

# **Spatio-temporal structures of solar wind turbulence**

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# Magnetohydrodynamic turbulence

Navier-Stokes eq.

$$\left(\partial_t - \underbrace{\nu \nabla^2}_{\text{Viscosity}}\right) \vec{v} = -\underbrace{\vec{v} \cdot \nabla \vec{v}}_{\text{Advection}} + \underbrace{\vec{b} \cdot \nabla \vec{b}}_{\text{Magnetic tension}} - \underbrace{\nabla p}_{\text{Total pressure grad. (thermal and magnetic)}}$$

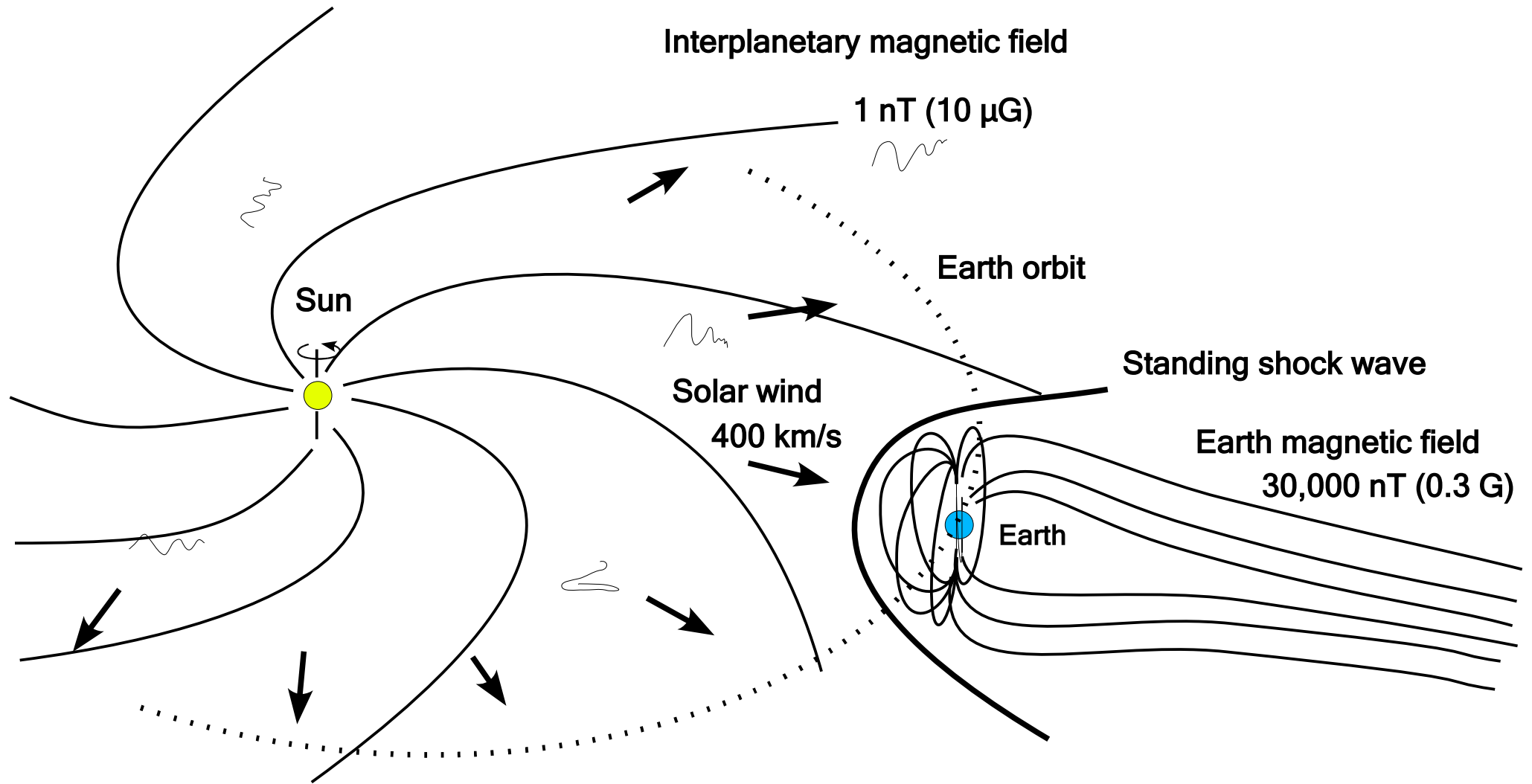
Induction eq. with Ampère's law

$$\left(\partial_t - \underbrace{\eta \nabla^2}_{\text{Resistivity}}\right) \vec{b} = \underbrace{-\vec{v} \cdot \nabla \vec{b} + \vec{b} \cdot \nabla \vec{v}}_{\text{Frozen-in magnetic field}}$$

Under conditions:

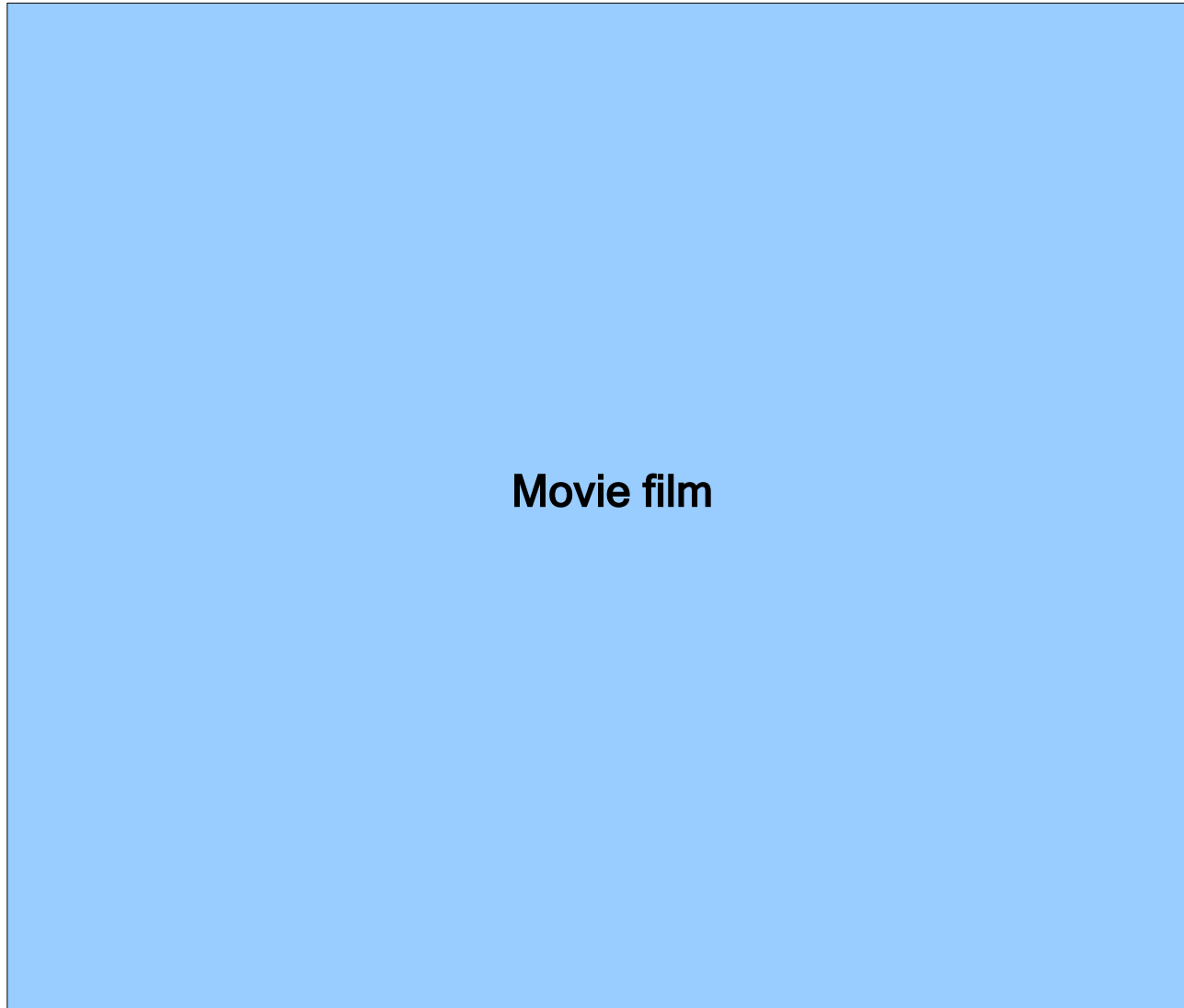
$$\underbrace{\nabla \cdot \vec{v}}_{\text{Incompressibility}} = 0 \quad , \quad \underbrace{\nabla \cdot \vec{b}}_{\text{No magnetic monopole}} = 0$$

# Near-Earth interplanetary space



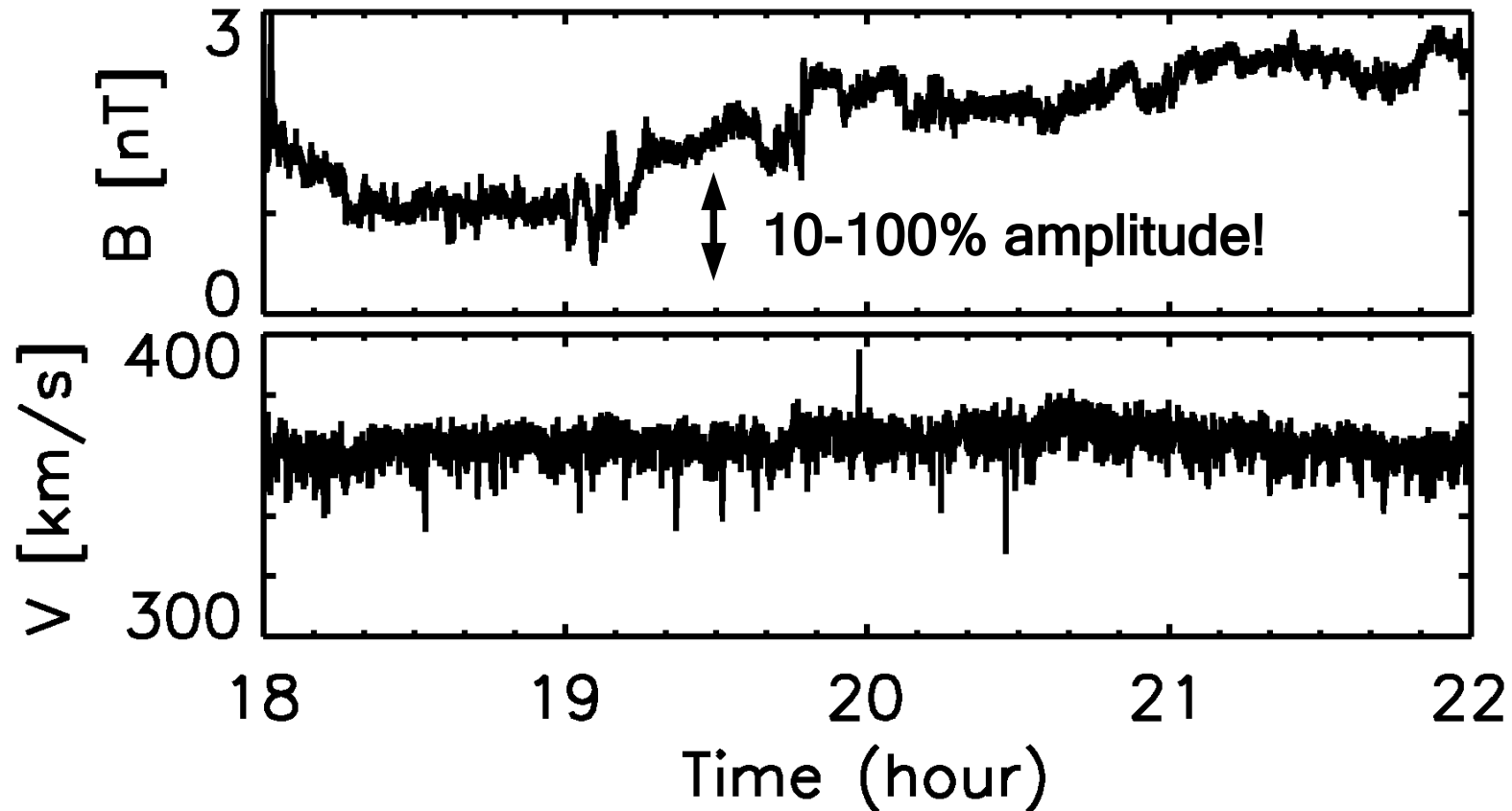
Solar wind is the only accessible natural laboratory of astrophysical plasma turbulence.

# Solar corona observed by SOHO spacecraft



# Large-amplitude fluctuations in the solar wind

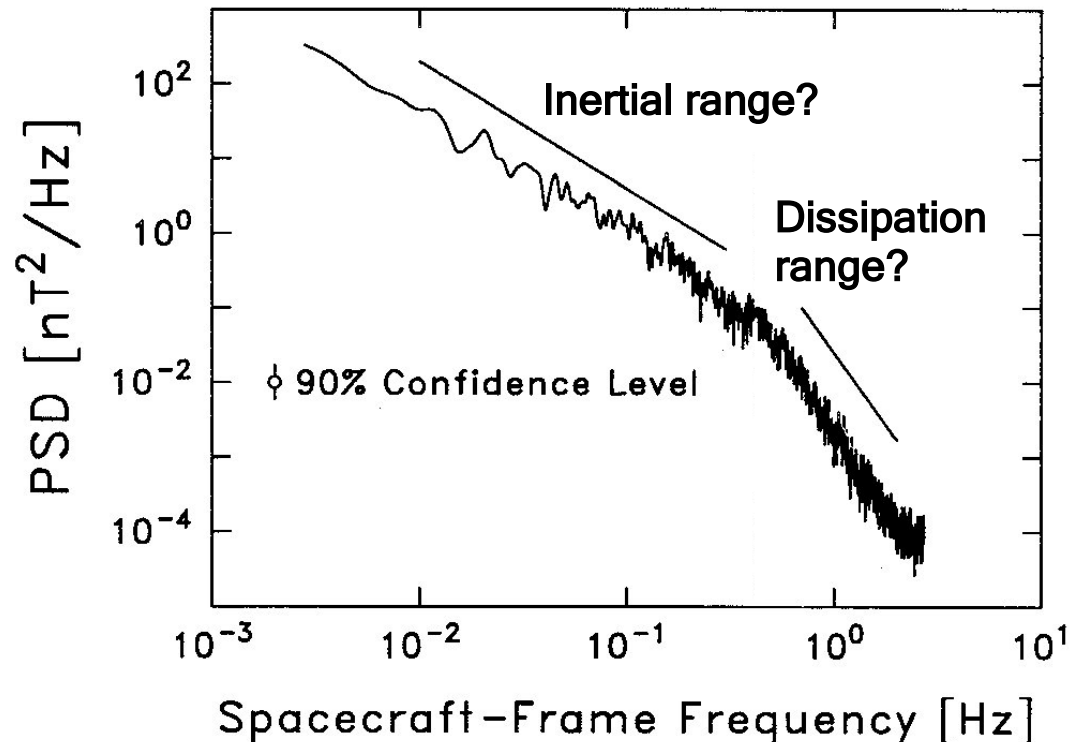
Cluster spacecraft on Mar. 12, 2005



Are the fluctuations temporal variations or spatial structures swept by the flow?

# Turbulence in the solar wind?

## Frequency spectrum of magnetic field fluctuations



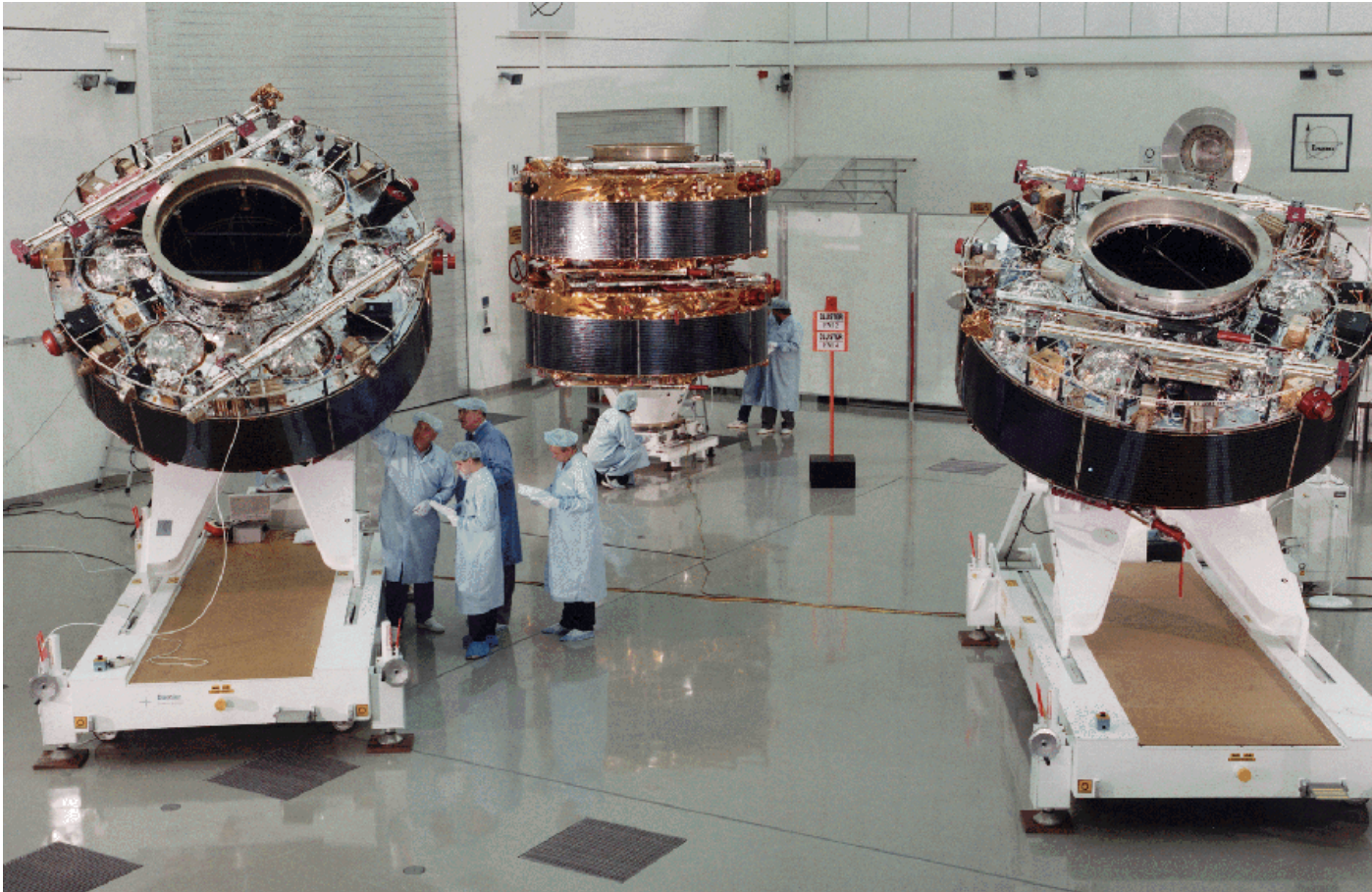
Leamon et al. (1998)

Motivations:

1. Is there any dispersion relation in solar wind turbulence?
2. What does the 3D spatial structure look like?

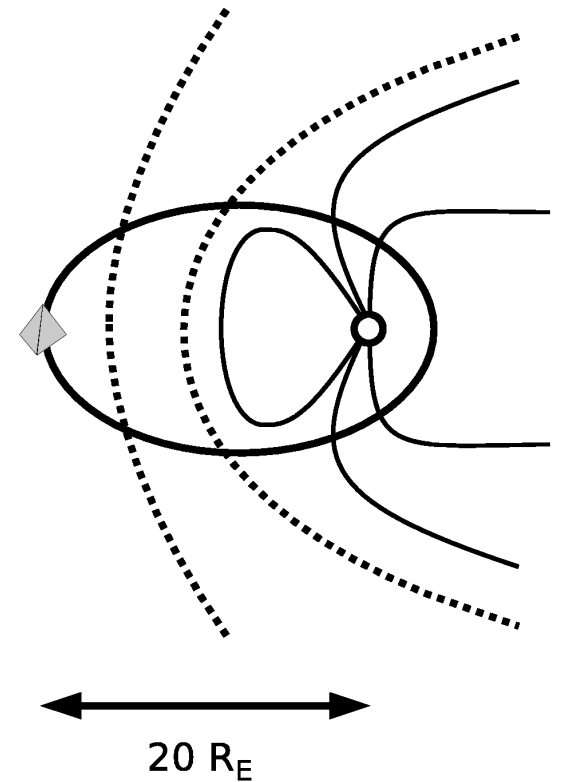
We can answer these questions using multi-spacecraft measurements!

# The Cluster mission

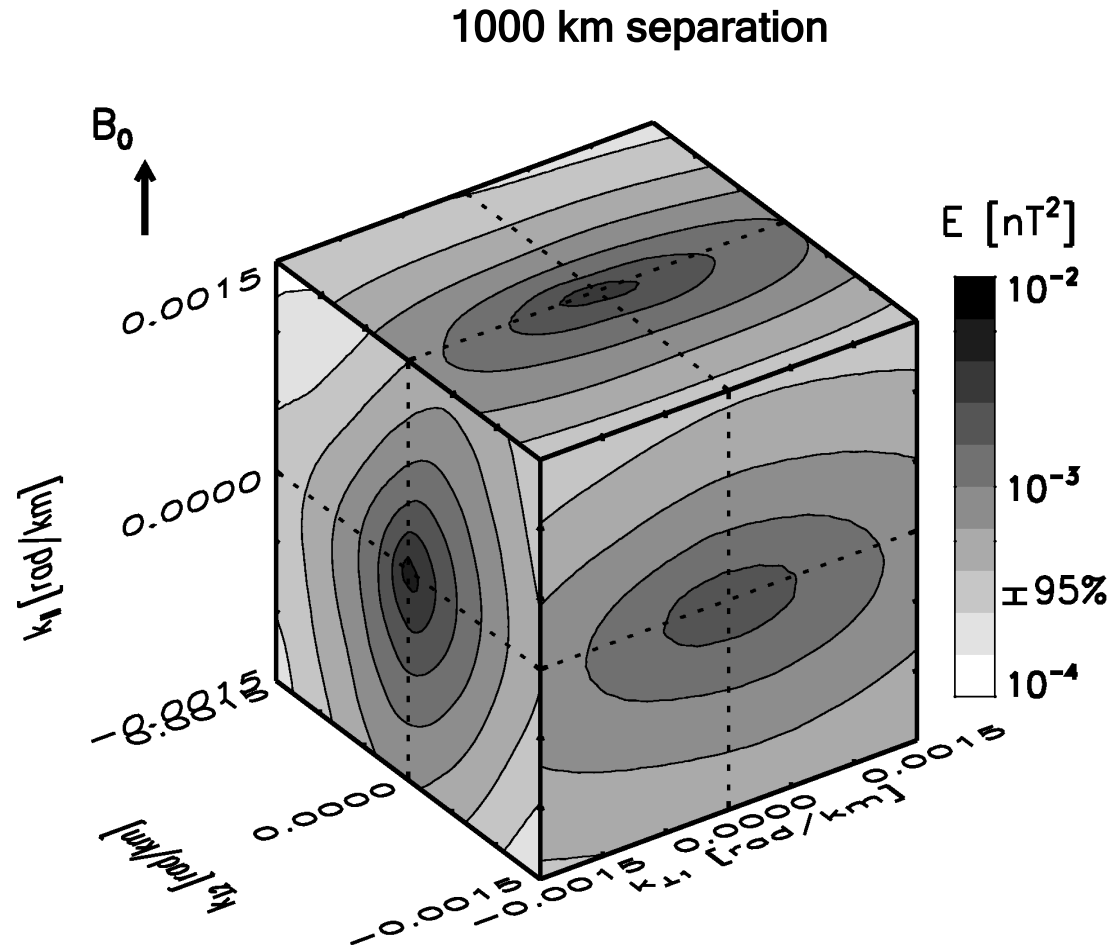


Wavelengths, propagation speeds and directions can be determined (interferometric method).

Taylor's hypothesis is no more necessary.



# Energy distribution in the wave vector domain



Narita et al. (PRL,2010)

Two discoveries:

1. Asymmetry around the large-scale magnetic field
2. Anisotropy between parallel and perpendicular directions

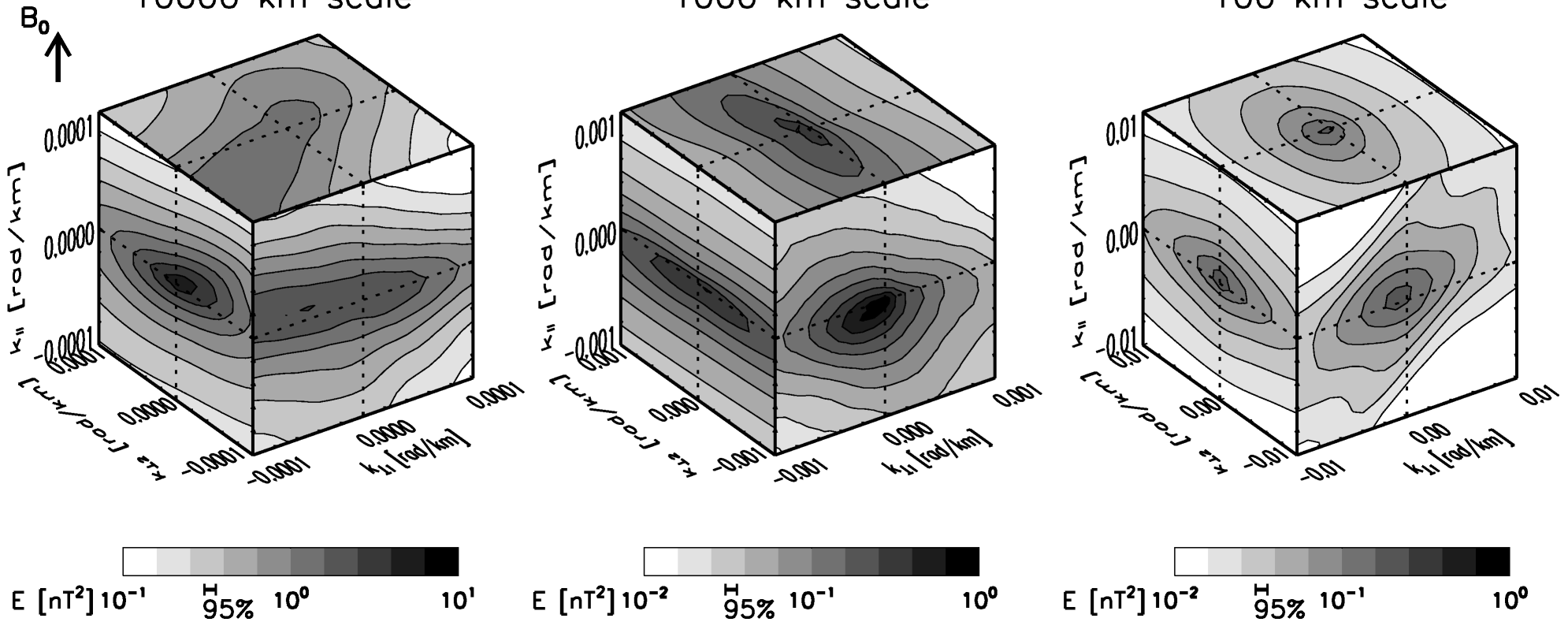


# More examples of 3D energy distributions

(1) Jan. 16, 2006  
10000 km scale

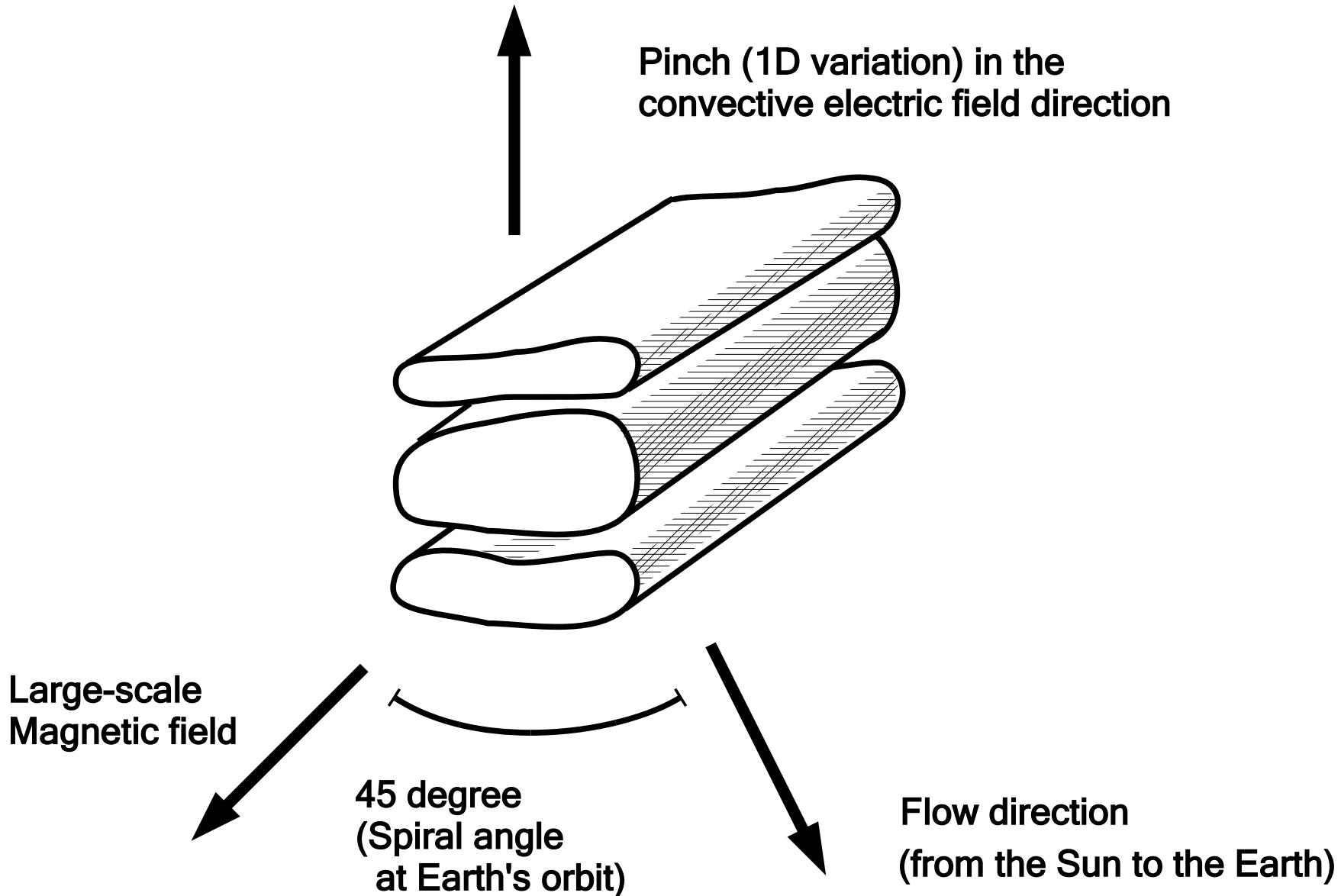
(2) Mar. 21, 2005  
1000 km scale

(3) Feb. 20, 2002  
100 km scale

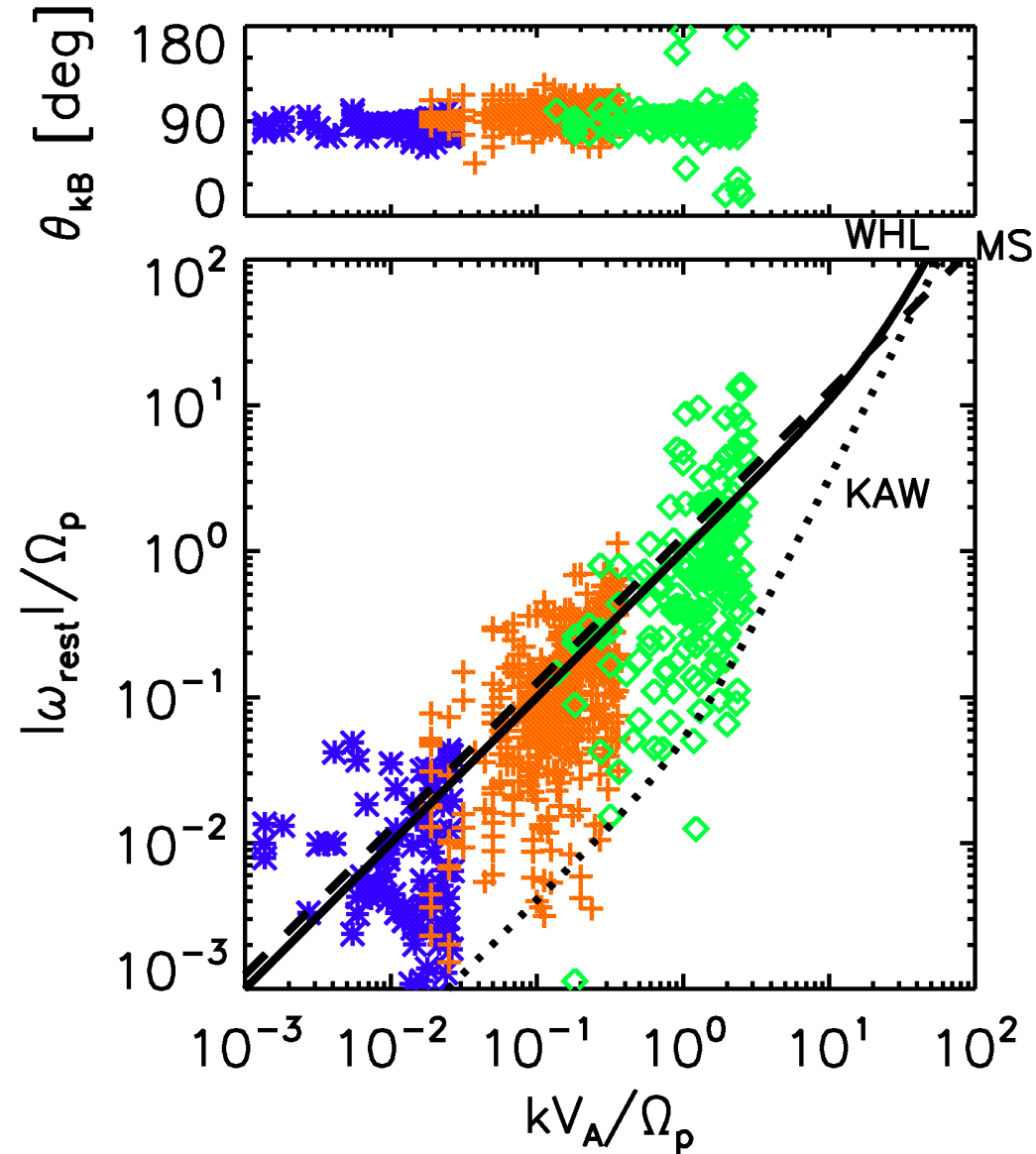


**Axial asymmetry exists on various spatial scales.  
Anisotropy prefers the direction perpendicular to the large-scale magnetic field.**

# Fluctuation geometry in the coordinate space



# Is there any dispersion relation?



Narita et al. (GRL, 2011)

# Summary

$\omega$  -  $k$  dependence of MHD turbulent fluctuations was determined for the first time using Cluster data.

Origin of anisotropy: Perpendicular cascade to the magnetic field?

Origin of axial asymmetry:

- Nature of MHD turbulence?
- Radial expansion of solar wind?
- Field structure in the solar corona?

My question to you:

“What does the energy distribution for fluid turbulence look like in the  $\omega$  -  $k$  domain?”