

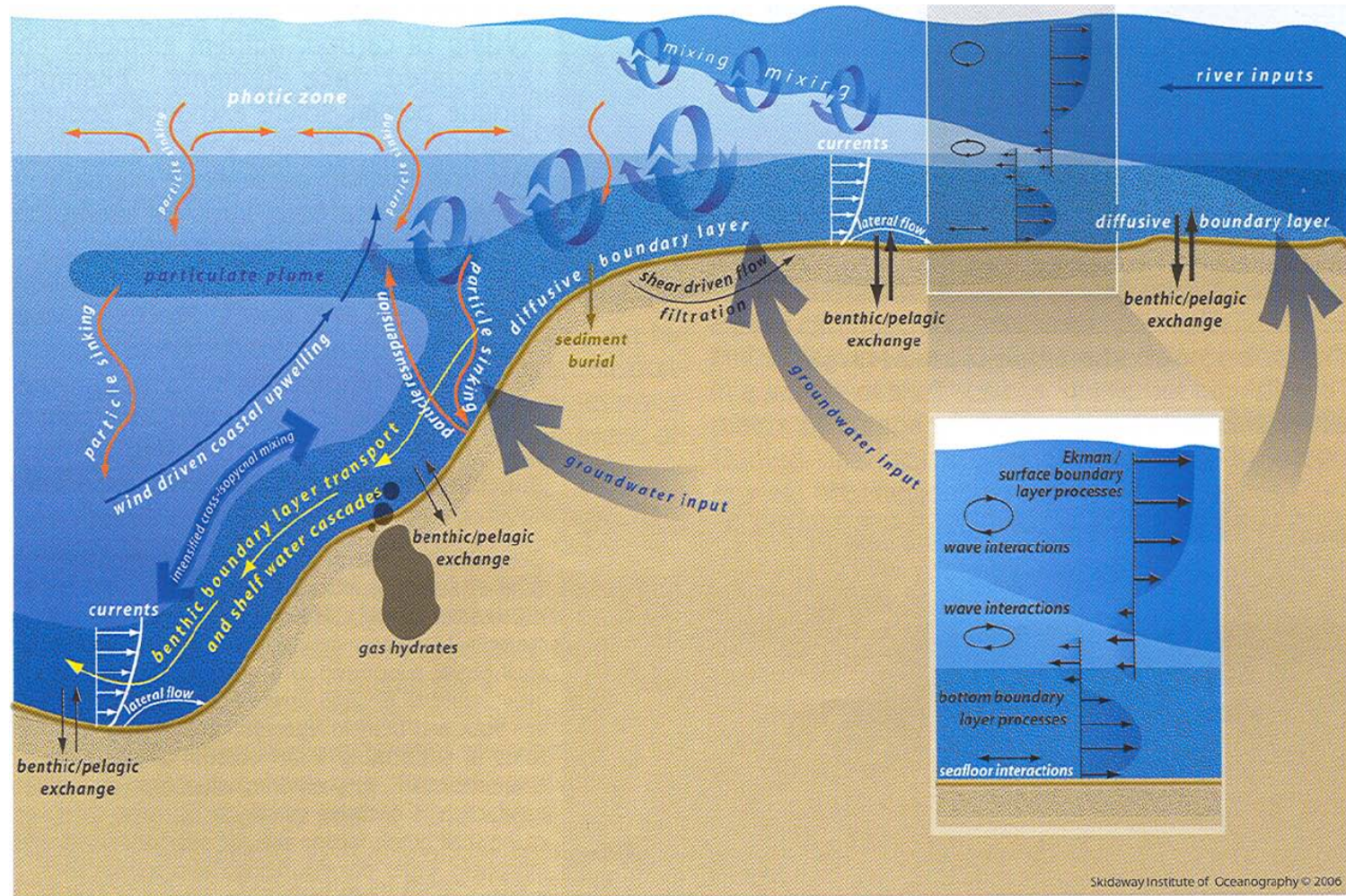
# *Double-diffusive sedimentation*

*Peter Burns and Eckart Meiburg*

*UC Santa Barbara*

- *Motivation*
- *Governing equations*
- *Results: buoyant river outflows:*
  - *double-diffusive sedimentation*
  - *'fingering' vs. 'leaking' modes*
- *Scaling analysis and physical interpretation*
- *Summary and outlook*

# Coastal margin processes

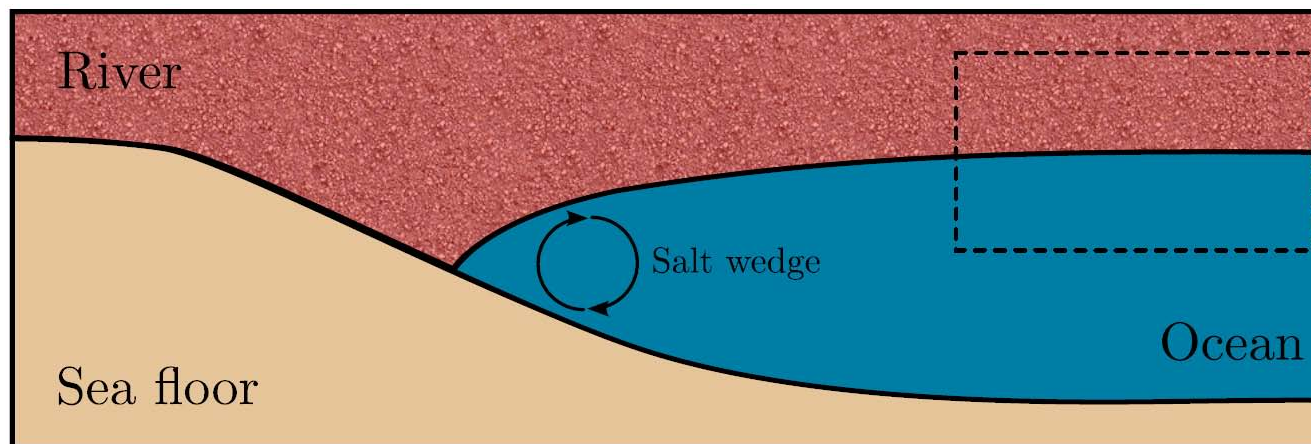


# *Sedimentation from river plumes: Configuration*

## *Hypopycnal river plumes:*

*density of the river (fresh water + sediment) < density of ocean (water + salinity)*

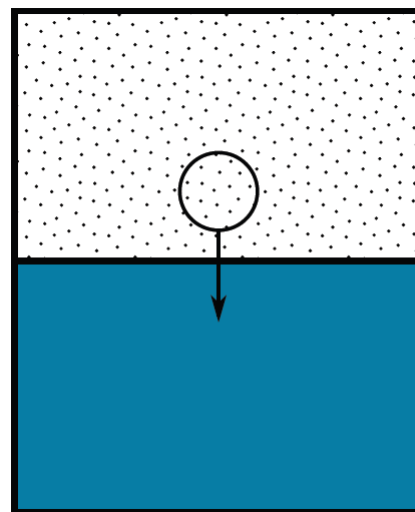
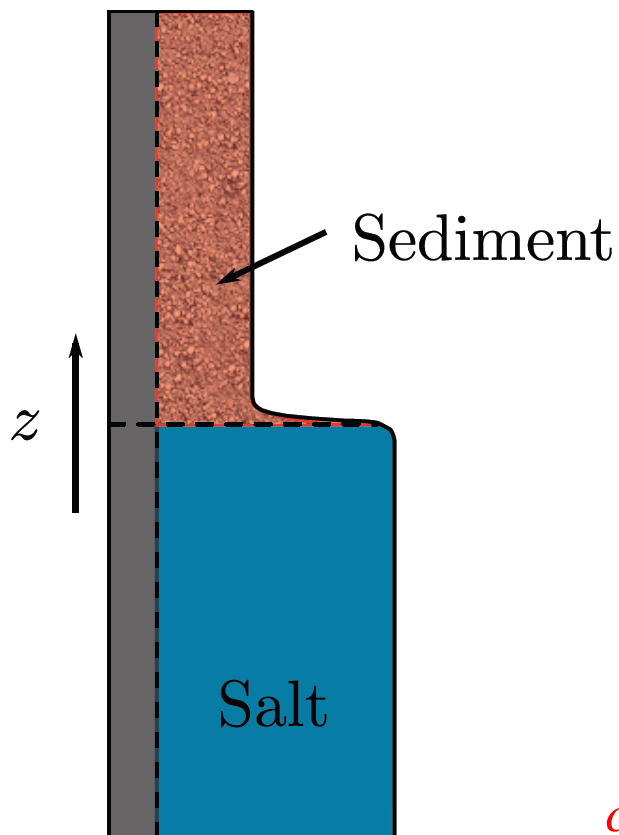
*→ river outflow propagates along the ocean surface*



- focus on the downstream density stratification*

# *Sedimentation from river plumes: Double-diffusion*

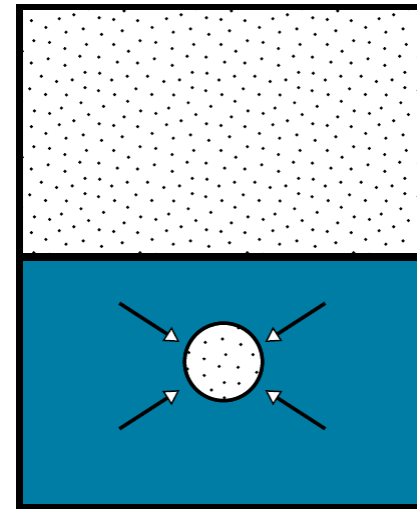
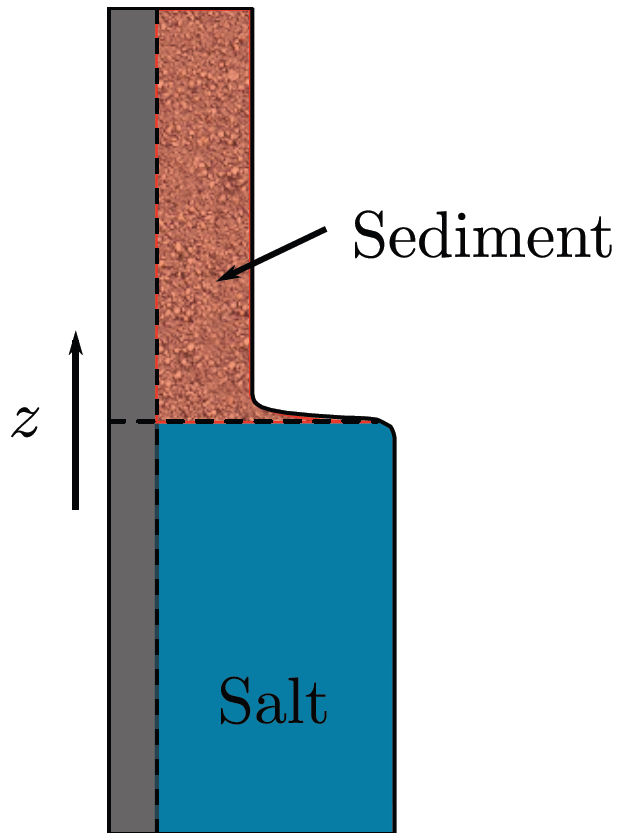
*Base density profile:*



*consider local downward perturbation of  
fluid element across opposing gradients*

# *Sedimentation from river plumes: Double-diffusion*

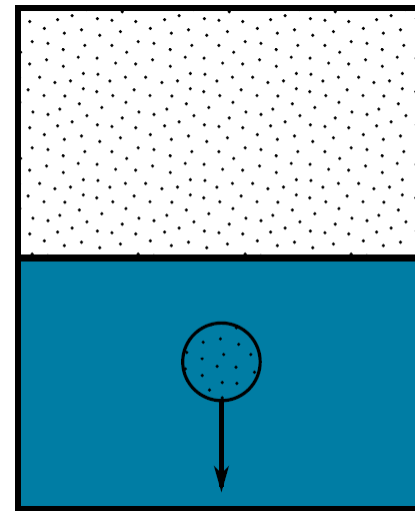
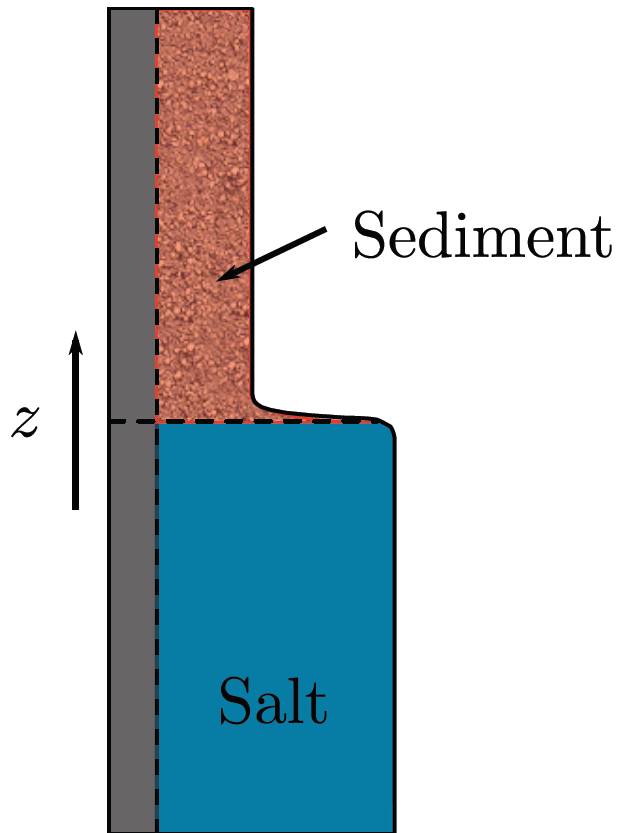
*Base density profile:*



*salinity diffuses inward more rapidly  
than particles diffuse outward*

# *Sedimentation from river plumes: Double-diffusion*

*Base density profile:*



*→ fluid element will continue to sink*

- potential for double-diffusive instability*

## *Traditional case: Salt fingers*

- *warm, salty water above cold, fresh water:*



*Huppert and Turner (1981)*

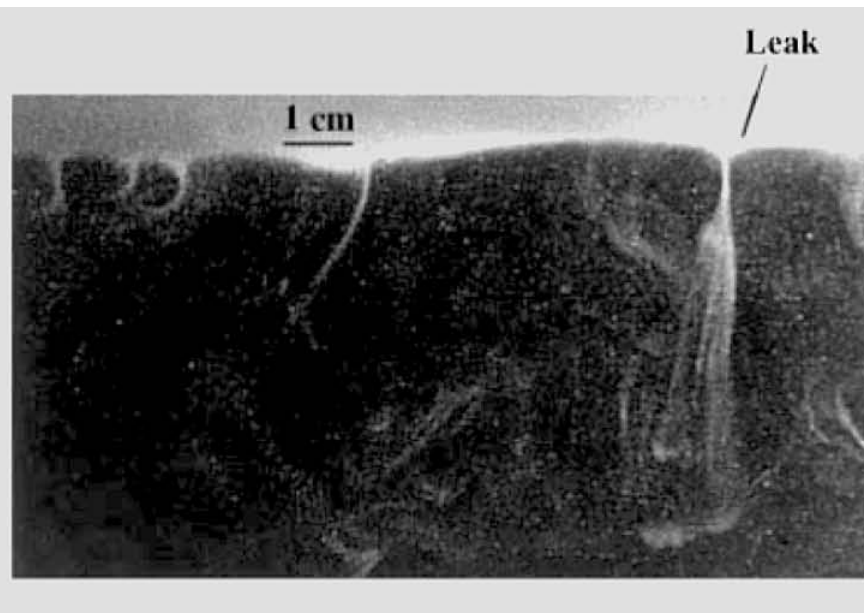
- *dominant process for the vertical flux of salt in the ocean*
  - *robust against shear*
  - *believed to be responsible for the formation of the thermohaline staircase*
- *for salt/sediment system, how does double-diffusion affect sedimentation?*

# *Sedimentation from river plumes: Experiments*

- previous experimental work by Parsons et al. (2001):*



*convective 'fingering' mode  
space filling*



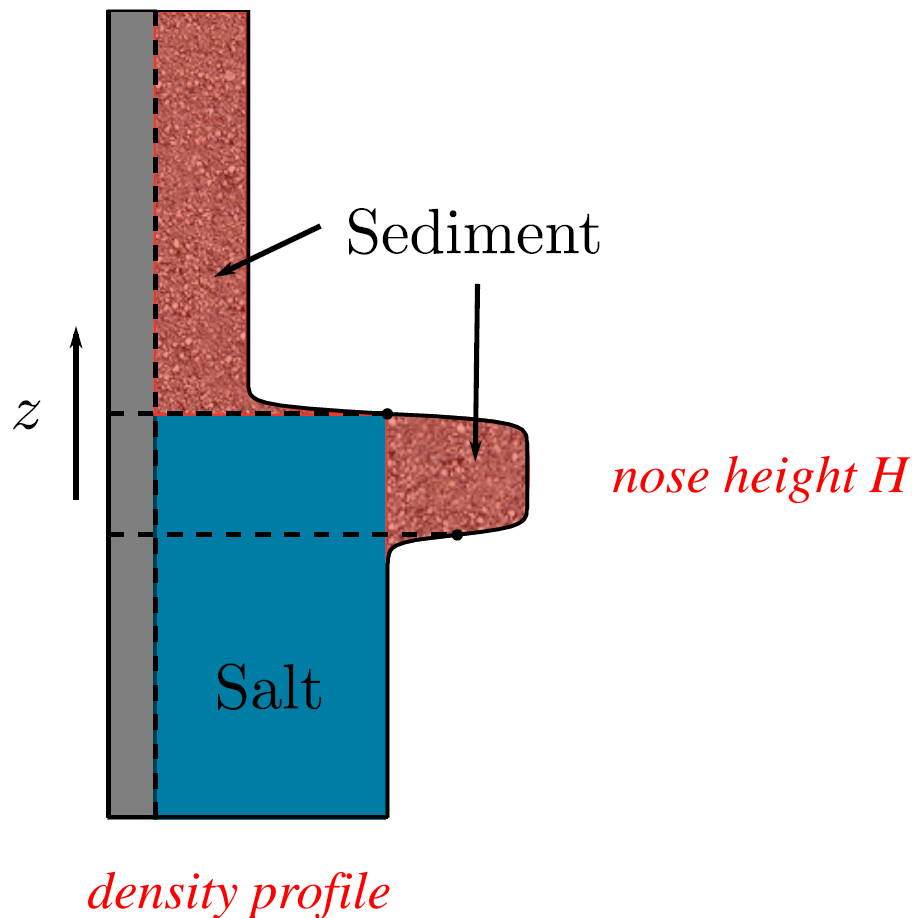
*'leaking' mode  
localized, structures move along interface*

*→ goal: understand mechanisms driving these modes, and their influence on  
the effective particle settling velocity*



# *Sedimentation from river plumes*

*Effect of settling velocity:*



- settling process creates potential for Rayleigh-Taylor instability*

## *Framework: Dilute flows*

### *Assumptions:*

- *volume fraction of particles  $< O(10^{-3})$*
- *particle radius  $\ll$  particle separation*
- *small particles with negligible inertia*

### *Dynamics:*

- *effects of particles on fluid continuity equation negligible*
- *coupling of fluid and particle motion primarily through momentum exchange, not through volumetric effects*
- *particle loading modifies effective fluid density*
- *particles follow fluid motion, with superimposed settling velocity*

## Moderately dilute flows: Two-way coupling (cont'd)

*Governing dimensionless eqns:*

$$\rho - 1 = \alpha S + \gamma C$$

$$\nabla \cdot \mathbf{u} = 0$$

$$\frac{\partial \mathbf{u}}{\partial t} + \mathbf{u} \cdot \nabla \mathbf{u} = \nabla^2 \mathbf{u} - \nabla \mathcal{P} + \rho' \frac{\mathbf{g}}{g'}$$

$$\frac{\partial S}{\partial t} + \mathbf{u} \cdot \nabla S = \frac{1}{Sc} \nabla^2 S$$

$$\frac{\partial C}{\partial t} - V_p \frac{\partial C}{\partial z} + \mathbf{u} \cdot \nabla C = \frac{1}{\tau Sc} \nabla^2 C$$

*Characteristic quantities:*

$$L^c = (\nu^2 / g')^{1/3}, \quad T^c = (L^{c2} / \nu),$$

$$U^c = (\nu g')^{1/3}, \quad g' = \frac{\Delta \rho_c}{\rho_0} g,$$

$$V_{st} = \frac{g d_p^2 (\rho_p - \rho_f)}{18 \mu_f}$$

*Dimensionless parameters:*

*settling velocity*  $V_p = \frac{V_{st}}{(\nu g')^{1/3}}$

*Schmidt number*  $Sc = \frac{\nu}{\kappa_s}$

*stability ratio*  $R_s = \frac{\alpha}{\gamma}$

*diffusivity ratio*  $\tau = \frac{\kappa_s}{\kappa_c}$

# *Sedimentation from river plumes: Numerical simulations*

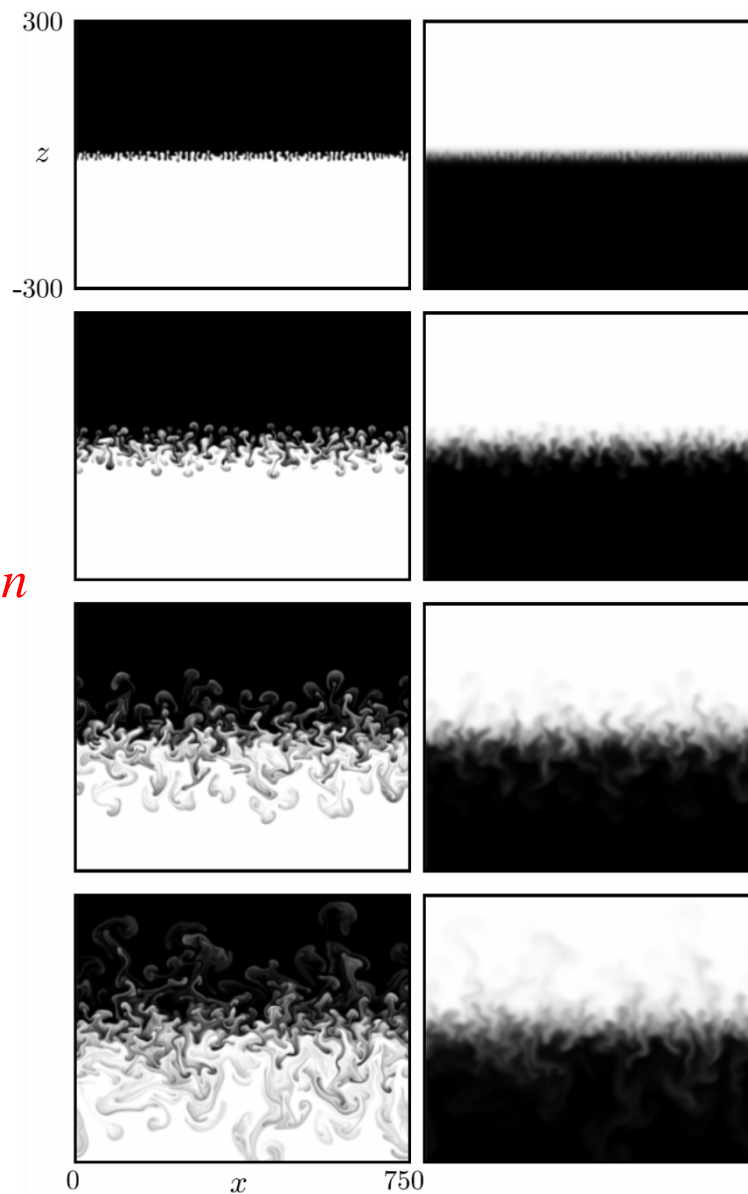
$$V_p = 0.04 ,$$

$$Sc = 0.7 ,$$

$$R_s = 2 ,$$

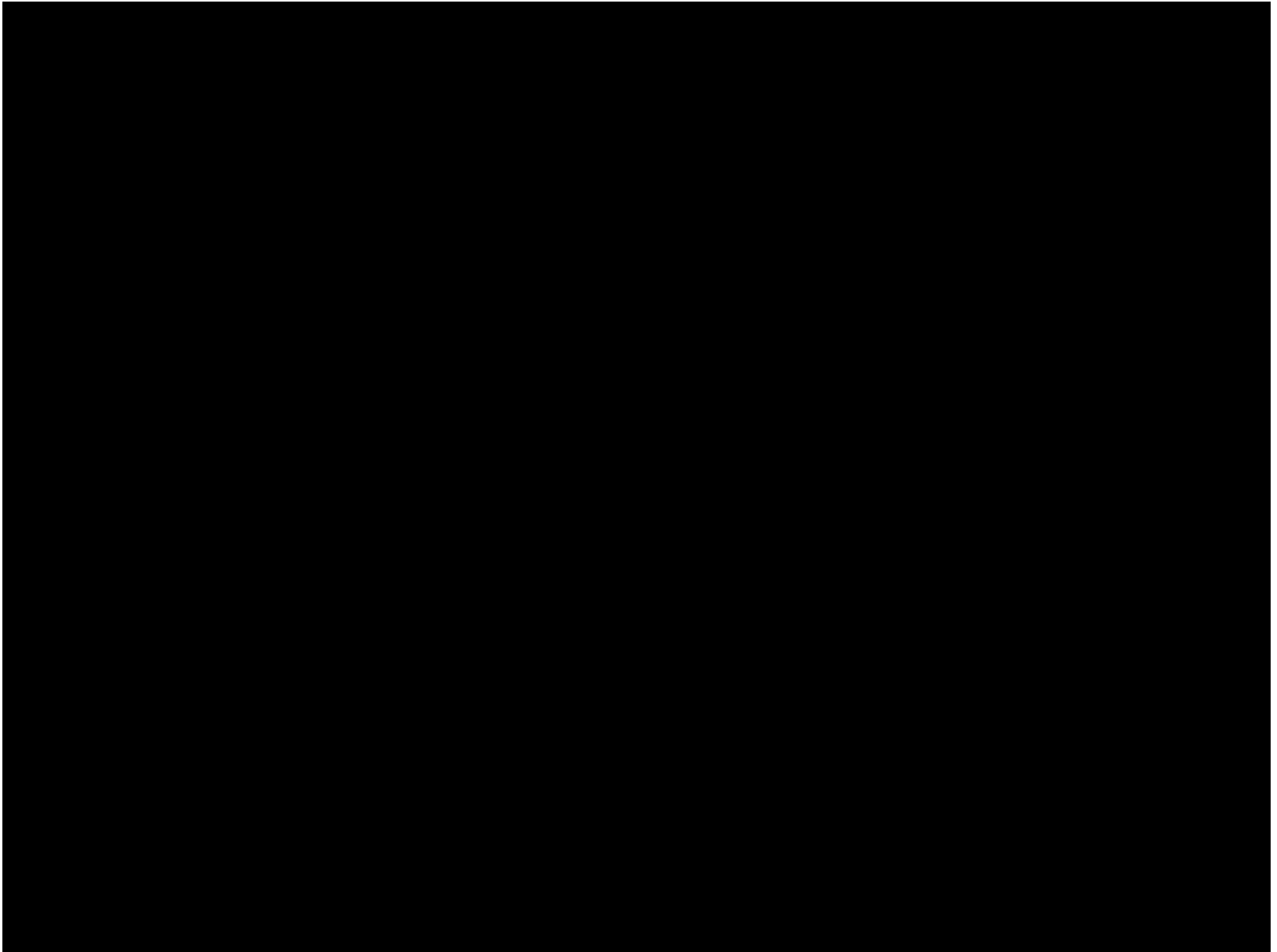
$$\tau = 25$$

*sediment concentration*



*salinity*

# *Sedimentation from river plumes: Numerical simulations*



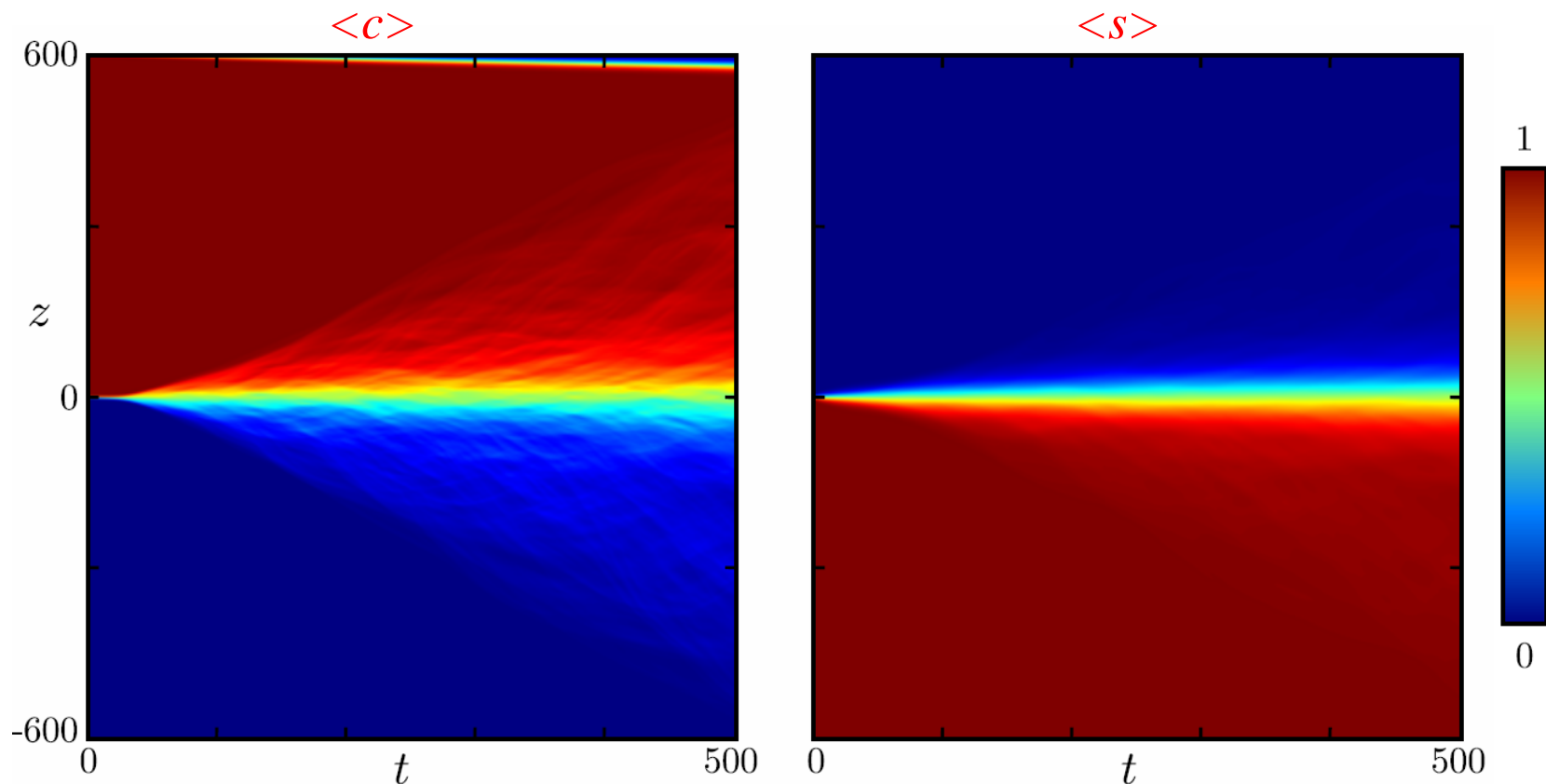
*Mammatus clouds*



*Volcanic ash plume*



## *Sedimentation from river plumes: Mean fields*



- *thickening of the plume-dominated region  $\sim$  time  $\rightarrow$  convectively dominated*
- *vigorous convective motion*
- *'streaks' due to the release of buoyant plumes*

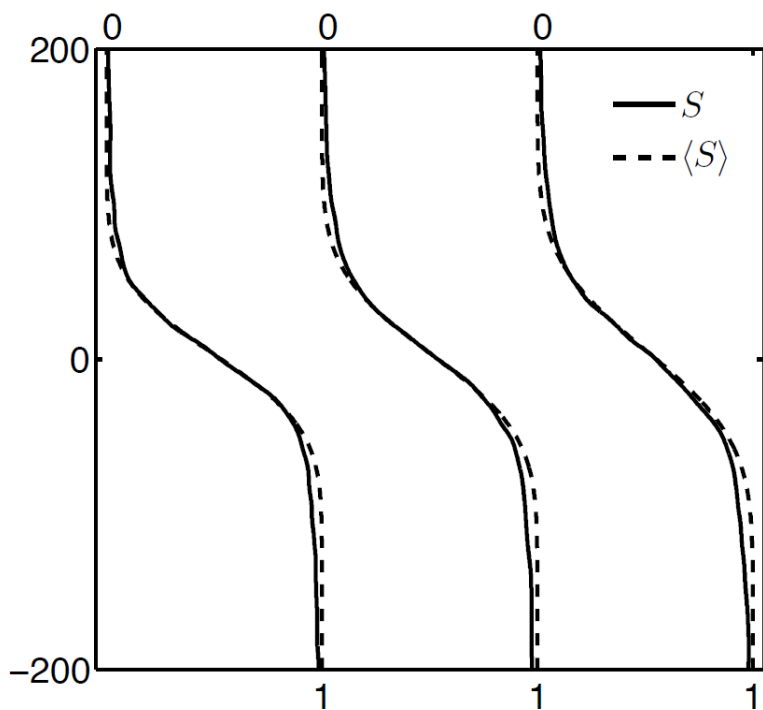
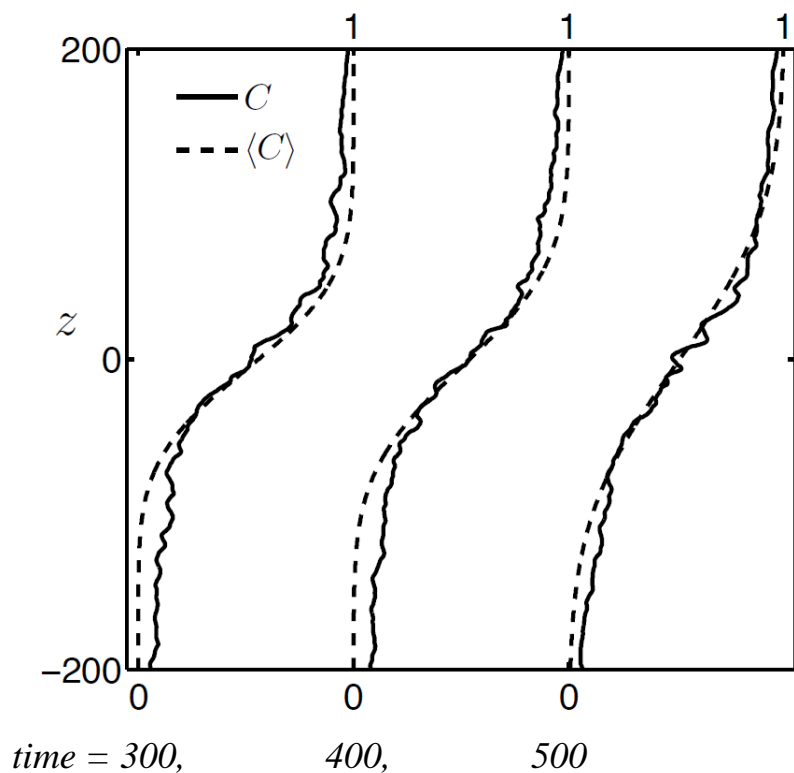


# *Sedimentation from river plumes: Mean fields*

*fit concentration profiles with erf  $\rightarrow$  determine interface location, thickness*

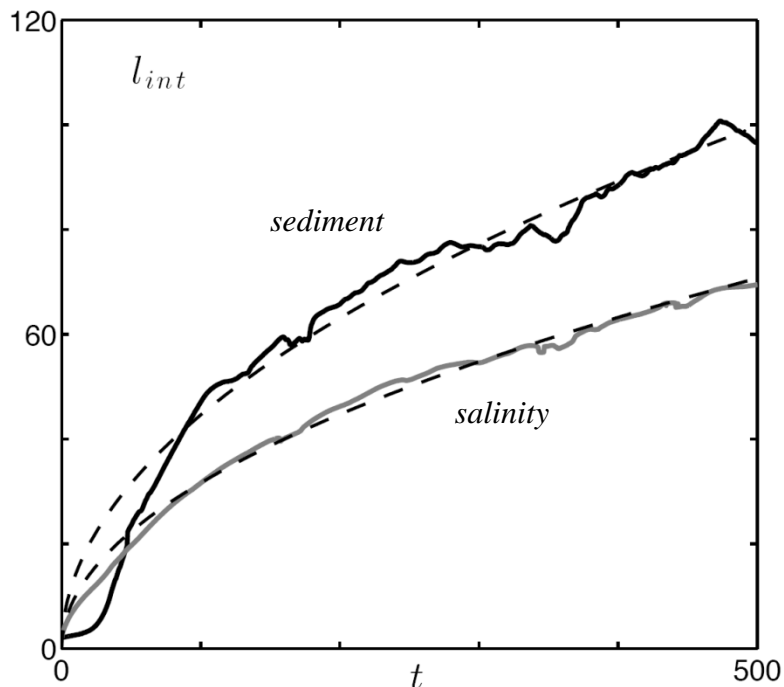
*sediment concentration*

*salinity*

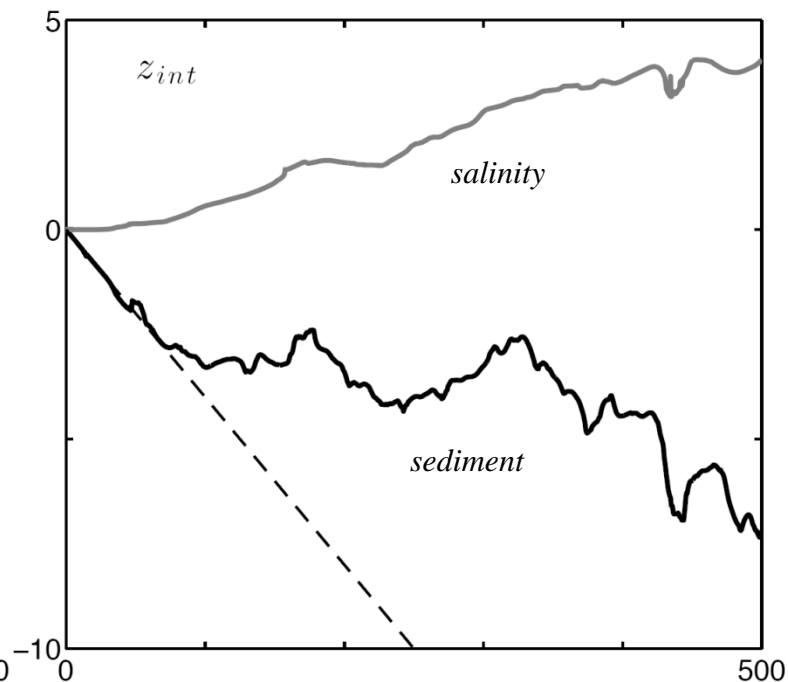


# *Sedimentation from river plumes: Mean fields*

*interface thickness*



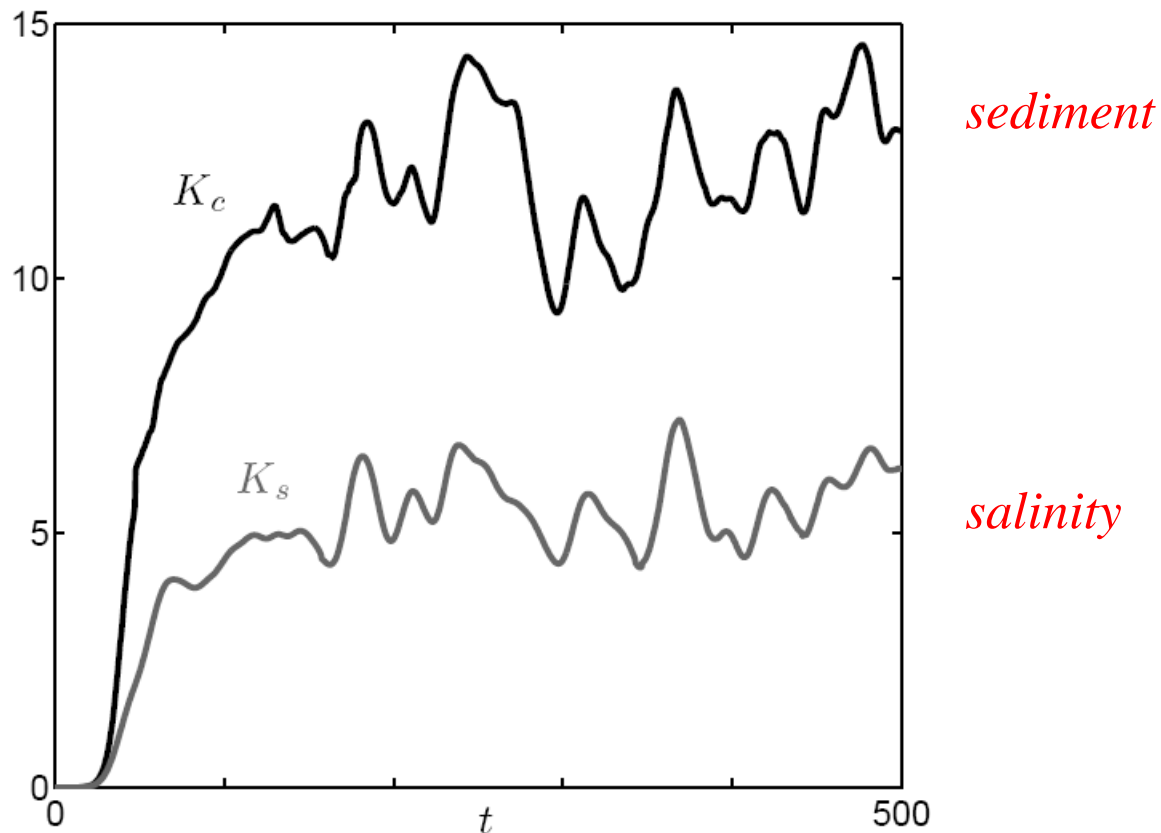
*interface location*



- *both interface thicknesses grow diffusively*
- *sediment interface thickness grows faster, in spite of smaller molecular diffusivity!*
- *sediment interface moves downward, but more slowly than Stokes settling velocity*
- *salinity interface moves upward*

# *Sedimentation from river plumes: Mean fields*

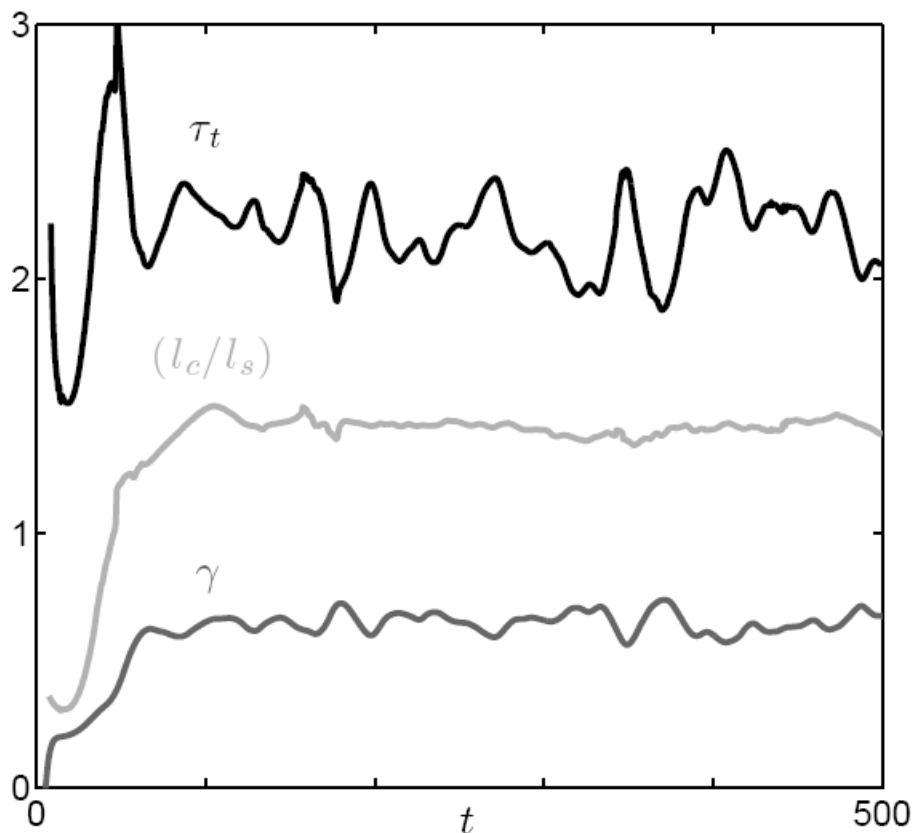
## *Turbulent diffusivities:*



- turbulent sediment diffusivity is about twice as high as turbulent salinity diffusivity, even though the molecular salinity diffusivity is 25 times larger than ‘molecular’ sediment diffusivity → consistent with numerical observations*

# Sedimentation from river plumes: Mean fields

## Quasisteady measures of sedimentation dynamics



ratio of turbulent diffusivities:

$$\tau_{turb} = K_c/K_s$$

ratio of interface thicknesses

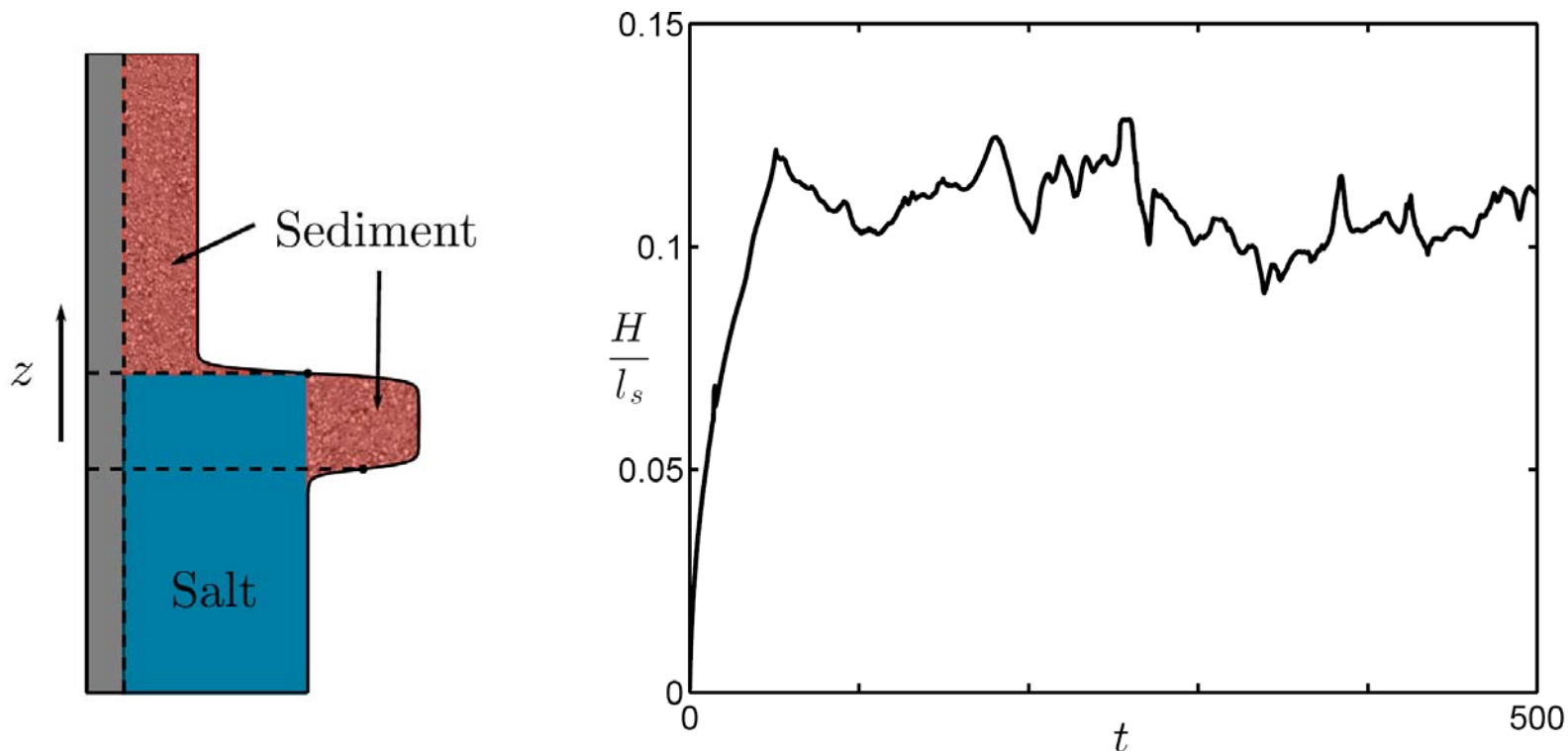
ratio of salinity flux to sediment flux:

$$\gamma = -\frac{F_s}{F_c}$$

- ratio of turbulent diffusivities, ratio of interface thicknesses and ratio of turbulent fluxes all approach quasisteady values  $\rightarrow$  will be important for scaling analysis

# *Sedimentation from river plumes: Mean fields*

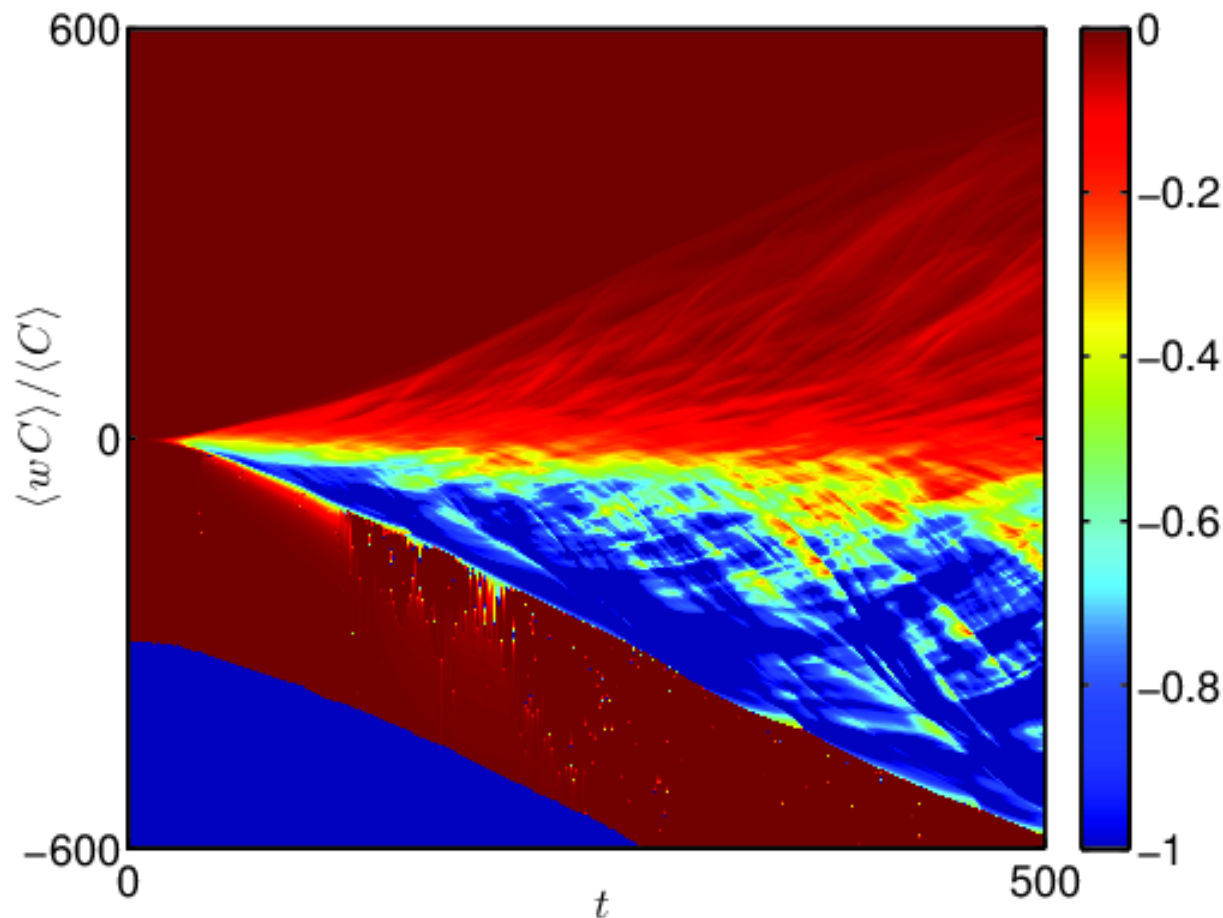
*Ratio of nose height to salinity interface thickness:*



- *ratio of nose height to salinity interface thickness approaches quasisteady state, and remains  $\ll 1$* 
  - *sediment interface remains embedded in the region of strong salinity gradient*
  - *double diffusion remains important*

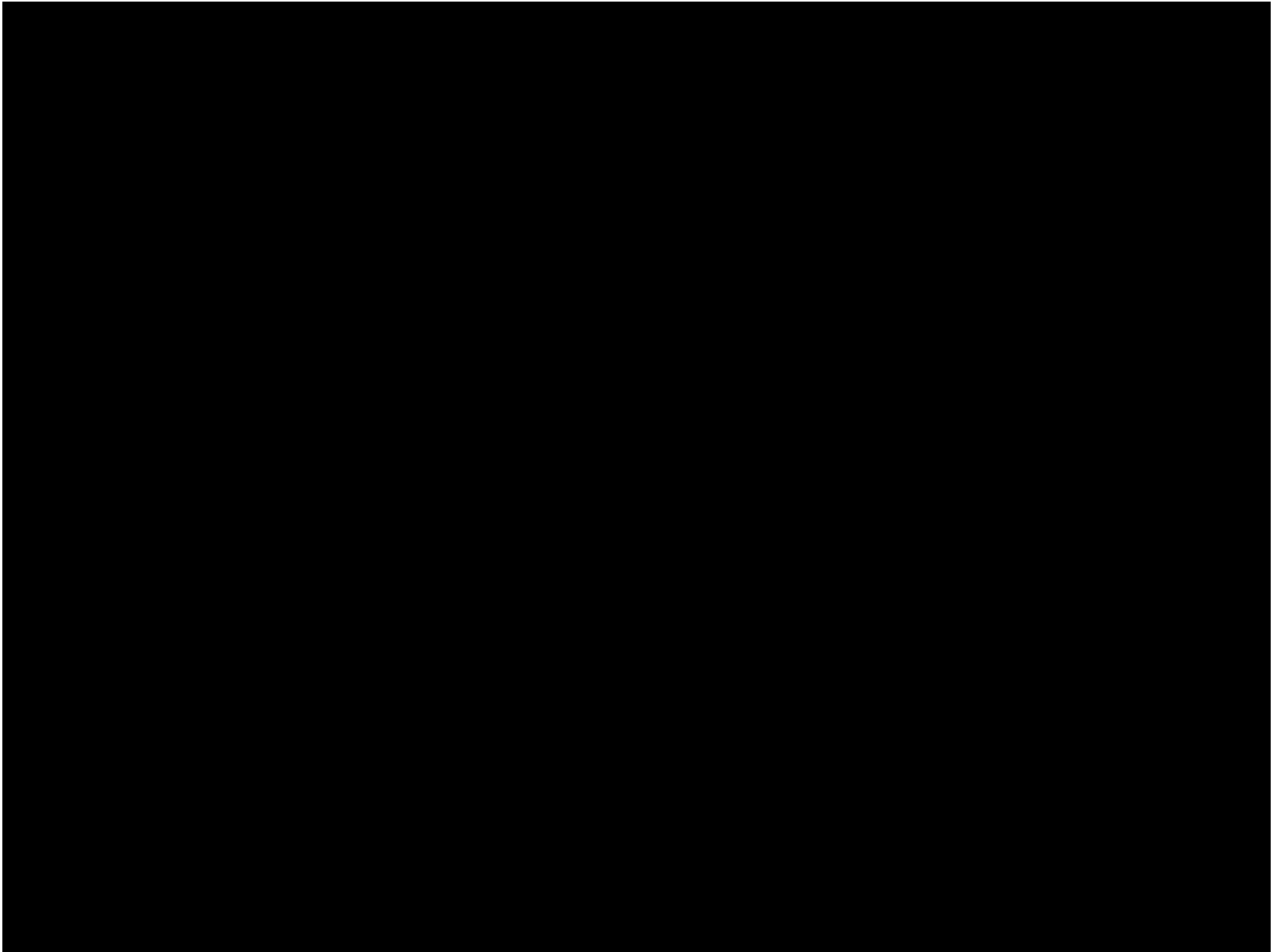
# *Sedimentation from river plumes: Effective settling velocity*

*Settling velocity enhancement:*



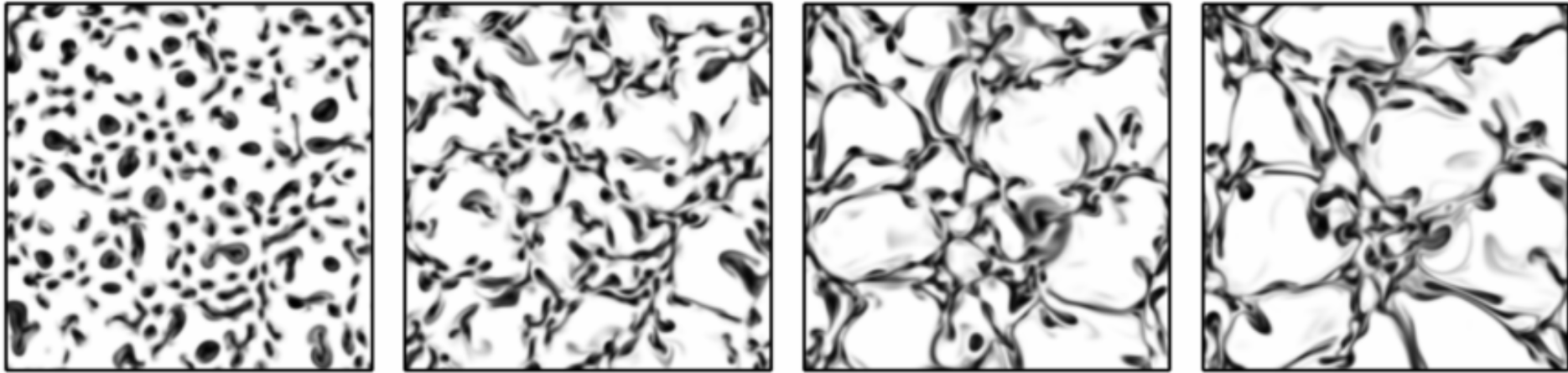
- in the region  $z < 0$ , the effective settling velocity is  $O(1)$ , rather than  $V_{st}=0.04$ , i.e., it scales with the buoyancy velocity of the system, not the Stokes velocity*

*Sedimentation from river plumes: Leaking mode (higher  $Sc$ )*



# *Sedimentation from river plumes: Leaking mode*

*horizontal cross-cuts through sediment concentration field:*



*→ time increases*

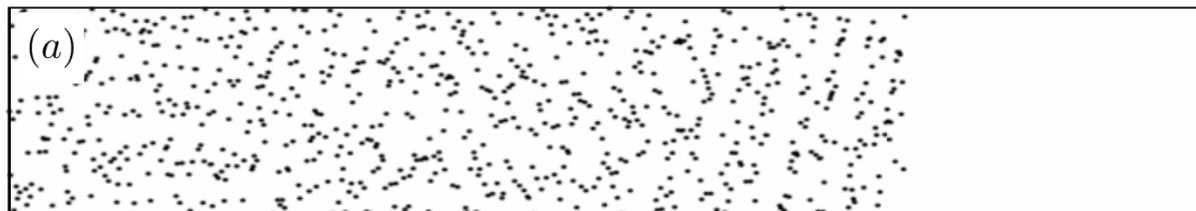
- nonlinear evolution of initial, localized plumes results in web-like structure*
- characterized by sheets, rather than plumes*



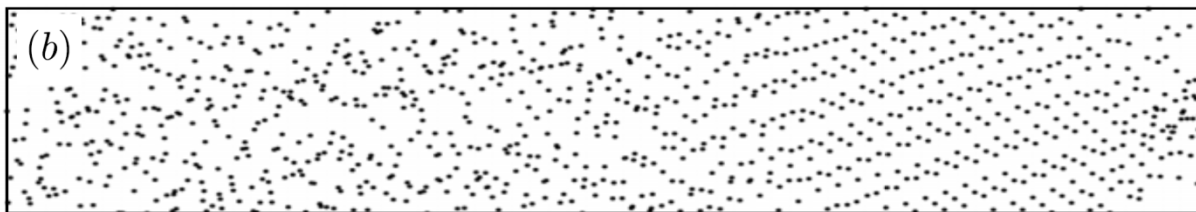
# *Sedimentation from river plumes: Leaking mode*

*Phase of horizontal Fourier mode vs. wave number:*

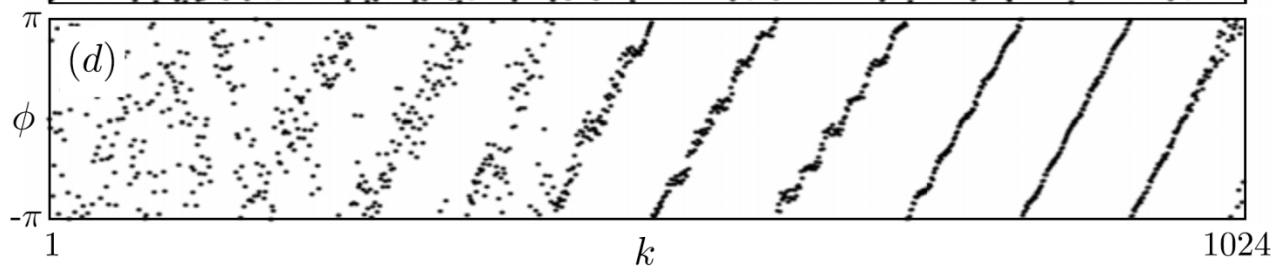
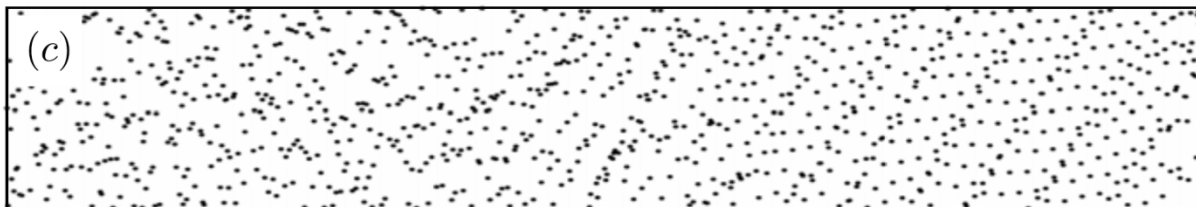
*fingering mode:*



*leaking mode:*



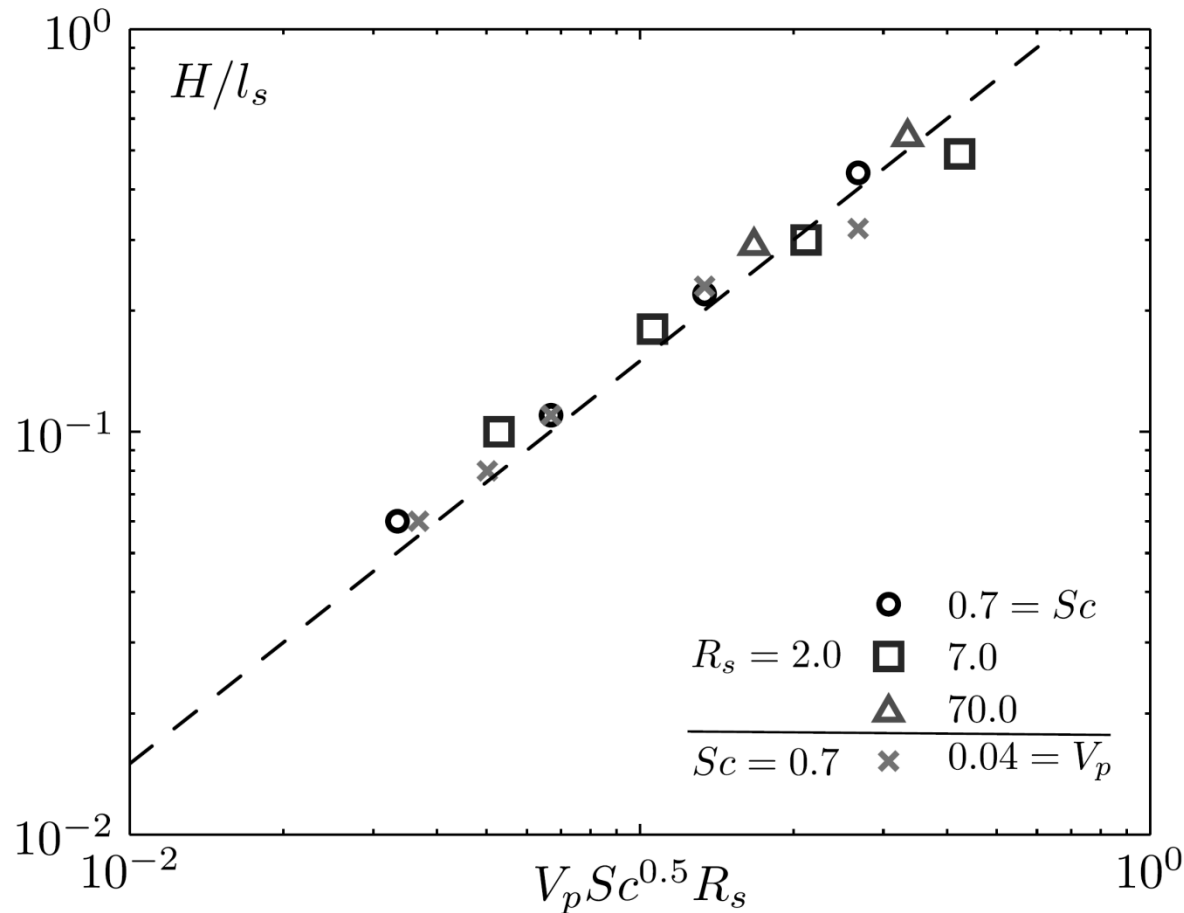
*time increases*



- “Phase locking” of the double-diffusive sediment fingers by Rayleigh-Taylor instability mode

# Sedimentation from river plumes: Scaling

Scaling of nose height with in-/outflow ratio:



→ quasisteady ratio of nose height to salinity interface thickness scales with ratio of sediment inflow into nose region to sediment outflow from nose region

# *Sedimentation from river plumes: Parametric study*

## *Physical interpretation:*

- for small settling velocity, the rate of sediment inflow from above is low → this low rate of sediment inflow can be balanced by conventional double-diffusive outflow of sediment below → there is little accumulation of sediment in the nose region → height of nose region remains small*
- for large settling velocity, the rate of sediment inflow from above is high → this high rate of sediment inflow cannot be balanced by traditional double-diffusive sediment outflow below → sediment accumulates in the nose region → height of nose region increases until it is thick enough for Rayleigh-Taylor instability to form, which leads to increased sediment outflow below → new balance between in- and outflow into the nose region is established*

## Summary

- *double-diffusive sedimentation in river outflows dramatically enhances the effective settling velocity*
- *settling velocity scales with buoyancy velocity, not with Stokes velocity*
- *two mechanisms drive the process:*
  - *double-diffusive instability of salt vs. sediment*
  - *settling of sediment creates ‘nose region,’ Rayleigh-Taylor instability*
- *ratio of nose height/salinity interface thickness  $H/l_s$  determines regime*
- *for low Schmidt numbers, low stability ratios and small Stokes settling velocities, traditional double-diffusive instability causes convective ‘fingering’ mode*
- *for high Schmidt numbers, large stability ratios and large Stokes settling velocities, settling of sediment causes ‘leaking’ mode, via interaction of Rayleigh-Taylor and double-diffusive instability modes through ‘phase-locking’*
- *overall dynamics is governed by the in-/outflow of sediment into/from the nose region*