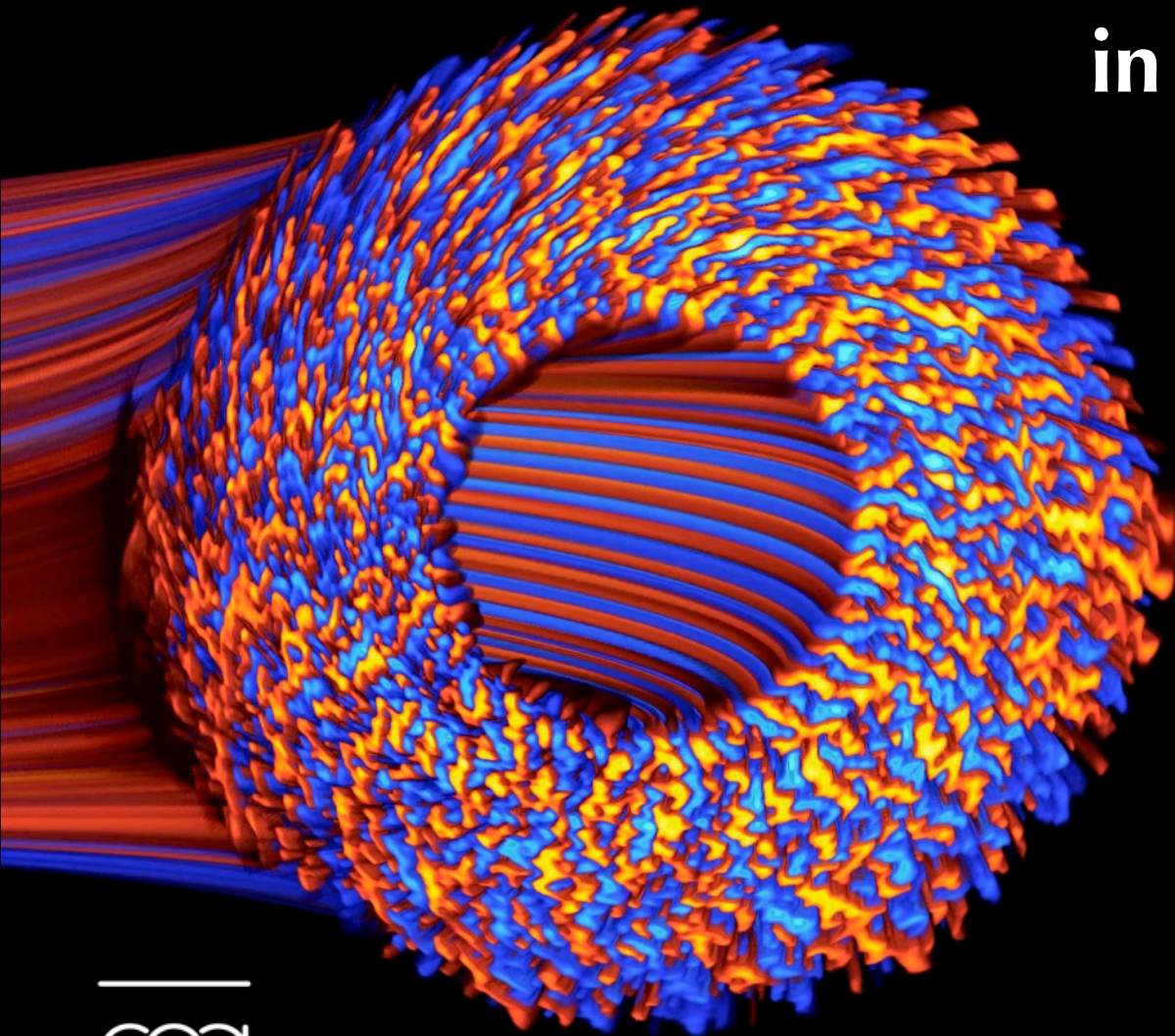


# Gyrokinetic simulations of transport barriers associated with sheared flows in tokamak plasmas



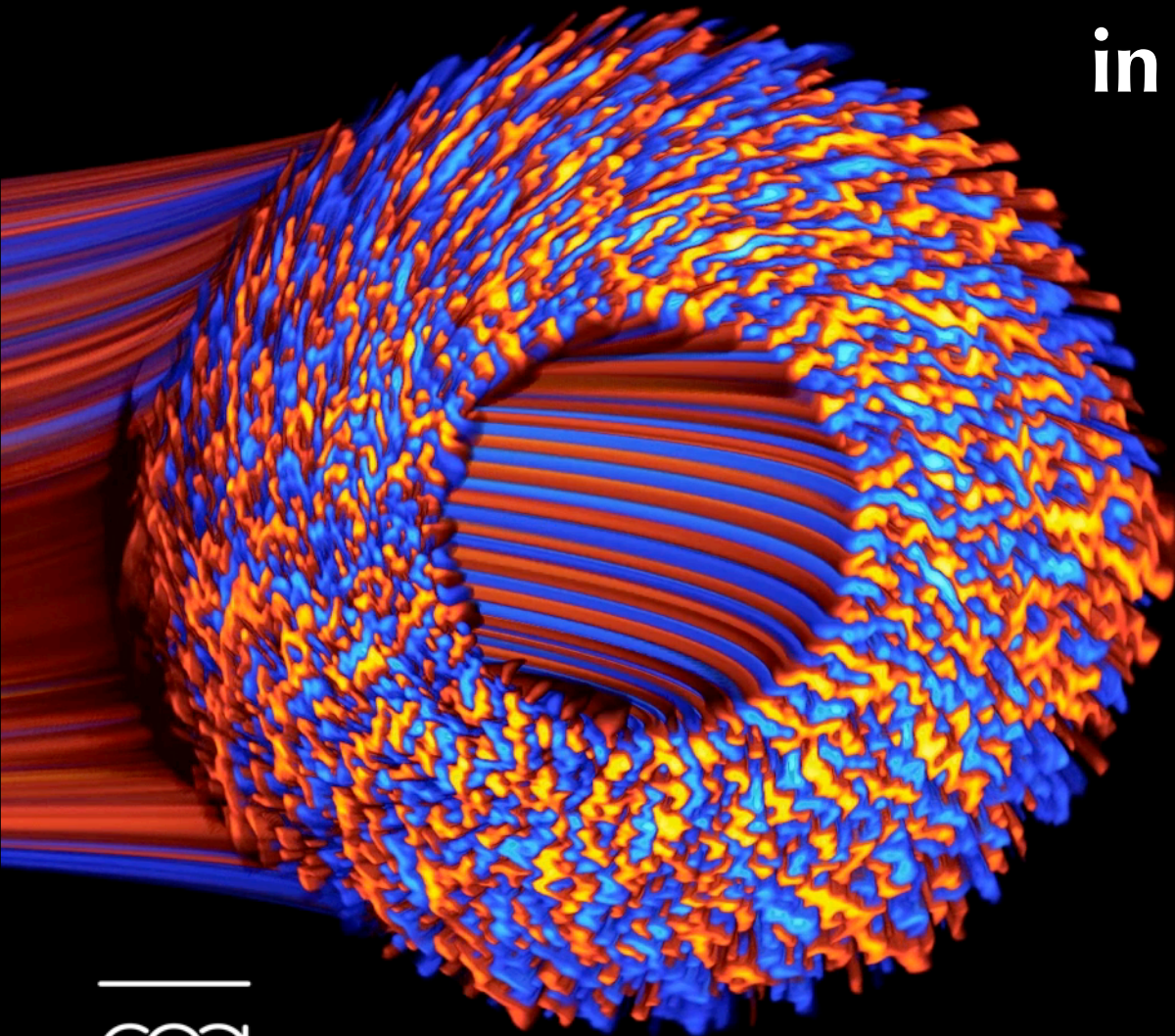
Antoine Strugarek

Wave — Mean-Flows  
Interactions in Fluids  
KITP, UCSB



With Y. Sarazin, A. S. Brun, and the GYSELA team  
Special thanks: Festival of theory

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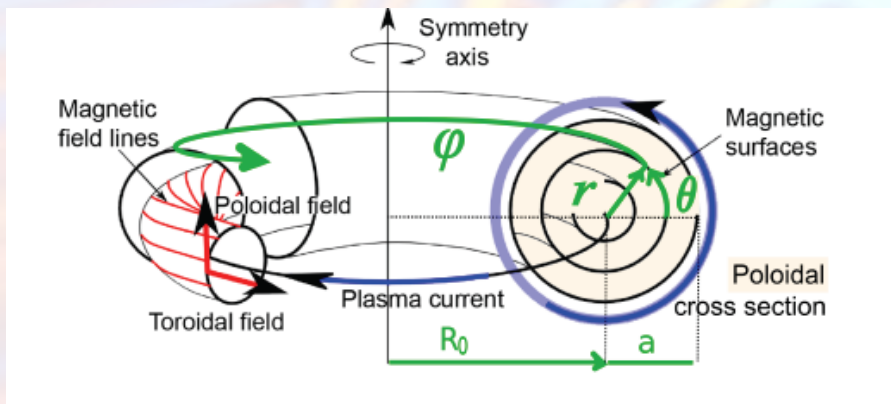


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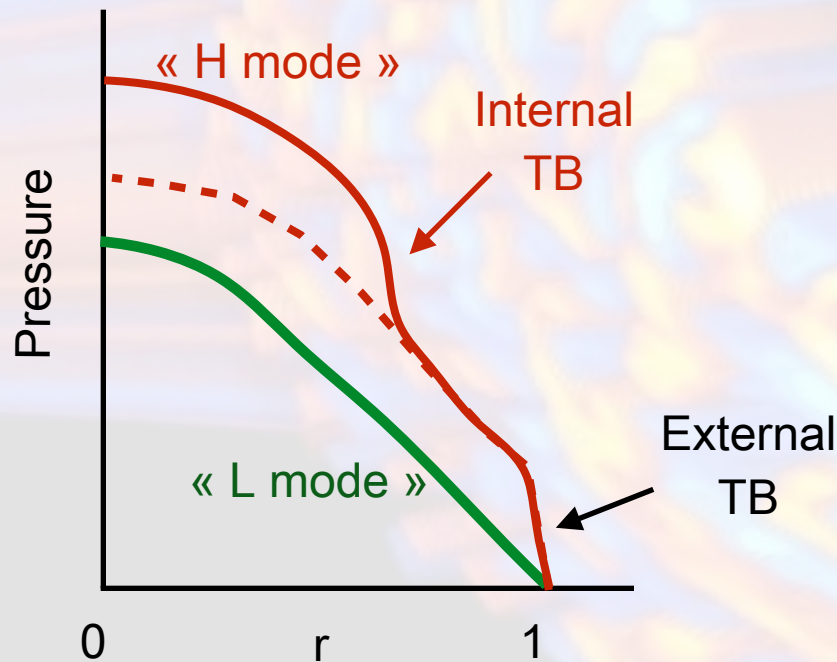
# Outline

- » Why study transport barriers?
- » Gyrokinetic (GK) formalism for turbulent transport and mean flows in tokamak plasma
- » How to impose sheared flows in a self-consistent GK simulation
- » Transport barrier and sheared flows: creation, sustainment and stability

# Transport barriers (TB) in a tokamak plasma



Tokamak geometry with circular cross-section



- » Goal: confine energy in the center
- » Use self-organization capability of the plasma to create TBs (ITER main scenarii)
- » Any external control on the TBs position, stability or strength is extremely beneficial in the path of building a fusion device

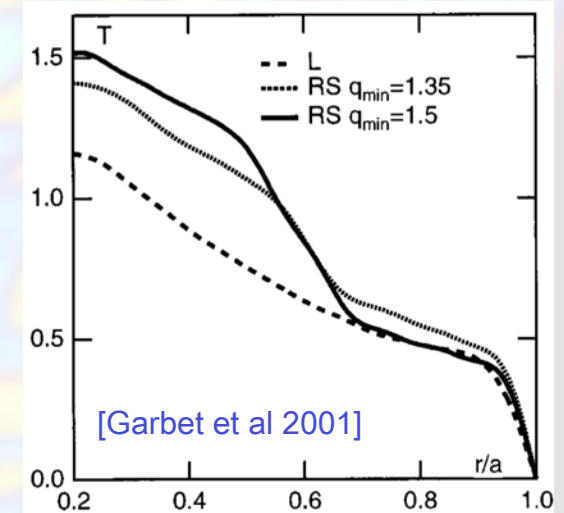
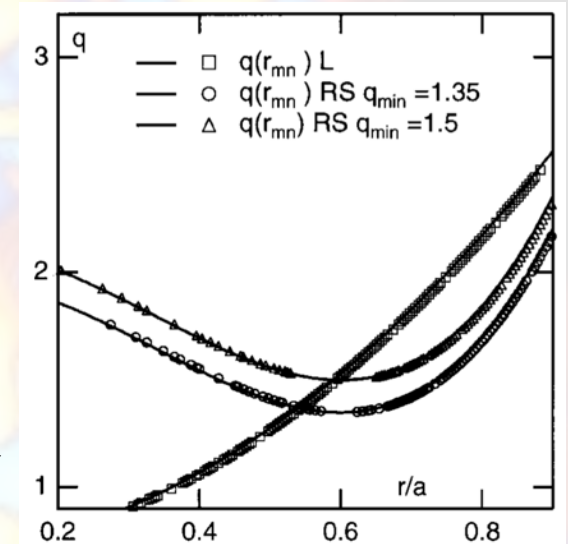
# How to generate transport barriers in a tokamak plasma

## Two possible mechanisms

### → Magnetic **topology** (magnetic shear)

- Magnetic shear → **linear stabilisation**
- « Inversed » profile → **role of non-resonant modes?**

[Joffrin et al 2003, Candy et al 2004, Sarazin, Strugarek et al 2010]



[Garbet et al 2001]

# How to generate transport barriers in a tokamak plasma

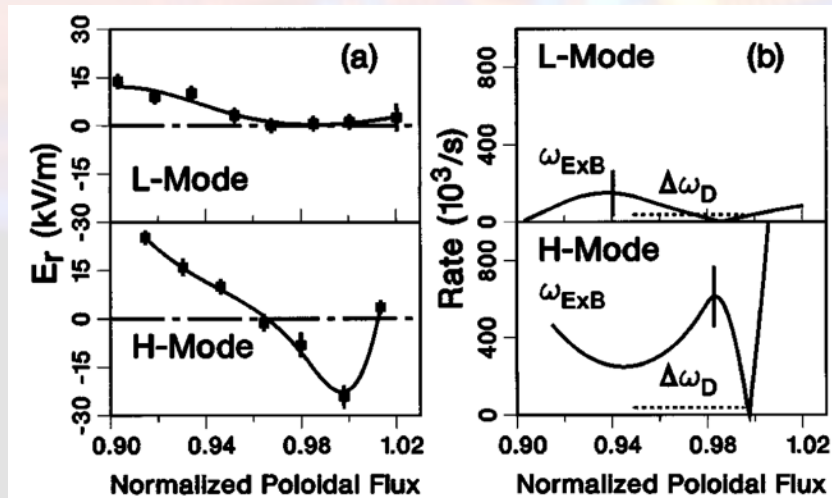
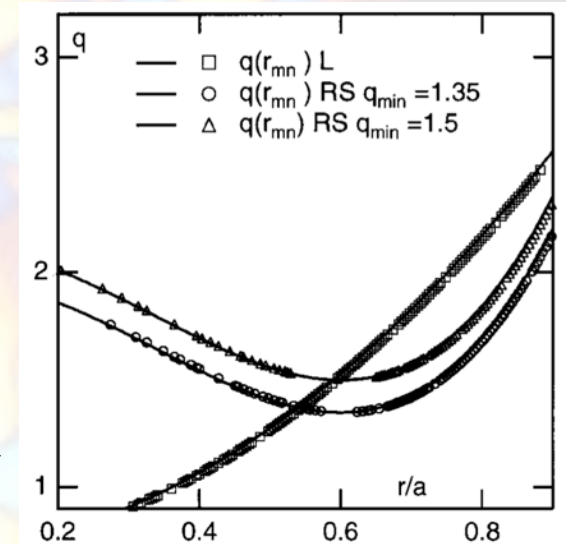
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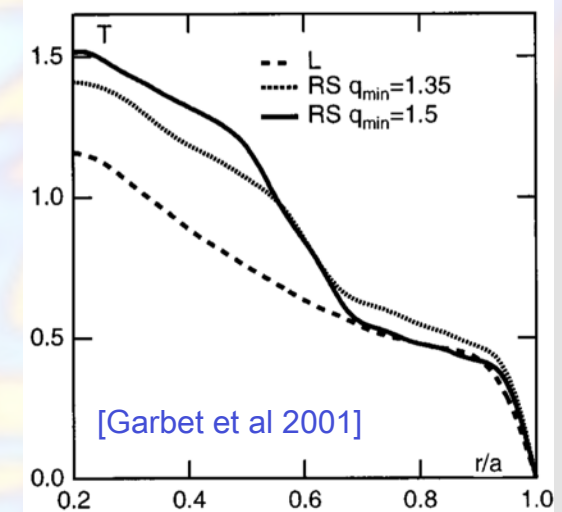
[Joffrin et al 2003, Candy et al 2004, Sarazin, Strugarek et al 2010]

- Velocity **shear**
  - Toroidal → transfer || momentum
  - Poloidal → **polarize the plasma**

[Terry 2000, Wolf 2003, Connor 2004, ...]



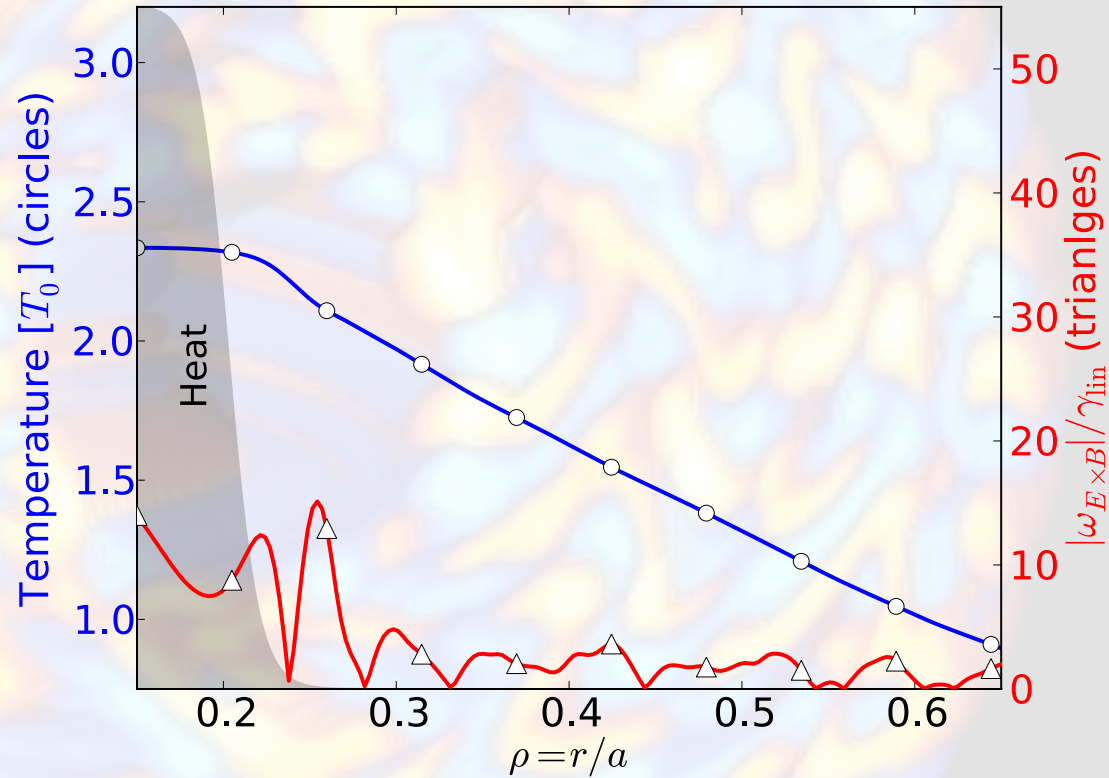
[Burrell 1997]  
(DIII-D)



[Garbet et al 2001]

# Turbulent transport, sheared flows and transport barriers

Heating power  $\rightarrow$  turbulent transport  $\rightarrow$  mean profiles



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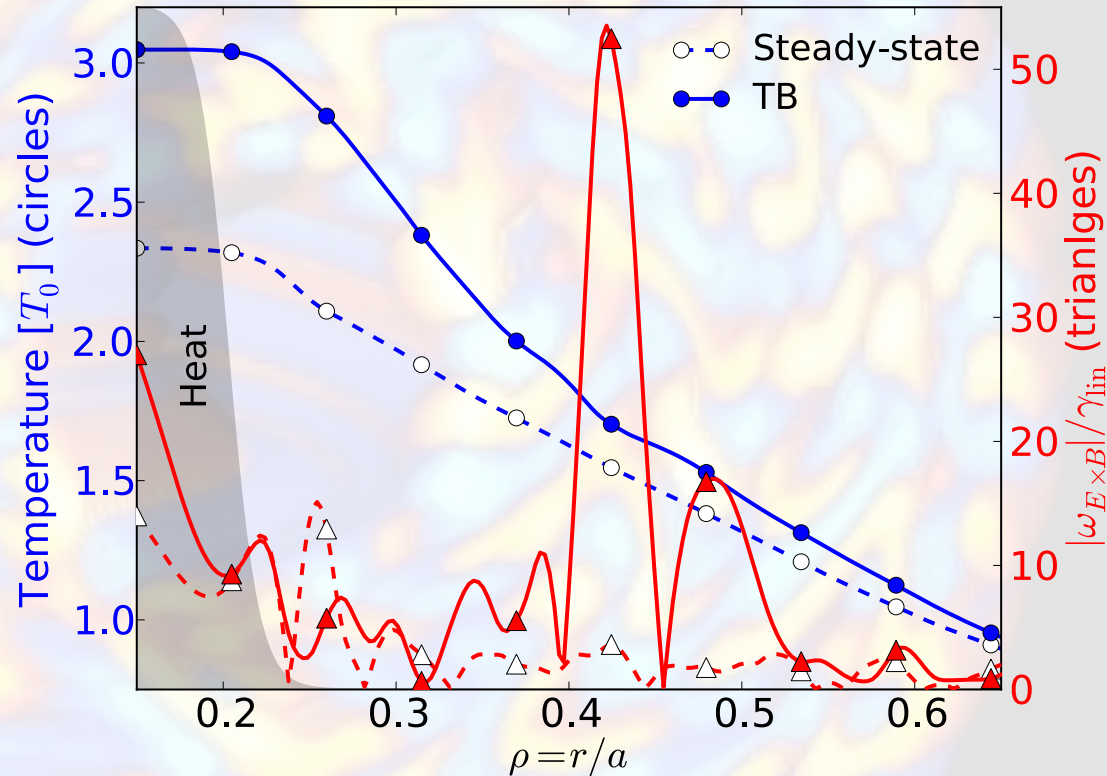
Transport barrier triggered

- with an externally imposed shear

[Ono et al 1988, Craddock et al 1991,  
Leblanc et al 95, 99]

- spontaneously thanks to  
intrinsic sheared flow developing  
the heat input increases

[Biglari et al 1990, Waltz et al 1994]





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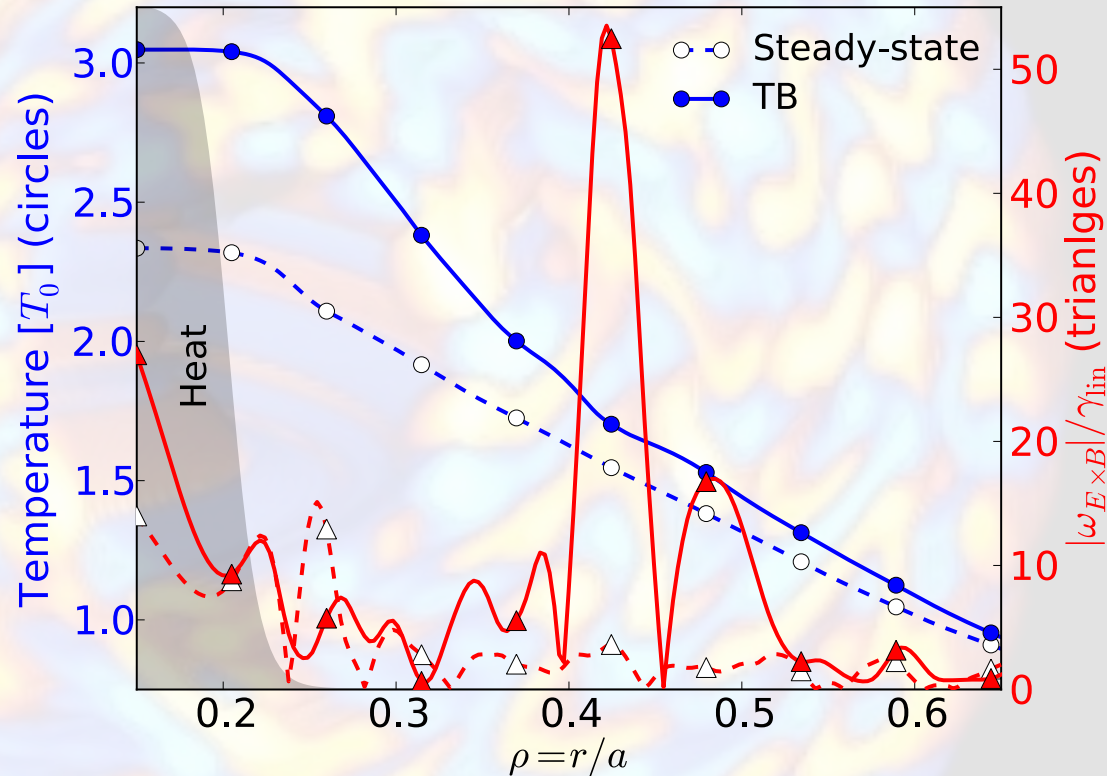
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How those sheared flows interact with  
turbulence to allow TBs creation?

# ITG turbulence with the GYSELA code

"Vlasov"  $\left\{ \begin{array}{l} \partial_t f + \nabla \cdot (\dot{\mathbf{Z}} f) = \mathcal{C}(f, f) \\ \text{Quasi-neutrality} \end{array} \right. \left\{ \begin{array}{l} - \underbrace{\sum_{\text{ions}} \nabla \cdot \left( \frac{n_s m_s}{B^2} \nabla_{\perp} \phi \right)}_{\leftrightarrow \text{Vorticity}} = \sum_{\text{species}} q_s \int dv \mathcal{J} \cdot \bar{f} \\ \text{+ adiabatic electrons} \end{array} \right.$

» **Global** code ( $\neq$  'flux-tube')

→ **large scale** transport events

→ boundary conditions

» **Full-f** and **flux-driven** code ( $\neq$  'δf', gradient-driven)

→ **Equilibrium & fluctuations**: no scale separation

→ **Profile relaxation**: statistical steady-state

→ Prescribed driving **flux**

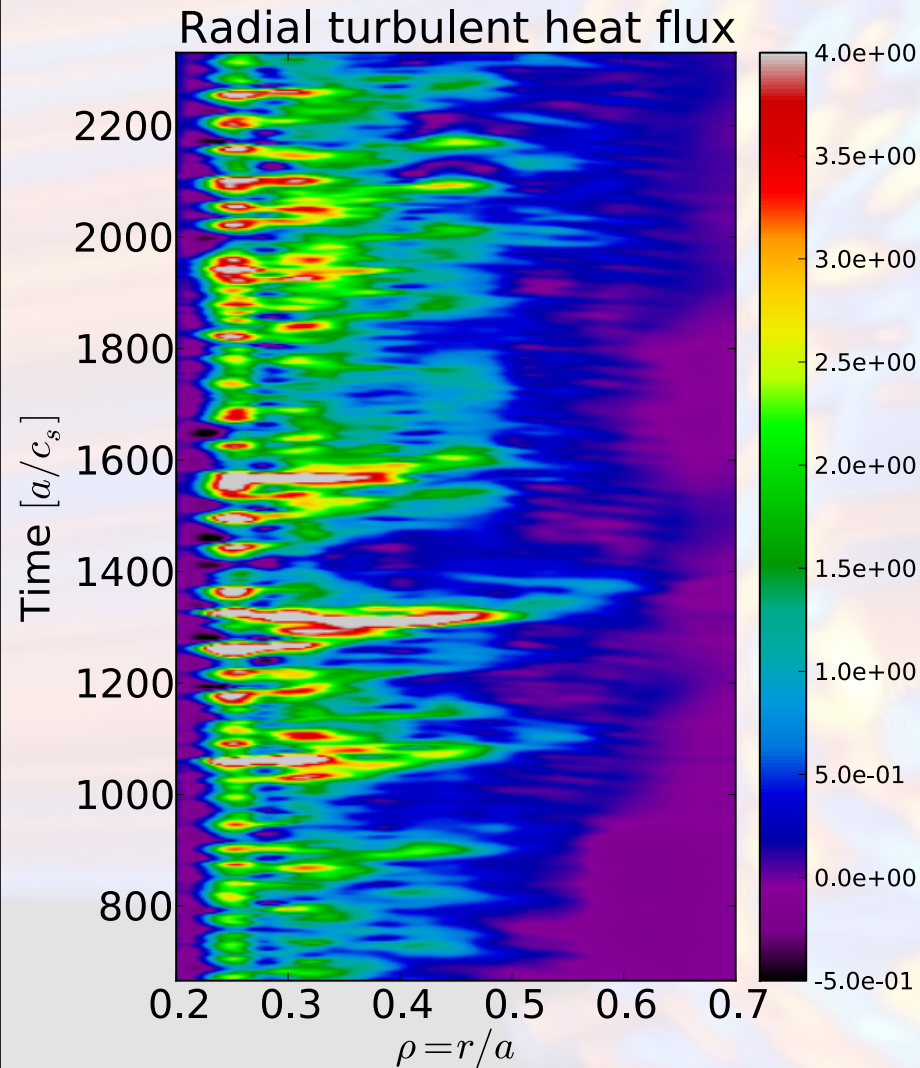
## Parameters

$$\rho_{\star} = 1/150$$

$$\nu_{\star} = 0.1$$

[Grandgirard et al 2007,2008]

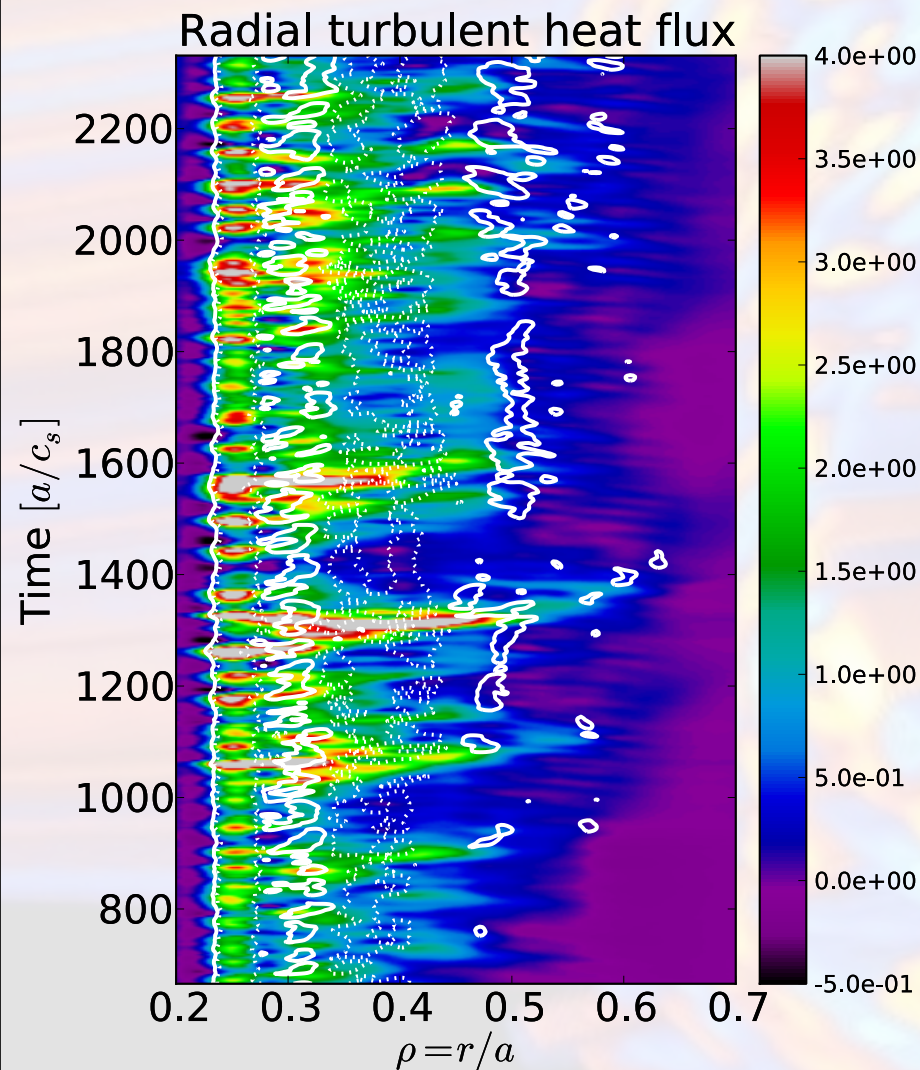
# Intrinsic shear in ITG turbulence: no transport barrier



» Intrinsic sheared flows observed in two regimes

– Highly correlated to the turbulent heat flux structure

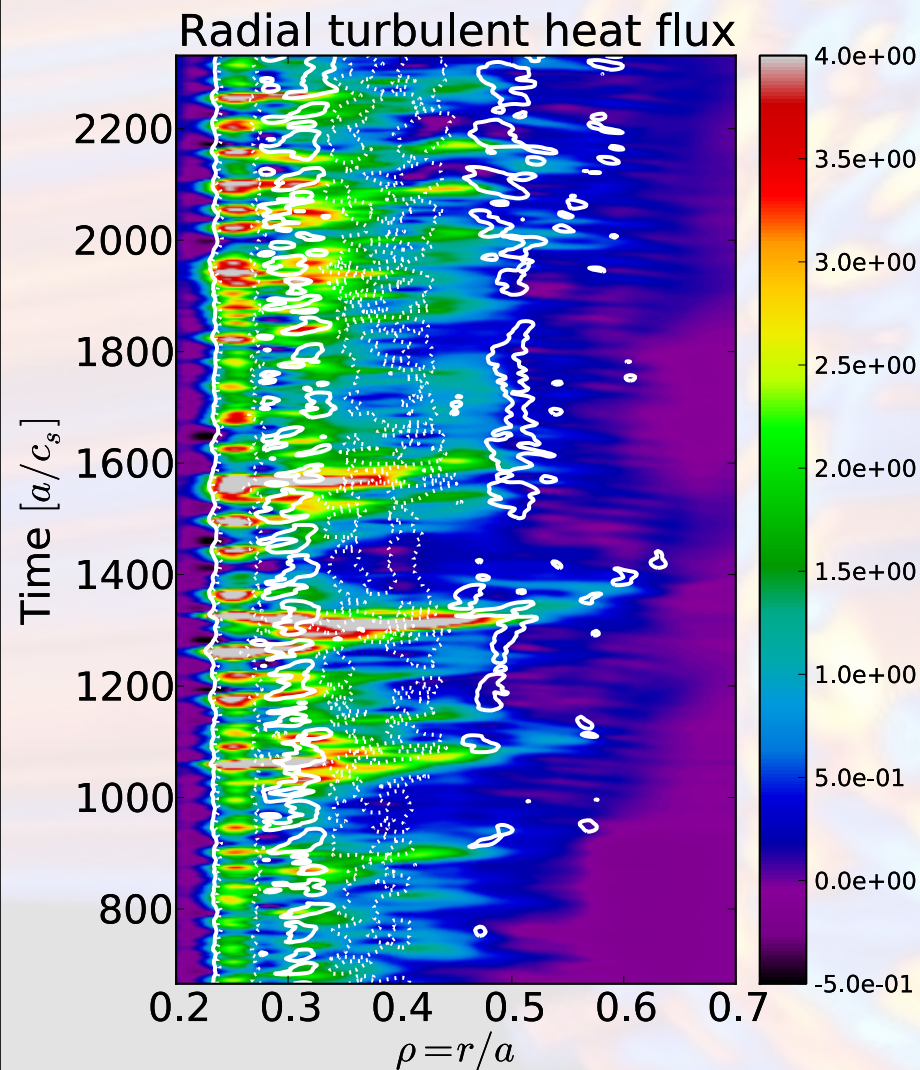
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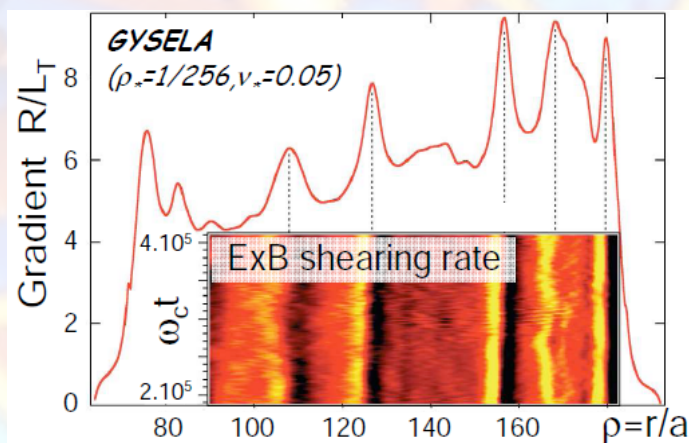
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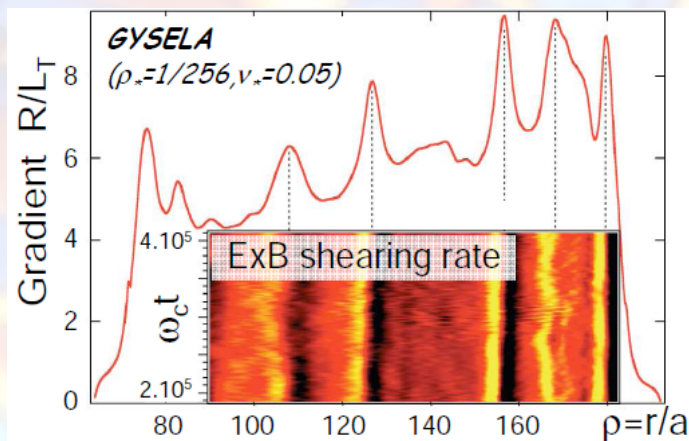
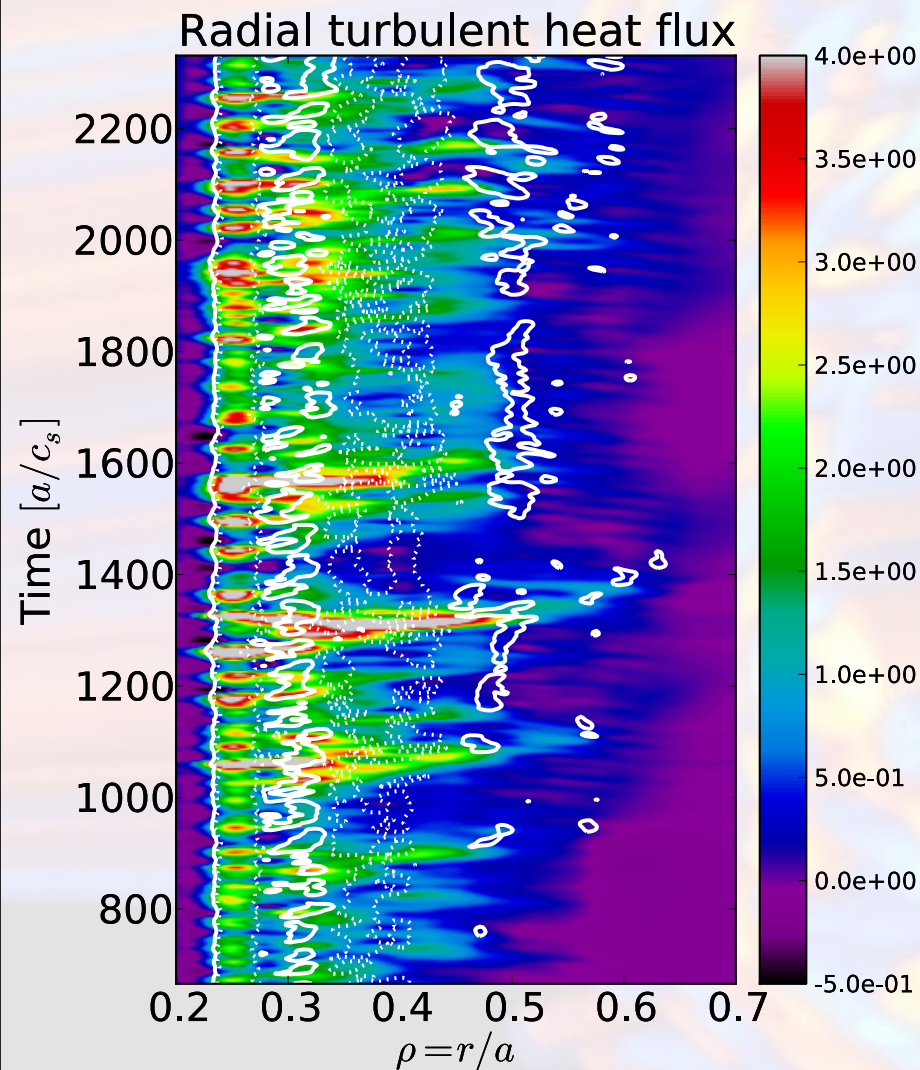
Close to threshold

[Dif-Pradalier et al, PRE 2010]

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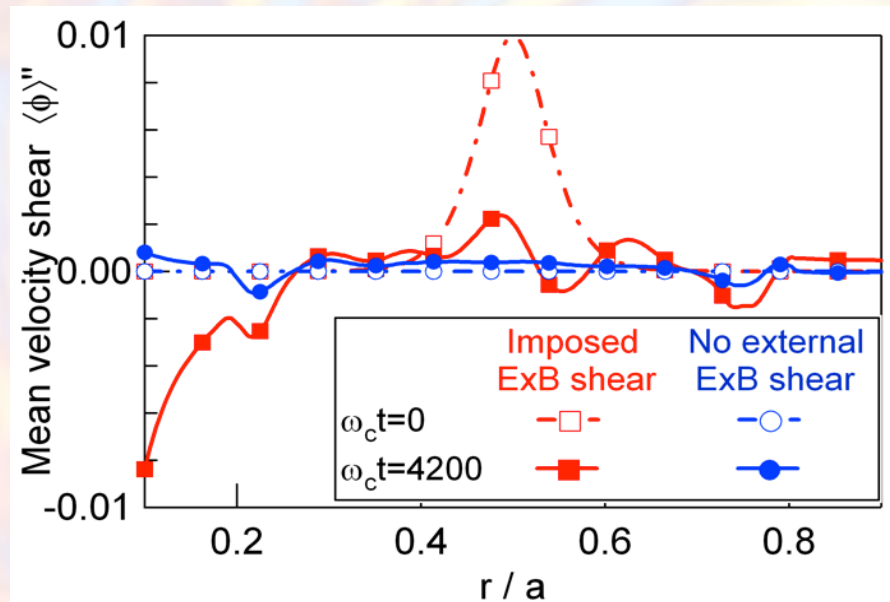
No strong transport barrier is driven



Externally impose a shear

# How to polarize the plasma in the GK formalism?

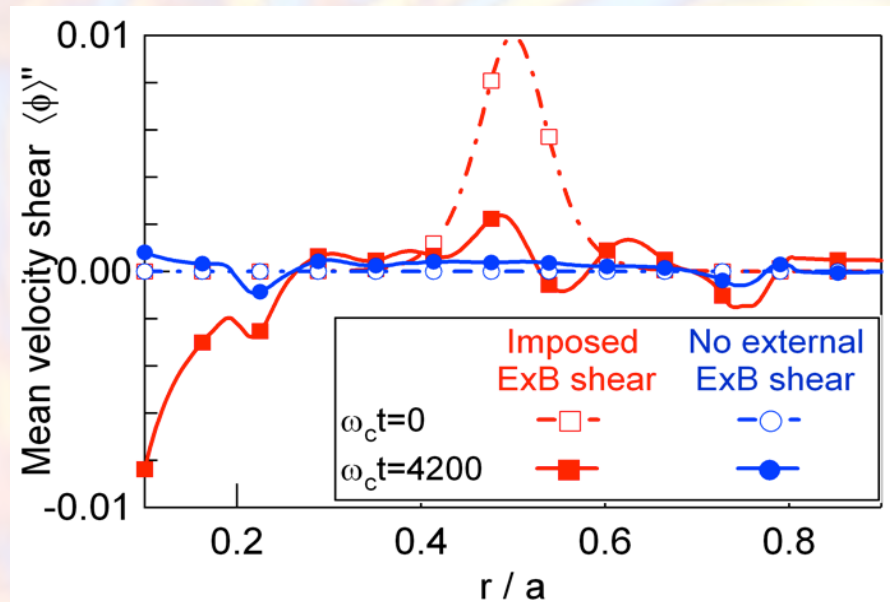
Adding a prescribed poloidal  $v_{E0}$  component to GK equation



[Sarazin et al 2008]

# How to polarize the plasma in the GK formalism?

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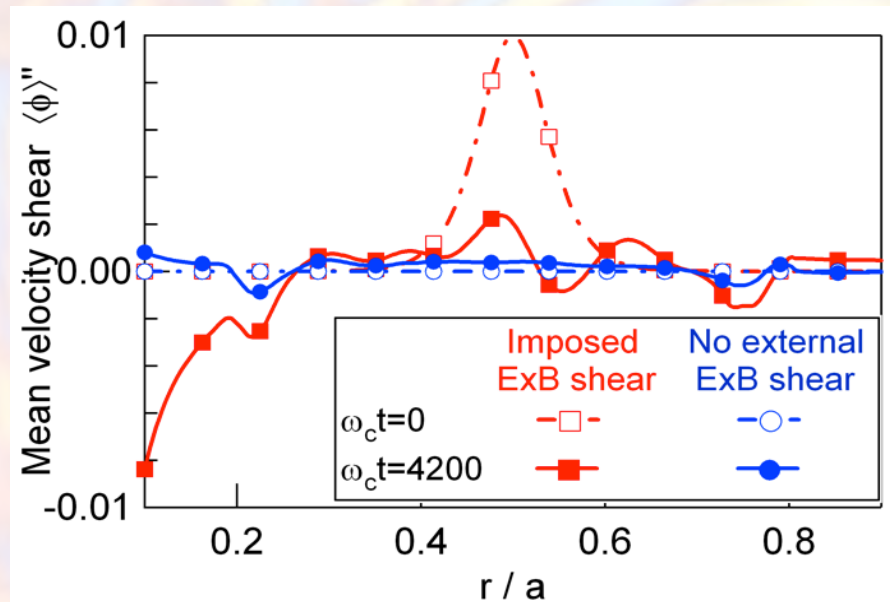


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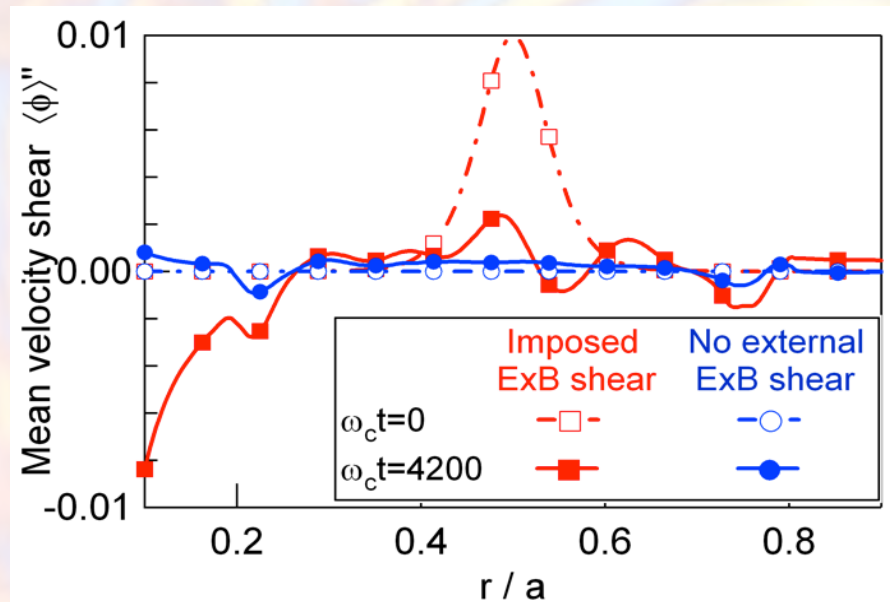
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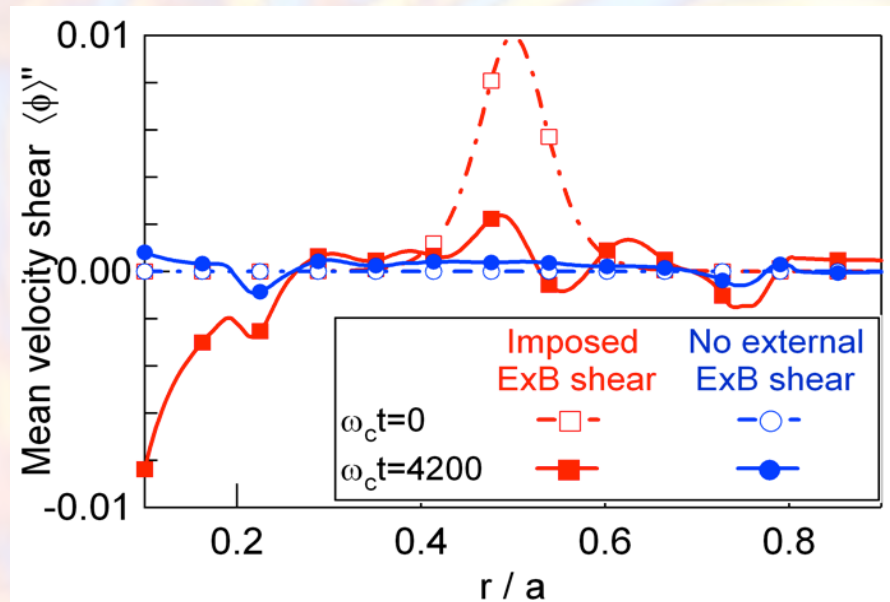
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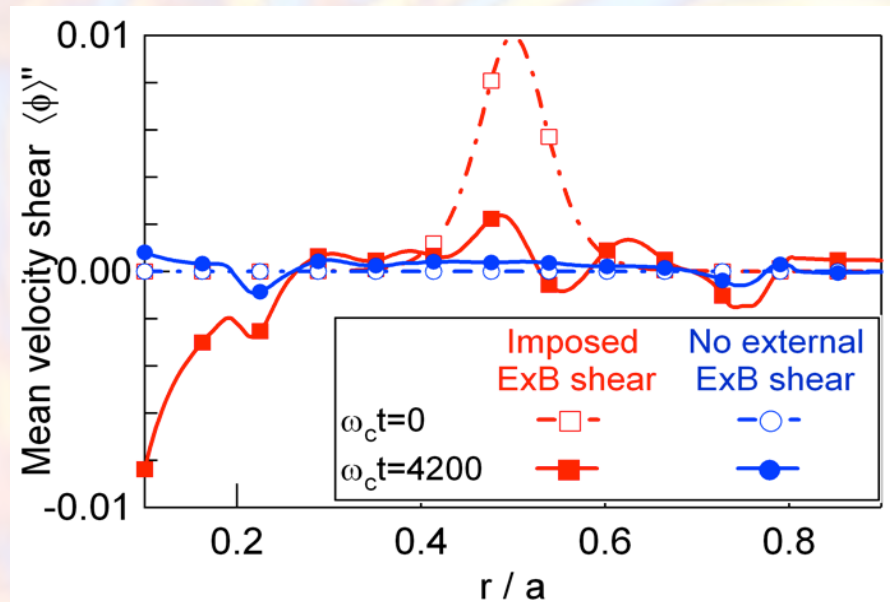
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Add a source term (in the GK eq.) mimicking experimental setup

$$\partial_t f + \nabla \cdot (\dot{\mathbf{Z}} f) = \mathcal{C}(f, f) + S_W$$

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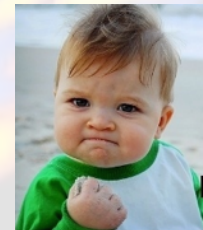
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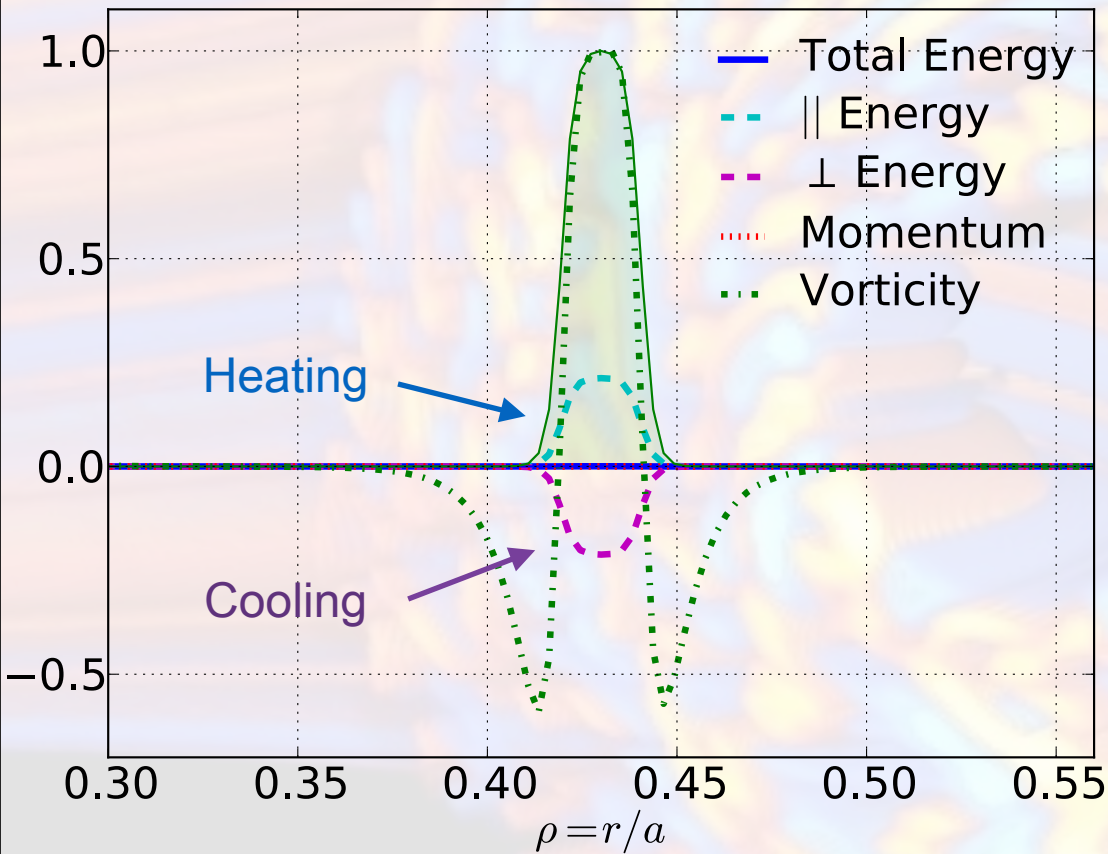
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$$\partial_t f + \nabla \cdot (\dot{\mathbf{Z}} f) = \mathcal{C}(f, f) + S_W$$



# Design of vorticity source(s) in the GK formalism

Normalized effective sources



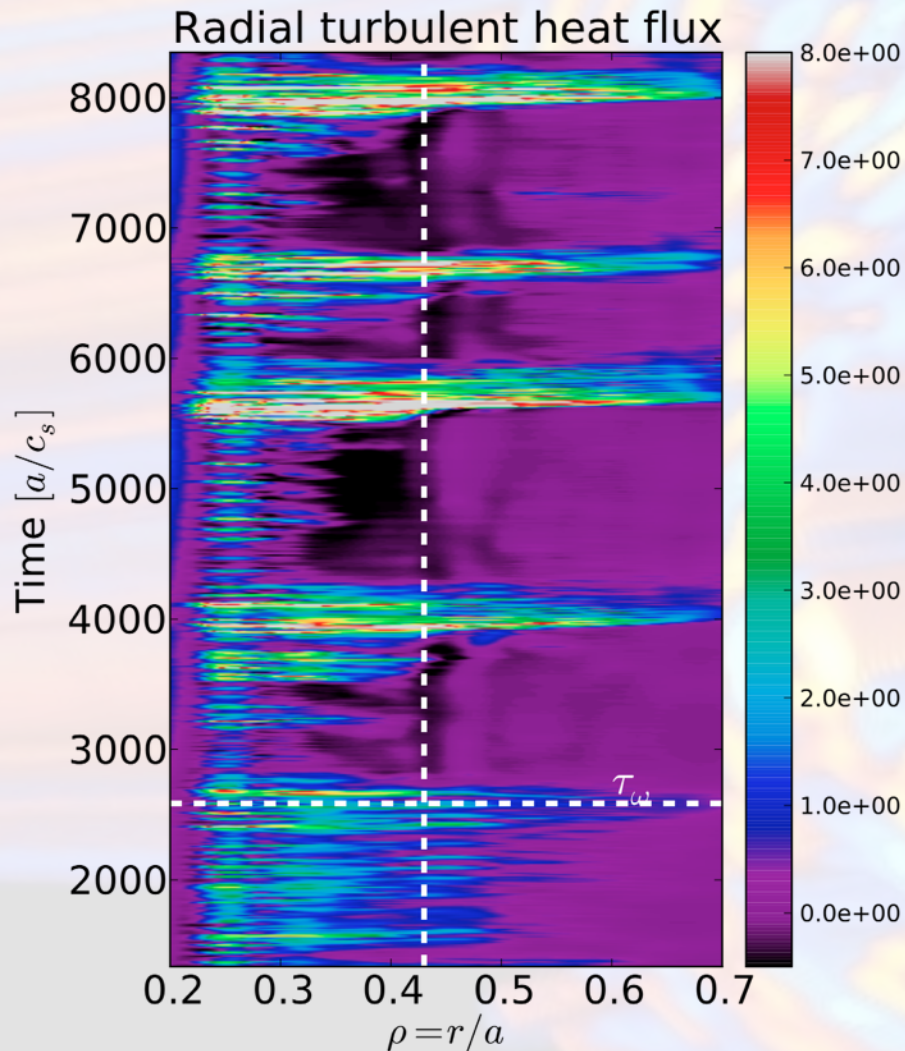
$$\partial_t f + \nabla \cdot (\mathbf{Z}f) = \mathcal{C}(f, f) + S_W$$

- »  $S_W$  acts mainly on **velocity space** over a certain radial domain
- »  $S_W$  generally acts on the density, momentum and energy locally
- » **Pure vorticity source:**

$$S_W \propto (v_{\parallel}^2 - \mu) e^{(-v_{\parallel}^2/2 - \mu)}$$

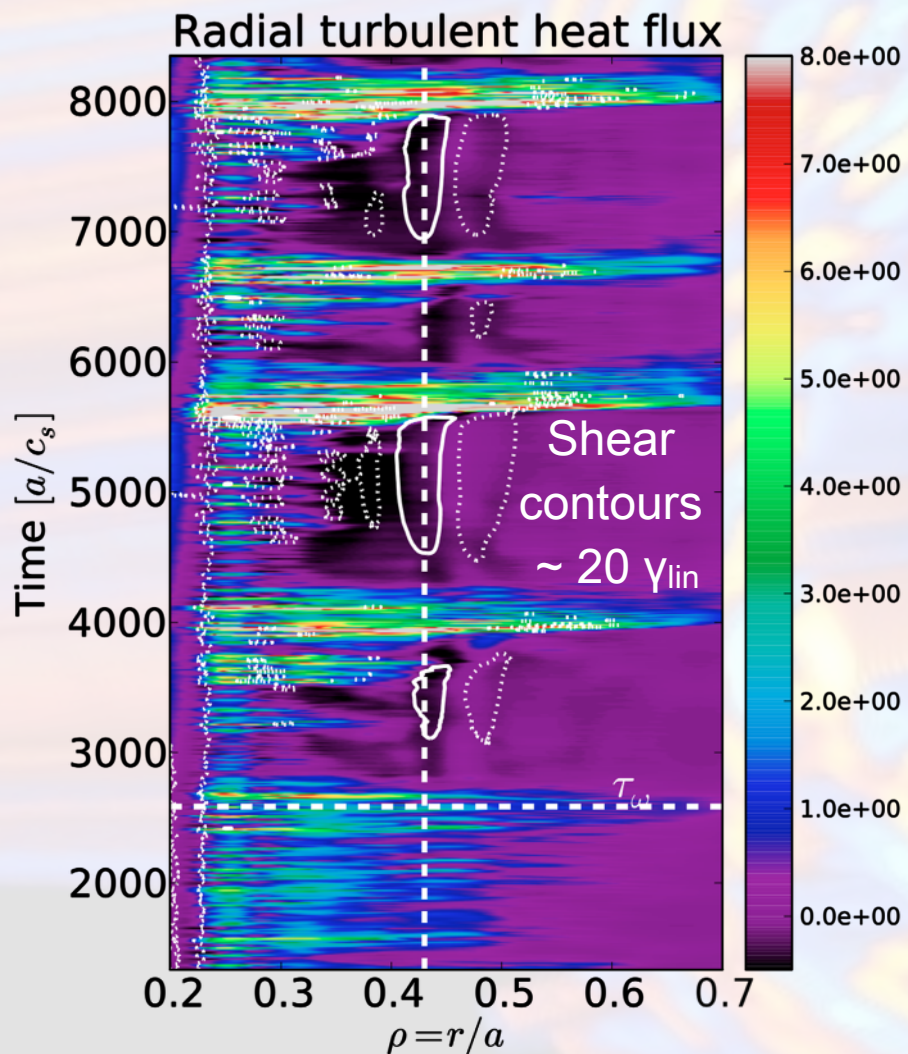
[Strugarek et al, 2013, PPCF+PRL]

# Quasi-periodic trigger/relaxation of transport barriers



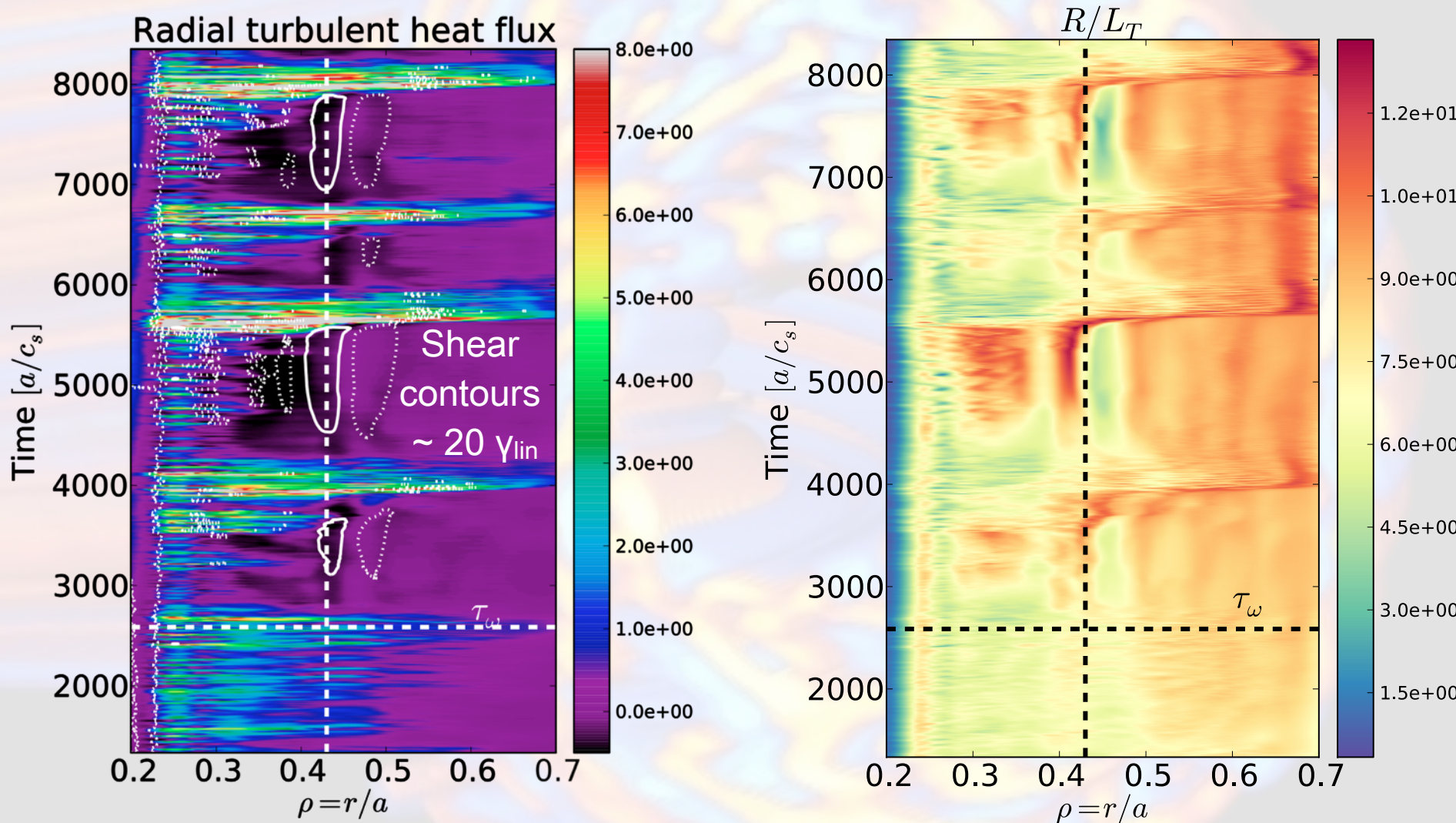
- » The turbulent transport is **suppressed** (flux/10) and the temperature profile **steepens**
- » Large heat bursts occur  
→ **barrier relaxation**
- » The barrier slowly **rebuilds and relaxes quasi-periodically**
- » The ExB shear is also destroyed quasi-periodically

# Quasi-periodic trigger/relaxation of transport barriers



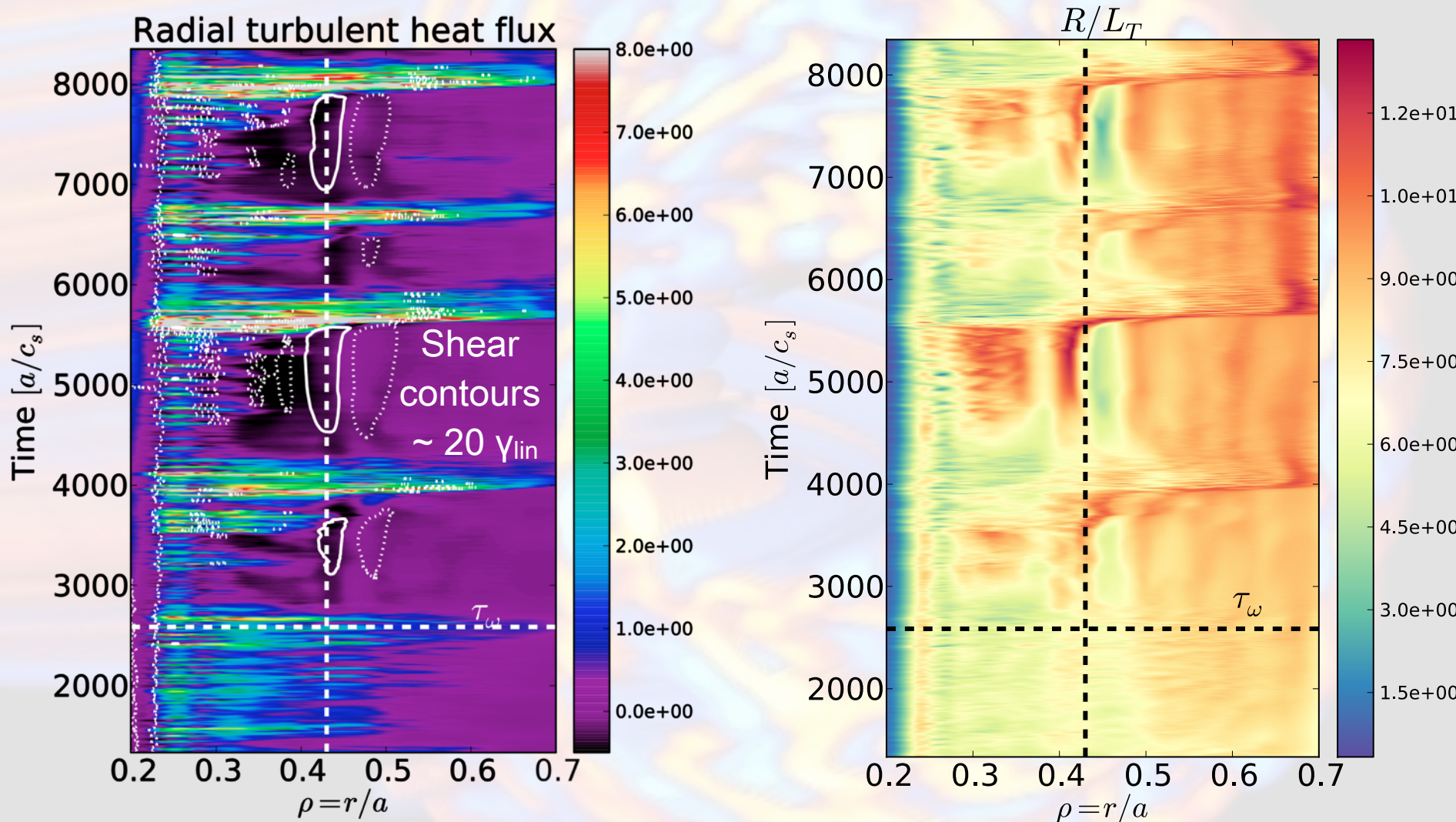
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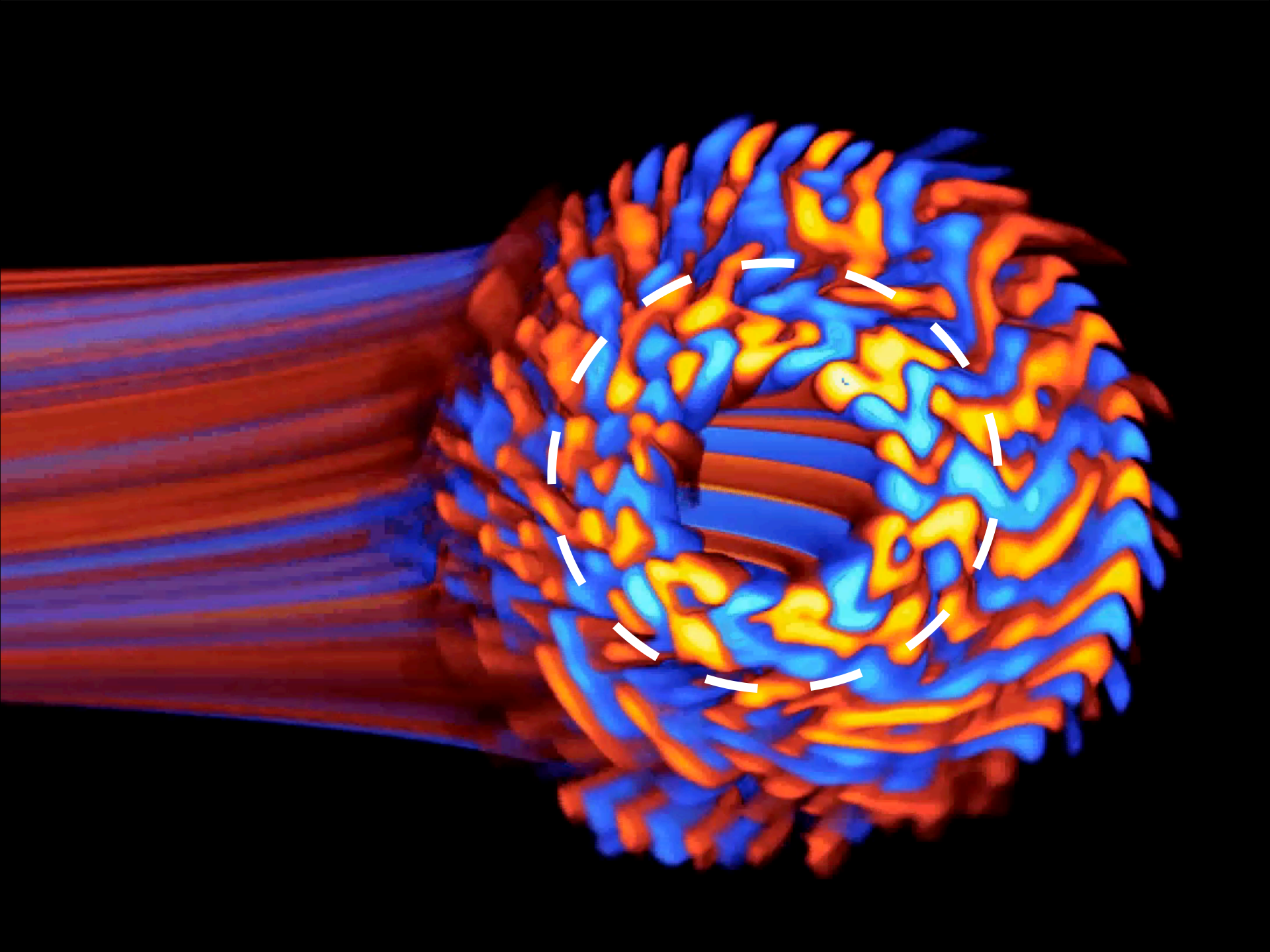


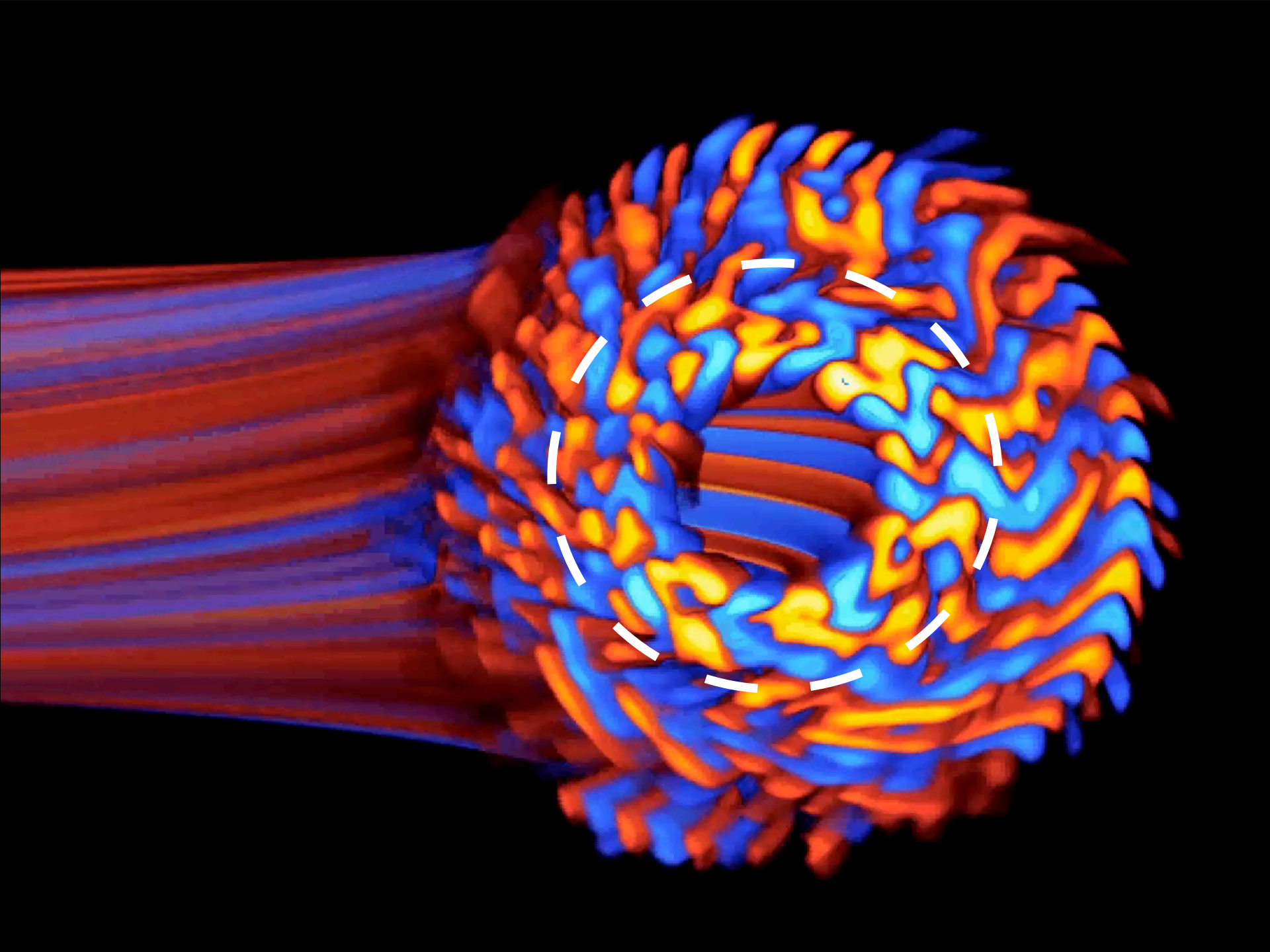


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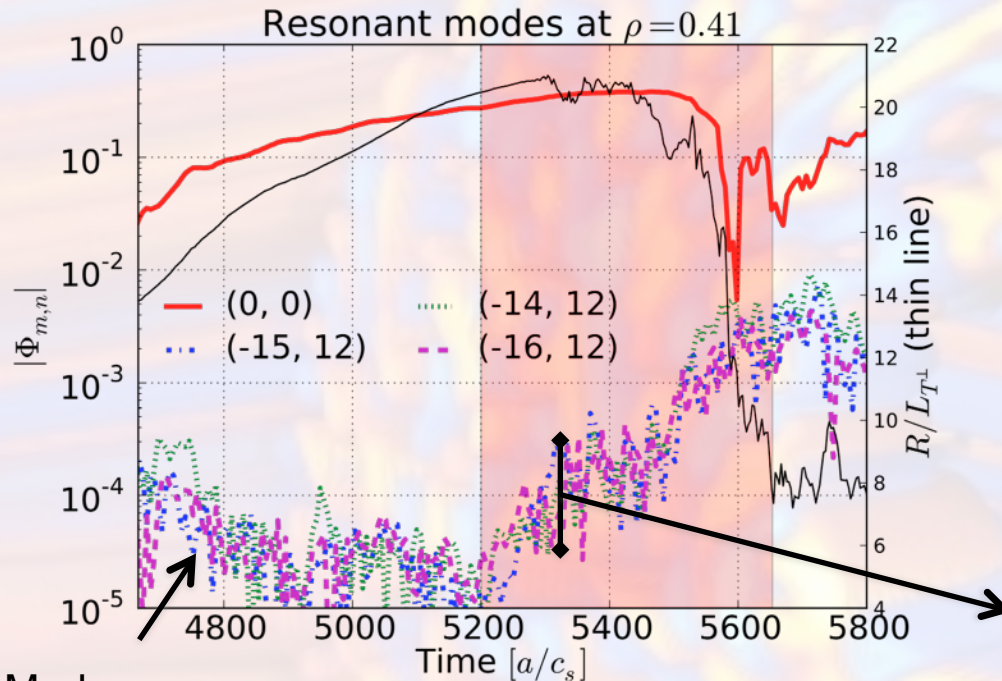


Why both the barrier and the shear are destroyed?

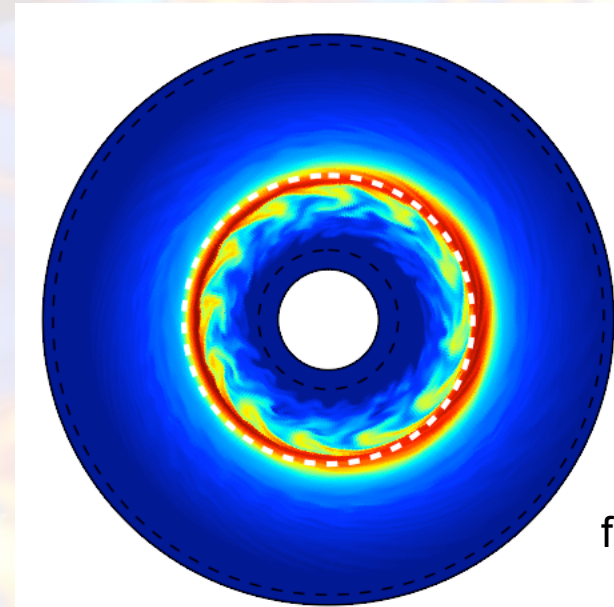




# ITG modes grow inside the barrier and suppress it



» ITG resonant modes **grow exponentially** on the inner side of the barrier (linearly unstable??)

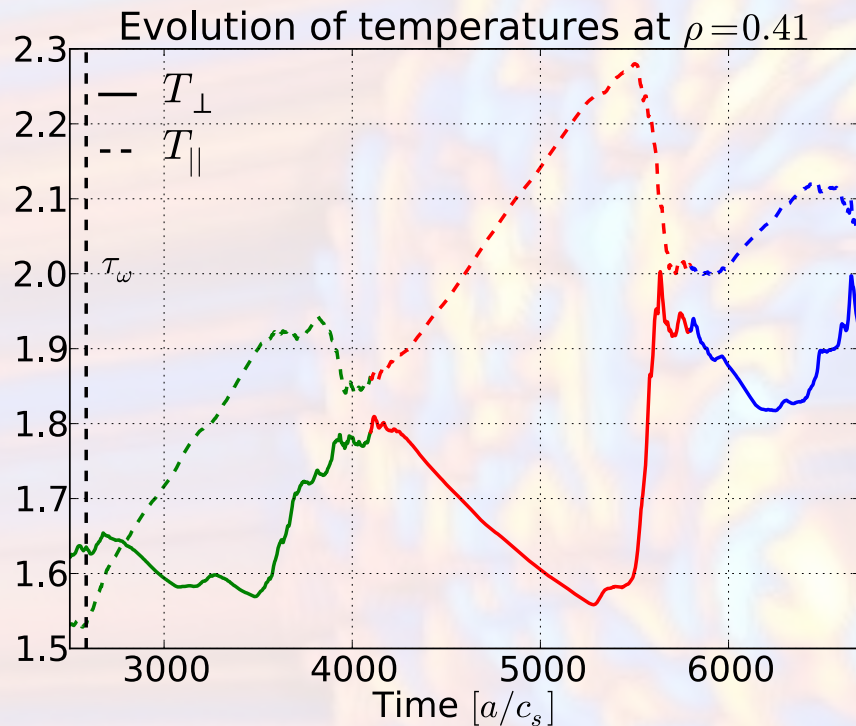


Modes near resonance

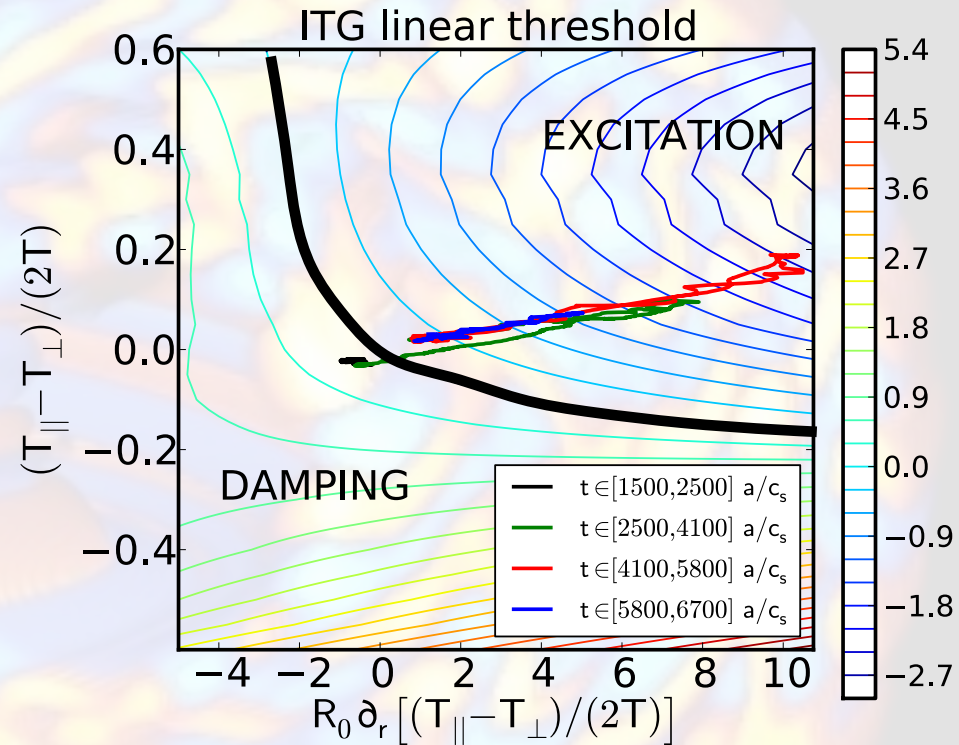
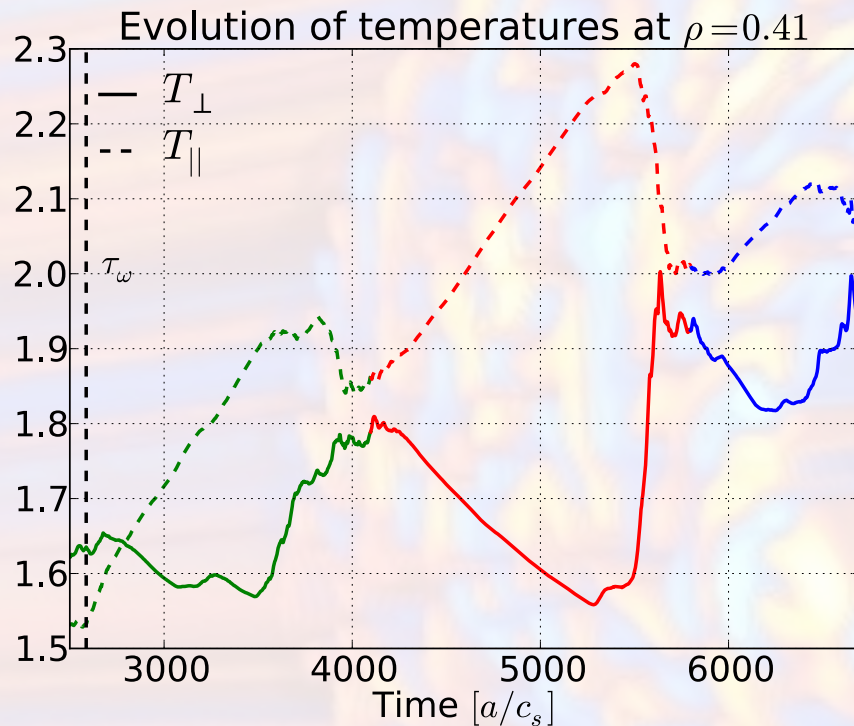
» The barrier (and shear) are destroyed at very different values of  $\omega_E$   
 → *a priori* not a shear instability

Heat transport → T gradient eroded → **Barrier suppressed**

# The anisotropic temperature lowers the threshold



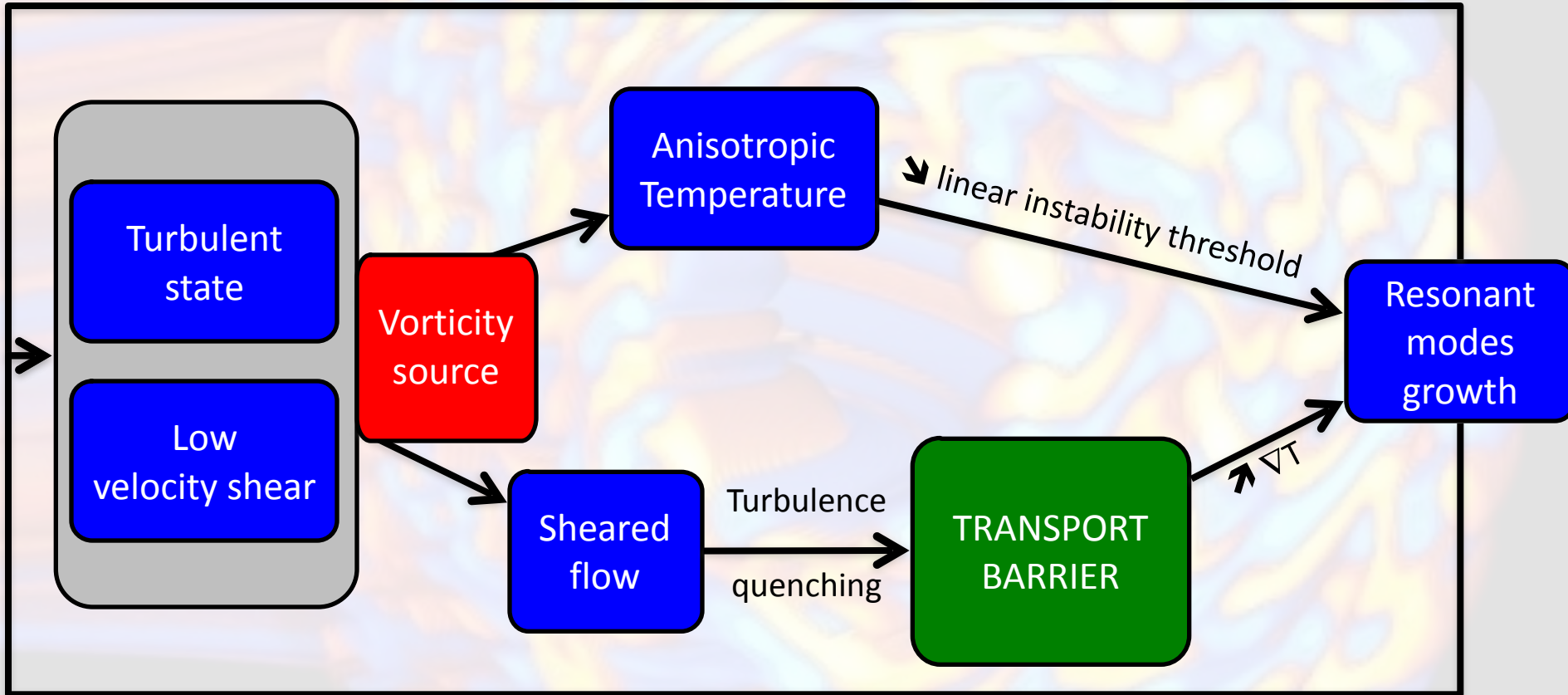
# The anisotropic temperature lowers the threshold



The ITG excitation threshold significantly lowers with the T anisotropy

# A new process for transport barrier relaxation

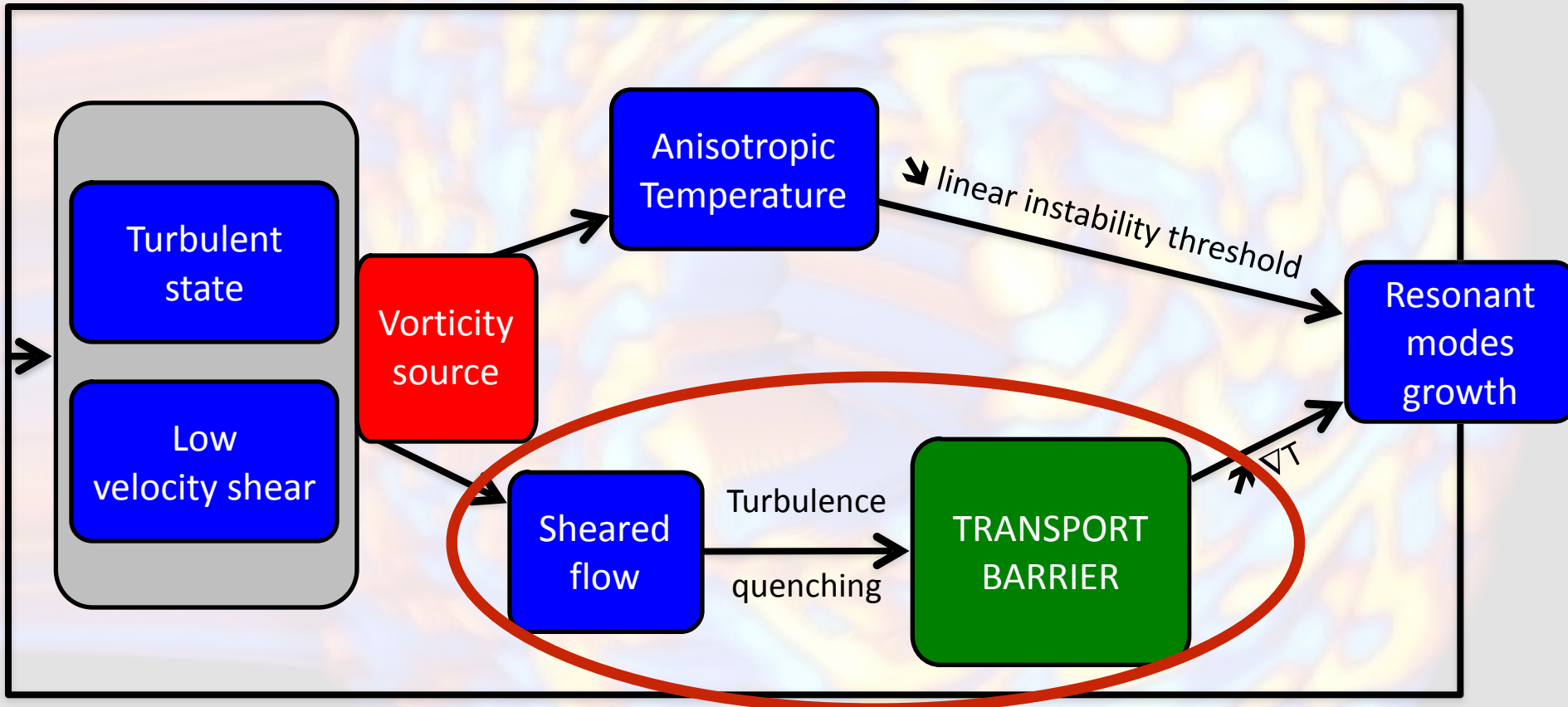
Turbulent heat transport



Turbulent vorticity transport

# A new process for transport barrier relaxation

Turbulent heat transport

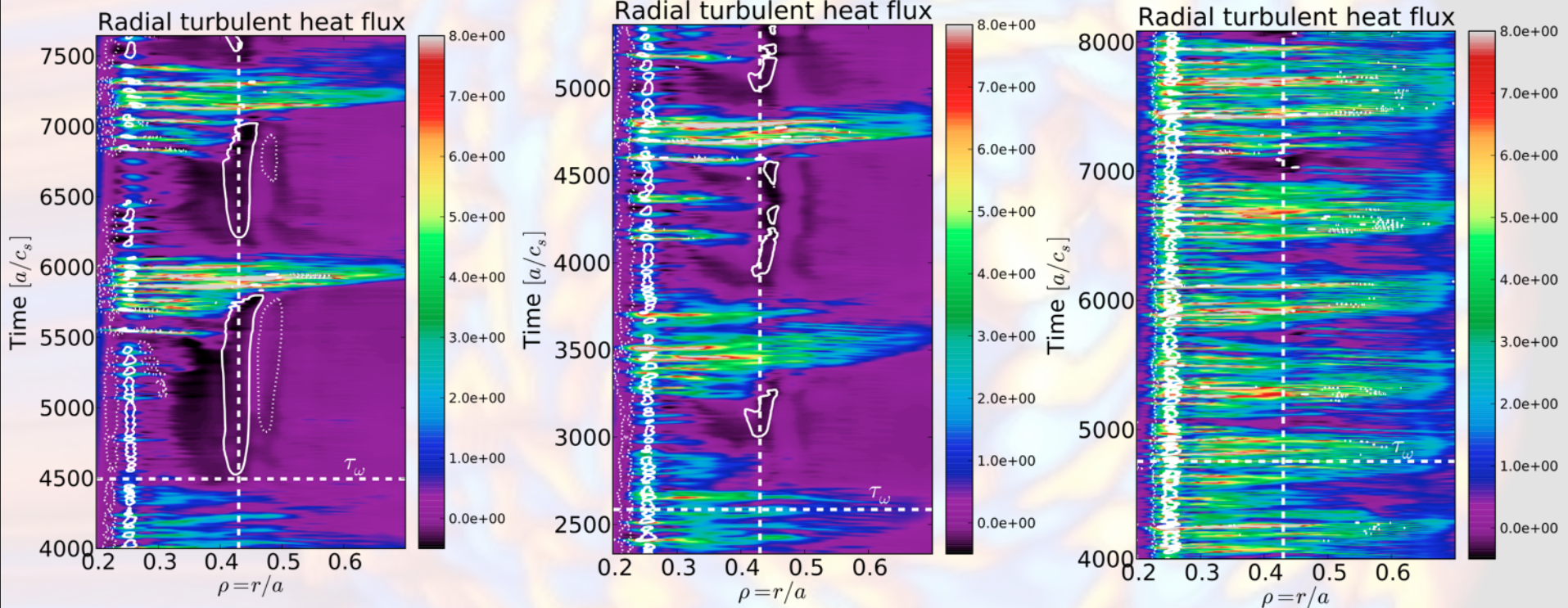
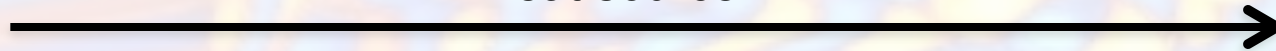


Turbulent vorticity transport



# Vorticity source vs turbulent transport

Heat source x 2



Competition:

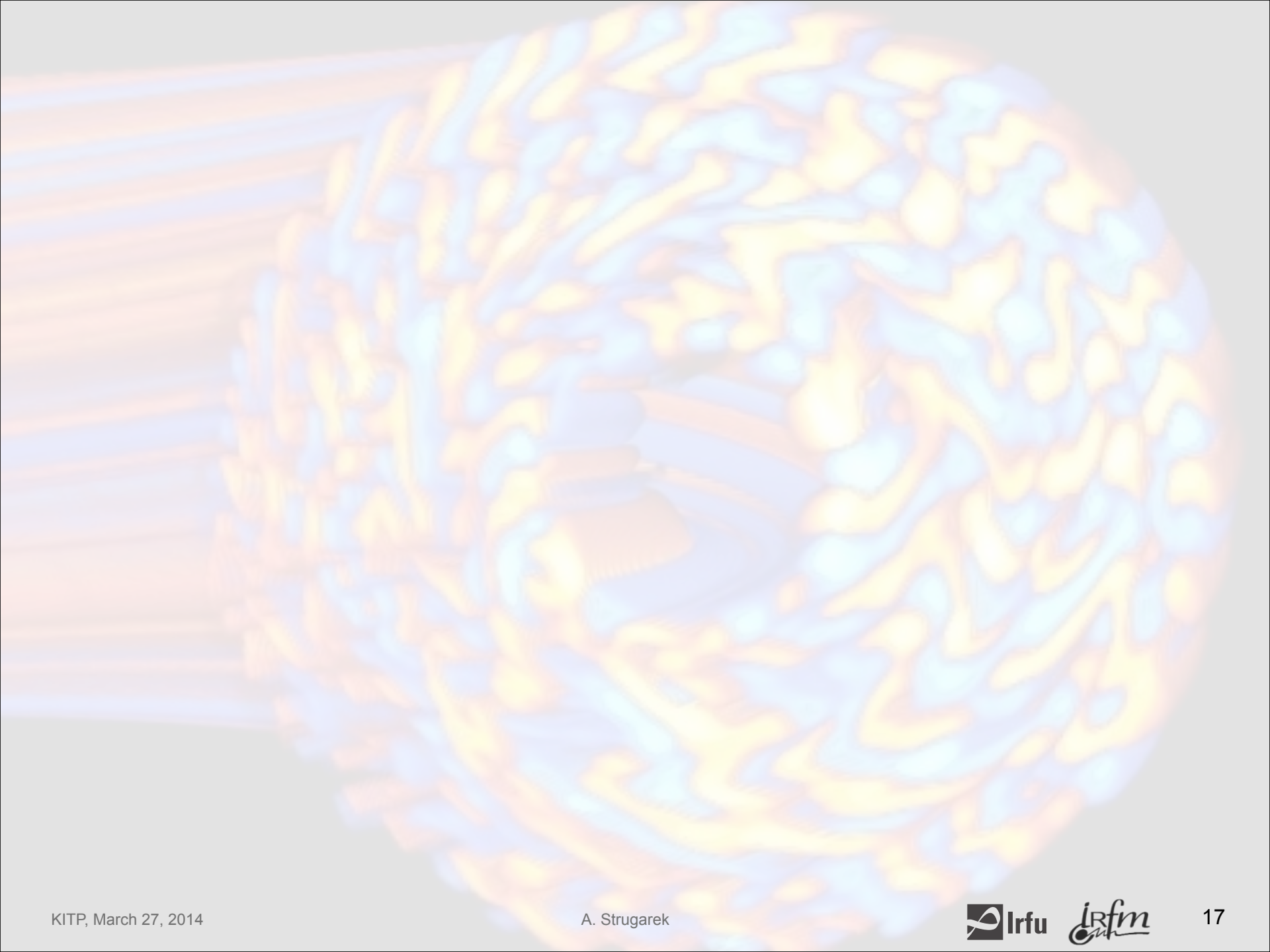
- » Vorticity source amplitude
- » Reynolds stress amplitude

$$\partial_t W = \underbrace{-\partial_r \mathcal{J}}_{\text{Turbulence}} + \underbrace{S}_{\text{Source}}$$

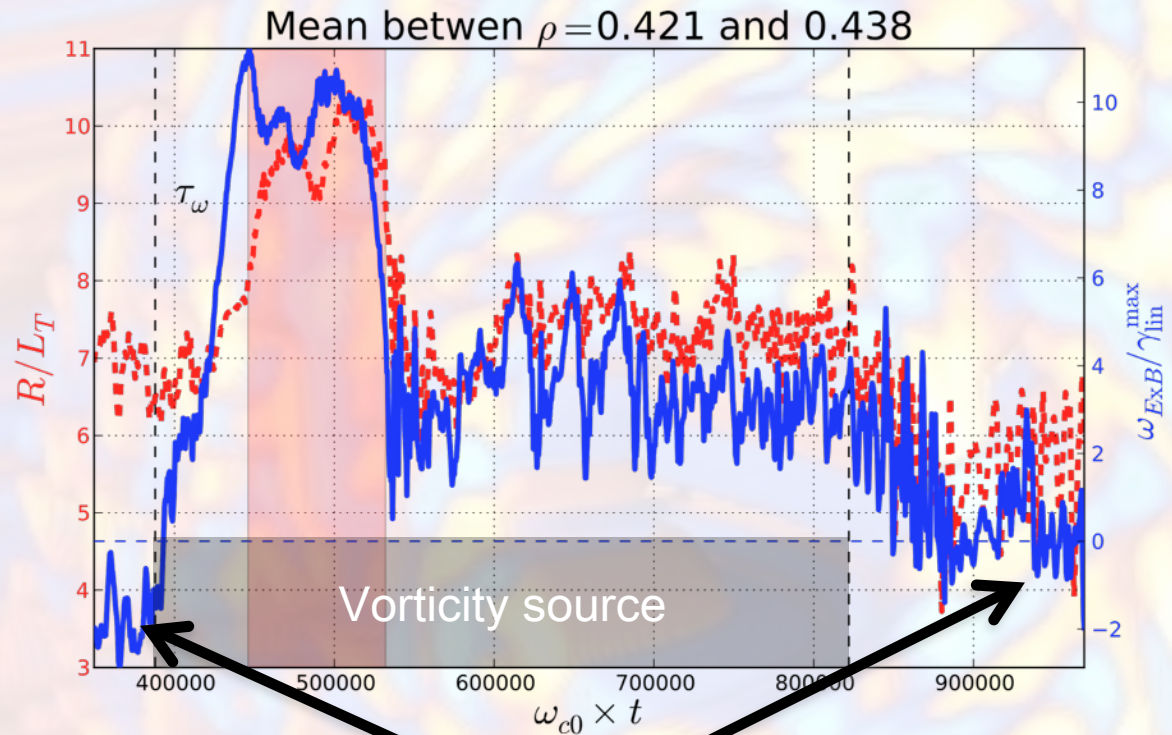
[cf Beyer et al 2007]

# Conclusions and Perspectives

- A **transport barrier** related to an **externally induced sheared flow** is observed in gyrokinetic simulations
- A new mechanism based on a **(physical) strong temperature anisotropy** is found to be at the origin of the destabilization of such barrier
- Our results promote a renewed interest in **experimental setup** where the plasma is **externally polarized**, e.g. with Ion Bernstein Waves
- A better **experimental determination of the temperature anisotropy** would also be highly valuable in the context of transport barrier stability
  - » The **vorticity source could be altered** to locally allow a heating/cooling of the plasma, this **reducing the T anisotropy**
  - » **Stable barriers** could also be simulated with an **ad-hoc on/off switch** on the vorticity source, with interesting experimental implications



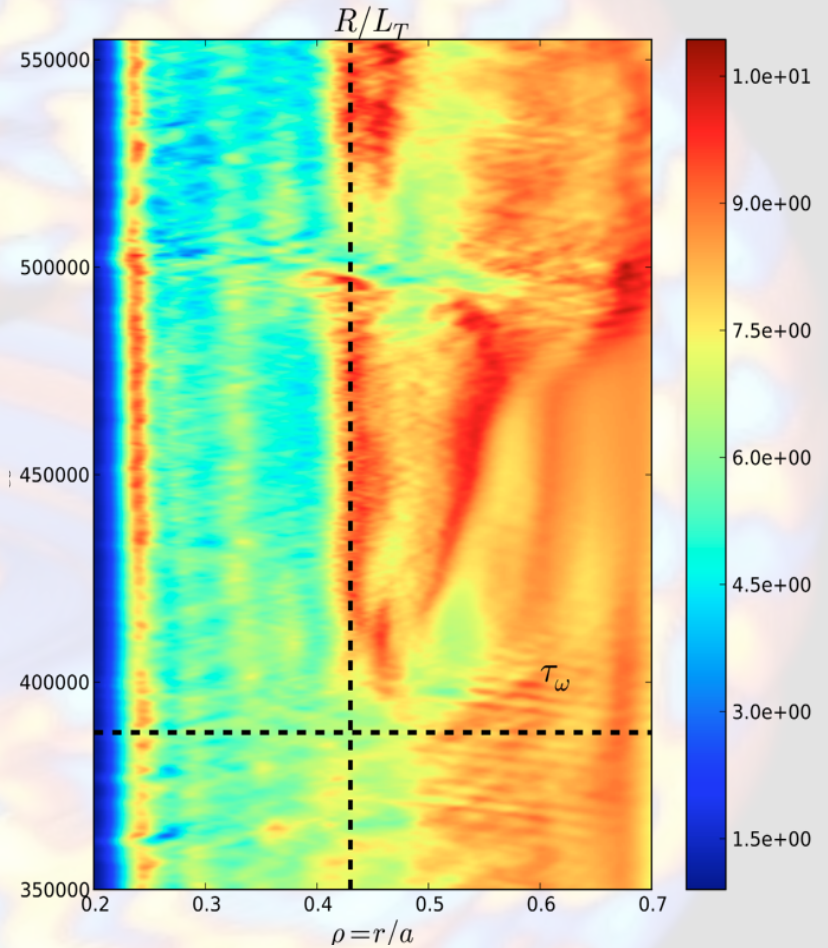
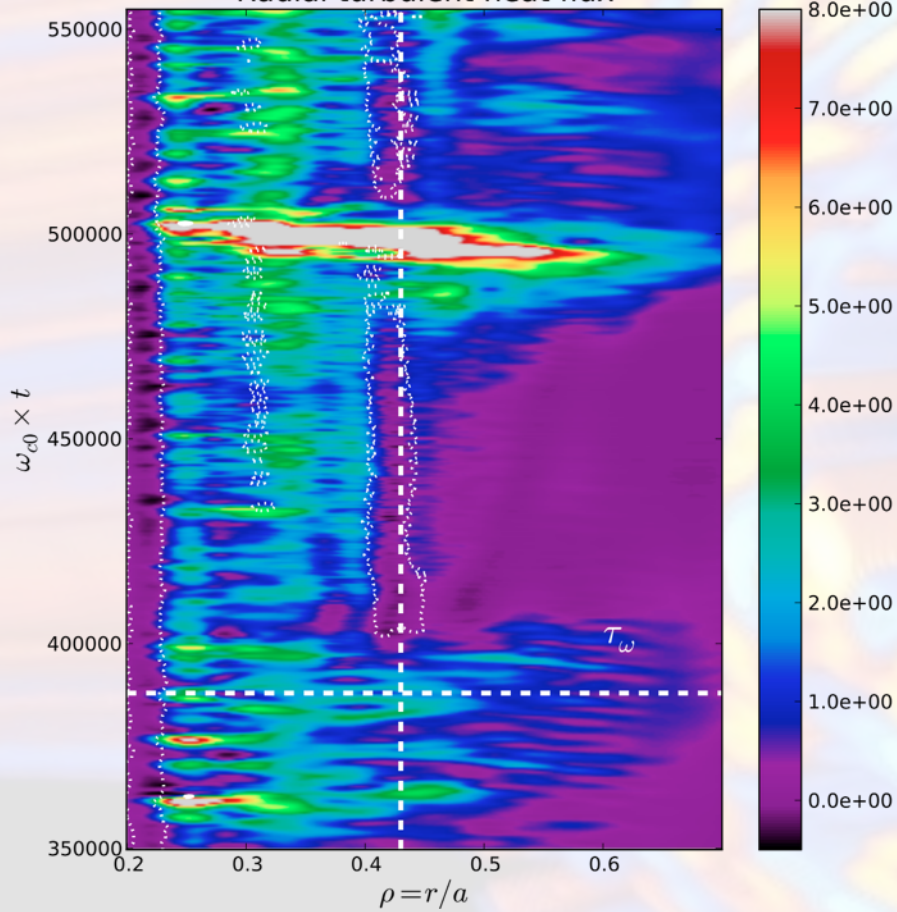
# No hysteresis



The system relaxes towards its initial state

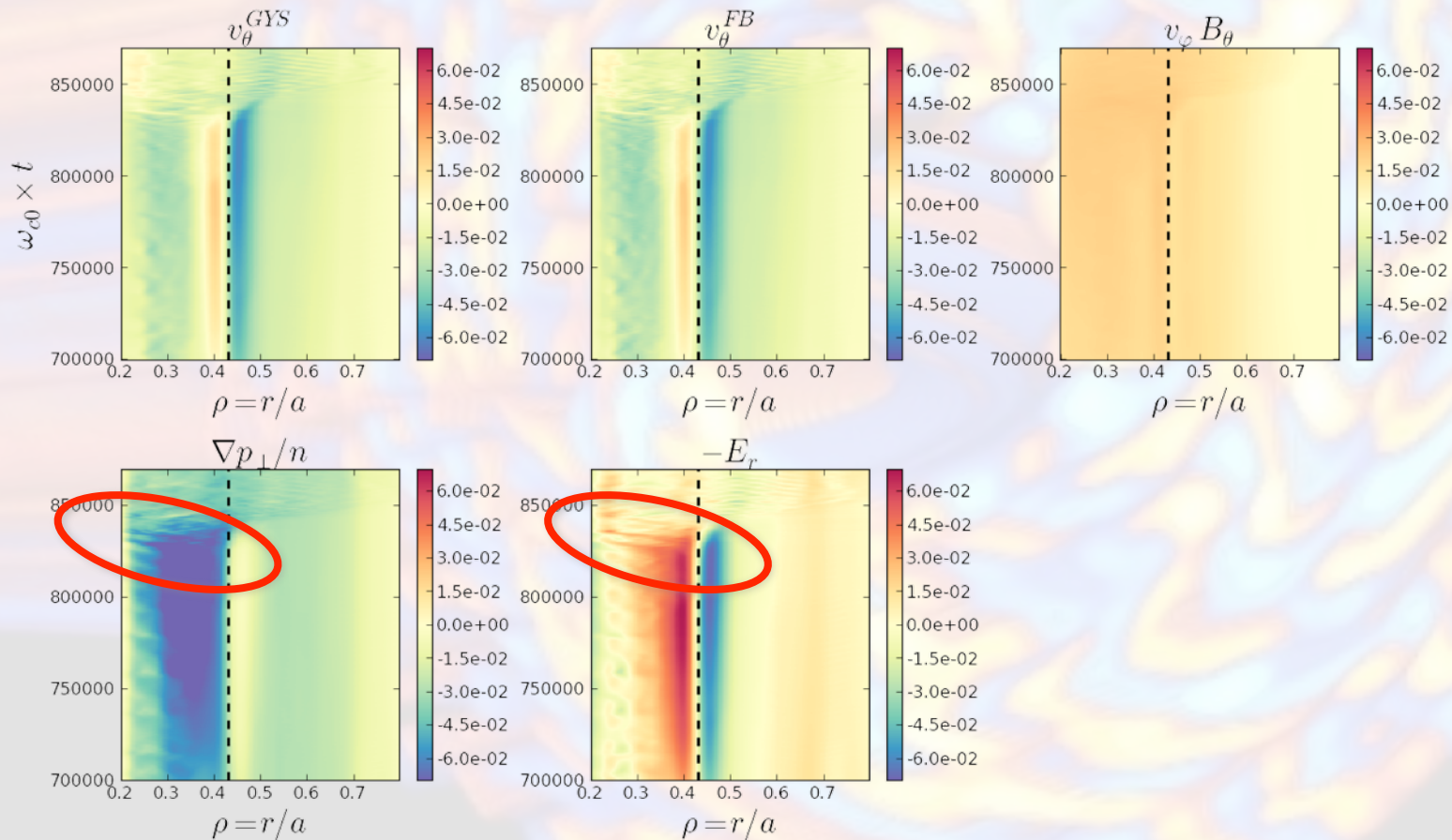
# Effect of the sign of the vorticity source

Radial turbulent heat flux



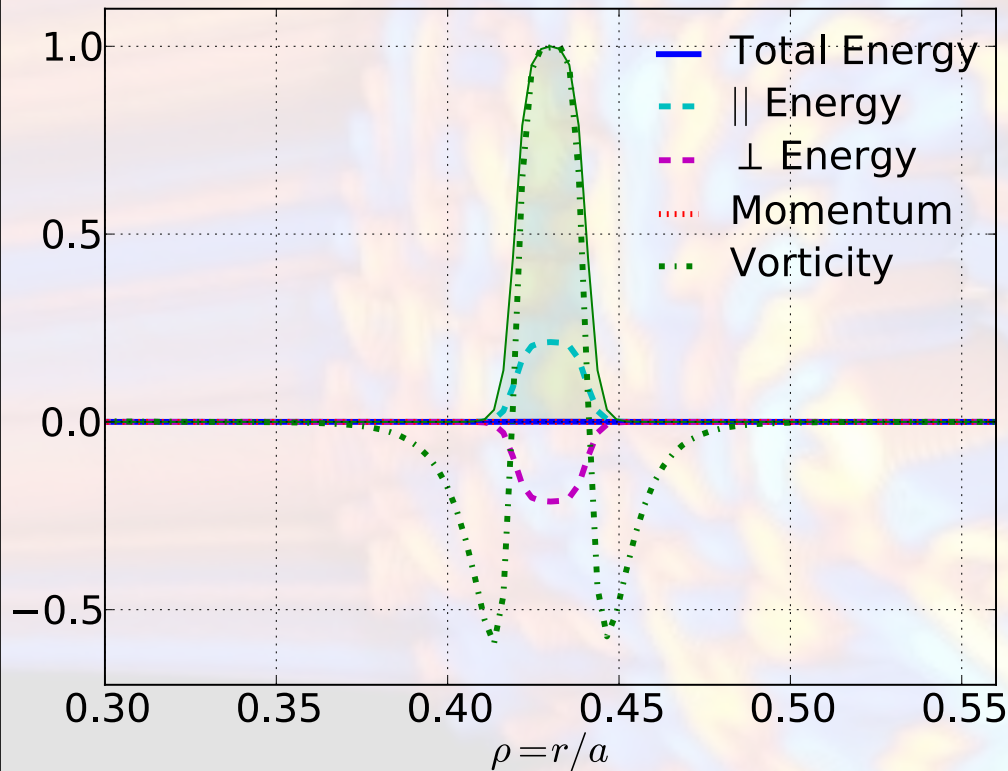
# Force balance

$$B_\varphi v_\theta = -E_r + \frac{\partial_r p_\perp}{en}$$



# Vorticity source effect

Normalized effective sources



Vorticity source effect

