

How does demography affect adaptation?

Sergey Kryazhimskiy

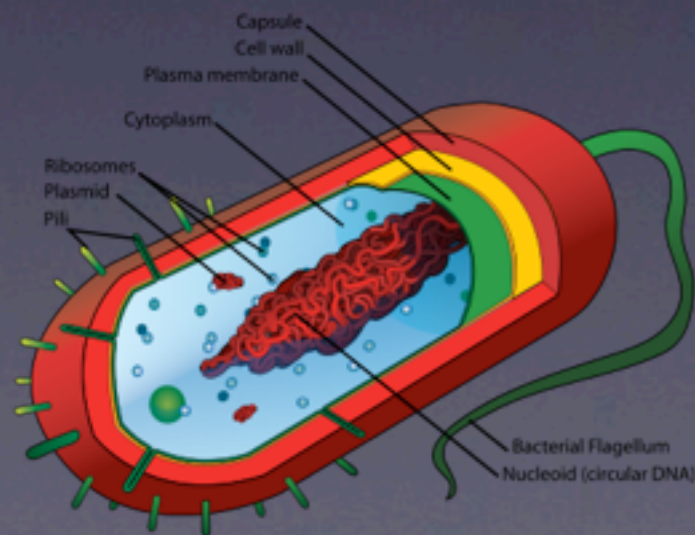
Desai Lab

Harvard University

Microbial and Viral Evolution
KITP

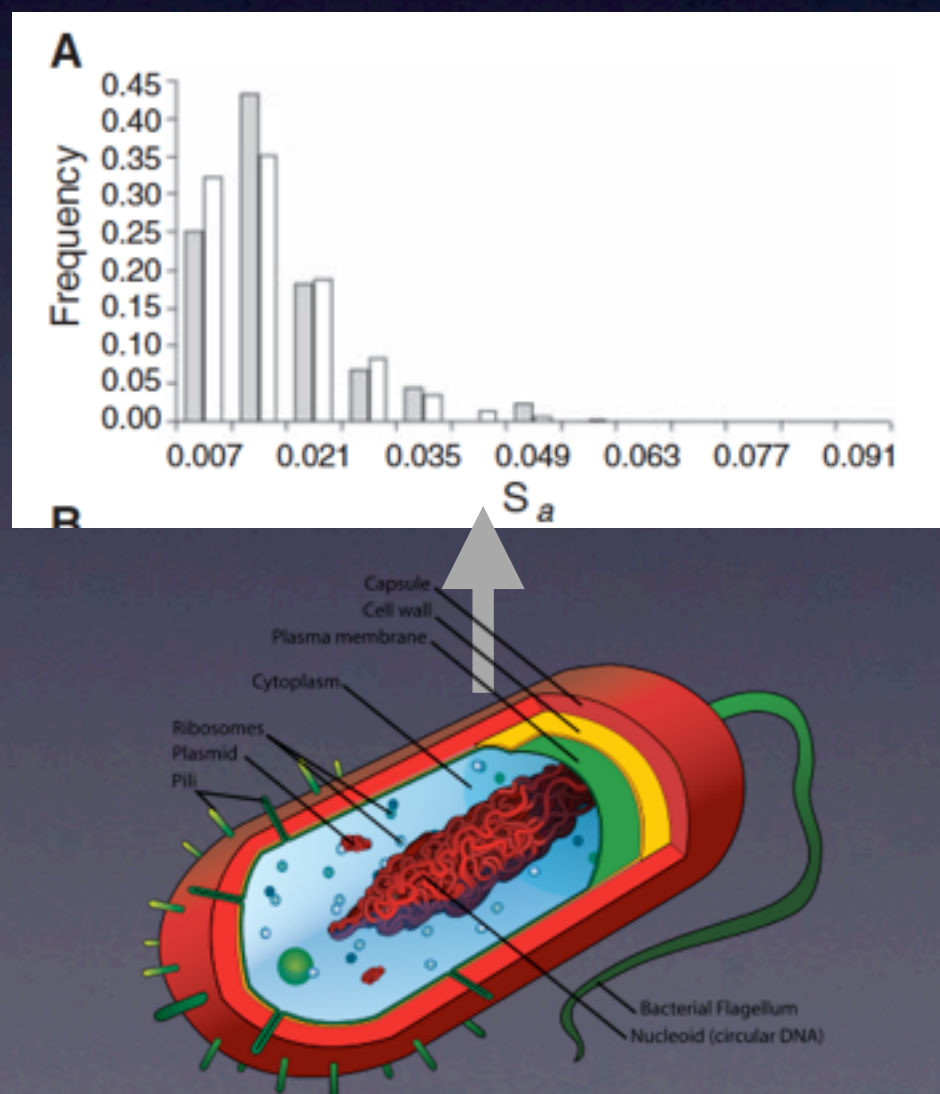
11 Jan 2011

Adaptation



Environment + cellular
architecture
Regulatory networks
Proteins

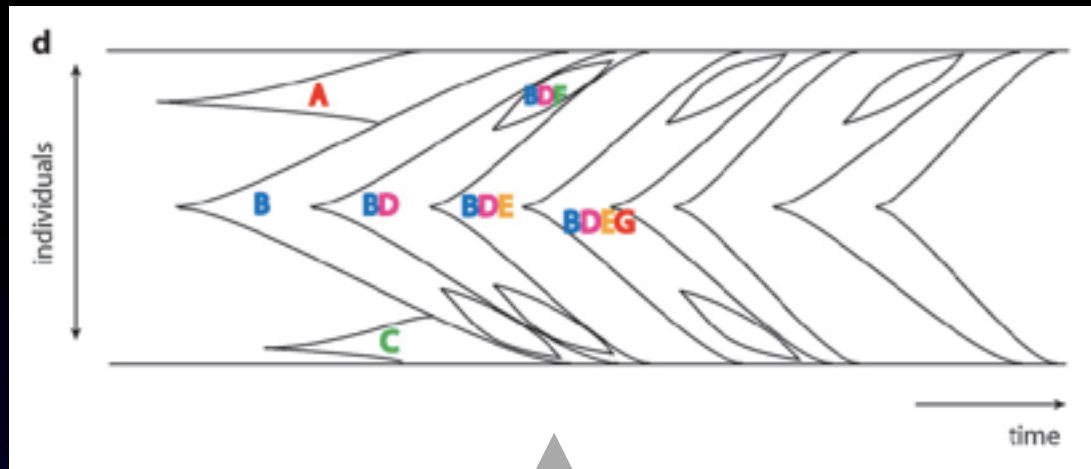
Adaptation



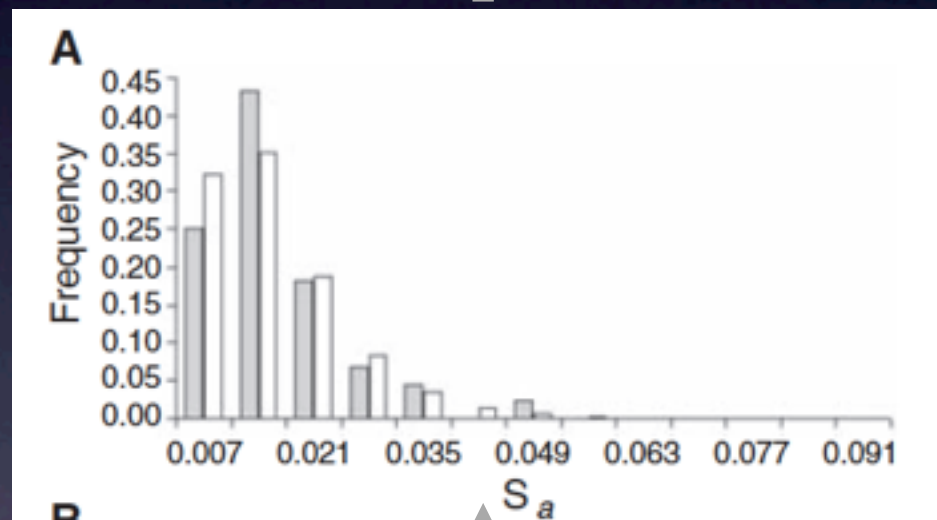
Fitness landscape:
Mutation rates
Distribution of fitness effects
Epistasis

Environment + cellular
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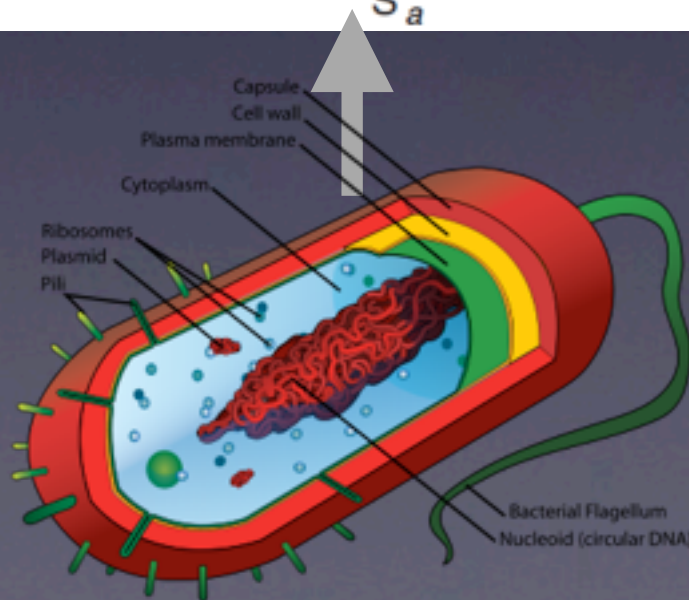
Adaptation



Dynamics of adaptation:
Population structure
Clonal interference
Multiple mutations



Fitness landscape:
Mutation rates
Distribution of fitness effects
Epistasis



Environment + cellular
architecture
Regulatory networks
Proteins

Simplest case

- Well-mixed asexual population of size N
- Beneficial mutations are rare

Fixation probability of a mutation with selective advantage s

$$\pi(s) = \frac{1 - e^{-2s}}{1 - e^{-2Ns}} \approx 2s$$

Population fitness F increases as

$$\frac{dF}{dt} = \mu N r(F), \quad F(0) = 1$$

r is the expected fitness increment of a mutation

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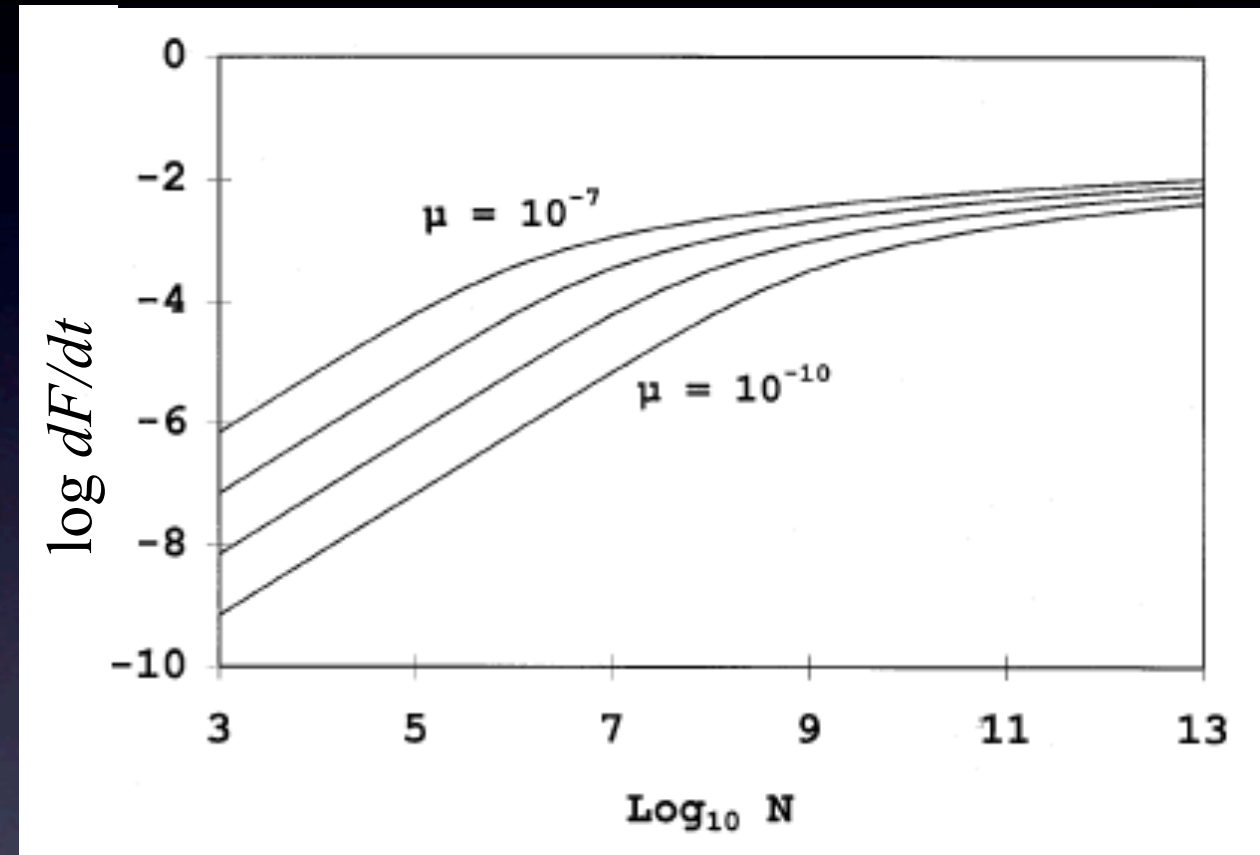
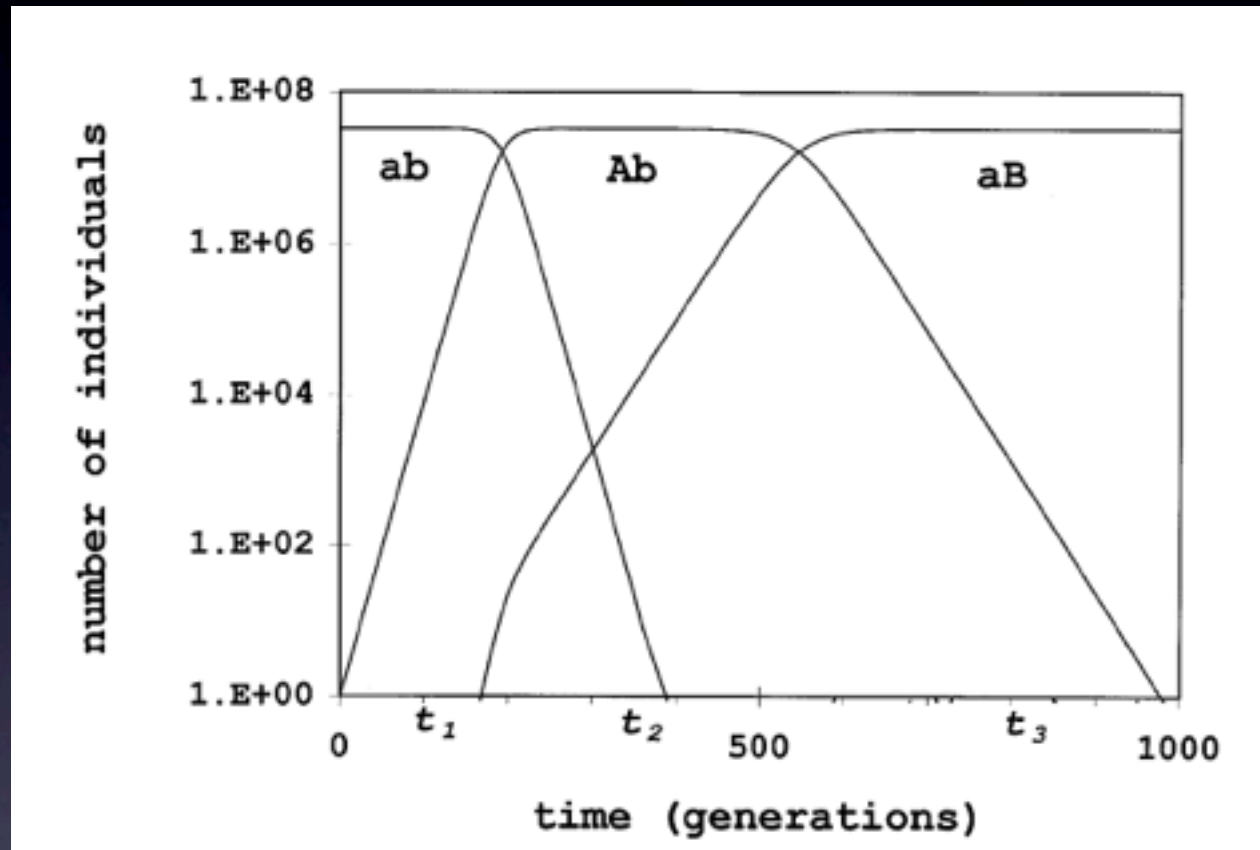
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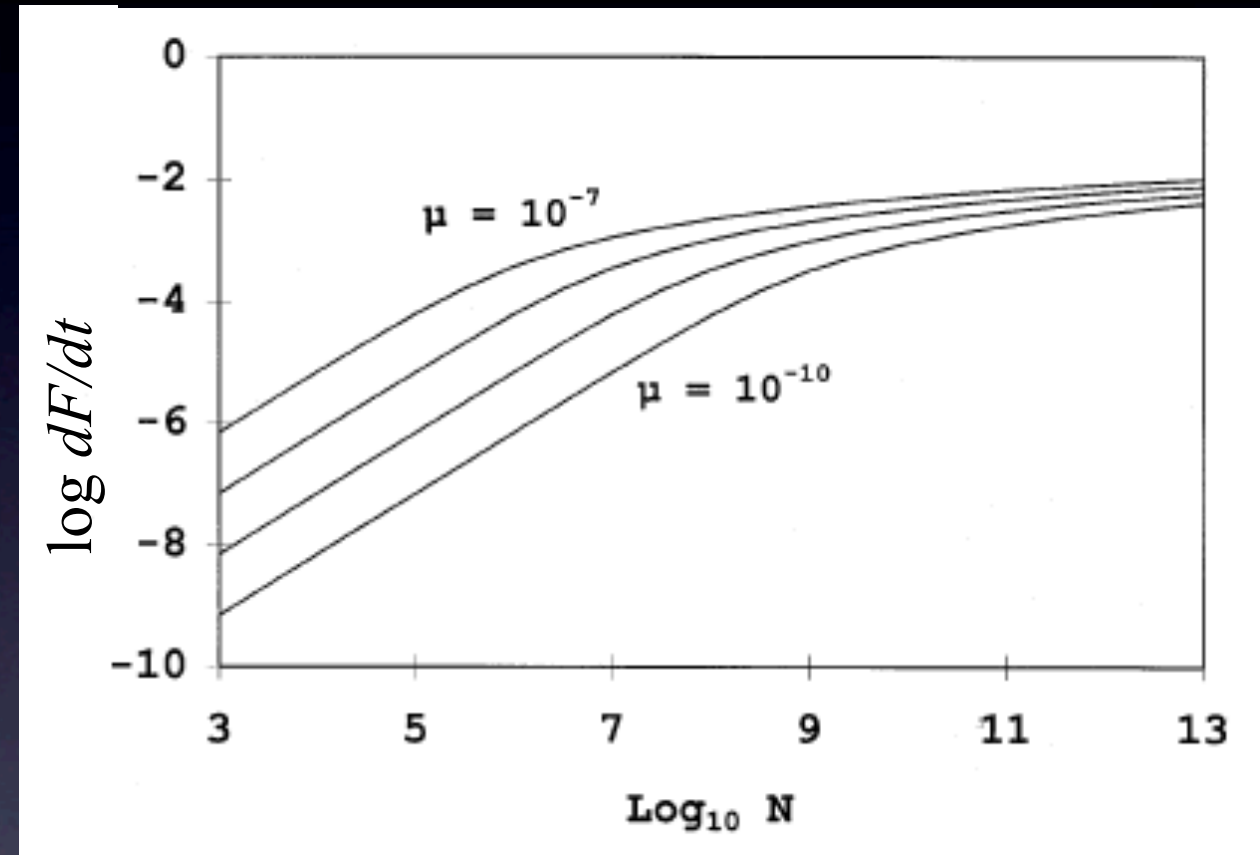
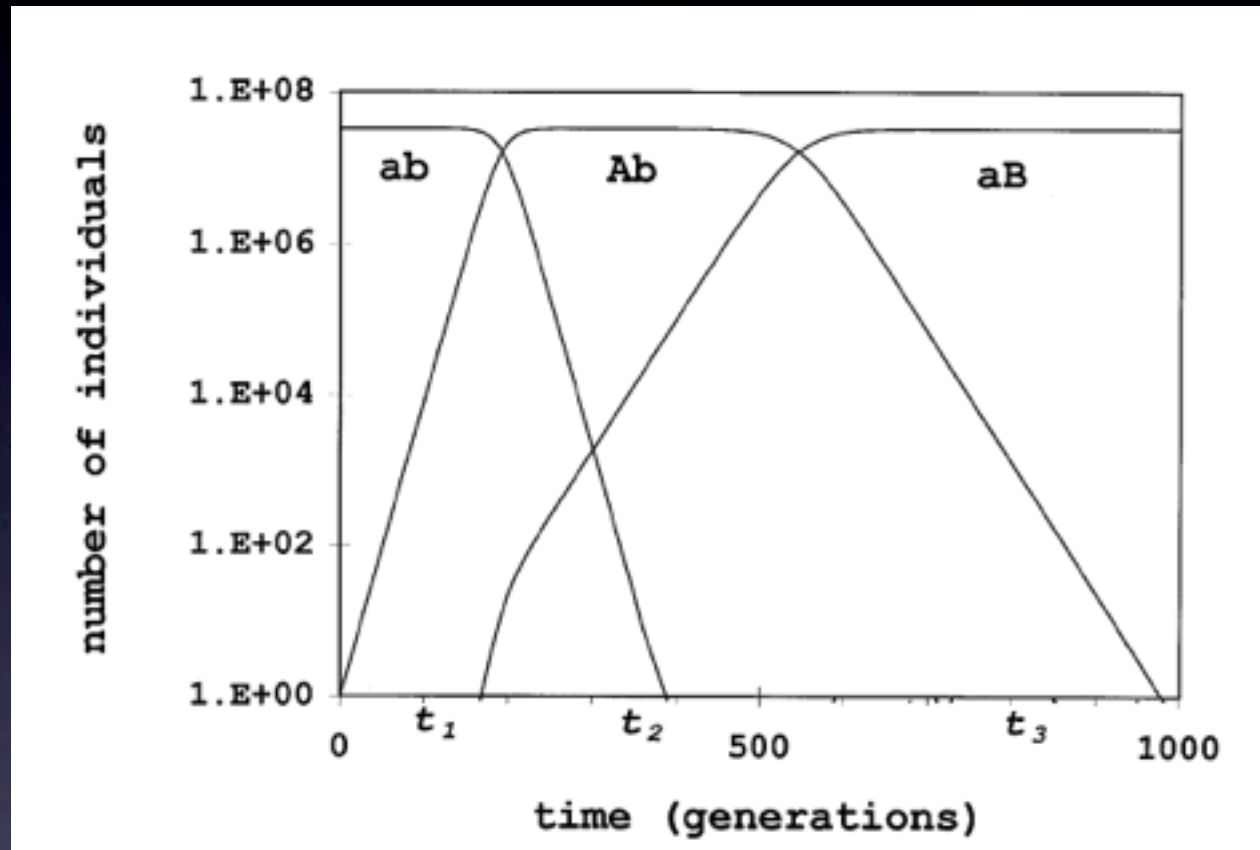
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Complication: clonal interference



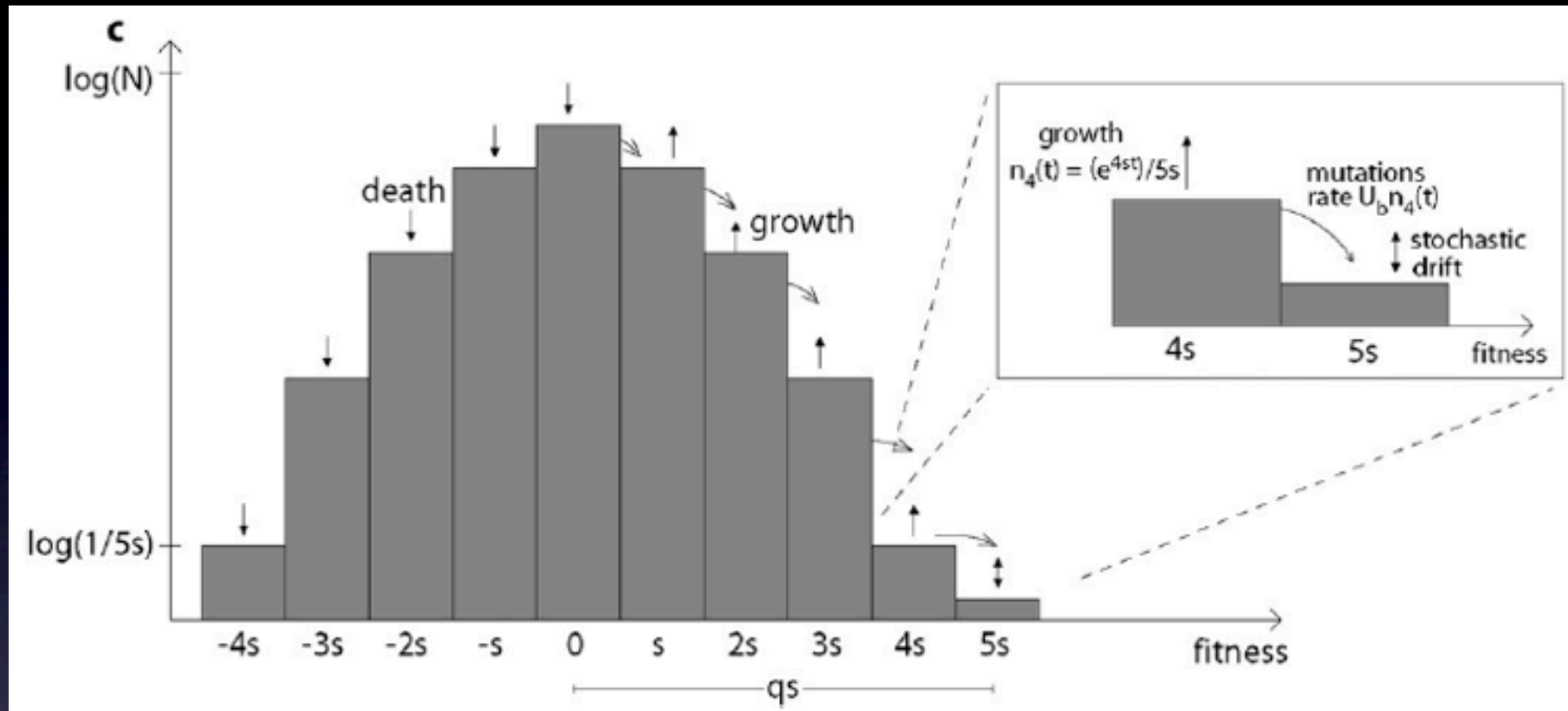
$$\frac{dF}{dt} = \alpha \mu N \int_0^{\infty} s \pi(s) e^{-\lambda(s, \alpha, \mu, N) - \alpha s} ds$$

Complication: clonal interference

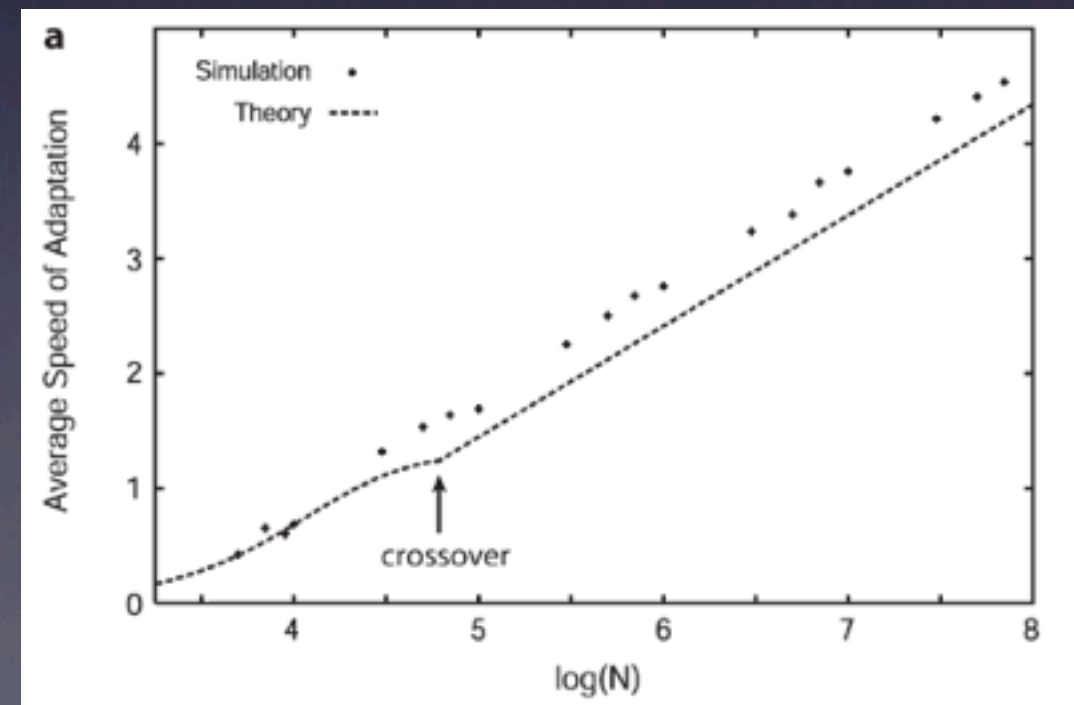


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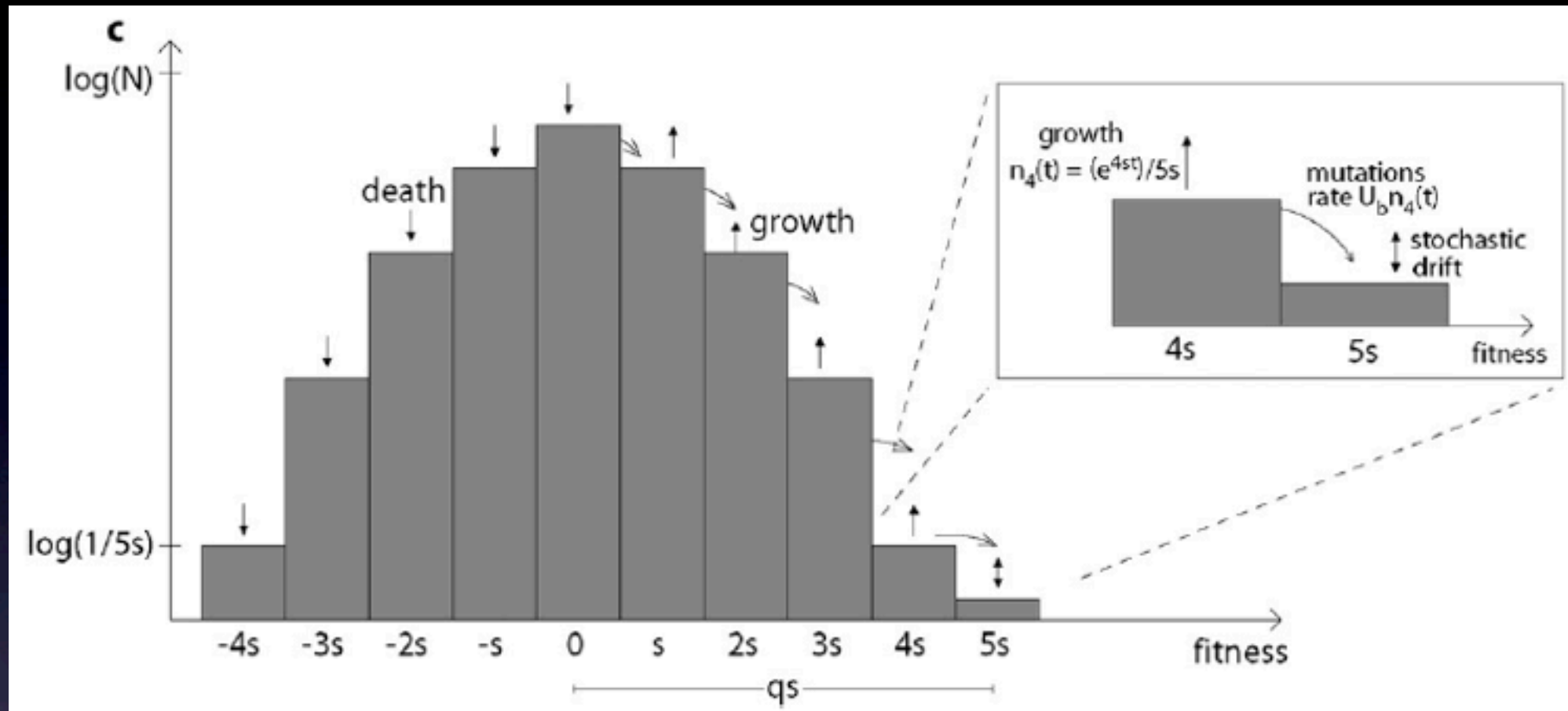
Complication: piggybacking



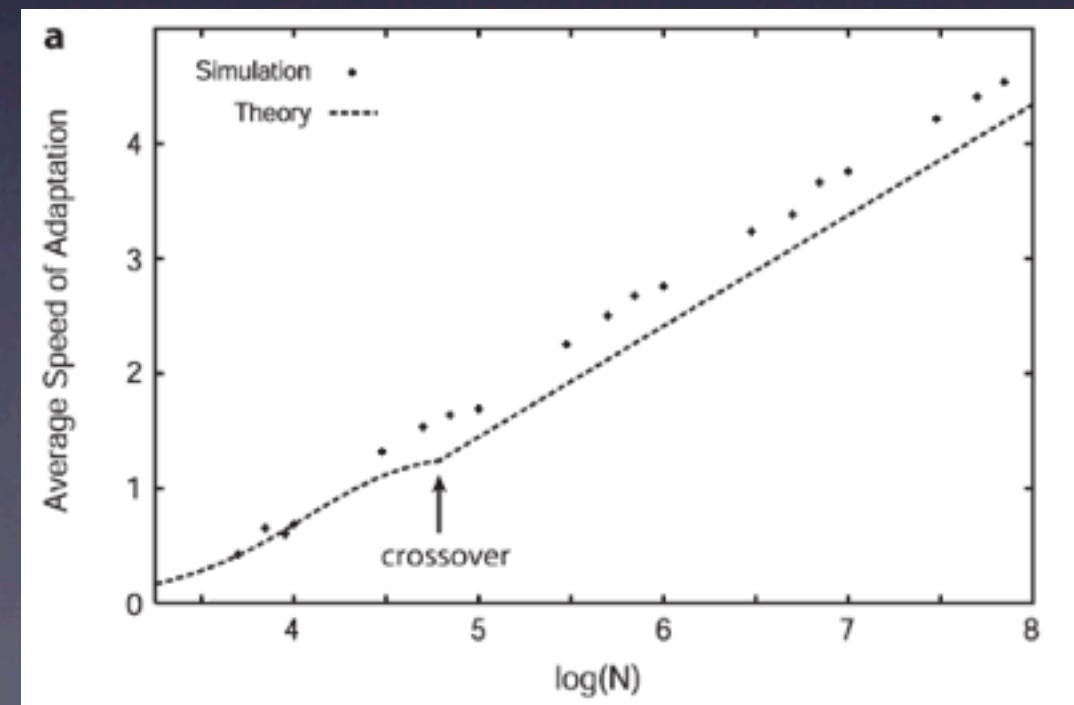
$$\frac{dF}{dt} = s^2 \frac{2 \log N s - \log s / \mu}{\log^2 s / \mu}$$



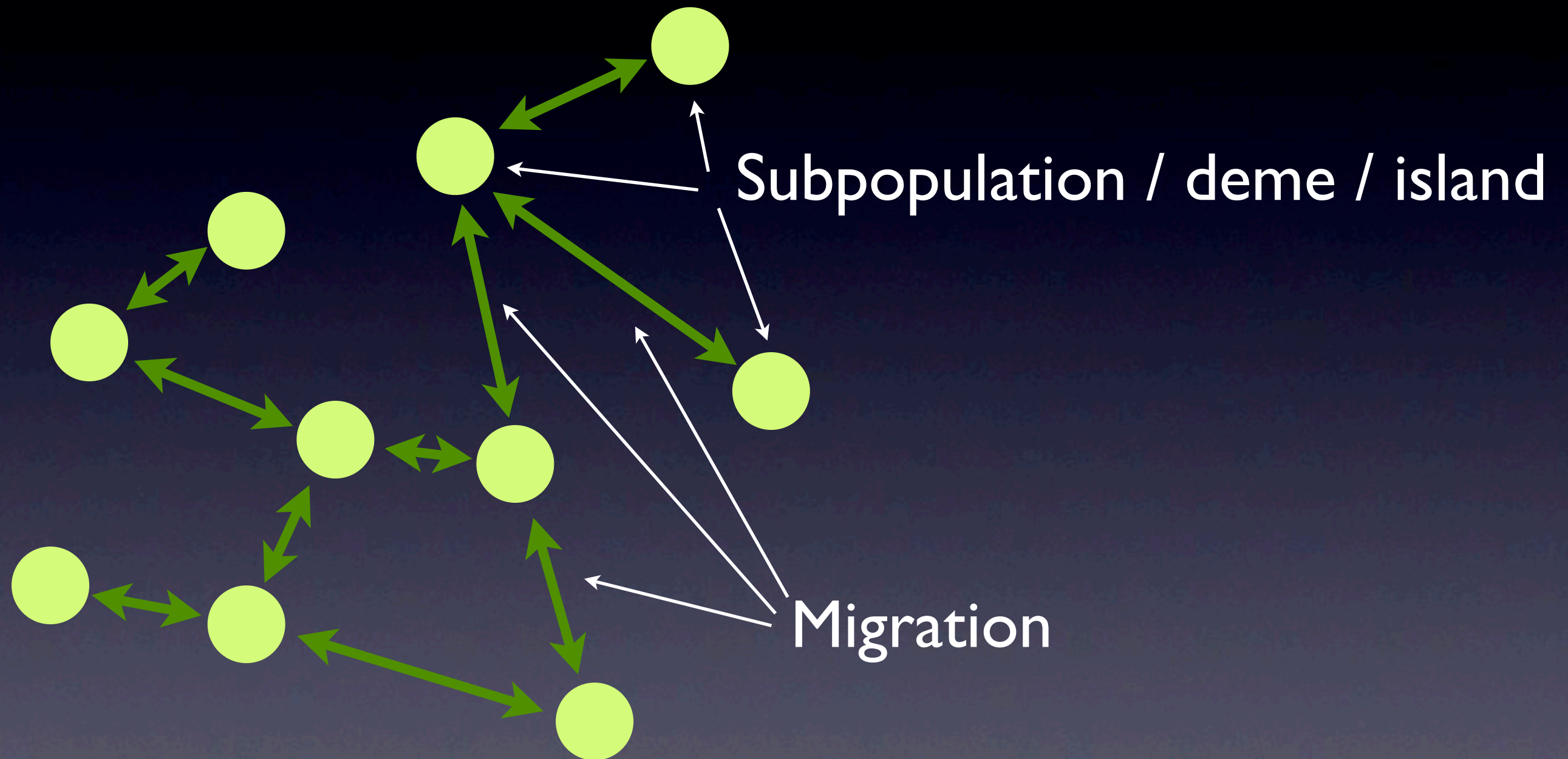
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$$\frac{dF}{dt} = s^2 \frac{2 \log N s - \log s / \mu}{\log^2 s / \mu}$$



Complication: population subdivision



Shifting balance theory (S.Wright)

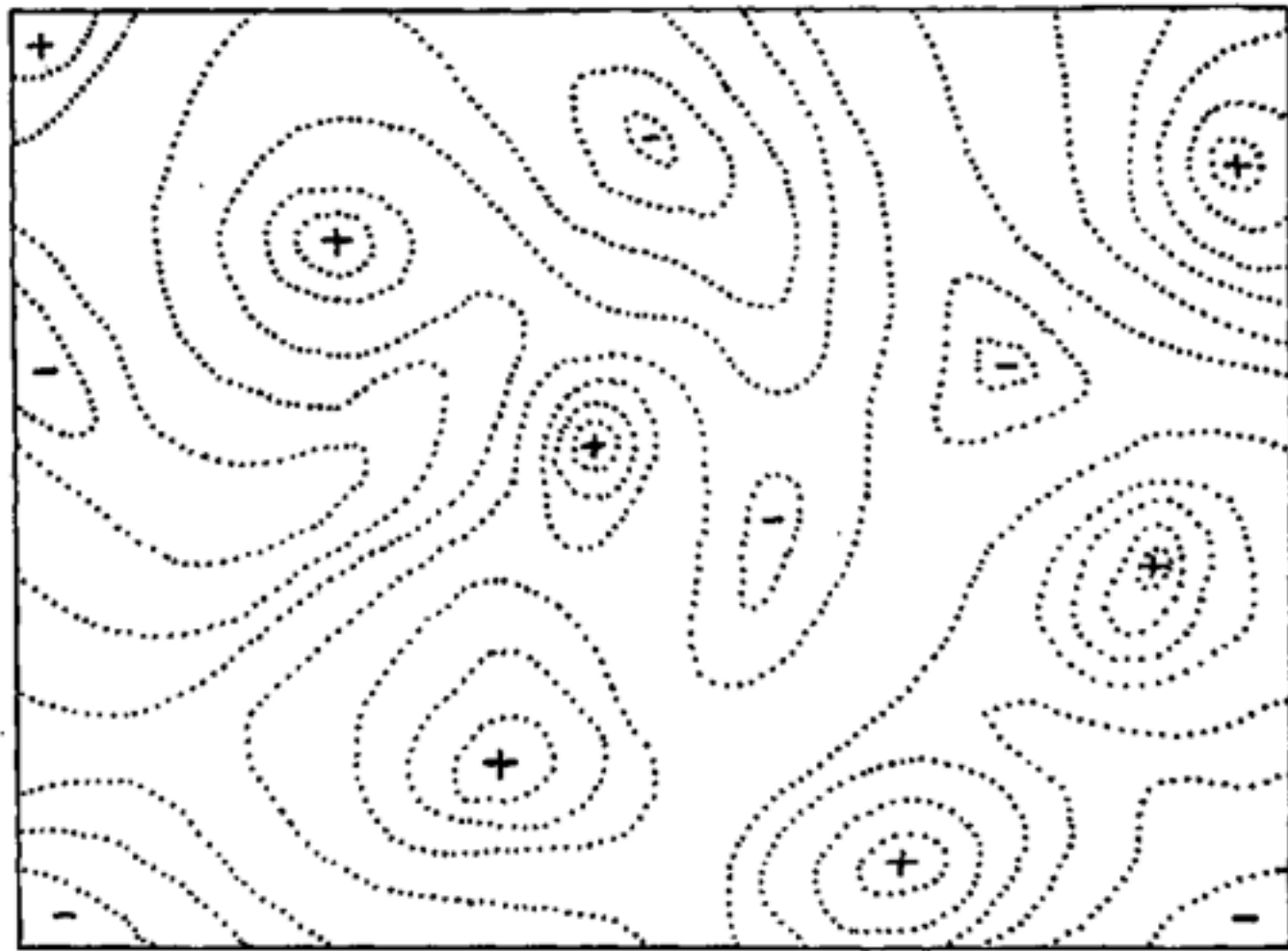


FIGURE 2.—Diagrammatic representation of the field of gene combinations in two dimensions instead of many thousands. Dotted lines represent contours with respect to adaptiveness.

“With 10^{1000} possibilities it may be taken as certain that there will be an enormous number of widely separated harmonious combinations. <...> In a rugged field of this character, selection will easily carry the species to the nearest peak, but there may be innumerable other peaks which are higher but which are separated by “valleys”. The problem of evolution as I see it is that of a mechanism by which the species may continually find its way from lower to higher peaks in such a field.”

Sewall Wright (1932)

Shifting balance theory (S.Wright)

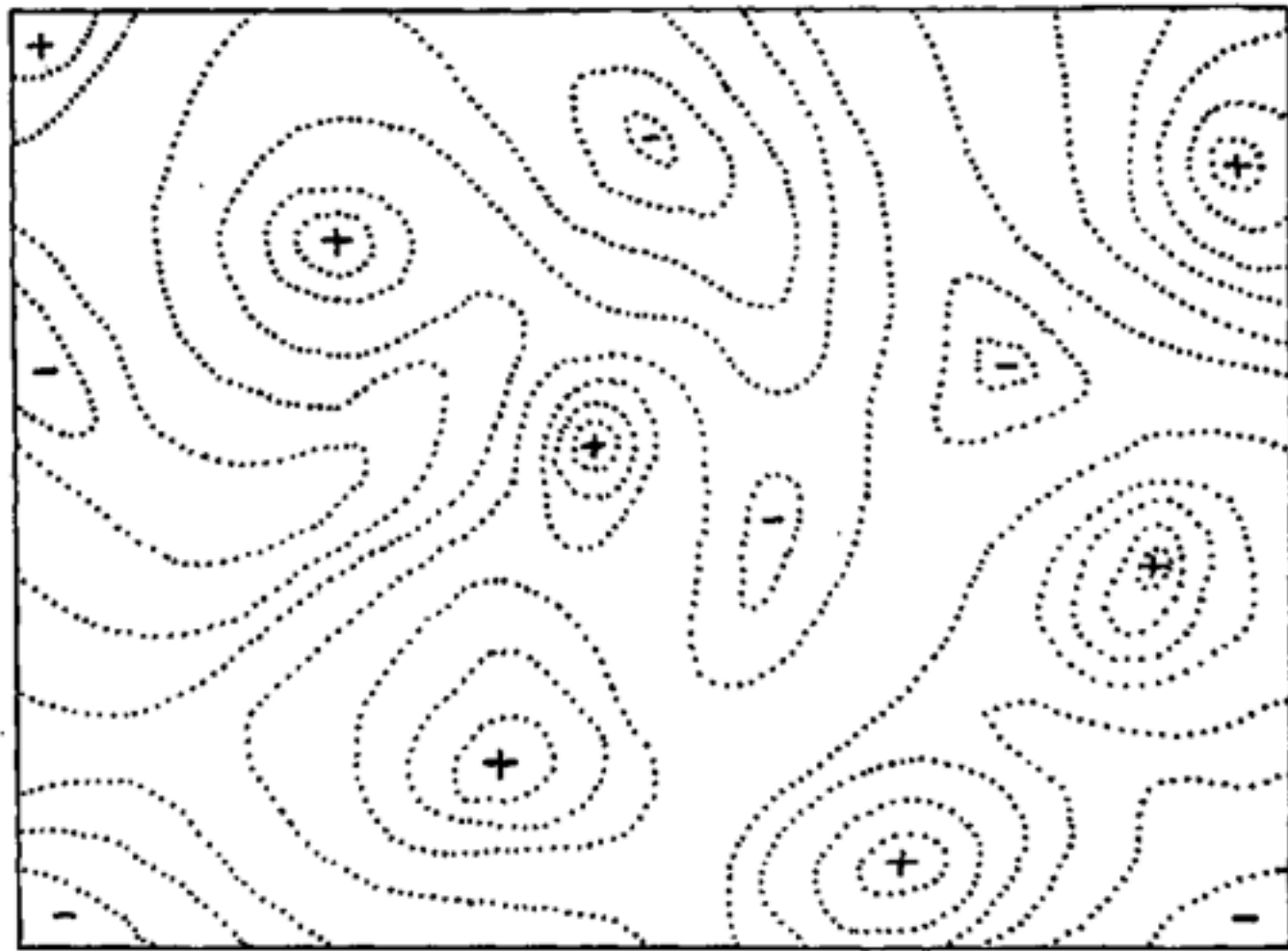


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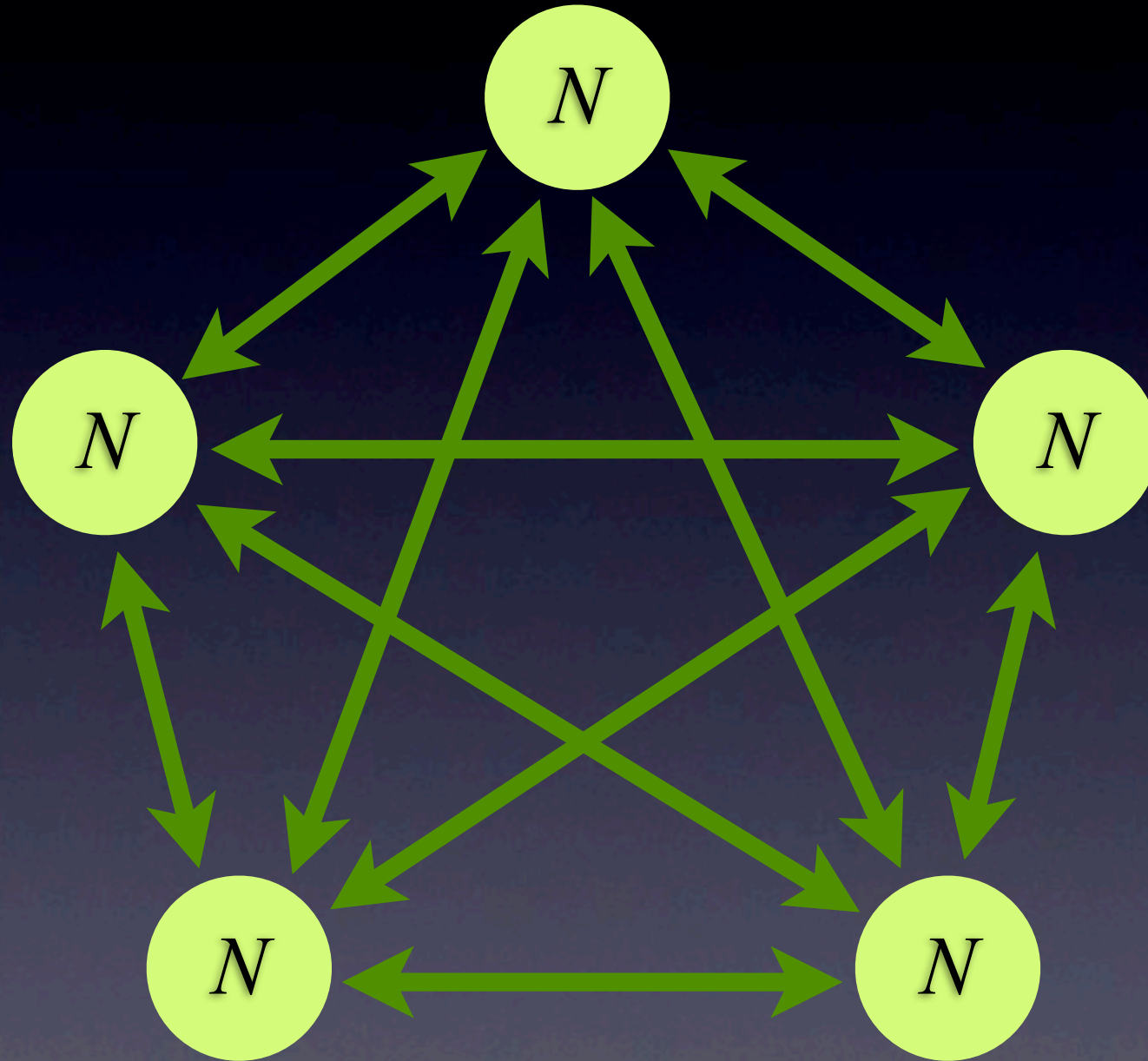
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Shifting balance theory (S.Wright)

- Phase I extensive local differentiation with stochastic variability in each locality
- Phase II occasional crossing of a saddle leading to a higher selective peak in a subpopulation
- Phase III excess proliferation and dispersal from local populations in which peak shift has occurred

The island model



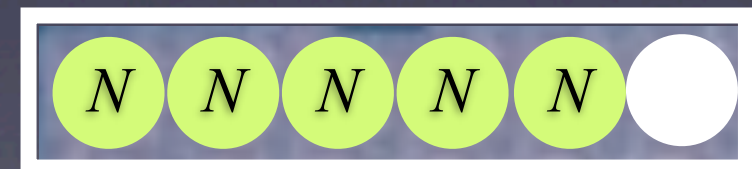
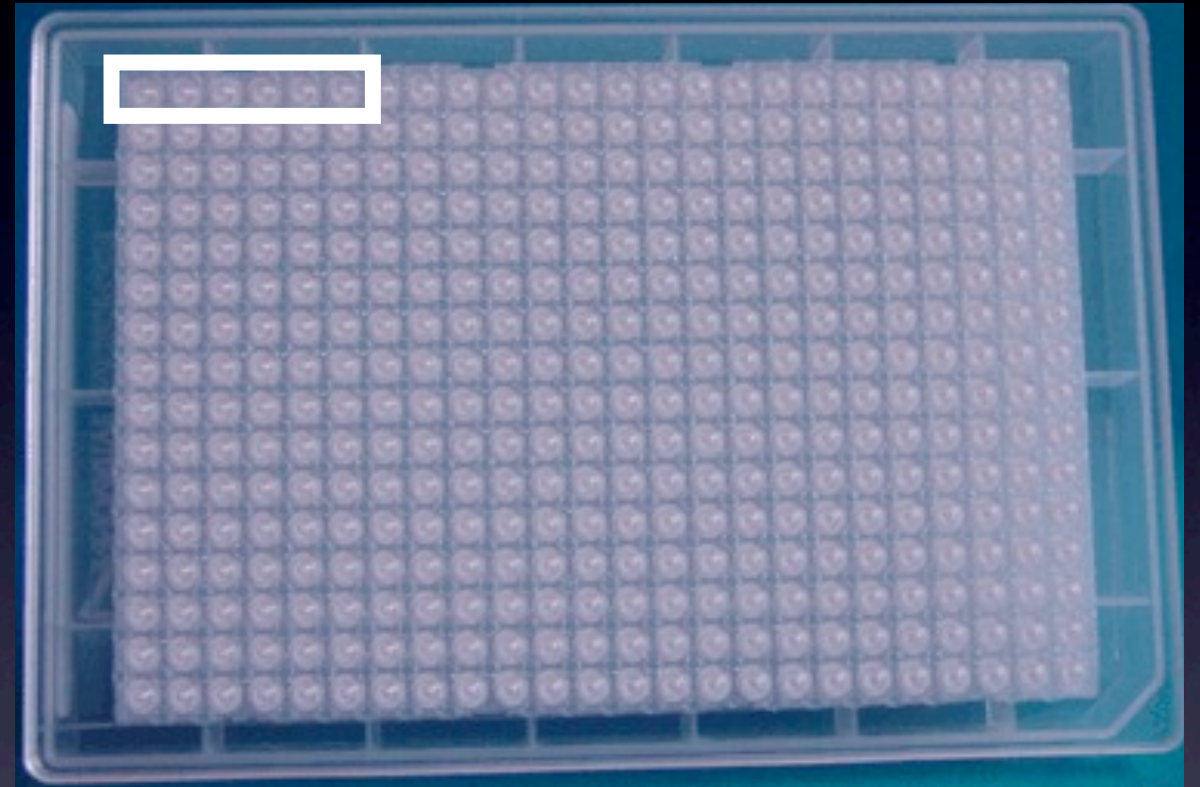
Deme size N

Number of demes d

Migration rate m

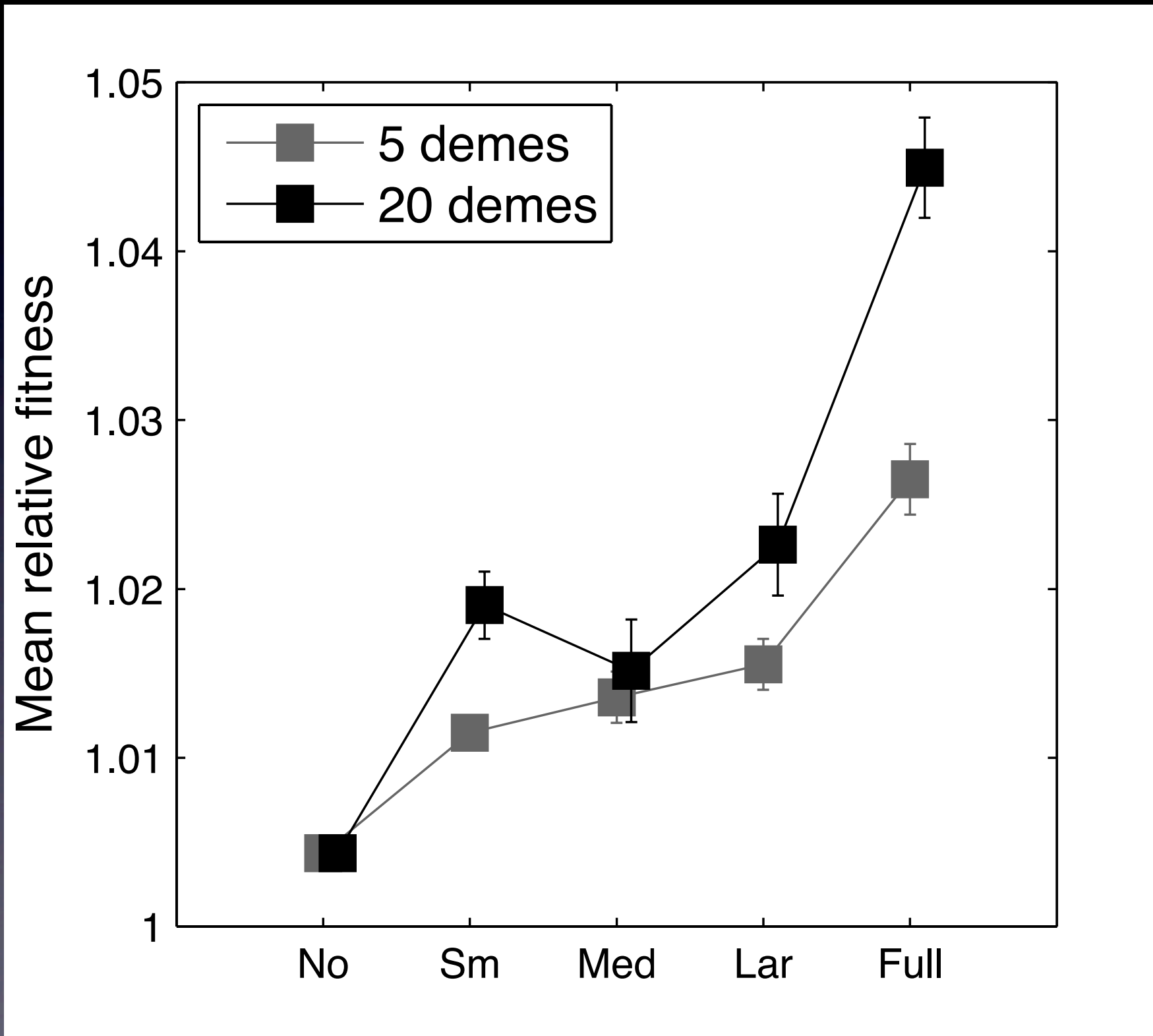
Experimental design

- Haploid yeast, asexual growth
- YPD
- 384-well plates, well volume 64 μ l
- Serial transfer every 24h, dilution 1:1000
- 550 generations (2 months)



$$N_b = 1000$$

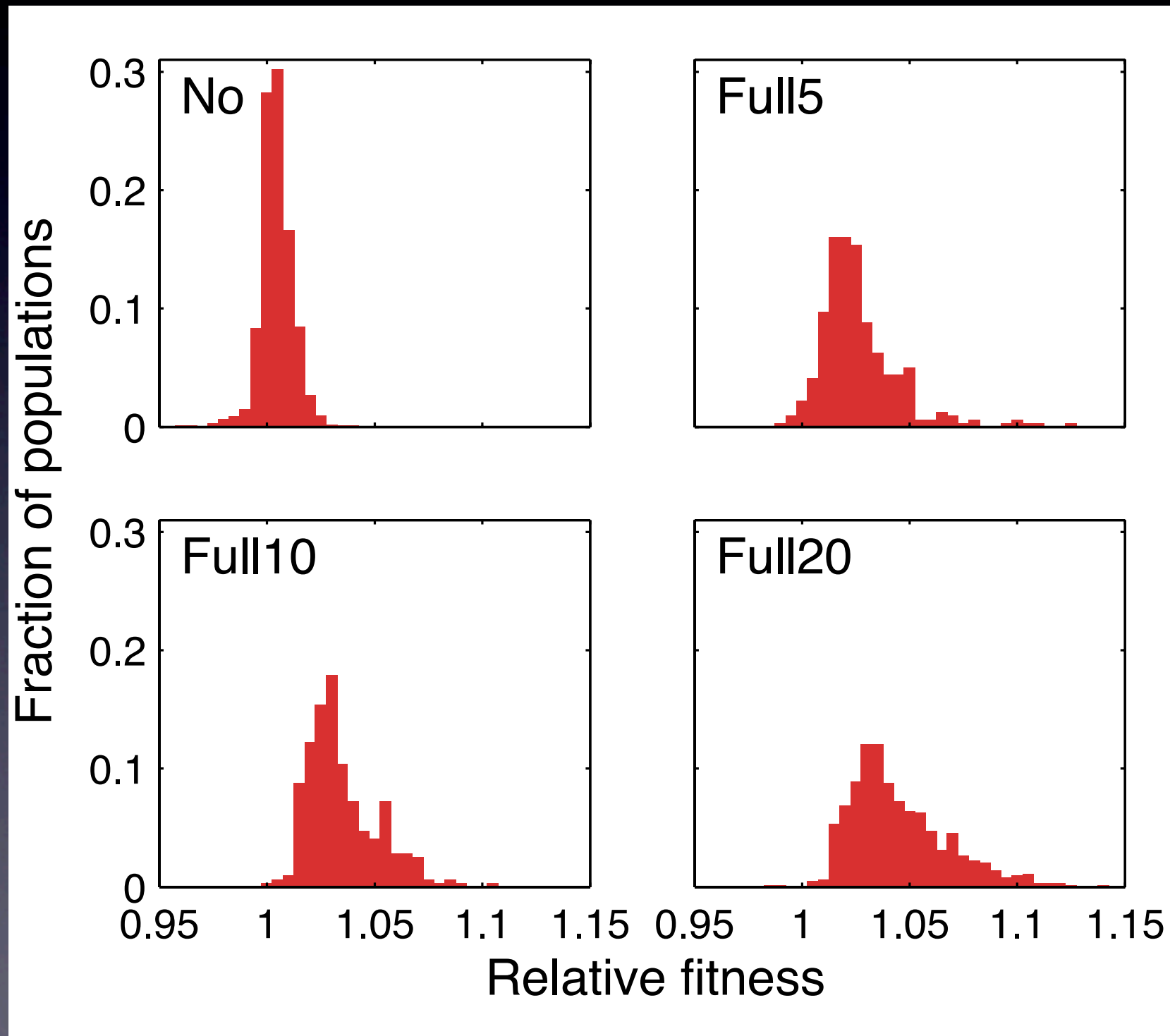
Mean fitness



	<i>m</i> imm/gen
No	0
Sm	5
Med	20
Lar	80
$N_b = 1000$	

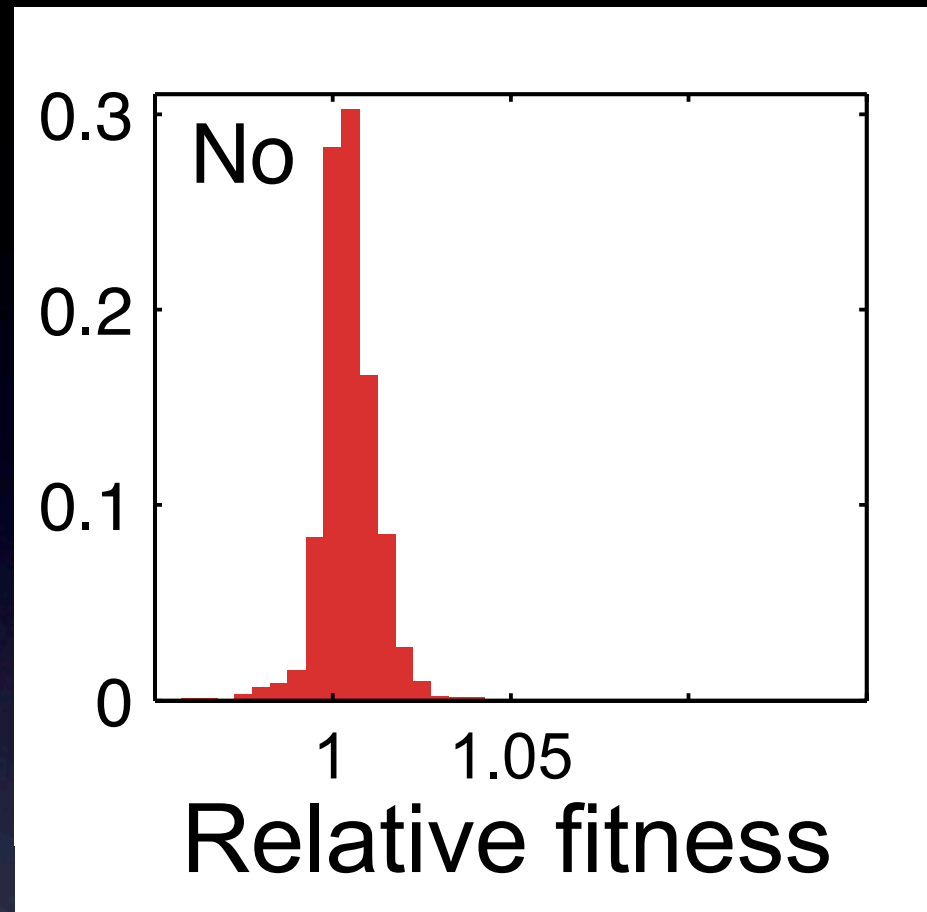
Well-mixed populations

Well-mixed populations. Distribution of mean fitnesses

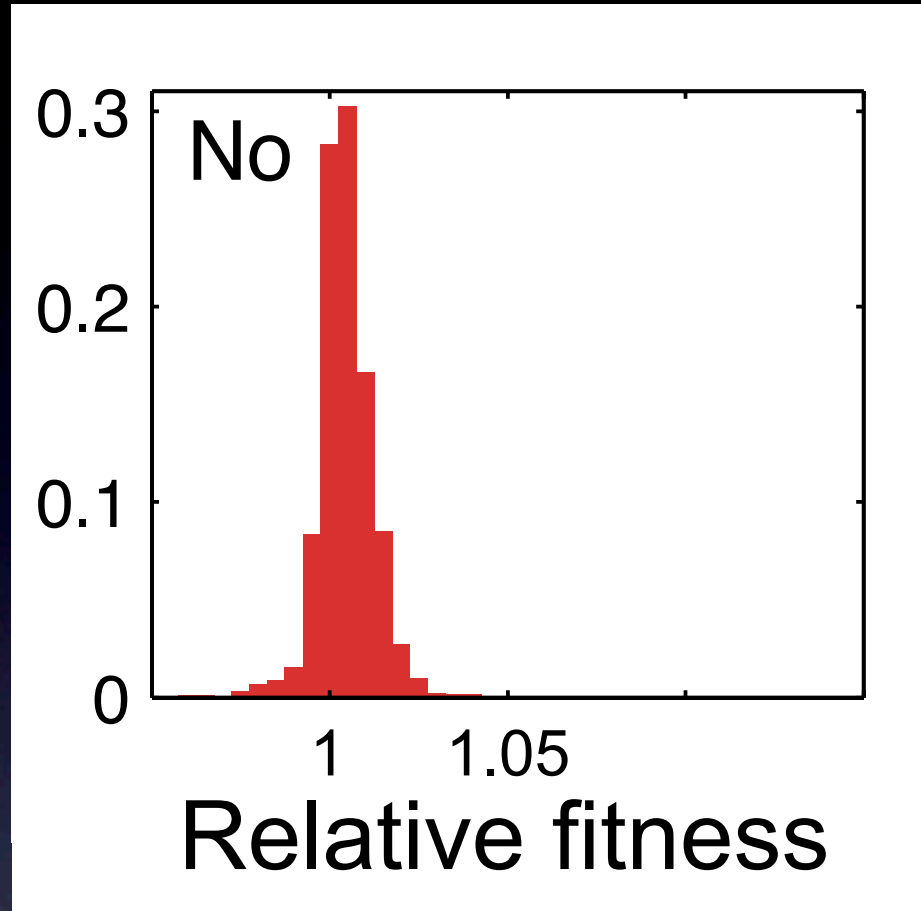


	N_b
No	10^3
Full5	5×10^3
Full10	10^4
Full20	2×10^4

Well-mixed populations

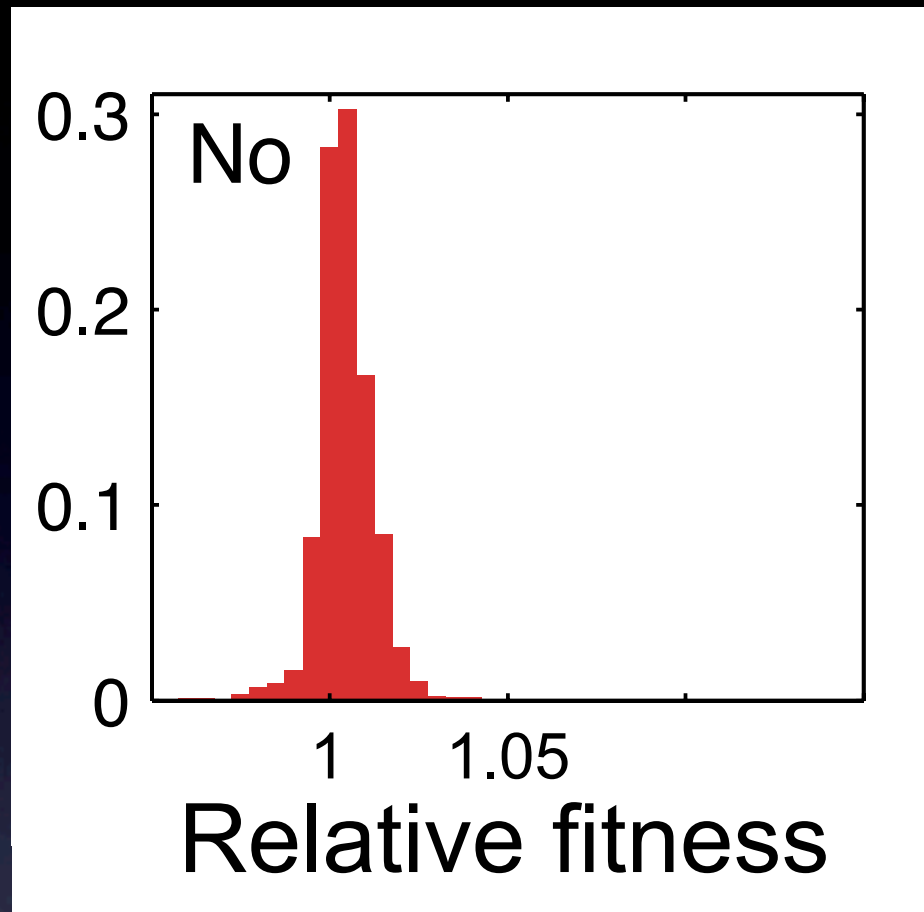


Well-mixed populations



Fraction of populations that
got one beneficial mutation

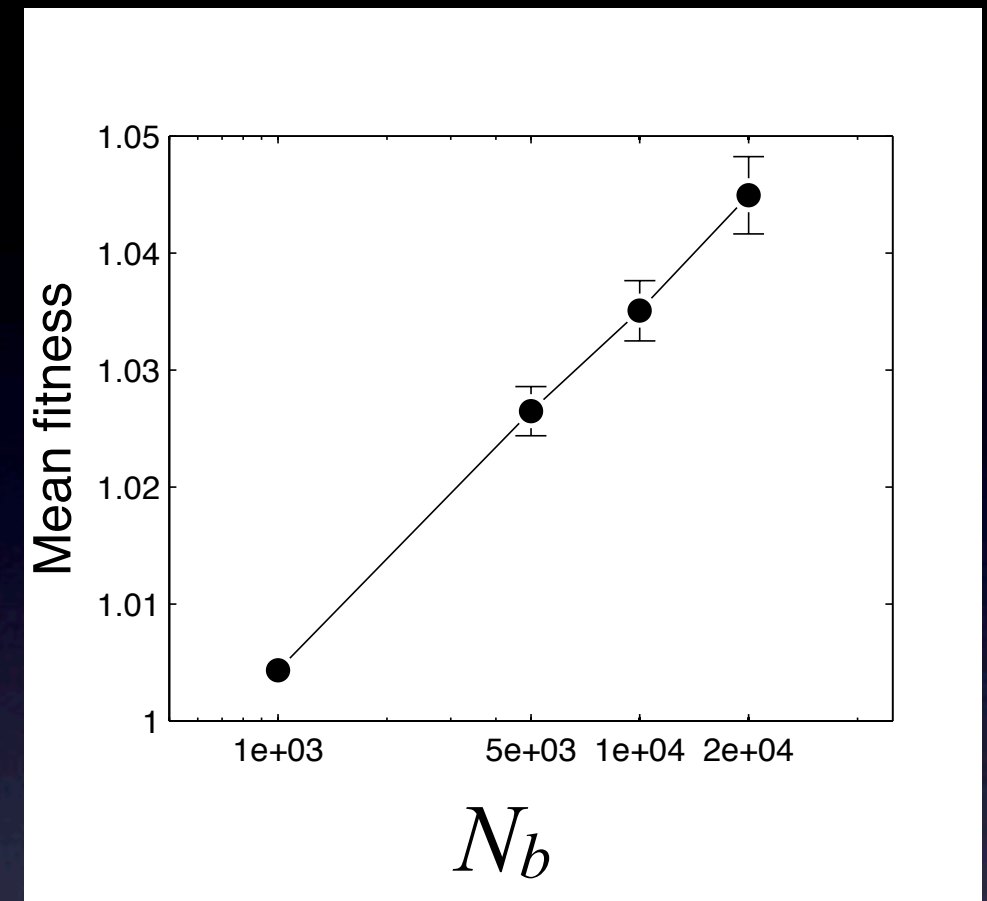
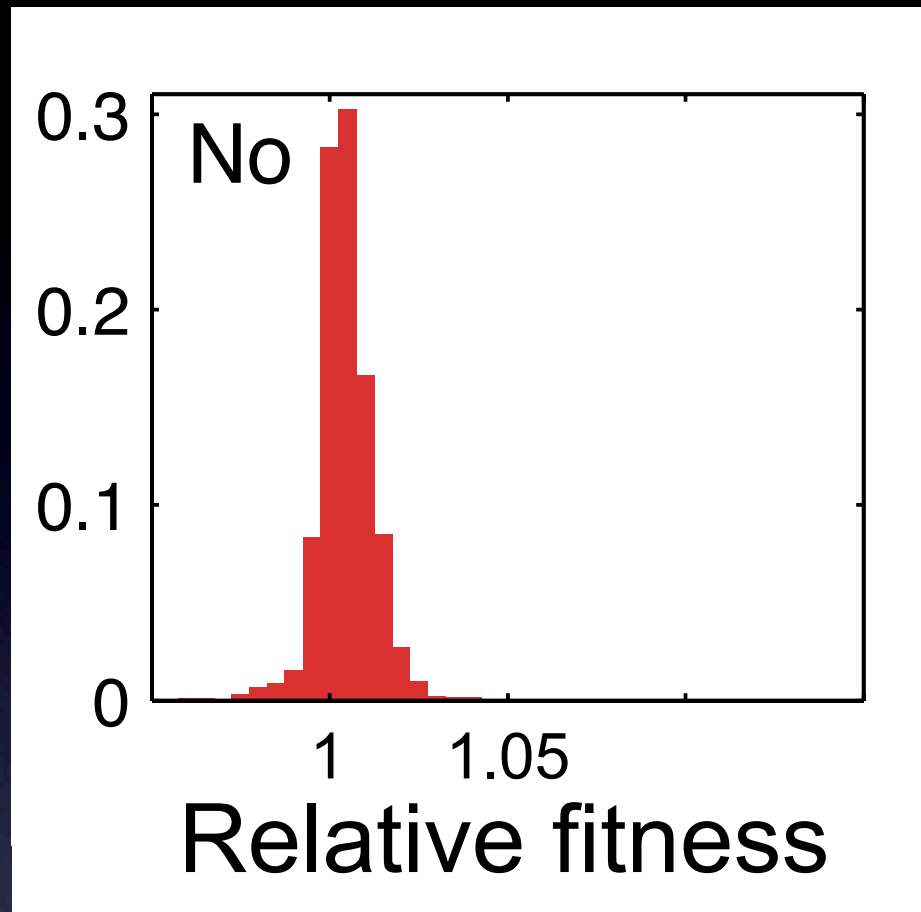
Well-mixed populations



Fraction of populations that
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$$P_1 = 2sN\mu T \approx 0.67$$

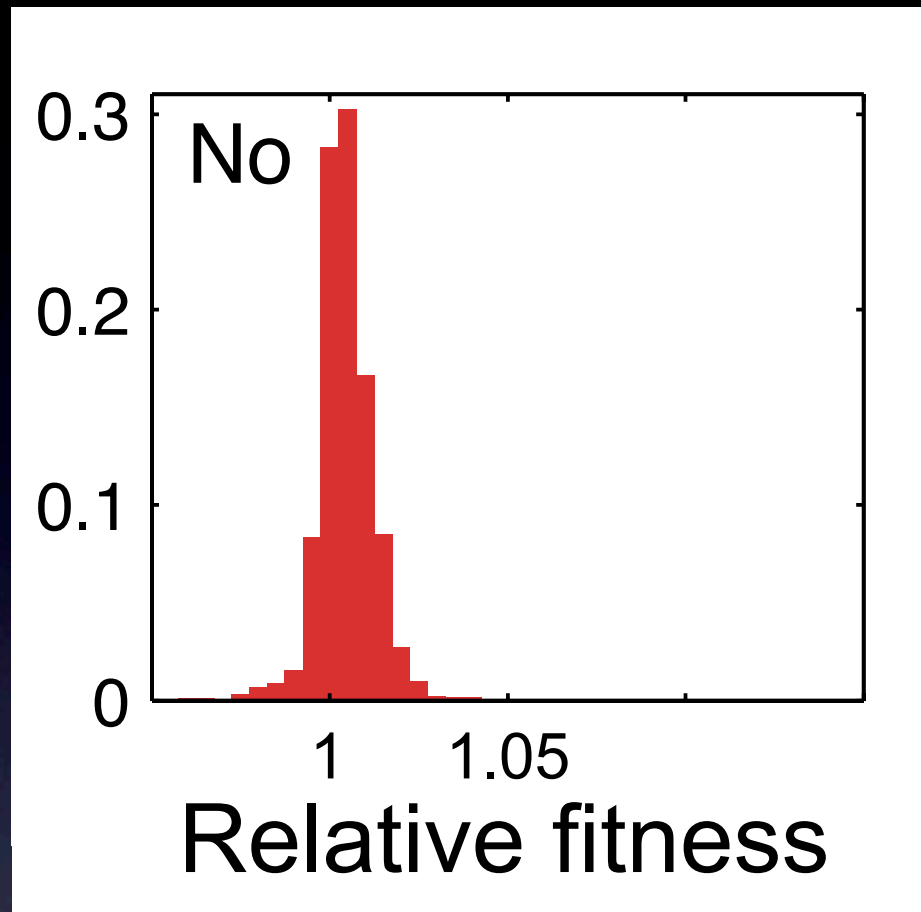
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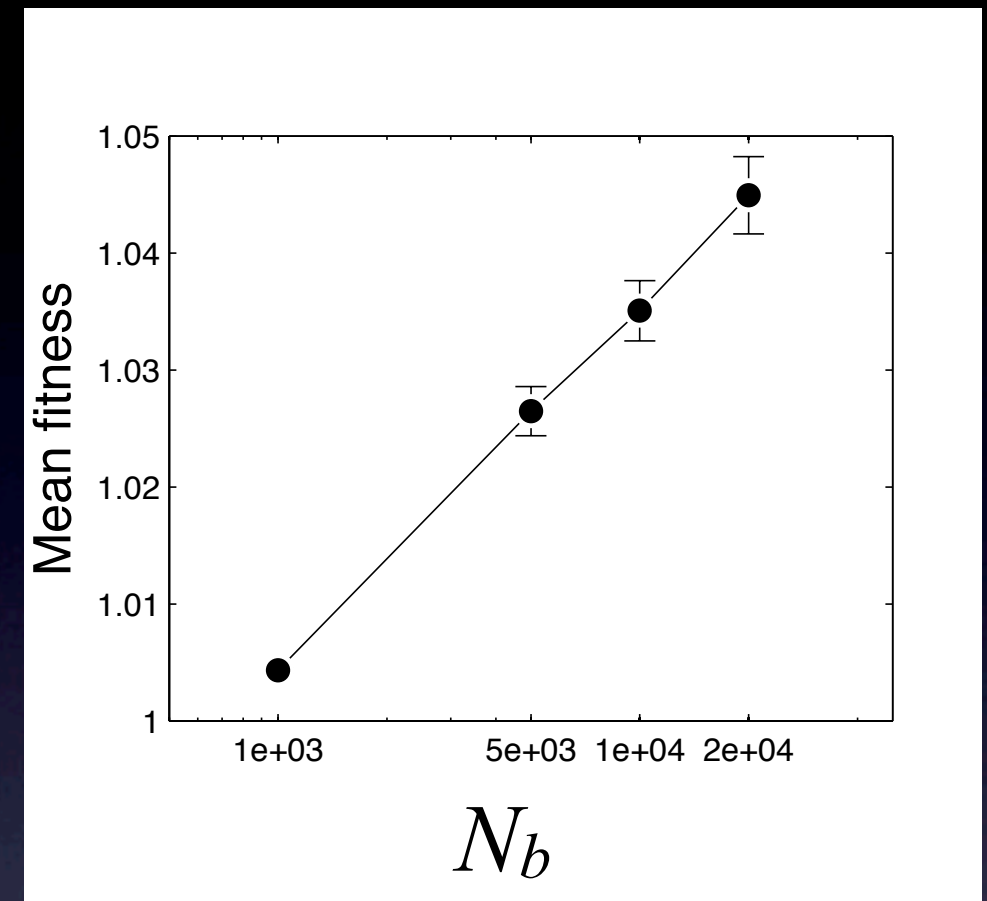
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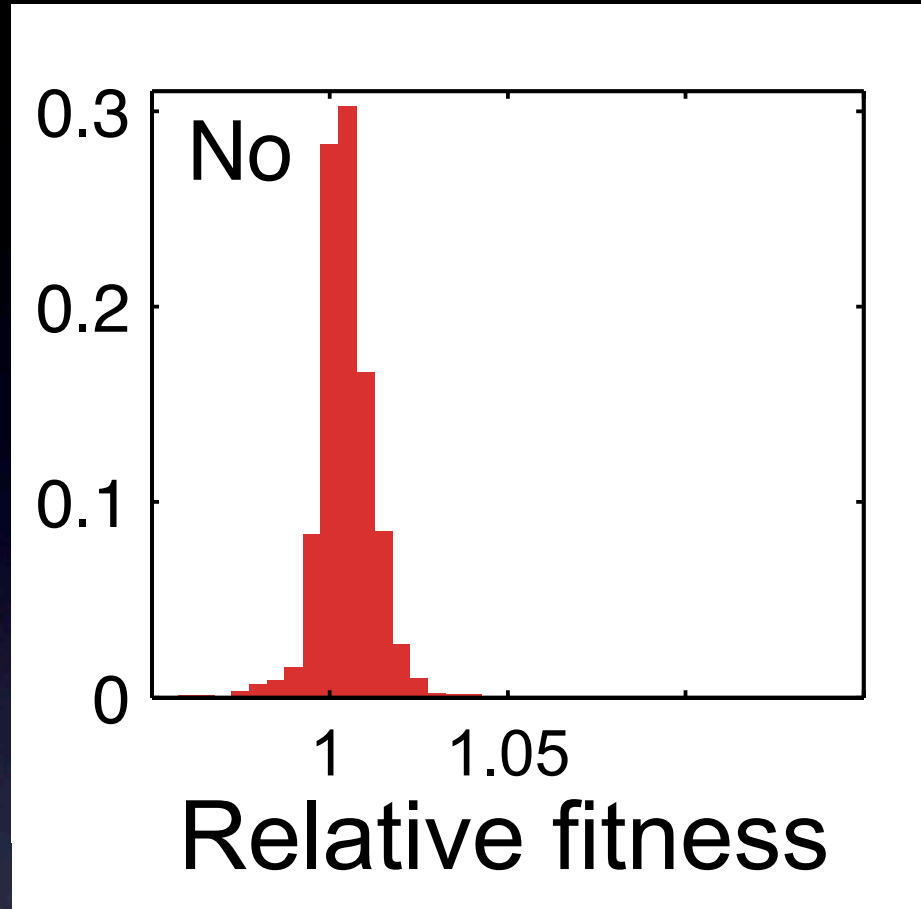
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Slope of mean fitness

$$k = \frac{2s^2T}{\log^2 s/\mu} \approx 0.013$$

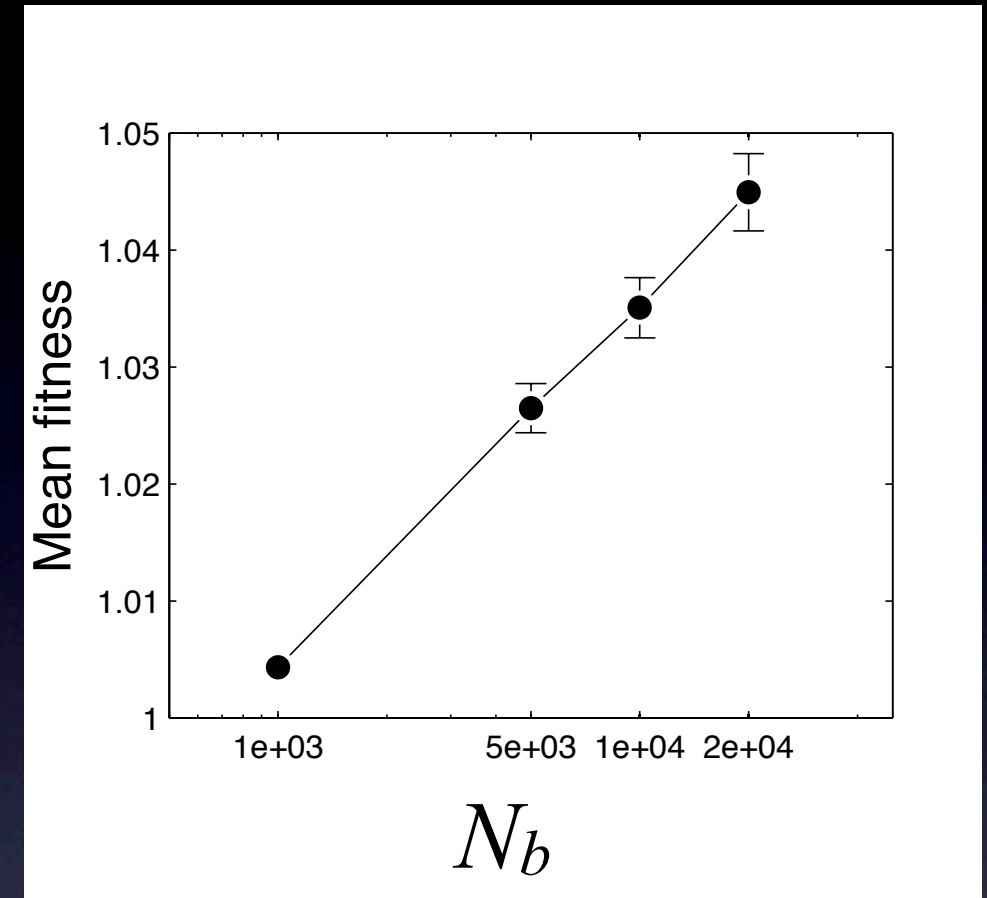
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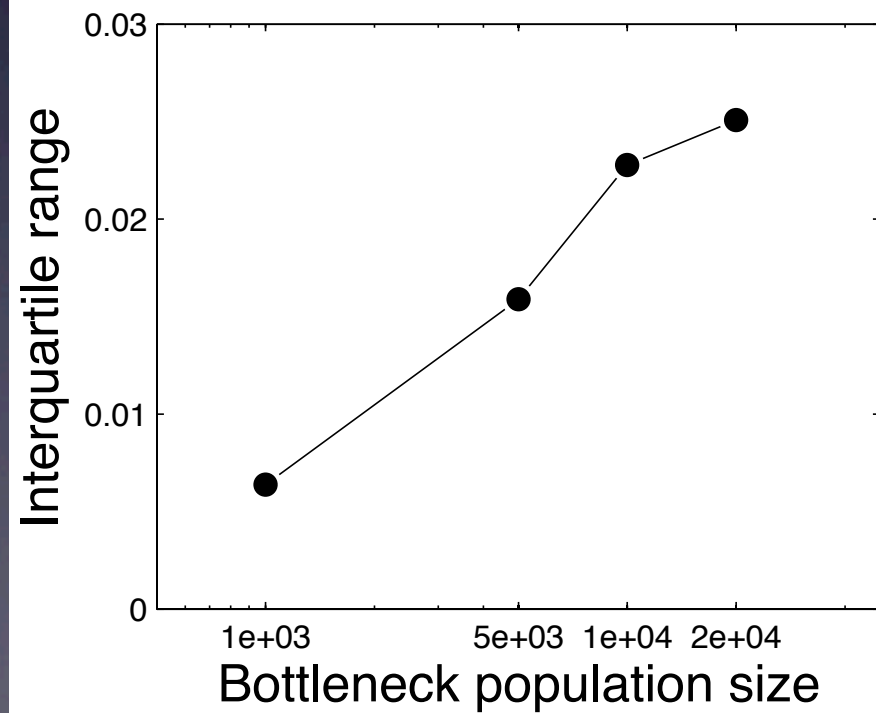
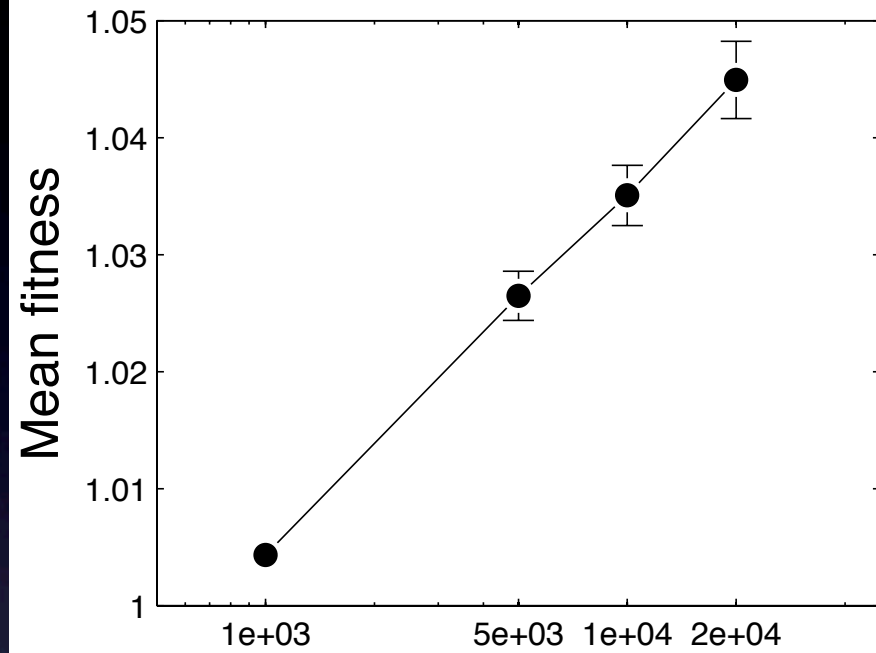
$$\mu \approx 2 \times 10^{-6}$$
$$s \approx 0.03$$



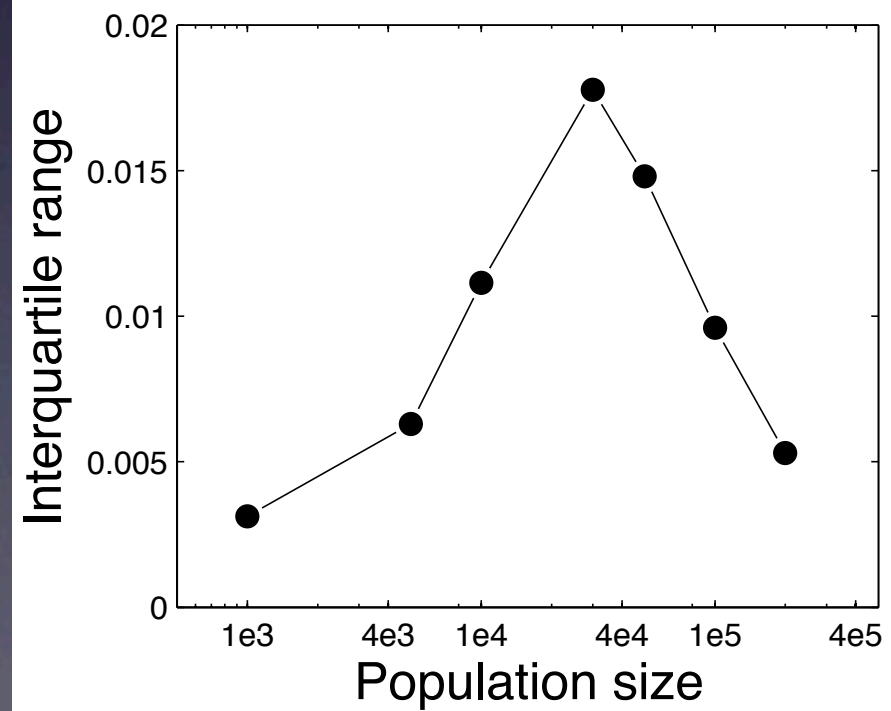
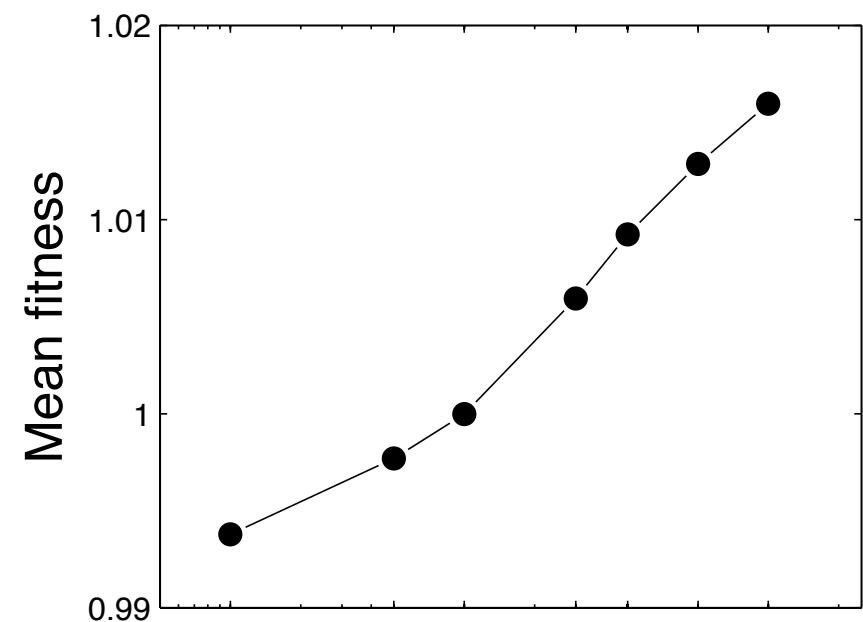
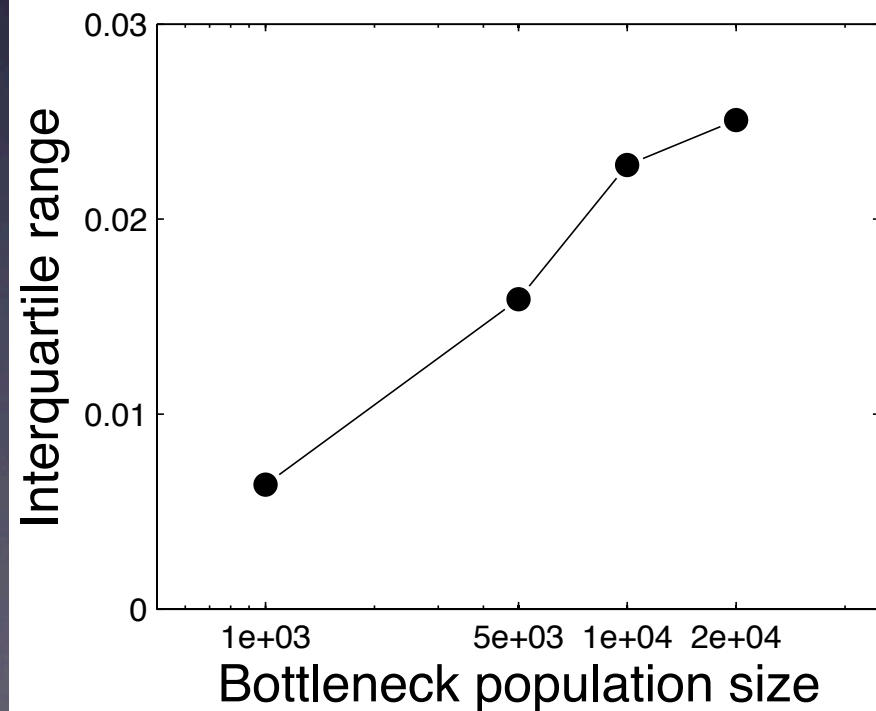
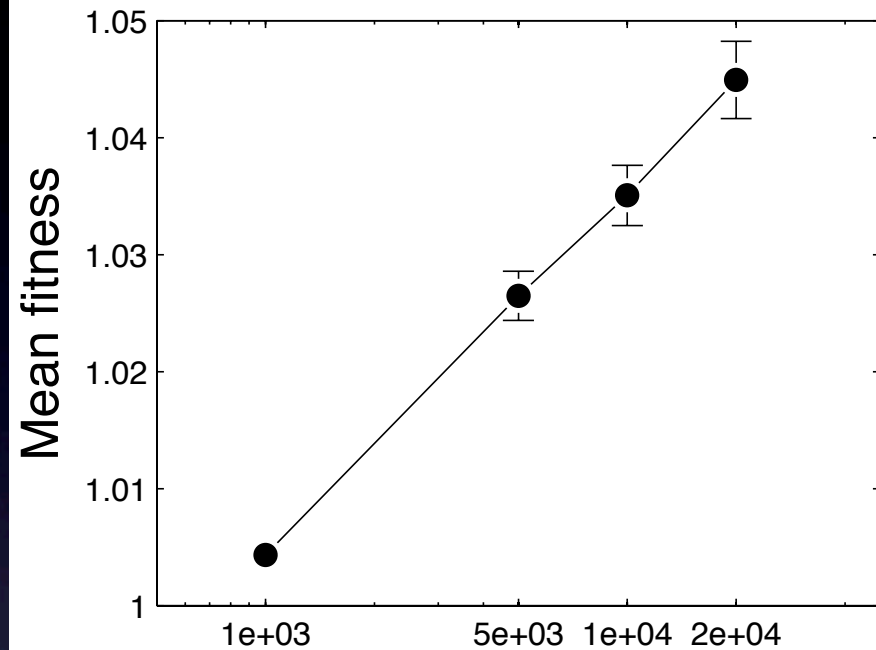
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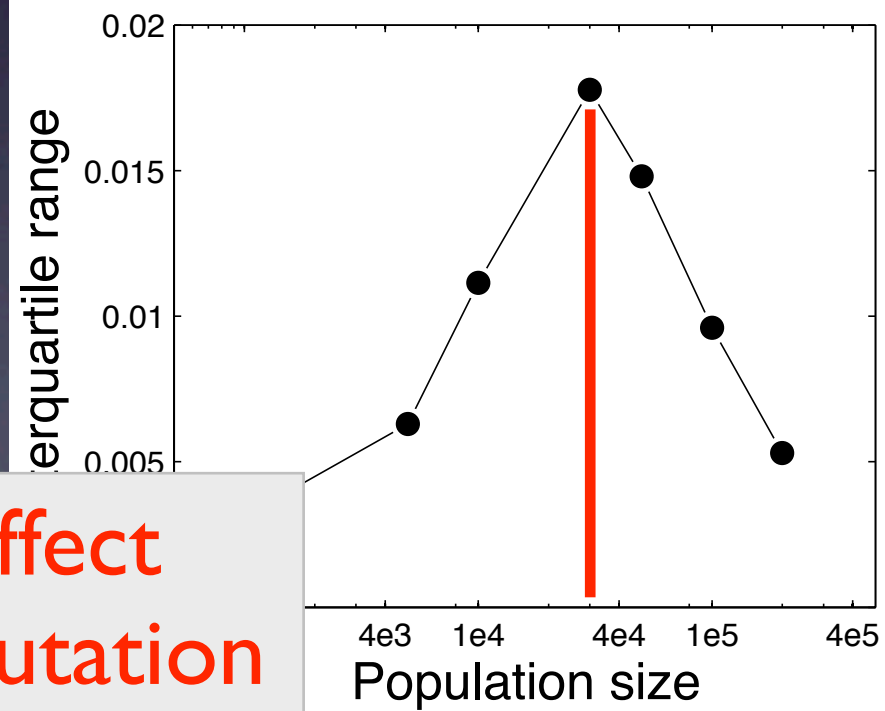
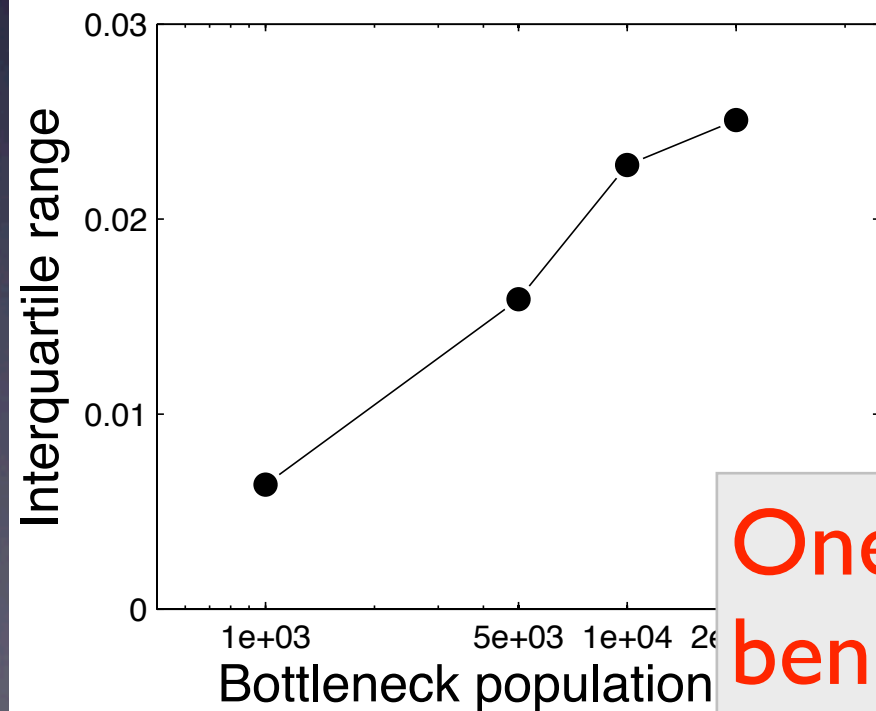
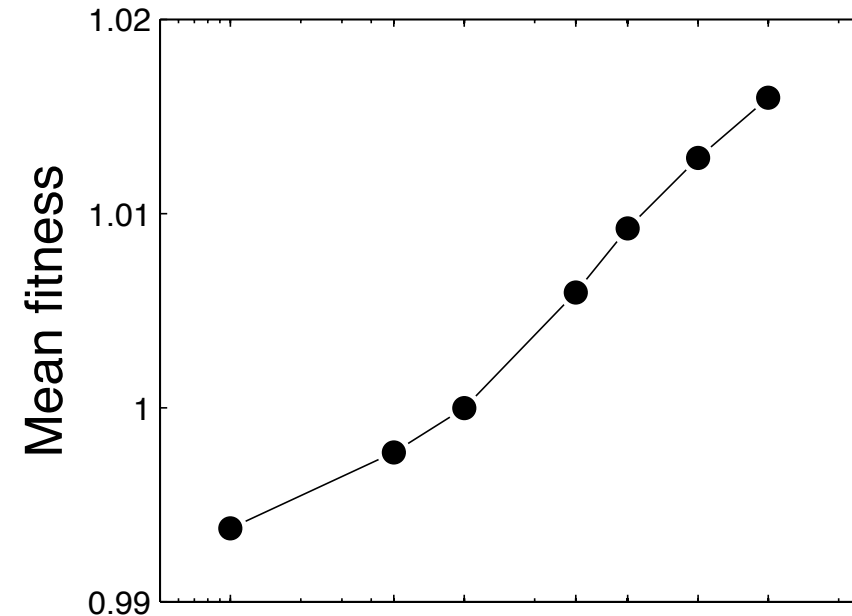
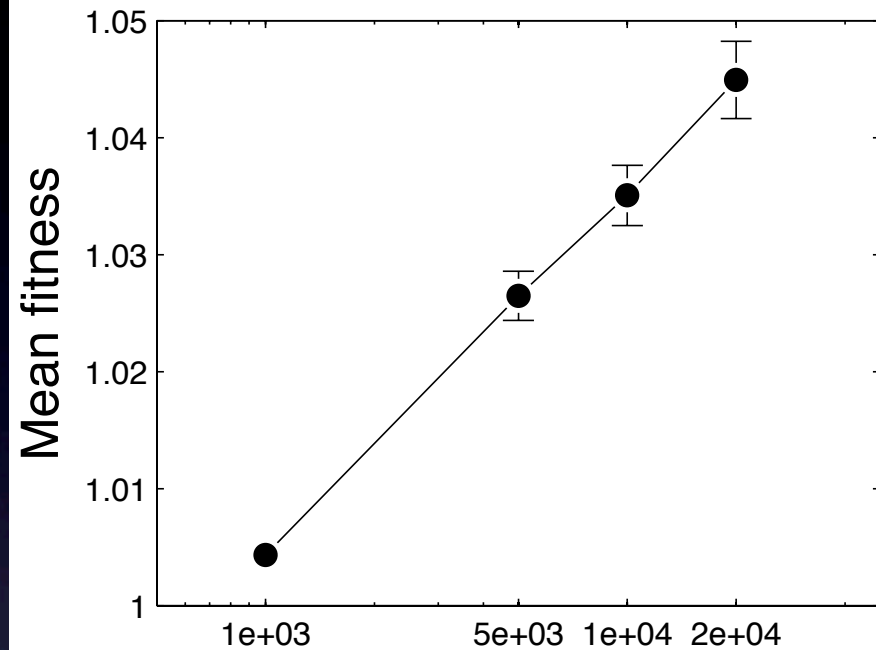
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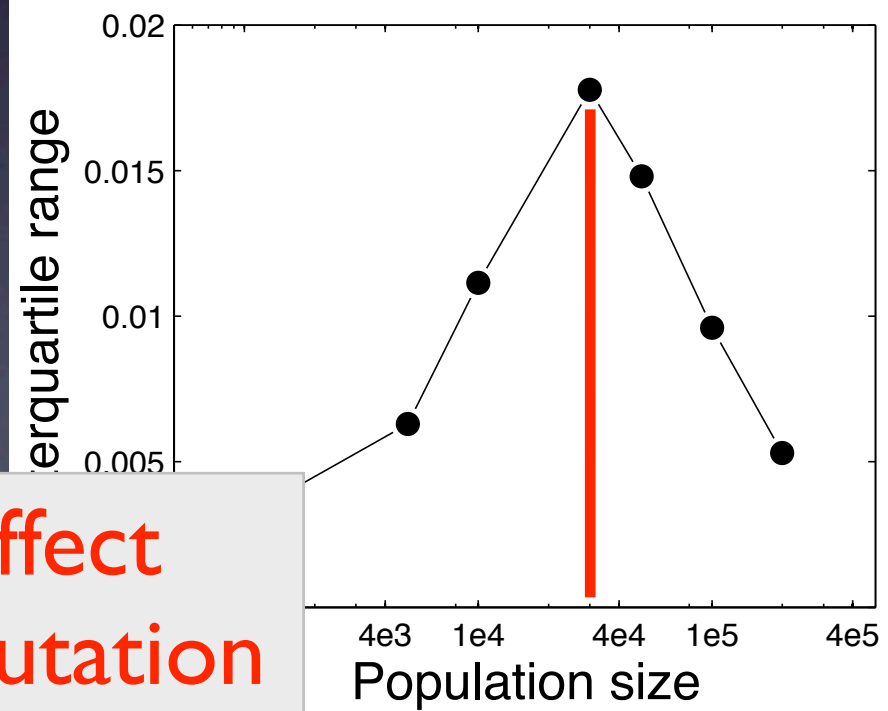
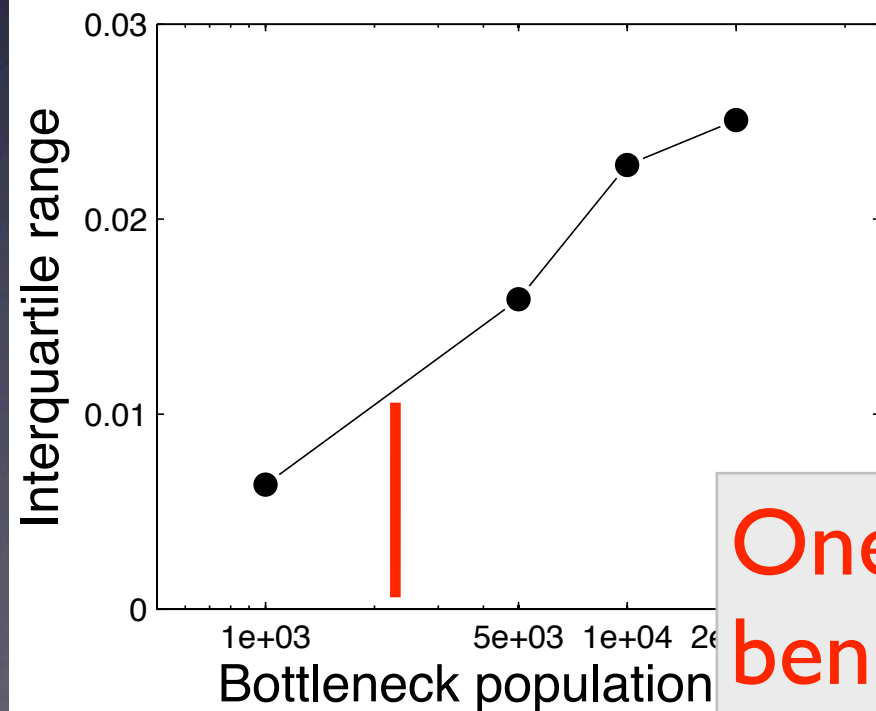
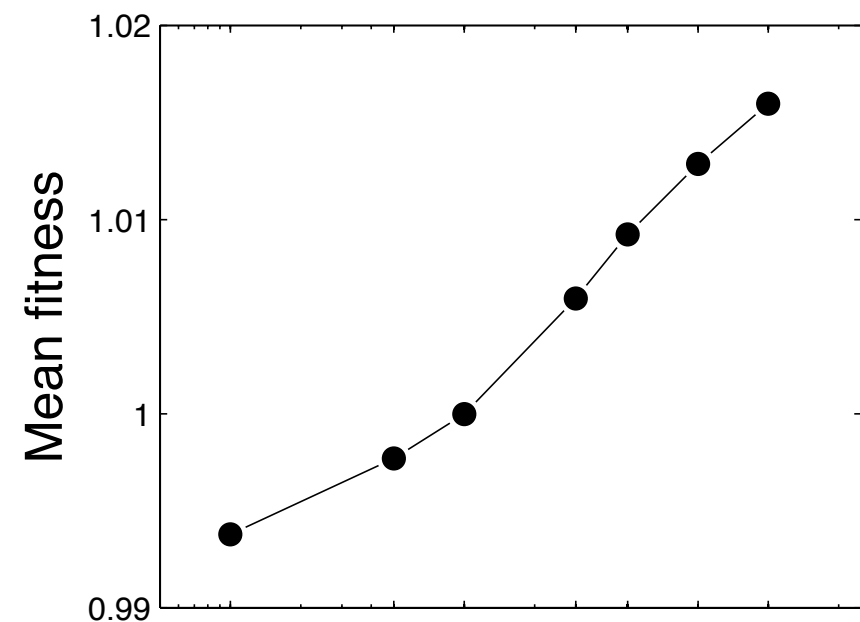
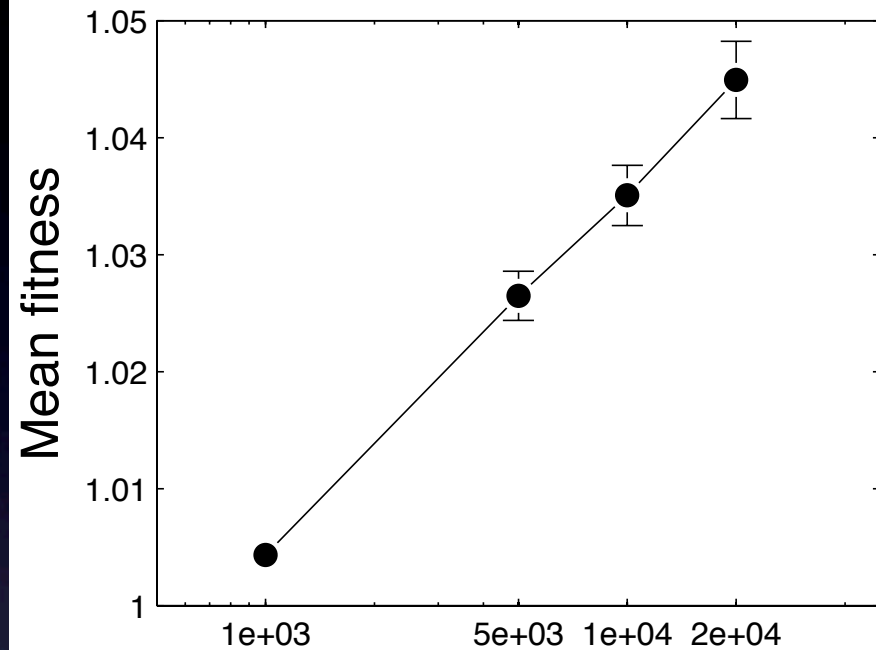


Well-mixed populations



One large-effect
beneficial mutation
per generation

Well-mixed populations



One large-effect
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Thanks

Michael Desai

Joshua Plotkin

Fei Li

Dan Rice

Desai Lab

Core facilities at Princeton University and
Harvard University