

**Simulations of the gravity and magnetic fields
to be measured by *Juno* at Jupiter**

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NASA *Juno* Mission to Jupiter

launched in August 2011

arriving in July 2016

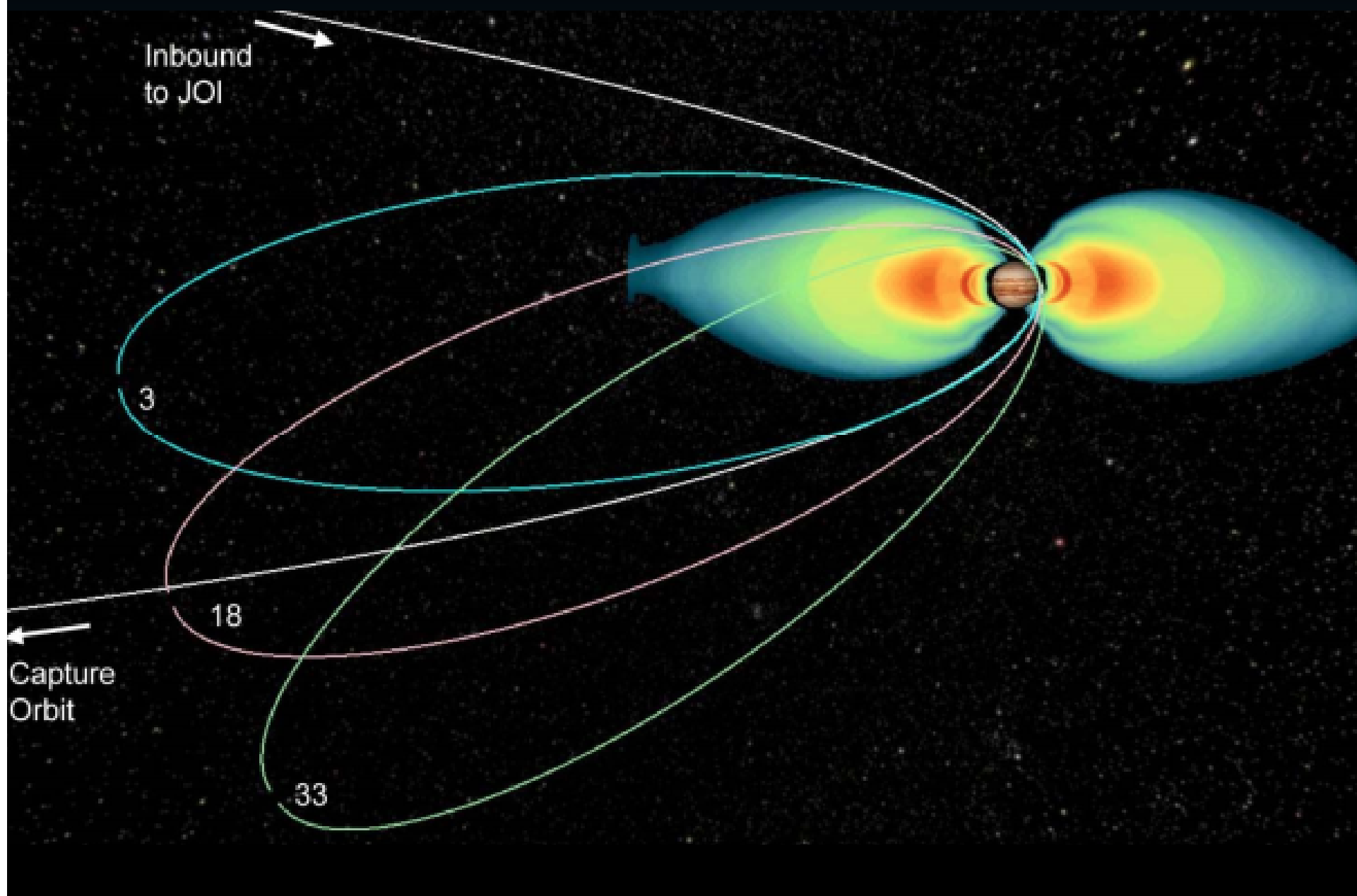
one year orbiting Jupiter

**11-day, eccentric, polar orbit
with closest approach of 5000 km**

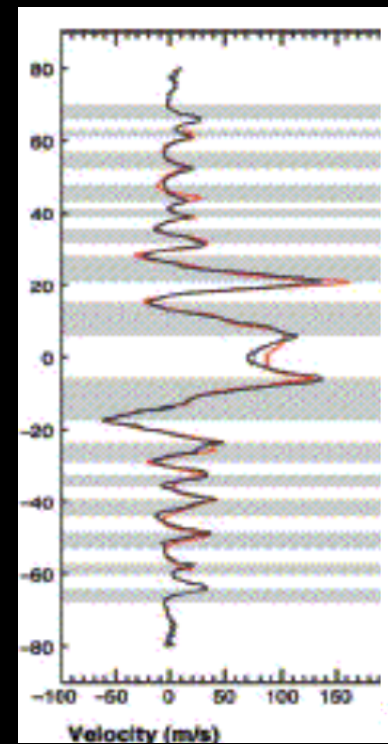
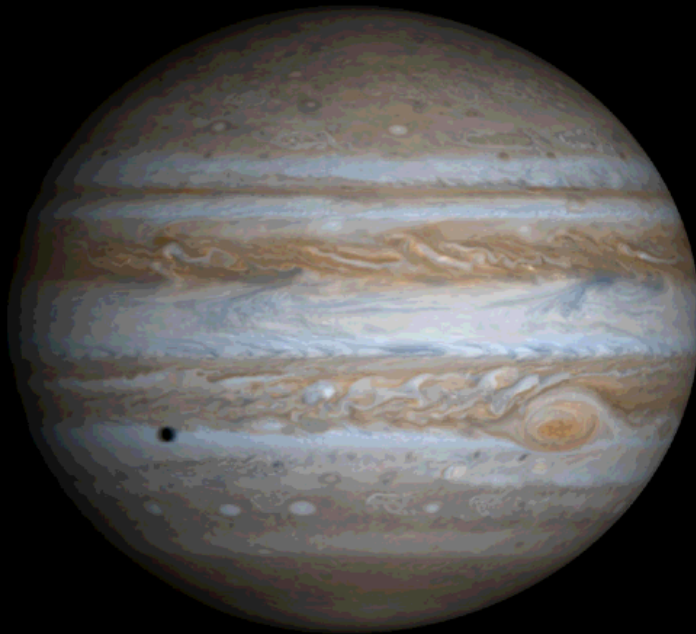
magnetosphere, atmosphere, interior

NASA *Cassini Soltice* Mission to at Saturn

NASA *Juno* Mission to Jupiter



What is the structure of the banded zonal winds deep below the surface and how is it maintained?



*Spherical harmonic expansions of the
gravitational and magnetic fields*

$$\Phi'_G(r, \theta, \phi, t) = \sum_{l,m} \Phi_l^m(r) Y_l^m(\theta, \phi)$$

For $m = 0$ and $r \geq r_{top}$,

$$\Phi_G(r, \theta, t) = -\frac{GM}{r} \left(1 - \sum_l J_l \left(\frac{r_{top}}{r} \right)^l P_l(\cos \theta) \right)$$

and

$$\Delta J_l \equiv J_l - \bar{J}_l = \left(\frac{2l+1}{4\pi} \right)^{1/2} \frac{r_{top}}{GM} \Phi_l^0(r_{top}).$$

Using all l and m , we can plot the three
components of

$$\mathbf{g}'(r, \theta, \phi, t) = -\nabla \Phi'_G$$

for $r \geq r_{top}$.

Similarly, for the external potential magnetic field (i.e., for $r \geq r_{top}$, $\nabla \times \mathbf{B} = 0$),

$$\mathbf{B} = -\nabla \Phi_B$$

where

$$\Phi_B = r_{top} \sum_{l,m} \left(\frac{r_{top}}{r} \right)^{l+1} (g_l^m \cos m\phi + h_l^m \sin m\phi) P_l^m .$$

For $m = 0$ and $r \geq r_{top}$, we can plot g_l^0 vs l .

Using all l and m , we can plot the three components of \mathbf{B} for $r \geq r_{top}$.

Numerical method and resolution

Spherical harmonic and Chebyshev polynomial expansions:

$$l_{max} = m_{max} = 511, n_{max} = 241$$

grid space: 1536 x 768 x 241

$\Delta t \approx 100$ s, 1 million time steps

Polytropic reference state fitted to models of Nettelmann et al. 2008 and French et al. 2012, using a polytropic index of 0.96.

$$\bar{p} \propto \bar{\rho}^{2.04}$$

$$\bar{T} \propto \bar{\rho}^{0.515}$$

$$r_{top} = 0.98R_J \quad r_{bot} = 0.10R_J \quad D = r_{top} - r_{bot} = 6.15 \times 10^9 \text{ cm}$$

$$\bar{\rho}_{bot}/\bar{\rho}_{top} = 52 \quad (4 \text{ density scale heights, } 8 \text{ pressure scale heights})$$

$$\Omega = 1.77 \times 10^{-4} \text{ radians/s}$$

$$\nu = 10^{10} \text{ cm}^2/\text{s} \text{ (constant)}$$

$$\kappa = 10^{12} \text{ cm}^2/\text{s} \text{ (constant)}$$

$$\eta_{top} = 10^{14} \text{ cm}^2/\text{s} \quad \eta_{0.86R_J} = \eta_{bot} = 10^{10} \text{ cm}^2/\text{s}$$

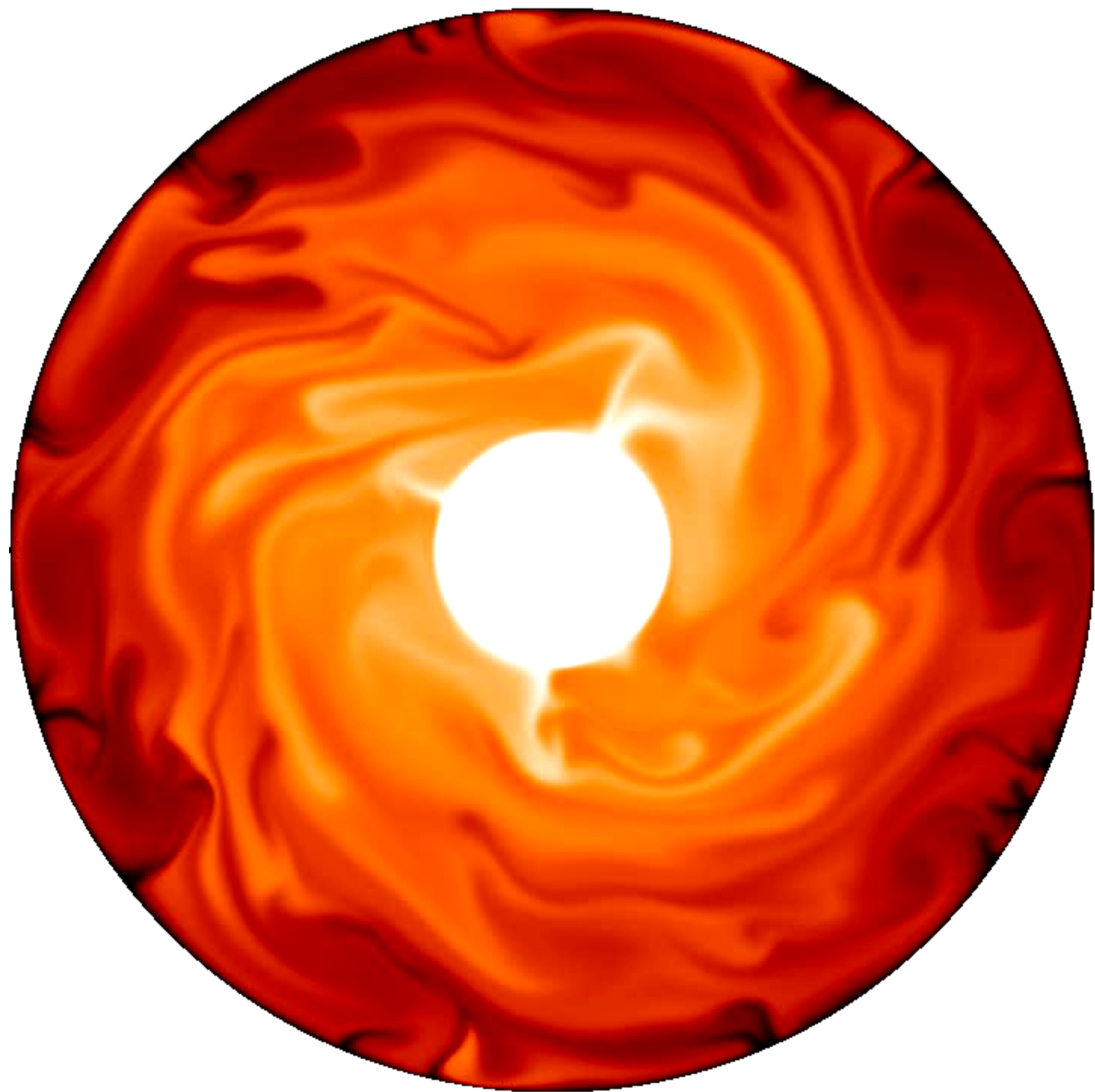
$$\text{Pr} = \frac{\nu}{\kappa} = 10^{-2}$$

$$\text{Ek} = \frac{\nu}{\Omega D^2} = 10^{-6}$$

$$\text{Re} = \left(\frac{UD}{\nu} \right) = 10^4$$

$$\text{Rm} = \left(\frac{UD}{\eta} \right) = 10^3$$

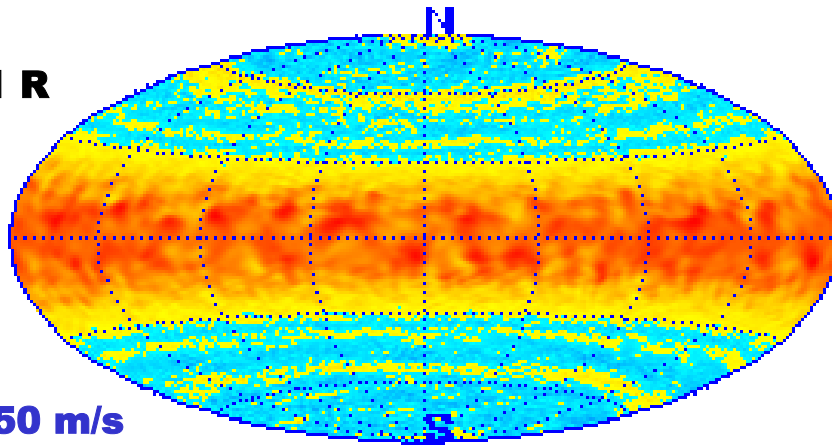
$$\text{Ro} = \left(\frac{U}{\Omega D} \right) = 10^{-2}$$



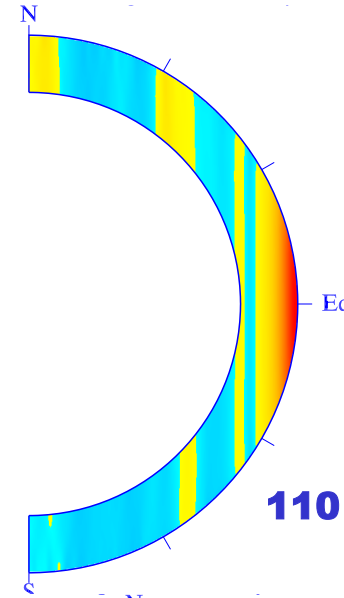
Zonal winds (differential rotation)

thin spherical shell

1 R

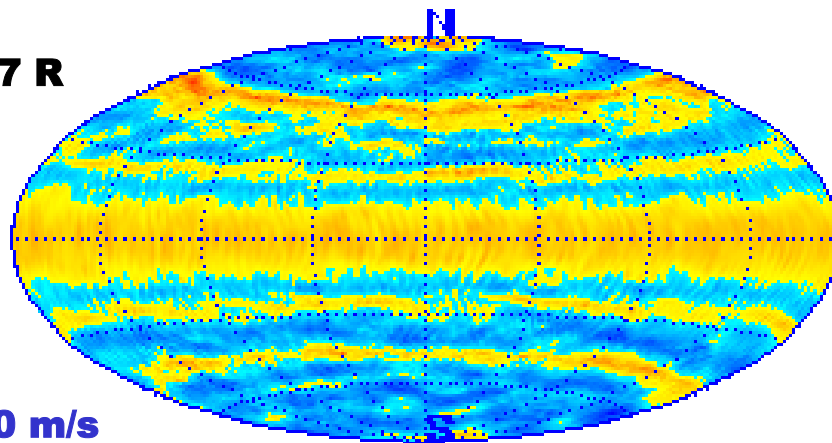


150 m/s

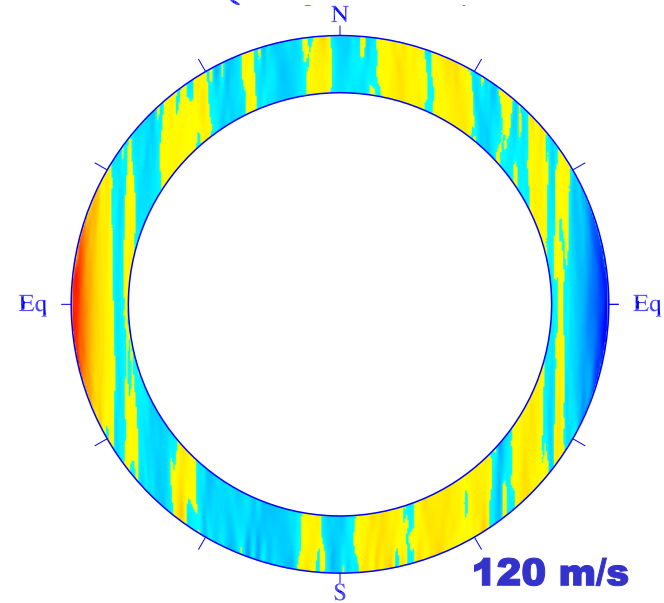


110 m/s

0.87 R



40 m/s

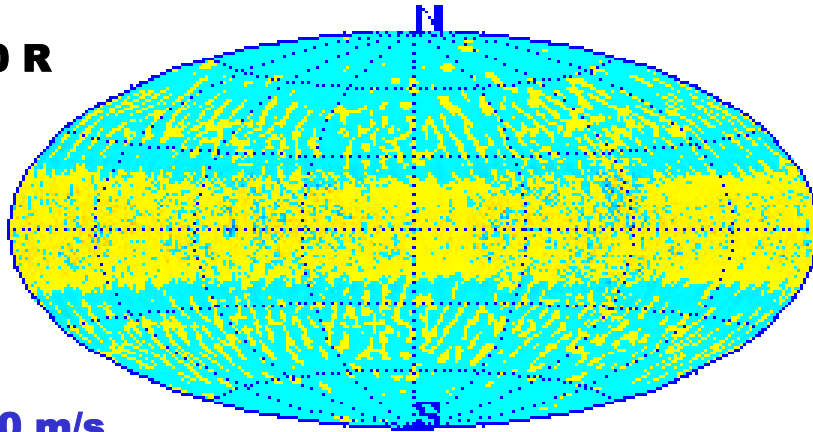


120 m/s

Zonal winds (differential rotation)

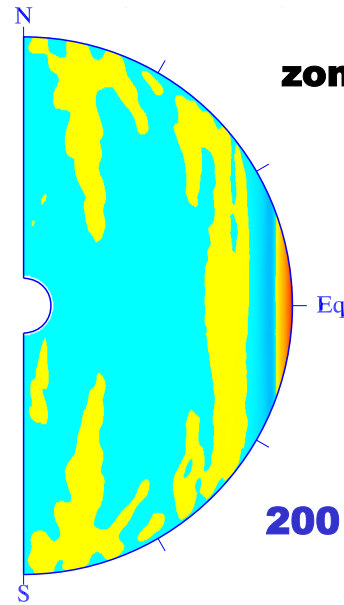
deep spherical shell

1.0 R



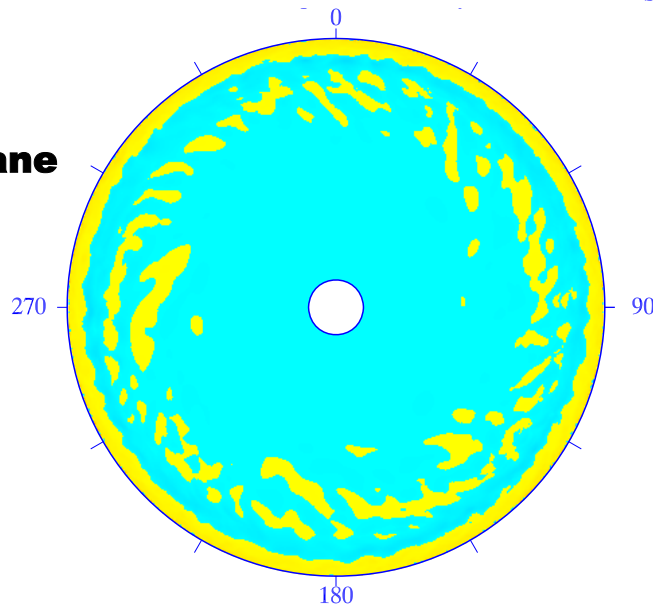
250 m/s

zonal ave



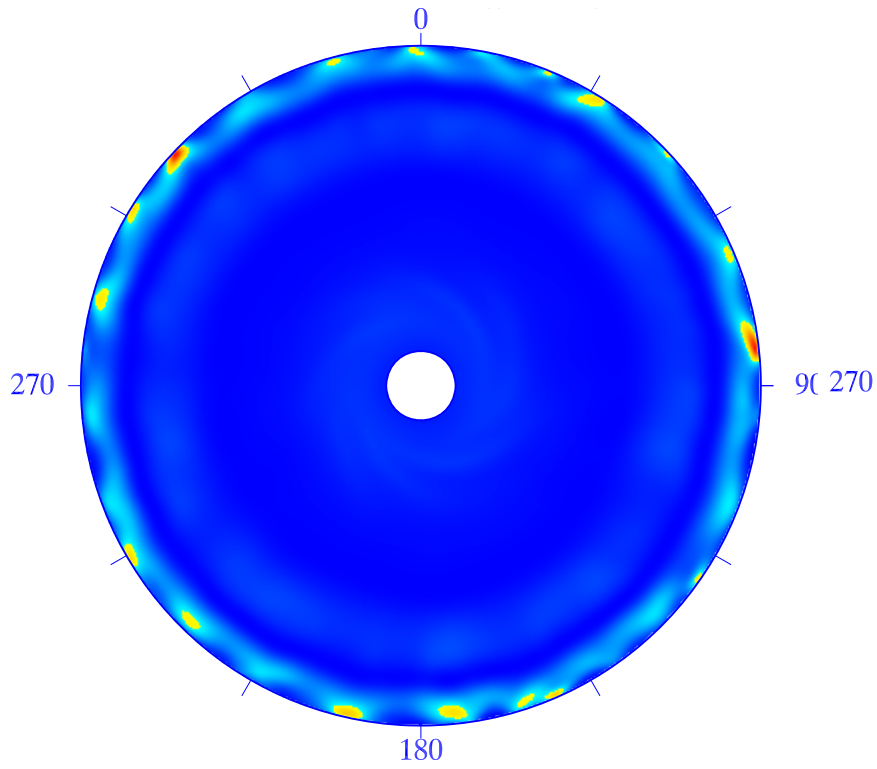
200 m/s

eq plane

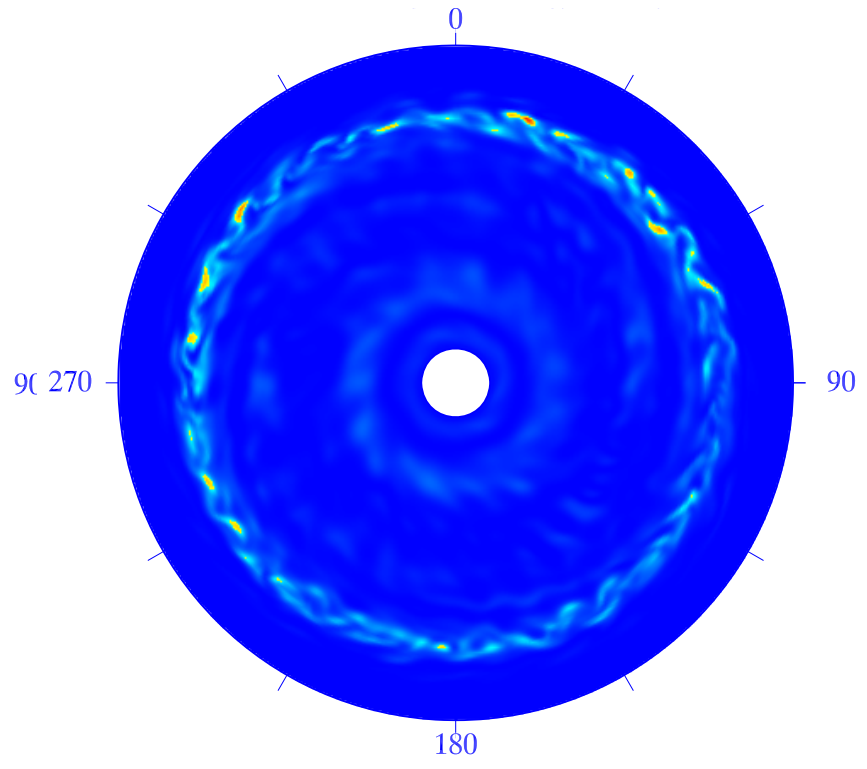


equatorial plane

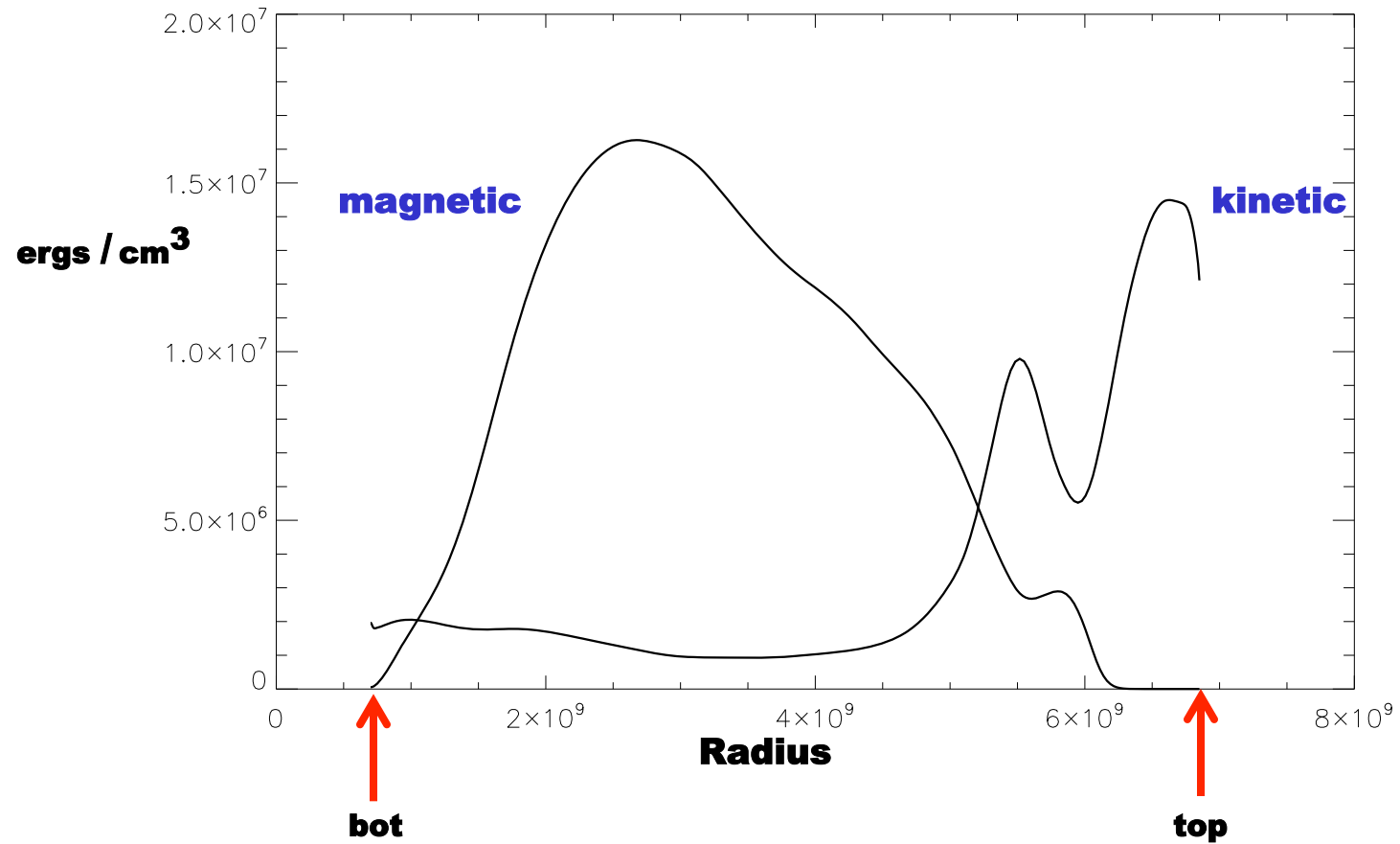
kinetic energy density



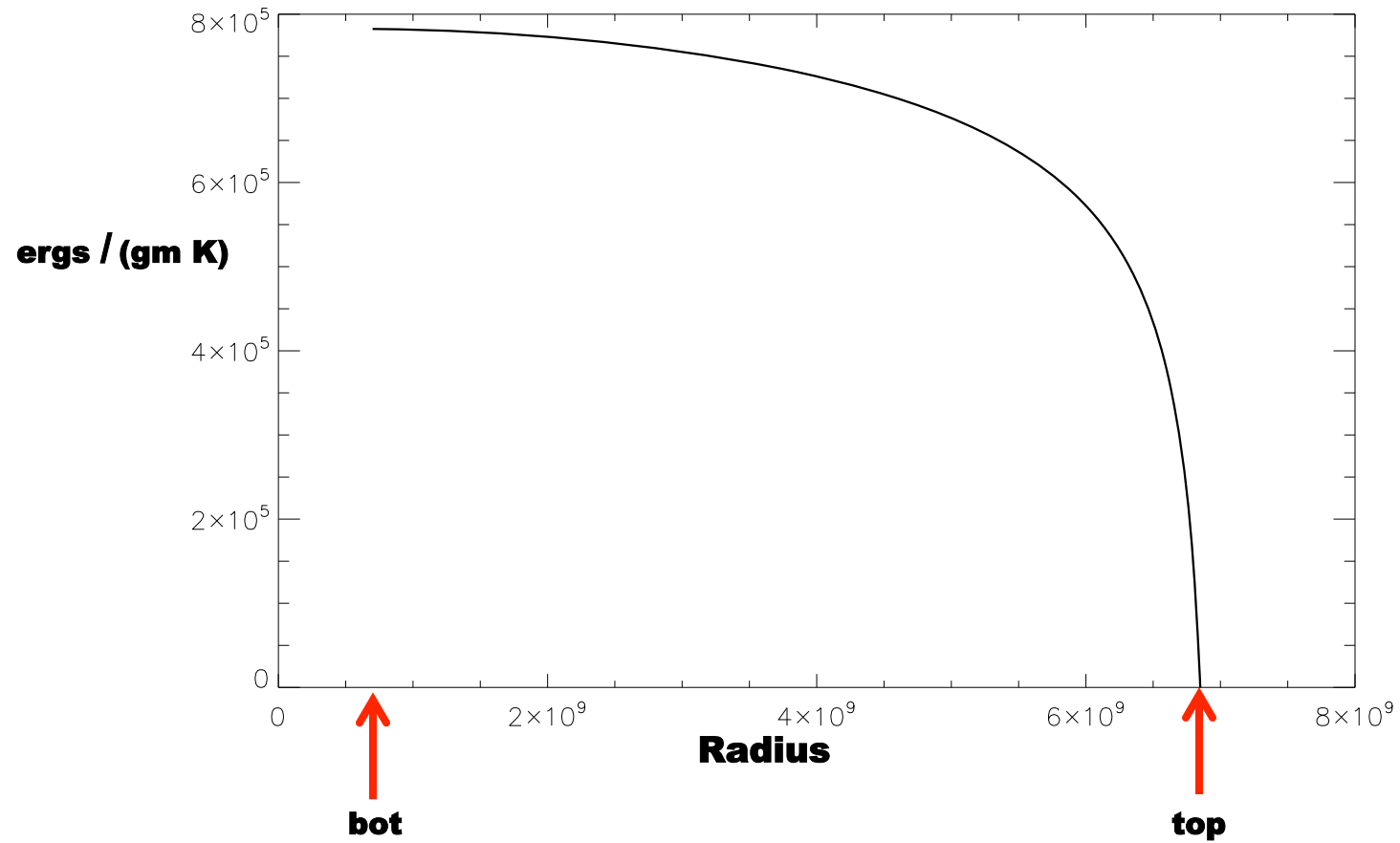
magnetic energy density



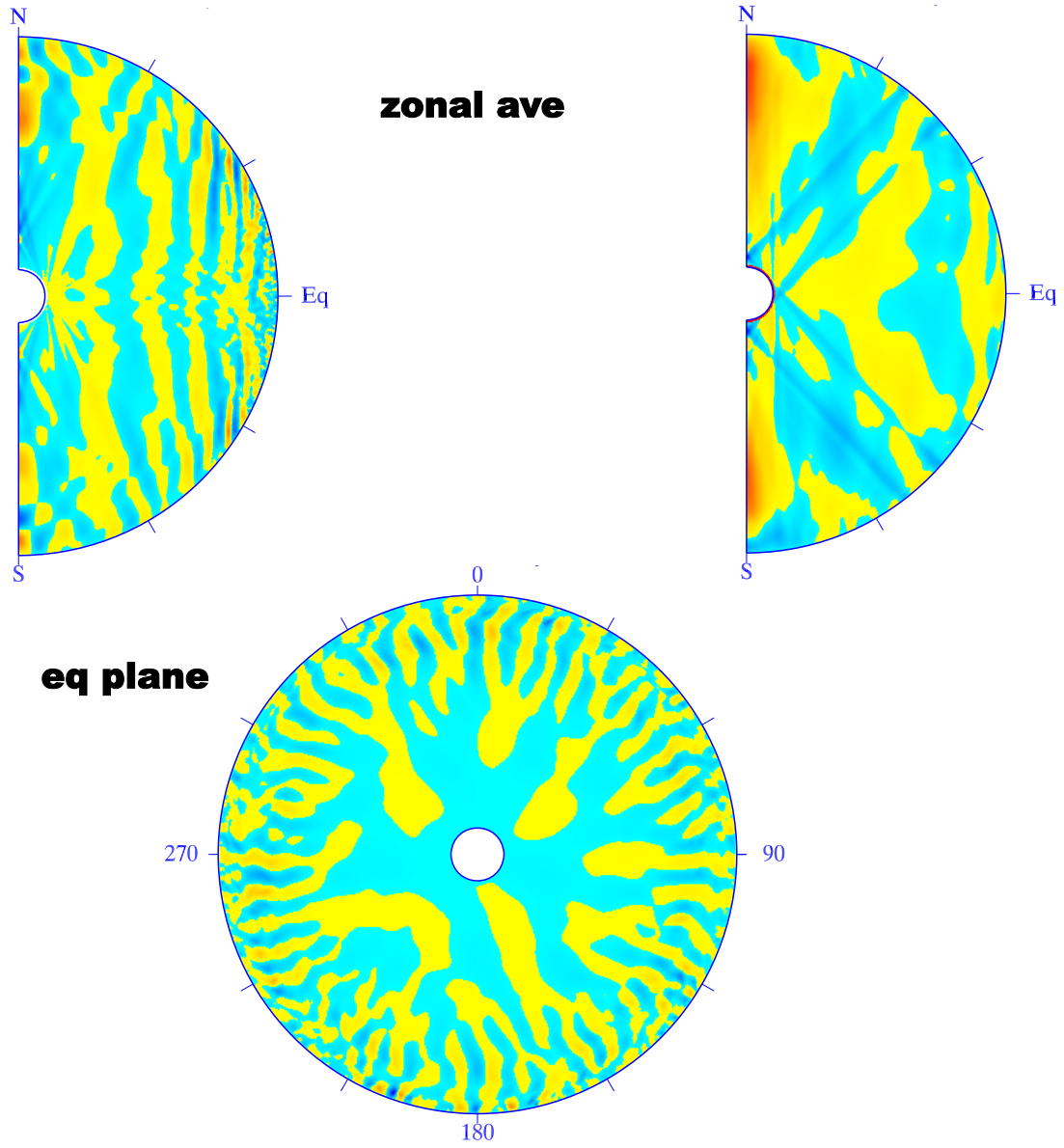
Magnetic energy density



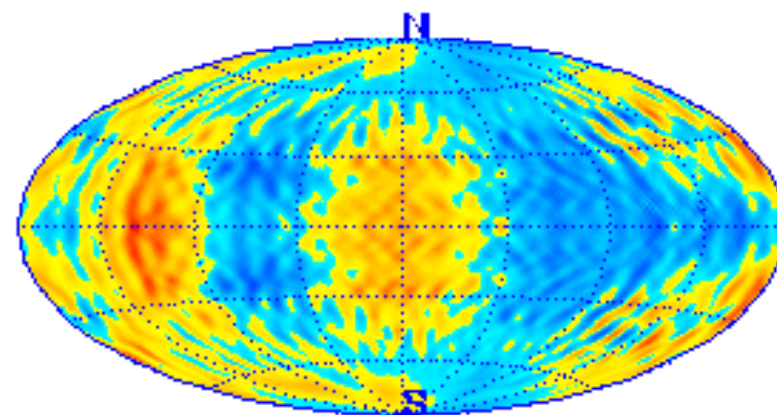
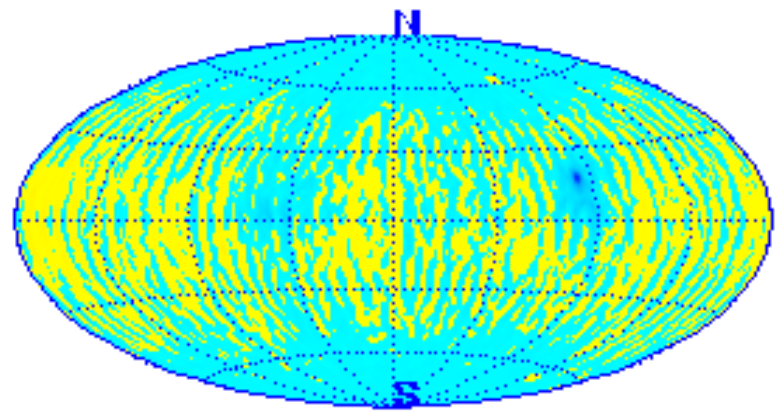
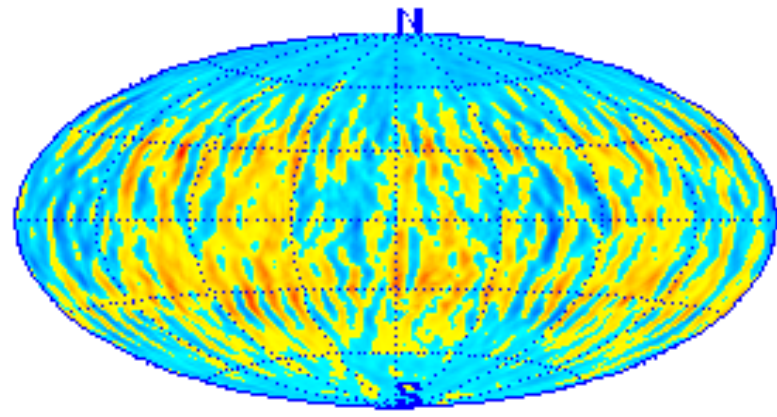
entropy perturbation vs radius



Radial velocity

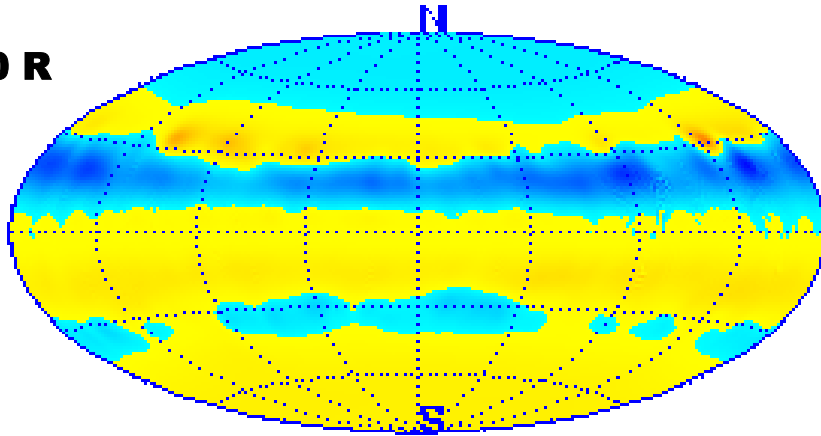


Entropy at surface

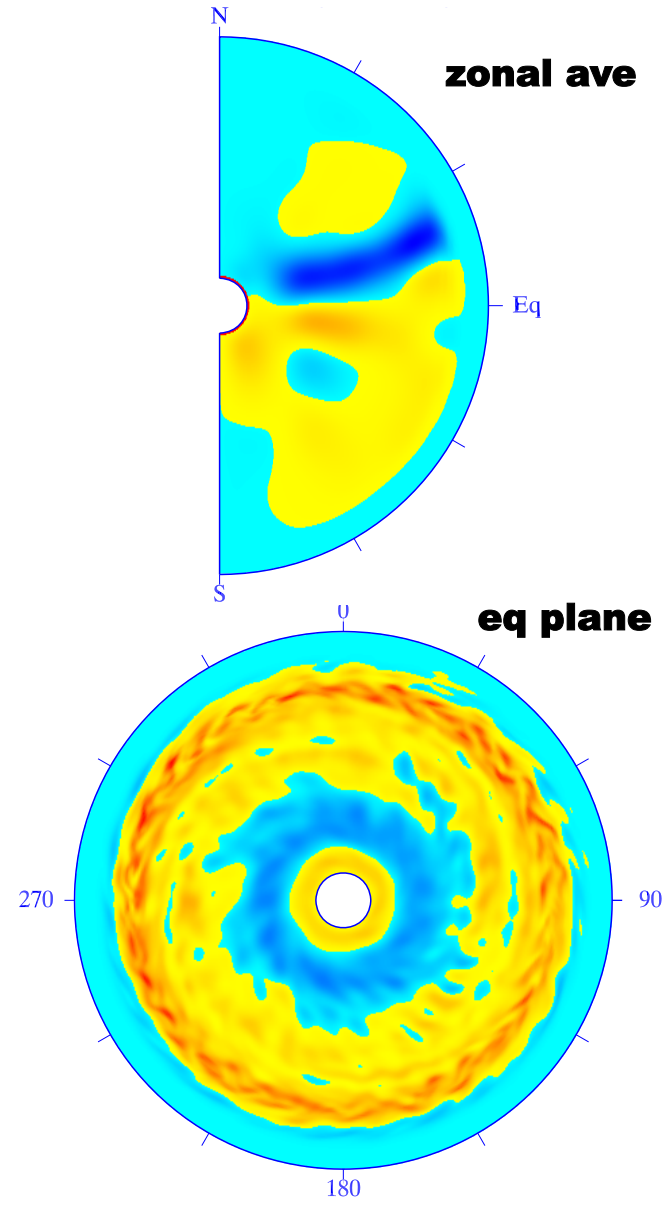
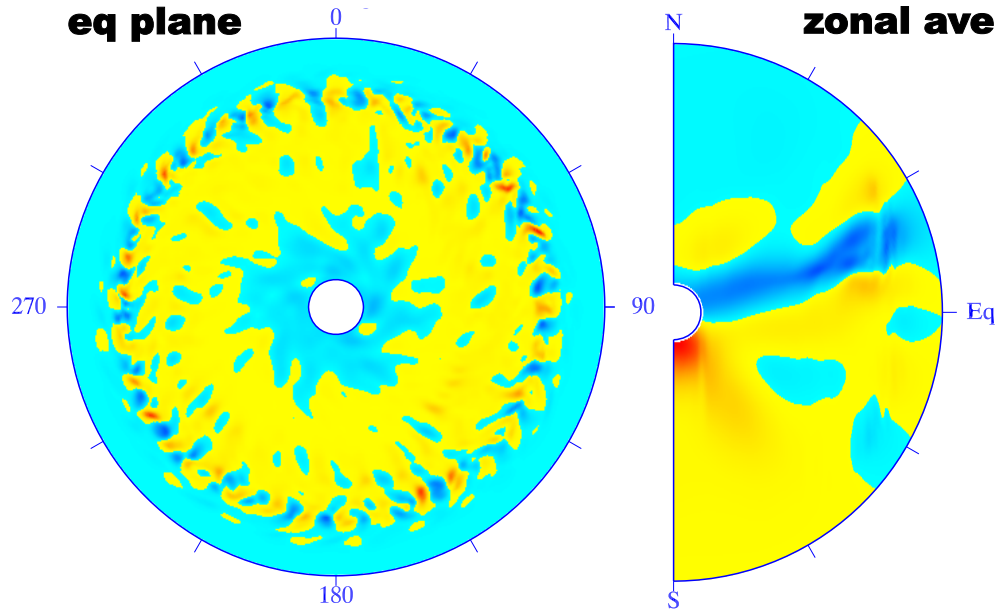


Radial magnetic field

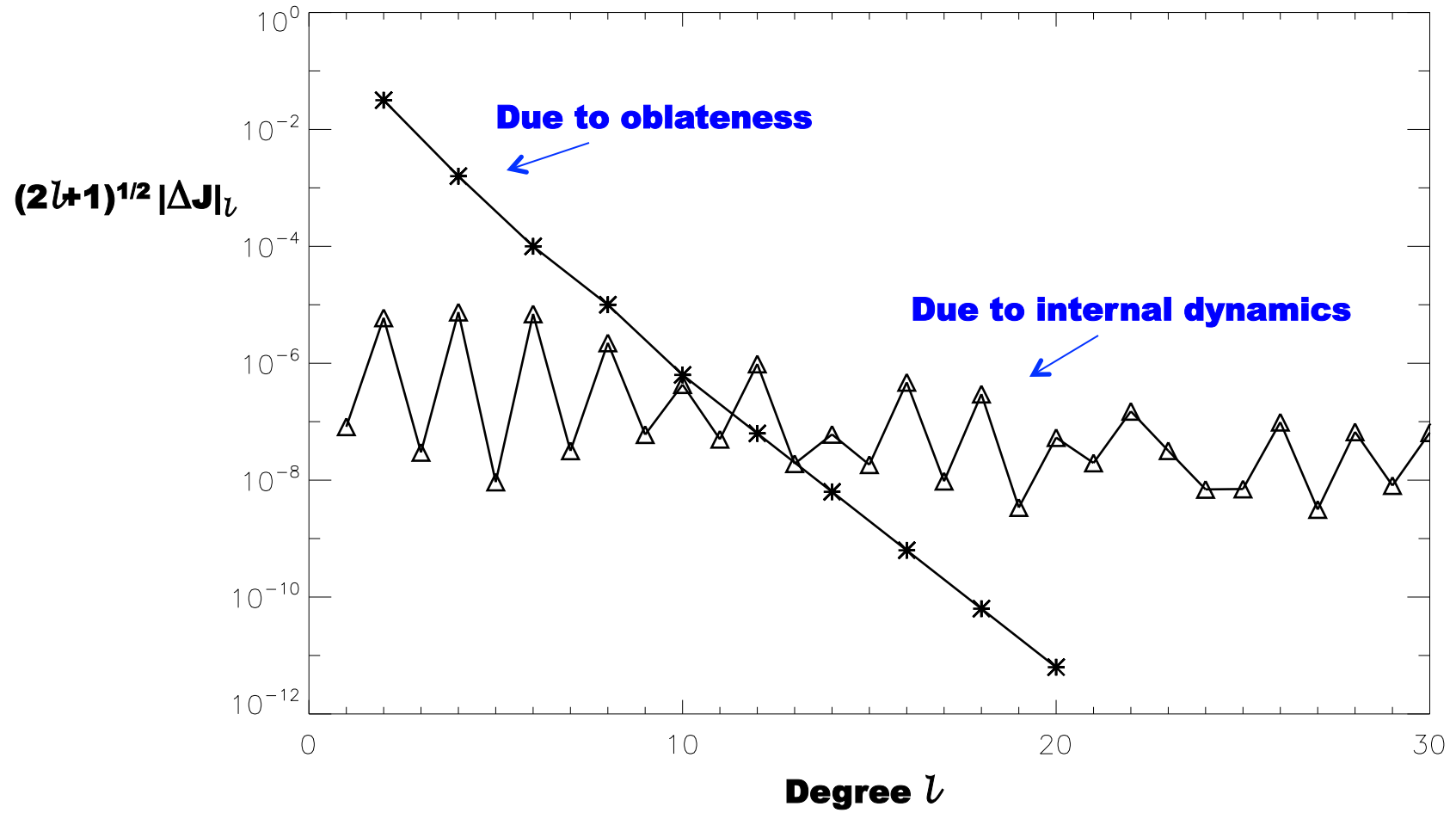
1.0 R



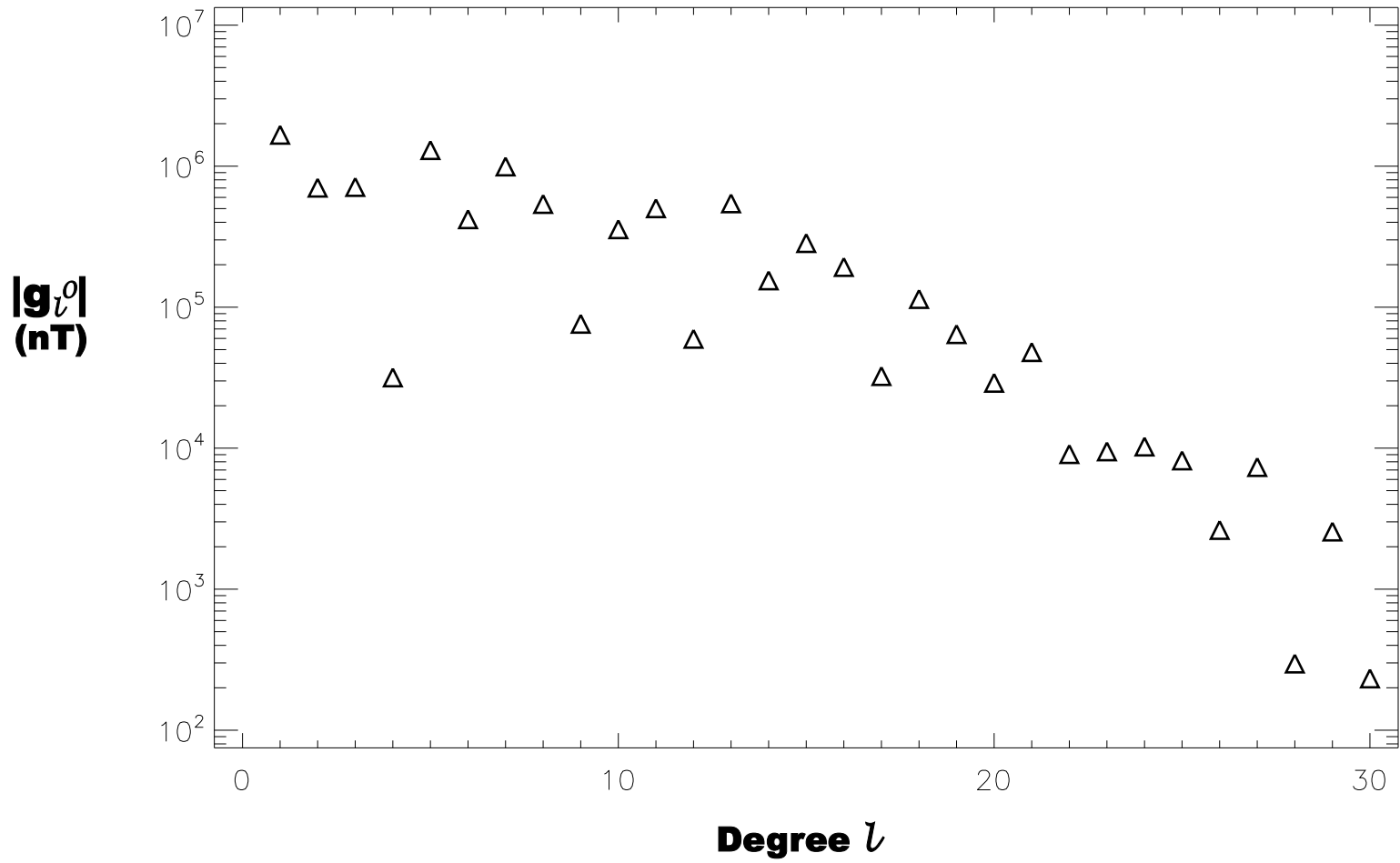
Longitudinal magnetic field



Gravitational field



Magnetic field

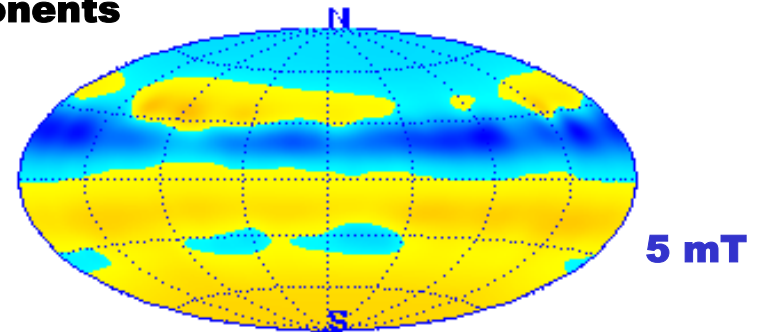
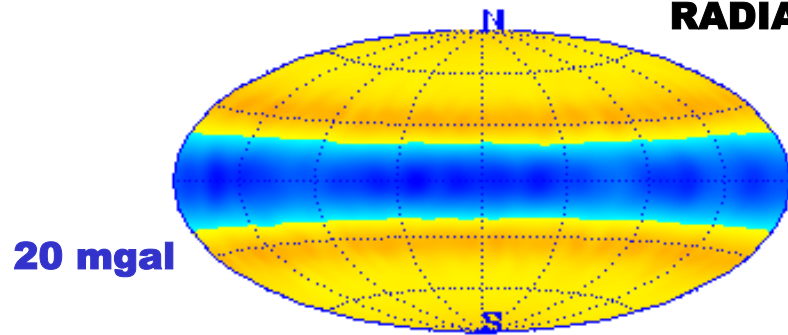


Perijove (1.07 R_J)

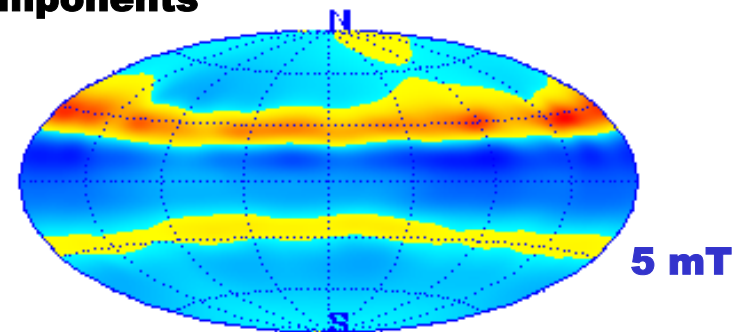
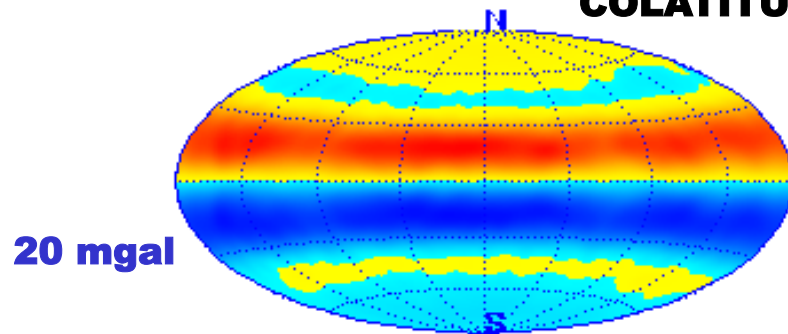
perturbed gravitational field

magnetic field

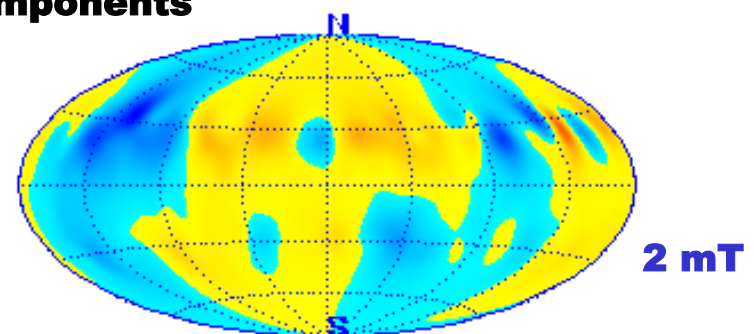
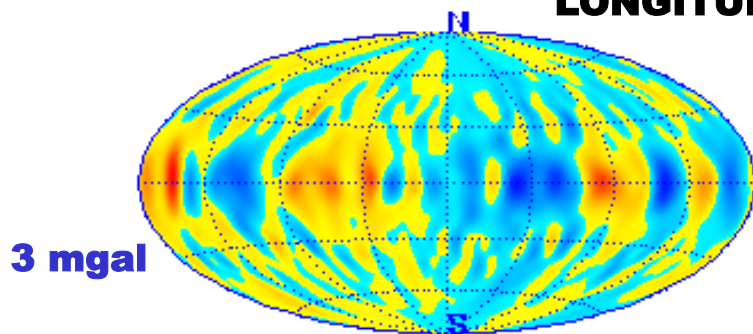
RADIAL components



COLATITUDINAL components



LONGITUDINAL components



To gain the most from the *Juno* mission, we will need to analyze the gravity and magnetic data together and in conjunction with what is predicted by 3D computer simulations that self-consistently solve for thermal convection, differential rotation, and the resulting gravitational and magnetic fields.

Latitudinally-banded structures observed in the gravity and magnetic data would indicate that the zonal winds extend deep below the surface.

Observing no banded structures in the data would suggest that the zonal winds are shallow atmospheric features.