Stuart Calder (ORNL)
- Craig Brown (NIST)



Ethan Coldren



Marty Gelfand



Huibo Cao

